

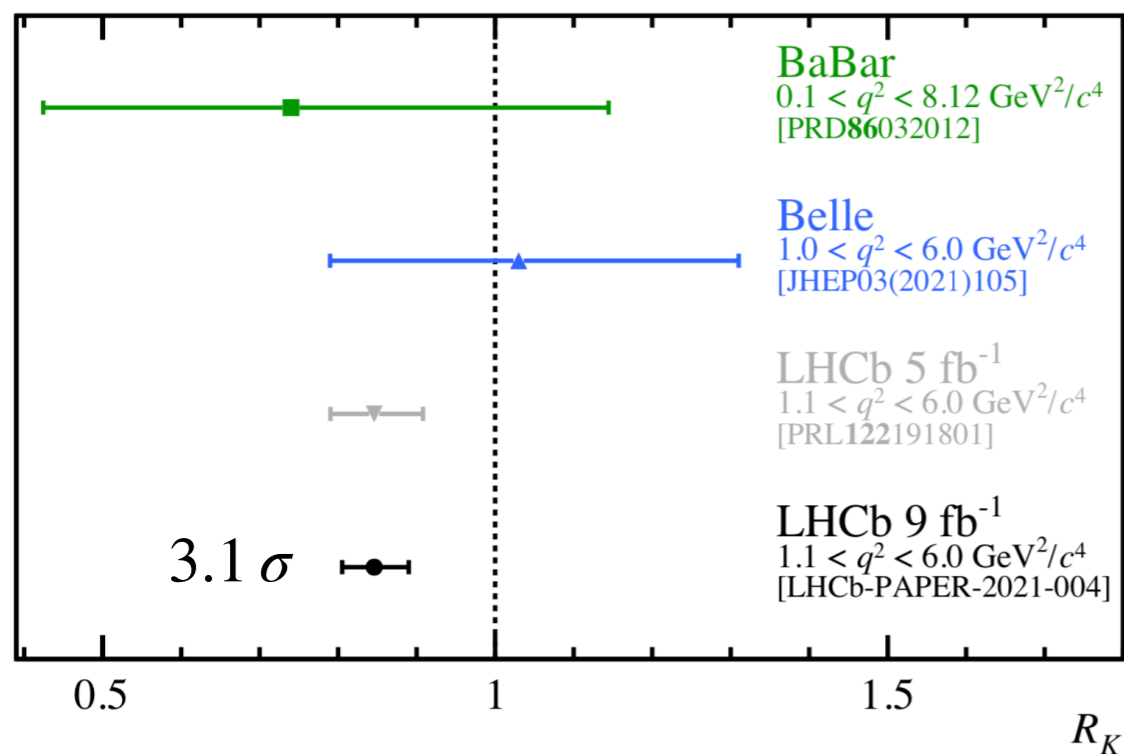
# Muonic force behind flavor anomalies

**Admir Greljo**

I will review our recent work on lepton flavor non-universal and anomaly-free  $U(1)$  gauge extensions of the SM. The phenomenological discussion will be centered around flavor anomalies in rare B-meson decays and muon  $g-2$ . This talk is based on [2103.13991](#) (AG, Stangl, and Thomsen) and [2107.07518](#) (AG, Soreq, Stangl, Thomsen, and Zupan).

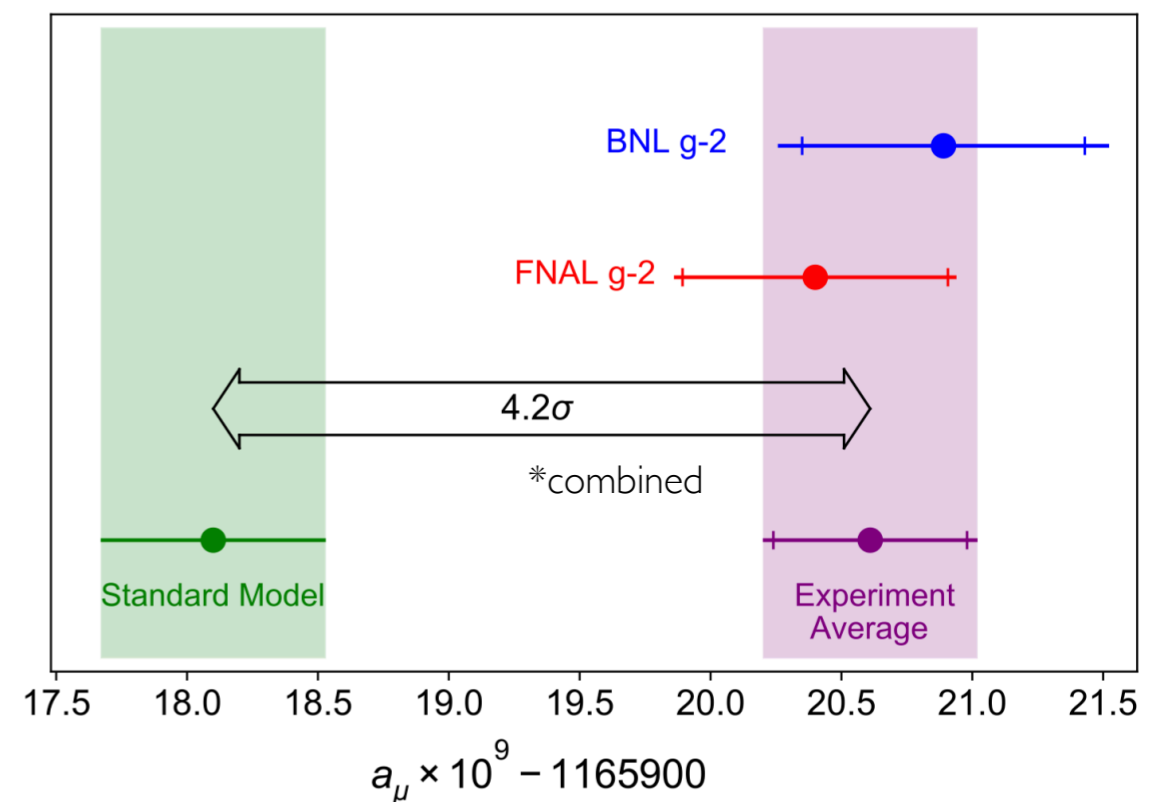
# Muon Anomalies

## Footprints of a next layer?



LHCb, CERN, 2103.11769

+ other  $b \rightarrow s \mu \mu$  observables

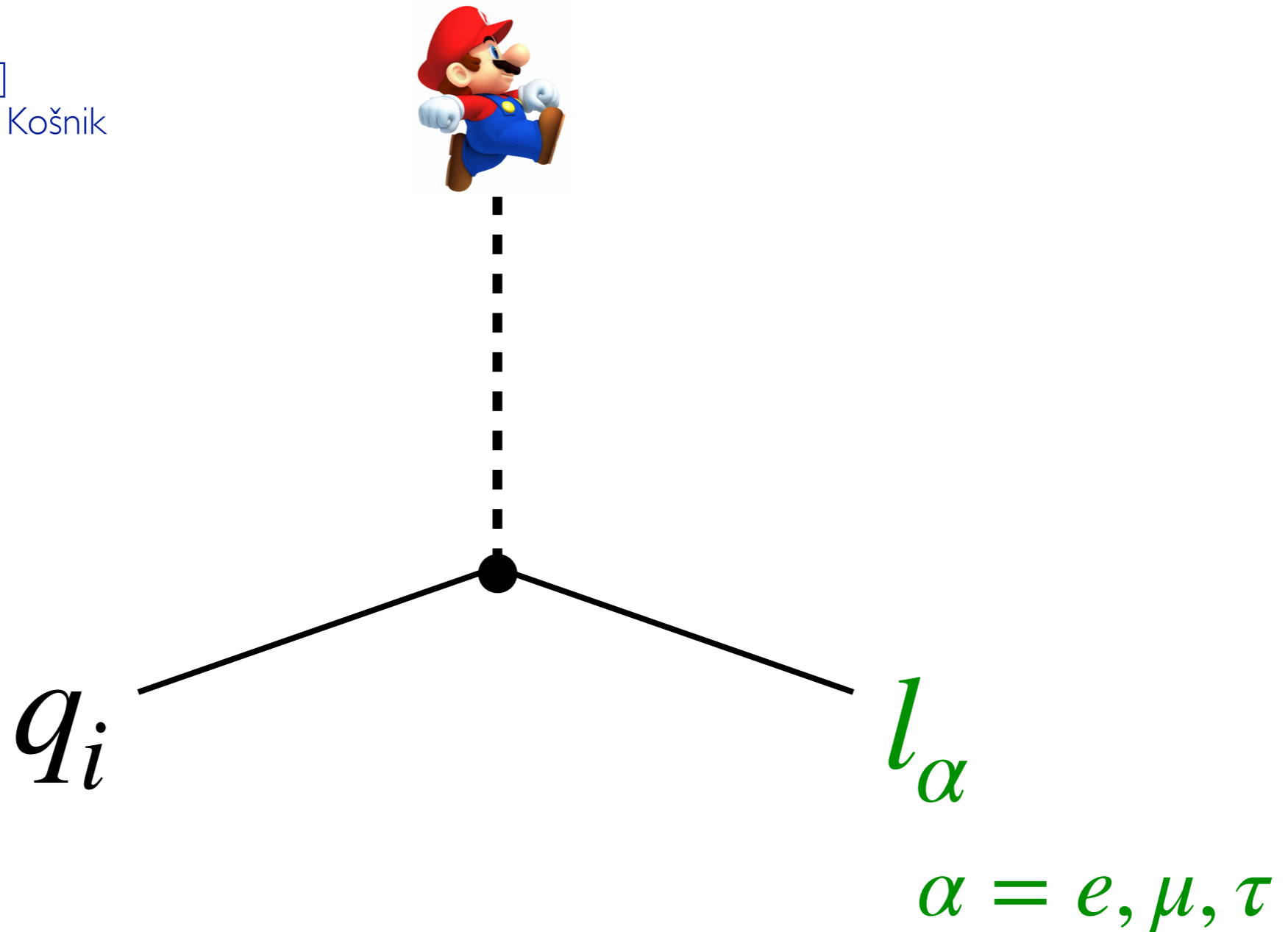


The Muon g-2, Fermilab, 2104.03281



# Leptoquark

[Phys.Rept. 641 (2016) 1-68]  
Doršner, Fajfer, AG, Kamenik, Košnik



- Portorož 2021's favourite game
- TeV-scale LQs were not exactly a popular game before the anomalies  
=> [next slide]

# Leptoquark

$$\mathcal{L}_4 = y_{ij} Q^i L^j S + z_{ij} Q^i Q^j S^\dagger$$

$B(S) = -\frac{1}{3}$                        $B(S) = \frac{2}{3}$

- Abrupt violation of the SM accidental symmetries (exact and approximate)

~~$U(1)_B$~~  Proton decay  $[z \cdot y]$  probes scales up to  $10^{13}$  TeV

~~$U(1)_e \times U(1)_\mu \times U(1)_\tau$~~   $\mu \rightarrow e \gamma$   $[i \neq j]$  probes scales up to  $10^5$  TeV

