

The Dark Matter Hypothesis

- Proposed by Fritz Zwicky, based on observations of the Coma galaxy cluster
- The galaxies move too quickly
- The observations require a stronger gravitational field than provided by the visible matter
- Dark matter?



The Rotation Curves of Galaxies

- Measured by Vera Rubin
- The stars also orbit 'too quickly'
- Her observations also required a stronger gravitational field than provided by the visible matter



- Scanned at the American Institute of Physics
- Further strong evidence for dark matter
- Also:
 - Structure formation, cosmic background radiation, ...

Rotation Curves

In galaxies In the Solar System • 50 150 Mercury NGC 6503 orbital speed (km/sec) 40 Venus 100 30 Earth V (km s Mars 20 Jupiter 50 Saturn 10 Uranus Neptune Pluto 10 20 30 50 10 40 mean distance from Sun (AU) Radius (kps)

- The velocities decrease with distance from Sun
- Mass lumped at centre

• The velocities do not decrease with distance

Observed

Dark Halo

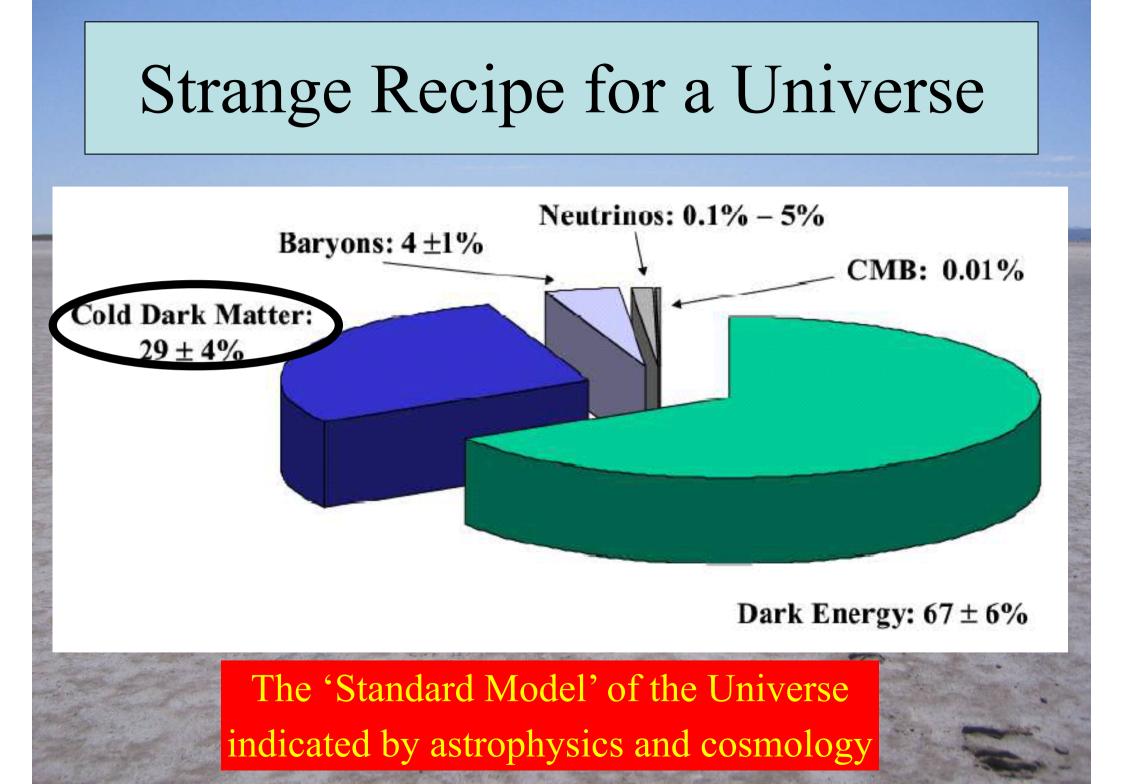
Stellar Disk

20

Gas

30

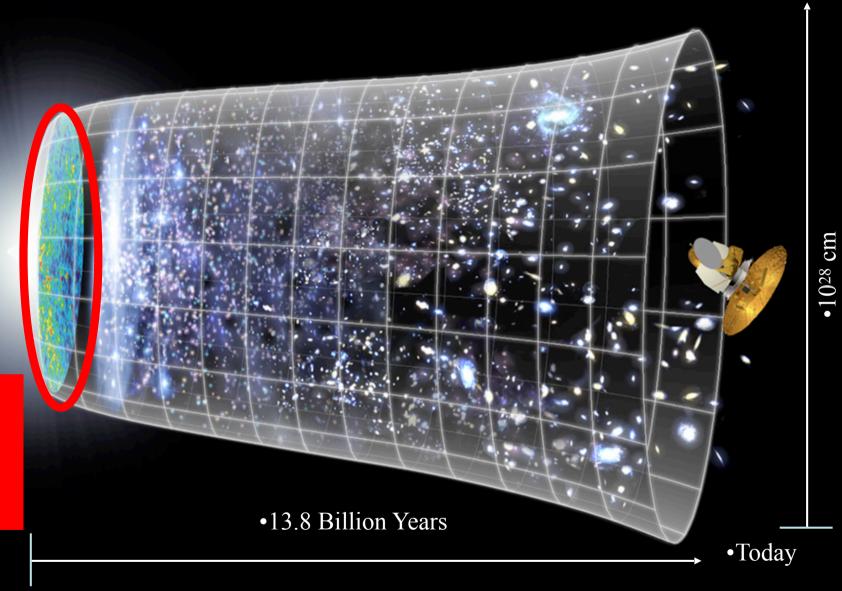
• Dark matter spread out



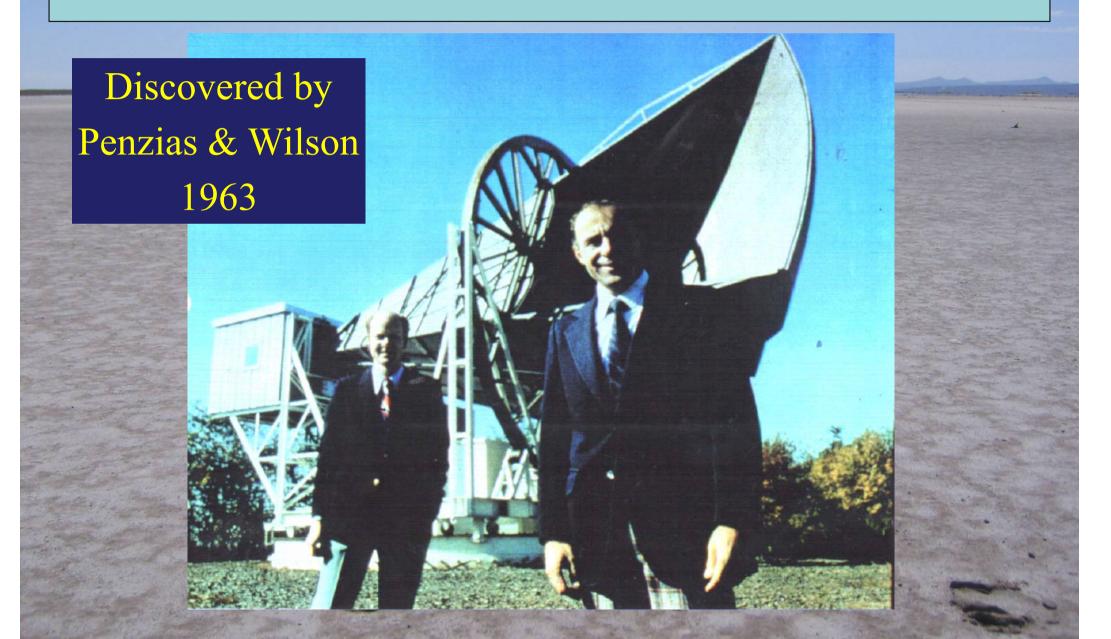
Evolution of the Universe

Big Bang

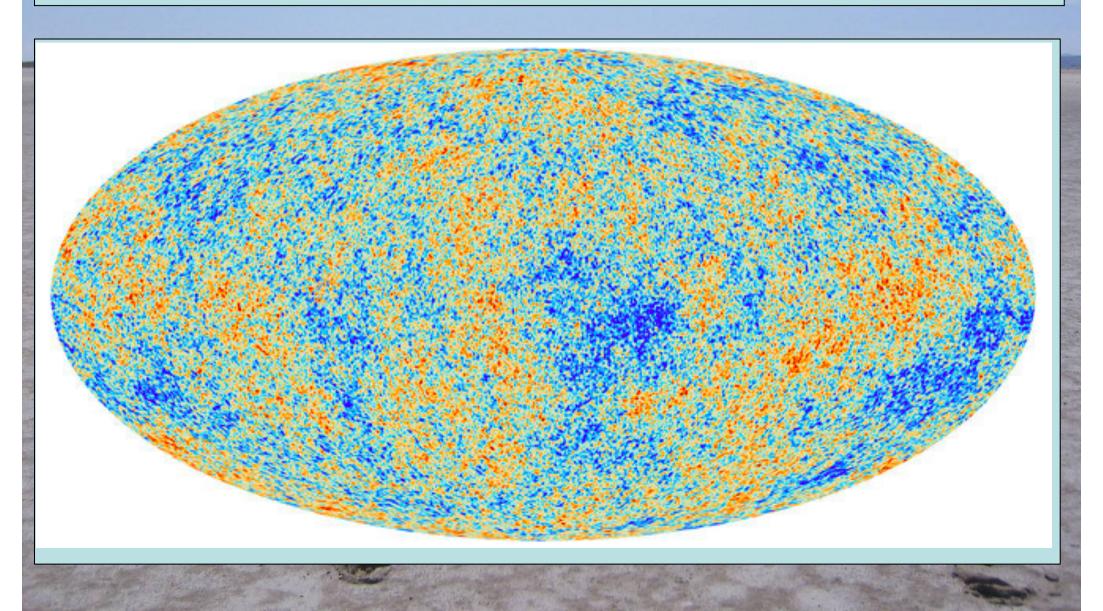
What happened then?



The Cosmic Microwave Background

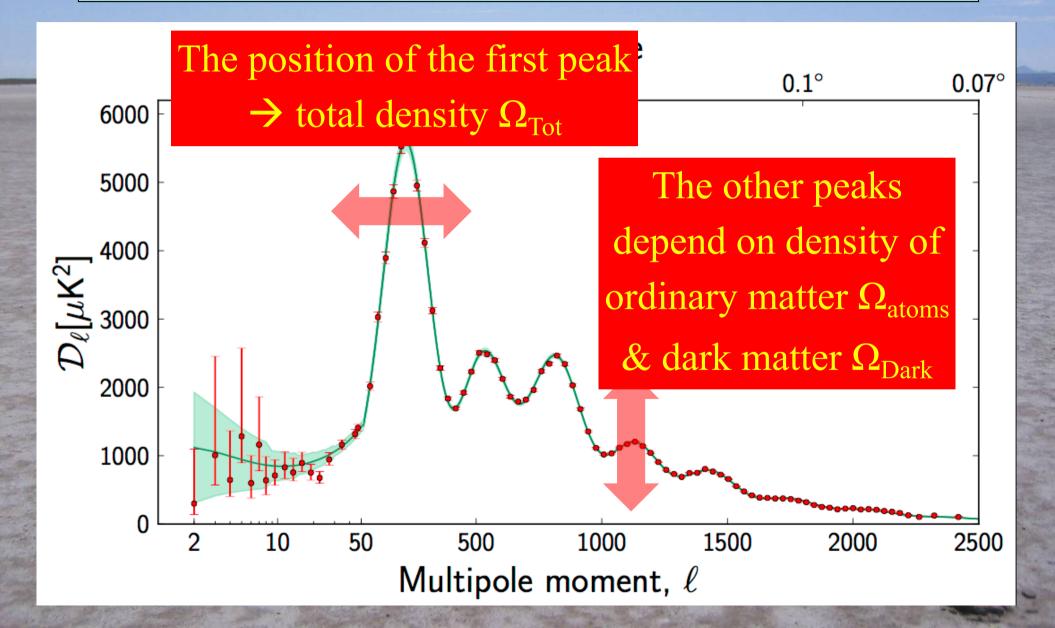


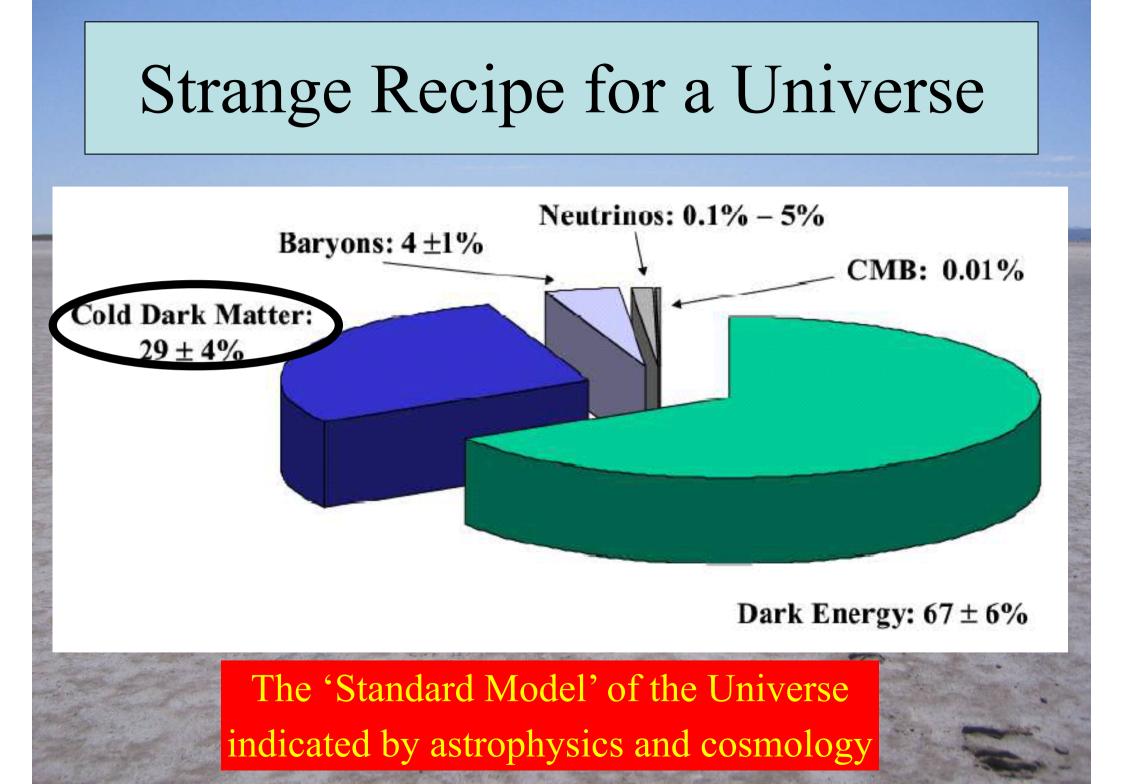
Cosmological Microwave Background as seen by Planck Satellite





