

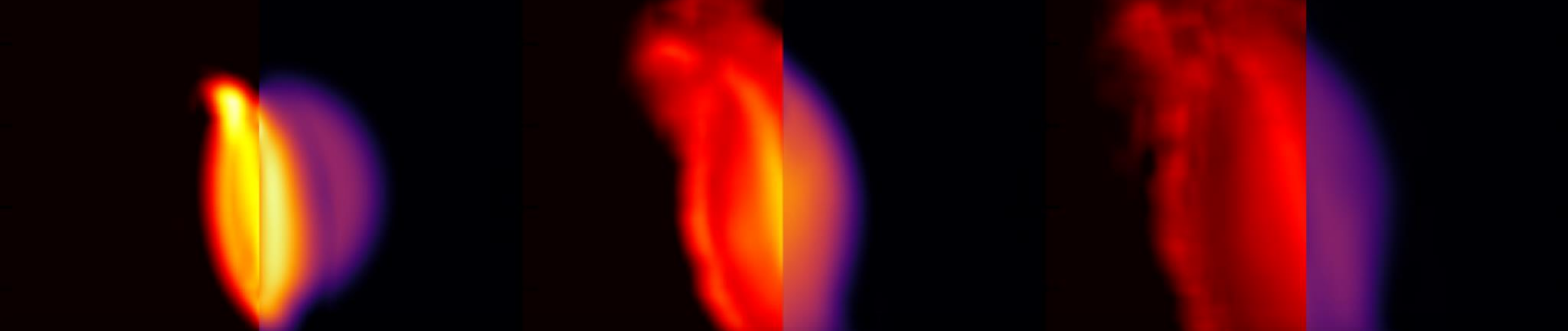


Dynamics of the QCD matter in heavy ion collisions and binary neutron star mergers

Strangeness in Quark Matter, Busan, Republic of Korea, 15 June 2022

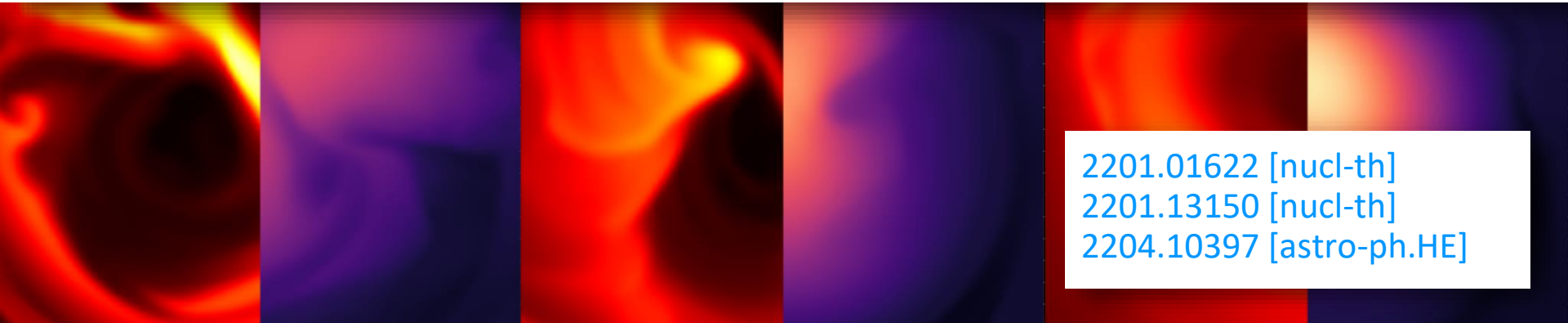
Anton Motornenko





Thanks to:

M. Bleicher, V. Dexheimer, M. Hanauske, A. Heger, P. Jakobus, E. Most, B. Müller, Y. Nara, M. Omana Kuttan, L. Rezzolla, J. Steinheimer,
and H. Stöcker



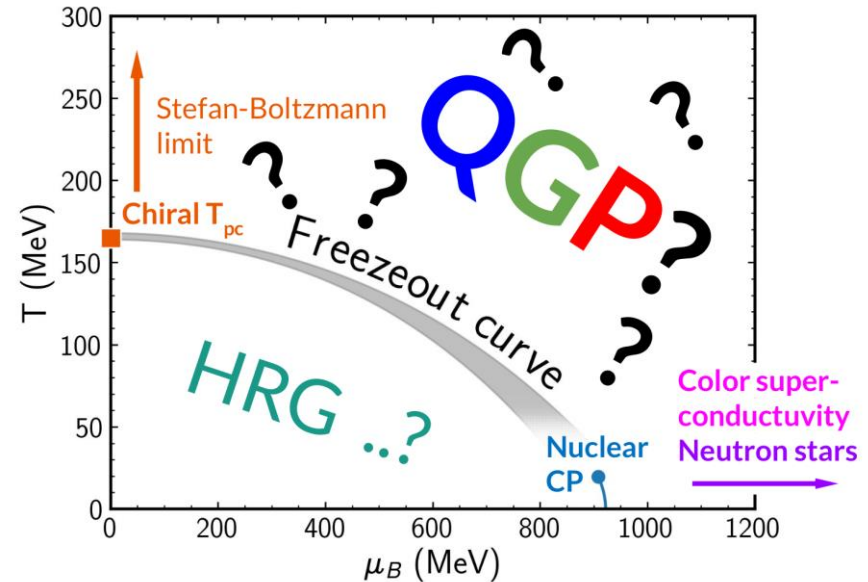
2201.01622 [nucl-th]
2201.13150 [nucl-th]
2204.10397 [astro-ph.HE]

QCD phase diagram

$$\mathcal{L}_{\text{QCD}} = \sum_{i,j} \bar{\psi}_i \left(i\gamma^\mu (\partial_\mu \delta_{ij} - \frac{i}{s} g \mathcal{A}_\mu^a \lambda_{a,ij}) - m_i \delta_{ij} \right) \psi_j - \frac{1}{4} G_{\mu\nu}^a G_a^{\mu\nu}$$
$$G_{\mu\nu}^a = \partial_\mu \mathcal{A}_\nu^a - \partial_\nu \mathcal{A}_\mu^a + g f^{abc} \mathcal{A}_\mu^b \mathcal{A}_\nu^c$$

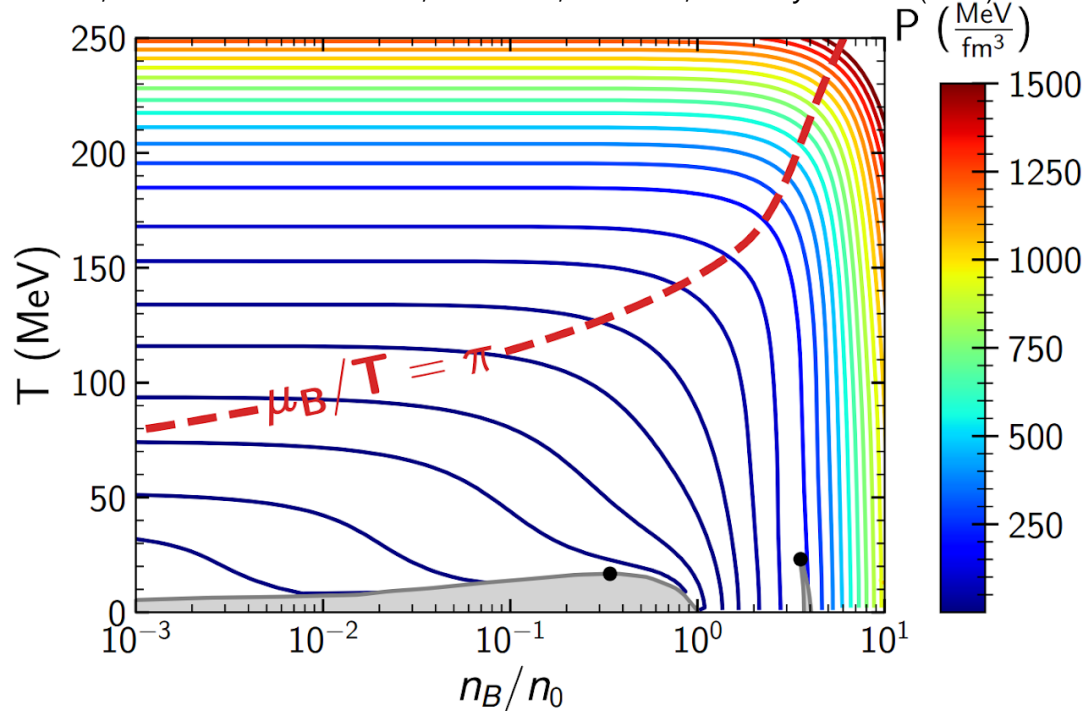


How to map the well established QCD theory to its phase diagram?



Beyond the lattice data

AM, Vovchenko Steinheimer, Schramm, Stoecker, *Nucl.Phys.A* 1005 (2021) 121836



Lines of CMF constant pressure. The grey shaded regions: mixed phases by nuclear liquid-vapor and chiral phase transitions. Black dots — critical endpoints.

First-principle lattice QCD data can be used at $\mu_B > 0$ by Taylor expansion:

$$P = P_0 + T^4 \sum_{i,j,k} \frac{1}{i!j!k!} \chi_{B,Q,S}^{i,j,k} \left(\frac{\mu_B}{T}\right)^i \left(\frac{\mu_Q}{T}\right)^j \left(\frac{\mu_S}{T}\right)^k$$

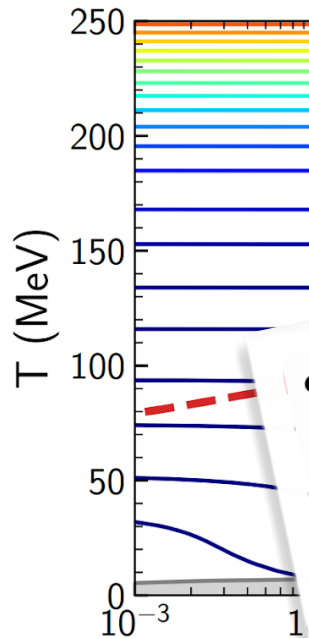
With limited radius of convergence (see recent progress at P. Parotto talk on Wednesday).

At finite densities the transition to fermion-dominated matter changes isobaric lines.

There is **need** for phenomenological models!

