

Formation of a fireball, (and clustering near CP)

Edward Shuryak

Center for Nuclear Theory, Stony Brook University

How the idea of **RAPID NONLINEAR QGP** fireball formation was developing

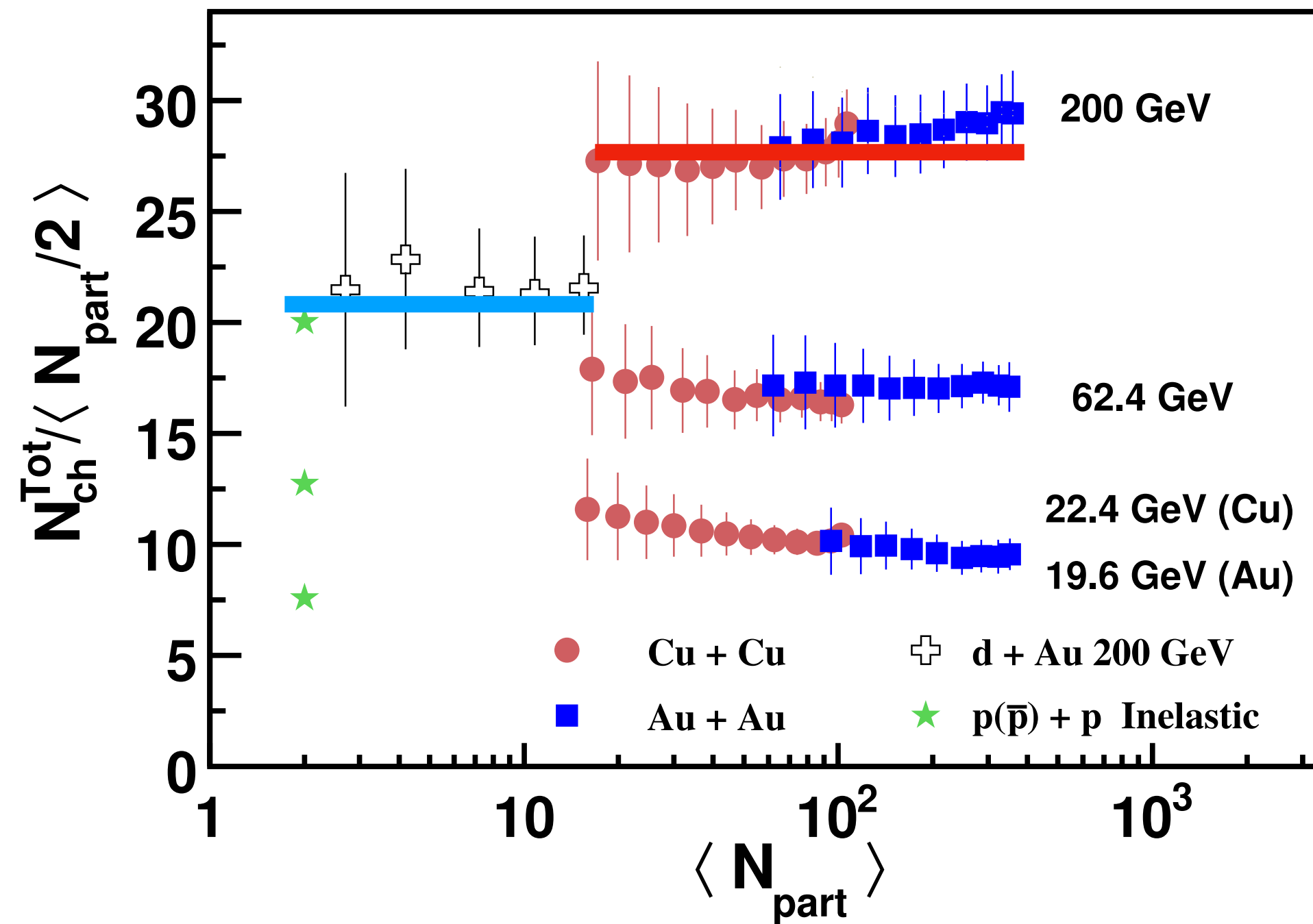
0. phenomenology of centrality dependence: multiplicity/wounded nucleons indicate an unexpected **jump between light and heavy ions**
1. The holography and use of the idea of **trapped surface** (from Gubser et al, 2008)
2. Finding trapped surface for non-central collisions (Shu Lin+ ES 2009) and discovery of **critical impact parameter**
3. deriving **string-string interaction** (Tigran Kalaydzhyan and ES, 2014)
4. **collective effects in “spaghetti”** multistring system in the transverse plane (Tigran Kalaydzhyan and ES, 2014)
5. Strings and multistrings **in holography** (Iatrakis, Ramamurti and ES, 2015)

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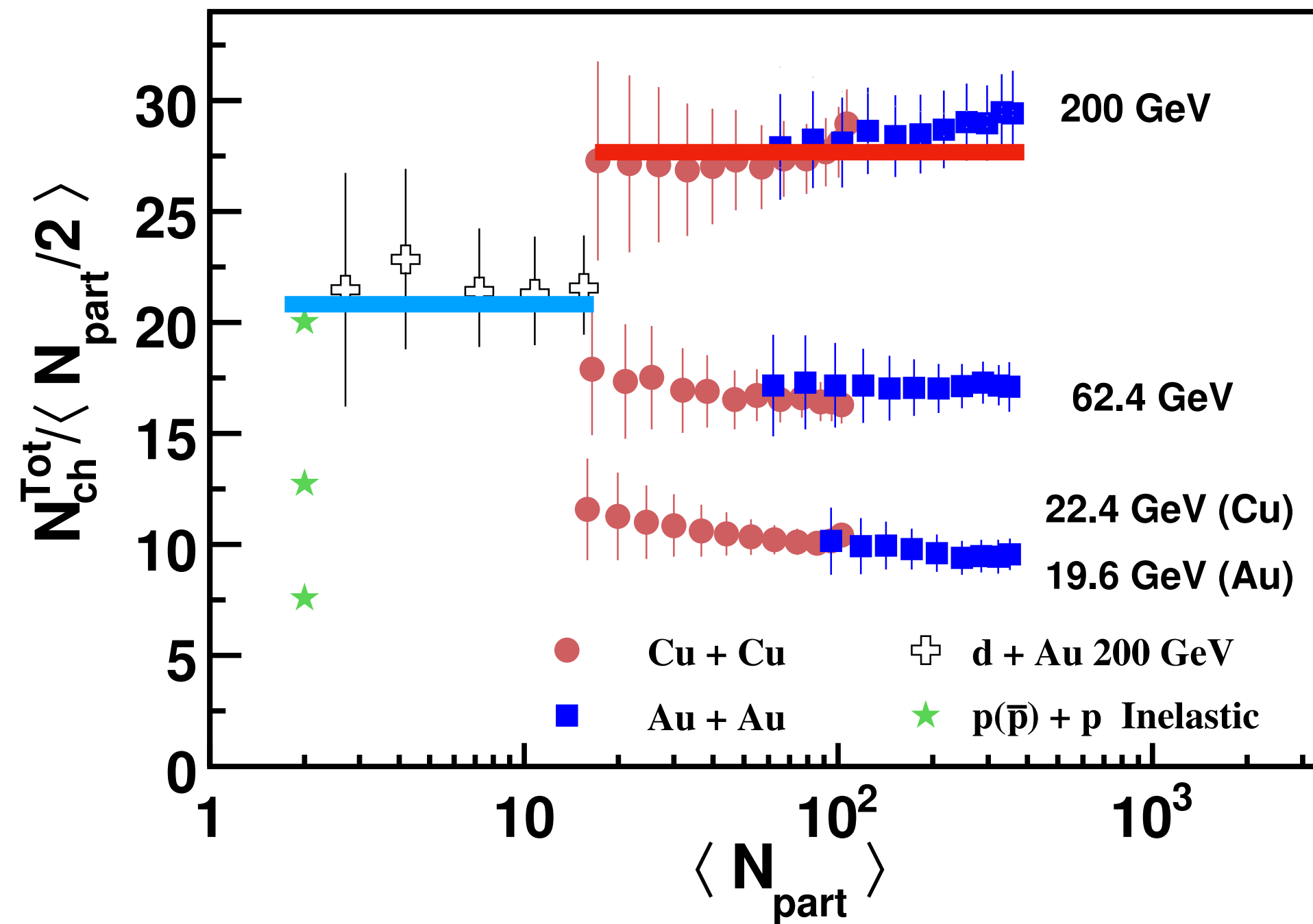
If I still have time, I will tell you what I worked on recently in connection to hypothetical critical point

To keep you interested, I start with phenomenology of light/heavy ion collisions



a 20-year old
PHOBOS data on **multiplicity per participant**
there seems to be **two** horizontal lines on this plot,
one for **light**
and one for **heavy** ions,
independent of centrality
jump at about 15 participants?

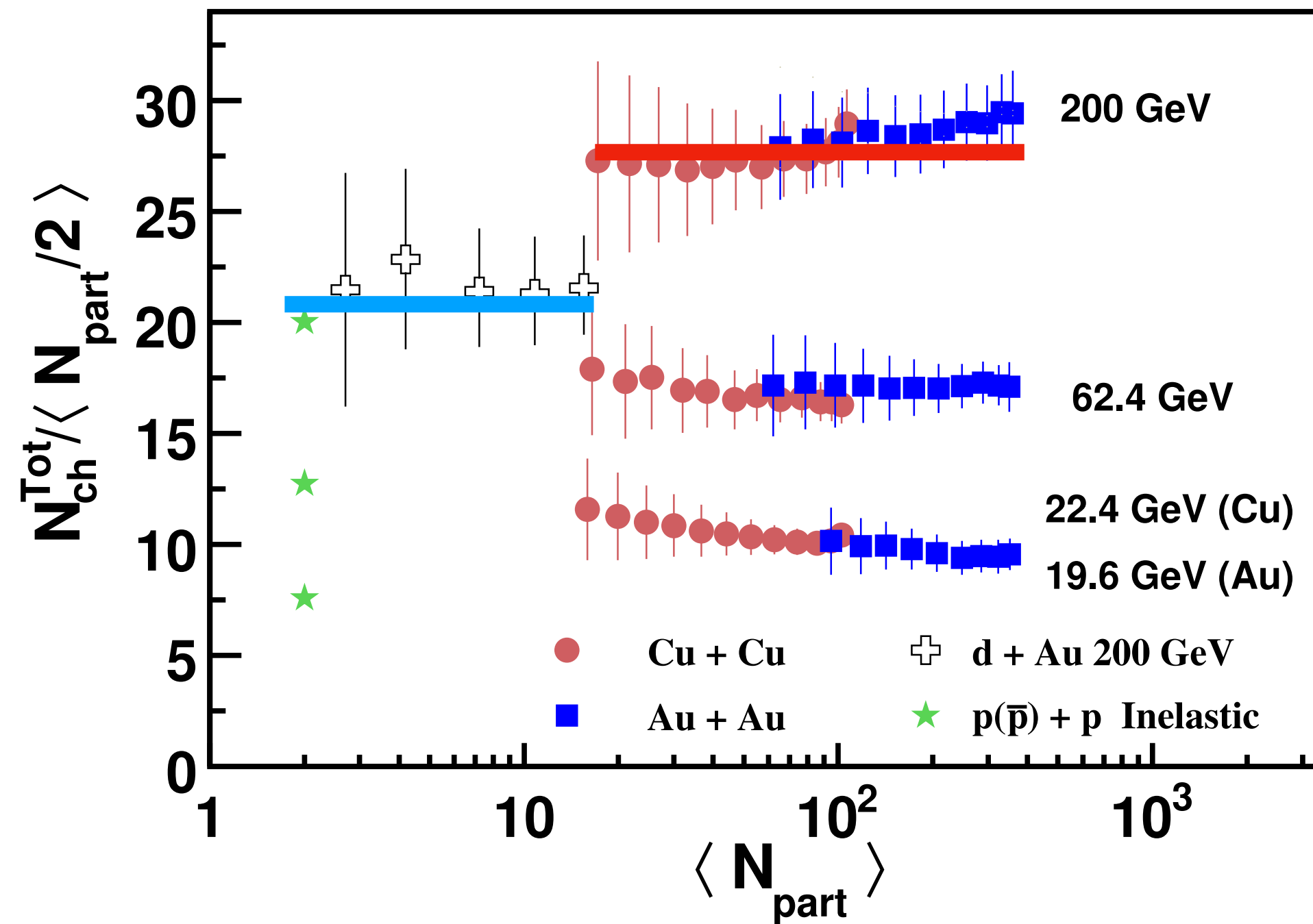
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 Is there some sharp transition between two regimes?

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Recent results from SHINE:
 central Be Be is nearly the same as pp
 but already Ar
 (atomic weight about 40)
 is already close to PbPb
 Again, a hint for rapid transition...

Entropy production in collisions of gravitational shock waves and of heavy ions

Steven S. Gubser,^{1,*} Silviu S. Pufu,^{1,†} and Amos Yarom^{2,‡}

**By that time it was clear that formation of QGP fireball
in holographic models
corresponds to formation of black hole
out of some falling objects in the “bulk”
e.g. Shu Lin and myself propose falling membrane
as a model of thermalization**



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find the “trapped surface”
technically it is a “null surface”
on which a massless particle
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If found, the entropy is given by
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it is inequality because the surface we find at time zero, and it may grow later



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Here is the setting:
 a central collision
 of two relativistic
 masses
 (black holes)
 their field is a
 gravitational
 “shock wave”

the flat surface
 is a boundary
 where we live

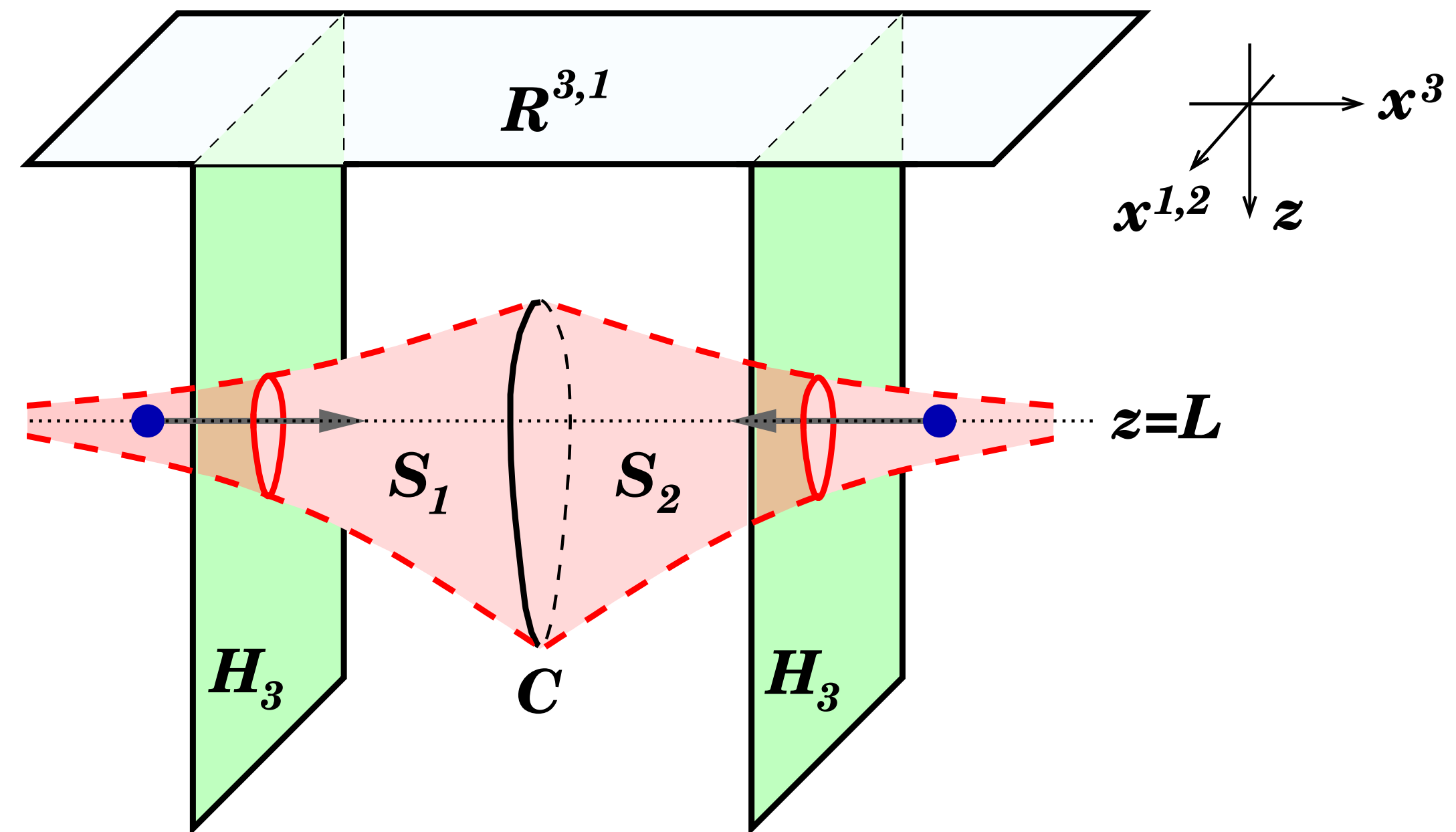


Figure 1: A projection of the marginally trapped surface that we use onto a fixed time slice of the AdS_5 geometry. The size of the trapped surface is controlled by the energy of the massless particles that generate the shock waves. These particles are shown as dark blue dots.

