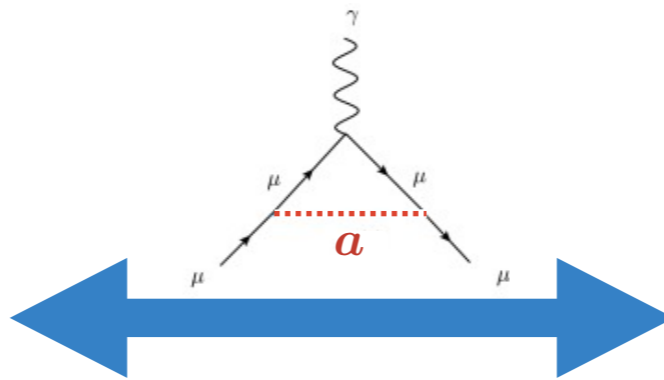


# $g-2$ from MeV ALPs

Robert Ziegler (KIT)



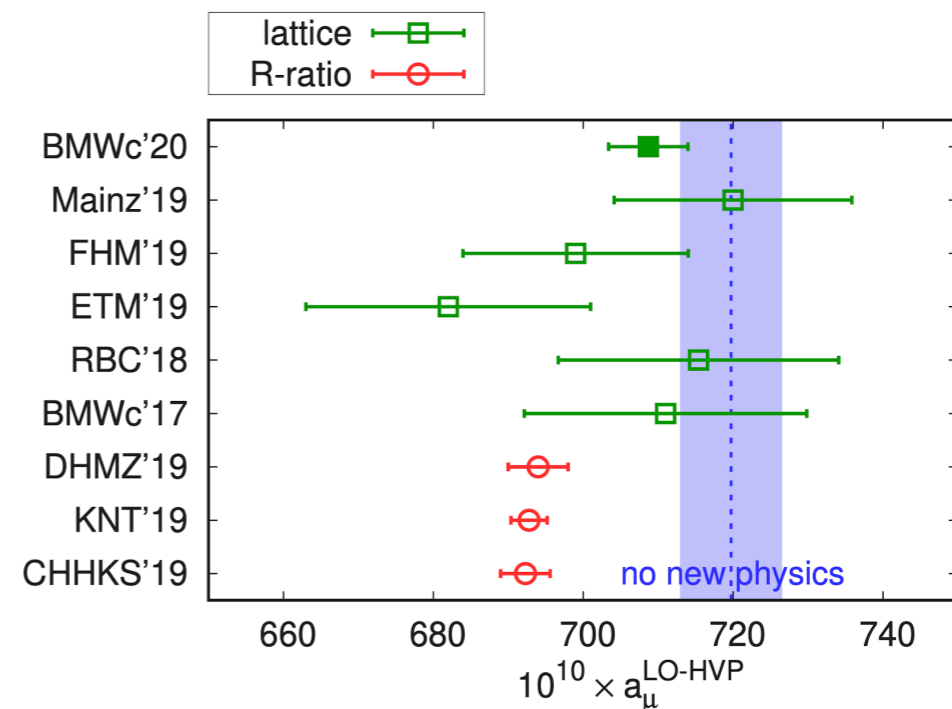
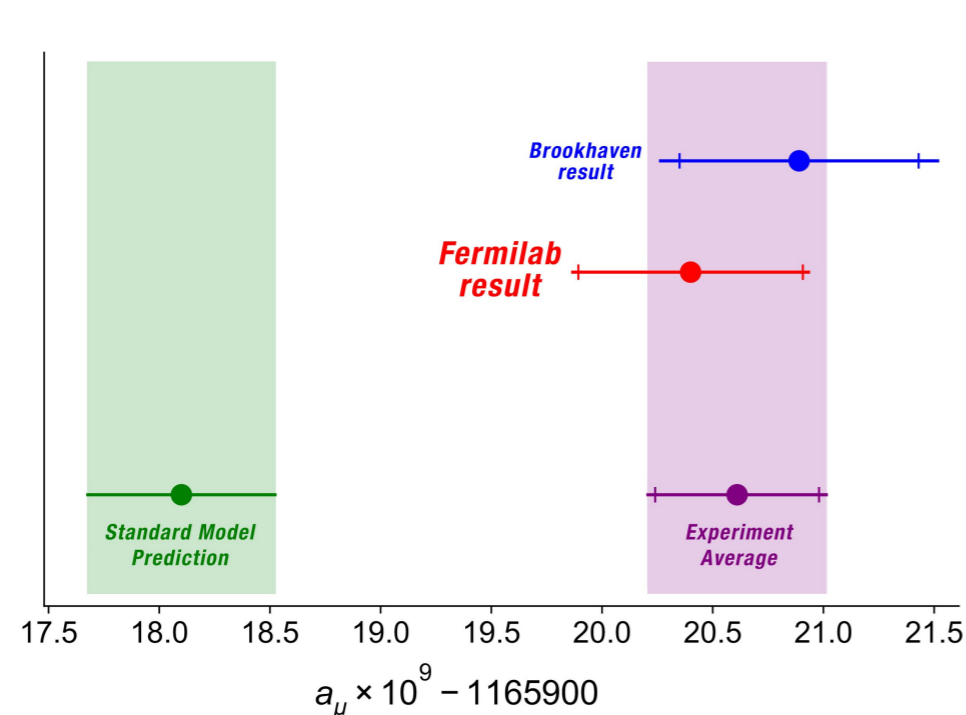
based on

