

# Safely Eating Junk: Pileup and Infrared Radiation AnNiHilAtion (PIRANHA)

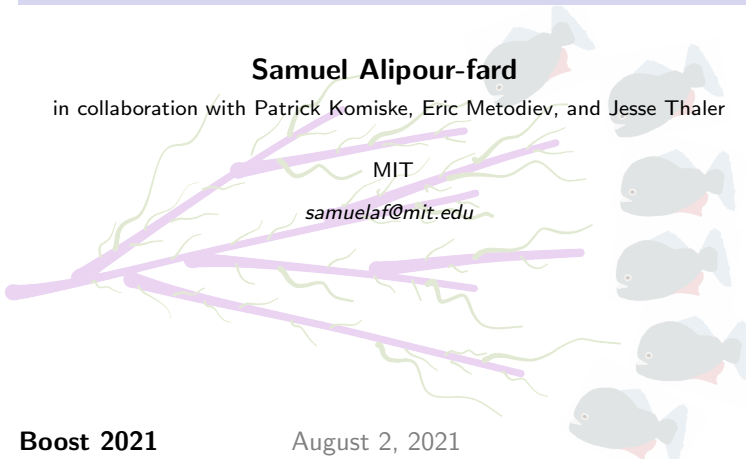


**Samuel Alipour-fard**

in collaboration with Patrick Komiske, Eric Metodiev, and Jesse Thaler

MIT

*samuelaf@mit.edu*



Motivation

PIRANHAS from  
Geometry

Strengths of  
PIRANHA  
Grooming

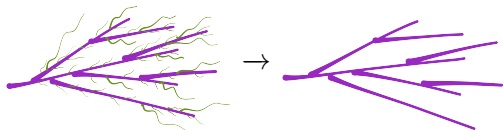
Boost 2021

August 2, 2021



## Grooming:

A systematic procedure for removing contaminating soft radiation from particle collision data.

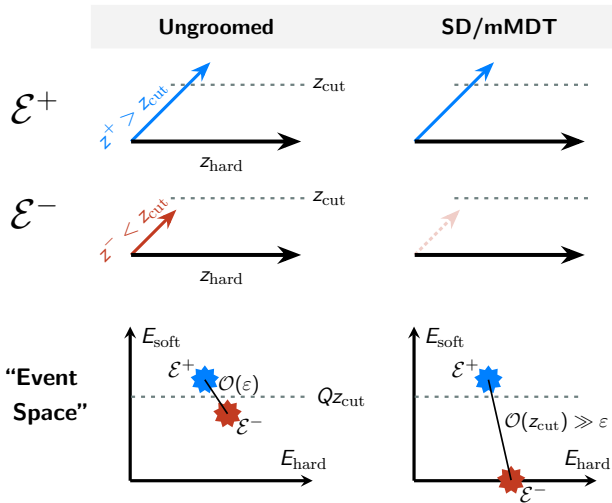


- ▶ **Experiment:** Groomed information is resilient to detector effects, pileup, initial state radiation  
[CMS: \[1807.05974\]](#), [ATLAS: \[1711.08341\]](#)
- ▶ **Theory:** Grooming can facilitate precision calculations of jet substructure observables  
[Frye-Larkoski-Schwartz-Yan: \[1603.09338\]](#)  
[Marzani-Schunk-Soyez: \[1712.05105\]](#)
- ▶ **Focus on mMDT** [Dasgupta-Fregoso-Marzani-Salam: \[1307.0007\]](#)  
(AKA Soft Drop with  $\beta = 0$ : [Larkoski-Marzani-Soyez-Thaler: \[1402.2657\]](#))

# Motivation



Grooming techniques such as Soft Drop/mMDT implement hard cutoffs ( $z_{\text{cut}}$ ), leading to **discontinuous behavior**:



Motivation

PIRANHAs from Geometry

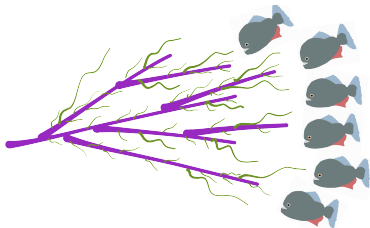
Strengths of PIRANHA Grooming



## PIRANHA:

A systematic procedure for *continuously* removing contaminating soft radiation (no hard cutoffs).

- ▶ Intuitively described as the optimal transport of piranhas hungry for soft radiation.



- ▶ **Recursive safe subtraction** is a tree-based PIRANHA grooming procedure analogous to procedures like Soft Drop/mMDT.

Motivation

PIRANHAS from  
Geometry

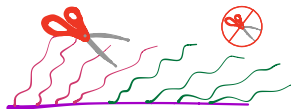
Strengths of  
PIRANHA  
Grooming

# Introducing: Recursive Safe Subtraction (RSS)



## Soft Drop/mMDT

- ▶ **Check**  $z > z_{\text{cut}}$ .
- ▶ **Failed:** Groom softer branch and continue.
- ▶ **Passed:** Keep remaining jet.



Motivation

PIRANHAs from  
Geometry

Strengths of  
PIRANHA  
Grooming

# Introducing: Recursive Safe Subtraction (RSS)

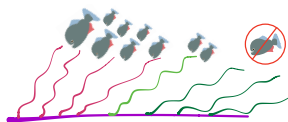
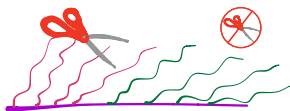


## Soft Drop/mMDT

- ▶ **Check**  $z > z_{\text{cut}}$ .
- ▶ **Failed:** Groom softer branch and continue.
- ▶ **Passed:** Keep remaining jet.

