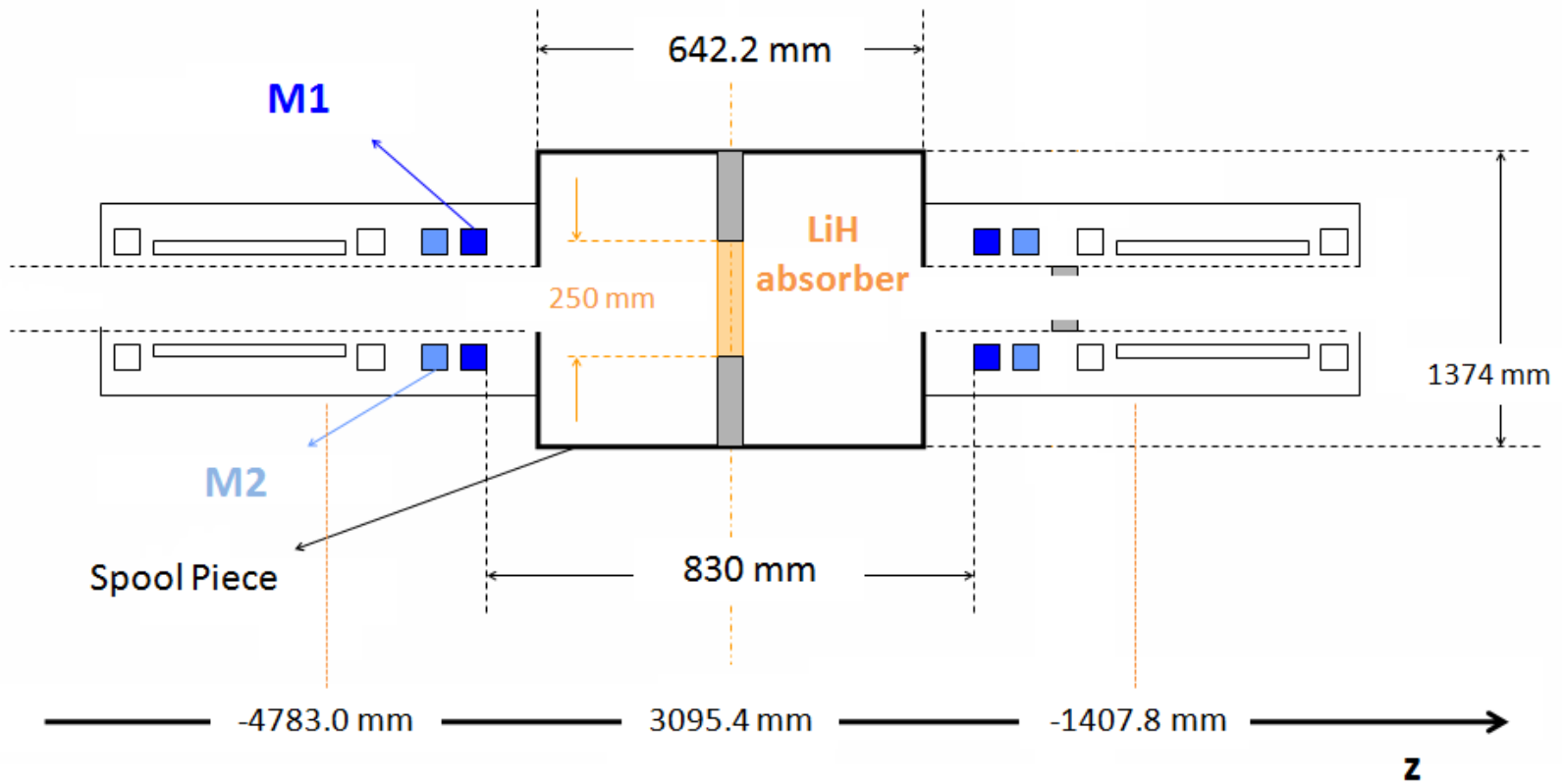


# A Comparison of Step 3 & Step 4

Timothy Carlisle, Oxford  
CM 28

# Step 3



## Matching Step 3

➤ Step 3 rematched for 830 mm spool piece

➤ Calc.  $B(z)$  & BetaFn with the following:

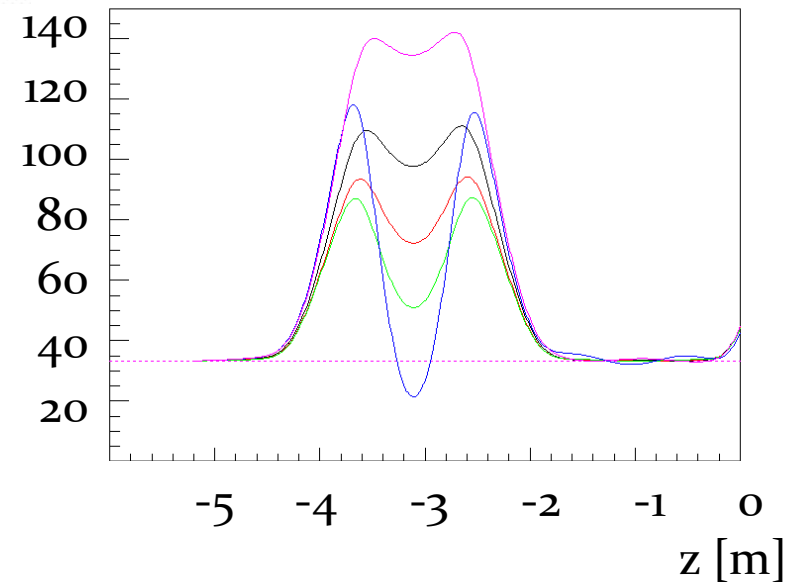
$$B_z = \frac{\mu_0 I n}{2} (\cos\alpha - \cos\beta)$$

$$2\beta\beta'' - (\beta')^2 + 4\beta^2\kappa^2 - 4 = 0$$

➤ Minimize  $F$  at 1 point in a const. field region in 2<sup>nd</sup> Tracker.

$$F = 0.5 * (\beta\gamma_0 - \alpha\alpha_0 + \beta_0\gamma)$$

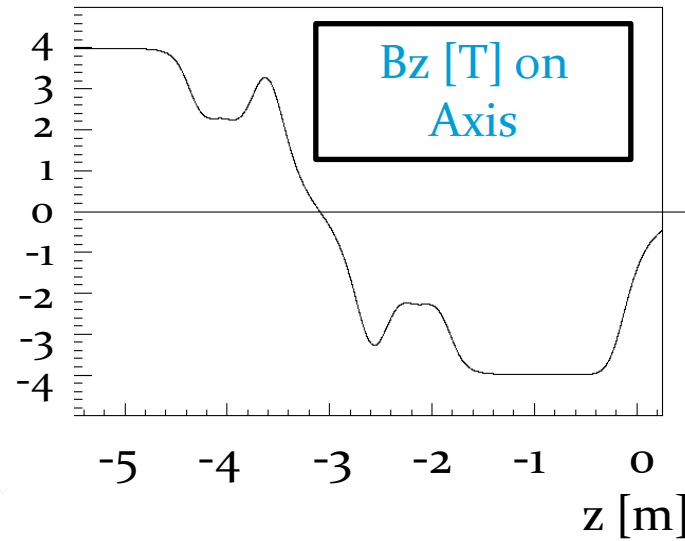
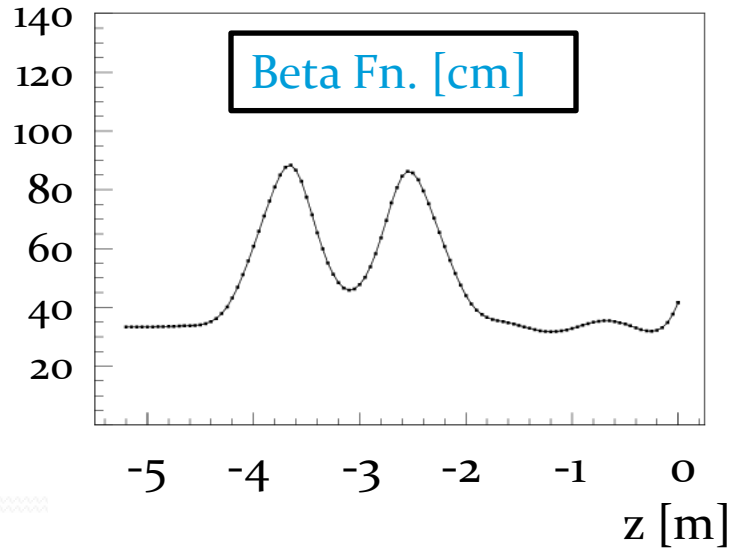
Beta Fn. [cm]



