Simulation of low energy nuclear recoils using Geant4

[heavy ions, T < 1 keV/amu]

Ricardo Pinho ricardo@lipc.fis.uc.pt

12th Geant4 Collaboration Workshop



LIP - Coimbra

Hebden Bridge 14 Set 2007

Outline

1. a review of Geant4's models of stopping power

2. nuclear recoils full cascade

3. nuclear quenching estimates

4. summary and present work

Versions used: geant4.8.2 and geant4.8.2.p01

ion = projecticle particle Z_1

 $atom = target particle Z_2$

ion = projecticle particle Z_1

G4hLowEnergyIonisation

G4hBetheBlochModel
G4hParametrisedLossModel
G4hIonEffChargeSquare

$$-\frac{dE}{dx} = S_e + S_n$$

(assuming no correlations)

G4hNuclearStoppingModel

ion = projecticle particle Z_1

G4hLowEnergyIonisation

G4hBetheBlochModel
G4hParametrisedLossModel
G4hIonEffChargeSquare

$$-\frac{dE}{dx} = S_e + S_n$$

(assuming no correlations)

G4hNuclearStoppingModel

- Low energy extension
- Physics list: only G4hLowEnergyIonisation
- Very small step sizes (~1% of the particle range)
- Continuous slowing down approximation:

- Cut energy very high: no deltarays
- Actually no secondaries what so ever! Just follow our primary till it stops (default MinKineticEnergy = 10eV)
- No fluctuations

ion = projecticle particle Z_1

G4hLowEnergyIonisation)

G4hBetheBlochModel
G4hParametrisedLossModel
G4hIonEffChargeSquare

$$-\frac{dE}{dx} = S_e + S_n$$

(assuming no correlations)

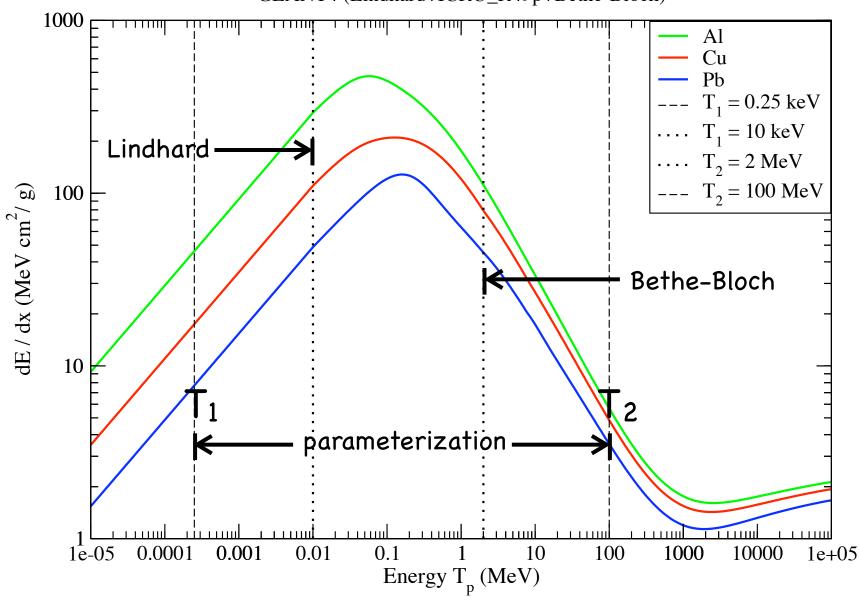
G4hNuclearStoppingModel

- Low energy extension
- Physics list: only G4hLowEnergyIonisation
- Very small step sizes (~1% of the particle range)
- Continuous slowing down approximation:
 - Geometry:
- just a square box, filled with pure material

- Cut energy very high: no deltarays
- Actually no secondaries what so ever! Just follow our primary till it stops (default MinKineticEnergy = 10eV)
- No fluctuations
- shoot primary from the center of the box, random direction

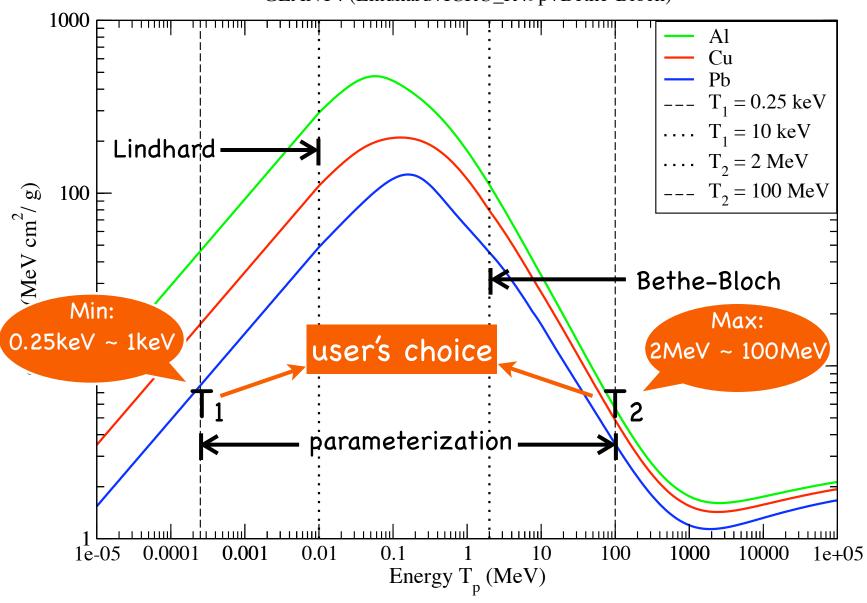
S_e: proton -> Al, Cu, Pb

GEANT4 (Lindhard+ICRU_R49p+Bethe-Bloch)



S_e: proton -> Al, Cu, Pb

GEANT4 (Lindhard+ICRU_R49p+Bethe-Bloch)



low energy stopping power is parameterized

- low energy stopping power is parameterized
- parameterization is for protons and alphas only

- low energy stopping power is parameterized
- parameterization is for protons and alphas only
- for other heavy ions, the stopping is scaled by:

- low energy stopping power is parameterized
- parameterization is for protons and alphas only
- for other heavy ions, the stopping is scaled by:

$$S_{ei}(T) = Z_{eff}^2 \cdot S_{ep}(T_p), \quad T_p = \frac{M_p}{M}T$$

- low energy stopping power is parameterized
- parameterization is for protons and alphas only
- for other heavy ions, the stopping is scaled by:

$$S_{ei}(T) = Z_{eff}^2 \cdot S_{ep}(T_p), \quad T_p = \frac{M_p}{M}T$$

proton stopping parameterizations

- default) ICRU_R49p
 - Ziegler1977p
 - Ziegler1985p
 - SRIM2000p

Geant4

Electronic stopping

- low energy stopping power is parameterized
- parameterization is for protons and alphas only
- for other heavy ions, the stopping is scaled by:

$$S_{ei}(T) = Z_{eff}^2 \cdot S_{ep}(T_p), \quad T_p = \frac{M_p}{M}T$$

proton stopping parameterizations

alpha stopping parameterizations

- default) ICRU_R49p
 - Ziegler1977p
 - Ziegler1985p
 - SRIM2000p

- ICRU_R49He
- Ziegler1977He

Geant4

Electronic stopping

- low energy stopping power is parameterized
- parameterization is for protons and alphas only
- for other heavy ions, the stopping is scaled by:

$$S_{ei}(T) = Z_{eff}^2 \cdot S_{ep}(T_p), \quad T_p = \frac{M_p}{M}T$$

proton stopping parameterizations

alpha stopping parameterizations

effective charge parameterization

$$Z_{eff}(v, v_F)$$

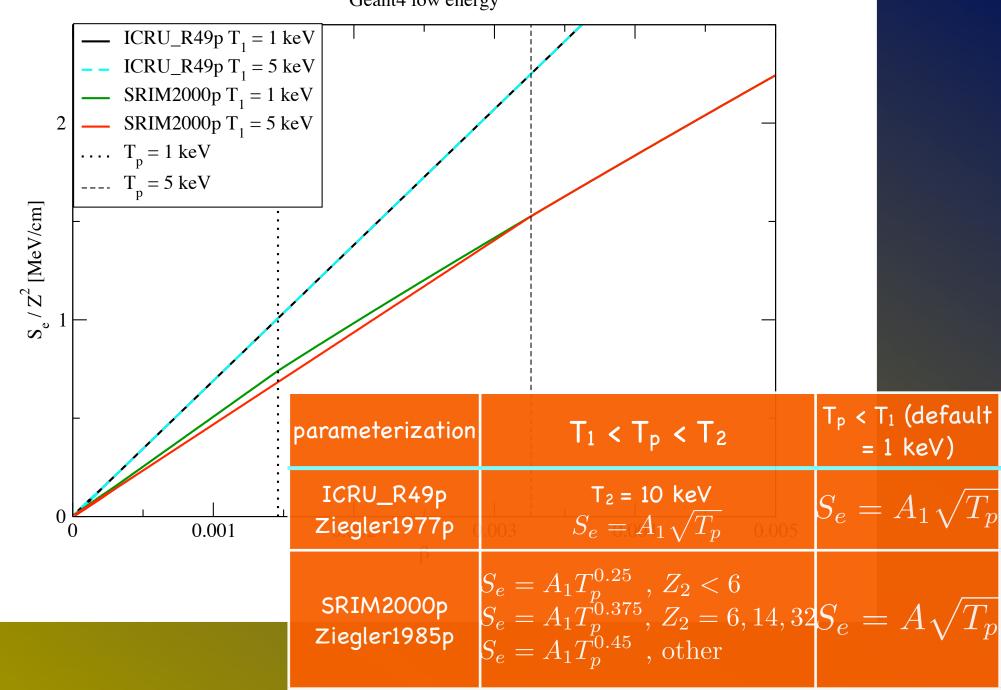
- default) ICRU_R49p
 - Ziegler1977p
 - Ziegler1985p
 - SRIM2000p

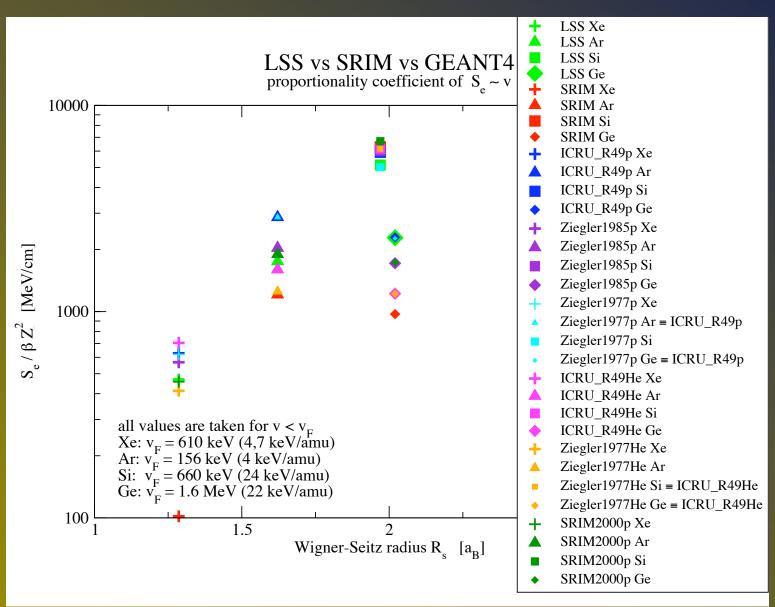
- ICRU_R49He
- Ziegler1977He

Ziegler, 1985,Brandt andKitagawa, 1982

S_e : Xe -> LXe

Geant4 low energy





ion-atom interaction potencial

ion-atom interaction potencial

$$V(r) = rac{Z_1 Z_2 e^2}{r} \Phi egin{cases} \lim_{r \to 0} & \Phi = 1 \\ \lim_{r \to \infty} & \Phi = 0 \end{cases}$$

ion-atom interaction potencial

$$V(r) = rac{Z_1 Z_2 e^2}{r} \Phi egin{cases} \lim_{r \to 0} & \Phi = 1 \\ \lim_{r \to \infty} & \Phi = 0 \end{cases}$$