Beyond the lattice data

AM, Vovchenko Steinheimer, Schramm, Stoecker, *Nucl.Phys.A* 1005 (2021) 121800



Bulletpoints from theory overview:
(see Joseph Kapusta talk on Monday)

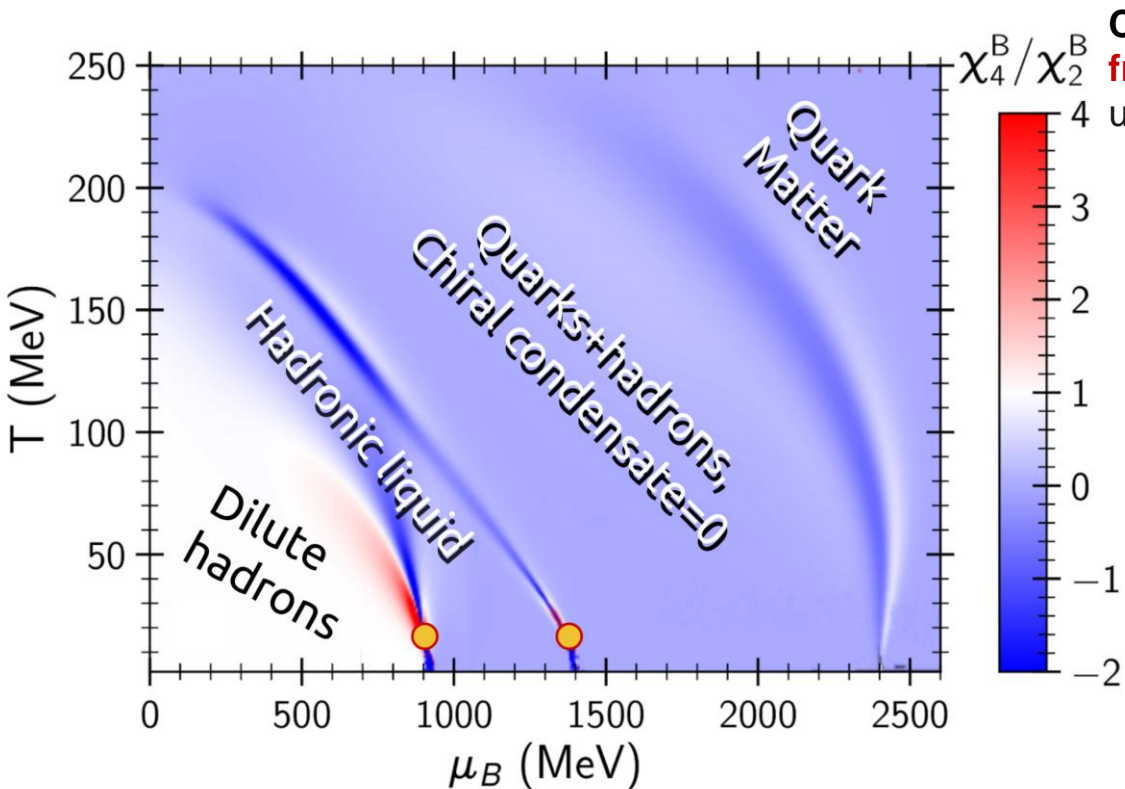
- To describe the matter created at RHIC beam energies and below, knowledge is required of the equation of state as a function of T , μ_B , μ_Q , and μ_S to conserve energy, baryon number, electric charge, and strangeness. This is nontrivial when there is critical behavior in the phase diagram.
- Such an equation of state is also needed for modeling neutron star mergers and closely related to the cold dense matter comprising neutron stars.

... principle lattice QCD data can
... $\mu_B > 0$ by Taylor

There is **need** for
phenomenological models!

Lines of CMF constant pressure. The grey shaded regions: mixed phases by nuclear liquid-vapor and chiral phase transitions. Black dots — critical endpoints.

An approach for QCD EOS: CMF model



Chiral Mean Field model is a **single framework** for QCD thermodynamics, can be used for

- analysis of lattice QCD data
- description of nuclear matter
- modeling of heavy ion collisions
- as well as neutron star description

Papazoglou, Schramm, Schaffner-Bielich, Stoecker, Greiner, nucl-th/9706024

Papazoglou, Zschesche, Schramm, Schaffner-Bielich, Stoecker, Greiner, nucl-th/9806087

Dexheimer, Schramm, 0901.1748

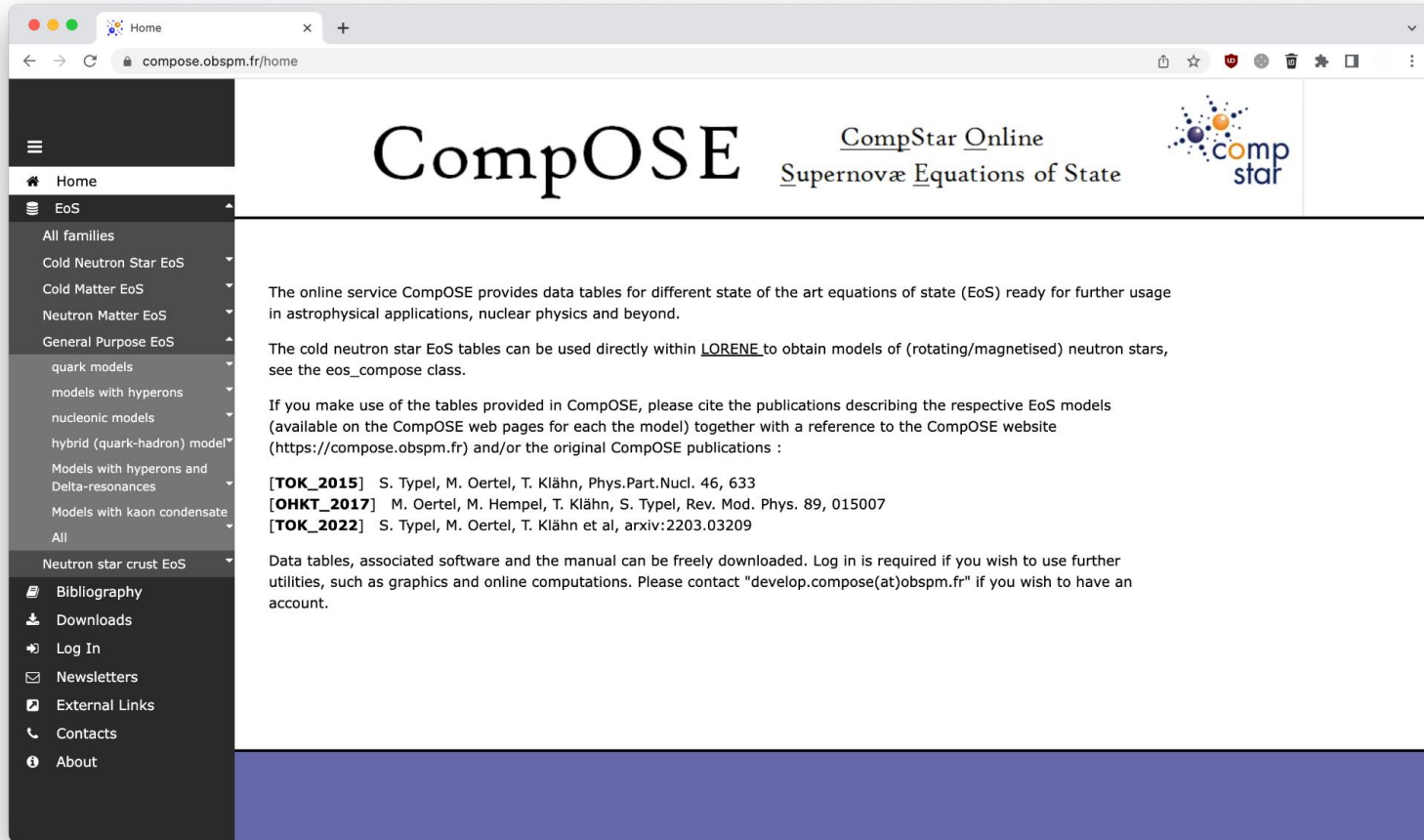
Steinheimer, Schramm, Stoecker 1009.5239

AM, Steinheimer, Vovchenko, Schramm, Stoecker, 1905.00866



AM, Steinheimer, Vovchenko, Schramm, Stoecker, *Phys. Rev. C* 101, no.3, 034904 (2020)

Separate EOS for astrophysics




The screenshot shows the homepage of the ComPOSE website. The browser address bar displays "compose.obspm.fr/home". The page features a dark sidebar on the left with a navigation menu. The main content area has a white background with the "CompOSE" logo in large black letters. To the right of the logo, it says "CompStar Online Supernovæ Equations of State" and includes the "comp star" logo. The main text describes the online service, provides instructions on using the data tables, and lists recent publications with their authors and titles.

Home

compose.obspm.fr/home

CompOSE

CompStar Online
Supernovæ Equations of State



The online service ComPOSE provides data tables for different state of the art equations of state (EoS) ready for further usage in astrophysical applications, nuclear physics and beyond.

The cold neutron star EoS tables can be used directly within [LORENE](#) to obtain models of (rotating/magnetised) neutron stars, see the `eos_compose` class.

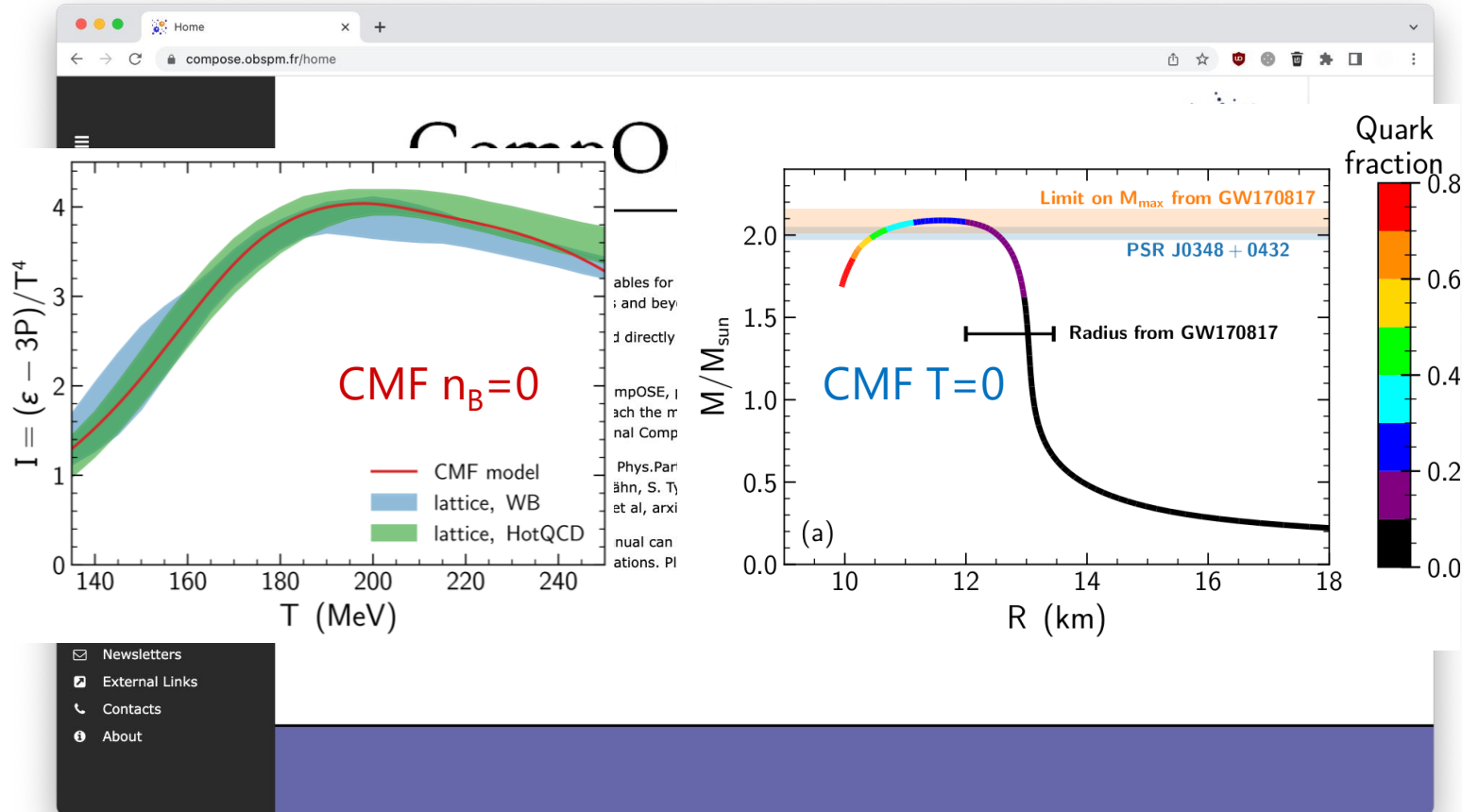
If you make use of the tables provided in ComPOSE, please cite the publications describing the respective EoS models (available on the ComPOSE web pages for each the model) together with a reference to the ComPOSE website (<https://compose.obspm.fr>) and/or the original ComPOSE publications :

[TOK_2015] S. Typel, M. Oertel, T. Klähn, Phys.Part.Nucl. 46, 633
[OHKT_2017] M. Oertel, M. Hempel, T. Klähn, S. Typel, Rev. Mod. Phys. 89, 015007
[TOK_2022] S. Typel, M. Oertel, T. Klähn et al, arxiv:2203.03209

Data tables, associated software and the manual can be freely downloaded. Log in is required if you wish to use further utilities, such as graphics and online computations. Please contact "develop.compose(at)obspm.fr" if you wish to have an account.

