

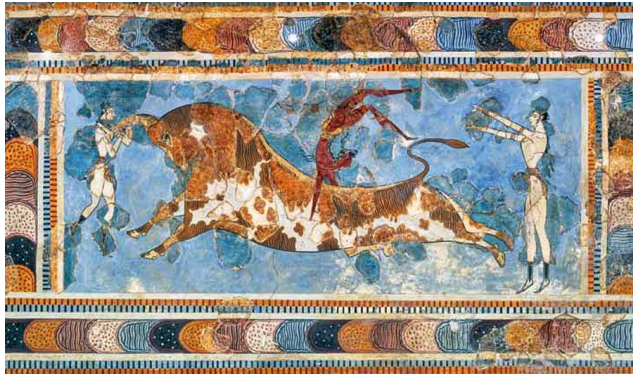
Ambiguities in the hadro-chemical freeze-out of Au+Au collisions at SIS18 energies and how to resolve them

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In collaboration with: **Jan Steinheimer, Volodymyr Vovchenko, Reinhard Stock, Horst Stöcker**

based on: [arXiv:2104.06036 \[hep-ph\]](https://arxiv.org/abs/2104.06036)



August 31, 2021

**10th International Conference
on New Frontiers in Physics**



FIAS Frankfurt Institute
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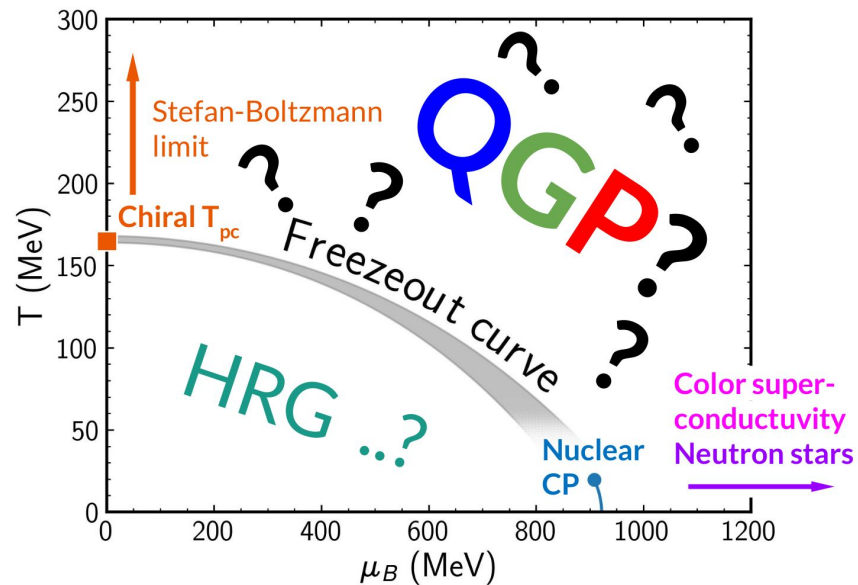


QCD phase diagram

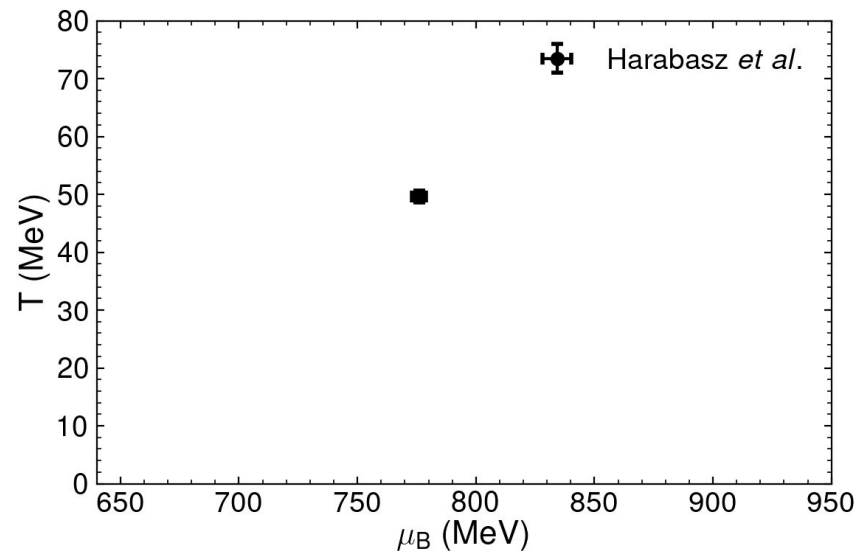
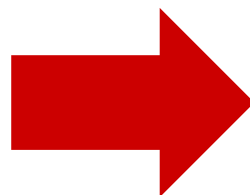
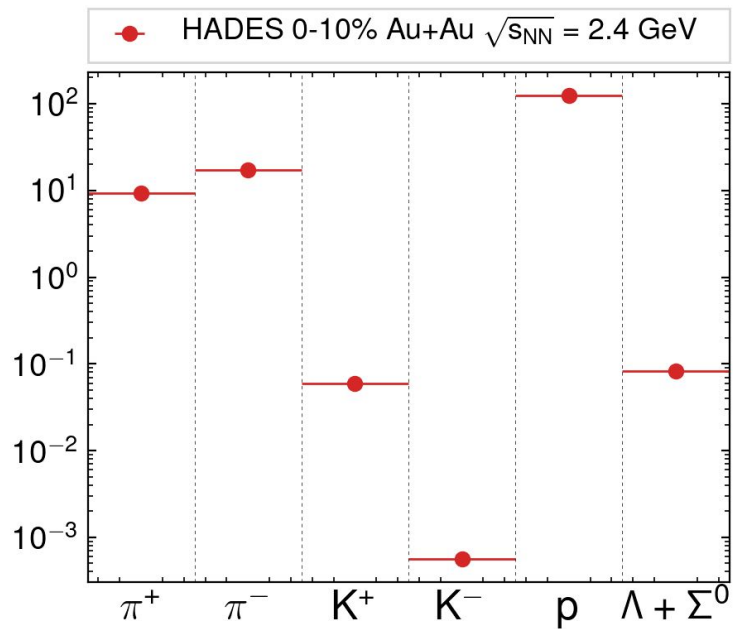
$$\mathcal{L}_{\text{QCD}} = \sum_{i,j} \bar{\psi}_i \left(i\gamma^\mu (\partial_\mu \delta_{ij} - \frac{i}{s} g \mathcal{A}_\mu^a \lambda_{a,ij}) - m_i \delta_{ij} \right) \psi_j - \frac{1}{4} G_{\mu\nu}^a G_a^{\mu\nu}$$
$$G_{\mu\nu}^a = \partial_\mu \mathcal{A}_\nu^a - \partial_\nu \mathcal{A}_\mu^a + g f^{abc} \mathcal{A}_\mu^b \mathcal{A}_\nu^c$$



How to map the well established QCD theory to its phase diagram?



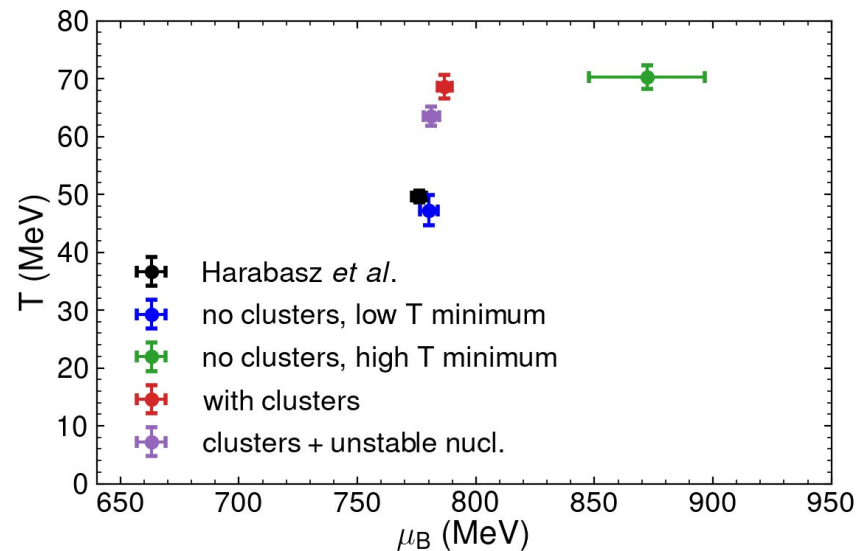
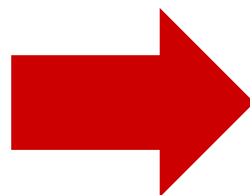
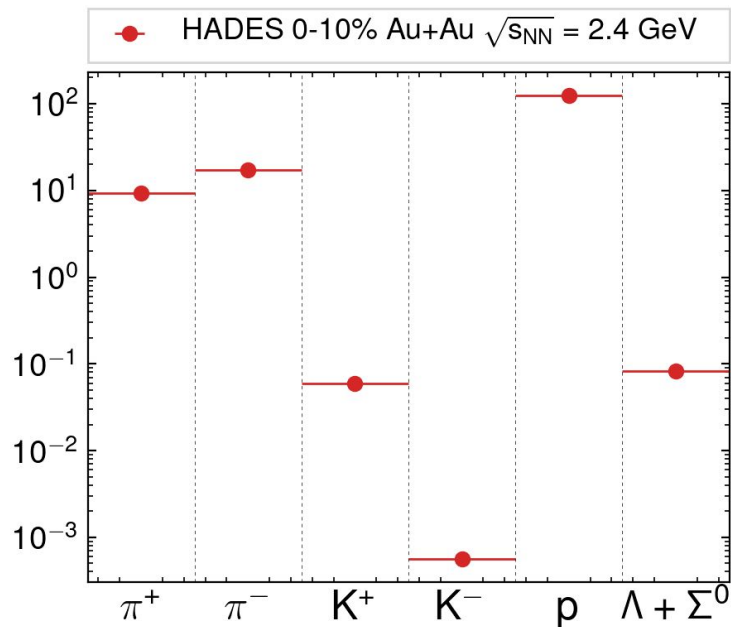
Chemical freeze-out at SIS18 energies



