

International  
Muon Collider  
Collaboration

# PDAC Challenges (2.2 GeV – 44 MHz)



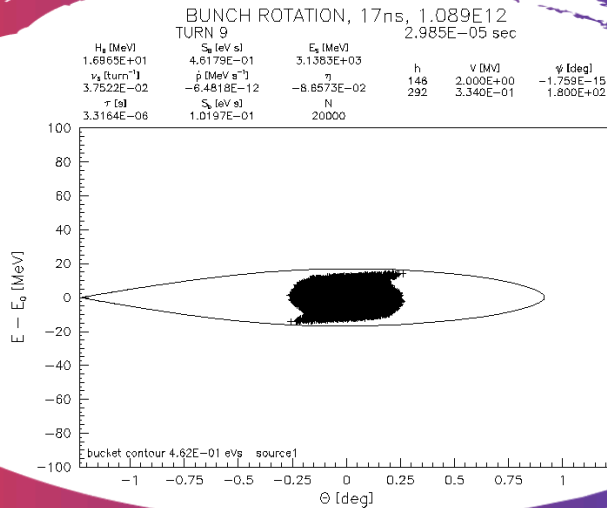
Mean beam power:  $P_{beam} = E_k N M f_{RepRate} = 4 \text{ MW}$

2.2 GeV

$\sim 1.1 \times 10^{12}$  p/b

140 bunches

75 Hz





**DESIGN OF A 2.2 GEV ACCUMULATOR AND COMPRESSOR FOR A  
NEUTRINO FACTORY**

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**Abstract**

The proton driver for a neutrino factory must provide megawatts of beam power at a few GeV, with nanosecond long bunches each containing more than  $1 \times 10^{12}$  protons. Such beam powers are within reach of a high-energy linac, but the required time structure cannot be provided without accumulation and compression. The option of a linac-based 2.2 GeV proton driver has been studied at CERN, taking into account the space charge and stability problems which make beam accumulation and bunch compression difficult at such a low-energy. A solution featuring two rings of approximately 1 km circumference has been worked out and is described in this paper. The subjects deserving further investigation are outlined.

=> <https://cds.cern.ch/record/442326/files/ps-2000-011.pdf>

7<sup>th</sup> European Particle Accelerator Conference  
26<sup>th</sup> - 30<sup>th</sup> June 2000  
Vienna, AUSTRIA

**Collective Effects and Final Bunch Rotation in a 2.2 GeV – 44 MHz  
Proton Accumulator – Compressor for a Neutrino Factory**

R. Cappi, J. Gareyte, E. Métral, D. Möhl

*Abstract*

This paper is a review of the collective effects and the final bunch rotation in the CERN scenario of a 4 MW proton driver for a neutrino factory.

NUFACT'00, Monterey, California, USA  
22-26 May 2000

=> <https://cds.cern.ch/record/466922/files/ps-2000-069.pdf>

Geneva, Switzerland  
29 September 2000

**Few-month  
(preliminary)  
study!**

## 2.2 GeV Accumulator and Compressor

- ◆ The geometry of the proton driver rings is determined by the preference that has been given to **install the 2 machines in the former ISR tunnel**. This tunnel has 150 m mean radius, with a width of about 15 m and height of 4 m
- ◆ **Choice of performing the bunch compression by means of a non-adiabatic process, imposes the use of 2 separate rings:** 1 for accumulation of the linac microbunches and 1 for compressing the resulting macrobunches. The RF cavities needed to perform the bunch rotation would be a potential source of problems if installed in the accumulator ring. Their high impedance and the unavoidably long filling time could drive beam instabilities during the accumulation period

## 2.2 GeV Accumulator and Compressor

- ◆ Accumulator lattice has been designed at **RAL**. All the optics computations for the compressor have been carried out at CERN by using different codes including space charge effects
- ◆ **In the accumulator ring**, the beam is accumulated during **2.2 ms**
- ◆ The final bunch rotation is performed **in the compressor ring in  $\sim 30 \mu\text{s}$**
- ◆ Since the bunch compression is much faster than the cavity filling time ( $\sim 100 \mu\text{s}$ ), the **phase shift due to the transient beam loading** increases almost linearly with time and **can be compensated by an appropriate frequency difference between generator and beam frequencies** ( $\sim 20 \text{ kHz}$  at  $44 \text{ MHz}$ )

# 2.2 GeV Accumulator and Compressor

Table 1: Summary of linac output beam characteristics.

