

Midrapidity cluster formation in heavy-ion collisions

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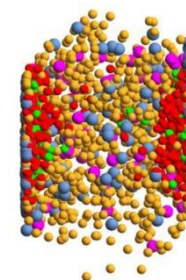
(GSI, Darmstadt & Uni. Frankfurt)

&

**Susanne Glaessel, Viktor Kireyeu, Joerg Aichelin, Vadym Voronyuk,
Christoph Blume, Gabriele Coci, Vadim Kolesnikov, Michael Winn,
Jan Steinheimer, Marcus Bleicher**

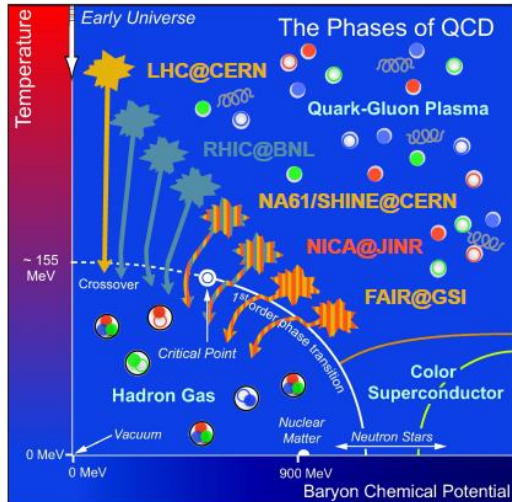


**The 20th International Conference on Strangeness
in Quark Matter (SQM 2022)**
13 - 17 June 2022, Busan, South Korea



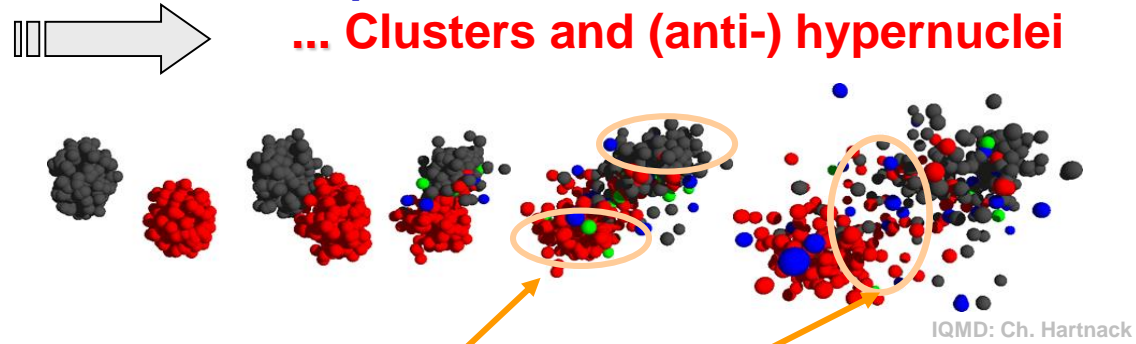
The ,holy grail‘ of heavy-ion physics:

The phase diagram of QCD



Experimental observables:

... Clusters and (anti-) hypernuclei



- projectile/target spectators \rightarrow heavy cluster formation
- midrapidity \rightarrow light clusters

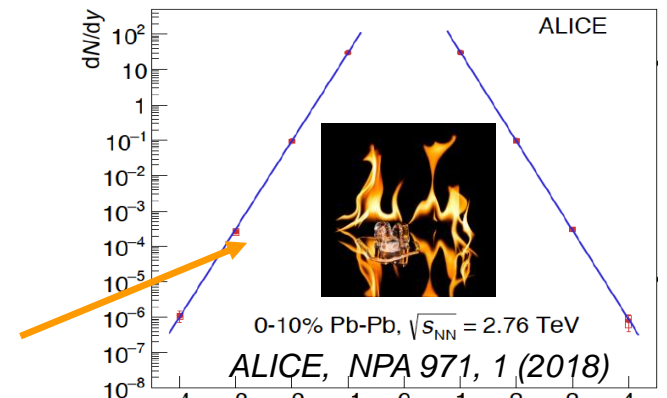
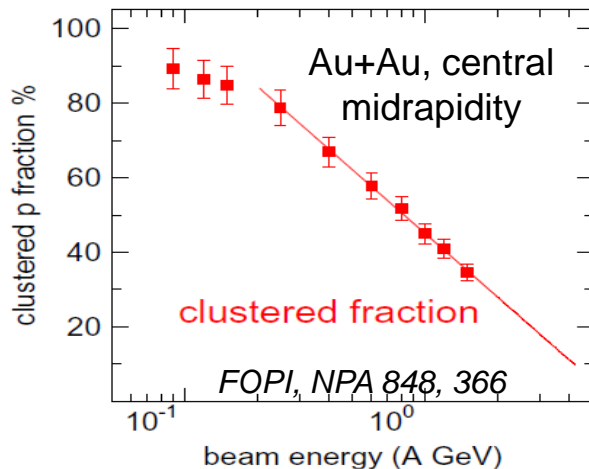
! Hyperons are created in participant zone

(Anti-) hypernuclei production:

- at mid-rapidity by coalescence of Λ with nucleons during expansion
- at projectile/target rapidity by rescattering/absorption of Λ by spectators

High energy HIC:
,Ice in a fire‘ puzzle:
how the weakly bound
objects can be formed
and survive in a hot
environment ?!

