

# New physics interpretation of the muon $g-2$ anomaly

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北原 鉄平

名古屋大学 高等研究院/KMI

Based on: Endo, Hamaguchi, Iwamoto, TK  
[2001.11025] [2104.03217]

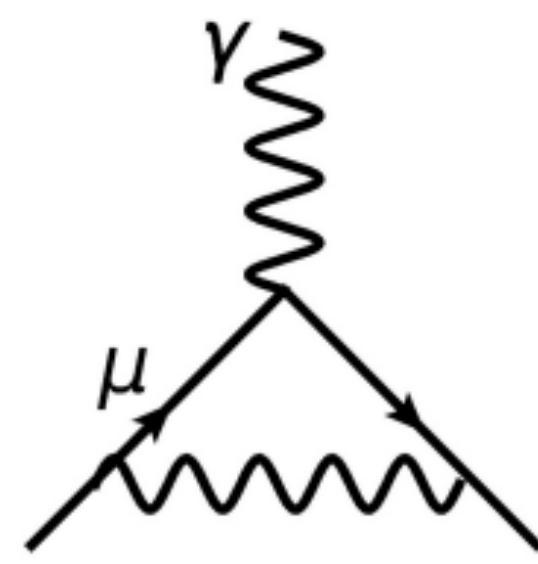


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2021年5月22日, 於 オンライン

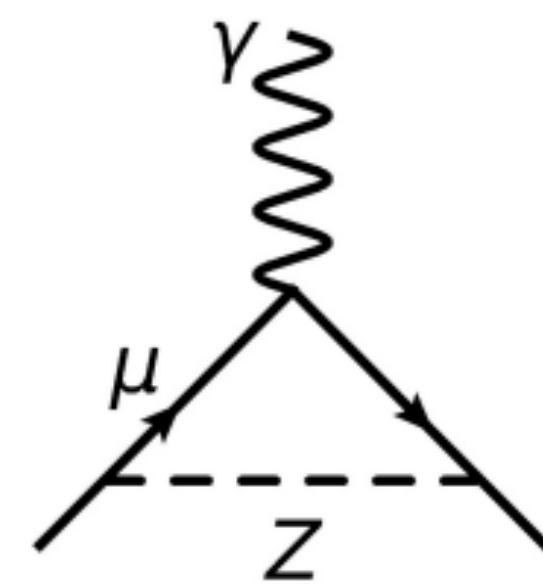


# Muon g-2

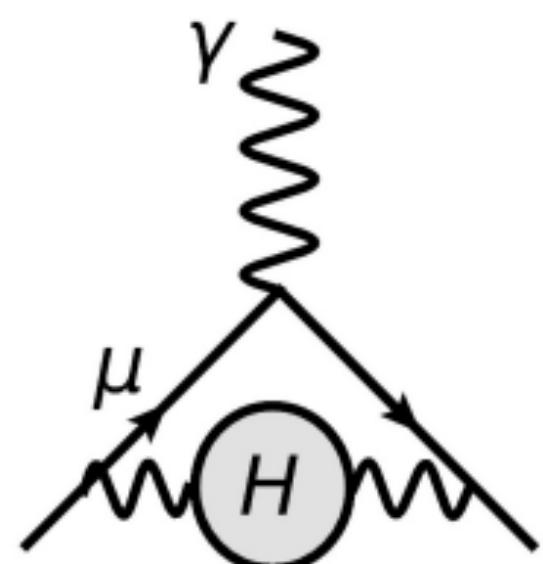
## Theory



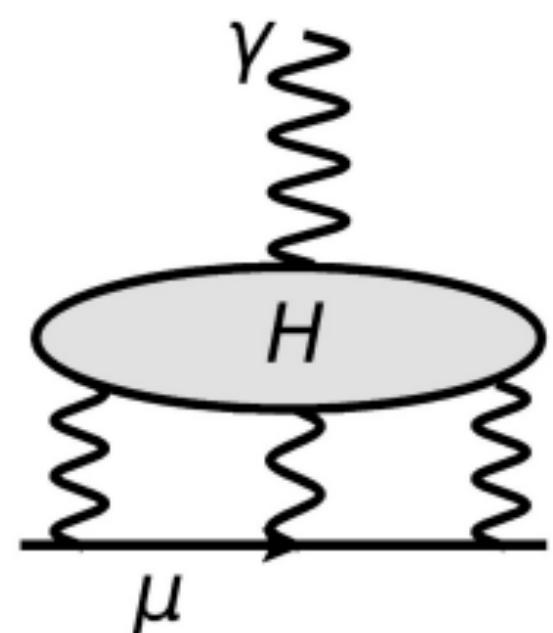
QED



EW



Hadronic vacuum  
polarization (HVP)



Hadronic light-  
by-light (HLbL)

Analytic

Analytic

Phenomenological

Lattice

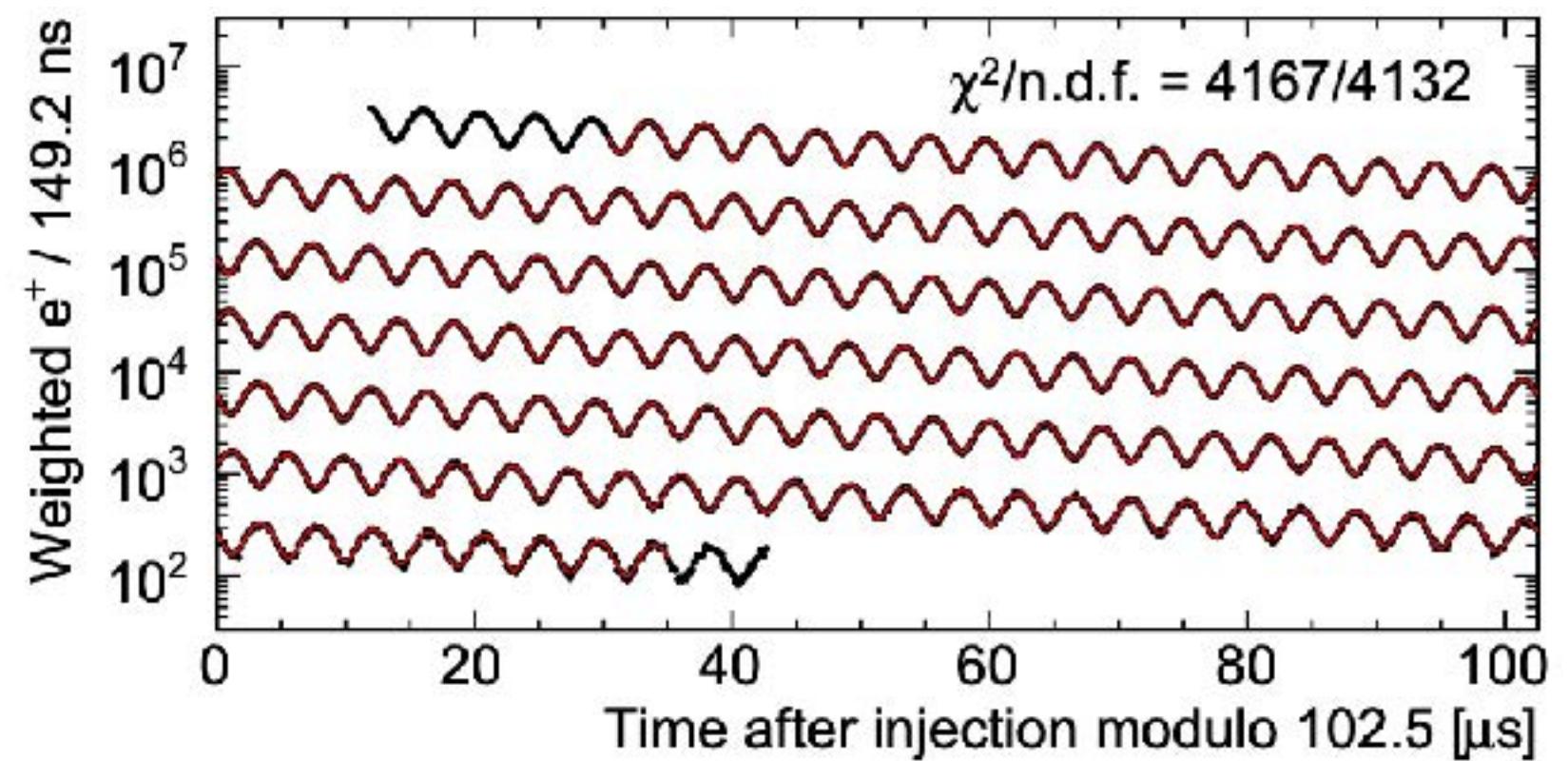
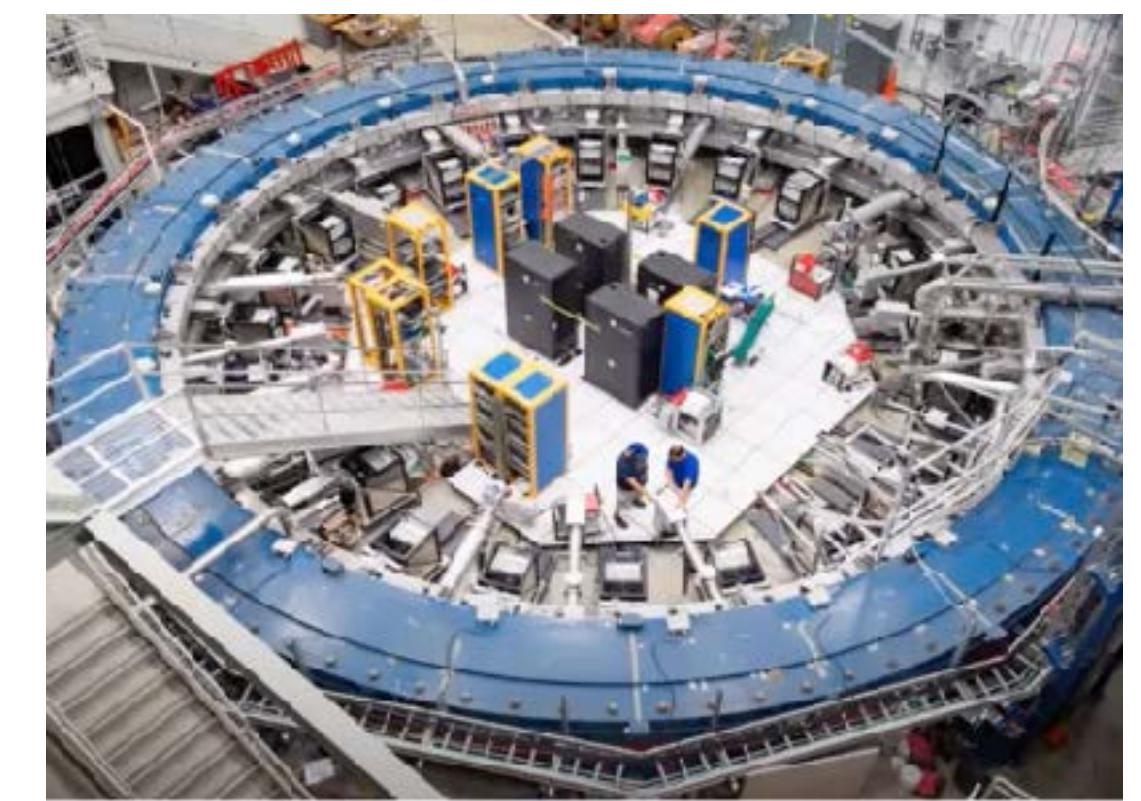
Problematic

