

# *Semi-hard reactions at the Forward Physics Facility*

Michael Fucilla

Università della Calabria & INFN - Cosenza

in collaboration with

A.D. Bolognino, F.G. Celiberto, D.Yu. Ivanov, M.M.A. Mohammed, A. Papa

## 2nd Forward Physics Facility Meeting



28th May 2021

*BFKL resummation*

*Semi-hard sector*

*Conclusions*

What is the BFKL resummation?

- The **Balitsky-Fadin-Kuraev-Lipatov (BFKL)** approach is the general framework for the resummation of energy-type logarithms
  - Leading-logarithm-Approximation (LLA):  $(\alpha_s \ln s)^n$
  - Next-to-leading-logarithm-Approximation (NLLA):  $\alpha_s (\alpha_s \ln s)^n$

In which contexts can BFKL approach be applied?

- **Semi-hard** collision processes, featuring the scale hierarchy

$$s \gg Q^2 \gg \Lambda_{\text{QCD}}^2, \quad Q^2 \text{ a hard scale}$$

$$\alpha_s(Q^2) \ln\left(\frac{s}{Q^2}\right) \sim 1 \implies \text{all-order resummation needed}$$

- **UGDs sector**  $\leftarrow$  [**Talk by F. Celiberto**]

The evolution of the **unintegrated gluon density**

$$\mathcal{F}(x, \vec{k}) \quad \text{t.c.} \quad f^g(x, Q^2) = \int \frac{d^2 \vec{k}}{\pi \vec{k}^2} \mathcal{F}(x, \vec{k}) \theta(Q^2 - \vec{k}^2)$$

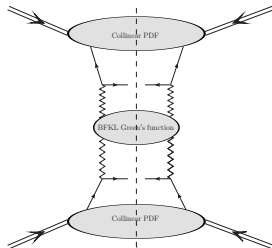
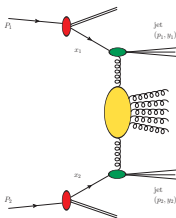
as a function of  $\ln(1/x) = \ln(s/Q^2)$ , is governed by BFKL:

$$\frac{\partial \mathcal{F}}{\partial \ln(1/x)} = \mathcal{F} \otimes \mathcal{K}$$

# Hybrid collinear/high-energy factorization

## Mueller-Navelet jets

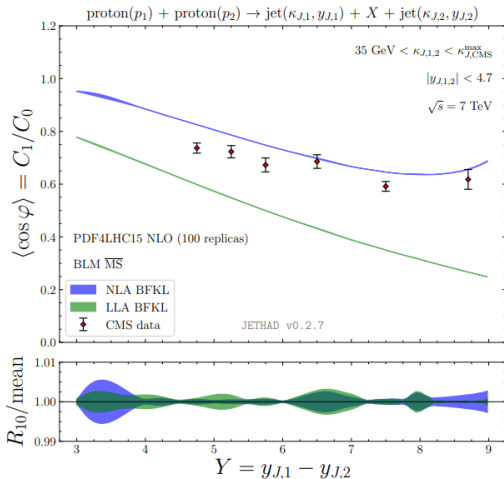
- Inclusive two jet production in proton-proton collision
- Large  $p_T$  and large rapidity separation
- Large energy logarithms  $\rightarrow$  BFKL resummed partonic cross section
- Moderate values of parton  $x \rightarrow$  collinear PDFs



$$\frac{d\sigma_{pp}}{dy_Q dy_J d|\vec{p}_Q| d|\vec{p}_J| d\phi_1 d\phi_2} = \frac{1}{(2\pi)^2} \left[ C_0 + 2 \sum_{n=1}^{\infty} \cos(n\phi) C_n \right]$$

- **Hybrid** formalism: can be extended to several type of semi-hard reactions

# Muller-Navelet: Theory vs Experiment



[B. Ducloué, L. Szymanowski, S. Wallon (2013)]

[F. Caporale, D.Yu. Ivanov, B. Murdaca, A. Papa (2014)]

