

Measurements of Warm Dark Matter Properties

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Warm dark matter observables

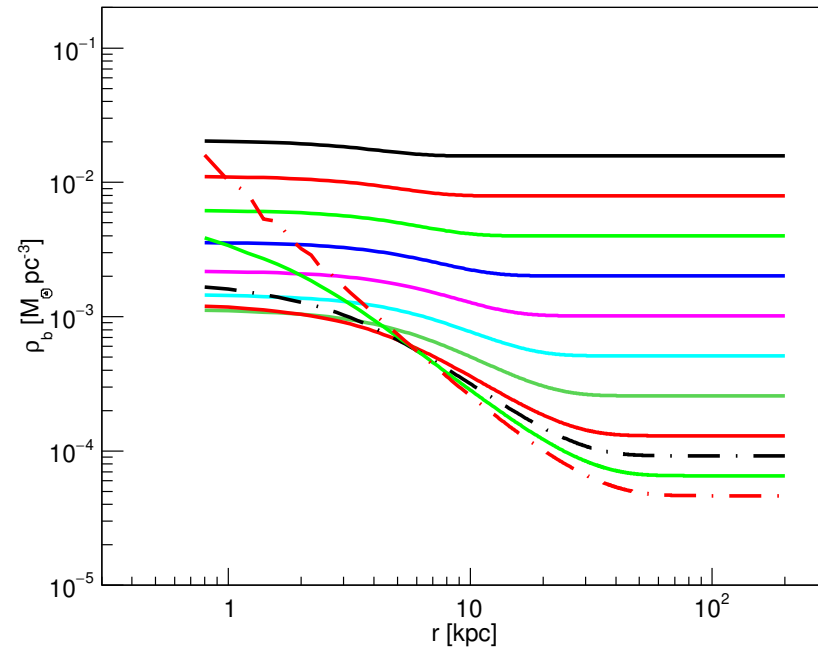
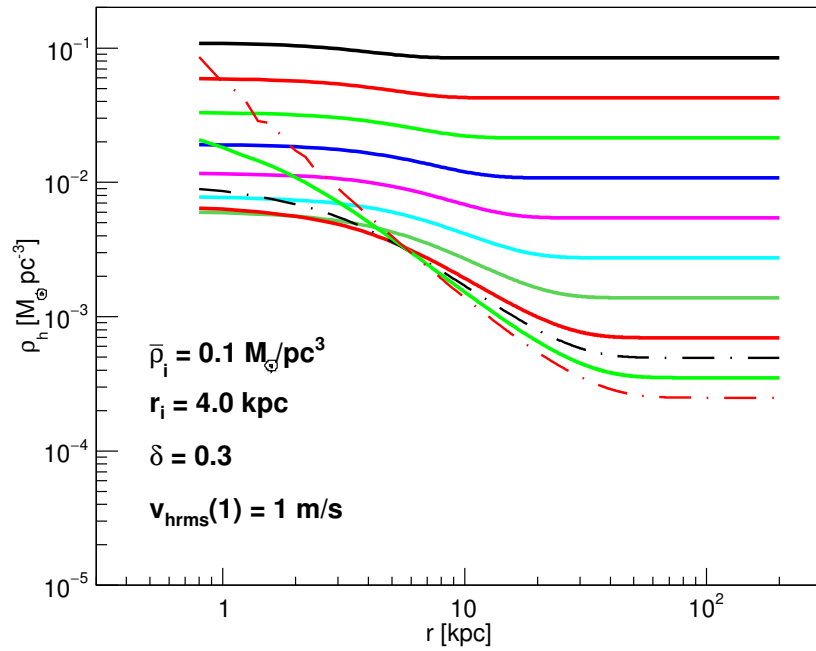
The adiabatic invariant:

$$v_{\text{hrms}}(1) \equiv v_{\text{hrms}}(a)a = v_{\text{hrms}}(a) \left[\frac{\Omega_c \rho_{\text{crit}}}{\rho_h(a)} \right]^{1/3},$$

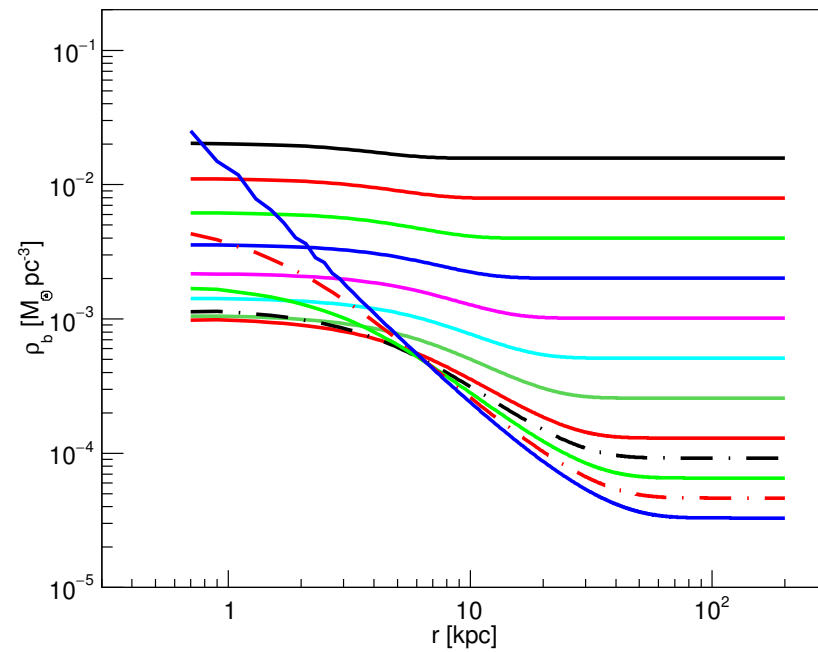
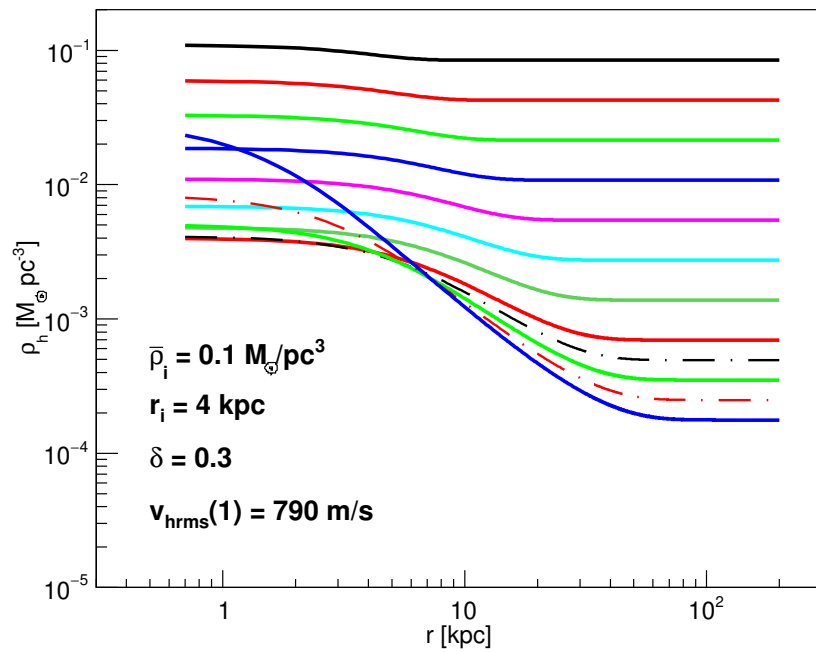
At t_{eq} , the free-streaming power spectrum cut-off factor is

$$\tau^2(k) \approx \exp(-k^2/k_{\text{fs}}^2(t_{\text{eq}})), \quad k_{\text{fs}}(t_{\text{eq}}) = \frac{1.455}{\sqrt{2}} \sqrt{\frac{4\pi G \bar{\rho}_m(1) a_{\text{eq}}}{v_{\text{hrms}}(1)^2}}.$$