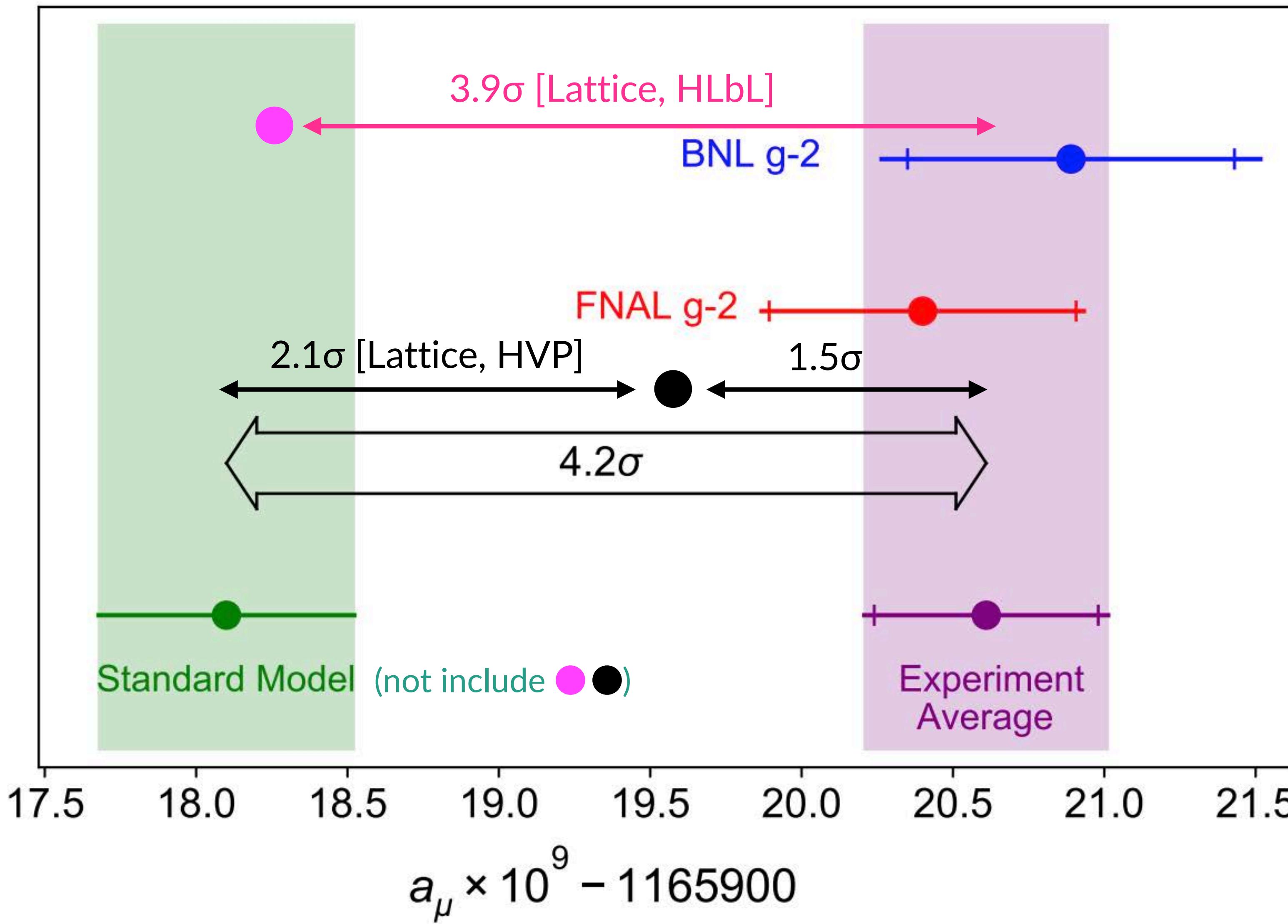
## Exp.

BNL '97-'01

FNAL ongoing

J-PARC  
near future





comments

Stat errors dominated

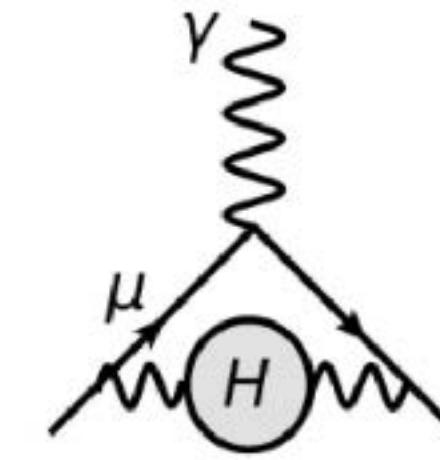
Almost no correlation  
between BNL and FNAL  
syst errors

The latest lattice result for  
HLbL slightly reduces tension  
[Mainz group, 2104.02632]

The latest lattice result for  
HVP significantly reduces  
tension [BMW, Nature '21]

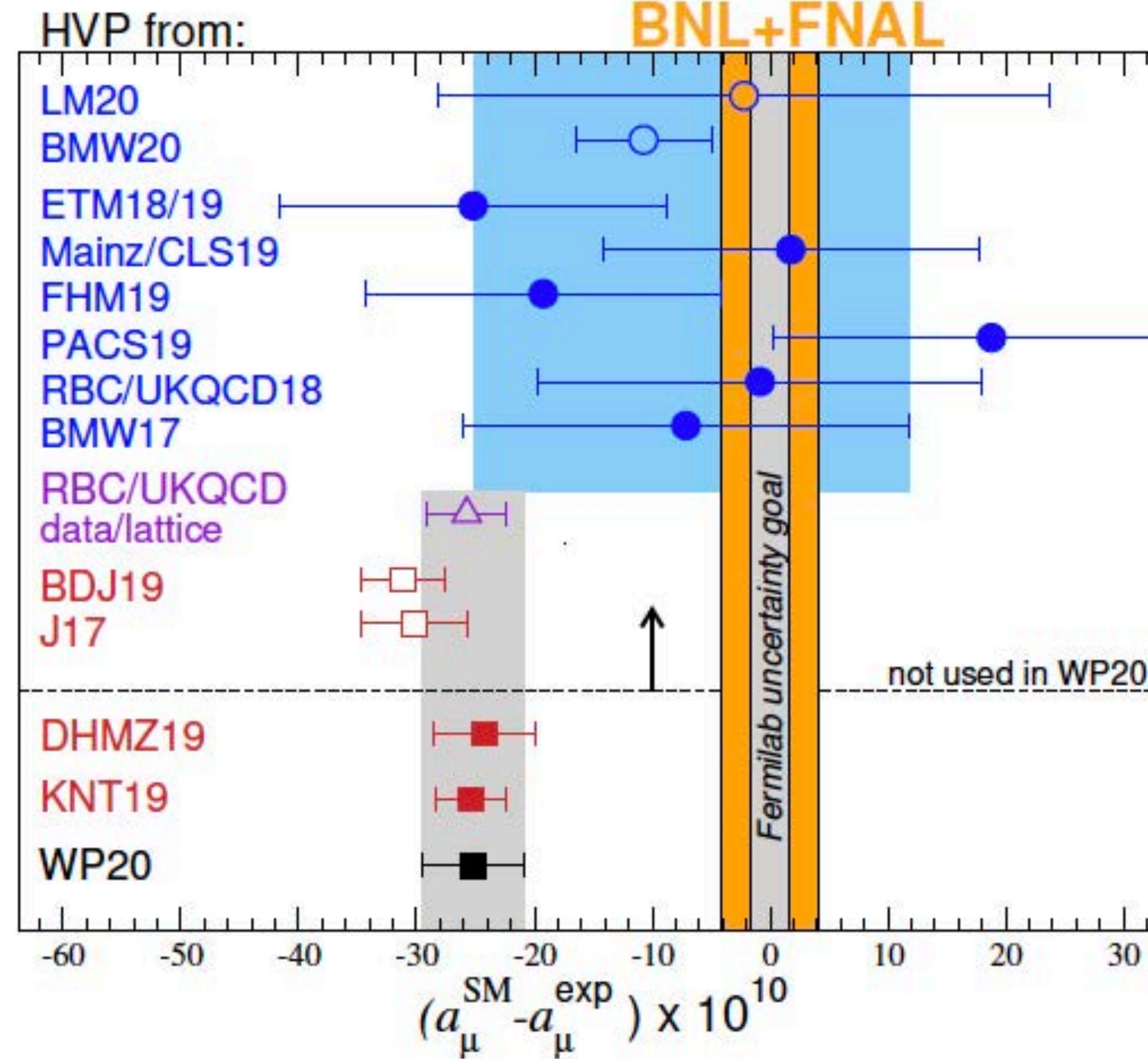
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# Status of HVP

