

# MODELING OF HgCdTe SWIR DETECTOR INTEGRATION RAMP FOR CONSTANT FLUX AND PERSISTENCE CURRENT

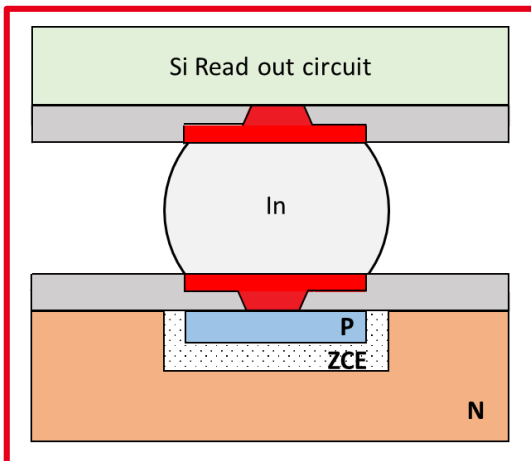
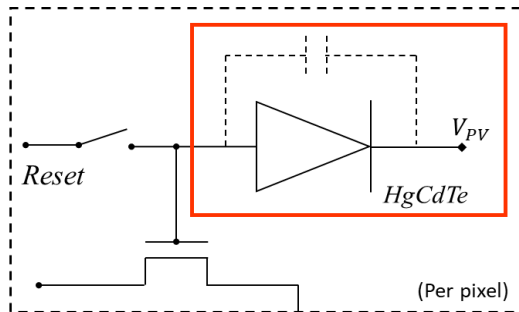
T. LE GOFF\*, T. PICHON\*\*, N. BAIER\*, O. GRAVRAND\*, O. BOULADE\*\*

\*CEA LETI, \*\*CEA IRFU

[titouan.legoff@cea.fr](mailto:titouan.legoff@cea.fr)

### Test Detectors

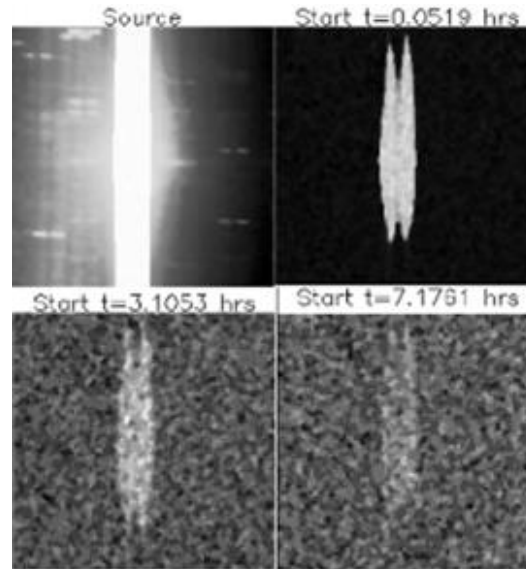
HgCdTe SWIR (2.1 $\mu$ m)  
 15 $\mu$ m pitch, P/N diodes  
 SFD ROIC architecture  
 No nodal capacitance



### Persistence :

= Influence from previous illumination

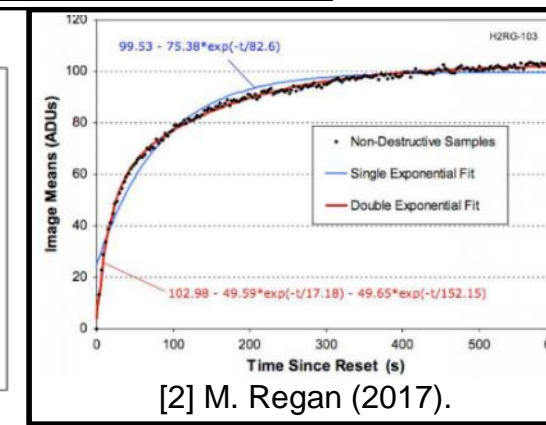
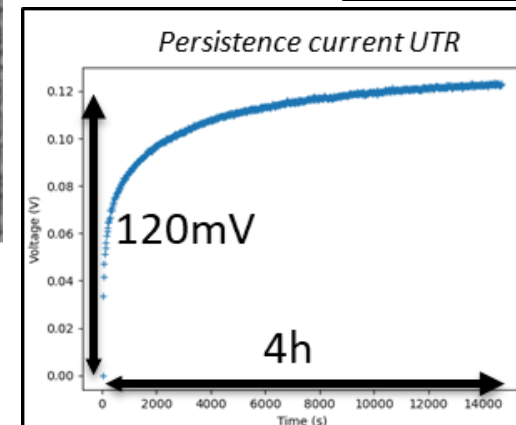
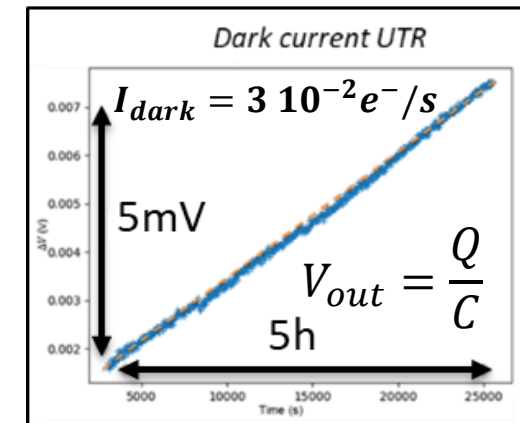
Fit : **sum of exponentials**  
**Signification** of this fit ?



[1] G. Barrick (2012)

### Objectives :

SFD integration ramp  
 Analytical model for persistence signal



[2] M. Regan (2017).

