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An expanding one-zone model for studying blazars emission

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Based on Boula & Mastichiadis, A&A, 2021

Epiphany 2022, Kraków

Outline

Introduction

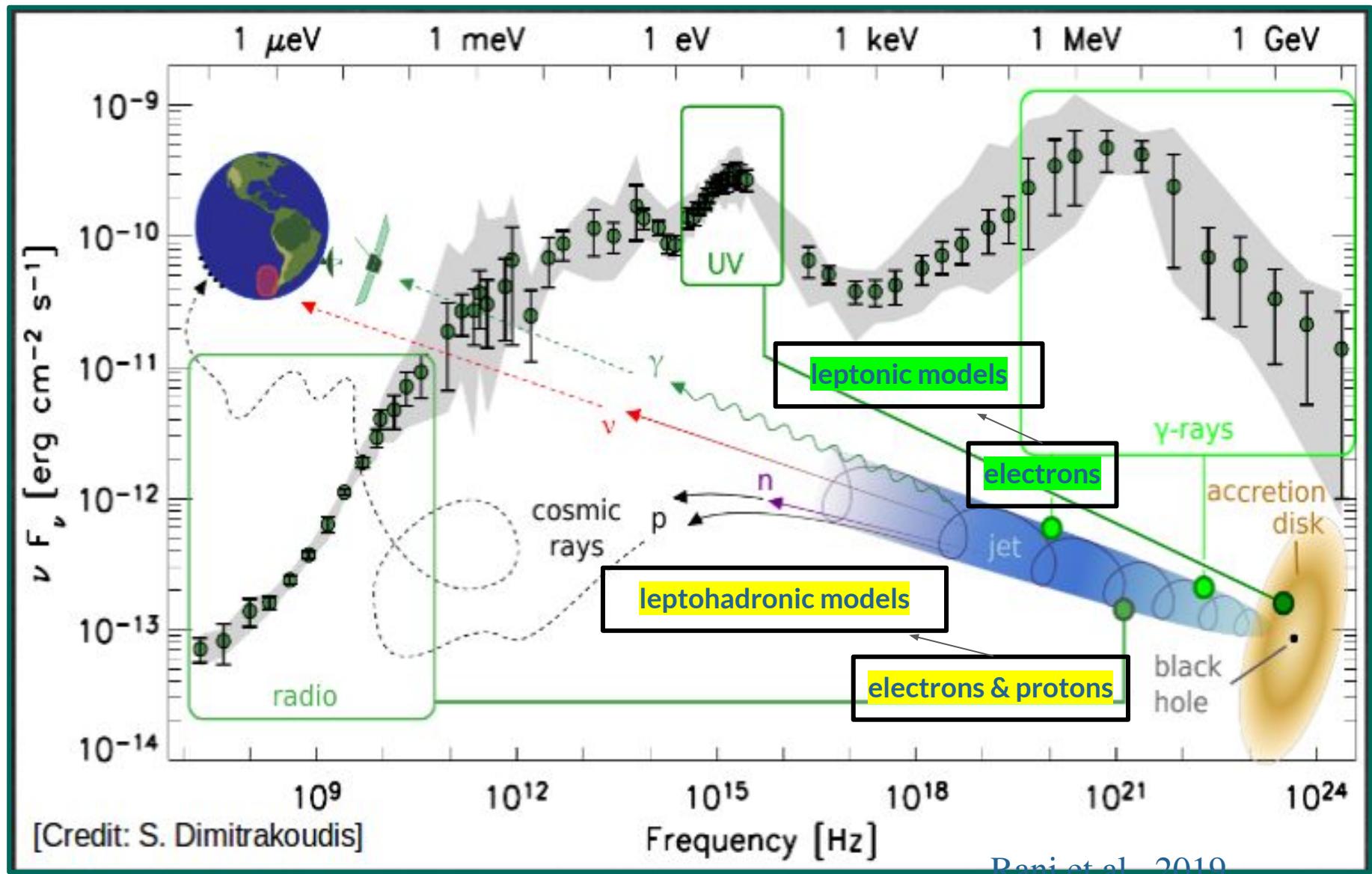
Model

Numerical Approach

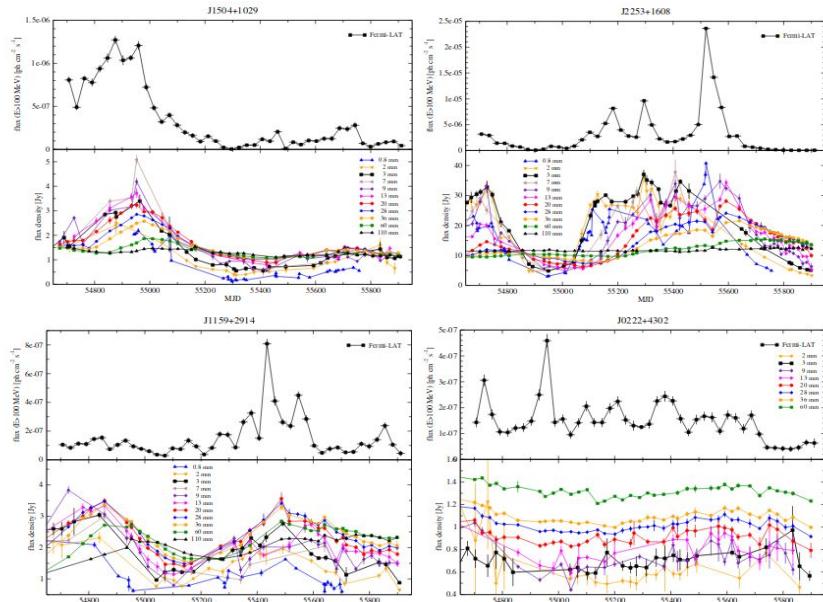
Results

Summary

Blazars Spectral Energy Distribution (SED)



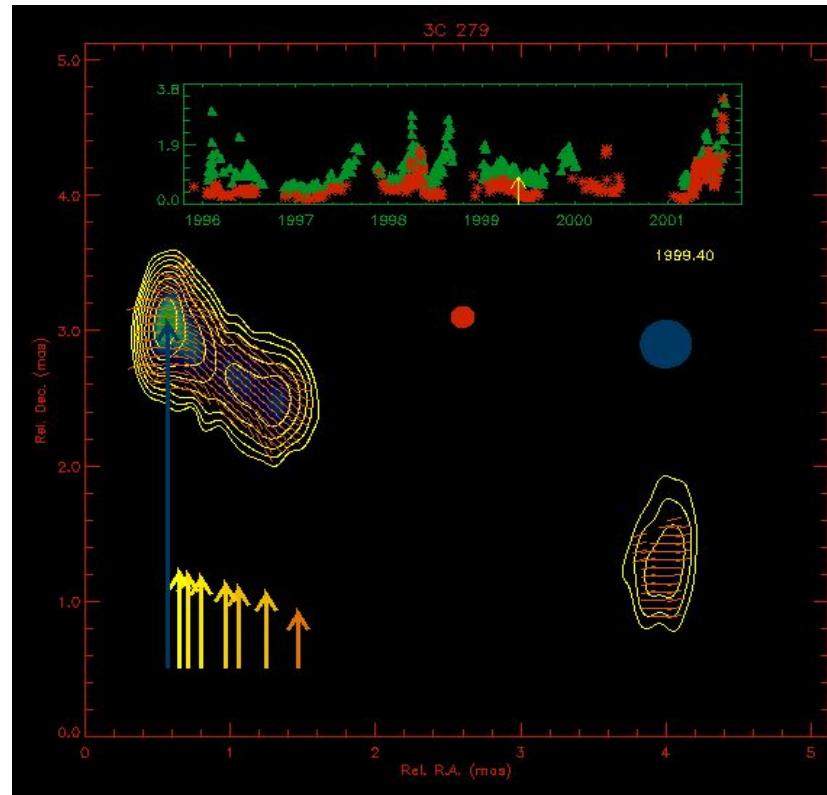
Blazars Monitoring Programs



F-gamma project

You can find a list of Blazars Monitoring Programs
at MOJAVE page:
<https://www.physics.purdue.edu/MOJAVE/blazarpogramlist.html>