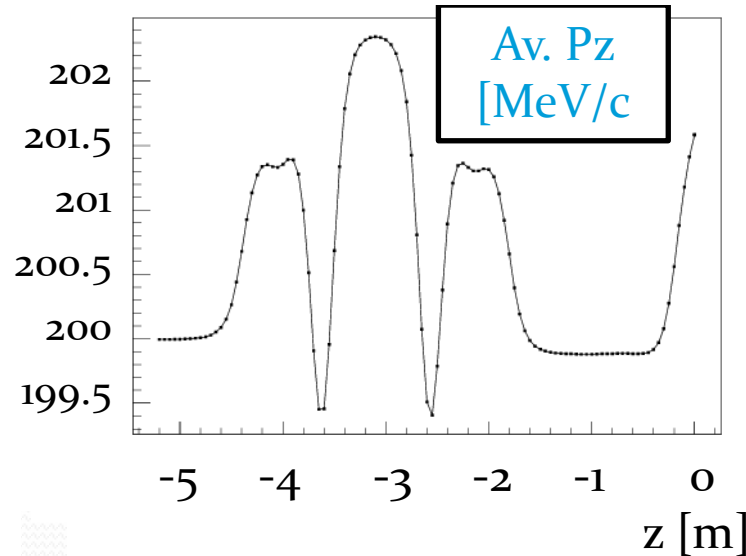
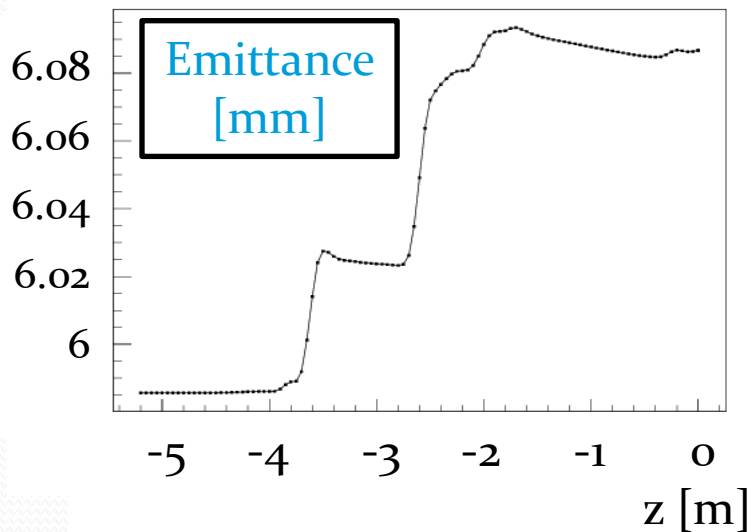
**Many solutions...**