## Modeling of SFD pixel integration ramp

SCR size variation :

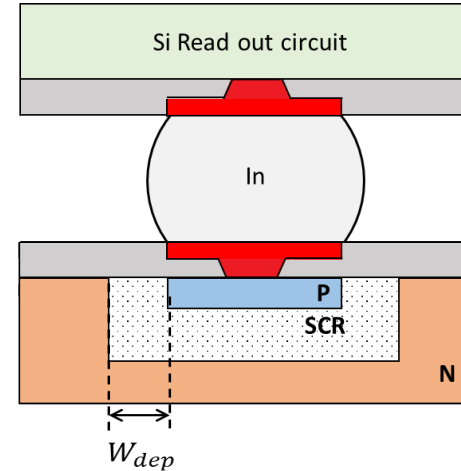
$$W_{dep}(t) = \sqrt{\frac{2\epsilon_{MCT}}{qN_D} [V_{bi} - (V_{app} + V_{out}(t))]}$$

Implies capa variation :  $C = C_{int} + \frac{A\epsilon}{W_{dep}}$

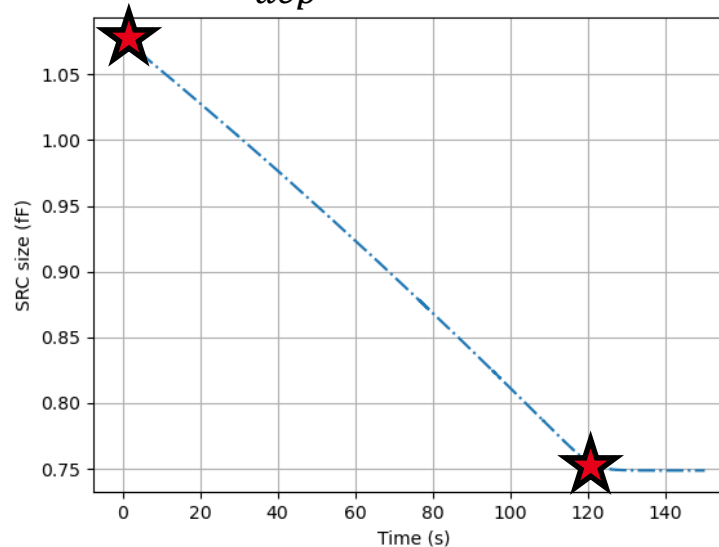
Then [3] :  $V_{out} = \frac{Q}{C}$  variation

With  $I(t) = -I_{sat} \left( e^{\frac{q(V_{app} + V_{float})}{nkT}} - 1 \right) + I_{\phi}$

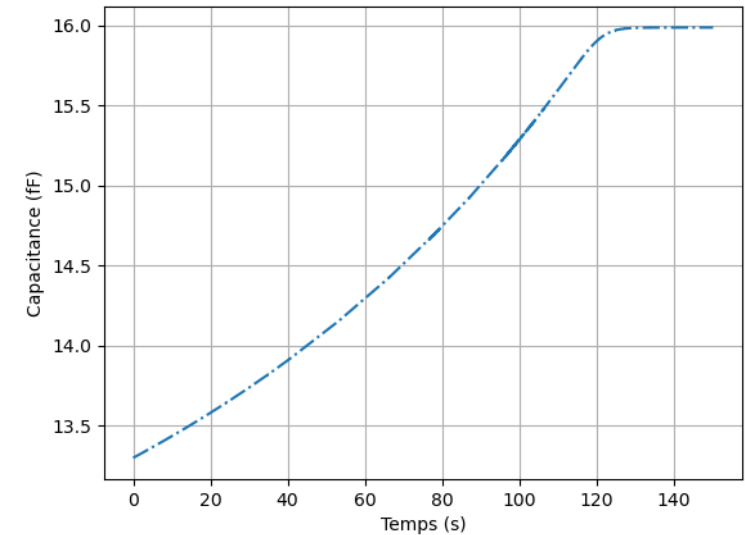
Open circuit equation [4] :  $\frac{dV}{dt} = \frac{I(t)}{C}$



$W_{dep}$  size variation



Pixel capacitance variation



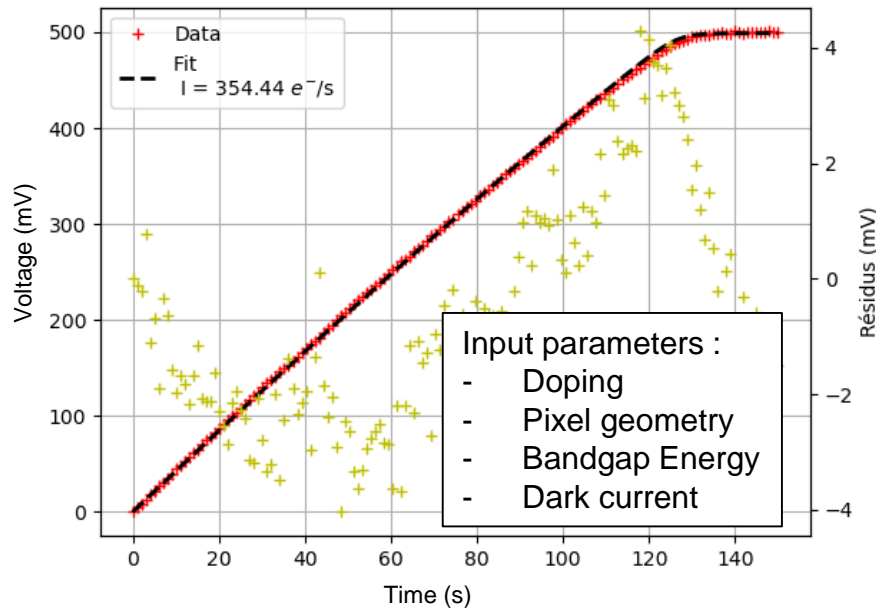
[3] : Bezawada N., Ives D., Atkinson D., SPIE, 2007  
 [4] : Weckler G.P., IEEE Journal of Solid-State Circuits, 1967