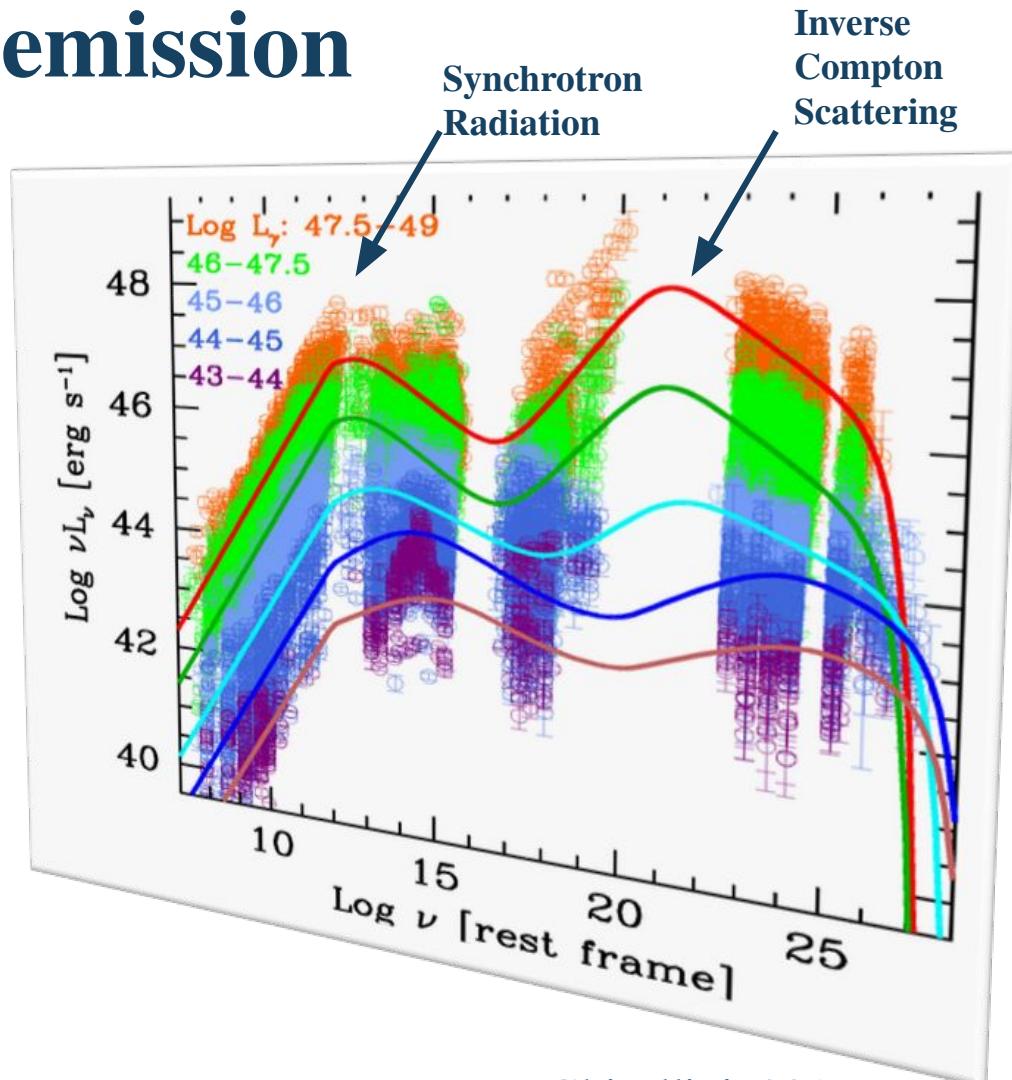
Boston University Blazar Group



Modeling the blazar emission

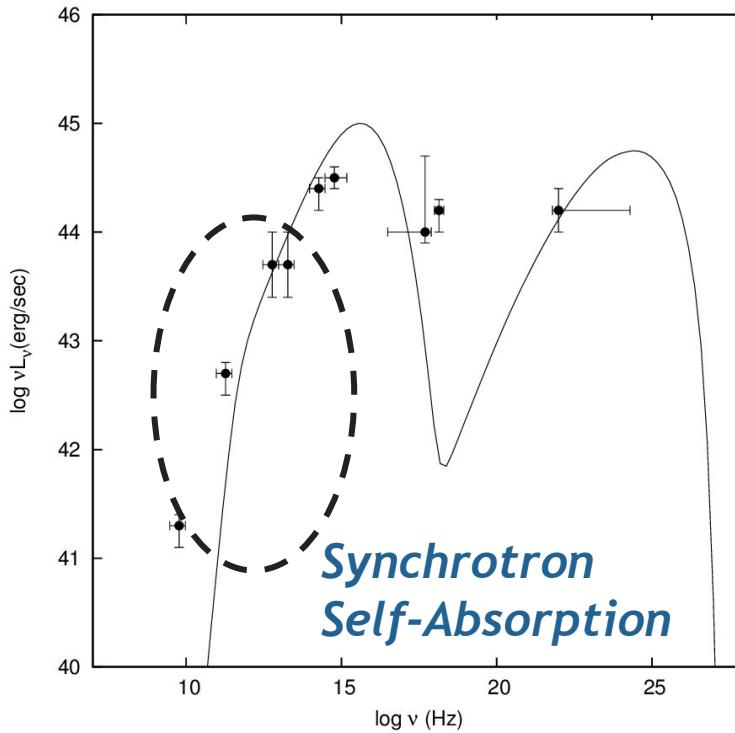
Parameters of the Leptonic Model:

- Radius of the source
- Magnetic field strength
- Electrons energy distribution
- Photon fields
- Bulk Lorentz factor
- Doppler factor