Classical (or statistical) treatment: the Thomas-Fermi atom Approximations:

- elastic
- static (velocity independent)
- $\Phi=\Phi(r/a)$ universal $\Phi=\Phi(r/a)$

no shell structure (as opposed to modern Hartree-Fock solid state models)

screening length

ion-atom interaction potencial

$$V(r) = rac{Z_1 Z_2 e^2}{r} \Phi egin{cases} \lim_{r \to 0} & \Phi = 1 \\ \lim_{r \to \infty} & \Phi = 0 \end{cases}$$

Classical (or statistical) treatment: the Thomas-Fermi atom Approximations:

- elastic
- static (velocity independent)
- universal $\Phi = \Phi(r/a)$

 no shell structure (as opposed to modern Hartree-Fock solid state models)

screening length

V(r) relation treatment do
$$S_n = \int T' d\sigma$$

T' = energy transferred to an atom at rest (target)

Universal screening functions proposed in the literature:

- Bohr
- Thomas-Fermi → Lindhard (LSS)
- Lenz-Jensen
- Moliere

Ziegler (ZBL) → SRIM

 (a universal fit to 522 (!) solid
 state interatomic potencials)

Universal screening functions proposed in the literature:

- Bohr
- Thomas-Fermi → Lindhard (LSS)
- Lenz-Jensen
- Moliere

Ziegler (ZBL) → SRIM

 (a universal fit to 522 (!) solid
 state interatomic potencials)

Geant4 Nuclear stopping

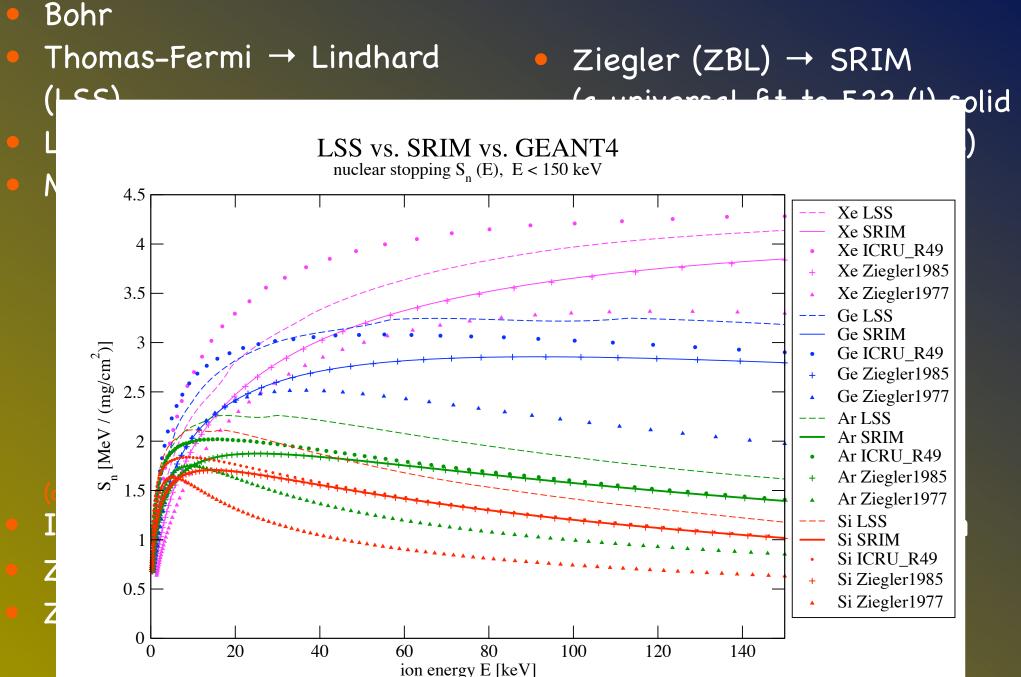
Universal stopping in reduced units scales back to ion-atom dependent stopping in physical units. Available choices:

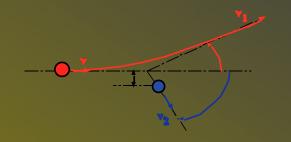
(default)

- ICRU_R49 parameterization of Moliere's screening function
- Ziegler1977 the ZBL universal potencial
- Ziegler1985

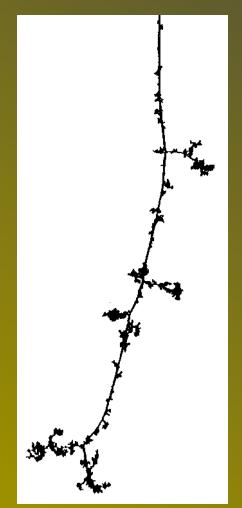
Universal screening functions proposed in the literature:

- Dala

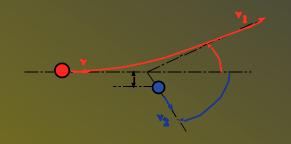




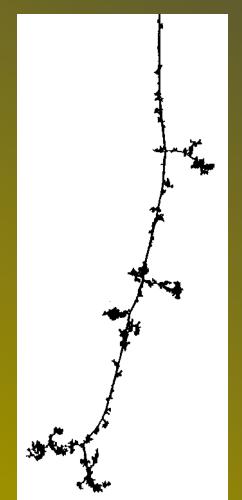
Note: the primary particle is already a recoil, doesn't matter if it originated from WIMPs or neutron scattering



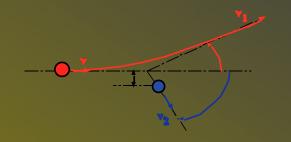
recoil CUT energy (default MinKineticEnergy = 10eV)



