



New Physics from B Decays

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What is experiment telling us?

No **direct evidence** for NP, yet many reasons to expect it [**presence of a mass gap?**]

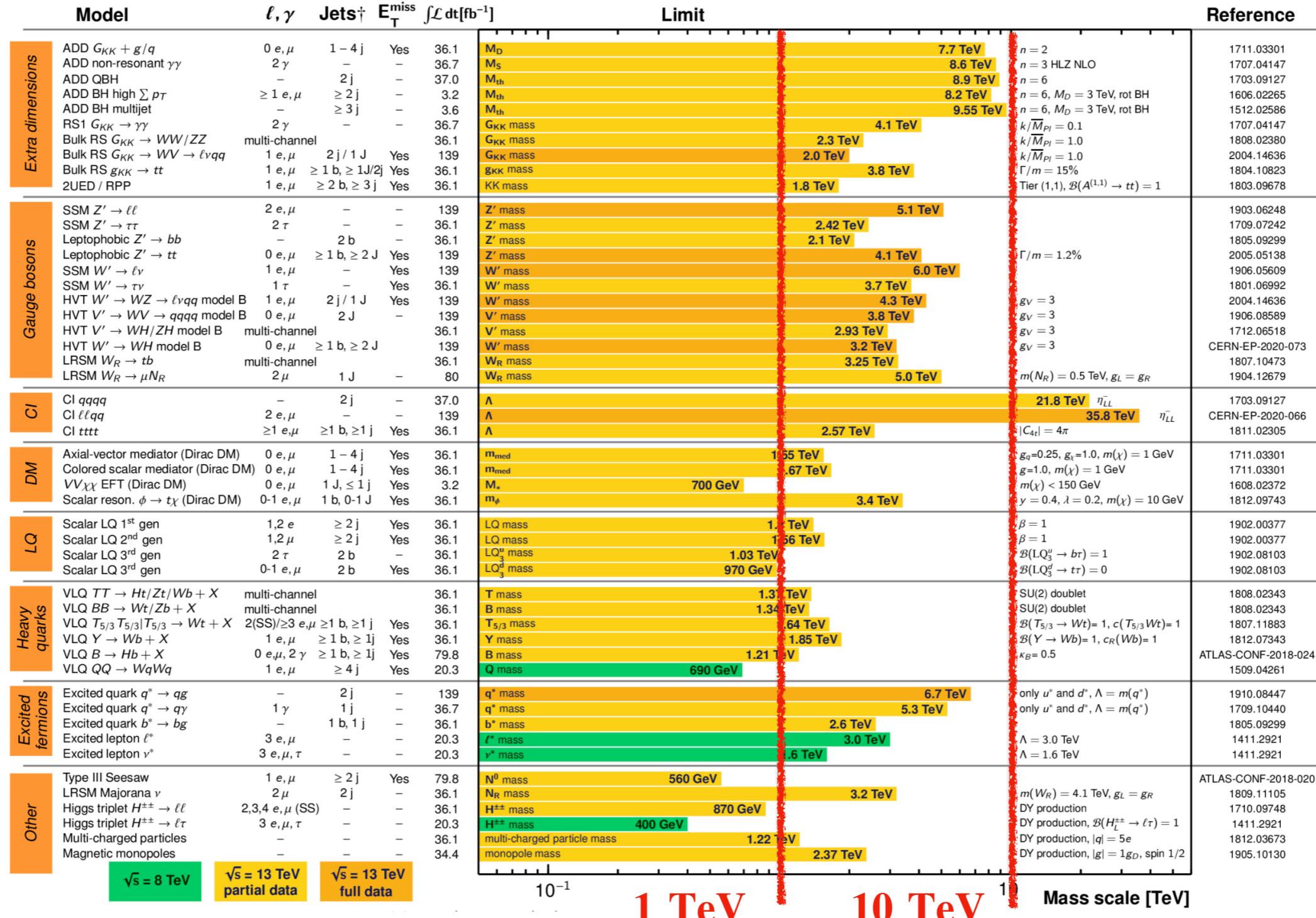
ATLAS Exotics Searches* - 95% CL Upper Exclusion Limits

Status: May 2020

ATLAS Preliminary

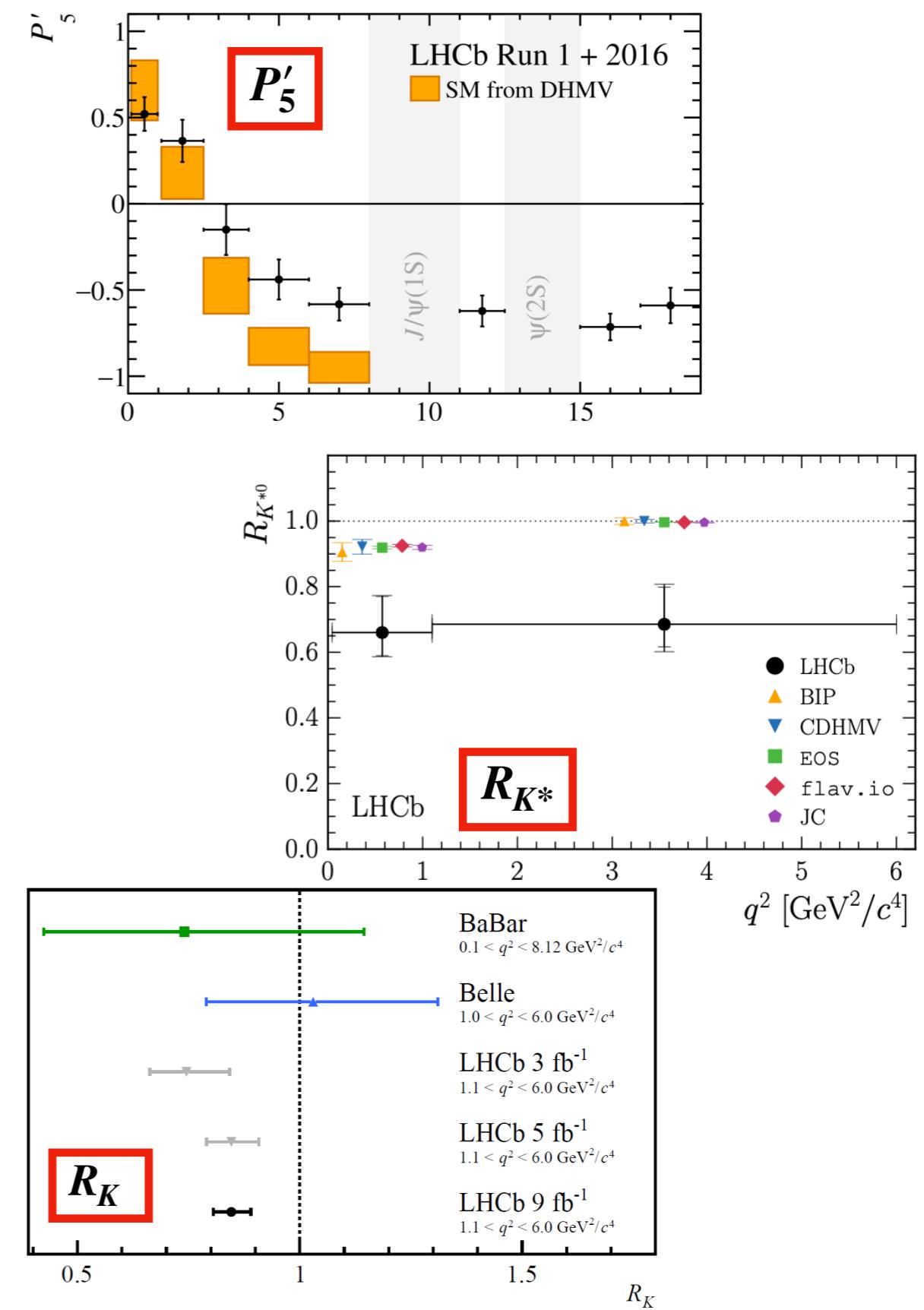
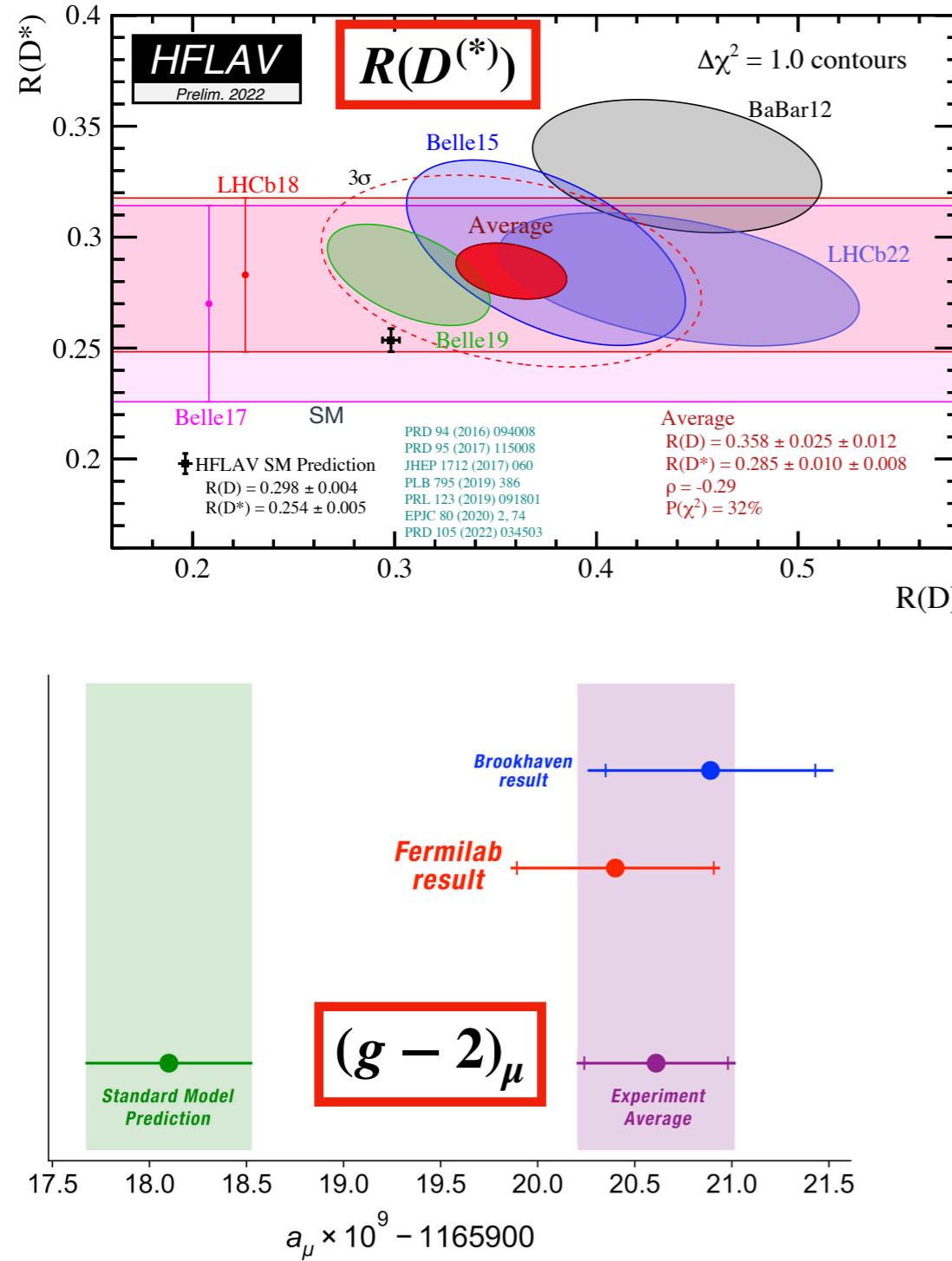
$$\int \mathcal{L} dt = (3.2 - 139) \text{ fb}^{-1}$$

$$\sqrt{s} = 8, 13 \text{ TeV}$$



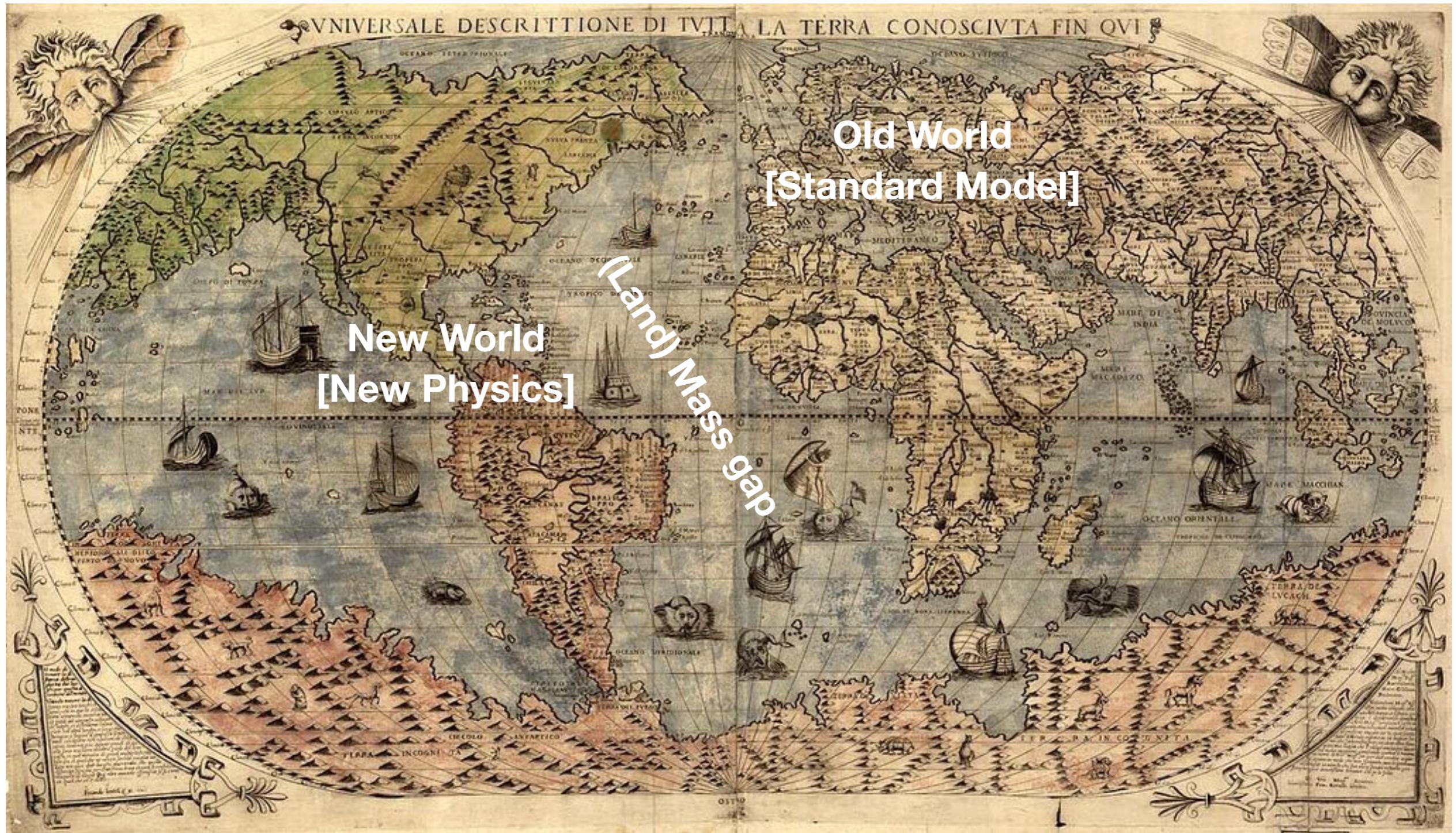
What is experiment telling us?

Footprints of NP in low-energy data?



The search for Terra Incognita

Particle Physics has entered an age of exploration



The SM Lagrangian: Naturalness problems

$$\mathcal{L} = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu}$$

$$+ i \bar{\psi} \gamma^\mu \psi$$

$$+ D_\mu \phi |^2 - V(\phi)$$

$$+ \bar{\psi}_i y_{ij} \psi_j \phi + h.c.$$

The SM Lagrangian contain a few unnatural features pointing towards NP

Higgs hierarchy problem

[Instability of the Higgs mass under quantum corrections]

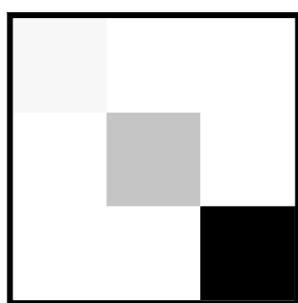
TeV-scale NP?

SM flavor puzzle

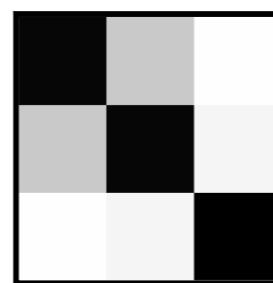
[Very hierarchical structure in the Yukawa couplings]

Similar structure also for NP?

$$M_{u,d,e} \sim$$



$$V_{CKM} \sim$$



Are these two features correlated?

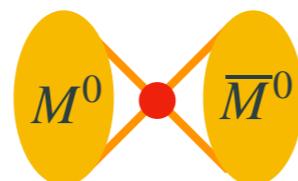
Multi-scale solution of the flavor puzzle/problem

$$\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{Gauge}} + \mathcal{L}_{\text{Higgs}} + \mathcal{L}_{\text{Yukawa}} + \sum_{i,d} \frac{1}{\Lambda_i^{d-4}} C_i \mathcal{O}_i^d$$

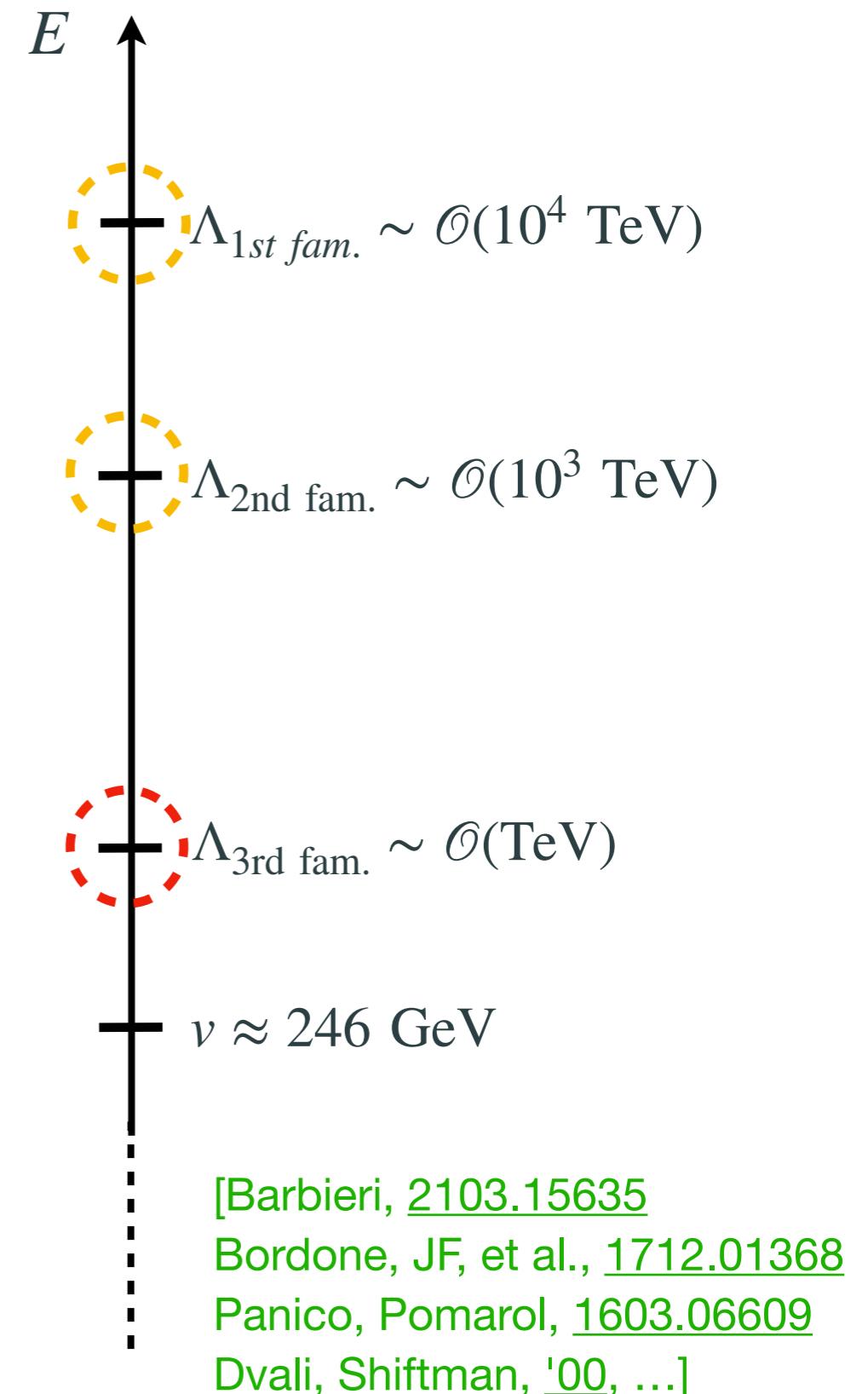
Non-trivial UV imprints

- ★ The SM Yukawas are very different because they originate at very separate scales!
- ★ TeV-scale NP dominantly coupled to third and (to a lesser extent) second families
[protection from flavor constraints]