Ghisellini, 2017

Limitations of the one zone leptonic models



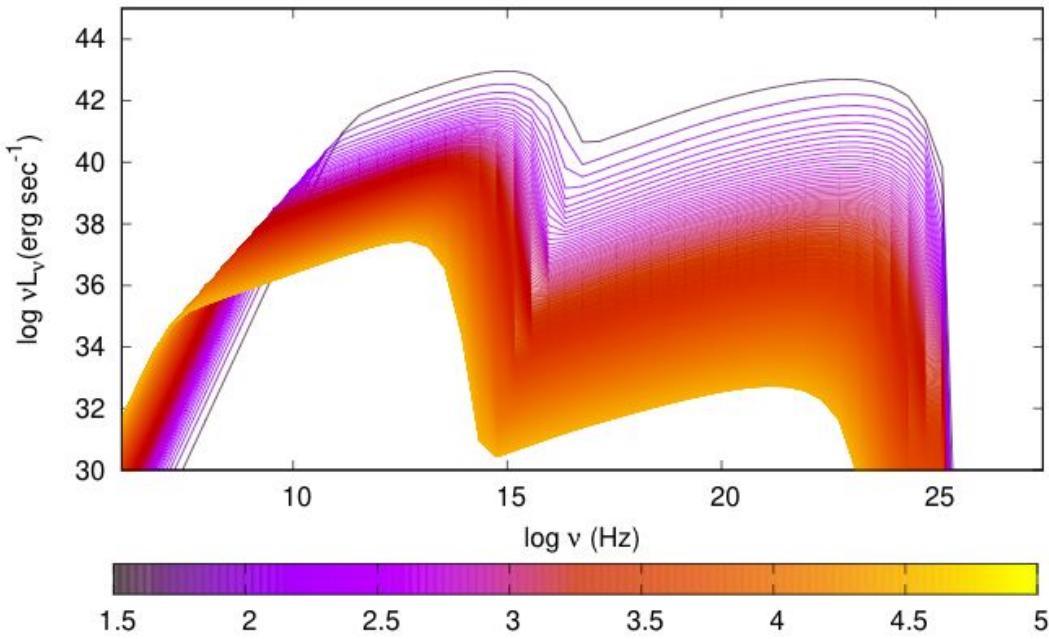
Numerical code:
Mastichiadis & Kirk, 1995, A&A

$$\nu_{ssa} = \left[\frac{\sqrt{3}q^3}{8\pi m} \left(\frac{3q}{2\pi m^3 c^5} \right)^{\frac{p}{2}} C(B \sin \alpha)^{\frac{p+2}{2}} \Gamma \left(\frac{3p+2}{12} \right) \Gamma \left(\frac{3p+22}{12} \right) R \right]^{\frac{2}{p+4}}$$

Rybicki & Lightman, 1974

A new numerical approach:

A one-zone expanding model



- Synchrotron Radiation
- Inverse Compton Scattering
- Synchrotron Self Absorption
- Photon-Photon Absorption
- Adiabatic Losses

in an **expanding** source

A new numerical code based on Mastichiadis & Kirk, 1995, 1997; see also Boula et al., 2019, Boula & Mastichiadis 2021

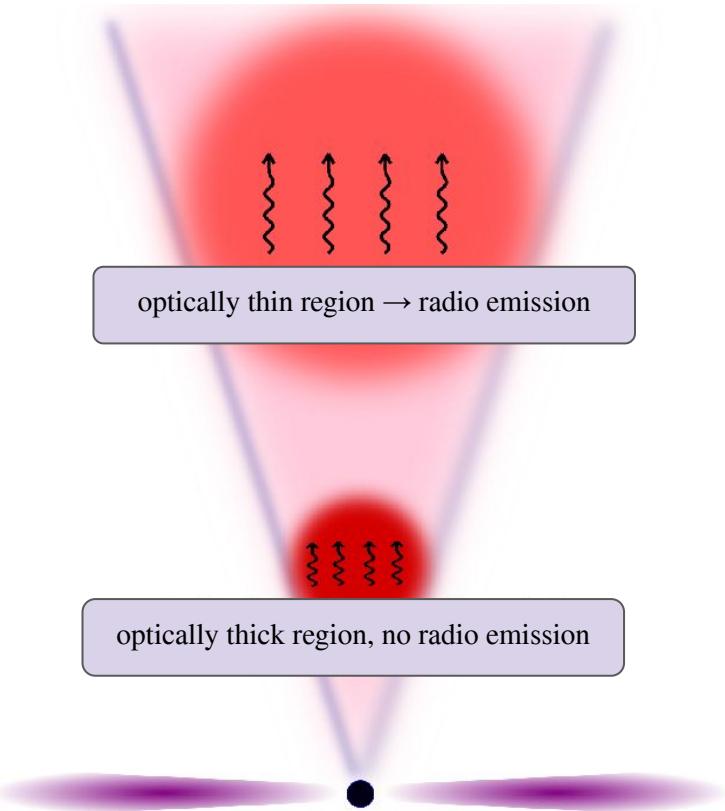
Model

- Spherical regions of accelerated particles, that move along the jet and at the same time are expanding.
- Superposition of the emission of these blobs leads to a continuous jet emission.

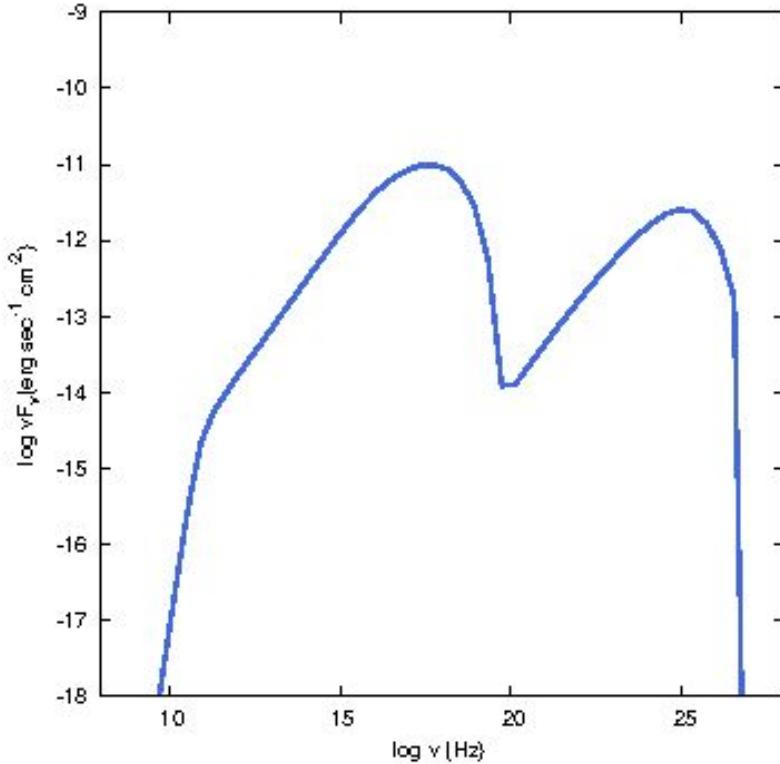
$$R(t) = R_0 + u_{exp} t, \quad B = B_0 (R_0/R)^s$$

$$\frac{\partial N(\gamma, R)}{\partial R} + \frac{\partial}{\partial \gamma} \left[(A_{syn}(\gamma, R) + A_{ICS}(\gamma, R) + A_{exp}(\gamma, R)) N(\gamma, R) \right] = Q_e(\gamma, R),$$

$$Q_e(\gamma, R) = q_e(R) \gamma^{-p} = q_{e0} \left(\frac{R_0}{R} \right)^\chi \gamma^{-p}, \quad \gamma_{min} \leq \gamma \leq \gamma_{max}.$$