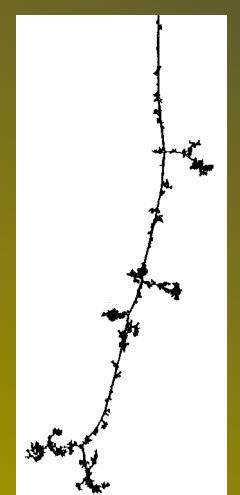
Note: the primary particle is already a recoil, doesn't matter if it originated from WIMPs or neutron scattering



recoil CUT energy (default MinKineticEnergy = 10eV)



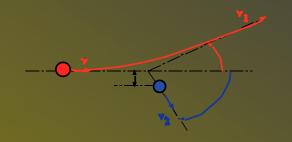
Note: the primary particle is already a recoil, doesn't matter if it originated from WIMPs or neutron scattering



recoil CUT energy (default MinKineticEnergy = 10eV)

Physics list:

Introduced a new physical process for the recoils

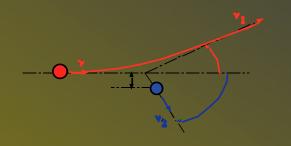


Note: the primary particle is already a recoil, doesn't matter if it originated from WIMPs or neutron scattering

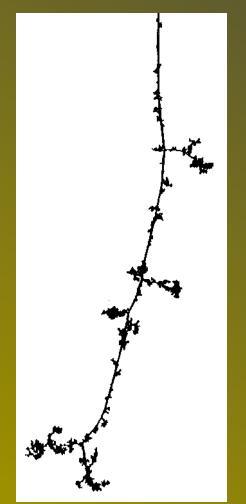


recoil CUT energy (default MinKineticEnergy = 10eV)

- Introduced a new physical process for the recoils
- Had to make some changes to G4hLowEnergyIonisation:

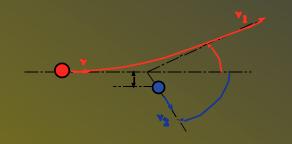


Note: the primary particle is already a recoil, doesn't matter if it originated from WIMPs or neutron scattering

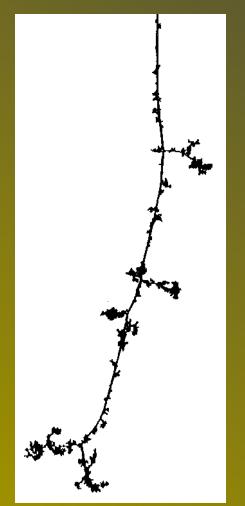


recoil CUT energy (default MinKineticEnergy = 10eV)

- Introduced a new physical process for the recoils
- Had to make some changes to G4hLowEnergyIonisation:
 - don't deposit T when T < CUT</p>

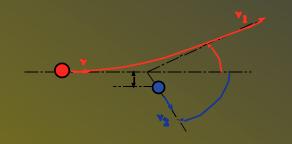


Note: the primary particle is already a recoil, doesn't matter if it originated from WIMPs or neutron scattering

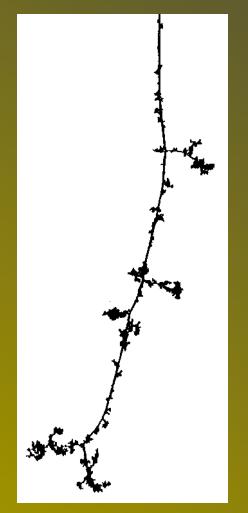


recoil CUT energy (default MinKineticEnergy = 10eV)

- Introduced a new physical process for the recoils
- Had to make some changes to G4hLowEnergyIonisation:
 - don't deposit T when T < CUT</p>
 - changed CUT from T_p to T

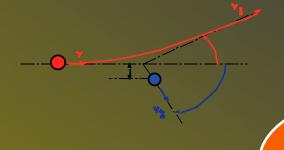


Note: the primary particle is already a recoil, doesn't matter if it originated from WIMPs or neutron scattering



recoil CUT energy (default MinKineticEnergy = 10eV)

- Introduced a new physical process for the recoils
- Had to make some changes to G4hLowEnergyIonisation:
 - don't deposit T when T < CUT</p>
 - changed CUT from T_P to T
 - SetNuclearStoppingOff() is mandatory

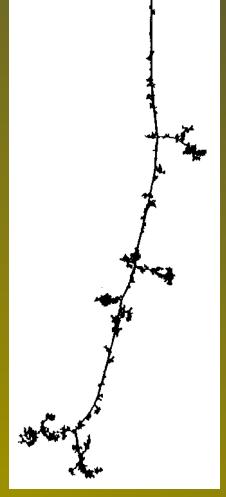


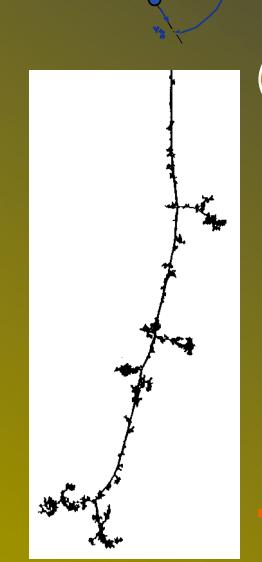
Note: the primary particle is already a recoil, doesn't matter if it originated from

code structure based on δ-electrons of emission, fluorescence and atom deexcitation of G4hLowEnergyIonisation and on the continous photon generation in G4Cerenkov

eticEnergy = 10eV)

- Introduced a new physical process for the recoils
- Had to make some changes to G4hLowEnergyIonisation:
 - don't deposit T when T < CUT</p>
 - t changed CUT from Tp to T
 - SetNuclearStoppingOff() is mandatory





Note: the primary particle is already a recoil, doesn't matter if it originated from

code structure based on δ -electrons of emission, fluorescence and atom deexcitation of G4hLowEnergyIonisation and on the continous photon generation in G4Cerenkov

- Introduced a new physical process for the recoils
- Had to make some changes to G4hLowEnergyIonisation:
 - don't deposit T when T < CUT</p>
 - changed CUT from Tp to T
 - SetV_{nuclear quenching} Off() is mandatory
- competition between total energy ultimately given to electrons and energy permanently lost to recoils