# Step 3 Empty: 6mm $\epsilon$ beam

SigPz = 1 MeV/c, 100k muons

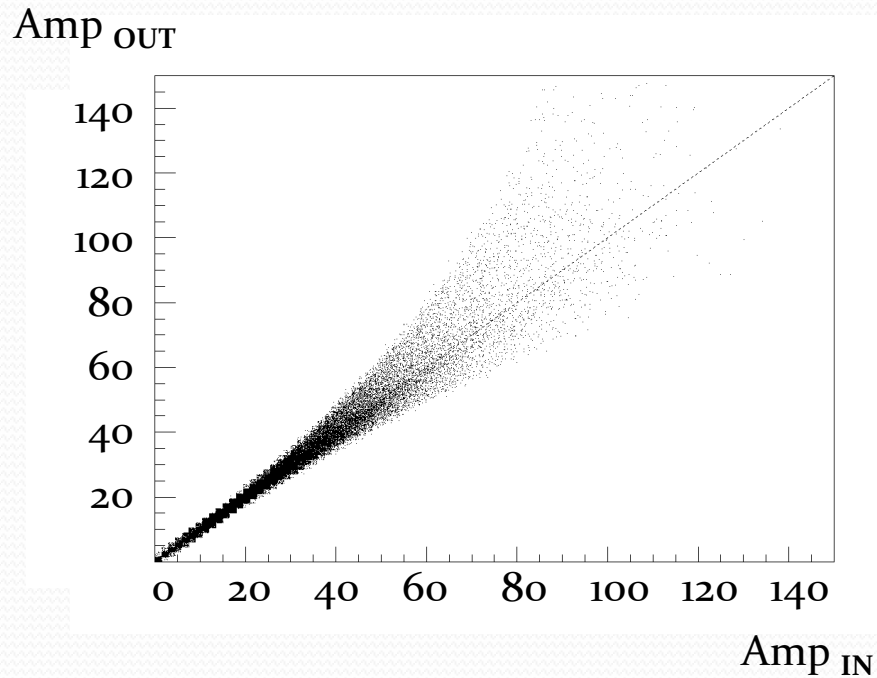


**M1 = 158.9**  
**M2 = 92.4**

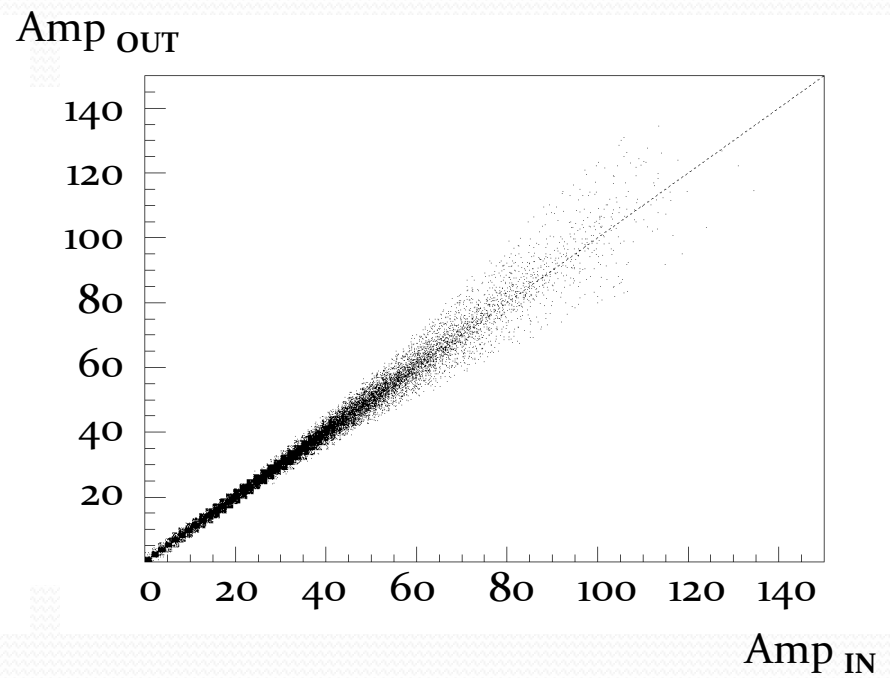


# Amplitude Cooling...

Step 3 empty



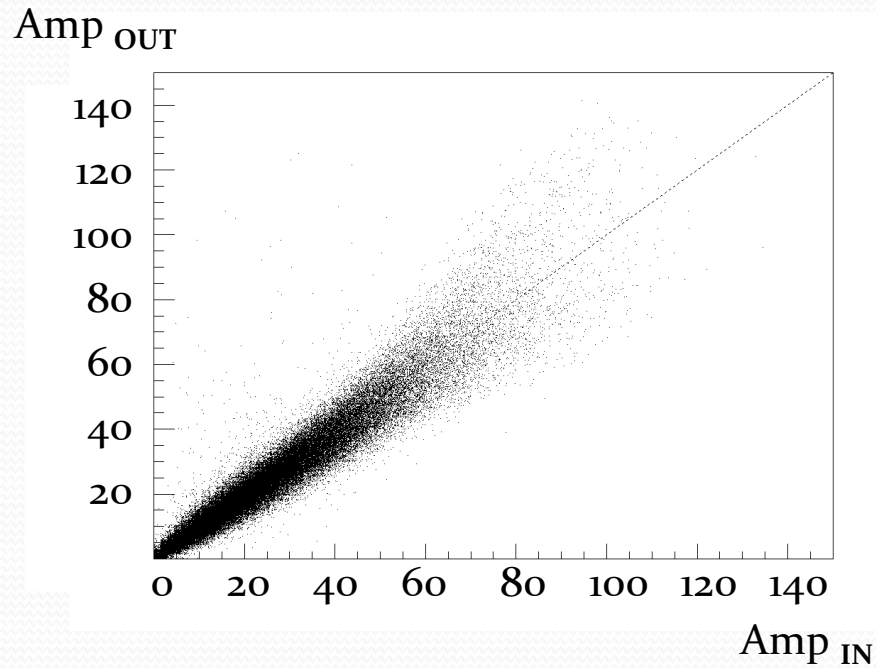
Step 4 empty



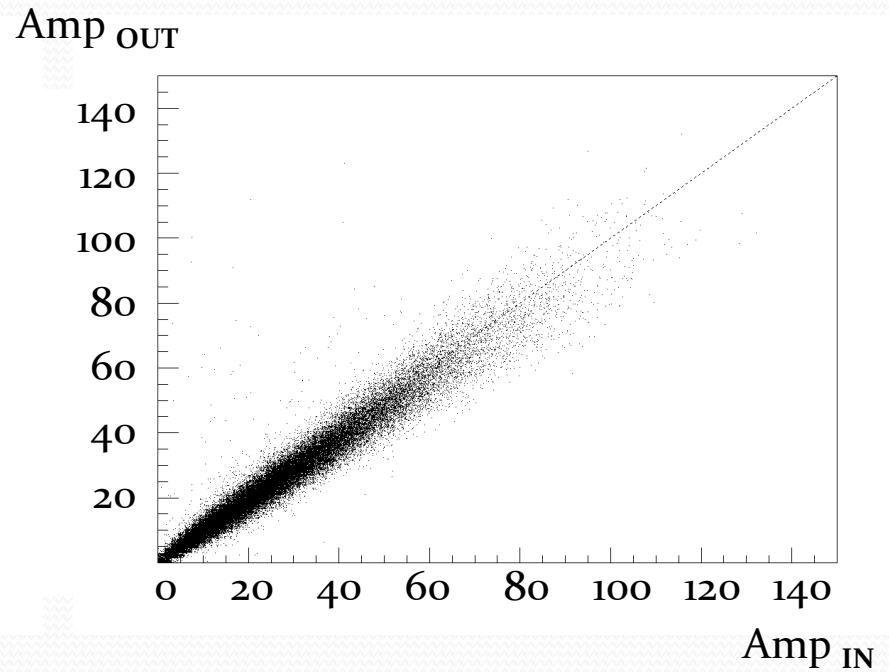
6mm beam, SigPz = 1 MeV/c, 100k muons

# Amplitude Cooling...

## Step 3: LiH

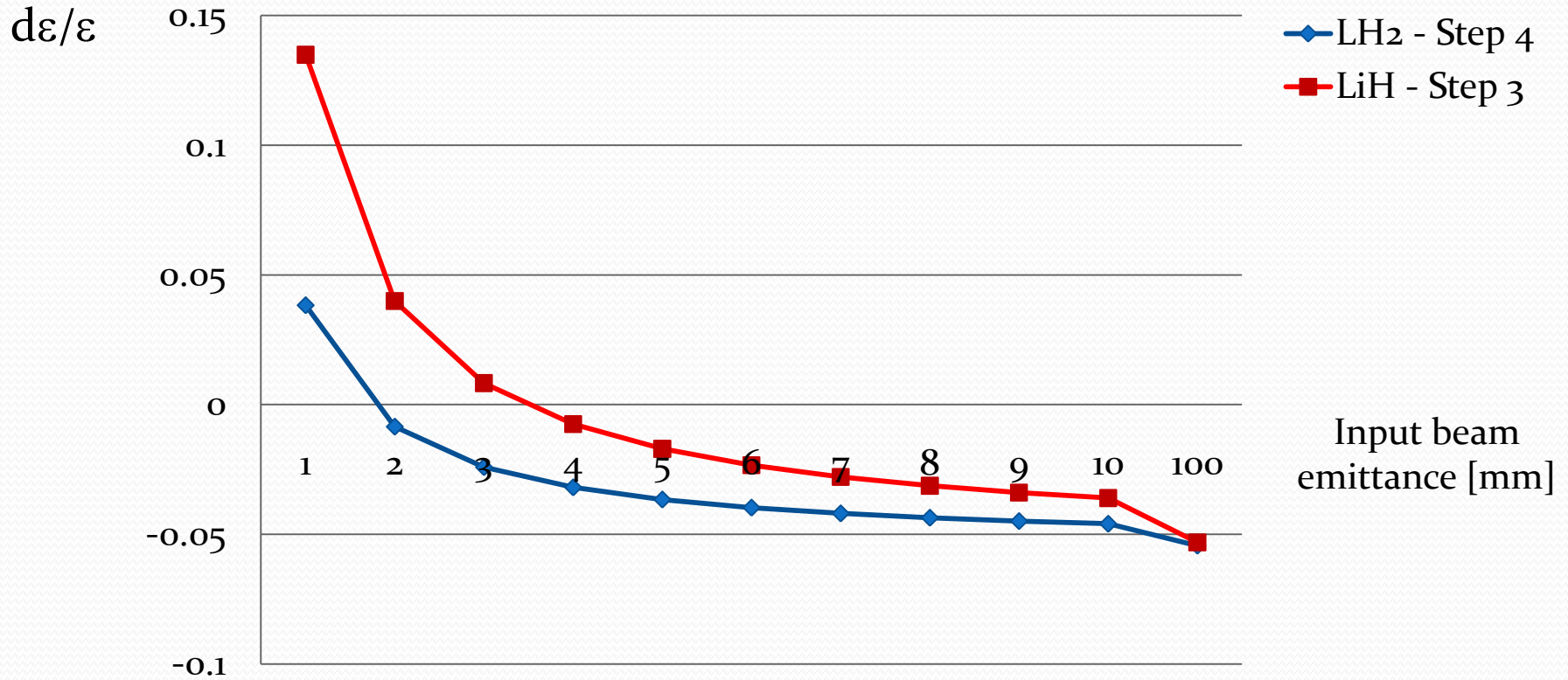


## Step 4: LH<sub>2</sub>



6mm beam, SigPz = 1 MeV/c, 100k muons