Steady State Emission of Mrk 421



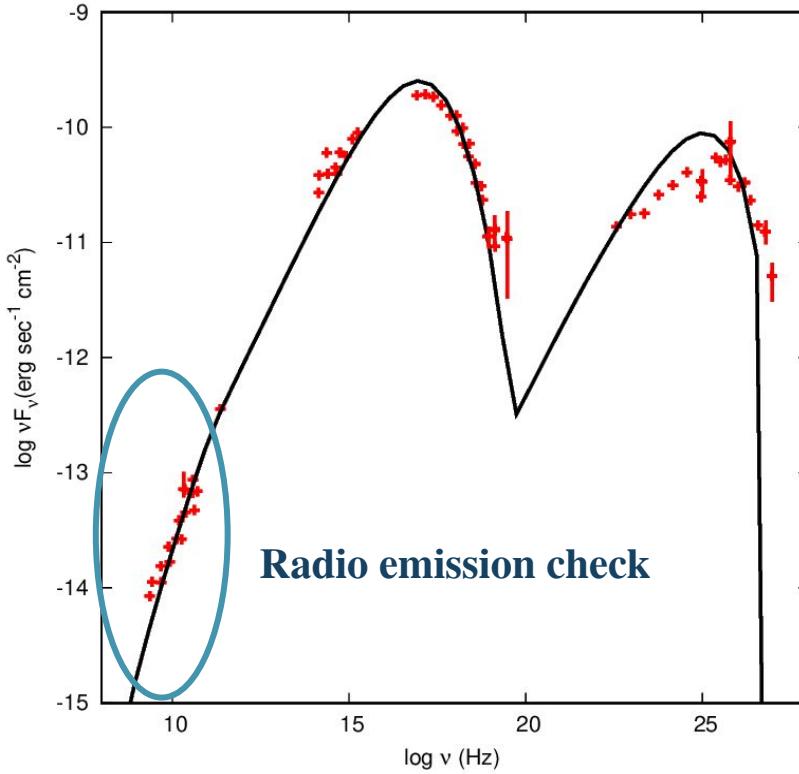
Produced by superposition of expanding blobs injected at $z_0 = 0.01$ pc with the following properties:

$$B_0 = 0.3 \text{ G}, R_0 = 1.e16 \text{ cm}, L_{\text{inj e0}} = 3.e41 \text{ erg/s}, u_{\text{exp}} = 0.2c, \gamma_{\text{min}} = 1, \gamma_{\text{max}} = 1.e6,$$

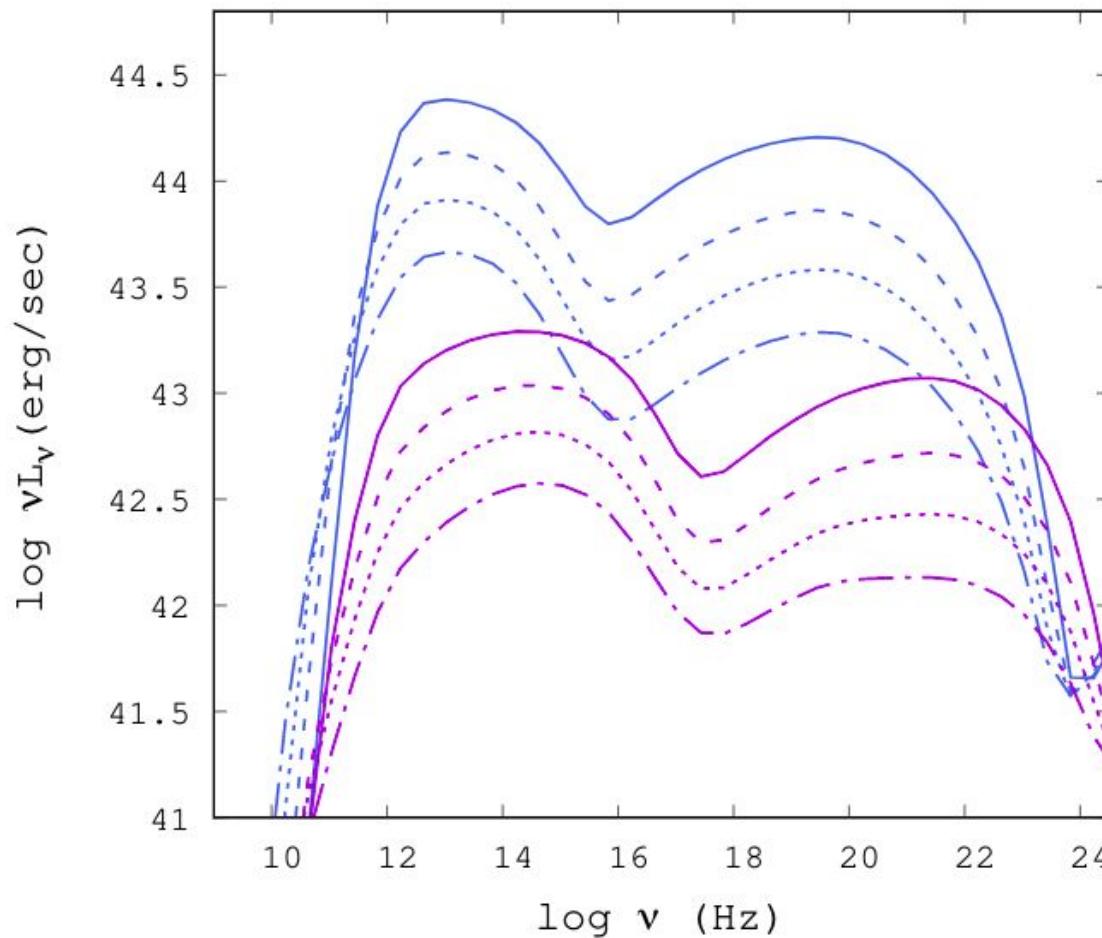
slope index = -2, $\delta = 10$.

The magnetic field and electron injection luminosity decrease linearly with radius