S. Harabasz et al., 2003.12992

J. Adamczewski-Musch et al. (HADES), 1703.08418
J. Adamczewski-Musch et al. (HADES), 1812.07304
M. Szala (HADES), ECT workshop, 2019*
J. Adamczewski-Musch et al. (HADES), 2005.08774

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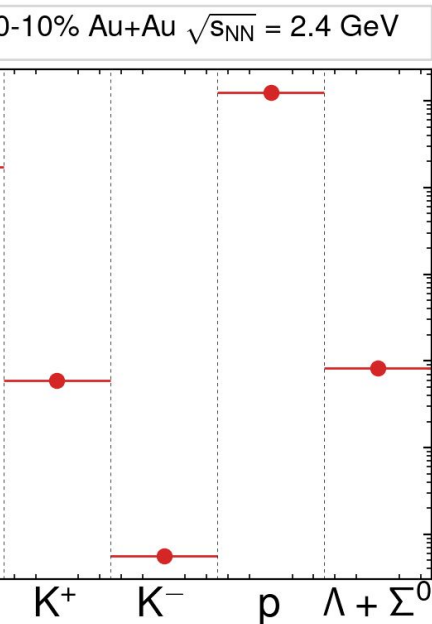


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Thermal-FIST

(Vovchenko, Stoecker, 1901.05249)

open source: github.com/vlvovch/Thermal-FIST



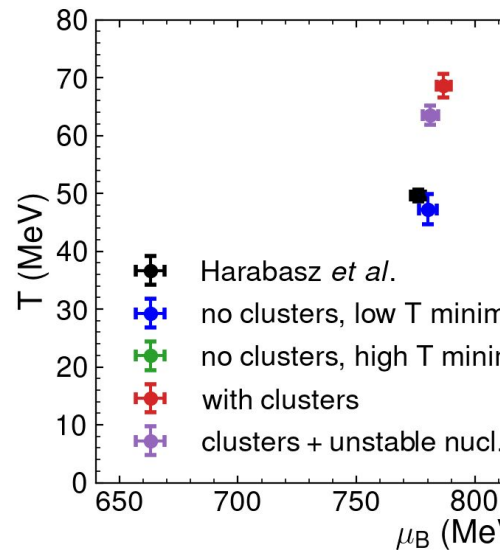
Fitting of the experimental data by **ideal non-interacting hadron resonance gas (HRG)**,

4 parameters are fitted:

- baryon chemical potential μ_B
- temperature T
- radius R
- strangeness suppression factor γ_S

2 parameters are extracted from constraints:

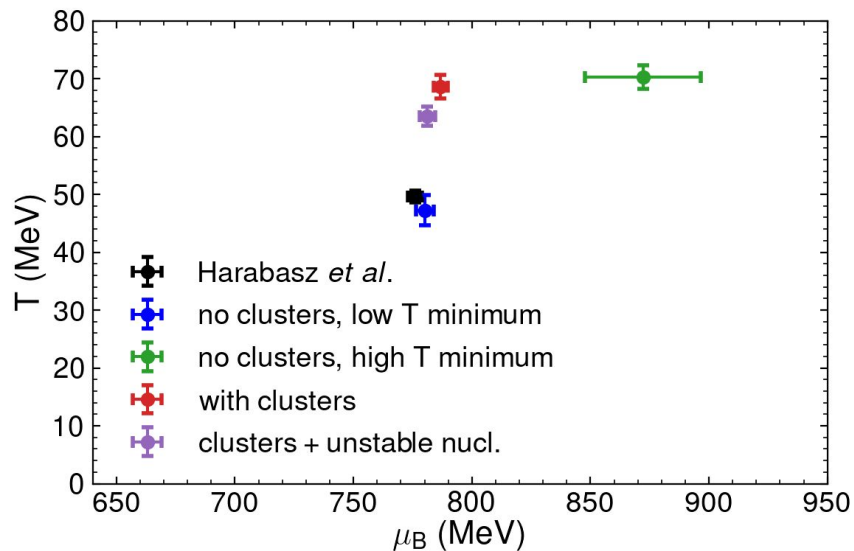
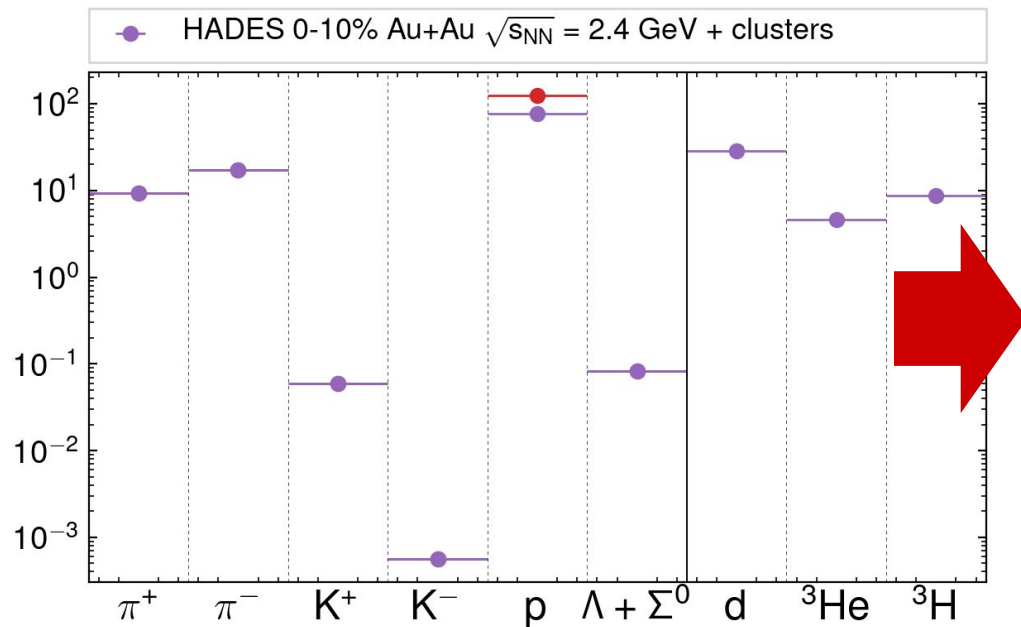
- strangeness chemical potential μ_S from strangeness neutrality $n_S=0$
- electric chemical potential μ_Q from strangeness $n_Q/n_B=0.4$



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Allows to map the experimental data to thermodynamic properties