- Clusters are very abundant at low energy



Modeling of cluster and hypernuclei formation

Existing models for clusters formation:

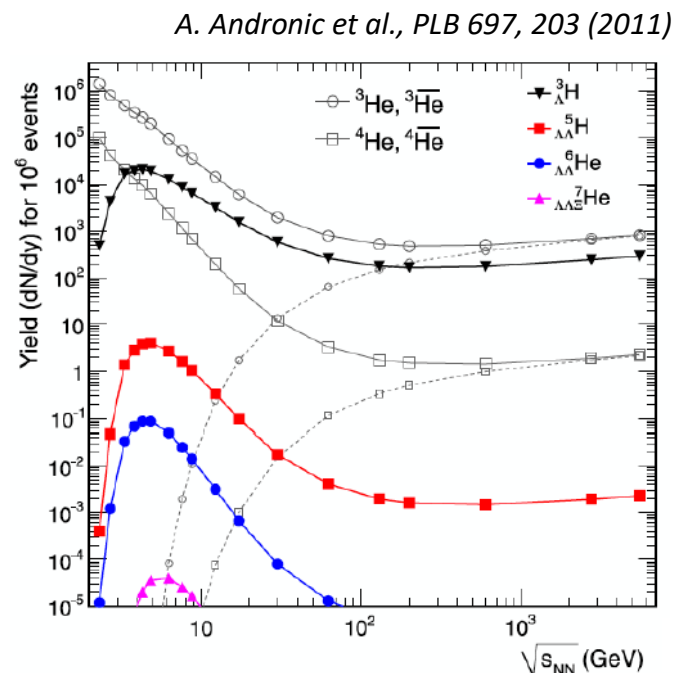
□ statistical model:

- assumption of thermal equilibrium

□ coalescence model:

- determination of clusters at a freeze-out time by coalescence radii in coordinate and momentum space

→ don't provide information on the dynamical origin of clusters formation



In order to understand the **microscopic origin** of cluster formation one needs a realistic model for the **dynamical time evolution** of the HIC

→ transport models:

dynamical modeling of cluster formation based on interactions:

– via potential interaction (**potential mechanism**) → discussed in this talk

-- by scattering (**kinetic mechanism**)

Cf. Posters: POS-LF-08: SMASH - Jan Staudenmaier
POS-RES-08: PHQMD – Gabriele Coci



PHQMD: a unified n-body microscopic transport approach for the description of heavy-ion collisions and **dynamical cluster formation** from low to ultra-relativistic energies

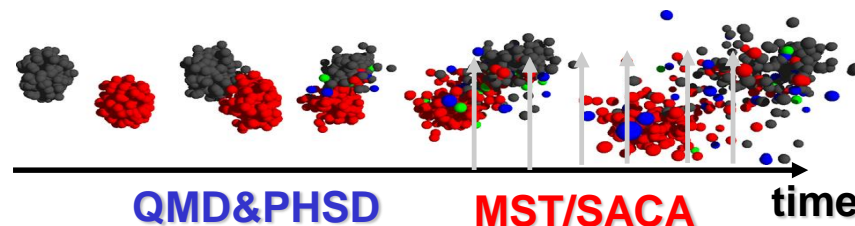
Realization: combined model **PHQMD = (PHSD & QMD) & (MST/SACA)**

Parton-Hadron-Quantum-Molecular Dynamics

Initialization → propagation of baryons:
QMD (Quantum-Molecular Dynamics)

Propagation of partons (quarks, gluons) and mesons
+ **collision integral** = interactions of hadrons and partons (QGP)
from **PHSD (Parton-Hadron-String Dynamics)**

Cluster recognition:
SACA (Simulated Annealing Clusterization Algorithm)
or **MST (Minimum Spanning Tree)**



QMD propagation

□ **Generalized Ritz variational principle:** $\delta \int_{t_1}^{t_2} dt \langle \psi(t) | i \frac{d}{dt} - H | \psi(t) \rangle = 0.$

Assume that $\psi(t) = \prod_{i=1}^N \psi(\mathbf{r}_i, \mathbf{r}_{i0}, \mathbf{p}_{i0}, t)$ for N particles (neglecting antisymmetrization !)