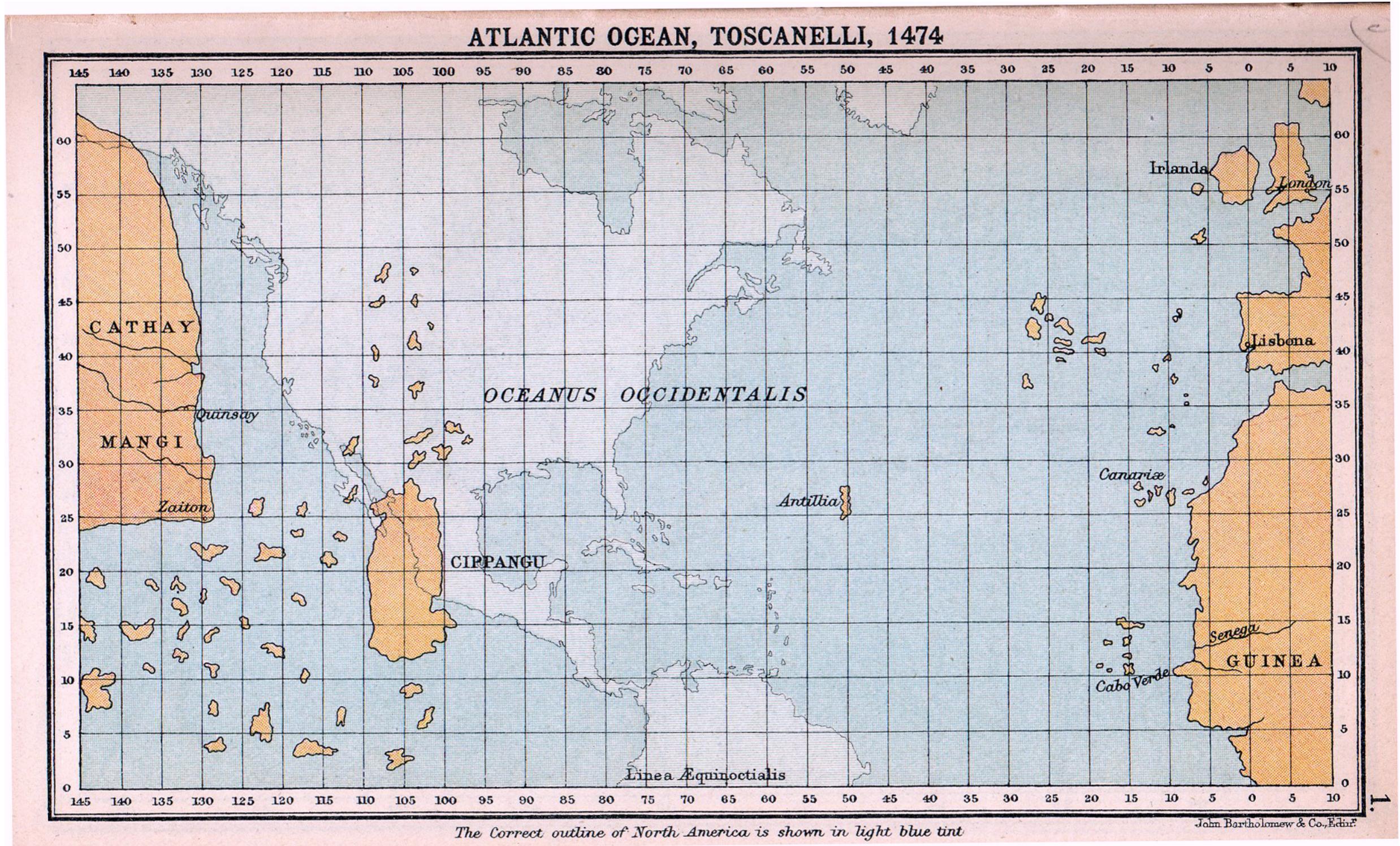
e.g. from $\frac{1}{\Lambda^2} (\psi_i \psi_j)^2$



- ★ Direct production of new states at the LHC is naturally more suppressed
[NP scale can be lower]



A closer look to the data and EFT analysis

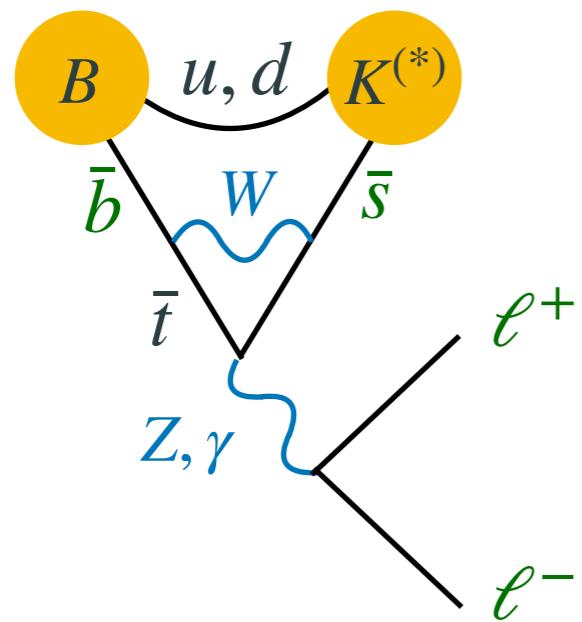


The B anomalies

Hints of Lepton Flavour Universality Violation (**LFUV**) in semileptonic B decays

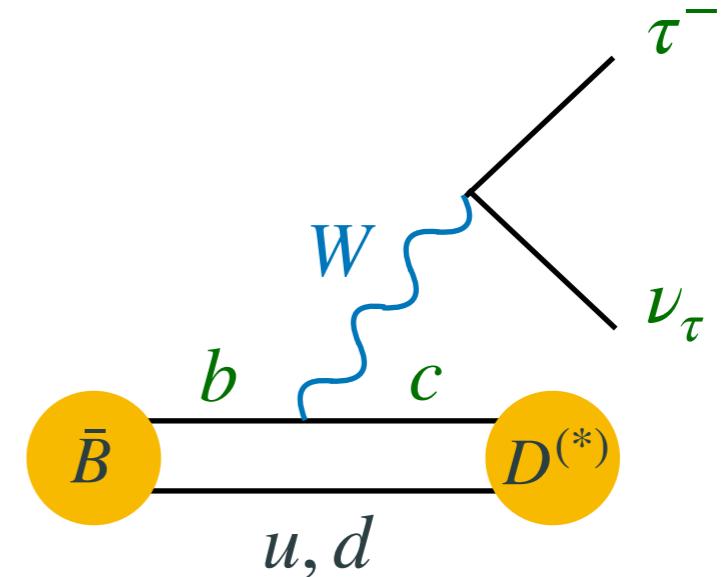
$$b \rightarrow s \ell^+ \ell^-$$

μ/e universality



$$b \rightarrow c \tau \nu$$

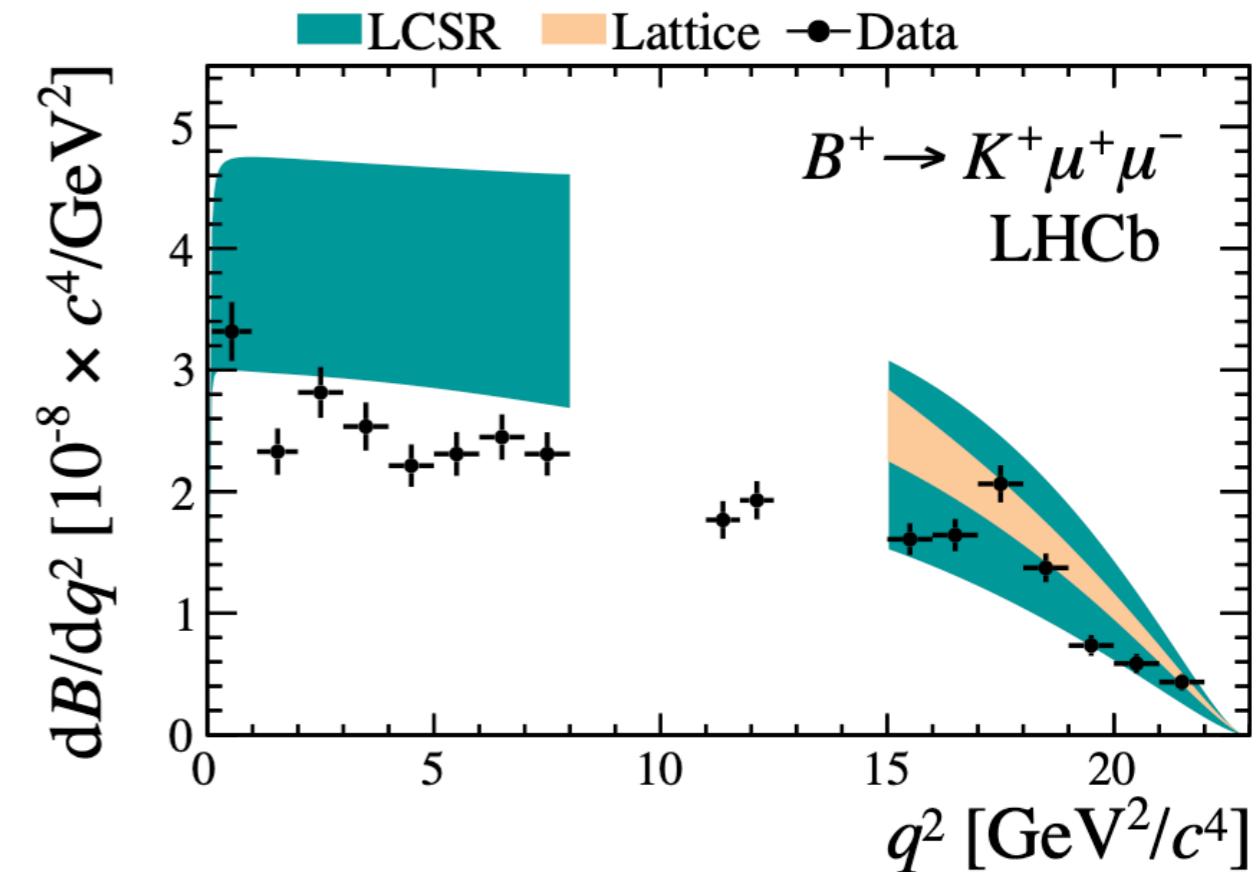
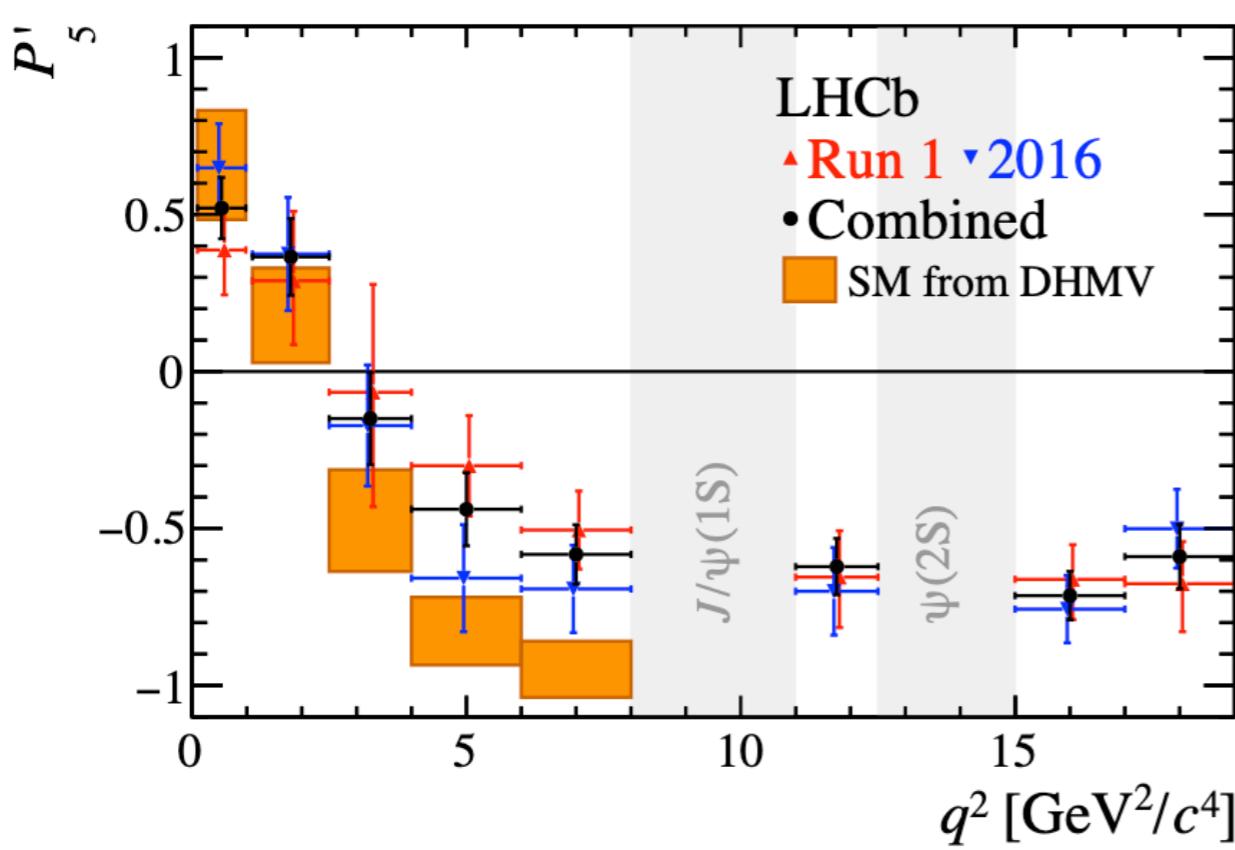
$\tau/\mu, e$ universality



The $b \rightarrow s\mu^+\mu^-$ anomalies

Several LHCb measurements deviate from SM predictions* by $2-3\sigma$:

- ▶ Angular observables in $B \rightarrow K^*\mu^+\mu^-$ [LHCb, [2003.04831](#), [2012.13241](#)]
- ▶ Branching ratios $B \rightarrow K^{(*)}\mu^+\mu^-$ and $B_s \rightarrow \phi\mu^+\mu^-$ [LHCb, [1403.8044](#), [1506.08777](#), [2105.14007](#)]



*: based on hadronic assumptions on which there is no theory consensus

The $b \rightarrow s\ell^+\ell^-$ anomalies

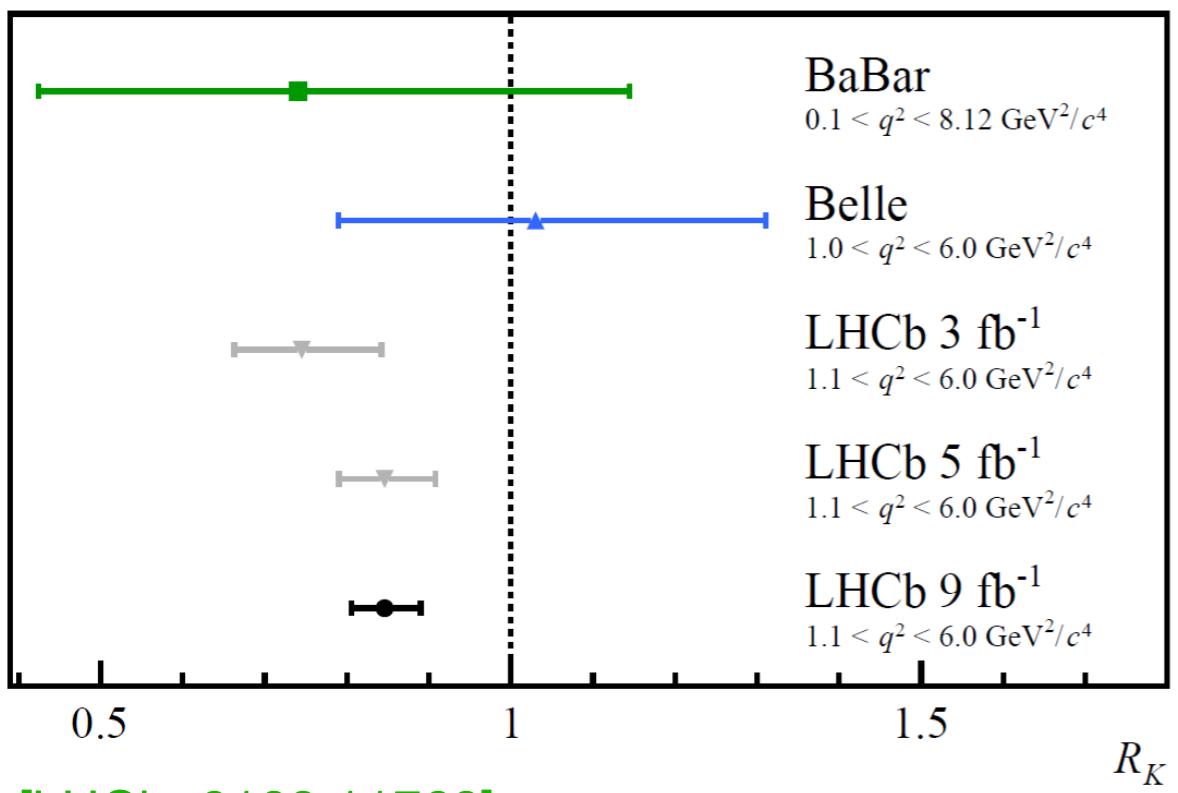
Lepton flavor universality ratios also show deviations from SM prediction

[Theoretically “very clean”: 1 % theory error (QED and lepton mass effects)]

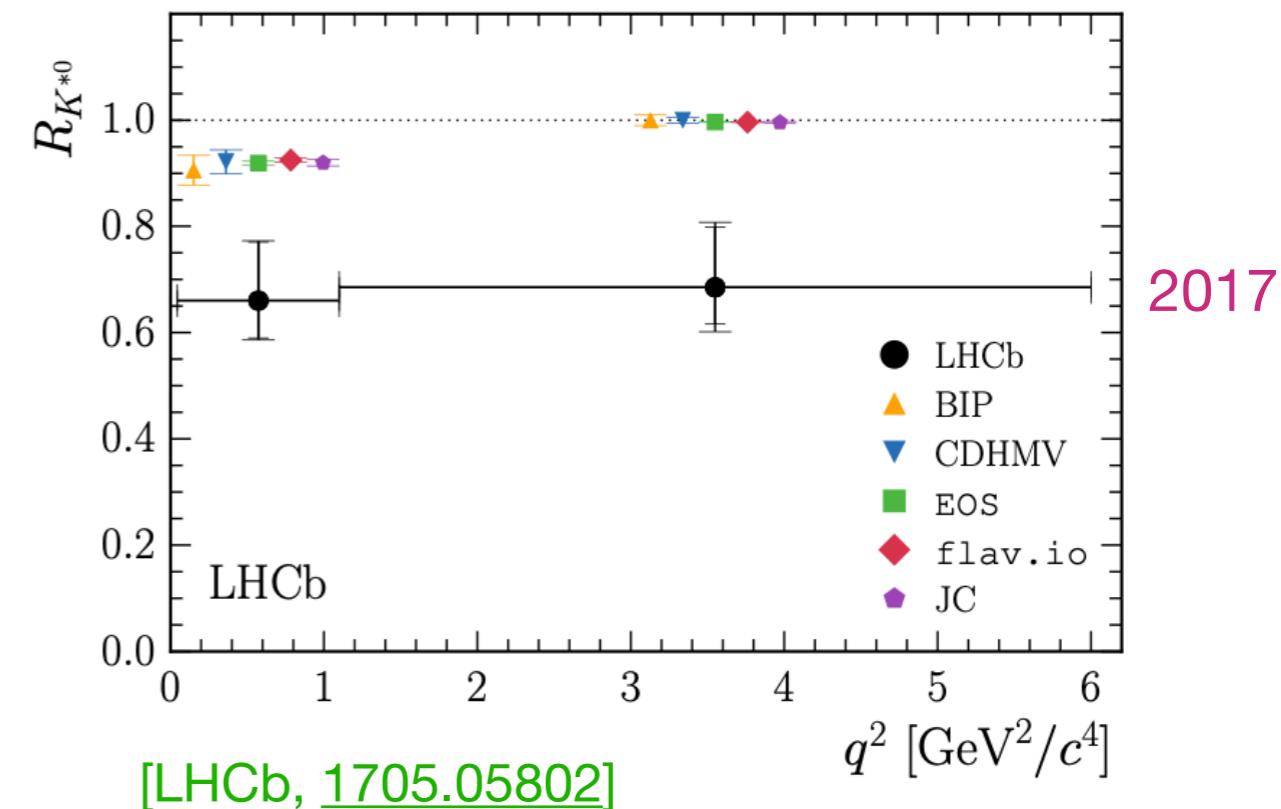
$$R_{K^{(*)}}^{[q_{\min}^2, q_{\max}^2]} \equiv \frac{\int_{q_{\min}^2}^{q_{\max}^2} d\Gamma(B \rightarrow K^{(*)}\mu^+\mu^-)}{\int_{q_{\min}^2}^{q_{\max}^2} d\Gamma(B \rightarrow K^{(*)}e^+e^-)}$$

$$R_{K^{(*)}}^{[1.1, 6] \text{ GeV}^2} = 1.00 \pm 0.01$$

[Isidori, Bordone, Pattori, [1605.07633](#)]



2014
2019
2021



Deviations in other LFUV ratios (R_{pK} , $R_{K^{*+}}$, R_{K^0}) (with larger errors)

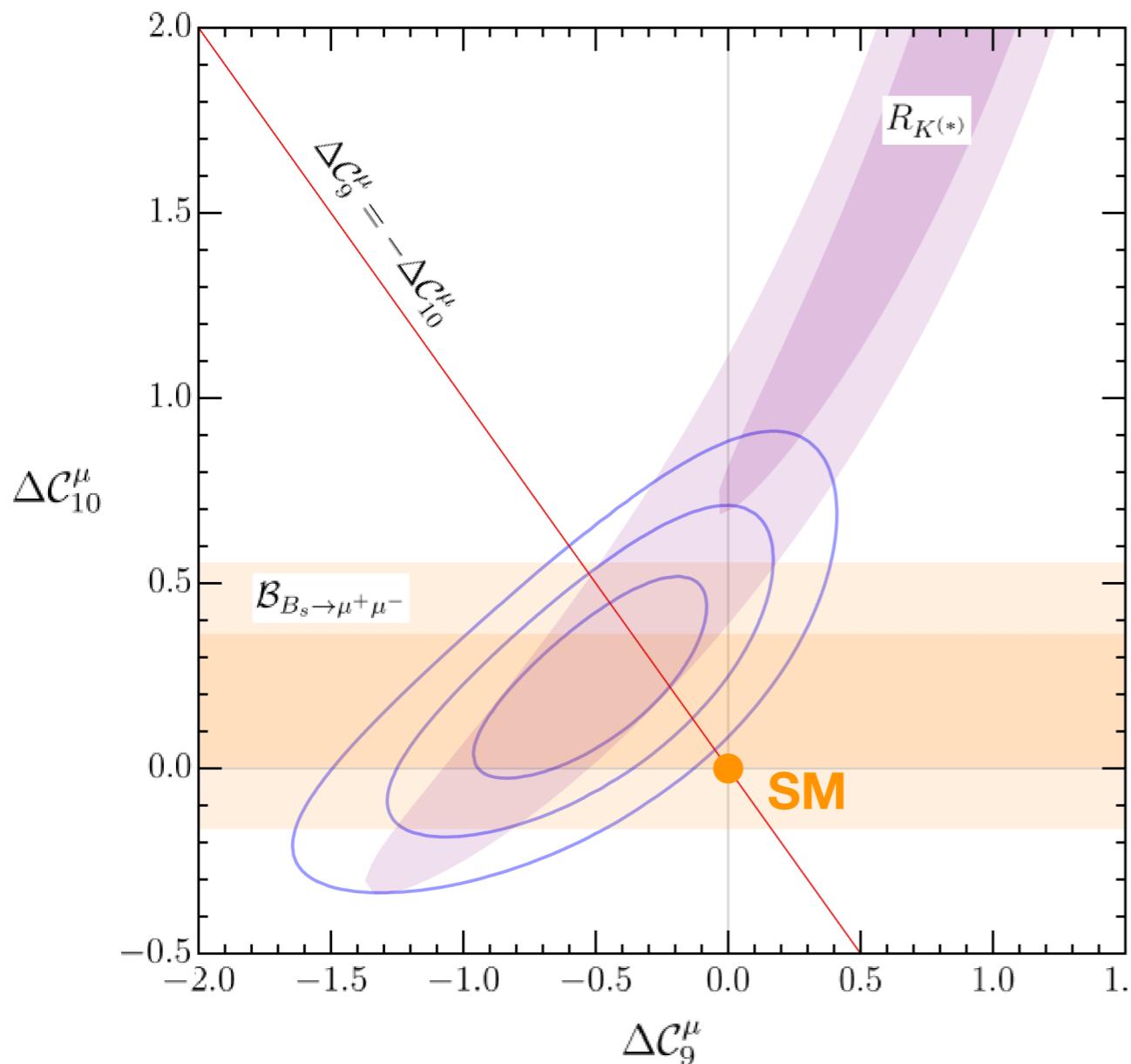
[LHCb, [2110.09501](#), [1912.08139](#)]