In this slide: [F. Celiberto (2021)]

# Mueller-Navelet: Theory vs Experiment

- CMS @7Tev with symmetric  $p_T$ -ragens, only! [CMS collaboration (2016)]
- LHC kinematic **domain** in between the sectors described by BFKL and DGLAP approaches
- Clearer manifestation of high-energy signatures expected at increasing energies (higher hadronic center-of-mass energy or higher rapidity difference between tagged jets)
- Need for more exclusive final states as well as more sensitive observables
- Strong manifestation of higher-order **instabilities** via scale variation

# Mueller-Navelet: Theory vs Experiment

- CMS @7Tev with symmetric  $p_T$ -ragens, only! [CMS collaboration (2016)]
- LHC kinematic **domain** in between the sectors described by BFKL and DGLAP approaches
- Clearer manifestation of high-energy signatures expected at increasing energies (higher hadronic center-of-mass energy or higher rapidity difference between tagged jets)
- Need for more exclusive final states as well as more sensitive observables
- Strong manifestation of higher-order **instabilities** via scale variation

NLA BFKL corrections to cross section with opposite sign with respect to the leading order (LO) result and large in absolute value...

- ◇ ...call for some optimization procedure...
- ◇ ...choose scales to mimic the most relevant subleading terms

- **BLM** [S.J. Brodsky, G.P. Lepage, P.B. Mackenzie (1983)]

- ✓ preserve the conformal invariance of an observable...
- ✓ ...by making vanish its  $\beta_0$ -dependent part

\* "Exact" BLM:

suppress NLO IFs + NLO Kernel  $\beta_0$ -dependent factors

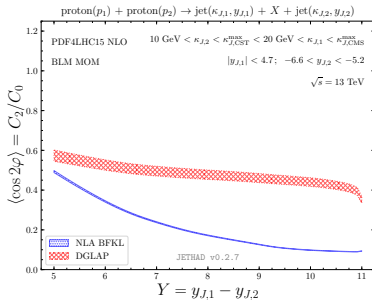
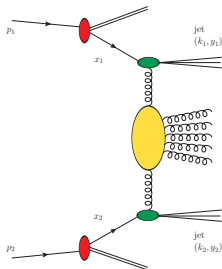
# BFKL vs High-energy DGLAP

- BFKL vs High-energy DGLAP

[F.G. Celiberto, D. Yu. Ivanov, B. Murdaca, A. Papa (2015)]

[F.G. Celiberto (2020)]

- NLA BFKL expression for the observables truncated to  $O(\alpha_s^3)$
- Investigated process: Mueller-Navelet jets production, Inclusive di-hadron production, Inclusive hadron-jet production
- Asymmetric  $p_T$ -ranges in order to suppress the Born contribution to the cross-section  $C_0$  (back-to-back).



- Main outcome

“Disjoint intervals for the transverse momenta of the emitted objects allow for a better discrimination of high energy effects”



# Heavy-quark hadroproduction: Open states

- LO Heavy-quark pair hadroproduction

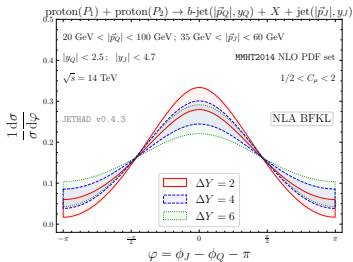
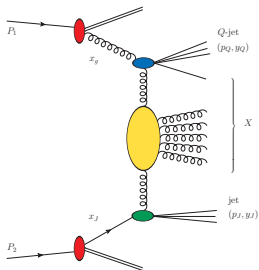
[A.D. Bolognino, F.G. Celiberto, M.F., D.Yu. Ivanov, A. Papa (2019)]

- Heavy-light dijet system

[A.D. Bolognino, F.G. Celiberto, M.F., D.Yu. Ivanov, A. Papa (2021)]