## Modeling of SFD pixel integration ramp – application for fitting

### Measured current estimation

Low residuals (~1%)  
 Consistant with linear fit (1,5% difference)

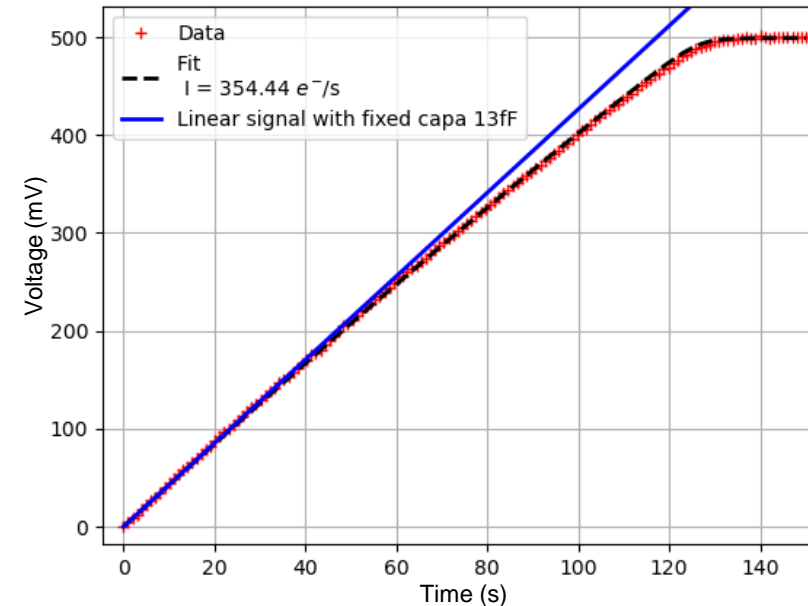
*Simu VS data and residuals*



### Limits for direct application

Time consuming (VS linear fit)  
 Accurate values of pixel parameters

*Model VS constant gain fitting*



➔ Next step for persistance : non linear current

**Usual explanation :**

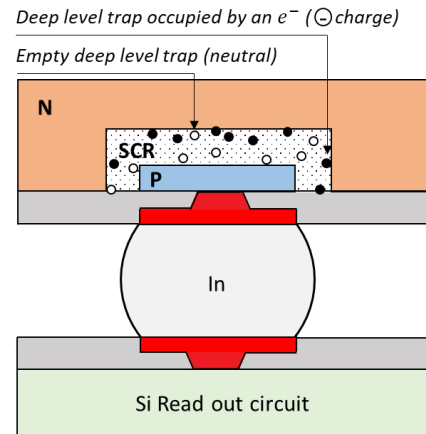
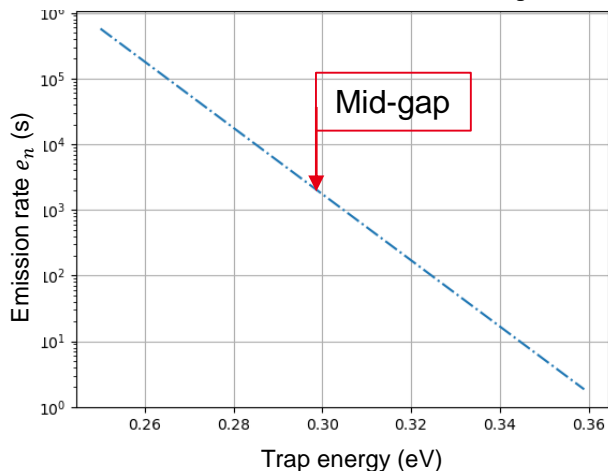
**Defects trapping/emission processes from diode SCR with moving edges**

Trap emission dynamics:

$$e_n(E_T) = \sigma_n v_{th} N_c \exp\left[-\frac{E_c - E_T}{kT}\right]$$

And  $\frac{dn}{dt} = e_n n_T(t)$  et  $\frac{dn_T}{dt} = -e_n n_T(t)$

Emission rate function of trap energy for  $E_g = 0,6eV$

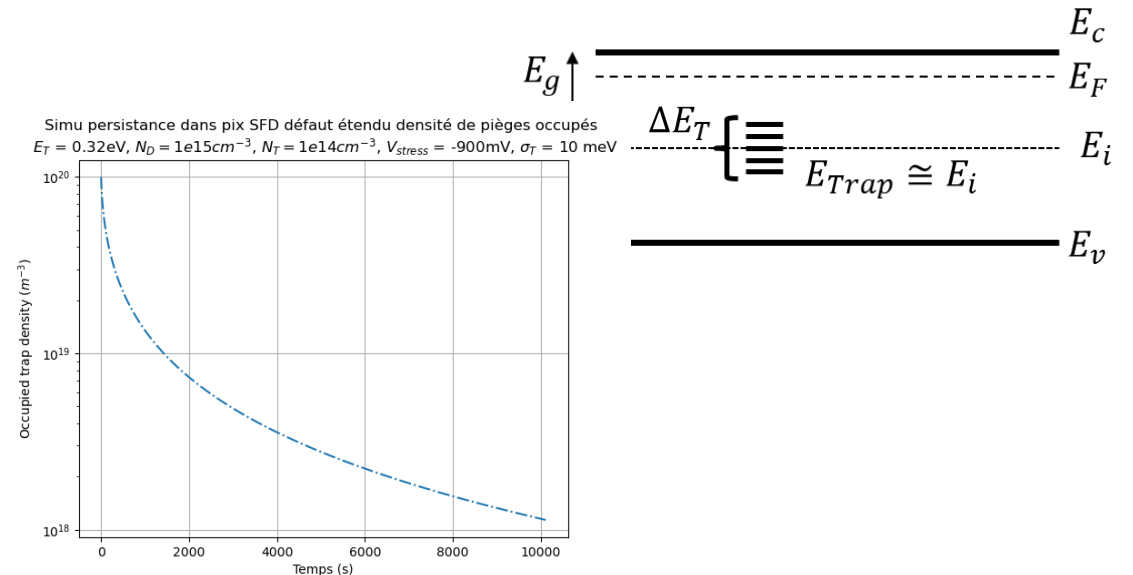


**New hypothesis :**

**Defects with extended energy level distribution**

$$[5] n_T(t) = n_T(0) \int_0^\infty g(E_{Ti}) \exp[-e_n(E_{Ti})t] dE_{Ti}$$

$$g(E_{Ti}) = \frac{1}{\sigma_T \sqrt{2\pi}} \exp\left[-\frac{(E_{T0} - E_{Ti})^2}{2\sigma_T^2}\right]$$