~~$CP$~~  Electron EDM  $[\text{Im } y]$  probes scales up to  $10^6$  TeV

~~$U(3)_L \times U(3)_E$~~  LFUV, ...  $R(K)$  probes up to  $10^2$  TeV

# Accidental symmetries

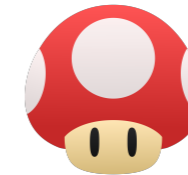
- Accidental symmetries emerge from:
  1. Spacetime + **Gauge symmetry** and Field content.
  2. Lagrangian(x) = infinite polynomial in fields and derivatives, but only a finite number of IR relevant operators  $\mathbf{dim}[\mathcal{L}] \leq 4$
- In the SM, all IR relevant operators respect:
$$U(1)_B \times U(1)_e \times U(1)_\mu \times U(1)_\tau$$

# Gauged lepton flavor $U(1)_X$

## Leptoquark



+



## Muonquark

= LQ with the  $U(1)_X$  charge:



✓  $q\mu S$

✗  $qeS, q\tau S, qqS^\dagger$   
 $qqS^\dagger H, qqS^\dagger \phi$

Hambye, Heeck; 1712.04871

Davighi, Kirk, Nardecchia, 2007.15016

AG, Stangl, Thomsen, 2103.13991

AG, Soreq, Stangl, Thomsen, Zupan; 2107.07518

- The accidental symmetry is  $U(1)_B \times U(1)_e \times U(1)_\mu \times U(1)_\tau$  and the LQ charge is  $(-1/3, 0, -1, 0)$

# The $U(1)_X$ atlas

- $SU(3)_C \times SU(2)_L \times U(1)_Y \times U(1)_X$  gauge group

- Chiral fermions:

$$\begin{array}{lll}
 Q_i \sim (\mathbf{3}, \mathbf{2}, \frac{1}{6}, X_{Q_i}), & U_i \sim (\mathbf{3}, \mathbf{1}, \frac{2}{3}, X_{U_i}), & D_i \sim (\mathbf{3}, \mathbf{1}, -\frac{1}{3}, X_{D_i}), \\
 L_i \sim (\mathbf{1}, \mathbf{2}, -\frac{1}{2}, X_{L_i}), & E_i \sim (\mathbf{1}, \mathbf{1}, -1, X_{E_i}), & N_i \sim (\mathbf{1}, \mathbf{1}, 0, X_{N_i})
 \end{array}$$

Left-handed  $\longleftrightarrow$  Right-handed

- The symmetry breaking scalar fields:

$$H = (\mathbf{1}, \mathbf{2}, \frac{1}{2}, X_H), \quad \phi = (\mathbf{1}, \mathbf{1}, 0, X_\phi)$$

- Without loss of generality  $X_H = 0$

\* By field redefinitions, shifting  $X_f \rightarrow X_f - aY_f$  for all fields, gives an equivalent theory.

# The $U(1)_X$ atlas

- $SU(3)_C \times SU(2)_L \times U(1)_Y \times U(1)_X$  gauge group

$$\begin{aligned}
 Q_i &\sim (\mathbf{3}, \mathbf{2}, \frac{1}{6}, X_{Q_i}), & U_i &\sim (\mathbf{3}, \mathbf{1}, \frac{2}{3}, X_{U_i}), & D_i &\sim (\mathbf{3}, \mathbf{1}, -\frac{1}{3}, X_{D_i}), \\
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 \end{aligned}$$

Anomaly cancelation conditions:

$$\begin{aligned}
 SU(3)_C^2 \times U(1)_X &: \sum_{i=1}^3 (2X_{Q_i} - X_{U_i} - X_{D_i}) = 0, \\
 SU(2)_L^2 \times U(1)_X &: \sum_{i=1}^3 (3X_{Q_i} + X_{L_i}) = 0, \\
 U(1)_Y^2 \times U(1)_X &: \sum_{i=1}^3 (X_{Q_i} + 3X_{L_i} - 8X_{U_i} - 2X_{D_i} - 6X_{E_i}) = 0, \\
 \text{Gravity}^2 \times U(1)_X &: \sum_{i=1}^3 (6X_{Q_i} + 2X_{L_i} - 3X_{U_i} - 3X_{D_i} - X_{E_i} - X_{N_i}) = 0, \\
 U(1)_Y \times U(1)_X^2 &: \sum_{i=1}^3 (X_{Q_i}^2 - X_{L_i}^2 - 2X_{U_i}^2 + X_{D_i}^2 + X_{E_i}^2) = 0, \\
 U(1)_X^3 &: \sum_{i=1}^3 (6X_{Q_i}^3 + 2X_{L_i}^3 - 3X_{U_i}^3 - 3X_{D_i}^3 - X_{E_i}^3 - X_{N_i}^3) = 0.
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 \end{aligned}$$

- Unification  $\Rightarrow$  Rational charges. Rescale  $g_X \Rightarrow$  Integer charges.

$$-10 \leq X_{F_i} \leq 10 \Rightarrow 21'546'920 \text{ inequivalent solutions (i.e. up to flavor permutation, etc)}$$

\*to be explored

# The $U(1)_X$ atlas

Quark flavor universal

- $Y^{u,d}$  are allowed  $\Rightarrow X_{Q_i} = X_{U_j} = X_{D_k}$   $-10 \leq X_{F_i} \leq 10$   
 $(X_H = 0)$  **[276 inequivalent solutions]**



# The $U(1)_X$ atlas

## Quark flavor universal

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[276 inequivalent solutions]  
 $(X_H = 0)$
- Muoquark requirement  
 eg.  $S_3$  LQ:  $X_{L_2} \neq \{X_{L_{1,3}}, -3X_q\}$  [273 inequivalent solutions]
- $Y^e$  allowed  $\Rightarrow$  **vector category** :  $X_{L_i} = X_{E_i}$  [252 inequivalent solutions]  
**chiral category** : the rest. [21 inequivalent solutions]

# The $U(1)_X$ atlas

## Third-family-quark

- The “2+1” charge assignment

$$X_{Q_i} = X_{U_j} = X_{D_k} \equiv X_{q_{12}} \quad \text{for all } i, j, k = 1, 2, \quad \text{and}$$

$$X_{Q_3} = X_{U_3} = X_{D_3} \equiv X_{q_3} \quad . \quad (X_H = 0)$$

- The CKM elements ( $V_{td}, V_{ts}$ ) at dim-5:

$$\mathcal{L} \supset \frac{x_i^u}{\Lambda} \bar{Q}_i \tilde{H} \phi U_3 + \frac{x_i^d}{\Lambda} \bar{Q}_i H \phi D_3 + \text{H.c.}$$

# The $U(1)_X$ atlas

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- The ACC conditions are satisfied provided

$$2X_{q_{12}} + X_{q_3} = 3X_q$$

\*The quark flavor-universal solutions can immediately be extended to the 2 + 1 case.

- The muoquark conditions slightly change:  $X_{q_{12}} = 0$

$$\text{eg. } S_3 \text{ LQ: } X_{L_2} \neq \{X_{L_{1,3}}, X_{L_{1,3}} - X_{q_3}, -X_{q_3}, -2X_{q_3}, -3X_{q_3}\} \quad \text{[171 inequivalent sol.]}$$

$$-10 \leq X_{F_i} \leq 10$$

# Example: Vector category

- Two scalar LQs:

$$S_3 = (\bar{\mathbf{3}}, \mathbf{3}, 1/3, X_{S_3}) \quad + \quad S_1 = (\bar{\mathbf{3}}, \mathbf{1}, 1/3, X_{S_1})$$

$$\mathcal{L} \supset \eta^{3L} Q_3 L_2 S_3$$

$$\mathcal{L} \supset \eta^{1L} Q_3 L_2 S_1 + \eta^{1R} U_3 E_2 S_1$$

See the talk by David Marzocca

(\*) The  $X_\mu$  decoupling:  $g_X \rightarrow 0, m_X \rightarrow \infty$

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- $U(1)_X$  examples: 
  - $U(1)_{B-3L_\mu}$  with LQ charges  $+8/3$
  - $U(1)_{B_3-\frac{8}{3}L_\mu-\frac{1}{3}L_\tau}$  with LQ charges  $+7/3$

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- $U(1)_X$  examples: 

-  $U(1)_{B-3L_\mu}$  with LQ charges  $+8/3$

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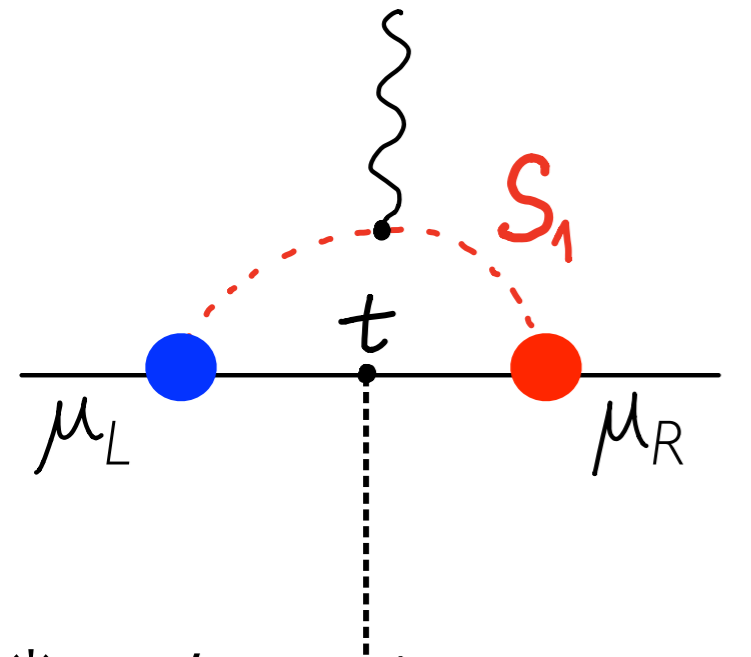
## Quark Flavour Structure

