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HEAVY-FLAVOR ANISOTROPIC FLOW AT RHIC AND LHC ENERGIES WITHIN A FULL TRANSPORT APPROACH

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Lucia Oliva



Università
di Catania

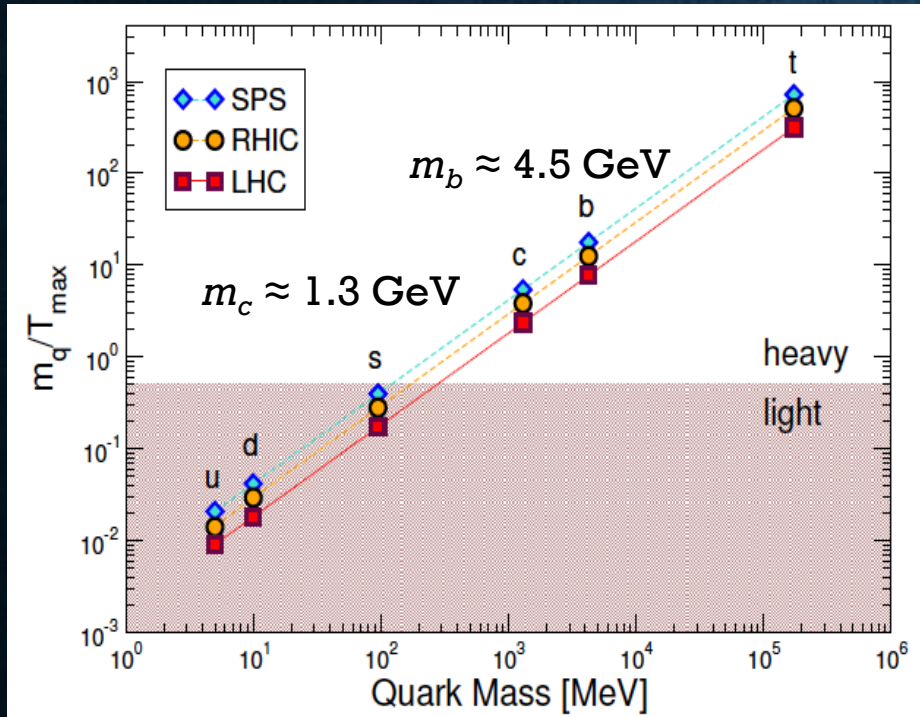
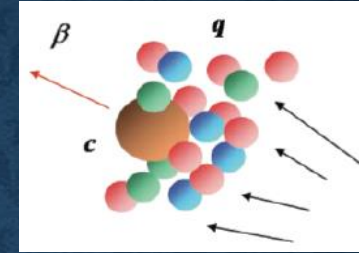


Istituto Nazionale di Fisica Nucleare
Sezione di Catania



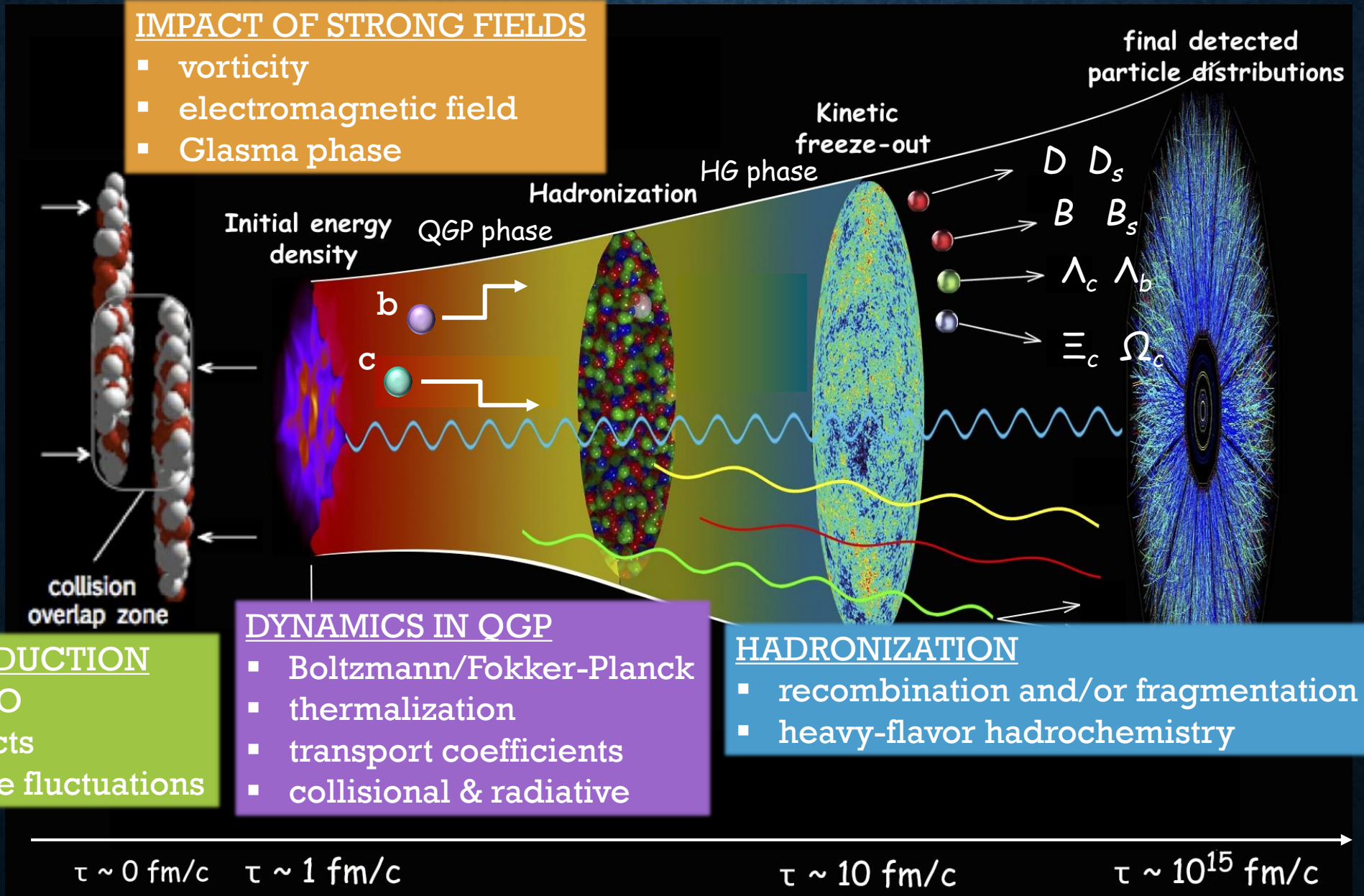
HEAVY QUARKS (HQ) IN QGP: BASIC SCALES

few Heavy-Flavor (HF) quarks and antiquarks
CHARM and **BOTTOM**
 produced in relativistic heavy-ion collisions



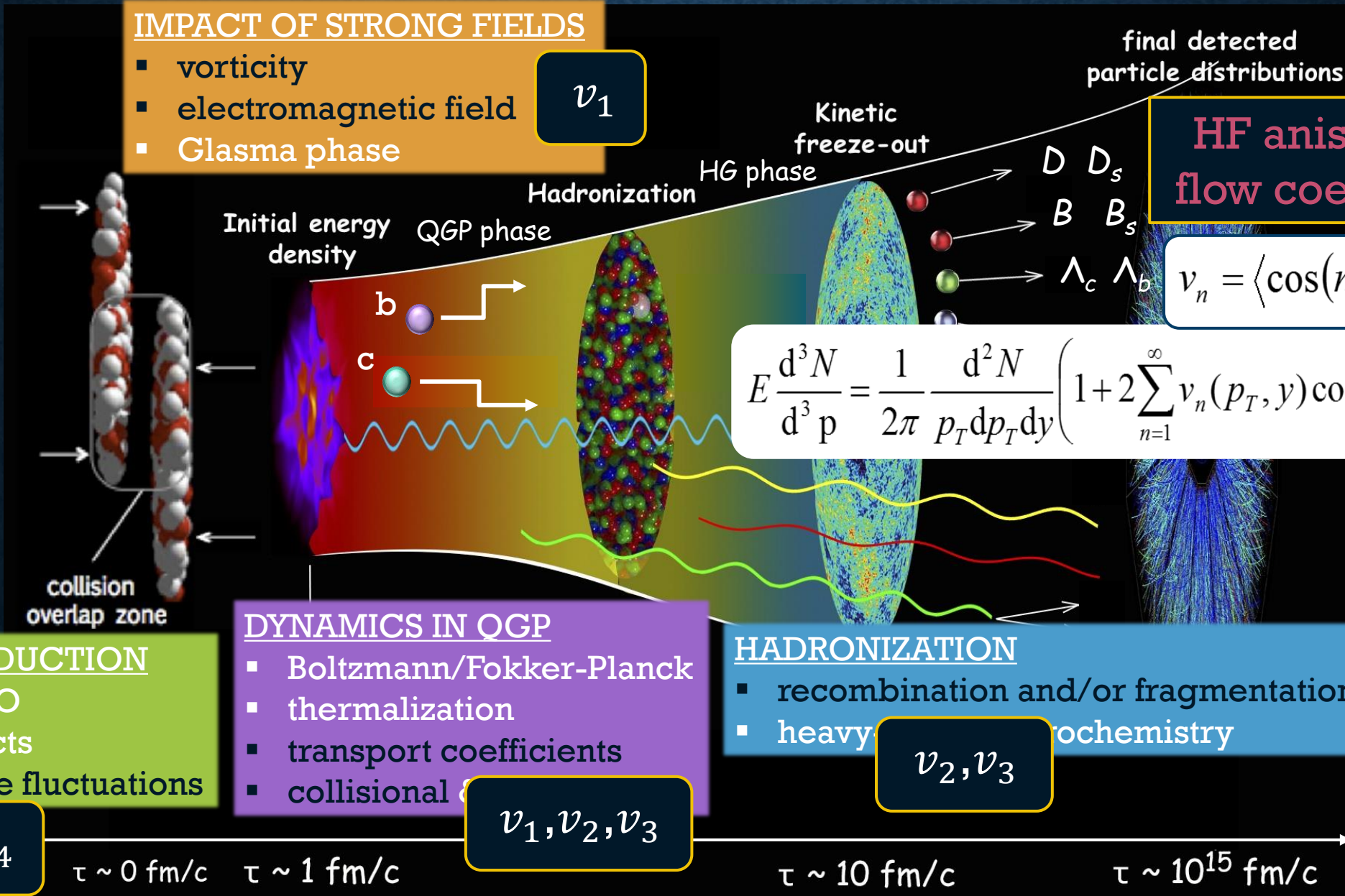
- $m_{\text{HQ}} \gg \Lambda_{\text{QCD}} \rightarrow$ HQ produced in pQCD initial hard scatterings
 - $m_{\text{HQ}} \gg T_{\text{HICs}} \rightarrow$ negligible thermal production of HQs
 HQ production points symmetric in the forward-backward hemispheres
 - $\tau_0^{\text{HQ}} < 0.08 \text{ fm/c} \ll \tau_0^{\text{QGP}} \rightarrow$ HQ production much earlier than QGP formation
 - $\tau_{\text{th}}^{\text{HQ}} \approx \tau^{\text{QGP}} \approx 5\text{-}10 \text{ fm/c} \gg \tau_{\text{th}}^{\text{QGP}} \rightarrow$ HQ thermalization time comparable to QGP life
- HQ final states keep a better memory of both initial stage and QGP evolution
- $q < m_{\text{HQ}}, p_{\text{HQ}}; m_{\text{HQ}} \ll gT_{\text{HICs}}$ (b or low momentum c) \rightarrow Brownian motion of HQs in QGP