- LO heavy-quark impact factor (plus NLO universal corrections)
- NLA BFKL Green function
- NLO jet impact factor

$$\frac{d\sigma_{pp}(\varphi, \Delta Y, s)}{\sigma_{pp} d\varphi} = \frac{1}{\pi} \left\{ \frac{1}{2} + \sum_{n=1}^{\infty} \cos(n\varphi) \langle \cos(n\varphi) \rangle \right\} \equiv \frac{1}{\pi} \left\{ \frac{1}{2} + \sum_{n=1}^{\infty} \cos(n\varphi) \frac{C_n}{C_0} \right\}$$



# Heavy-quark hadroproduction: Bound states

- $\Lambda_c$ -baryon hadroproduction (VFNS)

[F.G. Celiberto, M.F., D.Yu. Ivanov, A. Papa (2021, submitted)]

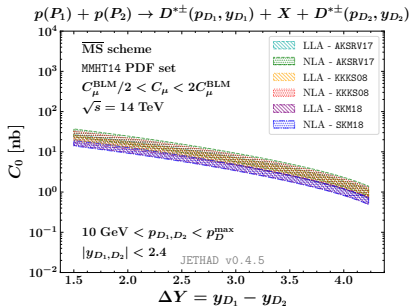
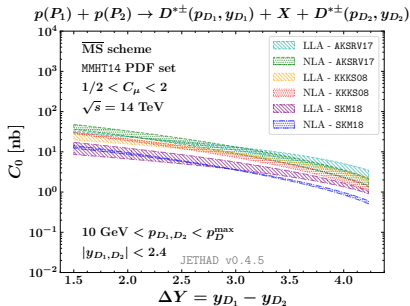
- Double D-meson hadroproduction (VFNS vs FFNS)

[F.G. Celiberto, M. Di Pace, M.F., D.Yu. Ivanov, A. Papa (in progress)]

- LO heavy-quark impact factor (plus NLO universal corrections) in FFNS
- NLO light parton impact factor in VFNS
- NLA BFKL Green function

$$C_0(\Delta Y, s) = \int_{p_Q^{\min}}^{p_Q^{\max}} d|\vec{p}_Q| \int_{p_J^{\min}}^{p_J^{\max}} d|\vec{p}_J| \int_{y_Q^{\min}}^{y_Q^{\max}} dy_Q \int_{y_J^{\min}}^{y_J^{\max}} dy_J \delta(y_Q - y_J - \Delta Y) C_0$$

Preliminary



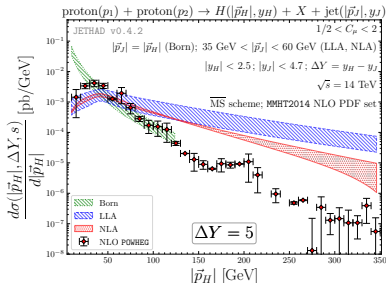
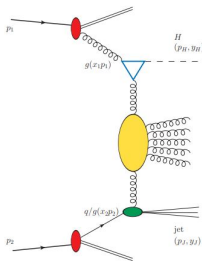
# Higgs + Jet Hadroproduction

- Higgs + Jet hadroproduction

- LO Higgs impact factor (plus NLO universal corrections)
- NLA BFKL Green function
- NLO jet impact factor

[F.G. Celiberto, D.Yu. Ivanov, M.M.A. Mohammed, A. Papa (2021)]

$$\frac{d\sigma(|\vec{p}_T|, \Delta Y, s)}{d|\vec{p}_T|d\Delta Y} = \int_{p_J^{min}}^{p_J^{max}} d|\vec{p}_J| \int_{y_H^{min}}^{y_H^{max}} dy_H \int_{y_J^{min}}^{y_J^{max}} dy_J \delta(y_H - y_J - \Delta Y) C_0$$



- Full NLO treatment (infinite top mass limit)

[F.G. Celiberto, M.F. D.Yu. Ivanov, M.M.A. Mohammed, A. Papa (in progress)]

