

# Testing anomalous $H - W$ couplings and Higgs self-couplings via double and triple Higgs production at $e^+e^-$ colliders

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# Introduction

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In the SM, the Higgs boson is part of an electroweak doublet. Gauge symmetry leads to some relations among its couplings:

$$V_{HHH}^{SM} = v V_{HHHH}^{SM}$$

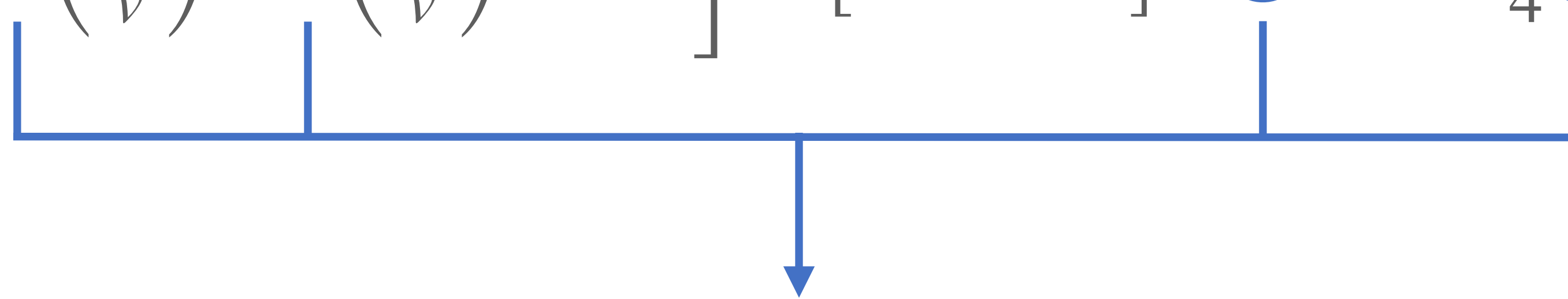
$$V_{HWW}^{SM} = v V_{HHWW}^{SM}$$

Deviations from this relations could point to new physics!

**EFTs are a useful tool to probe such BSM effects. In this work we will employ the Effective Chiral Lagrangian (EChL) and study its signals in  $e^+e^-$  colliders.**

# The EChL

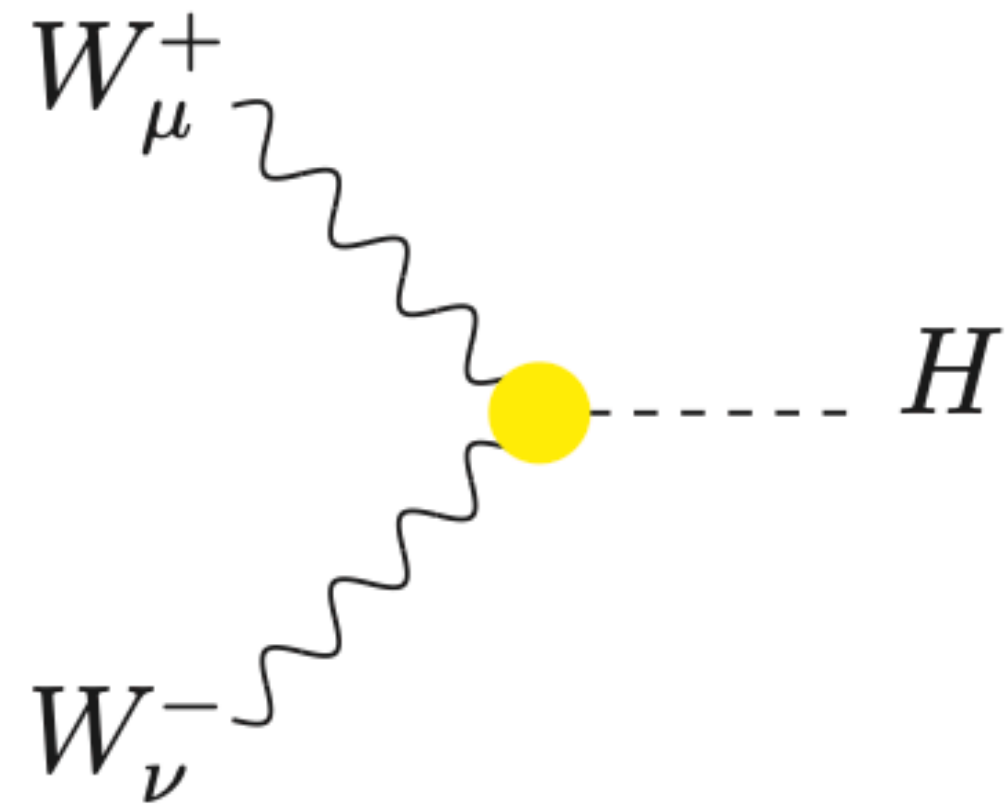
- The Higgs boson,  $H$ , is introduced as a singlet, being no longer part of a doublet.
- Thus, its triple and quartic couplings (to itself and to gauge bosons) are no longer correlated.
- The electroweak Goldstone bosons are placed in an exponential representation,  $U = \exp\left(\frac{i\vec{\omega}\vec{\tau}}{v}\right)$

$$\mathcal{L}_{\text{EChL}} \supset \frac{v^2}{4} \left[ 1 + 2a\left(\frac{H}{v}\right) + b\left(\frac{H}{v}\right)^2 + \dots \right] \text{Tr} \left[ D_\mu U^\dagger D^\mu U \right] - \kappa_3 \lambda v H^3 - \frac{1}{4} \kappa_4 \lambda H^4$$


Anomalous Higgs couplings: parametrize possible BSM effects.

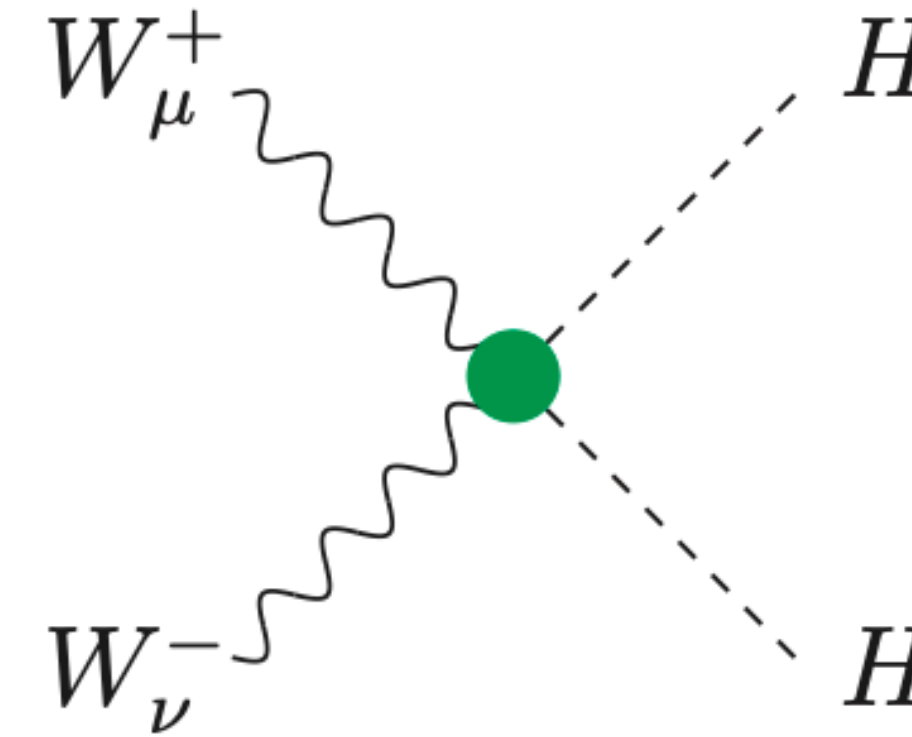
In the SM,  $a = b = \kappa_3 = \kappa_4 = 1$ , and the correlations are recovered.

# The EChL



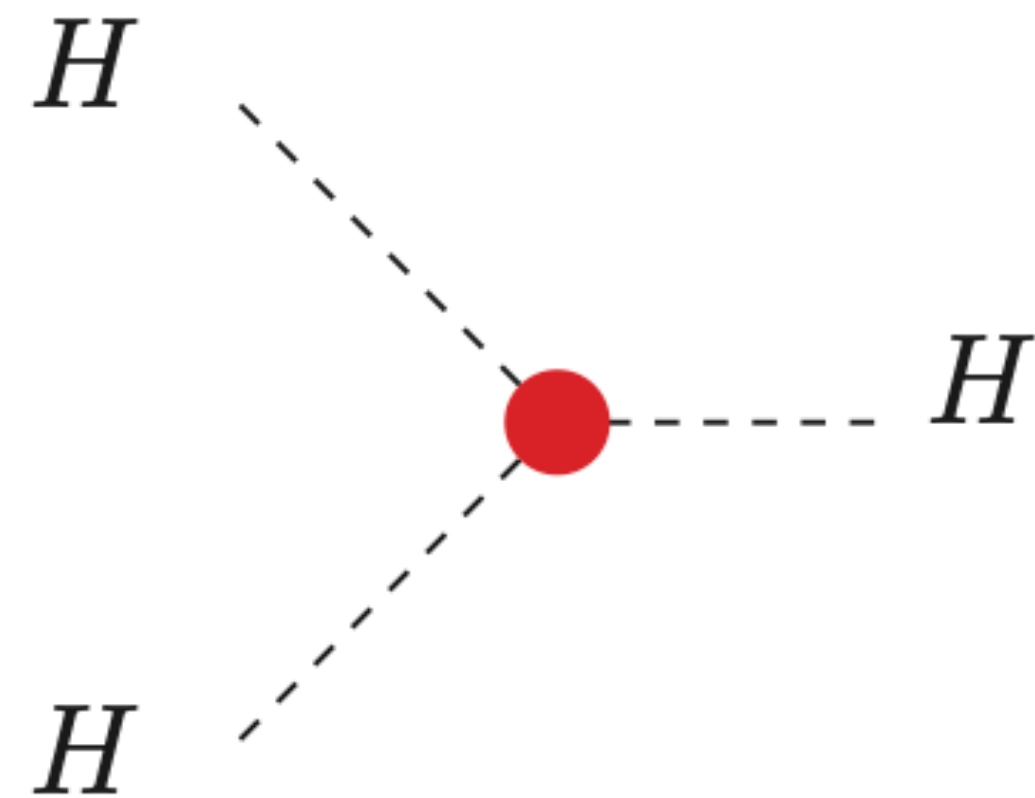
$$V_{WWH} = iagm_W g_{\mu\nu}$$

$$a^{\text{exp}} \in [0.97, 1.13]^{[1]}$$



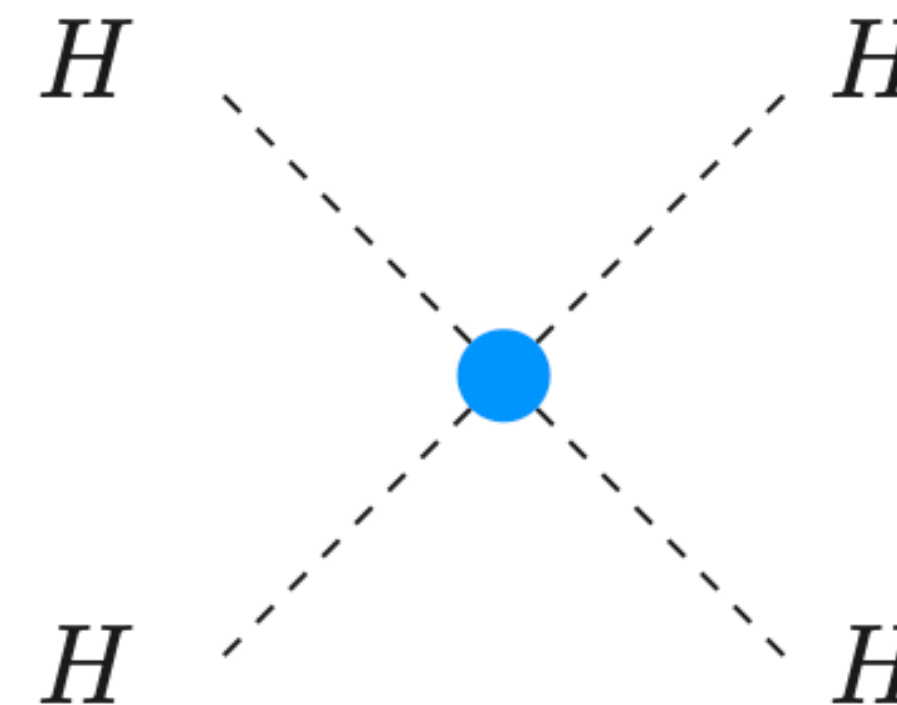
$$V_{WWHH} = \frac{ibg^2}{2} g_{\mu\nu}$$

$$b^{\text{exp}} \in [-0.76, 2.90]^{[2]}$$



$$V_{HHH} = -i\kappa_3 6\lambda$$

$$\kappa_3^{\text{exp}} \in [-2.3, 10.3]^{[3]}$$



$$V_{HHHH} = -i\kappa_4 6\lambda$$

$$\kappa_4^{\text{exp}} \in (-\infty, \infty)$$

<sup>[1]</sup>ATLAS, Phys. Rev. D **101** (2020) [1909.02845]

<sup>[2]</sup>ATLAS, JHEP **07** (2020) [2001.05178]

<sup>[3]</sup>ATLAS-CONF-2019-049

# Analysis strategy



We will study the sensitivity to BSM Higgs couplings in TeV-scale  $e^+e^-$  colliders, as they provide cleaner signals.