[arXiv:2011.08919](https://arxiv.org/abs/2011.08919) with D. Buttazzo, P. Panci and D. Teresi

+ work in progress

# The $(g-2)_\mu$ Anomaly

- New  $(g-2)_\mu$  world average has  $4.2\sigma$  tension with SM prediction, but disagreement between lattice vs. dispersive result for non-PT input



- Can be easily explained by new particles around electroweak scale

**In this talk: MeV axion with electroweak decay constant**

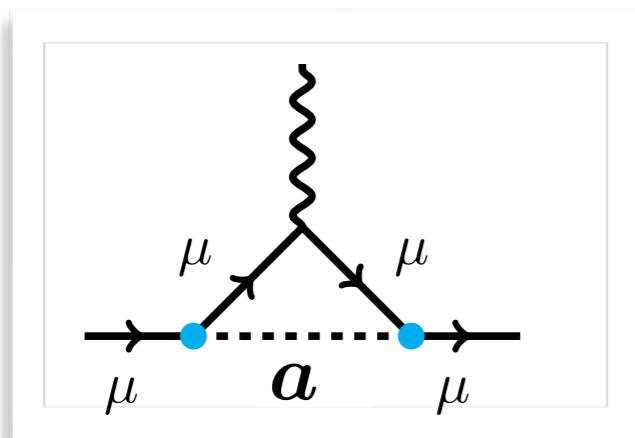
# Axion couplings to Muons

- Consider axion couplings to pseudo-scalar muon current

$$\mathcal{L}_\mu = -i \frac{c_{\mu a}}{f_a} m_\mu a \bar{\mu} \gamma_5 \mu = \frac{c_{\mu a}}{f_a} \frac{\partial_\mu a}{2} \bar{\mu} \gamma^\mu \gamma_5 \mu - \frac{c_{\mu a}}{f_a} \frac{\alpha}{4\pi} a F \tilde{F}$$

axion-dependent chiral field redefinition  
= EOM with anomaly term

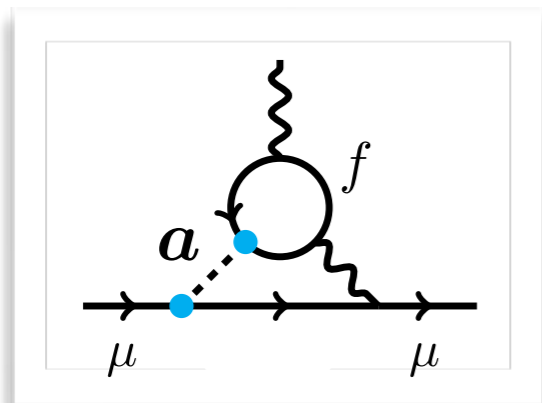
- Gives one-loop contribution to  $(g-2)_\mu$  with wrong sign



$$\Delta a_\mu^{1\text{-loop}} = -\frac{m_\mu^2 c_{\mu a}^2}{64\pi^2 f_a^2} h_1\left(\frac{m_a^2}{m_\mu^2}\right) \begin{cases} h_1(x \ll 1) = 1 \\ h_1(x \gg 1) \sim \log x/x \end{cases}$$