$$\eta^{1(3)L} \propto \mathcal{O}(V) \oplus 1$$

$$\eta^{1R} \propto \mathcal{O}(\Delta_u^\dagger V) \oplus 1$$

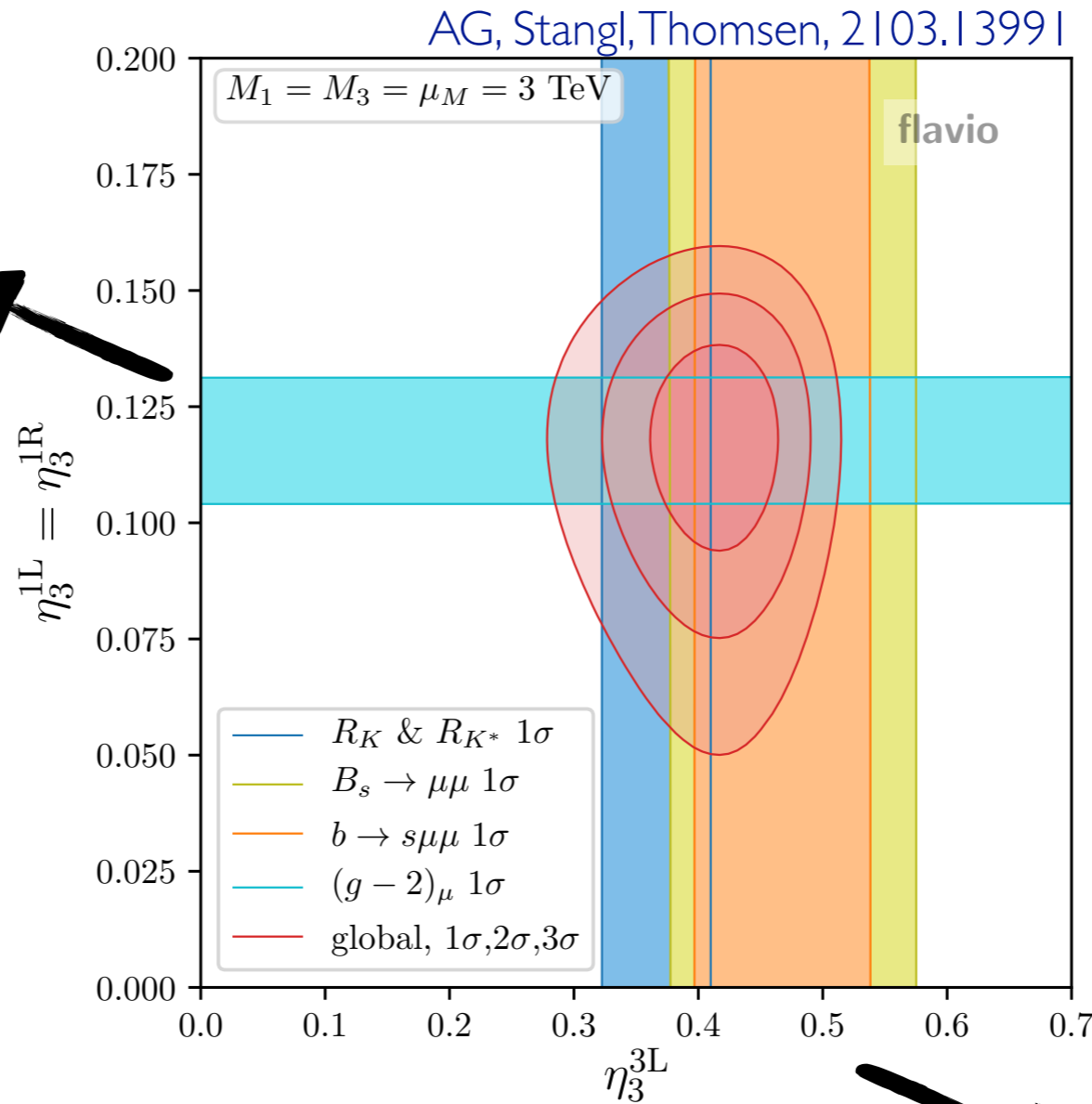
$V = (2, \mathbf{1}, \mathbf{1}) = (V_{td}, V_{ts})^T$ ,  $\Delta_u = (2, \bar{\mathbf{2}}, \mathbf{1})$  and  $\Delta_d = (2, \mathbf{1}, \bar{\mathbf{2}})$   
under  $U(2)_Q \times U(2)_U \times U(2)_D$  Barbieri et al; I 105.2296

# Example: Vector category



\*  $m_t/m_\mu$  enhancement

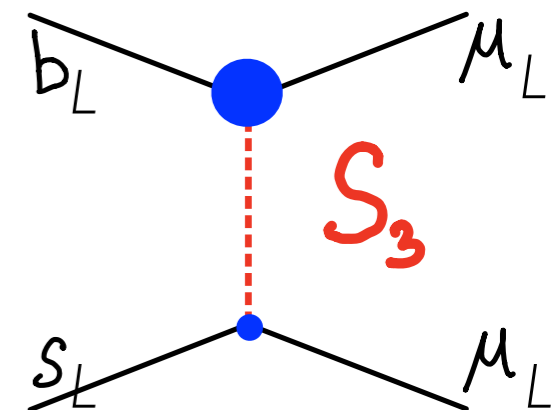
- Queiroz, Shepherd; 1403.2309,
- Dorsner, Fajfer, AG, Kamenik, Kosnik; 1603.04993,
- Coluccio Leskow, Crivellin, D'Ambrosio, Müller; 1612.06858
- Dorsner, Fajfer, Sumensari; 1910.03877
- Gherardi, Marzocca, Venturini; 2008.09548
- + many more



$$\eta_i^{3L} = (V_{td}, V_{ts}, 1) \eta_3^{3L}$$

\* V-A structure

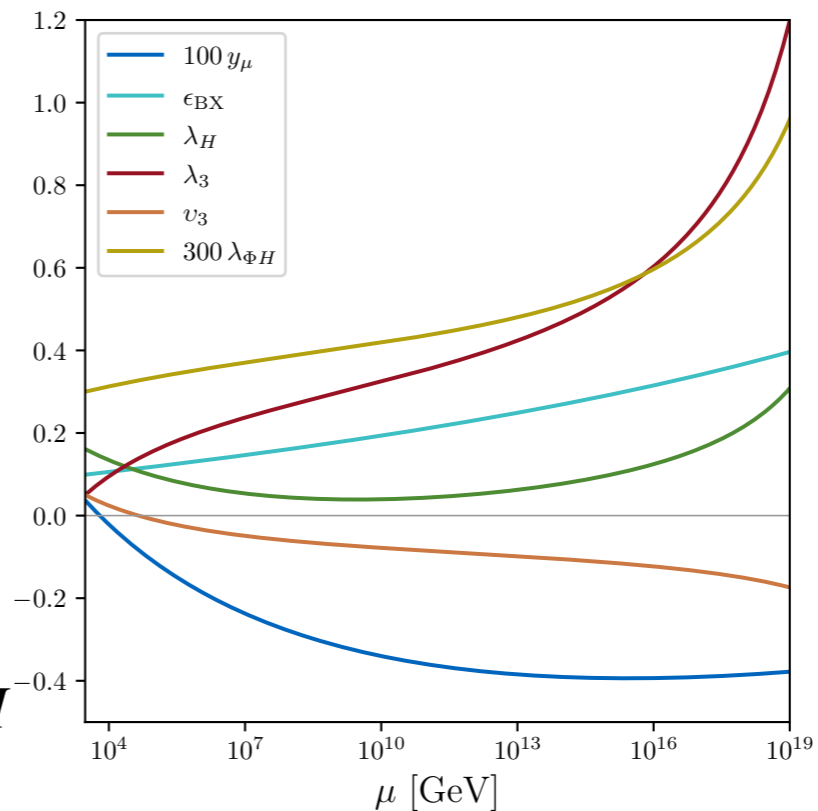
- Hiller, Schmaltz, 1408.1627,
- Dorsner, Fajfer, AG, Kamenik, Kosnik; 1603.04993,
- Buttazzo, AG, Isidori, Marzocca; 1706.07808,
- Gherardi, Marzocca, Venturini; 2008.09548
- + many more



- One-loop matching to SMEFT from 2003.12525
- 399 observables in **smelli** 1810.07698
- EW and flavor observables, LFV, LFU, magnetic moments, neutral meson mixing, semileptonic and rare  $B, D, K$  decays, etc.

- Present collider constraints:  
 $M_1 > 1.4 \text{ TeV}, M_3 > 1.7 \text{ TeV}$  [ATLAS]
- For  $M_{1,3} = 3 \text{ TeV}$  the largest coupling  $\sim 0.4$

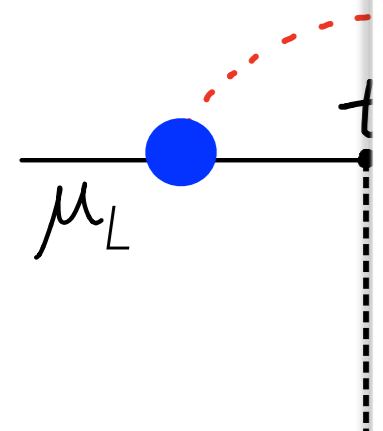
- No Landau poles up to the Planck and the potential is stable.



- Two loop Yukawa and quartic, three loop gauge (RGBeta 2101.08265)

- No fine tuning in  $m_H$  or  $m_\mu$  due to  $S_{1,3}$ .

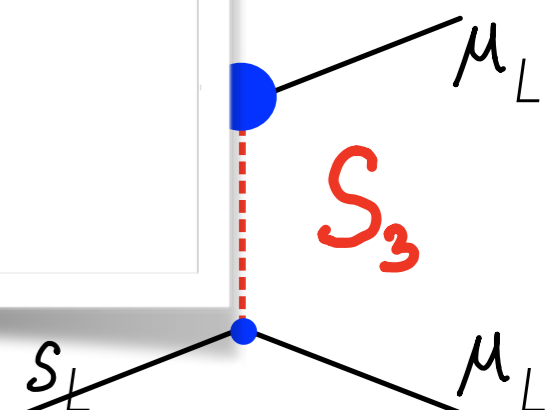
- This is contrary to the  $R(D^{(*)})$  models which should be “around the corner”, and sometimes even invoke tuned cancelations to pass complementary observables!



\*  $m_t/m_\mu$  error  
 Queiroz, Shepherdson, Dorsner, Fajfer, AG, 1603.04993,  
 Coluccio Leskow, Müller; 1612.0685  
 Dorsner, Fajfer, Surroget, Gherardi, Marzocca  
 + many more

structure

Waltz, 1408.1627,  
 Fajfer, AG, Kamenik,  
 1603.04993,  
 G, Isidori,  
 1606.07808,  
 Marzocca, Venturini;  
 1603.04993



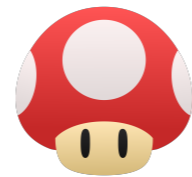
- One-loop matching  
 - 399 observables  
 - EW and flavor observables, LFV, LFU, magnetic moments, neutral meson mixing, semileptonic and rare  $B, D, K$  decays, etc.