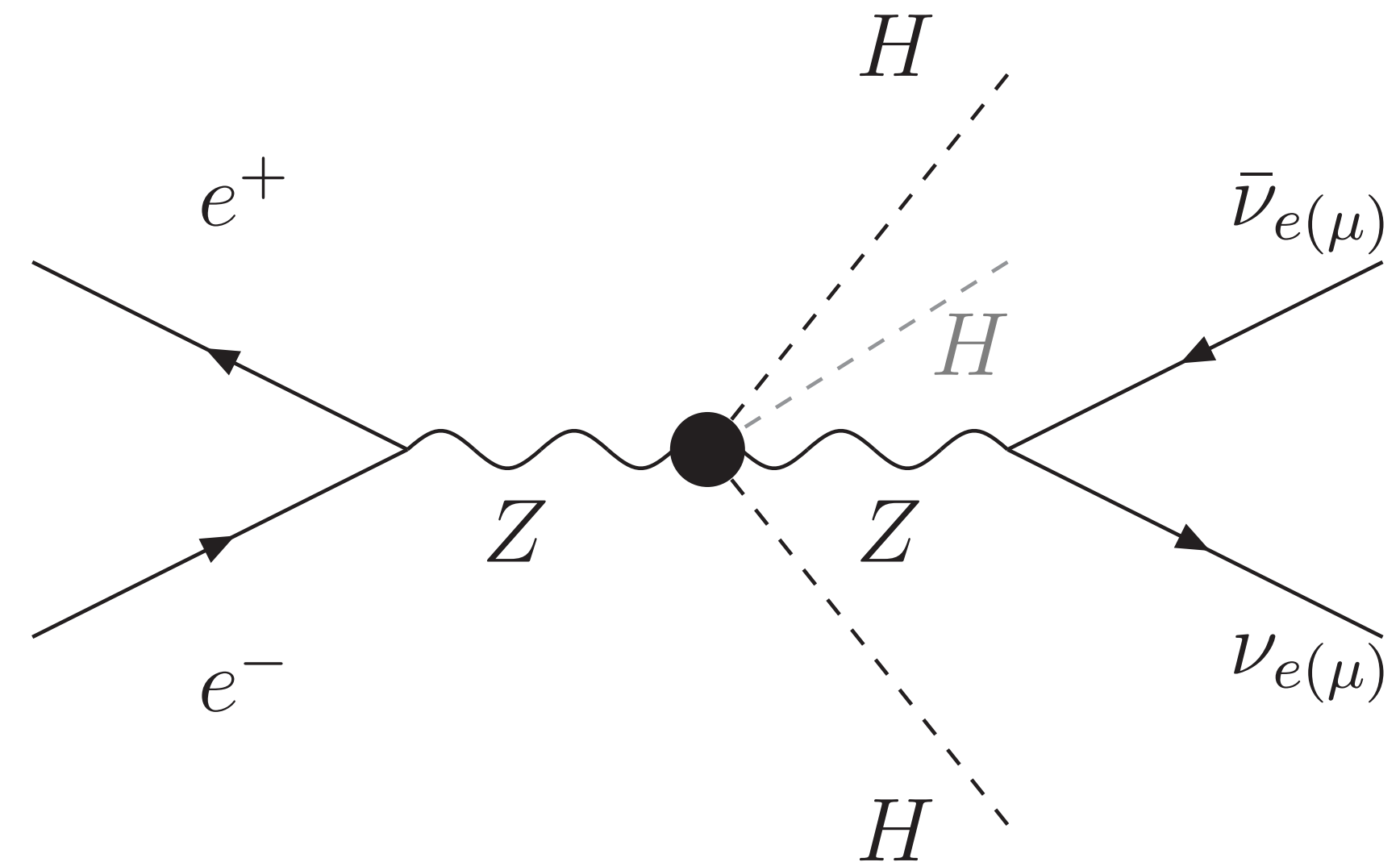
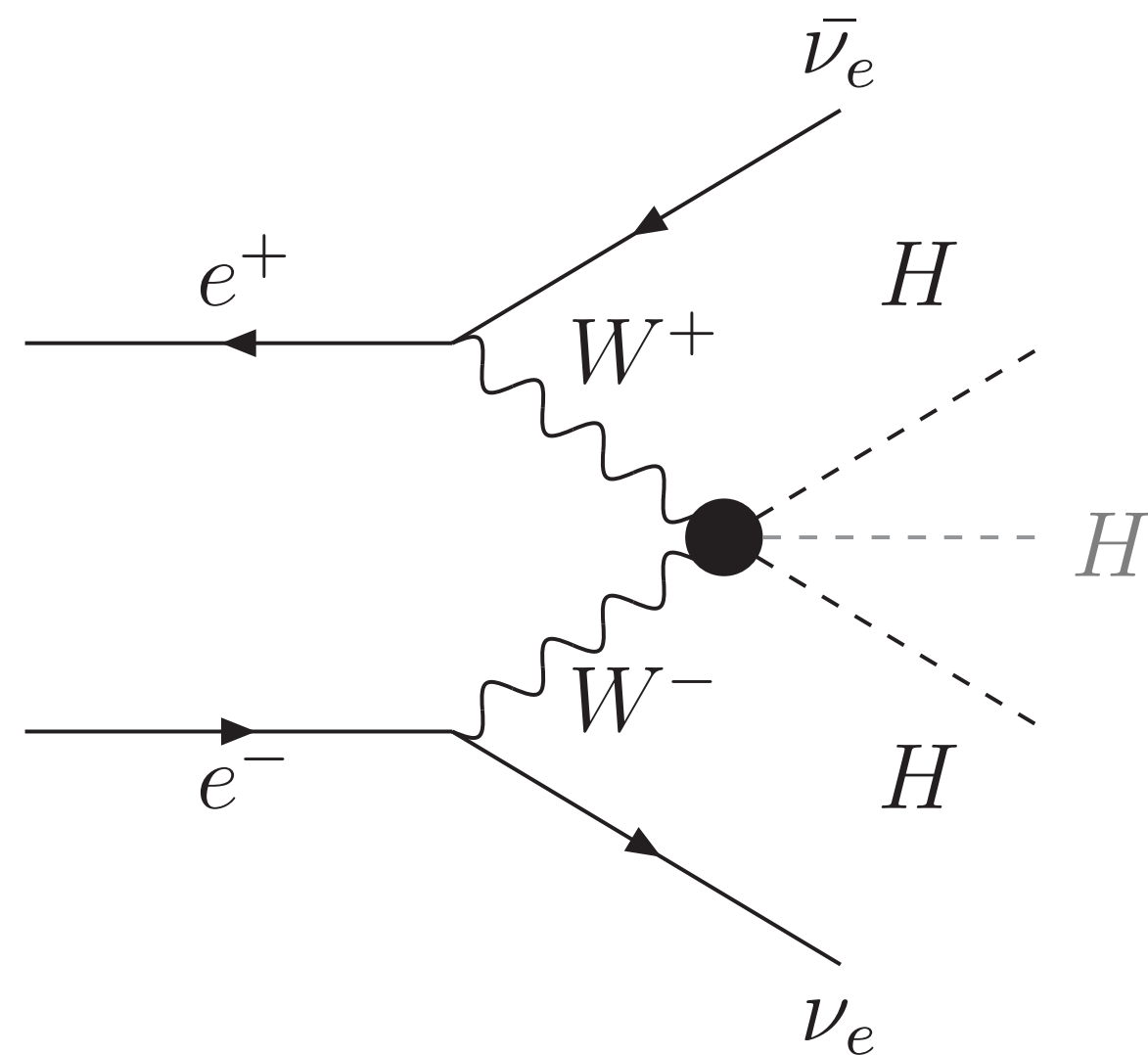
The process  $e^+e^- \rightarrow HH(H)\nu_e\bar{\nu}_e$  is dominated by  $WW$  scattering and, thus, particularly sensitive to anomalous Higgs couplings.

The problem will be factorized in two parts: the effects of  $a$  and  $b$  in  $HH$  production and those of  $\kappa_3$  and  $\kappa_4$  in  $HHH$  production.

Cross sections at the subprocess level will be computed via FeynArts and FormCalc, whereas MadGraph5 will be employed for those at the collider level.

# The role of $WW$ scattering

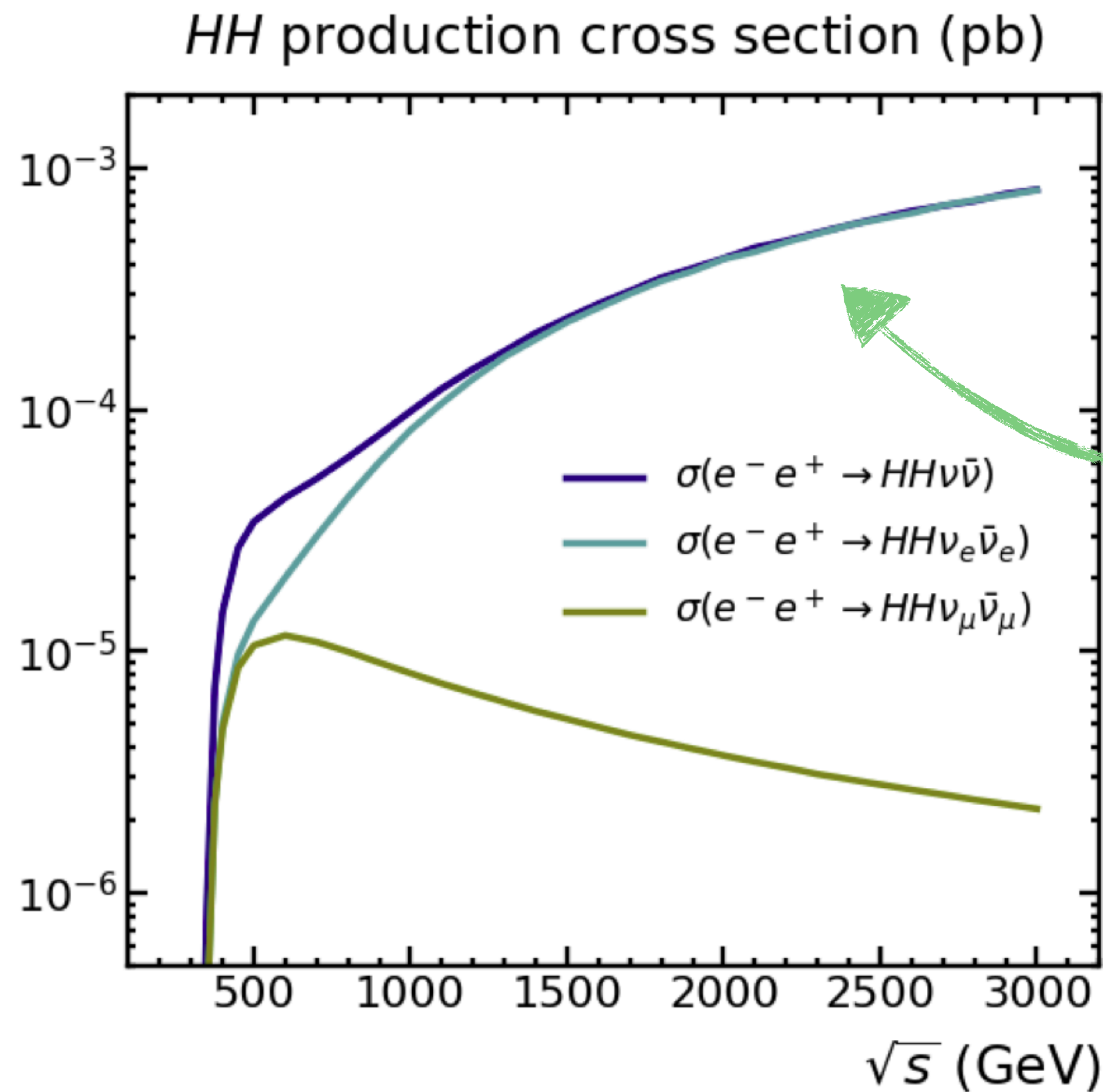
Multi-Higgs production at  $e^+e^-$  colliders may be mediated by VBS or by  $Z$  bosons produced in  $s$ -channel.