# Axion couplings to Photons

- Consider also 2-loop Barr-Zee contributions from other fermions



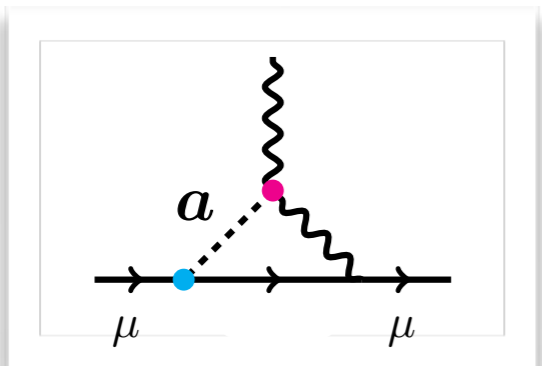
$$\Delta a_{\mu}^{2\text{-loop}} = N_c \frac{m_{\mu}^2 c_{\mu a} c_{f a}}{8\pi^2 f_a^2} \frac{\alpha}{\pi} g \left( \frac{m_a^2}{m_{\mu}^2}, \frac{m_a^2}{m_f^2} \right)$$

$$g(u, v) =: \int_0^1 dx dy dz \frac{ux}{u\bar{x} + uvxyz\bar{z} + vz\bar{z}x^2\bar{y}^2}$$

$$\xrightarrow{m_a \ll m_f, m_{\mu}} 3 + \log m_f^2/m_{\mu}^2$$

Get right sign when axion coupled to fermions with  $c_{\mu a} \ll c_{f a}$

- Induce effective axion couplings to photons



- general IR result  $(c_{\gamma a}, c_{\mu a})$  depends on cutoff

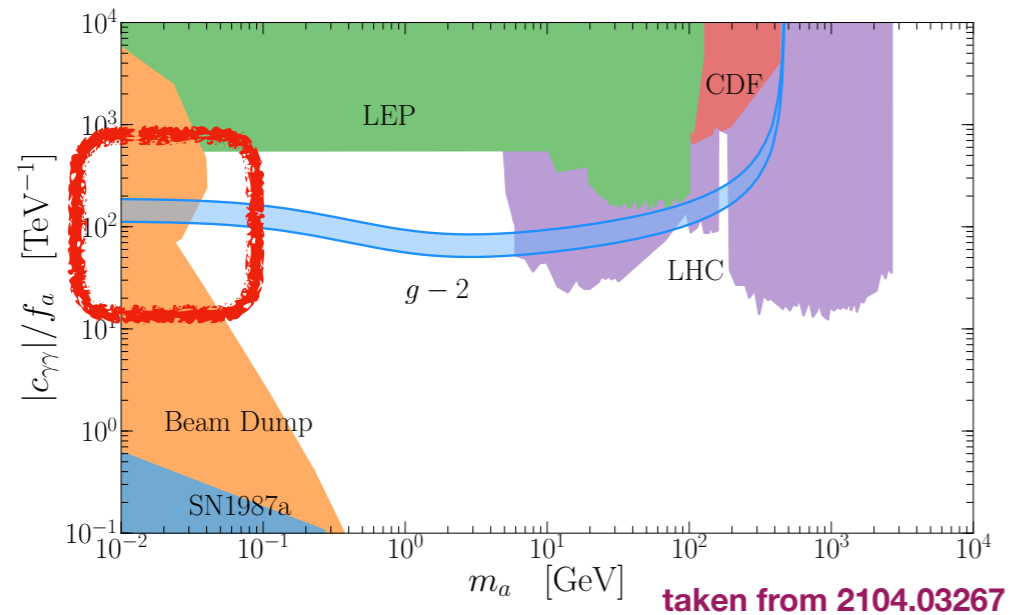
Marciano et al. '17, Bauer et al, '18, Buen-Abad et al. '21