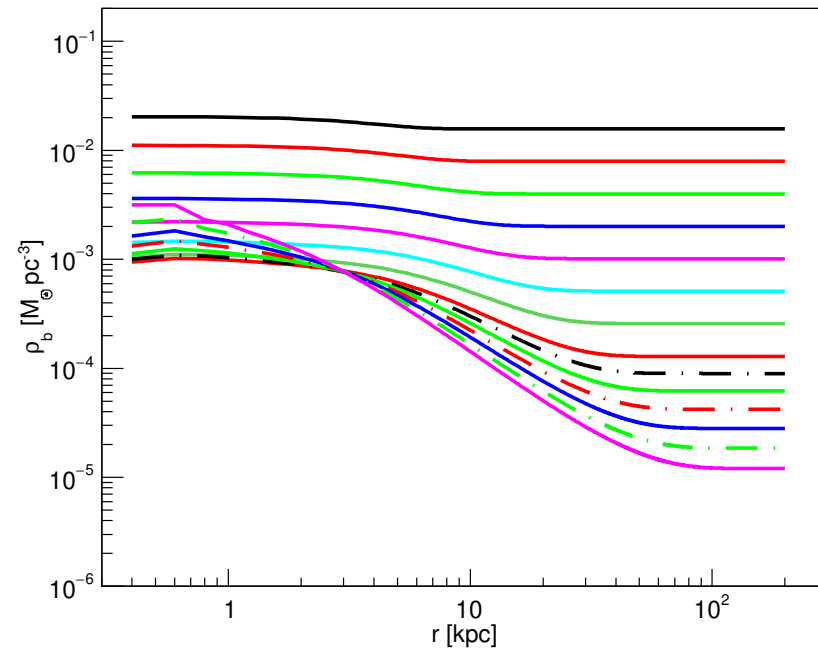
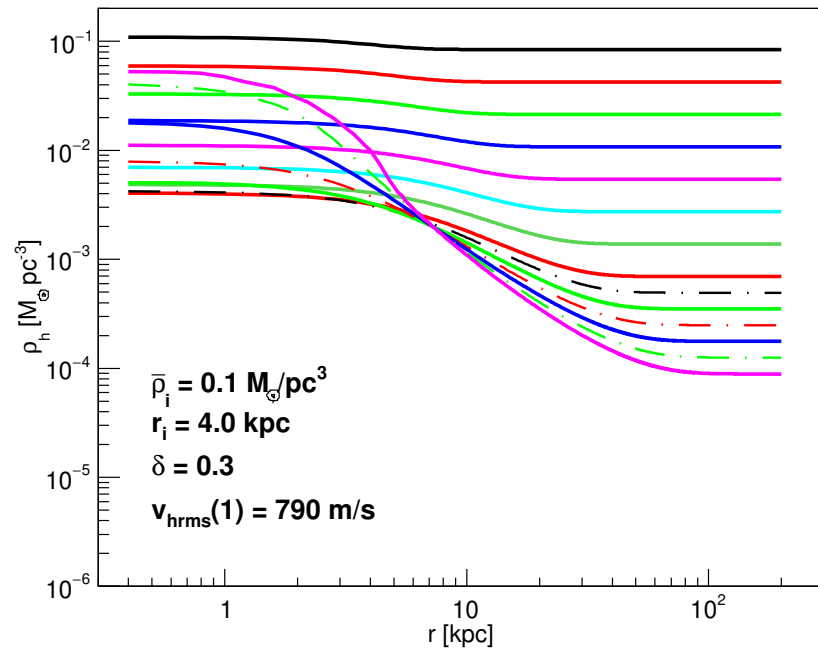
Challenge: Measure the adiabatic invariant $v_{\text{hrms}}(1)$, the comoving free-streaming cut-off wavenumber $k_{\text{fs}}(t_{\text{eq}})$, and the velocity dispersion linear perturbation cut-off mass M_{vd} , and check their consistency.



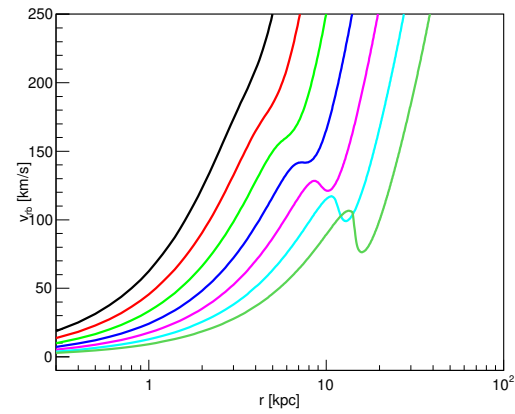
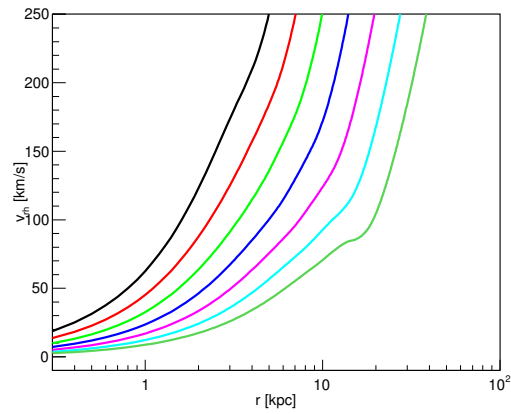
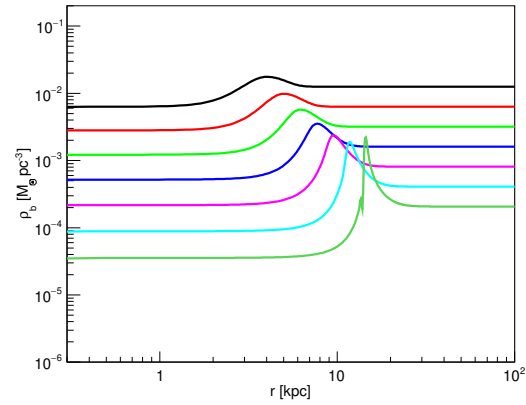
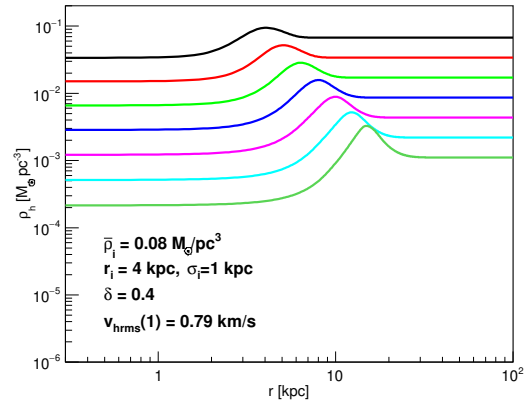
Shown are the **cold** dark matter and baryon densities as a function of r and t during the formation of a galaxy.