The $b \rightarrow s\ell^+\ell^-$ anomalies

^{*}: with new $\mathcal{B}_{B_s \rightarrow \mu^+\mu^-}$ from [CMS PAS BPH-21-006]

Conservative fit using “th clean observables” only *

$$[\Delta C_i^\mu = C_i^\mu - C_i^e]$$



[Update from Cornella, JF et al., [2103.16558](#)]

$$\mathcal{L}_{\text{eff}} = -\frac{4G_F}{\sqrt{2}} V_{ts}^* V_{tb} \frac{\alpha}{4\pi} \sum_i C_i \mathcal{O}_i$$

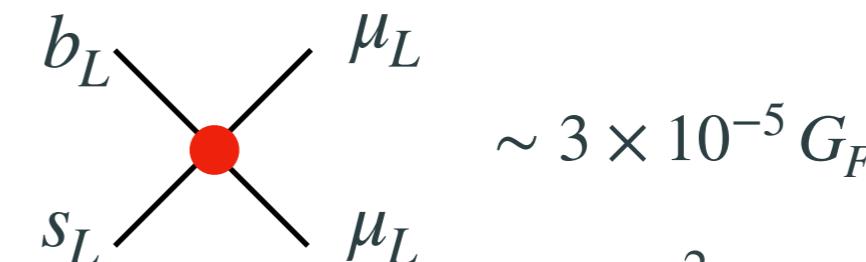
$$\mathcal{O}_9^\mu = (\bar{s}_L \gamma_\mu b_L)(\bar{\mu} \gamma^\mu \mu) \quad C_9^{\text{SM}} \approx 4.1$$

$$\mathcal{O}_{10}^\mu = (\bar{s}_L \gamma_\mu b_L)(\bar{\mu} \gamma^\mu \gamma_5 \mu) \quad C_{10}^{\text{SM}} \approx -4.2$$

Left-handed new physics [$\Delta C_9^\mu = -\Delta C_{10}^\mu$]
preferred over the SM by 3.9σ

[Consistent with $b \rightarrow s\mu^+\mu^-$ deviations
...considerably increasing NP significancy]

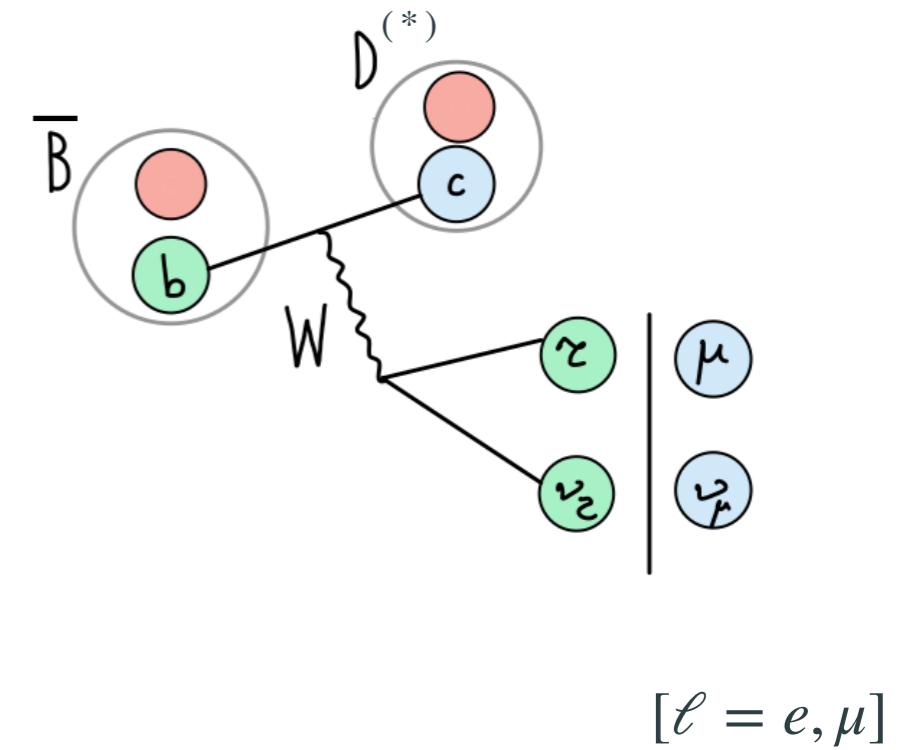
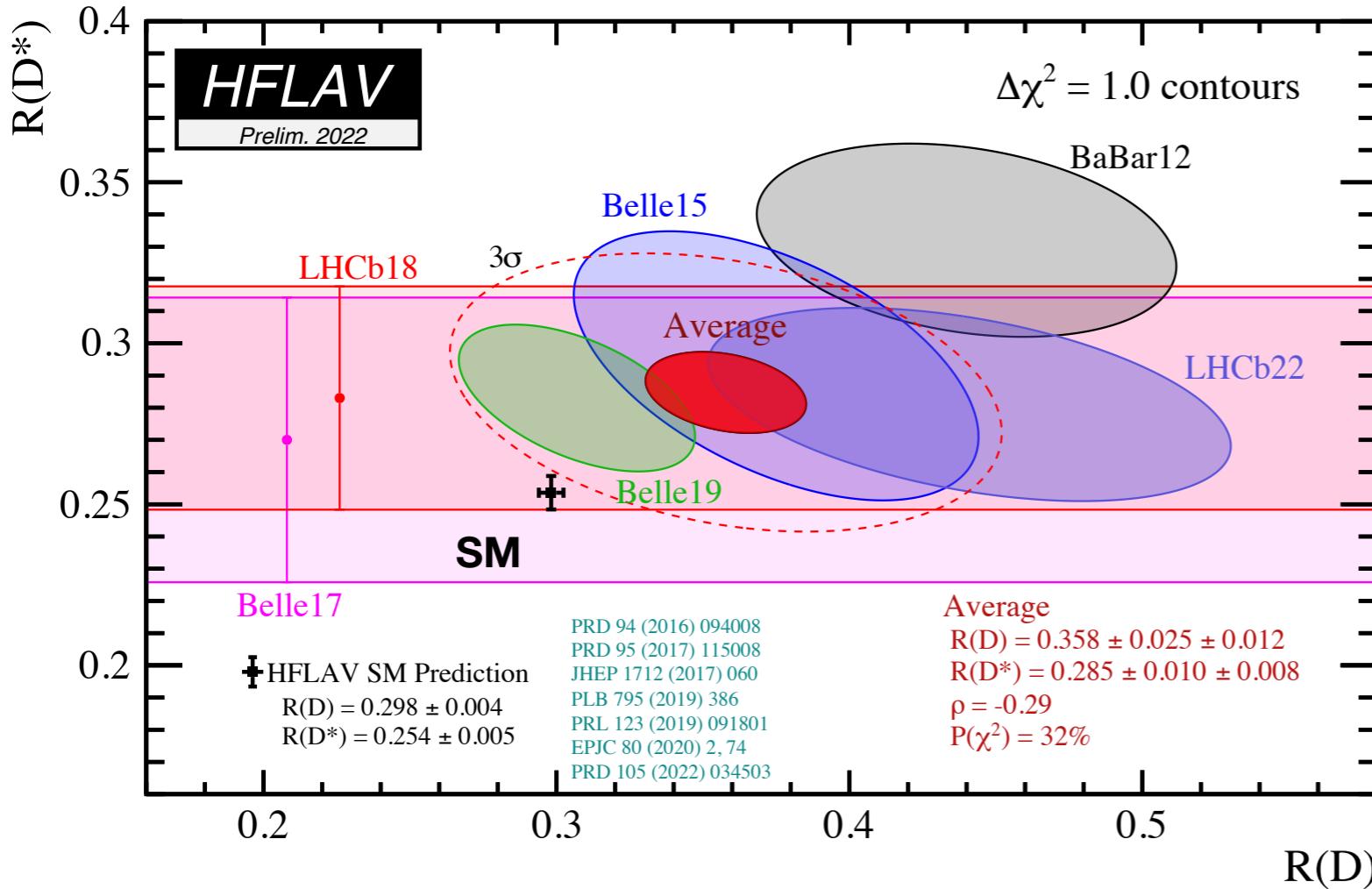
[See e.g. Algueró et al., [1903.09578](#)]



$$\sim 3 \times 10^{-5} G_F$$

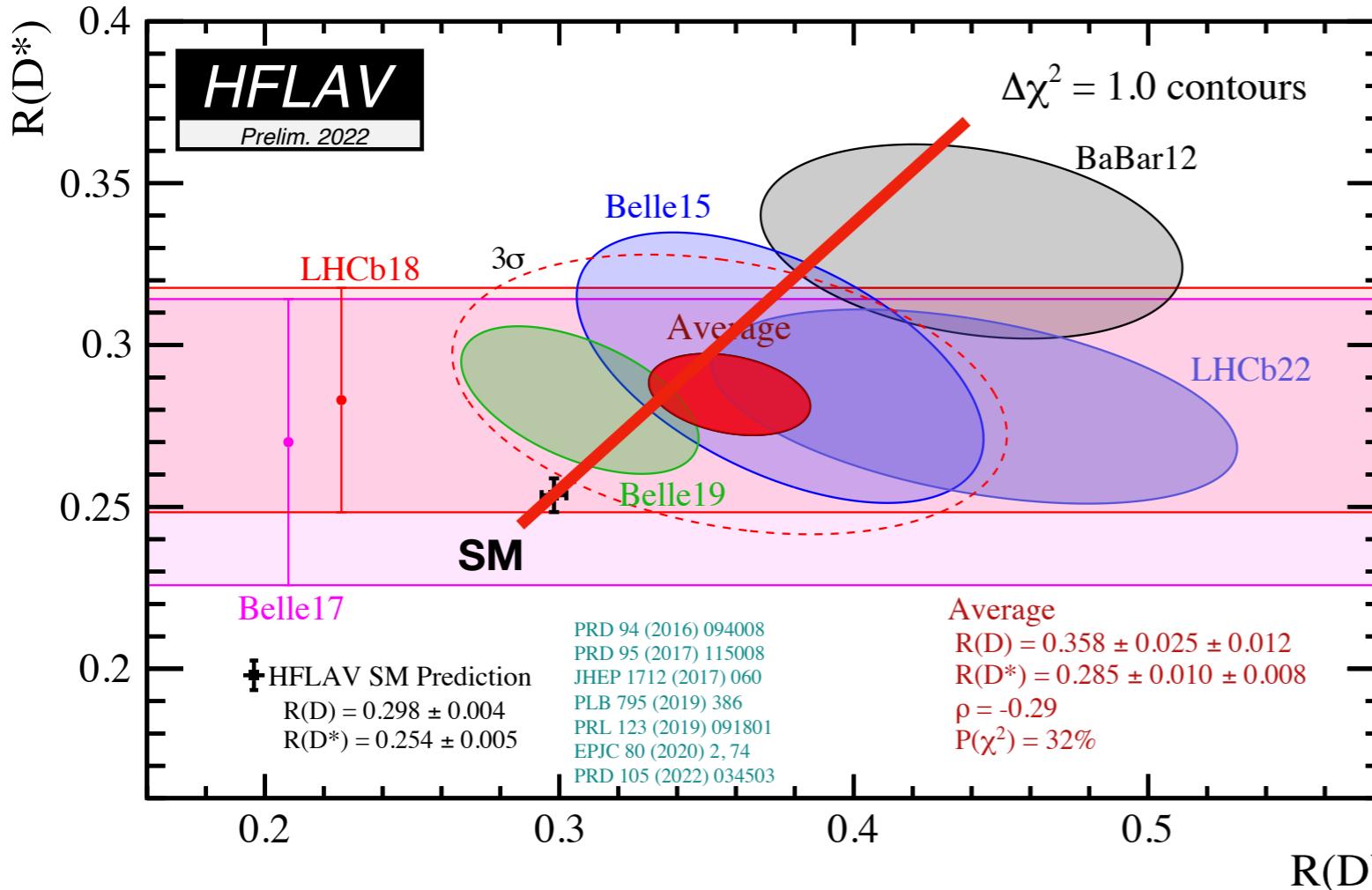
$$\implies \frac{g_{\text{NP}}^2}{M_{\text{NP}}^2} \sim \frac{1}{(40 \text{ TeV})^2}$$

The $b \rightarrow c\tau\bar{\nu}$ anomalies



- $\sim 15\%$ enhancement due to excess in tau mode
- **Theoretically clean:** QCD uncertainties cancel (to a large extent) in the ratios
- Measurements by Babar, Belle, LHCb in reasonable agreement
- 3.2σ tension (R_D and R_{D^*} combined)

The $b \rightarrow c\tau\bar{\nu}$ anomalies



Preference for left-handed new physics
[analogous to the SM]

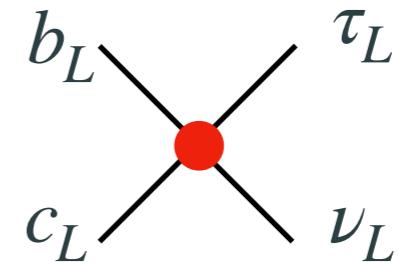
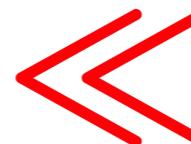
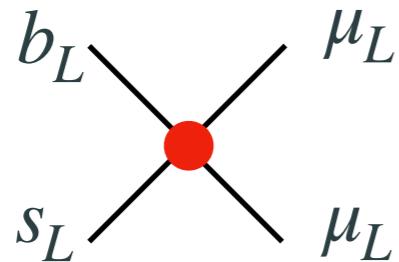
$$b_L \quad \tau_L \\ c_L \quad \nu_L \\ \Rightarrow \frac{g_{NP}^2}{M_{NP}^2} \sim \frac{1}{(3 \text{ TeV})^2} \sim 10^{-2} G_F$$

... with room for other NP structures

- ▶ $\sim 15\%$ enhancement due to excess in tau mode
- ▶ **Theoretically clean:** QCD uncertainties cancel (to a large extent) in the ratios
- ▶ Measurements by Babar, Belle, LHCb in reasonable agreement
- ▶ **3.2σ** tension (R_D and R_{D^*} combined)
- ▶ Recent measurement of $R(\Lambda_c)$ [$\Lambda_b \rightarrow \Lambda_c \ell \nu$] reduces the tension slightly [LHCb, [2201.03497](#)]

Consistency with a multi-scale picture?

$$C_{LL}^{ij\alpha\beta} (\bar{q}_L^i \gamma^\mu q_L^\alpha)(\bar{l}_L^\beta \gamma_\mu l_L^j)$$



$$C_{LL}^{2322} \sim \frac{1}{(40 \text{ TeV})^2}$$

$$C_{LL}^{2333} \sim \frac{1}{(3 \text{ TeV})^2}$$

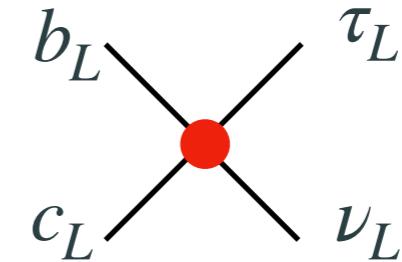
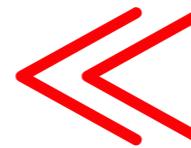
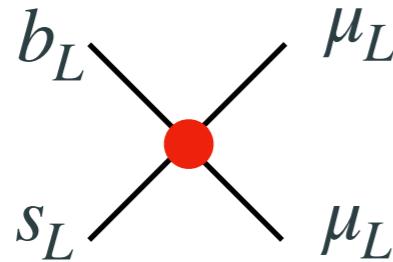
$$3_q \rightarrow 2_q 2_\ell 2_\ell$$

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The only source of **lepton flavor universality violation** in the SM (Yukawas) follows a very similar trend: $y_e \ll y_\mu \ll y_\tau$

Consistency with a multi-scale picture?

$$C_{LL}^{ij\alpha\beta} (\bar{q}_L^i \gamma^\mu q_L^\alpha)(\bar{l}_L^\beta \gamma_\mu l_L^j)$$



$$C_{LL}^{2322} \sim \frac{1}{(1 \text{ TeV})^2} |V_q| |V_\ell|^2$$

$$C_{LL}^{2333} \sim \frac{1}{(1 \text{ TeV})^2} |V_q|$$

$$3_q \rightarrow 2_q 2_\ell 2_\ell$$

$$3_q \rightarrow 2_q 3_\ell 3_\ell$$

The only source of **lepton flavor universality violation** in the SM (Yukawas) follows a very similar trend: $y_e \ll y_\mu \ll y_\tau$

Data consistent with **TeV-scale NP** with a Yukawa-like scaling with $|V_q|, |V_\ell| \sim 0.1$
[roughly the size inferred from the SM Yukawa $|V_q| \sim V_{cb} \approx 0.04$]

[JF, Isidori, Pagès, Yamamoto, [1909.02519](#)]

From EFT solutions to simplified BSM models



The main suspects

Leptoquarks (both scalars and vectors) have two important advantages:

1. $\Delta F = 2$ &
 $\tau \rightarrow \mu\nu\bar{\nu}$



2. Direct searches: t-channel versus resonant s-channel production

Model	$R_{K(*)}$	$R_{D(*)}$	$R_{K(*)} \& R_{D(*)}$
$S_1 = (3, 1)_{-1/3}$	✗	✓	✗
$R_2 = (3, 2)_{7/6}$	✗	✓	✗
$\tilde{R}_2 = (3, 2)_{1/6}$	✗	✗	✗
$S_3 = (3, 3)_{-1/3}$	✓	✗	✗
$U_1 = (3, 1)_{2/3}$	✓	✓	✓
$U_3 = (3, 3)_{2/3}$	✓	✗	✗

[Angelescu, Bećirević, Faroughy, Sumensary, [1808.08179](#)]

Three viable options in the market:

- ★ $U_1 + \text{UV completion}$

[di Luzio, Greljo, Nardecchia [1708.08450](#);
Calibbi, Crivellin, Li [1709.00692](#);
Bordone, Cornella, JF, Isidori [1712.01368](#);
Barbieri, Tesi, [1712.06844](#)...]

- ★ $S_1 + S_3$

[Crivellin, Muller, Ota [1703.09226](#);
Buttazzo et al. [1706.07808](#);
Marzocca [1803.10972](#),...]

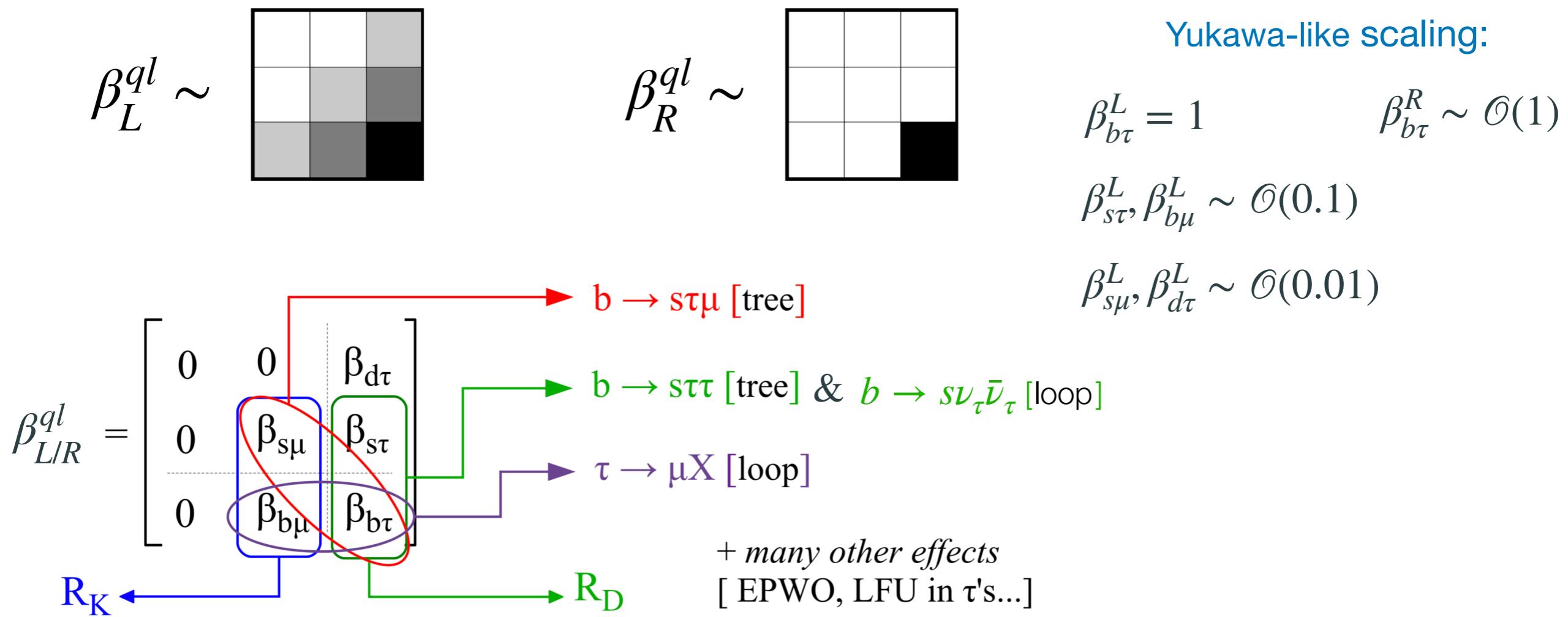
- ★ $S_3 + R_2$

[Bećirević et al., [1806.05689](#)]

The U_1 vector leptoquark

$$\mathcal{L} \supset \frac{g_U}{\sqrt{2}} U_1^\mu \left[\beta_L^{i\alpha} (\bar{q}_L^i \gamma_\mu \ell_L^\alpha) + \beta_R^{i\alpha} (\bar{d}_R^i \gamma_\mu e_R^\alpha) \right] + \text{h.c.} \quad U_1 \sim (3, 1, 2/3)$$

It provides a good description of **all low-energy data** with a “natural” flavor structure