The Spectrum of Fluctuations in the Cosmic Microwave Background

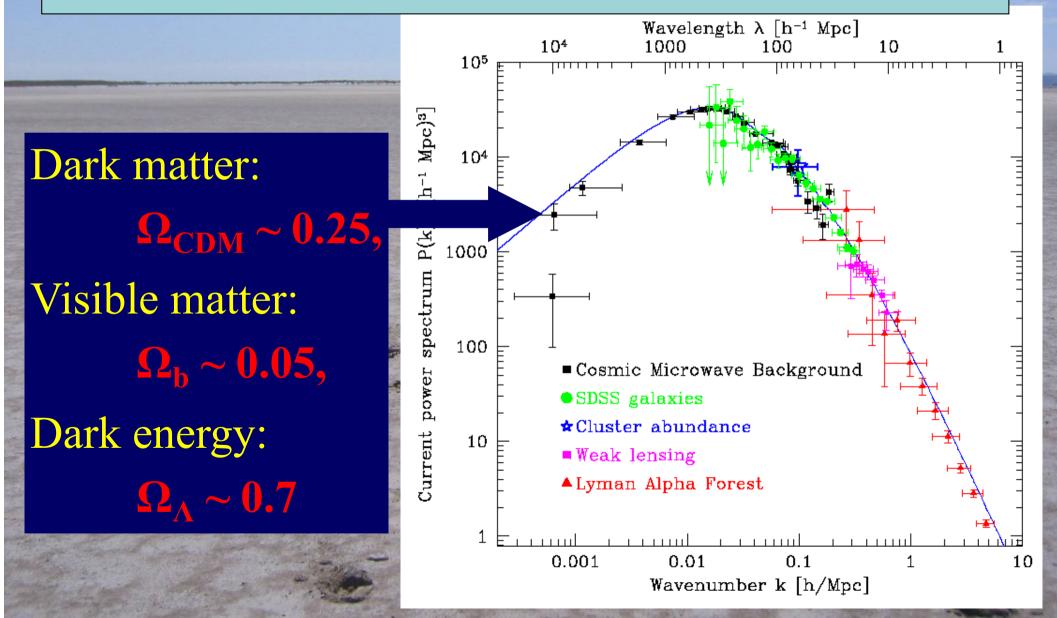




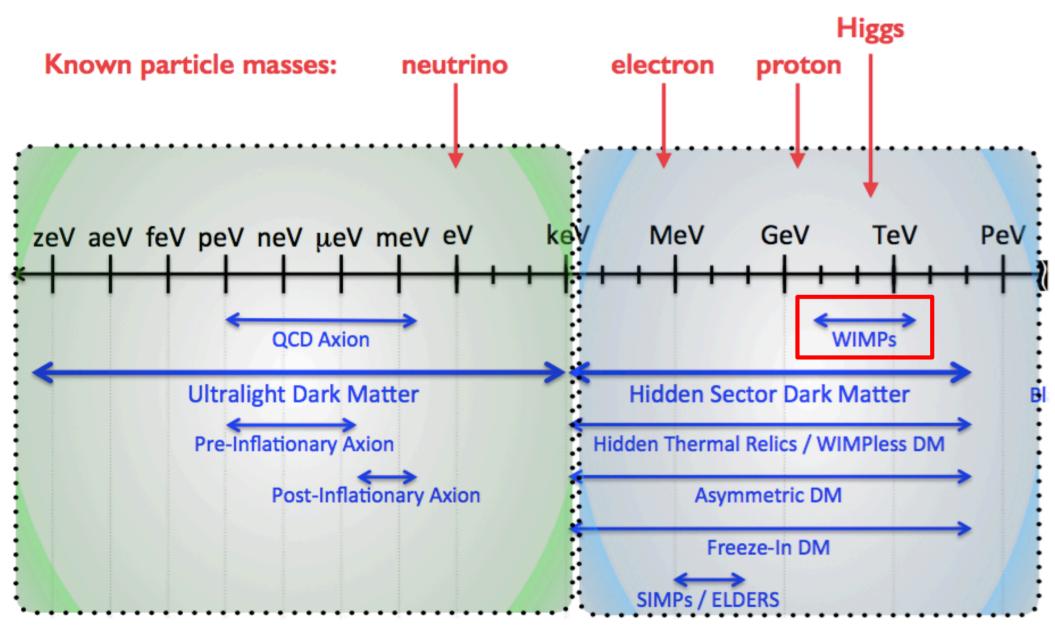
Properties of Dark Matter

- Should not have (much) electric charge
 Otherwise we would have seen it
- Should interact weakly with ordinary matter
 - Otherwise we would have detected it, either directly or astrophysically
- Should not be too light
 - Needed for forming and holding together structures in the Universe: galaxies, clusters, ...

A Successful Theory of the Formation of Structures in the Universe



Searches for Dark Matter

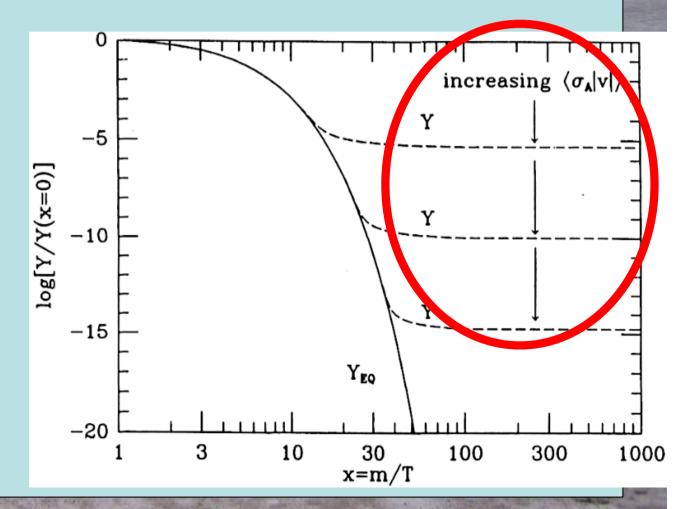


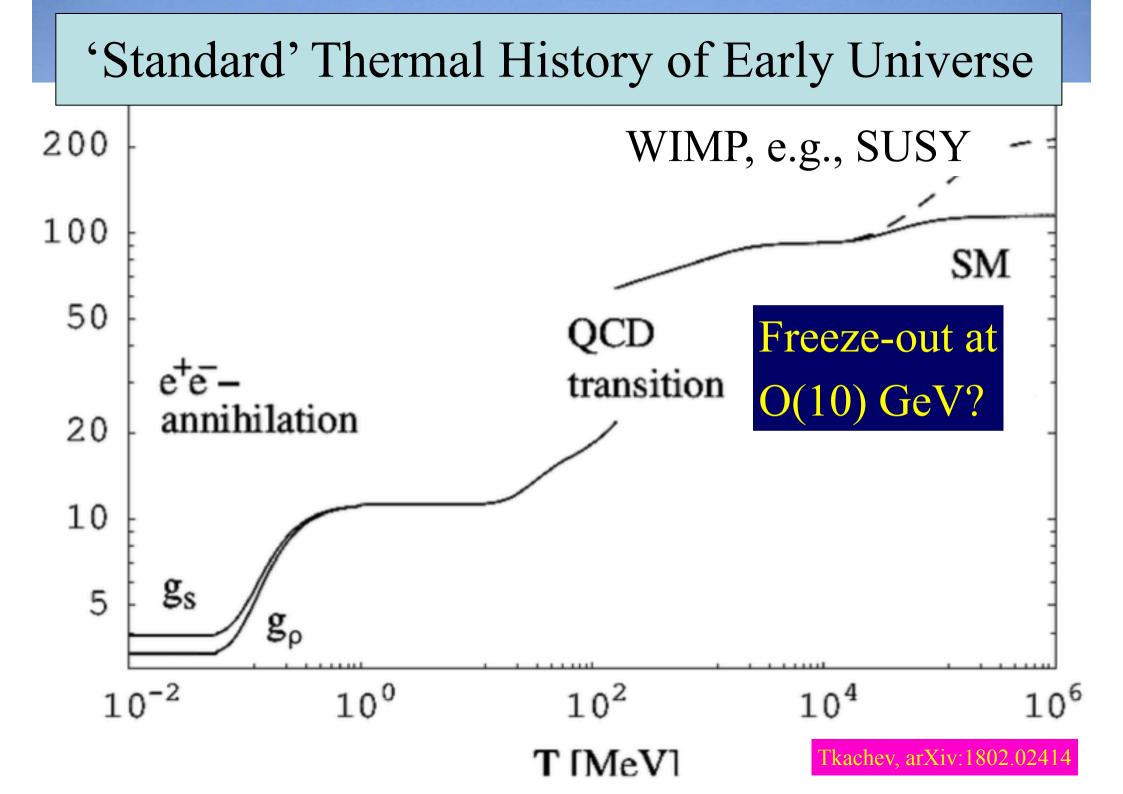
'Ultra-Light' dark matter

'Massive' dark matter

Weakly-Interacting Massive Particles (WIMPs)

- Expected to have been numerous in the primordial Universe when it was a fraction of a second old, full of a primordial hot soup
- Would have cooled down as Universe expanded
- Interactions would have weakened
- WIMPs decoupled from visible matter
- "Freeze-out"
- Larger $\sigma \rightarrow$ lower Y





The WIMP 'Miracle'

- The TeV scale from cosmology: TeV $\simeq \sqrt{M_{\rm Pl} \times 2.7 \,\rm K}$
- Generic density from freeze-out:

 $\Omega_{\rm X} h_0^2 \simeq \frac{1}{10^3 \langle \sigma v \rangle} \frac{1}{M_{\rm Pl} \times 2.7 \,\rm K} \simeq \frac{1}{10^3 \langle \sigma v \rangle} \frac{1}{\rm TeV^2}$ $\sigma v \simeq \frac{c \alpha^2}{2}$

Generic annihilation cross-section:

$$m \simeq \sqrt{M_{\rm Pl} \times 2.7 \,\mathrm{K}} \, 16\alpha \sqrt{C} \, \sqrt{\frac{\Omega_{\rm X} h_0^2}{0.25}}$$

$$\simeq \text{TeV } 16\alpha \sqrt{C} \sqrt{\frac{\Omega_{\rm X} h_{\rm C}^2}{0.25}}$$

Putting the numbers in:

Generic relic mass:

 $m \leq \frac{1}{2} \sqrt{10C \,\mathrm{TeV}} \leq 5 \,\mathrm{TeV}$

WIMP Candidates

- Could have right density if weigh 100 to 1000 GeV (accessible to LHC experiments?)
- Present in many extensions of Standard Model
- Particularly in attempts to understand strength of weak interactions, mass of Higgs boson
- Examples:
 - Extra dimensions of space
 - Supersymmetry

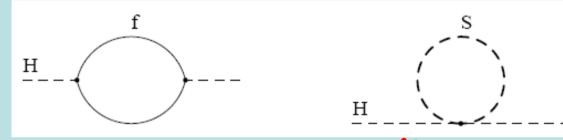
We still believe in supersymmetry

You must be joking!