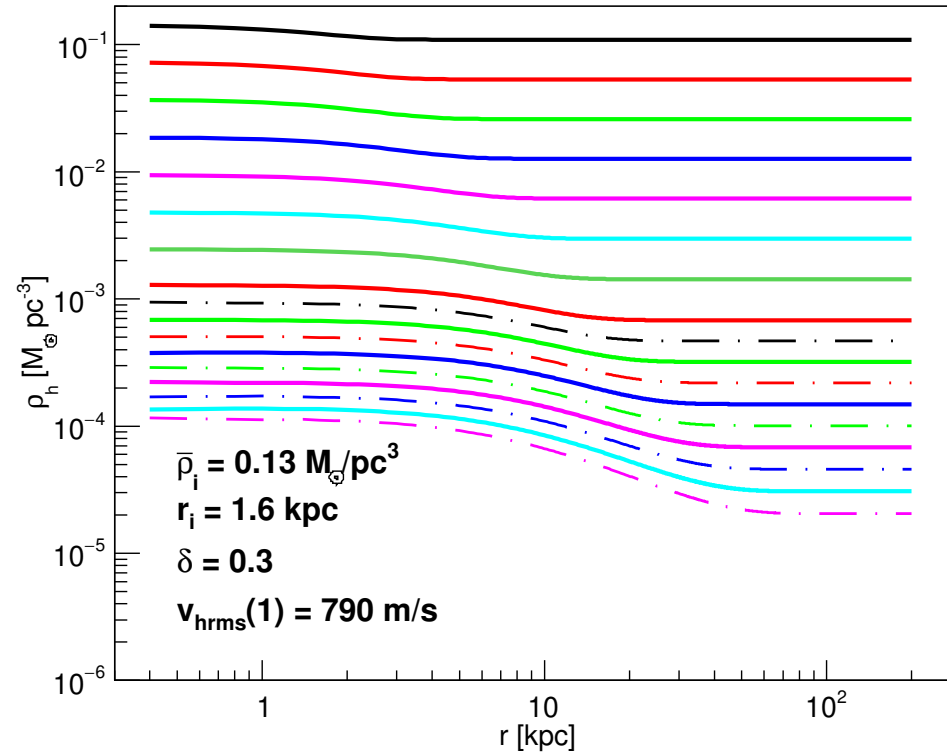
Shown are the **warm** dark matter and baryon densities as a function of r and t during the formation of an elliptical galaxy. Note: DM core, delayed formation, $\rho_b(0) > \rho_h(0) \rightarrow \text{stars}, v_{\text{hrms}}(1)$.



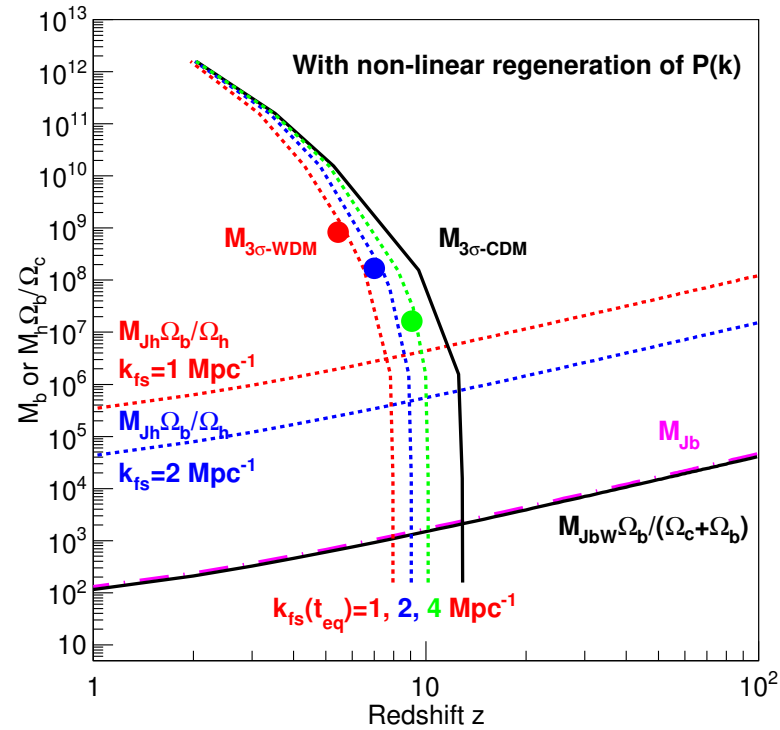
Shown are the **warm** dark matter and baryon densities as a function of r and t during the formation of a spiral galaxy with angular momentum.



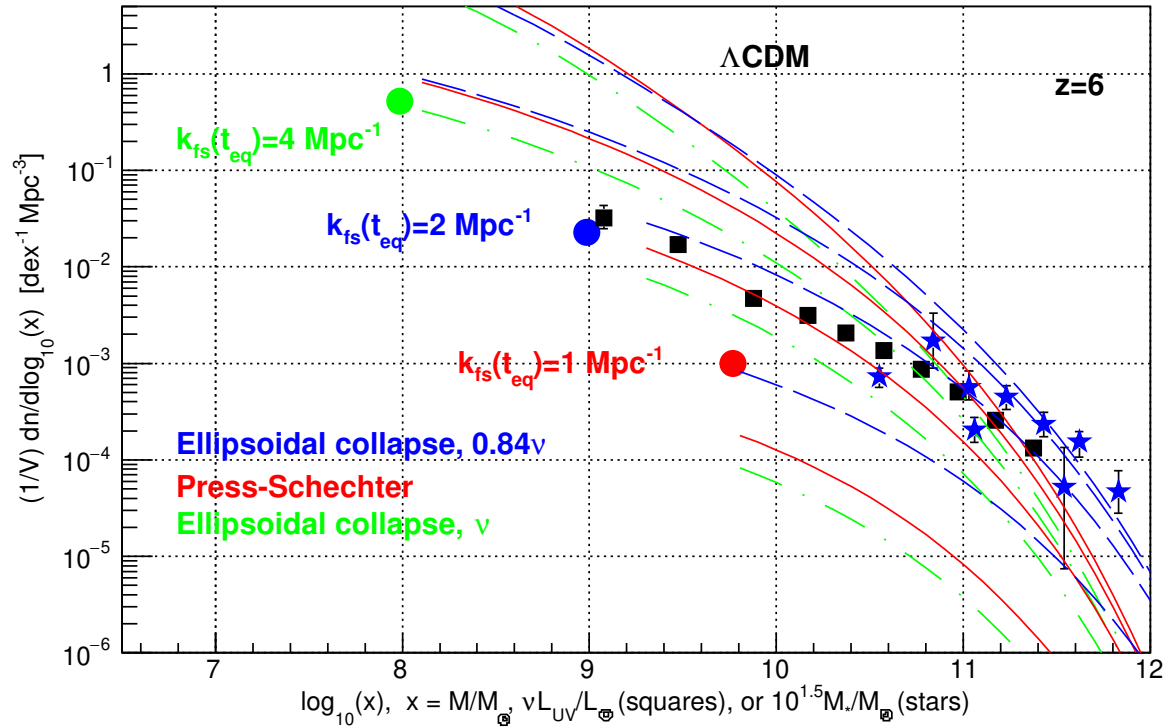
Shown are the **warm** dark matter and baryon densities and velocities as a function of r and t during the formation of a spherical sheet.