HEAVY FLAVORS IN RELATIVISTIC HICS



Modified from picture of Chun Shen (McGill University, Montreal QC, Canada)

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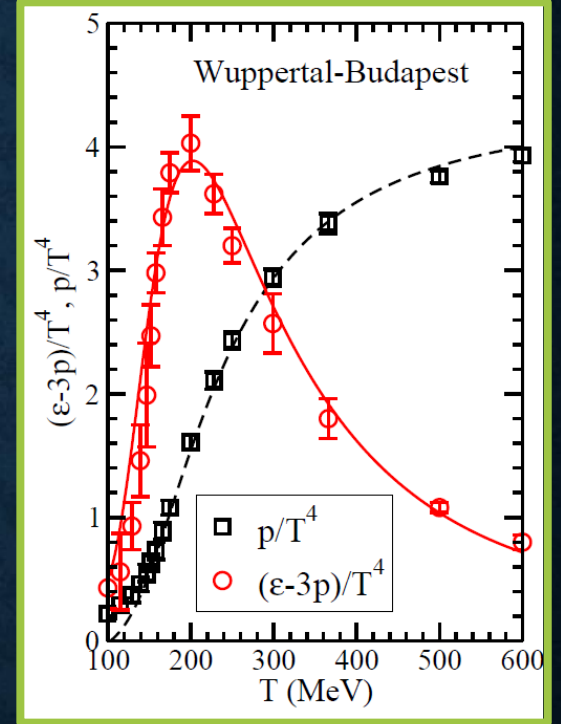
FULL BOLTZMANN TRANSPORT APPROACH

BULK EVOLUTION

$$p^\mu \partial_\mu f_q(x, p) + m(x) \partial_\mu^x m(x) \partial_p^\mu f_q(x, p) = C[f_q, f_g]$$

$$p^\mu \partial_\mu f_g(x, p) + m(x) \partial_\mu^x m(x) \partial_p^\mu f_g(x, p) = C[f_q, f_g]$$

Boltzmann transport equivalent to viscous hydro at $\eta/s \approx 0.1$



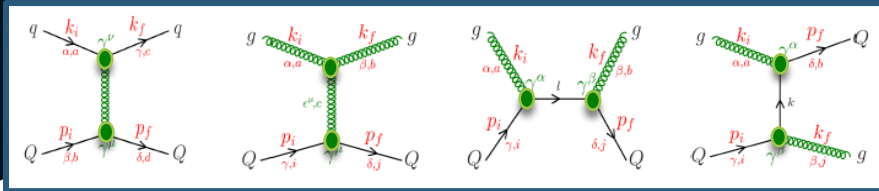
Free-streaming

Field interaction
 $\epsilon - 3p \neq 0$

collision kernel gauged to some $\eta/s \neq 0$
M. Ruggieri et al., Phys. Rev. C 89, 054914 (2014)

HQ EVOLUTION

$$p^\mu \partial_\mu f_Q(x, p) = C[f_q, f_g, f_Q](x, p)$$



$$C[f_Q] = \frac{1}{2E_1} \int \frac{d^3 p_2}{2E_2 (2\pi)^3} \int \frac{d^3 p'_1}{2E_1' (2\pi)^3} \times [f_Q(p'_1) f_{q,g}(p_2) - f_Q(p_1) f_{q,g}(p_2)] \times |\mathcal{M}_{(q,g)+Q}(p_1 p_2 \rightarrow p'_1 p'_2)|^2 \times (2\pi)^4 \delta^4(p_1 + p_2 - p'_1 - p'_2)$$

Scardina et al., Phys. Rev. C 96, 044905 (2017)

Non perturbative dynamics:
 \mathcal{M} scattering matrices ($q, g \rightarrow Q$)
evaluated by Quasi-Particle Model
fit to **lQCD thermodynamics**

S. Plumari et al., Phys. Rev. D 84, 094004 (2011)

$$m_g^2(T) = \frac{2N_c}{N_c^2 - 1} g^2(T) T^2$$

$$m_q^2(T) = \frac{1}{N_c} g^2(T) T^2$$

$$g^2(T) = \frac{48\pi^2}{(11N_c - 2N_f) \ln \left[\lambda \left(\frac{T}{T_c} - \frac{T_s}{T_c} \right) \right]^2}$$

extension of the QPM
(e.g., momentum dependence)

talk of M. L. SAMBATARO

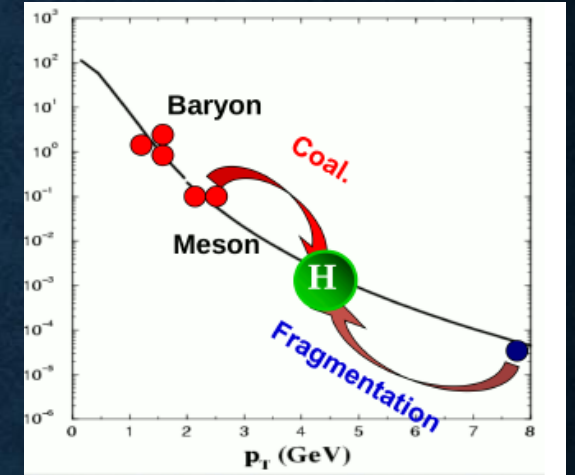
FULL BOLTZMANN TRANSPORT APPROACH

BULK EVOLUTION

$$p^\mu \partial_\mu f_q(x, p) + m(x) \partial_\mu^x m(x) \partial_p^\mu f_q(x, p) = C[f_q, f_g]$$

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M. Ruggieri et al., Phys. Rev. C 89, 054914 (2014)

HQ EVOLUTION

$$p^\mu \partial_\mu f_Q(x, p) = C[f_q, f_g, f_Q](x, p)$$

Hybrid hadronization scheme for heavy quarks

COALESCENCE + FRAGMENTATION

$$\frac{dN_{Hadron}}{d^2 p_T} = g_H \int \prod_{i=1}^n p_i \cdot d\sigma_i \frac{d^3 p_i}{(2\pi)^3} f_q(x_i, p_i) f_w(x_1, \dots, x_n; p_1, \dots, p_n) \delta(p_T - \sum_i p_{iT})$$

$$\frac{dN_h}{d^2 p_h} = \sum_f \int dz \frac{dN_f}{d^2 p_f} D_{f \rightarrow h}(z)$$

F. Scardina et al., Phys. Rev. C 96, 044905 (2017)

S. Plumari, V. Minissale et al., Eur. Phys. J. C 78, 348 (2018)

Remarkable impact of coalescence for the description of experimental data (e.g., R_{AA} , v_2 , v_3 for D mesons, charmed baryon/meson enhancement in pp)

talk of V. MINISSALE

INTENSE FIELDS AND HEAVY FLAVOR TRANSPORT

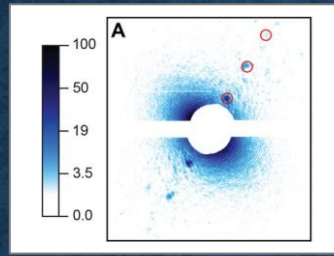
✓ HUGE ANGULAR MOMENTUM GENERATING A STRONG VORTICITY



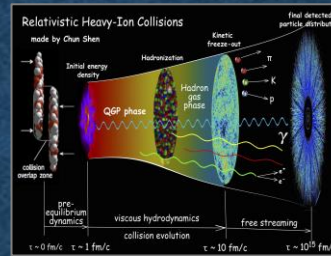
tornado cores
 $\sim 10^{-1} \text{ s}^{-1}$



Jupiter's spot
 $\sim 10^{-4} \text{ s}^{-1}$



He nanodroplets
 $\sim 10^7 \text{ s}^{-1}$



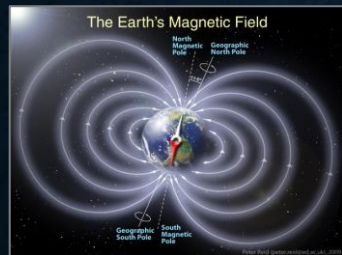
urHICs
 $\sim 10^{22} - 10^{23} \text{ s}^{-1}$

vorticity ω

since 2017

impact on HQ transport coefficients and D meson directed flow

✓ INTENSE ELECTROMAGNETIC FIELDS



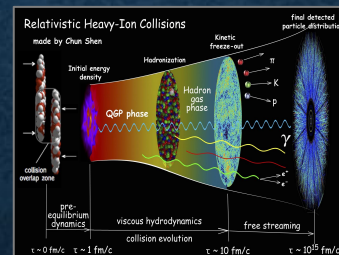
Earth's field
 $\sim 1 \text{ G}$



laboratory
 $\sim 10^6 \text{ G}$



magnetars
 $\sim 10^{14} - 10^{15} \text{ G}$



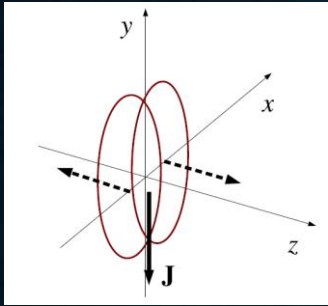
urHICs
 $\sim 10^{18} - 10^{19} \text{ G}$

magnetic field B

since 2016

impact on D meson directed flow

THE VORTICAL QUARK-GLUON PLASMA



- Huge **orbital angular momentum** of the colliding system
- in ultra-relativistic HICs $J \approx 10^5 - 10^6 \hbar$
 - dominated by the y component perpendicular to the reaction plane
 - **partly transferred to the plasma**

P. Bozek and I. Wyskiel,
Phys. Rev. C 81, 054902 (2010)



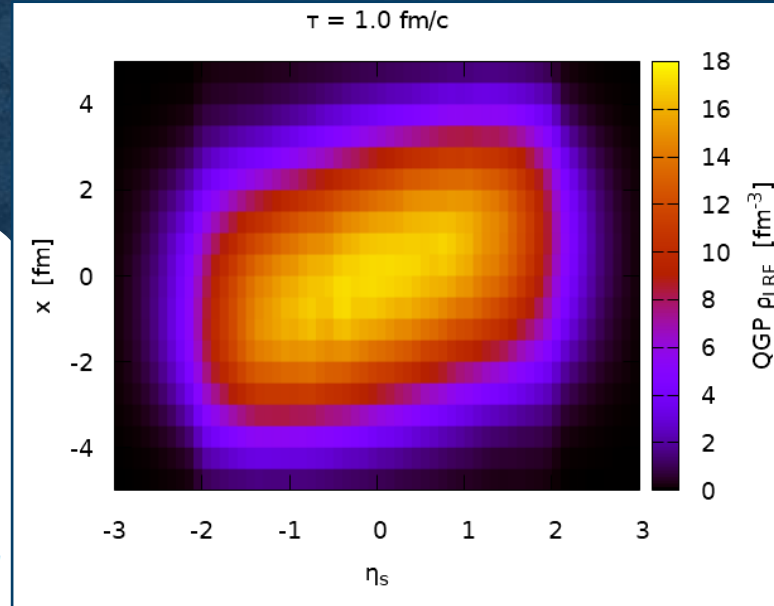
asymmetry in local participant density from forward and backward going nuclei

$$\rho(x_{\perp}, \eta_s) = \rho_0 \frac{W(x_{\perp}, \eta_s)}{W(0, 0)} \exp \left[-\frac{(|\eta_s| - \eta_{s0})^2}{2\sigma_{\eta}^2} \theta(|\eta_s| - \eta_{s0}) \right]$$

$$W(x_{\perp}, \eta_s) = 2(N_A(x_{\perp})f_-(\eta_s) + N_B(x_{\perp})f_+(\eta_s))$$