## PIRANHA-RSS

- ▶ **Check**  $z > z_{\text{cut}}^{(n)}$ .  
( $z_{\text{cut}}^{(0)} = z_{\text{cut}}$ )
- ▶ **Failed:** Groom softer branch, set  $z_{\text{cut}}^{(n+1)} = z_{\text{cut}}^{(n)} - z$ , and continue.
- ▶ **Passed:** Remove energy from the softer branch,  $z \rightarrow z - z_{\text{cut}}^{(n)}$ , and keep remaining jet.



Motivation

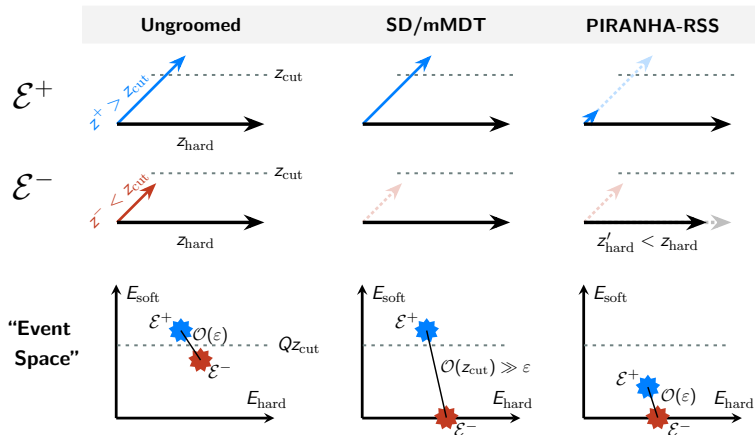
PIRANHAS from Geometry

Strengths of PIRANHA Grooming

# PIRANHA Grooming: Eating up the competition



Let's compare the continuity of PIRANHA-RSS grooming to that of Soft Drop/mMDT:



Motivation

PIRANHAS from Geometry

Strengths of PIRANHA Grooming

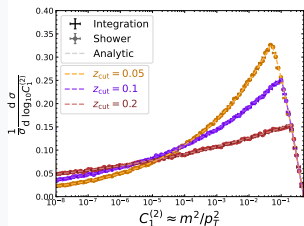
# Strengths of PIRANHA Grooming



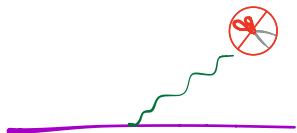
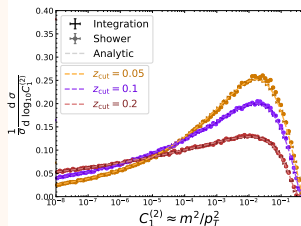
PIRANHA groomers are continuous!

Fixed coupling, **one emission** calculations:

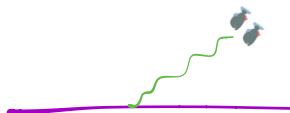
## Soft Drop/mMDT



## PIRANHA-RSS



Sharp cutoff  $\rightarrow$  kink



No sharp cutoff  $\rightarrow$  smooth

Motivation

PIRANHAS from  
Geometry

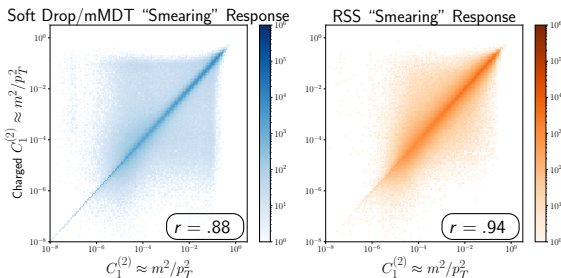
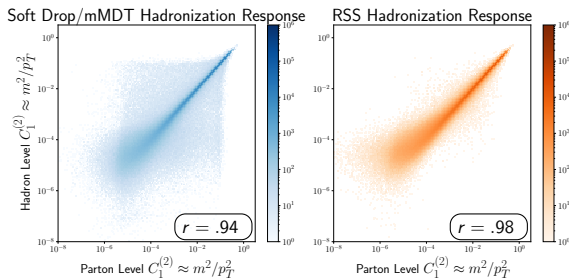
Strengths of  
PIRANHA  
Grooming



# Strengths of PIRANHA Grooming



PIRANHA in Pythia 8.244, QCD jets,  $P_T \geq 500$  GeV:



Motivation

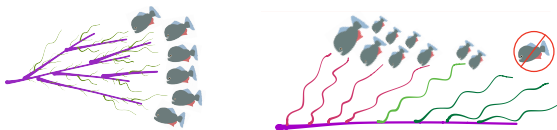
PIRANHAs from  
Geometry

Strengths of  
PIRANHA  
Grooming

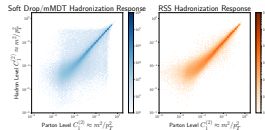
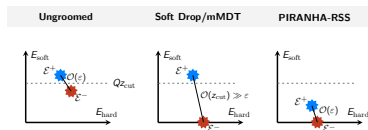
# Punchlines!



- ▶ Grooming is an important tool in the study of high energy microscopic physics.
- ▶ PIRANHA grooming is a continuous strategy for grooming based on geometry and optimal transport.



- ▶ PIRANHA grooming methods overcome discontinuities of previous methods.