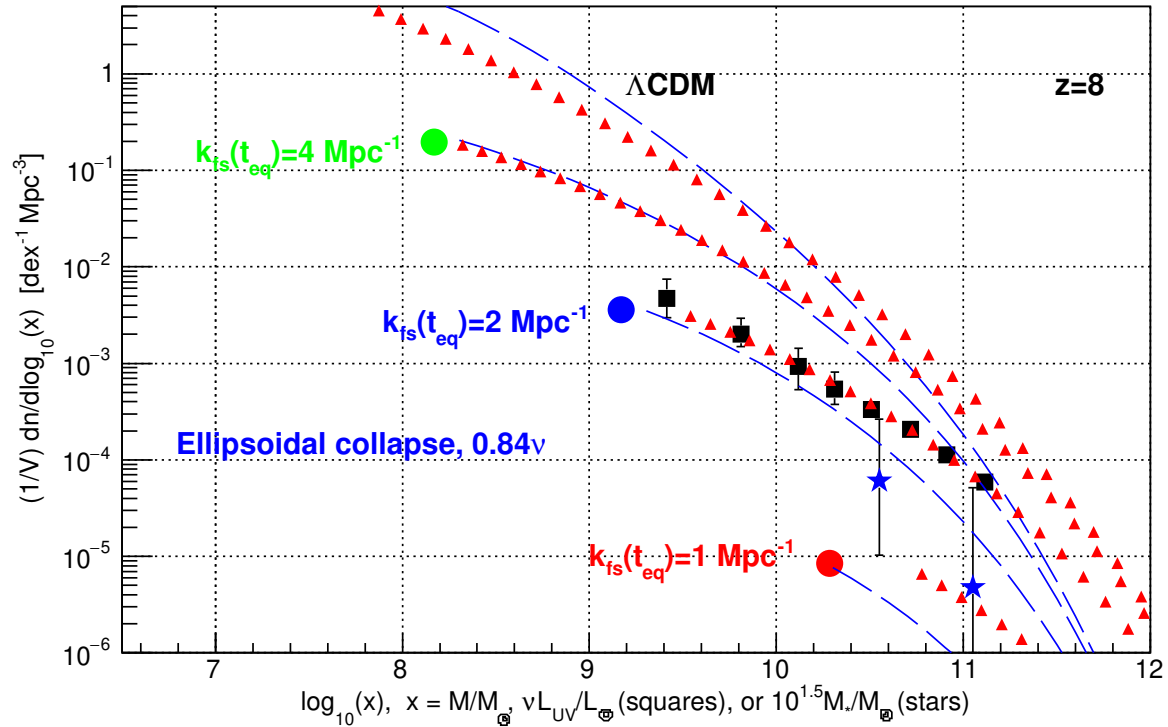
If the linear mass $M = M_h + M_b$ is below the **velocity dispersion cut-off** M_{vd} , formation of a gravitationally bound structure is delayed or absent.



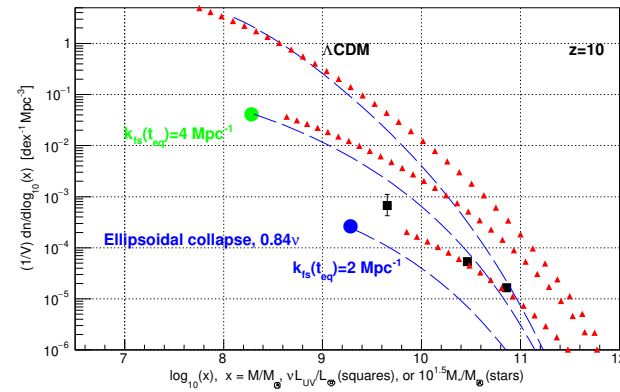
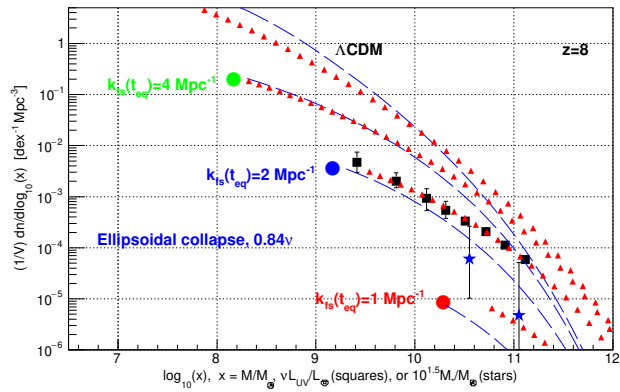
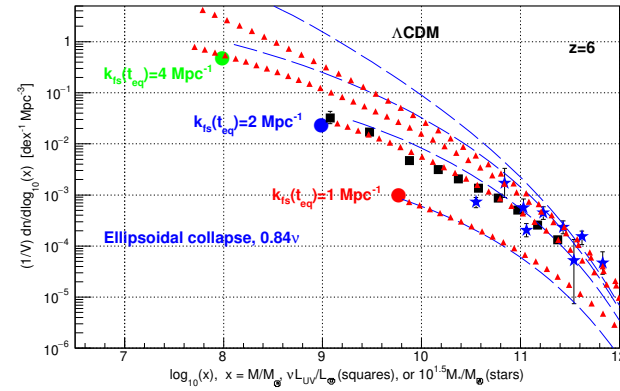
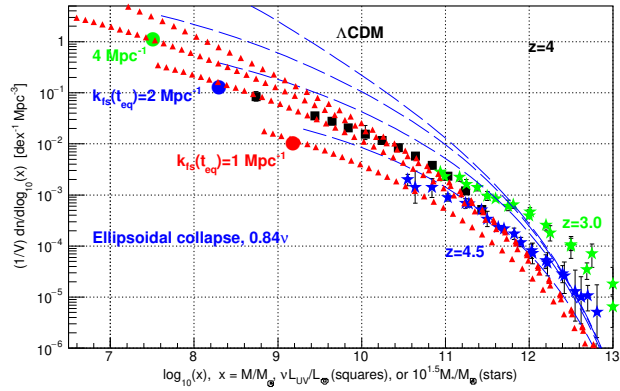
Contours of $1.686 = 3\sigma(M, k_{fs}, z)$ illustrate formation of “first” galaxies. Valid only above the velocity dispersion cut-offs indicated by dots. Note that $2 \text{ Mpc}^{-1} \lesssim k_{fs} \lesssim 4 \text{ Mpc}^{-1}$. Three observables of Λ WDM: $v_{hrms}(1)$, $k_{fs}(t_{eq})$, M_{vd} .



Shown are distributions of predicted linear masses M/M_{\odot} (lines), observed stellar masses $10^{1.5}M_*/M_{\odot}$ (blue stars), and rest frame ultra-violet luminosities $\nu L_{UV}/L_{\odot}$ (black squares), at redshift $z = 6$. Note that $k_{fs} \approx 2 \text{ Mpc}^{-1}$.



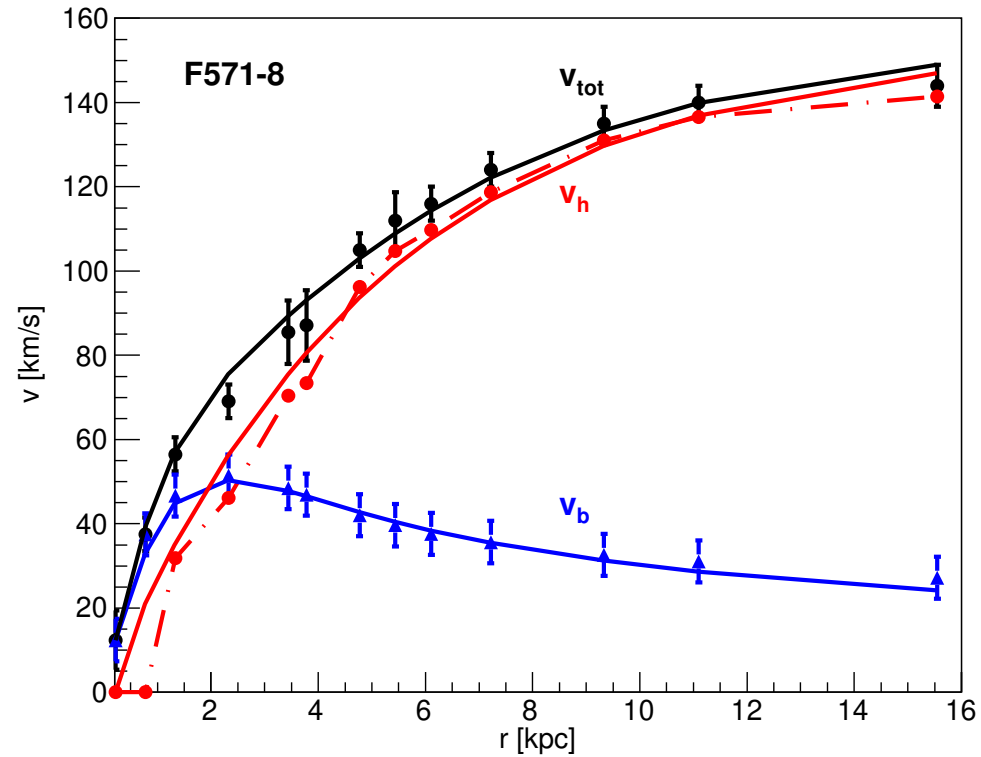
Shown are distributions of predicted linear masses M/M_{\odot} (lines), UV luminosities (red triangles), observed stellar masses $10^{1.5}M_*/M_{\odot}$ (blue stars), and rest frame ultra-violet luminosities $\nu L_{UV}/L_{\odot}$ (black squares), at redshift $z = 8$. Note that $k_{fs} \approx 2 \text{ Mpc}^{-1}$.