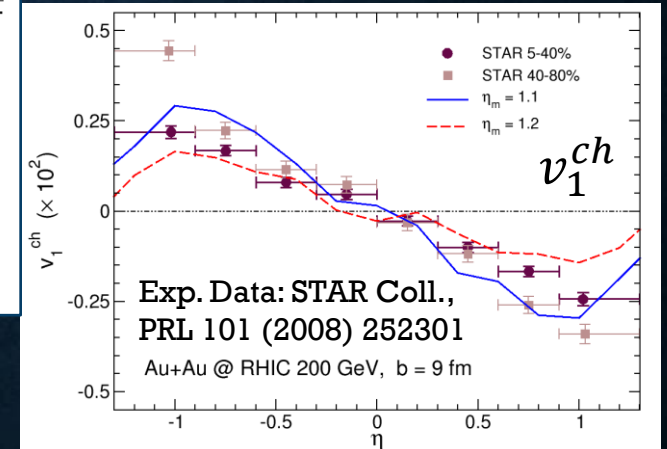
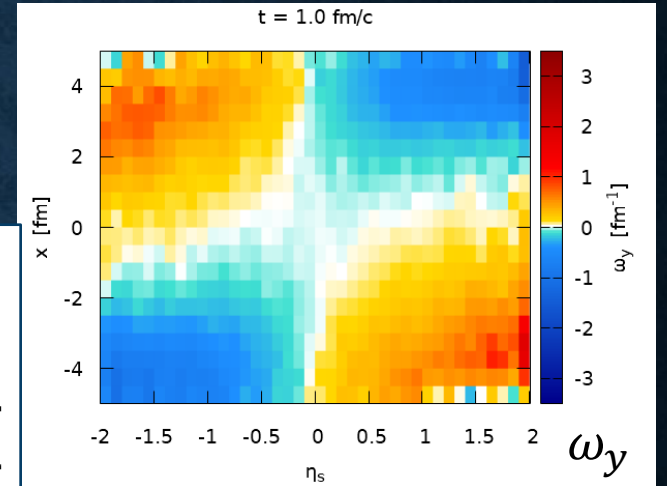
$$f_{\pm}(\eta_s) = f_{\mp}(-\eta_s) = \begin{cases} 0 & \eta_s < -\eta_m \\ \frac{\eta_s + \eta_m}{2\eta_m} & -\eta_m \leq \eta_s \leq \eta_m \\ 1 & \eta_s > \eta_m \end{cases}$$

tilted initial conditions for the QGP evolution



TILTED FIREBALL
on the reaction plane

huge vorticity in agreement with Λ polarization studies



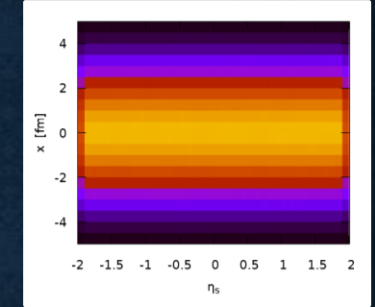
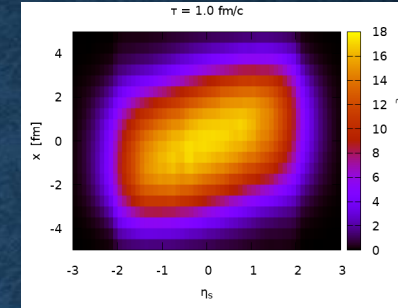
negative slope of charged particle $v_1(\eta)$

DIRECTED FLOW OF NEUTRAL D MESONS

Excellent qualitative prediction with LangevinV approach
 $dv_1^D/dy \approx 0.02-0.04$ ($\approx 10-15$ times larger than light charged)
 S. Chatterjee and P. Bozek, Phys. Rev. Lett. 120, 192301 (2018)

tilted fireball

HQs production points



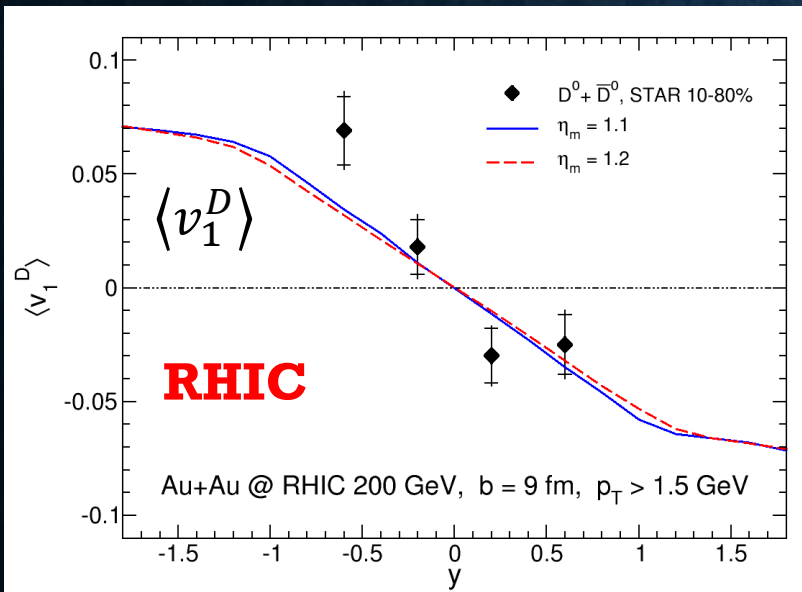
RHIC ENERGY

EXP: $dv_1^D/dy = -0.080 \pm 0.017(\text{stat}) \pm 0.016(\text{syst})$
 about 30 times larger than that of kaons

TH: $dv_1^D/dy = -0.065$ (25-30 times larger than ch.)
 relativistic BM equations for both QGP and HQs

LHC ENERGY

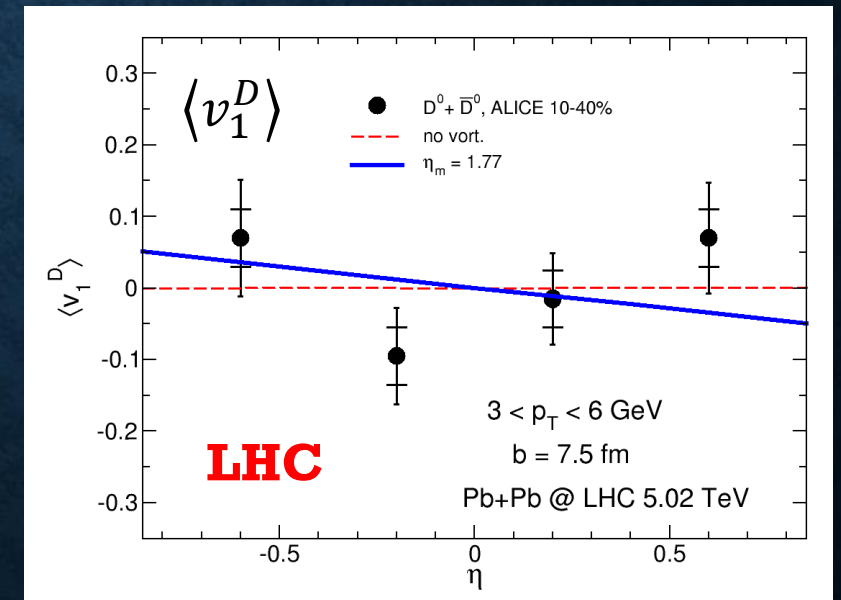
the slope of $\langle v_1^D \rangle$ is ~ 50 times smaller than that at RHIC
 (in line with model predictions) and is consistent with 0



Exp. data: ALICE Collaboration,
 Phys. Rev. Lett. 125, 022301 (2020)

Exp. data: STAR Coll.,
 Phys. Rev. Lett. 123 (2019) 162301

L. Oliva, S. Plumari and V. Greco, JHEP 05, 034 (2021)

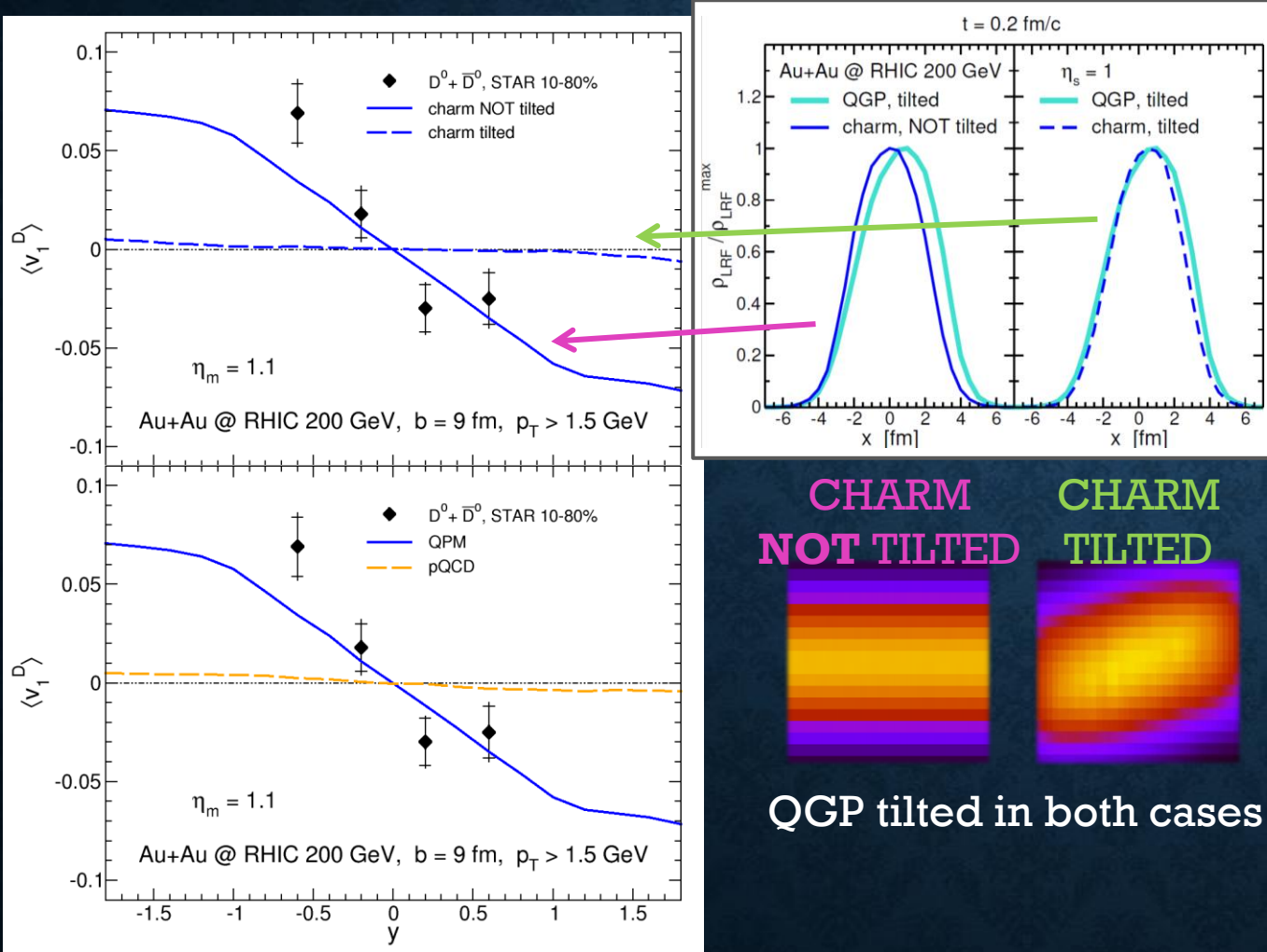


ORIGIN OF *D*-MESON DIRECTED FLOW

$$v_1(\text{HQs}) \gg v_1(\text{QGP})$$

origin of the large directed flow of HQs
different from the one of light particles