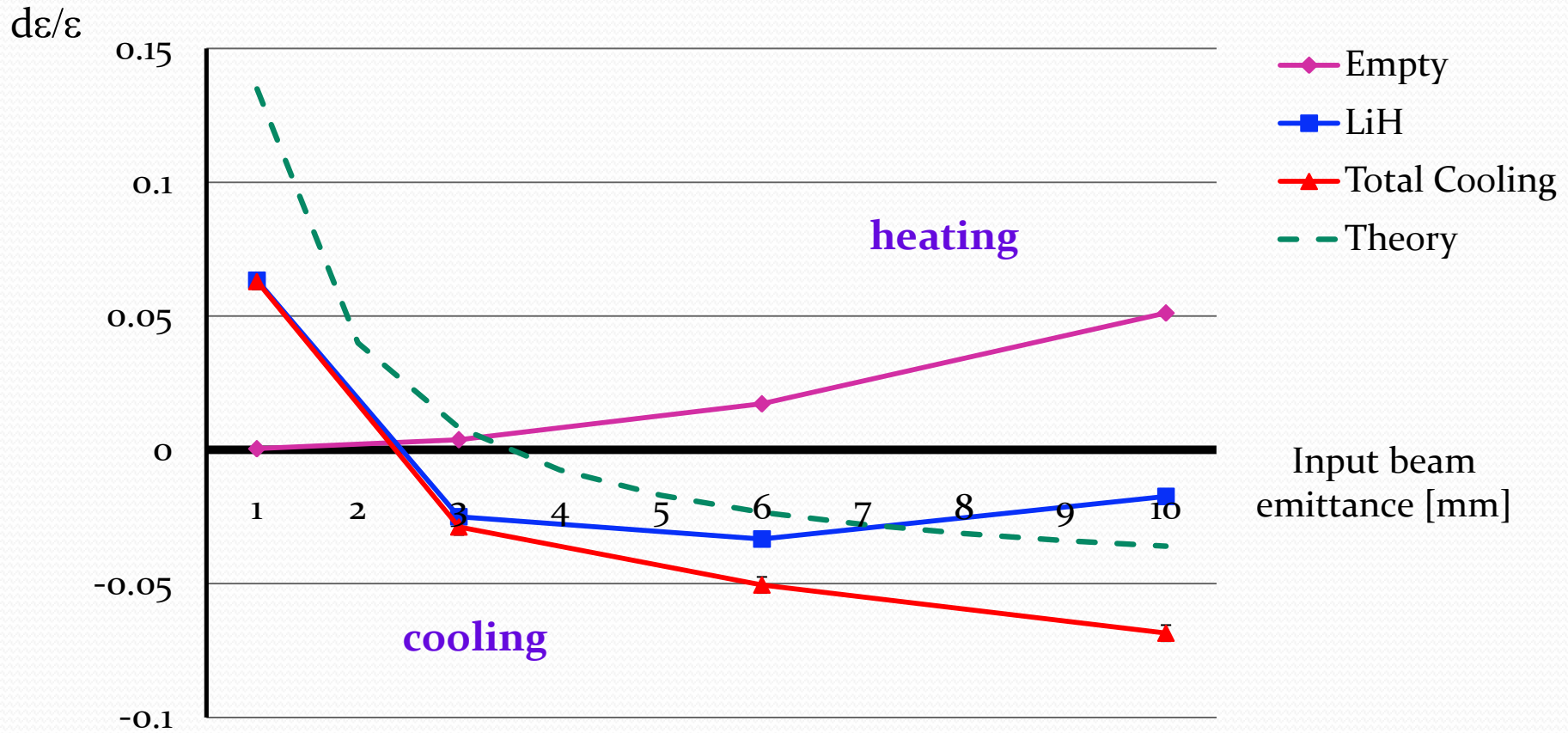
# Theoretical Cooling Performance



$$\frac{d\epsilon_n}{dz} = \frac{-\epsilon_n}{\beta^2 E} \left\langle \frac{dE}{dX} \right\rangle + \frac{\beta_t}{2\beta^3 E m_\mu X_0} (0.014 \text{ GeV})^2$$

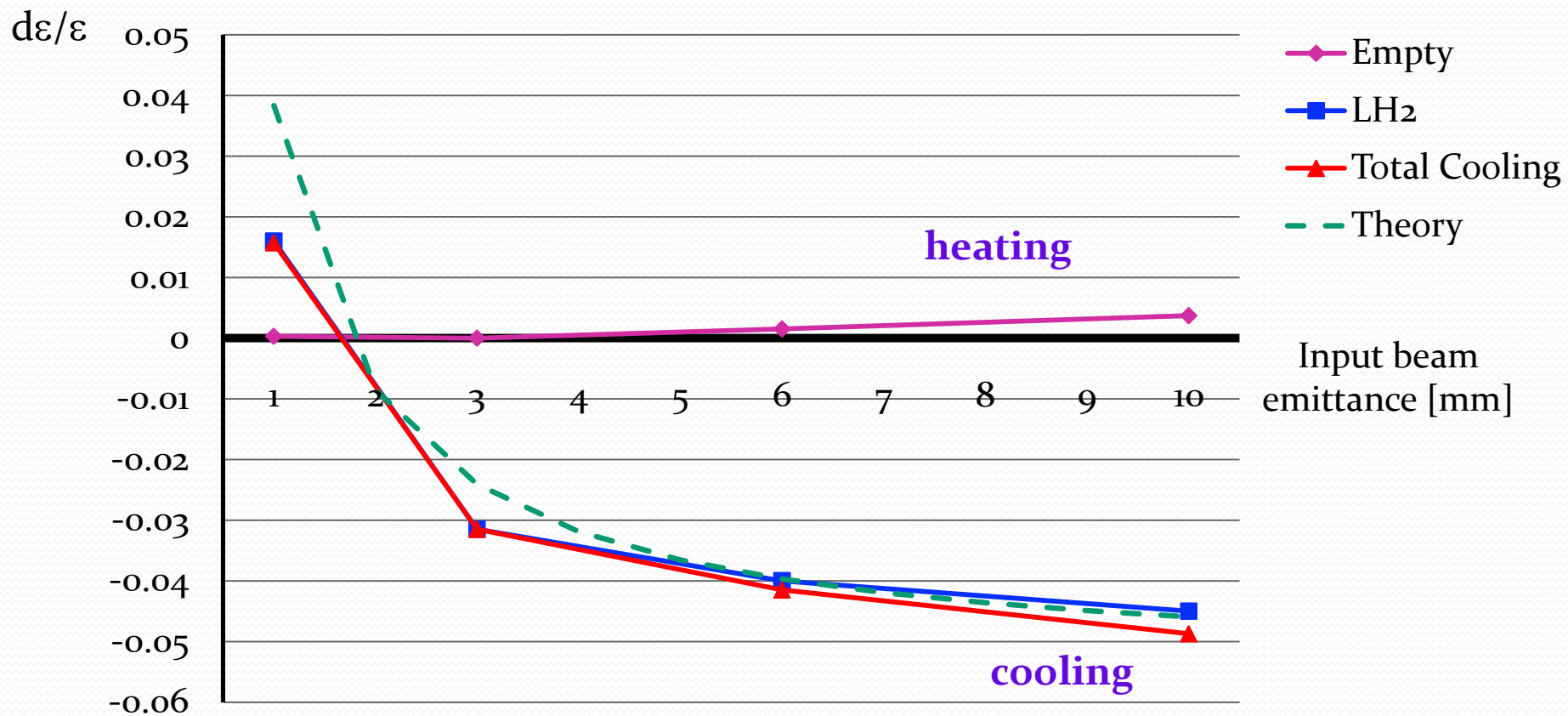
# Step 3

G4MICE : 100k mu, SigPz =1 MeV/c





# Step 4



# Step IV but without FC

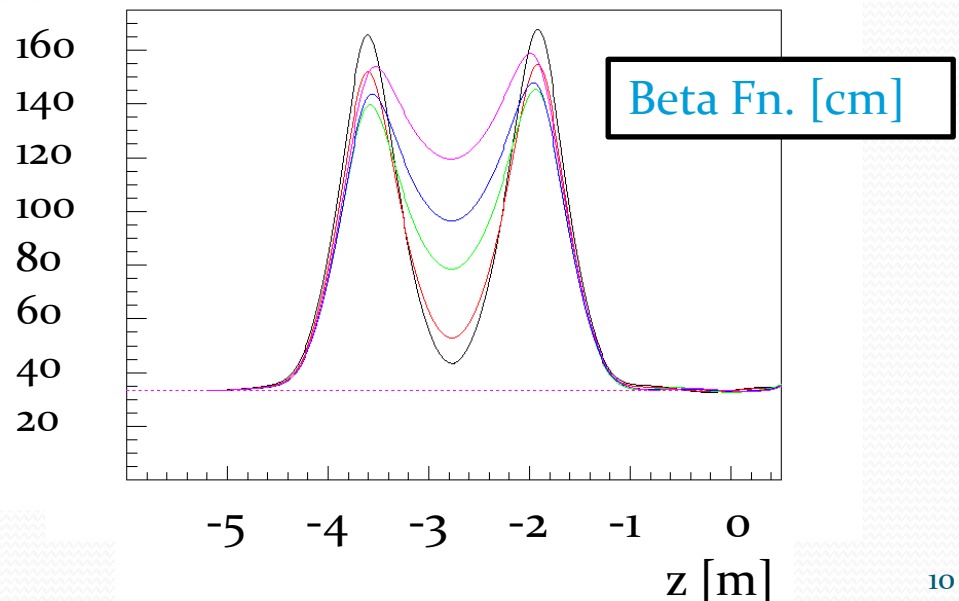
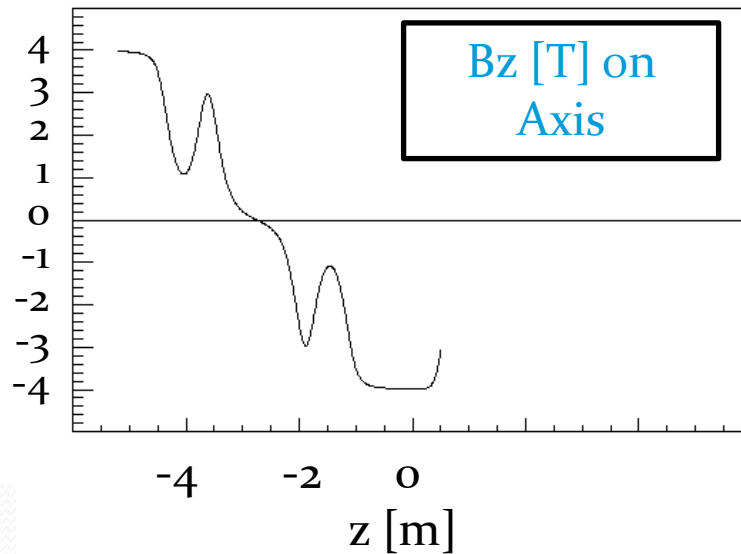
➤ Focus Coil switched off