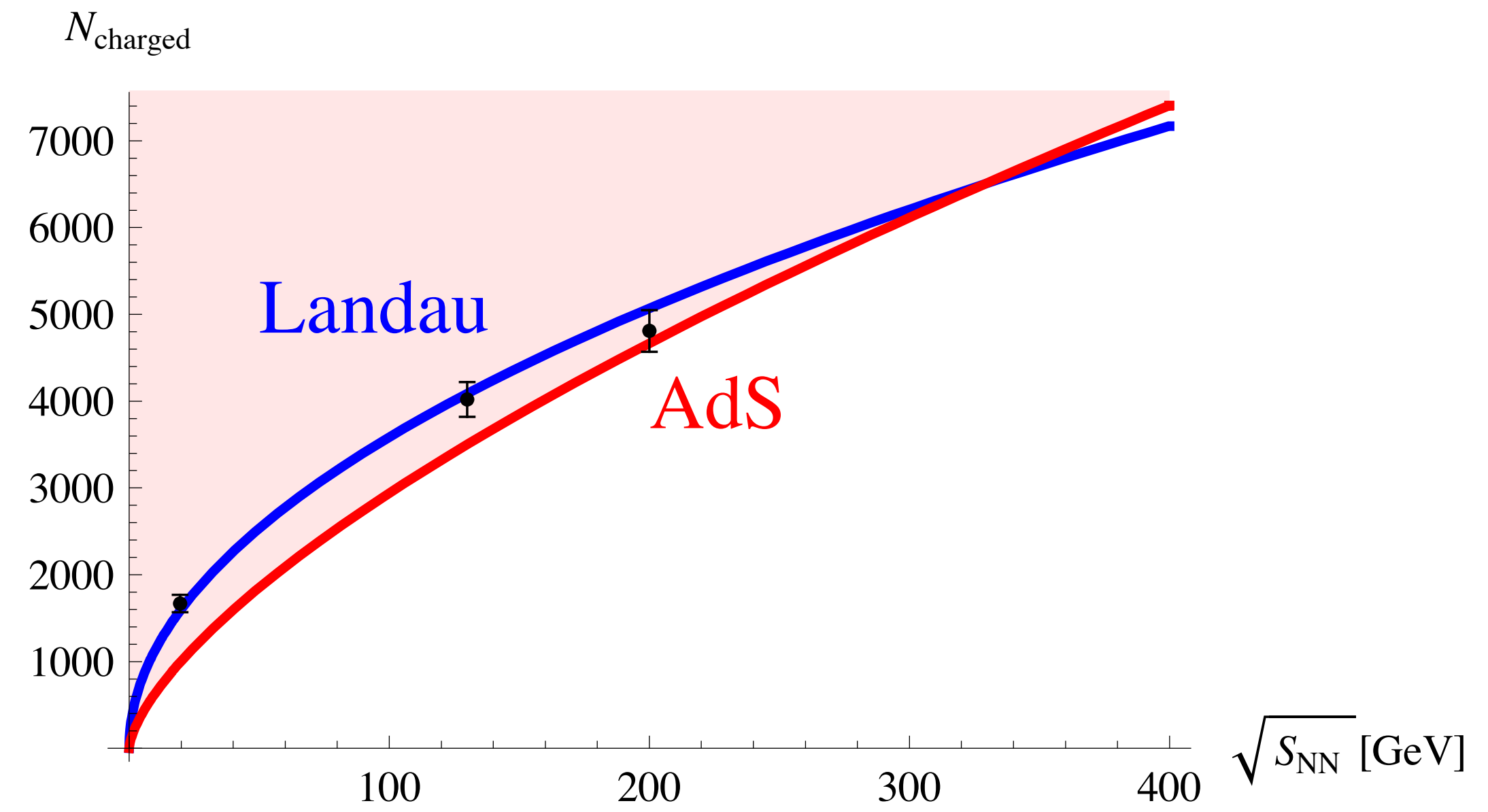
the main result:
 multiplicity should grow as
 $E(cm)^{(2/3)}$

$$S_{\text{trapped}} \approx \pi \left(\frac{L^3}{G_5} \right)^{1/3} (2EL)^{2/3} .$$

Famous Fermi-Landau initial condition
– the instant equilibration –
gives $E(\text{cm})^{1/2}$ or $s^{1/4}$
worked better for RHIC,
Gubser et al show

but the model is very schematic...

(it was before LHC)



Grazing Collisions of Gravitational Shock Waves and Entropy Production in Heavy Ion Collision

Shu Lin¹, and Edward Shuryak²

we started much more complicated project:
 nonzero impact parameter
 then trapped surface is not a sphere!
 one needs to find it from complicated eqn,
 which we turned to integral eqn and
 solved it numerically

we found that there is a
critical trapped surface
and at impact parameter
 $b > b_c$ no such surface exists!
 no black hole =
 no QGP fireball

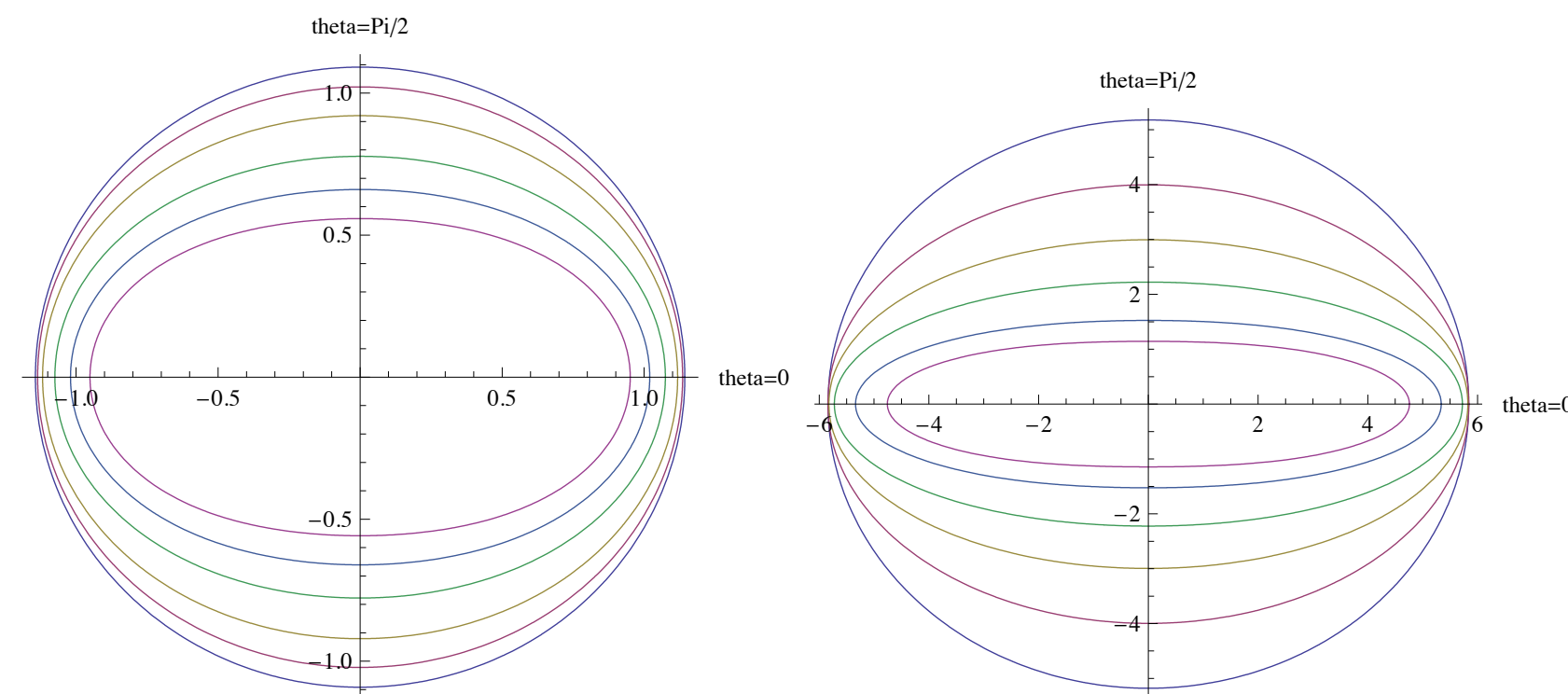


Figure 1: (left) The shapes of \mathcal{C} (the trapped surface at $u = v = 0$) at $\frac{G_5 E}{L^2} = 1$. The impact parameters used in the plot are $0.4L, 0.6L, 0.8L, 1.0L, 1.1L, 1.14L$ from the outer to the inner. The innermost shape being the critical trapped surface. (right) The shapes of \mathcal{C} (the trapped surface at $u = v = 0$) at $\frac{G_5 E}{L^2} = 100$. The impact parameters used in the plot are $1.0L, 2.0L, 3.0L, 4.0L, 5.0L, 5.3L$ from the outer to the inner. The innermost shape being the critical trapped surface. As collision energy grows, the trapped surface gets elongated in the axis of mismatch.

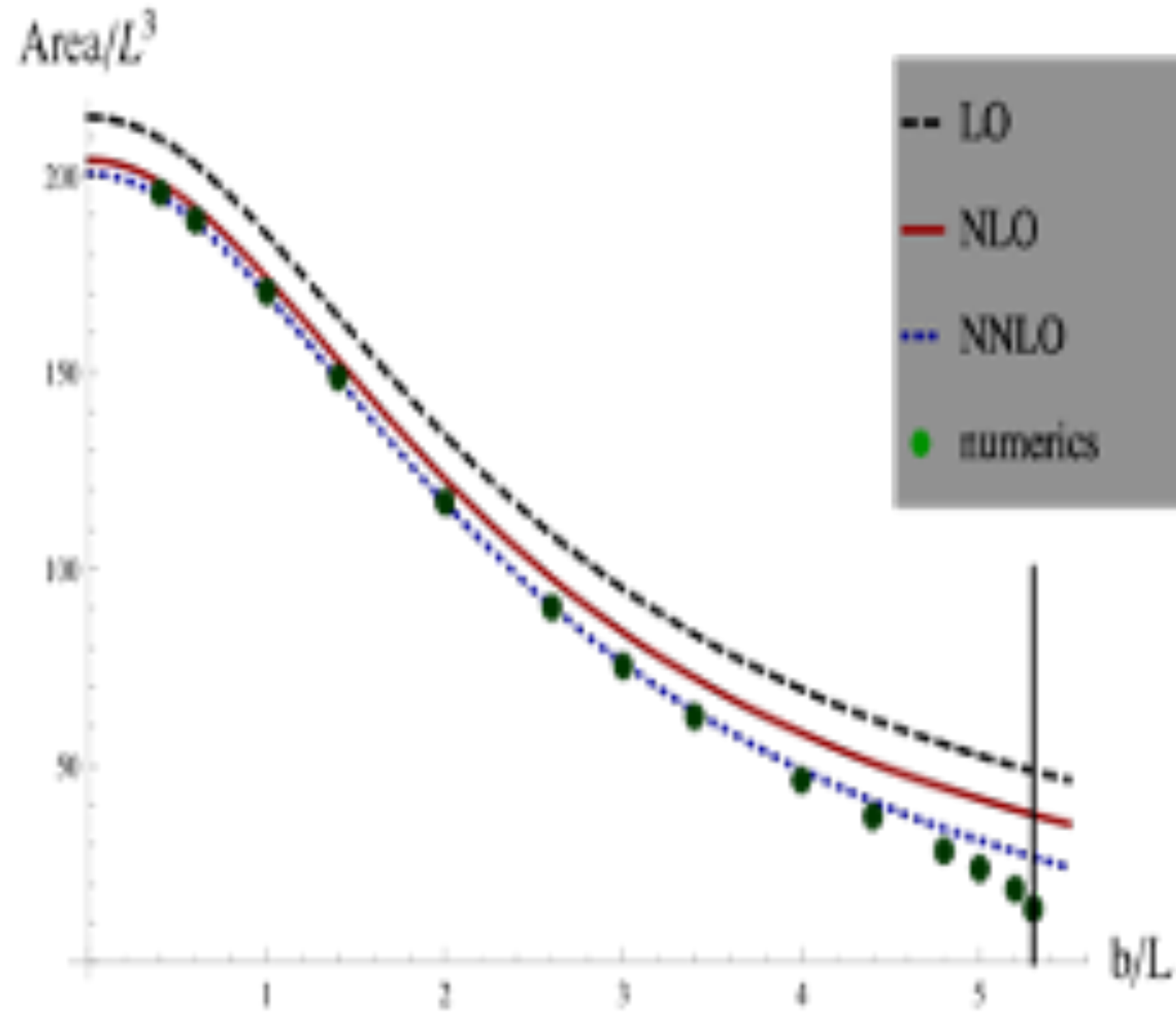


Figure 1: (Color online.) Comparisons between the numerics of [36] and the analytic formula (58). The black dashed curve represents the leading term in (58); the solid red curve corresponds to the first two terms in (58); the dotted blue curve represents the expression (58), which is correct up to a term of order $\mathcal{O}(1/\zeta^2)$; the green dots represent the numerical evaluations used in figure 3 of [36]; lastly, the vertical green line marks the place where, according to [36], the maximum impact parameter b_{max}/L occurs. We thank S. Lin and E. Shuryak for providing us with the results of their numerical evaluations.

For the first time ever we managed to do so BEFORE Gubser et al also did it in their second paper,

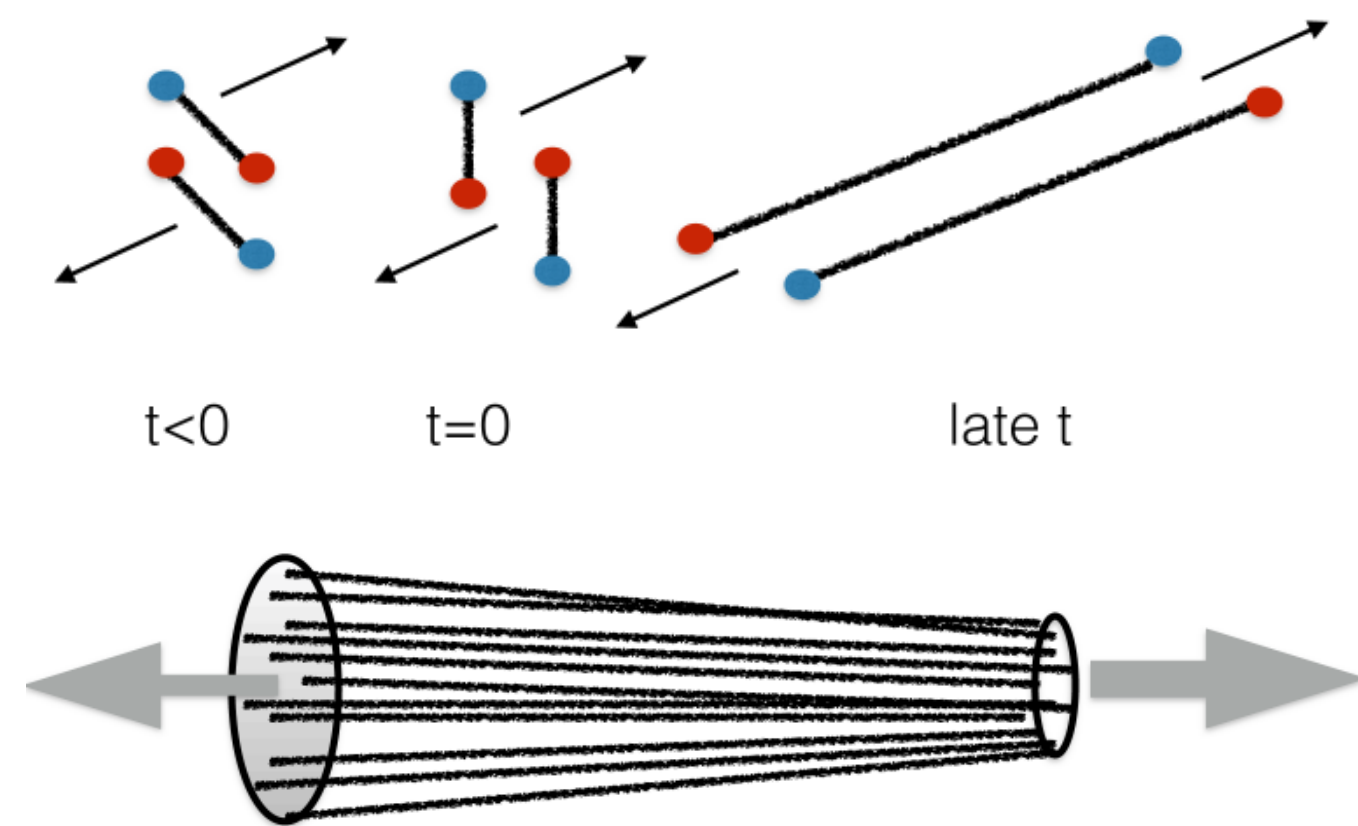
Here is a comparison from lines are theirs, the black dots are our numerical solution as you see, they match perfectly

It is the area (=entropy=multiplicity) versus the impact parameter the vertical line is the location of the critical value b_c

very peripheral collisions do NOT produce a fireball

Collective interaction of QCD strings and early stages of high multiplicity pA collisions

Tigran Kalaydzhyan and Edward Shuryak
*Department of Physics and Astronomy, Stony Brook University,
Stony Brook, New York 11794-3800, USA*

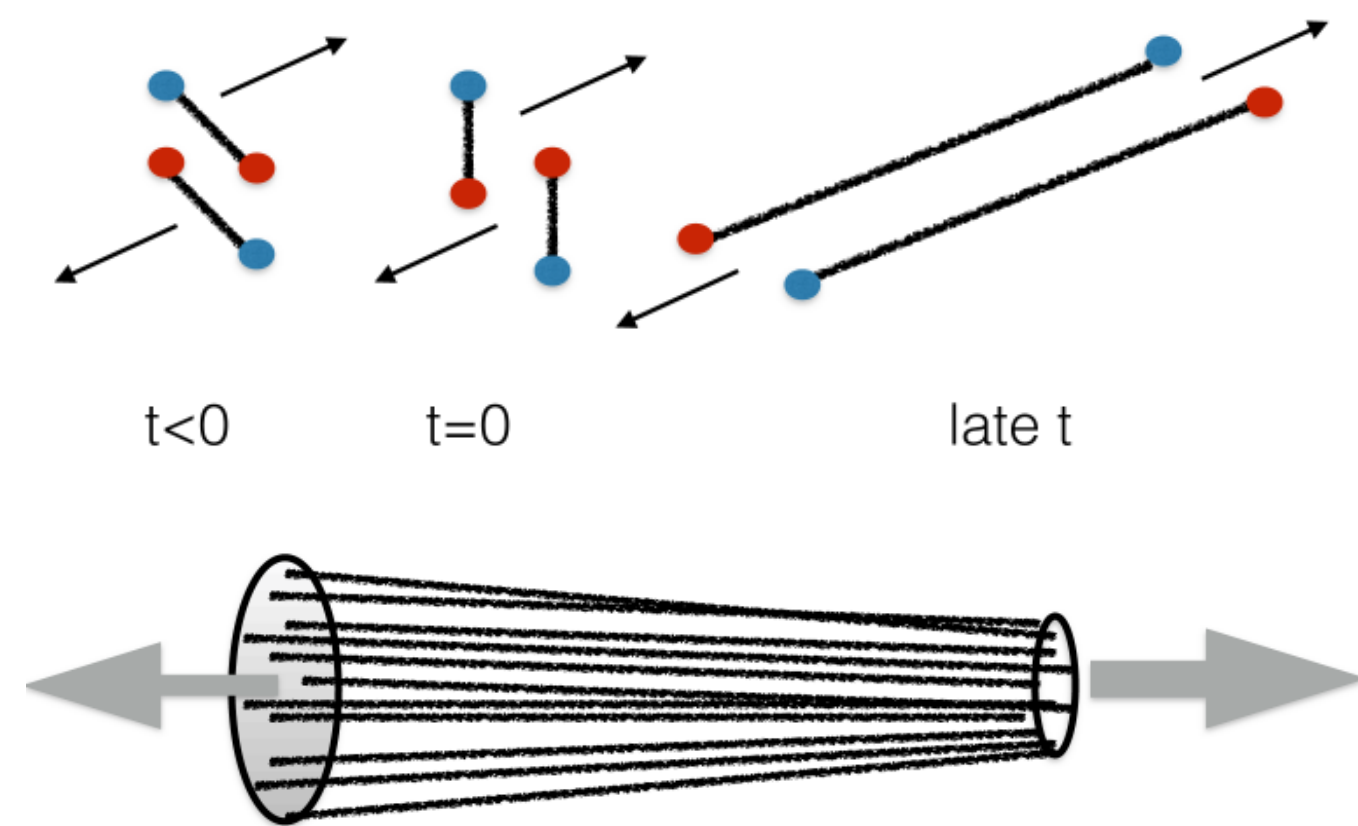


basic mechanism of production of QCD strings
(also called flux tubes)

multistring configuration after collision,
(spaghetti)
when strings are extended longitudinally
Lund model (Pythia etc) true for pp and light
nuclei assumes string are broken
INDEPENDENTLY
This cannot be true of the number is large...