L. Oliva, S. Plumari and V. Greco, JHEP 05, 034 (2021)



longitudinal asymmetry leads to
pressure push of the bulk on the HQs

ORIGIN OF *D*-MESON DIRECTED FLOW

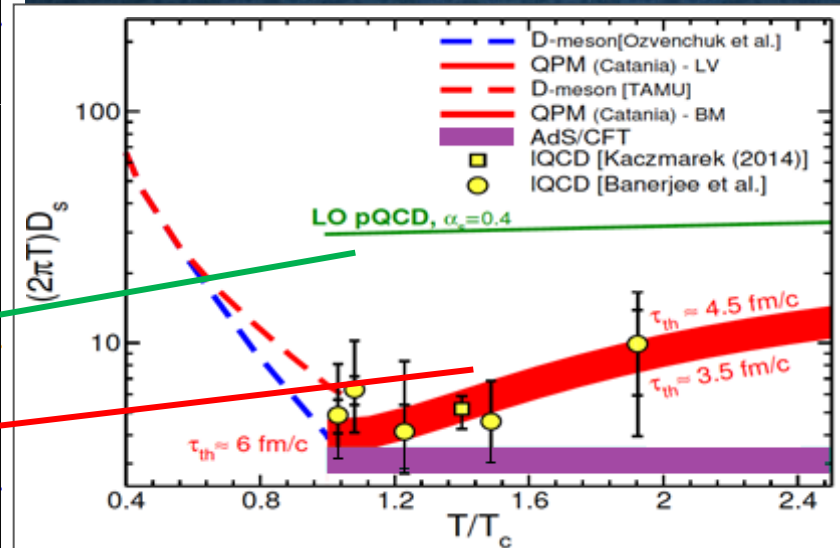
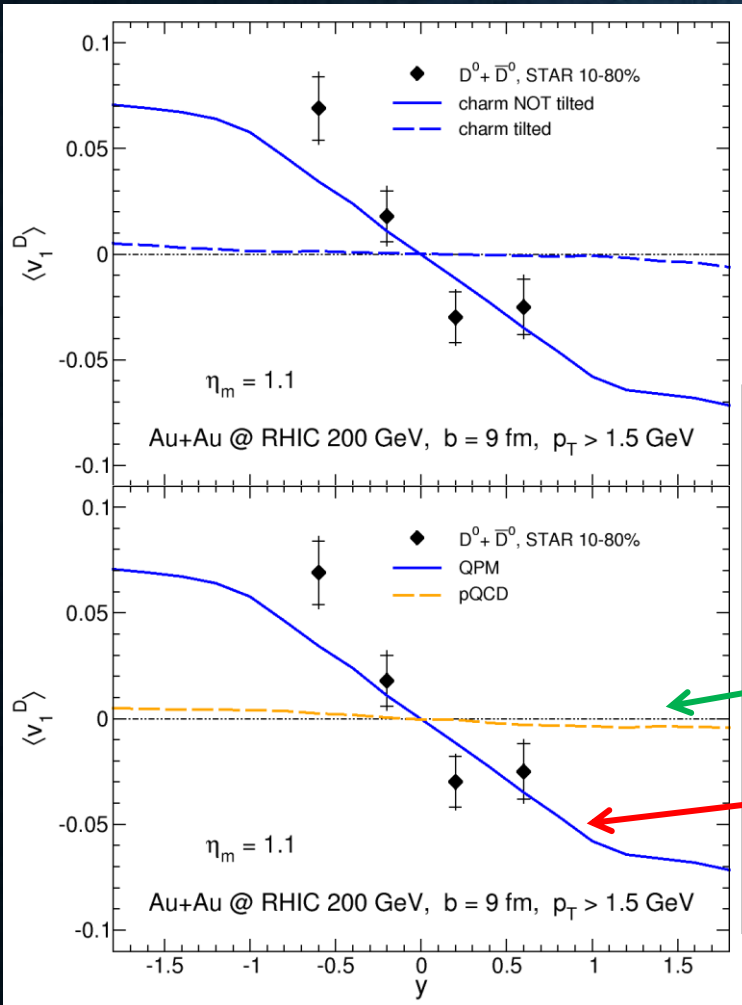
$$v_1(\text{HQs}) \gg v_1(\text{QGP})$$

origin of the large directed flow of HQs
different from the one of light particles

L. Oliva, S. Plumari and V. Greco, JHEP 05, 034 (2021)

longitudinal asymmetry leads to
pressure push of the bulk on the HQs

effective because the HQ interaction in
QGP is largely non-perturbative

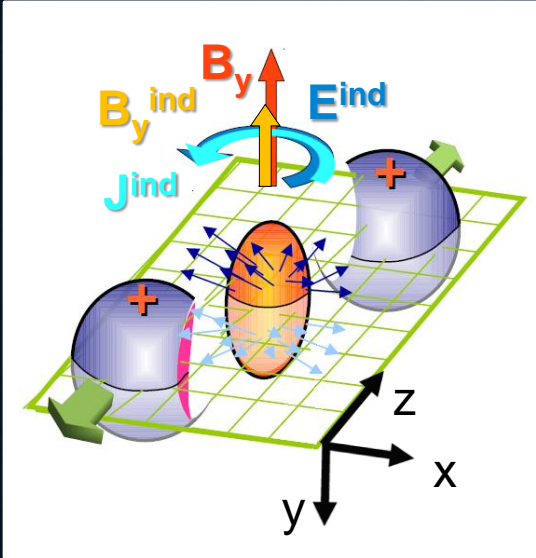


V. Greco, Nucl. Phys. A 967, 200 (2017)

Similar conclusions with
POWLANG approach
A. Beraudo et al., JHEP 05, 279 (2021)

strict connection between the
magnitude of the *D*-meson v_1
and the HQ diffusion coefficient

ELECTROMAGNETIC (EM) FIELDS IN HICS



Huge **magnetic field** in the overlap area up to $eB \approx 5-50 m_\pi^2$

- mainly produced by spectators protons
- dominated by the y component
- intense electric field generated by Faraday induction
- charged currents induced in the conducting QGP generates a magnetic field pointing towards the initial one

external charge and current produced by a point-like charge in longitudinal motion

$$J_{ind} = \sigma_{el} E$$

induced current from Ohm's law

$$\rho = \rho_{ext} \quad J = J_{ext} + J_{ind}$$

$$\rho_{ext} = e\delta(z - \beta t)\delta(x_\perp - x'_\perp)$$

$$J_{ext} = \hat{z}\beta e\delta(z - \beta t)\delta(x_\perp - x'_\perp)$$

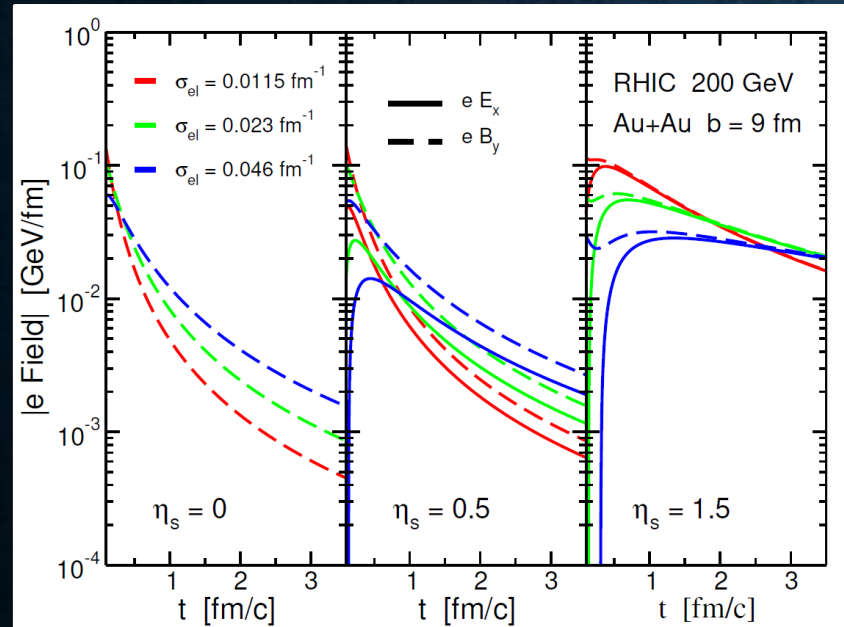
Maxwell equations can be solved analytically for a medium with **constant electric conductivity**

K. Tuchin, Adv. High Energy Phys. 2013, 1 (2013)

U. Gürsoy, D. Kharzeev, K. Rajagopal, Phys. Rev. C 89, 054905 (2014)

$$p^\mu \partial_\mu f(x, p) + q F_{ext}^{\mu\nu} p_\nu \partial_\mu^p f(x, p) = C[f]$$