Chemical freeze-out at SIS18 energies



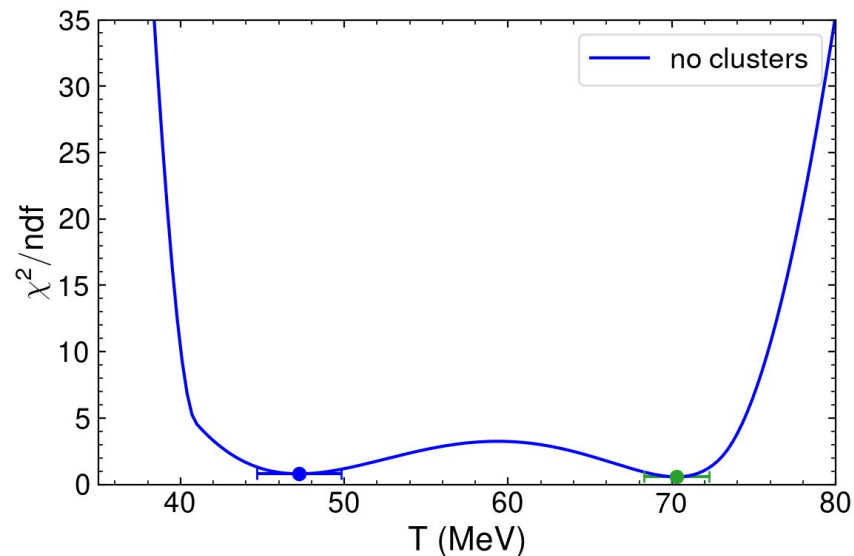
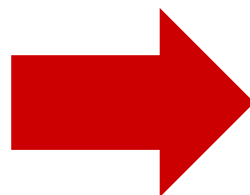
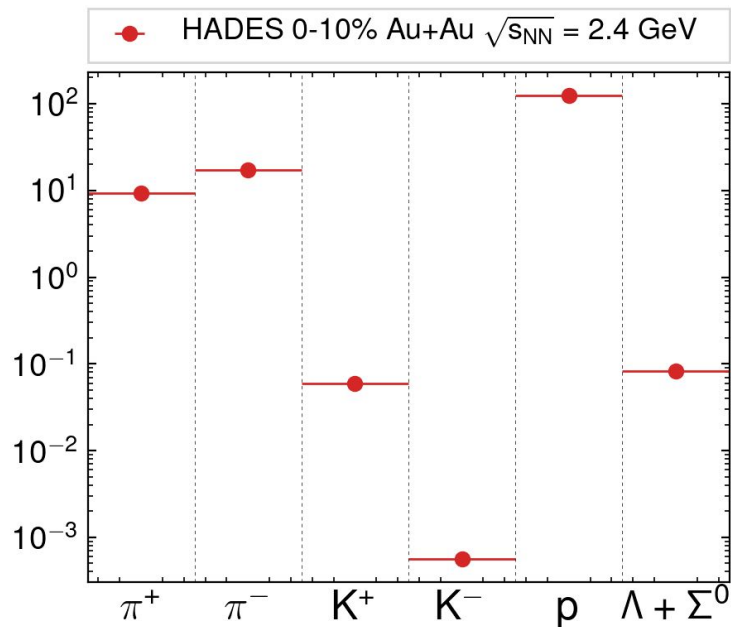
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Treatment of light nuclei is important:

- either $N_p = N_{p \text{ unbound}} + N_p(d) + N_p(^3\text{He}) + N_p(^3\text{H})$
- either $d, ^3\text{He}, ^3\text{H}$ are separate degrees of freedom

Ambiguities in the freeze-out: double minima

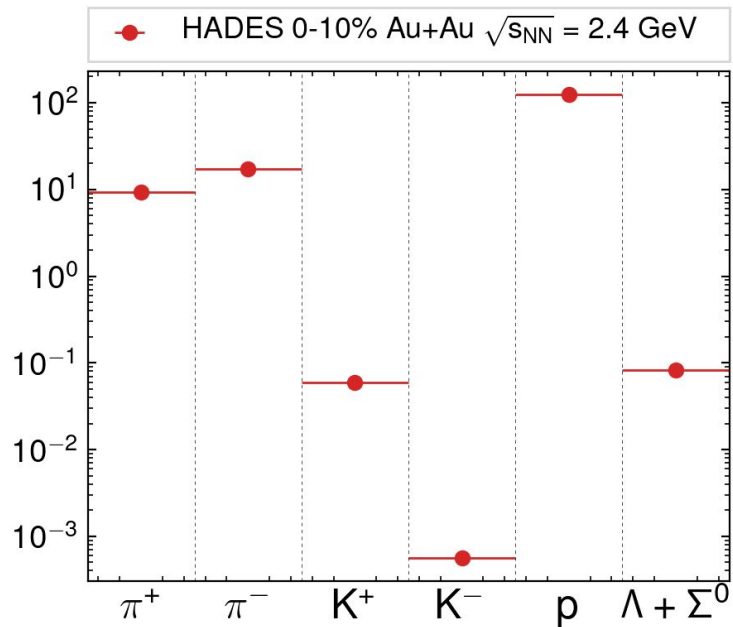


Thermal fit to the hadron yields has two degenerate solutions.

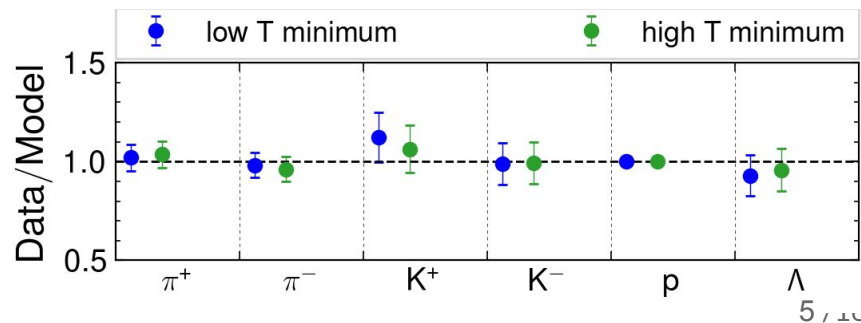
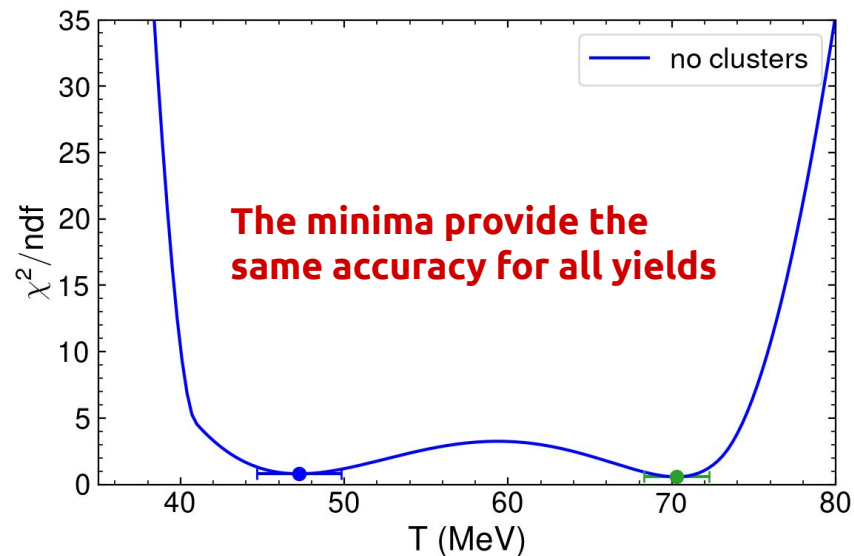
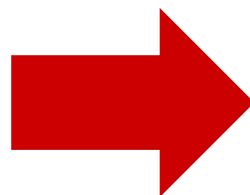
- Which solution to choose?
- Higher T solution was not found in *Harabasz et al.*
- No freeze-out at all?