Motivation

PIRANHA's from  
Geometry

Strengths of  
PIRANHA  
Grooming



Motivation

PIRANHAs from  
Geometry

Strengths of  
PIRANHA  
Grooming



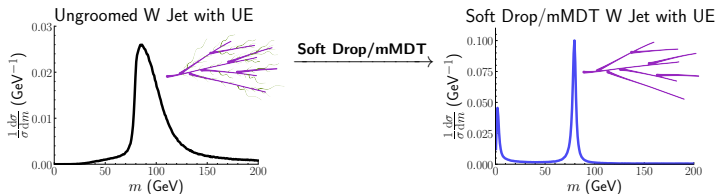
- ▶ **Experiment:** Groomed information is resilient to detector effects, pileup, initial state radiation

CMS: [1807.05974], ATLAS: [1711.08341]

- ▶ **Theory:** Grooming can facilitate precision calculations of jet substructure observables

Frye-Larkoski-Schwartz-Yan: [1603.09338]

Marzani-Schunk-Soyez: [1712.05105]



mMDT: Dasgupta-Fregoso-Marzani-Salam: [1307.0007]

Soft Drop: Larkoski-Marzani-Soyez-Thaler: [1402.2657]

- ▶ To simplify conclusions for the rest of the talk, we will limit ourselves to mMDT, or Soft Drop with  $\beta = 0$ .

Motivation

PIRANHAs from Geometry

Strengths of PIRANHA Grooming

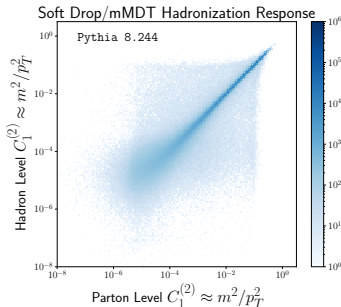
# Motivation



Grooming techniques such as Soft Drop/mMDT implement hard cutoffs ( $z_{\text{cut}}$ ), leading to **discontinuous behavior**.

## Consequences:

- ▶ Increased sensitivity to detector effects
- ▶ Theoretical complications [Hoang-Mantry-Pathak-Stewart: \[1906.11843\]](#)



Motivation

PIRANHAs from  
Geometry

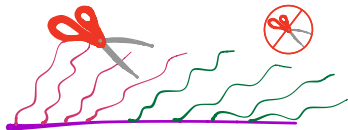
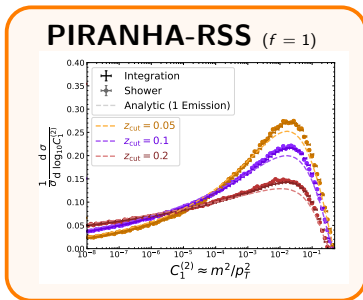
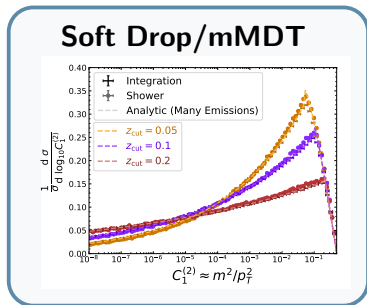
Strengths of  
PIRANHA  
Grooming

# Strengths of PIRANHA Grooming

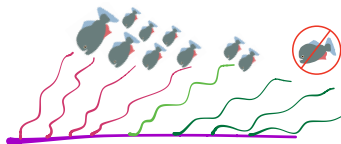


PIRANHA groomers are continuous!

Fixed coupling, **multiple emission** calculations:



Sharp cutoff  $\rightarrow$  kink



No sharp cutoff  $\rightarrow$  smooth

Motivation

PIRANHAS from  
Geometry

Strengths of  
PIRANHA  
Grooming

# Robustness of PIRANHA



PIRANHA groomers are continuous!

Let's examine the implications of the continuity of PIRANHA in Pythia 8.244 on QCD jets, with  $P_T \geq 500$  GeV:

- ▶ Hadronization (parton level vs. hadron level)
- ▶ Detector effects (**Proxy**: all vs. charged)
- ▶ Underlying event (UE: multi-parton interactions on vs. off)
- ▶ Comparing **Soft Drop/mMDT** and **PIRANHA-RSS**, both with  $z_{\text{cut}} = .1$ .

Motivation

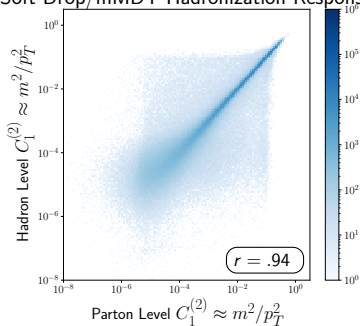
PIRANHAs from  
Geometry

Strengths of  
PIRANHA  
Grooming

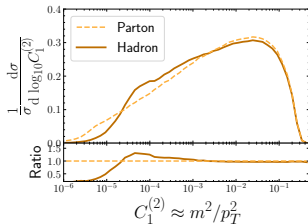
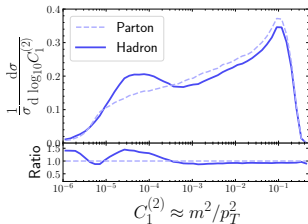
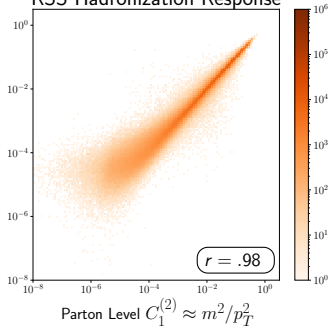
# Robustness of PIRANHA: Hadronization