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Original discussion was for pPb collisions at LHC
for which collective explosion similar to PbPb
was observed (radial and elliptic flows)

Note that its center bin corresponds to collision with about 16 nucleons
thus we speak about > 30 strings
the same applies to central collisions of light nuclei

QCD flux tubes were studied on the lattice

**Classification of flux tube in superconductor:
(Abrikosov)**

type I are attractive at large distances
due to which they are glued together to
macroscopic domain in which there is no
superconductivity

**Type II REPEL EACH OTHER
and form a lattice**

(therefore used in superconducting magnets)

The QCD vacuum is weak Type I

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here a group in Japan studied various operators in conjunction to the flux tube
here is depletion of quark chiral condensate
the curve is our formula for $m(\sigma)=600$ MeV like in nuclear forces

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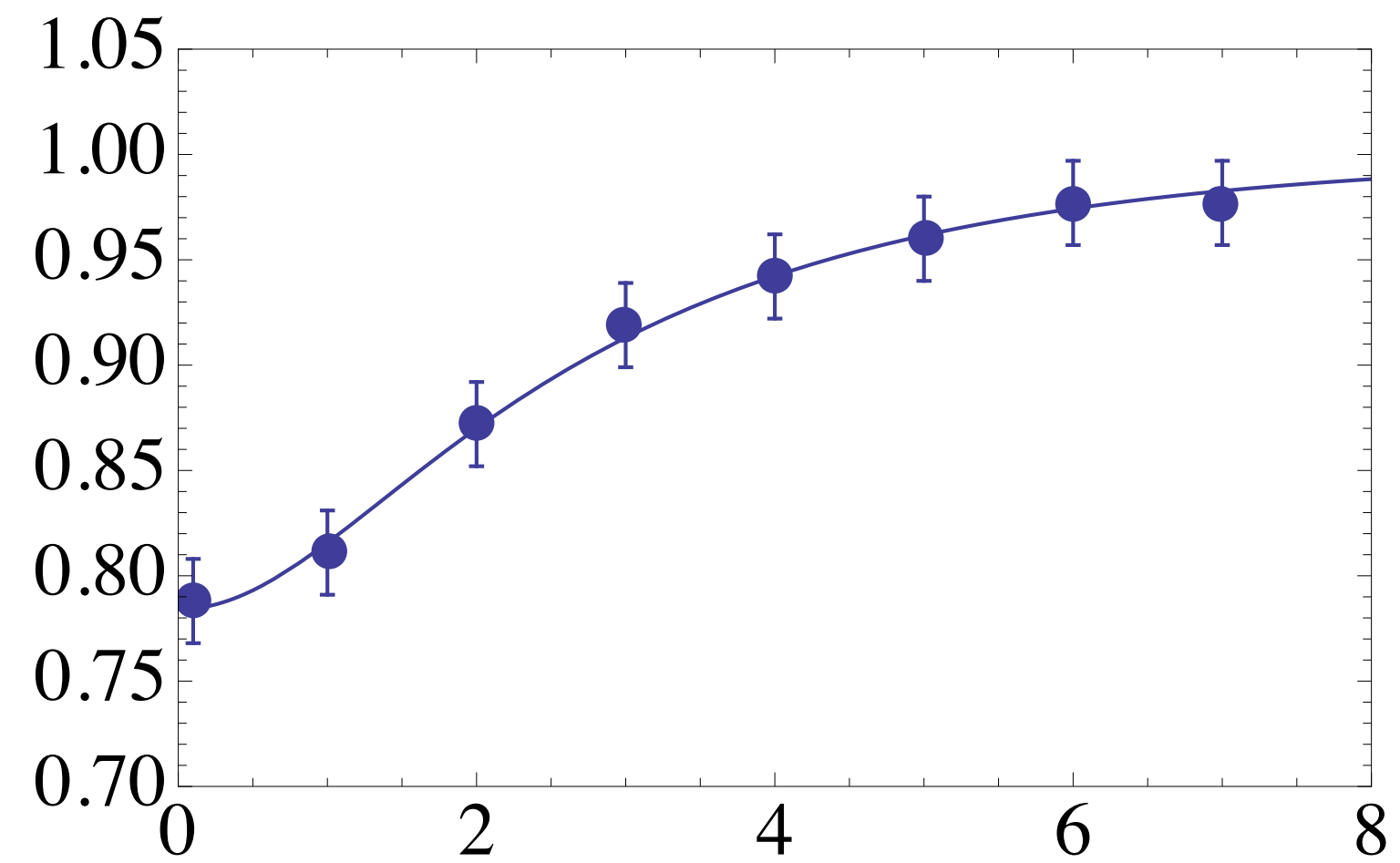


FIG. 3: (Color online) Normalized chiral condensate as a function of the radial coordinate transverse to the QCD string. Points are from the lattice data [23]. The curve is expression (7) with $C = 0.26$ and $s_{string} = 0.176$ fm.

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so one needs high density of string
to destroy the condensate**

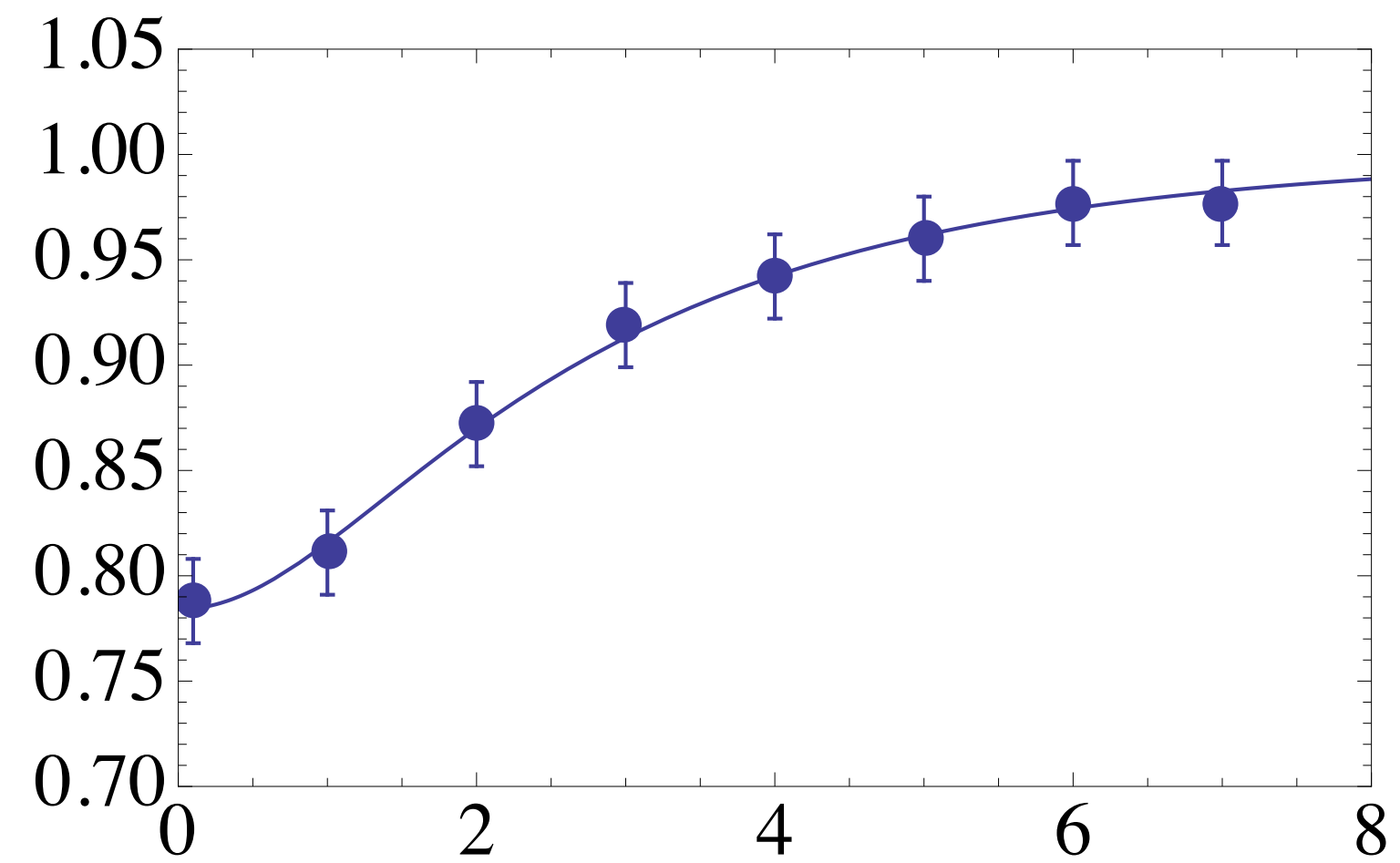


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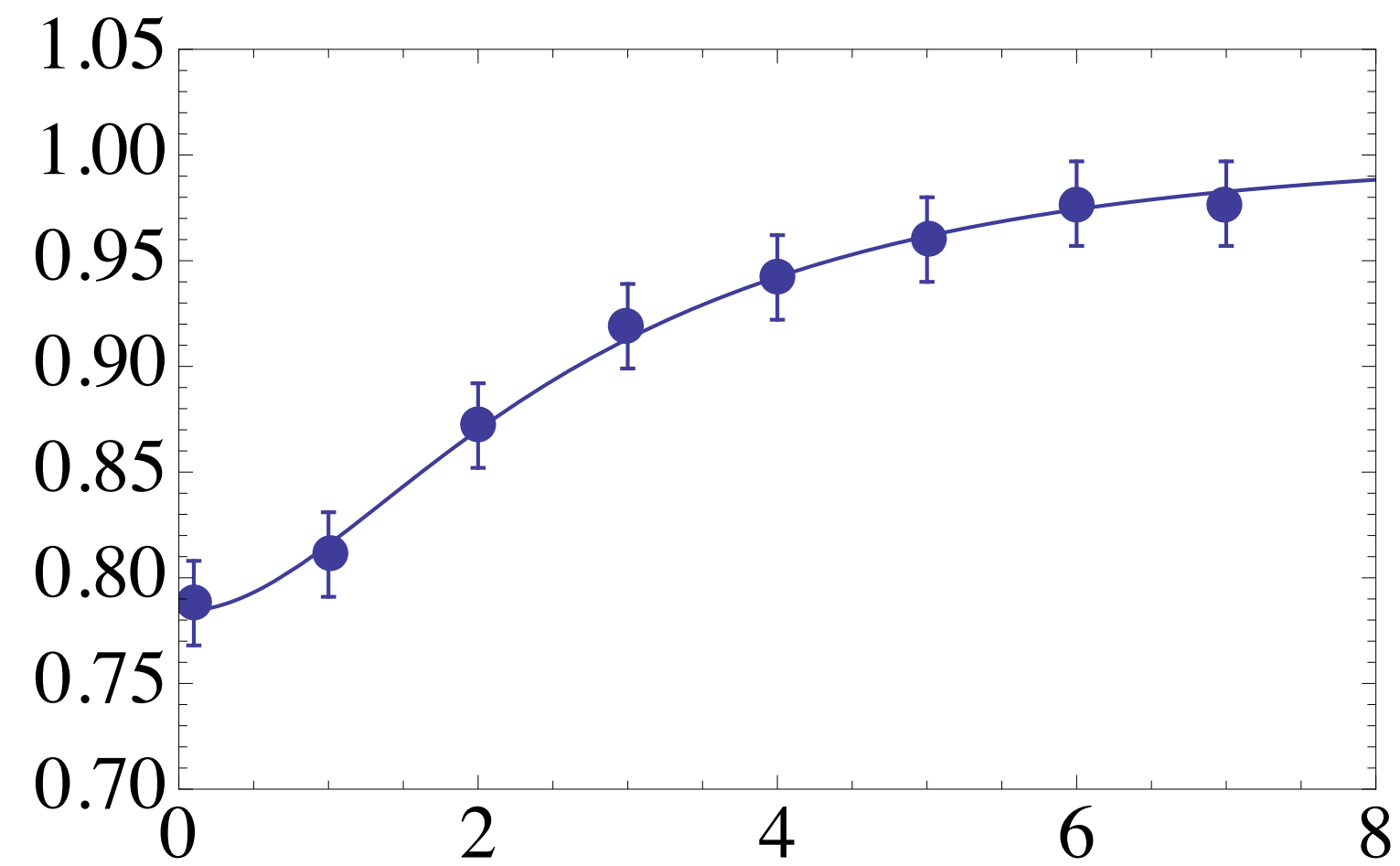


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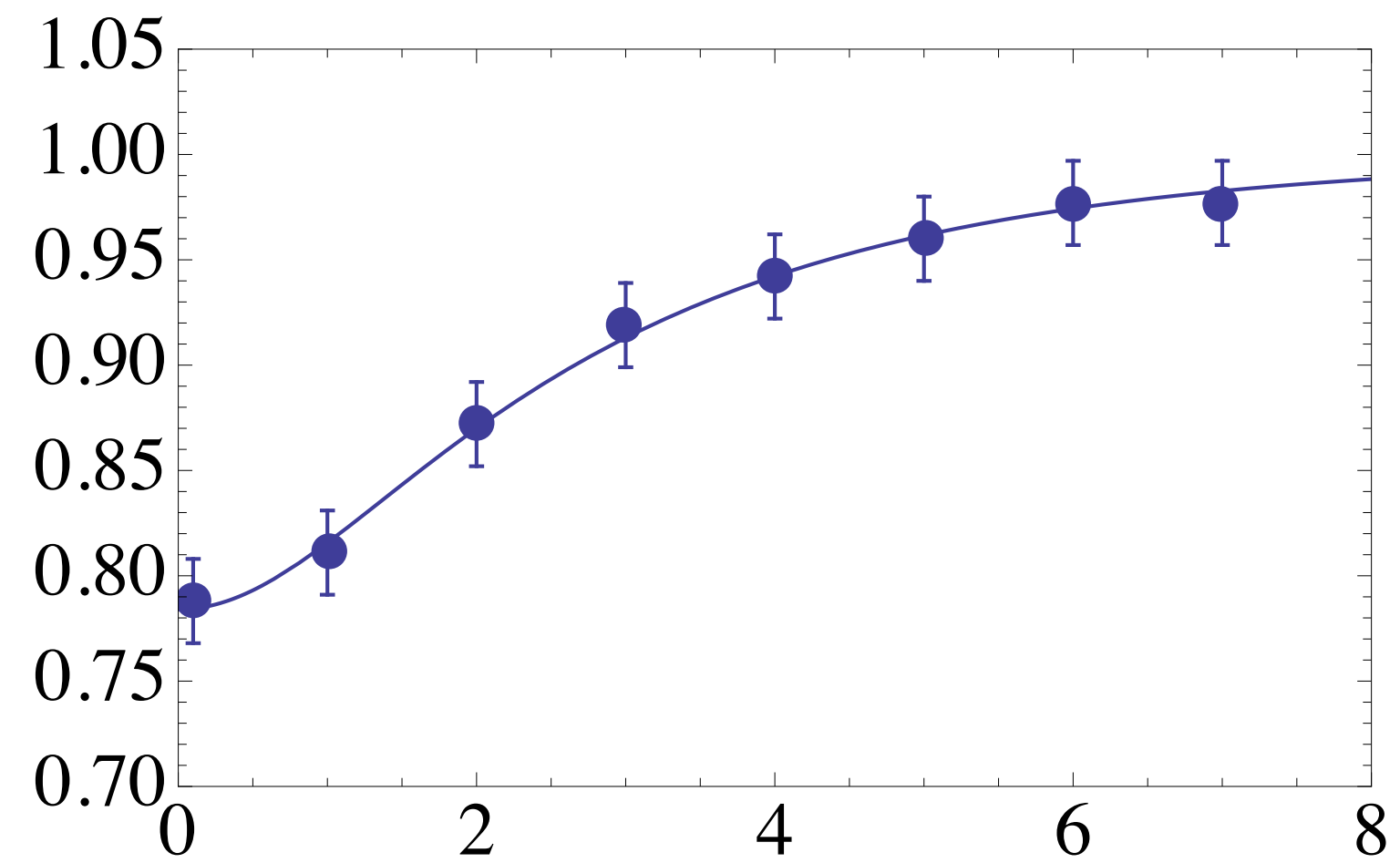


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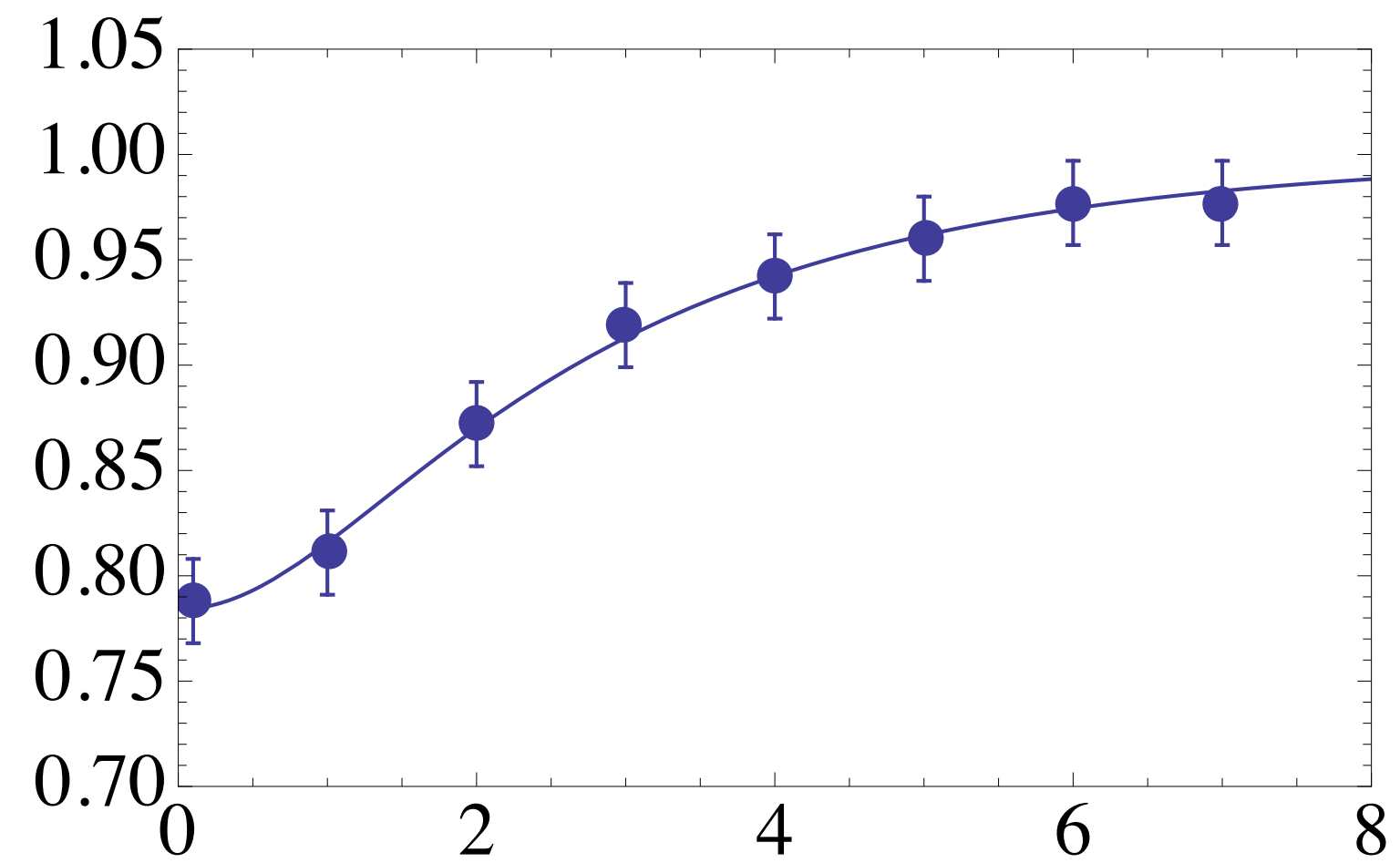