- Main outcome

*“Distributions in the production of Higgs, Heavy-quark jet and bound states show a stabilization under higher order corrections”*

## Conclusions

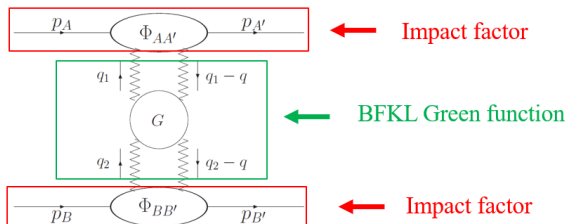
- The BFKL approach is an essential tool to study semi-hard reactions
- No less important is the possibility of using BFKL as a tool to increase our knowledge of other sectors of QCD:
  - Comparison and interpolation between DGLAP and BFKL (BFKL vs high energy DGLAP, collinear improvement, CCFM approach, ABF approach)
  - Understanding of the hadronic structure (PDFs and TMDs physics)
  - Investigation of a new class of interesting processes (Higgs sector, Heavy-flavor physics, Quarkonia)
- Experimental analyses at a **Forward Physics Facility** could significantly advance our knowledge of the high-energy regime of QCD

Thank you for the attention

# Backup

# BFKL resummation

- ▶ Diffusion  $A + B \rightarrow A' + B'$  in the **Regge kinematical region**
- ▶ Gluon Reggeization
- ▶ BFKL factorization for  $\Im \mathcal{A}_{AB}^{A'B'}$ : convolution of a **Green function** (process independent) with the **Impact factors** of the colliding particles (process dependent).



$$\Im \mathcal{A}_{AB}^{A'B'} = \frac{s}{(2\pi)^{D-2}} \int \frac{d^{D-2} q_1}{\vec{q}_1^2 (\vec{q}_1 - \vec{q})^2} \frac{d^{D-2} q_2}{\vec{q}_2^2 (\vec{q}_2 - \vec{q})^2} \times \sum_{\nu} \Phi_{A'A}^{(R,\nu)}(\vec{q}_1, \vec{q}, s_0) \int \frac{d\omega}{2\pi i} \left[ \left( \frac{s}{s_0} \right)^{\omega} G_{\omega}^{(R)}(\vec{q}_1, \vec{q}_2; \vec{q}) \right] \Phi_{B'B}^{(R,\nu)}(-\vec{q}_2, \vec{q}, s_0)$$

►  **$k_t$ -factorization** (or small- $x$  factorization)

1. Inclusive or exclusive processes
2. Small- $x$ , large- $k_T$
3. **UGD**

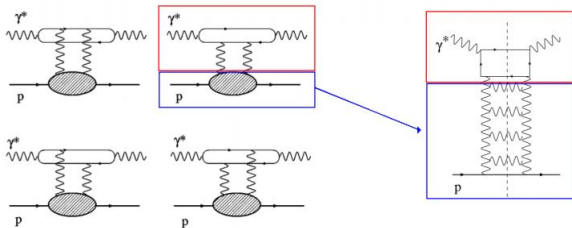
► **Example**

Photoabsorption in  $k_T$ -factorization:

$$\sigma_{tot}(\gamma^* p \rightarrow X) \propto \text{Im}_s \{ \mathcal{A}(\gamma^* p \rightarrow \gamma^* p) \} \equiv \Phi_{\gamma^* \rightarrow \gamma^*} \otimes \mathcal{F}(x, \vec{k}^2)$$

► **Small- $x$  limit**

$$\text{UGD} = [\text{BFKL gluon ladder}] \otimes [\text{proton impact factor}]$$





## *JETHAD, BFKL inspired but for HEP purposes!*

It is a Fortran2008-Python3 hybrid library by Cosenza collaboration

▶ Main features:

1. Modularity
2. Extensive use of structures and dynamic memory
3. Smart management of final-state phase-space integration

▶ Developed software:

1. BFKL tools (BFKL kernel and Impact factors)
2. UGD modular package

▶ External interfaces:

1. LHAPDF and native FF parametrizations
2. CUBA multi-dim integrators
3. QUADPACK one-dim integrators
4. CERLIB (multi-dim integrators, special functions, MINUIT, etc.)