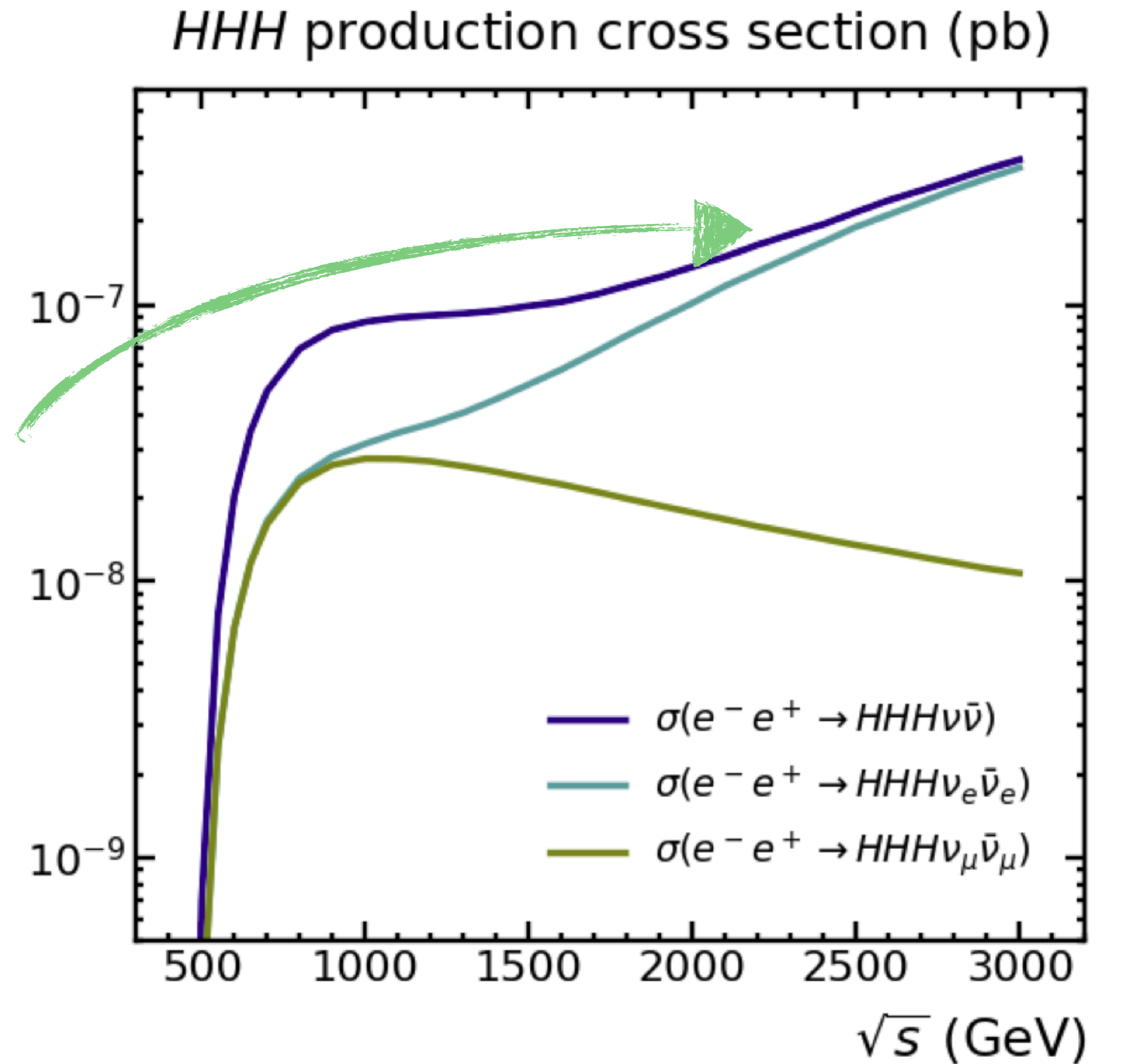
Identifying the dominant subprocesses is key to studying the sensitivity to the anomalous couplings.



# The role of $WW$ scattering

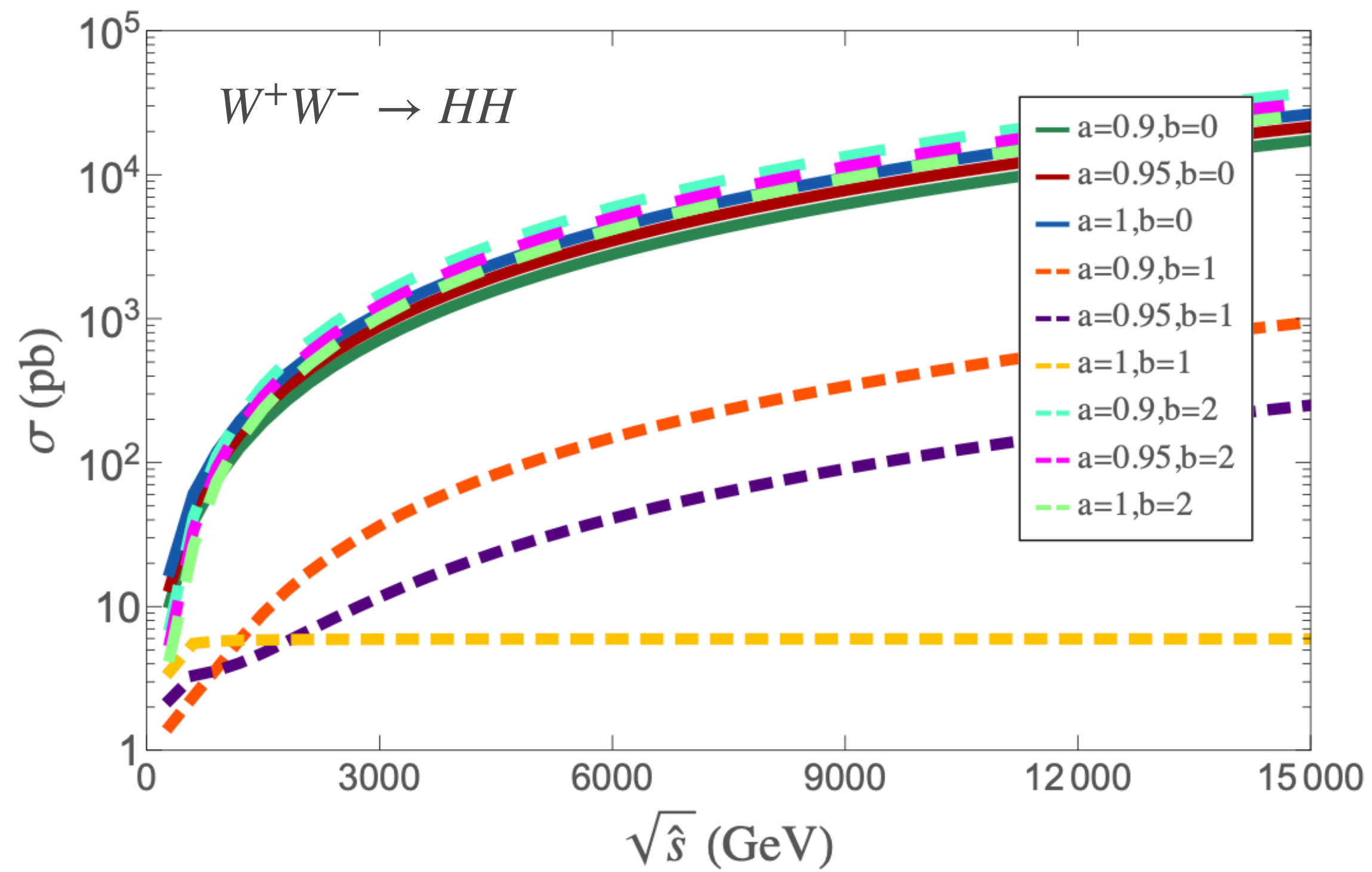


High-energy  
dominance of  
 $WW$ S!

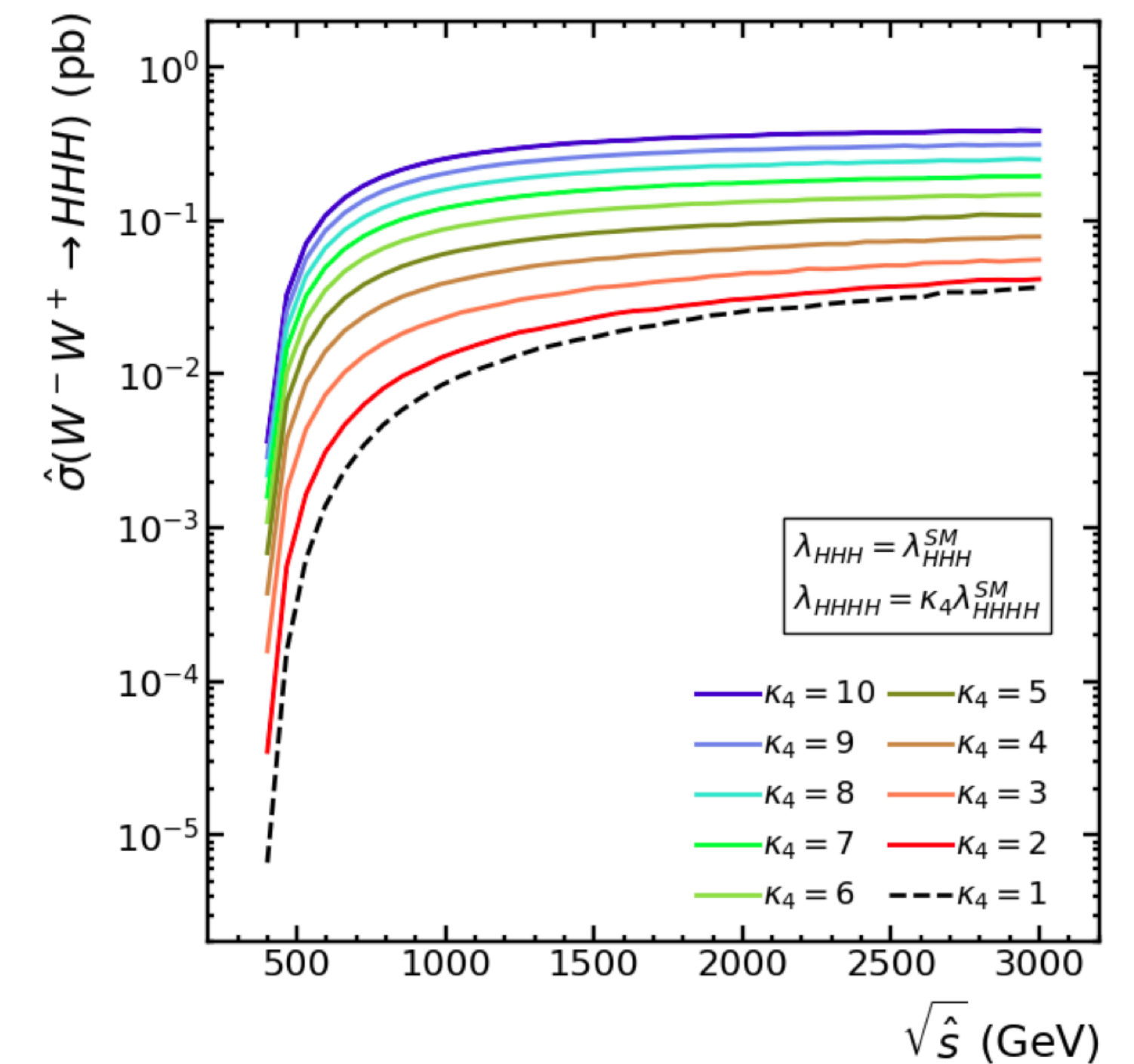
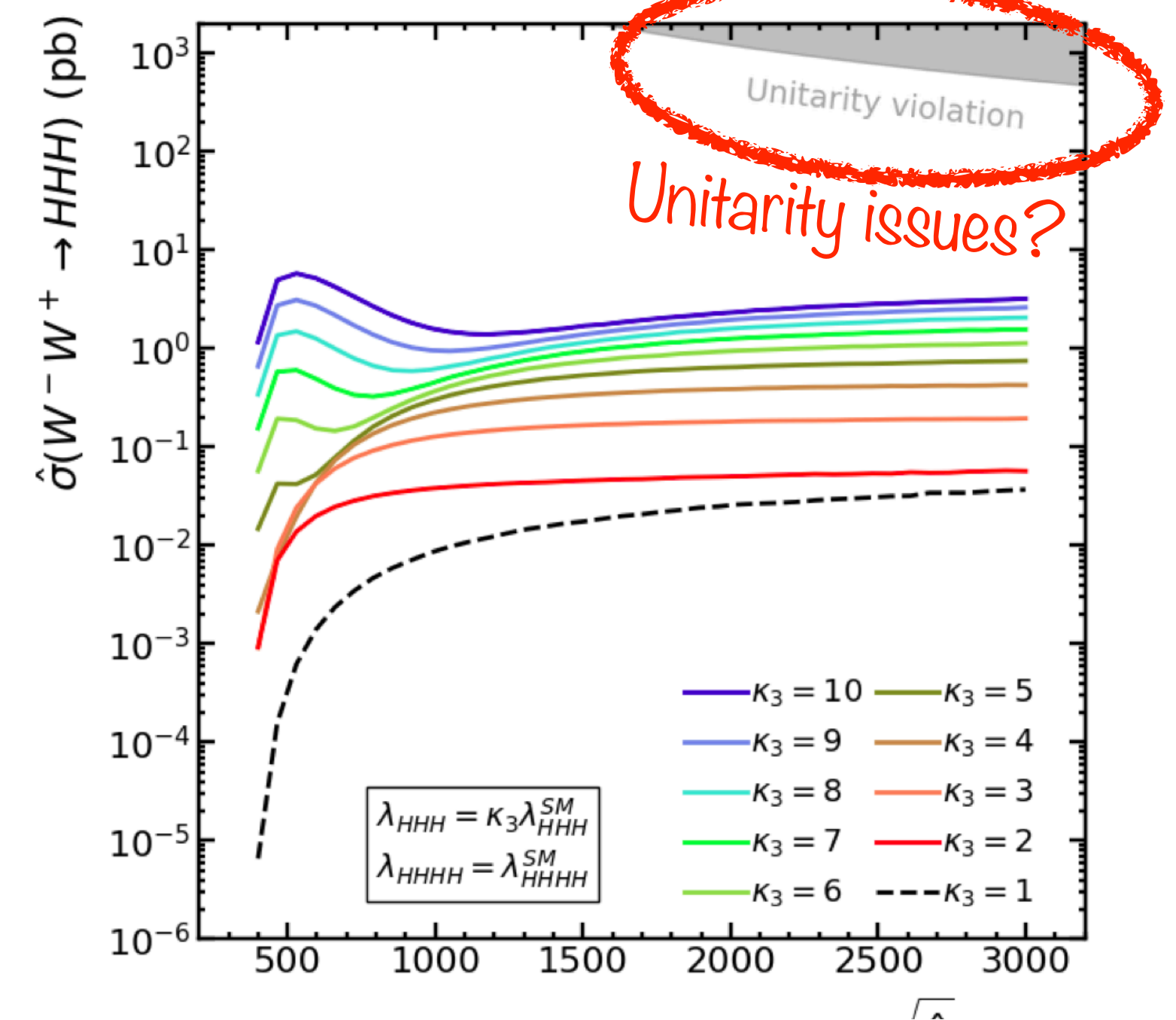