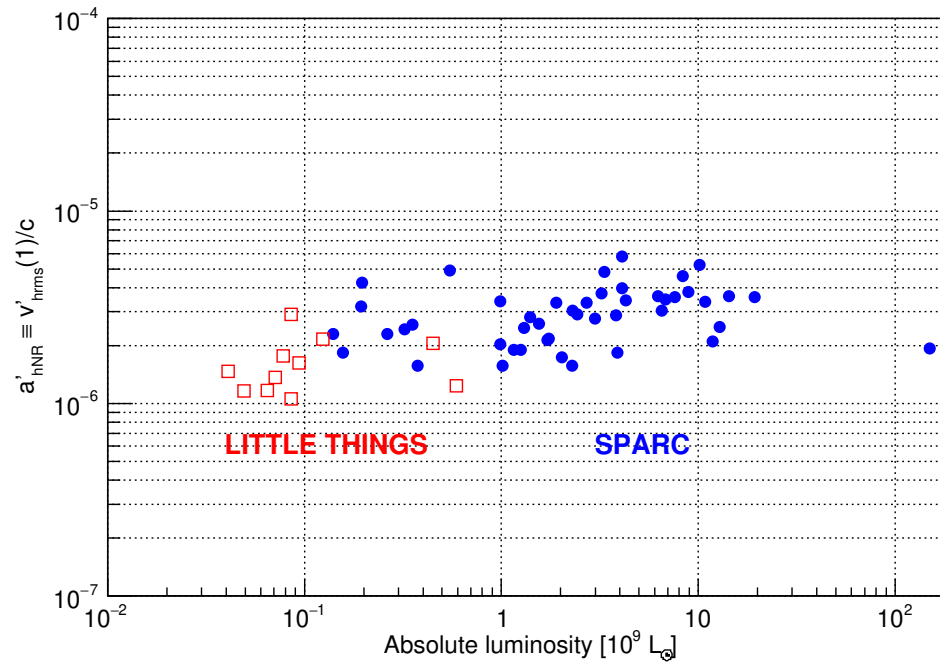
Same for $z = 4, 6, 8, 10$. Note that $k_{fs} \approx 2 \text{ Mpc}^{-1}$.

At $z = 8$, for each $k_{\text{fs}}(t_{\text{eq}})$ are presented the **velocity dispersion cut-off** M_{vd}/M_{\odot} of the linear total (dark matter plus baryon) mass $M/M_{\odot} \approx \nu L_{\text{UV}}/L_{\odot}$, the corresponding cut-off AB-magnitude M_{UV} , and the reionization optical depth τ . The Planck collaboration obtains $\tau = 0.054 \pm 0.007$. Note that $k_{\text{fs}} \approx 2 \text{ Mpc}^{-1}$.

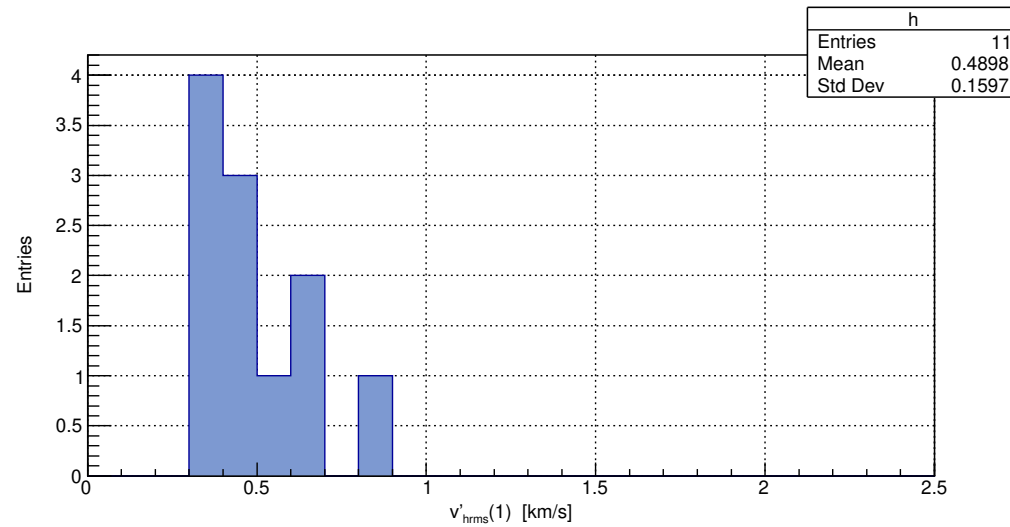
$k_{\text{fs}}(t_{\text{eq}})$	M_{vd}/M_{\odot}	M_{UV} cut-off	τ
1 Mpc^{-1}	2×10^{10}	-19.9	0.047 ± 0.006
2 Mpc^{-1}	1.5×10^9	-17.0	0.053 ± 0.006
4 Mpc^{-1}	1.5×10^8	-14.5	0.060 ± 0.008



Rotation curves of spiral galaxy F571-8 (in SPARC sample), compared to numerical calculation that obtains $\rho_h(r \rightarrow 0)$, $\langle v_{rh}^2 \rangle$, $\rho_b(r \rightarrow 0)$, and $\langle v_{rb}^2 \rangle$.



The expansion parameter at which dark matter becomes non-relativistic (uncorrected for dark matter rotation and relaxation) $a'_{hNR} \equiv v'_{hrms}(1)/c$, as a function of the absolute luminosity, of 11 LITTLE THINGS dwarf galaxies, and 46 spiral galaxies in the SPARC sample.



Distribution of the adiabatic invariant $v_{hrms}(1)$, uncorrected for rotation and relaxation, of 11 dwarf galaxies outside of the Milky Way. Peak corresponds to