# Example: Chiral category

Backup

# Part II



# What about the muonic force?

AG, Stangl, Thomsen, 2103.13991

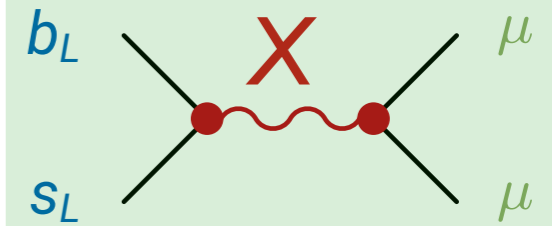
\*minimal



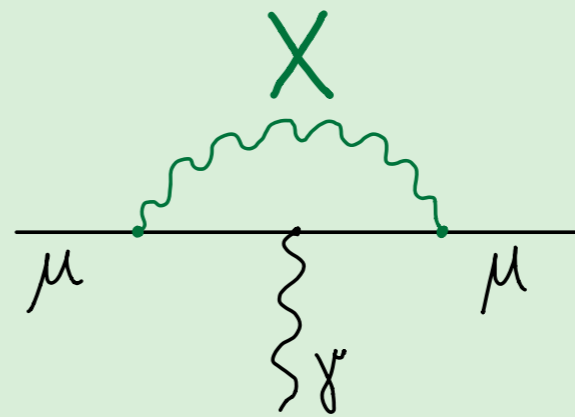
	Type A	Type B	Type C
$R_{K^{(*)}}, b \rightarrow s\mu\mu$	$S_3$	$S_3$	heavy $X$
$(g - 2)_\mu$	$S_1/R_2$	light $X$	$S_1/R_2$

# What about the muonic force?

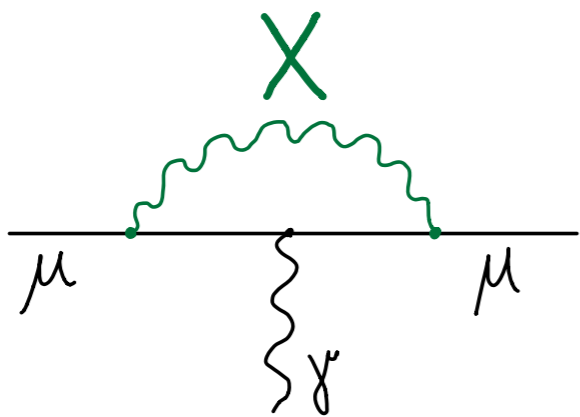
AG, Stangl, Thomsen, 2103.13991



	Type A	Type B	Type C
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# The muonic force

$(g - 2)_\mu :$ 


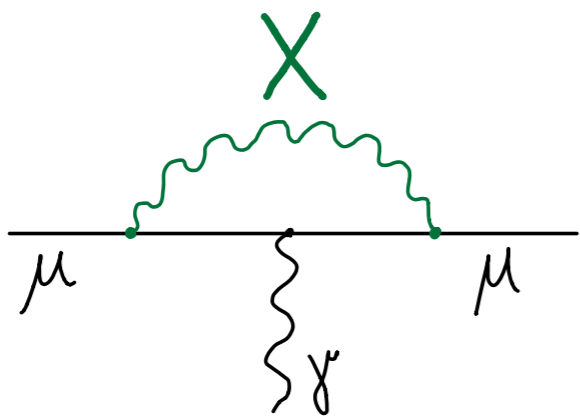
$$\mathcal{L} \supset g_X \bar{\mu} \not{X} (q_V - q_A \gamma_5) \mu \quad \Rightarrow$$

$$r_\ell = m_\ell / m_X$$

$$\Delta a_\mu = \frac{g_X^2}{8\pi^2} r_\mu^2 [q_V^2 I_V(r_\mu) + q_A^2 I_A(r_\mu)] = \frac{g_X^2}{8\pi^2} \begin{cases} q_V^2 - 2 r_\mu^2 q_A^2, & m_X \ll m_\mu \\ \frac{2}{3} r_\mu^2 [q_V^2 - 5 q_A^2], & m_X \gg m_\mu \end{cases}$$

- The right sign  $\Rightarrow$  mostly vector coupling  $\Rightarrow X_{L_2} \neq 0$

# The muonic force

$(g - 2)_\mu$ : 

$\mathcal{L}_{\text{eff}} \supset + g_X (q_V + q_A) \bar{\nu}_{\mu L} \not{X} \nu_{\mu L} + g_X \bar{\mu} \not{X} (q_V - q_A \gamma_5) \mu$

$r_\ell = m_\ell / m_X$

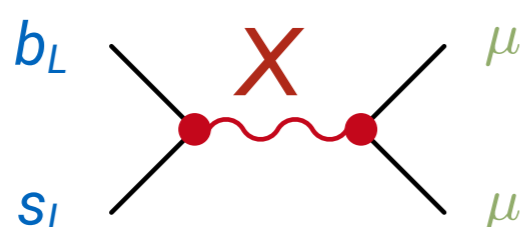
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- The right sign  $\Rightarrow$  mostly vector coupling  $\Rightarrow X_{L_2} \neq 0$
- From the  $\bar{L}_2 \not{D} L_2 \Rightarrow$  neutrino  $\nu_\mu$  couples to  $X_\mu$

$\Rightarrow$  Neutrino trident production:  $\nu_\mu N \rightarrow \nu_\mu N \mu^+ \mu^-$

# The muonic force

$b \rightarrow s\mu\mu$  :



$$\mathcal{L}_{\text{eff}} \supset + g_X (q_V + q_A) \bar{\nu}_{\mu L} \not{X} \nu_{\mu L} + g_X \bar{\mu} \not{X} (q_V - q_A \gamma_5) \mu$$

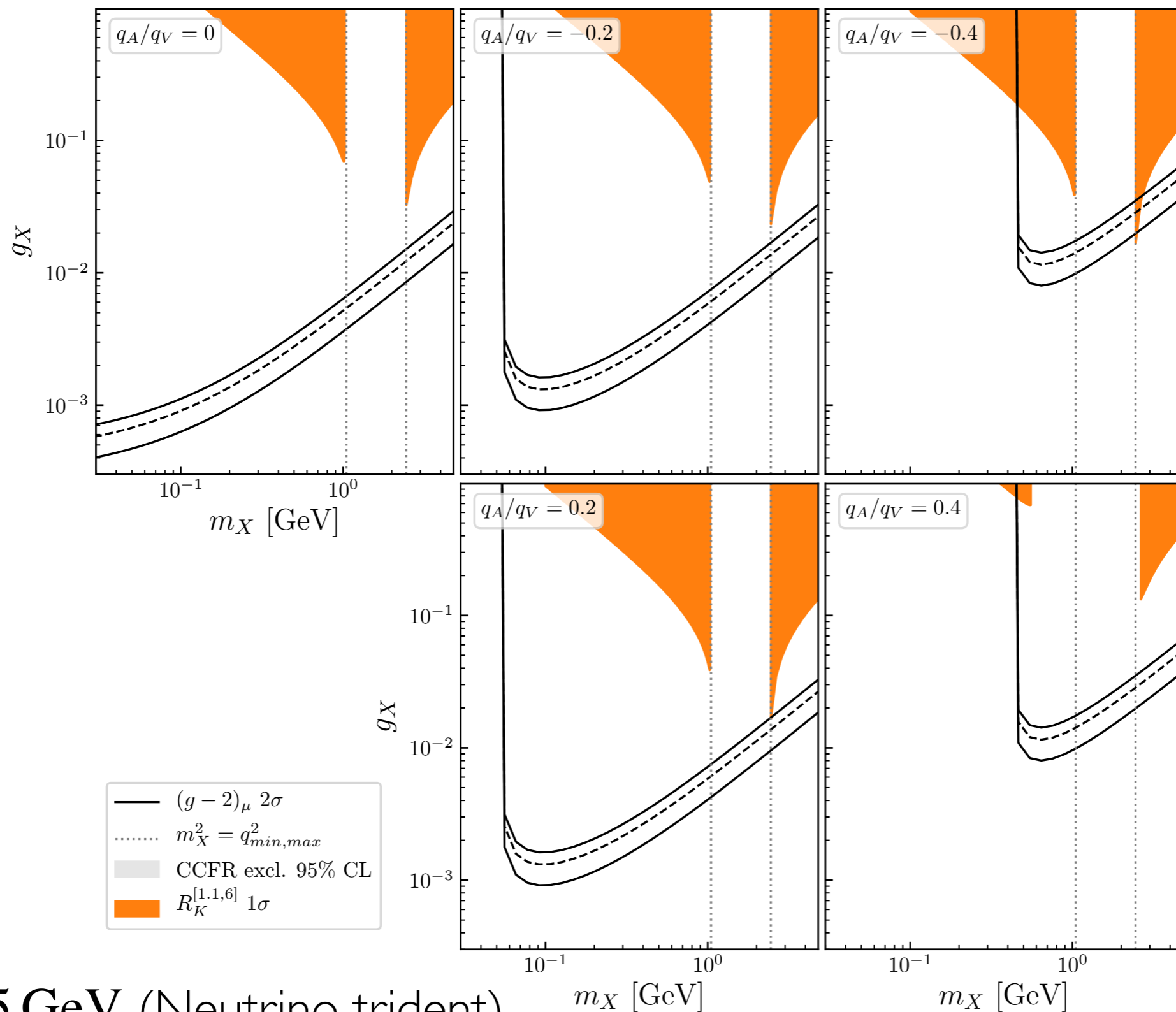
$$+ \left[ \bar{b} \not{X} (g_L^{bs} P_L + g_R^{bs} P_R) s + \text{H.c.} \right],$$

$$C_{9,10}^{(\prime)} = \frac{q_{V,A}}{N} \frac{g_X g_{L(R)}^{bs}}{q^2 - m_X^2 + im_X \Gamma_X}$$

- When  $m_X < m_B - m_K \Rightarrow$  strong limits from  $B \rightarrow KX$  where  $X \rightarrow \nu\nu$

$$g_L^{bs} \lesssim 0.7 \times 10^{-8} \frac{m_X}{\text{GeV}}$$

# The muonic force

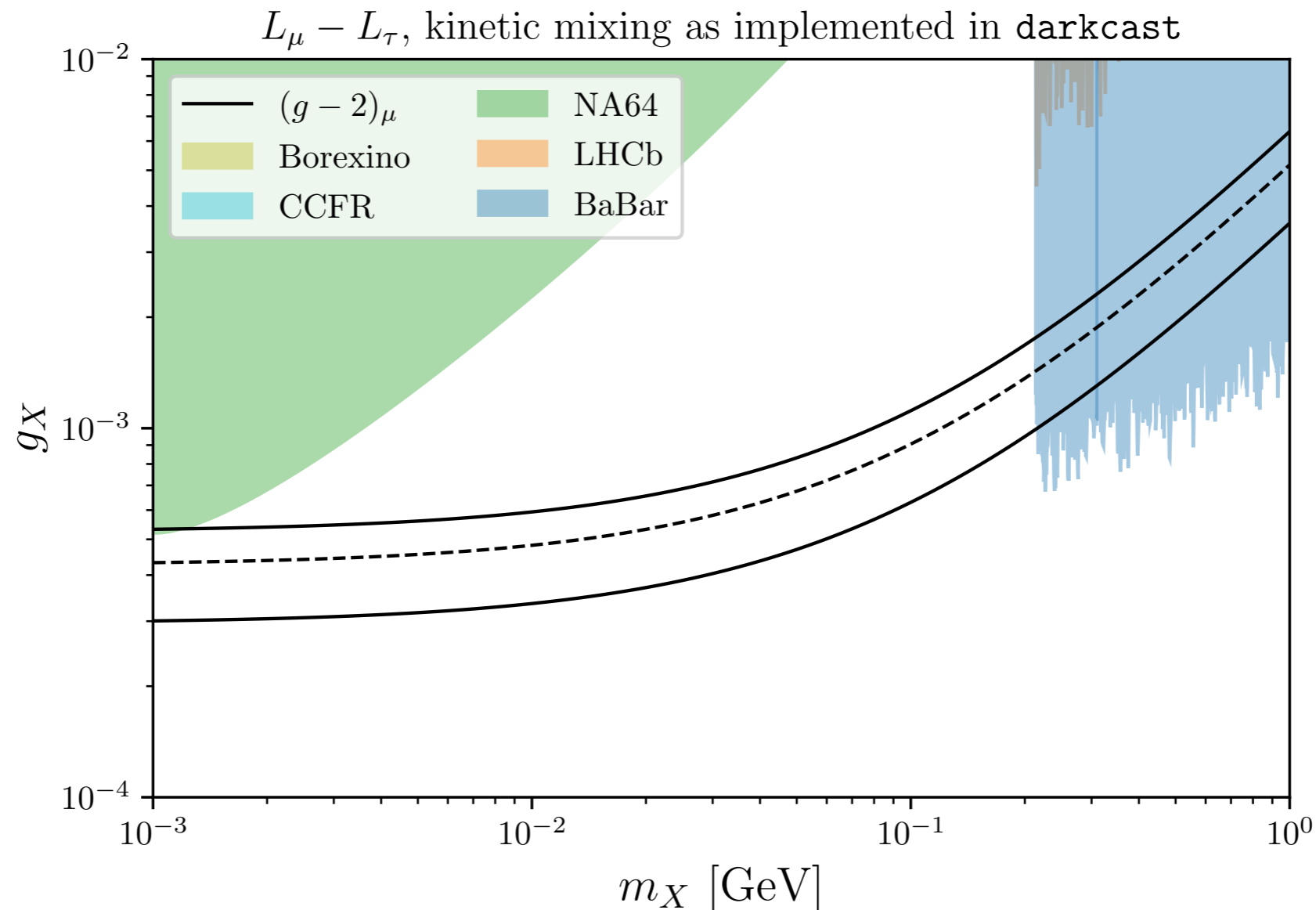


-  $m_X \lesssim 0.5$  GeV (Neutrino trident)

