

# $B_c$ Meson and X(3872) Transport in High-Energy Heavy-ion Collisions

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The 20th International Conference on Strangeness in Quark Matter  
2022, Busan, Korea, June 13-17, 2022

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# Outline

- Transport Approach
  - Rate Equation & Transport Parameters
- $B_c$  Meson in Heavy-Ion Collisions
- $X(3872)$  in Vacuum and Heavy-Ion Collisions
- Conclusion

- Rate equation used in calculating quarkonia ( $Q$ ) in URHICs

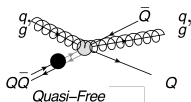
Reaction rate

$$\frac{dN_Q}{d\tau} = -\Gamma(T) [N_Q - N_Q^{\text{eq}}(T, \gamma_c)]$$

Primordial    Regeneration

- Quasi-free approximation

$$Q + q, g \rightleftharpoons Q + \bar{Q} + q, g$$



- Equilibrium limit from statistical model

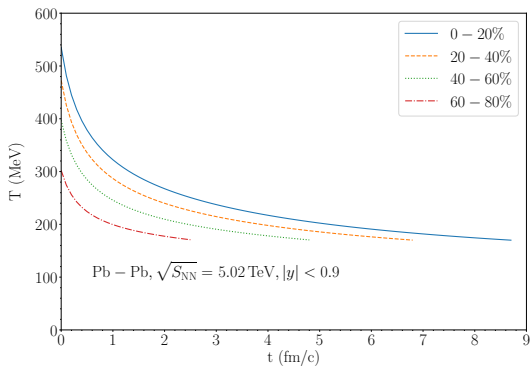
$$N_X^{\text{eq}} = dV_{\text{FB}} \gamma_c^2 \int \frac{d^3p}{(2\pi)^3} e^{-\sqrt{m_X^2 + p^2}/T}, \quad N_{B_c}^{\text{eq}} = dV_{\text{FB}} \gamma_c \gamma_b \int \frac{d^3p}{(2\pi)^3} e^{-\sqrt{m_{B_c}^2 + p^2}/T}$$

- Fugacity  $\gamma_Q(T)$ : Heavy Quark (HQ) number conservation

$$N_{Q\bar{Q}} = \frac{1}{2} \gamma_Q(T) n_{\text{op}} V_{\text{FB}} \frac{I_1(\gamma_Q(T) n_{\text{op}} V_{\text{FB}})}{I_0(\gamma_Q(T) n_{\text{op}} V_{\text{FB}})} + \gamma_Q^2(T) n_{\text{hid}} V_{\text{FB}}$$

$$N_{Q\bar{Q}} = \frac{N_{\text{coll}} \sigma_{\text{pp}}^{\text{pp}}}{\sigma_{\text{inel}}^{\text{pp}}}$$

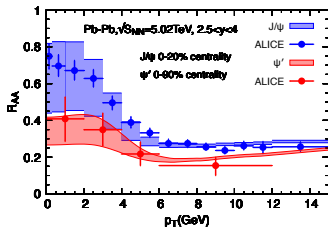
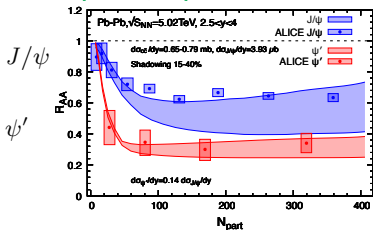
# The space time evolution



- Expanding fireball
- Conservation of entropy and EoS  $\Rightarrow T(t)$

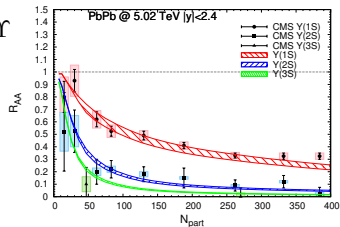
# Results of Quarkonia in 5 TeV Pb-Pb Collisions

[ALICE, '20]



- $R_{AA} = \frac{N^{PbPb}}{N_{coll} N^{PP}}$
- Charmonia with most recent open-charm cross section + shadowing
  - $\psi'$  results predictions
  - bottomonia within same approach

$\Upsilon$

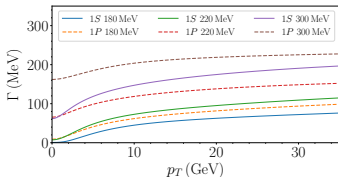
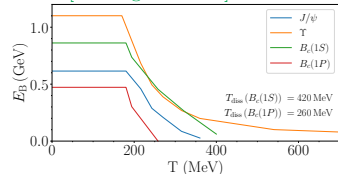
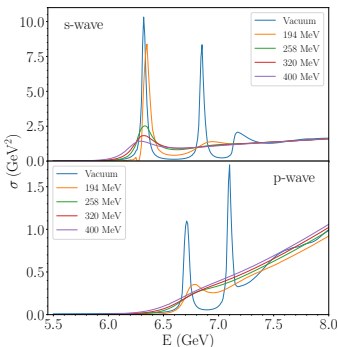