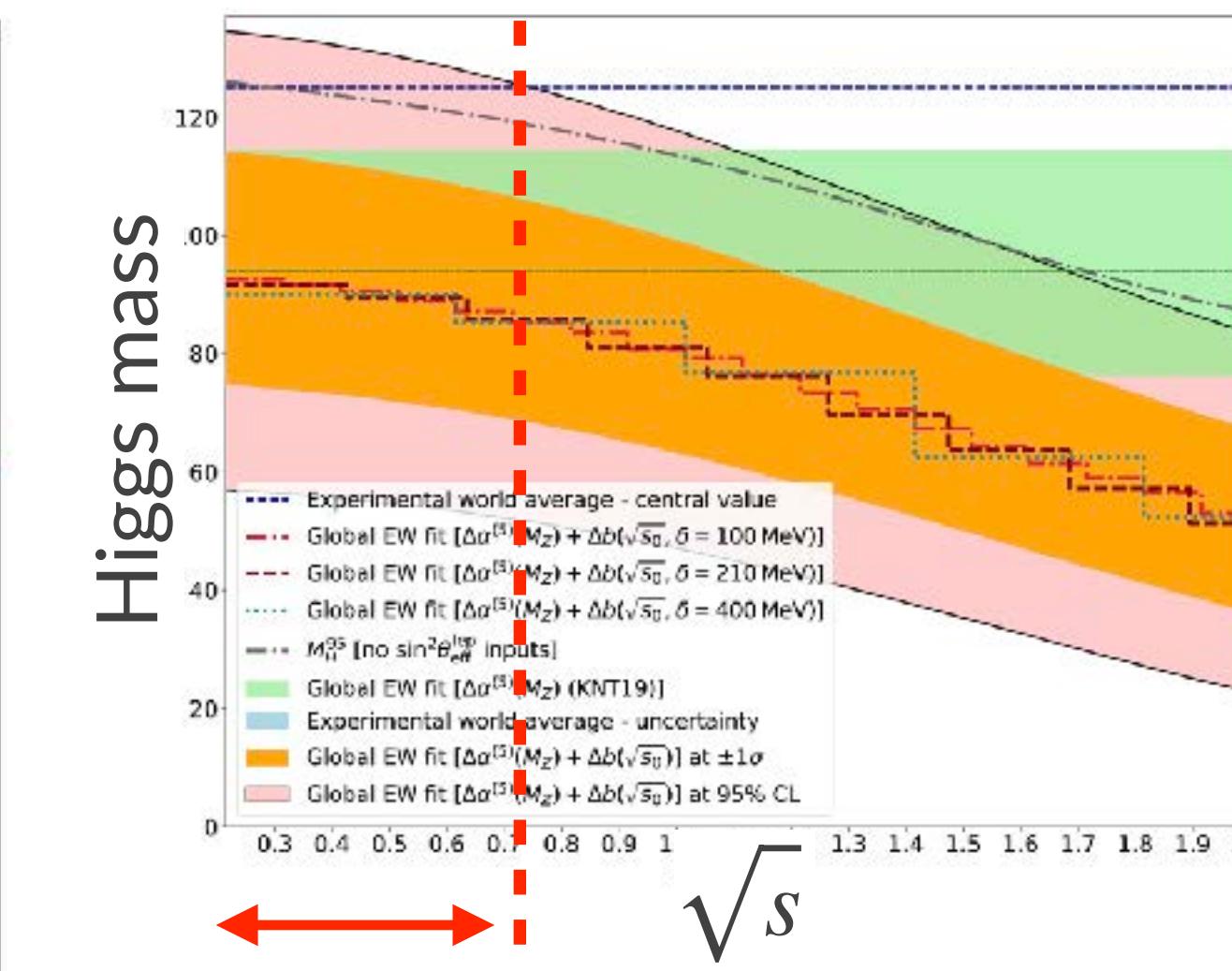


[Lehner, KEK-PH2021]

lattice  
hybrid  
 $e^+e^- \rightarrow \text{hadrons}$



[Keshavarzi et al, 2006.12666]



Several analyses show that EW fit could be no problem, **only when the low energy region of  $e^+e^- \rightarrow \text{hadrons}$  ( $\sqrt{s} \lesssim 0.7 \text{ GeV}$ ) are modified.**

Then, there is additional tension:

8% change of  $e^+e^- \rightarrow \rho$  resonance, or  
4% change of  $e^+e^- \rightarrow 2\pi$  data, see e.g.,  
[Colangelo et al, 2010.07943]

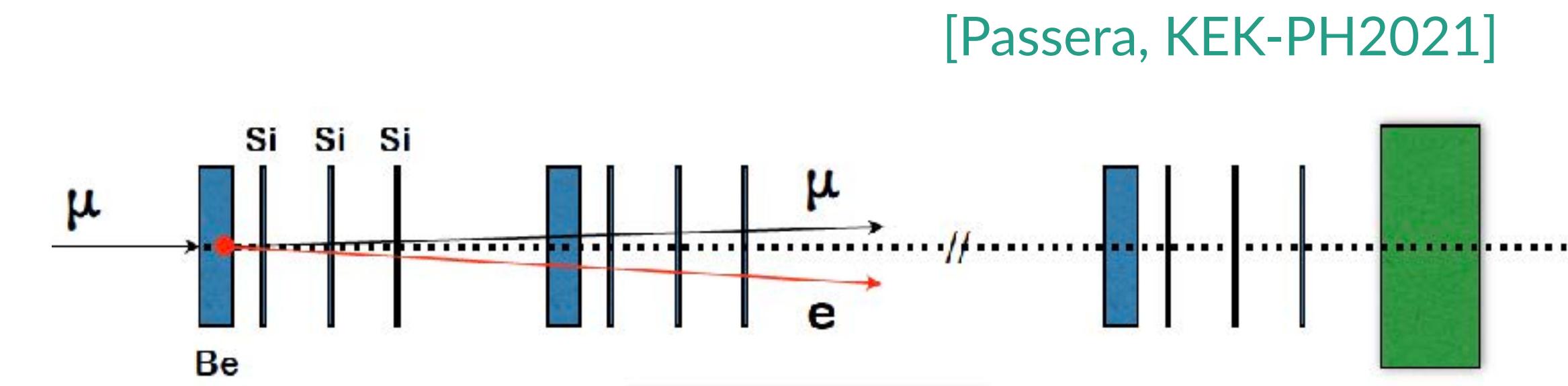
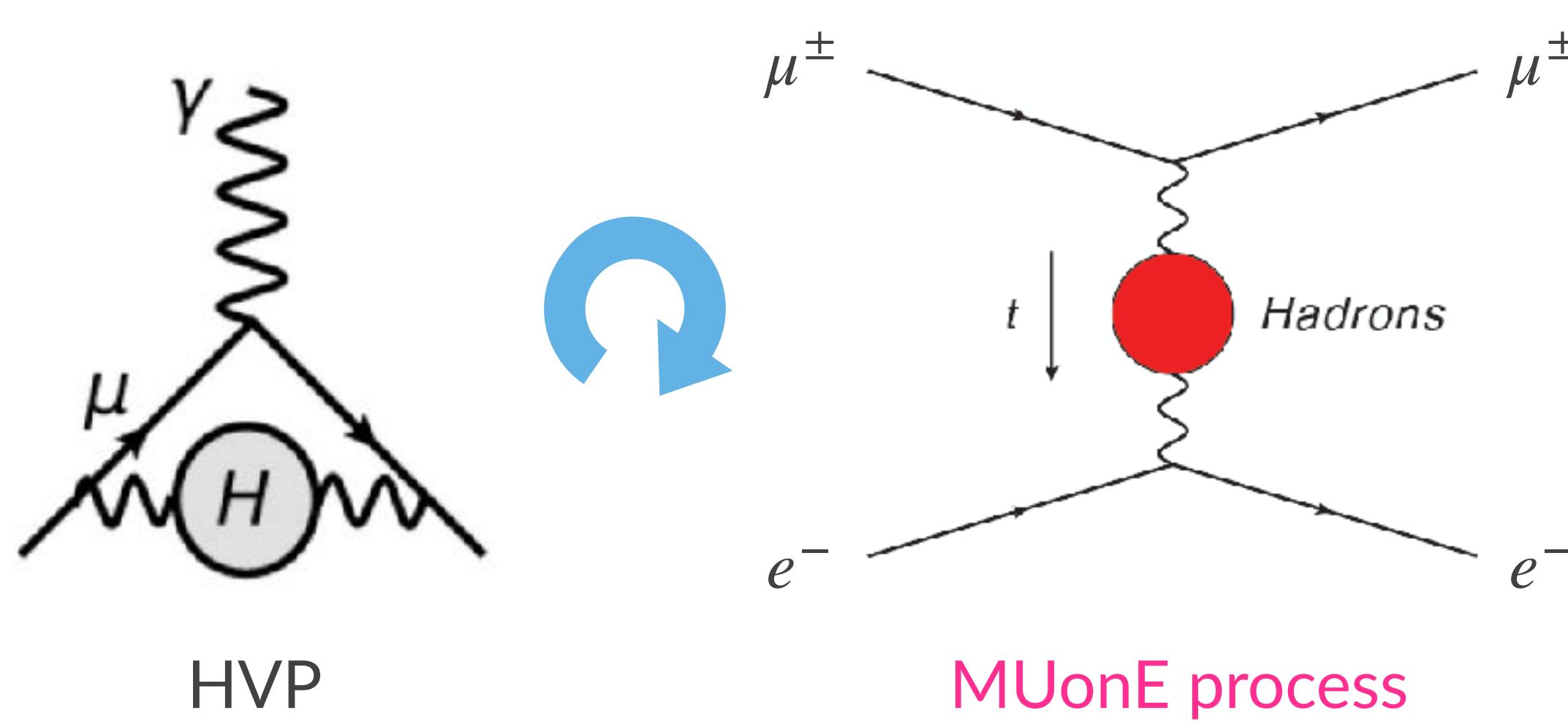
But, data fit is 1% error [Nomura et al, 1911.00367]

Updated RBC/UKQCD18 will be presented near future

# MUonE experiment



- ◆ The MUonE experiment at CERN can directly and precisely prove HVP [MUonE, 2004.13663]
- ◆ Use  $\mu^\pm + \text{fixed } e^- \rightarrow \mu^\pm e^-$  elastic scattering
- ◆ Test run was approved for 2021.



By using 3 years data, statistical sensitivity is 0.3 % on  $a_\mu^{\text{HLO}}$  (current **tension** is 2 % on  $a_\mu^{\text{HLO}}$ )

For theoretical uncertainties, NLO corrections were ready and NNLO is close to completion

muon g-2 anomaly = physics beyond the SM?

# Naive NP energy scale

- ◆ Muon g-2 anomaly implies that NP mass scale is around the electroweak scale.