Naturalness of hierarchy of mass scales

Loop Corrections to Higgs Mass²

• Consider generic fermion and boson loops:



• Each is quadratically divergent: $\int d^4k/k^2$

$$\Delta m_H^2 = -\frac{y_f^2}{16\pi^2} [2\Lambda^2 + 6m_f^2 \ln(\Lambda/m_f) + ...]$$

$$\Delta m_H^2 = \frac{\lambda_S}{16\pi^2} [\Lambda^2 - 2m_S^2 \ln(\Lambda/m_S) + \dots]$$

• Leading divergence cancelled if $\lambda_S = y_f^2 \ge 2$ Supersymmetry!

Minimal Supersymmetric Extension of Standard Model (MSSM)

• Double up the known particles:

$$\begin{pmatrix} \frac{1}{2} \\ 0 \end{pmatrix} e.g., \begin{pmatrix} \ell (lepton) \\ \tilde{\ell} (slepton) \end{pmatrix} or \begin{pmatrix} q (quark) \\ \tilde{q} (squark) \end{pmatrix} \\ \begin{pmatrix} 1 \\ \frac{1}{2} \end{pmatrix} e.g., \begin{pmatrix} \gamma (photon) \\ \tilde{\gamma} (photino) \end{pmatrix} or \begin{pmatrix} g (gluon) \\ \tilde{g} (gluino) \end{pmatrix}$$

- Two Higgs doublets
 - 5 physical Higgs bosons:
 - 3 neutral, 2 charged
- Lightest neutral supersymmetric Higgs looks like the single Higgs in the Standard Model

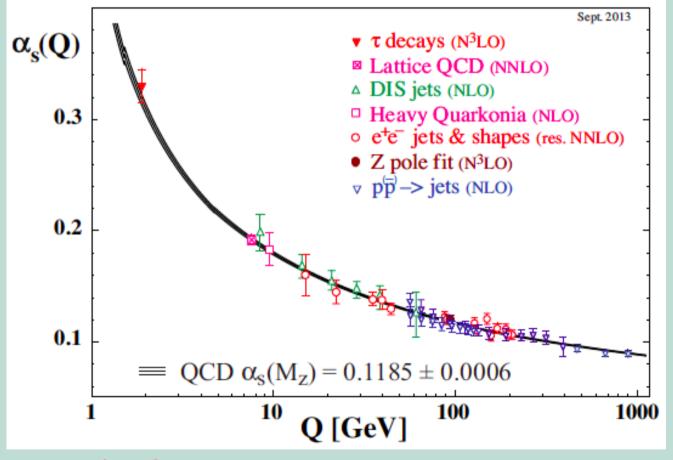
Towards Grand Unification

Pati & Salam Georgi & Glashow Georgi, Quinn & Weinberg

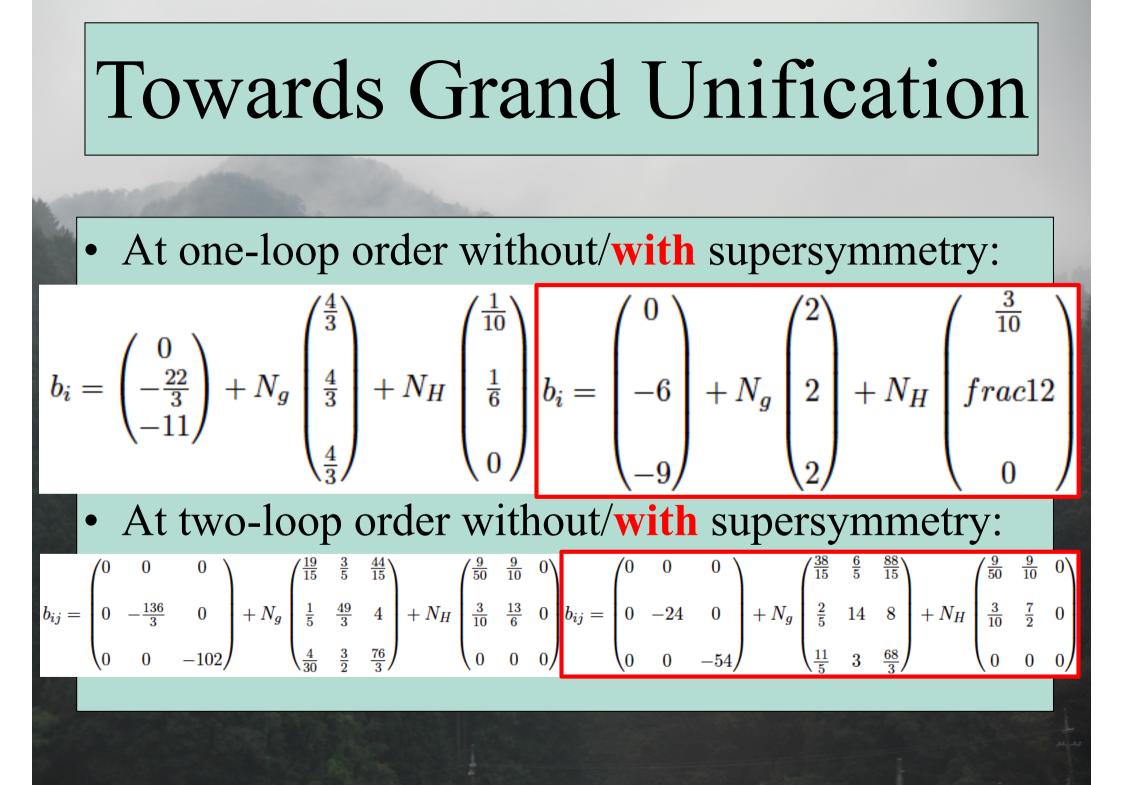
- The three Standard Model gauge couplings are different: $g_3 >> g_2$, g
- Ratio $\sin^2 \theta_W \equiv \frac{g'^2}{g'^2 + g_2^2}$ is free parameter in Standard Model
- All couplings vary energy scale, calculable using renormalisation group
- Best known is decrease of $\alpha_s \equiv \frac{g_3^2}{4\pi}$, "asymptotic freedom"
- Offers prospect of unifying couplings at high energy, as in simple group structure, and predicting $\sin^2 \theta_W$

Strong Coupling "Constant" ...

... is not constant: weaker at higher energies

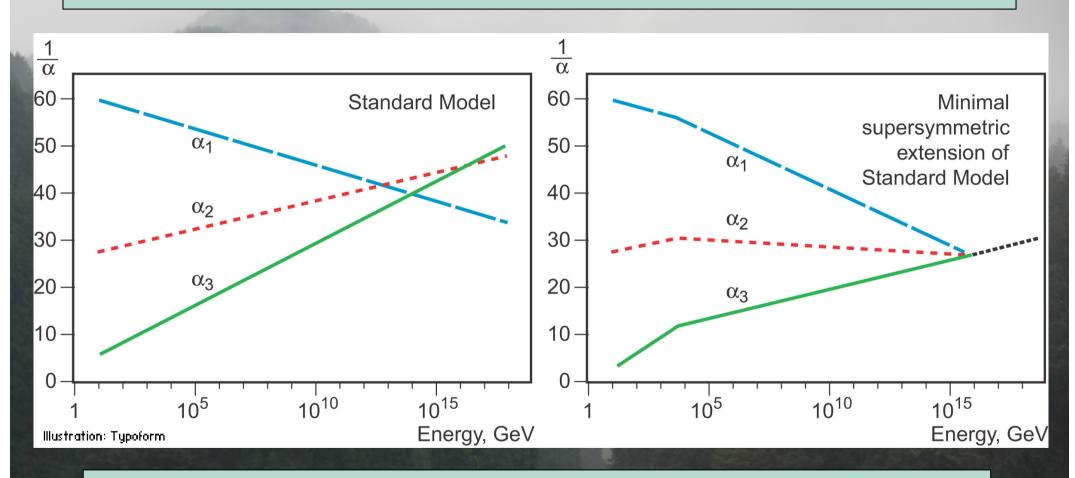


Asymptotic freedom



Georgi, Quinn & Weinberg

Grand Unification of Couplings



Almost works with just Standard Model particles Better with supersymmetric particles

Georgi & Glashow

Simplest Grand Unified Theory

- Electromagnetic charge embedded in simple group: charge quantized $\sum Q_i = 3Q_u + 3Q_d + Q_e = 0$
- Minimal model: SU(5)
- Fermions of a single generation accommodated

$$\bar{\mathbf{5}}:(\psi_i)_L = \begin{pmatrix} d_1 \\ \bar{d_2} \\ \bar{d_3} \\ e^- \\ -\nu_e \end{pmatrix}_L \mathbf{10}:(\chi^{ij})_L = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 & \bar{u}_3 & -\bar{u}_2 & u_1 & d_1 \\ -\bar{u}_3 & 0 & \bar{u}_1 & u_2 & d_2 \\ u_2 & -\bar{u}_1 & 0 & u_3 & d_3 \\ -u_1 & -u_2 & -u_3 & 0 & e^+ \\ -d_1 & -d_2 & -d_3 & -e^+ & 0 \end{pmatrix}_L$$