-  $R(K)$  needs a different mediator



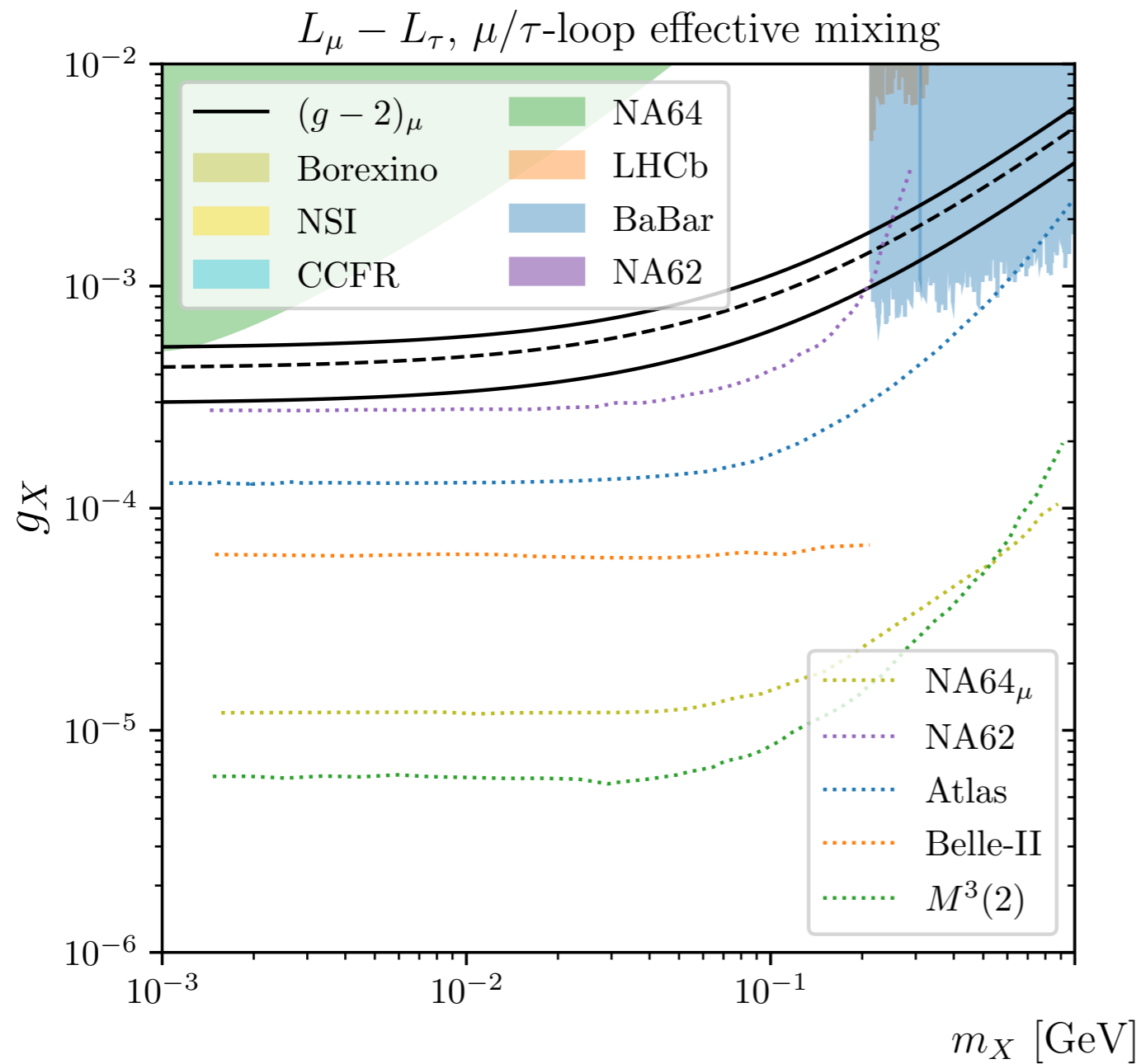
# Gauged $L_\mu - L_\tau$



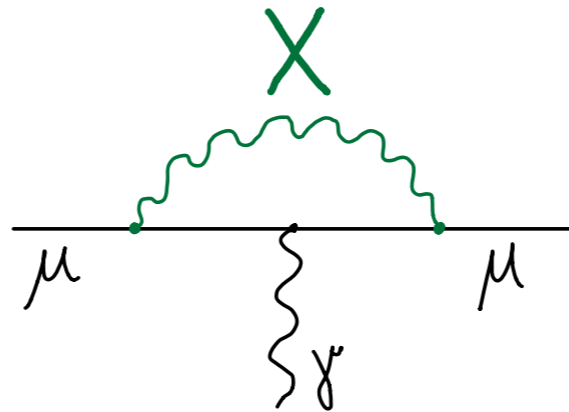
hep-ph/0104141,  
 hep-ph/0110146,  
 1311.0870,  
 1403.1269,  
 1406.2332,  
 ...

- Dimuon resonances:  $m_X \lesssim 0.21$  GeV
- Cosmology (BBN):  $m_X \gtrsim 0.01$  GeV
- Electron bounds (Borexino, NA64):  
 - Depend on the Kinetic mixing.

# Gauged $L_\mu - L_\tau$

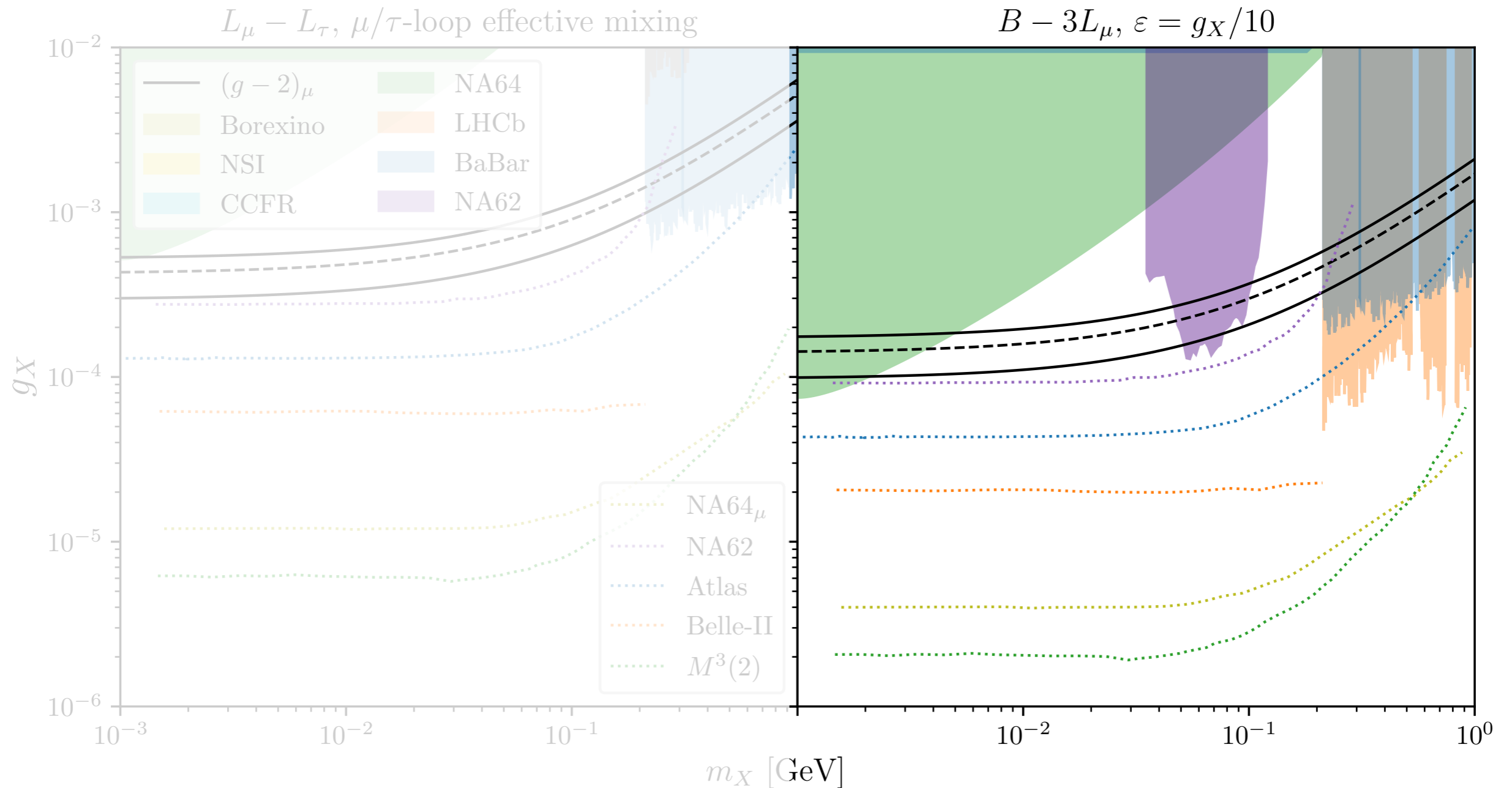


Promising projections!



What about other  $U(1)_X$ ?