➤ No LH<sub>2</sub>

➤ Minimized F<sub>n</sub> at z = -0.3 m  
~ centre of 2<sup>nd</sup> Tracker

$$F = 0.5 * (\beta \gamma_0 - \alpha \alpha_0 + \beta_0 \gamma)$$

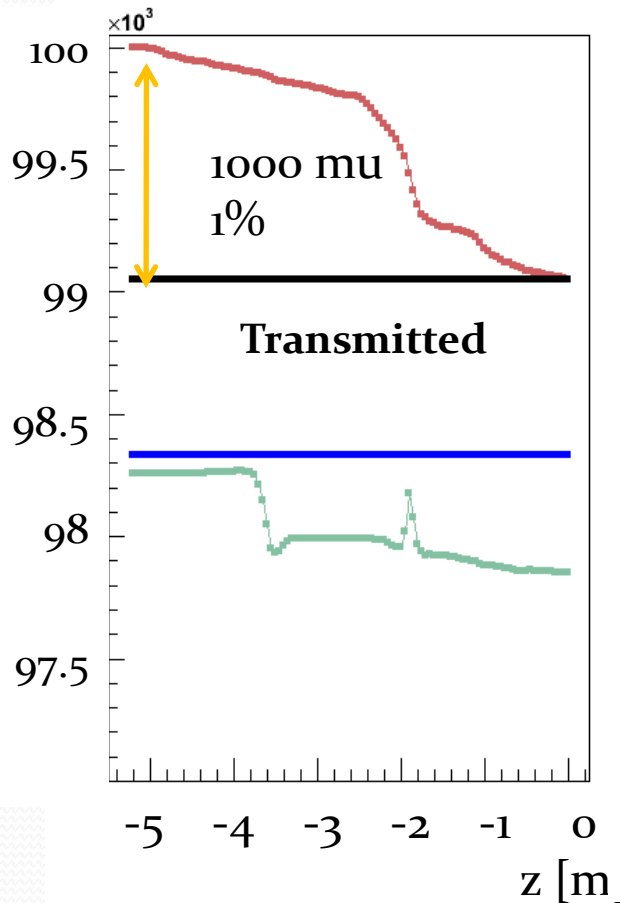
➤ Range of solutions:



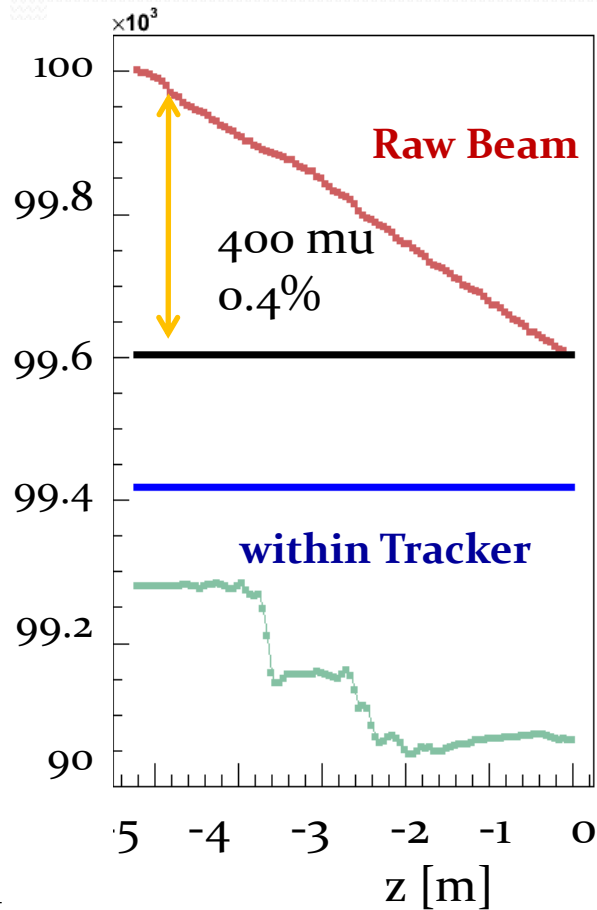
# Transmission

6mm beam, SigPz = 1 MeV/c, 100k muons

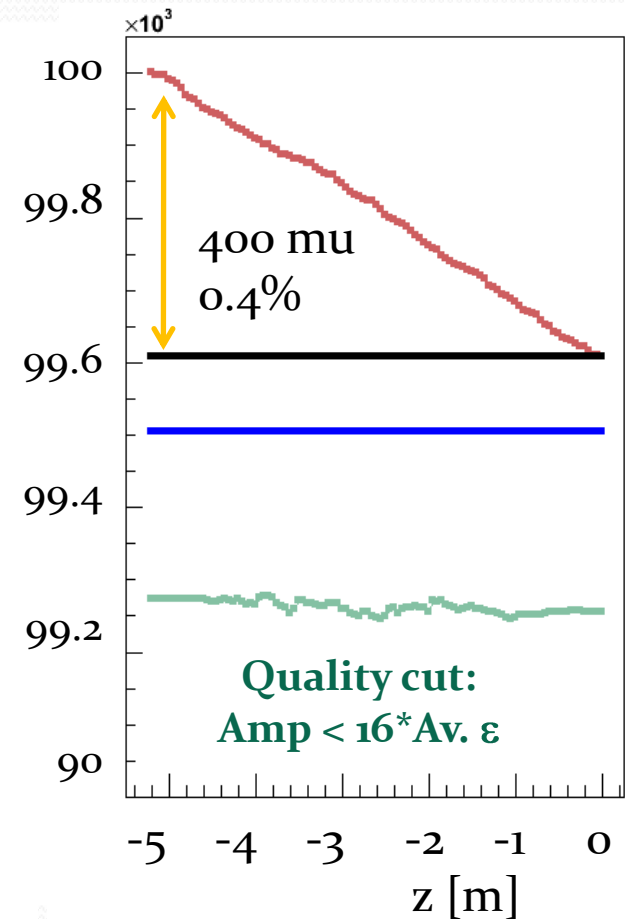
Step 4: No FC currents



Step 3: Empty



Step 4: Empty



# Conclusions

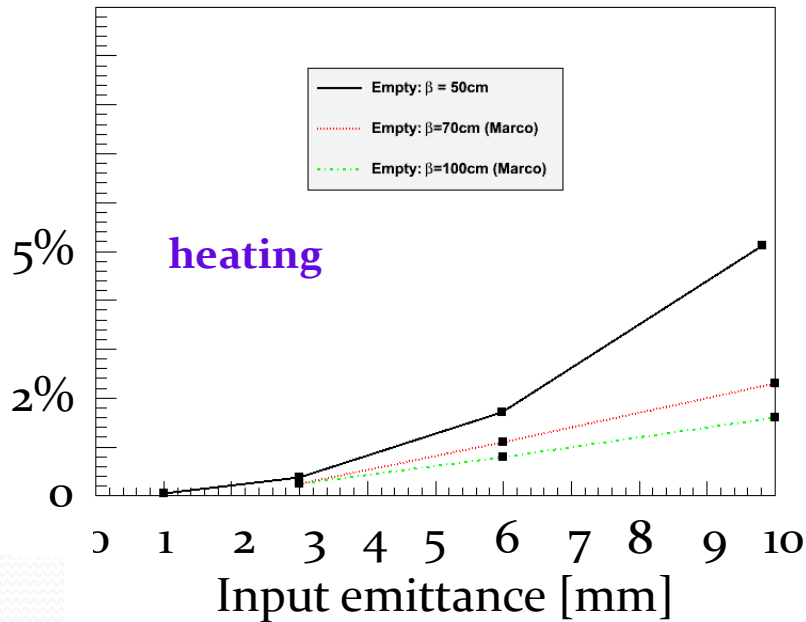
- Clearly more difficult to measure cooling in Step 3
  - ~10 x more heating than Step 4
- Step 3 cooling disagrees with theory
  - $\varepsilon_o < \text{theory}$  – don't know why (same in ICOOL)
- Need to include Tracker reconstruction...
- It appears we can run Step 4 without FC currents
  - Is this useful – Trackers?
- Can we run Step 4 with no currents in M<sub>1</sub>, M<sub>2</sub> & FC?
  - Alignments?



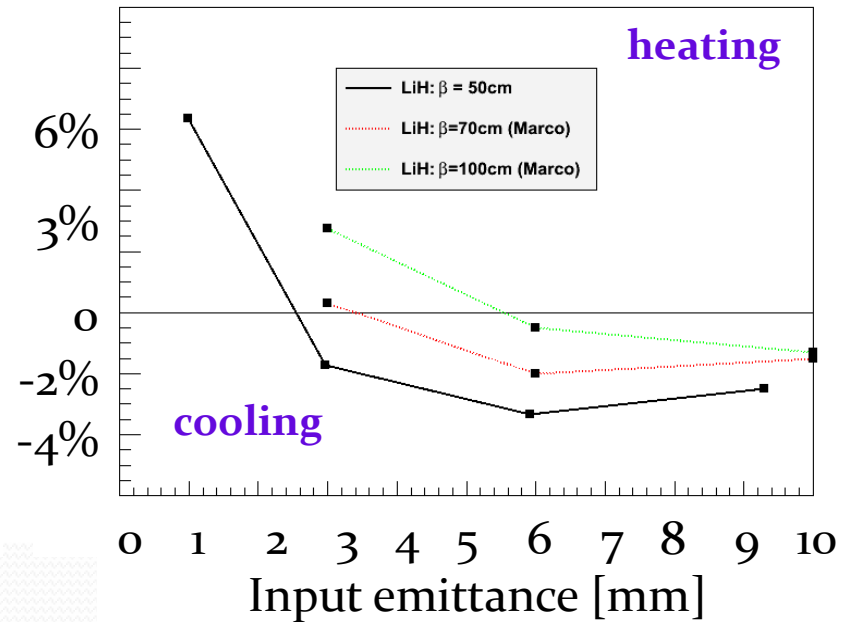
Extras...

# Step 3 — comparison with existing data..

## Empty Channel



## LiH absorber

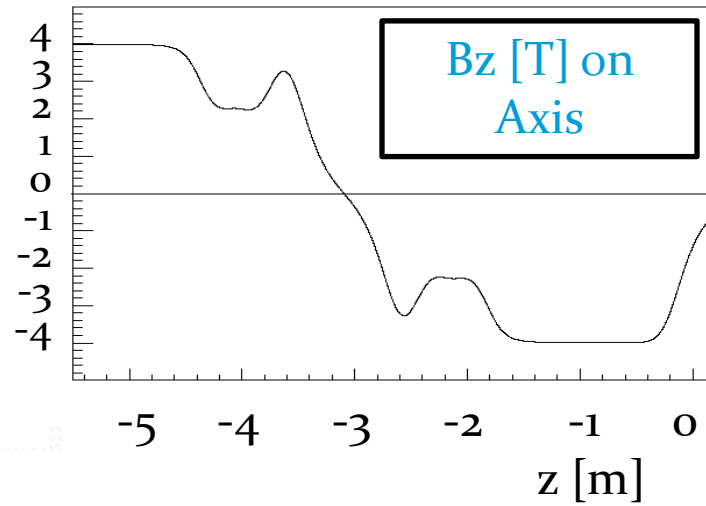
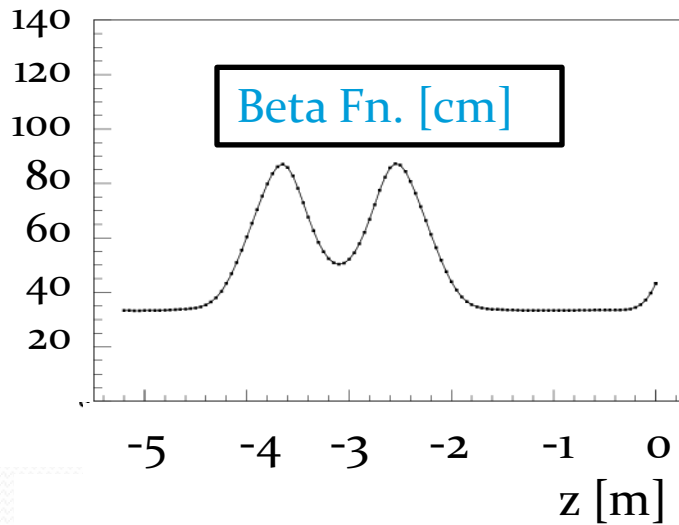


**Black Data:** 100k mu, SigPz = 1 MeV/c, G4MICE

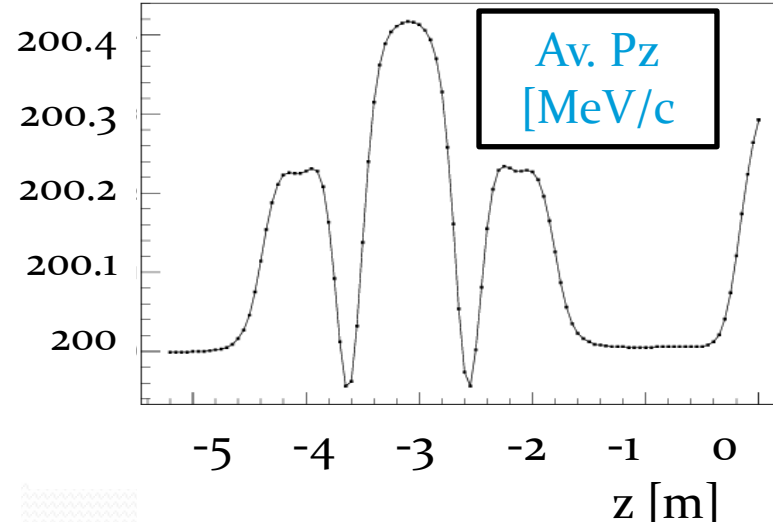
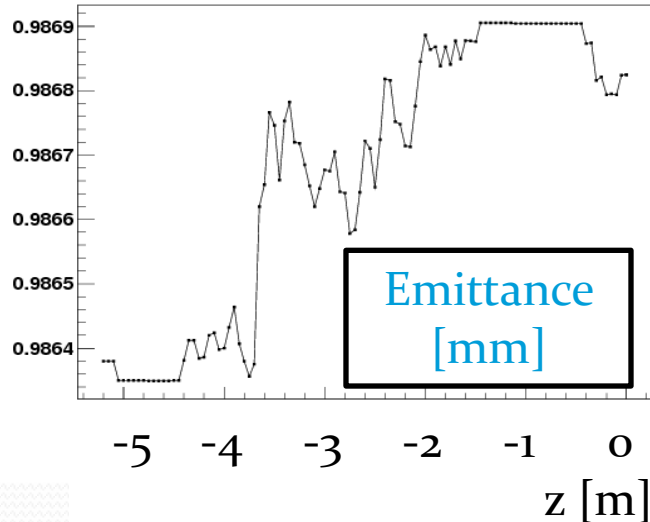
**Marco Data:** 10k mu, SigPz = big (10%), ICOOL – note 199

