# Lamb shift in muonic hydrogen

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OIL SPILLS There's more to come PLAGIARISM

It's worse than you think CHIMPANZEES The battle for survival

> SHRINKING THE PROTON New value from exotic atom trims radius by four per cent

NATUREJOBS Researchers for hire

ETH



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p and $d$ radii	Lamb shift in $\mu$ p, $\mu$ d	QED test, $R_{\infty}$	, lattice QC $5\sigma$ devia	CD/few-nucleon th. tion, New effects?
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 $E = \frac{R_{\infty}}{n^2}$  $V \sim 1/r$ 





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## The leading proton finite size contribution



Maxwell equation:  $\nabla E = 4\pi\rho$ 

$$V = \begin{cases} -\frac{Z\alpha}{2r_{\rm p}} \left(3 - \left(\frac{r}{r_{\rm p}}\right)^2\right) & (r < r_{\rm p}) \\ -\frac{Z\alpha}{r} & (r > r_{\rm p}) \end{cases}$$

$$\Delta V = \begin{cases} -\frac{Ze^2}{2r_{\rm p}} \left(3 - \left(\frac{r}{r_{\rm p}}\right)^2 - \frac{2r_{\rm p}}{r}\right) \\ 0 \end{cases}$$
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• Electron-proton scattering (1963, ... 2010)

 $ightarrow r_{
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- Hydrogen spectroscopy (1989, ...)
  - very precise measurements:  $d\nu/\nu = 1 \times 10^{-14}$  (1S-2S)
  - interpretation of the measurements need  $r_{\rm p}$
  - conversely assuming correctness of bound-state QED  $ightarrow r_{
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- Muonic hydrogen spectroscopy (2009 ...)

 $m_{\mu}/m_e \approx 200 \rightarrow \mu^-$  "orbit" is 200 times smaller than e<sup>-</sup> "orbit"  $\rightarrow$  large finite size effect  $\rightarrow r_p$  with  $u_r = 0.1\%$ 





$$\frac{|\Psi_{\mu}(0)|^2}{|\Psi_e(0)|^2} = \left(\frac{m_{\mu}}{m_e}\right)^3 \approx 10^7$$



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Muonic hydrogen









## Aim of the experiment

• Measure the 2S - 2P energy difference (Lamb shift) in  $\mu$ p  $\Delta E(2S - 2P) = 209.978(5) - 5.226 r_p^2 + 0.0347 r_p^3$  meV with 30 ppm precision.

- Extract  $r_p$  with  $u_r \approx 10^{-3}$  (rel. accuracy)
  - → bound-state QED test in hydrogen to a level of  $u_r \approx 3 \times 10^{-7}$  (10× better)
  - $\rightarrow$  improve Rydberg constant ( $R_{\infty} = mc\alpha^2/2h$ ) to a level of  $u_r \approx 1 \times 10^{-12}$  (6× better)
  - $\rightarrow$  benchmark for lattice QCD calculations
  - $\rightarrow$  confront with electron scattering results





## **Principle of the experiment**

- $\mu^-$  are produced with the PSI accelerator (p $\rightarrow \pi^- \rightarrow \mu^-$ )
- $\mu^-$  stop in a 1 mbar hydrogen target whereby muonic hydrogen is formed
- $\bullet$  Before stopping, the  $\mu^-$  trigger the laser system
- $\bullet$  The laser pulse excites the 2S-2P transition
- 2 keV X-ray are detected as a signature of the laser-induced transition

 $\mu p$  formation



1%: long-lived  $\mu p(2S)$ with 1  $\mu$ s lifetime (@ 1 mbar)





Laser at  $\lambda \approx 6 \,\mu$ m Signature: 2 keV X-ray A. Antognini, CERN 10.08.2010 – p.8