Steady State Emission of Mrk 421

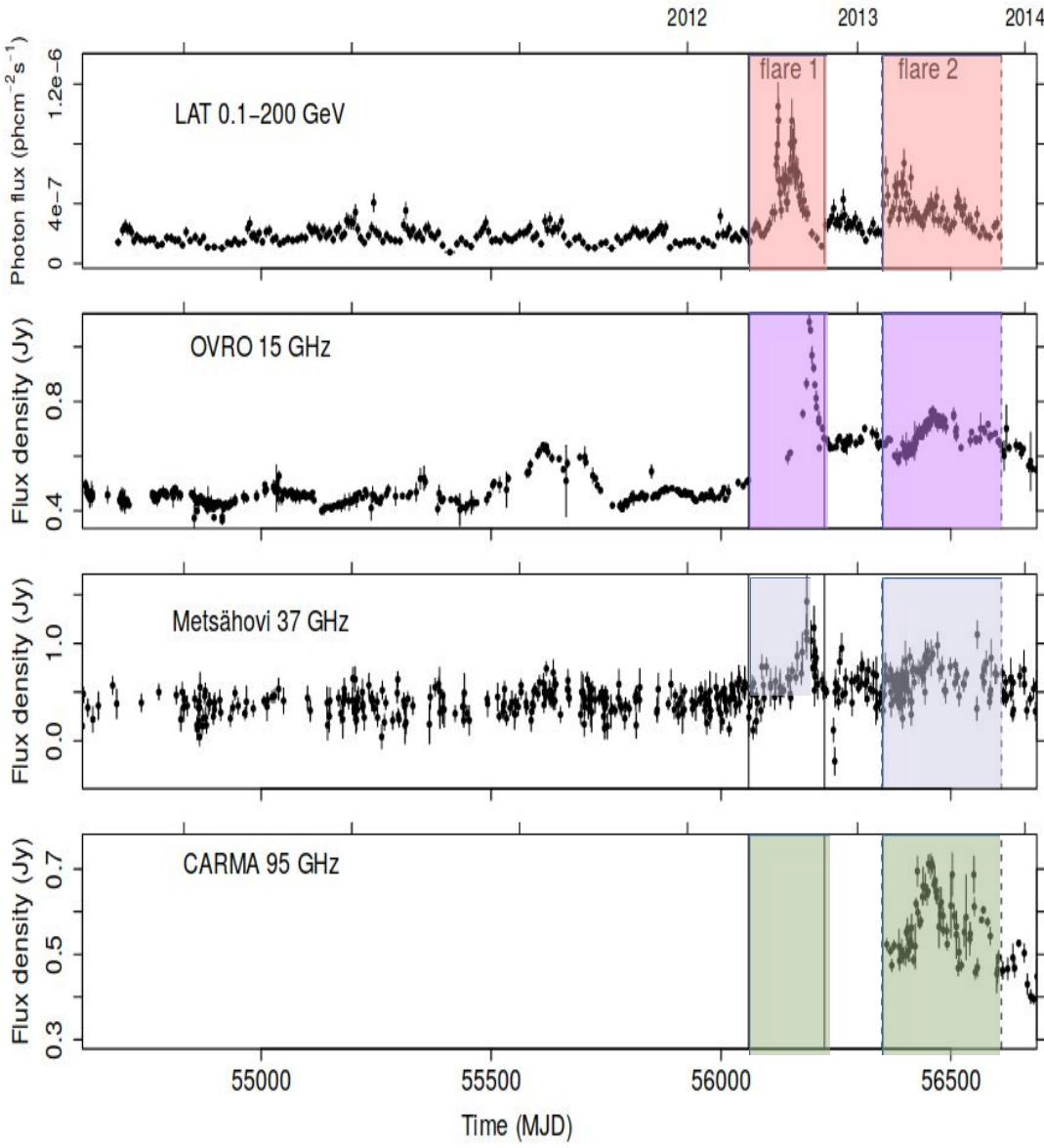


Different mass accretion rates and expansion velocities



B_0 (G)	$L_{e_0}^{inj}$ (erg/sec)	γ_{max}	Blazar Class
1.5	43.5	4	LBL
1.0	42.5	5	HBL

$$u_{exp} = 0.010, 0.025, 0.050, 0.100$$

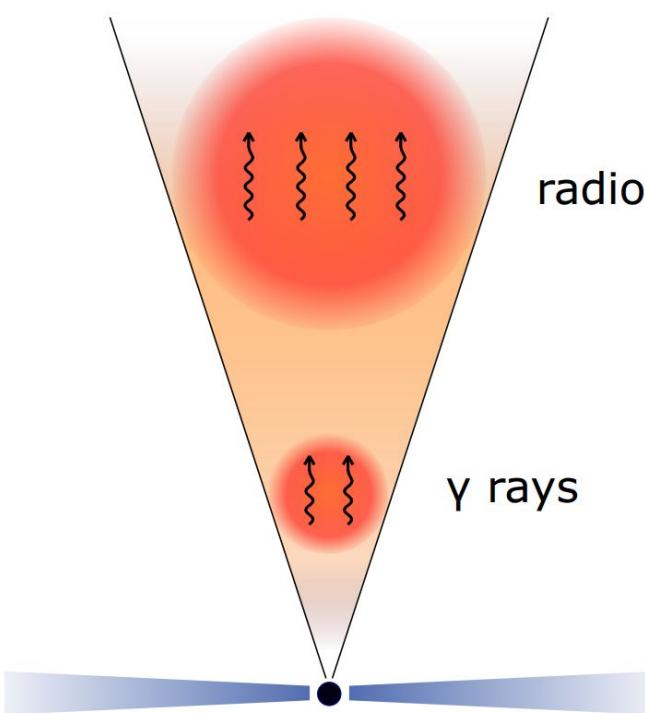


A combined radio and GeV gamma-ray view of the 2012 and 2013 flares of Mrk 421 (Hovatta et al., 2015)

Challenges: The connection of γ -ray and radio flare

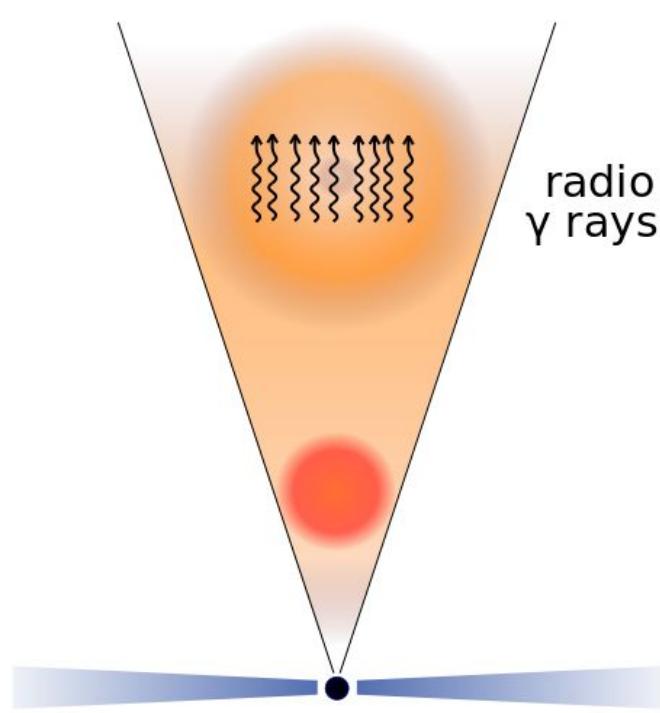
- Is there a causal connection between γ -ray and radio flares?
- What drives the time-lag between radio and γ -ray flares?