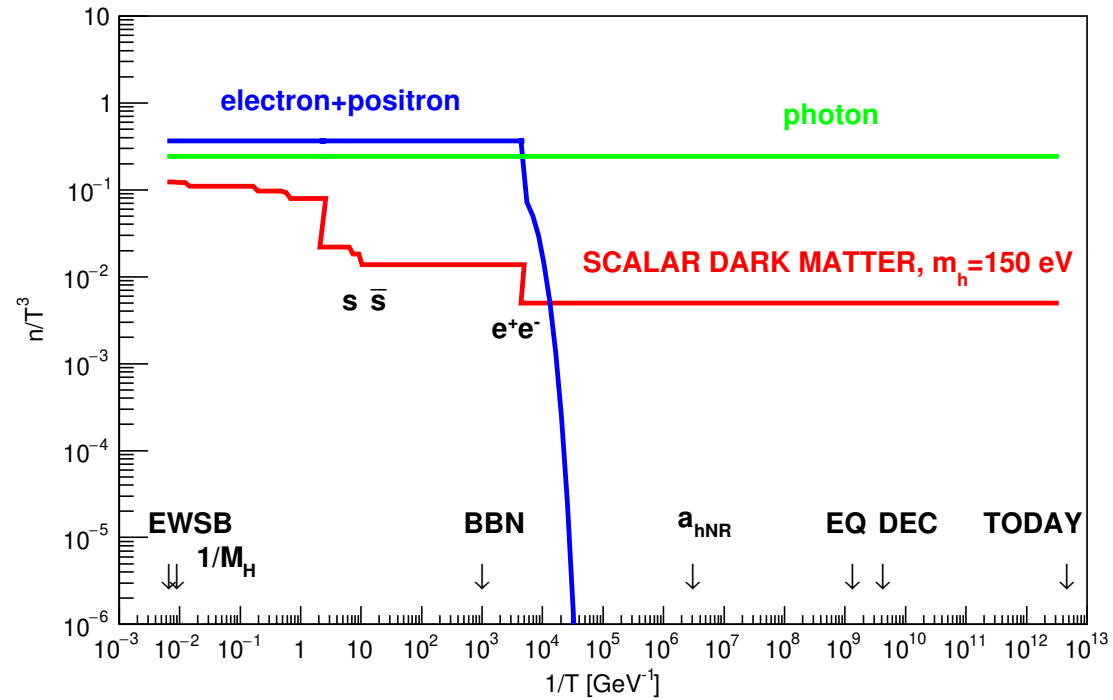
$$k_{fS} \approx 2 \text{ Mpc}^{-1}.$$

Measurements of the adiabatic invariant $v_{hrms}(1)$ with 56 spiral galaxy rotation curves, the comoving free-streaming cut-off wavenumber $k_{fs}(t_{eq})$ with galaxy stellar mass distributions at $z = 4.5, 6, 7$ and 8 , and galaxy UV luminosity distributions at $z = 4, 6, 8$ and 10 , reionization, first galaxies, M_{vd} , 11 dwarf galaxies, and predictions from the **no freeze-in and no freeze-out** scenario.

$a'_{hNR} \equiv v_{hrms}(1)/c$. After e^+e^- annihilation $0.424 \geq T_h/T \geq \mathbf{0.344}$, or $T_C < T_{dec} < \mathbf{m_t}$.

Observable	$v_{hrms}(1)$ [km/s]	$10^6 a'_{hNR}$	$k_{fs}(t_{eq})$ [Mpc $^{-1}$]	m_h [eV]
Spiral galaxies	0.79 ± 0.33	2.64 ± 1.10	$1.03^{+0.74}_{-0.30}$	
M_* distribution	$0.91^{+0.72}_{-0.30}$	$3.02^{+2.42}_{-0.99}$	$0.90^{+0.44}_{-0.40}$	
First galaxies	≈ 0.4 to 0.2	≈ 1.4 to 0.7	≈ 2 to 4	
M_* and L_{UV}	$0.41^{+0.14}_{-0.12}$	$1.36^{+0.45}_{-0.39}$	$2.0^{+0.8}_{-0.5}$	
Reionization	≈ 1.2 to 0.2	≈ 3.9 to 0.5	≈ 0.7 to 5.4	
Vel. disp. cut-off	< 0.54	< 1.8	> 1.5	
Dwarf galaxies	0.41 ± 0.07	1.35 ± 0.23	$2.01^{+0.41}_{-0.29}$	
Fermions spin 1/2 **				
No freeze-in/-out	1.93 to 0.83	6.43 to 2.78	0.42 to 0.98	54 to 101
Bosons				
No fr-in/-out spin 0	1.12 to 0.48	3.73 to 1.61	0.73 to 1.69	81 to 152
No fr-in/-out spin 1 *	2.24 to 0.97	7.46 to 3.22	0.36 to 0.84	40 to 76

No freeze-in and no freeze-out



The **no freeze-in and no freeze-out** warm dark matter scenario is illustrated with an example. T is the photon temperature, and the n 's are particle number densities.

For full details of this short talk, and for the **sources of all data** shown, see

- Hoeneisen, B. (2019) A Study of Dark Matter with Spiral Galaxy Rotation Curves. *International Journal of Astronomy and Astrophysics*, **9**, 71-96.
- Hoeneisen, B. (2019) The adiabatic invariant of dark matter in spiral galaxies. *International Journal of Astronomy and Astrophysics*, **9**, 355-367.
- Hoeneisen, B. (2022) Comments on Warm Dark Matter Measurements and Limits *International Journal of Astronomy and Astrophysics*, **12**, 94-109.
- +9
- Hoeneisen, B. (2022) Measurement of the Dark Matter Velocity Dispersion with Galaxy Stellar Masses, UV Luminosities, and Reionization *International Journal of Astronomy and Astrophysics*, **12**, 258-272.

and references therein.

Conclusions

- We have **independently** and redundantly obtained each of three observables (the adiabatic invariant $v_{hrms}(1)$, the free-streaming cut-off wavenumber $k_{fs}(t_{eq})$, and the velocity dispersion cut-off mass M_{vd}), from **DATA**. The data are spiral galaxy rotation curves, first galaxies, the distributions of galaxy stellar masses M_* and rest frame UV luminosities L_{UV} , reionization and dwarf galaxies. These measured observables turn out to be consistent with each other. They determine the temperature-to-mass ratio of dark matter, not separately temperature $T_h(a)$ or mass m_h .
- This measured temperature-to-mass ratio happens to be consistent with the **no freeze-in and no freeze-out** scenario for spin

0 warm dark matter that decouples early on from the standard model sector.

- One example is scalar dark matter S , that couples to the Higgs boson ϕ , and has a mass $m_h = 150 \pm 2$ eV.

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \frac{1}{2} \partial_\mu S \cdot \partial^\mu S - \frac{1}{2} \bar{m}_S^2 S^2 - \frac{\lambda_S}{4!} S^4 - \frac{1}{2} \lambda_{hS} (\phi^\dagger \phi) S^2.$$

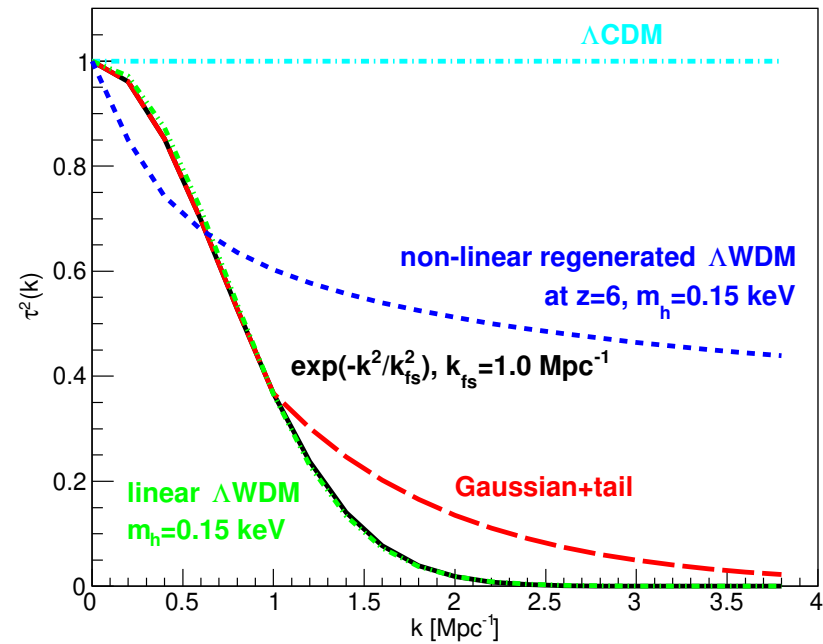
- According to “The Review of Particle Physics” (2022), limits on dark matter particle mass are $m_h > 70$ eV for fermions, and $m_h > 10^{-22}$ eV for bosons. May I suggest that **limits** on the “thermal relic mass” of order keV that can be found in the literature, which are in disagreement with the **measurements** presented above, be revised with the inclusion of the **non-linear regeneration of small scale structure**, and the **velocity dispersion cut-off**.