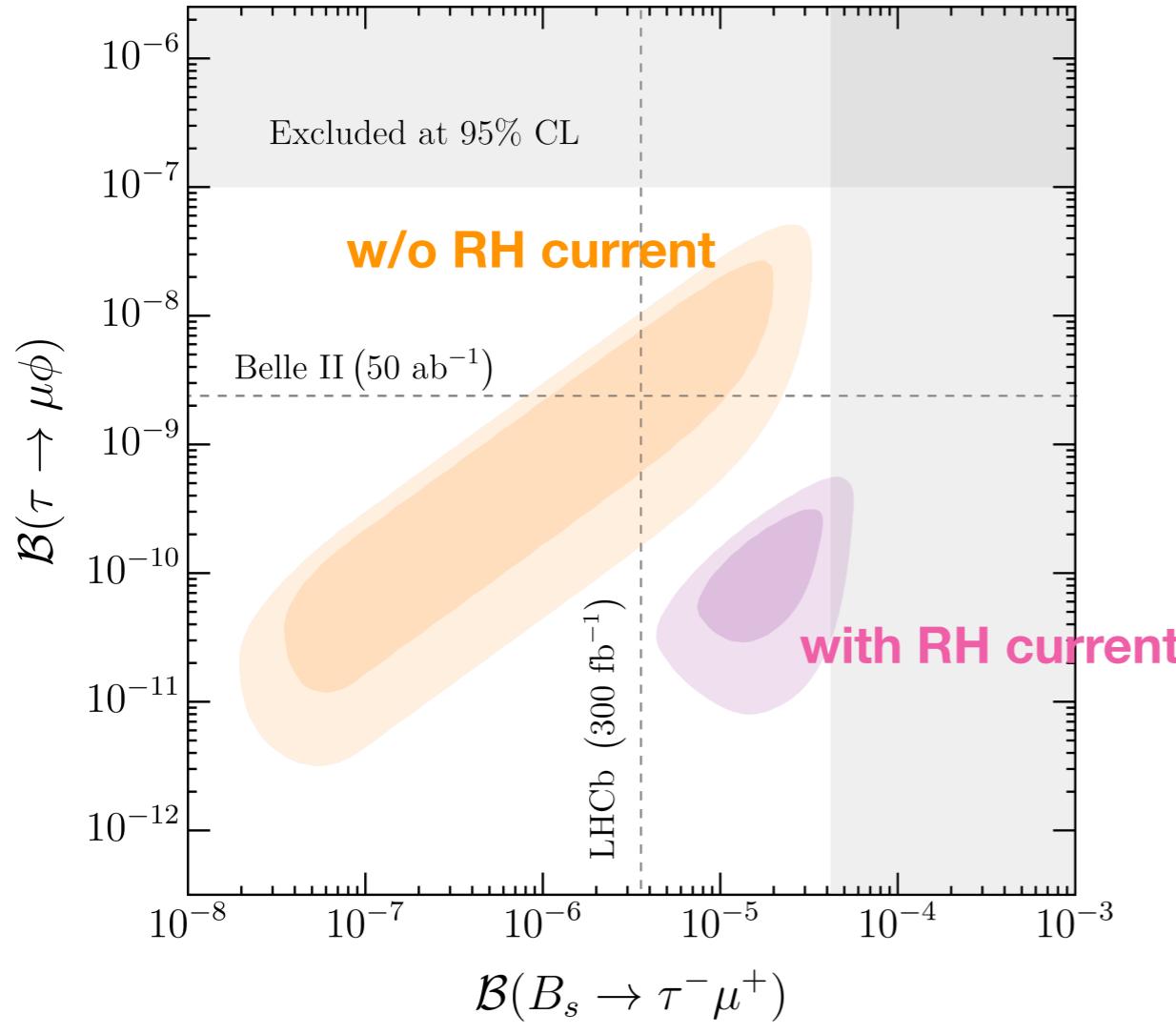


Some (key) low-energy predictions

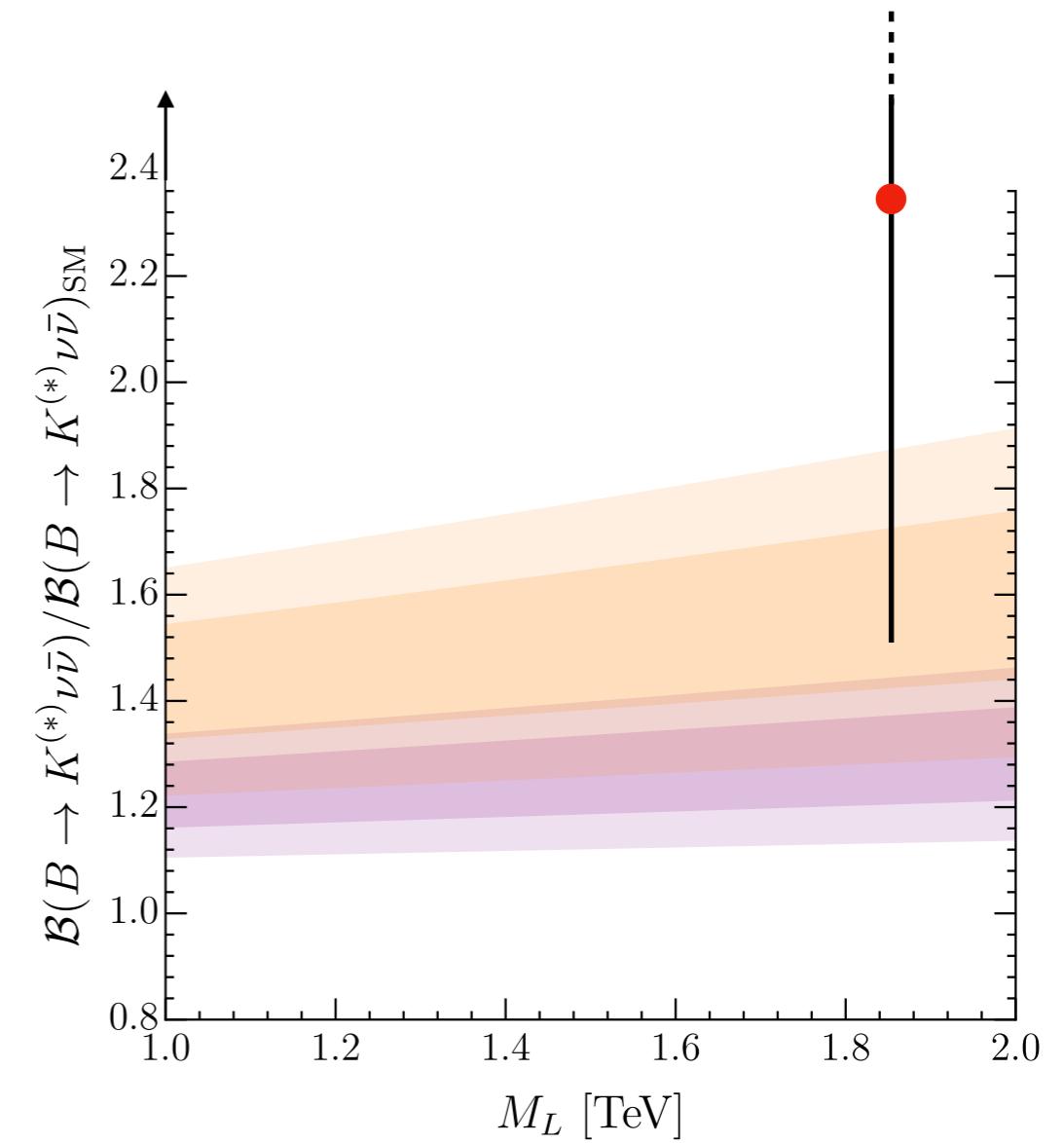
[Cornella, JF et al., 2103.16558]

LHCb & Belle II essential to confirm/exclude the new physics solution in a large class of correlated observables

$\tau - \mu$ Lepton Flavor Violation



$b \rightarrow s \nu_{(\tau)} \bar{\nu}_{(\tau)}$ (loop-level for U_1 model)
[$b \rightarrow s \tau^+ \tau^-$ also key (see backup)]

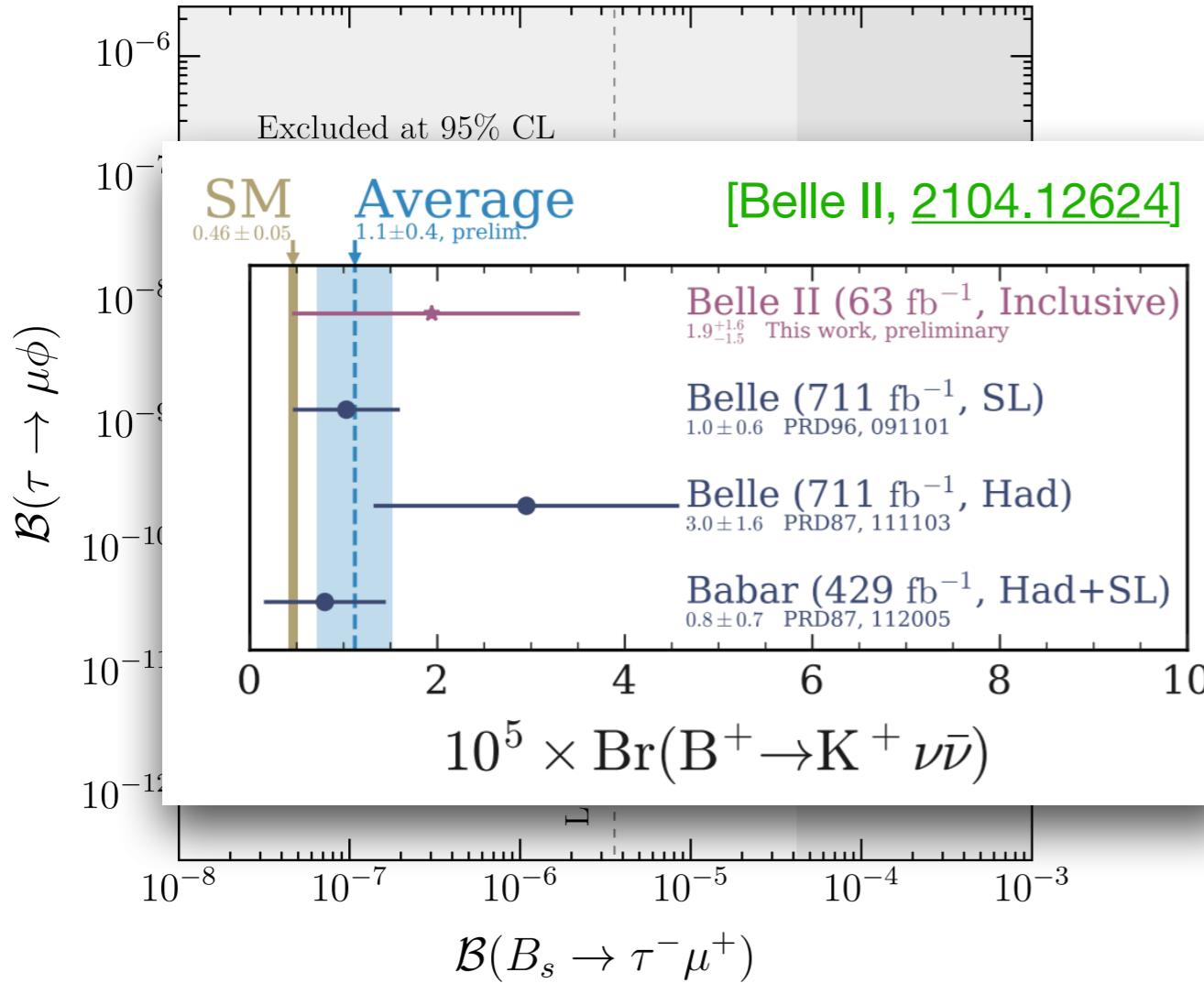


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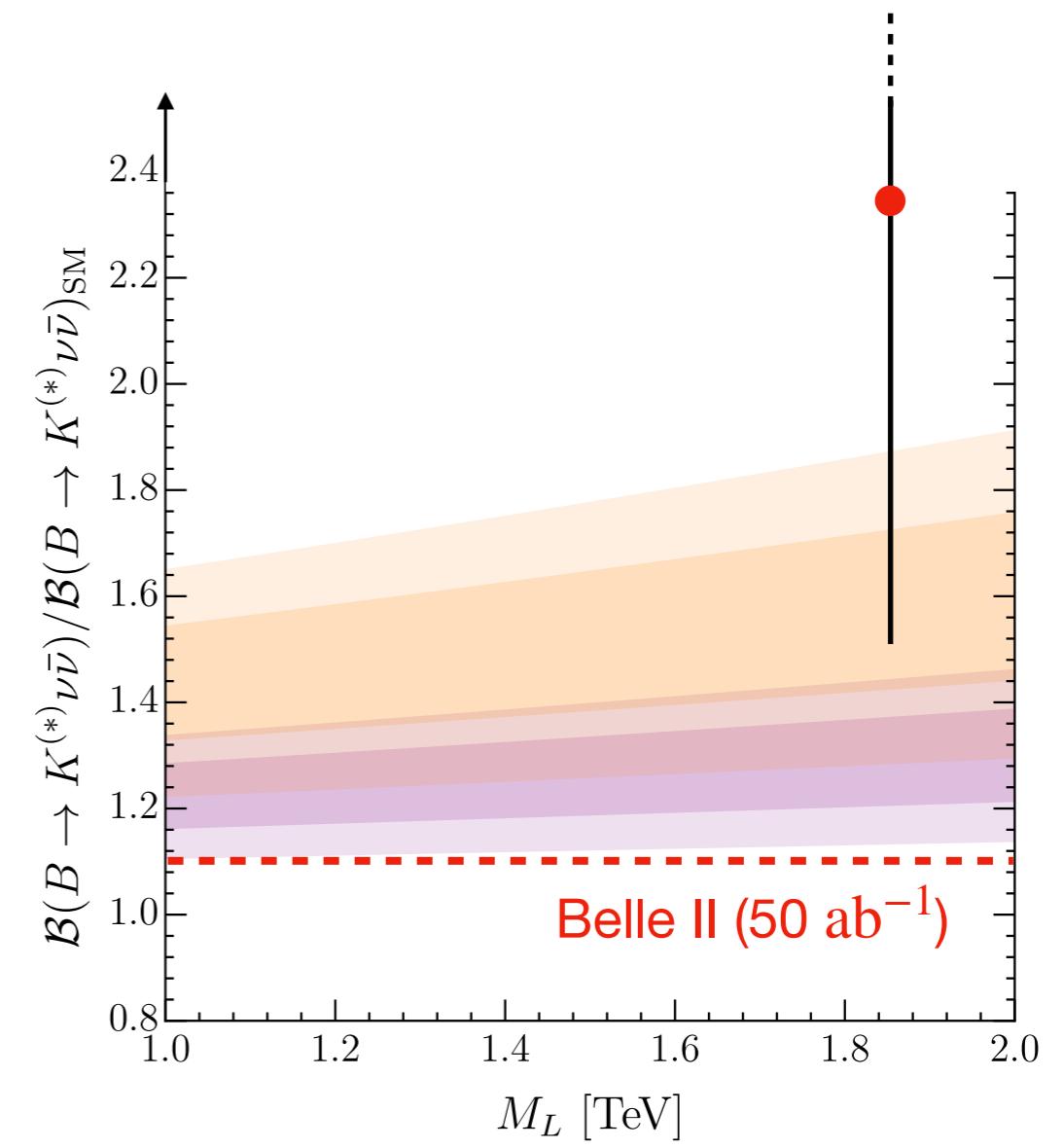
[Cornella, JF et al., [2103.16558](#)]

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A glimpse into possible UV completions



Gauge UV completion for the U_1 leptoquark

$$U_1 \sim (3,1,2/3) \longrightarrow SU(4) \longrightarrow PS = SU(4) \times SU(2)_L \times SU(2)_R$$

$$SU(4) \sim \begin{pmatrix} G^a & U^\alpha \\ (U^\alpha)^* & Z' \end{pmatrix} \quad \psi_{L,R} = \begin{bmatrix} q_{L,R}^1 \\ q_{L,R}^2 \\ q_{L,R}^3 \\ l_{L,R} \end{bmatrix}$$

Leptons as the fourth “color”

[Pati, Salam, [Phys. Rev. D10 \(1974\) 275](#)
(only 7 years after the SM was proposed)]

- ✓ $SU(4)$ is the smallest group containing the $U_1 \sim (3, 1, 2/3)$
- ✓ No proton decay (accidental baryon number symmetry like in the SM)
- ✗ Flavor-blind U_1 mediates $K_L \rightarrow \mu e \Rightarrow m_{U_1} \gtrsim 100 \text{ TeV}$
- ✗ Extra fermions can make the U_1 non-universal, but not the Z'
- ✗ Strongly coupled, universal Z' would be excessively produced at the LHC

4321 model(s)

[Georgi and Y. Nakai, [1606.05865](#); Diaz, Schmaltz, Zhong, [1706.05033](#); Di Luzio, Greljo, Nardecchia, [1708.08450](#); Bordone, Cornella, JF, Isidori [1712.01368](#)]

We can “protect” the light families by de-correlating $SU(4)$ from the SM color group ($g_4 \gg g_3$)

PS group:

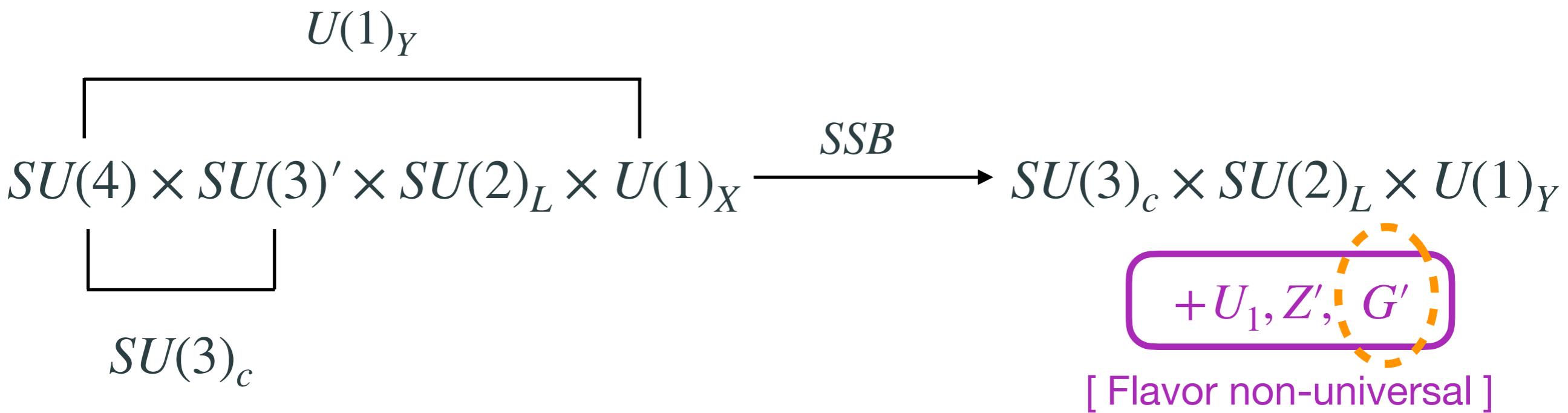
$$\mathcal{G}_{\text{PS}} \supset SU(4) \times SU(2)_L \times U(1)_R$$

[Flavor universal]

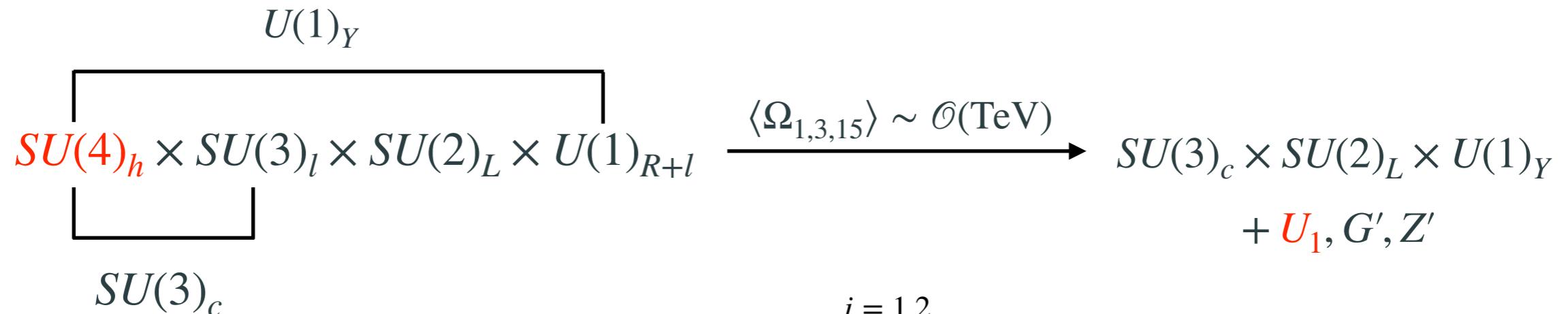
$$\Psi_{L,R}^{1,2,3}$$


$$\mathbf{4321 \ group: } \mathcal{G}_{4321} \equiv SU(4)_h \times SU(3)_l \times SU(2)_L \times U(1)_{R+l} \quad [\text{Flavor non-universal}]$$

$$\Psi_{L,R}^3 \quad \Psi_{L,R}^{1,2}$$



Third-family quark-lepton unification at the TeV scale

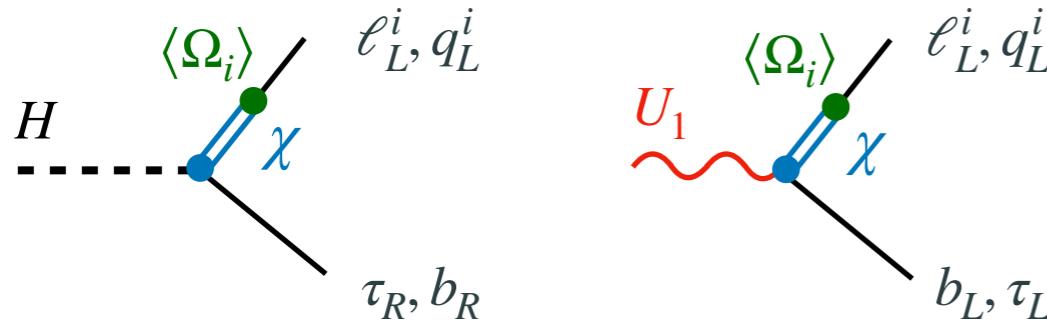


- ★ Third-family quark-lepton unification at the TeV

$$\psi_{L,R} = [q_{L,R}^1 \quad q_{L,R}^2 \quad q_{L,R}^3 \quad l_{L,R}]$$

- ★ Direct new physics couplings to 3rd family only
[as in the multi-scale picture]

- ★ CKM mixing and NP couplings to light families via (small) mixing with vectorlike fermions χ



Field	$SU(4)$	$SU(3)'$	$SU(2)_L$	$U(1)_X$
q_L^i	1	3	2	1/6
u_R^i	1	3	1	2/3
d_R^i	1	3	1	-1/3
ℓ_L^i	1	1	2	-1/2
e_R^i	1	1	1	-1
ψ_L	4	1	2	0
ψ_R^\pm	4	1	1	$\pm 1/2$
χ_L^i	4	1	2	0
χ_R^i	4	1	2	0
H	1	1	2	1/2
Ω_1	4	1	1	-1/2
Ω_3	4	3	1	1/6
Ω_{15}	15	1	1	0