# Gauged $B - 3L_\mu$

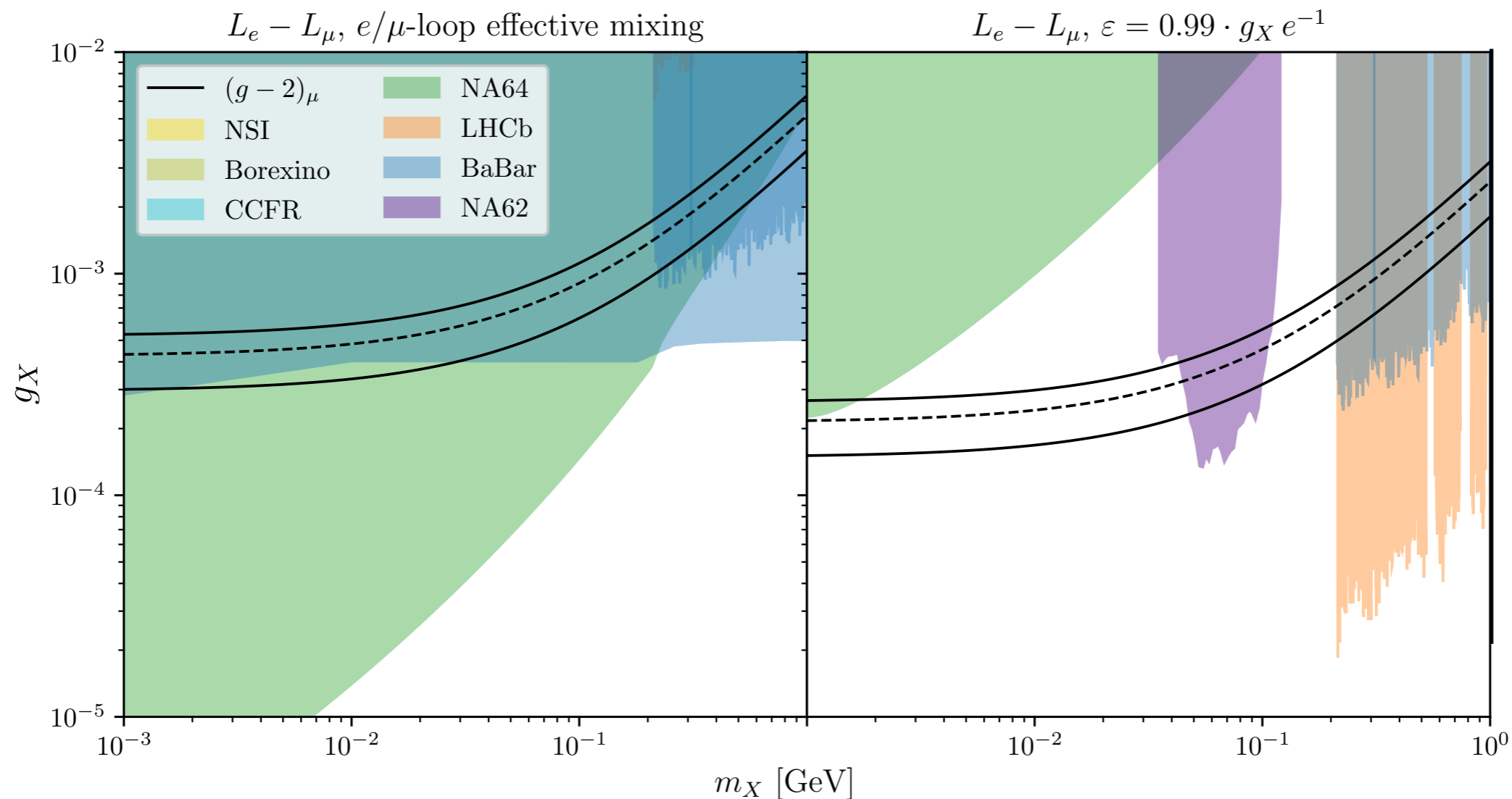


Neutrino NSI important for the valence quarks!

$$\mathcal{L}_{\text{NSI}} = -\frac{G_F}{2\sqrt{2}} \sum_{f,\alpha\beta} \varepsilon_{\alpha\beta}^f (\bar{f} \gamma_\mu f) (\bar{\nu}_\alpha P_L \nu_\beta)$$

$$f = \{e, p, n\}$$

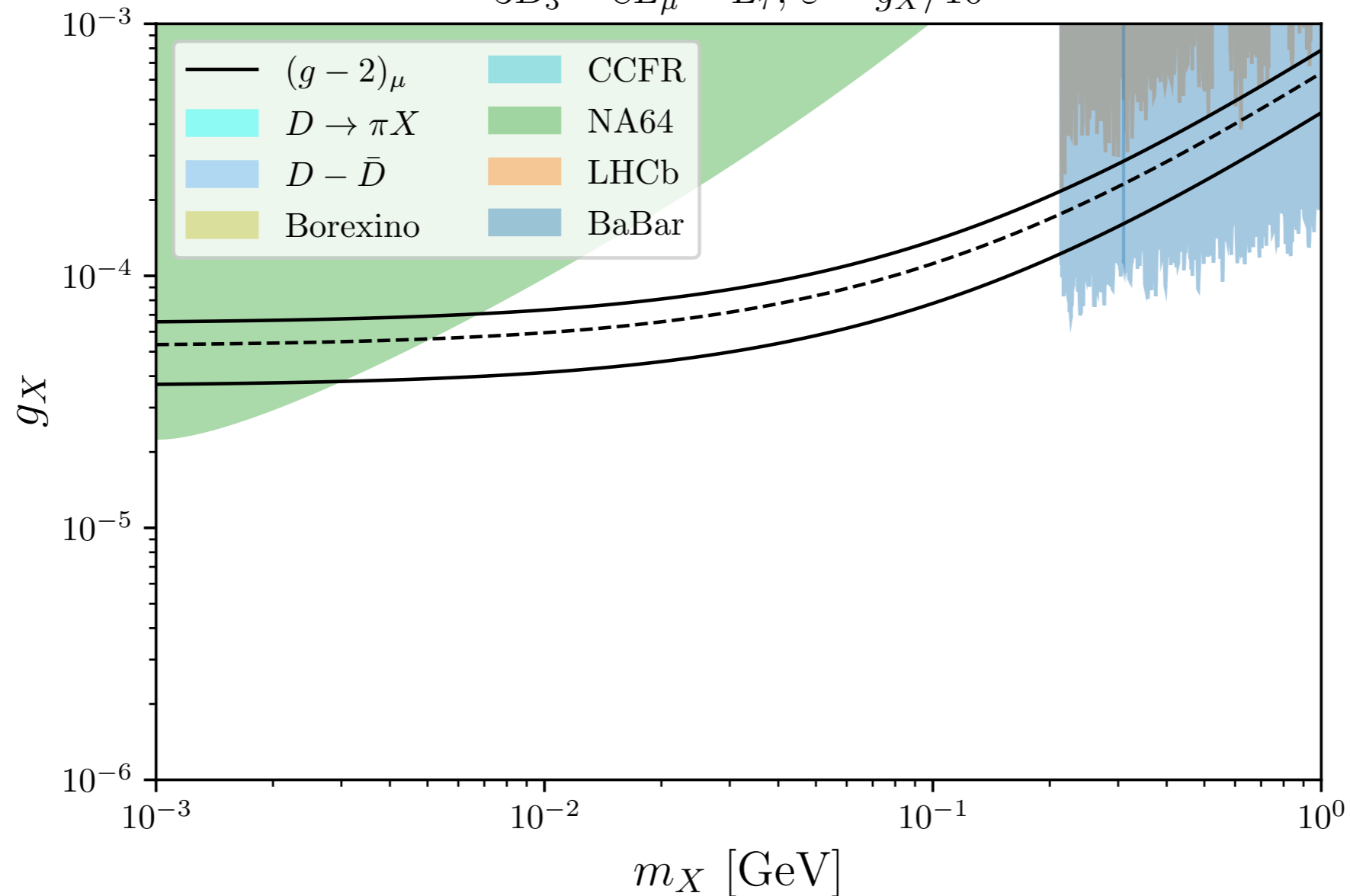
# Gauged $L_e - L_\mu$



- The electron induced bounds from NA64, Borexino and NSI
- The kinetic mixing can relax the first two, but not the NSI

# Gauged $3B_3 - 8L_\mu - L_\tau$

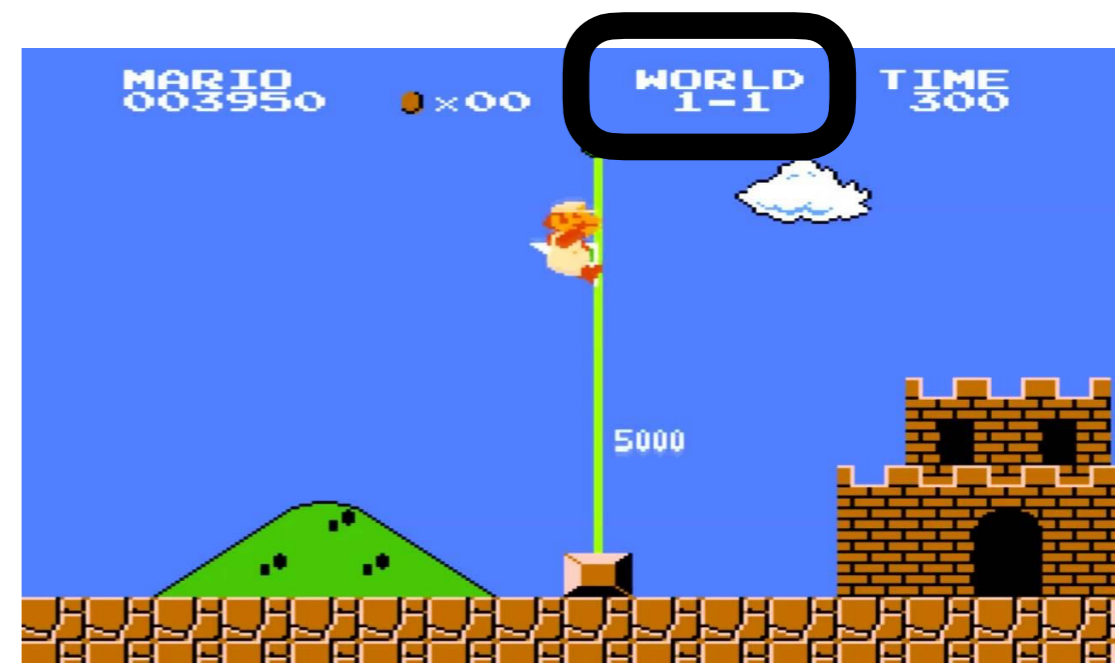
$$3B_3 - 8L_\mu - L_\tau, \varepsilon = g_X/10$$



- Third-family quark  $U(1)_X$  [down-alignment]
- FCNCs in  $X_\mu$  interactions call for the quark universality!