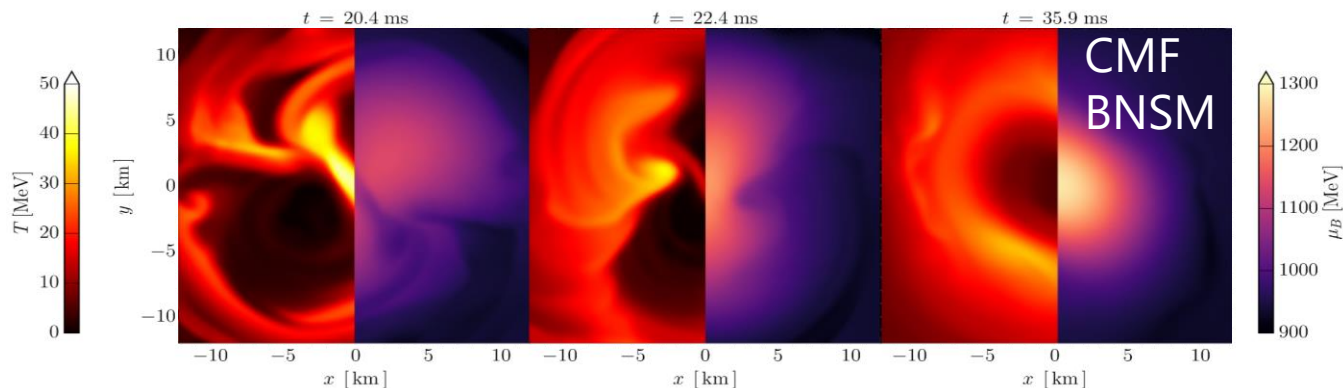
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 - Cold Matter EoS
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Separate Universal EOS for astrophysics and HIC

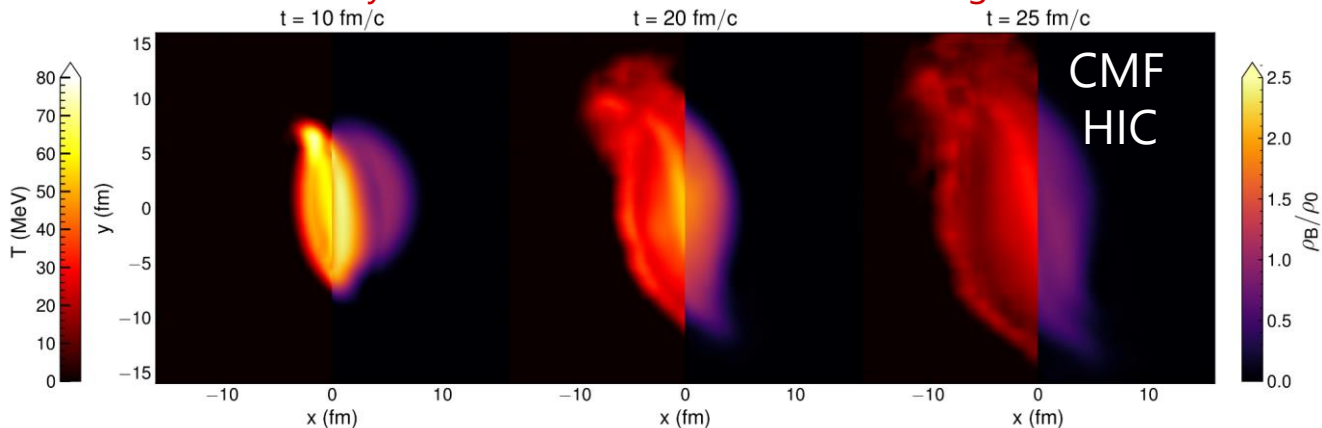


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Separate Universal EOS for astrophysics and HIC



CMF — single equation of state for full hydrodynamic modeling of both heavy ion collisions and neutron star mergers!



HIC vs BNSM: comparison

In the following we use ideal relativistic hydrodynamics, no viscosity and dissipations

Binary Neutron Star Mergers

General-relativistic magneto- hydrodynamics

Frankfurt/Illinois GRMHD (FIL) code

with Einstein Toolkit

Etienne, Paschalidis, Haas, Mosta, and Shapiro,

1501.07276 [astro-ph.HE]

Most, Papenfort, and Rezzolla, 1907.10328 [astro-

ph.HE]

F. Loffler et al., 1111.3344 [gr-qc].

Heavy Ion Collisions

Relativistic flux-corrected SHASTA code

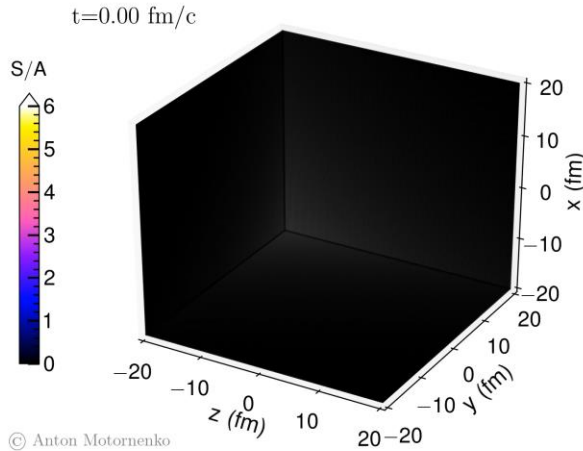
Boris, and Book, J. Comput. Phys. 11, 38 (1973)

Rischke, Bernard, and Maruhn, arXiv:nucl-

th/9504018

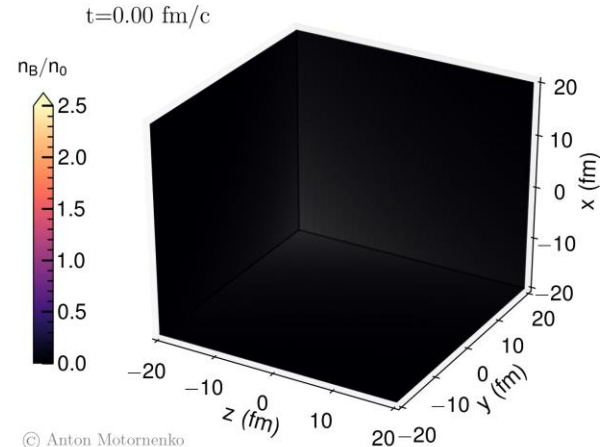
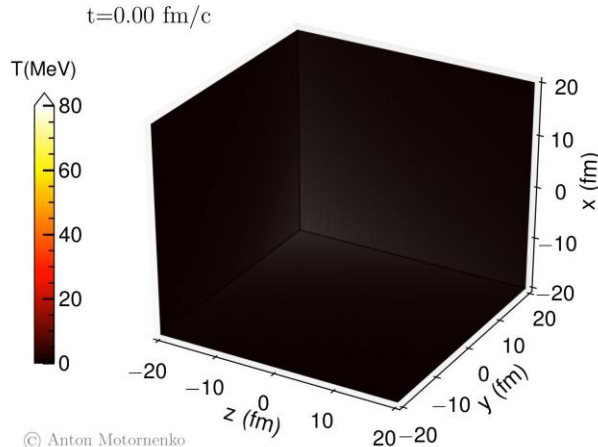
Both codes require equation of state as an input

Heavy ion collision evolution

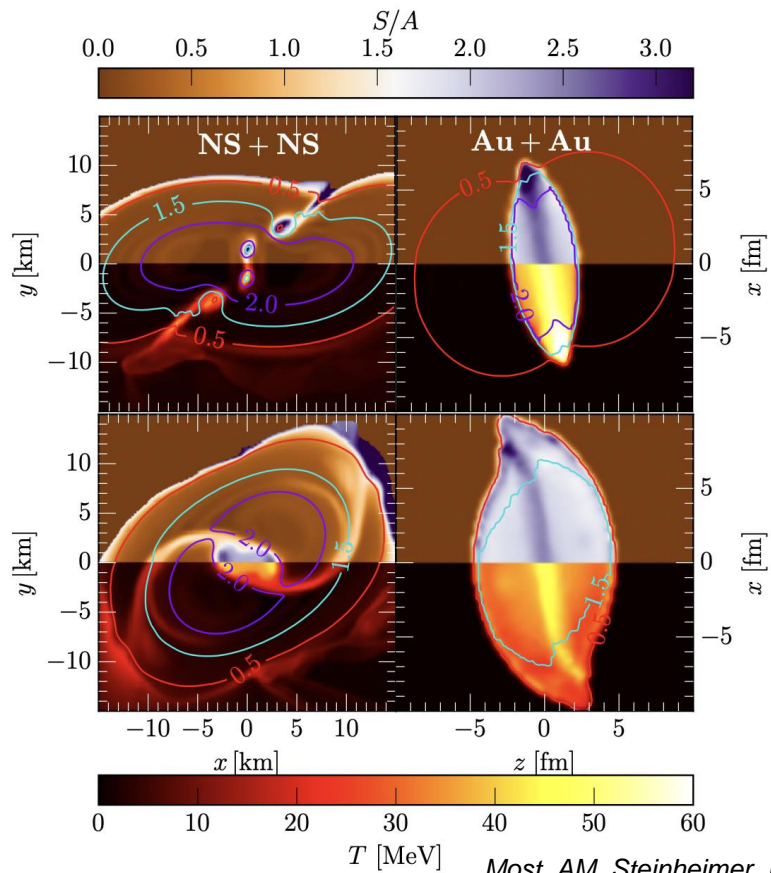


Au+Au collision at $E_{\text{lab}}=450$ MeV
Nuclei are initialised with Woods-Saxon distributions:

$$n_{WS} = \gamma_{CM} \frac{n_0}{1 + \exp\left(\frac{\Delta r - R}{a}\right)}$$



HIC vs BNSM: comparison



Geometry and scales are drastically different.
Thermodynamic conditions are similar!

Entropy per baryon S/A (top colormaps) and temperature T (bottom colormaps) for a BNS merger of mass $M_{\text{tot}} = 2.8 M_{\text{sun}}$, and Au + Au HIC at $E_{\text{lab}} = 450$ MeV.