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**A SCALAR EXCHANGE IS ATTRACTIVE
AND CANNOT BE SCREENED**

correctly neglected in situations for which the Lund model
was originally invented – when only $O(1)$ strings are created ,
but **not for spaghetti!**

MOLECULAR DYNAMICS STUDY

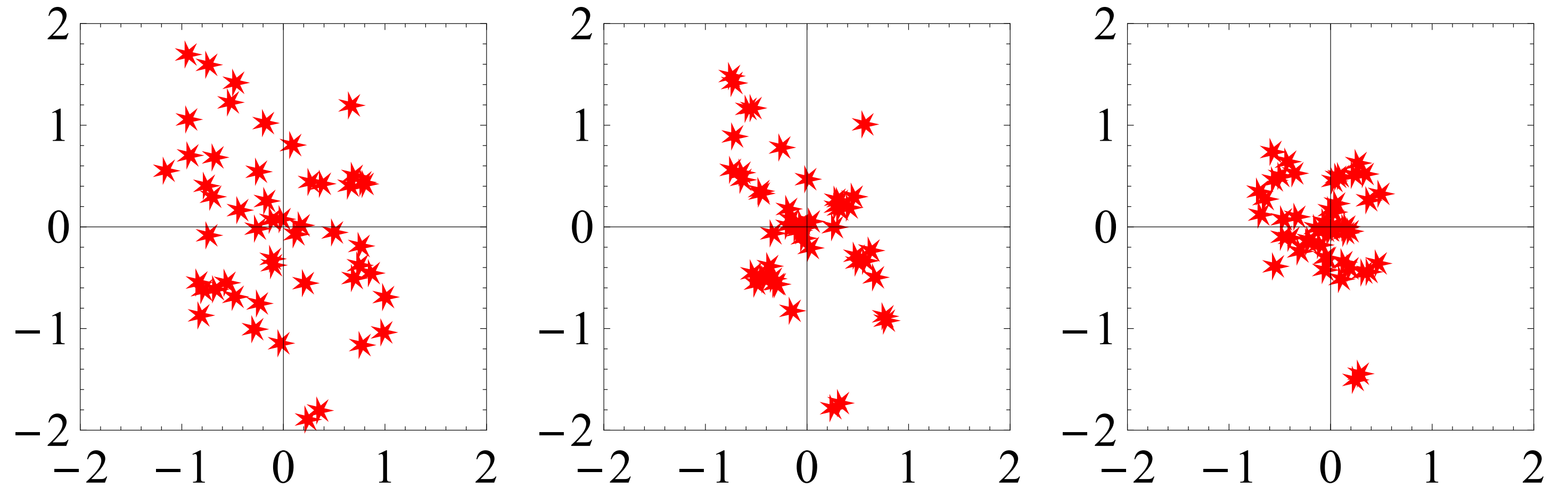


Table 1

Example of changing transverse positions of the 50 string set: the plots correspond to initial configuration evolved to times $\tau = 0.1, 0.5$ and 1 fm/c

the formation of chirally restored fireball

In the white region quarks become massless
which means they have full
pressure like in QGP
AND THERE IS AN EXPLOSION

WE ESTIMATED
THAT THE EFFECT
GETS IMPORTANT FOR
N STRING > 30

(each pair of wounded nucleons
mean 2 strings)

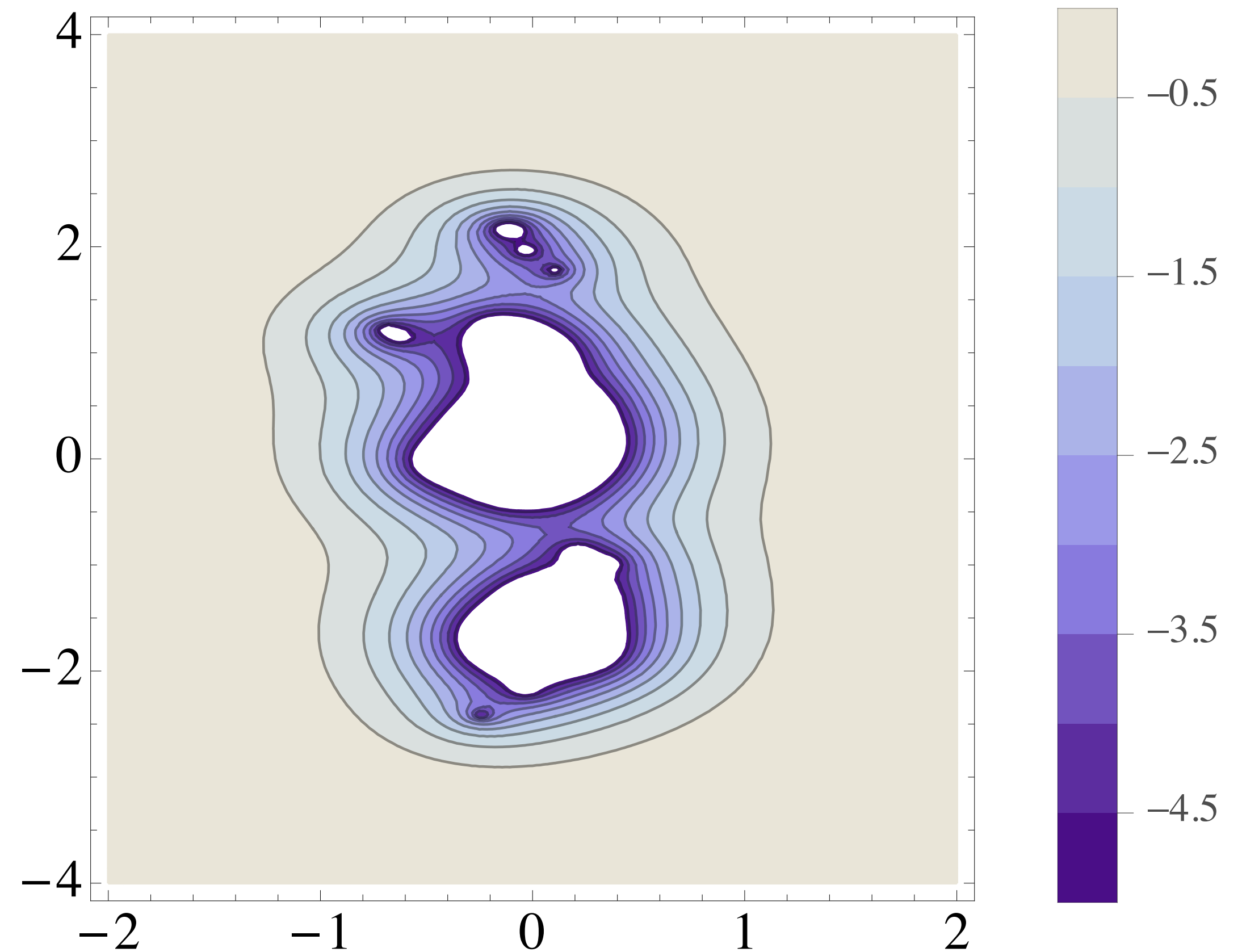


FIG. 10: (Color online) Instantaneous collective potential (in units of $2g_N\sigma_T$) for an AA configuration with $b = 11$ fm, $g_N\sigma_T = 0.2$, $N_s = 50$ at the moment in time $\tau = 1$ fm/ c . White regions correspond to the chirally restored phase.

Collective String Interactions in AdS/QCD and High Multiplicity pA Collisions

Ioannis Iatrakis,^{*} Adith Ramamurti,[†] and Edward Shuryak[‡]

**to calculate string interactions
one needs to understand
one of the most difficult
subject in hadronic spectroscopy
meson-glueball mixing
in **scalar 0^{++} channel****

without mixing, strings interact
only by glueball exchange,
and the lightest
scalar glueball has mass
of about 1.6 GeV

the mass of lightest scalar meson
sigma is only 0.4-0.6 GeV

sigma is the crucial
element for nuclear attractive
force and its binding

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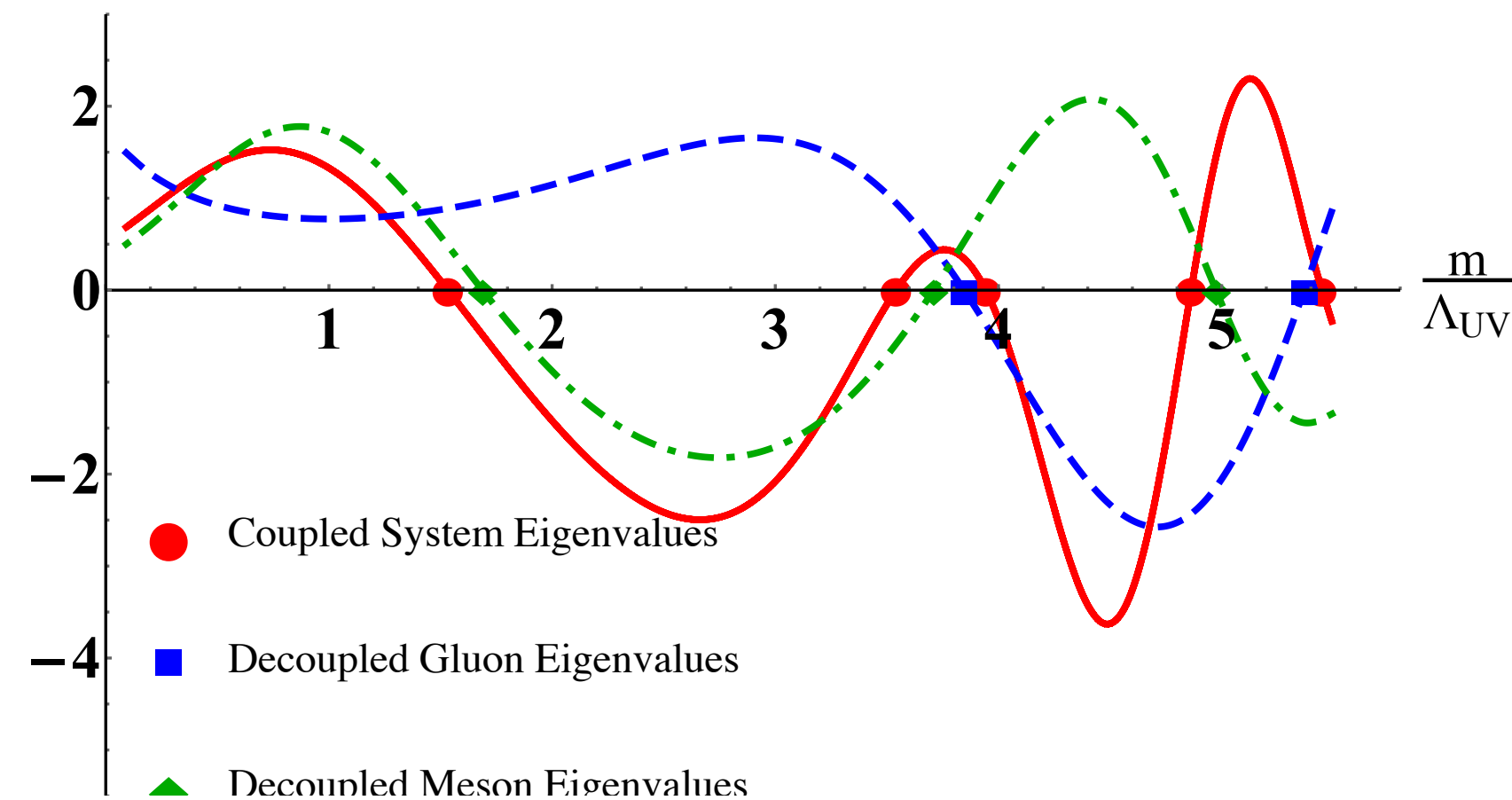
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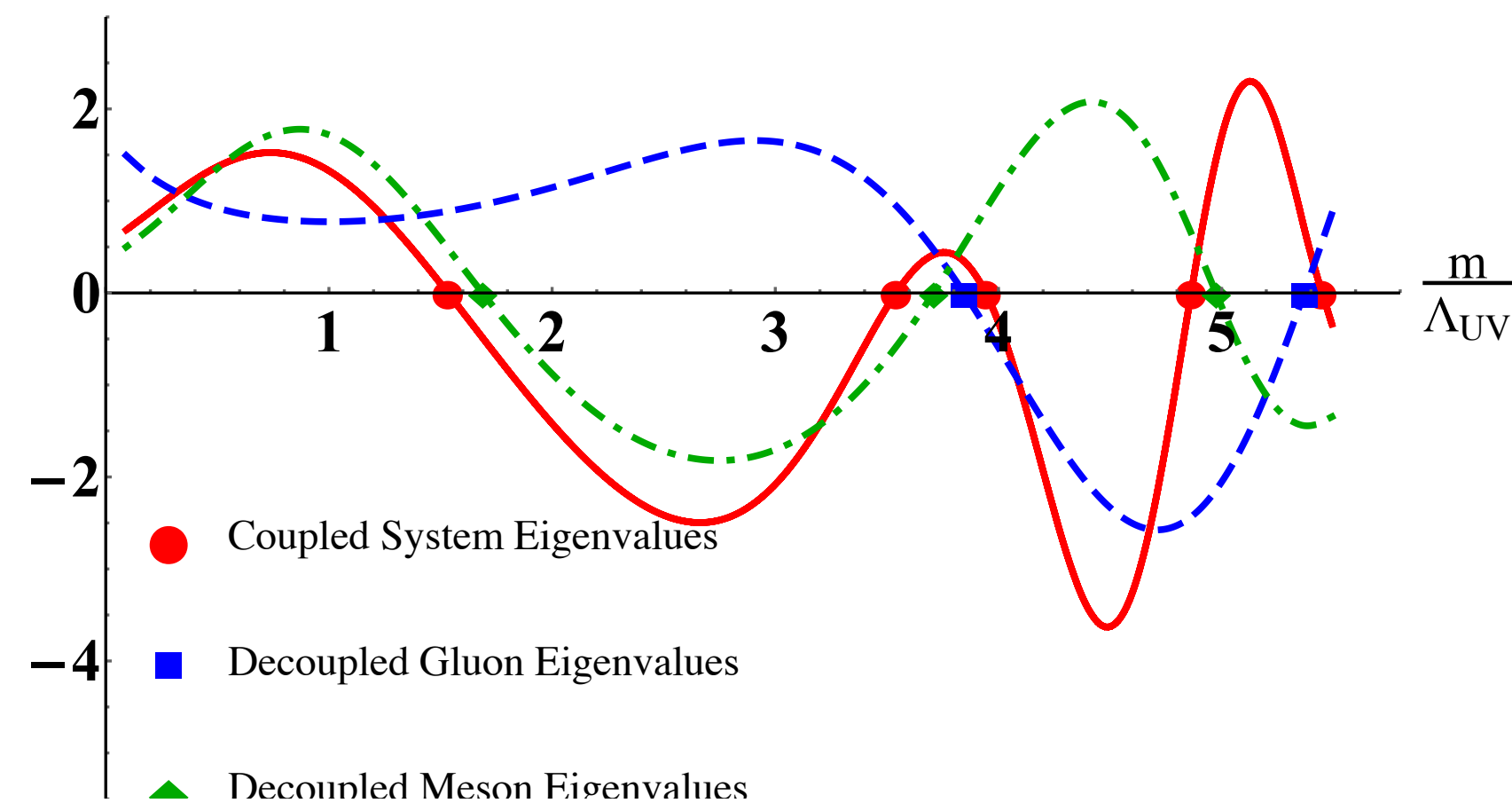
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effective model AdS/QCD WAS DEVELOPED BY Kiritsis et al in great details we had all the parameters, and just calculated the mixing of scalars

the results agreed with lattice finding of the coupling

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**snapshots of
string in x-z plane:
going to larger z
is falling toward AdS center
its hologram
means that **strings get fatter**
with time!
the factor is so big that
it appears as a fireball
at $z=0$ (our world)**