This is only a theoretical exercise! Neutrino flavors cannot be measured at colliders.

# BSM effects at subprocess level



Anomalous couplings  
induce a large cross  
section enhancement



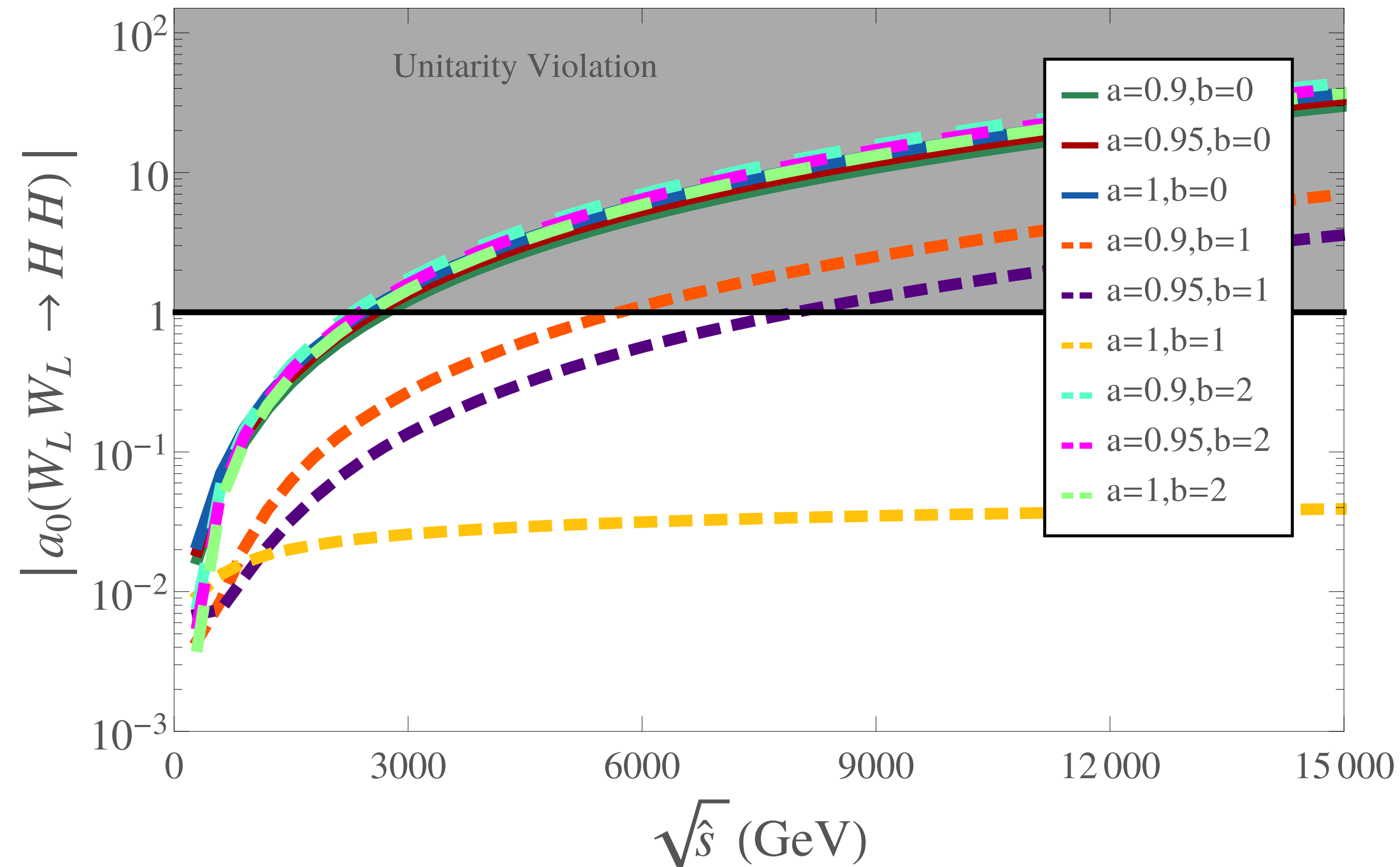


# Unitarity issues?

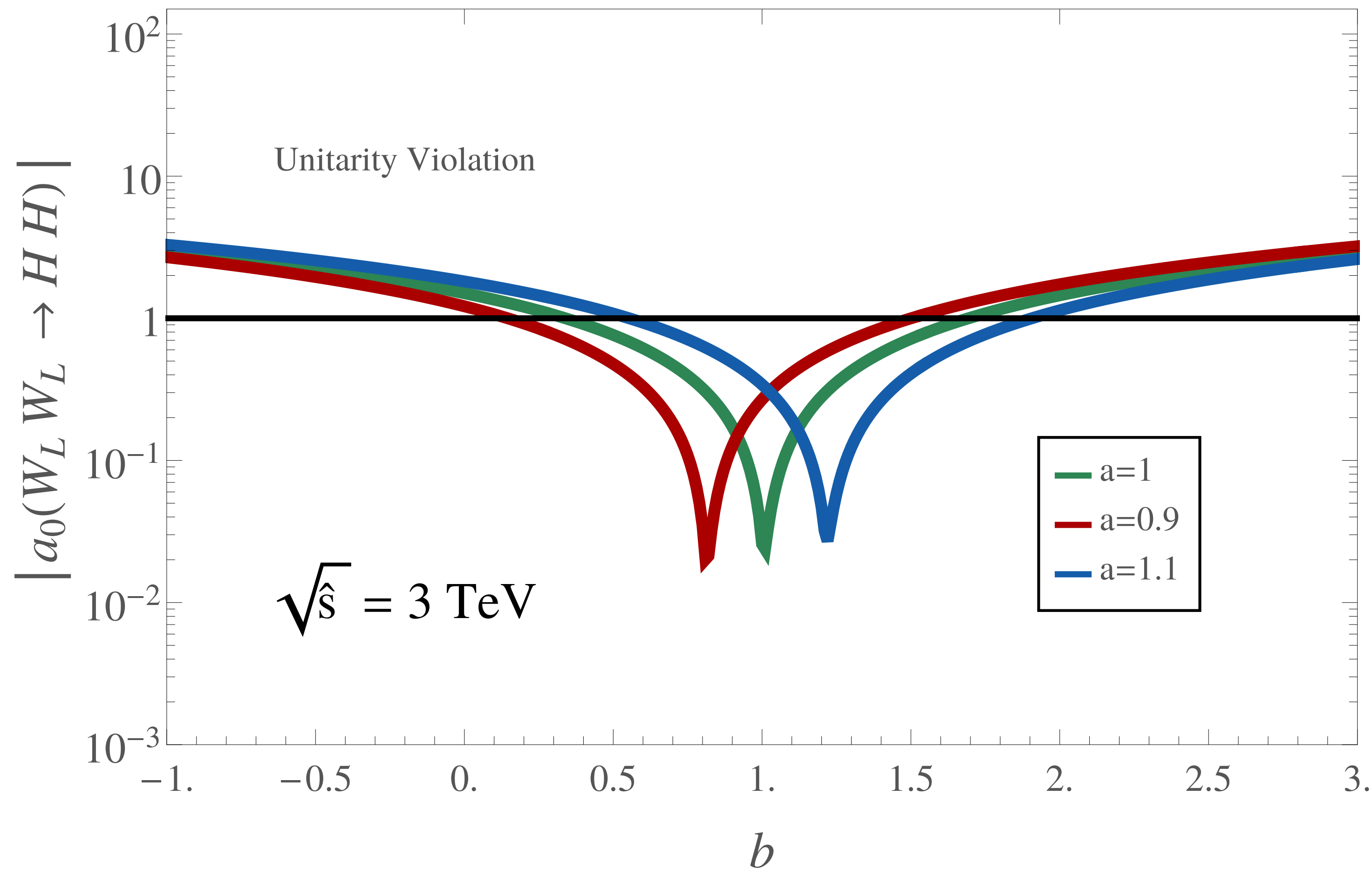
- ✓ Triple Higgs production cross sections are small enough to keep unitarity even for large anomalous couplings.
- ?
- Also the case for double Higgs production?

# Unitarity issues?

✗ Double Higgs cross sections grow beyond unitarity for large  $a$  and/or  $b$ . Some limits can be inferred.