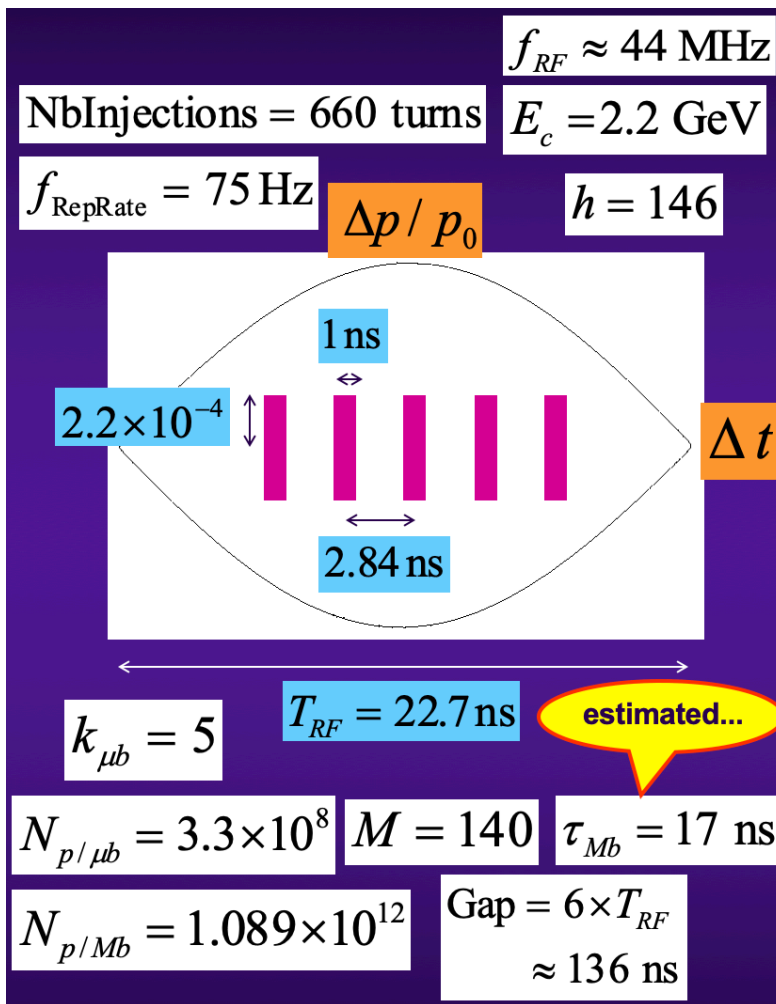
Parameter	Unit	Value
Mean beam power	MW	4
Kinetic energy	GeV	2.2
Rep. rate	Hz	75
Pulse duration	ms	2.2
# of micro-bunch trains $\times$ turns		$140 \times 660$
Pulse intensity		$1.5 \times 10^{14}$
Train spacing	ns	22.7
# of micro-bunches/train		5
Micro-bunch spacing	ns	2.84
Micro-bunch intensity		$3.3 \times 10^8$
Micro-bunch length	ns	0.5
Energy spread ( $2\sigma$ )	MeV	0.2
Energy jitter within pulse	MeV	$\pm 0.2$
Energy jitter between pulses	MeV	$\pm 2$
$\Delta p/p$ ( $2\sigma$ )		$0.08 \times 10^{-3}$
$\epsilon_l$	eVs	$0.2 \times 10^{-3}$
$\epsilon_{h/v}^* = \beta \gamma \sigma_{h,v}^2 / \beta_{h,v}$	$\mu\text{m}$	0.6

Table 2: Summary of output beam characteristics common to accumulator and compressor rings.

Parameter	Unit	Value
Pulse duration	$\mu\text{s}$	3.3
RF freq. $f_{RF}$	MHz	44.02
# of bunches/h		140/146
Bunch intensity	protons	$1.1 \times 10^{12}$
$\epsilon_l$	eVs	0.1
$\epsilon_{h/v}^* = \beta \gamma \sigma_{h,v}^2 / \beta_{h,v}$	$\mu\text{m}$	50

Table 3: Summary of geometrical and optical parameters of the accumulator and compressor ring.