Soft Drop/mMDT Hadronization Response



RSS Hadronization Response



Motivation

PIRANHAs from  
Geometry

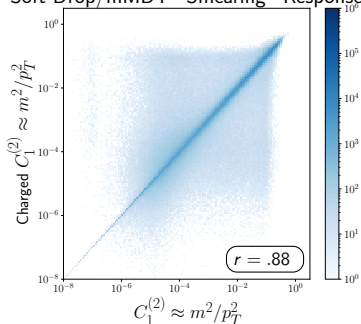
Strengths of  
PIRANHA  
Grooming



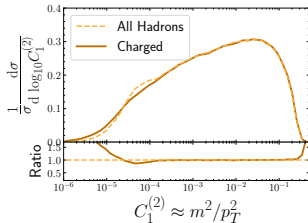
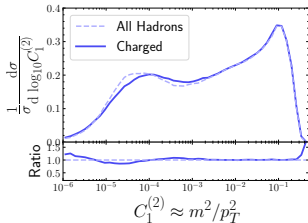
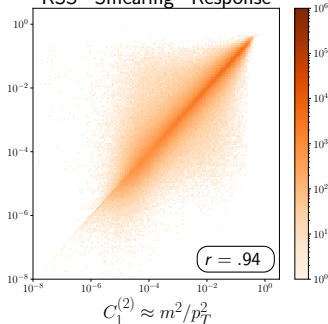
# Robustness of PIRANHA: Detector Proxy



Soft Drop/mMDT "Smearing" Response



RSS "Smearing" Response



Motivation

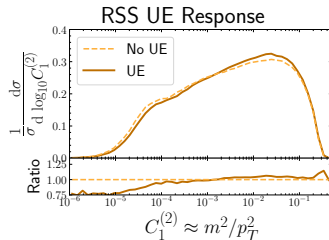
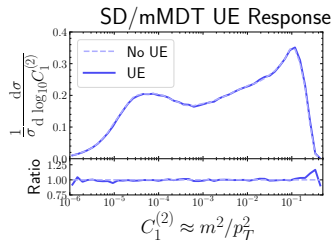
PIRANHAs from  
Geometry

Strengths of  
PIRANHA  
Grooming

# Subtleties of PIRANHA: Underlying Event



UE modeled by multi-parton interactions in Pythia:



- ▶ Unlike Soft Drop/mMDT, RSS can remove only a limited amount of energy, leading to slight responses to the underlying event.

Motivation

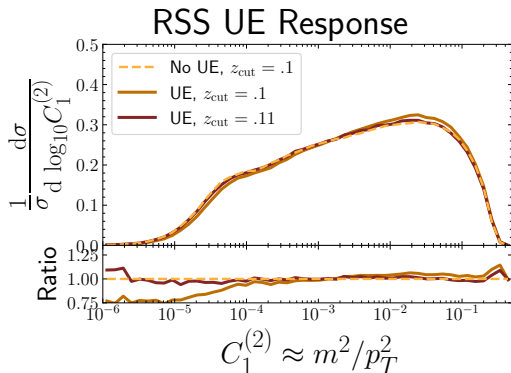
PIRANHAs from  
Geometry

Strengths of  
PIRANHA  
Grooming

# Subtleties of PIRANHA: Underlying Event



- ▶ For RSS, we can *increase*  $z_{\text{cut}}$  to remove additional radiation/corrections due to the underlying event:



Motivation

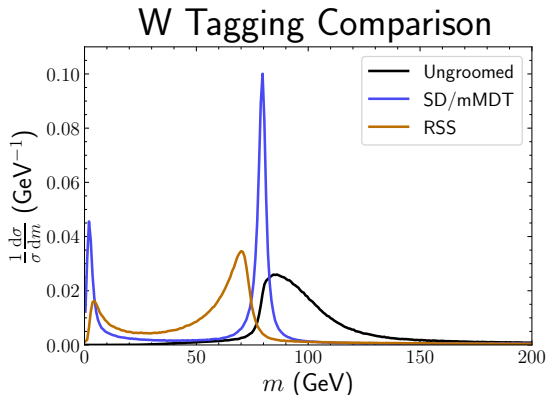
PIRANHAs from  
Geometry

Strengths of  
PIRANHA  
Grooming

# Subtleties of PIRANHA: W Tagging



**W Tagging:** RSS leads to shifted mass determinations and worse mass resolution:



- ▶  $z_{\text{cut}} = .1$  grooms too much!
- ▶ Mass shifted by  $\sim 12\%$

Motivation

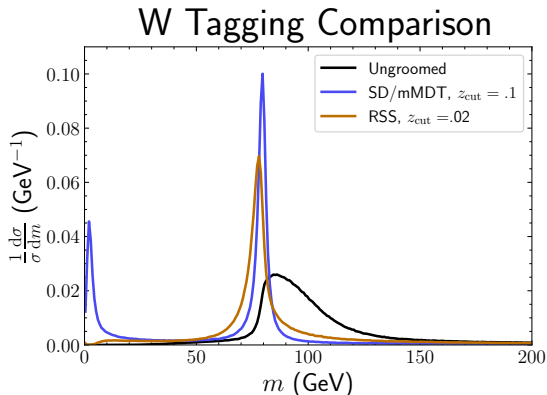
PIRANHAs from  
Geometry

Strengths of  
PIRANHA  
Grooming

# Subtleties of PIRANHA: W Tagging



**W Tagging:** RSS leads to shifted mass determinations and worse mass resolution:



- ▶ This time, *decrease*  $z_{\text{cut}}$  to remove less radiation.
- ▶ Mass shifted by  $\sim 2\%$ .