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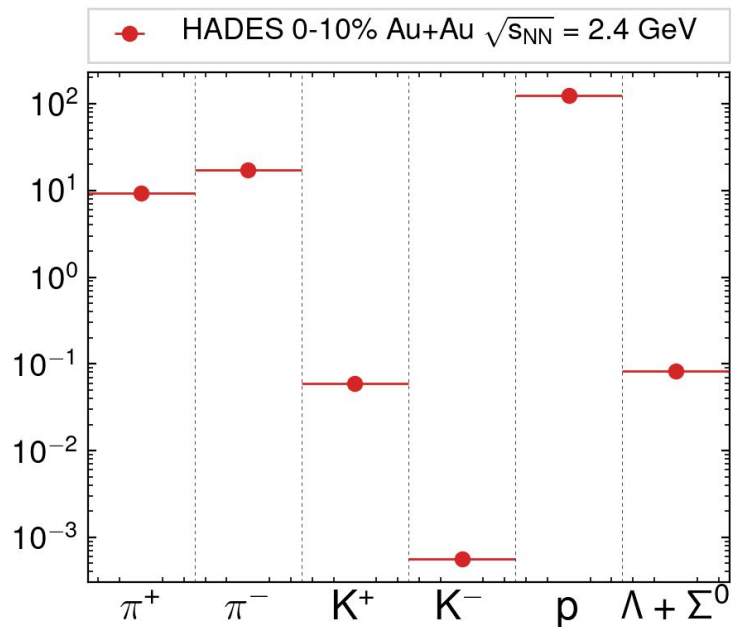
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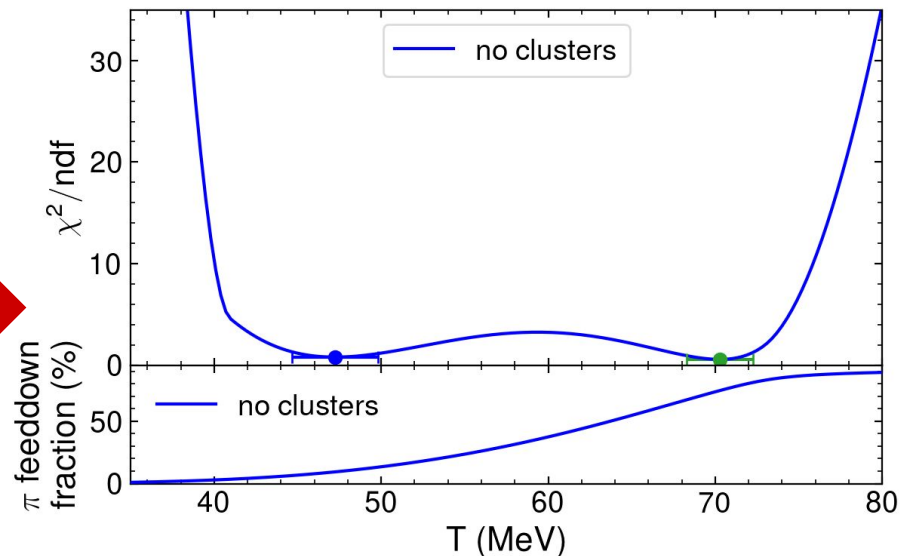
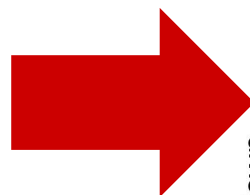
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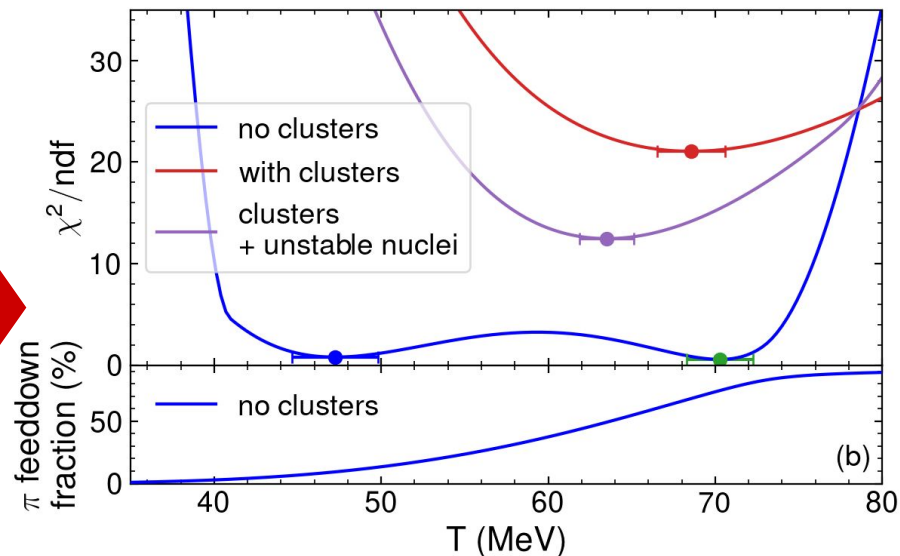
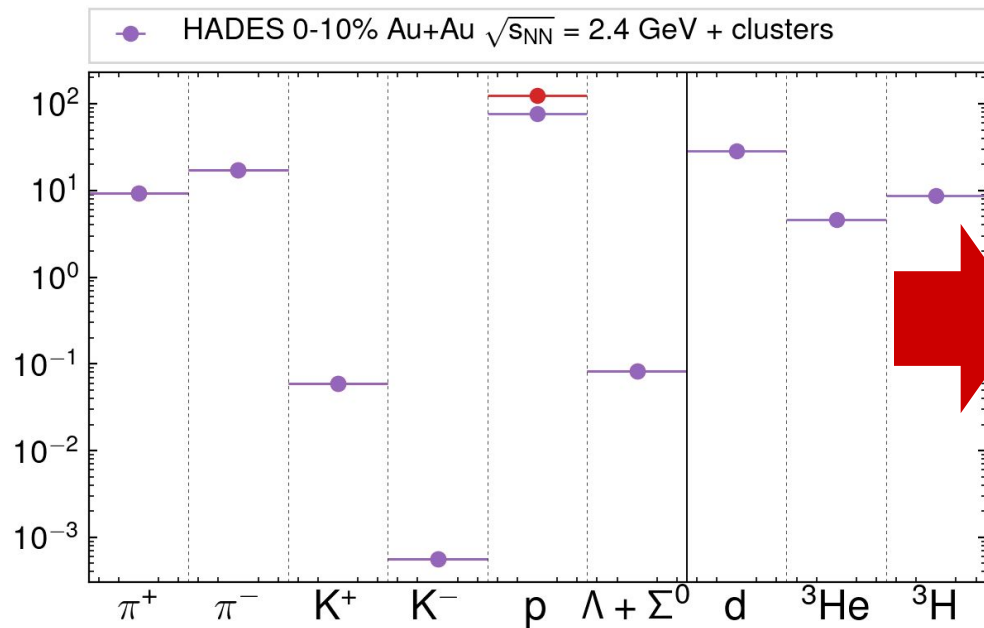
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Two minima have completely different resonance content.

At the higher temperature more than 70% of pions come from the resonance decays.

Ambiguities in the freeze-out: light nuclei



Fit with light nuclei as separate degrees of freedom:

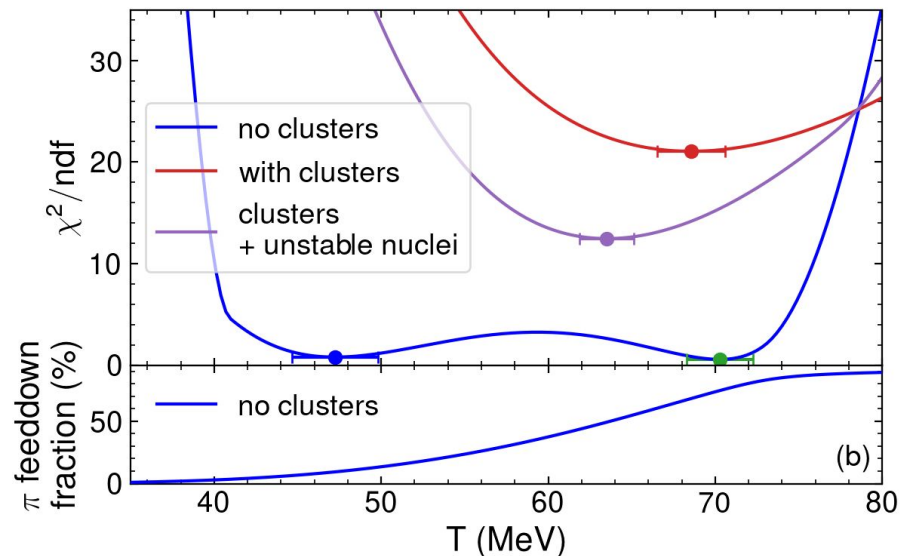
- Single minima
- Data is poorly described, $\chi^2/\text{ndf} > 10$

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Ambiguities in the freeze-out: all scenarios

Three scenarios:

- **no clusters** – light nuclei are formed after the chemical freeze-out, thus are omitted from the thermal model particle list. Protons that later-on bind into the light nuclei are counted as 'free'
- **clusters included** – light nuclei are formed at the chemical freeze-out. Only stable light nuclei are included in the thermal model particle list.
- **clusters and decays of unstable nuclei** – the model includes the feeddown from the decays of *unstable* $A = 4$, and $A = 5$ nuclei to the final yields of protons, deuterons, tritons, ${}^3\text{He}$, and ${}^4\text{He}$ at the chemical freeze-out (Vovchenko et al., 2004.04411).



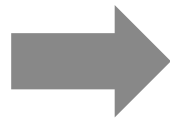
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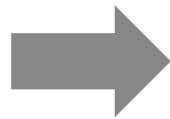
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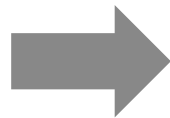
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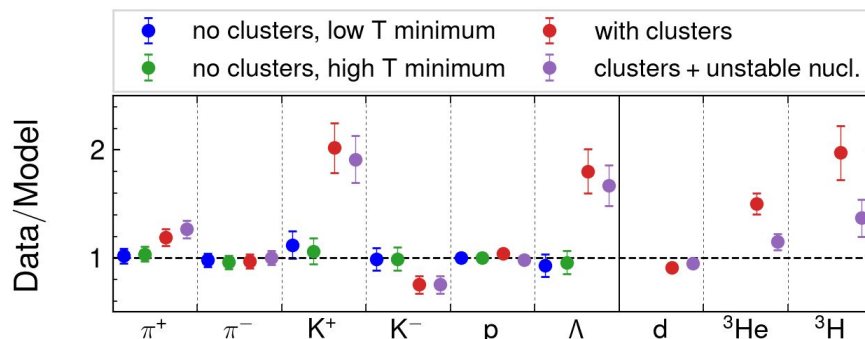
- **Good description, arbitrary T possible**
Which T to choose?



- Poor description, single minimum
Another mechanism for light nuclei formation should be considered.



- Improved description, single minimum
Perhaps this scenario can be improved?..