- result for pseudoscalar couplings must be finite

Chang et al. '00, generalized in 2011.08919

# Axion couplings to Electrons

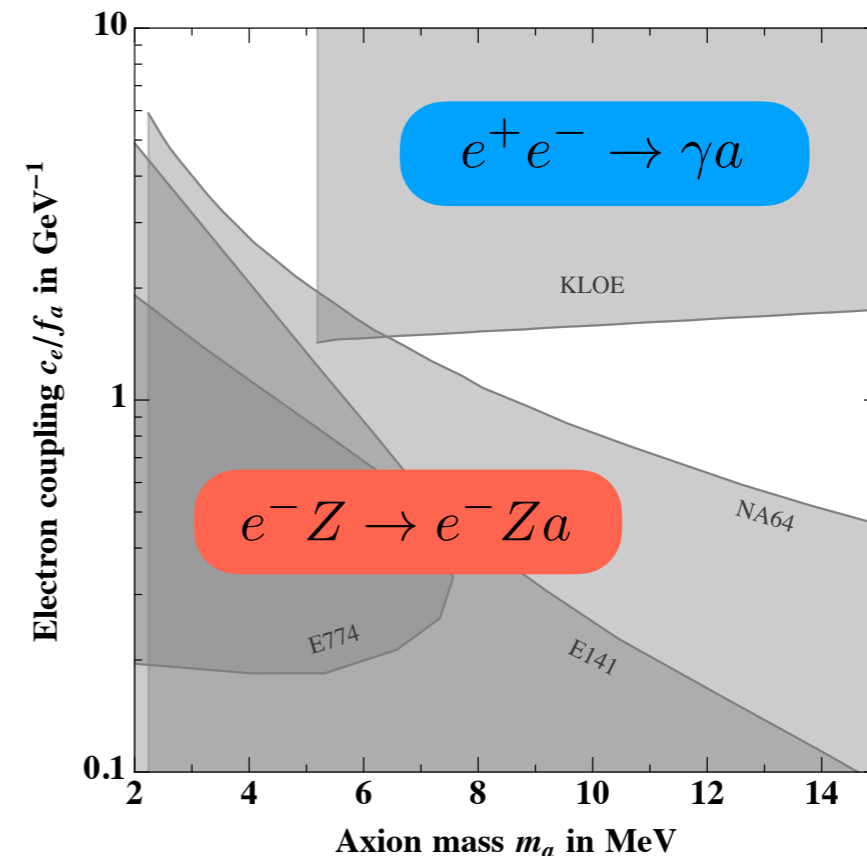
- Photon couplings of MeV axions are strongly constrained



...only if long-lived!

bounds disappear when axion decays promptly to electrons

- Need sizable axion couplings to electrons to avoid constraints from KLOE and beam dumps



# Axion couplings to Taus

- Get 1-loop contribution to  $(g-2)_e$  that is factor  $\sim 100$  too large

$$\Delta a_e^{1\text{-loop}} = -\frac{m_e^2 c_{ea}^2}{64\pi^2 f_a^2} h_1\left(\frac{m_a^2}{m_e^2}\right) \begin{cases} h_1(x \ll 1) = 1 \\ h_1(x \gg 1) \sim \log x/x \end{cases} \leftarrow$$

...but can tune against Barr-Zee contribution needed for  $(g-2)_\mu$

$$\Delta a_e^{2\text{-loop}} = N_c \frac{m_e^2 c_{ea} c_{fa}}{8\pi^2 f_a^2} \frac{\alpha}{\pi} g\left(\frac{m_a^2}{m_e^2}, \frac{m_a^2}{m_f^2}\right) \xrightarrow{m_e \ll m_a \ll m_f} 2 + \log m_f^2/m_a^2$$

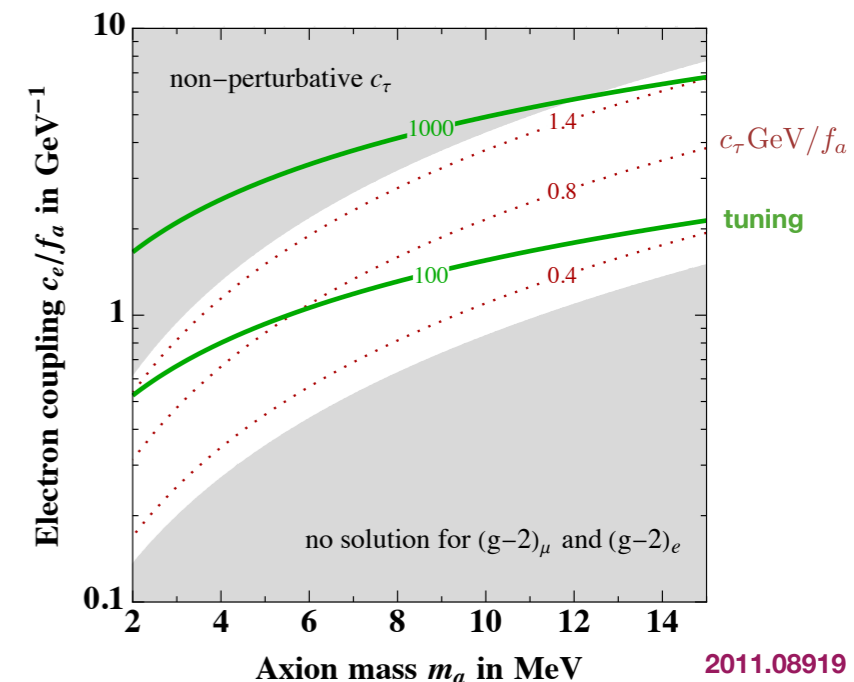
- 4-parameter model with couplings to all leptons