## Current from this trap emission [6]:

$I_e(t)$  : Carrier emission from traps

$$I_e(t) = qA \int_{W_0}^{W(t)} \frac{dn}{dt} dx = qA e_n n_T(t) [W(t) - W_0]$$

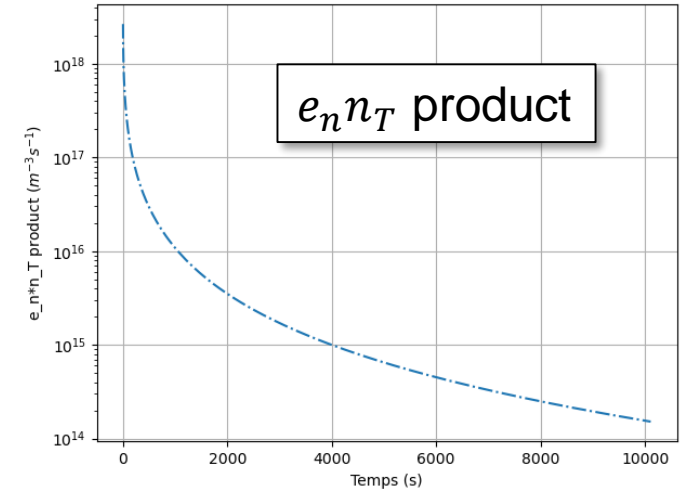
$I_d(t)$  : Electric field variation in the SCR due to charge concentration variation

$$I_d = qA \int_{W_0}^{W(t)} \frac{dn_T}{dt} \frac{x}{W(t)} dx = -qA e_n n_T(t) \left[ \frac{W(t)^2 - W_0^2}{2W(t)} \right]$$

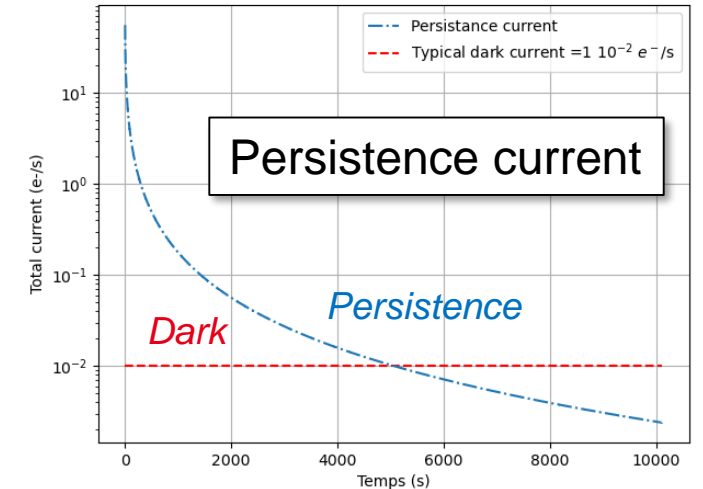
$$I_{tot} = I_e + I_d + I_l = qA \left[ W(t) - W_0 - \frac{W(t)^2 - W_0^2}{2W(t)} \right] e_n n_T(t)$$

$$I_{tot} = qA \left[ W(t) - W_0 - \frac{W(t)^2 - W_0^2}{2W(t)} \right] \int_0^\infty \underbrace{g(E_{Ti}) e_n(E_{Ti})}_{e_n} \underbrace{n_T(0) \exp[-e_n(E_{Ti})t]}_{n_T(t)} dE_{Ti}$$

Simu persistence dans pix SFD défaut étendu produit  $e_n n_T$   
 $E_T = 0.32\text{eV}$ ,  $N_D = 1\text{e}15\text{cm}^{-3}$ ,  $N_T = 1\text{e}14\text{cm}^{-3}$ ,  $V_{stress} = -900\text{mV}$ ,  $\sigma_T = 10\text{ meV}$



Simu persistence dans pix SFD défaut étendu courant de persistence  
 $E_T = 0.32\text{eV}$ ,  $N_D = 1\text{e}15\text{cm}^{-3}$ ,  $N_T = 1\text{e}14\text{cm}^{-3}$ ,  $V_{stress} = -900\text{mV}$ ,  $\sigma_T = 10\text{ meV}$