$i = 1, 2$

1st & 2nd families

3rd family

vectorlike fermions

4321 breaking scalars

[Bordone, Cornella, JF, Isidori [1712.01368](#), [1805.09328](#); Greljo, Stefanek, [1802.04274](#); Cornella, JF, Isidori [1903.11517](#)]

High- p_T predictions: vector-like leptons at high- p_T

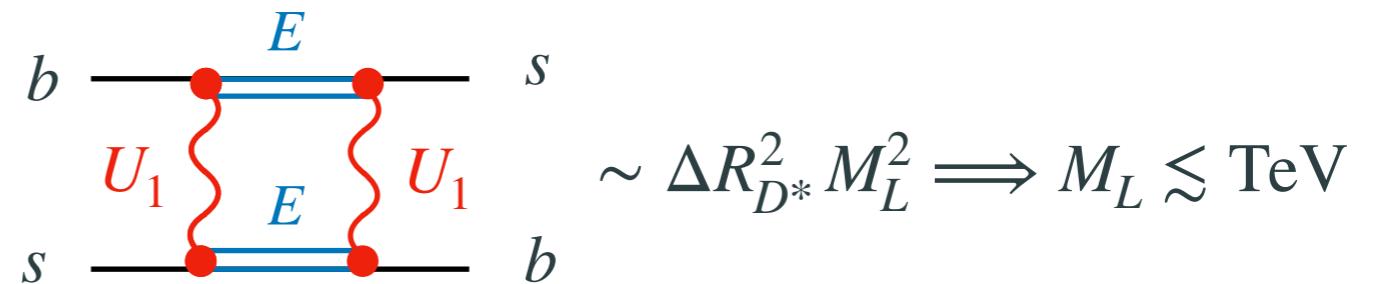
Some (important) effects appear only at one loop $\chi_{L,R} = (Q \ L)^T$

$$Q \sim (3, 2, 1/6)$$

$$Q = \begin{pmatrix} U \\ D \end{pmatrix}$$

$$L \sim (1, 2, -1/2)$$

$$L = \begin{pmatrix} N \\ E \end{pmatrix}$$

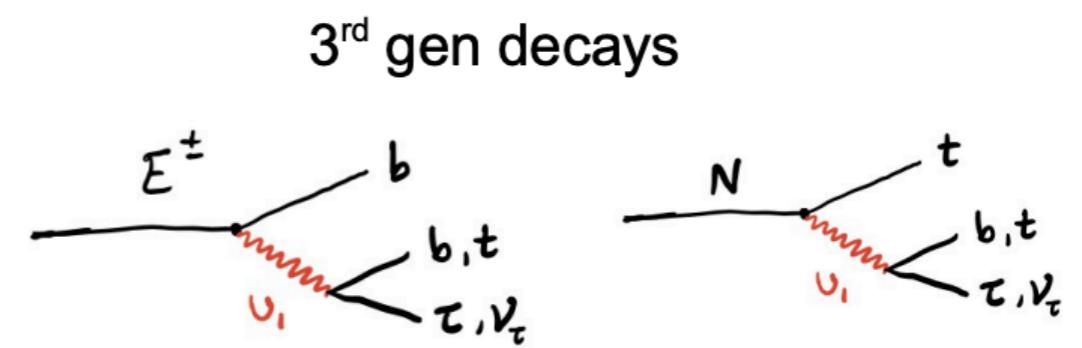
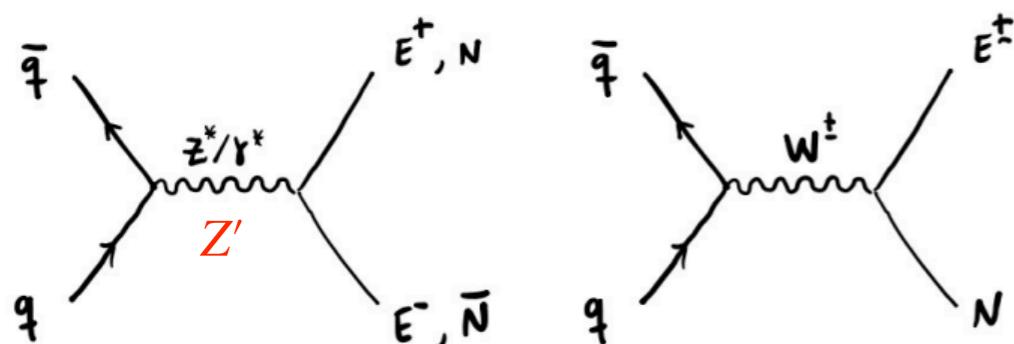


$$\sim \Delta R_{D^*}^2 M_L^2 \implies M_L \lesssim \text{TeV}$$

Analogously to the charm quark in the SM
[vectorlike leptons within the LHC reach!]

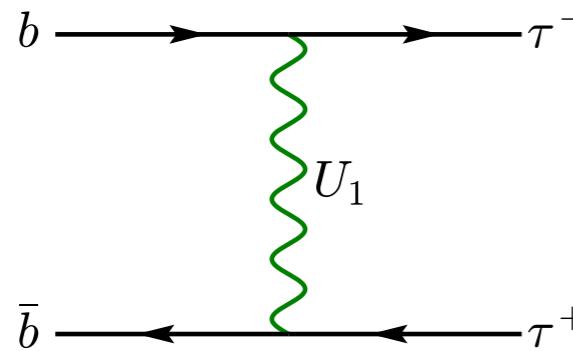
[di Luzio, JF, et al [1808.00942](#); Cornella, JF, Isidori [1903.11517](#); JF et al., [2009.11296](#)]

Electroweak (or Z') produced. Dominant **decay to three 3rd generation** SM fermions!

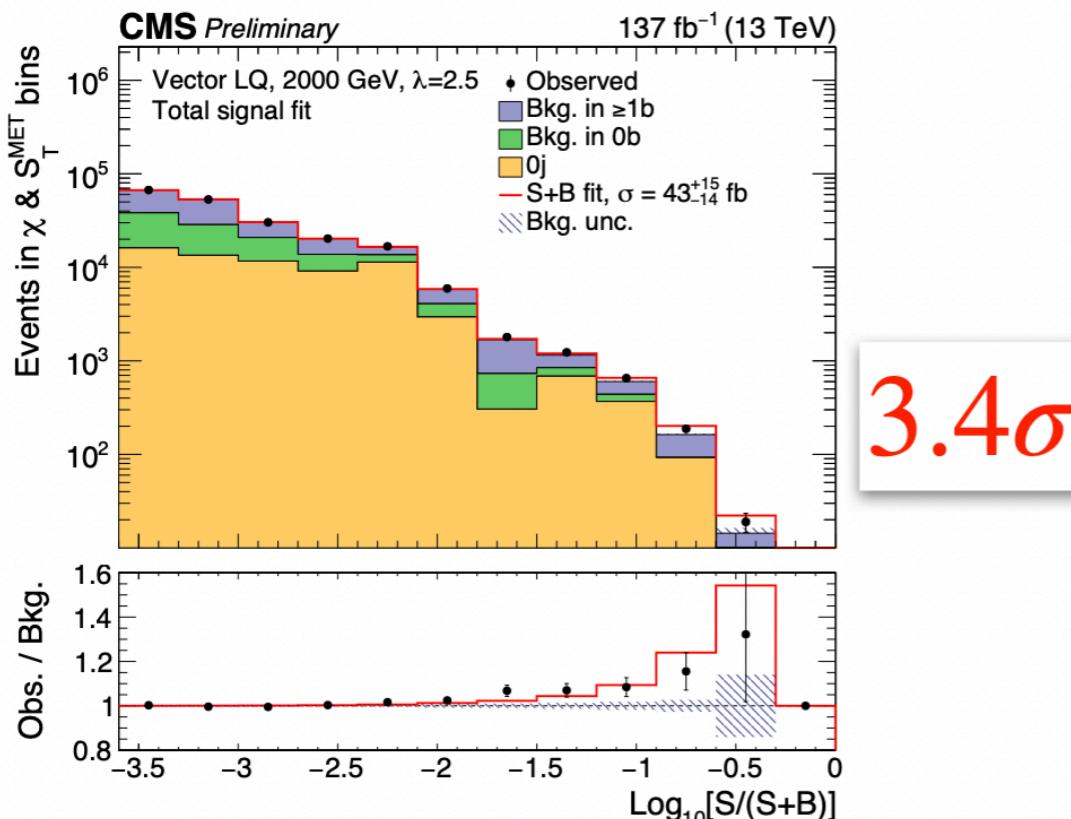


Exciting results for 4321 models from CMS

[See talk by Sabino Meola]

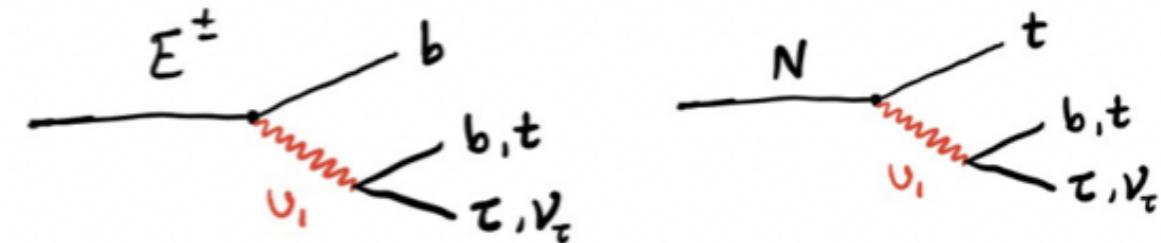


[Faroughy, Greljo, Kamenik, [1609.07138](#)]

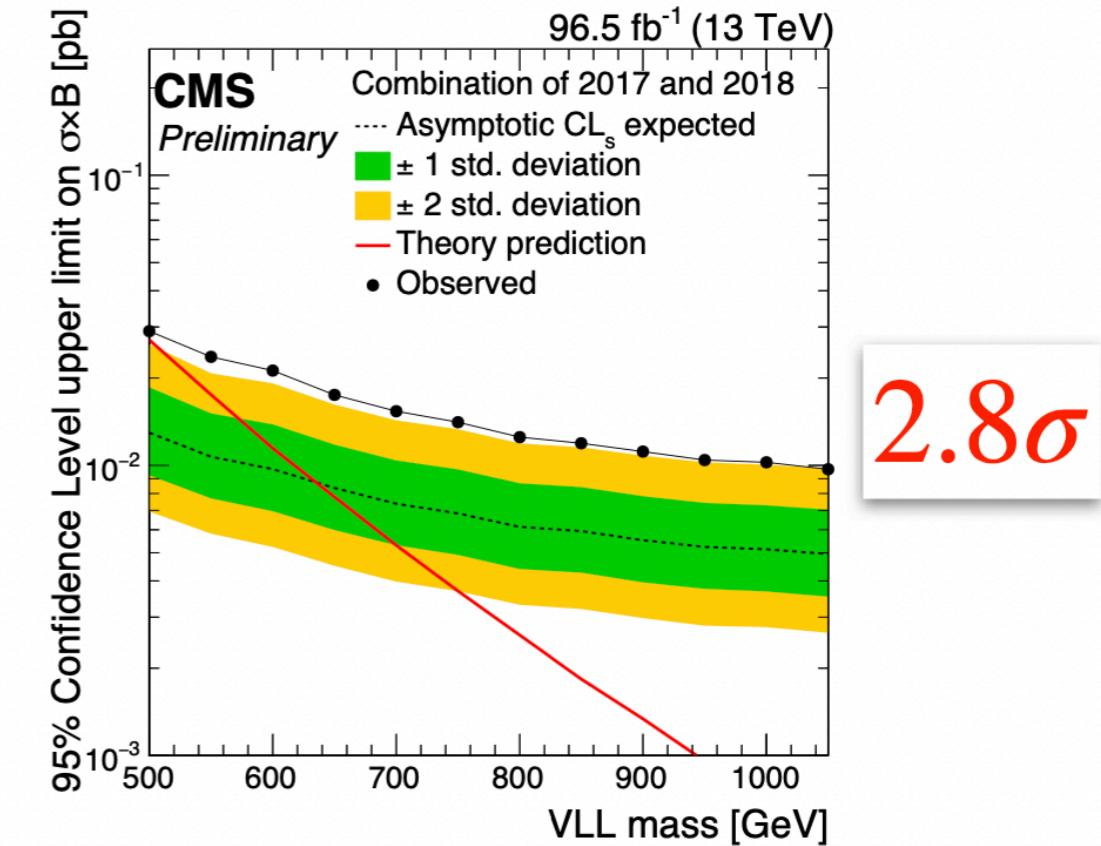


[CMS PAS EXO-19-016](#)

[No excess in ATLAS data (no dedicated search)]



[Di Luzio, JF, Greljo, Nardecchia, Renner, [1708.08450](#)]



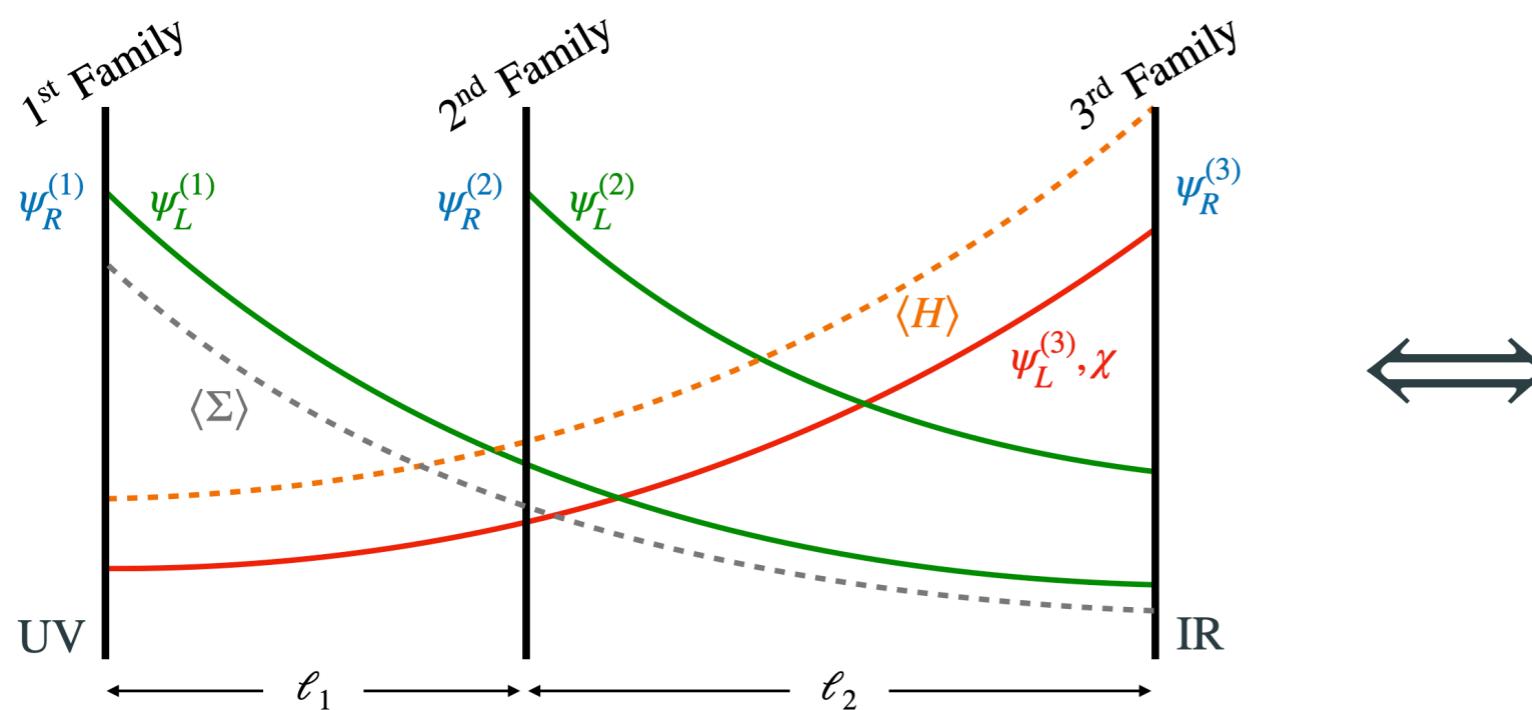
[CMS-B2G-21-004](#)

[ATLAS search currently ongoing]

Back to the multi-scale picture

$$\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{Gauge}} + \mathcal{L}_{\text{Higgs}} + \mathcal{L}_{\text{Yukawa}} + \sum_{i,d} \frac{1}{\Lambda_i^{d-4}} C_i \mathcal{O}_i^d$$

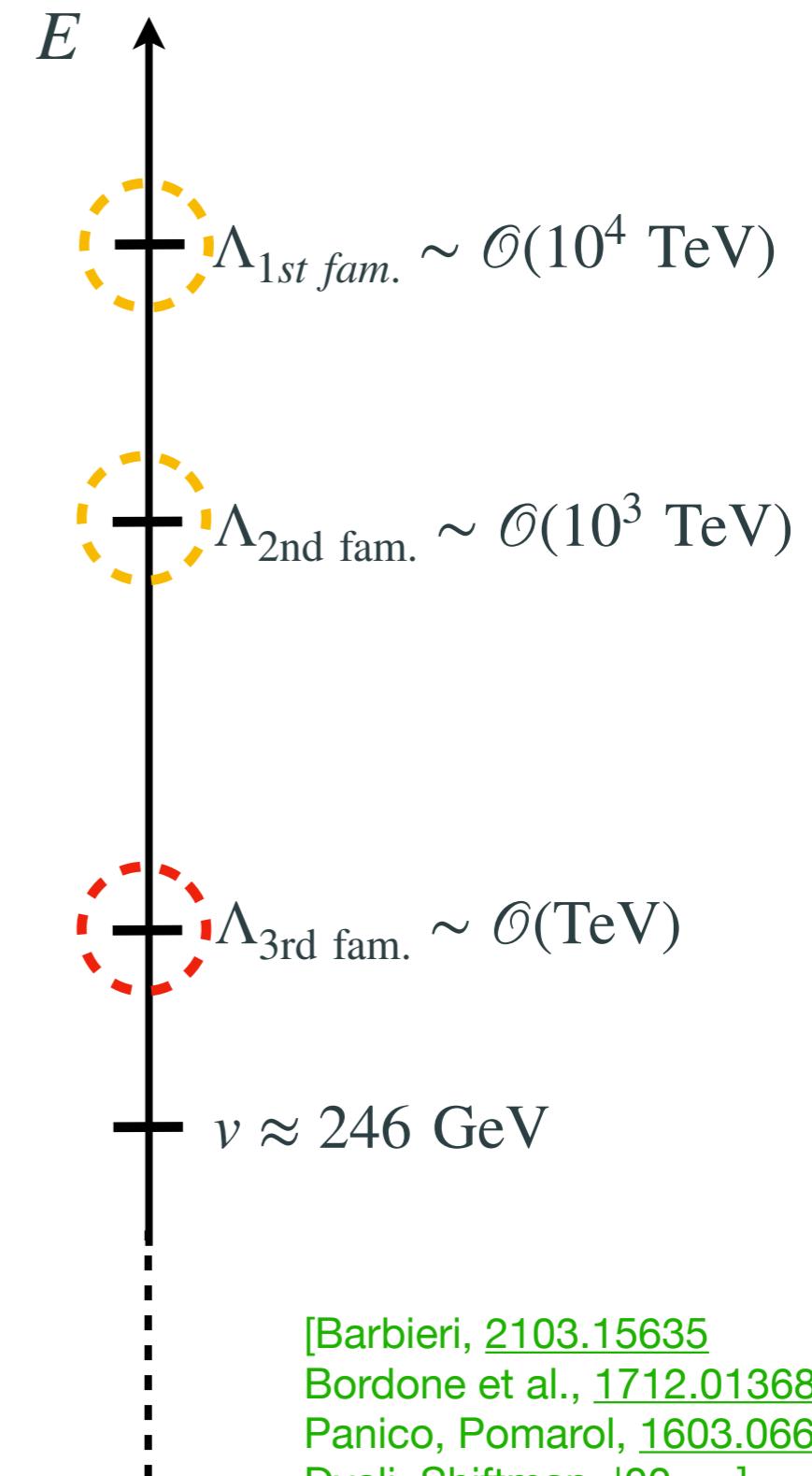
Non-trivial UV imprints



Flavor \longleftrightarrow fermion (quasi-)localization along
a warped extra dimension