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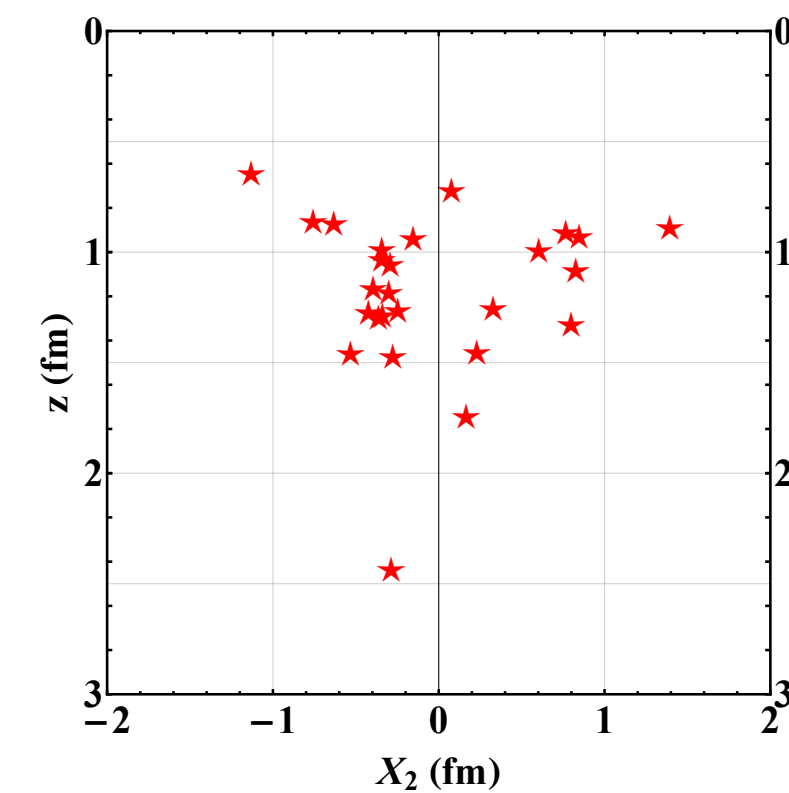
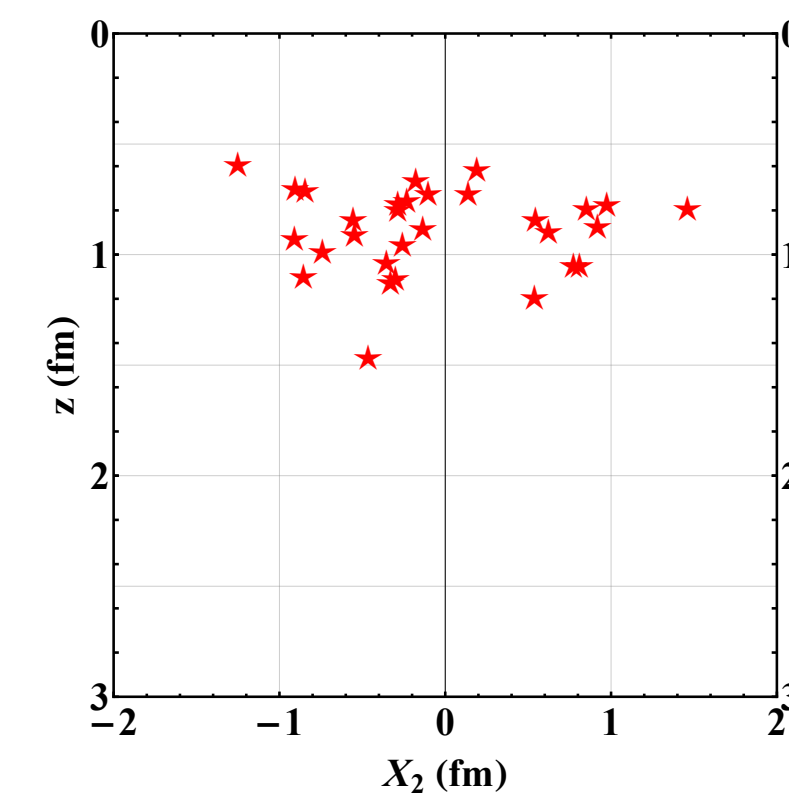
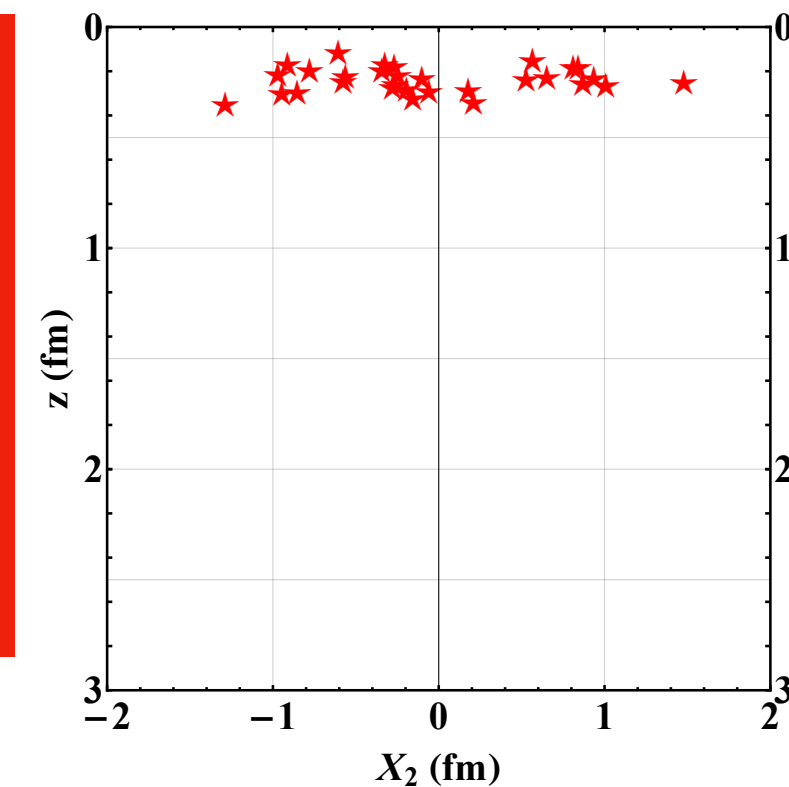
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Many-body forces and nucleon clustering near the QCD critical point

*ES and J. M. Torres-Rincon, Phys. Rev. C100, 024903 (2019),
arXiv:1805.04444 [hep-ph].*

*ES and J. M. Torres-Rincon, Phys. Rev. C101, 034914 (2020),
arXiv:1910.08119 [nucl-th].*

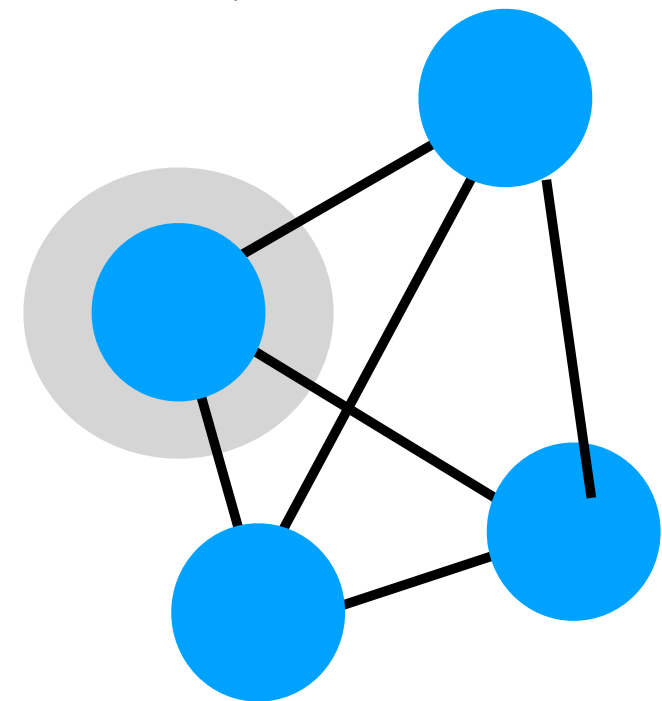
D. DeMartini and ES (2020), arXiv:2007.04863 [nucl-th].

Many-body forces and nucleon clustering near the QCD critical point D. DeMartini and E. Shuryak, e-Print: 2010.02785

• **The main idea of this work:**

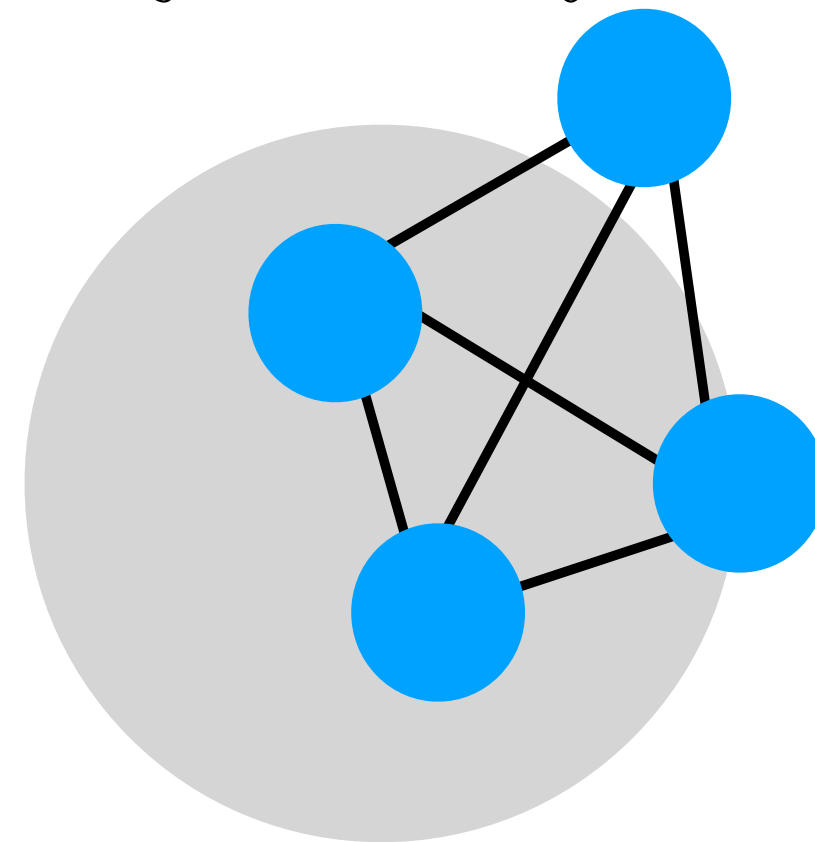
Suppose the CP indeed exists, and is located in the part of the phase diagram near the freezeout line of BES program collisions. Furthermore, while scanning this line, for some specific beam energy one happens to be in a state in which the correlation length reaches a value $\xi_{max} \sim 1.5-2fm$. What observables are sensitive to such scale of ξ ?

$$\xi_{min} \sim 1/m_\sigma \sim 0.4 fm$$



far from CP
nuclear forces are
short range,
binary forces
dominate

$$\xi_{max} \sim 2 fm$$



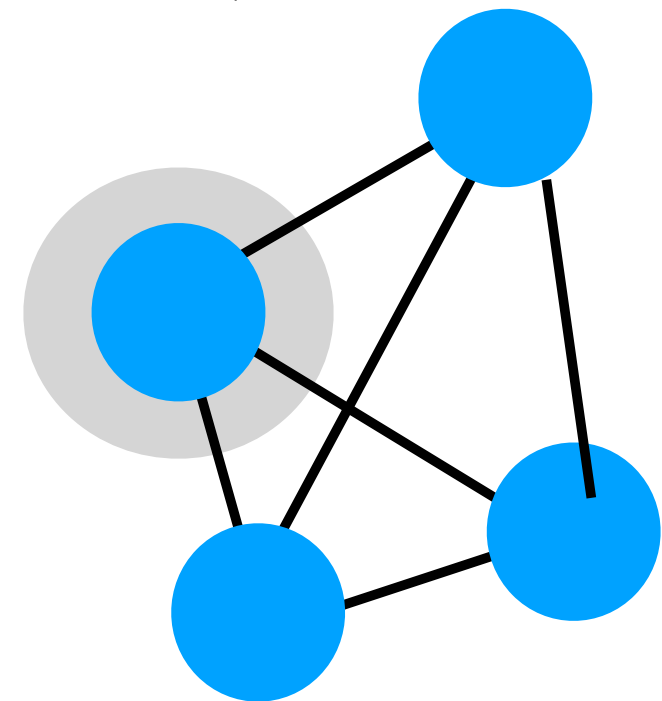
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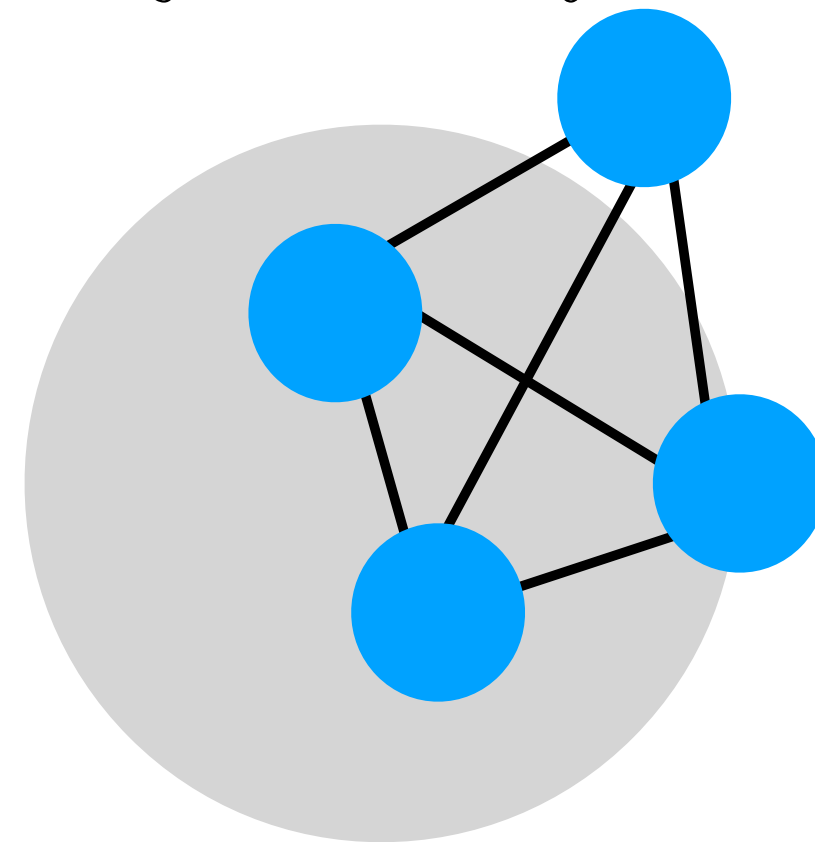
Side remark: too many domains. sound waves which we observed have the wavelength much larger than 2 fm, $2\pi R/m = 6\text{fm}$ or more

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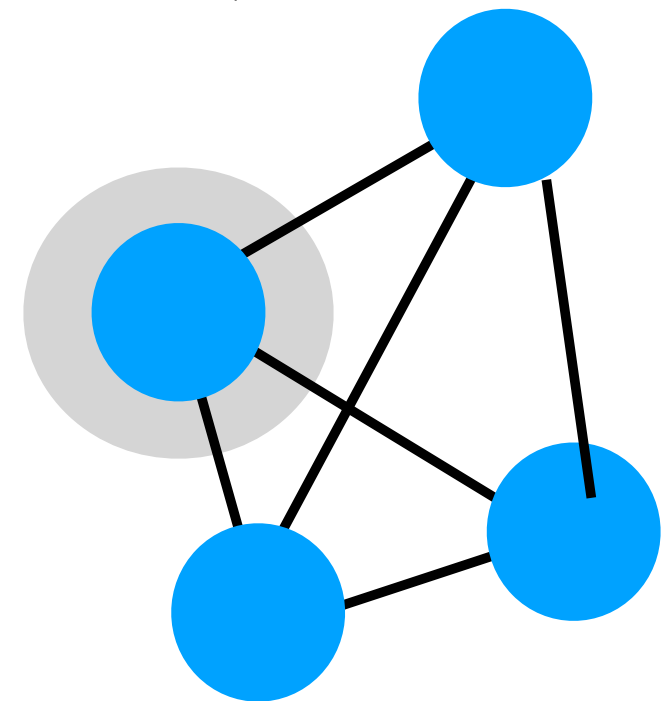
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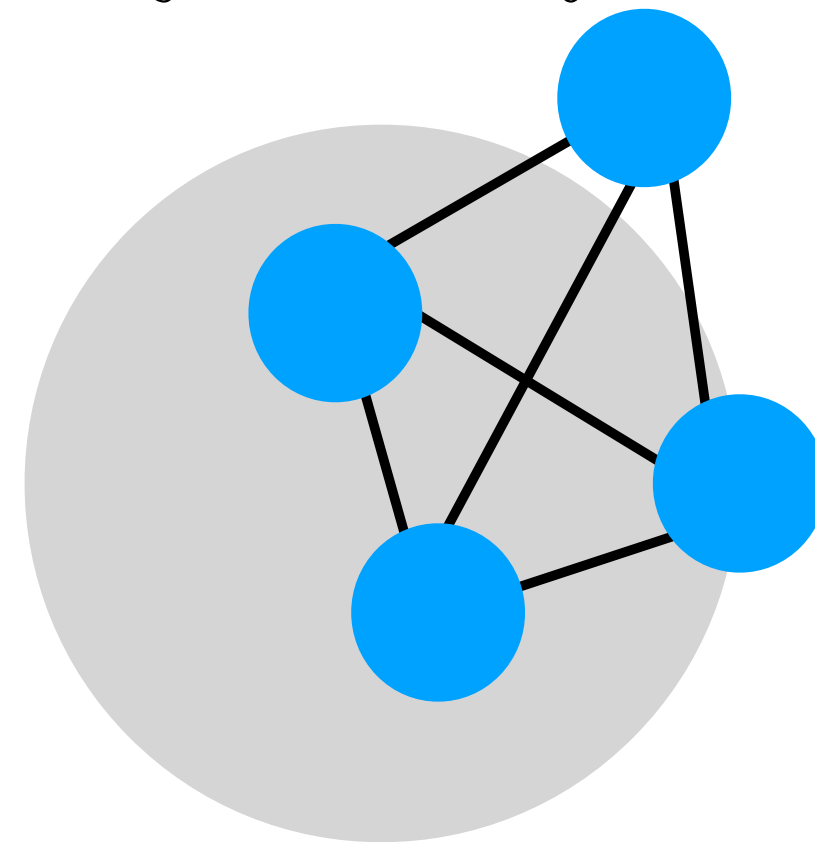
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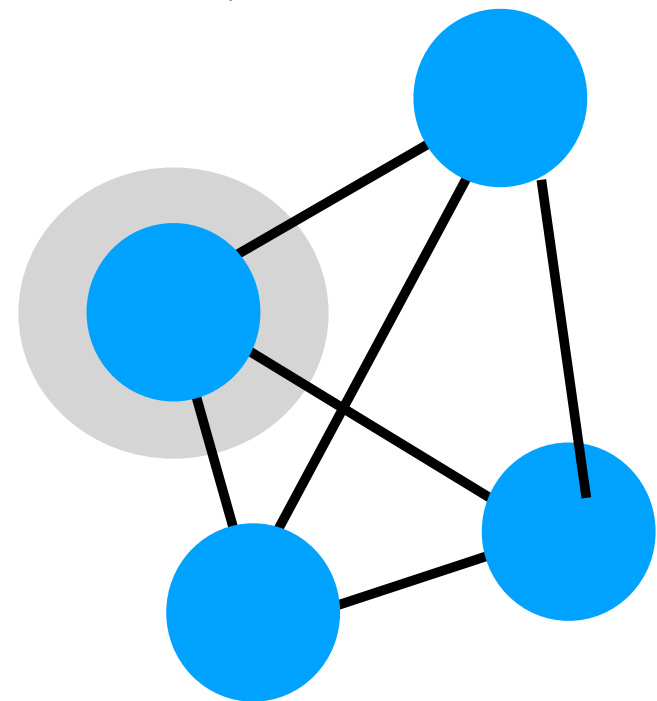
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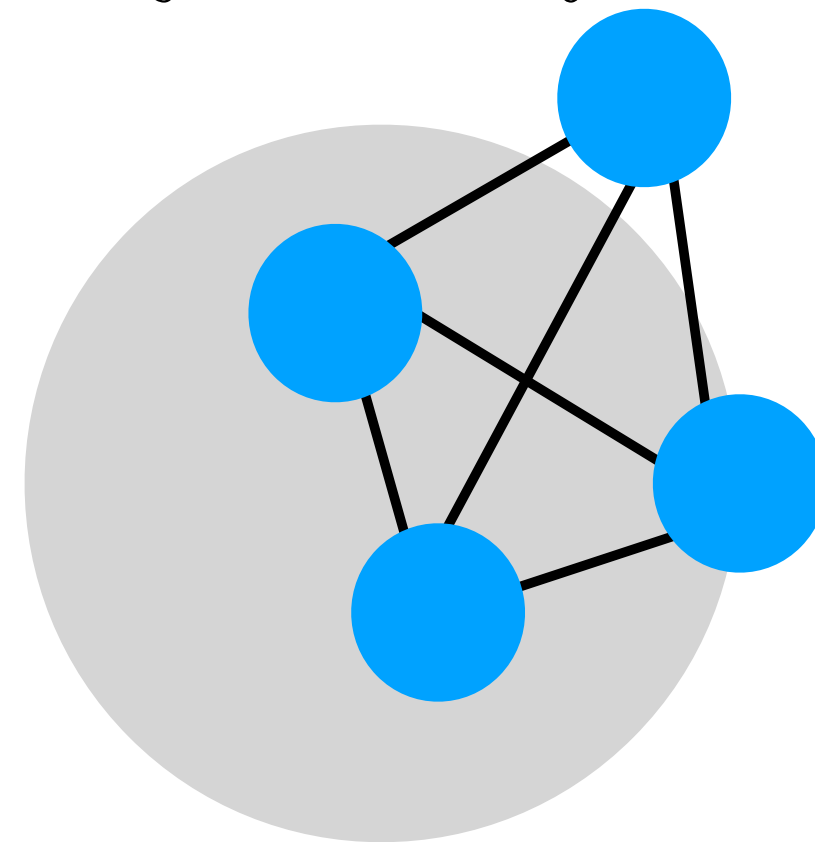
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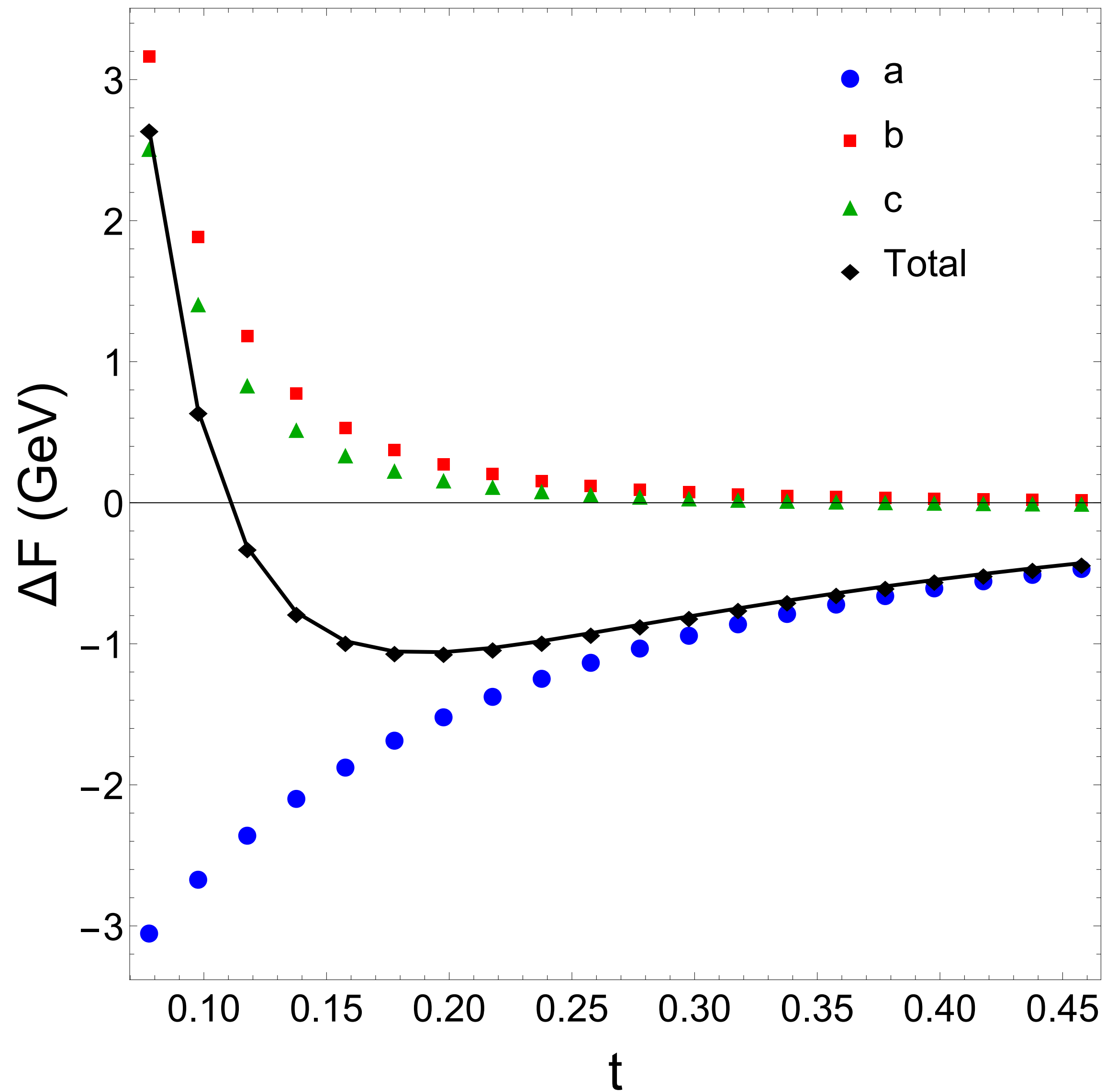