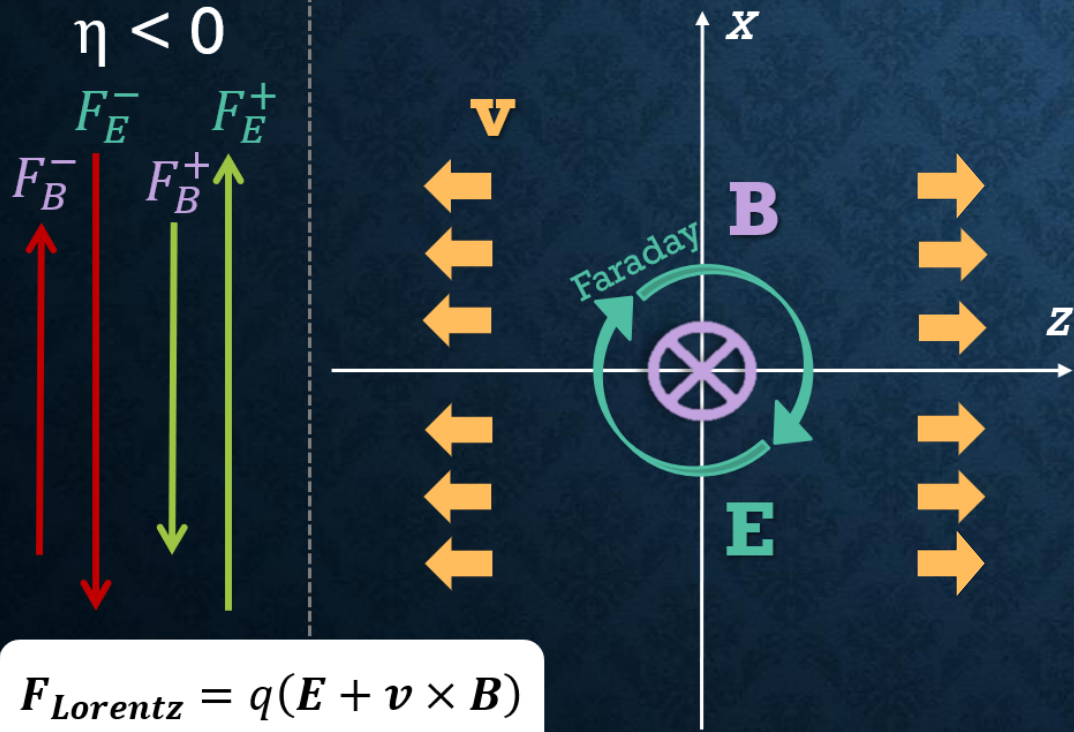
BM eq. with **EM interaction term**



EMF AND DIRECTED FLOW

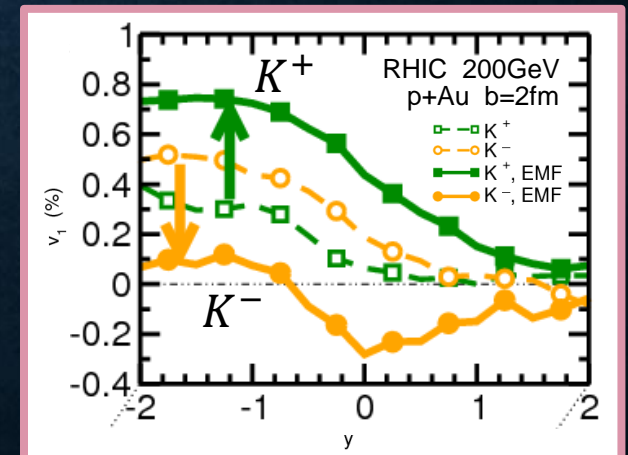
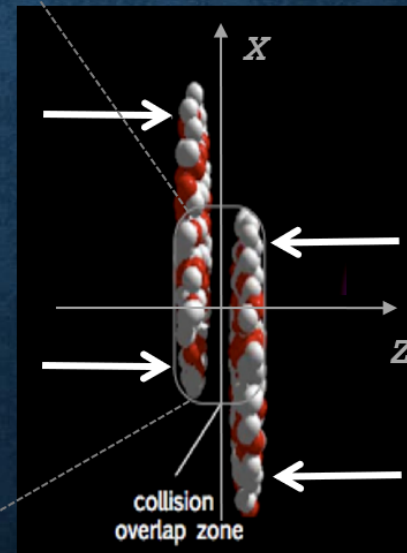
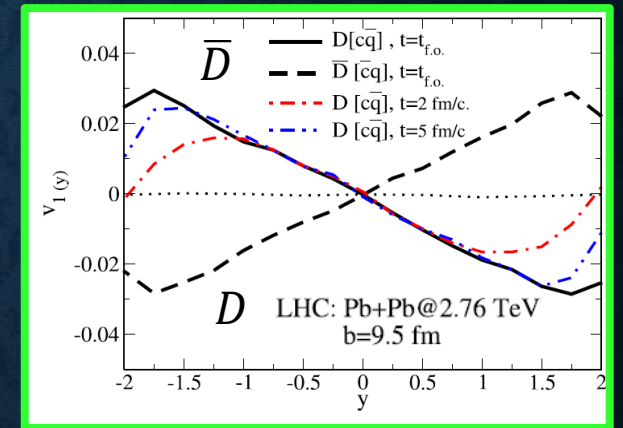
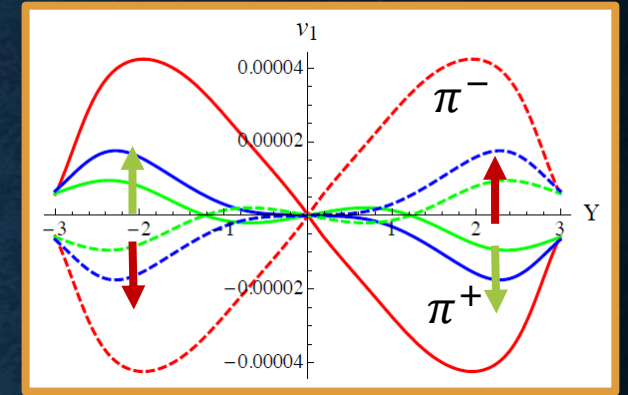
The huge EM fields induce a splitting in the DIRECTED FLOW of particles with the same mass and opposite charge

$$\Delta v_1 = v_1^+ - v_1^-$$



$$F_{Lorentz} = q(E + v \times B)$$

- Δv_1 of light hadrons in AA: $O(10^{-4}-10^{-3})$
U. Gursoy et al., Phys. Rev. C 89, 054905 (2014)
- Δv_1 of heavy mesons in AA: $O(10^{-2})$
S.K. Das et al., Phys. Lett. B 768, 260 (2017)
- Δv_1 of light mesons in pA: $O(10^{-2})$
L. Oliva et al., Phys. Rev. C 101, 014917 (2020)



L. Oliva, Eur. Phys. J. A 56, 255 (2020)

A. Dubla, U. Gursoy and R. Snellings, Mod. Phys. Lett. A 35, 2050324 (2020)

reviews

DIRECTED FLOW IN A+A AT RHIC ENERGY

L. Oliva, S. Plumari and V. Greco, JHEP 05, 034 (2021)

The electromagnetic fields induce a large splitting in the directed flow of HEAVY QUARKS

RHIC ENERGY

$$d(\Delta v_1)/dy|_{\text{exp}} = -0.011 \pm 0.024(\text{stat}) \pm 0.016(\text{syst})$$

$$d(\Delta v_1)/dy|_{\text{th}} = -0.01$$

≈ 10 times larger than charged
in agreement with

S.K. Das et al., Phys. Lett. B 768, 260 (2017)

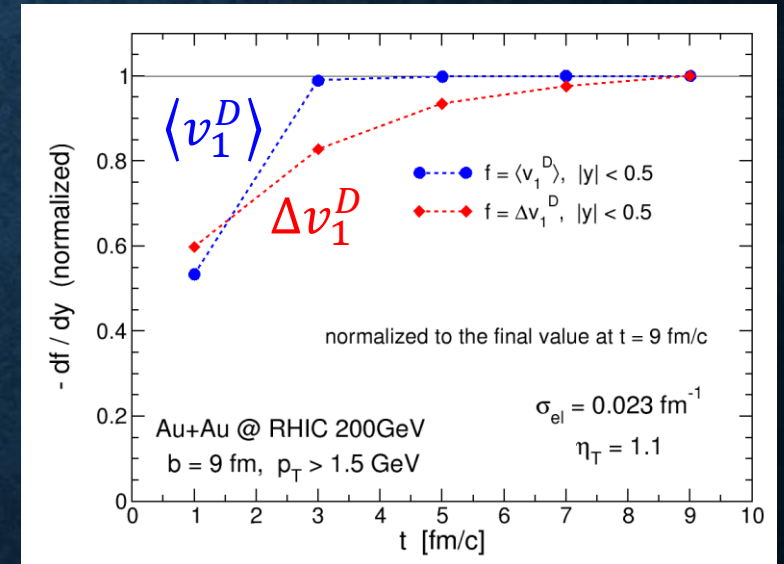
SLOPE TIME
EVOLUTION

BUT

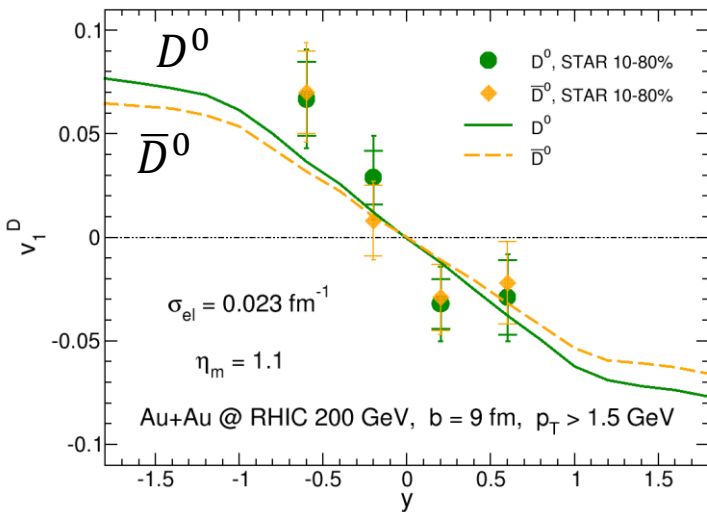
exp. Δv_1^D still consistent with
zero due to the large errors

$$\Delta v_1(\text{HQ}) \gg \Delta v_1(\text{QGP})$$

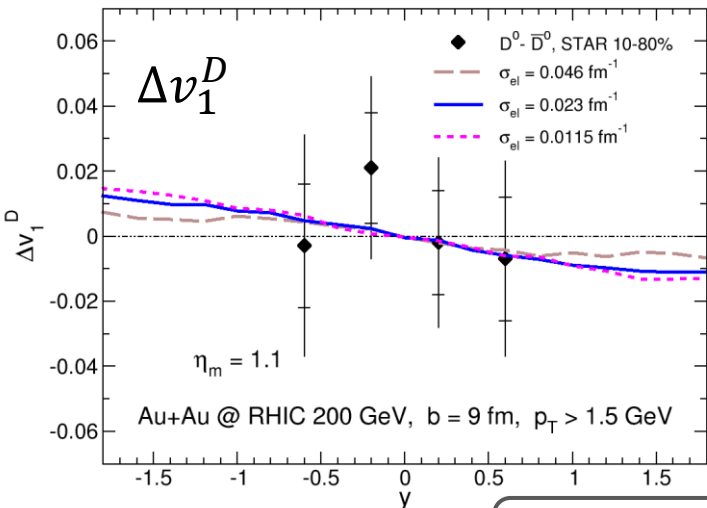
charm quarks are more sensitive to the
EM fields due to the early production



v_1^D more sensitive to the early
QGP evolution when T is higher,
while v_2^D probes more $T \sim T_c$
 \rightarrow include v_1^D in Bayesian fits



Exp. data: STAR Coll., PRL. 123 (2019) 162301



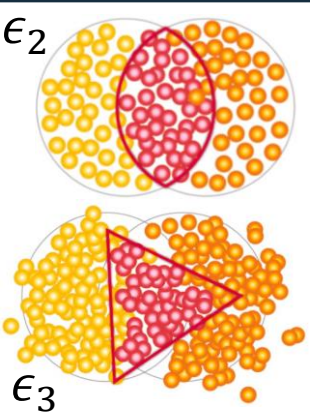
$$\Delta v_1^D = v_1(D^0) - v_1(\bar{D}^0)$$