Flaring Episodes



Case 1

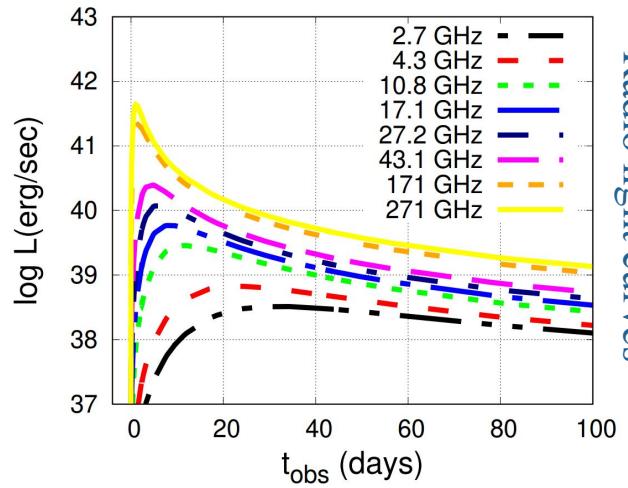
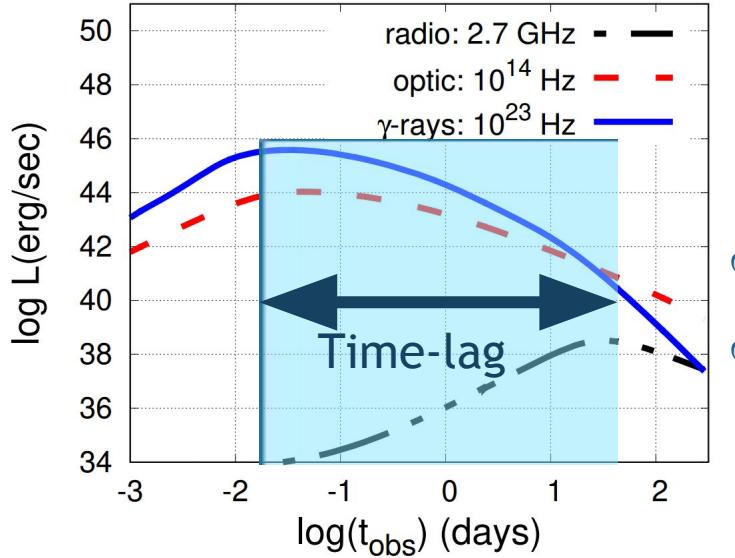
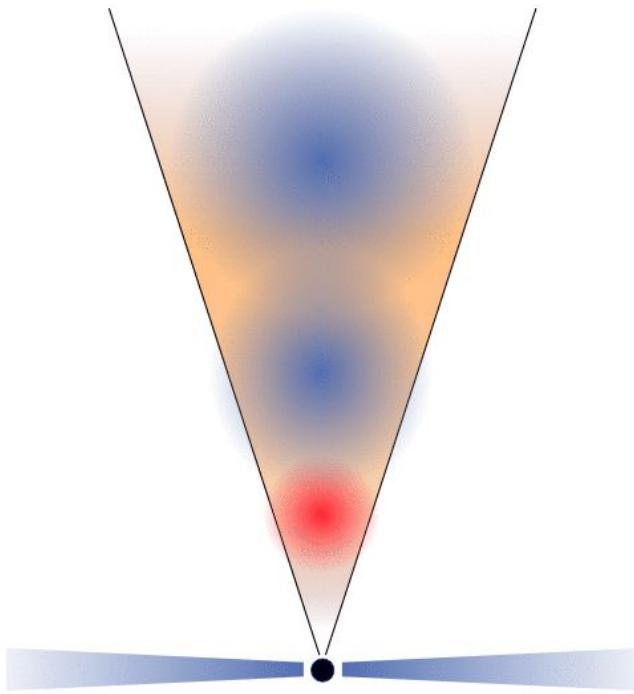
Blob with different initial properties → flare



Case 2

Particle re-acceleration at a distance z → flare

Case 1



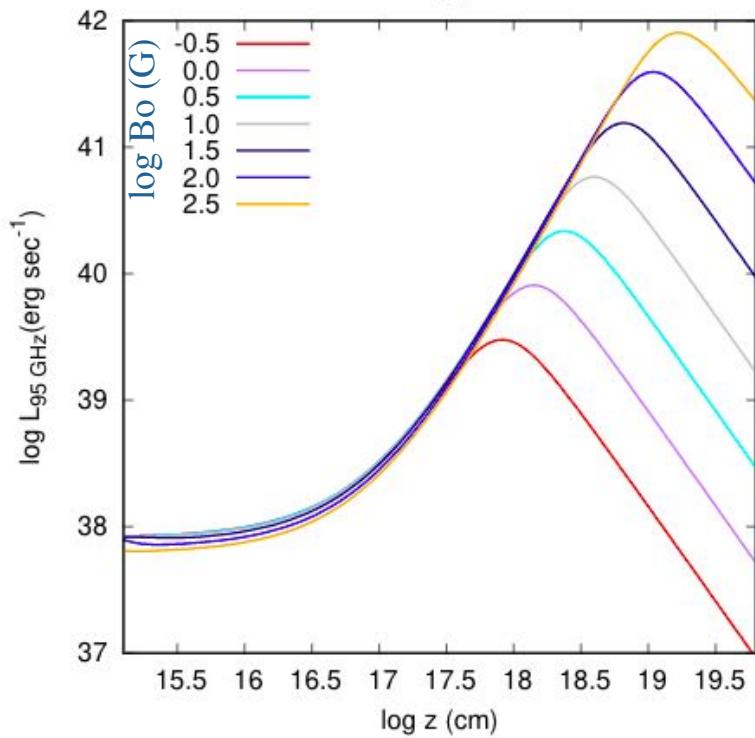
Produced by a single blob injected at $z_0 = 0.001$ pc with the following properties:

$$B_0 = 1 \text{ G}, R_0 = 1.e15 \text{ cm}, L_{\text{inj e0}} = 1.e43 \text{ erg/s}, u_{\text{exp}} = 0.4c, \gamma_{\text{min}} = 1, \gamma_{\text{max}} = 1.e5, p = 2, \delta = 10.$$

The magnetic field and electron injection luminosity decrease linearly with radius

Boula et al., 2019

The role of the initial Magnetic Field

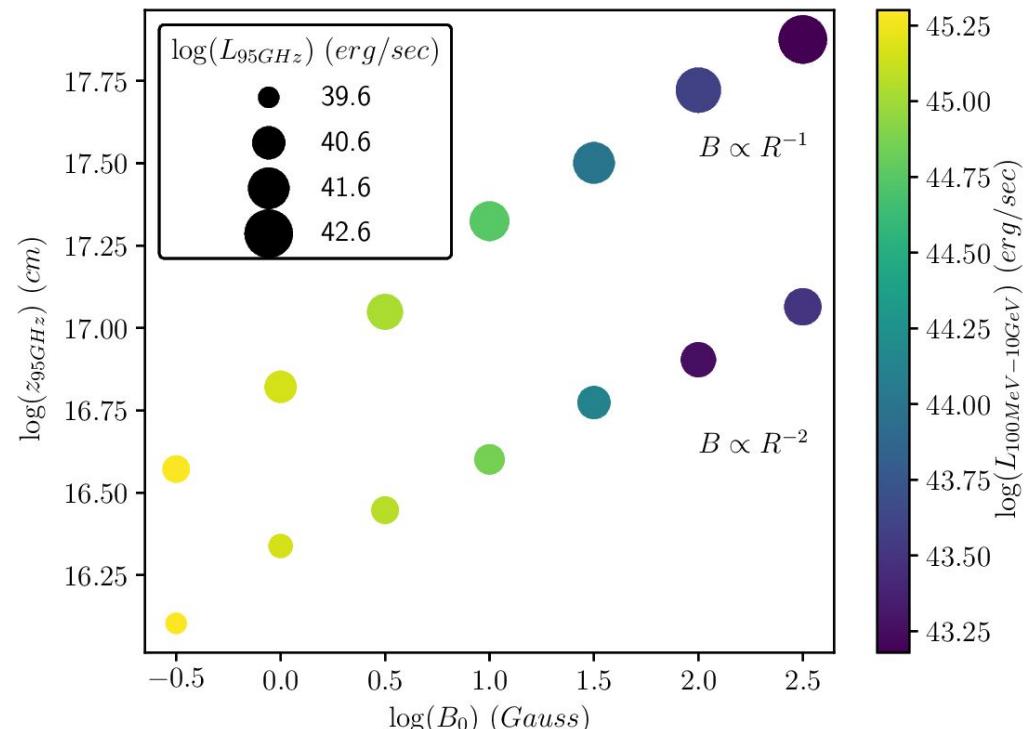


The values of the rest parameters:

$$R_0 = 1.e15 \text{ cm}, L_{\text{inj e}0} = 1.e42 \text{ erg/s}, u_{\text{exp}} = 0.01c,$$

$$\gamma_{\min} = 1, \gamma_{\max} = 1.e6, \text{slope index} = -2, \delta = 10.$$

The magnetic field strength and electron injection luminosity decrease linearly with radius



The values of the rest parameters:

$$R_0 = 1.e15 \text{ cm}, L_{\text{inj e}0} = 1.e42 \text{ erg/s}, u_{\text{exp}} = 0.1c,$$

$$\gamma_{\min} = 1, \gamma_{\max} = 1.e6, \text{slope index} = -2, \delta = 10.$$

The electron injection luminosity decrease linearly with radius

Case 2

A particle re-acceleration episode “somewhere” into the jet could produce a photon flare.