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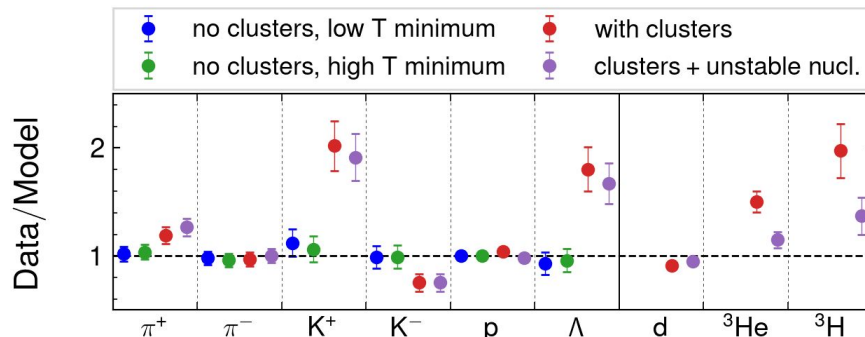
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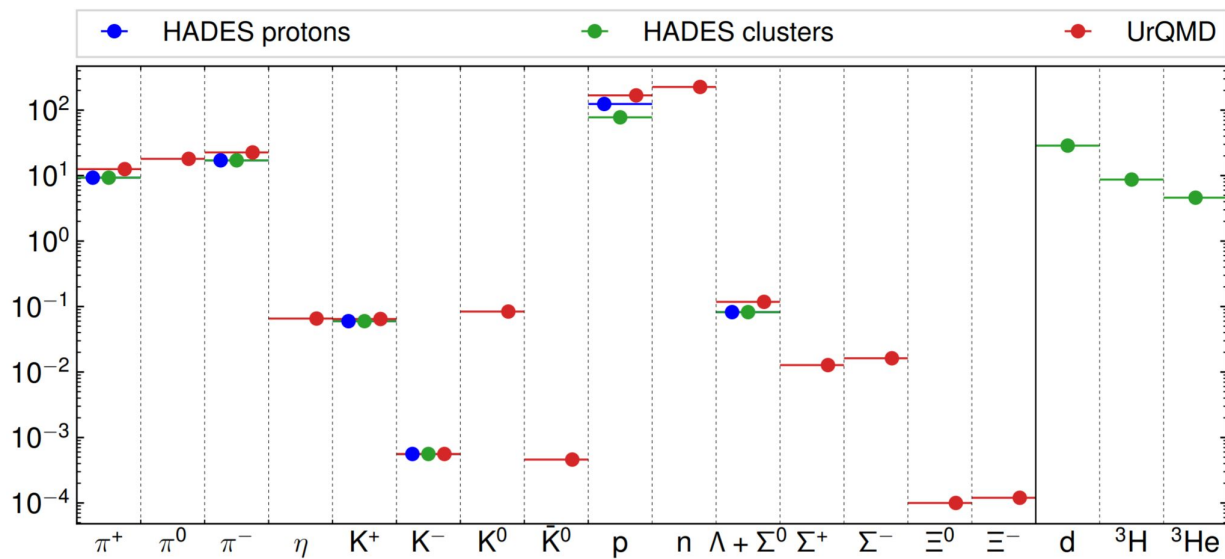
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Resolving ambiguities: freeze-out in UrQMD



UrQMD predictions for particle yields in Au+Au@ $\sqrt{s_{NN}} = 2.4$ GeV can be used as input to thermal model.

More stable hadrons in the fit — possibility for a unique solution.

UrQMD 3.4 extended with up-to-date resonance branching ratios works well in the HADES energy regime. Inclusion of density-dependent nuclear potentials is essential.

G. Graef et al., 1409.7954

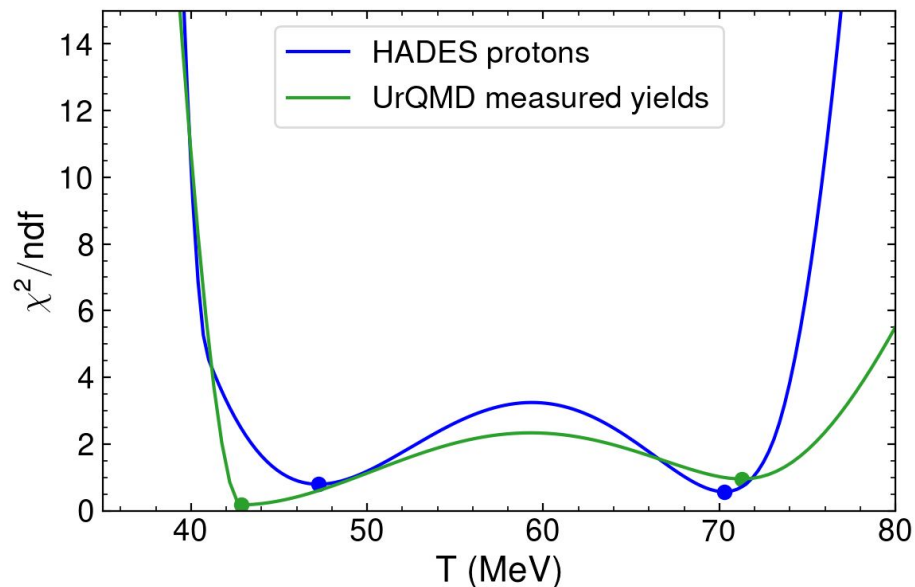
J. Steinheimer et al., 1503.07305

P. Hillmann et al., 1802.01951

F. Seck et al., 2010.04614

Resolving ambiguities: UrQMD χ^2 profiles

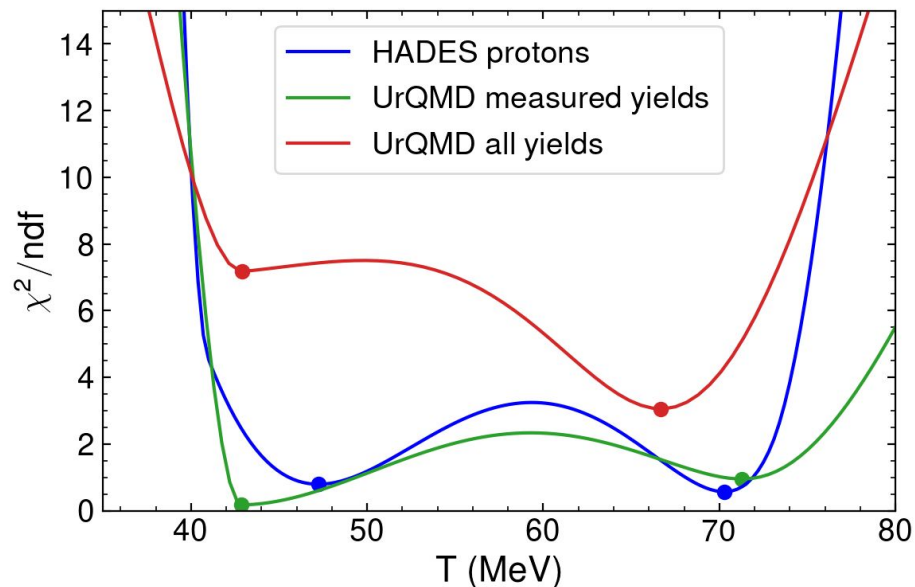
UrQMD prediction for particle yields **reproduces the double-minimum structure** for the fit to the measured ($\pi^{+\,-}$, $K^{+\,-}$, p , Λ) yields.



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The fit to all stable hadron yields **favors higher T minimum.**

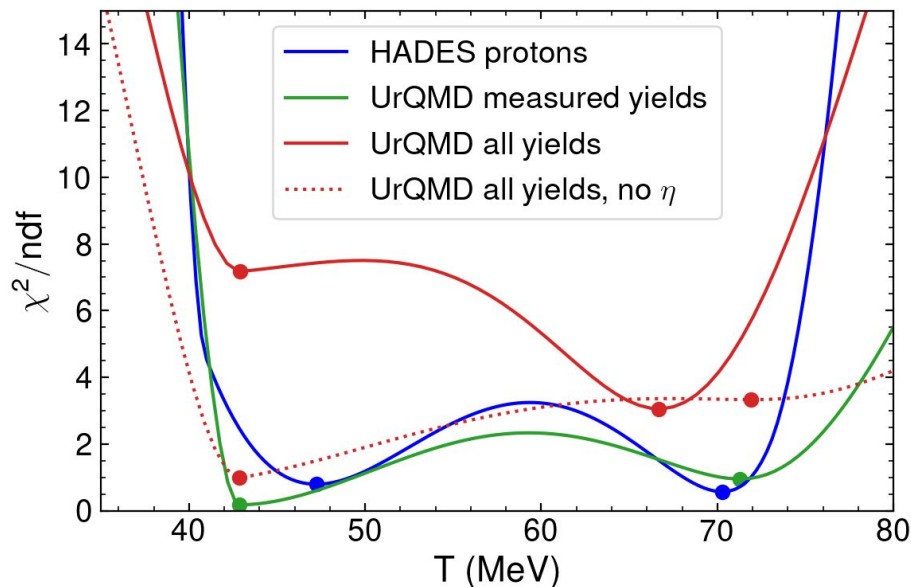


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However, it's very sensitive to the yield of the scalar η meson which is very temperature-sensitive.