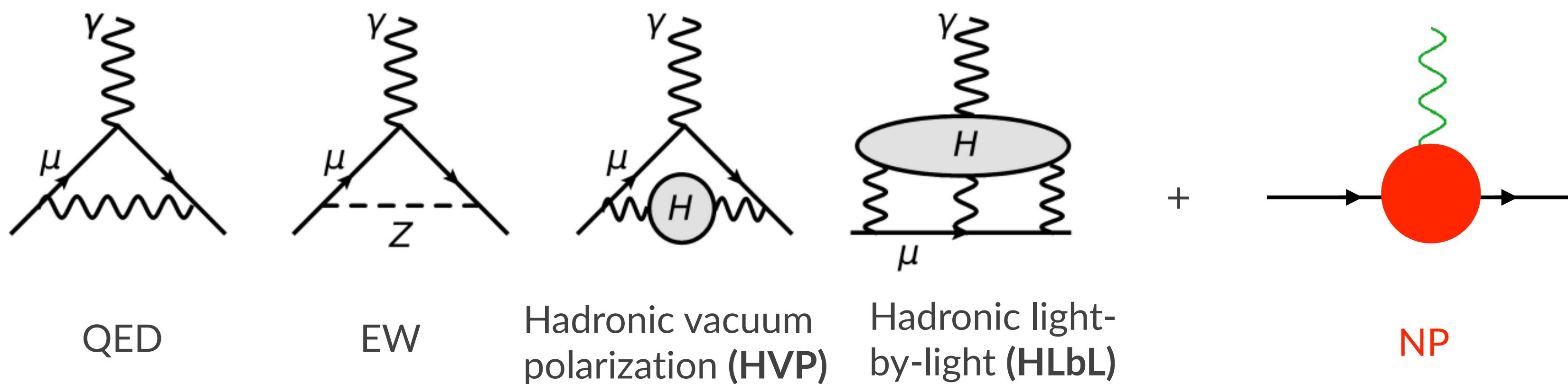
$$\Delta a_\mu \equiv a_\mu^{\text{BNL+FNAL}} - a_\mu^{\text{SM}} = (25.1 \pm 5.9) \times 10^{-10} \quad (4.2\sigma)$$
$$= \frac{m_\mu^2}{16\pi^2} \frac{g_{\text{NP}}^2}{M_{\text{NP}}^2}$$

→  $M_{\text{NP}} \sim g_{\text{NP}} \times 150 \text{ GeV}$

$M_{\text{NP}}$  is determined by size of the NP couplings to muon

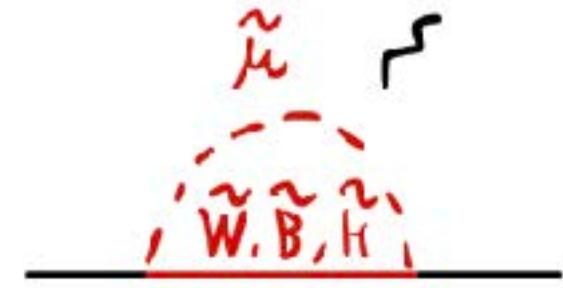
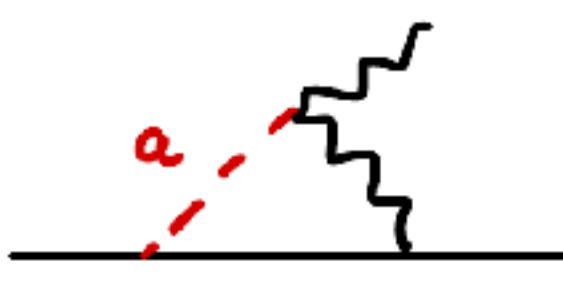
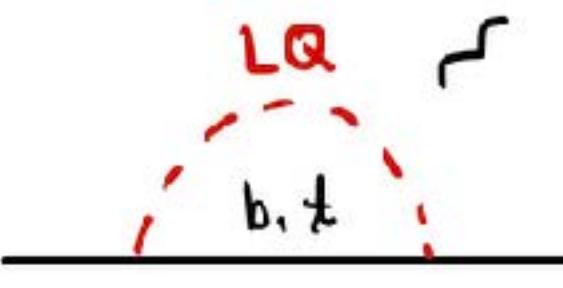
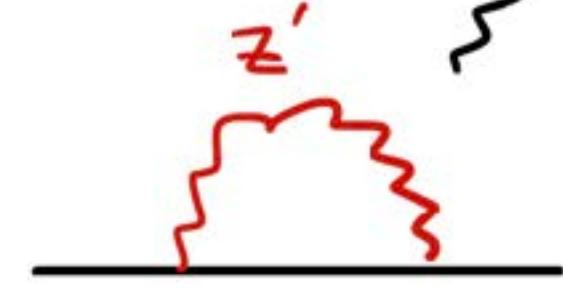
Large  $g_{\text{NP}}$  by certain mechanisms  
→ TeV scale NP  
Small  $g_{\text{NP}}$  → MeV NP

Positiveness ( $\Delta a_\mu > 0$ ) sets a strong constraint on light CP-odd scalar scenarios



# New physics interpretations

[Refs: Athron et al, 2104.03691; Buen-Abad et al, 2104.03267;  
Krnjaic et al, 1902.07715; Dermisek et al, 2103.05645]

NP type	diagrams	mass range	probe
Supersymmetry		200~500 GeV	$\tilde{\chi}_2^0 \tilde{\chi}_1^\pm \rightarrow (h \tilde{\chi}_1^0) (W^\pm \tilde{\chi}_1^0)$ $pp \rightarrow \gamma\gamma \rightarrow \tilde{\ell}\tilde{\ell}^*$
Scalar extensions		20~100 GeV, 150~250 GeV	$Z \rightarrow \tau^+ \tau^-$ $h \rightarrow AA$
Axion-like particle		40 MeV~6 GeV	$e^+ e^- \rightarrow \gamma a, a \rightarrow \gamma\gamma$
Leptoquark		1.5~2 TeV	$pp \rightarrow LQL\bar{Q}$ $Z \rightarrow \mu^+ \mu^-$
$U(1) \mu-\tau$		10~200 MeV	$e^+ e^- \rightarrow \mu^+ \mu^- Z'$ $K^- \rightarrow \mu^- \bar{\nu} Z'$
Vector-like lepton		< 7 TeV	$h, Z \rightarrow \mu^+ \mu^-$

# New physics interpretations

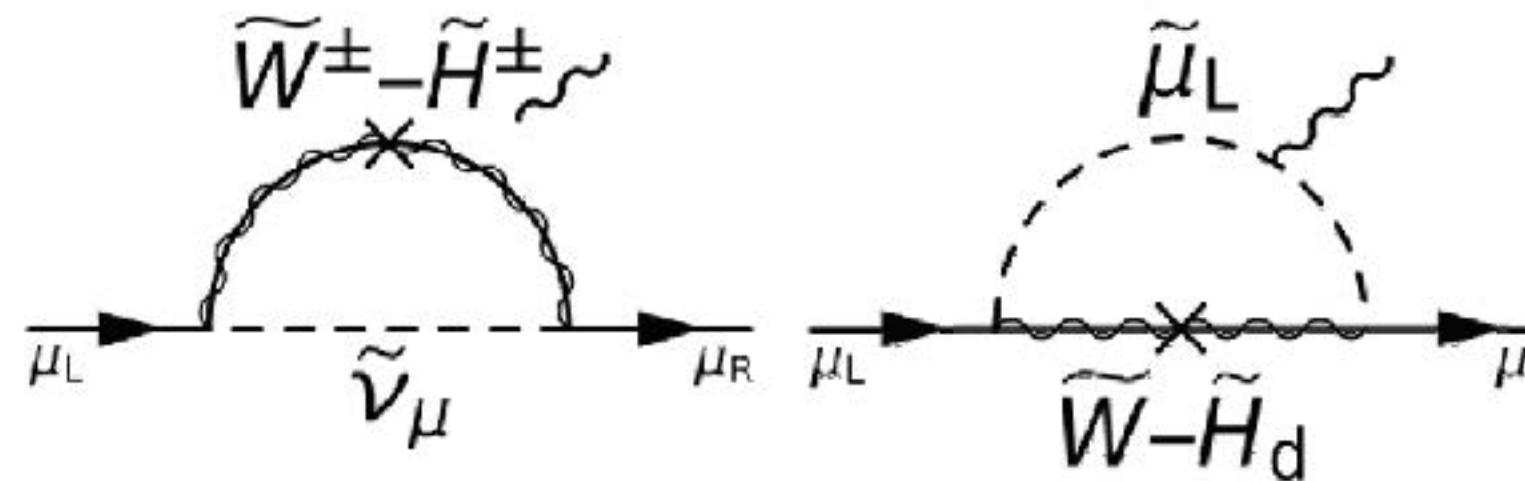
[Refs: Athron et al, 2104.03691; Buen-Abad et al, 2104.03267;  
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# Supersymmetry (SUSY)

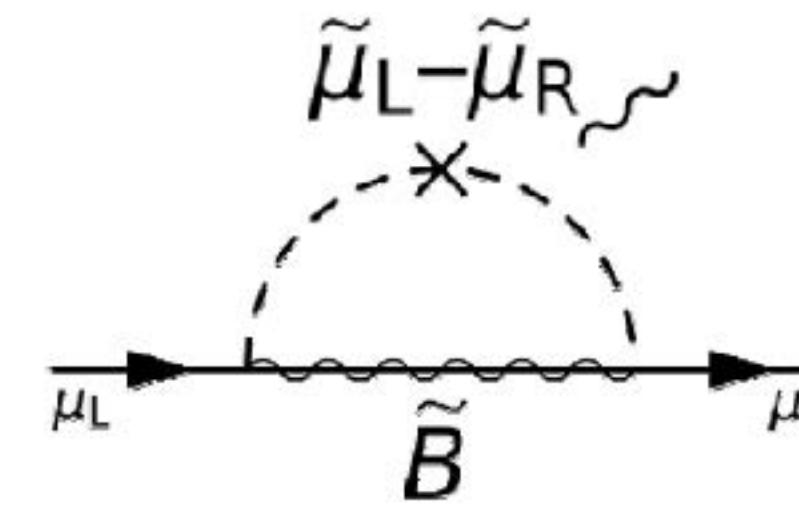
- ◆ Theoretical motivation other than muon g-2 anomaly; → SUSY is the most attractive scenario.
- ◆ gauge hierarchy problem, gauge coupling unification, and dark matter (DM)
- ◆ Under SUSY, slepton/squark ( $s=0$ ), gaugino ( $s=1/2$ ), and higgsino ( $s=1/2$ ) are required
- ◆ Four types of one-loop diagrams are responsible to explain the anomaly:

1, WHL scenario

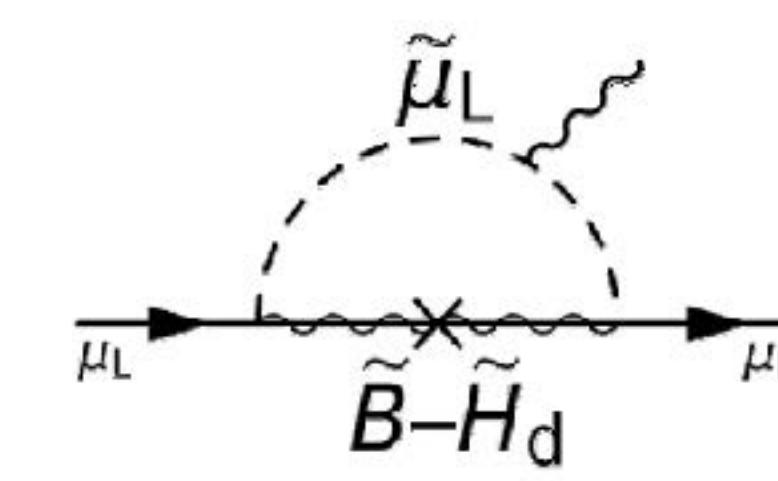


$\leftrightarrow$   
SU(2)<sub>L</sub>

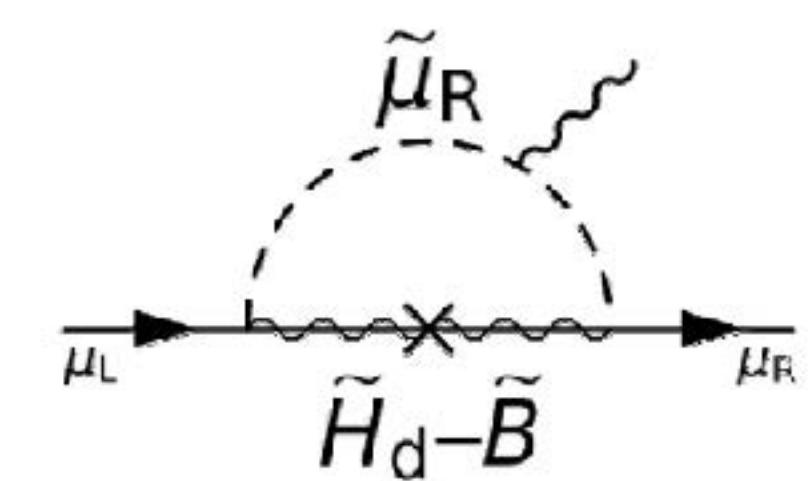
2, BLR scenario



3, BHL scenario



4, BHR scenario

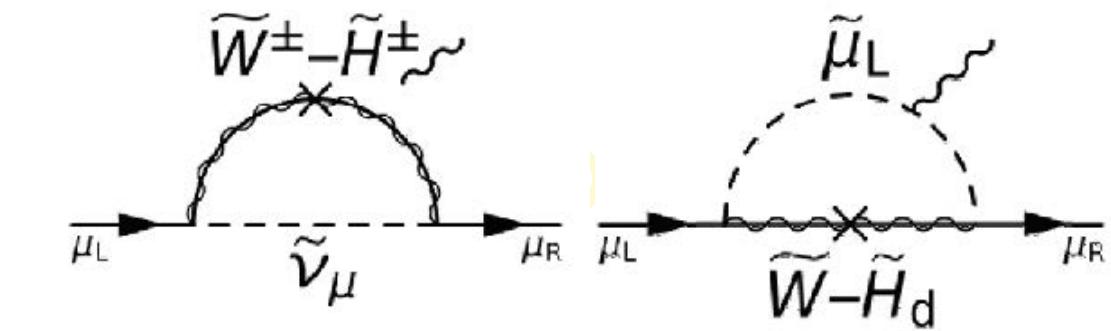


These diagrams are proportional to  $\tan \beta \equiv \langle H_u \rangle / \langle H_d \rangle \sim 1 - 60 \rightarrow \text{TeV scale NP}$

3, BHL and 4, BHR are constrained from DM direct detection (XENON1T)

[Endo et al, 1704.05287, Baum et al, 2104.03302]

# 1, Wino-Higgsino-LH slepton (WHL) scenario



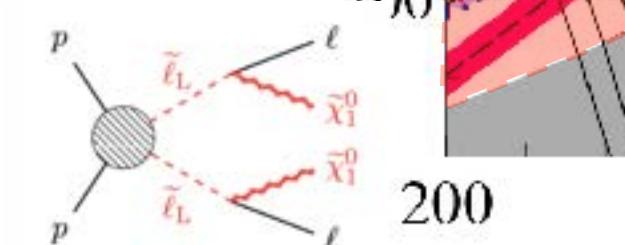
When bino is the lightest SUSY particle (LSP), regions of  $m_{\tilde{\mu}} < m_{\tilde{\chi}^\pm}$  are severely constrained from the LHC.  
 DM relic abundance can be explained by bino/wino coannihilation [Saha et al, 2104.03287]

$\tilde{\chi}_2^0 \tilde{\chi}_1^\pm \rightarrow (h \tilde{\chi}_1^0) (W^\pm \tilde{\chi}_1^0)$   
 will be able to probe.

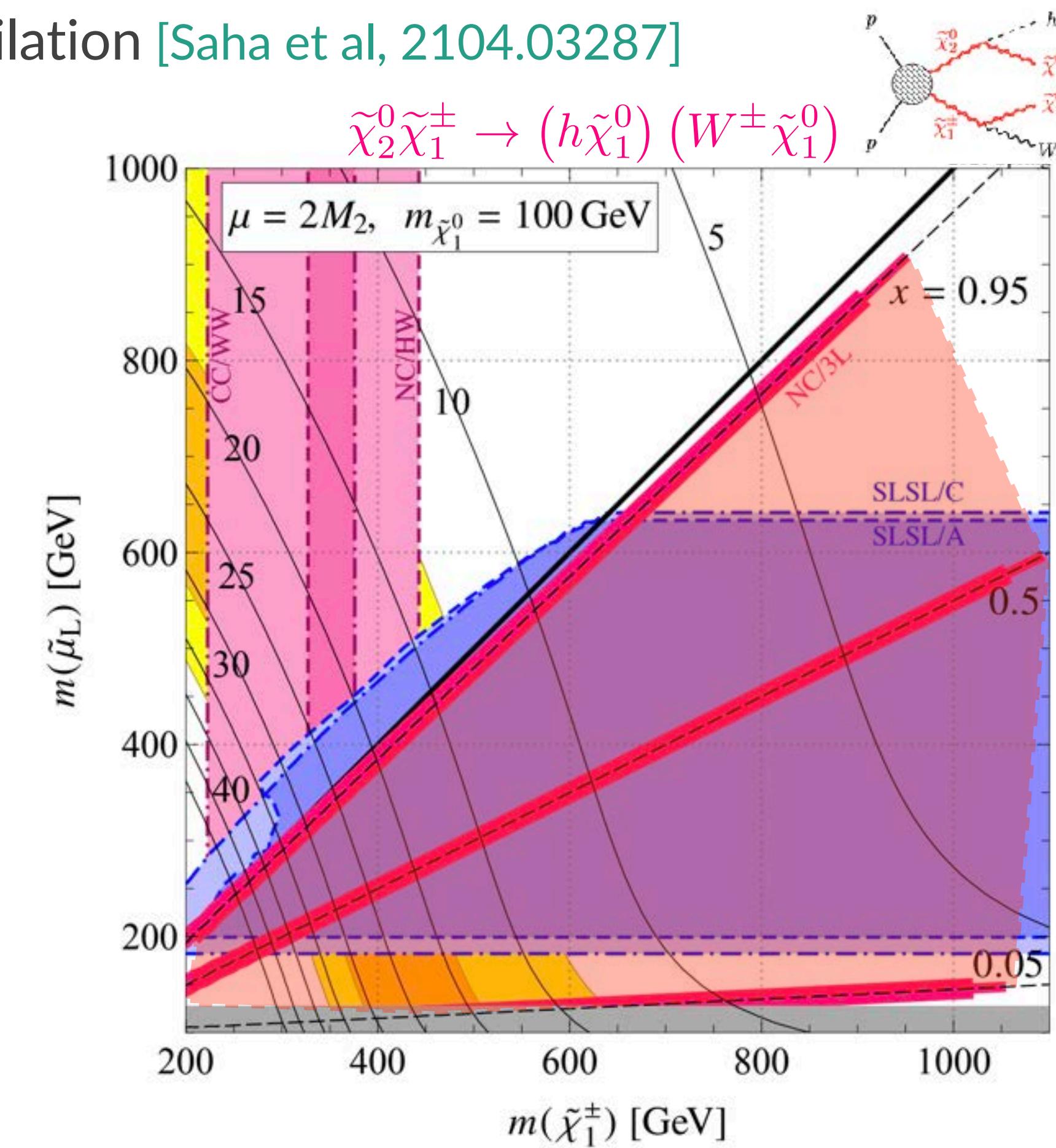
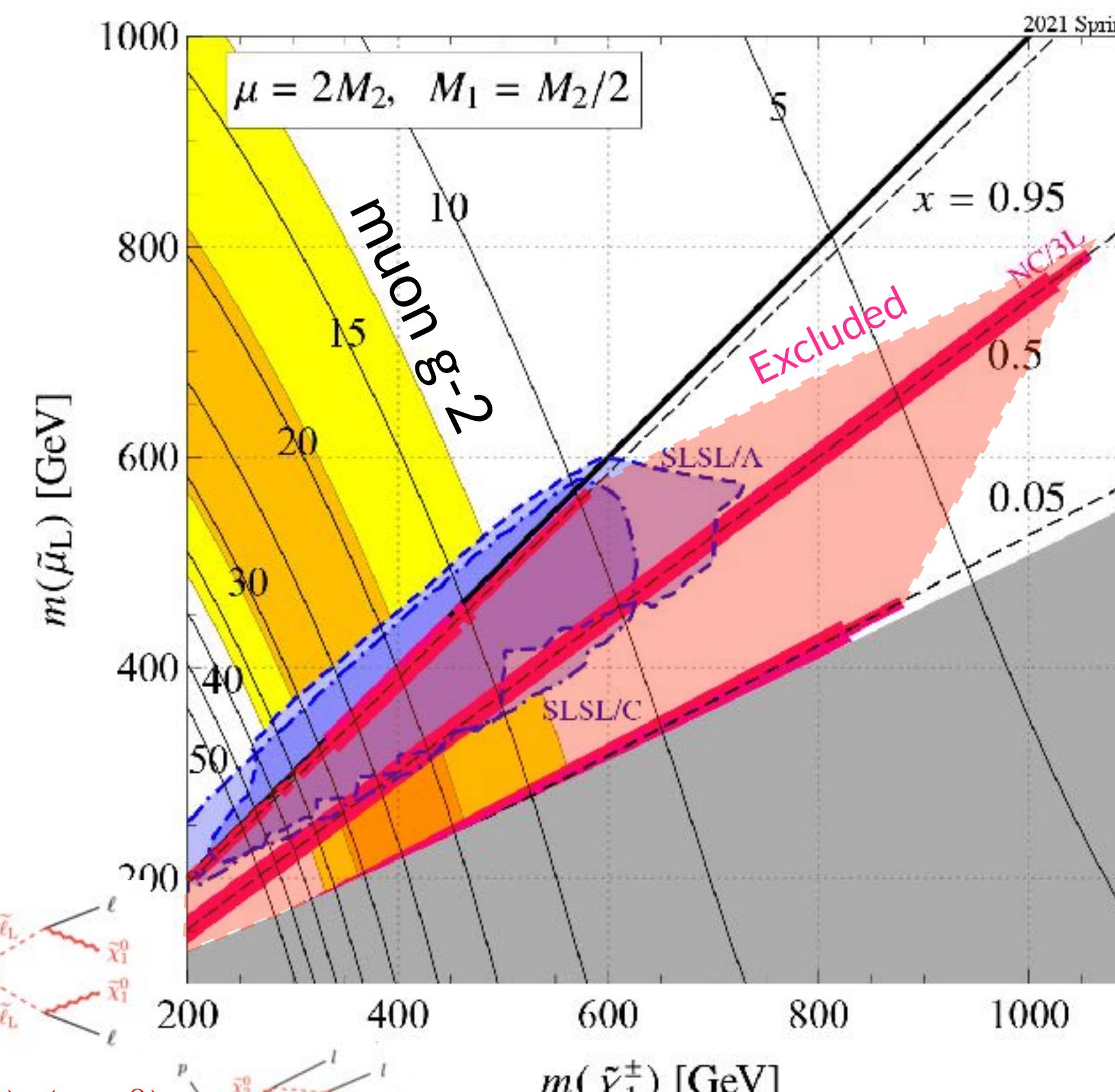
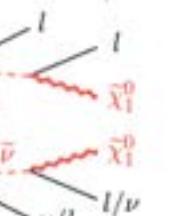
Point:  $\tilde{W}^0$  decays  
 into  $h$ . In general,  
 $\text{Br}(\tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 Z) \sim O(0.1)$

strong bound from:

$$\tilde{\ell}_L \tilde{\ell}_L^* \rightarrow (\ell \tilde{\chi}_1^0) (\bar{\ell} \tilde{\chi}_1^0)$$