# Conclusions

1. Muon anomalies might be footprints of physics beyond the SM.
2. Gauged lepton flavor is an interesting direction.
3. Successful mediators:  
*Muonquarks* and *Muonic forces*



# Backup



# Example: Chiral category

- The dimension-4 muon Yukawa is forbidden by  $U(1)_X$

$$X_{L_2} \neq X_{E_2}$$

- Introduce two scalar muoquarks  $S_{\pm} = (\mathbf{3}, \mathbf{2}, 7/6, X_{S_{\pm}})$

$$\mathcal{L} \supset \eta_L \bar{t}_R \ell_L^2 i\sigma_2 S_+ - \eta_R \bar{q}_L^3 \mu_R S_-$$

- Mix them via  $U(1)_X$  breaking

$$\mathcal{L} \supset -A\phi S_+^\dagger S_-$$

Charges:

$$X_{S_+} = -X_{L_2} + X_{U_i}$$

$$X_{S_-} = -X_{E_2} + X_{Q_i}$$

$$X_\phi = -X_{S_-} + X_{S_+}$$

Example:

$\tilde{L}_{\mu-\tau}$  model:

$$(X_{L_1}, X_{L_2}, X_{L_3}) = (0, 7, -7),$$

$$(X_{N_1}, X_{N_2}, X_{N_3}) = (5, 3, 8),$$

$$(X_{E_1}, X_{E_2}, X_{E_3}) = (-3, 8, -5),$$

$$X_{Q_i, D_i, U_i} = 0.$$

# Example: Chiral category

- The dimension-4 muon Yukawa is forbidden by  $U(1)_X$

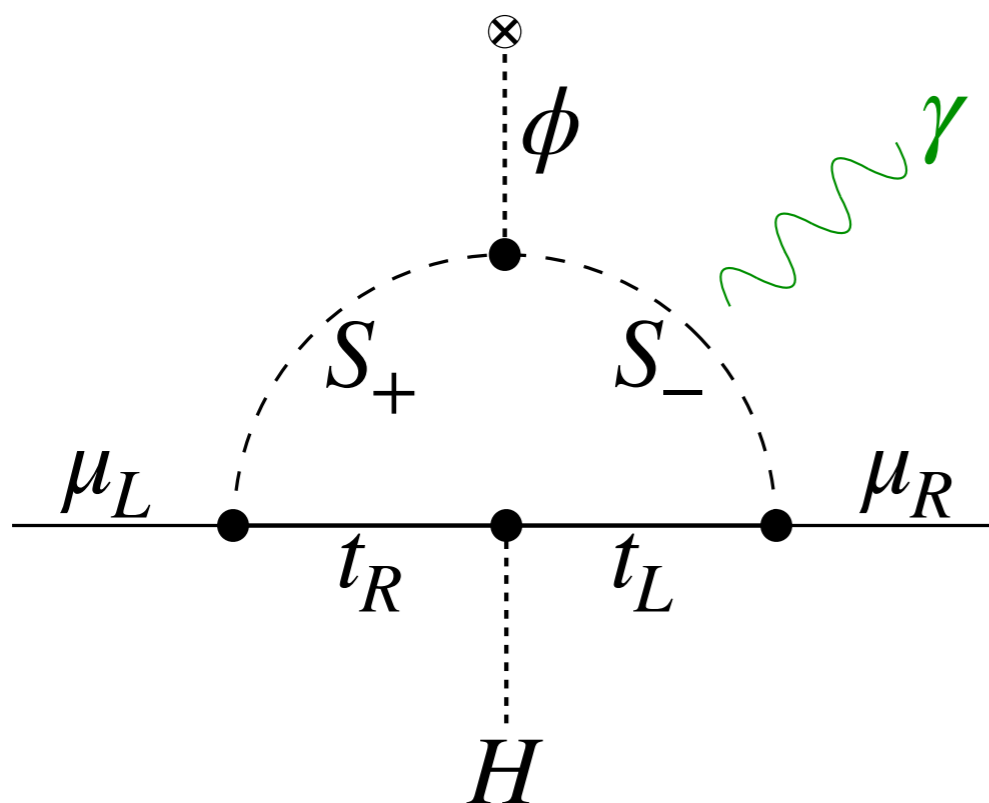
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$$\Rightarrow m_\mu, \Delta a_\mu$$

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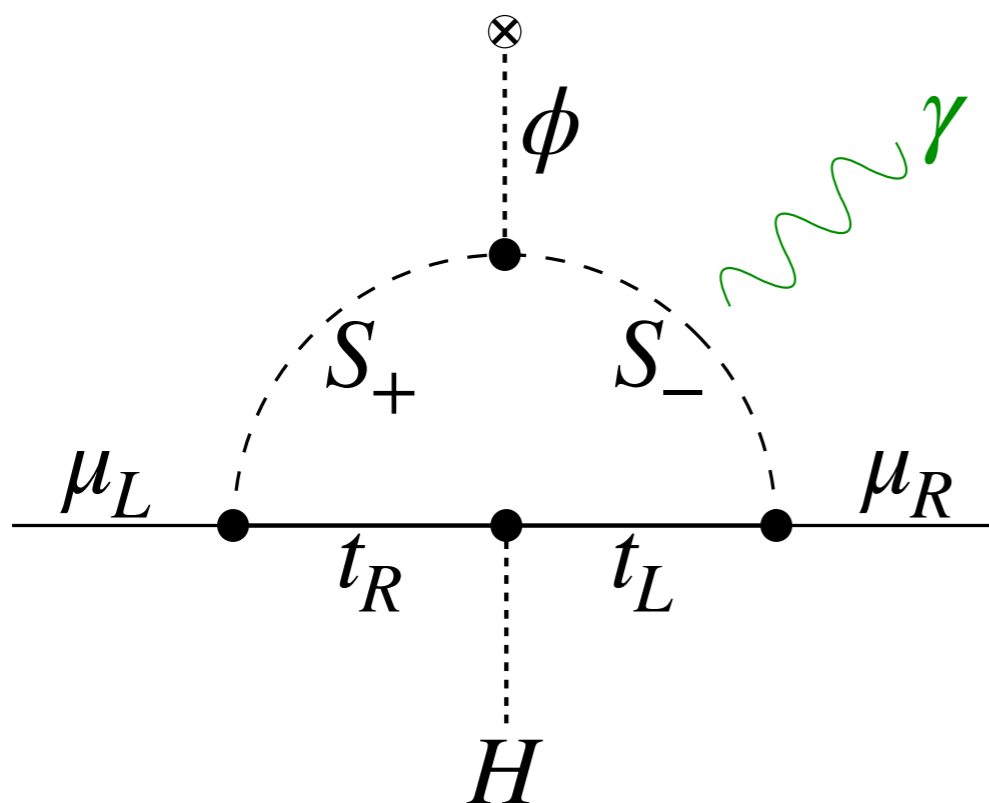
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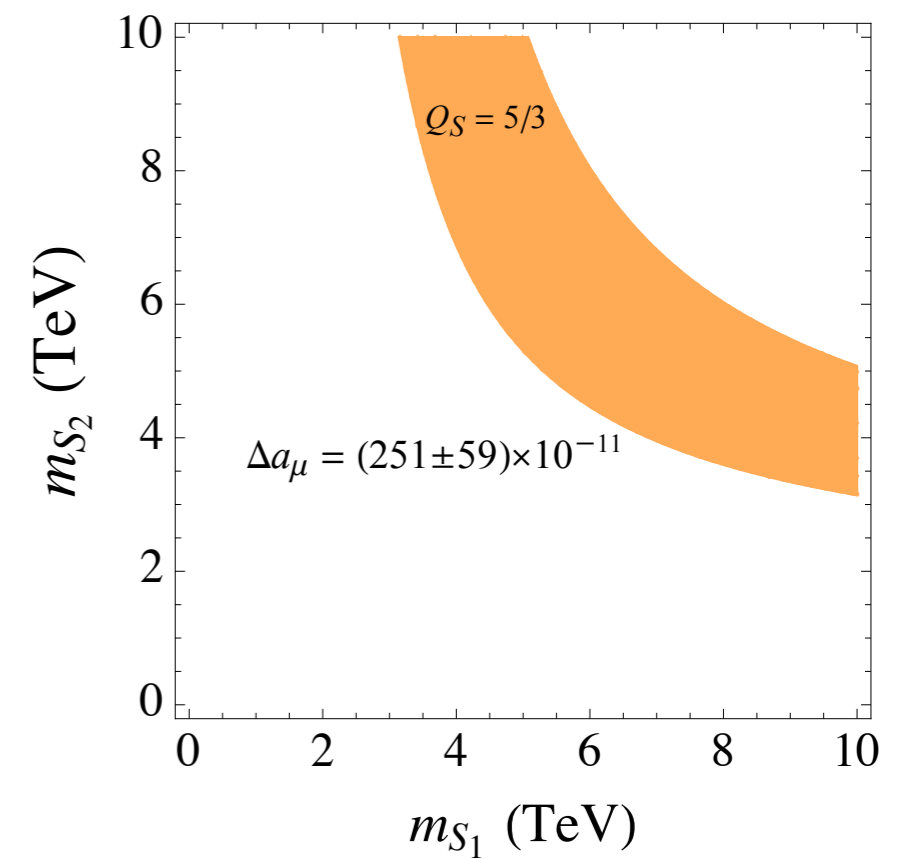
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- Mix them via  $U(1)_X$  breaking

$$\mathcal{L} \supset -A\phi S_+^\dagger S_-$$



$$\Rightarrow m_\mu, \Delta a_\mu$$



# Model Lagrangian

$$\begin{aligned}
\mathcal{L} = & \mathcal{L}_{\text{SM}-V_H} + |D_\mu \Phi|^2 + |D_\mu S_1|^2 + |D_\mu S_3|^2 - \frac{1}{4} X_{\mu\nu}^2 \\
& - \left( \eta_i^{3\text{L}} \bar{q}_L^{c i} \ell_L^2 S_3 + \eta_i^{1\text{L}} \bar{q}_L^{c i} \ell_L^2 S_1 + \eta_i^{1\text{R}} \bar{u}_R^{c i} \mu_R S_1 \right. \\
& \quad \left. + \tilde{\eta}_i^{1\text{R}} \bar{d}_R^{c i} \nu_{\mu,\text{R}} S_1 + \text{h.c.} \right) + \frac{1}{2} \varepsilon_{BX} B_{\mu\nu} X^{\mu\nu} \\
& - V_{H\Phi}(H, \Phi) - V_{13}(H, \Phi, S_1, S_3) + \bar{\nu}_R^i i \not{D} \nu_R^i \\
& - \left( y_\nu^{ij} \bar{\ell}_L^i \tilde{H} \nu_R^j + M_R^{ij} \bar{\nu}_R^{c i} \nu_R^j + y_\Phi^{ij} \Phi \bar{\nu}_R^{c i} \nu_R^j + \text{h.c.} \right)
\end{aligned}$$

- The rest of the potential:

$$\begin{aligned}
V_{13} = & M_1^2 |S_1|^2 + M_3^2 |S_3|^2 + \lambda_{\Phi 1} |\Phi|^2 |S_1|^2 + \lambda_{\Phi 3} |\Phi|^2 |S_3|^2 + \frac{1}{2} \lambda_1 (S_1^\dagger S_1)^2 + \lambda_{H1} |H|^2 |S_1|^2 + \lambda_{H3} |H|^2 |S_3|^2 \\
& + \kappa_{H3} H^\dagger \sigma^I \sigma^J H (S_3^{\dagger I} S_3^J) + (\kappa_{H13} H^\dagger \sigma^I H (S_1^\dagger S_3^I) + \text{h.c.}) + \frac{1}{2} \lambda_3 (S_3^\dagger S_3)^2 + \frac{1}{2} \kappa_3 (S_3^{\dagger I} S_3^J) (S_3^{\dagger J} S_3^I) \\
& + \frac{1}{2} \nu_3 (S_3^{\dagger I} S_3^J) (S_3^{\dagger I} S_3^J) + \lambda_{13} |S_1|^2 |S_3|^2 + \kappa_{13} (S_3^{\dagger I} S_1) (S_1^\dagger S_3^I) + (\nu_{13} (S_1^\dagger S_3^I) (S_1^\dagger S_3^I) + \text{h.c.}).
\end{aligned}$$

# Neutrino masses

- The minimal type-I seesaw mechanism

$$m_\nu \simeq -v^2 y_\nu (M_R + y_\Phi \langle \Phi \rangle)^{-1} y_\nu^T$$

- The  $U(1)_{B-3L_\mu}$  imposes a flavor structure for  $y_\nu, M_R, y_\Phi$ .
- The Dirac mass matrix splits into  $2 \times 2$   $e\tau$  block and a diagonal  $\mu$ .
- The Majorana mass matrix is entirely populated except (2,2) entry.
- There is enough parametric freedom to accommodate for:
  - *Neutrino oscillations data,*
  - *The Planck limit on the sum of neutrino masses,*
  - *The absence of neutrinoless double beta decay.*
- Not the case for all  $U(1)_{X_\mu}$ . Example is  $U(1)_{L_\mu-L_\tau}$ , see 1907.04042.
- However, in general, it is always possible to introduce additional  $U(1)_X$  symmetry-breaking scalars whose VEVs then populate the missing entries in the mass matrix.