Motivation

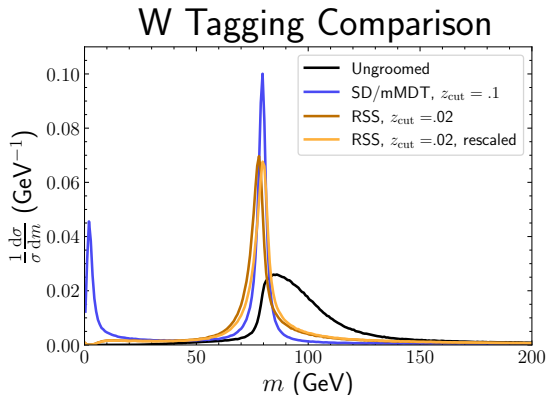
PIRANHAs from  
Geometry

Strengths of  
PIRANHA  
Grooming

# Subtleties of PIRANHA: W Tagging



**W Tagging:** RSS leads to shifted mass determinations and worse mass resolution:



- ▶ This time, *decrease*  $z_{\text{cut}}$  to remove less radiation.
- ▶ Mass shifted by  $\sim 2\%$ .

Motivation

PIRANHAs from  
Geometry

Strengths of  
PIRANHA  
Grooming



## Strengths:

- ▶ **Hadronization:** RSS is more robust to the effects of hadronization than Soft Drop/mMDT.
- ▶ **Detector effects:** Using simple models of smearing, RSS appears to be more robust to detector effects than Soft Drop/mMDT.

## Subtleties:

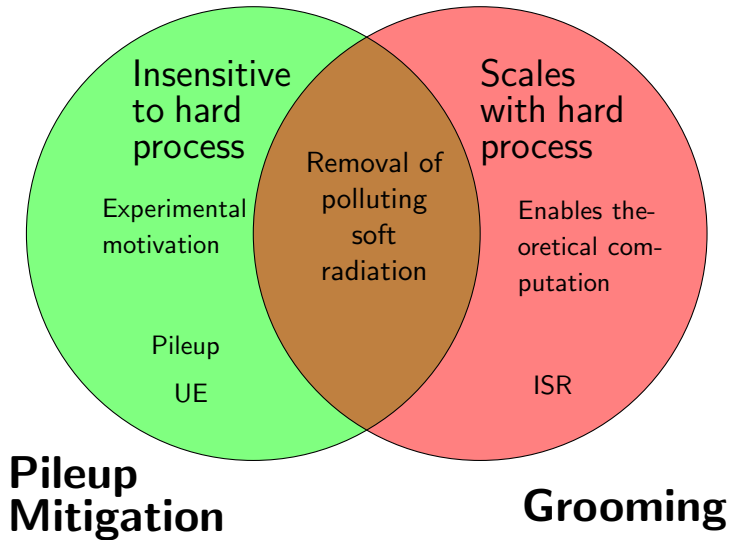
- ▶ **Underlying event:** Distributions of observables in RSS jets are robust against UE, especially if we shift  $z_{\text{cut}}$  to account for UE.
- ▶ **W Tagging:** RSS leads to shifted mass determinations and worse mass resolution, but potentially greater acceptance.

Motivation

PIRANHAs from  
Geometry

Strengths of  
PIRANHA  
Grooming

# Grooming vs. Pileup Mitigation



Motivation

PIRANHAs from Geometry

Strengths of PIRANHA Grooming



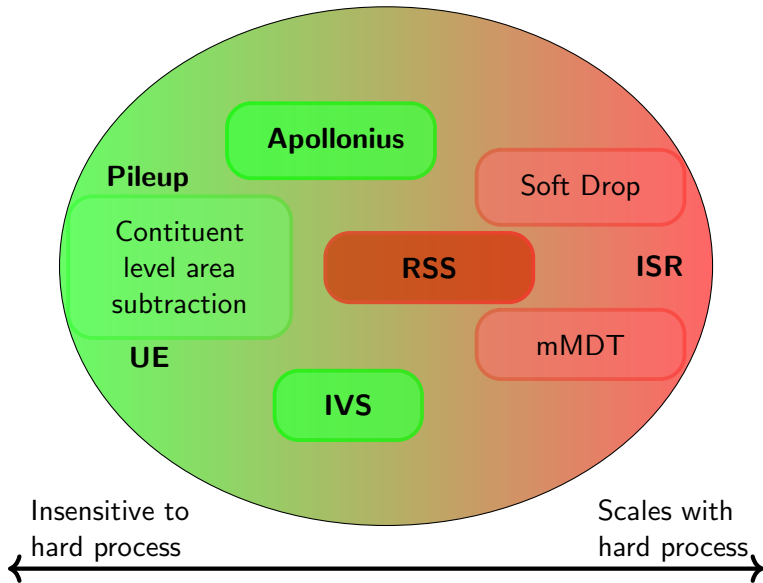
# Grooming vs. Pileup Mitigation



Motivation

PIRANHAs from  
Geometry

Strengths of  
PIRANHA  
Grooming



# Generations of Groomers



c. 2008

**1<sup>st</sup> Generation** (Mass Drop): **IRC safety**



c. 2015

**2<sup>nd</sup> Generation** (mMDT, Soft Drop): **Calculability**



c. 2021

**PIRANHA** (Apollonius, IVS, RSS): **Continuity**

Motivation

PIRANHAs from  
Geometry

Strengths of  
PIRANHA  
Grooming



## All Observables

*Measurable at a collider*

## Defined on Energy Flows

*Invariant to exact infrared & collinear emissions everywhere except a negligible set of events*