[CMS, '19]

[Du et al., '17]

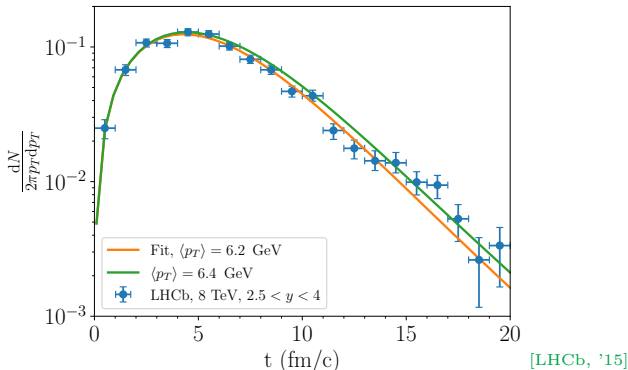
# $B_c$ In-medium Binding Energy and Reaction Rates

[Z. Tang et al. '21]



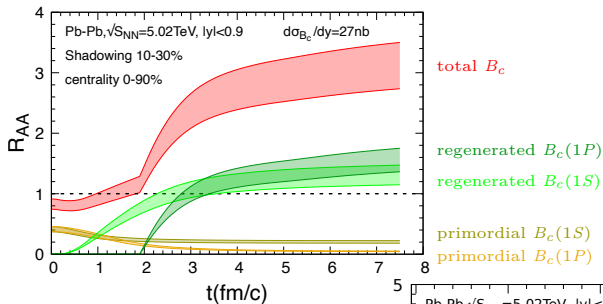
- $B_c$  spectral functions: In-medium T-matrix calculation.
- Vacuum mass:  $B_c(1S) = 6.324$  GeV,  $B_c(2S) = 6.850$  GeV
- PDG:  $B_c(1S) = 6.274$  GeV,  $B_c(2S) = 6.871$  GeV
- $T_{\text{diss}}(1S) = 420$  MeV and  $T_{\text{diss}}(1P) = 260$  MeV

# $B_c$ $p_T$ spectra and cross section in 5 TeV $pp$ Collisions

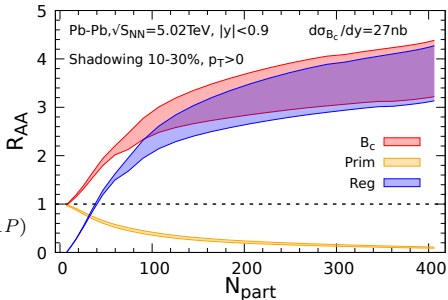


- $\frac{dN_{pp}^{B_c}}{2\pi p_T dp_T} = \frac{N}{(1 + \frac{p_T}{A\langle p_T \rangle})^n}$ , fitted to 8 TeV, forward-rapidity [S. Acharya *et al.*, '19,'17]
- $\langle p_T \rangle \Rightarrow 5.02 \text{ TeV}$  and mid-rapidity
- Theoretical calculations:  $\text{BR}(B_c \rightarrow J/\psi \mu \bar{\nu}) \sim 1.4\% - 7.5\%$
- $\text{BR} \sim 4 \pm 2\%$ ,  $\frac{d\sigma_{B_c}^{pp}}{dy} = 27 - 82 \text{ nb}$

# $B_c$ Time Evolution in 5.02 TeV Pb-Pb Collisions



- $$R_{AA} = \frac{N_{\text{Coll}} N_{B_c}^{\text{PP}} S_{B_c} + N_{B_c}^{\text{reg}}}{N_{\text{Coll}} N_{B_c}^{\text{PP}}}$$
- Regeneration forms at  $T_{\text{diss}}$
- $N^{\text{tot}}(1S) = N^{\text{dir}}(1S) + \text{BR}(1P \rightarrow 1S) N^{\text{dir}}(1P)$
- $\text{BR}(1P \rightarrow 1S) = 100\%$
- regeneration predicted without new parameters