Parameter	Accumulator	Compressor
Radius (m)	151	151
Main dip. field (T)	0.69	0.49
$\gamma_{tr}$	14.837	15.089
$\eta$	-0.0848	-0.0849
$\beta_h^{\max} / \beta_v^{\max}$ (m)	26.4/26.2	24.5/25.5
$D_h^{\min} / D_h^{\max}$ (m)	0.0/4.6	0.0/1.8
$Q_h / Q_v$	11.23/13.30	17.18/16.40
Super-symmetry	8	8
Vac. pipe half width (m)	0.09	0.09
Vac. pipe half height (m)	0.09	0.09
# of dip.-quad./super-per.	3 - 22	5 - 17
Length of s.s./super-per. (m)	73.4	86.2



# Collective effects

- ◆ Mechanisms looked at in the accumulator ring
  - Transverse space charge
  - RF matching w/o and w/ space charge
  - Longitudinal microwave instability from a broad-band impedance
  - Longitudinal coupled-bunch instability from RF HOMs
  - Transverse head-tail instability (single-bunch and coupled-bunch) from RW
  - TMCI from a broad-band impedance
  - BBU (single-bunch and multi-bunch) from a broad-band impedance
- ◆ Mechanisms looked at in the compressor ring
  - Bunch rotation with longitudinal space charge (analytically and using the ESME program)



# Collective effects: preliminary conclusions (at that time)

- ◆ The CERN 2.2 GeV – 44 MHz scenario for the proton driver of a neutrino factory looks promising
- ◆ **No major obstacles** have been found with the current parameters
- ◆ **More detailed investigations have to be performed to investigate**
  - **Electron-cloud effects**
  - **Halo formation and beam losses in both rings**



# Collective effects: preliminary conclusions (at that time)

- ◆ Some other scenarios were also briefly looked at
  - **Other RepRates: 50 Hz and 25 Hz**
  - **RCS (2-30 GeV) as an alternative to PDAC**
  
- ◆ Several meetings with RAL
  - At CERN (20-21/01/2000)
  - At Oxford (04-05/05/2000)
  - At London (22/02/2001)

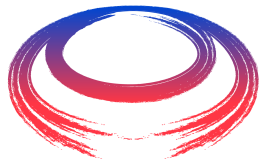
# Next

- ◆ All this should be carefully checked (with detailed simulations) and updated

...E.g.:

correct description of the phenomenon. On the other hand, as concerns the transverse mode coupling instability, the threshold number of protons per bunch given by Eq. (19) can be considered to be a conservative estimate, since in this case space charge seems to have a strong stabilizing effect [11].

=> We know, since, that (strong) space charge has a destabilizing effect...



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***Thank you  
for your attention***

# Appendix

## APPENDIX: List of the Accumulator (A), Compressor (C) and beam parameters

$$a = (a_x + a_y) / 2$$

Average beam radius.  $a^{\mu b} = 2.16$  mm.

$$a^{MbA} = a^{MbC} = 1.98$$
 cm

$$a_{x,y} = \sqrt{2} \left[ \varepsilon_{x,y}^{\text{rms}} \beta_{x,y} + (D_{x,y} \sigma_p / p_0)^2 \right]^{1/2}$$

$\sqrt{2} \times$  the rms horizontal and vertical beam dimensions.

$$a_x^{\mu b} = 2.25$$
 mm,  $a_y^{\mu b} = 2.07$  mm,  $a_x^{MbA} = a_x^{MbC} = 2.06$  cm,

$$a_y^{MbA} = a_y^{MbC} = 1.89$$
 cm

$$b = b_x = b_y = 9$$
 cm

Radius of the circular vacuum chamber of A and C

$$B = f_0 \tau_b$$

Bunching factor



$$c = 2.997925 \times 10^8 \text{ m}^{-1}$$

$$D_{x,y}$$

$$e = 1.6 \times 10^{-19} \text{ C}$$

$$E = E_0 + E_c = 3.138 \text{ GeV}$$

$$E_0 = 0.938 \text{ GeV}$$

$$E_c = 2.2 \text{ GeV}$$

$$f_0 = 301.536 \text{ kHz}$$

$$f_r^{BB} = c / (2\pi b) = 0.53 \text{ GHz}$$

$$f_{\text{RepRate}} = 75 \text{ Hz}$$

$$f_{RF} = h f_0 = 44.0243 \text{ MHz}$$

$$f_{\xi_{x,y}} = (\xi_{x,y} / \eta) Q_{x,y} f_0$$

$$h = 146$$

$$I_p = 3 e N_b / 2 \tau_b$$

$$I_0 = N_b e f_0$$

$$j = \sqrt{-1}$$

$$L$$

$$L_r \approx (M_{\text{bunch}} - 1) \times t_{\text{sep}}^{\text{bunch}} = 11.36 \text{ ns}$$