**mu+tau couplings fixed to reproduce  $(g-2)_{\mu,e}$**

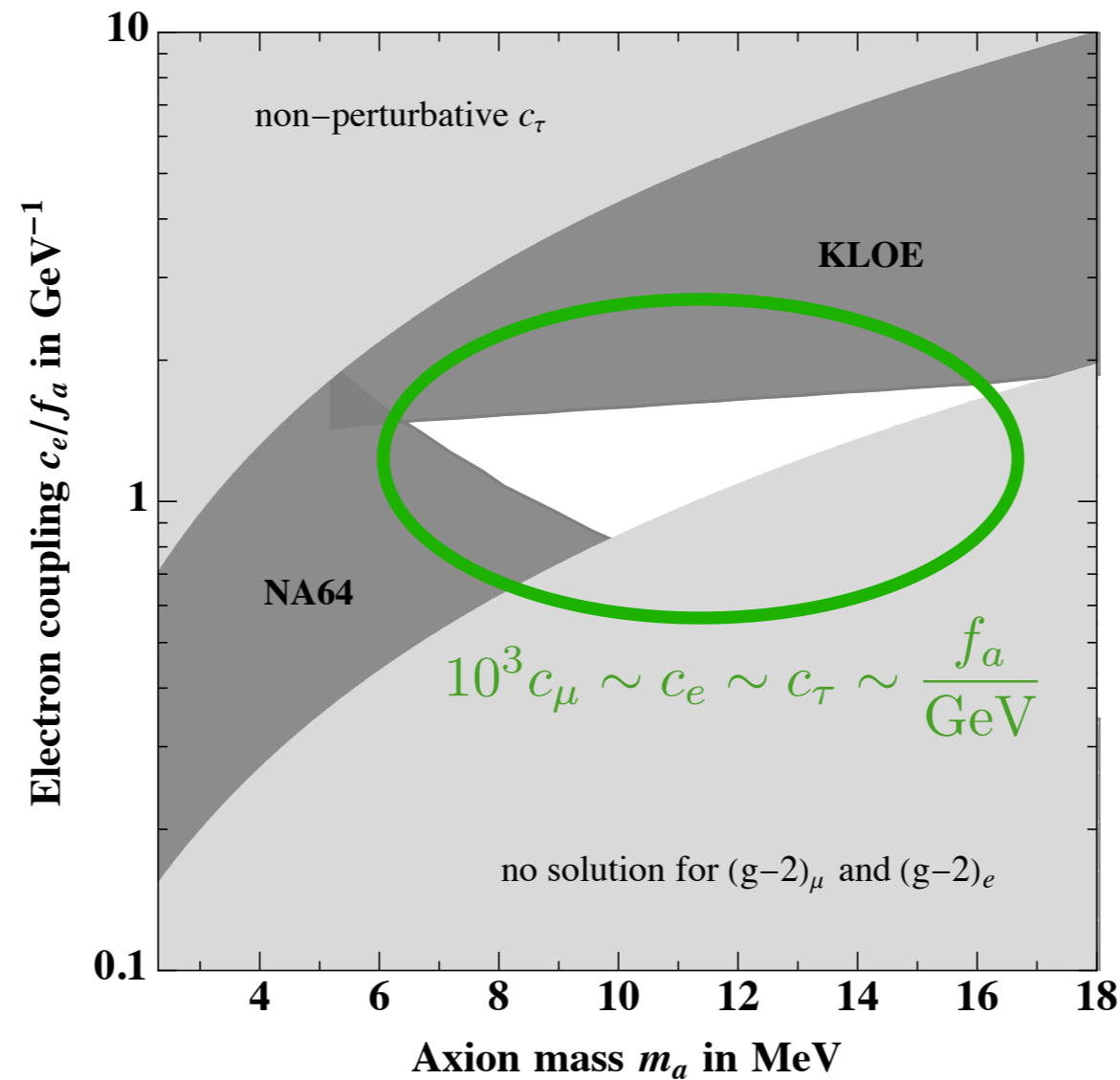
with single tuning of 1%, not always possible