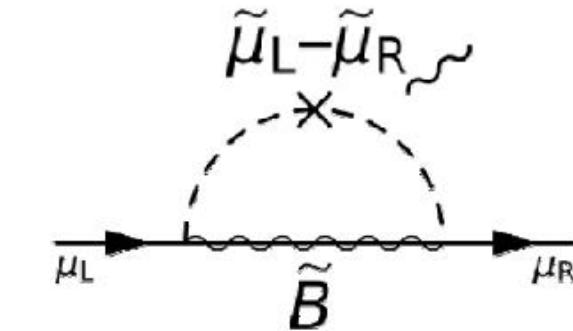


$$\tilde{\chi}_2^0 \tilde{\chi}_1^\pm \rightarrow (l \tilde{l}_L) (\nu \tilde{l}_L) \rightarrow (ll \tilde{\chi}_1^0) (\nu l \tilde{\chi}_1^0)$$



[Endo, Hamaguchi, Iwamoto, TK, 2001.11025, 2104.03217]

## 2, Bino-LH-RH sleptons (BLR) scenario



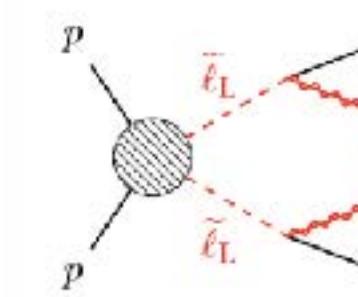
The bino/slepton coannihilation scenario still works.

We found the heavy  $\mu$  and small  $\tan\beta$  are favored in this study (under the vacuum decay condition)

XENONnT (DM direct detection) can probe this scenario

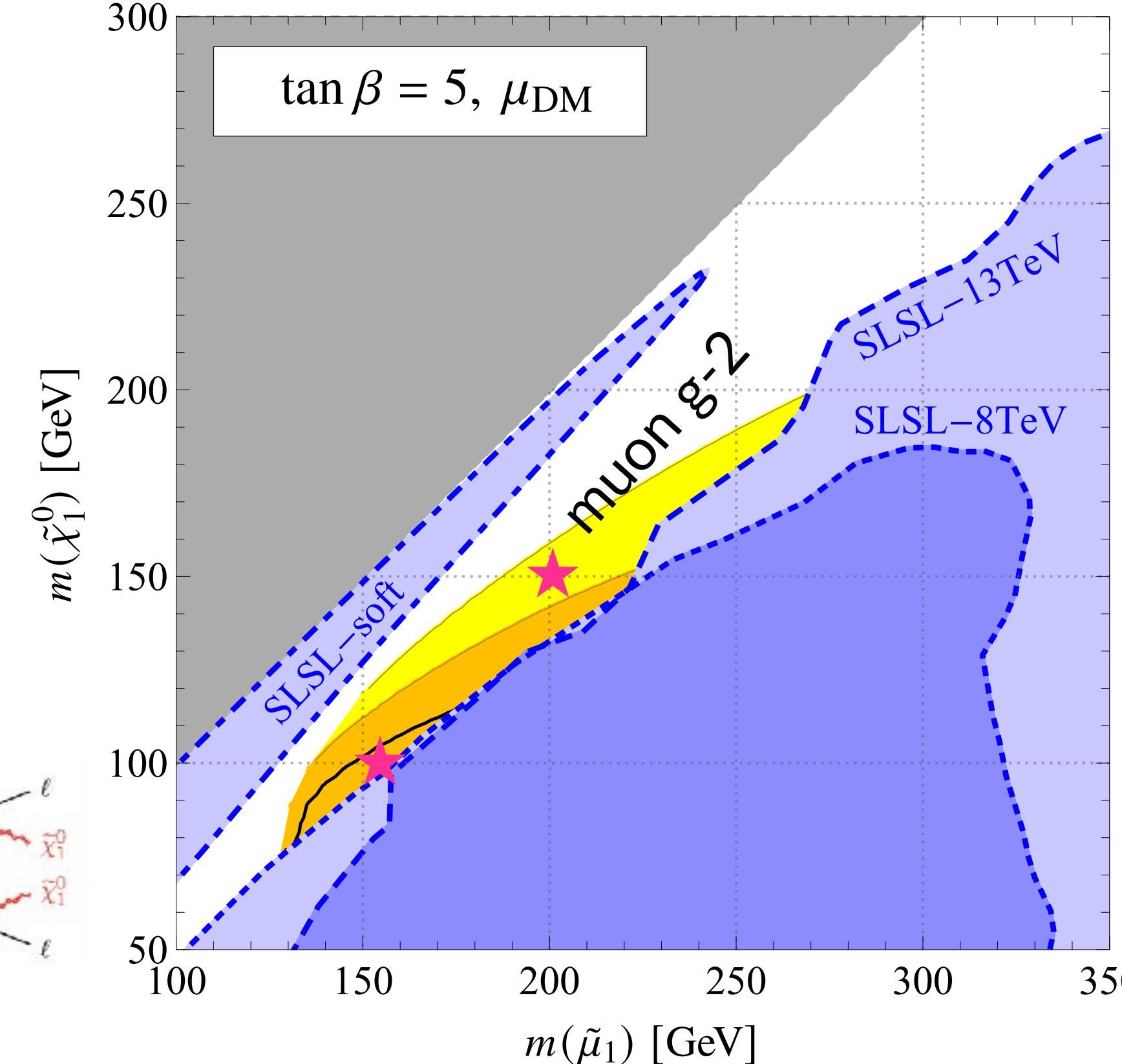
strong bound from:

$$\tilde{\ell}_L \tilde{\ell}_L^* \rightarrow (\ell \tilde{\chi}_1^0) (\bar{\ell} \tilde{\chi}_1^0)$$



[Endo, Hamaguchi, TK, Yoshinaga 1309.3065;  
Endo, Hamaguchi, Iwamoto, TK, 2104.03217]

pure-bino contribution with correct  $\Omega_{\text{DM}}$   
with universal slepton mass



Benchmark points

	BLR1	BLR3
$M_1$	100	150
$m_L = m_R$	150	200
$\tan\beta$	5	5
$\mu$	1323	1922
$m_{\tilde{\mu}_1}$	154	202
$m_{\tilde{\mu}_2}$	159	207
$m_{\tilde{\tau}_1}$	113	159
$m_{\tilde{\tau}_2}$	190	242
$m_{\tilde{\nu}_{\mu,\tau}}$	137	190
$m_{\tilde{\chi}_1^0}$	99	150
$m_{\tilde{\chi}_2^0}, m_{\tilde{\chi}_3^0}, m_{\tilde{\chi}_1^\pm}$	1323–1324	1922–1923
$a_\mu^{\text{SUSY}} \times 10^{10}$	27	17
$\Omega_{\text{DM}} h^2$	0.120	0.120
$\sigma_p^{\text{SI}} \times 10^{47} [\text{cm}^2]$	1.7	0.8
$\mu_{\gamma\gamma}$	1.01	1.01

stau mass < 200 GeV → good target for ILC500?

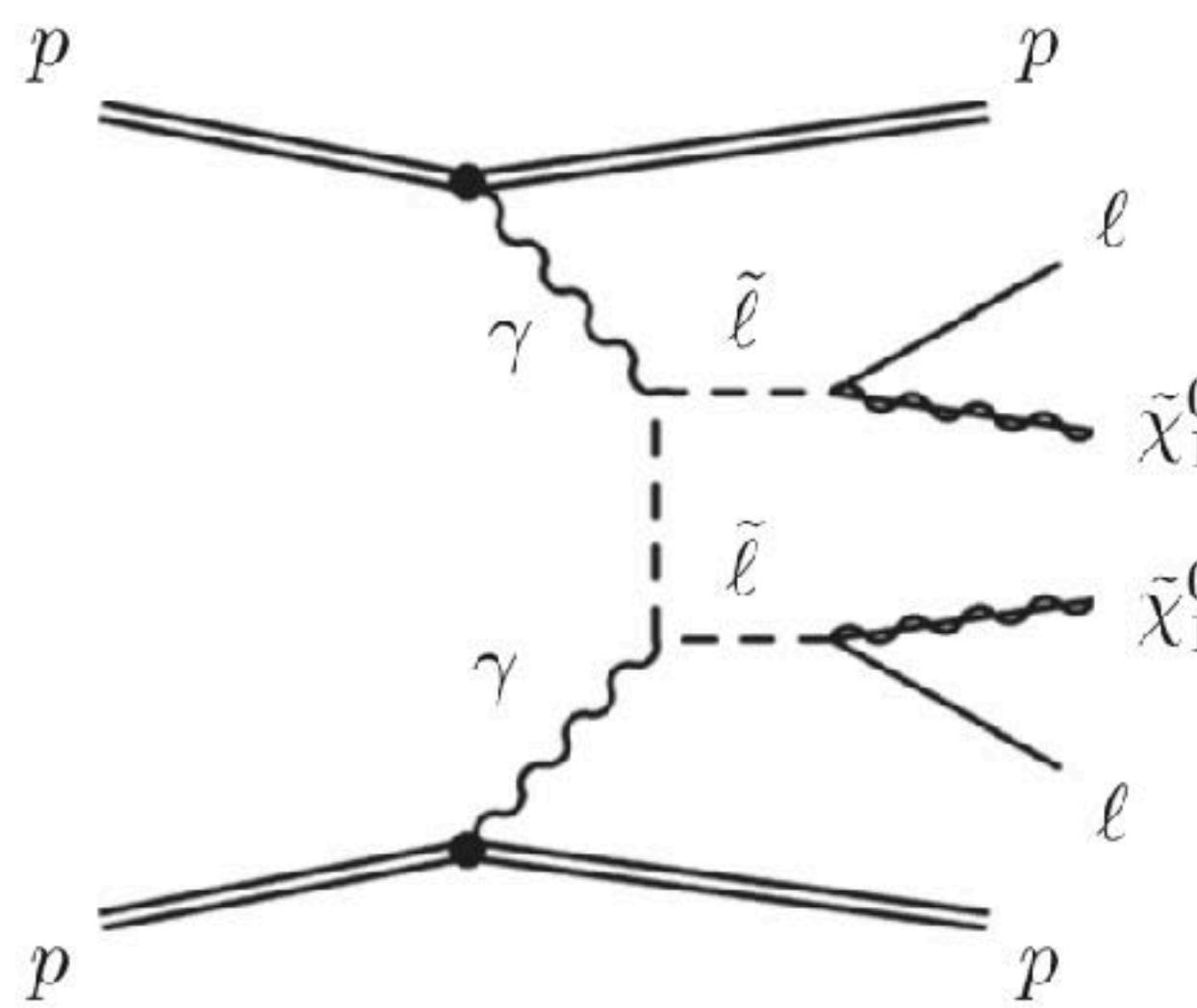
“Reconstruction” of muon g-2 by LHC500 is studied  
[Endo, Hamaguchi, Iwamoto TK, Moroi 1310.4496]