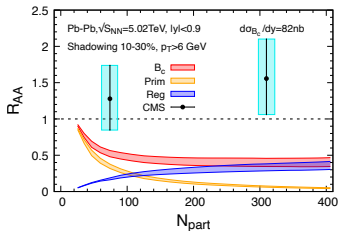
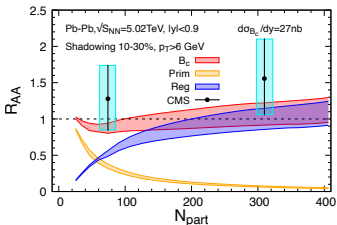
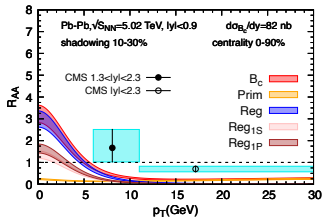
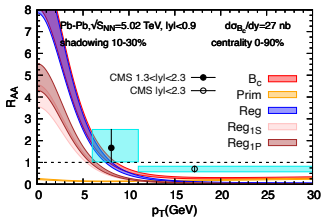




# $B_c$ in 5 TeV Pb-Pb Collisions

$$\frac{d\sigma_{B_c}^{pp}}{dy} = 27 \text{ nb}$$

$$\frac{d\sigma_{B_c}^{pp}}{dy} = 82 \text{ nb}$$

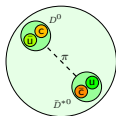


- $B_c(p_T)$ : coalescence:  $\bar{b} + c \rightarrow B_c^+$

- Dominated by regeneration, better agreement for smaller  $\sigma_{B_c}^{pp}$

# X(3872): Molecular vs. Tetraquark Scenario

- Vacuum mass of  $X(3872) \approx \bar{D}^{*0}(2007) + D^0(1865) \sim$



- Vacuum width:  $\Gamma(X(3872)) < 1.2 \text{ MeV} \sim$



- Reaction rate in fireball:  $\Gamma \sim \Gamma_0 \left( \frac{T}{T_0} \right)^n$

- Molecular: Loosely-bound molecular state

$$\Gamma_0 \sim 300\text{-}500 \text{ MeV} \quad [\text{Cleven et al.}'19]$$

- Tetraquark: Compact diquark anti-diquark bound state

$$\Gamma_0 \sim 30\text{-}50 \text{ MeV}$$

- Weak dependence on  $n$

- Initial condition at hadronization

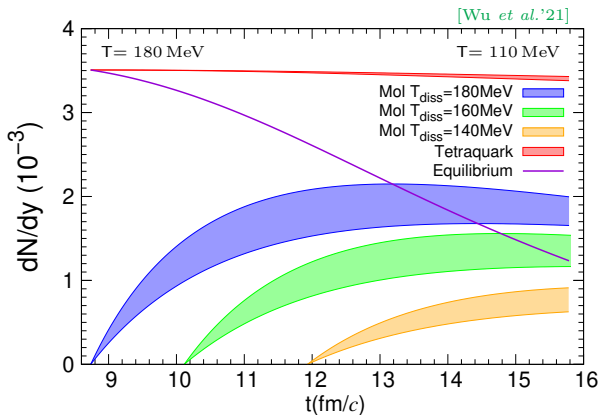
- Molecular:  $N(T = T_C) = 0$

Small binding energy, destroyed in QGP

- Tetraquark:  $N(T = T_C) = N^{eq}(T_C)$

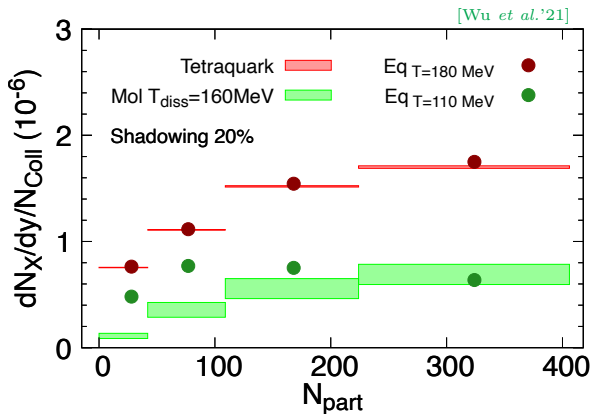
Likely to form in the QGP phase

# X(3872) Time Evolution in 5 TeV Pb-Pb Collisions



- Tetraquark: small reaction rate  $\Rightarrow$  mainly from the initial yield at hadronization
- Molecular: large reaction rate  $\Rightarrow$  approaches to equilibrium at  $T = 110 \text{ MeV}$

# X(3872) Centrality Dependence



- Molecular is close to the thermal freeze-out equilibrium limit
- Tetraquark is close to the equilibrium limit at hadronization
- Final ratio  $N_{Tet}/N_{Mol} \sim 3$  for all centralities