Geant4 Recoil cascade

- Geant4 has no nuclear recoils (at least heavy ion)
- It also doesn't have the respective cross sections (neither differential nor integrated)

Geant4

Recoil cascade

- Geant4 has no nuclear recoils (at least heavy ion)
- It also doesn't have the respective cross sections (neither differential nor integrated)
- 1st approximation, using only what Geant4 already has:
 - the recoil atom kinetic energy is taken from the parameterized nuclear stopping power

$$T' = \left(-\frac{dE}{dx}\right)_n \Delta x = S_n \times \text{step size}$$

Geant4

Recoil cascade

- Geant4 has no nuclear recoils (at least heavy ion)
- It also doesn't have the respective cross sections (neither differential nor integrated)
- 1st approximation, using only what Geant4 already has:
 - the recoil atom kinetic energy is taken from the parameterized nuclear stopping power

$$T' = \left(-\frac{dE}{dx}\right)_n \Delta x = S_n \times \text{step size}$$

- the so called continuous slowing down approximation (in a loosely sense) => a continuous process
- major disadvantage: very strong dependence on step size=> an external parameter in need of fine tuning

Geant4

Recoil cascade

- Geant4 has no nuclear recoils (at least heavy ion)
- It also doesn't have the respective cross sections (neither differential nor integrated)
- 1st approximation, using only what Geant4 already has:
 - the recoil atom kinetic energy is taken from the parameterized nuclear stop actually, we shouldn't even try to approximate nuclear collisions as a

$$T' = \left(-\frac{dE}{dx}\right)_n$$
 approximate nuclear collisions as a continuous process (as opposed to electronic stopping) as you're not supposed to get a recoil every step in

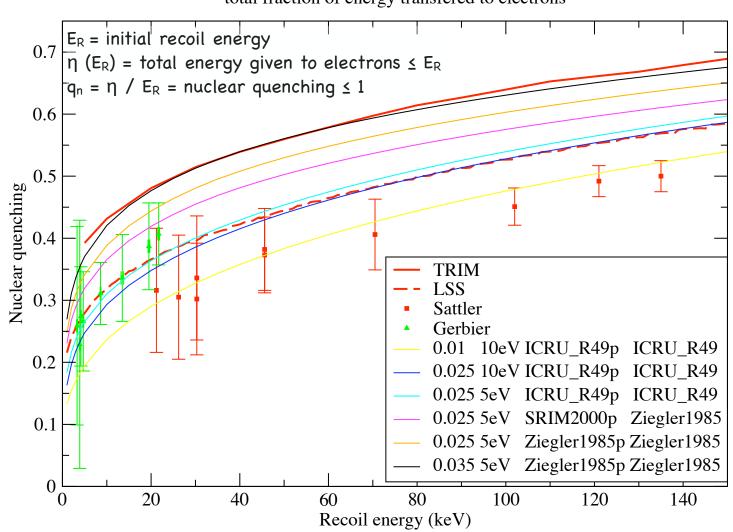
supposed to get a recoil every step, just the so called continuous gevery now and then

- loosely sense) => a continuous process
- major disadvantage: very strong dependence on step size => an external parameter in need of fine tuning

Geant4 Nuclear quenching: Si

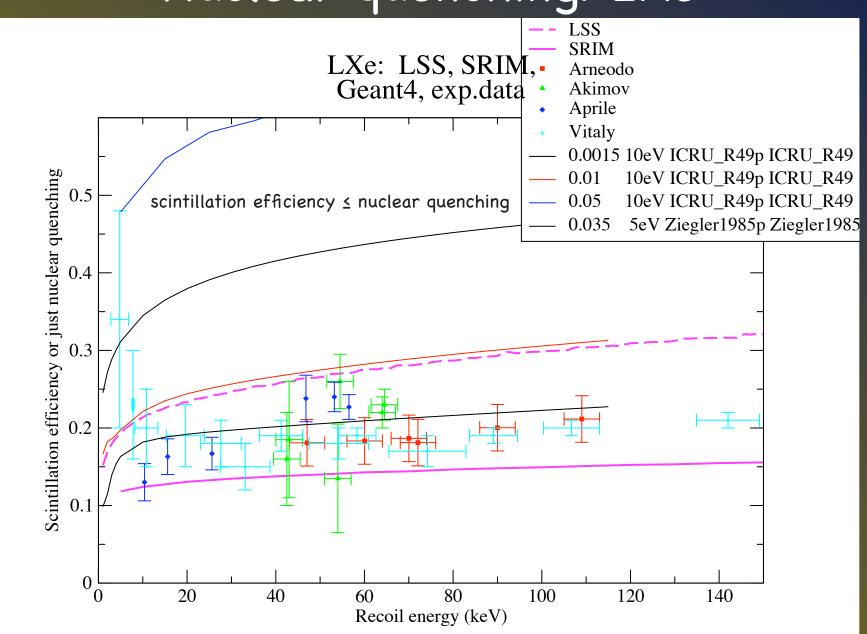
Si: LSS vs. SRIM vs. GEANT4 vs. exp. data

total fraction of energy transfered to electrons



Geant4

Nuclear quenching: LXe



1. Geant4 provides a good parameterization of both electronic and nuclear stopping powers (not shown here, is our validation of Geant4's stopping by comparing with NIST databases as well as experimental data, in different target materials, besides SRIM and LSS)

- 1. Geant4 provides a good parameterization of both electronic and nuclear stopping powers (not shown here, is our validation of Geant4's stopping by comparing with NIST databases as well as experimental data, in different target materials, besides SRIM and LSS)
- 2. The user has a total of 3x6 combinations of stopping parameterizations at his/her disposal

- 1. Geant4 provides a good parameterization of both electronic and nuclear stopping powers (not shown here, is our validation of Geant4's stopping by comparing with NIST databases as well as experimental data, in different target materials, besides SRIM and LSS)
- 2. The user has a total of 3x6 combinations of stopping parameterizations at his/her disposal
- 3. The continuous approximation provides a good prediction of the nuclear quenching of the recoils cascade, but also provides to much flexibility, by fine-tuning the total of 4 parameters that control the simulation:
 - electronic Se:

 - step size

- nuclear recoils:
- the parameterization the parameterization
 - energy cut

- 1. Geant4 provides a good parameterization of both electronic and nuclear stopping powers (not shown here, is our validation of Geant4's stopping by comparing with NIST databases as well as experimental data, in different target materials, besides SRIM and LSS)
- 2. The user has a total of 3x6 combinations of stopping parameterizations at his/her disposal
- 3. The continuous approximation provides a good prediction of the nuclear quenching of the recoils cascade, but also provides to much flexibility, by fine-tuning the total of 4 parameters that control the simulation:
 - electronic Se:
 - the parameterization
 - step size
 - mean free path $\sim rac{1}{\sigma}$

- nuclear recoils:
- the parameterization
 - energy cut

- 1. Geant4 provides a good parameterization of both electronic and nuclear stopping powers (not shown here, is our validation of Geant4's stopping by comparing with NIST databases as well as experimental data, in different target materials, besides SRIM and LSS)
- 2. The user has a total of 3x6 combinations of stopping parameterizations at his/her disposal
- 3. The continuous approximation provides a good prediction of the nuclear quenching of the recoils cascade, but also provides to much flexibility, by fine-tuning the total of 4 parameters that control the simulation:

electronic Se:

- the parameterization
- step size
 - mean free path $\sim rac{1}{\sigma}$

- nuclear recoils:
- screening function
- energy cut

+ dσ — a full discrete process (for the recoils)

- 1. Geant4 provides a good parameterization of both electronic and nuclear stopping powers (not shown here, is our validation of Geant4's stopping by comparing with NIST databases as well as experimental data, in different target materials, besides SRIM and LSS)
- 2. The user has a total of 3x6 combinations of stopping parameterizations at his/her disposal
- 3. The continuous approximation provides a good prediction of the nuclear quenching of the recoils cascade, but also provides to much flexibility, by fine-tuning the total of 4 parameters that control the simulation:

electronic Se:

- the parameterization
- step size
 - mean free path $\sim rac{1}{2}$

nuclear recoils:

- screening function
- energy cut

work in progress

+ dσ --- a full discrete process (for the recoils)

$$d\sigma = \Pi a^2 \frac{f(t^{1/2})}{2t^{3/2}}$$

Thomas-Fermi, Lenz-Jensen, Moliere, ZBL, ect.

$$d\sigma = \Pi a^2 \frac{f(t^{1/2})}{2t^{3/2}}$$

Thomas-Fermi, Lenz-Jensen, Moliere, ZBL, ect.

 $\sigma(T,T_c)$

numerical integration

$$d\sigma = \Pi a^2 \frac{f(t^{1/2})}{dt^2}$$

 $d\sigma = \Pi a^2 \frac{f(t^{1/2})}{243/2}$

Thomas-Fermi, Lenz-Jensen, Moliere, ZBL, ect.

numerical integration

 $\sigma(T,T_c)$

To do:

put it in tables and load them in Geant4, with interpolation

 $d\sigma = \Pi a^2 \frac{f(t^{1/2})}{2t^{3/2}}$

Thomas-Fermi, Lenz-Jensen, Moliere, ZBL, ect.

numerical integration

$$\sigma(T,T_c)$$

To do:

put it in tables and load them in Geant4, with interpolation

write the DiscreteProcess functions

 $d\sigma = \Pi a^2 \frac{f(t^{1/2})}{2t^{3/2}}$

implement the sampling

Thomas-Fermi, Lenz-Jensen, Moliere, ZBL, ect.

numerical integration

$$\sigma(T,T_c)$$

To do:

put it in tables and load them in Geant4, with interpolation

write the DiscreteProcess functions

 $d\sigma = \Pi a^2 \frac{f(t^{1/2})}{2t^{3/2}}$

implement the sampling

$$T' = \gamma T \sin^2 \frac{\theta}{2}$$

Thomas-Fermi, Lenz-Jensen, Moliere, ZBL, ect.

numerical integration

$$\sigma(T,T_c)$$

To do:

put it in tables and load them in Geant4, with interpolation

write the DiscreteProcess functions

Thomas-Fermi, Lenz-Jensen, Moliere, ZBL, ect.

 $d\sigma = \Pi a^2 \frac{f(t^{1/2})}{2t^{3/2}}$

numerical integration

 $\sigma(T,T_c)$

implement the sampling

To do:

put it in tables and load them in Geant4, with interpolation

write the

DiscreteProcess functions

$$T' = \gamma T \sin^2 \frac{\theta}{2}$$

Opposed to the standard method of solving the scattering integral:

Thomas-Fermi, Lenz-Jensen, Moliere, ZBL, ect.

numerical integration

 $\sigma(T,T_c)$

implement the sampling

To do: write the

put it in tables and load them in Geant4, with interpolation

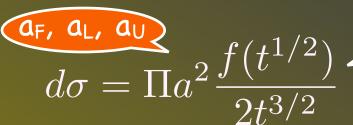
 $T' = \gamma T \sin^2 \frac{\theta}{2}$

DiscreteProcess functions

Opposed to the standard method of solving the scattering integral: SRIM/TRIM (the standard!)

ricardo@lipc.fis.uc.pt

Present work



implement the sampling

$$T' = \gamma T \sin^2 \frac{\theta}{2}$$

Thomas-Fermi, Lenz-Jensen, Moliere, ZBL, ect.

numerical integration $\sigma(T,T_c)$

To do:

put it in tables and load them in Geant4, with interpolation

write the DiscreteProcess functions

Opposed to the standard method of solving the scattering integral: SRIM/TRIM (the standard!)