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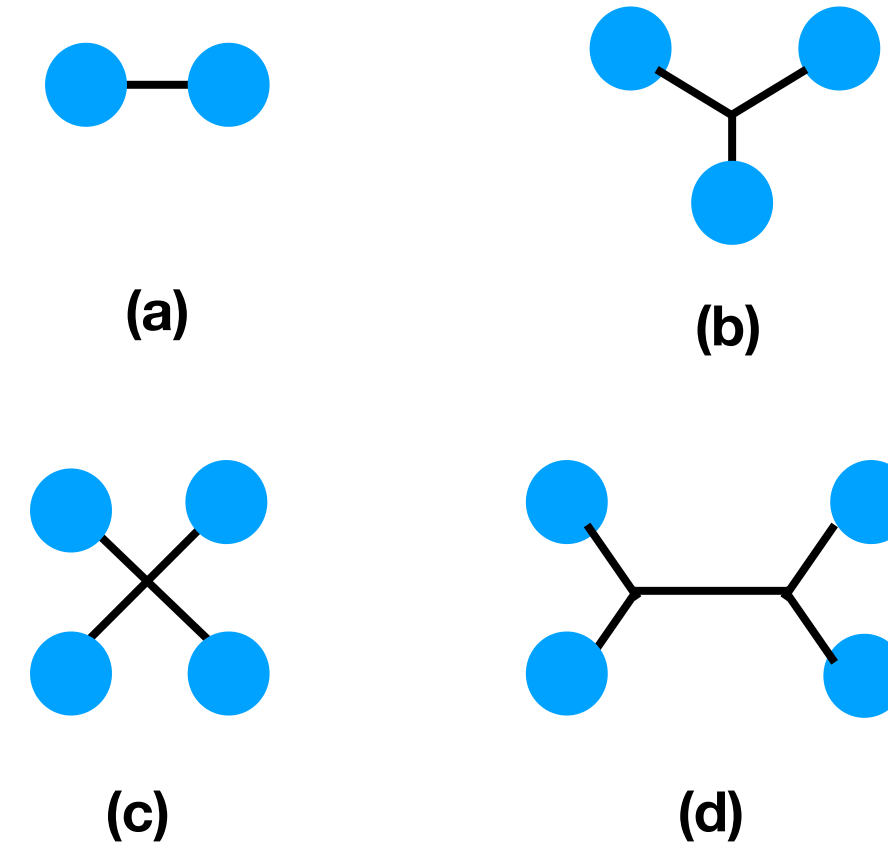
As we will show, the interplay of attractive binary
And **repulsive manybody forces**
Will lead to very non-monotonous signal

Energy of 4-N cluster
 $\rho=2 \text{ fm}$
 $t=T/T_c-1$



$$V = -\frac{4 \cdot 3}{2} \frac{g_c^2}{4\pi} \frac{\exp(-r_{ij}/\xi)}{r_{ij}} + 4 \cdot 3! \lambda_3 \left(\frac{g_c}{4\pi}\right)^3 V_b$$

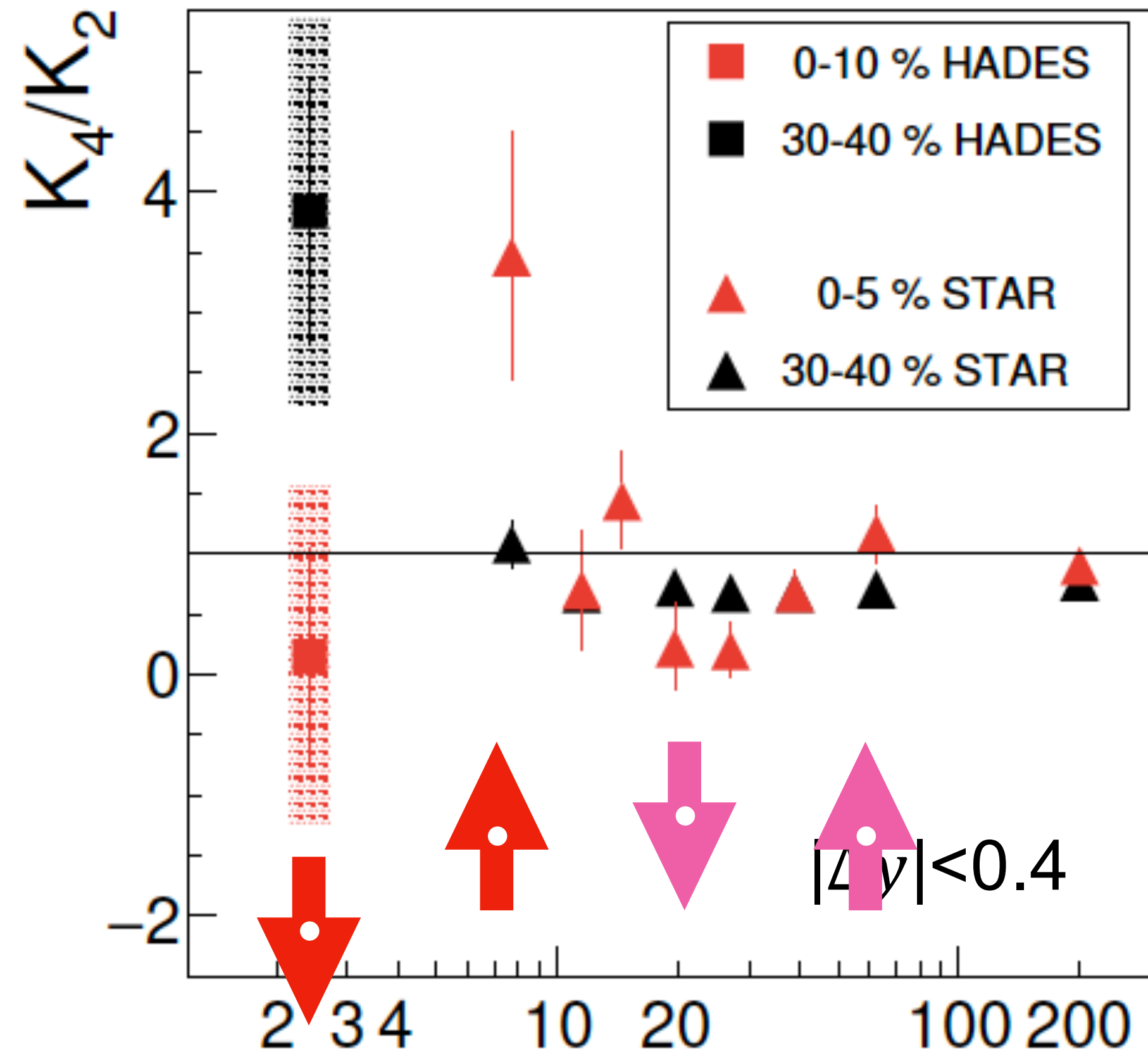
$$+ 4! \lambda_4 \left(\frac{g_c}{4\pi}\right)^4 V_c - 4! \frac{\lambda_3^2}{8\pi} \left(\frac{g_c}{4\pi}\right)^4 V_d$$



Repulsive three and four
 Body forces overcome
 Attraction near CP
 and kill clustering

•Let us now look at experimental **kurtosis**

•Older STAR data have shown large effect



• e-Print: [2001.02852](#)