# Slepton search via photon collision

See also, Kawade-san talk page 25-

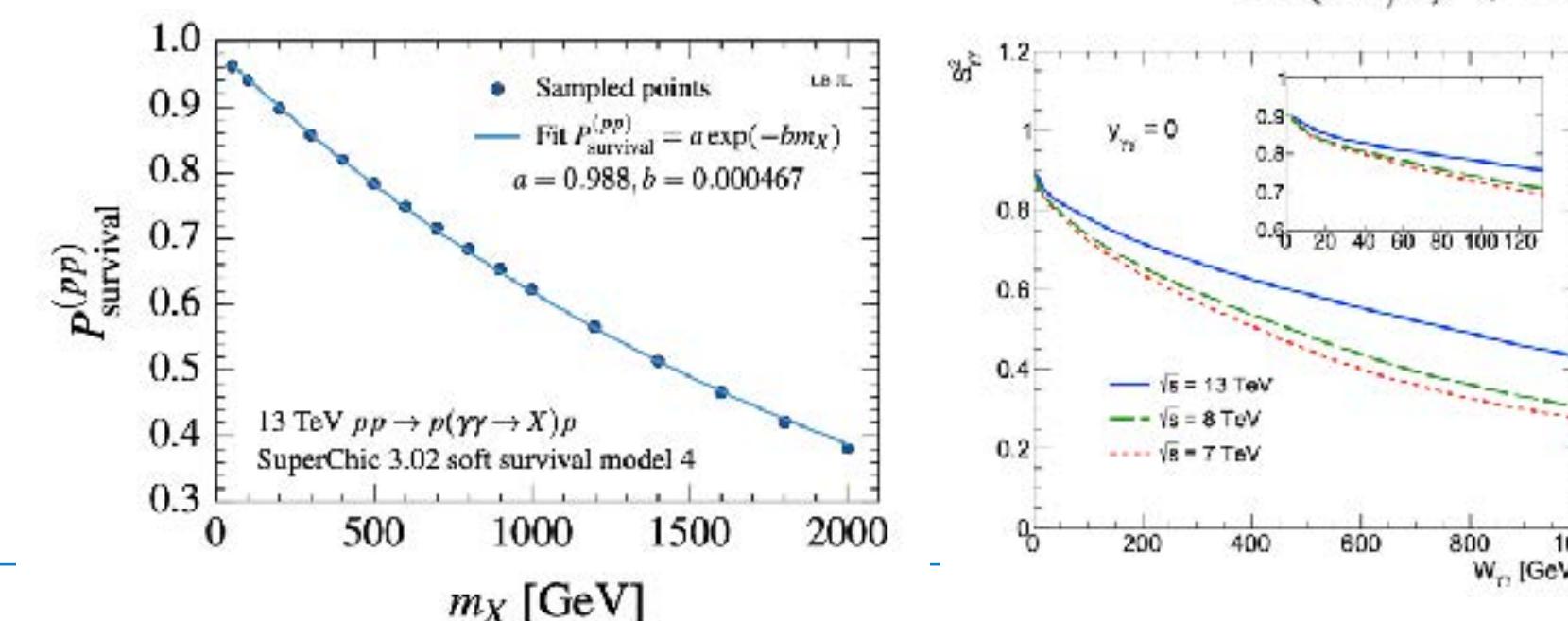
- ◆ Novel (?) idea that slepton can be probed via photon collision in the LHC [Beresford, Liu 1811.06465]

$$pp \rightarrow \gamma\gamma pp \rightarrow \tilde{\ell}\tilde{\ell}^* \rightarrow (\ell\tilde{\chi}_1^0)(\bar{\ell}\tilde{\chi}_1^0)$$

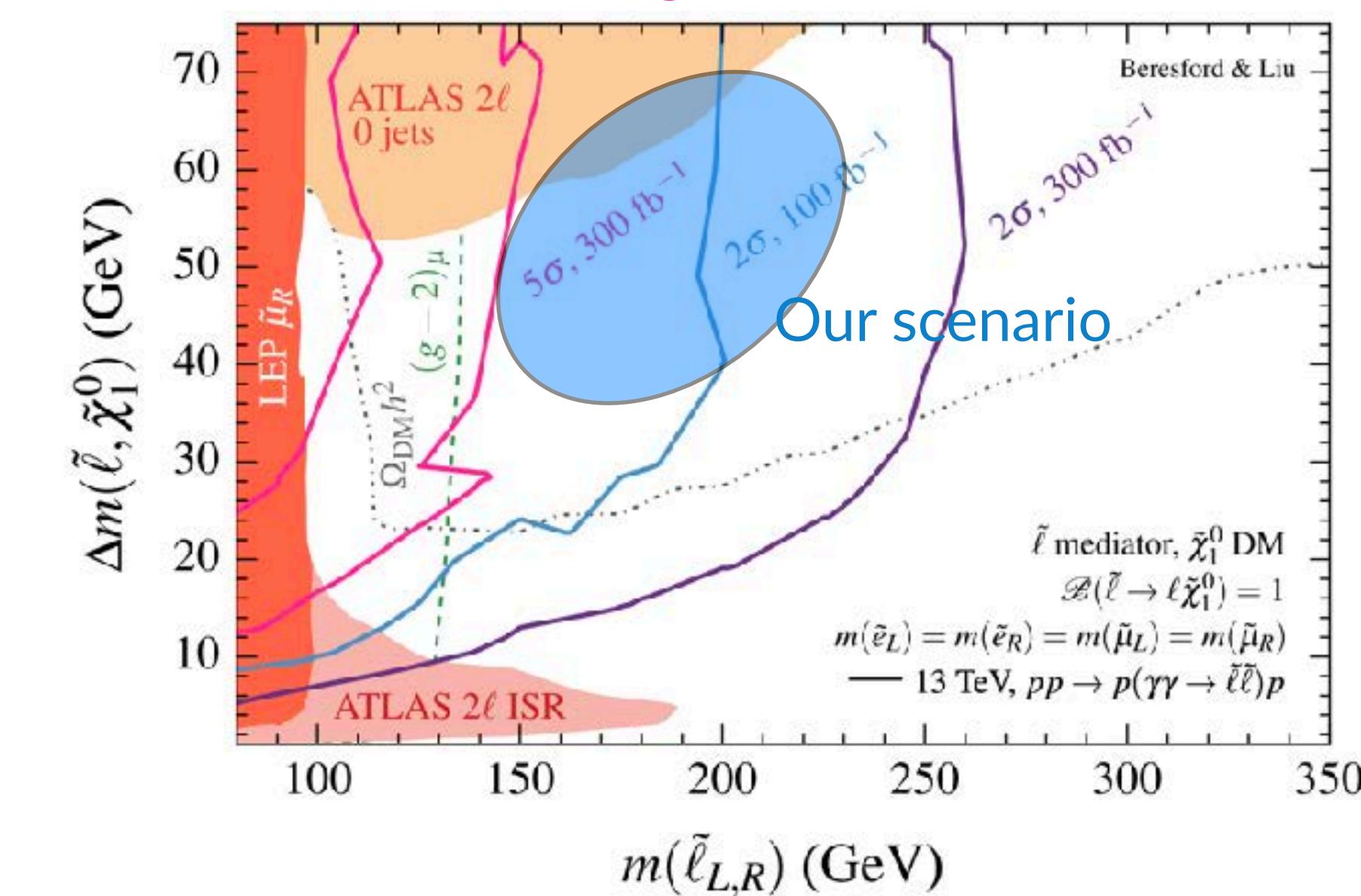


- 1, measure outgoing proton  $E_p$  by forward detector
- 2, measure lepton 4-momentum
- 3, reconstruct missing momentum 4-vector

Proton soft survival probability they used.  
Slightly optimistic?  
→ next slide