M.H. Mendenhalla and R.A. Weller, An algorithm for computing screened Coulomb scattering in GEANT4, Nuclear Instruments and Methods in Physics Research B227, 3 (2005) 420

Extras

Electronic Stopping Se

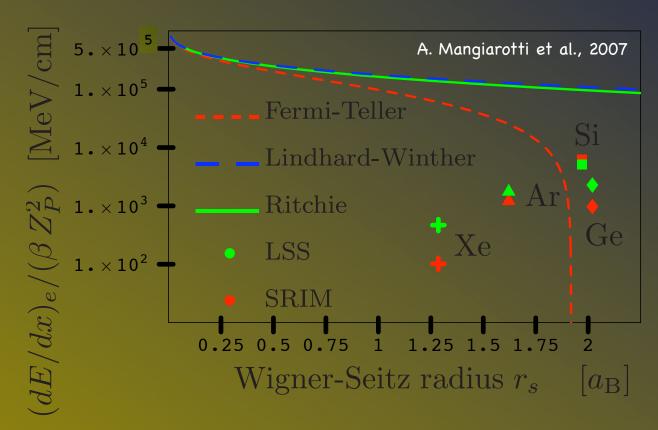
Fermi-Teller: $S_e \propto v$ (ion velocity) if $v < v_F \sim v_0$

Lindhard: uniform free electron gas, Thomas-Fermi atom, particleplasma interaction as a perturbation

$$S_e = k\epsilon^{1/2}$$
 if $v < \text{Bragg peak} \ (\sim v_0 Z_1^{2/3} \approx 500 MeV \text{ for Xe})$

0.10 < k < 0.20 (reduced units) $k_{Xe} \approx 0.166$

SRIM: local density approximation using Hartree-Fock solid state atoms; semi-empirical fit of charge state of the ion



 E = initial particle energy (e.g. E_Y = 122keV for Co57 or E_R for recoils produced by neutrons or WIMPs)

- E = initial particle energy (e.g. E_Y = 122keV for Co57 or E_R for recoils produced by neutrons or WIMPs)
- η (E) = total energy ultimately given to electrons ≤ E $(η_Y ≈ E_Y)$

- E = initial particle energy (e.g. E_Y = 122keV for Co57 or E_R for recoils produced by neutrons or WIMPs)
- η (E) = total energy ultimately given to electrons \leq E ($\eta_Y \approx E_Y$)
- $q_n = \eta_R / E_R = nuclear$ quenching (of the recoils) ≤ 1

- E = initial particle energy (e.g. E_Y = 122keV for Co57 or E_R for recoils produced by neutrons or WIMPs)
- η (E) = total energy ultimately given to electrons \leq E ($\eta_Y \approx E_Y$)
- $q_n = \eta_R / E_R = nuclear$ quenching (of the recoils) ≤ 1
 - But what do we actually measure in the lab ?!

- E = initial particle energy (e.g. E_{γ} = 122keV for Co57 or E_{R} for recoils produced by neutrons or WIMPs)
- η (E) = total energy ultimately given to electrons \leq E ($\eta_Y \approx E_Y$)
- $q_n = \eta_R / E_R = nuclear$ quenching (of the recoils) ≤ 1
 - But what do we actually measure in the lab ?!
- relative scintillation efficiency $pprox rac{\eta_R(E_R)}{E_R} imes rac{W_S(E_\gamma)}{W_S(E_R)}$

- E = initial particle energy (e.g. E_{γ} = 122keV for Co57 or E_{R} for recoils produced by neutrons or WIMPs)
- η (E) = total energy ultimately given to electrons \leq E ($\eta_Y \approx E_Y$)
- $q_n = \eta_R / E_R = nuclear$ quenching (of the recoils) ≤ 1
 - But what do we actually measure in the lab?!
- ullet relative scintillation efficiency $pprox rac{\eta_R(E_R)}{E_R} imes rac{W_S(E_\gamma)}{W_S(E_R)}$

where we redefine:

$$\begin{array}{c} \gamma: \ W_S = E_\gamma/N_{ph} \\ R: \ W_S = \eta_R/N_{ph}' \end{array} \right\} W_S \left\{ \begin{array}{c} \text{now they refer to the energy} \\ \text{transfered to electrons only!} \\ \text{and are both just functions of LET} \end{array} \right.$$

- E = initial particle energy (e.g. $E_Y = 122$ keV for Co57 or E_R for recoils produced by neutrons or WIMPs)
- η (E) = total energy ultimately given to electrons \leq E ($\eta_{Y} \approx E_{Y}$)
- $q_n = \eta_R / E_R = nuclear$ quenching (of the recoils) ≤ 1
 - But what do we actually measure in the lab?!

relative scintillation efficiency
$$pprox \frac{\eta_R(E_R)}{E_R} imes \frac{W_S(E_\gamma)}{W_S(E_R)}$$

where we redefine:

$$\begin{array}{c} \gamma: \ W_S = E_\gamma/N_{ph} \\ R: \ W_S = \eta_R/N_{ph}' \end{array} \right\} W_S \left\{ \begin{array}{c} \text{now they refer to the energy} \\ \text{transfered to electrons only!} \\ \text{and are both just functions of LET} \end{array} \right.$$

- E = initial particle energy (e.g. $E_Y = 122 \text{keV}$ for Co57 or E_R for recoils produced by neutrons or WIMPs)
- η (E) = total energy ultimately given to electrons \leq E ($\eta_V \approx E_V$)
- $q_n = \eta_R / E_R = nuclear$ quenching (of the recoils) ≤ 1
 - But what do we actually measure in the lab?!

relative scintillation efficiency
$$pprox \frac{\eta_R(E_R)}{E_R} imes \frac{W_S(E_\gamma)}{W_S(E_R)}$$
 where we redefine:

where we redefine:

$$\left. egin{array}{ll} \gamma: & W_S = E_\gamma/N_{ph} \ R: & W_S = \eta_B/N_{ph}' \end{array}
ight.
ight.
ight.
ight.$$

 $\begin{array}{c} \gamma: \ W_S = E_\gamma/N_{ph} \\ R: \ W_S = \eta_R/N_{ph}' \end{array} \right\} W_S \left\{ \begin{array}{c} \text{now they refer to the energy} \\ \text{transfered to electrons only!} \\ \text{and are both just functions of LET} \end{array} \right.$