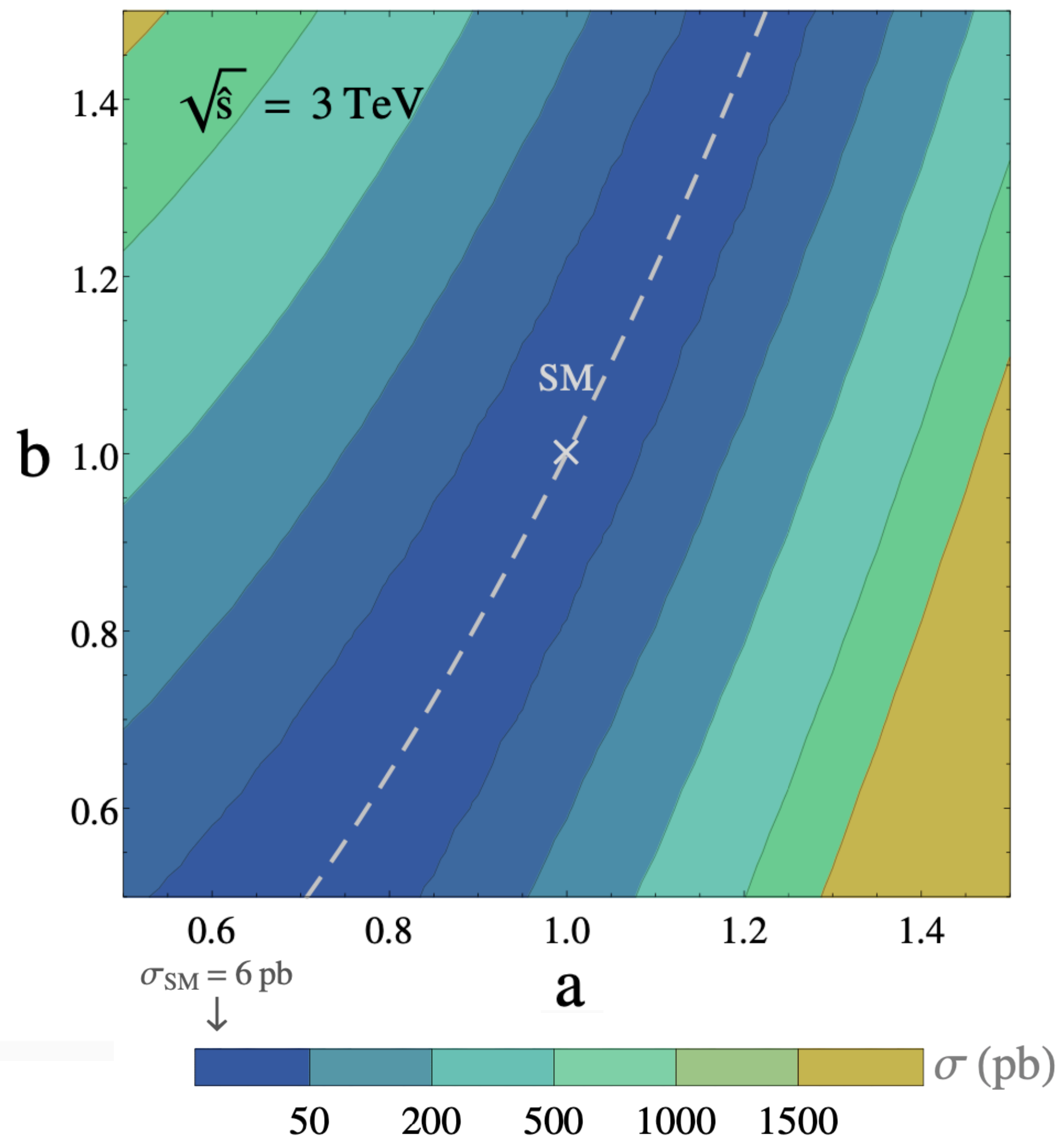


# Unitarity issues?

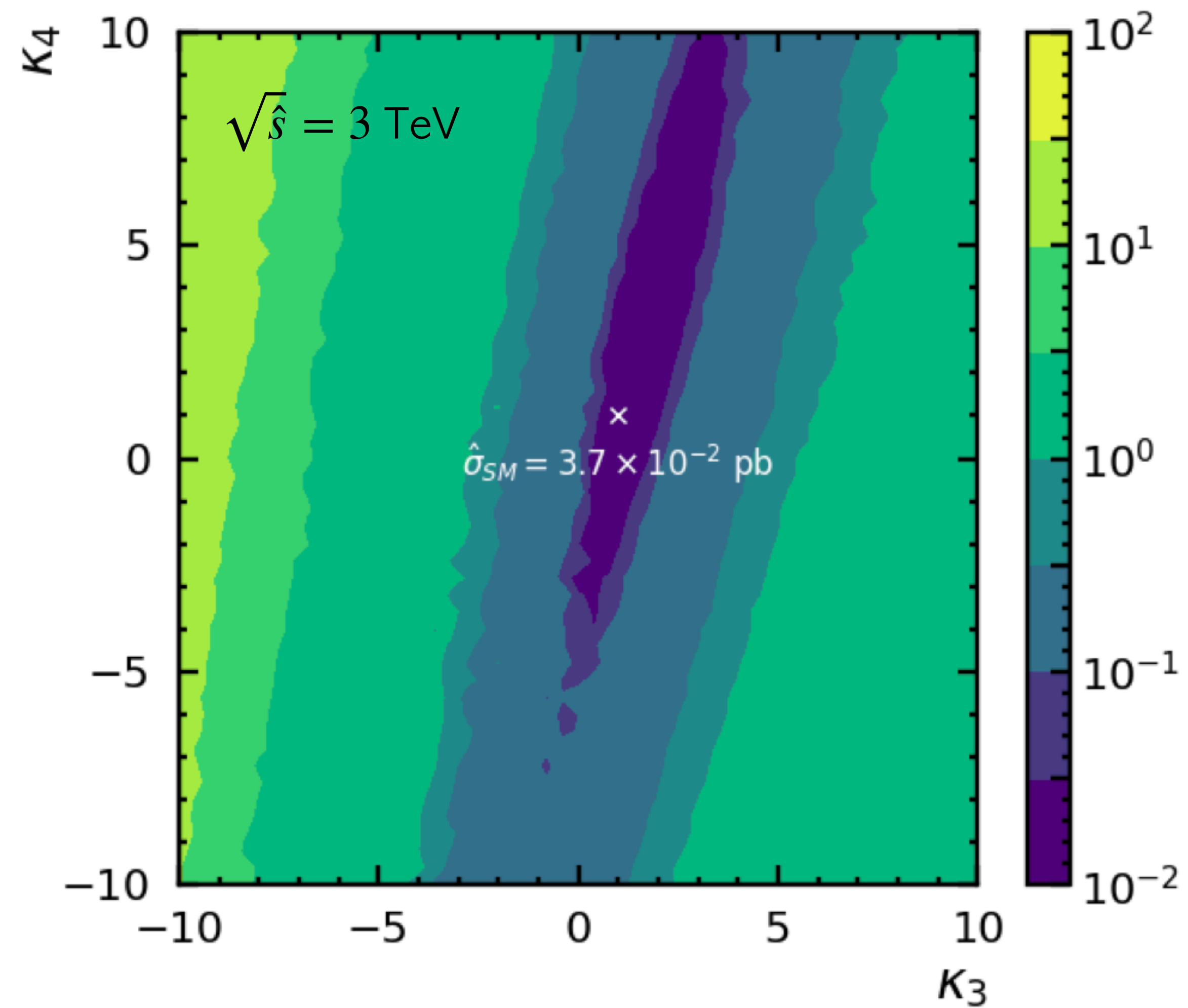


We will stay within  
the range  
 $b \in [0.5, 1.5]$ .  
Experimental  
constraints on  $a$  are  
stronger than any  
that could be derived  
from unitarity.