Questions?

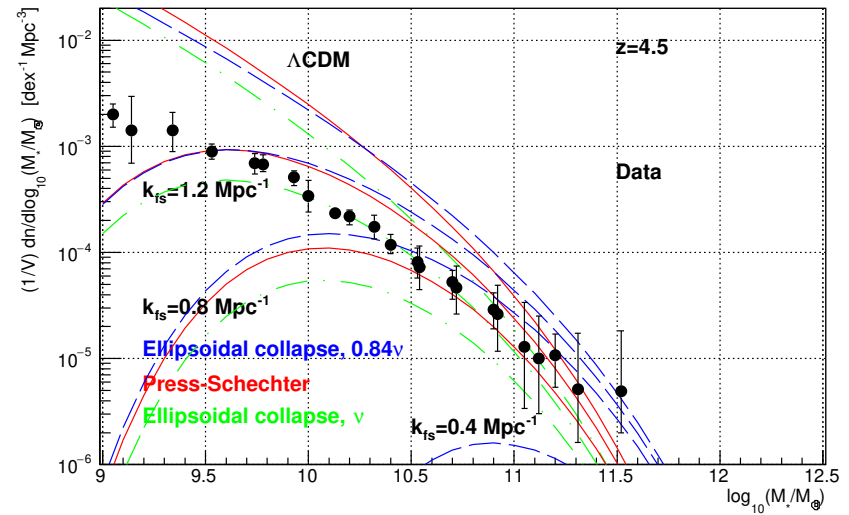
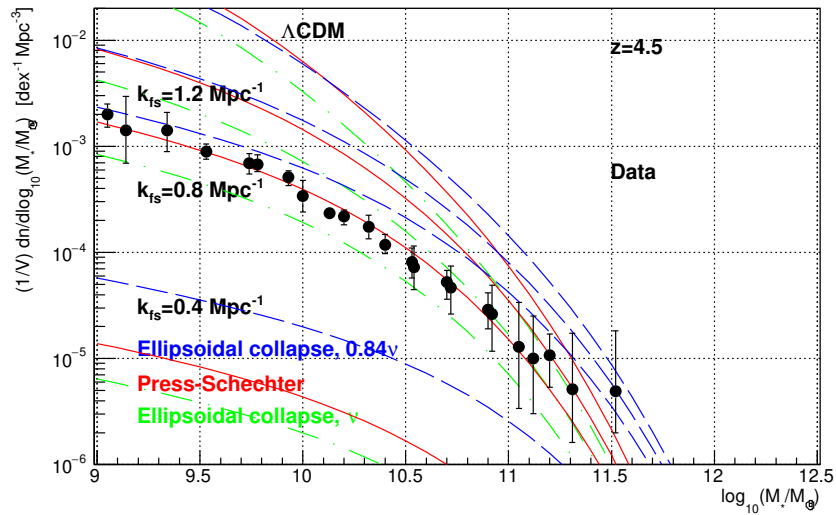
Summary of measurements and predictions. After e^+e^- annihilation, while dark matter is ultra-relativistic, $0.424 \geq T_h/T \geq \mathbf{0.344}$, corresponding to decoupling at $T_C < T_{\text{dec}} < \mathbf{m}_t$.

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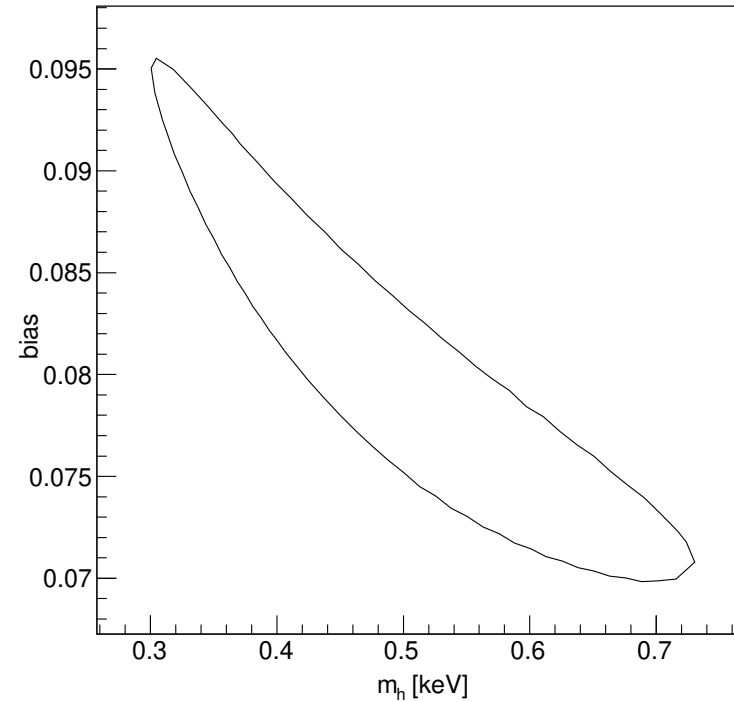
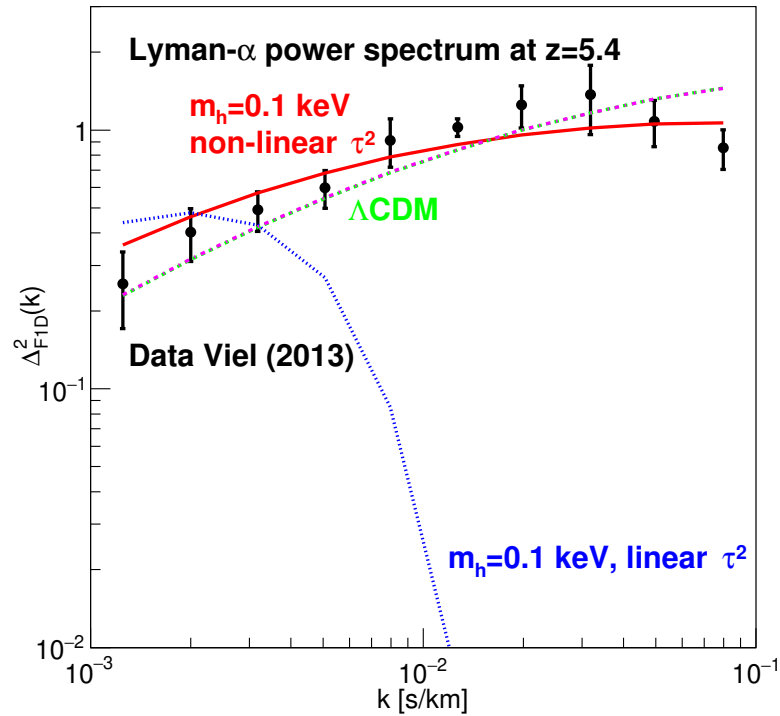
Backup Slides