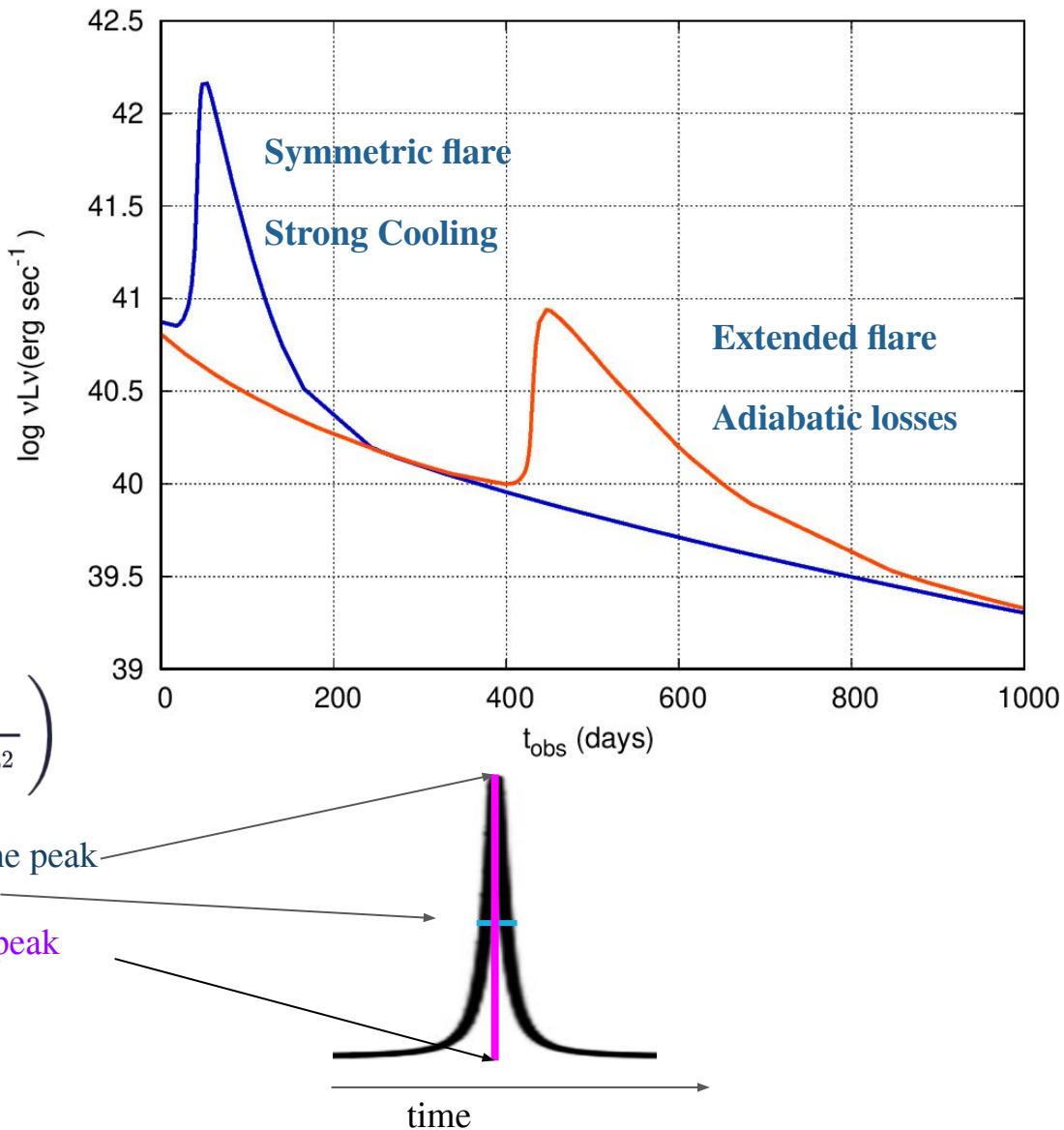
Here we use the assumption that this injection has the form of a lorentzian distribution.

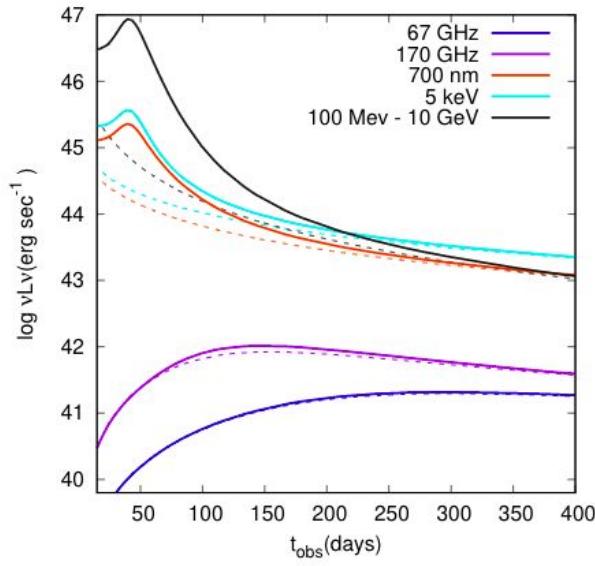
$$Q_e(\gamma, t) = q_e(t)\gamma^{-p} \left(1 + \frac{\alpha w^2}{4(t-t_0)^2+w^2} \right)$$