**Need sizable tau couplings  $\sim$  electron couplings**

constrained by perturbativity



# A sweet spot in the multi-MeV region



allows to explain XENON1T excess & can be visible QCD axion

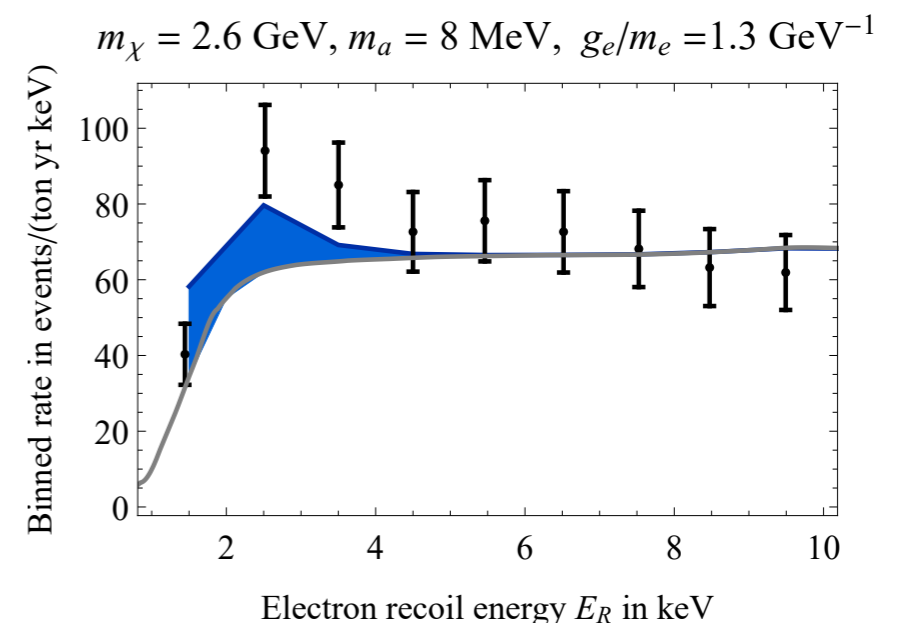
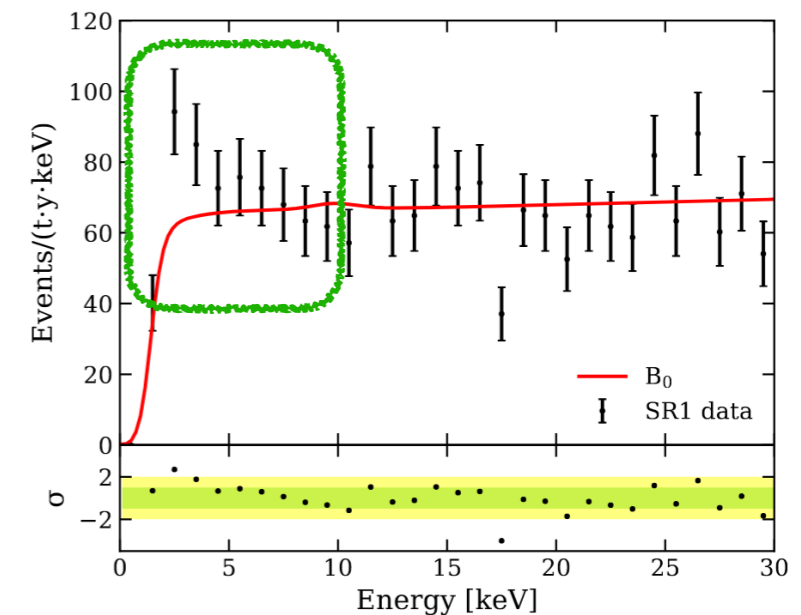
# Connection to the XENON1T Excess