# Step3 Empty: 1mm $\epsilon$ beam

SigPz = 1 MeV/c, 100k muons

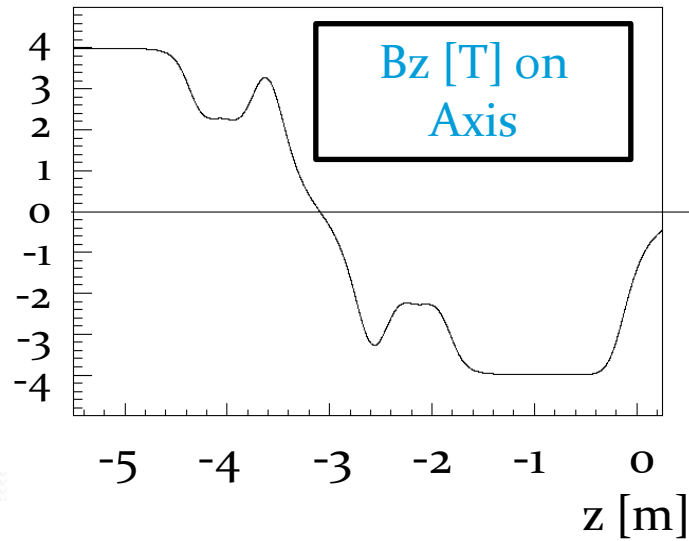
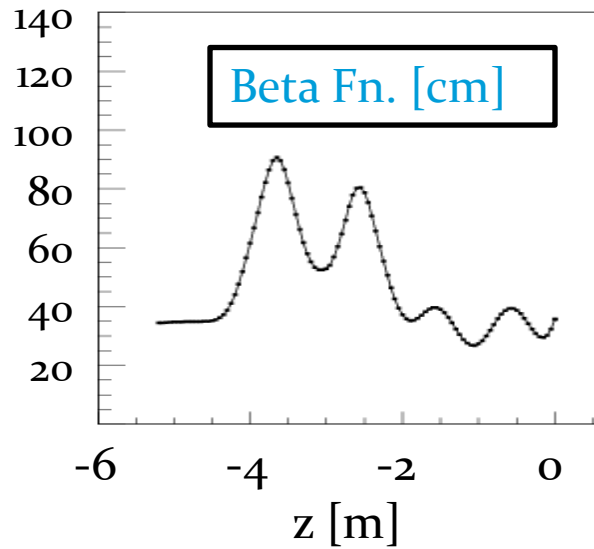


$M_1 = 158.9$   
 $M_2 = 92.4$

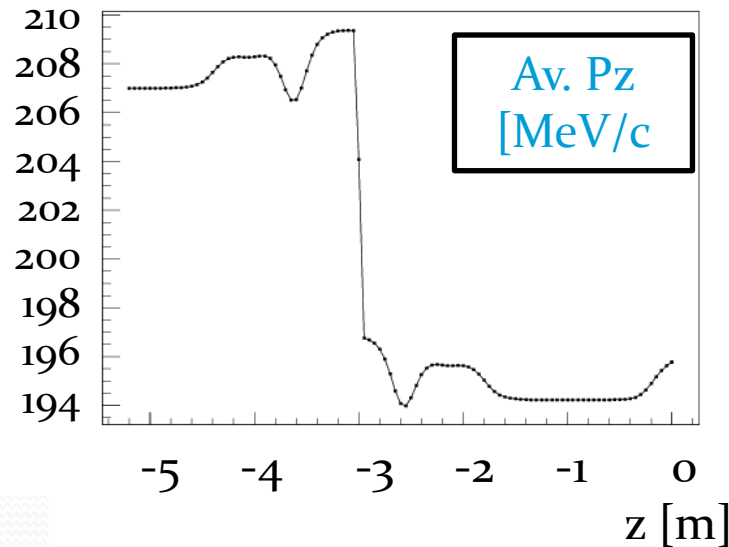
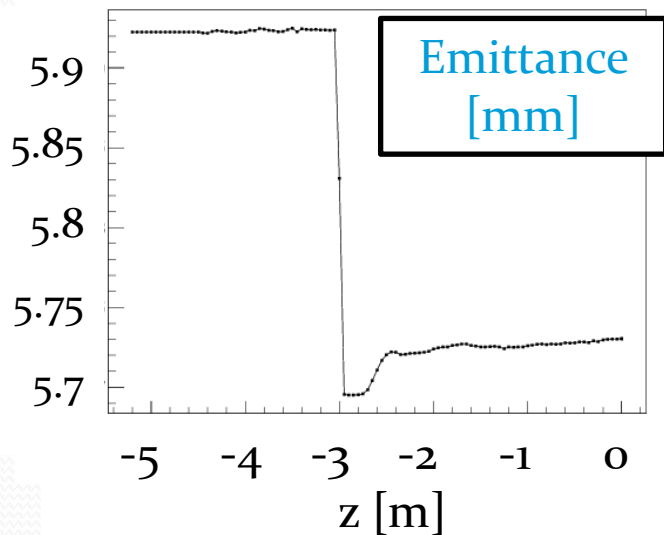