$$m_0 = 1.67 \times 10^{-27} \text{ kg}$$

$$M$$

$$N_{\text{injections}} = 660$$

$$N_b$$

$$P_{\text{beam}} = E_c N_{\text{MBC}} M_{\text{MBC}} f_{\text{RepRate}} = 4 \text{ MW}$$

$$Q_r^{BB} \approx 1$$

$$Q_x = f_x / f_0$$

$$Q_{x,y}$$

$$r_p = 1.54 \times 10^{-18} \text{ m}$$

$$R = 151 \text{ m}$$

$$R_{r,i}^{BB} = (f_r^{BB} / f_0) \times |Z_r^{BB}(p) / p|$$

$$R_{r,i}^{BB} = 2 c R_{r,j}^{BB} / (2\pi f_r^{BB} b^2)$$

Velocity of light

Average transverse dispersion functions.

$$D_x^A = R / (Q_x^A)^2 = 1.20 \text{ m}, \quad D_x^C = R / (Q_x^C)^2 = 0.51 \text{ m},$$

$$D_y^A = 0 \text{ m}, \quad D_y^C = 0 \text{ m}$$

Elementary charge

Proton total energy

Proton rest energy

Proton kinetic energy

Average revolution frequency in A and C

Resonance frequency of the broadband impedances (cut-off frequency of the vacuum chamber)

Repetition rate of the proton driver

Average RF frequency in A and C

Transverse chromatic frequencies.  $f_{\xi}^A = 39.93 \text{ MHz}$ ,

$$f_{\xi}^C = 47.29 \text{ MHz}$$

Harmonic number in A and C

Bunch peak current considering a parabolic line density.

$$I_p^{\text{bunch}} = 0.16 \text{ A}, \quad I_p^{\text{MBA}} = 15.37 \text{ A}, \quad I_p^{\text{MBC}} = 65.34 \text{ A}$$

Bunch average current.  $I_0^{\text{bunch}} = 0.000016 \text{ A}$ ,

$$I_0^{\text{MBA}} = I_0^{\text{MBC}} = 0.053 \text{ A}$$

Imaginary unit

Total ( $4\sigma$ ) bunch length (in meters).  $L_{\text{bunch}} = 0.143 \text{ m}$ ,

$L_{\text{MBA}} = 4.863 \text{ m}$  ("estimated" length of a macro-bunch at the end of accumulation),  $L_{\text{MBC}} = 1.144 \text{ m}$

Length (in meters) of the Linac train

Proton rest mass

Number of bunches.  $M_{\text{bunch}} = 5$  (per Linac injection train),

$$M_{\text{MBA}} = M_{\text{MBC}} = 140$$

Number of injection turns in A

Number of protons per bunch.  $N_{\text{bunch}} = 3.3 \times 10^8$ ,

$$N_{\text{MBA}} = N_{\text{MBC}} = 1.089 \times 10^{12}$$

Mean beam power

Quality factor of the broad-band impedances

Synchrotron tune

Transverse coherent tunes (in the absence of wake fields).

$$Q_x^A = 11.23, \quad Q_x^C = 13.30, \quad Q_x^C = 17.18, \quad Q_y^C = 16.40$$

Classical proton radius

Average machine radius of A and C

Longitudinal shunt impedance of the broadband resonator

Transverse shunt impedance of the broadband resonator

$$t_{\text{sep}}^{\text{bunch}} = 2.84 \text{ ns}$$

$$T_{\text{accumulation}} = T_0 N_{\text{injections}} = 2.2 \text{ ms}$$

$$T_0 = 1 / f_0 = 3.32 \text{ } \mu\text{s}$$

$$T_{RF} = 1 / f_{RF} = 22.715 \text{ ns}$$

$$Z_0 = 377 \text{ } \Omega$$

$$\beta = \sqrt{1 - \gamma^{-2}} = 0.9543$$

$$\beta_{x,y} = R / Q_{x,y}$$

$$\gamma = E / E_0 = 3.345$$

$$\gamma_{tr}$$

$$\gamma_{tr}^C = 15.089$$

$$\epsilon_0 = 8.84 \times 10^{-12} \text{ Fm}^{-1}$$

$$\epsilon_i$$

$$\epsilon_{x,y}^{\text{norm},1\sigma} = \beta \gamma \epsilon_{x,y}^{\text{rms}}$$