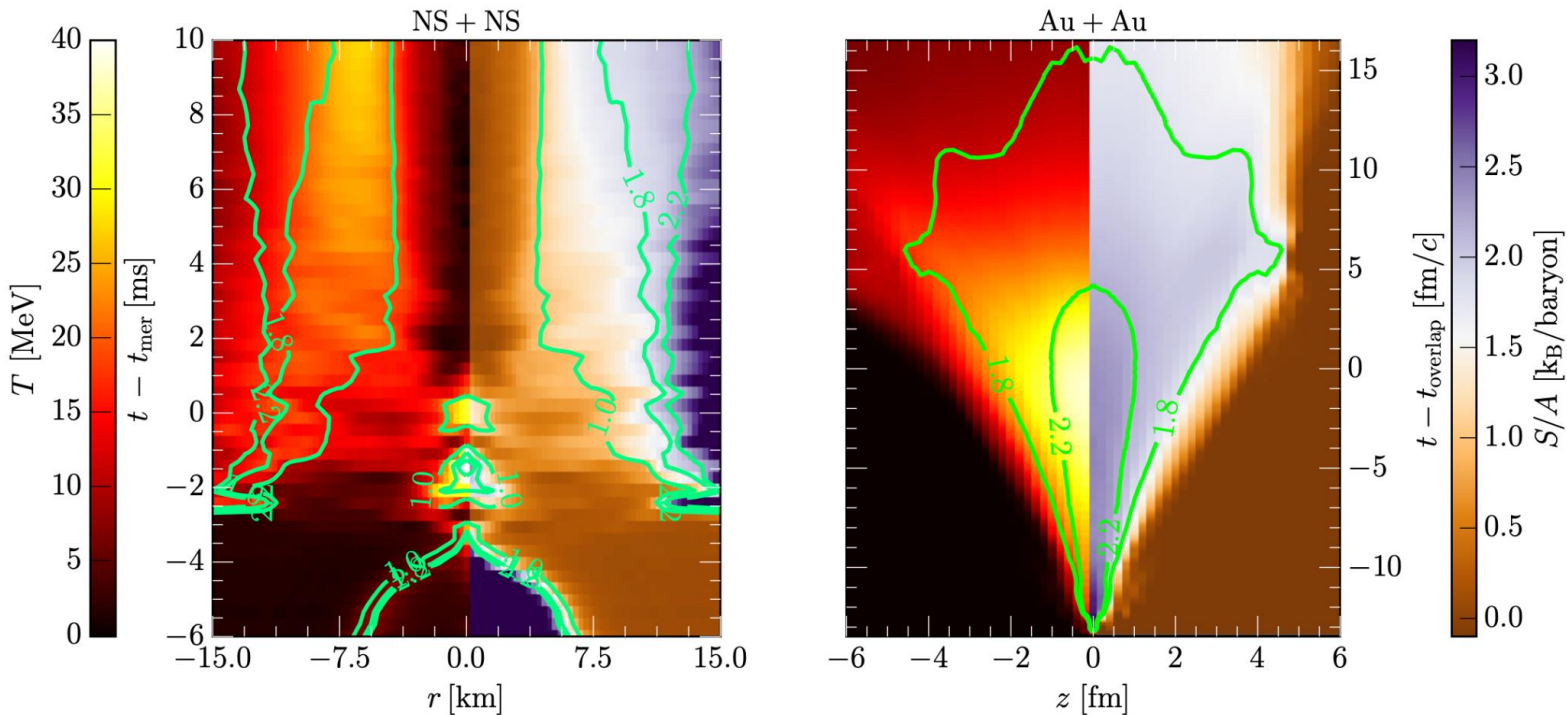
Colored lines mark density contours in units of n_{sat} . The snapshots refer to $t = -2, 3$ ms before and after merger for the BNS, respectively, and to $t = \pm 5$ fm/c before and after the full overlap for the HIC.

Most, AM, Steinheimer, Dexheimer, Hanauske, Rezzolla, Stoecker
e-Print: [2201.13150](https://arxiv.org/abs/2201.13150) [nucl-th]

HIC vs BNSM: comparison

Spacetime diagrams for the evolution of the temperature and entropy.

The green contours correspond to lines of constant entropy per baryon $S/A=1.8, 2.2$.



HIC:
The whole system
expands with approx.
constant entropy

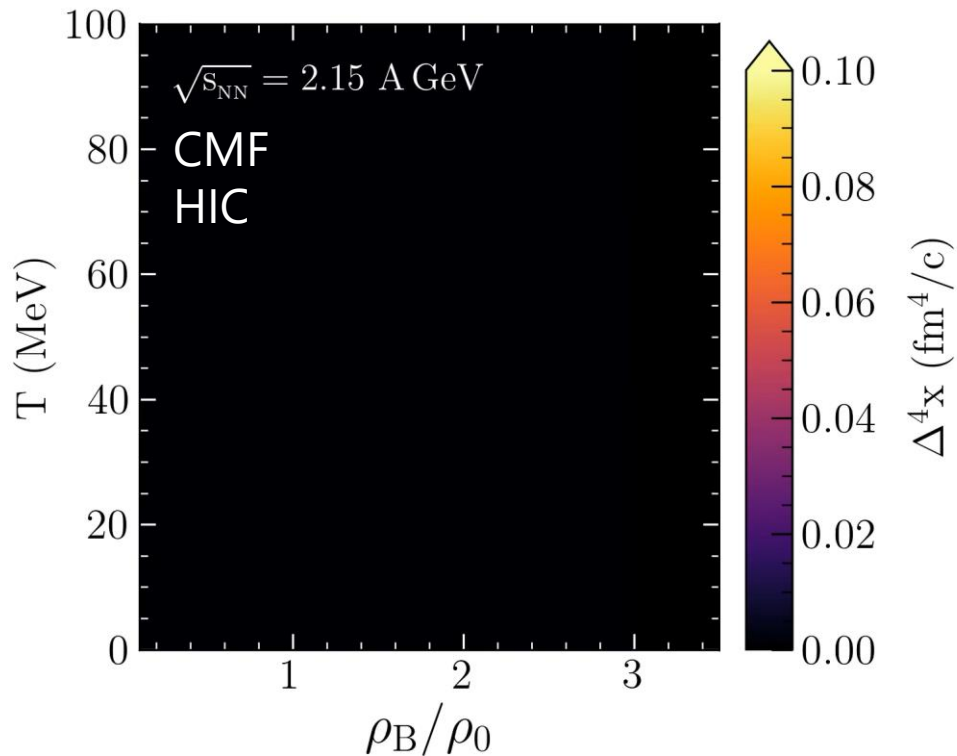
BNSM:
Entropy is localized
in a "ring" structure

Most, AM, Steinheimer, Dexheimer, Hanauske, Rezzolla, Stoecker
e-Print: [2201.13150](https://arxiv.org/abs/2201.13150) [nucl-th]

HIC:

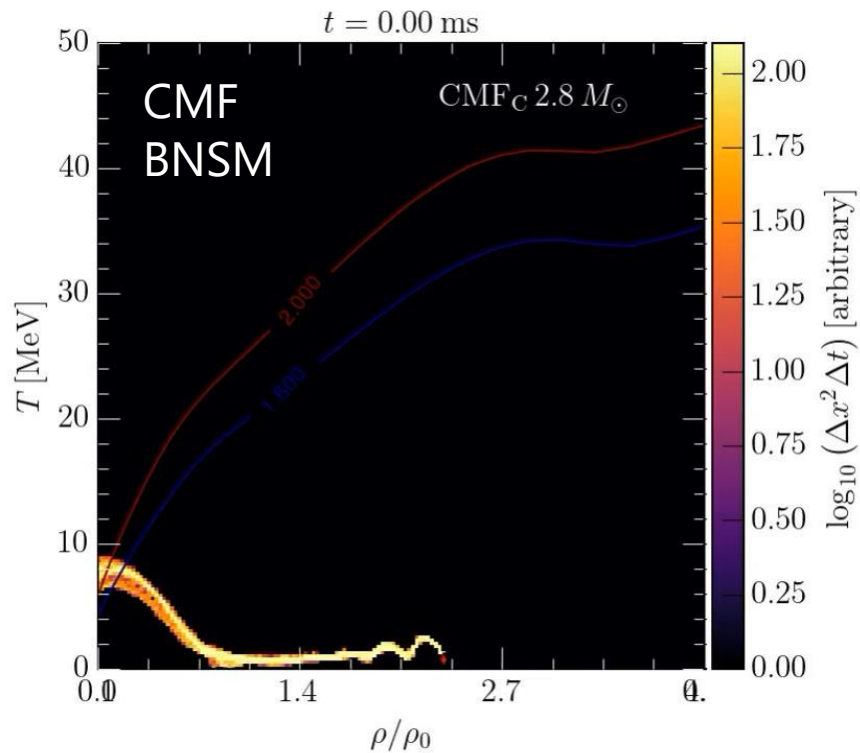
The whole system
expands with approx.
constant entropy

$$t = 0.16 \text{ fm}/c$$

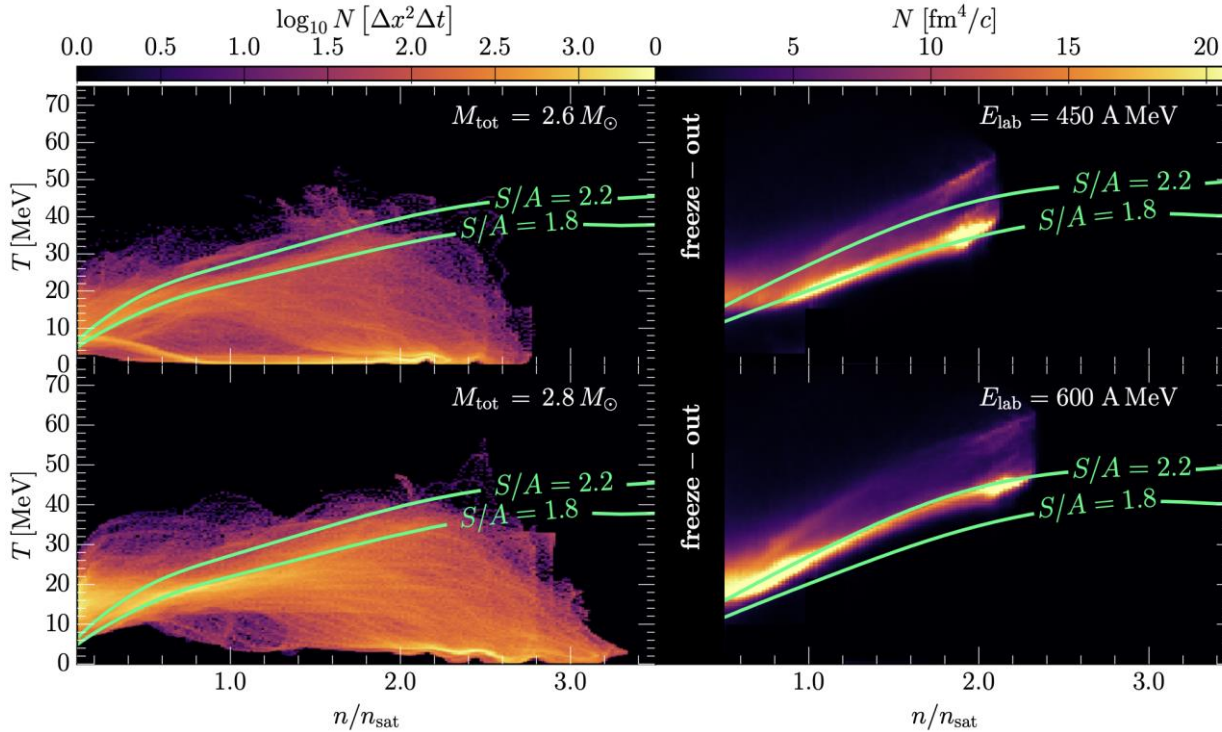


BNSM:

Entropy is localized
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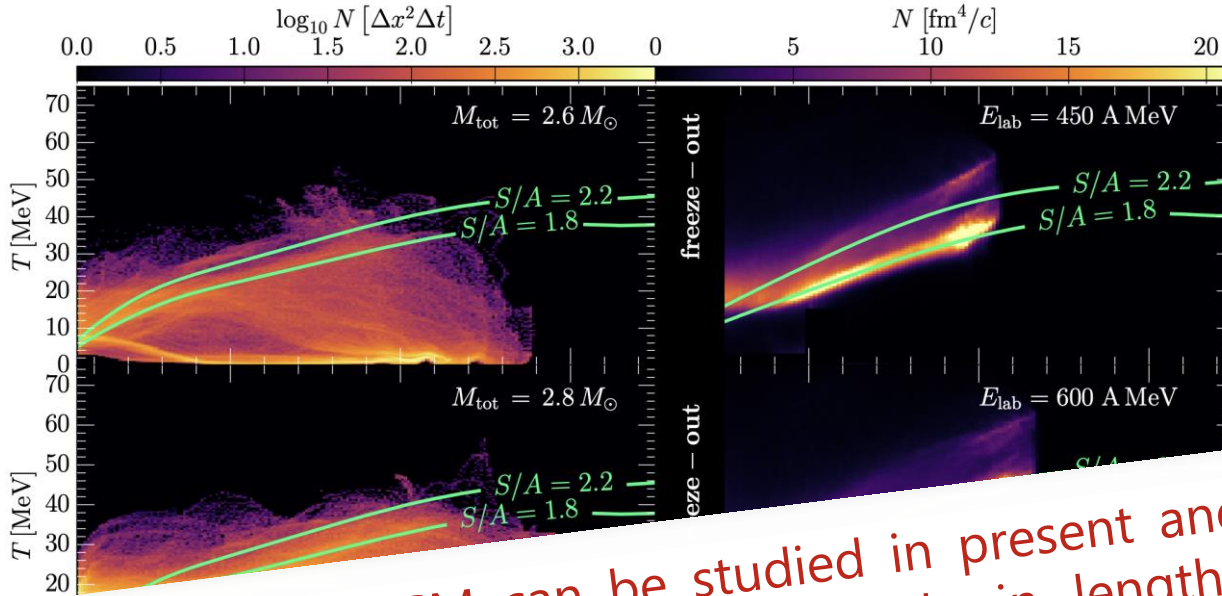


HIC vs BNSM: comparison



Regions of the QCD phase-diagram probed by BNS mergers and by HICs. The colorcode reports the number of cells N in the various spacetimes having a given value of temperature and density. The green lines show contours of constant entropy per baryon. Only cells with density above freeze-out, $n > 1/2 n_{\text{sat}}$, are shown for the HIC.

HIC vs BNSM: comparison

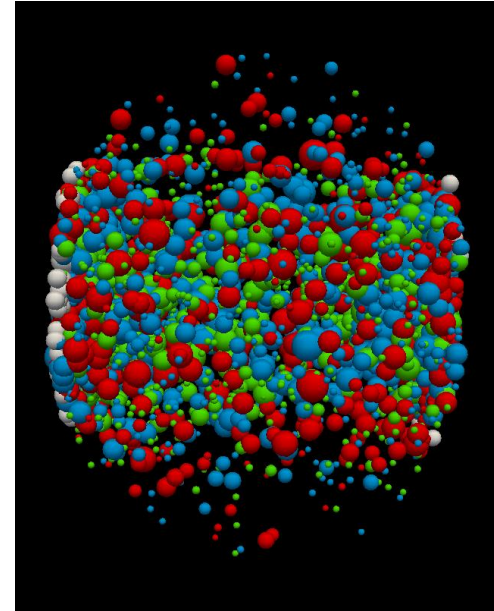
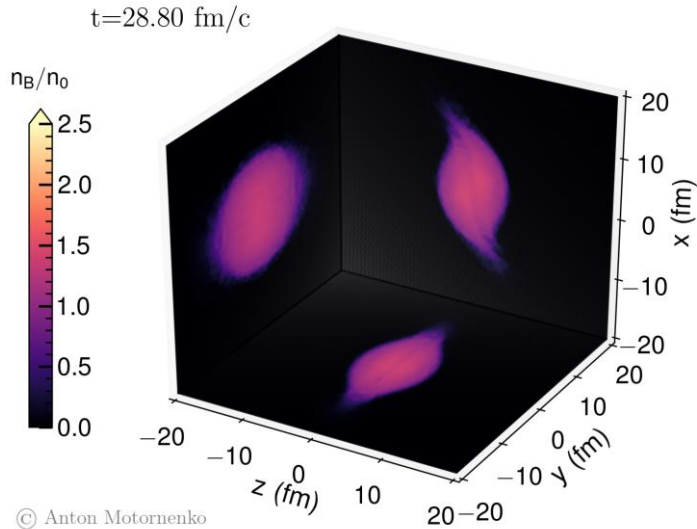


Physical conditions of BNSM can be studied in present and future HIC experiments, bridging 18 orders of magnitude in length scale, from microscopic ion collisions to macroscopic astrophysical compact objects.

... of the colorcode reports the number of cells N in the various ... and density. The green lines show contours of constant entropy per baryon. Only cells ... out, $n > 1/2 n_{\text{sat}}$, are shown for the HIC.

Predictions for experiments

How to relate Bulk matter evolution to microscopic picture? So a comparison with experiment can be done...



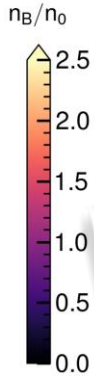
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Cooper-Frye at these low energies is problematic!

Predictions for experiments

How to relate Bulk matter evolution to microscopic picture? So a comparison with experiments

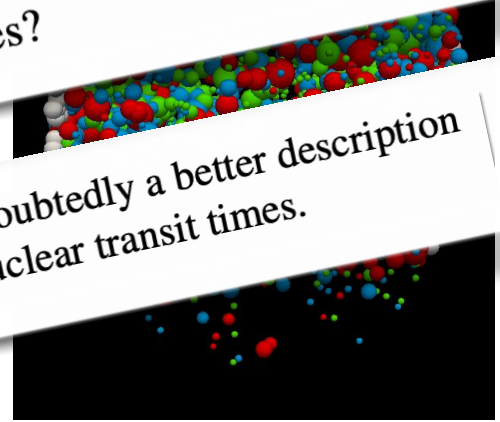
$t=28.80 \text{ fm}/c$



Bulletpoints from theory overview:
(see Joseph Kapusta talk on Monday)

- Is the standard model of viscous hydrodynamics coupled with an hadronic afterburner the correct one for lower beam energies?

- Transport theory with hadrons and mean fields is undoubtedly a better description at lower beam energies. Better able to handle longer nuclear transit times.



MADAI.us

Cooper-Frye at these low energies is problematic!

Predictions for experiments: QMD approach

Hamiltons equations of motion in a transport model (UrQMD) can be calculated as:

$$\dot{\mathbf{p}}_i = -\frac{\partial H}{\partial \mathbf{r}_i} = -\frac{\partial V(n_B)}{\partial n_B} \cdot \frac{\partial n_B(\mathbf{r}_i)}{\partial \mathbf{r}_i}$$

Density n_B is calculated by assuming that each particle can be treated as a Gaussian wave packet:

$$n_B(r_i) = \left(\frac{\alpha}{\pi}\right)^{3/2} \sum_{j, j \neq i} B_j \exp(-\alpha(\mathbf{r}_i - \mathbf{r}_j)^2)$$

The mean field potential energy per baryon can be related to a density dependent single particle energy:

$$U_i(n_B) = \frac{\partial(n_B \cdot V_i(n_B))}{\partial n_B}$$

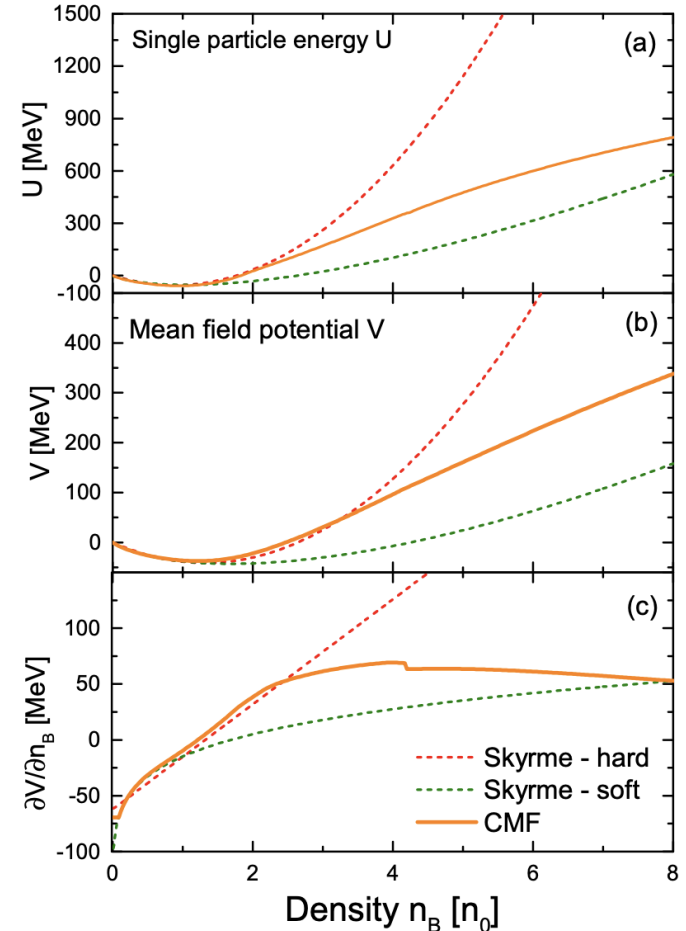
In the CMF model (or any other EOS) the single nucleon potential at $T = 0$, can be calculated from the self energy of the nucleons:

$$V_{CMF} = E_{\text{field}}/A = E_{CMF}/A - E_{FFG}/A,$$

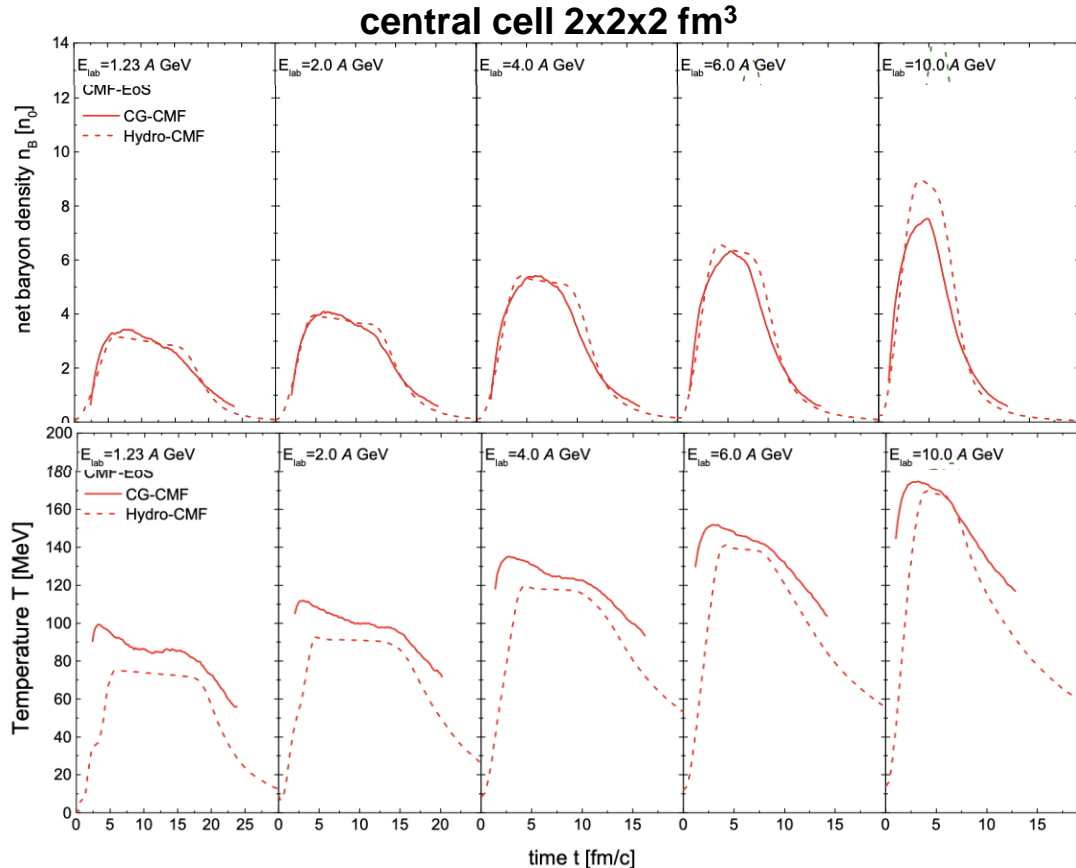
Predictions for experiments: QMD approach

CMF features:

1. A nuclear incompressibility compatible with experimental observations.
2. Stiff at super-saturation densities: explains astrophysical observations.
3. "Softens" at even higher densities due to the slow approach to the high density limit of a free gas quarks.