- "Explain" "random" quantum numbers
- Renormalization prediction $\sin^2 \theta_{W} \simeq 0.23$

Supersymmetry Breaking

- Supersymmetry must be broken, many models, no clear guidance from theory
- Assume universality at GUT scale? (CMSSM)
 - Renormalisation effects increase \tilde{q} masses relative to $\tilde{\ell}, \tilde{g}$ mass relative to \tilde{W}^{\pm}
 - Lighter stop squark may have $m_{\tilde{t}_1} < m_{\tilde{q}}$
 - Renormalization can drive $m_H^2 < 0$, enabling spontaneous gauge symmetry breaking
- Alternatively: treat particle masses as free parameters (pMSSM)

Lightest Supersymmetric Particle

• Stable in many models because of conservation of R parity:

R = (-1) 2S - L + 3B

where S = spin, L = lepton #, B = baryon #

• Particles have R = +1, sparticles R = -1:

Sparticles produced in pairs

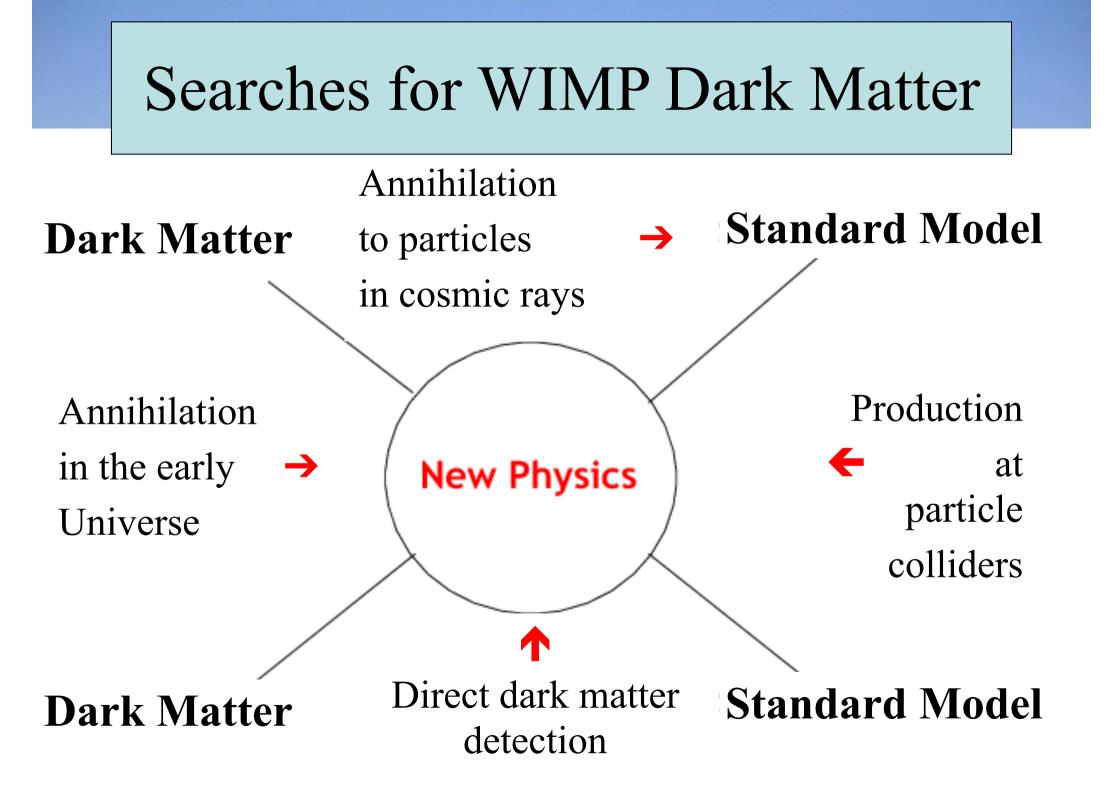
Heavier sparticles \rightarrow lighter sparticles

• Lightest supersymmetric particle (LSP) stable

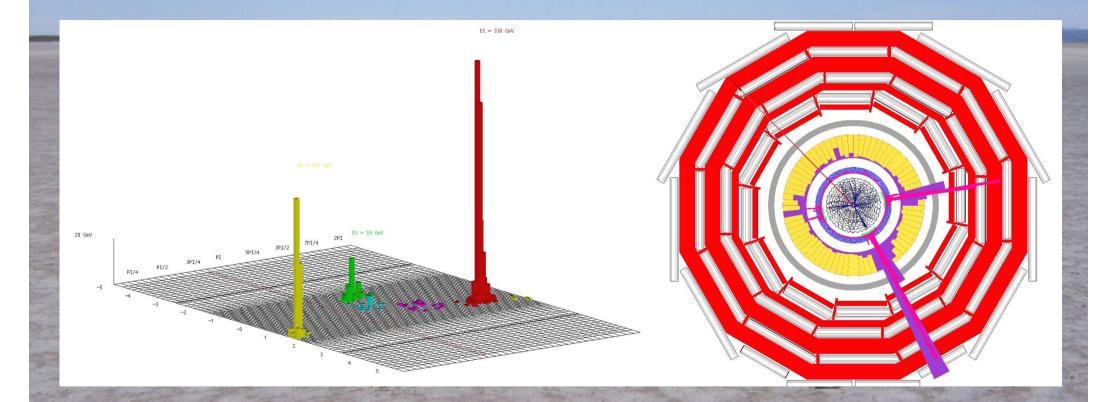
Lightest Sparticle as Dark Matter?

- No strong or electromagnetic interactions Otherwise would bind to matter Detectable as anomalous heavy nucleus
- Possible weakly-interacting scandidates
 Sneutrino
 - (Excluded by LEP, direct searches) **Lightest neutralino** χ (partner of Z, H, γ) **Gravitino**

(nightmare for detection)