## Infrared & Collinear Safe

*EMD continuous everywhere except a negligible set of events*

### EMD Hölder Continuous

*Everywhere invariant to infinitesimal  
infrared & collinear emissions*

### Sudakov Safe

*Discontinuous on some  
N-particle manifolds*

Motivation

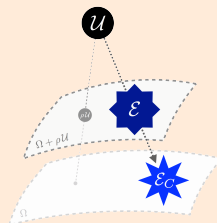
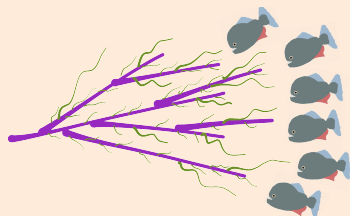
PIRANHAs from  
Geometry

Strengths of  
PIRANHA  
Grooming



**Grooming:** Remove contaminating soft radiation.

**PIRANHA:** *Continuously* subtract off contaminating soft radiation *using geometry*.



Komiske-Metodiev-Thaler: [2004.04159]

**First Solution:**

$$\mathcal{E}_{\text{groomed}} = \mathcal{E}_C = \operatorname{argmin}_{\mathcal{E}'} \operatorname{EMD}(\mathcal{E}, \mathcal{E}' + \rho\mathcal{U}) \quad (1)$$

Motivation

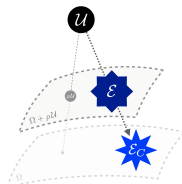
PIRANHAs from  
Geometry

Strengths of  
PIRANHA  
Grooming



## Solution:

$$\mathcal{E}_{\text{groomed}} = \mathcal{E}_C = \operatorname{argmin}_{\mathcal{E}'} \operatorname{EMD}(\mathcal{E}, \mathcal{E}' + \rho\mathcal{U})$$



Motivation

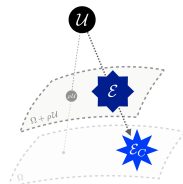
PIRANHAs from  
Geometry

Strengths of  
PIRANHA  
Grooming

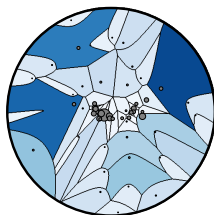


## Solution:

$$\mathcal{E}_{\text{groomed}} = \mathcal{E}_C = \operatorname{argmin}_{\mathcal{E}'} \operatorname{EMD}(\mathcal{E}, \mathcal{E}' + \rho \mathcal{U})$$



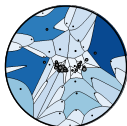
Well studied in optimal transport  $\rightarrow$  **Apollonius grooming!**



$$p_{T,i}^{\text{groomed}} = p_{T,i} - \rho A_i^{\text{Apoll.}}$$



- ▶ **Apollonius grooming:** Closest to optimal transport



$$p_{T,i}^{\text{groomed}} = p_{T,i} - \rho A_i^{\text{Apoll.}}$$

- ▶ Weakness: computationally expensive
- ▶ Would like to develop models of the geometric grooming procedure
- ▶ Keep IRC safety/continuity in event space while improving computational power

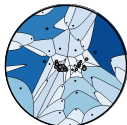
Motivation

PIRANHAs from  
Geometry

Strengths of  
PIRANHA  
Grooming

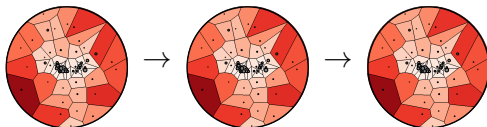


- ▶ **Apollonius grooming:** Closest to optimal transport



$$p_{T,i}^{\text{groomed}} = p_{T,i} - \rho A_i^{\text{Apoll.}}$$

- ▶ **Iterated Voronoi Subtraction:** Efficient variant



$$p_{T,i, n^{\text{th}}\text{step}}^{\text{groomed}} = p_{T,i, n^{\text{th}}\text{step}} - \rho A_{i, n^{\text{th}}\text{step}}^{\text{Voronoi}}$$

- ▶ **Recursive Safe Subtraction:** Closest to traditional grooming methods

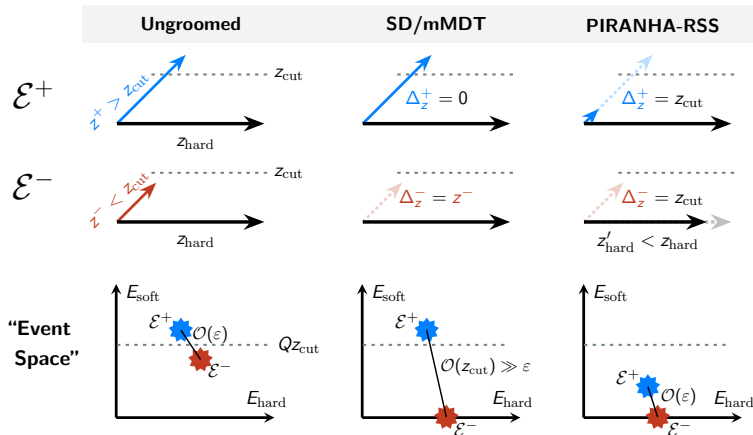
Motivation

PIRANHAS from  
Geometry

Strengths of  
PIRANHA  
Grooming



# PIRANHA Grooming: Eating up the competition



Motivation

PIRANHAS from Geometry

Strengths of PIRANHA Grooming

# Introducing: Recursive Safe Subtraction



**SD/mMDT**

**PIRANHA-RSS**

Motivation

PIRANHAs from  
Geometry

Strengths of  
PIRANHA  
Grooming

In RSS,  $f$  is the fraction of energy removed from the softer branch.