DIRECTED FLOW OF
NEUTRAL D MESONS

EVENT-BY-EVENT FLUCTUATIONS

Event-by-event fluctuations in the initial nucleon positions

n th-order spatial eccentricities

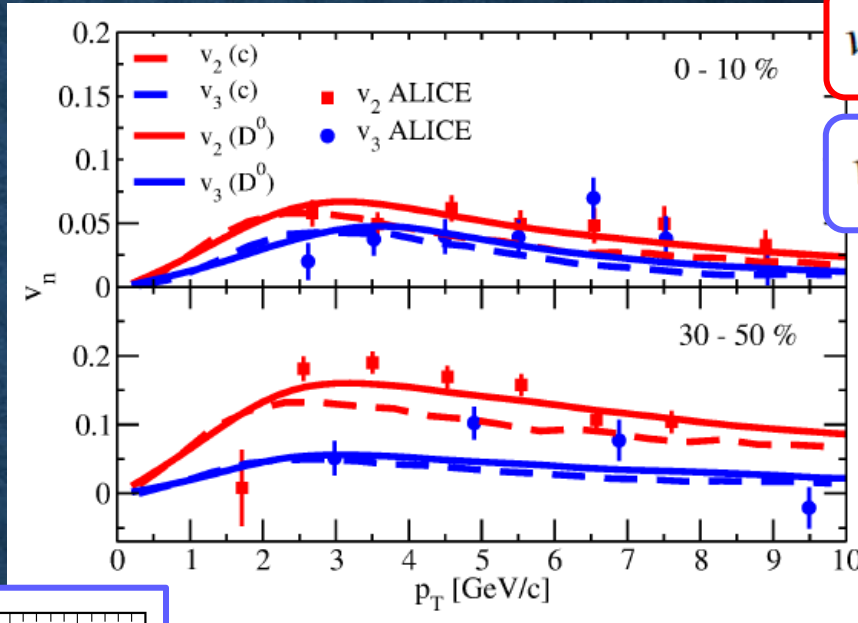


$$\epsilon_n = \frac{r_{\perp}^n \cos[n(\phi - \Psi_n)]}{r_{\perp}^n}$$

$$\Psi_n = \frac{1}{n} \arctan \frac{r_{\perp}^n \sin(n\phi)}{r_{\perp}^n \cos(n\phi)}$$

$$r_{\perp} = \sqrt{x^2 + y^2} \quad \phi = \arctan(y/x)$$

M. L. Sannataro et al., 2206.03160



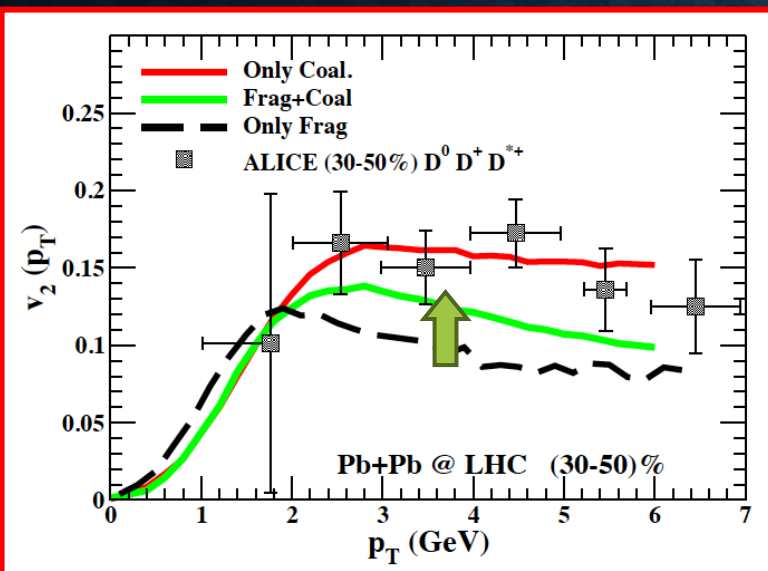
elliptic flow

$$v_2 = \langle \cos[2(\phi - \Psi_2)] \rangle$$

$$v_3 = \langle \cos[3(\phi - \Psi_3)] \rangle$$

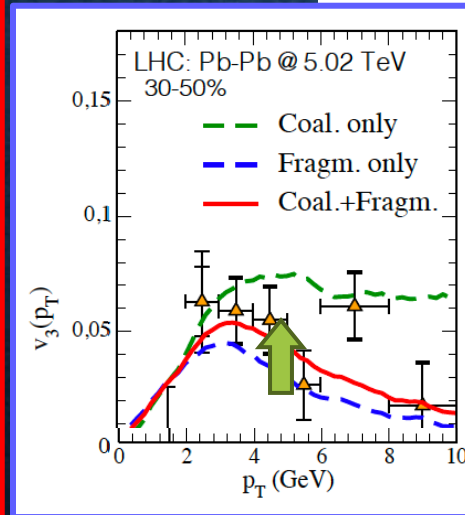
triangular flow

Exp. Data: ALICE Coll.,
Phys. Lett. B 813, 136054
(2021)



F. Scardina et al.,

Phys. Rev. C 96, 044905 (2017)



S. Plumari et al.,

Phys. Lett. B 805, 135460 (2020)

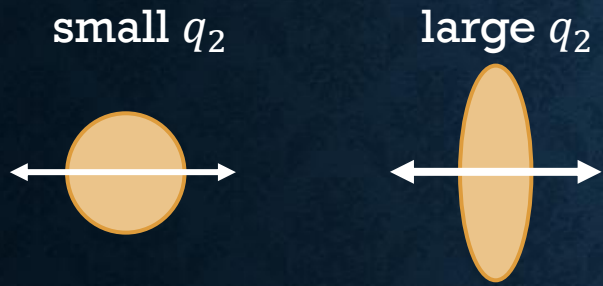
D-MESON v_2 AND v_3

- v_2 larger in more peripheral collisions
→ mainly generated by the geometry of overlap region
- v_3 not much sensitive to the collision centrality
→ mainly driven by the fluctuations of the triangularity of overlap region
- **coalescence** increases v_2 and v_3 at $p_T > 2$ GeV

EVENT-SHAPE ENGINEERING (ESE)

M. L. Sambataro et al., 2206.03160

ESE technique: selection of events with **same centrality** but **different average bulk flow** on the basis of the magnitude of the 2^o-order harmonic reduced flow vector q_2



$$q_2 = |\vec{Q}_2|/\sqrt{M}$$

$$\vec{Q}_2 = \sum_{j=1}^M e^{i2\phi_j}$$

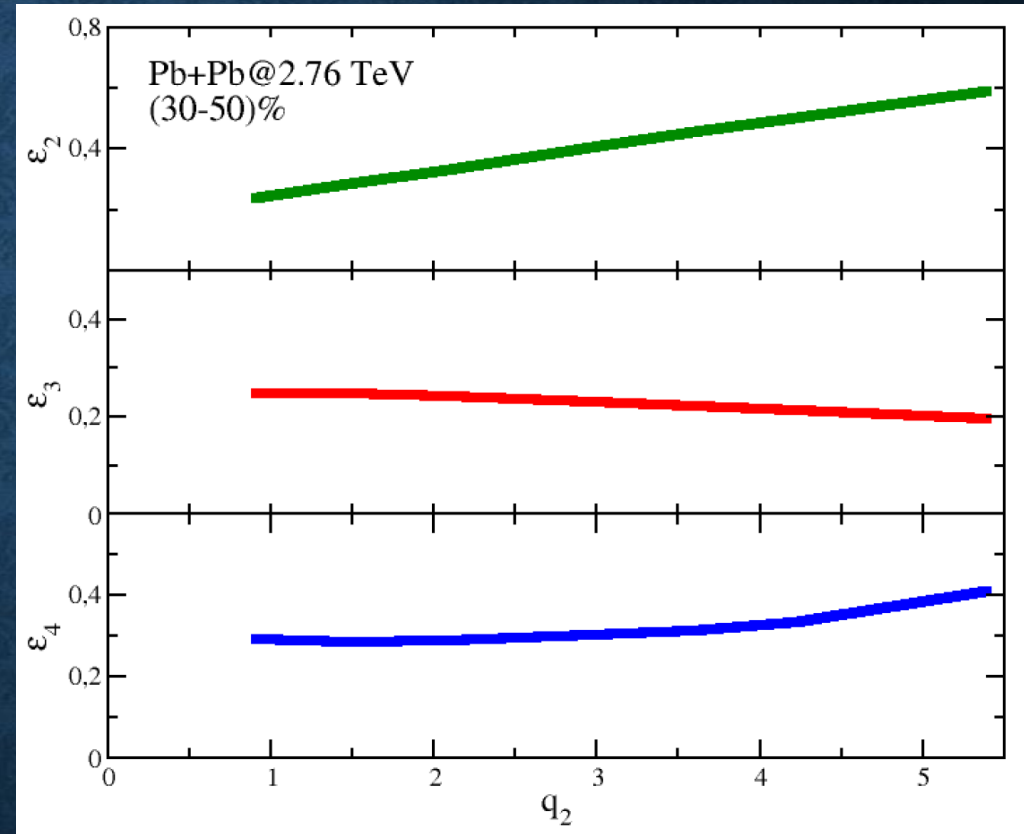
$v_2 \propto \epsilon_2, v_3 \propto \epsilon_3$ for small values of η/s



access to the **initial fireball geometry**
small/large $q_2 \rightarrow$ small/large ϵ_2

Increasing interest on studying observables with multi-differential methods based on event shape
➤ Transverse spherocity analysis in small systems

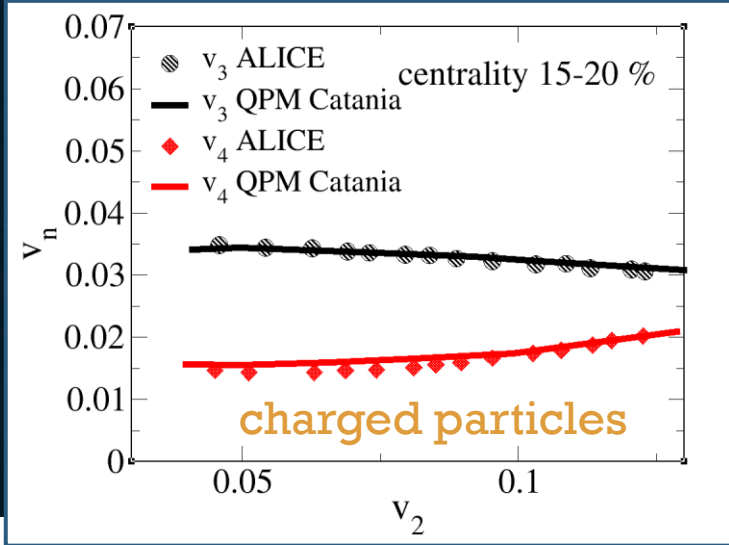
SPATIAL ECCENTRICITIES



- ❑ Anti-correlation between ϵ_2 and ϵ_3
- ❑ Non-linear correlation between ϵ_2 and ϵ_4