- Xenon1T saw excess in electron recoils with significance  $\sim 3.5\sigma$
- Can be addressed when axion has large coupling to DM fermion 2011.08919

$$\mathcal{L} = -ia (g_\chi \bar{\chi} \gamma_5 \chi + g_e \bar{e} \gamma_5 e)$$

pseudoscalar structure gives steeply falling recoil spectrum that can improve fit because excess is close to exp. threshold at few keV

large annihilation cross-section of few GeV DM to axions: **natural asymmetric DM scenario**





# Connection to the QCD Axion

- Need axion with mass ~few MeV and decay constant ~GeV

perfectly fits QCD  
Axion relation!

$$m_a = 6 \mu\text{eV} \frac{10^{12} \text{GeV}}{f_a} = 6 \text{MeV} \frac{\text{GeV}}{f_a}$$

- Such a heavy QCD axion is actually **not experimentally excluded!**  
[and gives nice solution to PQ quality problem!] 1710.03764 by D. Alves & N. Weiner

**a)**  $J/\psi, \Upsilon \rightarrow \gamma a$   $\xrightarrow{\text{fix by}}$  **small axion couplings = PQ charges of b,c**

**b)**  $K^+ \rightarrow \pi^+ a_{\text{invis}}$   $\xrightarrow{\text{fix by}}$  **prompt decay to e's & small axion-pion mixing**

$$\text{Br}(K^+ \rightarrow \pi^+ a)_{\text{invis}} \sim \theta_{a\pi}^2 < 10^{-10}$$

$$\theta_{a\pi} \sim \frac{c_u m_u - c_d m_d}{m_u + m_d} f_\pi / f_a \sim 0.1 \frac{\text{GeV}}{f_a}$$

$$\text{Br}(K^+ \rightarrow \pi^+ (a \rightarrow e^+ e^-)) \lesssim 10^{-6}$$

$$c_u \approx 2c_d \rightarrow \theta_{a\pi} \sim 10^{-3} \frac{\text{GeV}}{f_a}$$

# Towards a complete model

- UV-complete model with couplings only to first generation fermions

2102.10118 by C. Wagner et al.

- \* DFSZ-like model: add doublet + singlet scalars charged under PQ

$$\mathcal{L}_{\text{PQ}}^{\text{Yuk}} \supset - \sum_{i=1,2,3} (\bar{Q}^i Y_u^{i1} H_u u_R^1 + \bar{Q}^i Y_d^{i1} H_d d_R^1 + \bar{L}^i Y_e^{i1} H_e e_R^1)$$

$$\mathcal{L}_{\text{SM}}^{\text{Yuk}} \supset - \sum_{i=1,2,3} \sum_{j=2,3} (\bar{Q}^i Y_u^{ij} \tilde{H} u_R^j + \bar{Q}^i Y_d^{ij} H d_R^j + \bar{L}^i Y_e^{ij} H e_R^j)$$

$$V_{\text{PQ}} = (A_u \phi_u^* H \cdot H_u + A_d \phi_d^* H^\dagger H_d + A_e \phi_e^* H^\dagger H_e + A_\phi \phi_u^* \phi_d^2 + B_\phi \phi_d^* \phi_e^n)$$

$$V_{\text{dia}} = \sum -\mu_\Phi^2 \Phi^\dagger \Phi + \lambda_\Phi (\Phi^\dagger \Phi)^2,$$

- \* PQ invariance + orthogonality of axion on Goldstone eaten by Z fixes all PQ charges in terms of Higgs vevs