Comparing QMD approach and hydro: central cell



The bulk evolution of the density in this new description agrees well with a relativistic 1-fluid simulation with the CMF equation of state.

The initial compression depends dominantly on the underlying EOS and only marginally on the model used for the dynamical description.

The compression is reproduced and thus predictions for experiment can be done!

Supernova explosions: another application of CMF

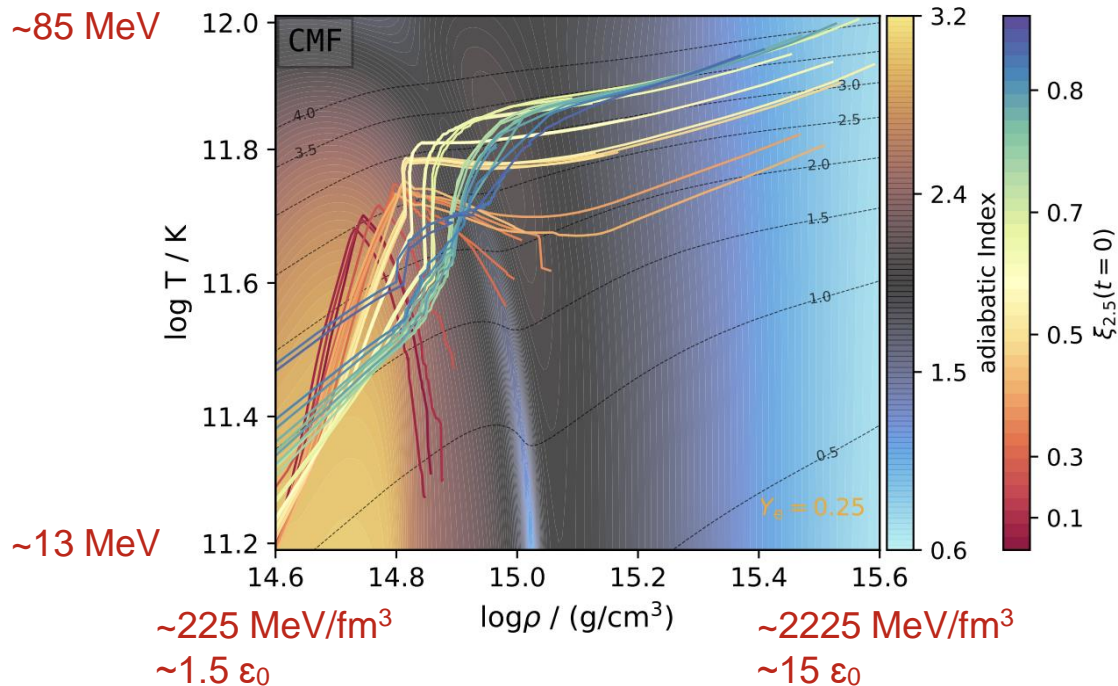


Figure 8. Phase diagram with trajectories of the central density and temperature (thick solid lines) of selected CMF models. The background displays the colour-coded adiabatic index at fixed electron fraction $Y_e = 0.25$ for the CMF EoS. The black dashed lines are isentropes for different entropy values (indicated as contour labels).

Jakobus, Müller, Heger, AM, Steinheimer,
and Stoecker,
e-Print: [2204.10397](https://arxiv.org/abs/2204.10397) [astro-ph.HE]

Supernova explosions: another application of CMF

~85 MeV

12.0

CMF

Bulletpoints from theory overview:
(see Joseph Kapusta talk on Monday)

0.8

- To describe the matter created at RHIC beam energies and below, knowledge is required of the equation of state as a function of T , μ_B , μ_Q , and μ_S to conserve energy, baryon number, electric charge, and strangeness. This is nontrivial when there is critical behavior in the phase diagram.
- Such an equation of state is also needed for modeling neutron star mergers and closely related to the cold dense matter comprising neutron stars.
..... and supernova!

~2225 MeV/fm³

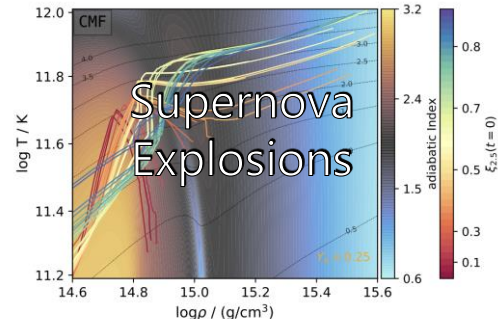
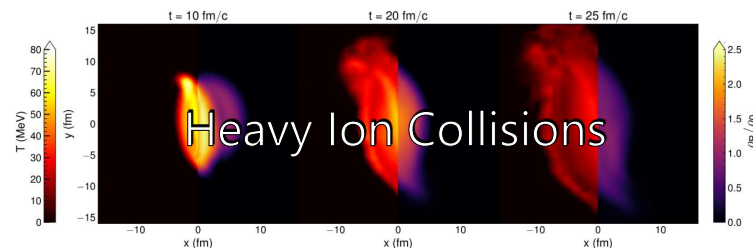
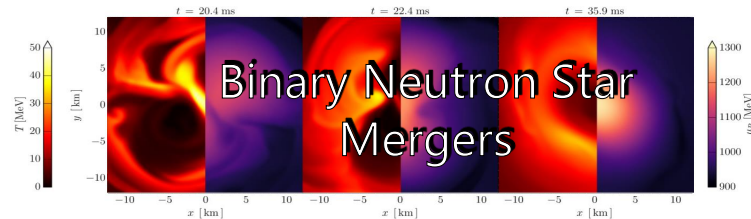
~15 ϵ_0

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Jakobus, Müller, Heger, AM, S
and Stoecker,
e-Print: [2204.10397](https://arxiv.org/abs/2204.10397) [astro-ph.HE]

Summary

- CMF + relativistic hydrodynamics = simulations of
- Astrophysical conditions can be probed by low energy nuclear collisions
- Predictions for laboratory experiments can be done by UrQMD with density dependent equation of state



Thank you for the attention!

Backup

Lattice QCD based qualitative phase diagram

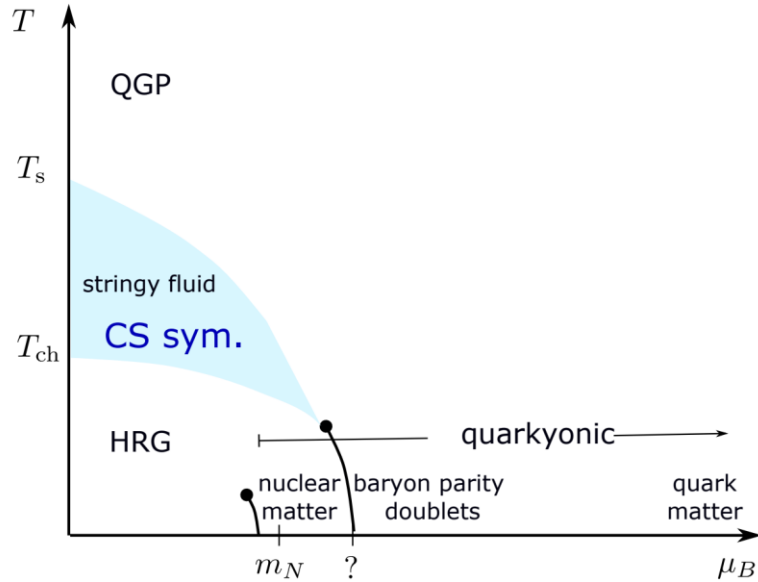
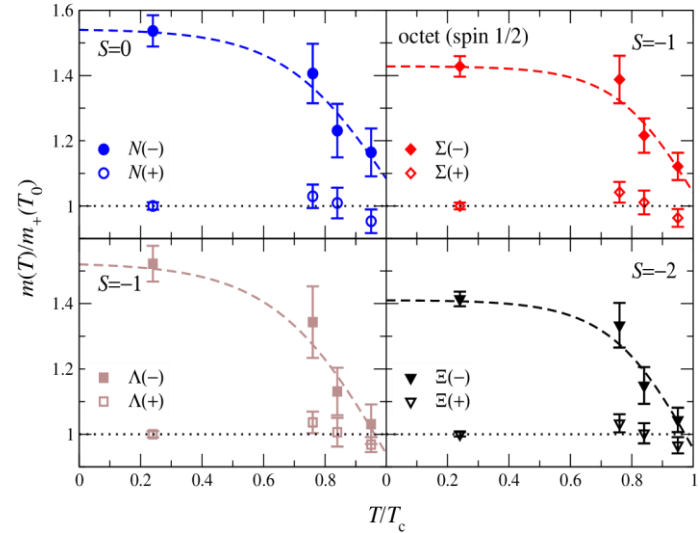


Figure 4. Qualitative sketch of a possible QCD phase diagram with a band of approximate chiral spin symmetry terminating at the critical end point of a non-analytic chiral phase transition.