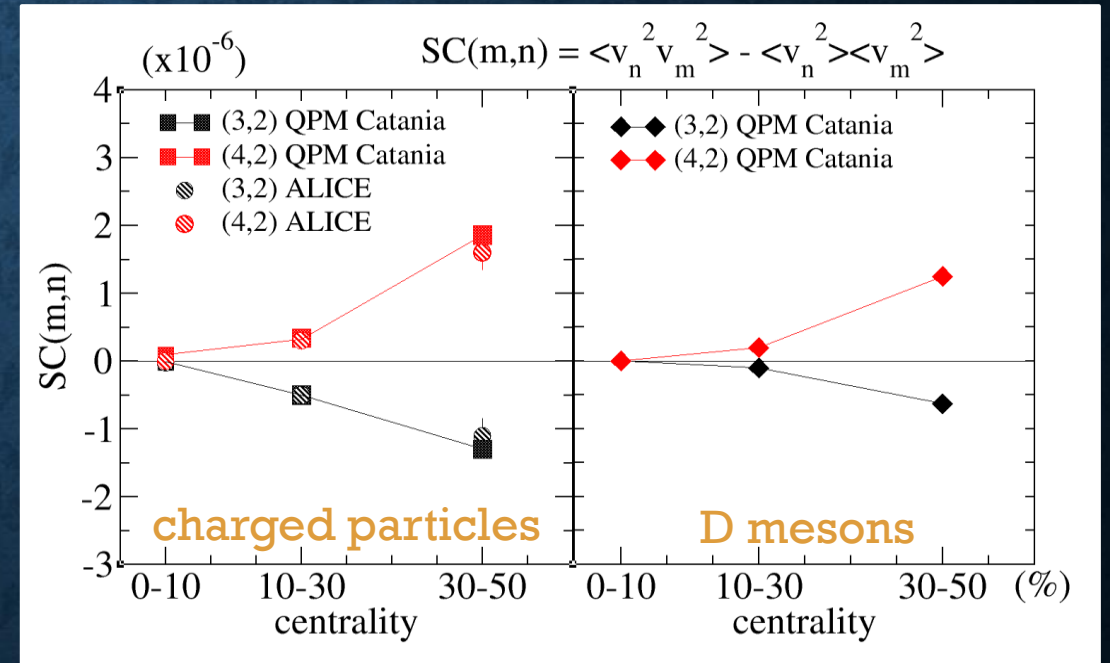
ESE: $v_n - v_m$ CORRELATIONS

Exp. Data: S. Mohapatra, Nucl. Phys. A 956, 59 (2016)



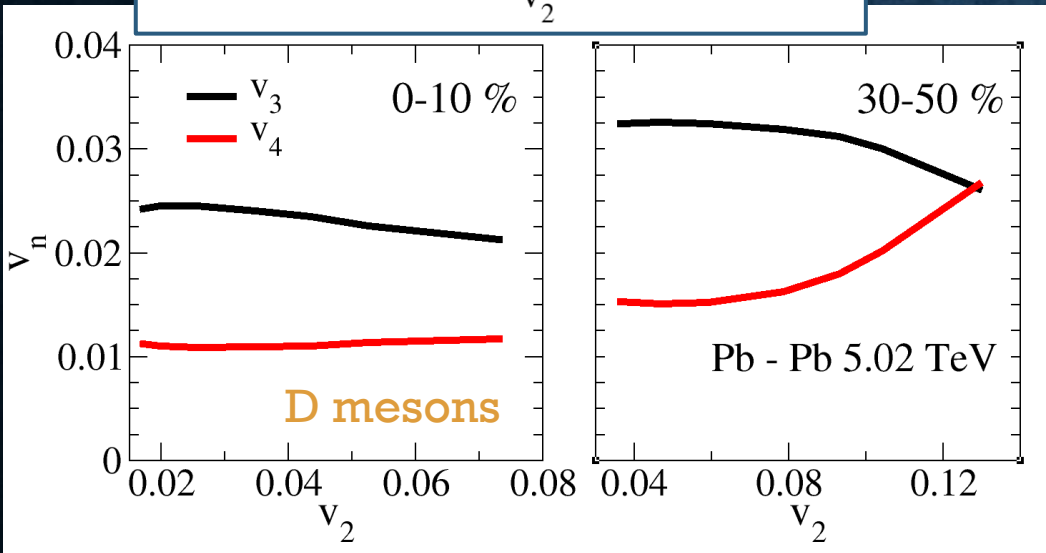
- Good description of experimental data for charged particles
- Prediction of comparable *D*-meson correlations w.r.t. bulk

Exp. data: ALICE Coll., Phys. Lett. B 818, 136354 (2021)



SYMMETRIC CUMULANT CORRELATOR

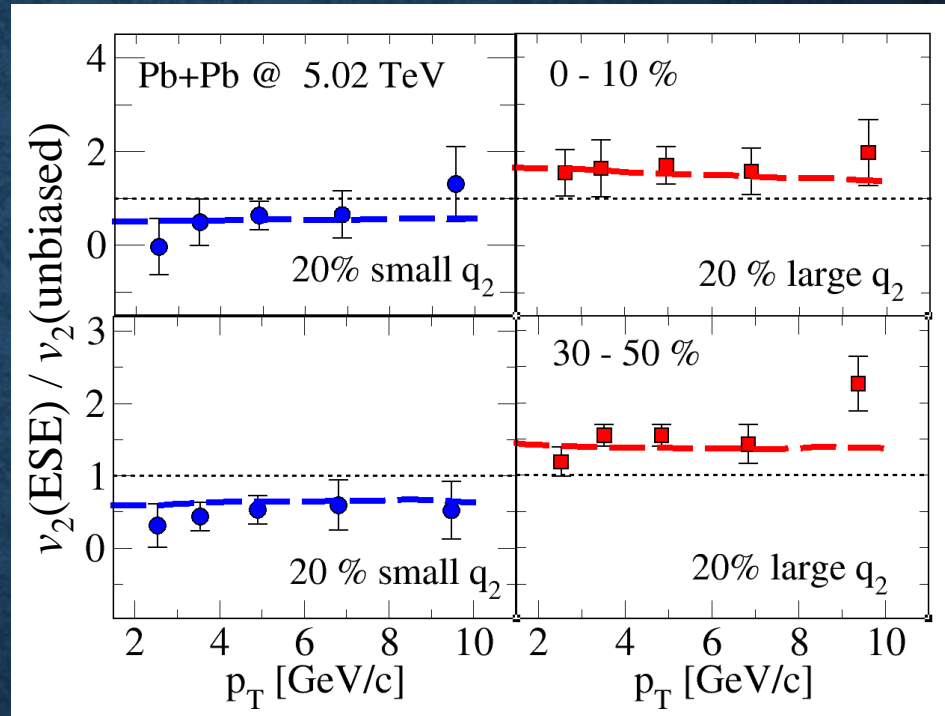
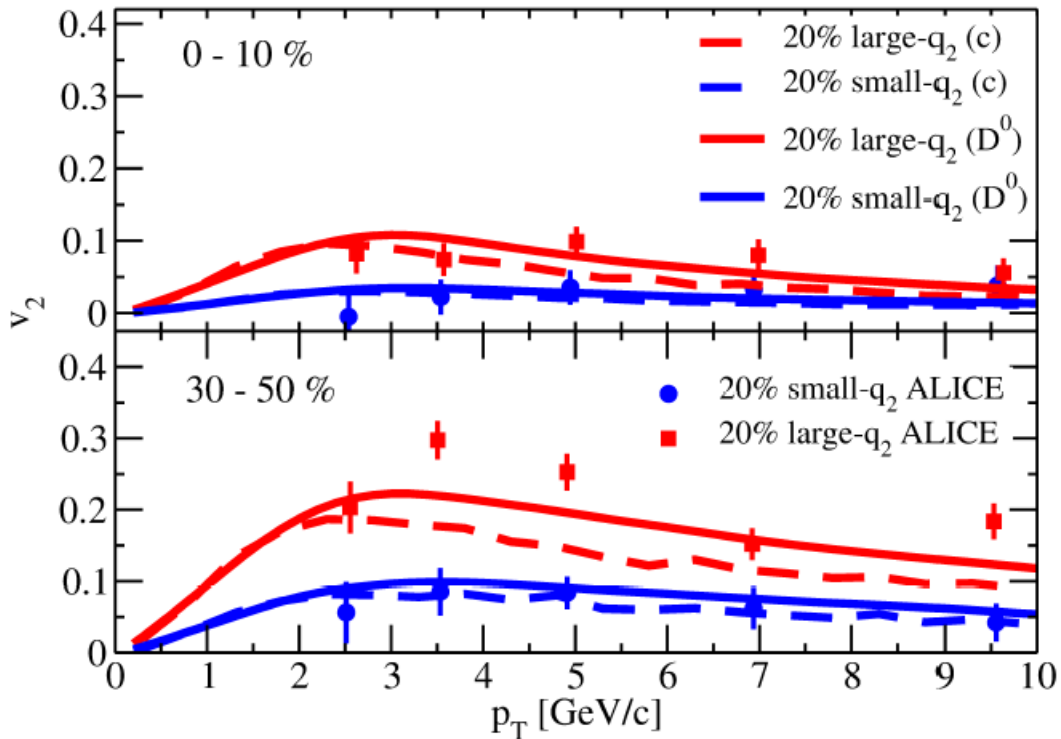
Same approach and $D_s(T)$ describing $R_{AA}(p_T)$ & $v_2(p_T)$



$v_n - v_m$ CORRELATIONS

ESE: q_2 -SELECTED ELLIPTIC FLOW

Exp. Data: ALICE Collaboration, Phys. Lett. B 813, 136054 (2021)

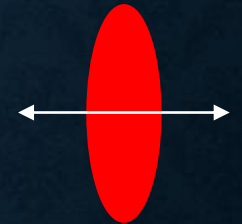


D -MESON $v_2(p_T)$ RATIO

20% small q_2



20% large q_2



q_2 -SELECTED D -MESON $v_2(p_T)$

v_2 (small q_2) < v_2 (unbiased)

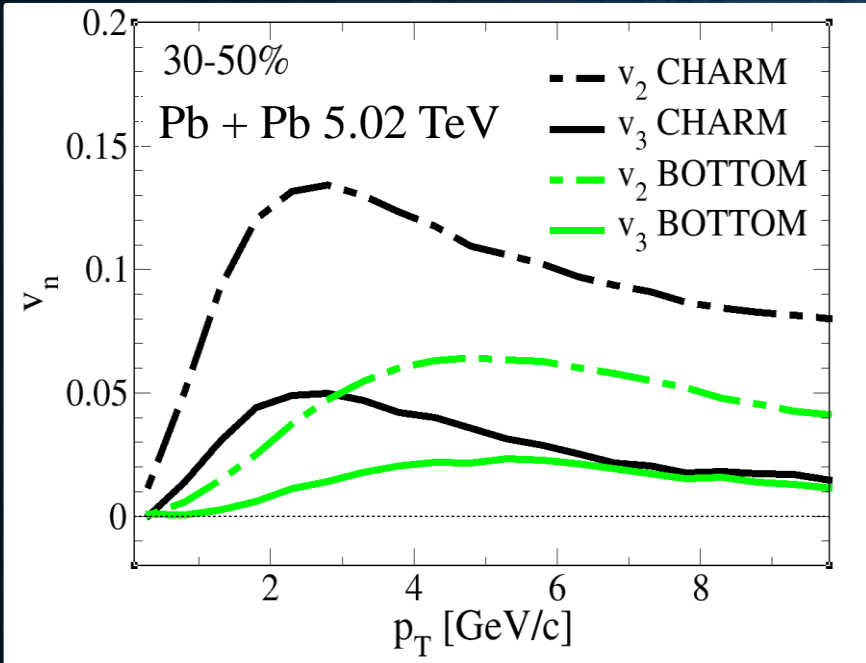
v_2 (large q_2) > v_2 (unbiased)

about 50% difference between q_2 -selected and unbiased events in both centrality class with no transverse momentum dependence
 \Rightarrow ESE selection related to a global property of the events