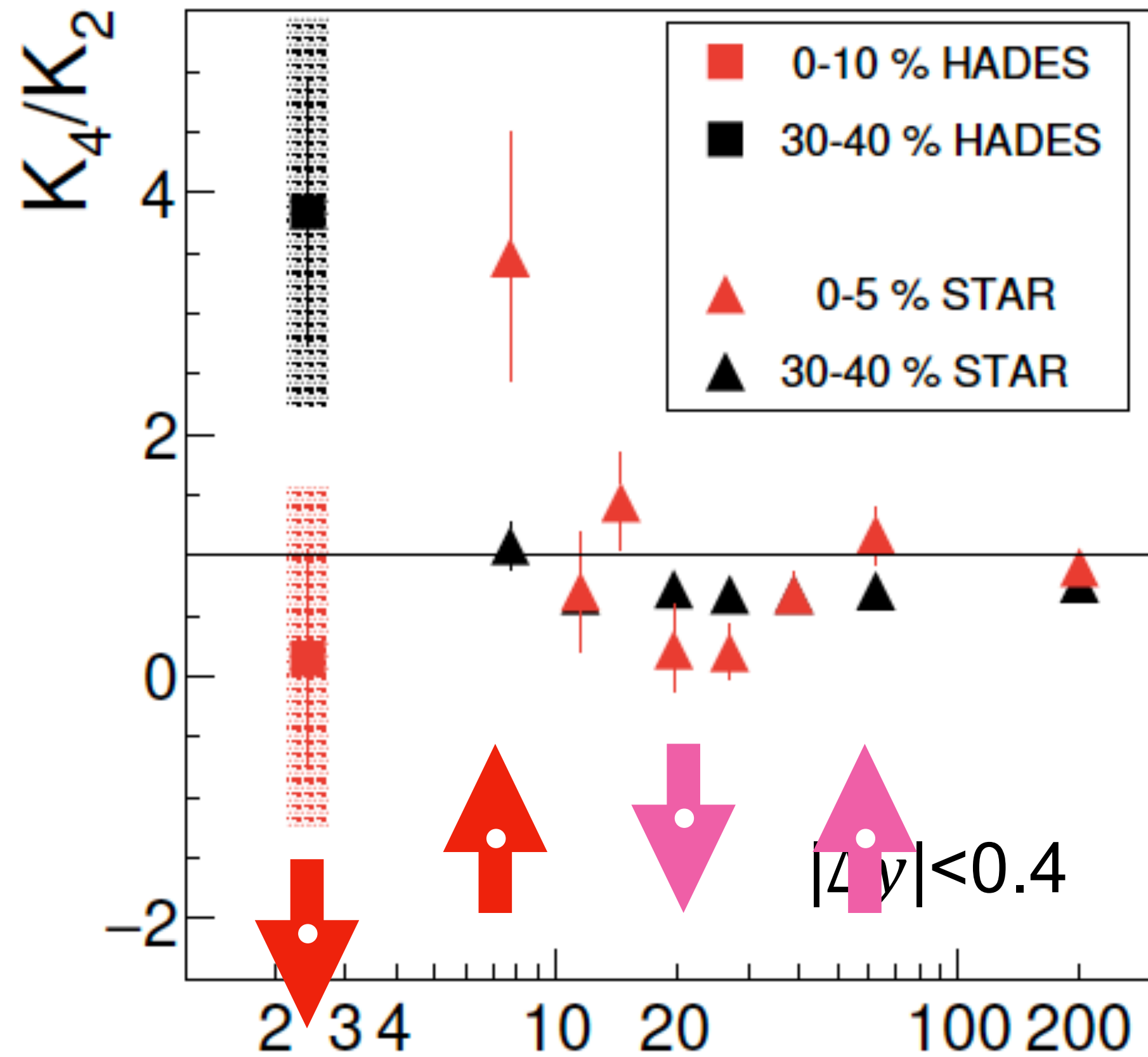
Two dips for central bins
large at 2 and smaller at 20 GeV?
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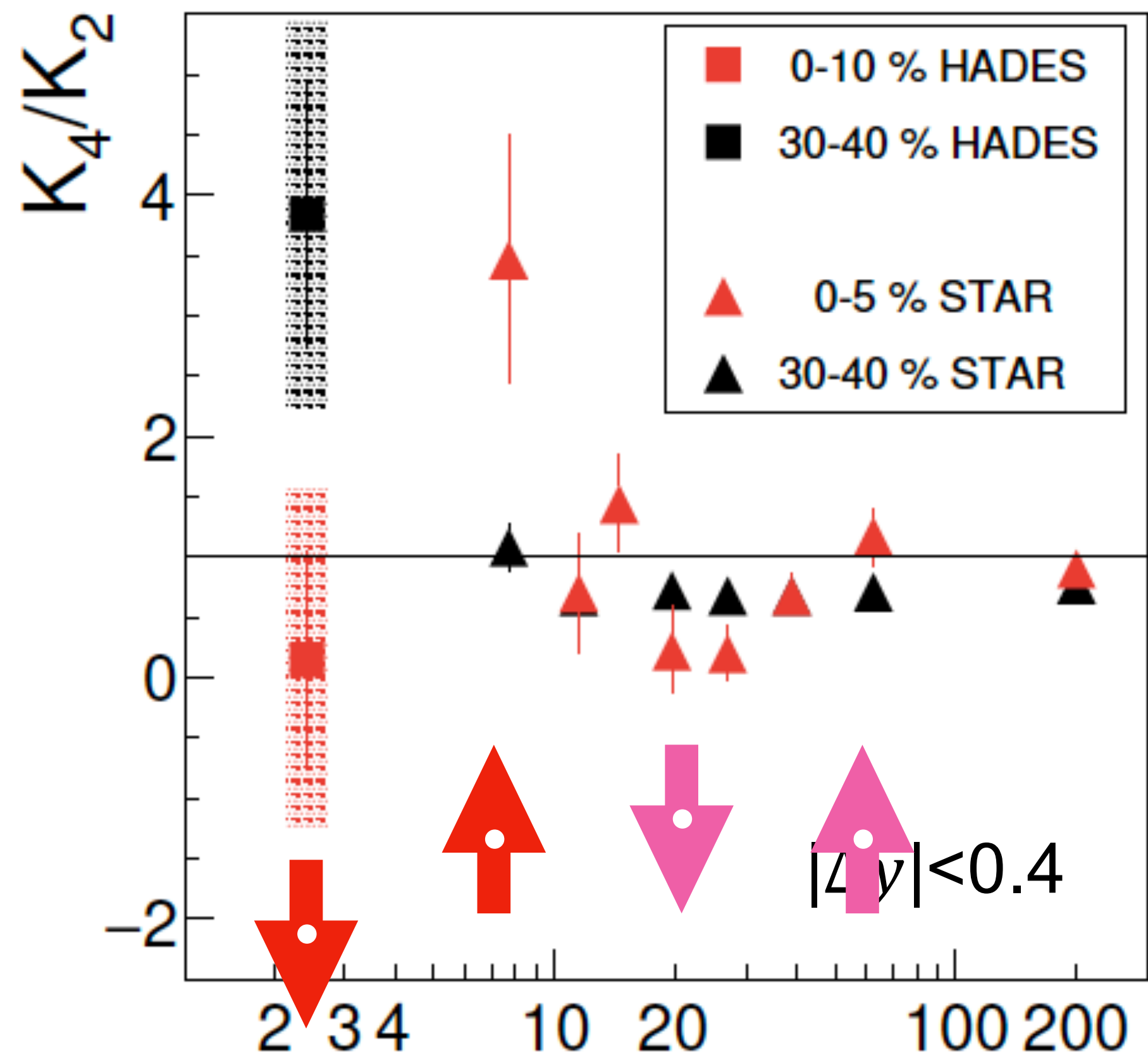
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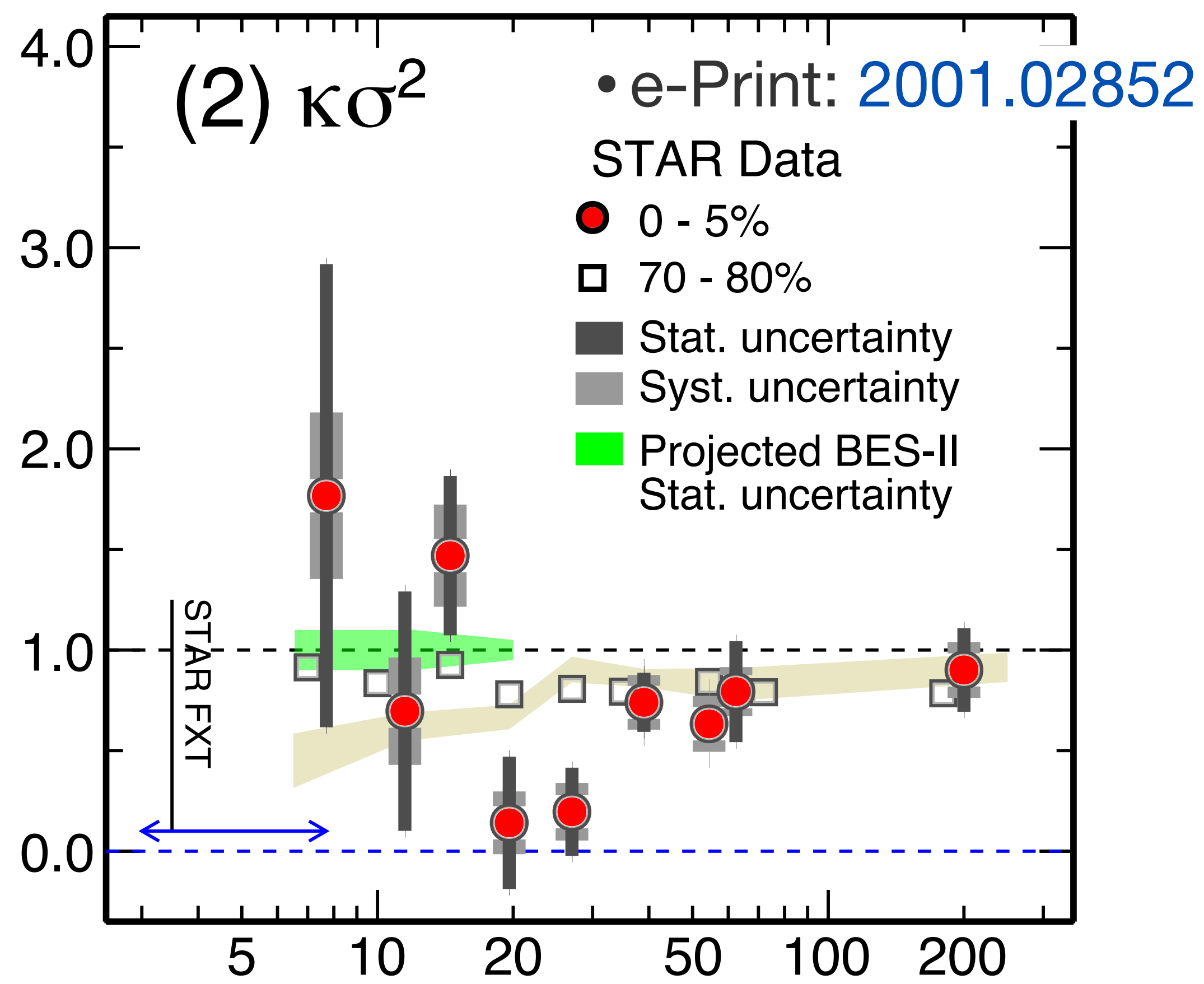
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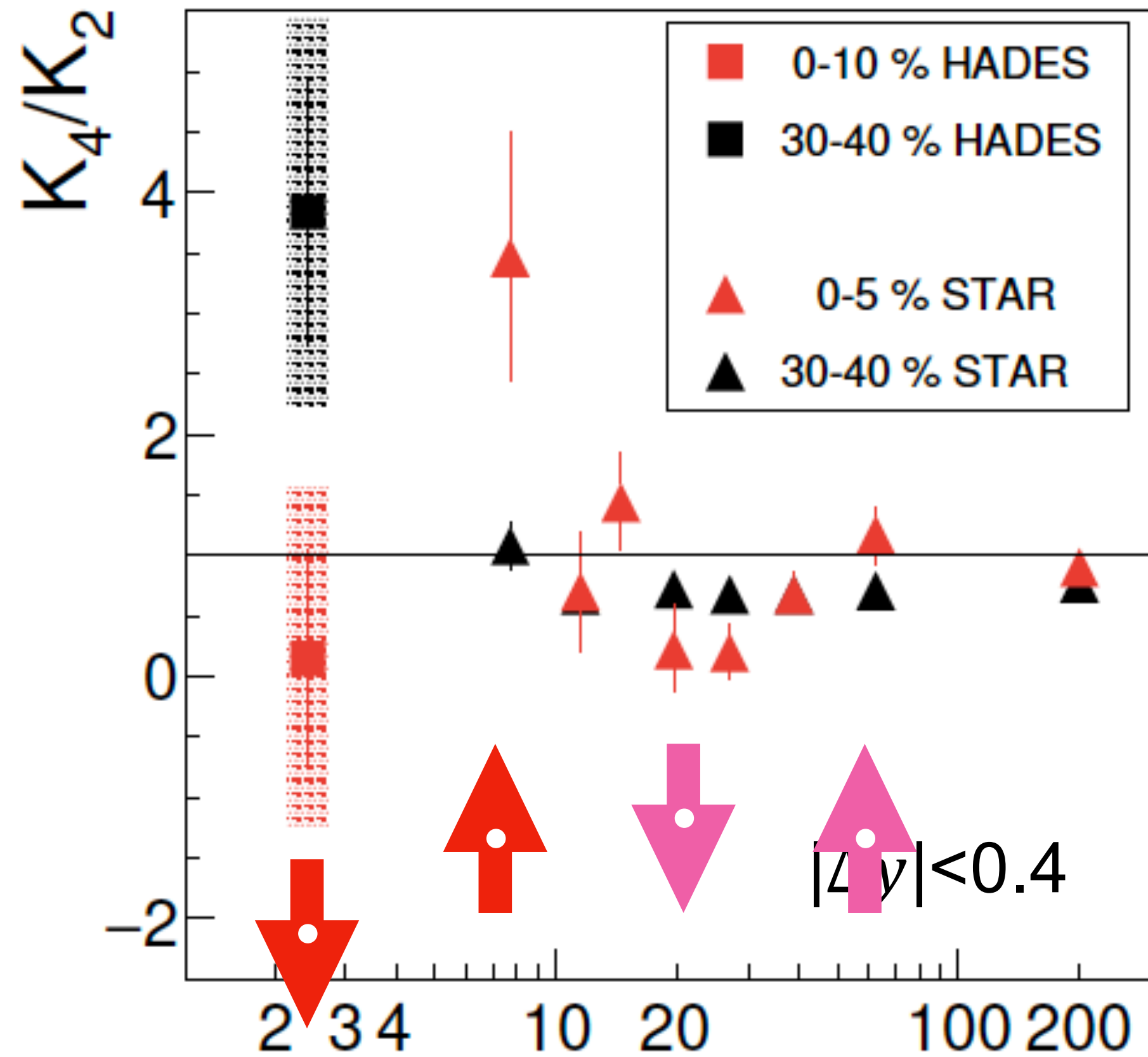
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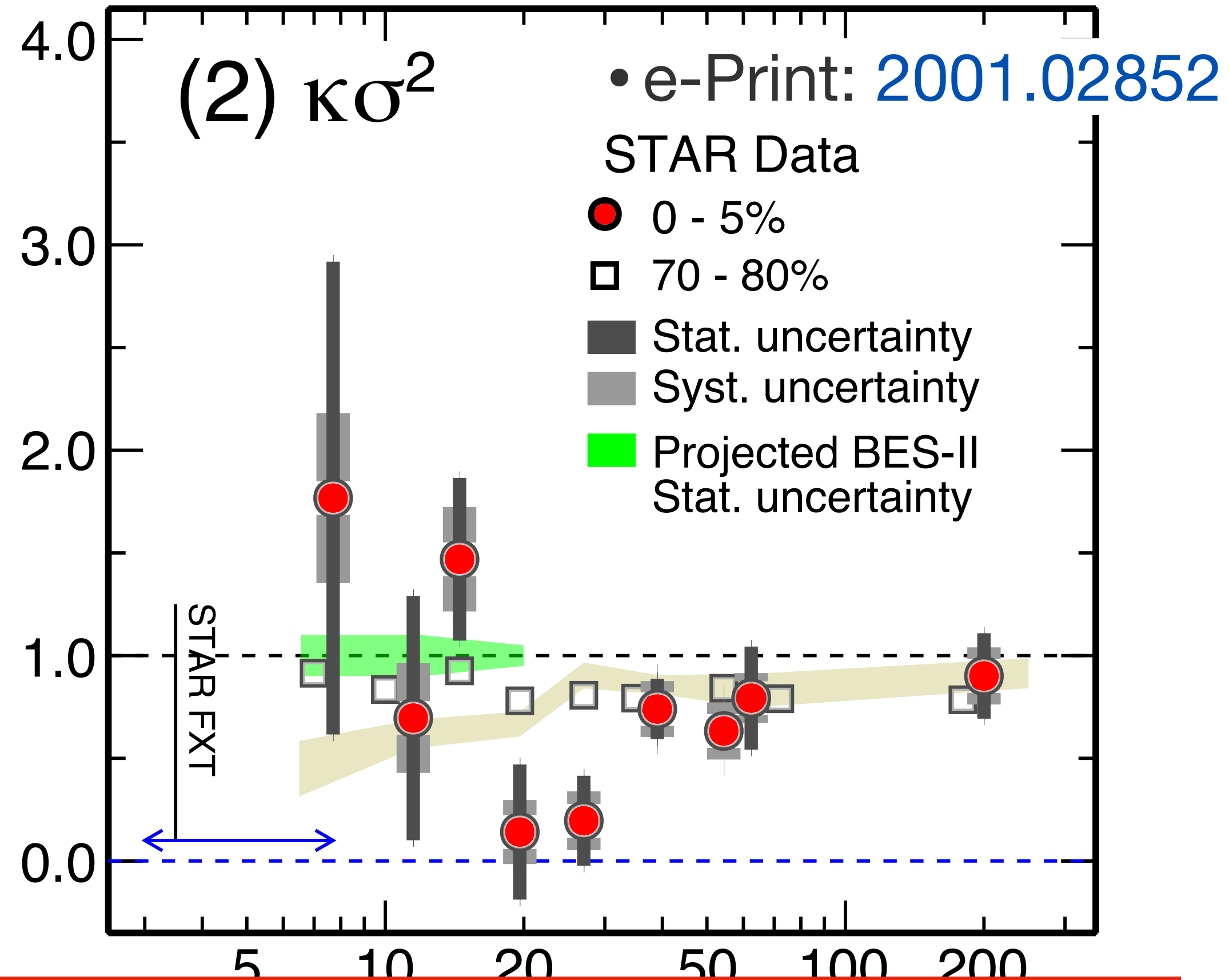
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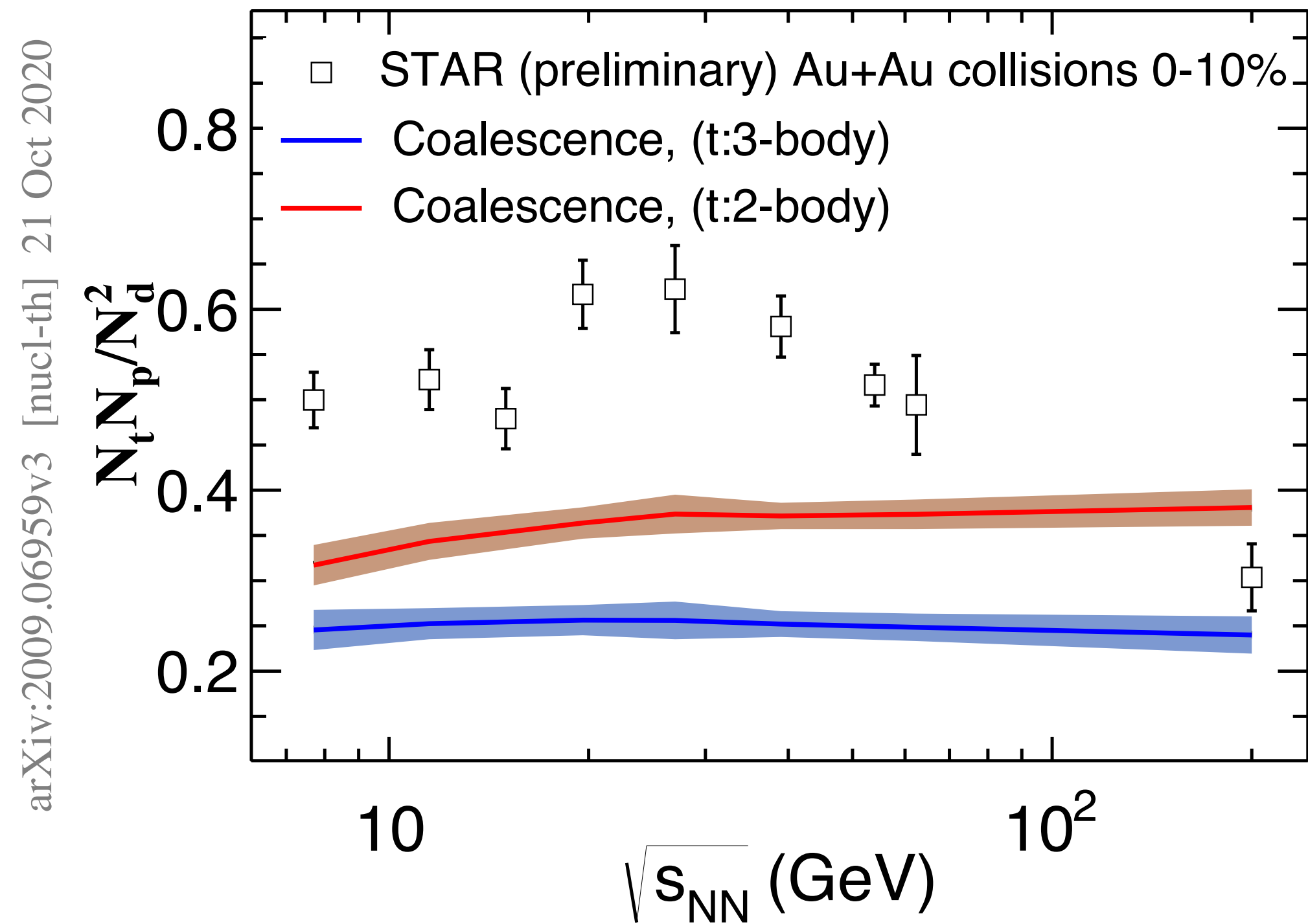
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Still non-monotonous signal? Clearly much more accurate measurements from BeS-II are needed

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In this ratio the main driver
 — fugacity $\exp(\mu/T)$ -
 Cancels out