# Introducing: Recursive Safe Subtraction



## SD/mMDT

- ▶ **Check**  
 $z > z_{\text{cut}} \theta^\beta.$

## PIRANHA-RSS

- ▶ **Check**  $z > fz_{\text{cut}}^{(n)}.$   
( $z_{\text{cut}}^{(0)} = z_{\text{cut}}$ )

Motivation

PIRANHAs from  
Geometry

Strengths of  
PIRANHA  
Grooming

In RSS,  $f$  is the fraction of energy removed from the softer branch.

# Introducing: Recursive Safe Subtraction



## SD/mMDT

- ▶ **Check**  
 $z > z_{\text{cut}} \theta^\beta.$
- ▶ **Failed:**  
Groom softer branch and continue

## PIRANHA-RSS

- ▶ **Check**  $z > fz_{\text{cut}}^{(n)}$ .  
( $z_{\text{cut}}^{(0)} = z_{\text{cut}}$ )
- ▶ **Failed:** Groom energy from both branches (softer branch completely), set  $z_{\text{cut}}^{(n+1)} = z_{\text{cut}}^{(n)} - z/f$ , and continue

In RSS,  $f$  is the fraction of energy removed from the softer branch.

Motivation

PIRANHA from Geometry

Strengths of PIRANHA Grooming

# Introducing: Recursive Safe Subtraction



## SD/mMDT

- ▶ **Check**  
 $z > z_{\text{cut}}\theta^\beta.$
- ▶ **Failed:**  
Groom softer branch and continue
- ▶ **Passed:**  
Keep remaining jet

## PIRANHA-RSS

- ▶ **Check**  $z > fz_{\text{cut}}^{(n)}$ .  
( $z_{\text{cut}}^{(0)} = z_{\text{cut}}$ )
- ▶ **Failed:** Groom energy from both branches (softer branch completely), set  $z_{\text{cut}}^{(n+1)} = z_{\text{cut}}^{(n)} - z/f$ , and continue
- ▶ **Passed:** Groom energy from both branches,  $z \rightarrow z - fz_{\text{cut}}^{(n)}$ , and keep remaining jet.

In RSS,  $f$  is the fraction of energy removed from the softer branch.

Motivation

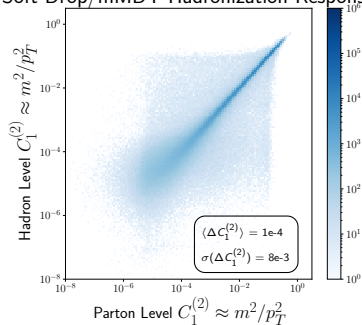
PIRANHAs from Geometry

Strengths of PIRANHA Grooming

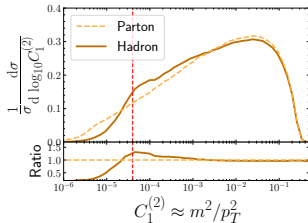
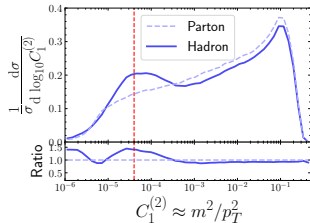
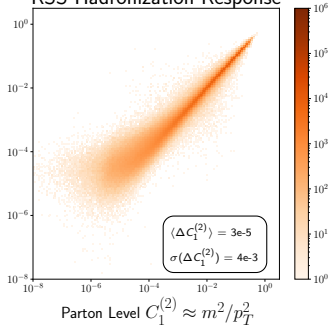
# Robustness of PIRANHA: Hadronization



Soft Drop/mMDT Hadronization Response



RSS Hadronization Response



Motivation

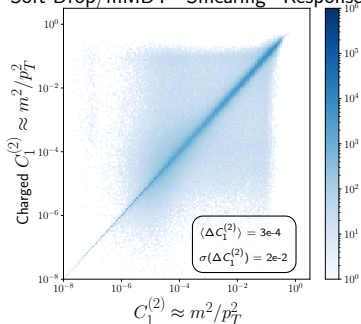
PIRANHAs from  
Geometry

Strengths of  
PIRANHA  
Grooming

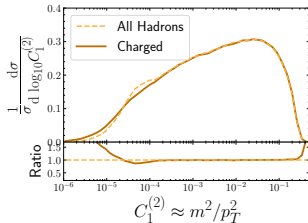
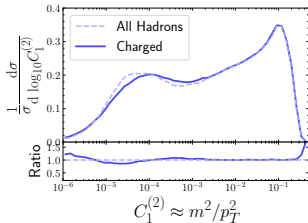
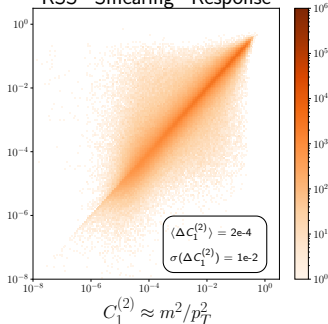
# Robustness of PIRANHA: Detector Proxy