Same approach and $D_s(T)$ describing $R_{AA}(p_T)$ & $v_2(p_T)$

EXTENSION TO BOTTOM DYNAMICS

CHARM vs BOTTOM FLOW COEFFICIENTS



substantial v_2 and v_3 of bottom quarks though smaller than that of charm but still

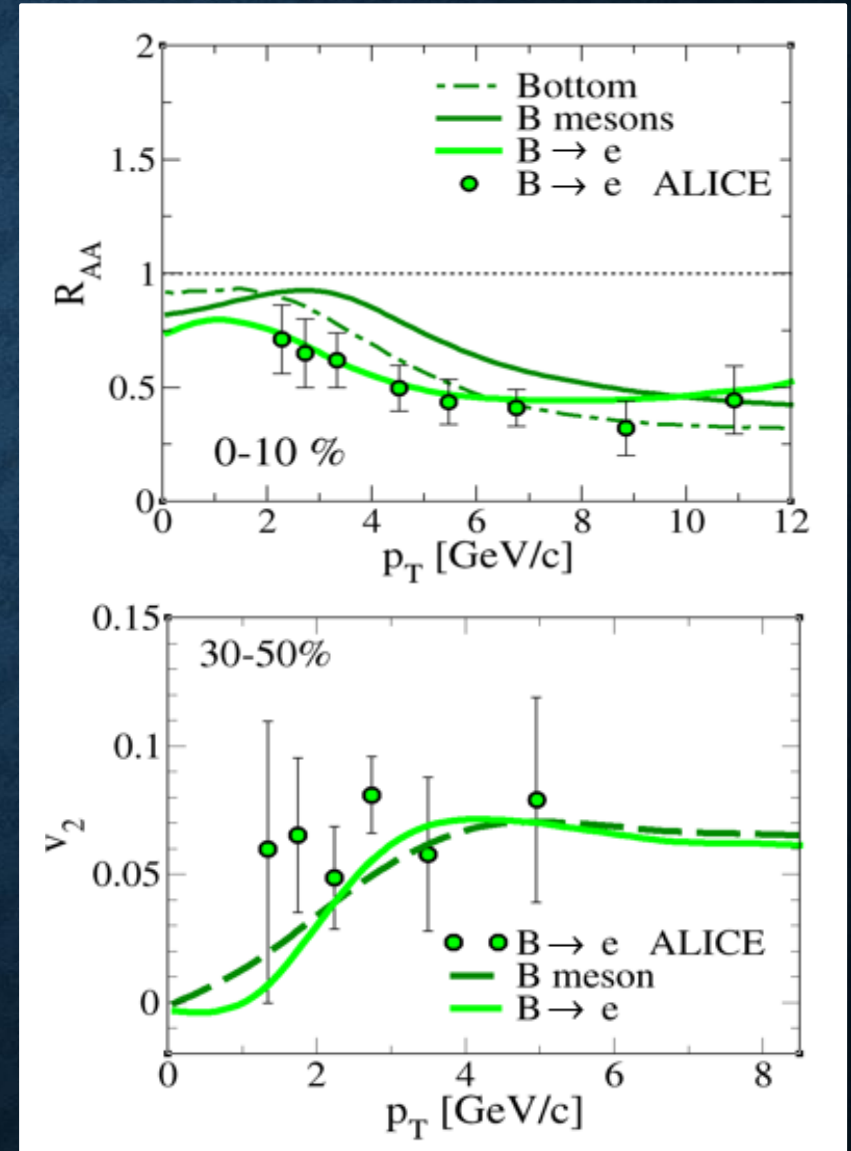


- Good description of R_{AA} and v_2 of electrons from semileptonic B decay
- Prediction of R_{AA} and v_2 for B meson

indication for a strong coupling of bottom quarks with collectively expanding bulk

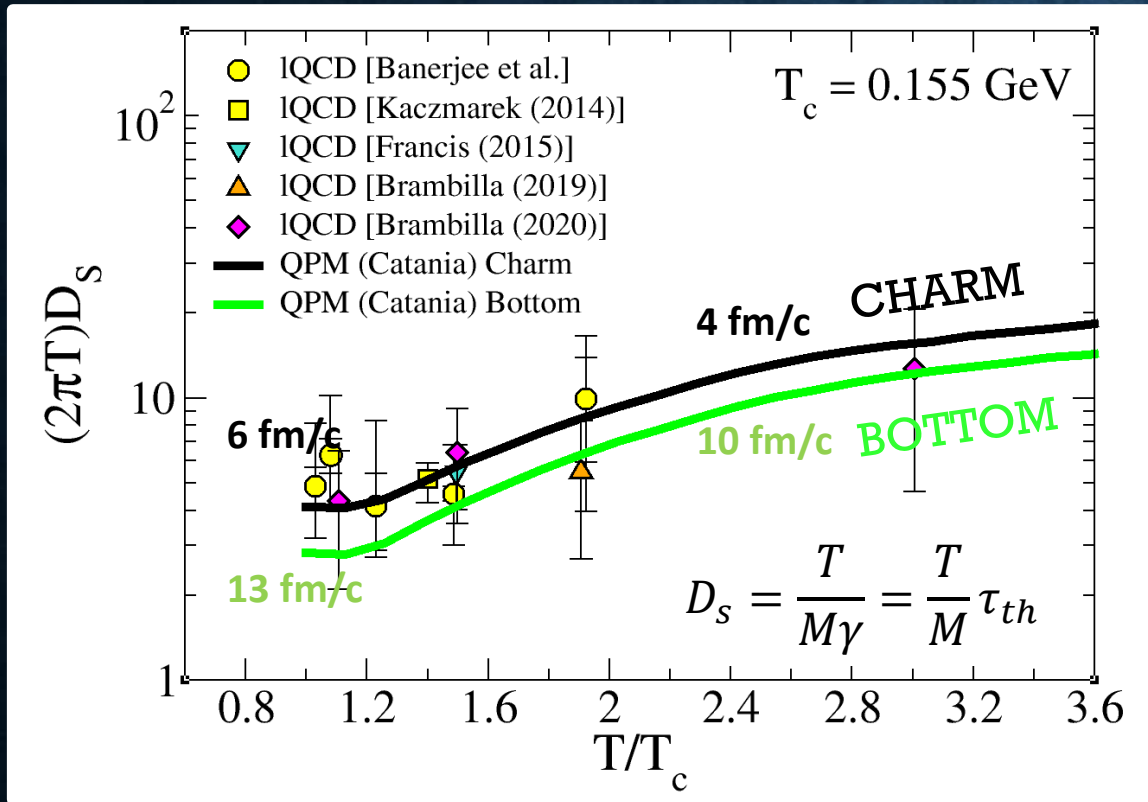
Exp. data from talk of R. Arnaldi at HP2020

NUCLEAR MODIFICATION FACTOR



BOTTOM SPATIAL DIFFUSION COEFFICIENT

Results from $R_{AA}(p_T)$ and $v_2(p_T)$ of B mesons



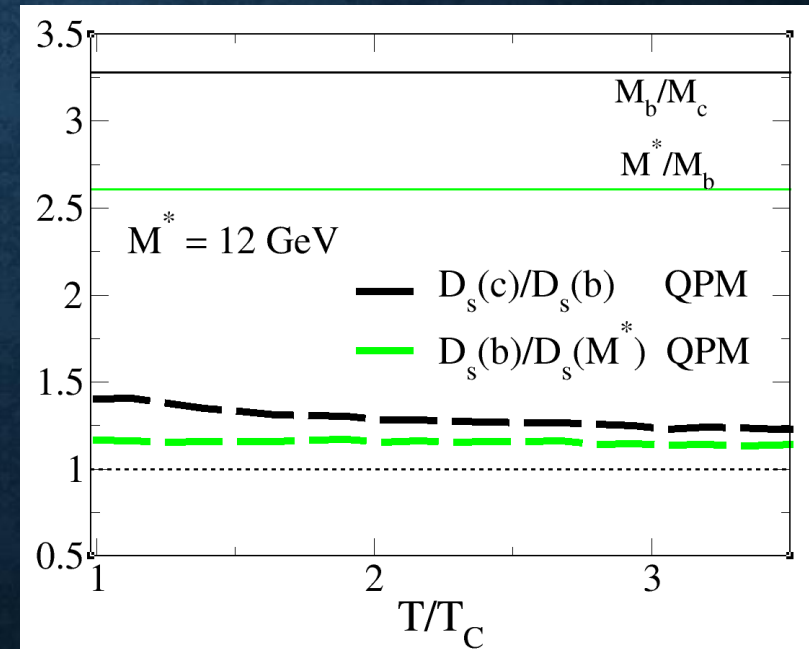
□ D_s is ideally M independent ($M \rightarrow \infty$)

since from kinetic theory:

$$\tau_{th}^b / \tau_{th}^c \approx \gamma_c / \gamma_b \approx M_b / M_c$$

□ D_s is a measure of thermalization time:

$$\tau_{th} \approx 1.3 M \frac{2\pi T D_s}{(T/T_c)^2} \text{ fm/c}$$

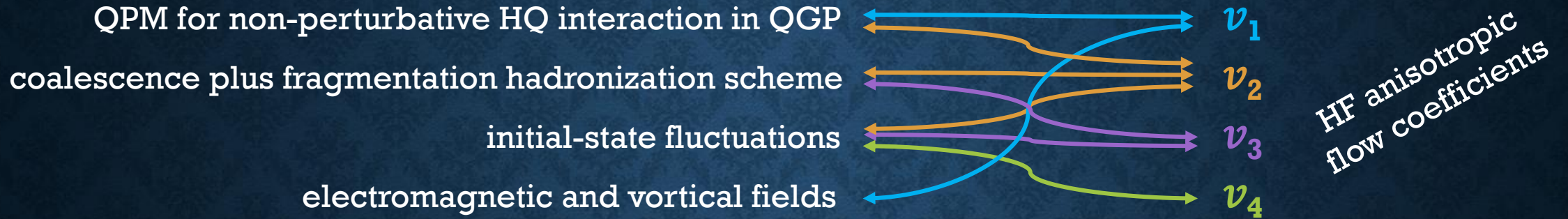


CHARM vs BOTTOM SPATIAL DIFFUSION COEFFICIENT

- In QPM approach $D_s(c)$ is 30-40% larger than $D_s(b)$
- Bottom quarks expected to be fully thermalized @ FCC

CONCLUSIONS

Full Boltzmann transport approaches for the description of HQ dynamics in relativistic heavy-ion collisions



- ✓ The D^0 -meson v_1 gives information on the transport properties of the hot QCD matter: magnitude associated with the HQ diffusion coefficient and splitting connected to the QGP electric conductivity
- ✓ For D mesons v_1 is more sensitive to the early QGP evolution when T is higher, while v_2 probes more $T \sim T_c$. Inclusion in Bayesian fit and for $D_s(T)$ estimate?
- ✓ Spatial diffusion coefficient $D_s(T)$ that reproduces D -meson R_{AA} and v_2 gives correct predictions for v_3 and q_2 -selected anisotropic coefficients
- ✓ Prediction for significant $v_n - v_m$ correlation of D mesons, comparable to that of bulk particles
- ✓ Indication for a strong coupling of bottom quarks with the collectively expanding bulk

Thank you for your attention!