 $\mu$ p spectroscopy

#### **Principle of the experiment**



#### **Principle of the experiment**





- Low energy muon beam line at PSI
- Laser system
- Detectors and DAQ

#### The experimental hall at PSI



## 5 keV energy muon beam line



- $\bullet$  Production of 20-50 keV  $\mu^-$ 
  - $10^8 \ \pi^-$  injected in CT
  - $\pi^-$  decay in MeV  $\mu^-$
  - $\mu^-$  decel. to 20-50 keV by crossing the foil
- Extraction of  $\mu^{-}$  from CT  $\frac{T_{\parallel}(0)}{T_{\perp}(0)} < \left(\frac{B_{\max}}{B_{0}} - 1\right) - \frac{qV}{T_{\perp}(0)}$
- Momentum selection
  - toroidal magnetic field
     → vertical drift
  - eliminate  $e^- \mbox{ and } n \mbox{ bg}$
- $\mu^-$  detection
- $\mu p$  formation and laser exp. A. Antognini, CERN 10.08.2010 – p.12
#### **Inside the 5 Tesla solenoid**

5 keV  $\mu^-$ , 400 s<sup>-1</sup> with stop vol. in 1 hPa H<sub>2</sub> gas of  $5 \times 15 \times 190$  mm<sup>3</sup>

- Stacks of C foils are used as non-destructive muon detector
  - $\mu^-$  loses few keV energy per foil
  - secondary electrons are emitted
  - ExB velocity dependent drift
- Laser is triggered by the electrons signals from the C stacks (coincidence with TOF)
- $\bullet~\mu^-$  enter in 1 hPa hydrogen wherby  $\mu p$  is formed



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A. Antognini, CERN



#### **Animation of the experiment**



(T.W. Hänsch)



## The laser system



#### **Impressions from the laser hut**



#### **Disk laser oscillators**



#### **Disk amplifier laser heads**



## **Disk laser doubling stages**



#### Measurements





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Laser frequency known with 300 MHz uncertainty





Systematics: 300 MHz Statistics: 700 MHz

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#### ... and the time spectrum



Time-spectrum fit around laser time  $\Rightarrow$  Extract precise bgr. value



## **Proton radius from** $\mu p$ **Lamb shift**

• Measurement (no theory input needed):

$$\nu(2S_{1/2}^{F=1} - 2P_{3/2}^{F=2}) = 49881.88(76) \text{ GHz}$$

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$$\begin{split} L^{\text{exp.}} &= 206.2949(32) \text{ meV} \\ L^{\text{th.}} &= 209.9779(49) - 5.2262 \, r_{\text{p}}^2 + 0.0347 \, r_{\text{p}}^3 \text{ meV} \end{split} \right\} \Rightarrow \boxed{r_{\text{p}} = 0.84184(36)^{\text{exp}}(56)^{\text{th}} \text{ fm}} \\ & u_r^{\text{exp}} = 4.3 \times 10^{-4} \\ & u_r^{\text{th}} = 6.7 \times 10^{-4} \end{split}$$

$$r_{\rm p} = 0.84184(67) \; {\rm fm} \qquad u_r^{\rm th} = 8 \times 10^{-4}$$

Pohl et al., Nature **466**, issue 7303, 213-216 (2010)



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CODATA 2006:  $r_{\rm p} = (0.8768 \pm 0.0069)$  fm, from H e-p scattering:  $r_{\rm p} = (0.895 \pm 0.018)$  fm (2%)

 $3.0\sigma$  from e-p scatt.  $5.0\sigma$  from CODATA  $r_{\rm p}$  4% smaller

## What may be wrong?



# What may be wrong?



#### $\mu$ p experiment wrong?

- Frequency mistake by 75 GHz  $\Leftrightarrow u_r = 0.15\%$ ? (Linewidth =20 GHz) (in spectroscopy people measure frequency with  $u_r \sim 10^{-14}$  and Hz precison)
- Two consistent ways to calibrate the frequency of the laser:
  - 1) at 6  $\mu m$  with  $H_2O$  lines (20 measurements of 5 different lines )
  - 2) at 708 nm with lambdameter, wavemeter and FP calibated to  $I_2$ , Rb, Cs lines:

 $\nu^{6\mu m} = \nu^{708nm} - 3 \cdot \hbar \omega_{\rm vib}$ 

- Zeeman + AC/DC Stark + pressure shift  $\cdots < 50 \text{ MHz} (\sim 1/m)$ 



## What may be wrong?



#### $\mu p$ theory wrong?

Discrepancy=0.31 meV Th. uncertainty=0.005 meV  $\implies 60\delta$ (theory) deviation

#	Contribution	Value	Unc.
3	Relativistic one loop VP	205.0282	
4	NR two-loop electron VP	1.5081	
5	Polarization insertion in two Coulomb lines	0.1509	
6	NR three-loop electron VP	0.00529	
7	Polarisation insertion in two and three Coulomb lines (corrected)	0.00223	
8	Three-loop VP (total, uncorrected)		
9	Wichmann-Kroll	-0.00103	
10	Light by light electron loop ((Virtual Delbrück)	0.00135	0.00135
11	Radiative photon and electron polarization in the Coulomb line $lpha^2(Zlpha)^4$	-0.00500	0.0010
12	Electron loop in the radiative photon of order $lpha^2(Zlpha)^4$	-0.00150	
13	Mixed electron and muon loops	0.00007	
14	Hadronic polarization $lpha(Zlpha)^4m_r$	0.01077	0.00038
15	Hadronic polarization $\alpha (Z\alpha)^5 m_r$	0.000047	
16	Hadronic polarization in the radiative photon $lpha^2 (Zlpha)^4 m_r$	-0.000015	
17	Recoil contribution	0.05750	
18	Recoil finite size	0.01300	0.001
19	Recoil correction to VP	-0.00410	
20	Radiative corrections of order $\alpha^n (Z\alpha)^k m_r$	-0.66770	
21	Muon Lamb shift 4th order	-0.00169	
22	Recoil corrections of order $\alpha (Z\alpha)^5 \frac{m}{M} m_r$	-0.04497	
23	Recoil of order $\alpha^6$	0.00030	
24	Radiative recoil corrections of order $\alpha(Z\alpha)^n \frac{m}{M}m_r$	-0.00960	
25	Nuclear structure correction of order $(Z\alpha)^5$ (Proton polarizability)	0.015	0.004
26	Polarization operator induced correction to nuclear polarizability $lpha(Zlpha)^5 m_r$	0.00019	
27	Radiative photon induced correction to nuclear polarizability $lpha(Zlpha)^5m_r$	-0.00001	
	Sum	206.0573	0.0045



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 $e^{-}$   $e^{+}$ 

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11	Radiative photon and electron polarization in the Coulomb line $lpha^2(Zlpha)^4$	-0.00500	0.0010	
12	Electron loop in the radiative photon of order $\alpha^2 (Z\alpha)^4$	-0.00150		333
13	Mixed electron and muon loops	0.00007		
14	Hadronic polarization $\alpha (Z\alpha)^4 m_r$	0.01077	0.00038	
15	Hadronic polarization $\alpha (Z\alpha)^5 m_r$	0.000047		
16	Hadronic polarization in the radiative photon $lpha^2 (Zlpha)^4 m_r$	-0.000015		~~~~ <u>~</u> ~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~
17	Recoil contribution	0.05750		$\overline{\langle \cdot \rangle}$
18	Recoil finite size	0.01300	0.001	μ <sup>+</sup> γ μ <sup>+</sup> γ
19	Recoil correction to VP	-0.00410		<u> </u>
20	Radiative corrections of order $\alpha^n (Z\alpha)^k m_r$	-0.66770		
21	Muon Lamb shift 4th order	-0.00169		$\mu^+ \overleftarrow{\mu^-} e^+ \overleftarrow{e^-}$
22	Recoil corrections of order $\alpha (Z\alpha)^5 \frac{m}{M} m_r$	-0.04497		$e^+ \bigcirc e^-$
23	Recoil of order $\alpha^6$	0.00030		<u> </u>
24	Radiative recoil corrections of order $\alpha (Z\alpha)^n \frac{m}{M} m_r$	-0.00960		
25	Nuclear structure correction of order $(Z\alpha)^5$ (Proton polarizability)	0.015	0.004	ىمى
26	Polarization operator induced correction to nuclear polarizability $lpha (Zlpha)^5 m_r$	0.00019		$\frac{2}{2}$
27	Radiative photon induced correction to nuclear polarizability $lpha(Zlpha)^5 m_r$	-0.00001		e +
	Sum	206.0573	0.0045	<u> </u>