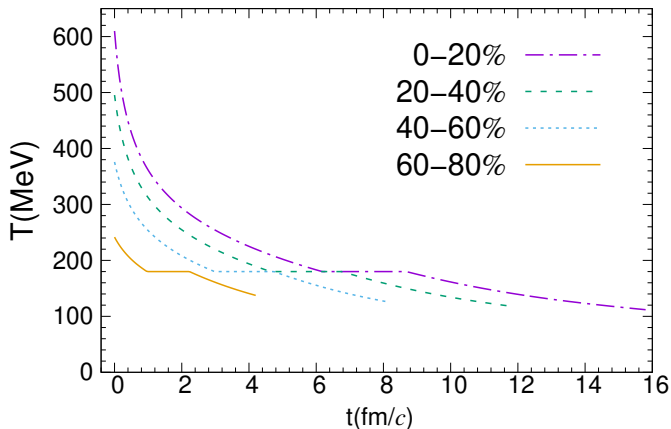
# Conclusion

- Calculated  $B_c$  and X(3872) in URHICs using the rate equation
- $R_{AA}$  of  $B_c$  meson dominated by the regeneration
- Sensitive to the cross section  $\sigma_{B_c}^{pp}$
- X(3872) structure information: reaction rate and initial condition
- Molecule produced later than tetraquark  $\Rightarrow$  suppressed by a factor about 3 (equilibrium limit drops with  $T$ )
- $N_{Tet} > N_{Mol} \Rightarrow$  qualitatively different from coalescence model predictions

Thank you!

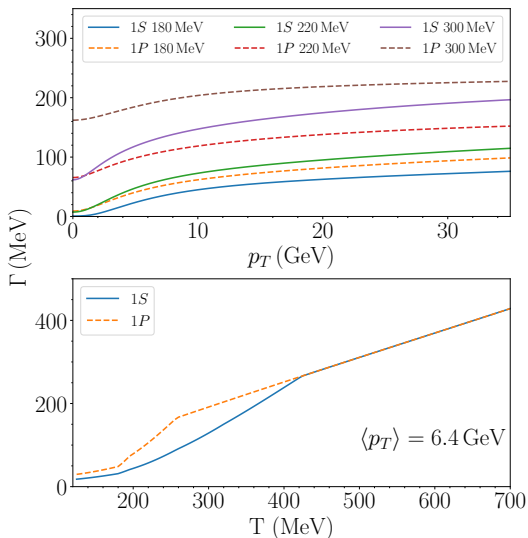
# Backup

# Temperature of the Fireball



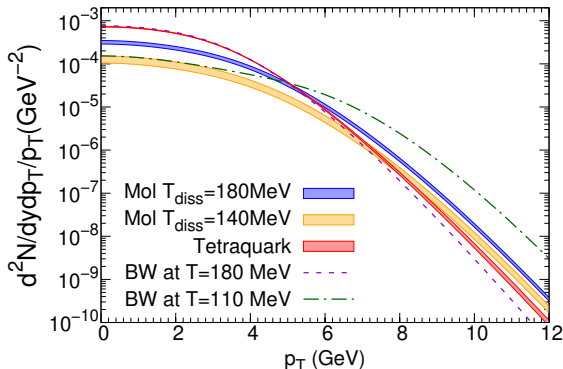


# Temperature of the Fireball



# X(3872) $p_T$ Spectra in 5 TeV Pb-Pb Central Collisions

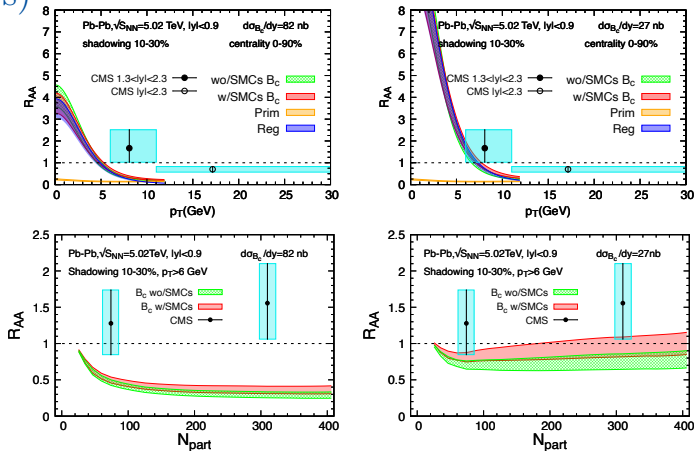
[Wu *et al.*'21]



- Both scenarios in between of the blast wave  $p_T$  spectra at hadronization and thermal freeze-out
- Tetraquark: close to the blast wave  $p_T$  at hadronization
- Molecular: produced later  $\Rightarrow$  has harder  $p_T$  spectra

# Results with/without Momentum Space Correlations (SMCs)

[He et al., PRL 128, 162301]



- $B_c p_T$  is harder than the spectra without SMCs.
- $B_c R_{AA}$  is enhanced by the implement of SMCs.