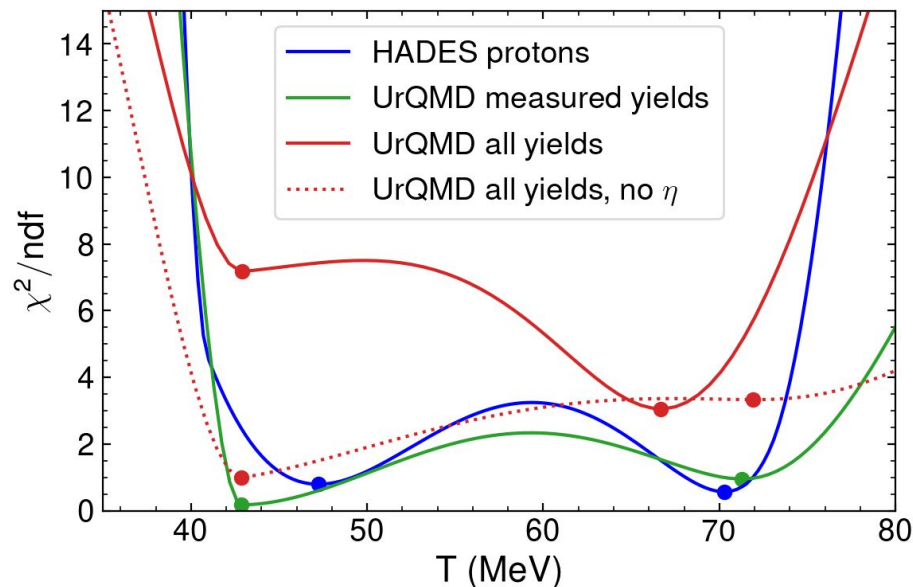


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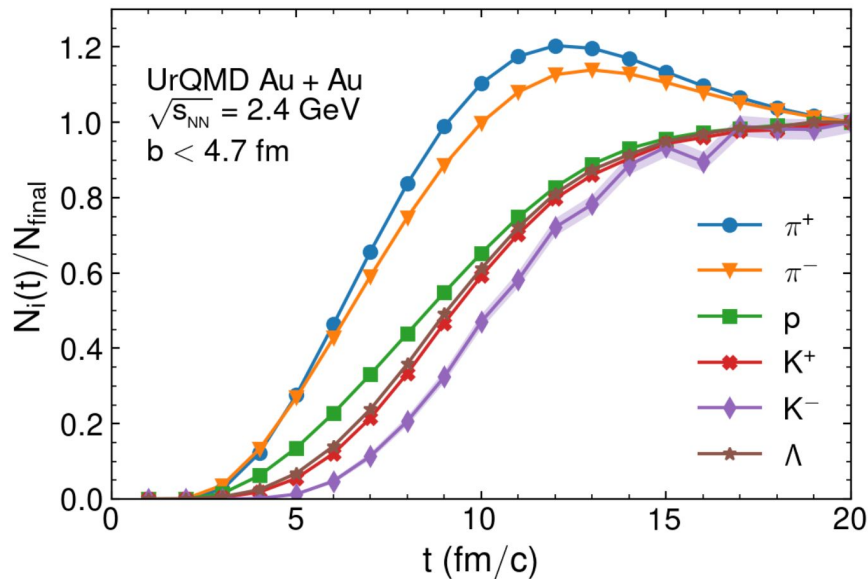
If the best fit depends strongly on the choice of included hadron multiplicities, perhaps, there is no universal chemical freeze-out?..

Resolving ambiguities: fit evolution

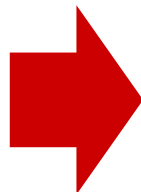
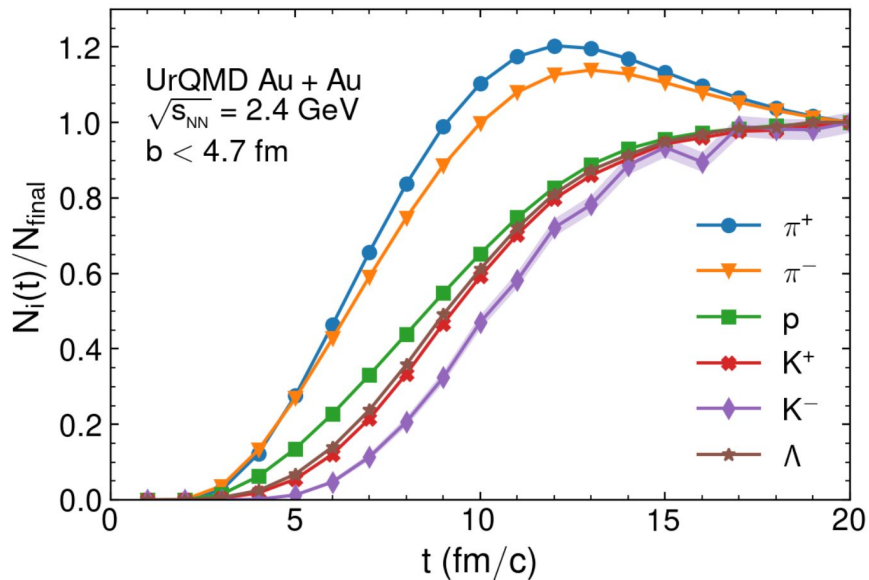
How do the minima reveal themselves during the fireball evolution? Perhaps they appear one after another?

The evolution can be tracked by **fitting time-dependent particle yields** extracted from UrQMD (*Steinheimer et al., 1603.02051*):

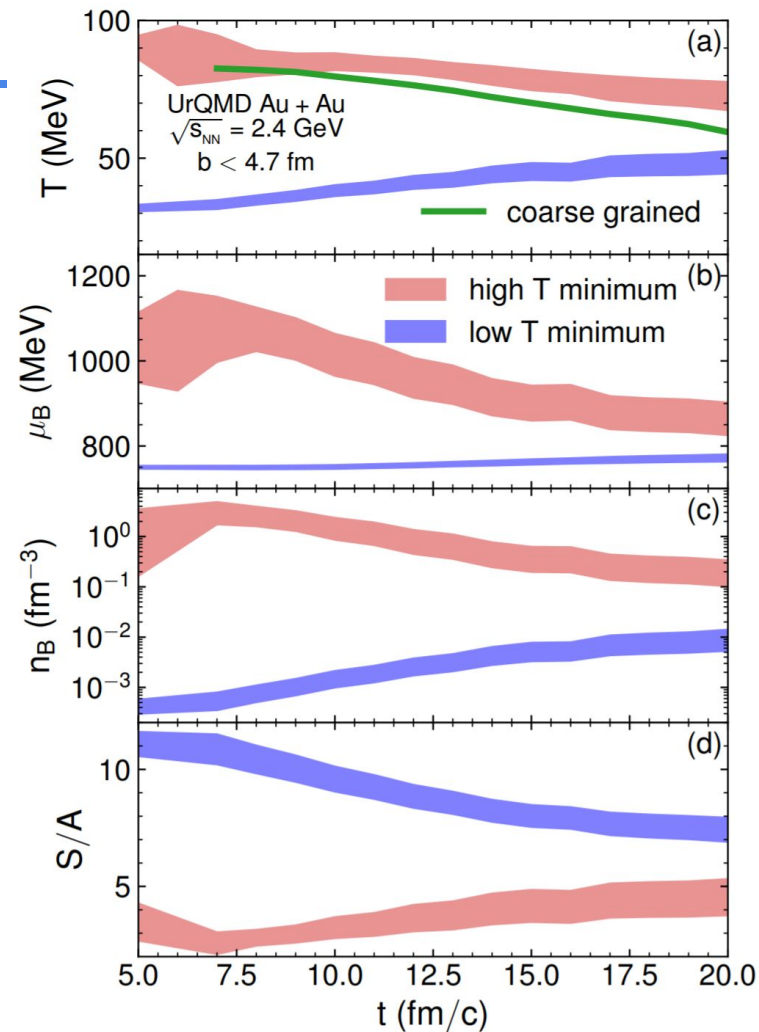
- the UrQMD evolution is stopped at time t
- all unstable hadrons are forced to decay
- the calculated hadron yields are related to time t



Resolving ambiguities: fit evolution



Fit to time-dependent particle yields allows to extract thermodynamic properties at each time t .