α =the value of the luminosity at the peak

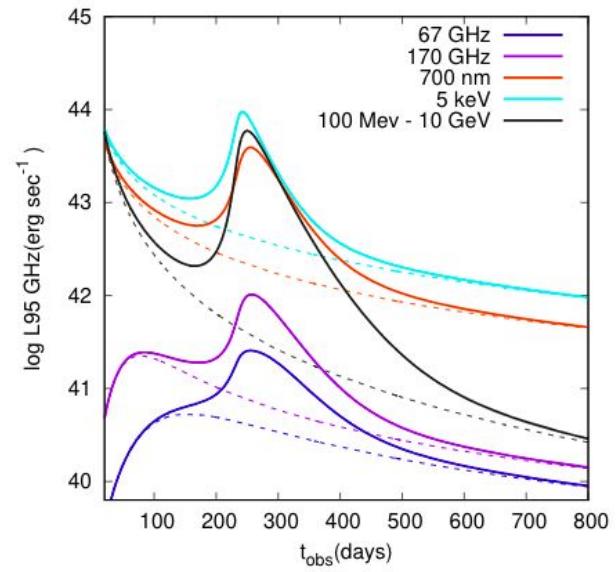
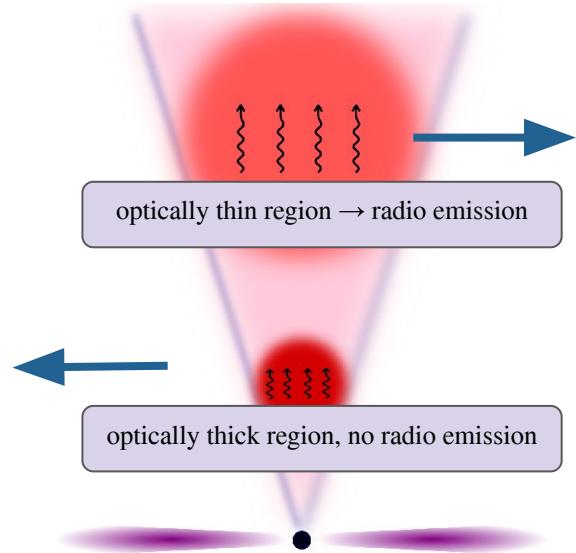
w =the width of the injection

t_0 =the time of the injection at the peak





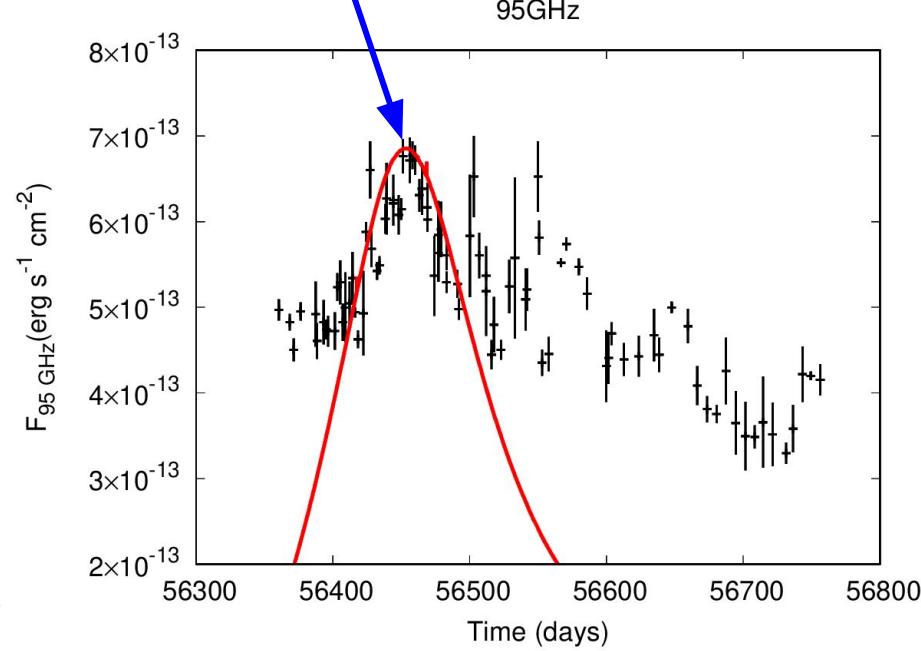
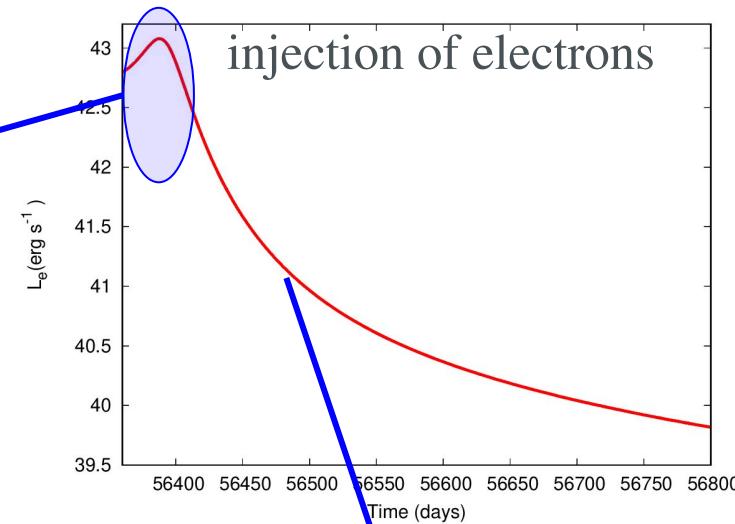
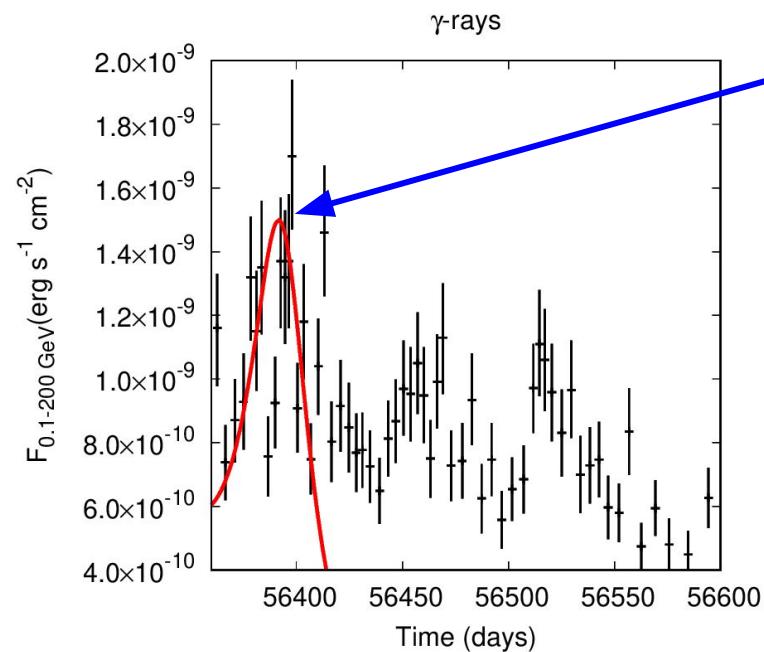
optically thick region



optical thin region

Gamma-ray flare is produced by a re-acceleration episode close to the central engine and radio flare is produced by the transition from the optical thick to the optically thin region

Application to Mrk 421 2013 flaring episode



$$B_0 = 1.25 \text{ G}, R_0 = 4.e16 \text{ cm}, L_{\text{inj } e0} = 1.58e42 \text{ erg/s},$$

$$u_{\text{exp}} = 0.05c, \gamma_{\min} = 1, \gamma_{\max} = 1.e5, p = 2,$$

$$\delta = 10.$$

$$t_{\text{inj}} = 40t_{\text{cross}}, \alpha = 60, w = 22t_{\text{cross}}$$

$$B \propto R^{-1}$$

$$L_e \propto R^{-2}$$

Data by Hovatta et al., 2015

“Keep” home message

- Development of a new one-zone expanding radiation model.
- Study of the steady state emission.
- Prediction of zero or positive time lags, i.e., the γ -rays come first and the radio follow.
- Flares in radio and γ -rays with a wide range of time-lags may be produced by re-acceleration of electrons.
- Correlations between γ -rays and radio flares are studied.



thank you!
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