Classic LHC Dark Matter Signature

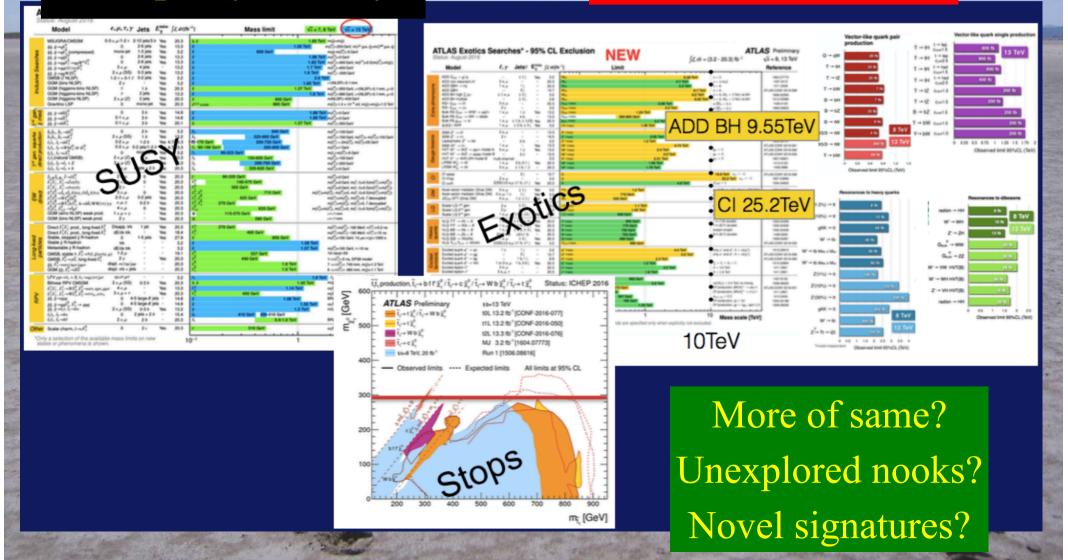


Missing transverse energy carried away by dark matter particles

Nothing (yet) at the LHC

No supersymmetry

Nothing else, either

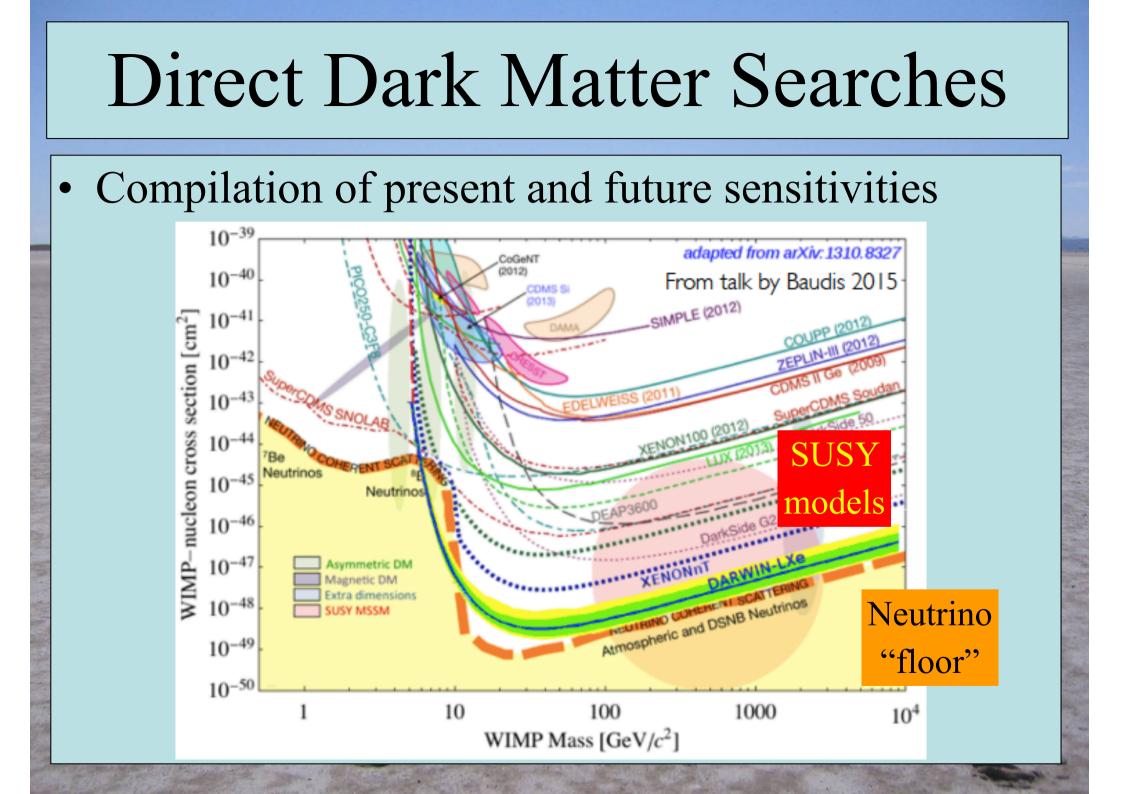


Direct Dark Matter Detection

Electrons

- Scattering of dark
 matter particle in
 deep underground
- laboratory

Incoming Particle → Outgoing Particle



Summary

Visible matter

Standard Model

Dark Matter (& Dark Energy)

Known knowns (= SM) Known unknowns (= DM) Unknown unknowns Lepton flavour violation in B decays? $g_{\mu} - 2$? Lepton Flavour Universality Violation in $B \rightarrow K\ell^+\ell^-$ Decays?

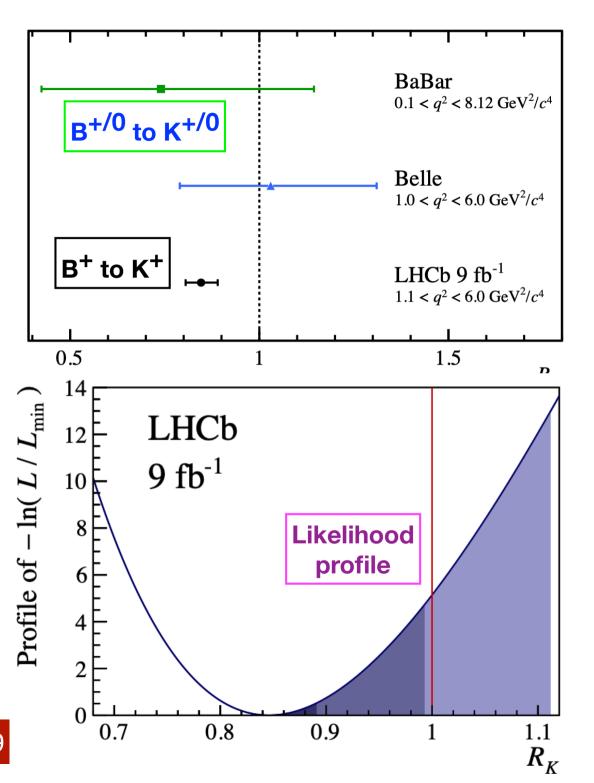
B decays to
$$e^+e^- > \mu^+\mu^-$$

Prima facie violation of lepton universality

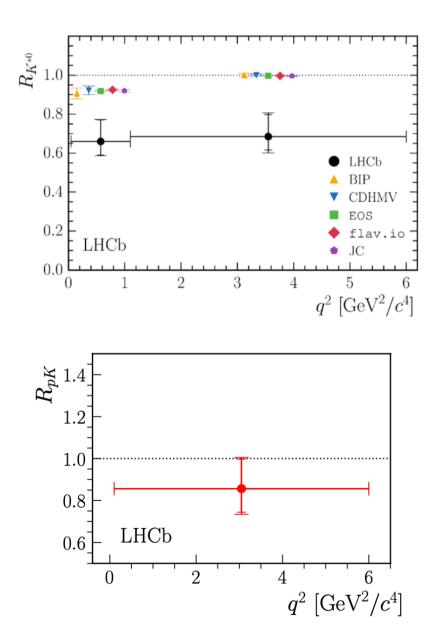
SM interactions flavouruniversal

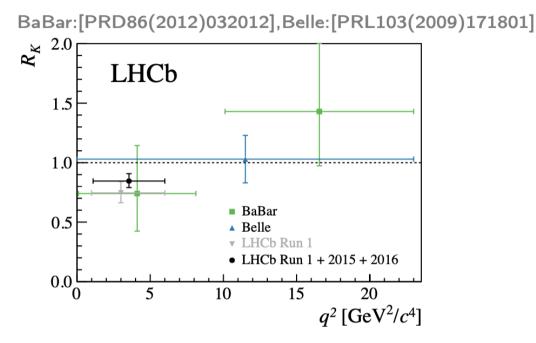
Except for Higgs couplings ∝ masses

LHCb Collaboration, arXiv:2103.11769



Previous LHCb & Other Measurements

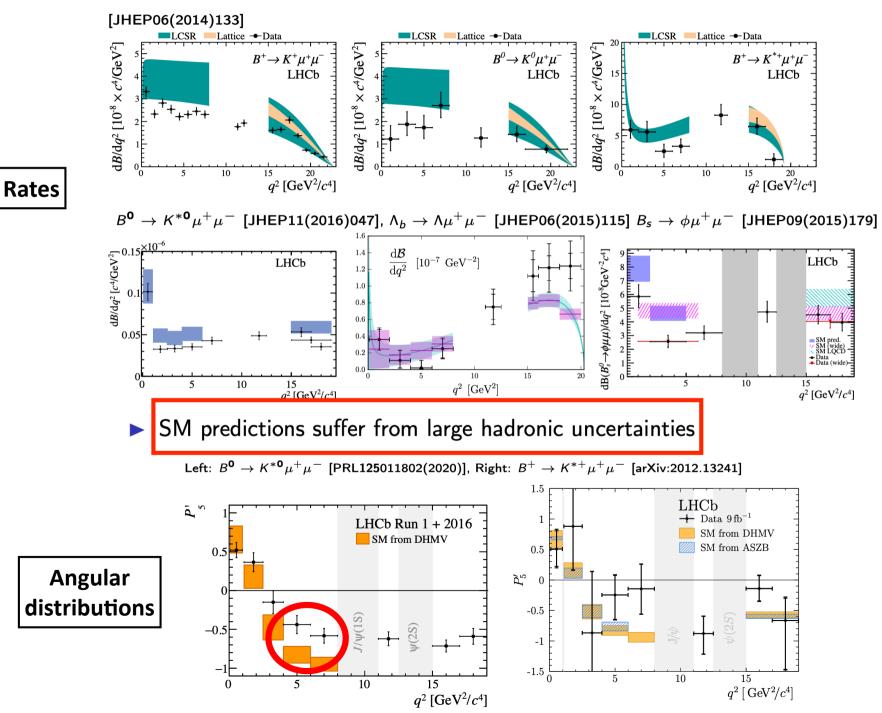


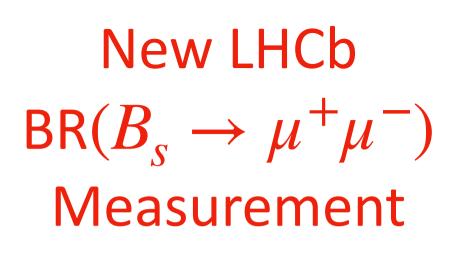


Left: $B^0 \to K^{*0} \ell^+ \ell^- R_{K^*}$ 3fb⁻¹ [JHEP08(2017)055] Right: $B^+ \to K^+ \ell^+ \ell^- R_K$ 5fb⁻¹ [PRL122(2019)191801]