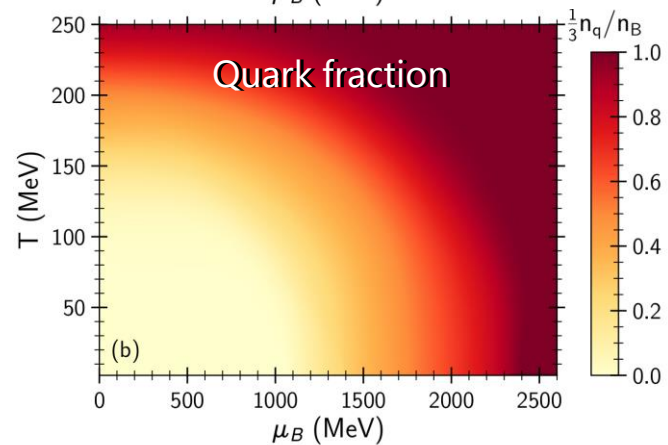
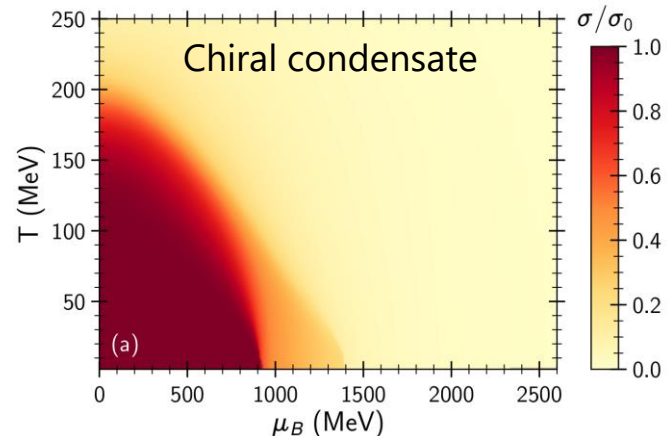
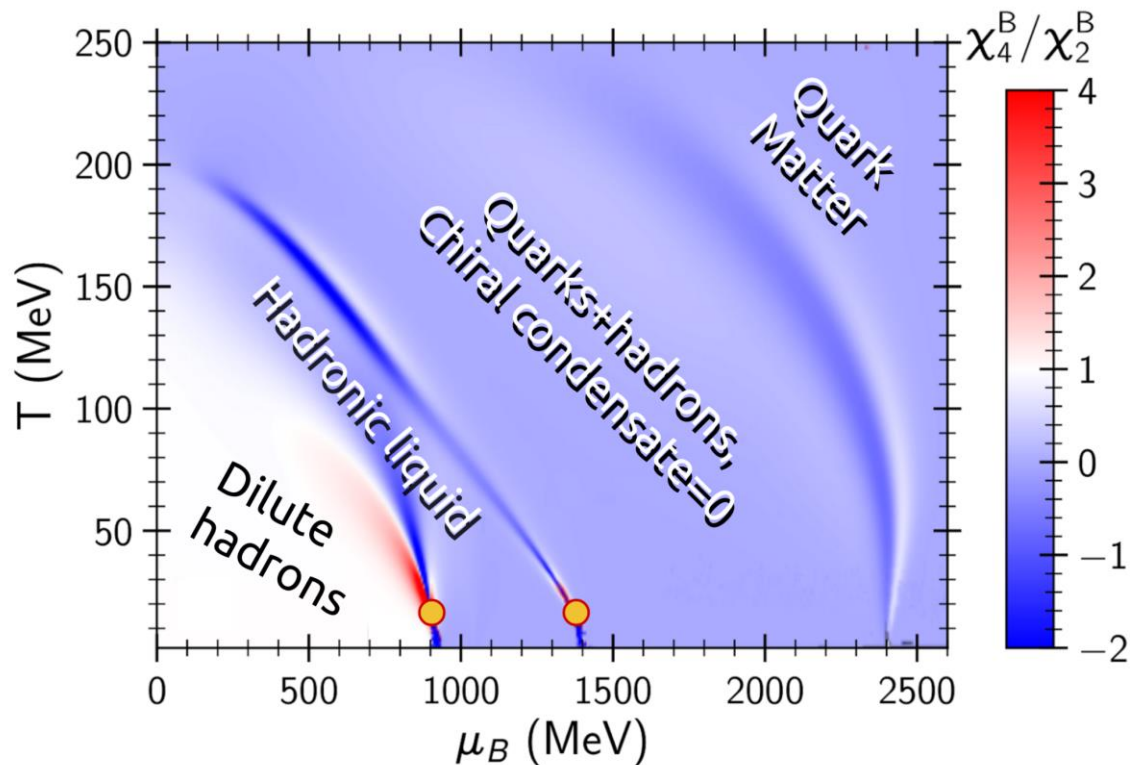
Glozman, Philipsen, Pisarski, e-Print: [2204.05083](https://arxiv.org/abs/2204.05083) [hep-ph]



Aarts et al., e-Print: [1710.08294](https://arxiv.org/abs/1710.08294) [hep-lat]

The CMF phase diagram

AM, Steinheimer, Vovchenko, Schramm, Stoecker, *Phys. Rev. C* 101, no.3, 034904 (2020)



The CMF model

$$\Omega = \Omega_q + \Omega_{\bar{q}} + \Omega_h + \Omega_{\bar{h}} - (U_{sc} + U_{vec} + U_{Pol})$$

Baryon octet:

$$\begin{aligned} \mathcal{L}_B &= \sum_b (\bar{B}_b i \not{\partial} B_b) + \sum_b (\bar{B}_b m_b^* B_b) \\ &+ \sum_b [\bar{B}_b \gamma_\mu (g_{\omega b} \omega^\mu + g_{\rho b} \rho^\mu + g_{\phi b} \phi^\mu) B_b] \\ \mu_b^* &= \mu_b - g_{\omega b} \omega - g_{\phi b} \phi - g_{\rho b} \rho \\ m_{b\pm}^* &= \sqrt{[(g_{\sigma b}^{(1)} \sigma + g_{\zeta b}^{(1)} \zeta)^2 + (m_0 + n_s m_s)^2]} \pm g_{\sigma b}^{(2)} \sigma \end{aligned}$$

Repulsive vector mean fields:

$$\begin{aligned} U_{vec} &= -\frac{1}{2} (m_\omega^2 \omega^2 + m_\rho^2 \rho^2 + m_\phi^2 \phi^2) \\ &- g_4 \left[\omega^4 + 6\beta_2 \omega^2 \rho^2 + \rho^4 + \frac{1}{2} \phi^4 \left(\frac{Z_\phi}{Z_\omega} \right)^2 \right. \\ &\left. + 3(\rho^2 + \omega^2) \left(\frac{Z_\phi}{Z_\omega} \right) \phi^2 \right]. \end{aligned}$$

Attractive scalar fields:

$$\begin{aligned} U_{sc} &= V_0 - \frac{1}{2} k_0 I_2 + k_1 I_2^2 - k_2 I_4 + k_6 I_6 + k_4 \ln \frac{\sigma^2 \zeta}{\sigma_0^2 \zeta_0} - U_{sb} \\ I_2 &= (\sigma^2 + \zeta^2), \quad I_4 = -(\sigma^4/2 + \zeta^4), \quad I_6 = (\sigma^6 + 4\zeta^6) \\ U_{sb} &= m_\pi^2 f_\pi \sigma + \left(\sqrt{2} m_K^2 f_K - \frac{1}{\sqrt{2}} m_\pi^2 f_\pi \right) \zeta \end{aligned}$$

Hadrons:

$$\begin{aligned} \rho_i &= \frac{\rho_i^{\text{id}}(T, \mu_i^* - v_i P)}{1 + \sum_{j \in \text{HRG}} v_j \rho_j^{\text{id}}(T, \mu_j^* - v_j P)} \\ \mu_j^{\text{eff}} &= \mu_j^* - v_j P, \end{aligned}$$

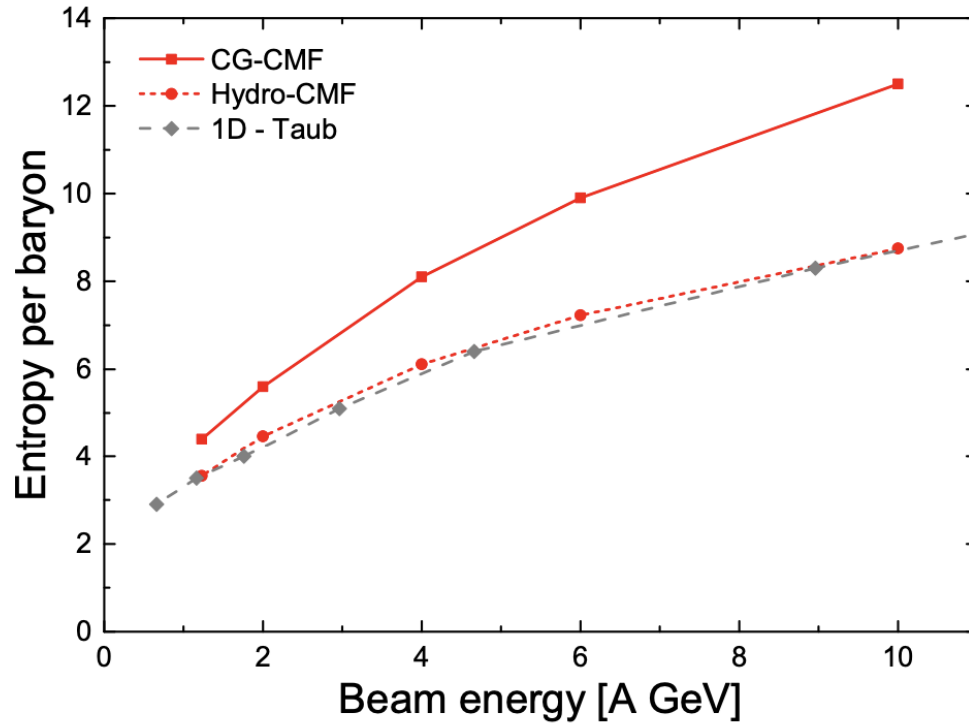
u,d,s quarks:

$$\begin{aligned} \Omega_q &= -VT \sum_{q_i \in Q} \frac{d_{q_i}}{(2\pi)^3} \int d^3k \frac{1}{N_c} \ln [1 + 3\Phi e^{-(E_{q_i}^* - \mu_{q_i}^*)/T} \\ &+ 3\bar{\Phi} e^{-2(E_{q_i}^* - \mu_{q_i}^*)/T} + e^{-3(E_{q_i}^* - \mu_{q_i}^*)/T}], \\ m_{u,d}^* &= -g_{u,d} \sigma + \delta m_{u,d} + m_{0u,d} \\ m_s^* &= -g_s \zeta + \delta m_s + m_{0s}. \end{aligned}$$

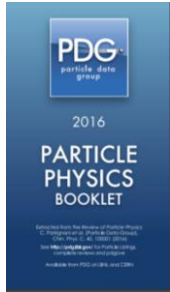
Polyakov loop:

$$\begin{aligned} U_{Pol}(\Phi, \bar{\Phi}, T) &= -\frac{1}{2} a(T) \Phi \bar{\Phi} + b(T) \ln [1 - 6\Phi \bar{\Phi} \\ &+ 4(\Phi^3 + \bar{\Phi}^3) - 3(\Phi \bar{\Phi})^2], \\ a(T) &= a_0 T^4 + a_1 T_0 T^3 + a_2 T_0^2 T^2, \\ b(T) &= b_3 T_0^4. \end{aligned}$$

Entropy production: hydro vs QMD

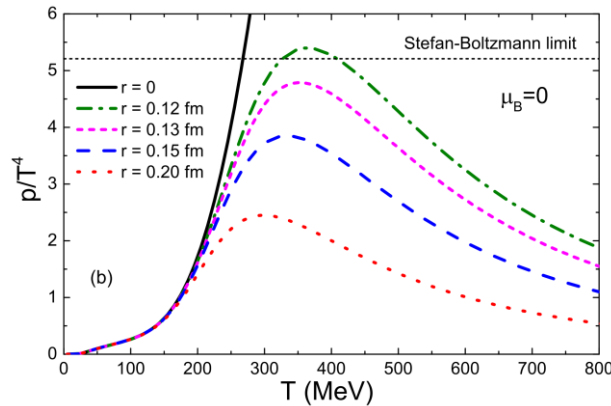


Hadronic part: QCD matter at low densities



$$\rho_i = \frac{\rho_i^{\text{id}}(T, \mu_i^* - v_i p)}{1 + \sum_j v_j \rho_j^{\text{id}}(T, \mu_j^* - v_j p)}$$
$$\varepsilon_i = \frac{\varepsilon_i^{\text{id}}(T, \mu_i^* - v_i p)}{1 + \sum_j v_j \rho_j^{\text{id}}(T, \mu_j^* - v_j p)}$$

PDG list of known hadrons is included with Excluded Volume interactions.
EV suppress hadrons at high energy densities.



EV of baryons: 1 fm^3
EV of mesons: $1/8 \text{ fm}^3$

EV triggers the switch between hadron and quark degrees of freedom: **hadron** pressure is **suppressed** as function of T and μ_B — quarks are dominant at high densities.