Soft Drop/mMDT "Smearing" Response



RSS "Smearing" Response



Motivation

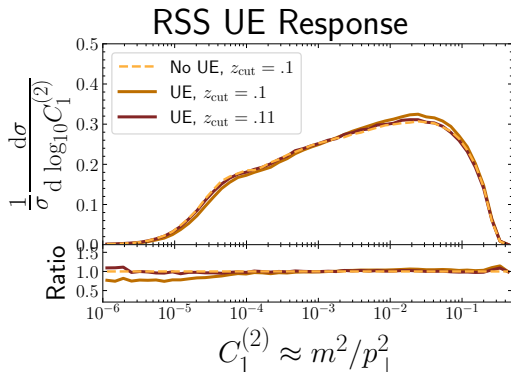
PIRANHAs from  
Geometry

Strengths of  
PIRANHA  
Grooming

# Subtleties of PIRANHA: Underlying Event



- ▶ In RSS, we may increase  $z_{\text{cut}}$  to remove additional radiation/corrections due to the underlying event:



- ▶ UE,  $z_{\text{cut}} = .1$ : Max is 106% the max of no UE
- ▶ UE,  $z_{\text{cut}} = .11$ : Max is 101% the max of no UE

Motivation

PIRANHAs from  
Geometry

Strengths of  
PIRANHA  
Grooming





- ▶ Dropped energy

$$\Delta_E = E(\mathcal{E}) - E(\mathcal{E}_{\text{groomed}})$$

- ▶ Generalized jet energy correlation functions (GECFs)

$$C_1^{(\beta)} = \sum_{i,j \in \text{jet}} z_i z_j \theta^\beta,$$

$$(C_1^{(2)} \sim m^2/p_T^2)$$

Motivation

PIRANHAs from  
Geometry

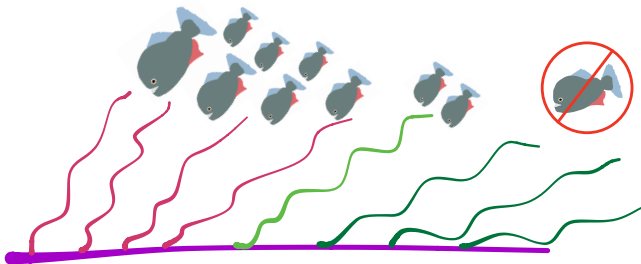
Strengths of  
PIRANHA  
Grooming

# Emissions of RSS Groomed Jets



RSS where at every branch, only the softer branch is groomed ( $f = 1$ ). There will be three types of emissions:

- ▶ **Pre-critical emissions:** completely groomed away, using up some of the grooming parameter
- ▶ One **critical emission:** the first emission to survive the grooming process
- ▶ **Subsequent emissions:** emissions after the critical emission, completely ungroomed



Motivation

PIRANHAS from  
Geometry

Strengths of  
PIRANHA  
Grooming



$$\iint_{\text{blue oval}} d \log \theta \, z \, d \log z \, \frac{\alpha_s}{\pi} [\bar{\rho}(z)]_+^{(1/2)} \triangleq \text{graph (2)},$$

(2)

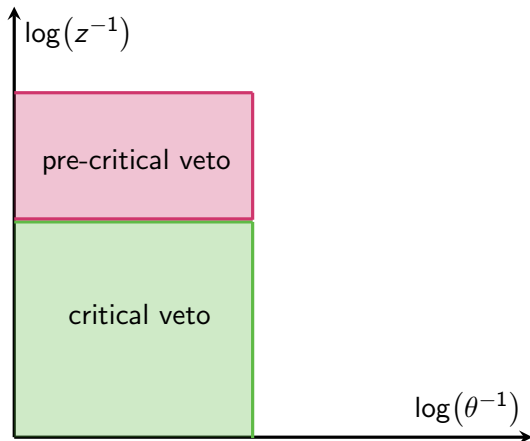
$$\text{blue square} = 0, \quad \text{blue square with white oval} = - \text{graph (3)}.$$

(3)

Motivation

PIRANHAs from  
Geometry

Strengths of  
PIRANHA  
Grooming



Motivation

PIRANHAs from  
Geometry

Strengths of  
PIRANHA  
Grooming



$$\Sigma_{\text{crit}}(\theta) \approx \exp \left[ - \int_{\theta' < \theta}^{z < z_{\text{cut}}} \right]$$
$$= \exp \left[ - \frac{\alpha_s}{\pi} \int_{\theta}^1 \frac{d\theta'}{\theta'} \int_{z_{\text{cut}}}^{1/2} \bar{p}(z) \right]$$

Motivation

PIRANHAs from  
Geometry

Strengths of  
PIRANHA  
Grooming



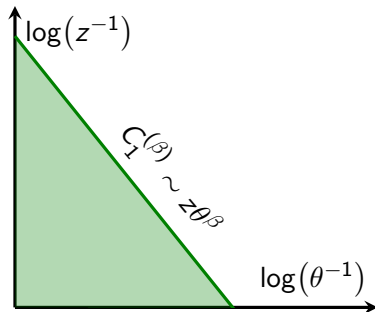
$$\Sigma_{\text{pre}}(z_{\text{pre}}|\theta_{\text{crit}})\Sigma_{\text{crit}}(\theta_{\text{crit}}) = \exp \left[ - \int \right]$$
A 2D coordinate system with a vertical y-axis and a horizontal x-axis. A rectangular region is shaded, divided into two parts: a green rectangle at the bottom and a pink rectangle on top. The entire shaded region is enclosed within large square brackets, with a minus sign to the left of the opening bracket.

Motivation

PIRANHAs from  
Geometry

Strengths of  
PIRANHA  
Grooming

# Lund Diagrammar: Subsequent Emissions



$$\Sigma_{\text{sub}}(C_1^{(\beta)}) \approx \exp \left[ - \left( \text{diagram} \right) \right]$$

Motivation

PIRANHAs from  
Geometry

Strengths of  
PIRANHA  
Grooming