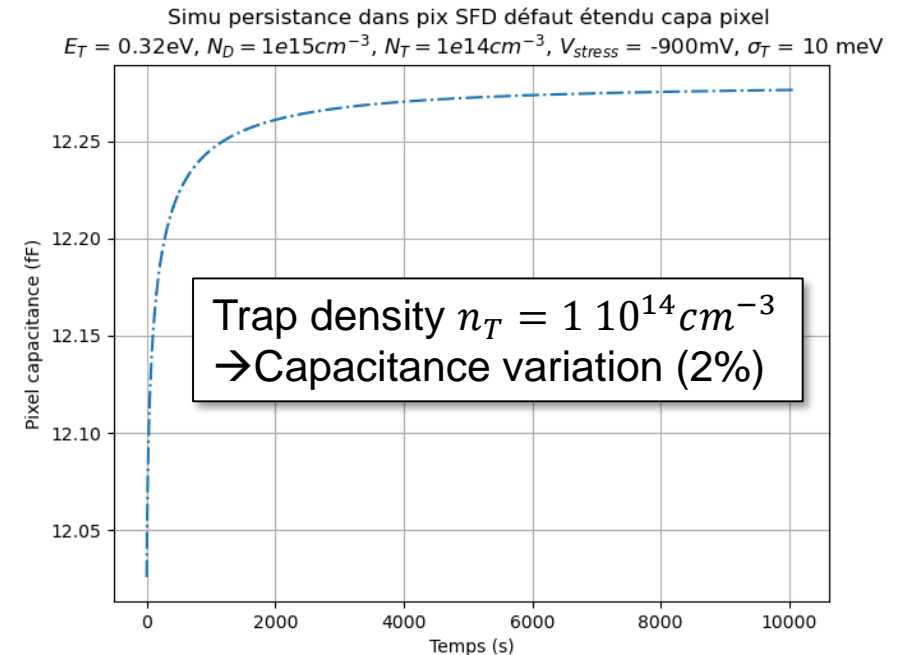
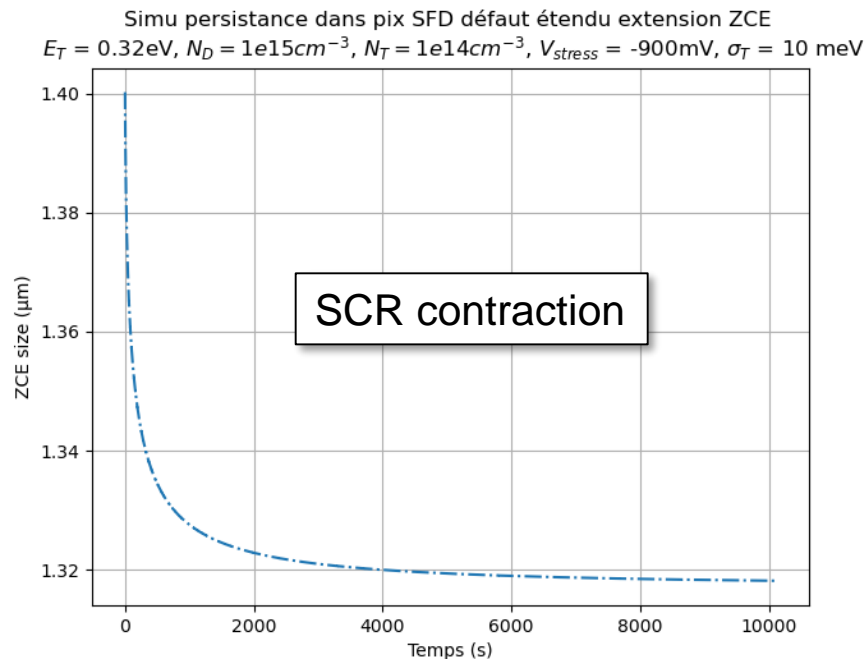
**But also capacitance variation :**

SFD equations:  $C = C_{int} + \frac{A\epsilon}{W_{dep}}$  ;  $\frac{dV}{dt} = \frac{I(t)}{C}$

Persistence in an SFD pixel

- Current transient
- And changing  $V/e^-$  conversion gain (if  $\frac{n_T}{N_D} \gg 0$ )