Bottom: $\Lambda_b \to p K \ell^+ \ell^- R_{pK} 4.7 \text{fb}^{-1}$ [JHEP05(2020)040]

Other Previous Measurements

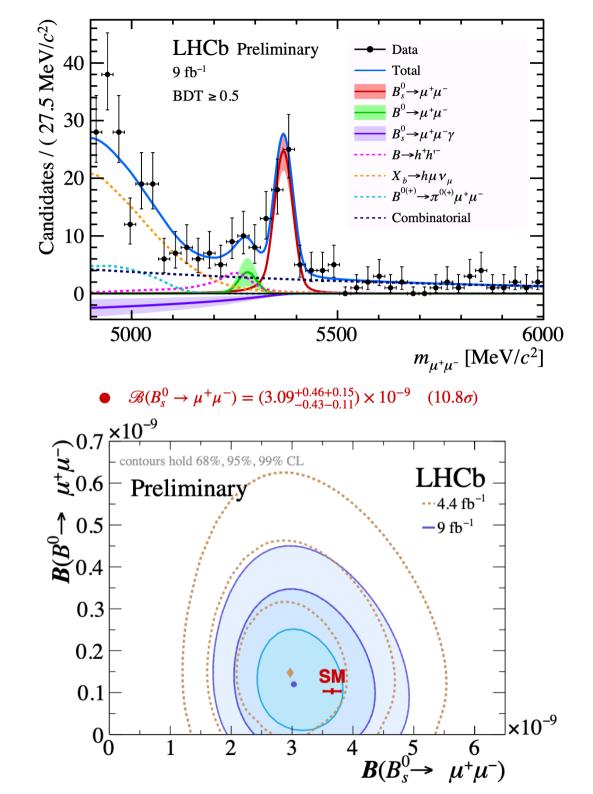




Rare decay induced by loop diagrams in SM

Measured value < SM prediction (insignificantly)

Include in search for new physics associated with the muon



Flavour Anomalies in b->s Decays

• Parametrize using effective dimension-6 operators:

$$\mathcal{H}_{\text{eff}} = \mathcal{H}_{\text{eff}}^{\text{SM}} - \frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \frac{e^2}{16\pi^2} \sum_{\ell=e,\mu} \sum_{i=9,10,S,P} \left(C_i^{bs\ell\ell} O_i^{bs\ell\ell} + C_i'^{bs\ell\ell} O_i'^{bs\ell\ell} \right) + \text{h.c.}$$

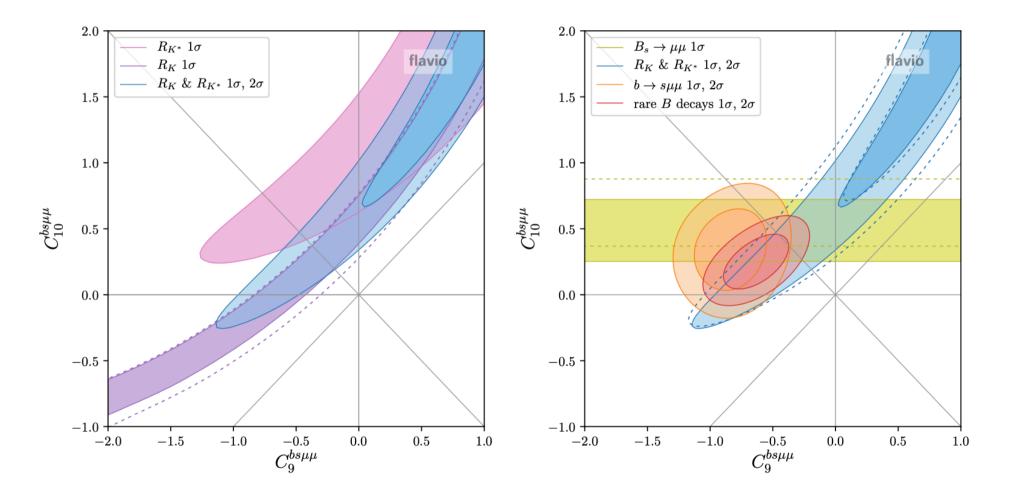
• Operators appearing in analysis:

$$\begin{aligned} O_{9}^{bs\ell\ell} &= (\bar{s}\gamma_{\mu}P_{L}b)(\bar{\ell}\gamma^{\mu}\ell) \,, \\ O_{10}^{bs\ell\ell} &= (\bar{s}\gamma_{\mu}P_{L}b)(\bar{\ell}\gamma^{\mu}\gamma_{5}\ell) \,, \\ O_{S}^{bs\ell\ell} &= m_{b}(\bar{s}P_{R}b)(\bar{\ell}\ell) \,, \\ O_{P}^{bs\ell\ell} &= m_{b}(\bar{s}P_{R}b)(\bar{\ell}\gamma_{5}\ell) \,, \end{aligned} \qquad \begin{aligned} O_{9}^{\prime bs\ell\ell} &= (\bar{s}\gamma_{\mu}P_{R}b)(\bar{\ell}\gamma^{\mu}\gamma_{5}\ell) \,, \\ O_{10}^{\prime bs\ell\ell} &= m_{b}(\bar{s}P_{L}b)(\bar{\ell}\ell) \,, \\ O_{S}^{\prime bs\ell\ell} &= m_{b}(\bar{s}P_{L}b)(\bar{\ell}\ell) \,, \\ O_{P}^{bs\ell\ell} &= m_{b}(\bar{s}P_{L}b)(\bar{\ell}\gamma_{5}\ell) \,. \end{aligned}$$

- Evidence for non-zero coefficient of $O_9^{\mu} \equiv (\bar{s}\gamma_{\mu}P_L b)(\bar{\mu}\gamma^{\mu}\mu)$
- Maybe also non-zero coefficient of $O_{10}^{\mu} \equiv (\bar{s}\gamma_{\mu}P_{L}b)(\bar{\mu}\gamma^{\mu}\gamma_{5}\mu)$
- No evidence of operators with electrons

Flavour Anomalies in b->s Decays

• Results from global fit to $C_{9,10}^{bs\mu\mu}$



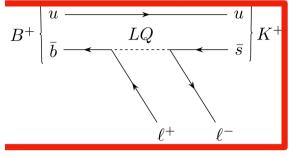
Altmannhofer & Stangl, arXiv:2103.133702

Flavour Anomalies in b->s Decays

• Results for operator coefficients

	$b \rightarrow s\mu$	μ	LFU, B_s –	$ ightarrow \mu \mu$	all rare B decays	
Wilson coefficient	best fit	pull	best fit	pull	best fit	pull
$C_9^{bs\mu\mu}$	$\left -0.87^{+0.19}_{-0.18} \right $	4.3σ	$-0.74\substack{+0.20\\-0.21}$	4.1σ	$-0.80\substack{+0.14\\-0.14}$	5.7σ
$C_{10}^{bs\mu\mu}$	$+0.49^{+0.24}_{-0.25}$	1.9σ	$+0.60\substack{+0.14\\-0.14}$	4.7σ	$+0.55\substack{+0.12\\-0.12}$	4.8σ
$C_9^{\prime bs\mu\mu}$	$+0.39^{+0.27}_{-0.26}$	1.5σ	$-0.32\substack{+0.16\\-0.17}$	2.0σ	$-0.14\substack{+0.13\\-0.13}$	1.0σ
$C_{10}^{\prime bs\mu\mu}$	$\left -0.10^{+0.17}_{-0.16} \right $	0.6σ	$+0.06\substack{+0.12\\-0.12}$	0.5σ	$+0.04\substack{+0.10\\-0.10}$	0.4σ
$C_9^{bs\mu\mu} = C_{10}^{bs\mu\mu}$	$\left -0.34^{+0.16}_{-0.16} \right $	2.1σ	$+0.43\substack{+0.18\\-0.18}$	2.4σ	$-0.01\substack{+0.12\\-0.12}$	0.1σ
$C_9^{bs\mu\mu} = -C_{10}^{bs\mu\mu}$	$\left -0.60^{+0.13}_{-0.12} \right $	4.3σ	$-0.35\substack{+0.08\\-0.08}$	4.6σ	$-0.41\substack{+0.07 \\ -0.07}$	5.9σ

Leptoquarks?