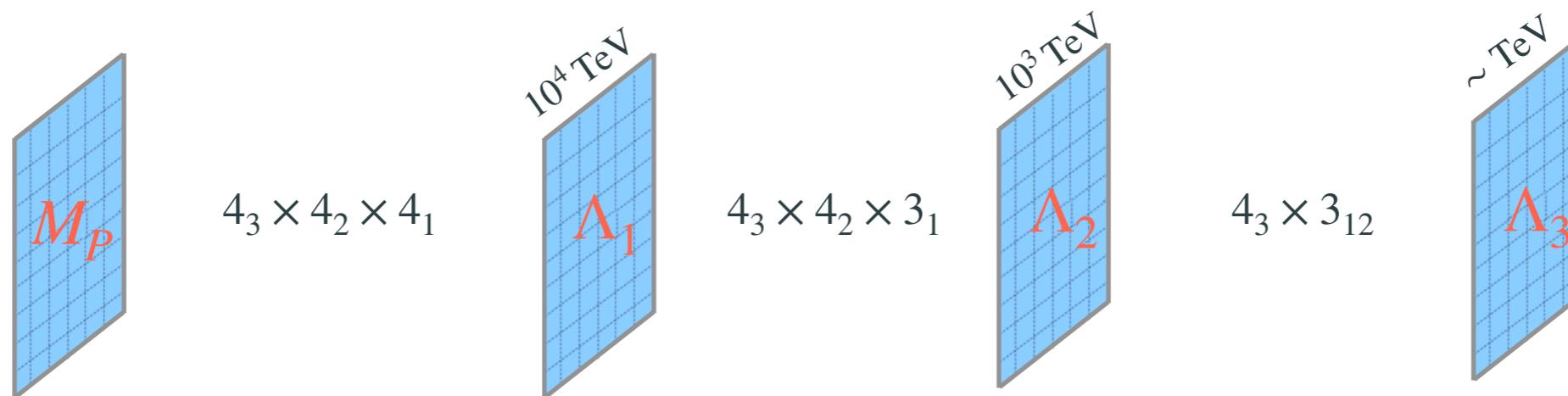
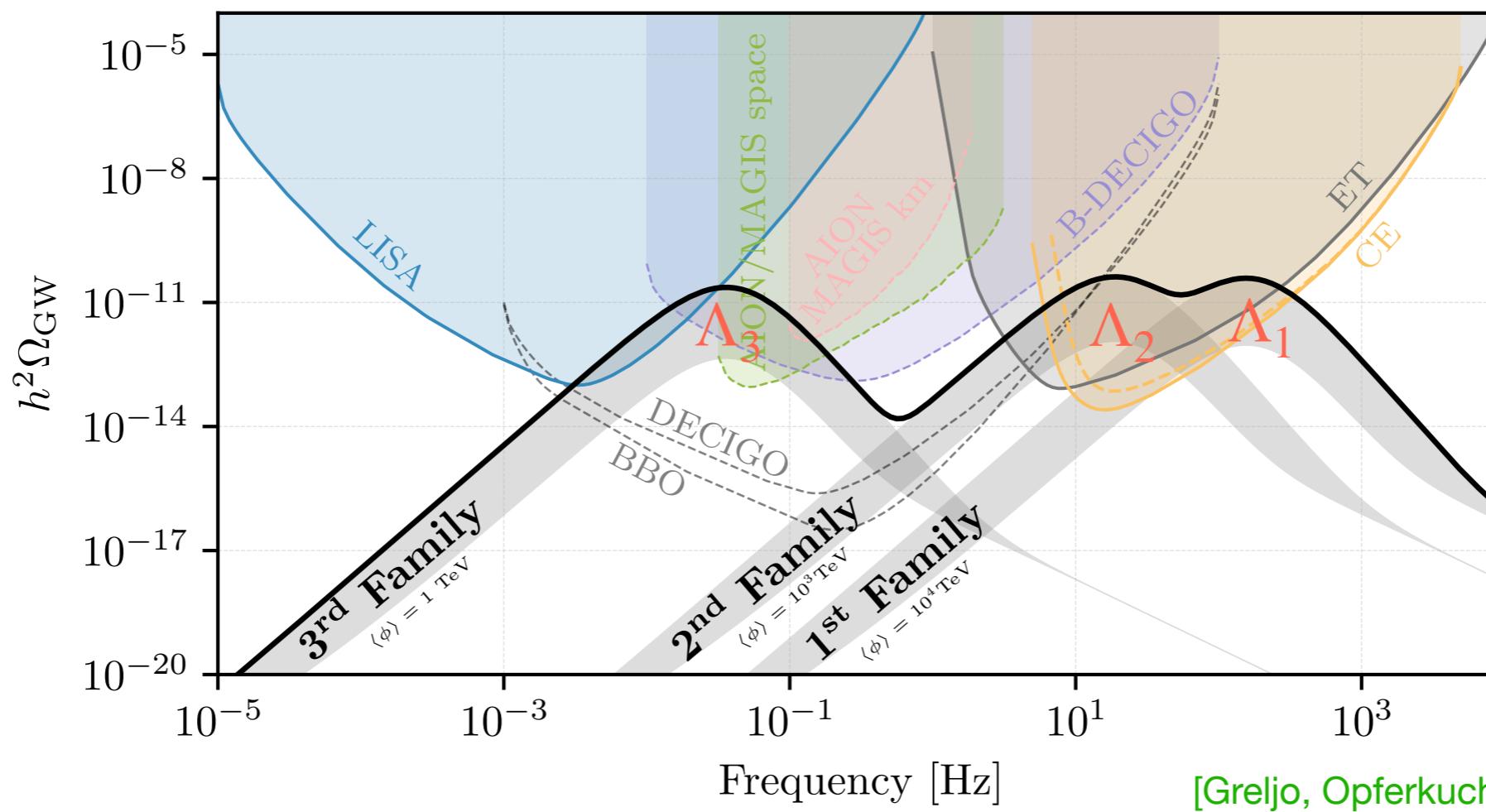
[JF, Isidori, Pagès, Stefanek, [2012.10492](#)

JF, Isidori, Lizana, Selimovic, Stefanek, [2203.01952](#)]



[Barbieri, [2103.15635](#)
Bordone et al., [1712.01368](#)
Panico, Pomarol, [1603.06609](#)
Dvali, Shifman, '00, ...]

Cosmological signatures in multi-scale picture



Conclusions

In combination, $b \rightarrow s\ell^+\ell^-$ and $b \rightarrow c\tau^-\bar{\nu}$ anomalies point to TeV-scale new physics with a flavor structure similar to that of the SM Yukawas

→ Possible connection to the origin of SM flavor and electroweak hierarchies from a multi-scale picture

New physics solution consistent with low- & high-energy data, but new physics effects should emerge soon in multiple observables

→ Closing in the mass gap or new physics mirage ?

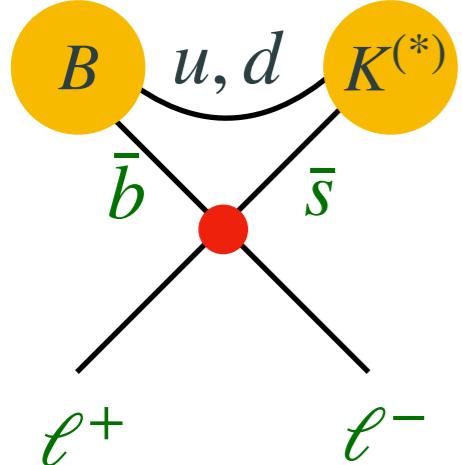
Plenty of upcoming measurements from both the energy and intensity frontiers
[e.g. part of LHC run II data still to be analyzed and Belle II data coming soon]

Thank you!



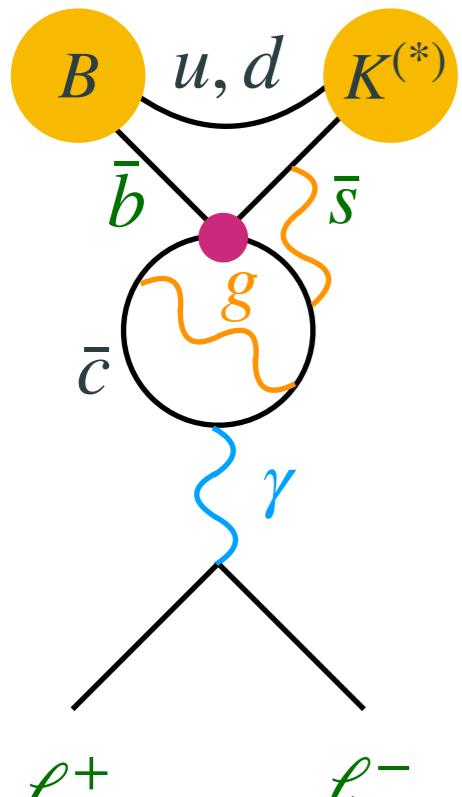
Backup

Anatomy of $b \rightarrow s \ell^+ \ell^-$ decays



Short-distance
(semileptonic int.)

“Easy” to compute



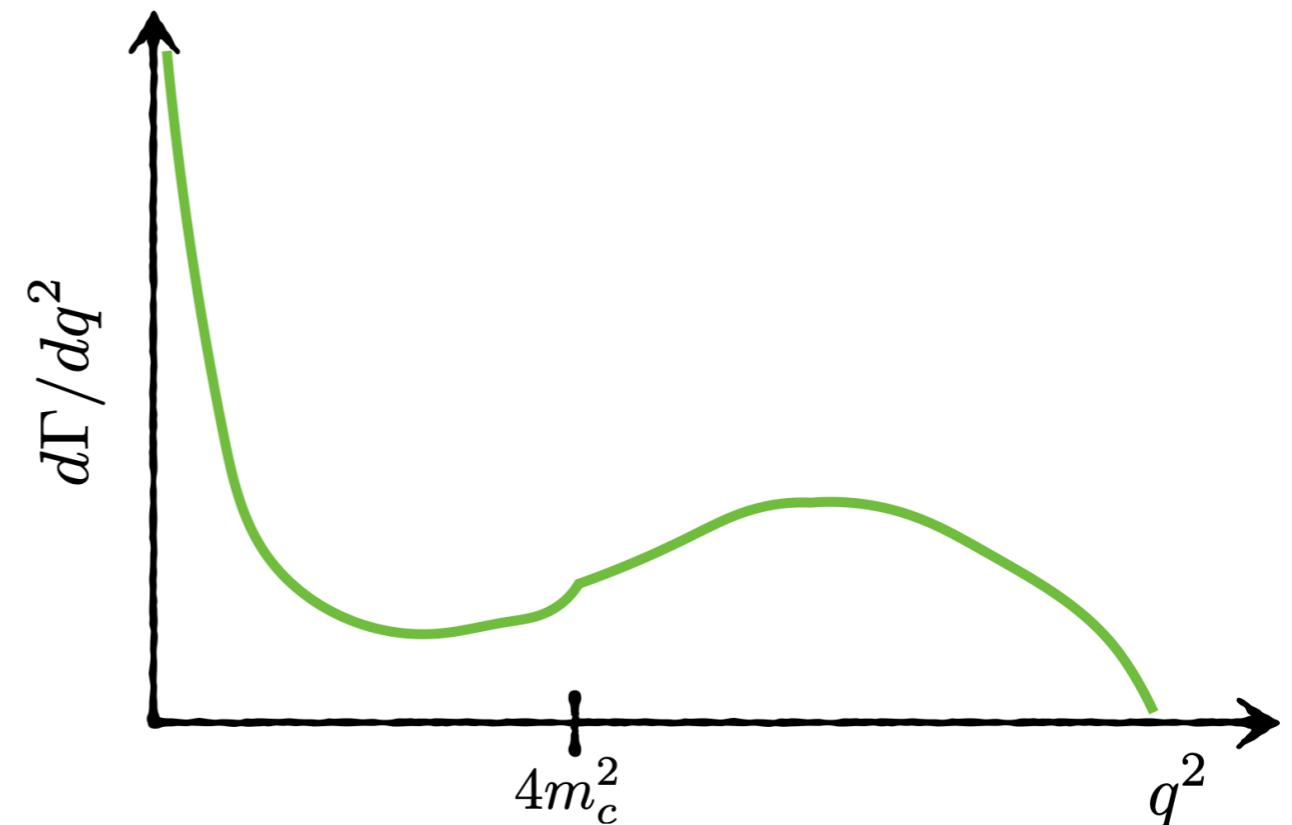
Long-distance
(four-quark int.)

Difficult to estimate

Induces a vectorial
and lepton-universal
contribution

$$\mathcal{O}_9^\ell = (\bar{s}_L \gamma_\mu b_L)(\bar{\ell} \gamma^\mu \ell)$$

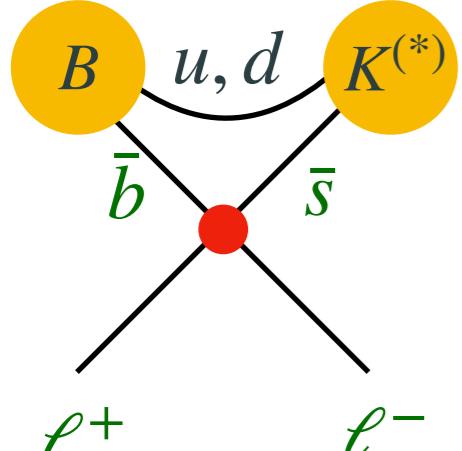
In an ideal world



[Figure from Uli Haisch]

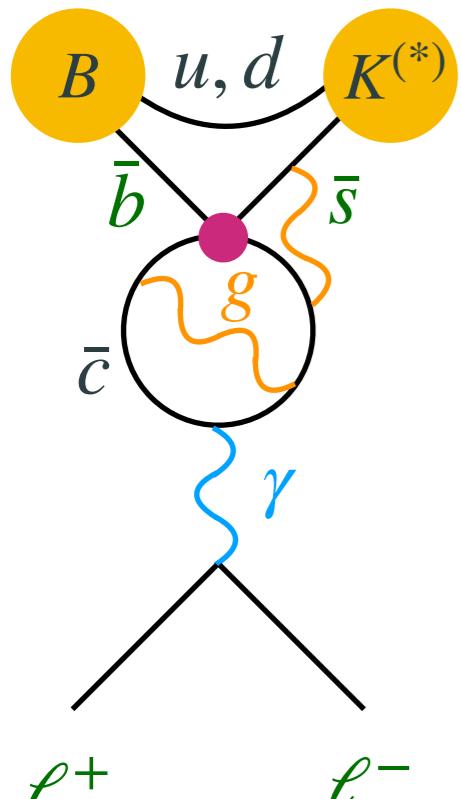
- ★ Long-distance effects cannot induce:
 - Breaking of lepton universality
 - Axial-current contributions
(no effect in $B_s \rightarrow \mu^+ \mu^-$)

Anatomy of $b \rightarrow s \ell^+ \ell^-$ decays



Short-distance
(semileptonic int.)

“Easy” to compute



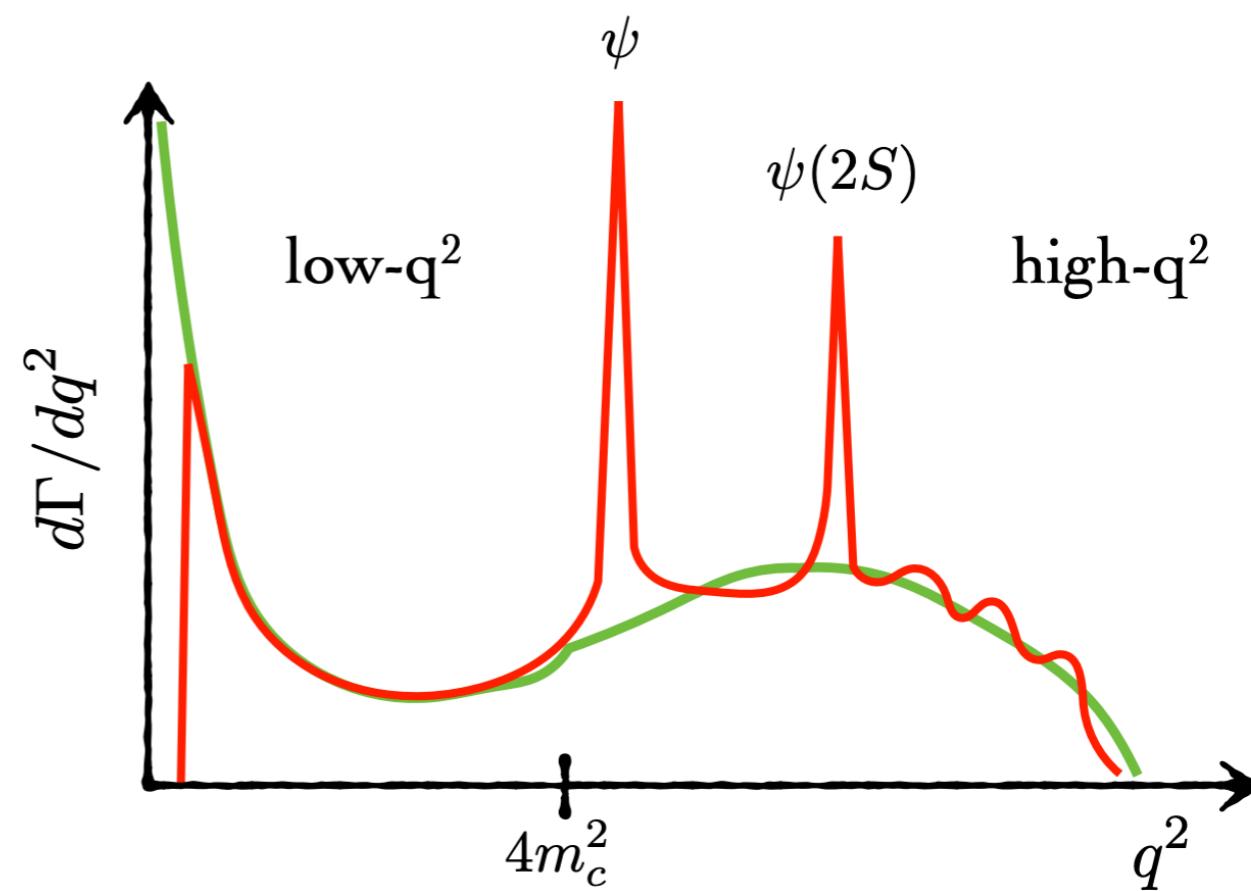
Long-distance
(four-quark int.)

Difficult to estimate

Induces a vectorial
and lepton-universal
contribution

$$\mathcal{O}_9^\ell = (\bar{s}_L \gamma_\mu b_L)(\bar{\ell} \gamma^\mu \ell)$$

... but in reality

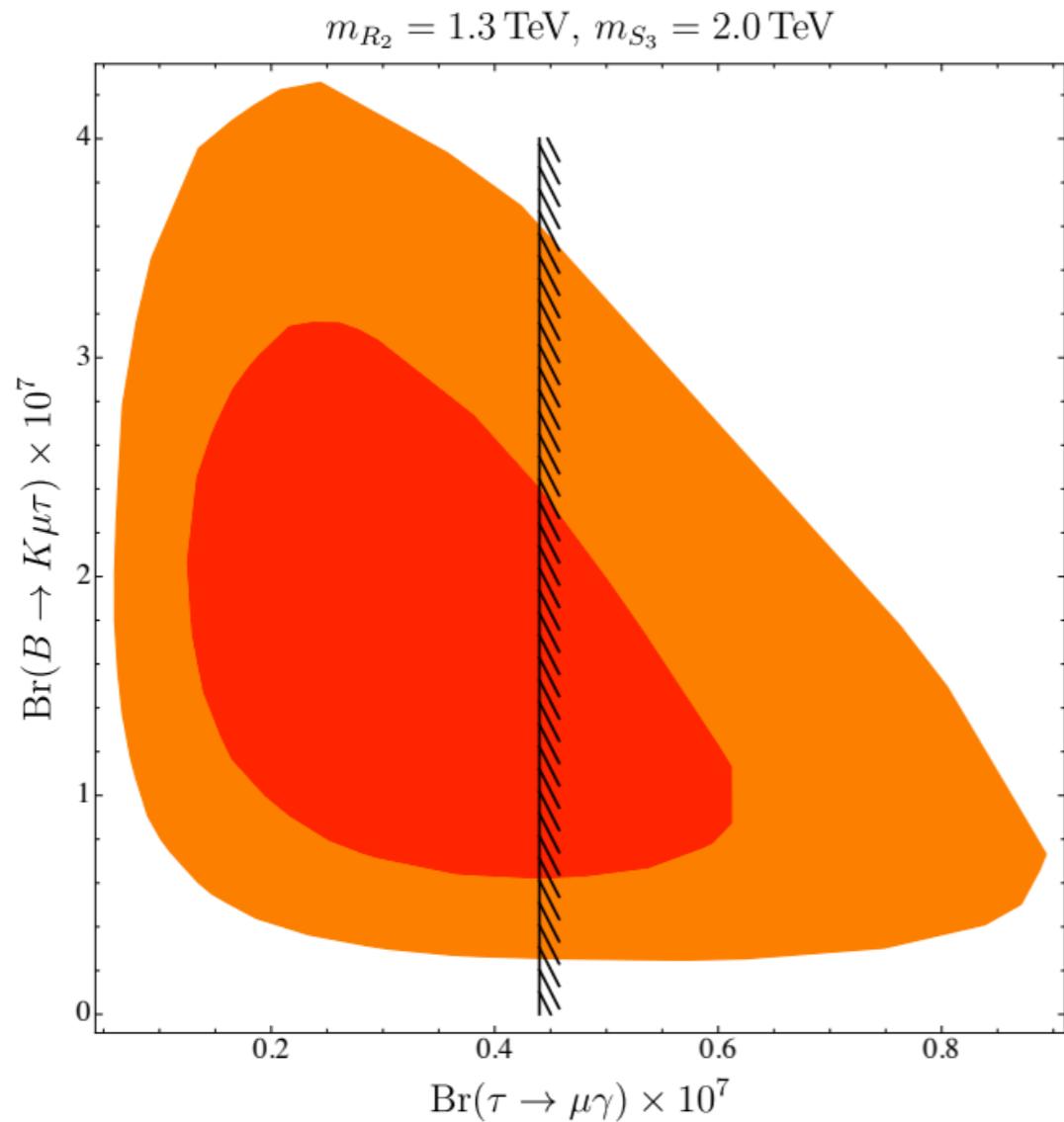


[Figure from Uli Haisch]

- ★ Long-distance effects cannot induce:
 - Breaking of lepton universality
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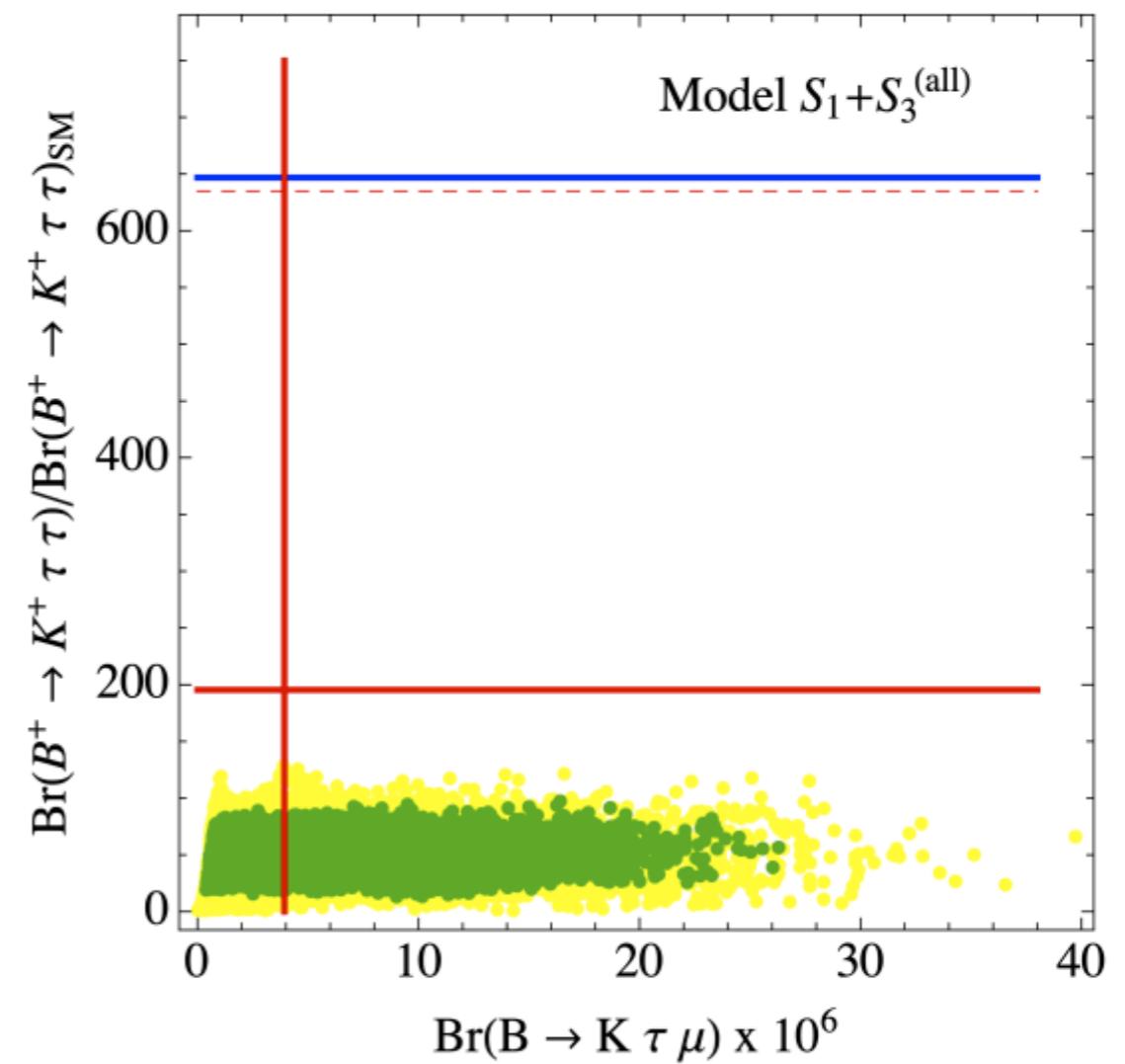
LFV predictions in other leptoquark models