$$\eta$$

$$\eta = \gamma_{tr}^{-2} - \gamma^{-2}$$

$$\xi_{x,y} \approx -1$$

$$\rho_{tr} = 10^{-6} \text{ } \Omega\text{m}$$

$$\tau_b$$

$$\phi_2 = -\phi_1$$

$$\omega_0 = 2\pi f_0$$

$$\omega_r^{BB} = 2\pi f_r^{BB}$$

$$\omega_{RF} = 2\pi f_{RF}$$

$$\omega_{x,y} = Q_{x,y} \omega_0$$

$$\omega_{\xi_{x,y}} = 2\pi f_{\xi_{x,y}}$$

$$\Delta p / p_0 = \pm 2 \sigma_p / p_0$$

$$(\Delta p / p_0)_{\text{FWHM}} = 2\sqrt{2} (\sigma_p / p_0)$$

$$\sigma_p / p_0$$

Separation in time between (the centres of) 2 consecutive micro-bunches

Accumulation time

Average revolution period in A and C

Average RF period in A and C

Free space impedance

Relativistic velocity factor

Average transverse betatron functions.  $\beta_x^A = 13.45 \text{ m}$ ,

$$\beta_y^A = 11.35 \text{ m}, \quad \beta_x^C = 8.79 \text{ m}, \quad \beta_y^C = 9.21 \text{ m}$$

Relativistic mass factor

Relativistic mass factor at transition energy.  $\gamma_{tr}^A = 14.837$ ,

$$\gamma_{tr}^C = 15.089$$

Permittivity of free space

Longitudinal bunch emittance.  $\epsilon_r^{\text{MBA}} = 0.1 \text{ eVs}$

Normalized rms transverse emittances.

$$(\epsilon_{x,y}^{\text{norm},1\sigma})_{\text{bunch}} = 0.6 \text{ } \mu\text{m}, \quad (\epsilon_{x,y}^{\text{norm},1\sigma})_{\text{MBA}} = (\epsilon_{x,y}^{\text{norm},1\sigma})_{\text{MBC}} = 50 \text{ } \mu\text{m}$$

Slippage (or off-momentum) factor.  $\eta^A = -0.08481$ ,

$$\eta^C = -0.08496$$

Transverse (relative) chromaticities in A and C

Vacuum chamber resistivity (stainless steel)

Total ( $4\sigma$ ) bunch length (in seconds).  $\tau_{\text{bunch}} = 0.5 \text{ ns}$ ,

$\tau_{\text{MBA}} = 17 \text{ ns}$  ("estimated" length of a macro-bunch at the end of accumulation),  $\tau_{\text{MBC}} = 4 \text{ ns}$

Bunch half length (in RF phase).

$$\phi_2^{\text{MBA}} = -\phi_1^{\text{MBA}} = 134.7 \text{ deg}$$

Transverse betatron angular frequencies

Maximum relative bunch momentum spread

Full width at half height of the bunch momentum distribution (considering a parabolic distribution)

Rms relative bunch momentum spread.

$$(\sigma_p / p_0)_{\text{bunch}} = 4 \times 10^{-5}, \quad (\sigma_p / p_0)_{\text{MBA}} = 7.25 \times 10^{-4},$$

$$(\sigma_p / p_0)_{\text{MBC}} = 2.25 \times 10^{-3}$$

Transverse betatron angular frequencies

Maximum relative bunch momentum spread

Full width at half height of the bunch momentum distribution (considering a parabolic distribution)

Rms relative bunch momentum spread.

$$(\sigma_p / p_0)_{\text{bunch}} = 4 \times 10^{-5}, \quad (\sigma_p / p_0)_{\text{MBA}} = 7.25 \times 10^{-4},$$

$$(\sigma_p / p_0)_{\text{MBC}} = 2.25 \times 10^{-3}$$

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