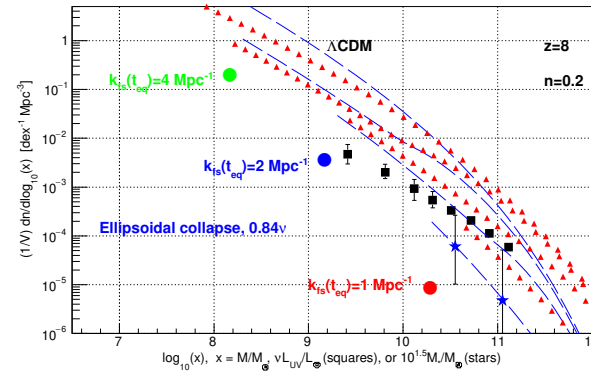
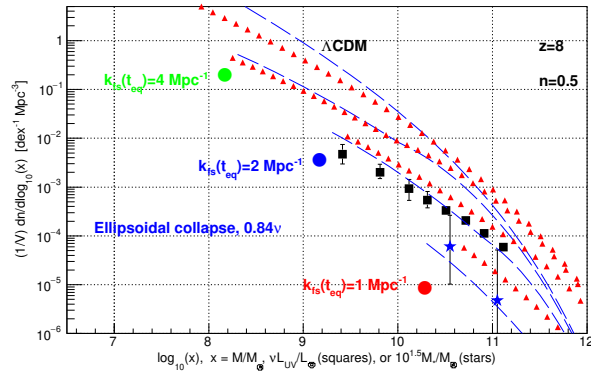
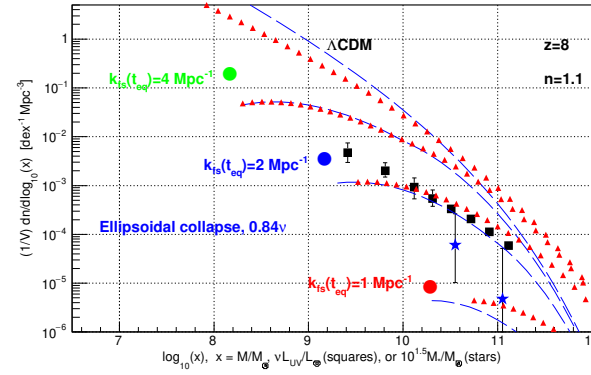
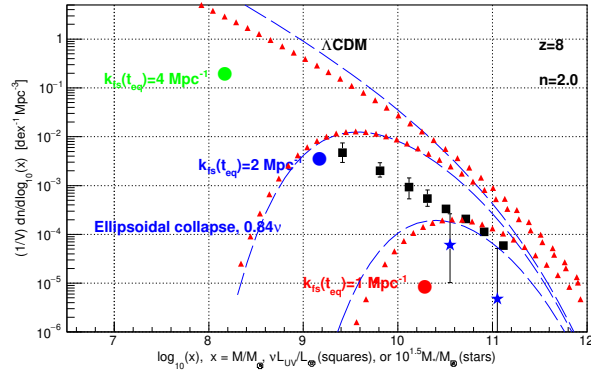
Power spectrum free-streaming cut-off factor $\tau^2(k)$ without, and with, non-linear regeneration of small scale structure.



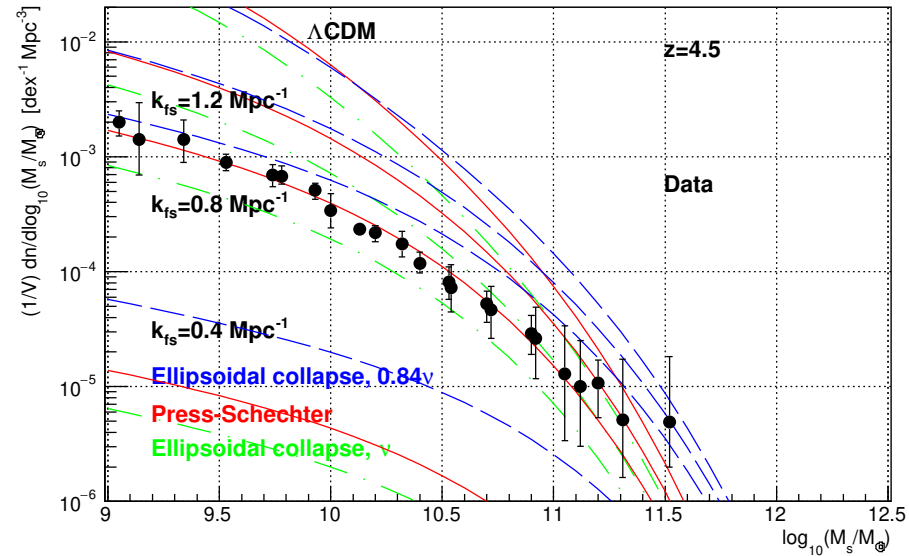
Comparison of data with the Press-Schechter predictions for Gaussian and sharp- k window functions assuming no non-linear regeneration of small scale structure.



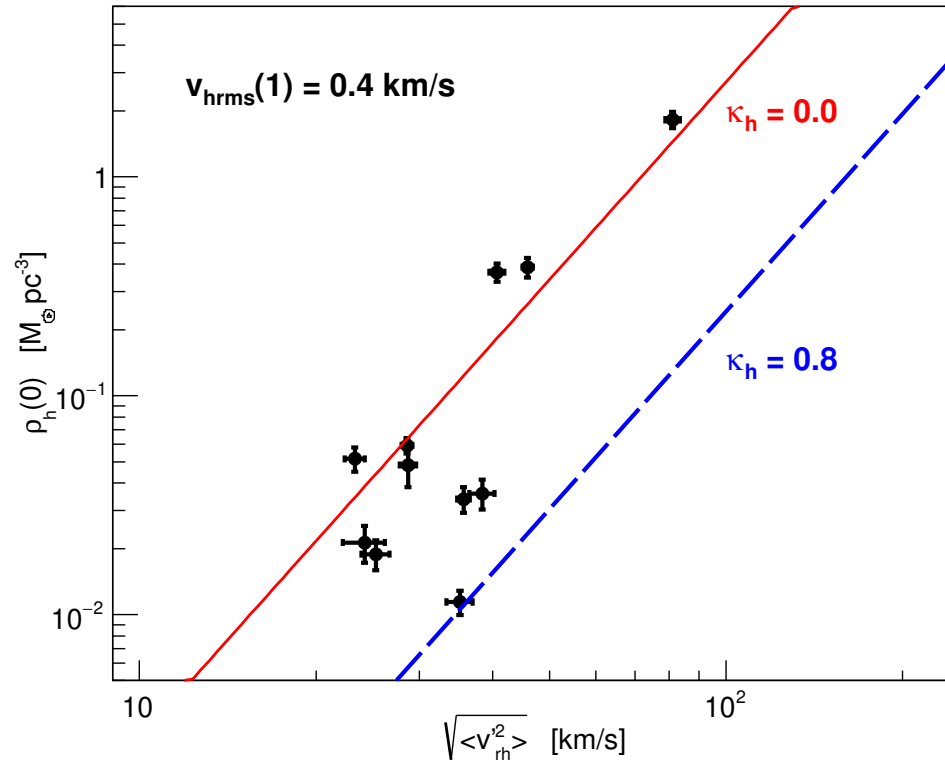
Measured Lyman- α 1D power spectrum at $z = 5.4$, compared with predictions of Λ CDM, and Λ WDM with the free-streaming cut-off factor $\tau(k)$ without, and with, a non-linear re-generated “tail” .



$\tau^2(k) = \exp(-k^2/k_{fs}^2(t_{eq}))$ if $k < k_{fs}(t_{eq})$, else $= \exp(-k^n/k_{fs}^n(t_{eq}))$ with $n = 2.0, 1.1, 0.5, \text{ or } 0.2$. The window function is sharp- k . $n = 2$ corresponds to no non-linear regenerated tail.



Calculated stellar mass functions with the Press-Schechter, Ellipsoidal Collapse with $\tilde{\nu} = \nu$, and Ellipsoidal Collapse with $\tilde{\nu} = 0.84\nu$ approximations, for Λ CDM, and Λ WDM with $k_{fs} = 1.2, 0.8$ and 0.4 Mpc^{-1} , at redshift $z = 4.5$, compared with observations.



Shown are $\sqrt{\langle v'^2_{rh} \rangle}$ vs. $\rho_h(0)$, of 11 LITTLE THINGS galaxies, with statistical uncertainties only. Dark matter halo rotation and relaxation increase $v'_{hrms}(1)$.