$R_2 + S_3$



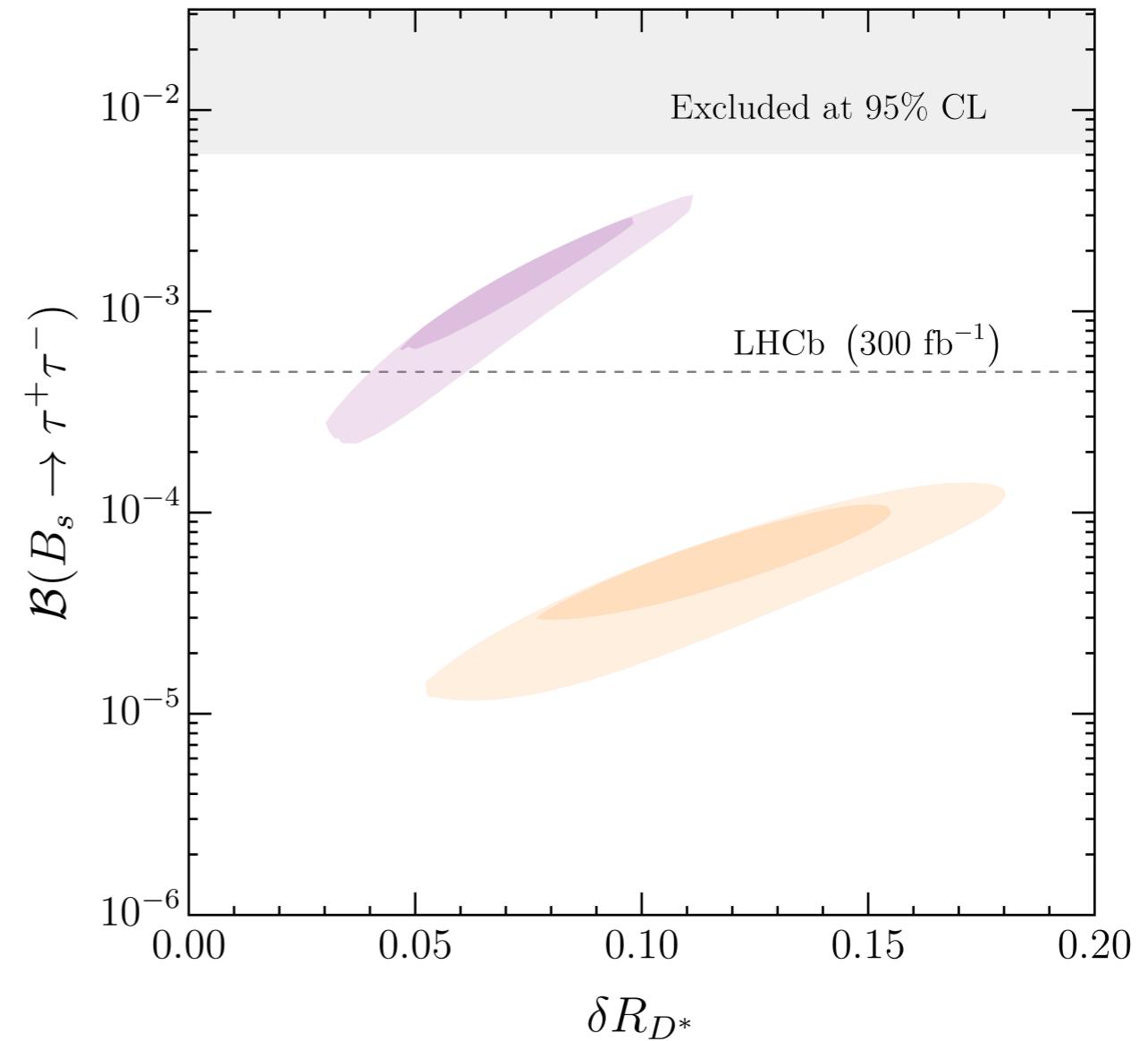
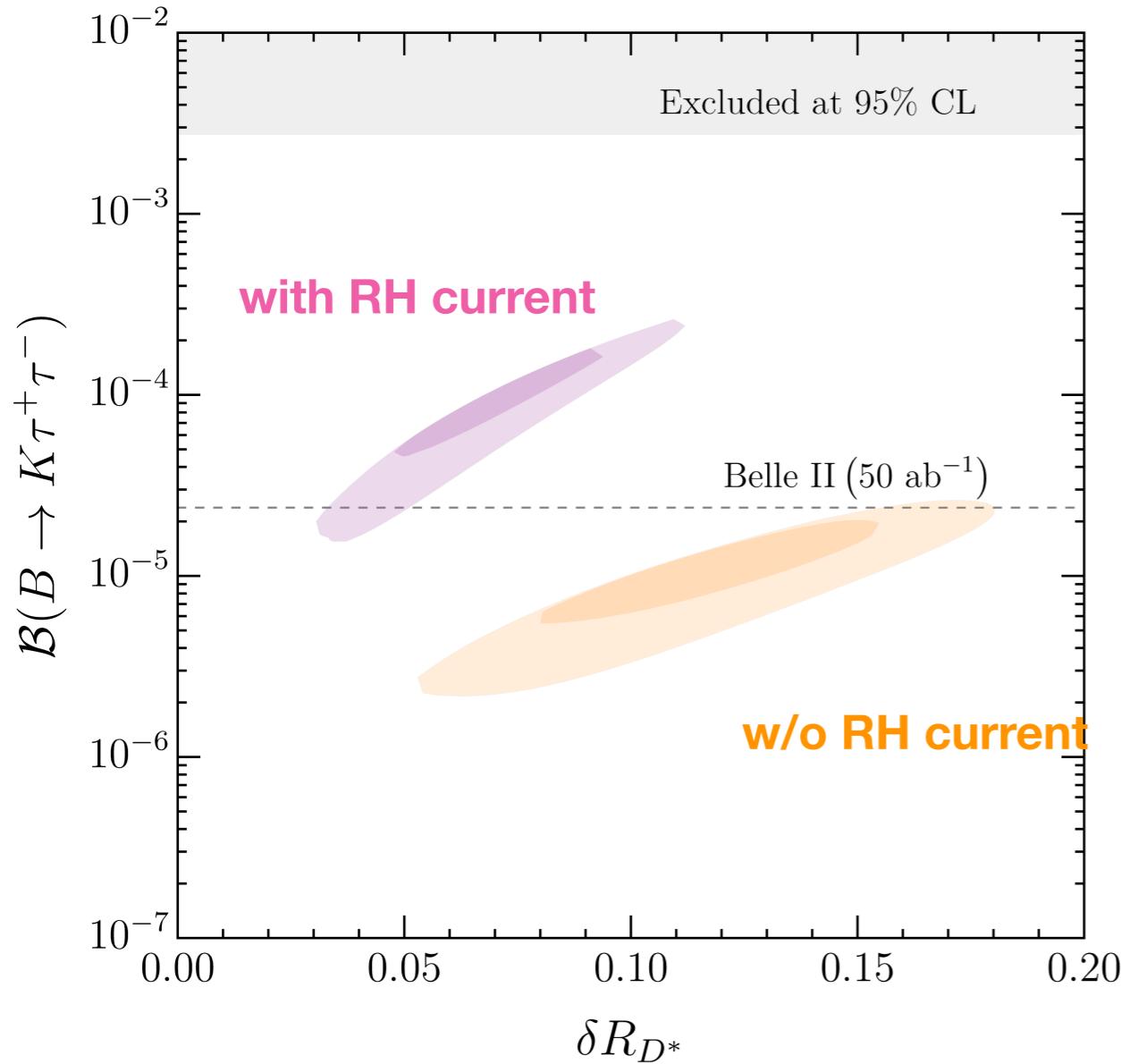
[Bečirević et al., [2206.09717](#)]

$S_1 + S_3$



[Gherardi, Marzocca, Venturini, [2008.09548](#)]

Corroborating the U_1 hypothesis: $b \rightarrow s\tau^+\tau^-$

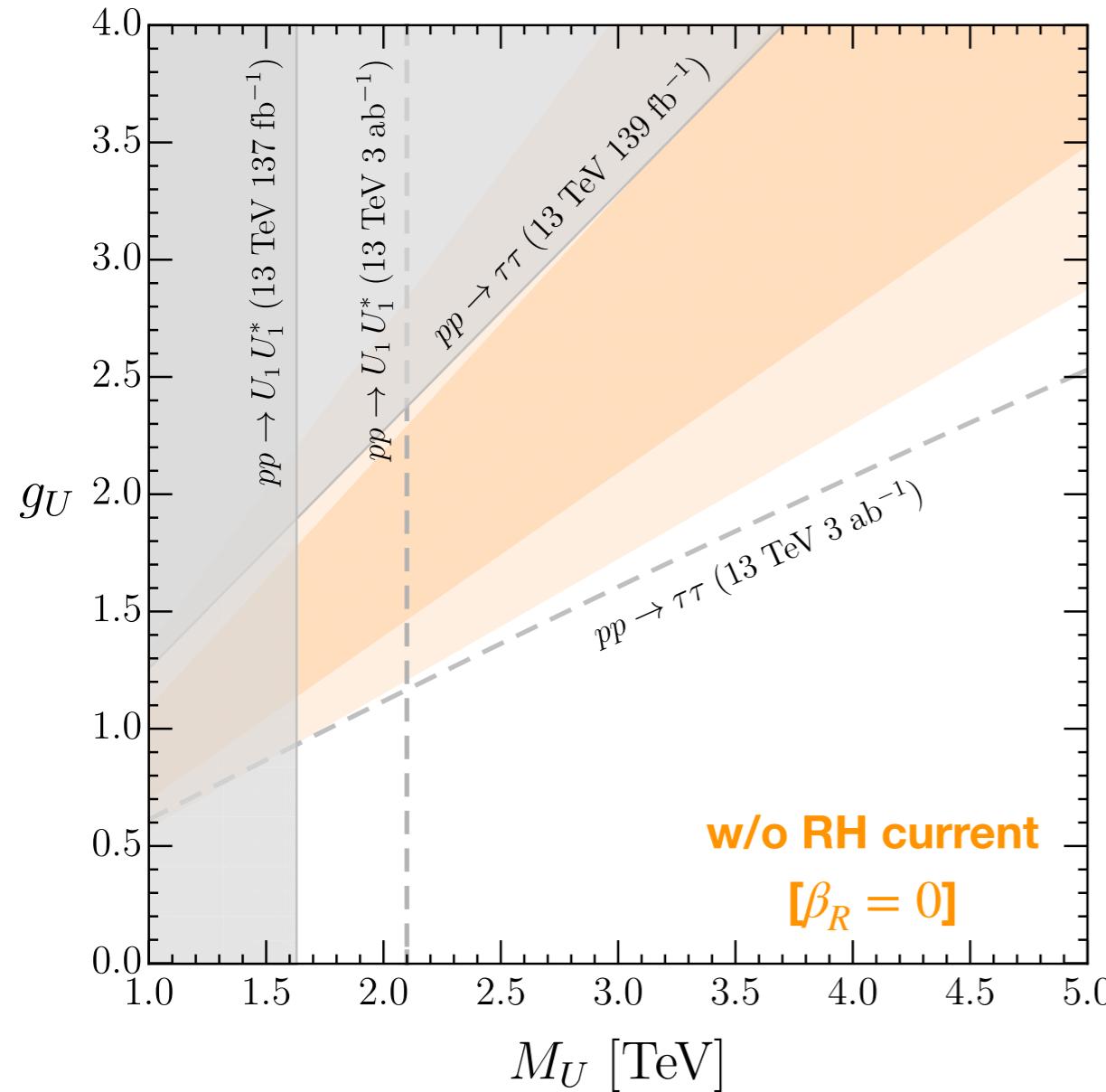


[Cornella, JF et al., [2103.16558](#)]

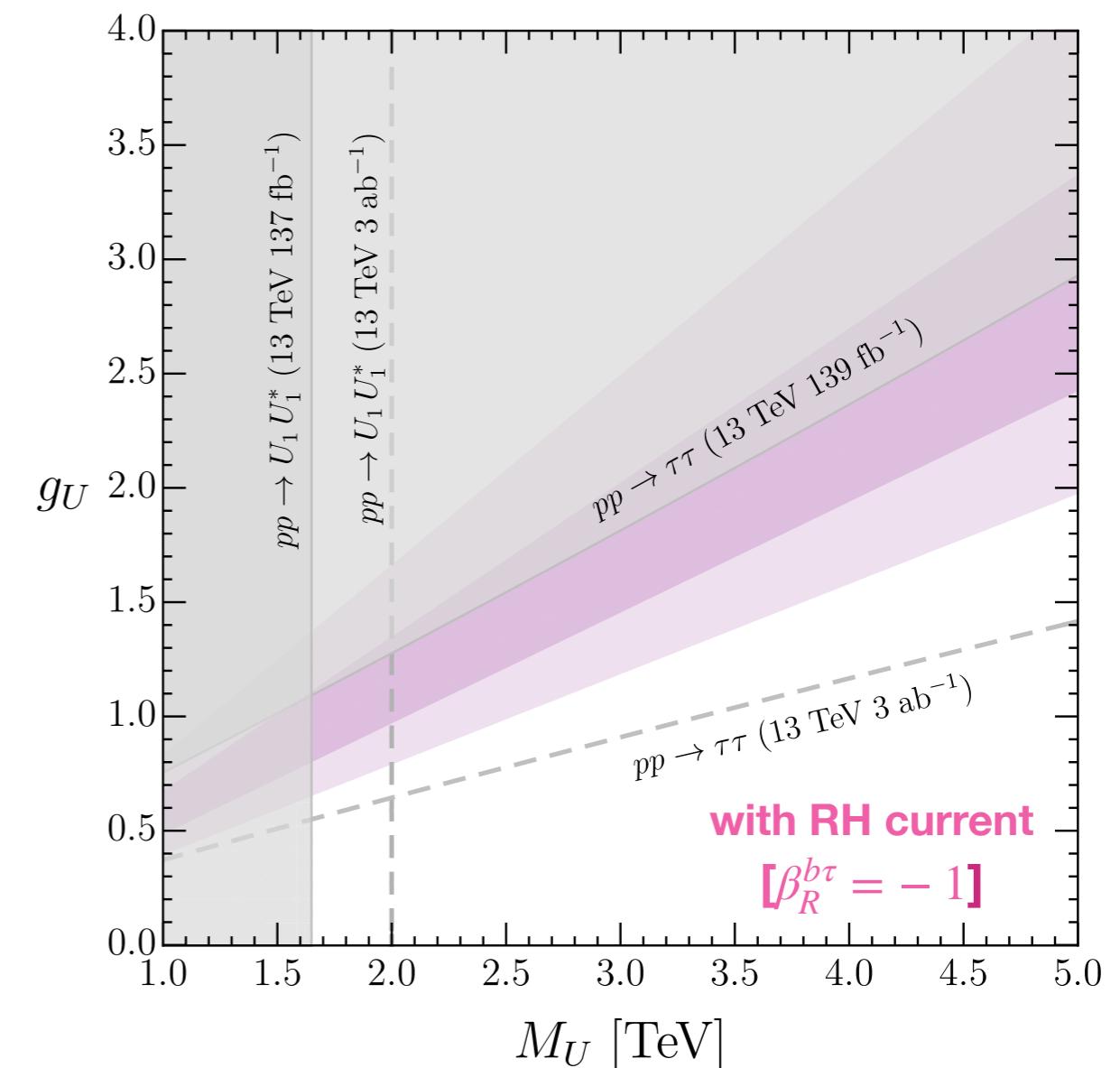
$$\text{N.B: } \delta R_{D^*} = \frac{R_{D^*} - R_{D^*}^{SM}}{R_{D^*}^{SM}}$$

U_1 searches at LHC

U_1 leptoquark solution also consistent with high- p_T data and **within the HL-LHC reach!**
 [Expected **enhancement** of high- p_T $\tau^+\tau^-$ pairs in Drell-Yan data]

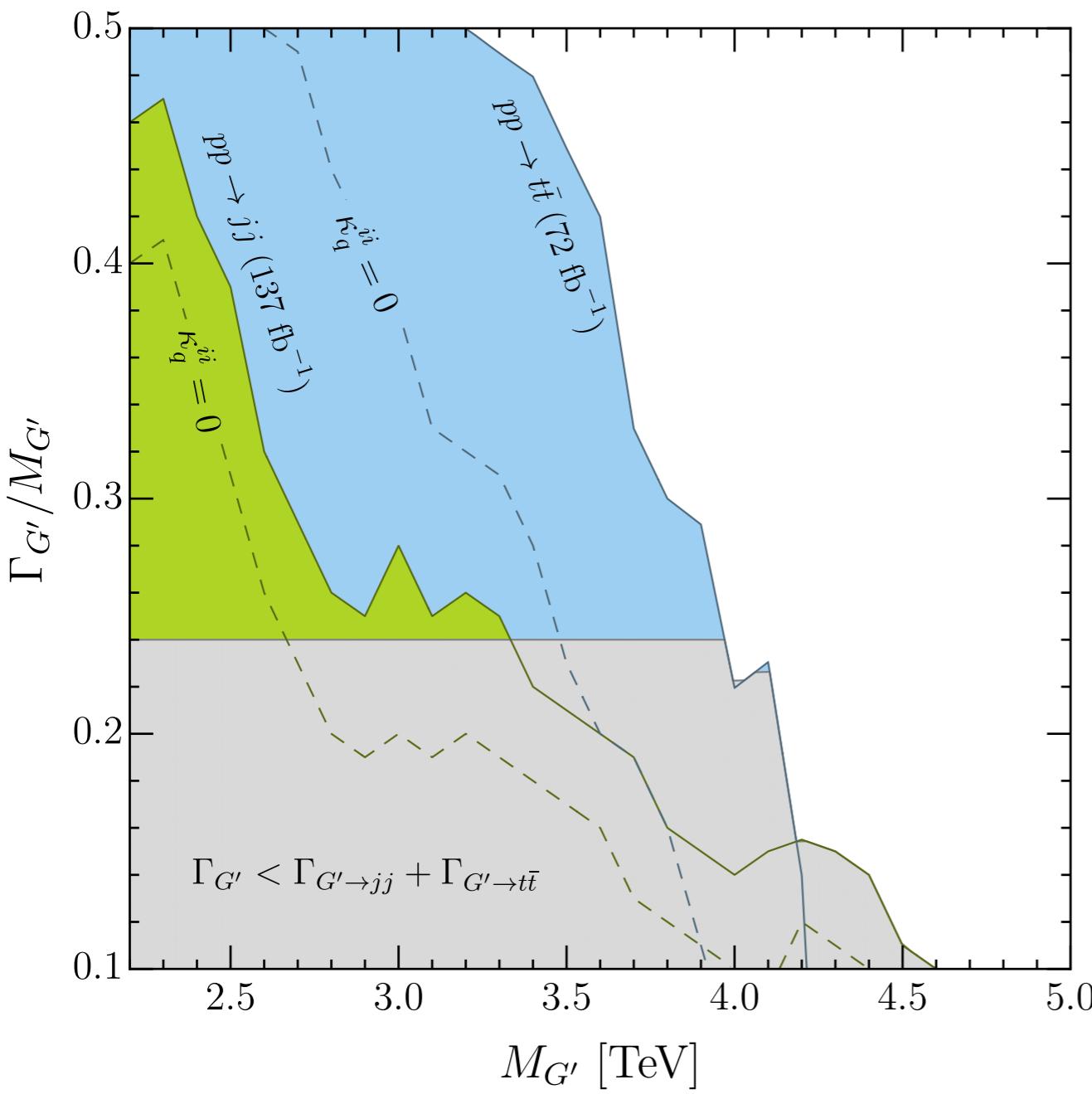


[Cornella, JF et al., [2103.16558](#)]

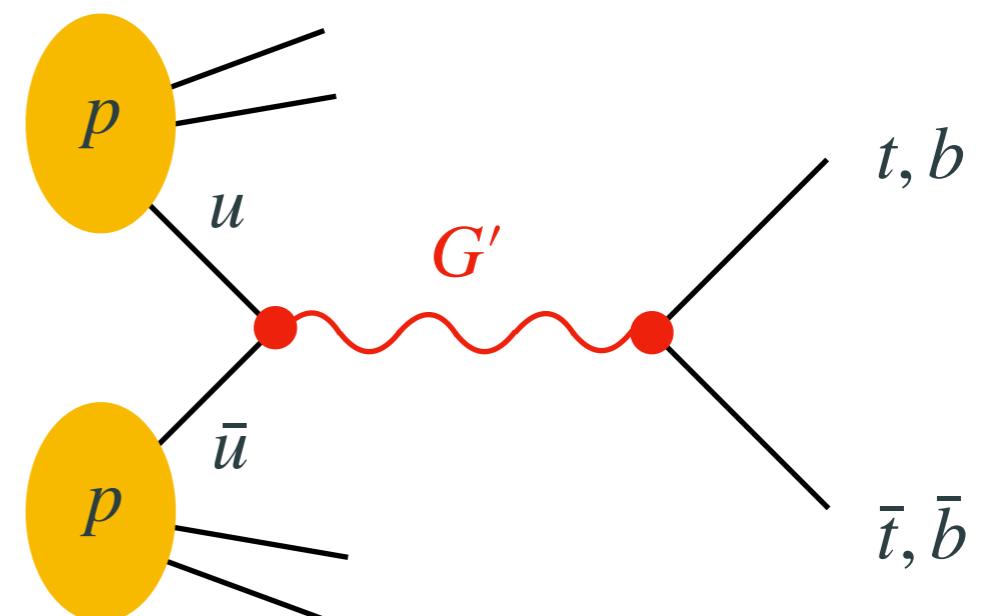


[$pp \rightarrow \tau\tau$ for U_1 originally proposed in
 Faroughy, Greljo, Kamenik, [1609.07138](#)]

Coloron direct searches at the LHC



Relevant collider signatures for G'
("coloron" = heavy color-octet vector)