#	Contribution	Value	Unc.	
3	Relativistic one loop VP	205.0282		
4	NR two-loop electron VP	1.5081		
5	Polarization insertion in two Coulomb lines	0.1509		
6	NR three-loop electron VP	0.00529		
7	Polarisation insertion in two and three Coulomb lines (corrected)	0.00223		
8	Three-loop VP (total, uncorrected)			
9	Wichmann-Kroll	-0.00103		
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26	Polarization operator induced correction to nuclear polarizability $lpha(Zlpha)^5m_r$	0.00019		
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23	Recoil of order $\alpha^6$	0.00030	22	-
24	Radiative recoil corrections of order $\alpha(Z\alpha)^n \frac{m}{M} m_r$	-0.00960	55	
25	Nuclear structure correction of order $(Z\alpha)^5$ (Proton polarizability)	0.015	0.004	
26	Polarization operator induced correction to nuclear polarizability $lpha(Zlpha)^5 m_r$	0.00019		
27	Radiative photon induced correction to nuclear polarizability $lpha(Zlpha)^5 m_r$	-0.00001		
	Sum	$2\overline{06.0573}$	0.0045	



# Lamb shift prediction

radius dependent contributions

Contribution Value		
Leading nuclear size contribution	-5.19745	$< r_{\rm p}^2 >$
Radiative corrections to nuclear finite size effect	-0.0275	$< r_{\rm p}^2 >$
Nuclear size correction of order $(Z\alpha)^6 < r_{ m p}^2 >$	-0.001243	$< r_{\rm p}^2 >$
Total $< r_{\rm p}^2 >$ contribution	-5.22619	$< r_{\rm p}^2 >$
Nuclear size correction of order $(Z\alpha)^5$	0.0347	$< r_{\rm p}^{3} >$
Nuclear size correction of order $(Z\alpha)^6 < r_{\rm p}^4 >$	-0.000043	$< r_{\rm p}^2 >^2$



• A1 collaboration at MAMI, Mainz has started the reevaluation of the various proton moments:  $< r_{\rm p}^2 >$ ,  $R_{\rm Zemach}$ ,  $< r_{\rm p}^4 > \dots$ 



New evaluations of structure leads to a shift < 10% of the measured discrepancy.

 $E(2S_{1/2}^{F=1} - 2P_{3/2}^{F=2}) = 209.9779(49) - 5.2262 r_{\rm p}^2 + 0.0347 r_{\rm p}^3 \,\mathrm{meV}$  (HFS+FS included)



 $\mu p$  theory wrong?

Discrepancy=0.31 meV Th. uncertainty=0.005 meV  $\implies 60\delta$ (theory) deviation

#### Main contributions to the $\mu p$ Lamb shift







H experiments wrong?

H theory wrong?