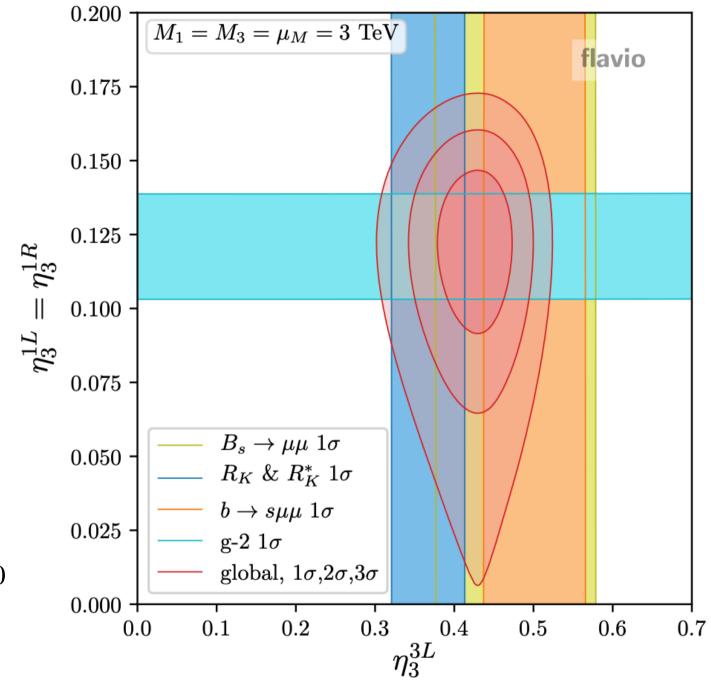
Bosons that couple leptons to quarks

$$\begin{aligned} \mathcal{L} &= \mathcal{L}_{\rm SM-V_{H}} + |D_{\mu}\Phi|^{2} + |D_{\mu}S_{1}|^{2} + |D_{\mu}S_{3}|^{2} - \frac{1}{4}X_{\mu\nu}^{2} \\ &- \left(\eta_{i}^{3\rm L}\,\bar{q}_{\rm L}^{c\,i}\ell_{\rm L}^{2}\,S_{3} - \eta_{i}^{1\rm L}\bar{q}_{\rm L}^{c\,i}\ell_{\rm L}^{2}S_{1} - \eta_{i}^{1\rm R}\overline{u}_{\rm R}^{c\,i}\mu_{\rm R}S_{1} \right) \\ &- \tilde{\eta}_{i}^{1\rm R}\overline{d}_{\rm R}^{c\,i}\nu_{\mu,{\rm R}}S_{1} + \text{h.c.} + \frac{1}{2}\varepsilon_{BX}B_{\mu\nu}X^{\mu\nu} \\ &- V_{H\Phi}(H,\Phi) - V_{13}(H,\Phi,S_{1},S_{3}) + \bar{\nu}_{\rm R}^{i}i\not{D}\nu_{\rm R}^{i} \\ &- \left(y_{\nu}^{ij}\bar{\ell}_{\rm L}^{i}\tilde{H}\nu_{\rm R}^{j} + M_{\rm R}^{ij}\bar{\nu}_{\rm R}^{ci}\nu_{\rm R}^{j} + y_{\Phi}^{ij}\Phi\,\bar{\nu}_{\rm R}^{ci}\nu_{\rm R}^{j} + \text{h.c.} \right) \,, \end{aligned}$$

Greljo, Stangl & Thomsen, arXiv:2103.13991

Leptoquark Model of $B \to K$ **Anomalies** and $g_{\mu} - 2$ B decays indicate $\eta_3^{3L} \neq 0$

$$g_{\mu} - 2$$
 indicates $\eta_3^{1L,1R} \neq 0$



Greljo, Stangl & Thomsen, arXiv:2103.13991

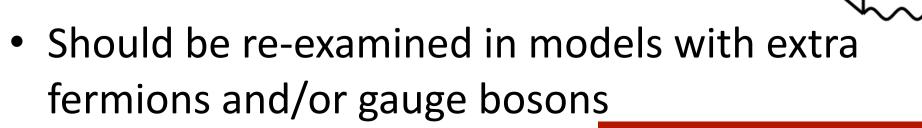
Possible Z' Interpretations

- Coupling to muons, not electrons (LEP), tau?
- Prefer vector-like coupling to muons
- Coupling to LH charge 1/3 quarks
- Prefer universal couplings to 1st/2nd generation quarks (FCNC)
- Different coupling to 3rd generation quarks to get bs flavour change
- Non-zero couplings of RH charge 2/3 quarks?
- Additional 'dark' sector or heavy vector-like lepton?

Formulation of U(1)' Models

(also for dark matter?)

- Gauge bosons of U(1)' may have vector and/or axial-vector couplings
- Consistency of theory requires cancellation of anomalous triangle diagrams
- Standard Model has quark-lepton cancellation



Anomaly Cancellation Conditions

- Colour/U(1)': (a) $[SU(3)_C^2] \times [U(1)']$, which implies $Tr[\{\mathcal{T}^i, \mathcal{T}^j\}Y'] = 0$,
- $SU(2)_W/U(1)'$: (b) $[SU(2)_W^2] \times [U(1)']$, which implies $Tr[\{T^i, T^j\}Y'] = 0$,
- $U(1)_{Y}^{2}/U(1)'$: (c) $[U(1)_{Y}^{2}] \times [U(1)']$, which implies $Tr[Y^{2}Y'] = 0$,
- $U(1)_{Y}/U(1)'^{2}$: (d) $[U(1)_{Y}] \times [U(1)'^{2}]$, which implies $Tr[YY'^{2}] = 0$,
- $U(1)'^3$: (e) $[U(1)'^3]$, which implies $Tr[Y'^3] = 0$,
- Gravity/U(1)':: (f) Gauge-gravity, which implies Tr[Y'] = 0.
- Non-trivial set of constraints

U(1)' models of **Flavour Anomalies & Dark Matter**

JE, Fairbairn & Tunney, arXiv:1705.03447

2.0

1.5

1.0

0.5

0.0

-0.5

-1.0

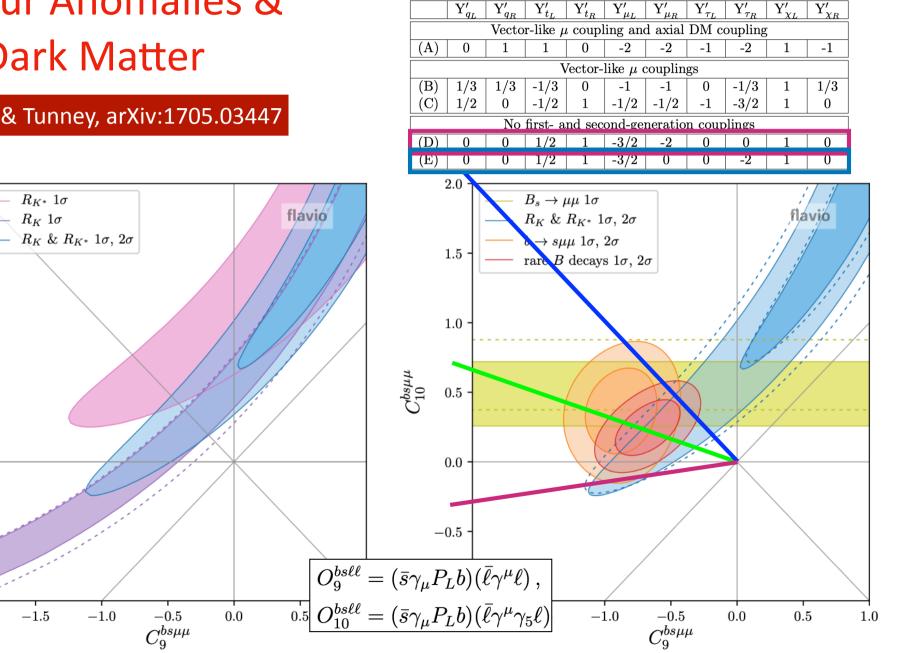
-2.0

 $\mathcal{C}^{bs\mu\mu}_{10}$

Models with only left-handed quark couplings and two dark fermions

Y_{q_L}'	Y'_{t_L}	Y'_{μ_L}	Y'_{μ_R}	$Y'_{ au_L}$	$\mathrm{Y}_{ au_R}'$	Y'_{A_L}	Y'_{A_R}	Y'_{B_L}	Y'_{B_R}
1/3	-2/3	2/3	1/3	-2/3	-1/3	0	1	-1/3	-4/3

Models with right-handed charge 2/3 quark couplings and one DM fermion



Possible Experimental Signatures

- 2 'dark' SM-singlet fermions?
 - Decays of heavier mass eigenstate
 - -Z' coupling to muons not vector-like

$$Y'_{\mu_V}/Y'_{\mu_A}\,=\,-3$$

- Strong LHC dilepton constraint
- -No DM candidate with axial coupling
- If RH quark charges and one DM fermion?
 - Models with vector-like muon, axial Z' DM couplings
 - Models without 1st/2nd generation couplings have weaker LHC constraints:

$$Y'_{\mu_V}/Y'_{\mu_A}=7$$
 $Y'_{\mu_V}/Y'_{\mu_A}=-1$

Summary

Visible matter

Standard Model

B decays