Persistence:  $W(t) = \sqrt{\frac{2\epsilon_{MCT}}{q[N_D - n_T(t)]} [V_{bi} - (V_{stress} + V_{float}(t))]}$  ;  $I_{tot} = qA \left[ W(t) - W_0 - \frac{W(t)^2 - W_0^2}{2W(t)} \right] e_n n_T(t)$



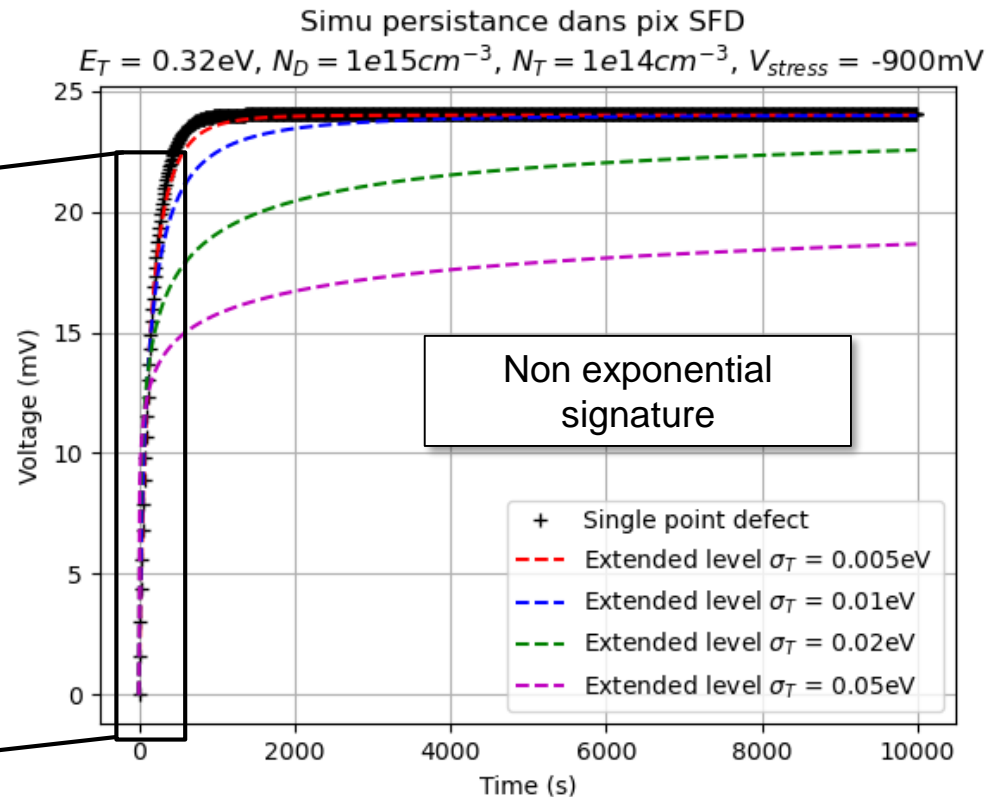
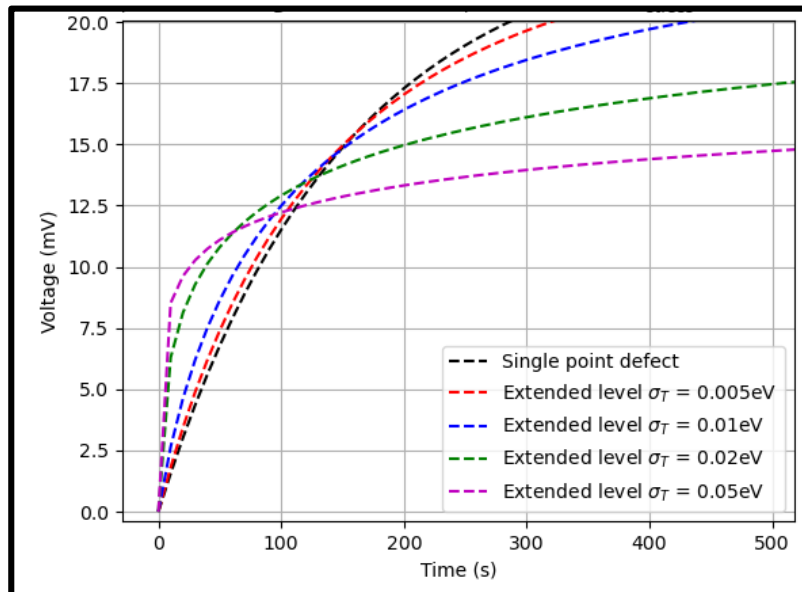
**Persistence dynamics : extended defect**