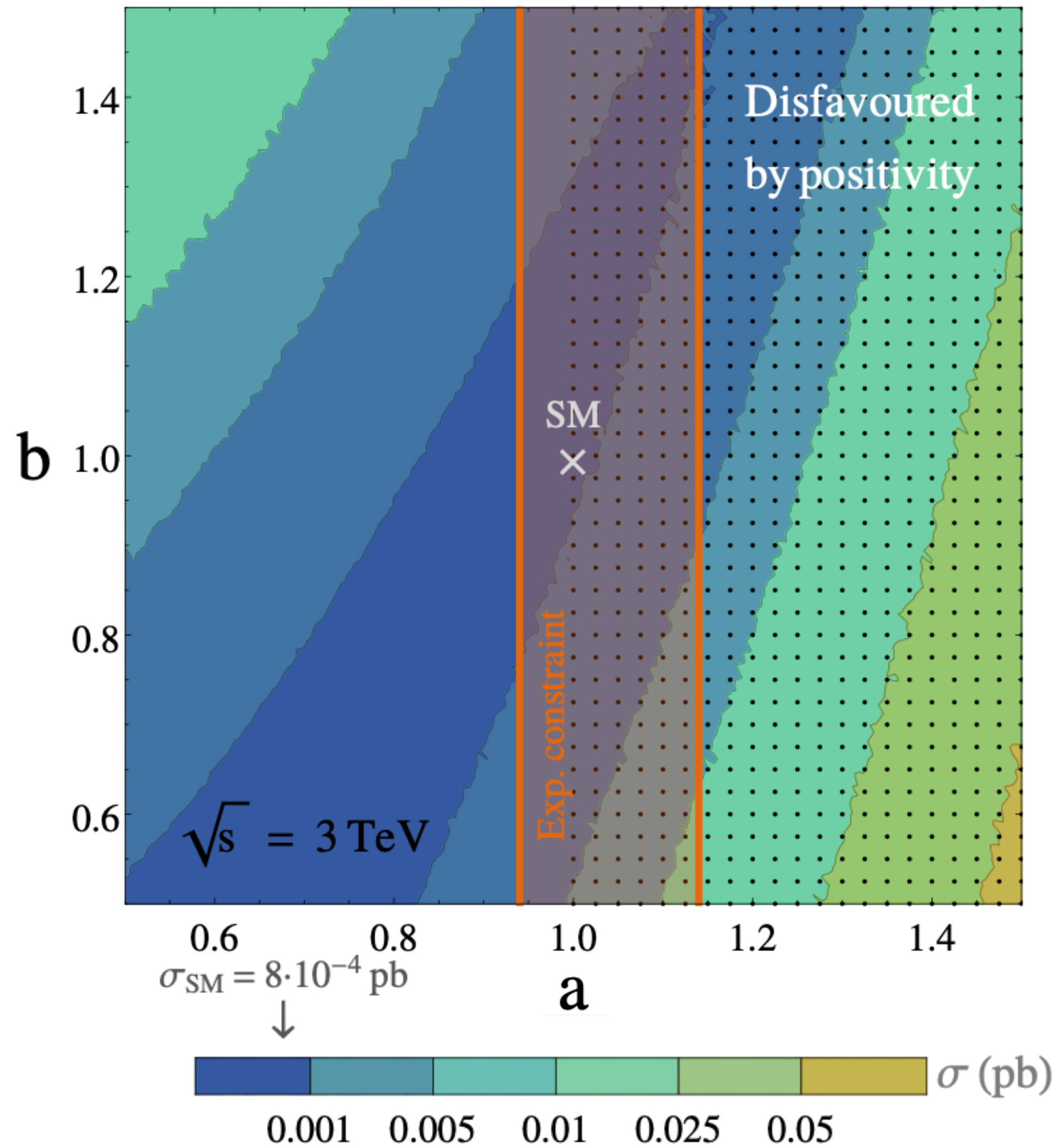
$$W^+W^- \rightarrow HH$$



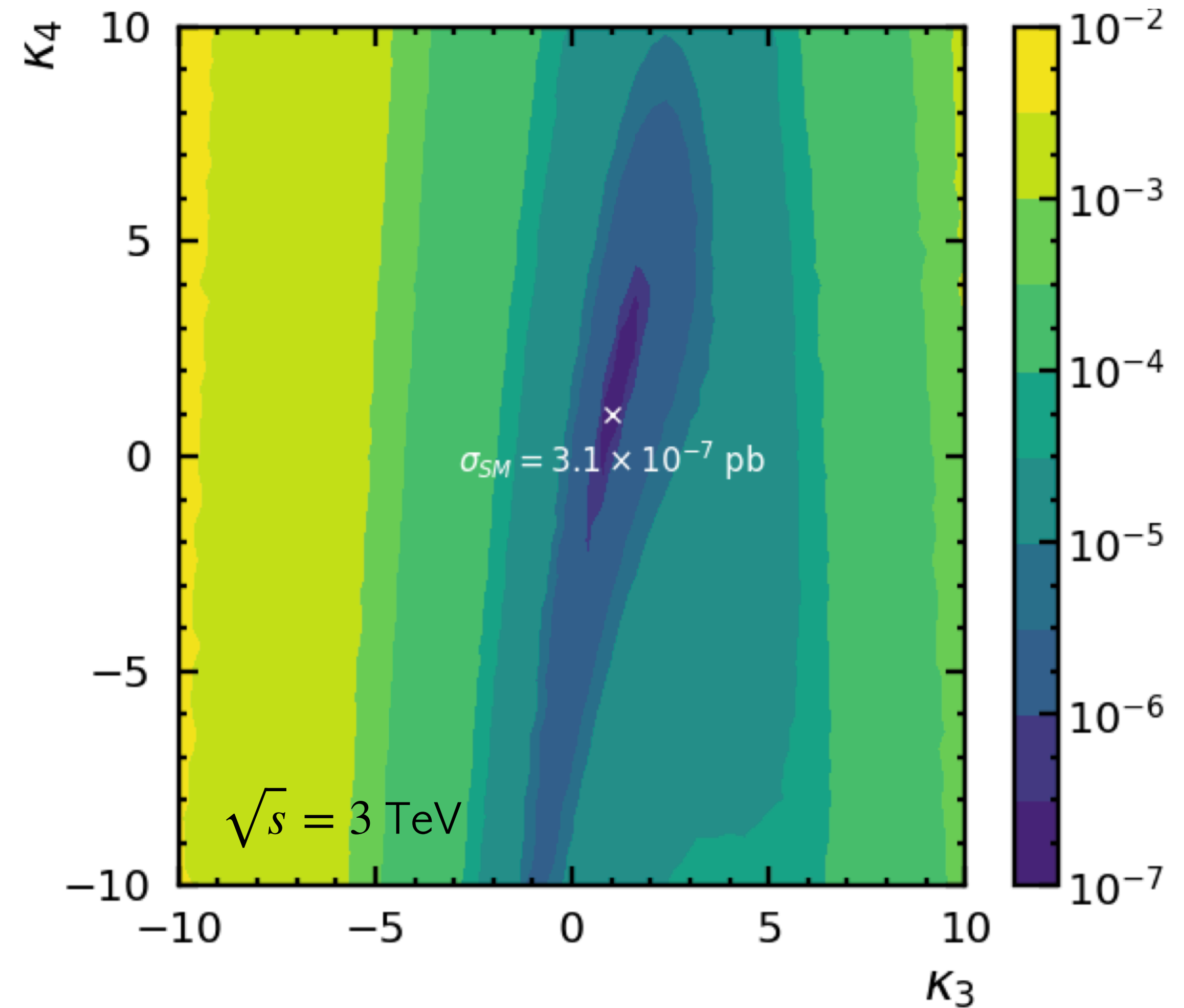
$$W^+W^- \rightarrow HHH$$



$$e^+e^- \rightarrow HH\bar{\nu}_e\nu_e$$



$$e^+e^- \rightarrow HHH\bar{\nu}_e\nu_e$$



The behavior of the subprocess is inherited due to WWS dominance

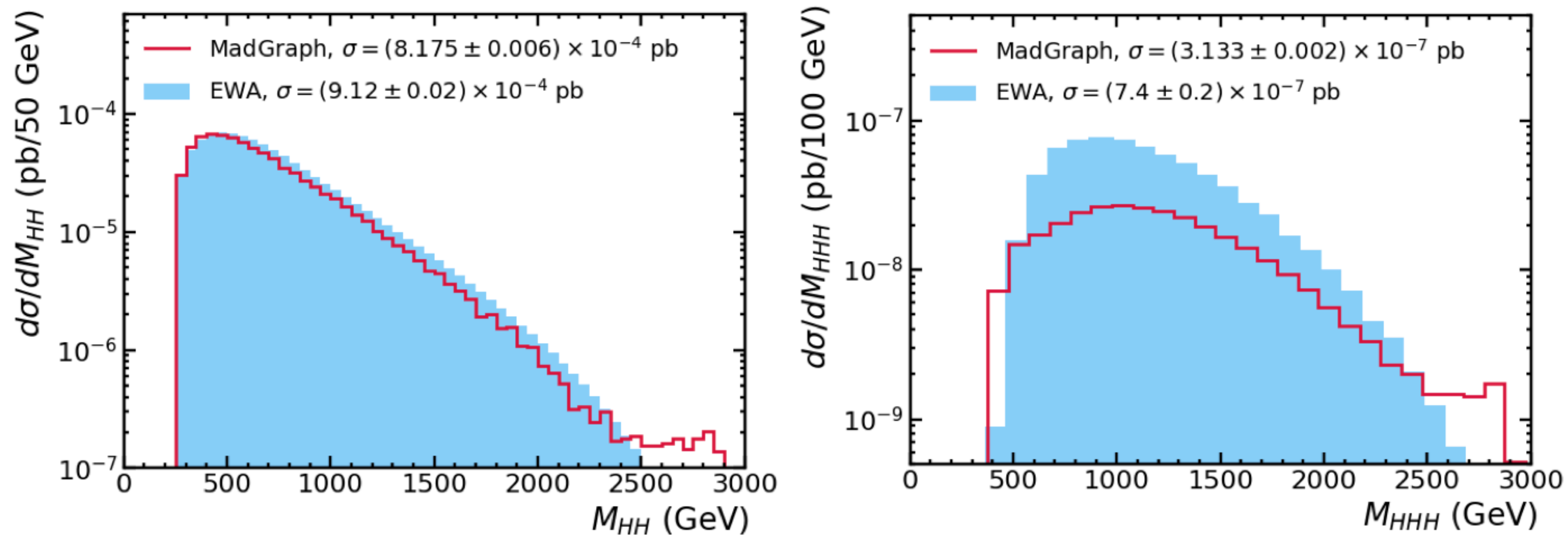


# The effective $W$ approximation

$W$ 's are treated as partons inside electrons. Their “PDFs” allow to compute full cross sections from subprocess.<sup>[4]</sup>

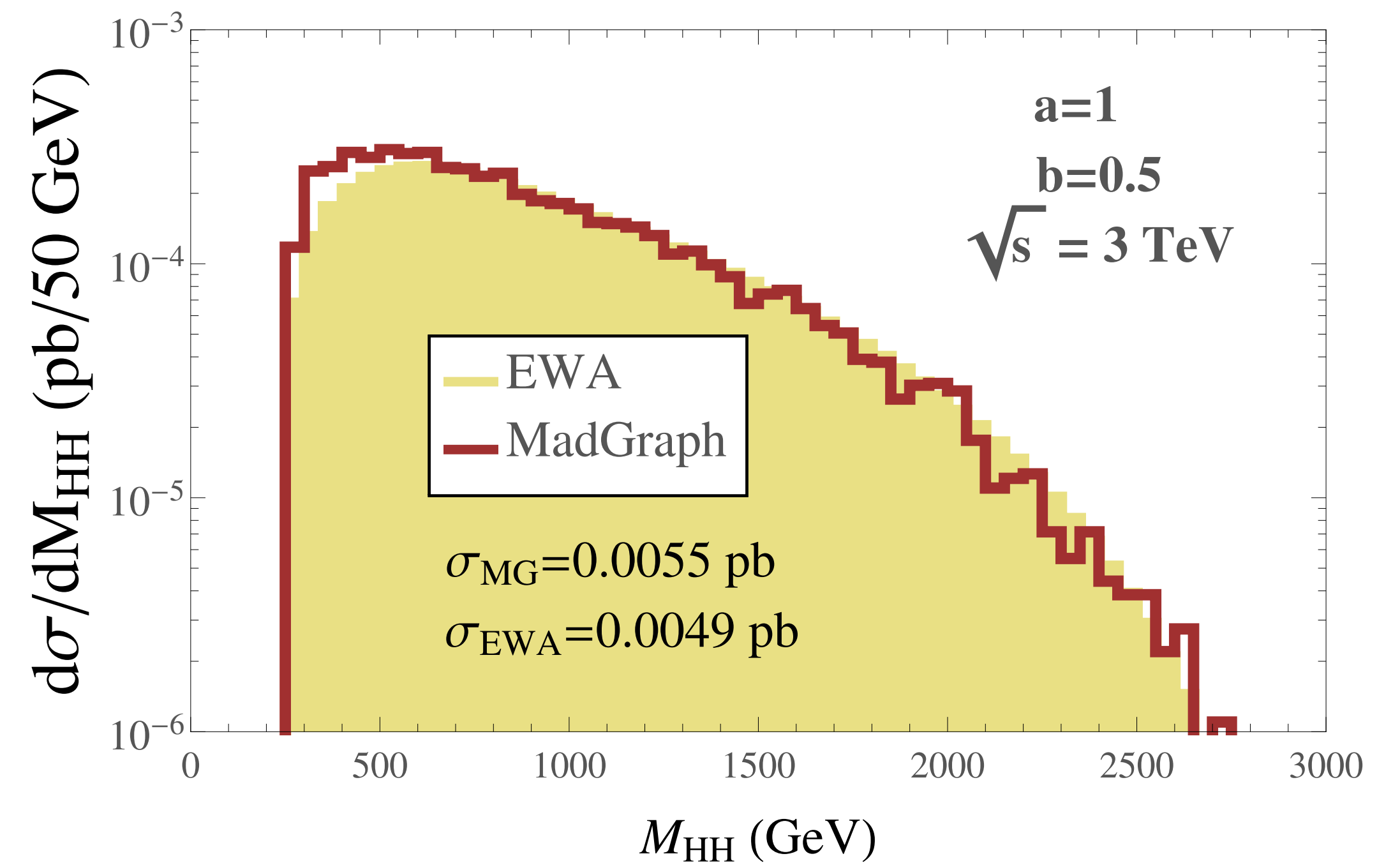
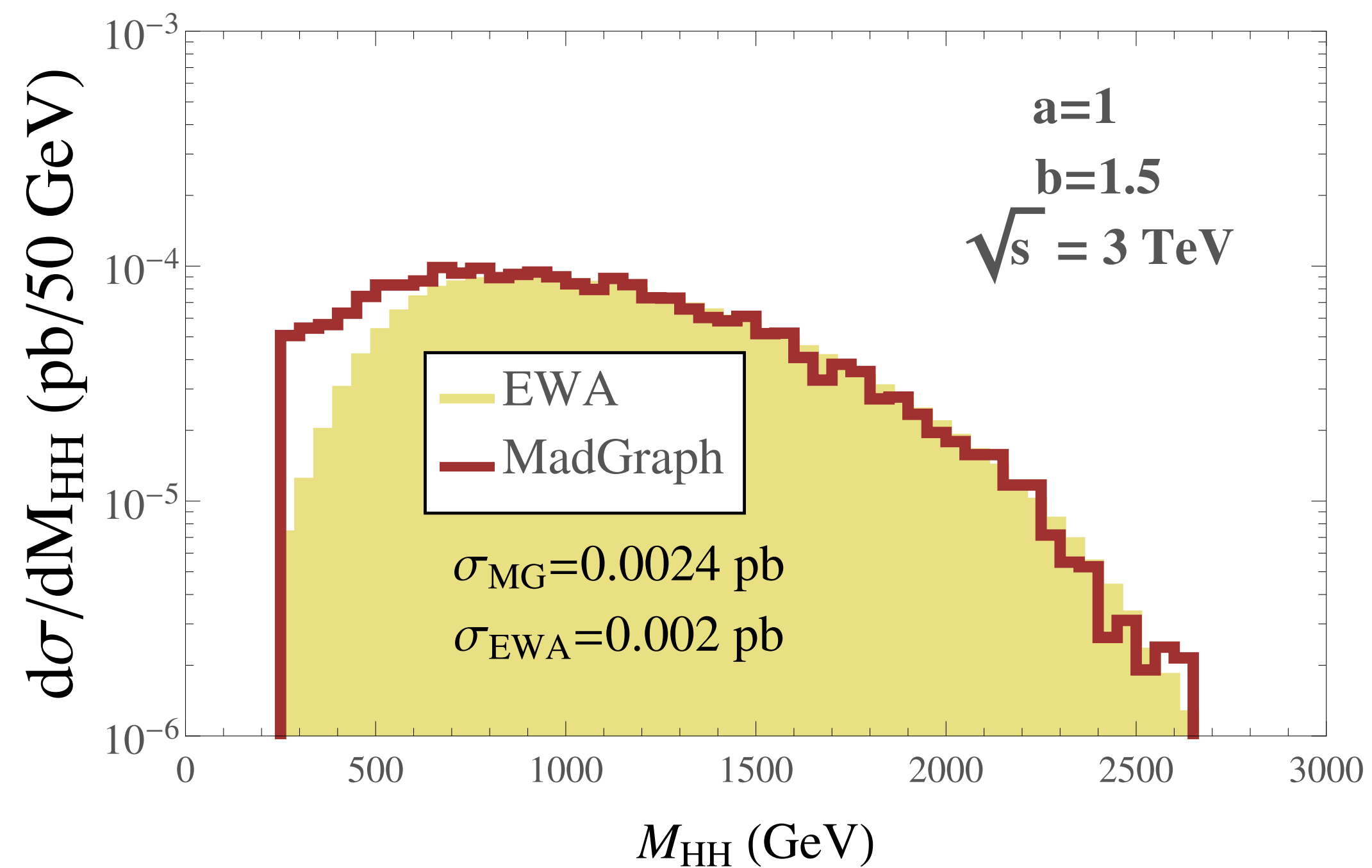
<sup>[4]</sup>S. Dawson, Nucl. Phys. B **249** (1985)

$$\sigma(e^+e^- \rightarrow HH\nu\bar{\nu}) = \int dx_1 \int dx_2 f(x_1)f(x_2)\hat{\sigma}(W^+W^- \rightarrow HH)$$



Good approximation for  $HH$ , not so good for  $HHH$

# The effective $W$ approximation



Even better approach for BSM!