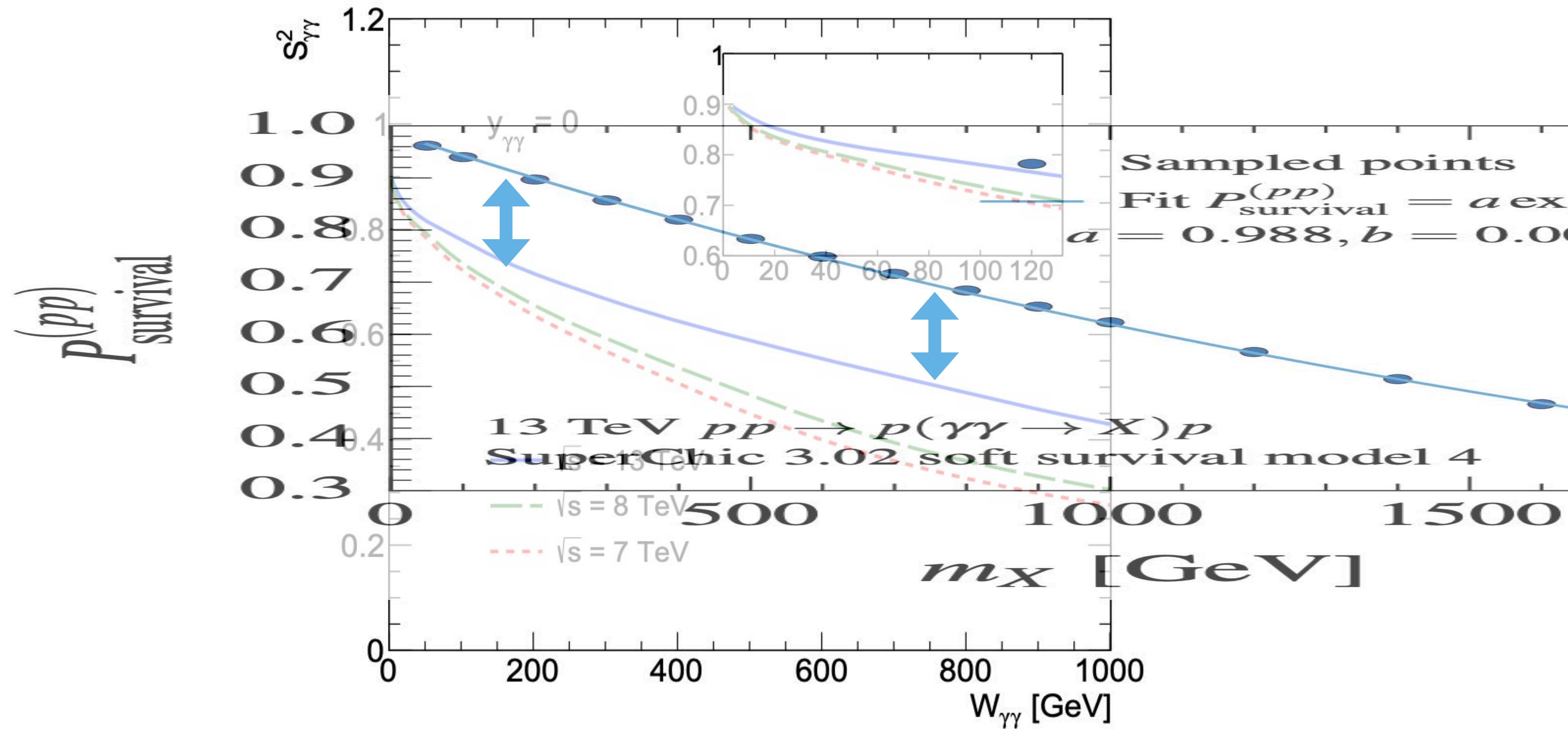


Slepton mass gap could be covered.



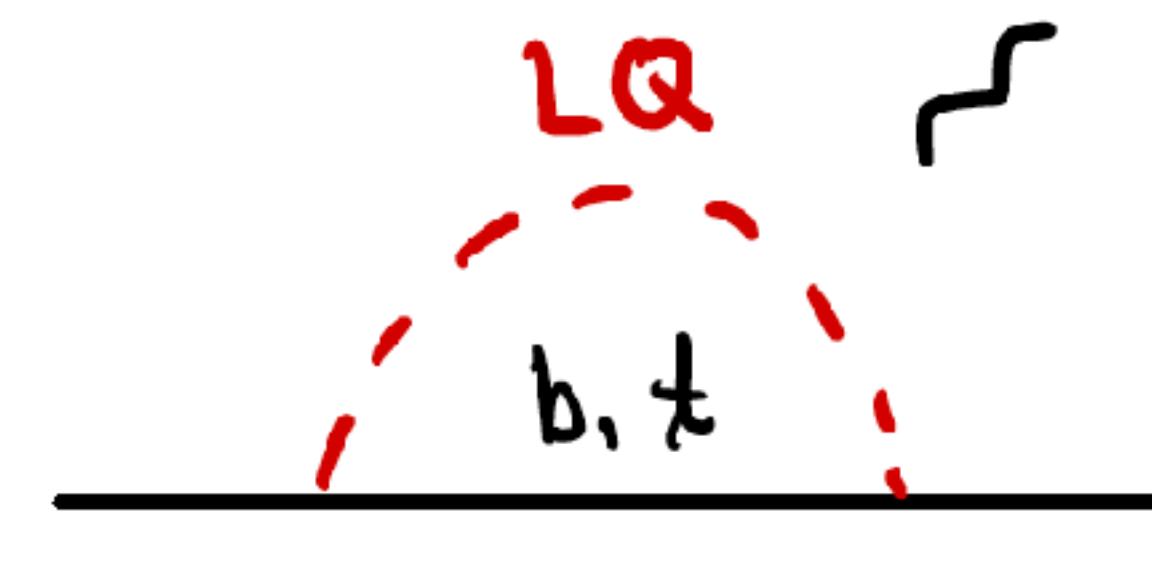
ATLAS first result  
[ATLAS, 2009.14537]  
agrees on [Dyndal et al,  
1410.2983]

# Comparison of proton survival probabilities



# Leptoquark models

- ◆ TeV-scale scalar/vector leptoquark can also explain muon  $g-2$  anomaly.

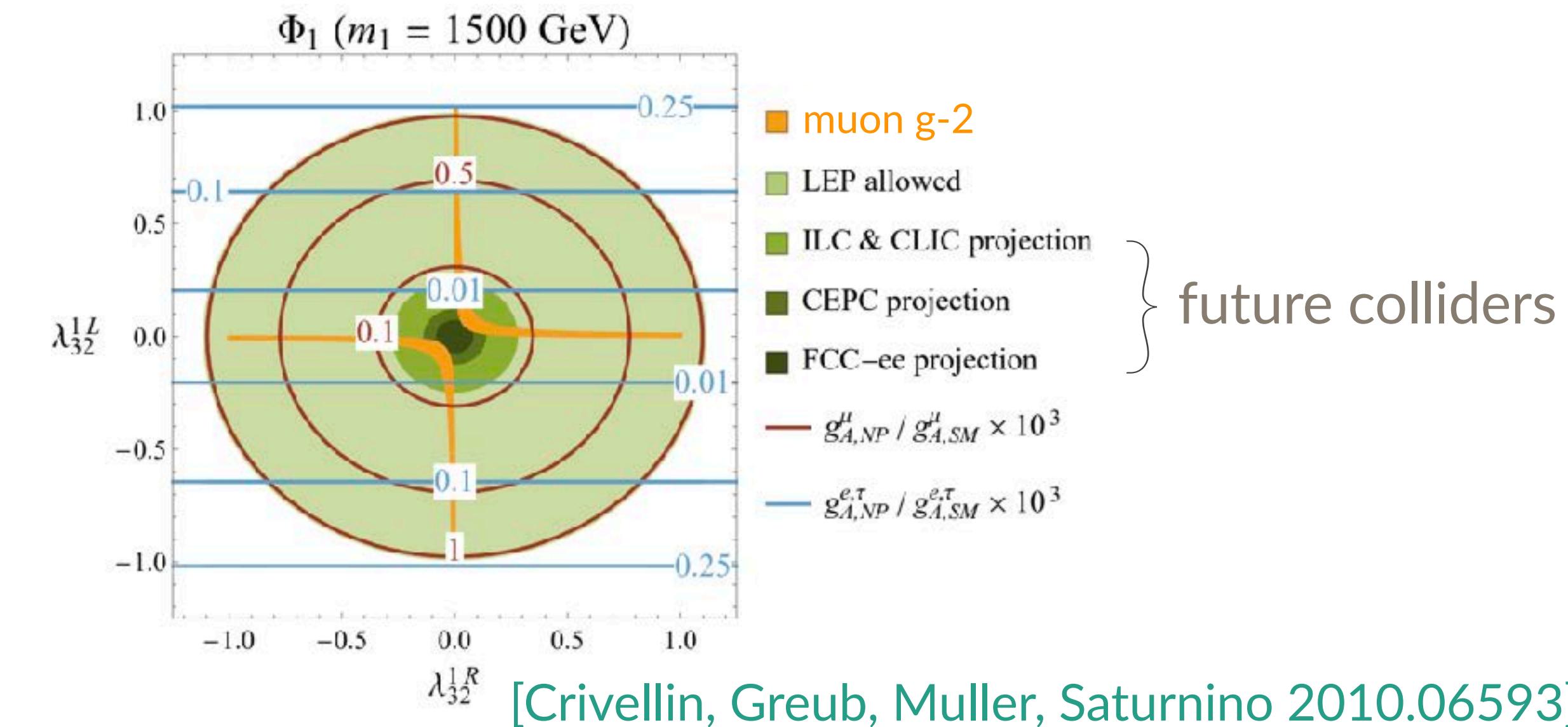


Top are preferred for the muon  $g-2$  anomaly because chirality enhancement is significant  
 $m_t/m_\mu \sim 2000 \rightarrow$  TeV scale leptoquark is possible

Correlation with  $Z \rightarrow \mu^+\mu^-$  can be probed by future colliders.

e.g., Low scale Pati-Salam model ( $SU(4) \times SU(2)_L \times SU(2)_R$ ) predicts TeV-scale leptoquark.

The charm, strange (2nd generation-philic) couplings are strongly constrained by flavor precision constraints. [Kowalska, Sessolo, Yamamoto 1812.06851]



[Crivellin, Greub, Muller, Saturnino 2010.06593]

*B* anomaly + muon g-2 anomaly = ?

# $(B + \text{muon } g-2)$ anomaly =?

- ◆ 5 (and more) examples on arXiv

Refs	particles	solve	mass scale
Arcadi et al, 2104.03228	Vector-like fermion + scalars	muon g-2, R(K), DM	0.1~1 TeV VL
Nomura, Okada 2104.03248	Scalar LQs	muon g-2, R(K), $m_\nu$	$\sim$ 5 TeV LQ
Bhattacharya et al, 2104.03947	ALP	muon g-2, $K\pi$ puzzle	$\sim$ 140 MeV ALP
Marzocca, Trifinopoulos, 2104.05730	Scalar LQ + scalar	muon g-2, R(K), R(D), CAA	$\sim$ 5 TeV LQ
Du et al, 2104.05685; Ban et al, 2104.06656	Vector LQ	muon g-2, R(K), R(D)	$\sim$ 2 TeV LQ

# Summary

- ◆ Fermilab collaboration confirmed the BNL muon  $g-2$  data.
- ◆ The standard model prediction is still controversial. Other lattice group's result or MUonE experiment at CERN will shed light on the HVP contributions.
- ◆ Several TeV scale or MeV scale new physics models have been suggested.
- ◆ Supersymmetric solutions are still survived.
  - ◆ But, mass spectrum would be not attractive (or we don't know such a SUSY breaking), e.g., gaugino masses.
  - ◆ Can the slepton search from photon collisions be possible in the LHC Run3?
- ◆  $B$  anomalies can be correlated with several TeV new physics models.