#### Are H experiments wrong?

$$L_{1S}^{\rm th}(r_{\rm p}^{\mu p}) - L_{1S}^{\rm exp} = 96(19)(4)(2) \text{ kHz}$$
$$\delta L^{\rm exp} \quad \delta L^{\rm QED} \quad \delta L^{r_{\rm p}} \qquad \delta L^{\rm exp} = \delta L^{R_{\infty}}$$

 $L_{1S}^{exp}$  extracted from 1S - 2S and 2S - 8/12S transition

- 1S 2S has to be corrected by thousands of  $\sigma$  to explain the discrepancy
- 2S 8/12S has to be corrected by  $5\sigma$  to explain the discrepancy  $d\nu/\nu = 1 \times 10^{-11} \sim 1/100 \ \Gamma$  (systematics  $\sim n^3$ )



#### **Free and bound-state QED**

#### • Free QED

 $g-2 \rightarrow$  electron anomaly: test of QED, determination of  $\alpha$ , NP

$$a_e = C_2 \left(\frac{\alpha}{\pi}\right) + C_4 \left(\frac{\alpha}{\pi}\right)^2 + C_6 \left(\frac{\alpha}{\pi}\right)^3 + C_8 \left(\frac{\alpha}{\pi}\right)^4 + C_{10} \left(\frac{\alpha}{\pi}\right)^5 + \Delta(\text{had., NP})$$

#### • Bound-state QED in Hydrogen

- Binding effects ( $Z\alpha$ ) bad convergence, all-order approach/expansion
- Radiative corrections ( $\alpha$  and  $Z\alpha$ )
- Recoil corrections (m/M and  $Z\alpha$ ) relativity  $\Leftrightarrow$  two-body system
- Radiative-recoil corrections ( $\alpha$ , m/M and  $Z\alpha$ )
- Proton structure corrections ( $r_{\rm p}$ ,  $r_{\rm Zemach}$  and  $Z\alpha$ )

## **Critical contributions in hydrogen**



 $\Delta E_{SE}^{(2)} = m \left(\frac{\alpha}{\pi}\right)^2 \frac{(Z\alpha)^4}{n^3} G_n(Z\alpha) \qquad B_{60} = -86(15), \ G_{60}^{h.o.} = -101(15) \text{ Yerokin (2009)}$   $G_n = B_{40} + (Z\alpha)B_{50} + (Z\alpha)^2 \left[B_{63}\ln^3(Z\alpha)^{-2} + B_{62}\ln^2(Z\alpha)^{-2} + B_{61}\ln(Z\alpha)^{-2} + G_{h.o}\right] + \cdots$   $G_n = 1.409 - 0.177 + \left[-0.015 - 0.003 + 0.026 - 0.003 + \cdots\right] + \cdots$ 

Bad convergence of the  $(Z\alpha)$  expansion



## Is the theory in hydrogen wrong?

- The critical terms are coming from two-loop contributions
- The difference between all-order and expansion approaches shifts the  $L_{1S}$  by 7 kHz
- Higher order remainder for the two-loop self-energy  $G^{h.o}(Z = 1) < 15 \text{ kHz}$

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• Compare these th. uncertainties with:  $L_{1S}^{exp} - L_{1S}^{th}(r_p^{\mu p})$ =96 kHz

The theory should be corrected by  $25 \times \delta(\text{theory})$  to bring the value of  $r_{\rm p}$  extracted from H-spectroscopy in agreement with our value





The origin of the discrepancy?

- QED th. in  $\mu$ p: 60  $\delta$ (theory)
- QED th. in H: 25  $\delta$ (theory)
- $R_{\infty}$ : 5  $\sigma$
- QED term(s) missing?

- Consistent use of  $r_{\rm p}$  definition?
- Something fundametally wrong with bound-state QED? In muonic sector?
- New effects or new physics? In muonic sector? In proton sector?

A. Antognini, CERN 10.08.2010 – p.37

- Bernauer et al. arXiv:1007.5076v2 (2010)

- Mohr at al., Rev. Mod. Phys. 80 633 (2008)

- Wang et al., Phys. Rev. D 79 094001 (2009)

- Sick, Phys. Lett. B 576 62 (2003)

- Belushkin et al., Phys. Rev. C 75 035202 (2007)


• Pressure shift?

- pressure shift of H(1S-2S) transition in H $_2$  gas  $\sim 10$  MHz/mbar
- $\mu p$  is  $m_e/m_\mu$  smaller (stronger E-fields). less disturbed by external fields
  - smaller state mixing

MC simulations give a pressure shift of 1 MHz for 1 mbar

• Molecular formations leading to line shift?