**Reproduce a multi-exponential shape**

**No impact on persistence amplitude**

Point defect : single exponential signature

Extended defect : multi exponential

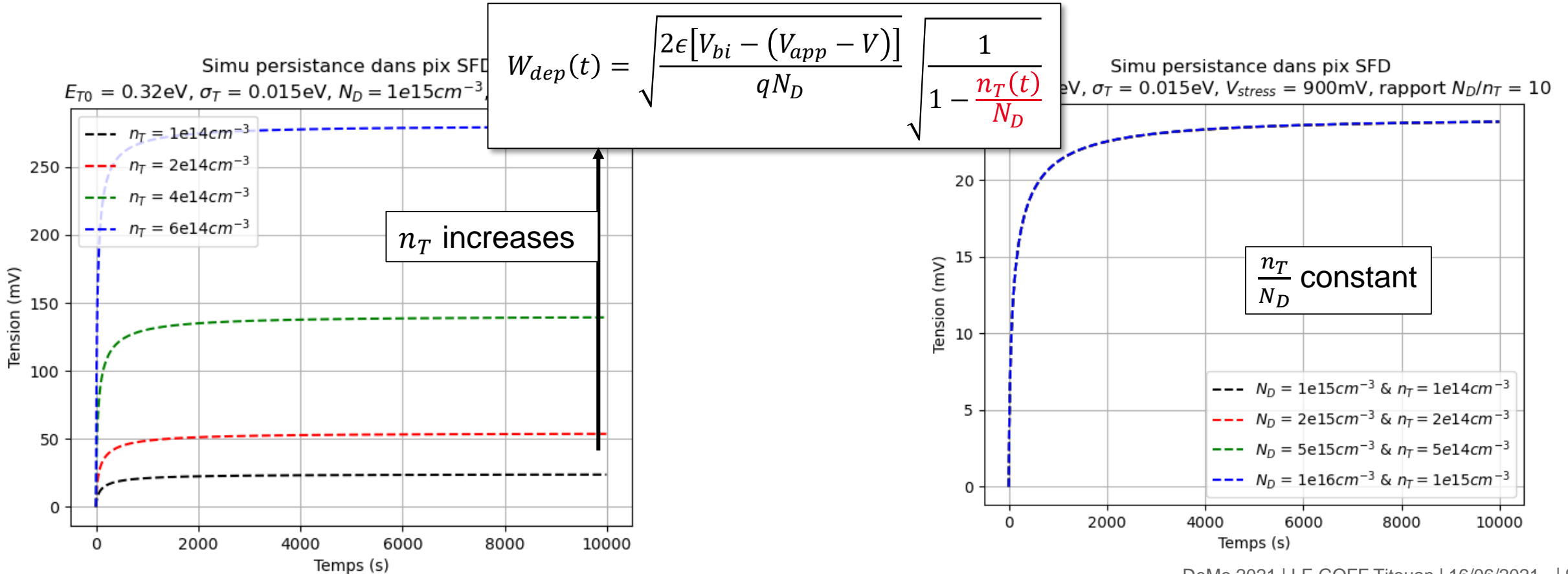




## Persistence amplitude : trap density

Increases persistence amplitude

Ratio  $\frac{n_T}{N_D}$  prevails



### Measurement protocole

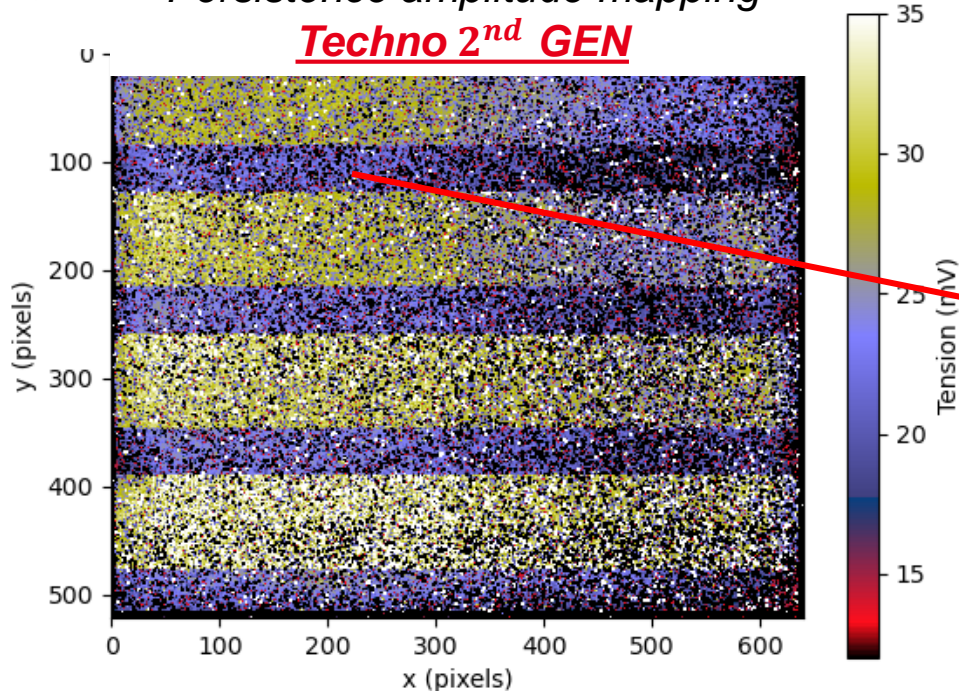
**Electrical stress** ( $0V \rightarrow V_{stress}$ )

**All traps are filled**

Maximizes persistence signal

Persistence amplitude mapping

**Techno 2<sup>nd</sup> GEN**



2-3% persistence, eq to  $3 ke^-$  emitted

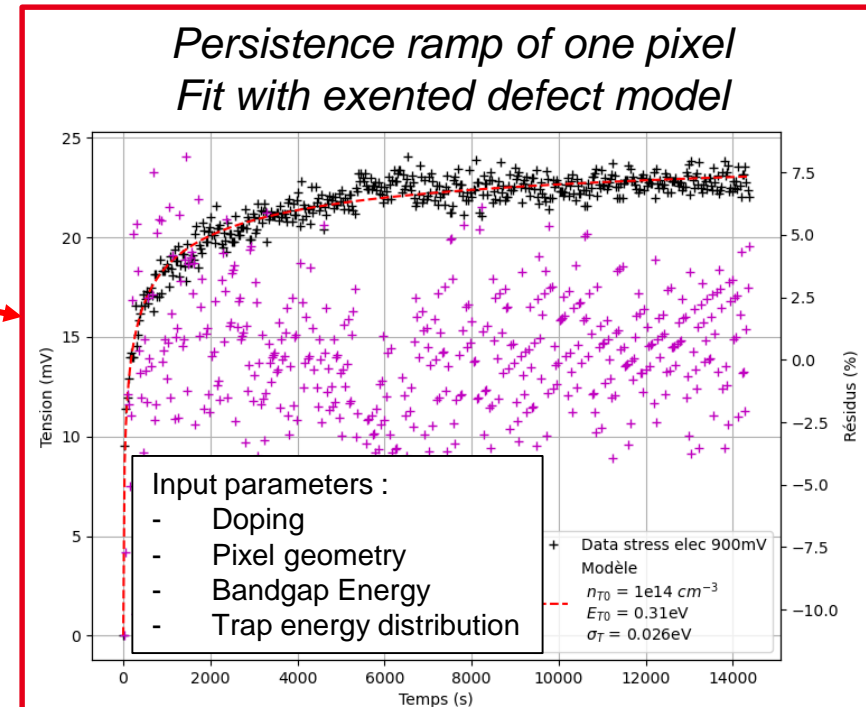
### Data fitting (1 pixel)