# Proton decay

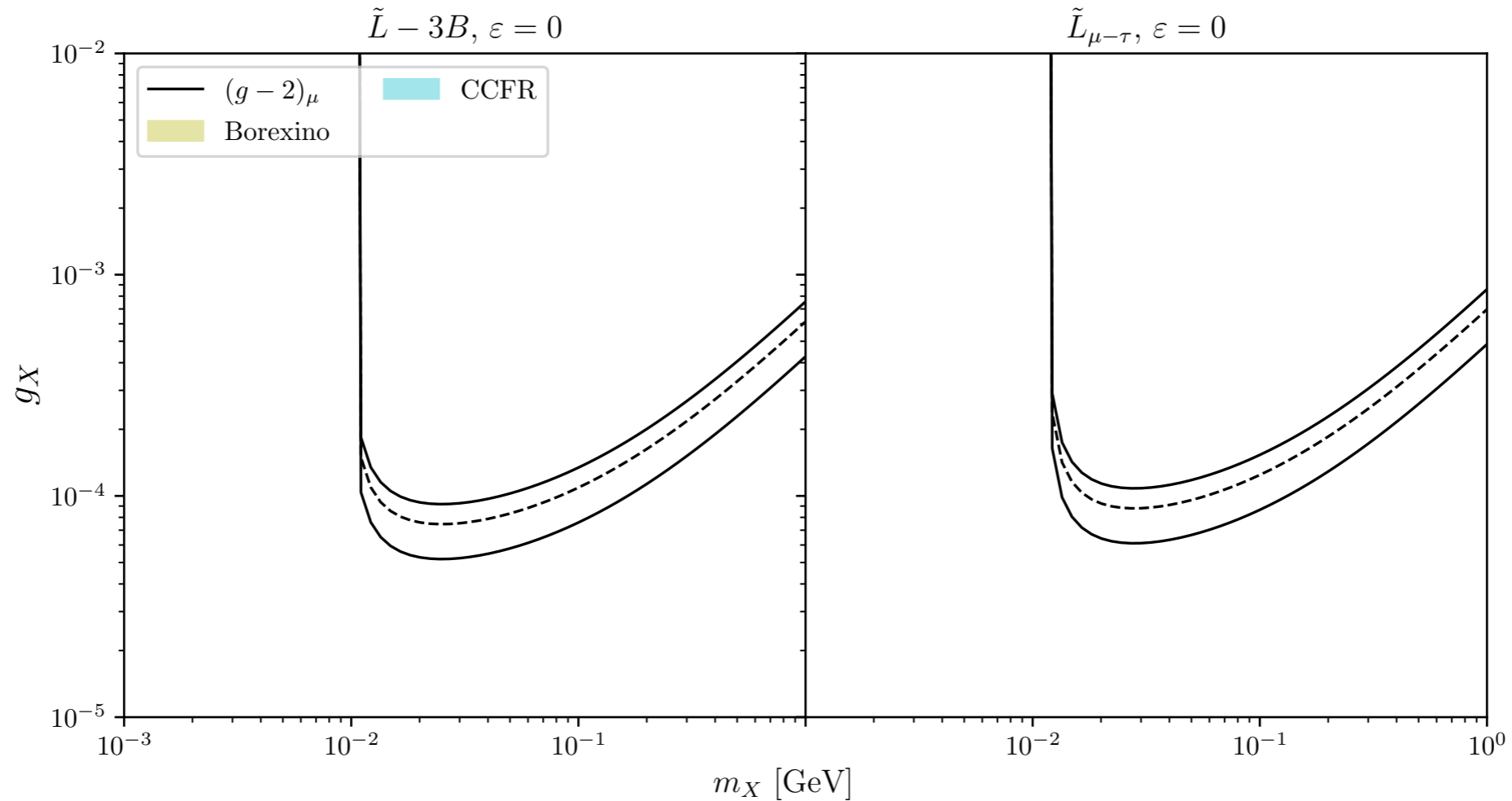
- What  $U(1)_{B-3L_\mu}$  does to a leptoquark?
  - Interacts only with muons
  - No proton decay up to dim-6

$$\mathcal{L} \supset Q_L L_L^{(2)} S_3$$

~~$$QQS_3^\dagger \quad QQS_3^\dagger \phi^\dagger$$~~

- The  $U(1)_{B-3L_\mu}$  gauge symmetry and the available field content ensure that  $B$  number is conserved also at the dim-5 effective Lagrangian.
- This is not the case for e.g.  $L_\mu - L_\tau$ . Quantum gravity is expected to break global charges and dim-5 diquark can be dangerous.
- If  $\frac{1}{M_P} q S^\dagger \phi^\dagger q$ , together with  $q \ell S$  needed for the muon anomalies and TeV-scale  $S$  mass, leads to dangerous proton decay.

# Chiral models



$\tilde{L} - 3B$  model:

$$(X_{L_1}, X_{L_2}, X_{L_3}) = (-3, 8, 4),$$

$$(X_{N_1}, X_{N_2}, X_{N_3}) = (-1, 3, 7),$$

$$(X_{E_1}, X_{E_2}, X_{E_3}) = (-2, 9, 2),$$

$$X_{Q_i, D_i, U_i} = -1,$$

$\tilde{L}_{\mu-\tau}$  model:

$$(X_{L_1}, X_{L_2}, X_{L_3}) = (0, 7, -7),$$

$$(X_{N_1}, X_{N_2}, X_{N_3}) = (5, 3, 8),$$

$$(X_{E_1}, X_{E_2}, X_{E_3}) = (-3, 8, -5),$$

$$X_{Q_i, D_i, U_i} = 0.$$

- + the NSI seems difficult

# The size of the effect

- $b \rightarrow s\mu\mu$

Heavy NP:

$$\mathcal{L}_{NP} = G_{NP} \bar{b}_L \gamma^\mu s_L \bar{\mu}_L \gamma^\mu \mu_L \implies G_{NP} \sim \text{few} \times 10^{-5} G_F$$

- $(g - 2)_\mu$

Light NP: With chiral suppression

$$\mathcal{L}_{NP} = G_{NP} y_\mu \frac{ev_{EW}}{16\pi^2} \bar{\mu}_L \sigma^{\mu\nu} \mu_R F_{\mu\nu} \implies G_{NP} \sim G_F$$

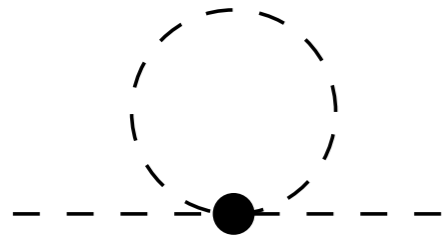
Heavy NP: No chiral suppression

$$\mathcal{L}_{NP} = G_{NP} \frac{ev_{EW}}{16\pi^2} \bar{\mu}_L \sigma^{\mu\nu} \mu_R F_{\mu\nu} \implies G_{NP} \sim \text{few} \times 10^{-4} G_F$$



# Finite naturalness

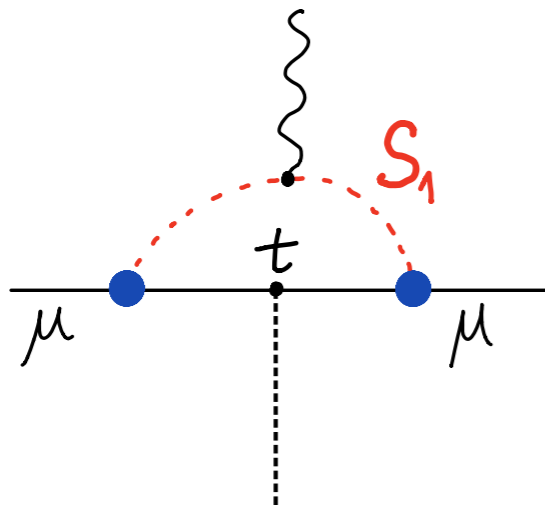
- The Higgs mass



$$\delta\mu_H^2 = -\frac{9(\lambda_{H3} + \kappa_{H3})}{(4\pi)^2} M_3^2 \left(1 + \ln \frac{\mu_M^2}{M_3^2}\right) + \frac{3\lambda_{H1}}{(4\pi)^2} M_1^2 \left(1 + \ln \frac{\mu_M^2}{M_1^2}\right) + \mathcal{O}(\mu^4/M_{1,3}^2)$$

For a small RGE-induced quartic couplings  $\mathcal{O}(0.05)$ , no tuning only if  $M_{1,3} \lesssim$  a few TeV

- The muon Yukawa



- Removing the photon  $\rightarrow$  correction to the muon Yukawa

$$\delta y_\mu = -\frac{3}{(4\pi)^2} \left(1 + \ln \frac{\mu_M^2}{M_1^2}\right) \eta_i^{1L*} y_u^{ij} \eta_j^{1R}$$

- $(g - 2)_\mu$  requires larger couplings for heavier leptoquark
- No tuning only if  $M_{1,3} \lesssim$  a few TeV, see also the RG flow

- Finite naturalness provides argument for direct searches at colliders

# Implications for Higgs physics

$$V_{H\Phi} = -\mu_H^2 |H|^2 - \mu_\Phi^2 |\Phi|^2 + \frac{1}{2} \lambda_H |H|^4 + \frac{1}{4} \lambda_\Phi |\Phi|^4 + \lambda_{\Phi H} |\Phi|^2 |H|^2$$

- From  $(g - 2)_\mu$  we have  $g_X \sim 10^{-4}$  and  $m_X \in [10, 200] \text{ MeV}$ .

$$v_\Phi = \sqrt{2} m_X / |q_\Phi| g_X \sim 60 \text{ GeV} / |q_\Phi|$$

- Mixing between real scalars  $h$  and  $\phi$ .

$$g_X : X \rightarrow \nu_\mu \bar{\nu}_\mu \quad \xrightarrow{\lambda_{\Phi H}, \lambda_\Phi} \quad h \rightarrow \text{inv}$$

$$\lambda_\Phi : \phi \rightarrow XX$$

- This scenario has a chance to leave observable imprints in the overall Higgs couplings or in the invisible Higgs decays.