 $\mu p(2S) + H_2 \rightarrow \{ [(pp\mu)^+]^* pee \}^* \rightarrow \mu p(1S) + \dots$ 

- If a molecule is formed there is immediate Auger emission followed by

a deexcitation to the ground state.

Fitted linewidth corresponds to theoretically expected, and discrepancy= $5\Gamma$ 



- Pressure shift? Shift of 1 MHz.
- Molecular formations leading to line shift? No because of fast  $2S \rightarrow 1S$  deexcitation.



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  - Dipole and Gauss models of proton shift the energy by < 500 MHz.
  - Fast convergence of the expansion:-5.19745<  $r_{\rm p}^2$  >, -0.000043<  $r_{\rm p}^2$  ><sup>2</sup>.



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- Dark photons? Vector Bosons with few MeV mass? [Maxim Pospelov]... From simple atoms there are constraints on light bosons with ultraweak coupling Mass from 1 eV to 1 keV:  $\alpha_{spin-ind} = 10^{-13}$ ,  $\alpha_{spin-dep} = 10^{-17}$  [PRL 104,220406 (2010)]



#### Other measurements

 $\mu p (2S_{1/2}(F=0) \rightarrow 2P_{3/2}(F=1)) at \lambda = 5.5 \mu m$ 



 $\mu d ( 2S_{1/2}(F=3/2) \rightarrow 2P_{3/2}(F=5/2) )$ 



• $\sigma_{\text{position}} = 880 \text{ MHz} \iff 17 \text{ ppm}$  ( $\Gamma = 19 \text{ GHz}$ )

• Position does not fit with prediction:  $3.5\sigma$  deviation

Extract  $r_{\rm d}$  and d. pol.

 $\mu d (2S_{1/2}(F=1/2) \rightarrow 2P_{3/2}(F=3/2 \text{ and } 1/2))$ 



• $\sigma_{\text{position}} = 2.2 \text{ GHz} \iff 43 \text{ ppm}$  ( $\Gamma = 19 \text{ GHz}$ )

- $\bullet$  Relative pos. fit to each others but not with the first  $\mu d$  line
- Background well know from previous  $\mu d$  line

# The role of nuclear physics in atomic physics

Atomic physics means high-precison measurements. However their interpertations are usually limited by nuclear-physics effects

Interpertation of H, D,  $^{3,4}$ He<sup>+</sup>,  $\mu$ p,  $\mu$ d,  $\mu^{3,4}$ He<sup>+</sup>:



Bound-stated QED is important and interesting:

- Bindings effects and two-body problem (no exact solution)
- QED is essential to extract nucl. parameters from atomic meas. (or bound systems)





## Isotope shift, $r_{\rm d}$ and deuteron pol.







A. Antognini, CERN 10.08.2010 – p.46

# **Summary & outlook**

 $\bullet$  We have measured 5 transitions in  $\mu p$  and  $\mu d$  with 20 ppm accuracy



- When (and if) discrepancy is solved:
  - $r_{\rm p}$ ,  $r_{\rm d}$  determination (10× better)
  - $r_{\rm Zemach}$  determination
  - Deuteron polarizability
  - $R_{\infty}$  determination (6× better)
  - QED test in hydrogen/deuterium and muonic hydrogen/deuterium
- New experiment:  $\mu He^+$ 
  - May illuminate discrepancy, enhance sensitivity to QED effects, few-nucleon th.

Test of proton and deuteron models: lattice QCD, few-nucleon ab initio th.

Best test of H energy levels Fundamental constants

ETH

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#### Like a Hollywood movie:

Everything goes bad till five minutes before THE END!

### **The Paul Scherrer Institute**



### Nothing can hide in hydrogen

The spectrum of hydrogen atom has proved to be the "Rosetta stone" of modern physics.

T.W. Hänsch