Resolving ambiguities: fit evolution

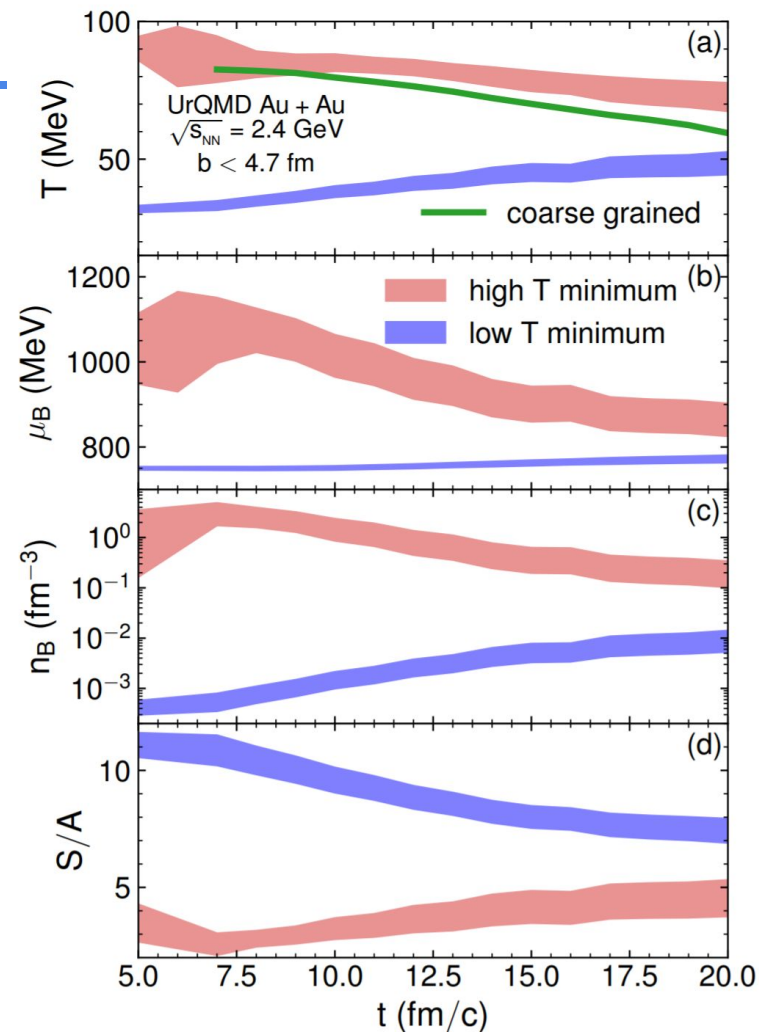
The double minimum structure in the fit is found throughout the whole evolution.

The **high temperature** minimum behaves as “classical” picture of the fireball evolution:

temperature and density (chemical potential) decrease with time as a result of the fireball cooling during the expansion.

The **low temperature** minimum seems to violate the second law of thermodynamics:

total entropy per baryon strongly decreases with time $\Delta S/A(t) < 0$, temperature increases, density decreases



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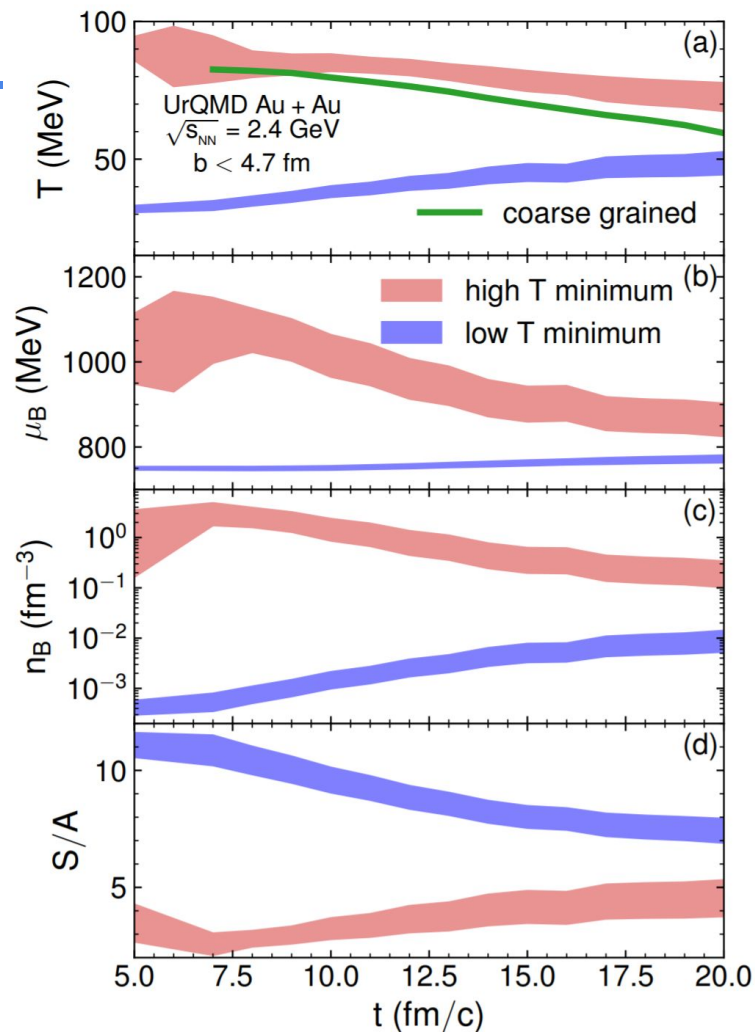
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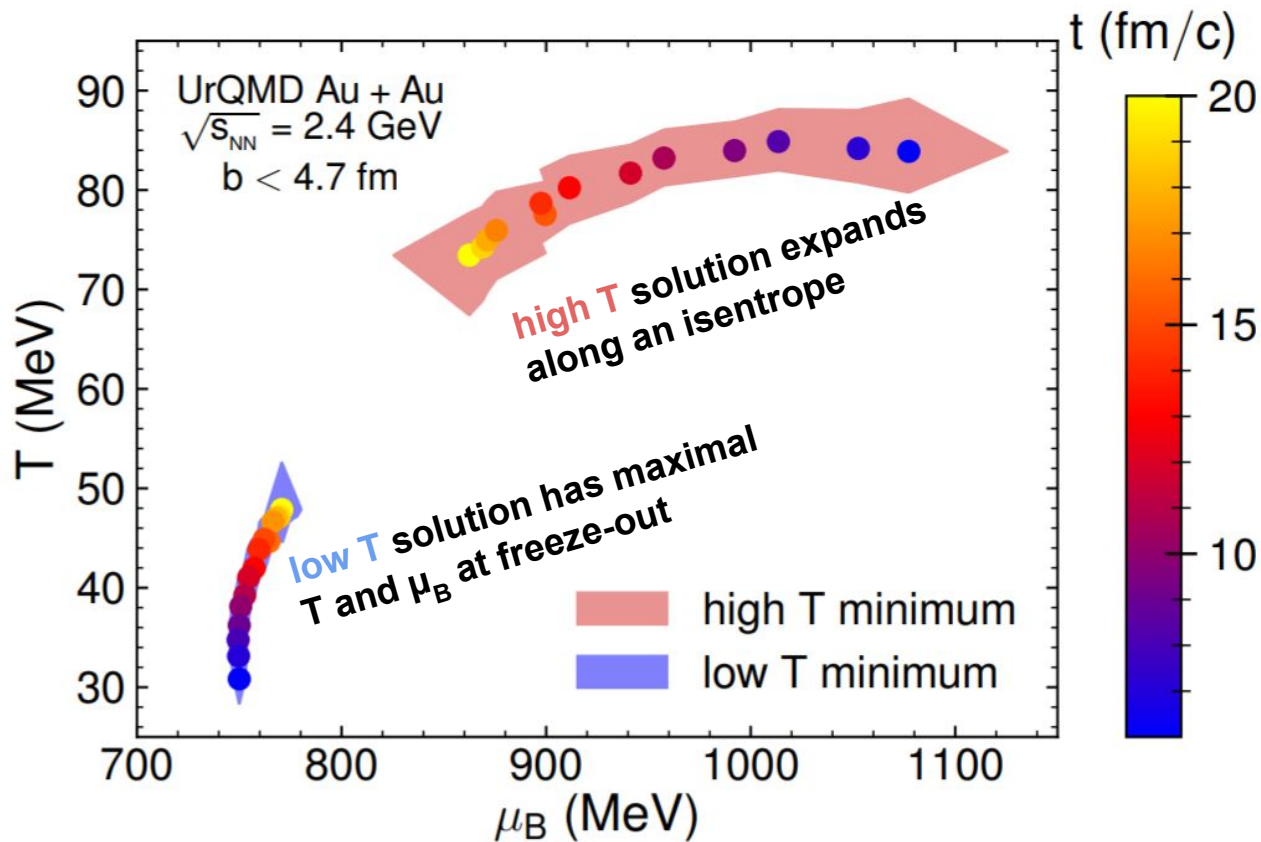
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The low temperature solution behaves unphysically!