**Final  
results**

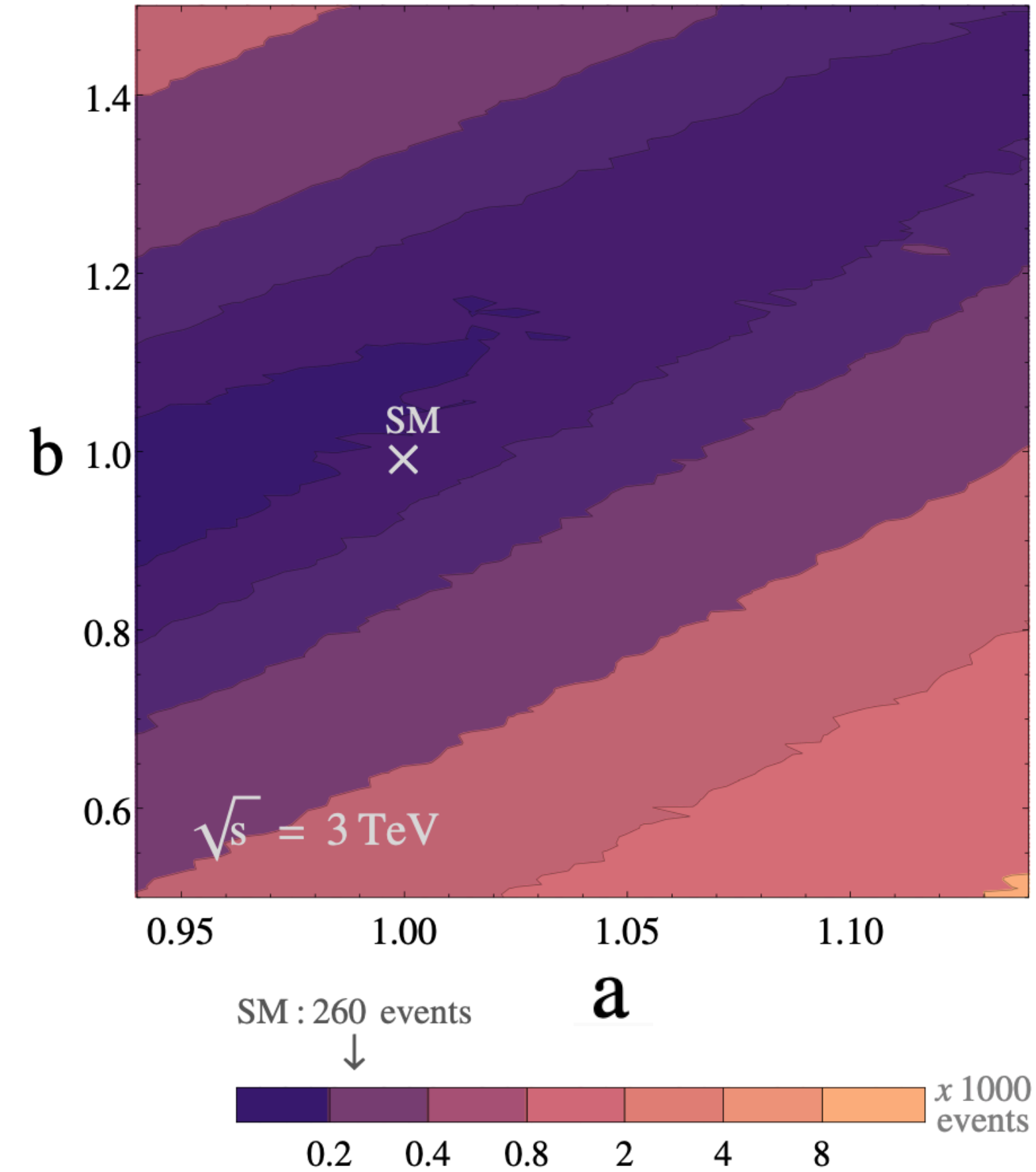
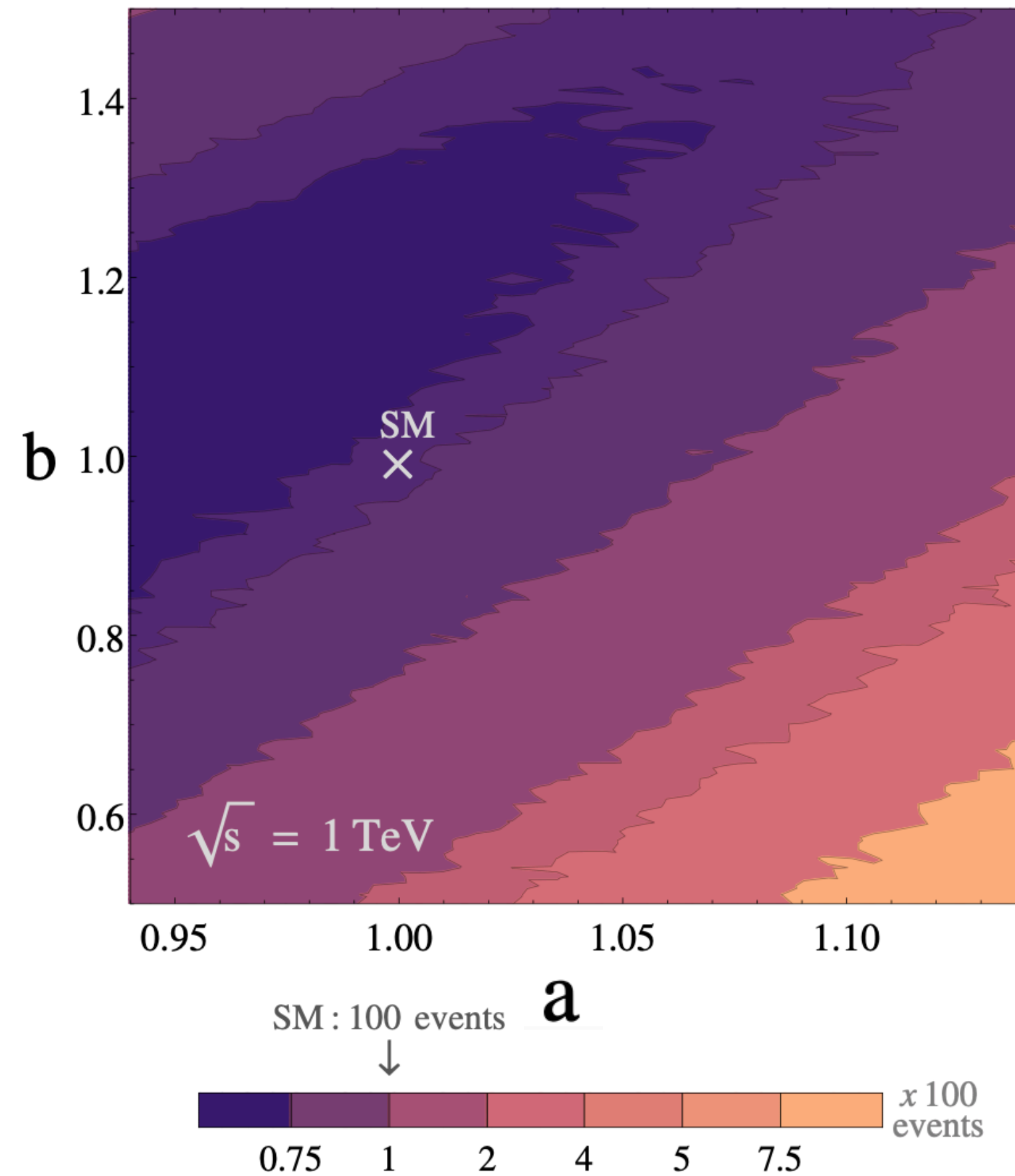
We choose the main Higgs decay channel,  $H \rightarrow b\bar{b}$ . The final states will consist of  $b$ -jets and missing energy.

No background simulations are performed. Proper cuts and the presence of neutrinos may reduce backgrounds to negligible levels.

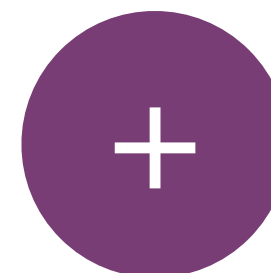
We will focus on the ILC (1 TeV, 8 ab<sup>-1</sup>) and CLIC (3 TeV, 5 ab<sup>-1</sup>).

# Sensitivity to $a$ and $b$

$$e^+e^- \rightarrow 4b + E_T^{\text{mis}}$$



- ✓  $p_T^j > 20 \text{ GeV}$
- ✓  $|\eta^j| < 2$
- ✓  $\Delta R_{jj} > 0.4$
- ✓  $E_T^{\text{mis}} > 20 \text{ GeV}$

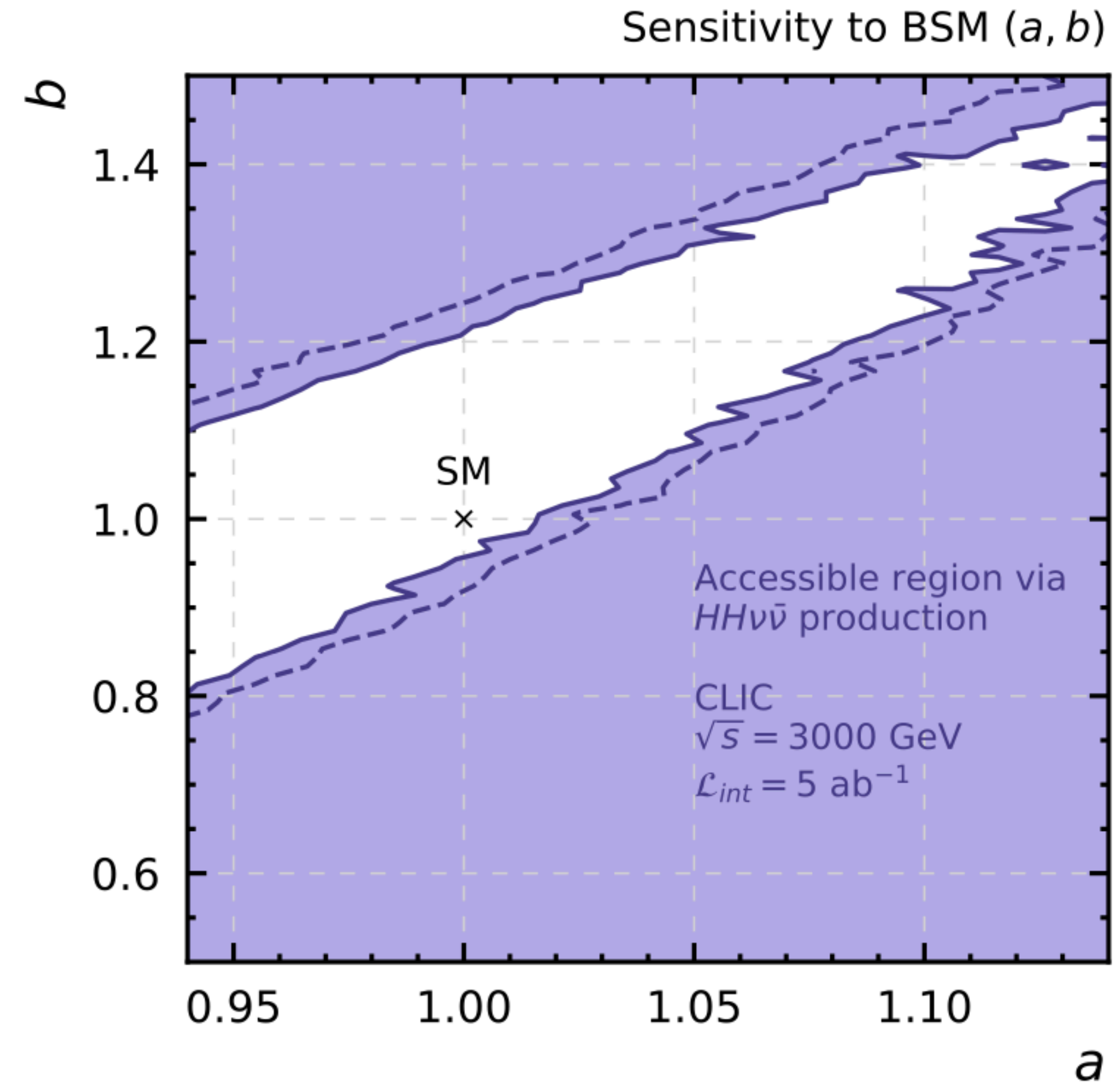
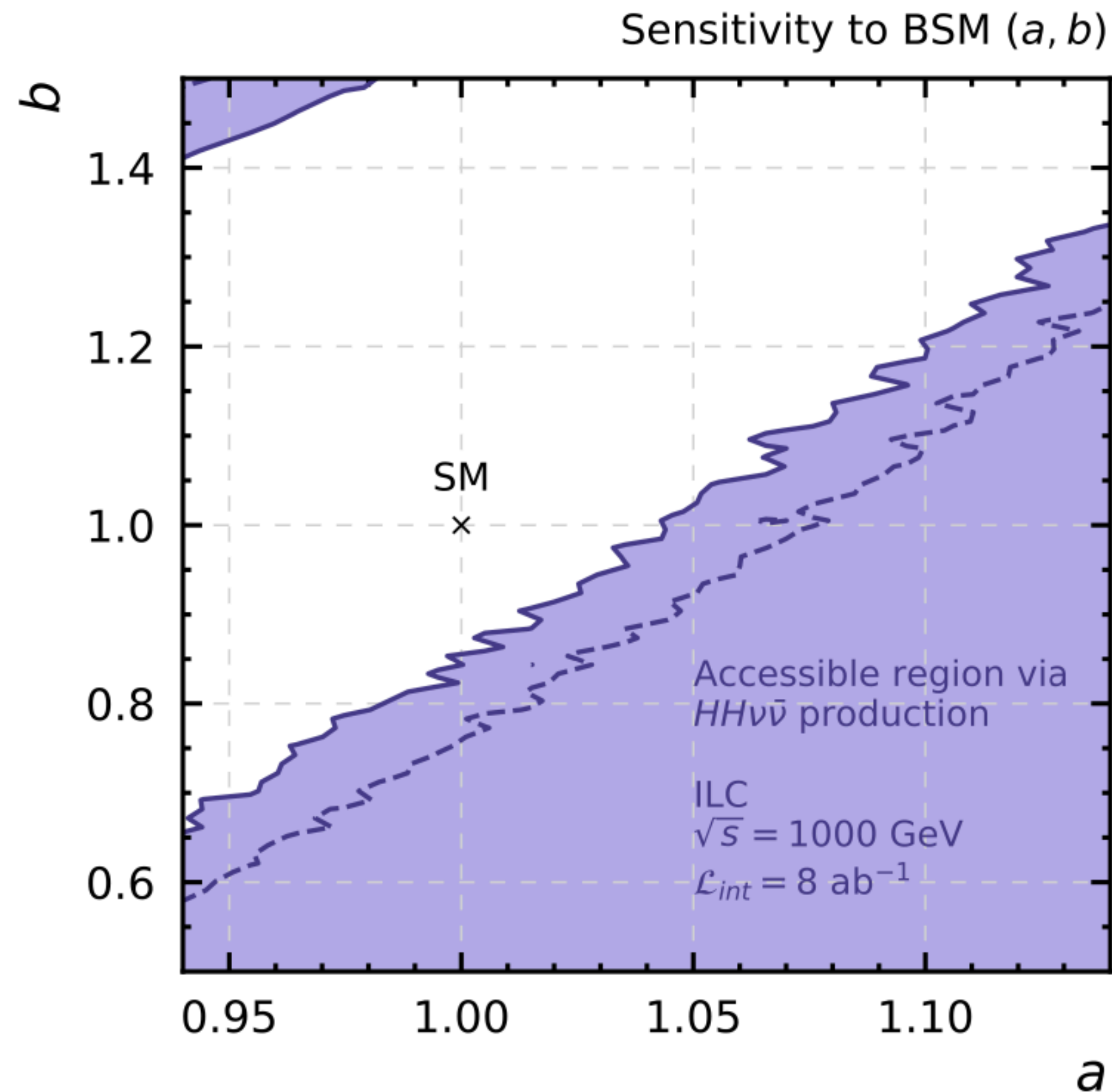