V. Vovchenko, D. Anchishkin, M. Gorenstein, 1412.5478

SU(3)_f octet and parity doubling

We include all states of the **SU(3)_f** baryon octet:

$$\begin{pmatrix} \frac{\Sigma^0}{\sqrt{2}} + \frac{\Lambda}{\sqrt{6}} & \Sigma^+ & p \\ \Sigma^- & -\frac{\Sigma^0}{\sqrt{2}} + \frac{\Lambda}{\sqrt{6}} & n \\ \Xi^- & \Xi^0 & -2\frac{\Lambda}{\sqrt{6}} \end{pmatrix}$$

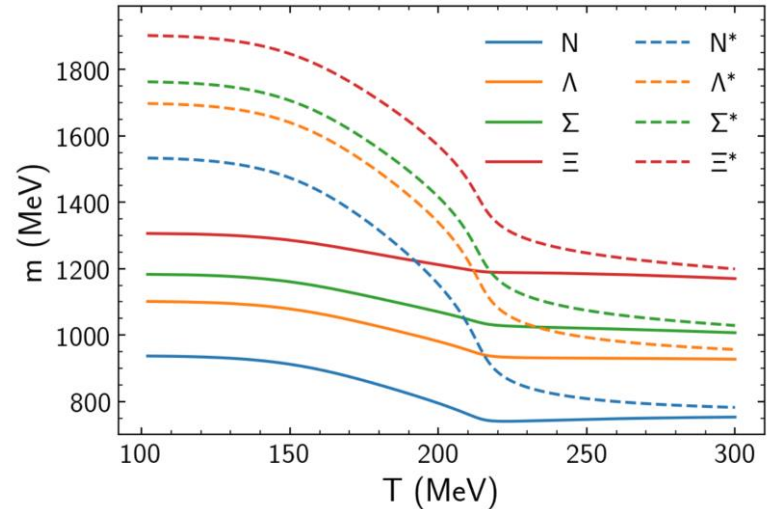
together with their **parity partners** (G. Aarts et al., 1710.08294), i.e. states with the same quantum numbers but **opposite parity**. Those interact within SU(3)_f σ model:

$$\begin{aligned} \mathcal{L}_B = & \sum_i (\bar{B}_i i \not{\partial} B_i) + \sum_i (\bar{B}_i m_i^* B_i) \\ & + \sum_i (\bar{B}_i \gamma_\mu (g_{\omega i} \omega^\mu + g_{\rho i} \rho^\mu + g_{\phi i} \phi^\mu) B_i) \end{aligned}$$

with effective masses generated by chiral fields σ and ζ :

$$m_{i\pm}^* = \sqrt{[(g_{\sigma i}^{(1)} \sigma + g_{\zeta i}^{(1)} \zeta)^2 + (m_0 + n_s m_s)^2]} \pm g_{\sigma i}^{(2)} \sigma \pm g_{\zeta i}^{(2)} \zeta$$

‘+’ stands for positive and ‘-’ for negative parity states



Including Quarks: PNJL-like approach

Quarks are included within **PNJL** inspired approach:

$$\Omega_q = -VT \sum_{i \in Q} \frac{d_i}{(2\pi)^3} \int d^3k \frac{1}{N_c} \left[\ln \left(1 + 3\Phi e^{-(E_i^* - \mu_i^*)/T} + 3\bar{\Phi} e^{-2(E_i^* - \mu_i^*)/T} + e^{-3(E_i^* - \mu_i^*)/T} \right) \right. \\ \left. + \ln \left(1 + 3\bar{\Phi} e^{-(E_i^* + \mu_i^*)/T} + 3\Phi e^{-2(E_i^* + \mu_i^*)/T} + e^{-3(E_i^* + \mu_i^*)/T} \right) \right]$$

Polyakov loop Φ — is deconfinement order parameter:

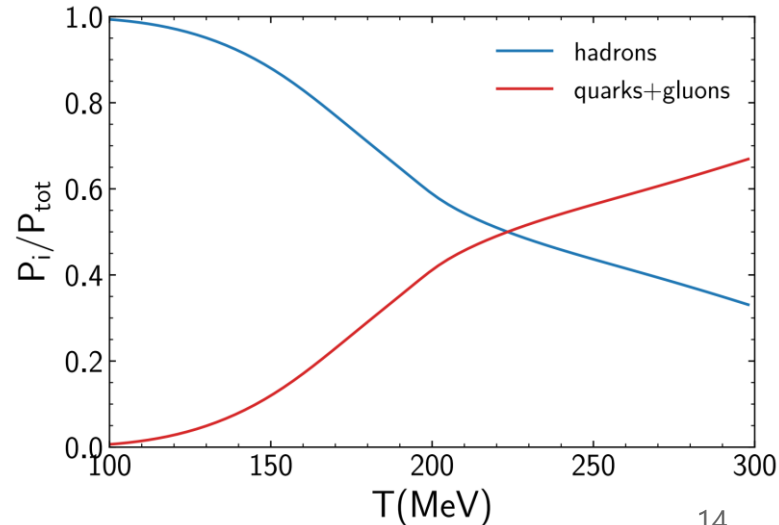
$\Phi=0$ — no quarks, **$\Phi=1$** — free quarks.

Φ is controlled by the **potential $U(\Phi)$** :

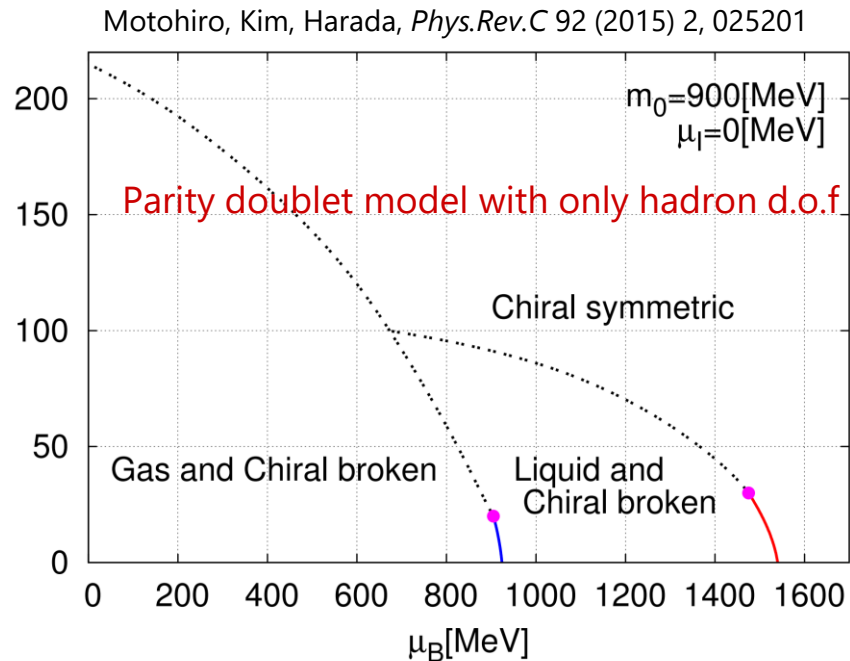
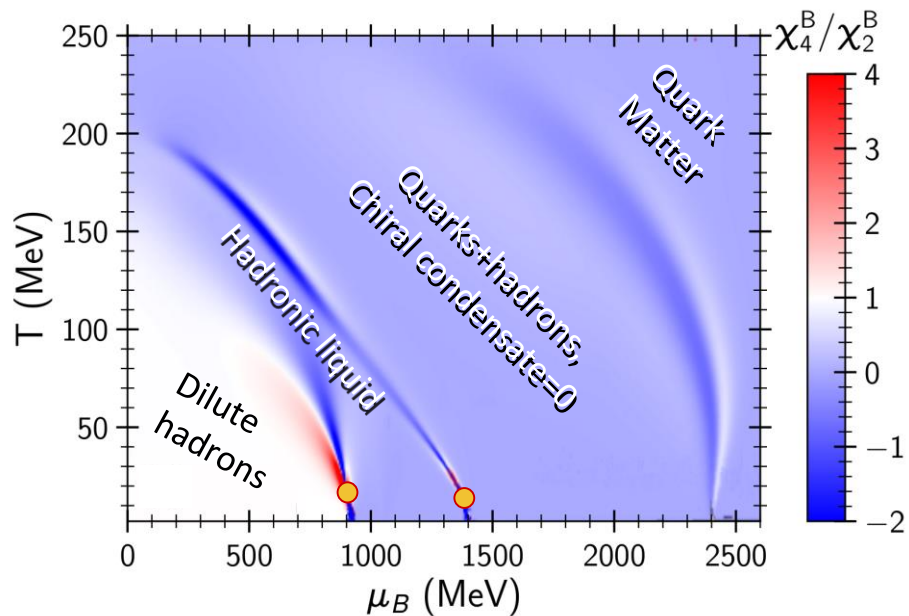
$$U = -\frac{1}{2}(a_0 T^4 + a_1 T_0 T^3 + a_2 T_0^2 T^2)\Phi\Phi^* \\ + b_3 T_0^4 \log[1 - 6\Phi\Phi^* + 4(\Phi^3 + \Phi^{*3}) - 3(\Phi\Phi^*)^2]$$

Fukushima, hep-ph/0310121

Roessner, Ratti, Weise, hep-ph/0609281

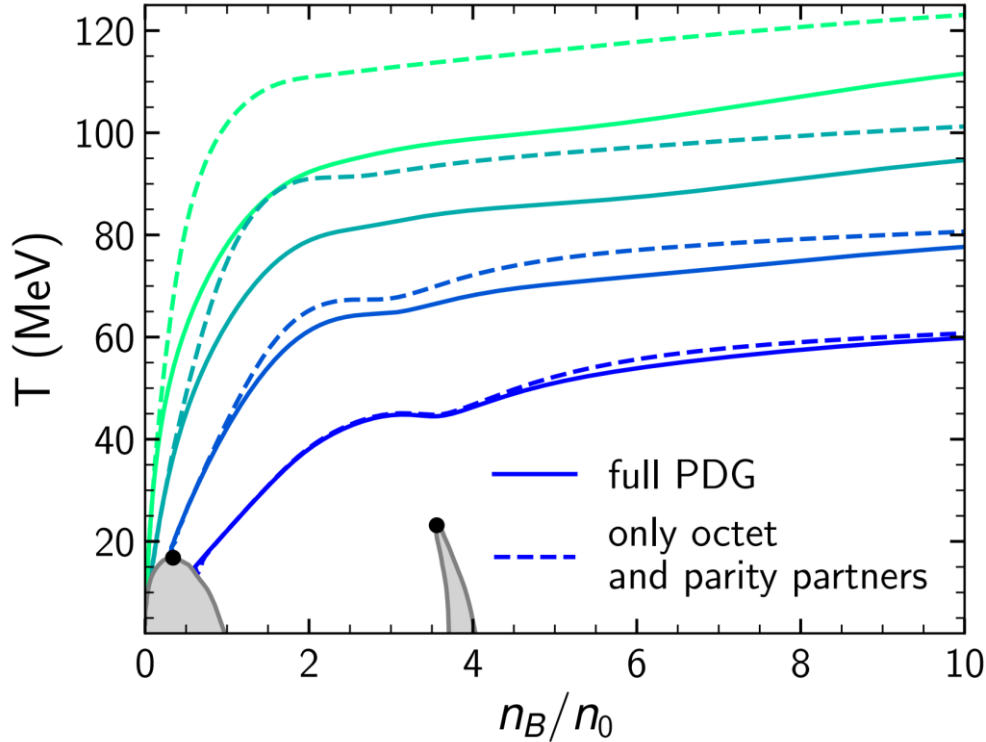


The CMF phase diagram



The phase transitions are only driven by **hadrons**. **Deconfinement is always smooth**.

Importance of HRG list



CMF isentropic trajectories, lines of constant entropy per baryon S/A with:

- the full particle list (solid);
- only the stable baryons+quarks (dashed), mesons and resonances are neglected.

Note the increase of temperature for the isentropes where the mesons and resonances are neglected.