White residuals

**Trap density**  $n_T = 1 \cdot 10^{14} \text{ cm}^{-3} = 10\% N_D$

**Trap level**  $E_T = 0,31eV \cong \frac{1}{2} E_g$

Trap band extension  $\sigma_T = 26meV = 9\% E_T$



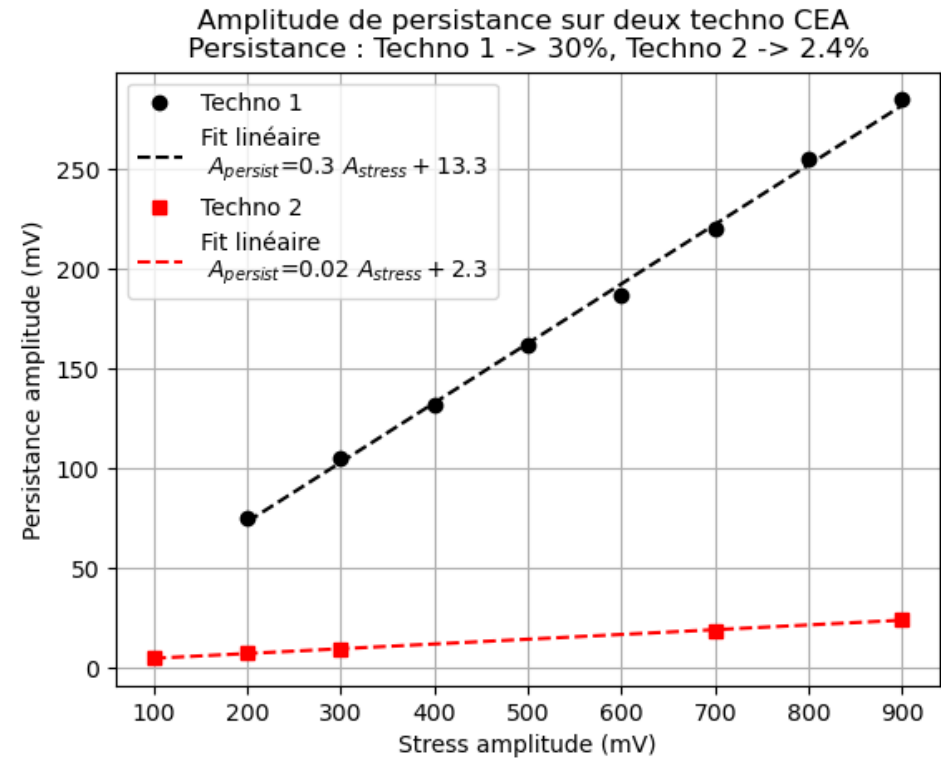
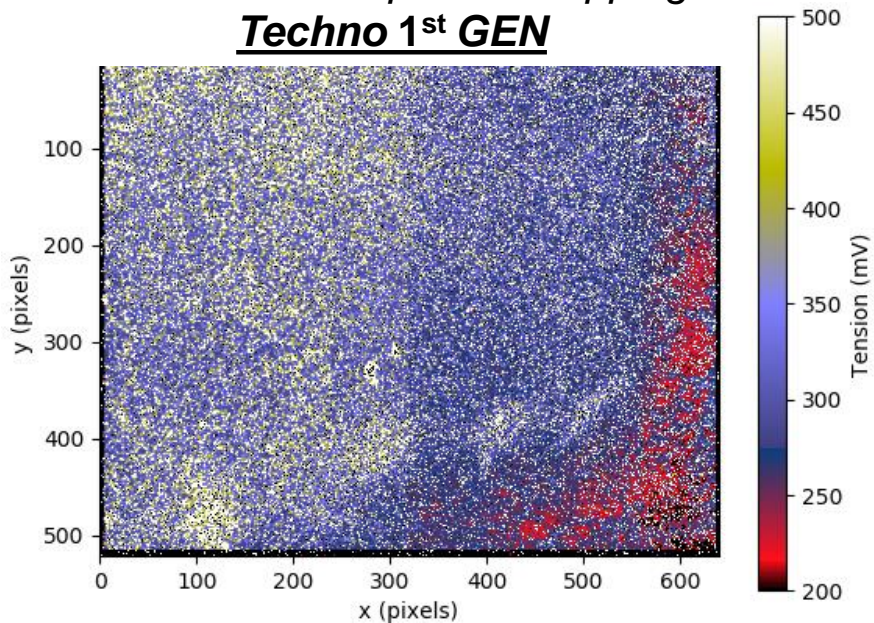
## Model limits

### High persistence amplitude

**Techno 1<sup>st</sup> gen** : 20-30% persistence  $\rightarrow n_T = 80\% N_D$

**Techno 2<sup>nd</sup> gen** : 2-3% persistence  $\rightarrow n_T = 10\% N_D$

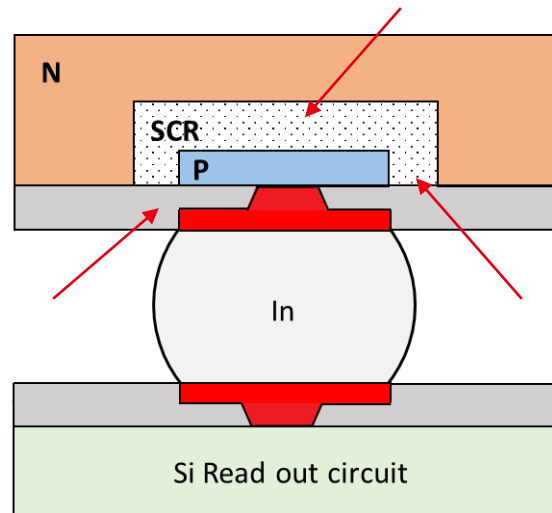
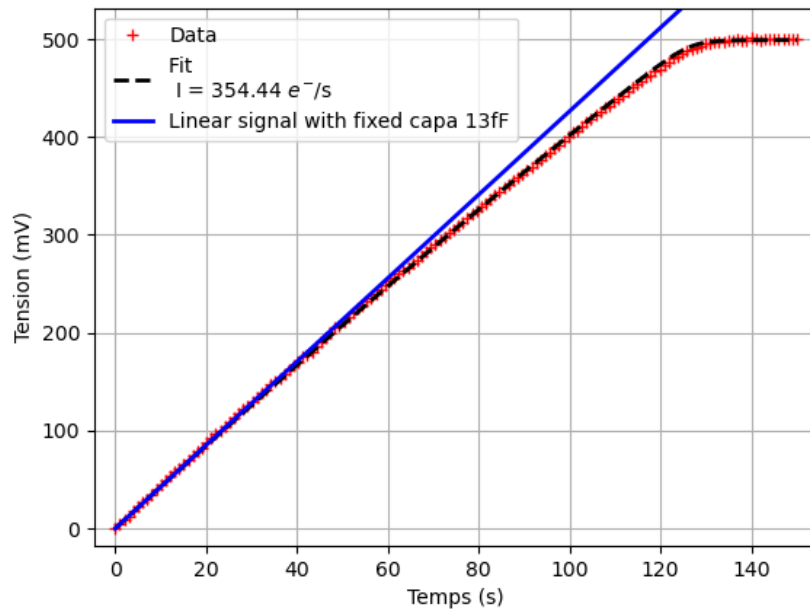
Persistence amplitude mapping  
**Techno 1<sup>st</sup> GEN**



## Analytical model for persistence

### SFD integration ramp

**Persistence current** : trap emission process  
 Trap properties : **extended defects**



### Multi exponential signature

**Consistent** with measurement on Techno 2<sup>nd</sup> gen  
**Needs improvements** and high persistence amplitude

*Persistence ramp of one pixel  
 Fit with exented defect model*