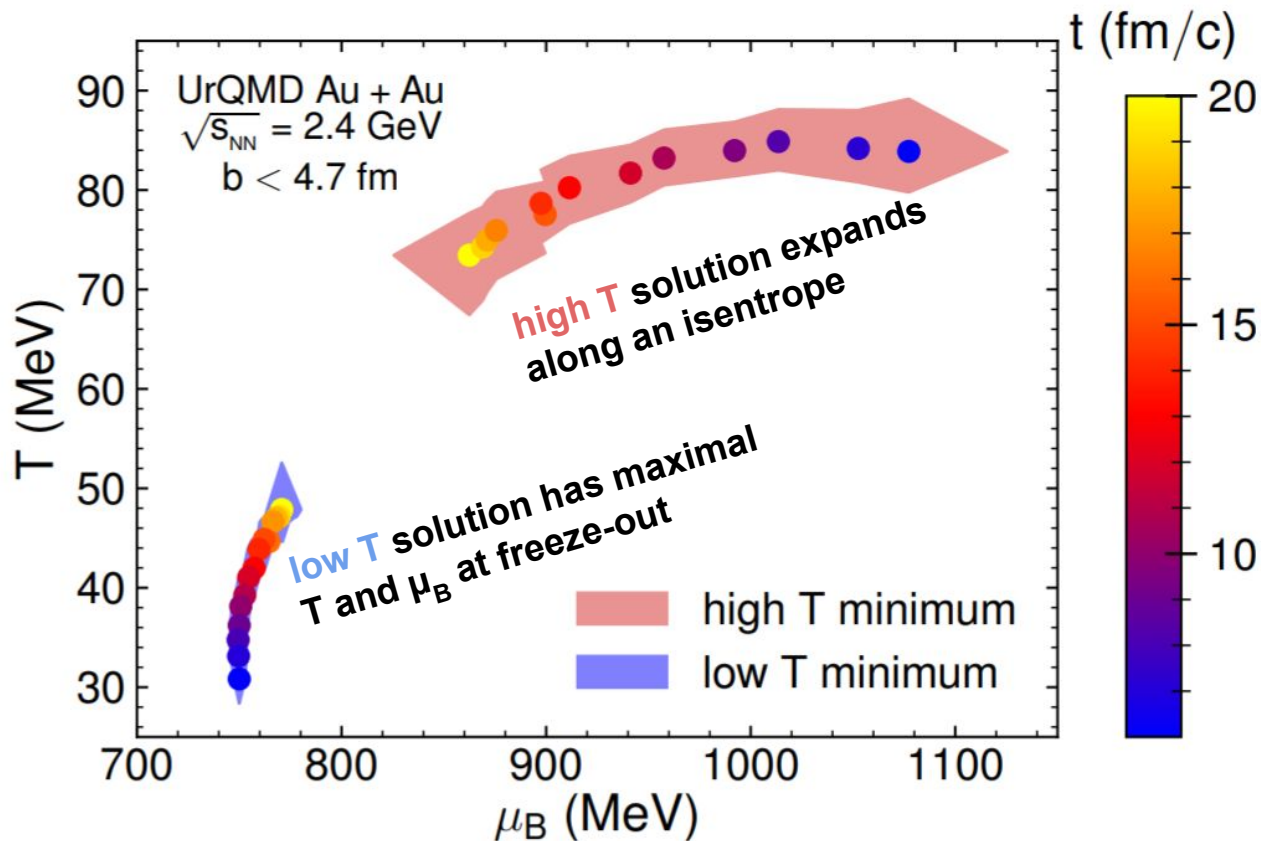


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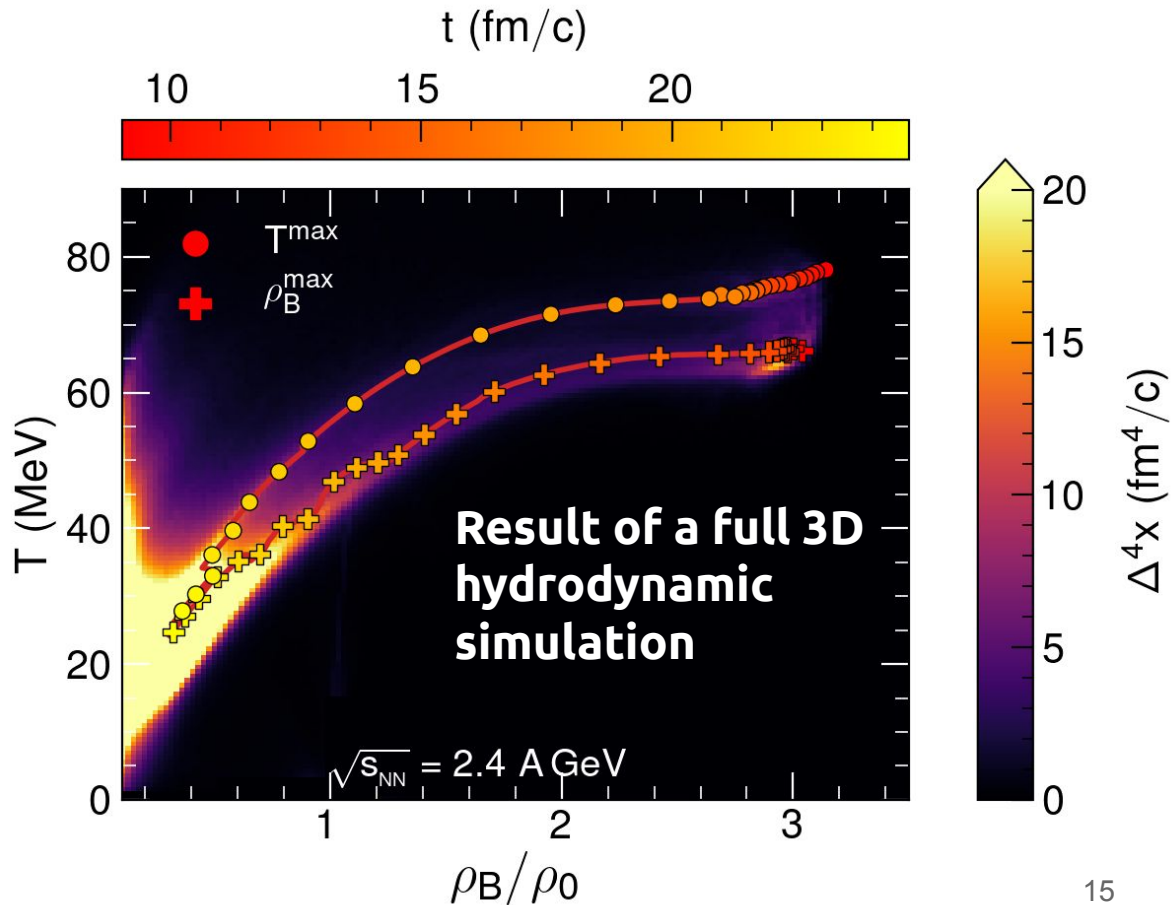
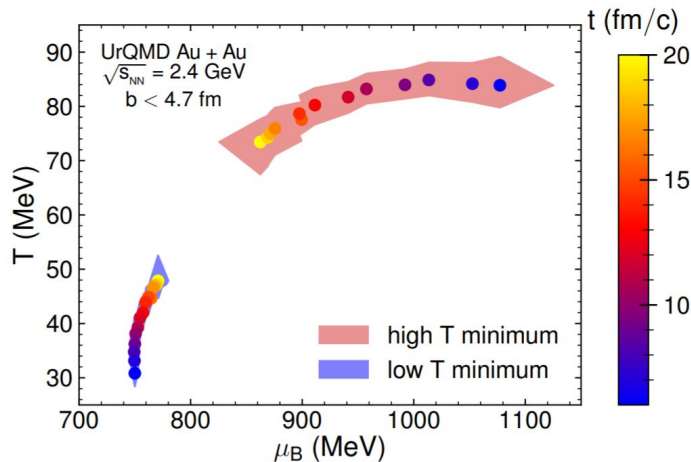
Resolving ambiguities: fit evolution

Only the high T solution can be considered physical.



Resolving ambiguities: fit evolution

One shouldn't forget:
Heavy ion collision is a very complex system where thermal model description is a very rude approximation.
More involving models are required.



Summary

- Thermal model **can not uniquely describe** freeze-out at SIS18 energies:
 - **two degenerate x^2 minima** are present
- Description of **light nuclei** at the freeze-out is unsatisfactory
 - ... possible **room for improvement**
- Analysis of **UrQMD** data yields the **same degenerate x^2 minima**
- Additional **not-yet-measured hadrons do not allow to discern** the minima
 - **unstable hadronic species** may be helpful, but technical (*Motornenko, 1905.00866*)
- A detailed study of the time evolution of the particle yields suggests that only **the high T solution behaves physically, low T solution should be disregarded**

Heavy ion collision is a complex dynamical system, simple approach like thermal model is not capable for all the details

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Thank you for the attention!