Strongest constraint on the model scale from
 $p\bar{p} \rightarrow t\bar{t}$

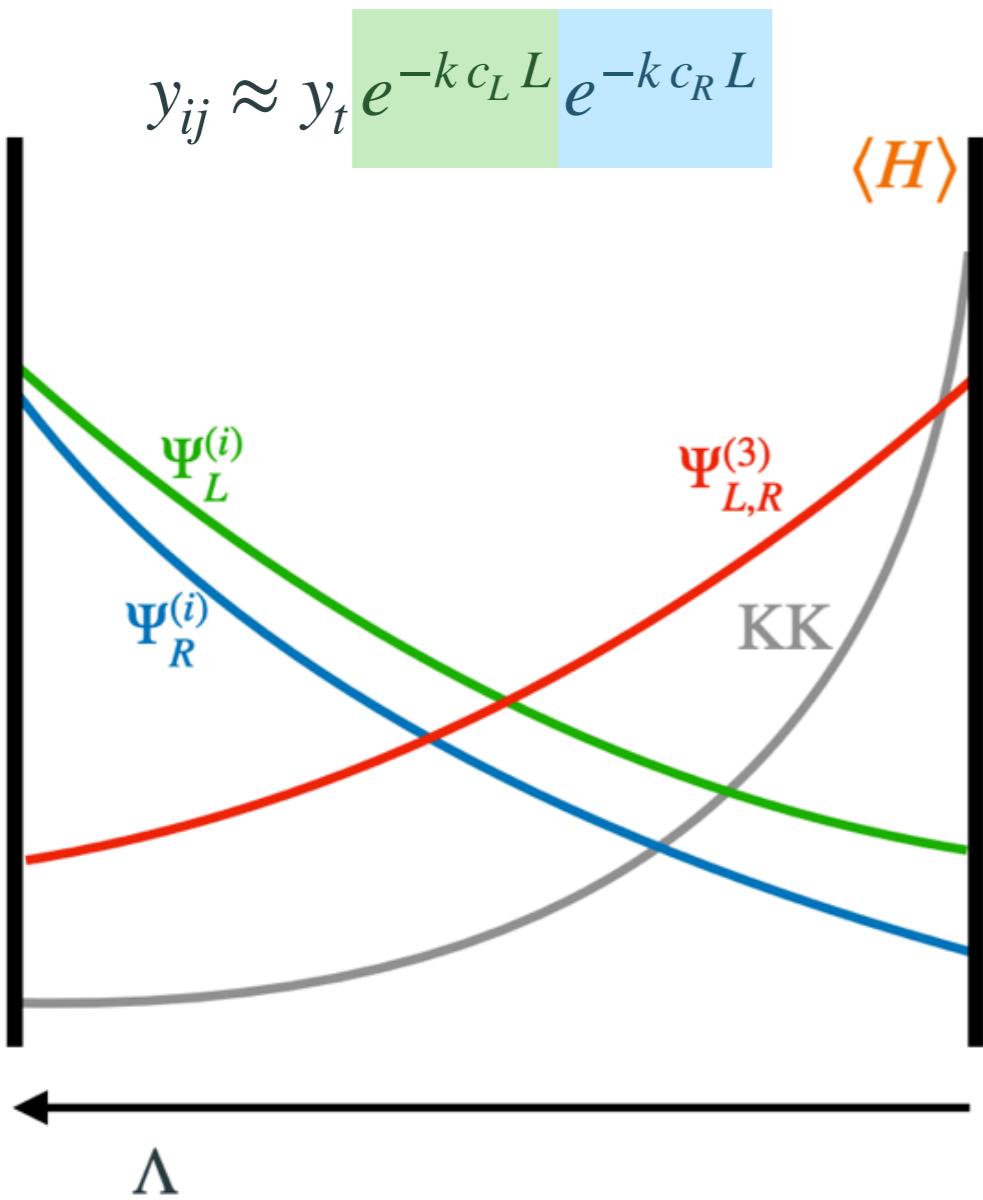
[Cornella, JF et al., 2103.16558]

Flavor in Randall-Sundrum

Curvature of the AdS slice

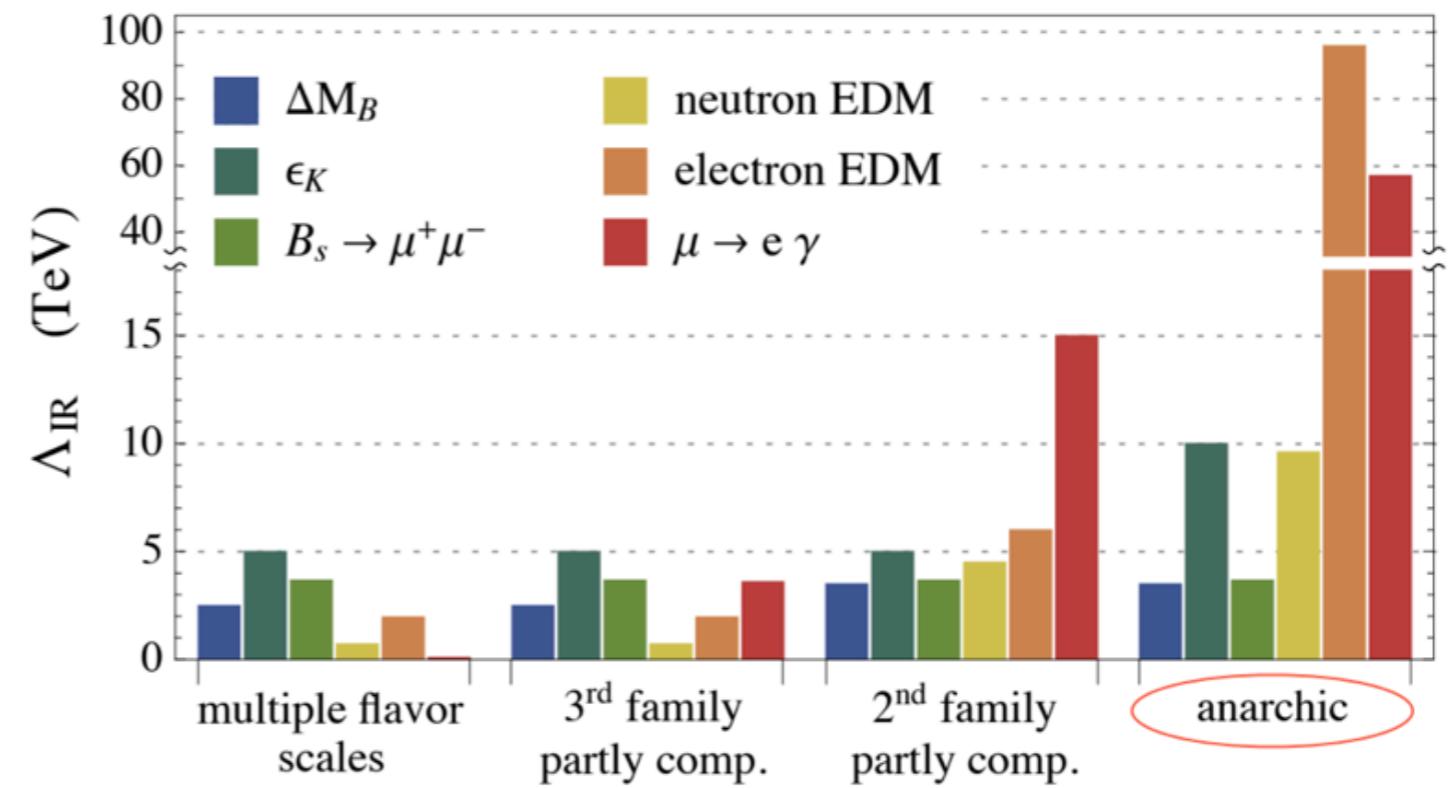
Warped 5D geometry (RS): $ds^2 = e^{-2ky} \eta_{\mu\nu} dx^\mu dx^\nu - dy^2$

- ▶ Justification of the Yukawa hierarchies through exponentiation + flavor anarchy
- ▶ Analogous to anarchic partial compositeness in composite models



Dangerous dipoles (among others)
generated at the IR scale

$$\sim \frac{g_*^2}{16\pi^2} \frac{m_e}{\Lambda_{\text{IR}}^2} \bar{e}_L \sigma_{\mu\nu} e_R F^{\mu\nu}$$

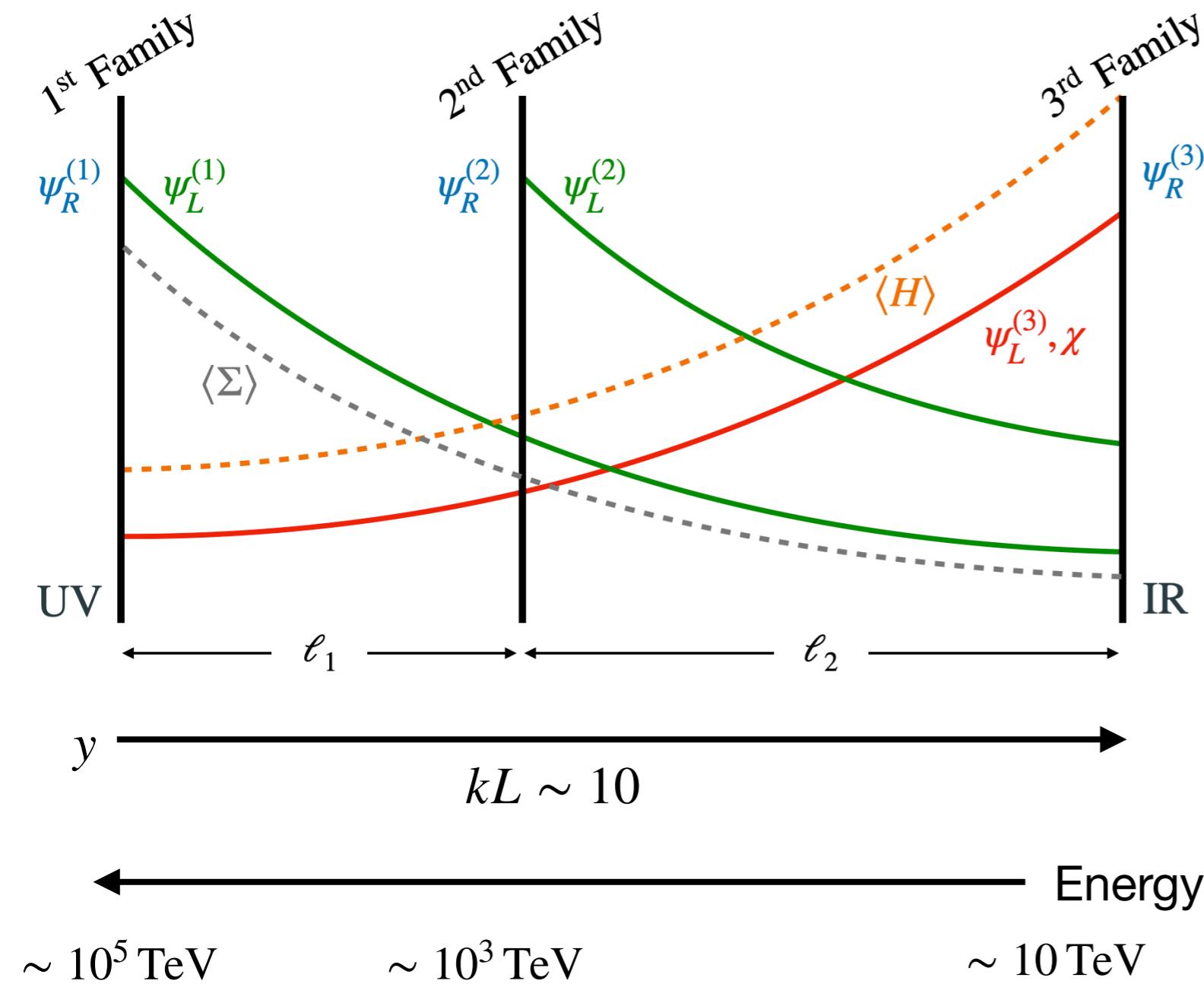


[Panico, Pomarol, [1603.06609](#)]

A 5D UV completion of 4321

[JF, Isidori, Pagès, Stefanek, [2012.10492](#)
 JF, Isidori, Lizana, Selimovic, Stefanek, [2203.01952](#)]

Attempt to construct a [full theory of flavor](#) by embedding the 4321 group in a compact warped extra dimension ([AdS₅](#)) with multiple four-dimensional branes



Flavor \longleftrightarrow fermion (quasi-)localization
 in each of the branes
 [Dvali, Shifman, '00; Panico, Pomarol, [1603.06609](#)]

$$y_{ij} \approx y_t e^{-k(L-\ell_j)} e^{-k(c_i - 1/2)(y_i - \ell_j)}$$

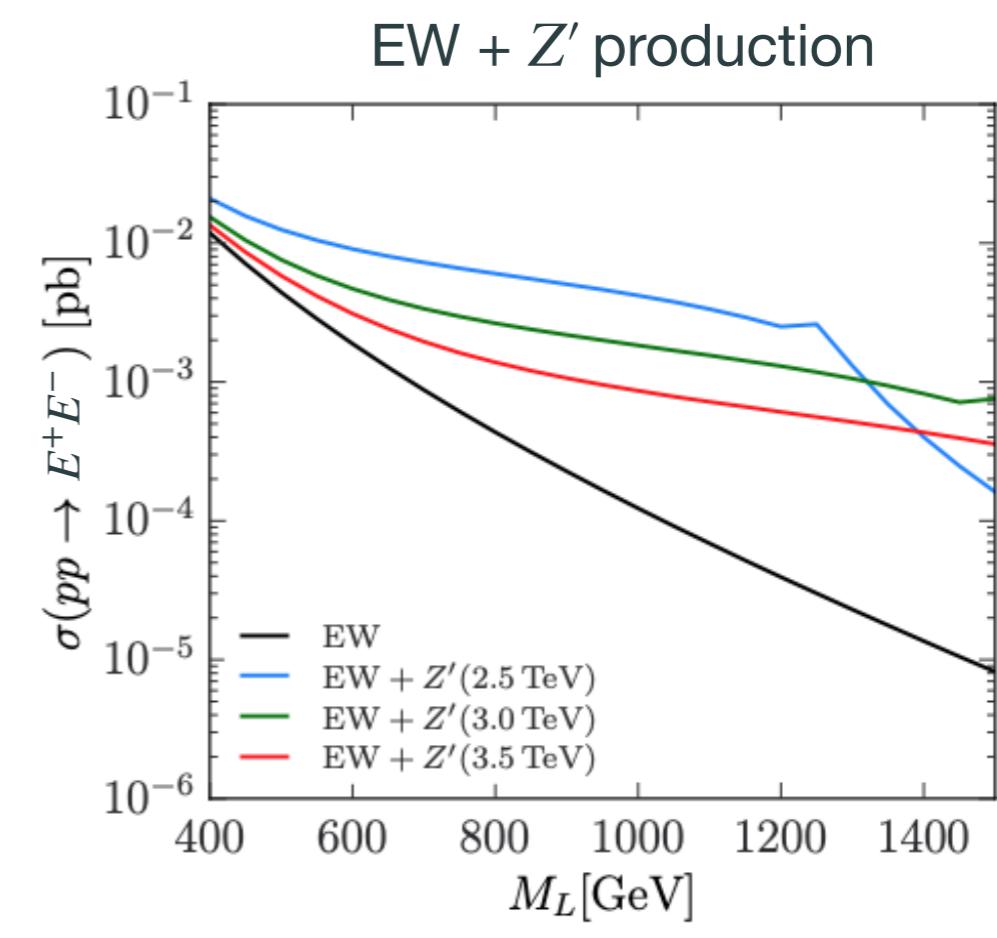
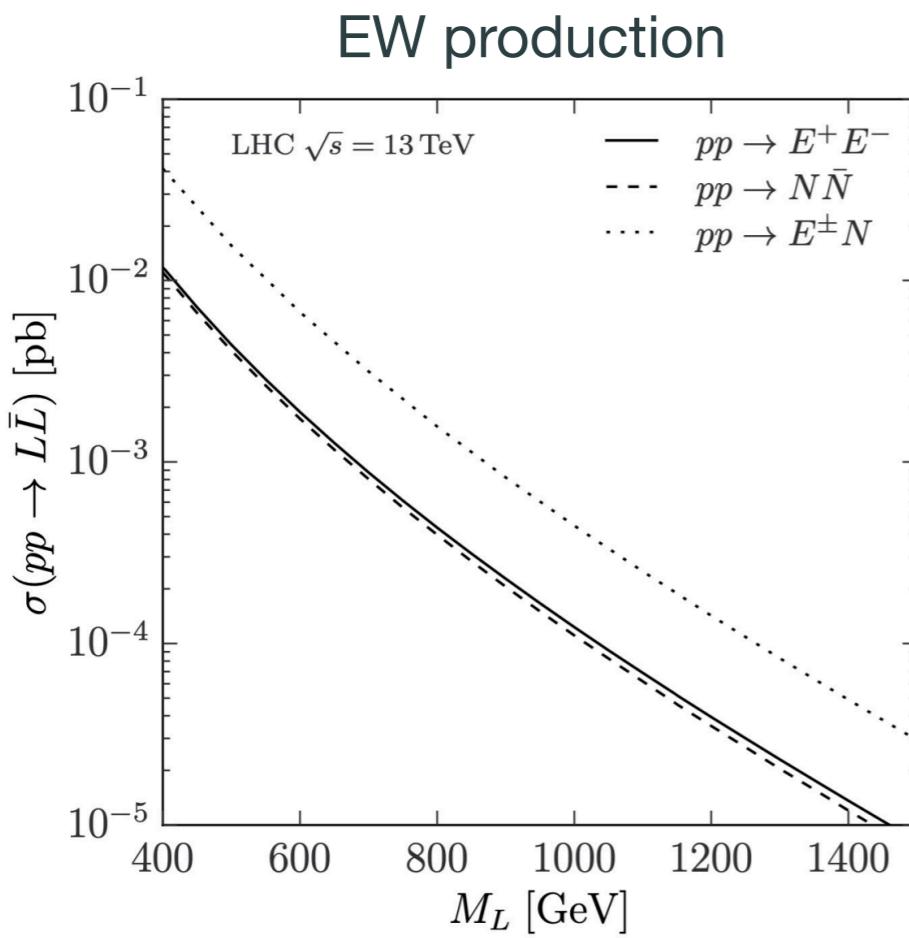
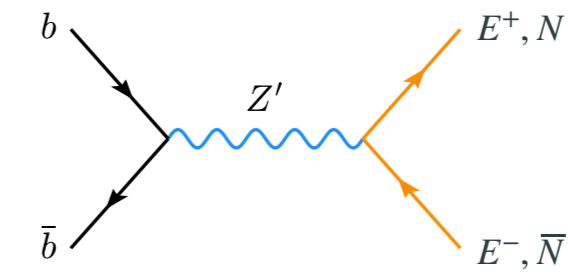
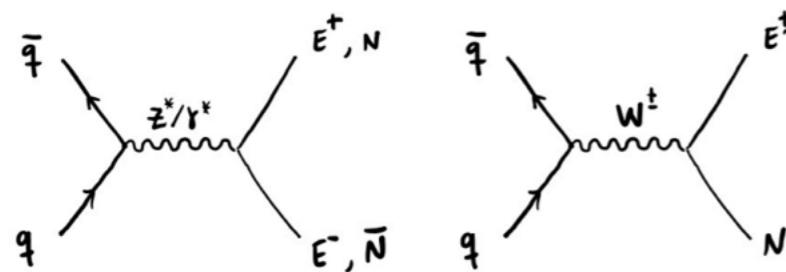
Same dynamics that breaks 4321
 also generates a pNGB Higgs \longleftrightarrow
 stabilization of the EW hierarchy with
 an $\mathcal{O}(0.1\%)$ tuning (little hierarchy)

Anarchic neutrino masses via
 inverse see-saw mechanism

Hunting 4321 vectorlike fermions at high- p_T

New search for pair produced heavy lepton doublet decaying into 3rd generation fermions

[K. Cormier, Darius Faroughy, JFM, V. Mikuni, w.i.p]



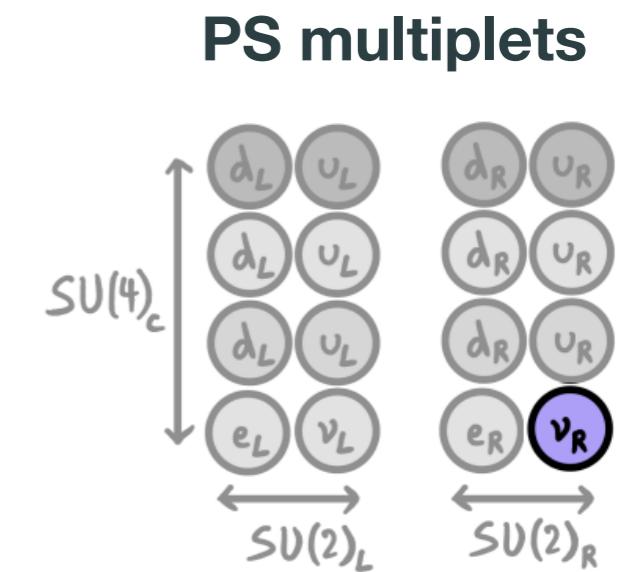
Third-family quark-lepton unification at the TeV scale

In first approximation, third-family quark-lepton unification implies

$$y_\tau = y_b \quad \checkmark$$

$$[y_\tau = 0.8 y_b \text{ at 2 TeV}]$$

$$y_{\nu_\tau} = y_t$$



TeV-scale unification limits Majorana mass for ν_R to $m_{\nu_R} \lesssim \text{TeV}$

Type-I see-saw: $m_\nu \approx \frac{m_D^2}{m_{\nu_R}} \sim 10 \text{ GeV} \quad \times$

$$m_D \equiv y_\nu v / \sqrt{2}$$

Solution: Inverse seesaw via new fermion singlets S_L^i with hierarchical Majorana masses μ^i

[Greljo, Stefanek, [1802.04274](#)
Fileviez, Wise, [1307.6213](#)]

$$m_\nu \approx m_D m_R^{-1} \mu (m_R^{-1})^\intercal m_D^\intercal$$



$$\mu^i \sim (10^7, 10^{-1}, 10^{-9}) \text{ GeV}$$

$$m_D^i \approx m_u^i \sim (10^{-2}, 1, 10^2) \text{ GeV}$$

Third-family quark-lepton unification at the TeV scale

Model prediction: mixing between active neutrino and pseudo-Dirac heavy neutral leptons yields

PMNS unitarity violation

with the expected pattern:

$$\eta \equiv |1 - NN^\dagger| \sim \left| \frac{m_D^3}{m_R^3} \right|^2 \begin{pmatrix} \epsilon_L^4 & \epsilon_L^3 & \epsilon_L^2 \\ \epsilon_L^3 & \epsilon_L^2 & \epsilon_L \\ \epsilon_L^2 & \epsilon_L & 1 \end{pmatrix} \quad \epsilon_L \approx 0.1$$

First sign of violation in 33 entry:

$$\eta_{33} \approx \left| \frac{m_D^3}{m_R^3} \right|^2 \sim \left| \frac{100 \text{ GeV}}{2 \text{ TeV}} \right|^2 = 2.5 \times 10^{-3}$$

$$\eta_{33}^{\text{exp}} < 5.3 \times 10^{-3} \quad (90\% \text{ C.L.})$$

[Antusch, Fischer, [1407.6607](#)]