Factor of  $\varepsilon^4$ , where  $\varepsilon = 0.8$  is the  $b$ -tagging efficiency.



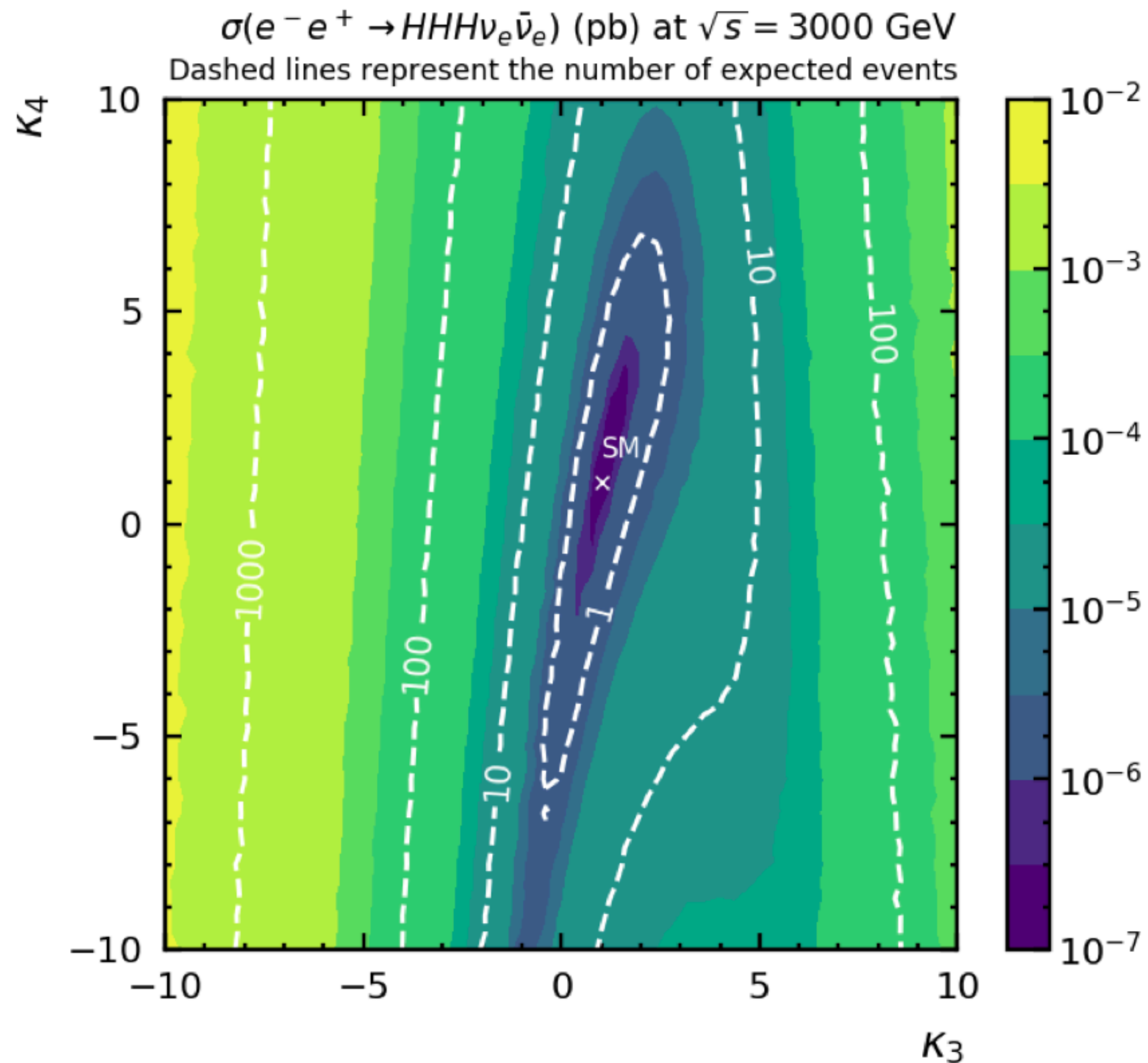
# Sensitivity to $a$ and $b$

Solid (dashed) lines bound regions with  $R < 5$  (10), with  $R = (N_{\text{BSM}} - N_{\text{SM}})/\sqrt{N_{\text{SM}}}$ .



**Large accessible regions!**

$$e^+e^- \rightarrow 6b + E_T^{\text{mis}}$$



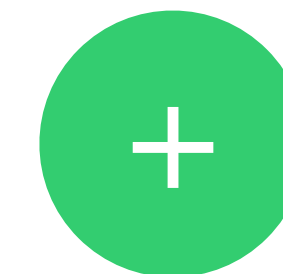
# Sensitivity to $\kappa_3$ and $\kappa_4$

$$\checkmark p_T^j > 20 \text{ GeV}$$

$$\checkmark N_j \geq 6$$

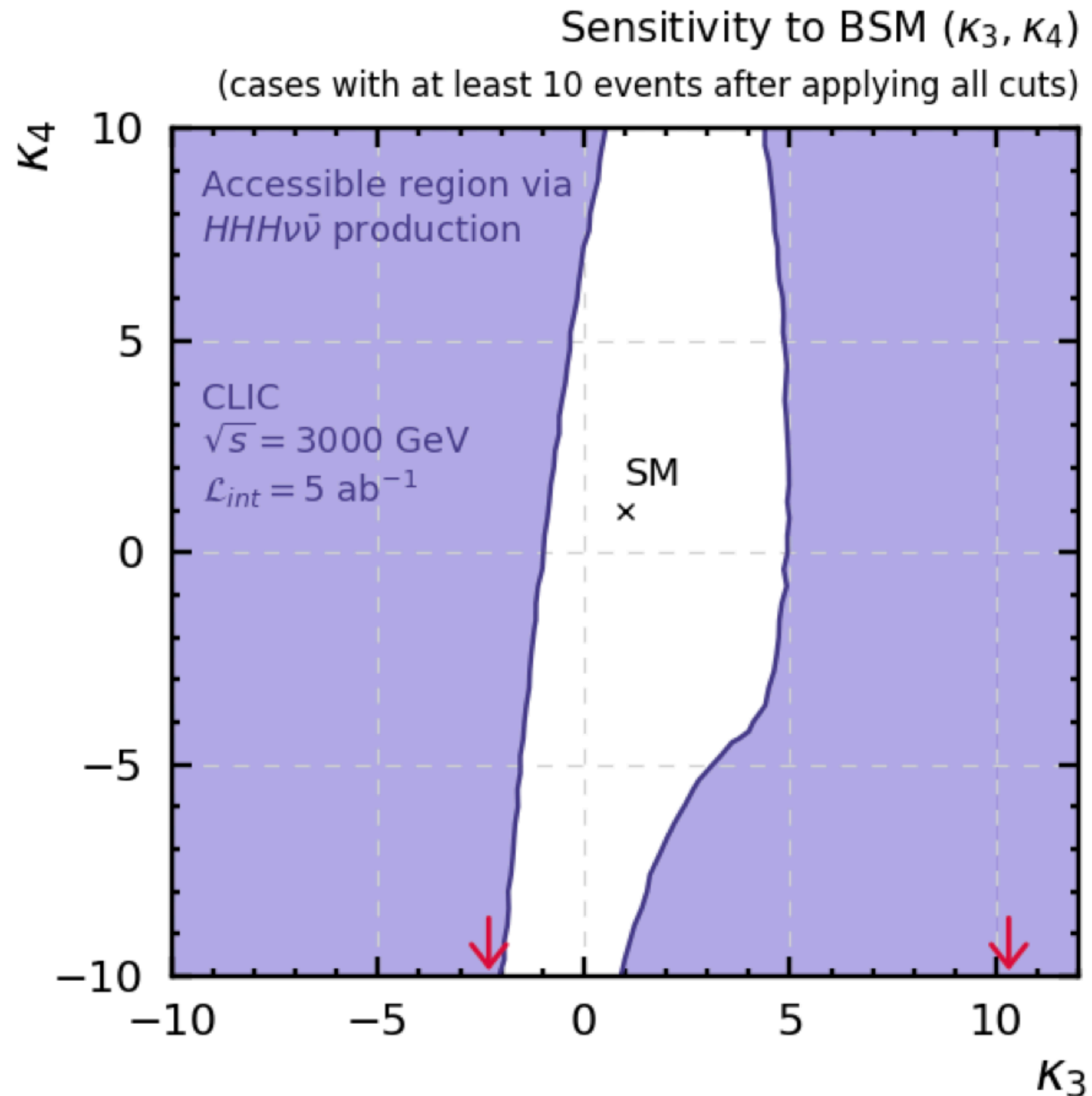
$$\checkmark |\eta^j| < 2.72$$

$$\checkmark E_T^{\text{mis}} > 20 \text{ GeV}$$



Requiring at least 5  $b$ -tagged  
jets:  $\varepsilon_5 = 6 \times \varepsilon^5/5 + \varepsilon^6$

10 events required for accessibility



## Sensitivity to $\kappa_3$ and $\kappa_4$

**Very interesting sensitivity  
to the quartic Higgs-  
coupling!**

# Summary

- ✓ **BSM physics could lead to deviations in Higgs couplings to W's and to itself.**
- ✓ **The EChL is an EFT which encodes these effects in the anomalous couplings.**
- ✓  **$e^+e^-$  colliders show promising prospects to improve sensitivity to anomalous couplings.**
- ✓ **Interestingly, CLIC could access to the Higgs quartic coupling, so far untested experimentally.**

thank you!