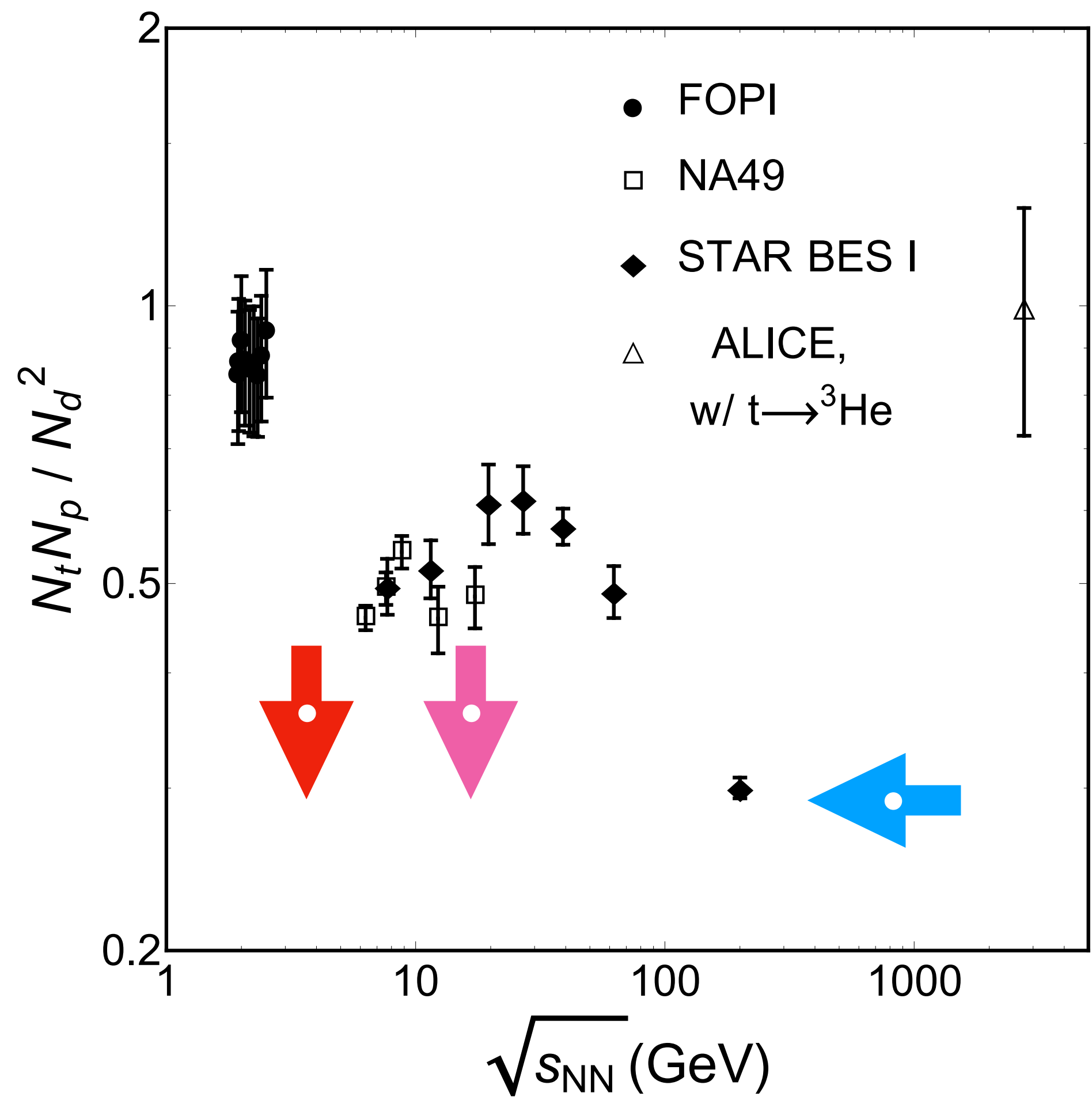
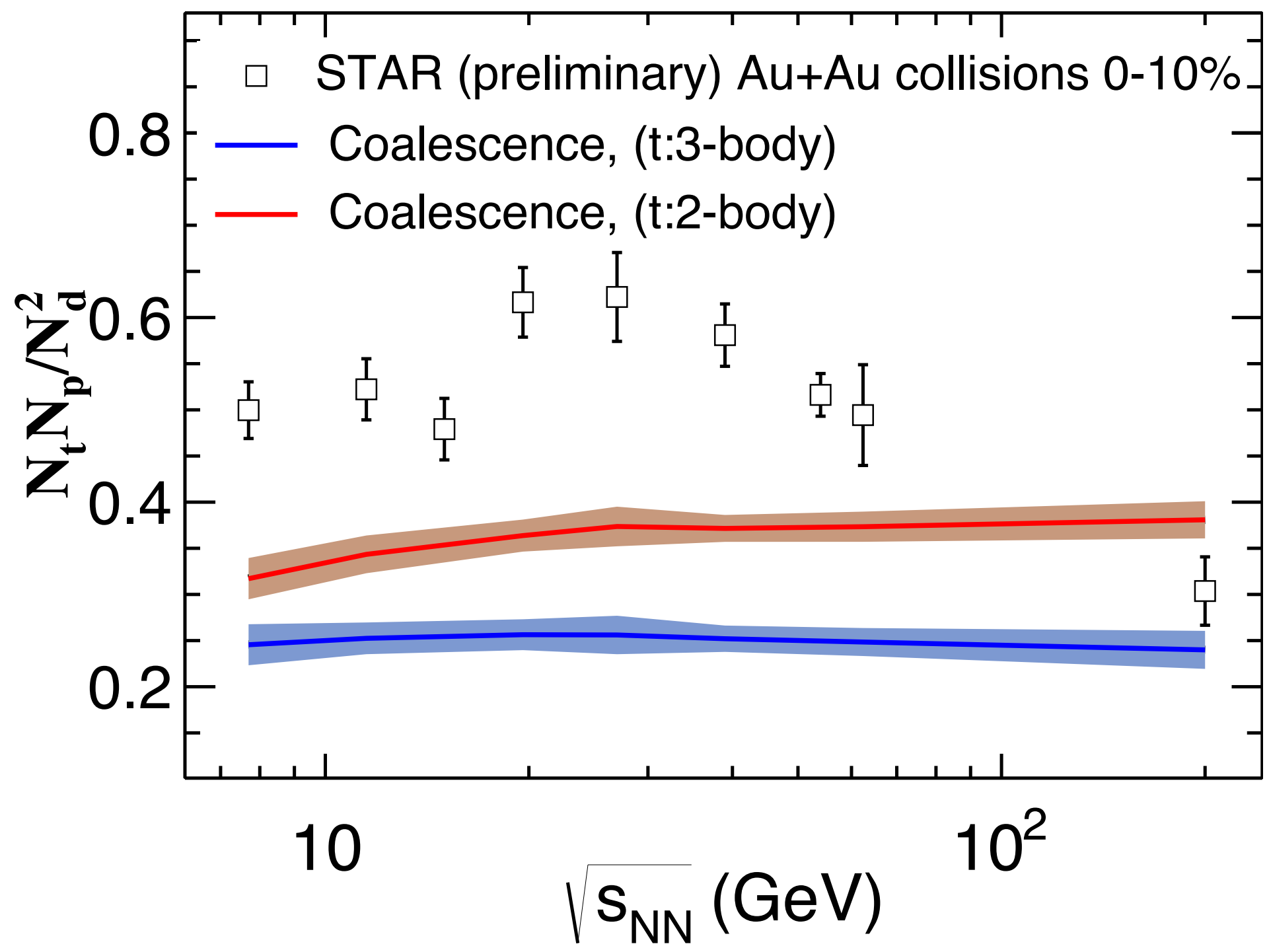
Wenbin Zhao,^{1,2,3,4} Chun Shen,^{5,6} Che Ming Ko,⁷ Quansheng Liu,^{1,2} and Huichao Song^{1,2,3}

Extra source of t is needed:
 4-N reclusters =>
 50 states of He4 =>
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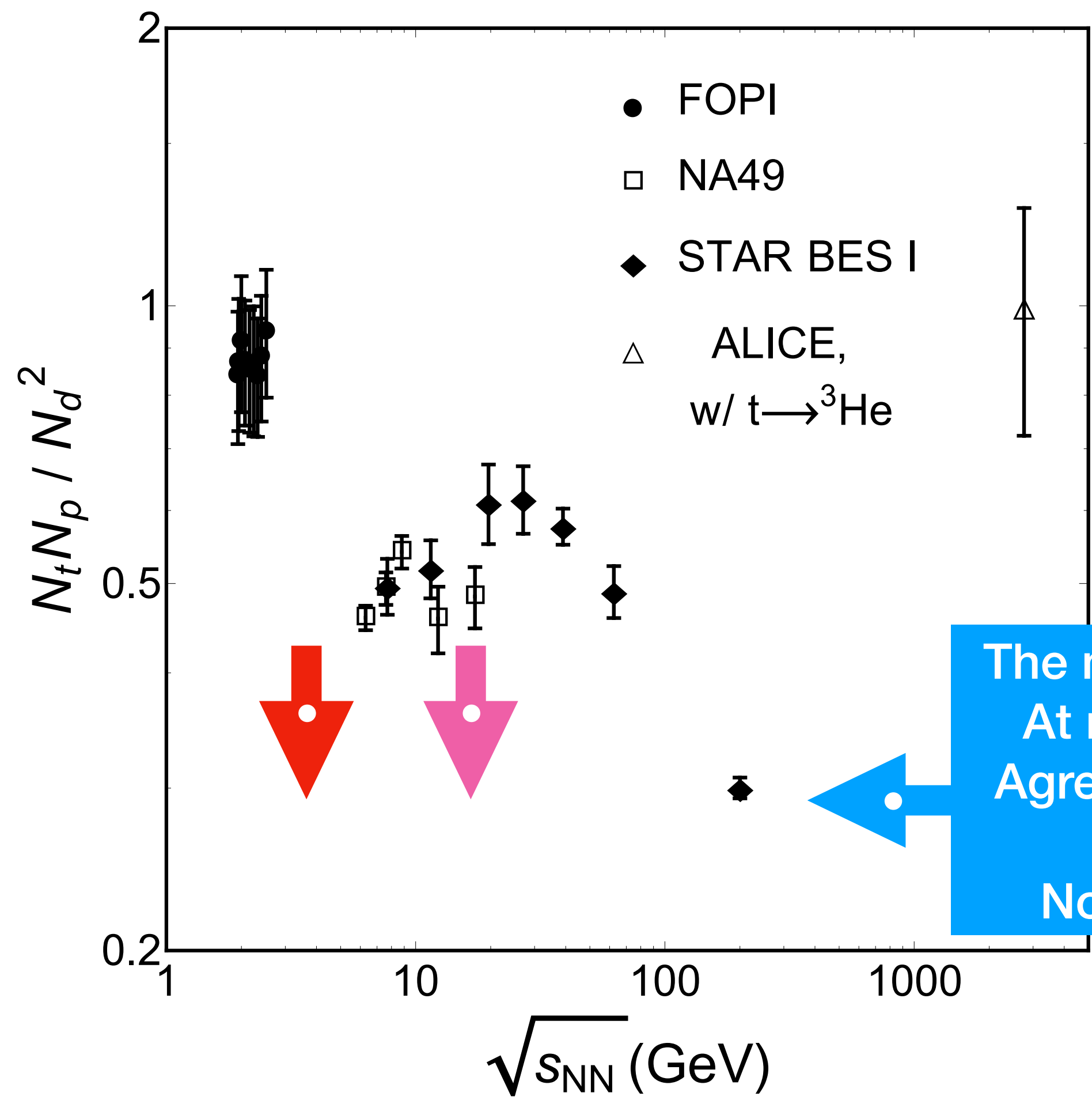
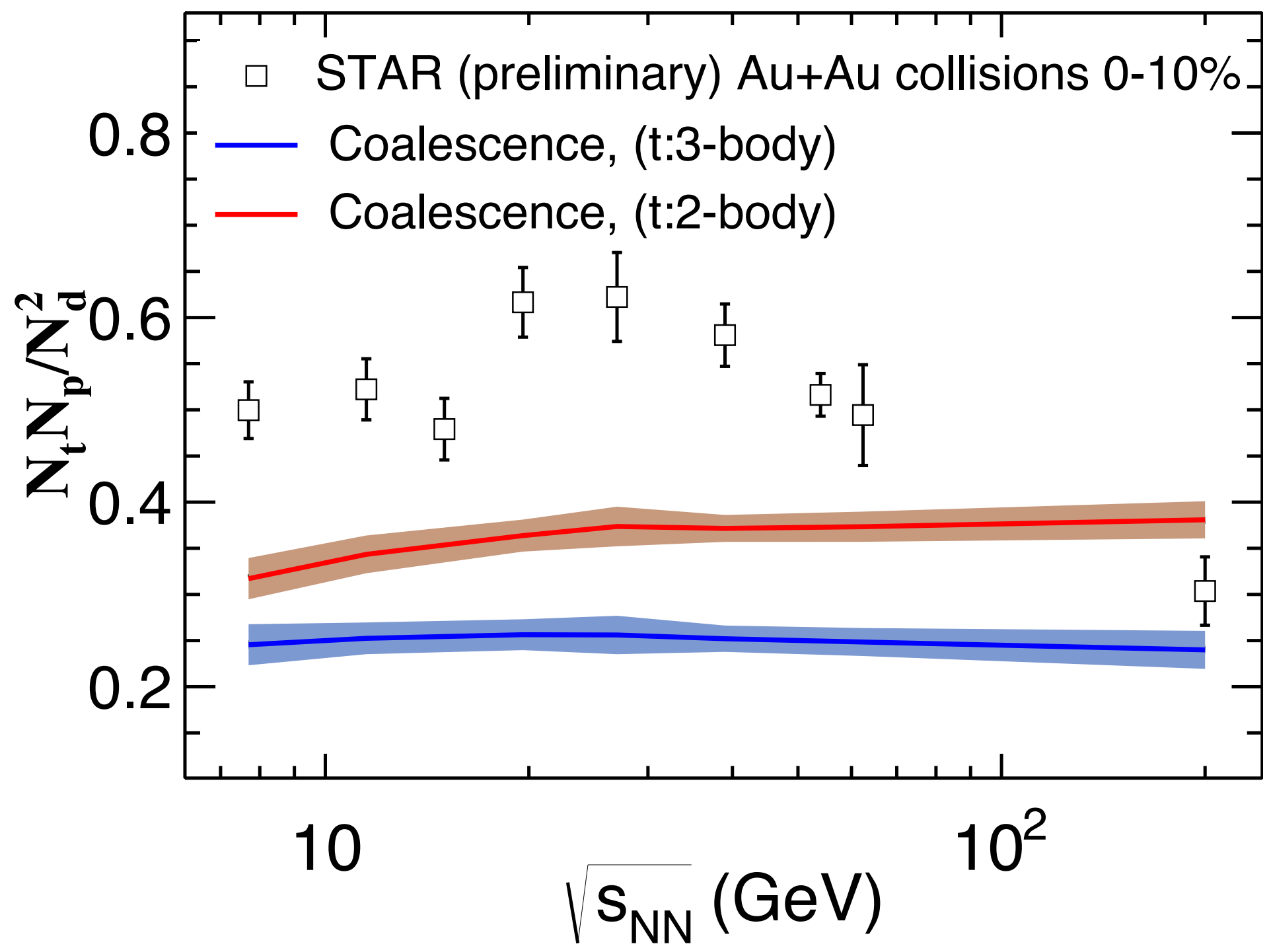
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 At main RHIC energy
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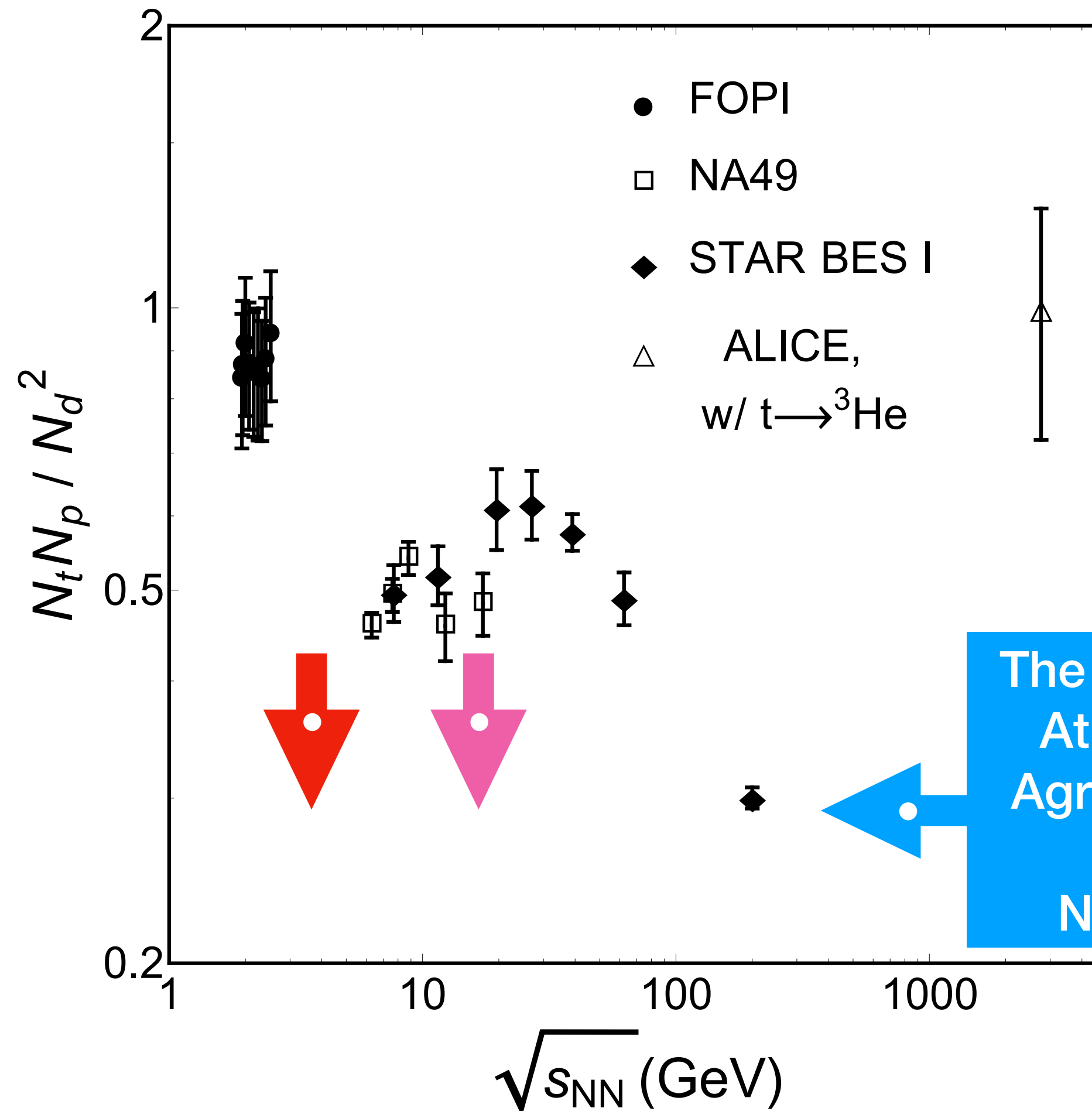
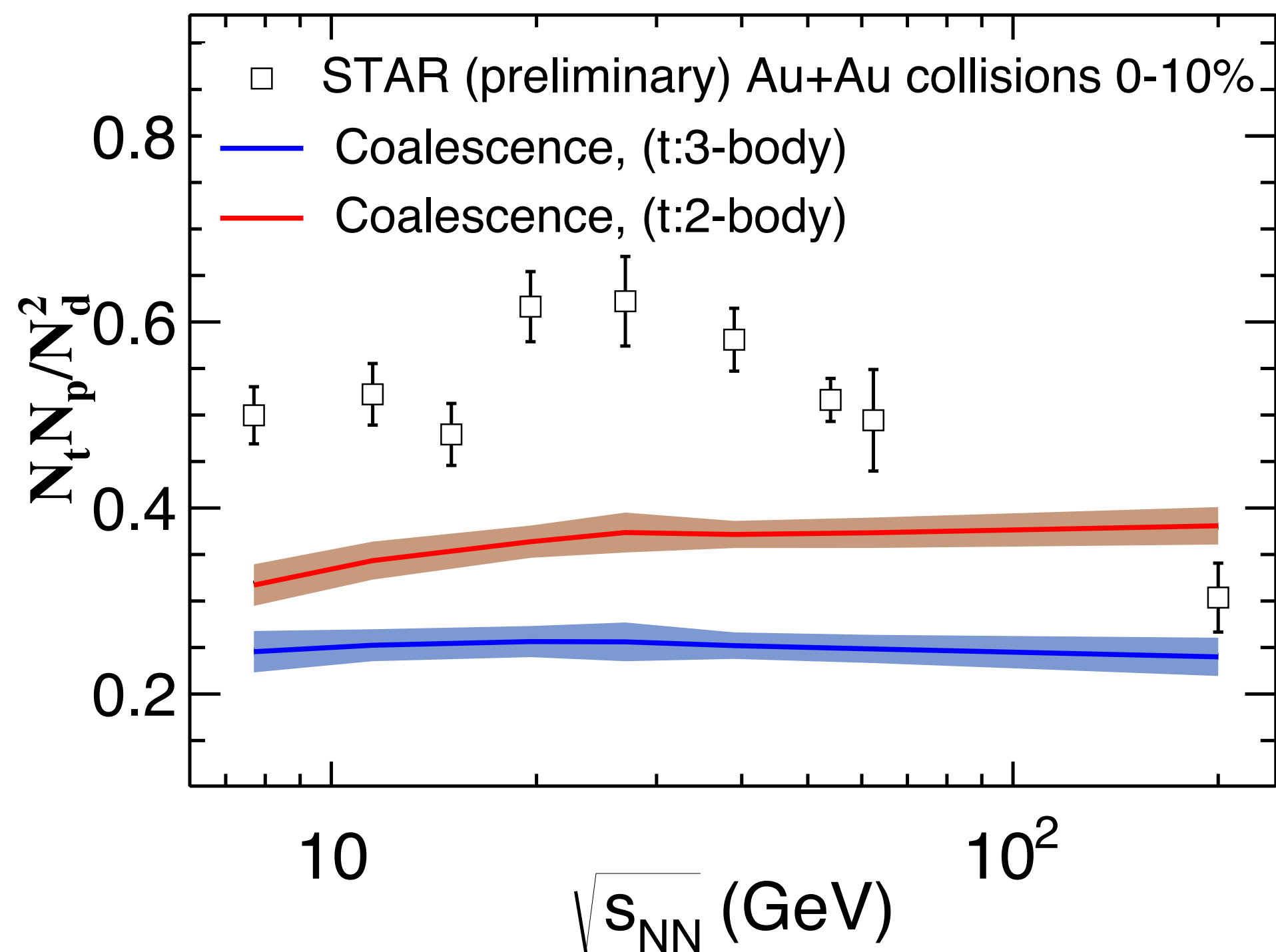
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