(relative) Scintillation efficiency

$$q_n \times \frac{W_S(E_\gamma)}{W_S(E_R)}$$

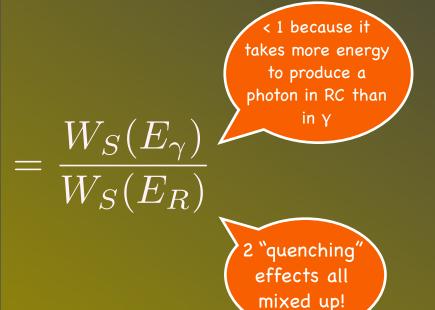
Is everybody clear about this definition ?!

derivation from the traditional/experimental formula

comparison with Hitachi definition

traditional definition of $W_S=rac{E}{N_{ph}}$ for γ , Recoils, whatever!

traditional definition of $\,W_S=rac{E}{N_{ph}}\,$ for Y, Recoils, whatever!



traditional definition of $W_S=rac{E}{N_{ph}}$ for Y, Recoils, whatever!

$$=\frac{W_S(E_\gamma)}{W_S(E_R)}=\frac{\frac{E_\gamma}{N_{ph}}}{\frac{E_R}{N'_{ph}}}$$

traditional definition of $\,W_S = rac{E}{N_{ph}}\,$ for Y, Recoils, whatever!

$$=\frac{W_S(E_\gamma)}{W_S(E_R)}=\frac{\frac{E_\gamma}{N_{ph}}}{\frac{E_R}{N'_{ph}}}=\frac{\frac{E_\gamma}{N_{ph}}}{\frac{\eta_R/q_n}{N'_{ph}}}$$
 remember our definition of qn = η_R / ER

traditional definition of $\,W_S = rac{E}{N_{ph}}\,$ for Y, Recoils, whatever!

traditional/experimental definition of relative scintillation efficiency

$$=\frac{W_S(E_\gamma)}{W_S(E_R)}=\frac{\frac{E_\gamma}{N_{ph}}}{\frac{E_R}{N_{ph}'}}=\frac{\frac{E_\gamma}{N_{ph}}}{\frac{\eta_R/q_n}{N_{ph}'}}=q_n\frac{W_S(E_\gamma)}{W_S(E_R)}$$
 we redefine:
$$\frac{\gamma\colon W_S=E_\gamma/N_{ph}}{R\colon W_S=\eta_R/N_{ph}'}$$

back

traditional definition of $\,W_S = rac{E}{N_{ph}}\,$ for Y, Recoils, whatever!

$$=\frac{W_S(E_\gamma)}{W_S(E_R)}=\frac{\frac{E_\gamma}{N_{ph}}}{\frac{E_R}{N'_{ph}}}=\frac{\frac{E_\gamma}{N_{ph}}}{\frac{\eta_R/q_n}{N'_{ph}}}=q_n\frac{W_S(E_\gamma)}{W_S(E_R)}^{\text{we redefine:}}$$

what we measure $\frac{RC}{\gamma} = \frac{q_n^{(R)}q_{el}^{(R)}}{q_n^{(\gamma)}q_{el}^{(\gamma)}}$

what we measure $\frac{RC}{\gamma} = \frac{q_n^{(R)}q_{el}^{(R)}}{q_n^{(\gamma)}q_{el}^{(\gamma)}}$

q ≡ quenching or
scintillation efficiency
of the recoils

what we measure $\frac{RC}{\gamma} = \frac{q_n^{(R)}q_{el}^{(R)}}{q_n^{(\gamma)}q_{el}^{(\gamma)}}$

q ≡ quenching or
scintillation efficiency
of the recoils

what we measure $\frac{RC}{\gamma} = \frac{q_n^{(R)}q_{el}^{(R)}}{q_n^{(\gamma)}q_{el}^{(\gamma)}} \text{ scintillation efficiency of the } \frac{recoils}{q_n^{(\gamma)}q_{el}^{(\gamma)}} = q_n^{(R)}\frac{q_{el}^{(R)}}{q_{el}^{(\gamma)}}$

what we measure $\frac{RC}{\gamma} = \underbrace{\frac{q_n^{(R)}q_{el}^{(R)}}{q_n^{(\gamma)}q_{el}^{(\gamma)}}}_{\text{scintillation efficiency}} \text{of the } \underbrace{\frac{RC}{q_{el}^{(\gamma)}q_{el}^{(\gamma)}}}_{\text{competition between}} = q_n^{(R)}\underbrace{\frac{q_{el}^{(R)}}{q_{el}^{(\gamma)}}}_{\text{recombination processes}}$

what we measure $\frac{RC}{\gamma} = \frac{q_n^{(R)}q_{el}^{(R)}}{q_n^{(\gamma)}q_{el}^{(\gamma)}} \text{ scintillation efficiency of the recoils} \\ = q_n^{(R)}q_{el}^{(\gamma)} \text{ scintillation only competition between} \\ = q_n^{(R)}q_{el}^{(\gamma)} \text{ recombination processes} \\ = q_n^{(r)}q_{el}^{(r)} \text{ recombination}$

what we measure $\frac{RC}{\gamma} = \frac{q_n^{(R)}q_{el}^{(R)}}{q_{el}^{(\gamma)}q_{el}^{(\gamma)}} \text{ scintillation efficiency of the } \underbrace{\frac{RC}{\gamma}}_{\text{competition between}} = q_n^{(R)} \underbrace{\frac{q_{el}^{(\gamma)}}{q_{el}^{(\gamma)}}}_{\text{recombination processes}} \underbrace{\frac{q_{el}^{(R)}q_{el}^{(R)}}{q_{el}^{(\gamma)}}}_{\text{recombination}} \text{ electrons escaping } \underbrace{\frac{q_{el}^{(R)}q_{el}^{(R)}}{q_{el}^{(\gamma)}}}_{\text{recombination}} \text{ recombination}$