$$0 = X_H v_H^2 + X_{H_i} v_{H_i}^2$$

- \* Axion mass and all its couplings determined by small doublet + singlet vevs

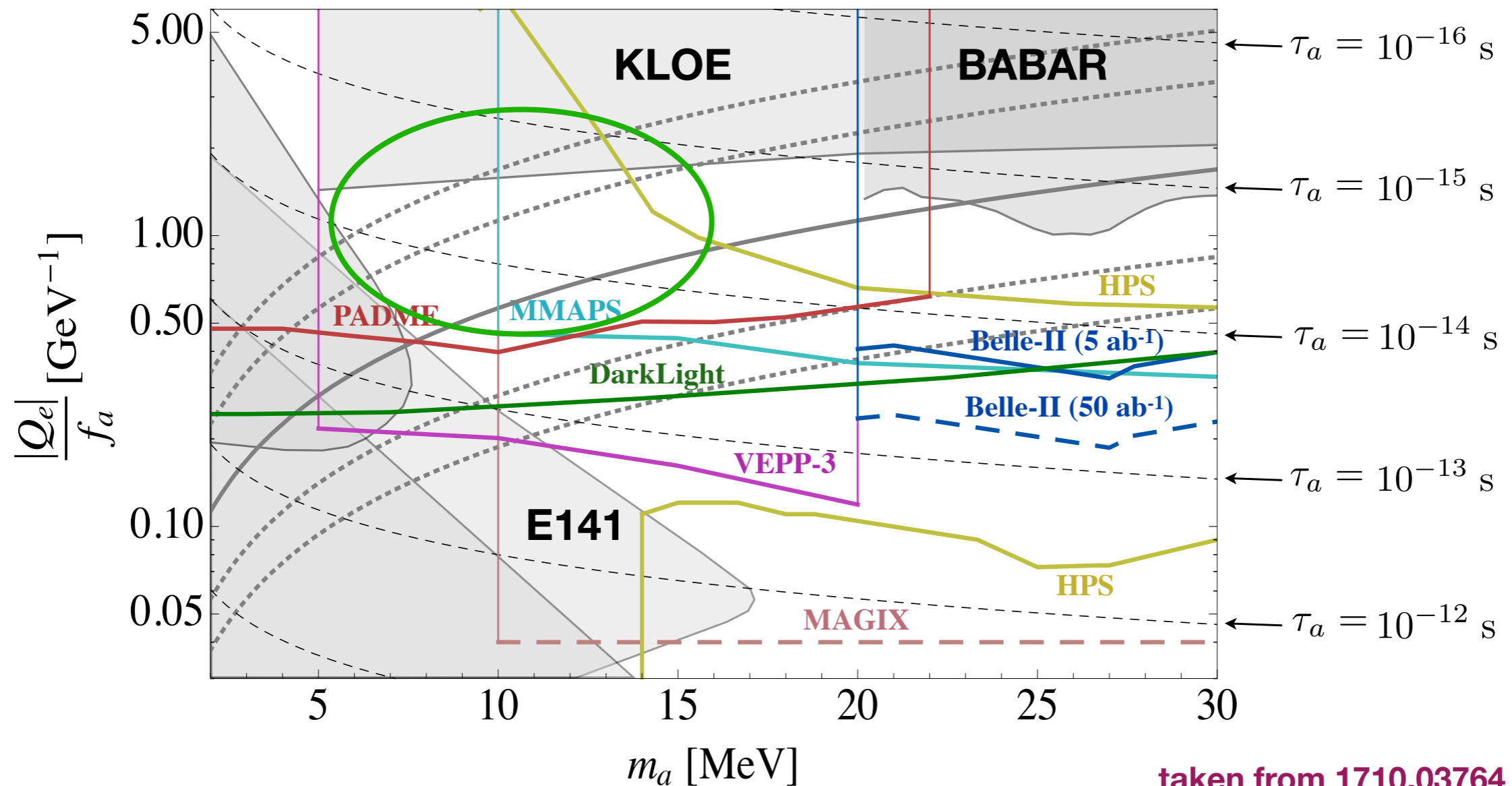
$$m_a = \frac{5.7 \text{ MeV}}{\eta 246}, c_u = \frac{2}{3}, c_d = \frac{1}{3}, c_e = \frac{1}{3n}, c_{\text{rest}} \propto \epsilon^2$$

$$\epsilon \equiv \frac{v_{H_i}}{v_H} \approx \frac{v_{H_i}}{v} \ll \eta \equiv \frac{v_{\phi_i}}{v}$$

- \* Can make scalar sector sufficiently heavy with large A-terms

# Experimental Prospects

Sweet spot will be covered by next-generation experiments



taken from 1710.03764

# Summary

- ★ Can address  $(g-2)_\mu$  with 7-17 MeV ALP that couples to all charged leptons [need 1% tuning to satisfy  $(g-2)_e$ ]
- ★ Beam dump constraints are avoided since axion promptly decays to electrons
- ★ Also accounts for XENON1T excess in electron recoils when axion coupled to DM fermion [that can be ADM]
- ★ ALP can be QCD axion when coupled also to first generation quarks such that pion-phobic [new contrihs to  $g-2$  are small]