# Semi-hard sector

## Total inclusive and exclusive processes

- ▶  $A = A' = \text{quark}, B = B' = \text{gluon}$  [M. Ciafaloni and G. Rodrigo (2000)]  
[V.S. Fadin, R. Fiore, M.I. Kotsky, A. Papa (2000)]
- ▶  $A = \gamma_L^*, A' = V_L$ , with  $V_L = \rho, \omega, \phi$  (forward)  
[D.Yu. Ivanov, M.I. Kotsky, A.Papa (2004)]
- ▶  $A = A' = \gamma^*$  (forward)  
[J. Bartels, S. Gieseke, C.F. Qiao (2001)]  
[J. Bartels, S. Gieseke, A. Kyrieleis (2002)]  
[J. Bartels, D. Colferai, S. Gieseke, A. Kyrieleis (2002)]  
[V.S. Fadin, D.Yu. Ivanov, M.I. Kotsky (2003)]  
[J. Bartels, A. Kyrieleis (2004)]  
[I. Balitsky, G.A. Chirilli (2013)] [G.A. Chirilli, Yu.V. Kovchegov (2014)]

## Partially inclusive processes

- ▶ Mueller-Navelet jet production
  1. NLO jet vertex  
[J. Bartels, D. Colferai, G.P. Vacca (2003)]  
[F. Caporale, D.Yu. Ivanov, B. Murdaca, A. Papa, A. Perri (2011)]  
[D.Yu. Ivanov, A. Papa (2012)]  
[D. Colferai, A. Niccoli (2015)]
  2. Azimuthal correlations (full NLA)  
[B. Ducloué, L. Szymanowski, S. Wallon (2013,2014)]  
[F. Caporale, D.Yu. Ivanov, B. Murdaca, A. Papa (2014)]  
[F.G. Celiberto, D.Yu. Ivanov, B. Murdaca, A. Papa (2015)]
  3. Compatible with CMS (7 TeV)

- ▶ Hadron - hadron production
  1. NLO hadron vertex [D.Yu. Ivanov, A. Papa (2012)]
  2. Azimuthal correlations (full NLA) [F.G. Celiberto, D.Yu. Ivanov, B. Murdaca, A. Papa (2016,2017)]
- ▶ Hadron - jet production (full NLA) [A.D. Bolognino, F.G. Celiberto, D.Yu. Ivanov, M.M.A. Mohammed, A. Papa (2018)]
- ▶ Three / four jet production (partial NLA) [F. Caporale, G. Chachamis, B. Murdaca, A. Sabio Vera (2016)] [F. Caporale, F.G. Celiberto, G. Chachamis, A. Sabio Vera (2016)] [F. Caporale, F.G. Celiberto, G. Chachamis, D.G. Gomez, A. Sabio Vera (2016,2017)]
- ▶  $J/\Psi$  - jet production (partial NLA) [R. Boussarie, B. Ducloué, L. Szymanowski, S. Wallon (2018)]
- ▶ Drell-Yan pair - jet (partial NLA) [K. Golec-Biernat, L. Motyka, T. Stebel (2018)]
- ▶ Higgs - jet (partial NLA) [F.G. Celiberto, D.Yu. Ivanov, M.M.A. Mohammed, A. Papa (2020)]
- ▶ Heavy-quark pair photoproduction (partial NLA) [F.G. Celiberto, D.Yu. Ivanov, B. Murdaca, A. Papa (2017)]
- ▶ Heavy-quark pair hadroproduction (partial NLA) [A.D. Bolognino, F.G. Celiberto, M.F, D.Yu. Ivanov, A. Papa (2019)]
- ▶ Heavy-light meson pair hadroproduction (partial NLA) [A.D. Bolognino, F.G. Celiberto, M.F, D.Yu. Ivanov, A. Papa (in preparation)]