# Step 3 LiH: 6mm $\epsilon$ beam

SigPz = 1 MeV/c, 100k muons



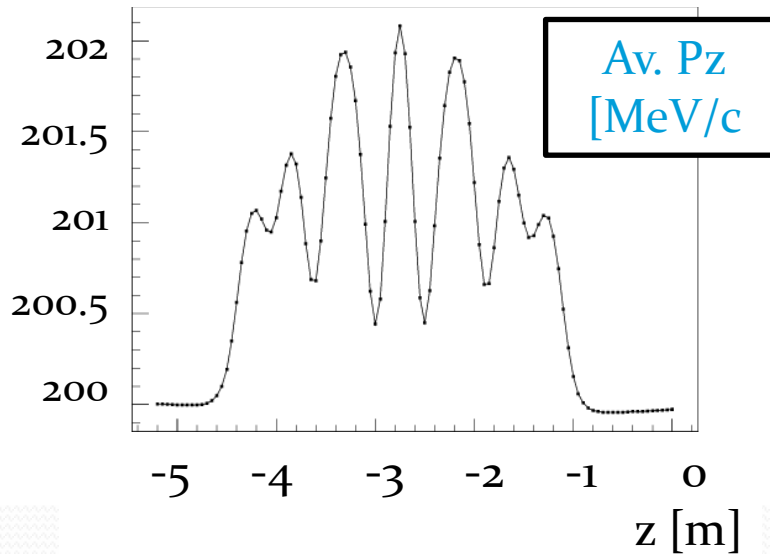
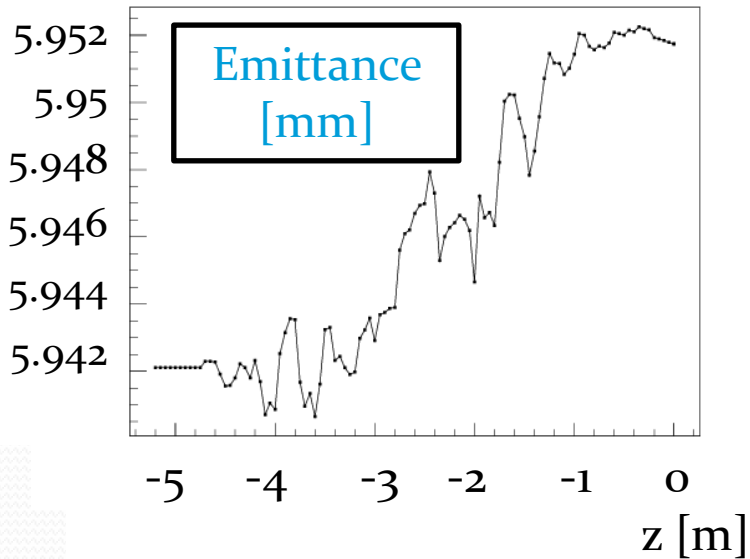
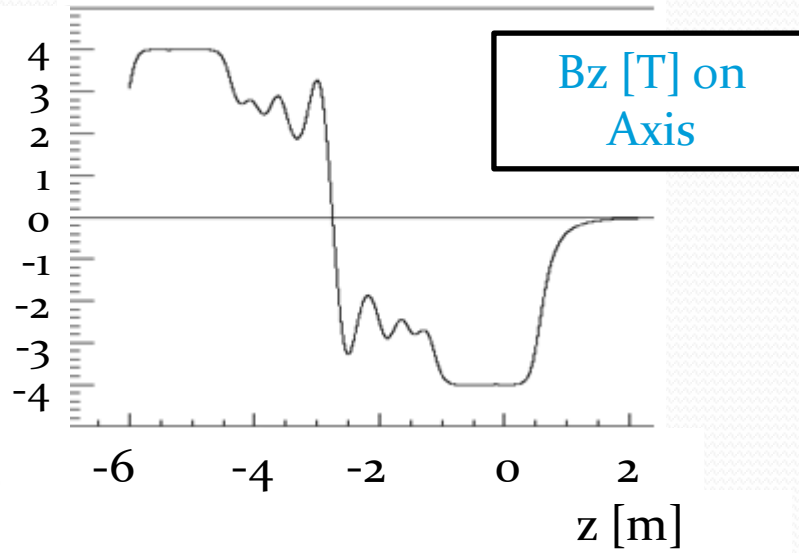
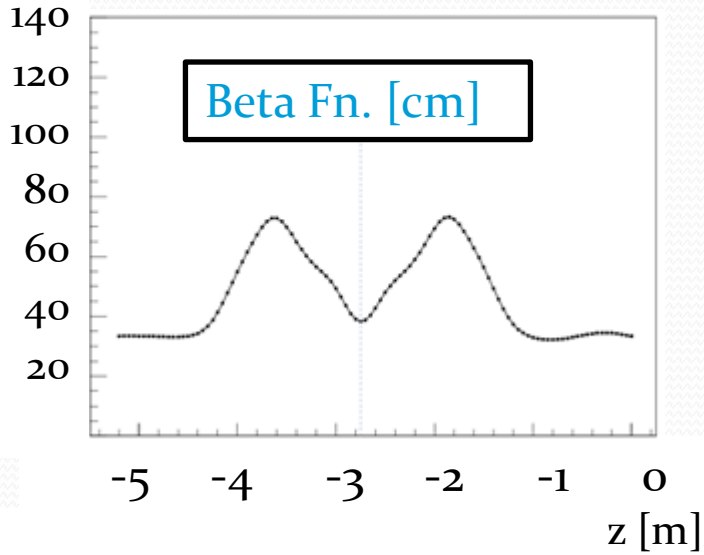
**M1 = 158.9**  
**M2 = 92.4**





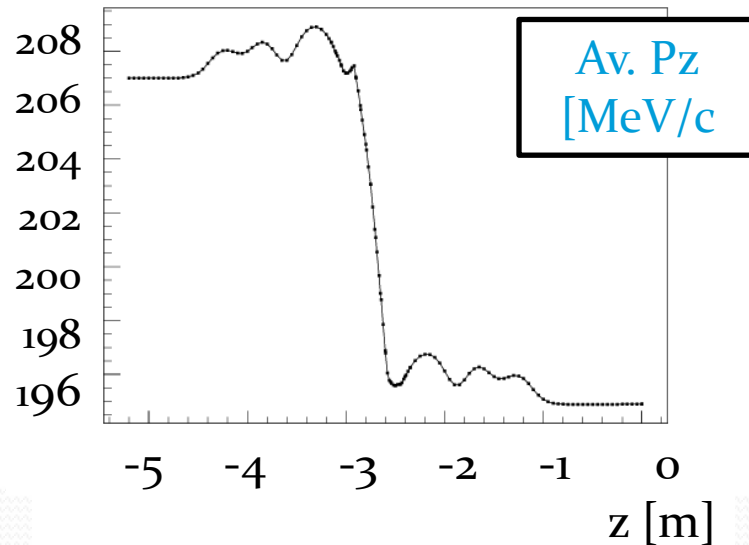
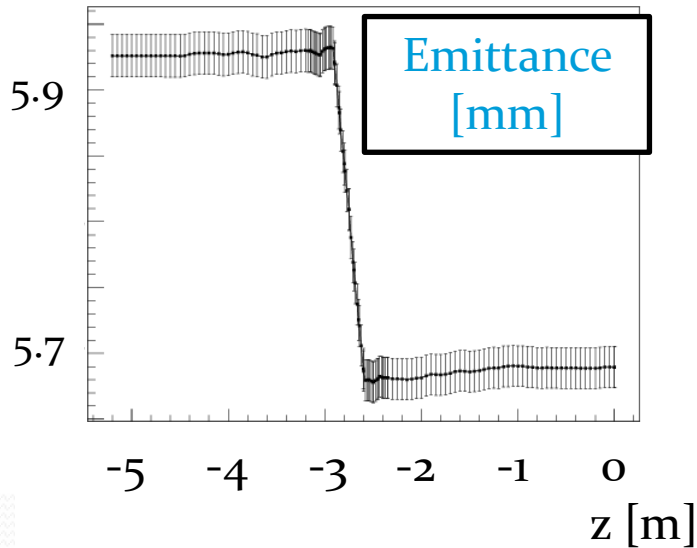
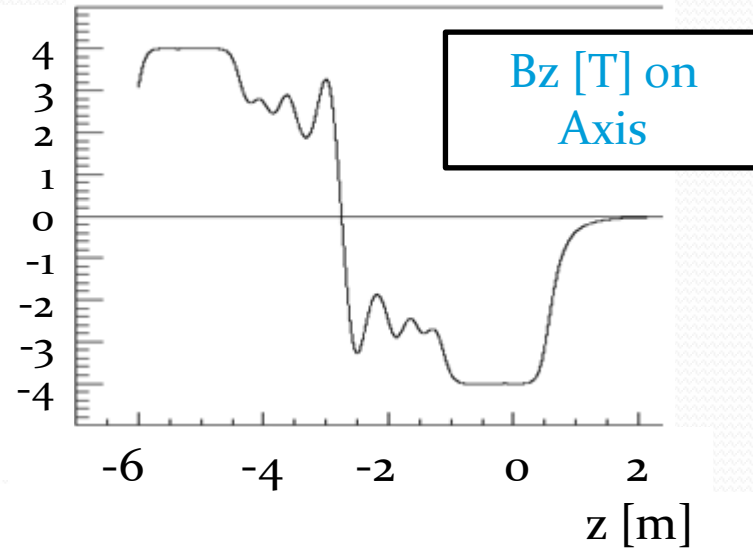
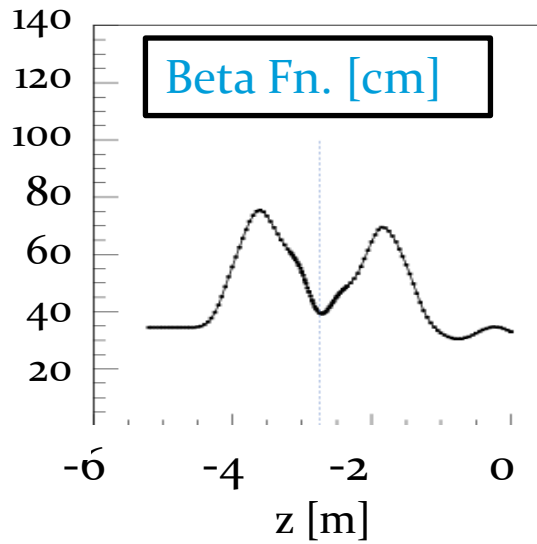
# Step 4 Empty: 6mm $\epsilon$ beam

SigPz = 1 MeV/c, 100k muons



# Step 4 LH2: 6mm $\epsilon$ beam

SigPz = 1 MeV/c, 70k muons



# Output AmpSq