Ansatz: **trial wave function** for one particle "i" :

Gaussian with width L centered at r_{i0}, p_{i0}

$$\psi(\mathbf{r}_i, \mathbf{r}_{i0}, \mathbf{p}_{i0}, t) = C e^{-\frac{1}{4L} \left(\mathbf{r}_i - \mathbf{r}_{i0}(t) - \frac{\mathbf{p}_{i0}(t)}{m} t \right)^2} \cdot e^{i \mathbf{p}_{i0}(t) (\mathbf{r}_i - \mathbf{r}_{i0}(t))} \cdot e^{-i \frac{\mathbf{p}_{i0}^2(t)}{2m} t}$$

$$L = 4.33 \text{ fm}^2$$

□ **Equations-of-motion (EoM)** for **Gaussian centers** in coordinate and momentum space:

$$\dot{r}_{i0} = \frac{\partial \langle H \rangle}{\partial p_{i0}} \quad \dot{p}_{i0} = - \frac{\partial \langle H \rangle}{\partial r_{i0}}$$

Hamiltonian: $H = \sum_i H_i = \sum_i (T_i + V_i) = \sum_i (T_i + \sum_{j \neq i} V_{i,j})$

$$V_{i,j} = V(\mathbf{r}_i, \mathbf{r}_j, \mathbf{r}_{i0}, \mathbf{r}_{j0}, t) = V_{\text{Skyrme}} + V_{\text{Coul}}$$

QMD interaction potential and EoS

The expectation value of the Hamiltonian:

$$\langle H \rangle = \langle T \rangle + \langle V \rangle = \sum_i (\sqrt{p_{i0}^2 + m^2} - m) + \sum_i \langle V_{Skyrme}(\mathbf{r}_{i0}, t) \rangle$$

□ **Skyrme potential ('static') *** :

$$\langle V_{Skyrme}(\mathbf{r}_{i0}, t) \rangle = \alpha \left(\frac{\rho_{int}(\mathbf{r}_{i0}, t)}{\rho_0} \right) + \beta \left(\frac{\rho_{int}(\mathbf{r}_{i0}, t)}{\rho_0} \right)^\gamma$$

	α (MeV)	β (MeV)	γ	K [MeV]
S	-390	320	1.14	200
H	-130	59	2.09	380

□ **modified interaction density (with relativistic extension):**

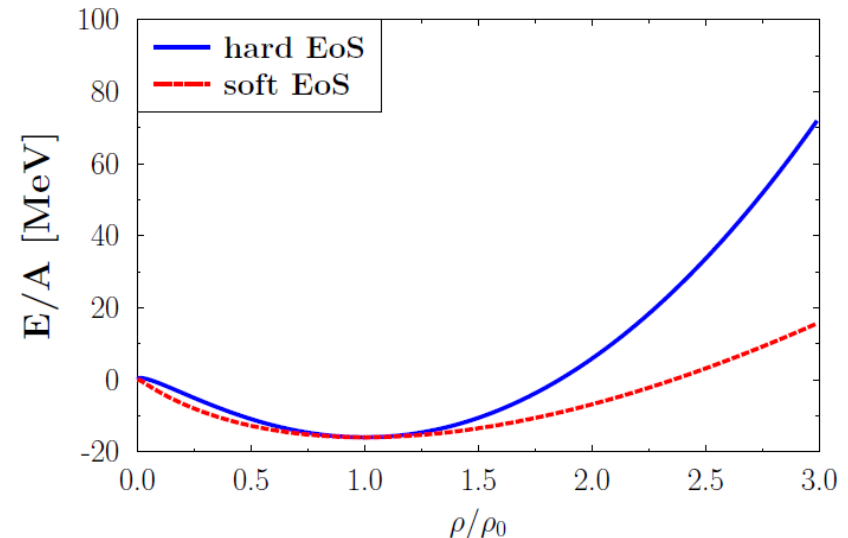
$$\rho_{int}(\mathbf{r}_{i0}, t) \rightarrow C \sum_j \left(\frac{4}{\pi L} \right)^{3/2} e^{-\frac{4}{L} (\mathbf{r}_{i0}^T(t) - \mathbf{r}_{j0}^T(t))^2} \times e^{-\frac{4\gamma_{cm}^2}{L} (\mathbf{r}_{i0}^L(t) - \mathbf{r}_{j0}^L(t))^2},$$

❖ **HIC ↔ EoS for infinite matter at rest**

○ **compression modulus K of nuclear matter:**

$$K = -V \frac{dP}{dV} = 9\rho^2 \frac{\partial^2 (E/A(\rho))}{(\partial\rho)^2} \Big|_{\rho=\rho_0}$$

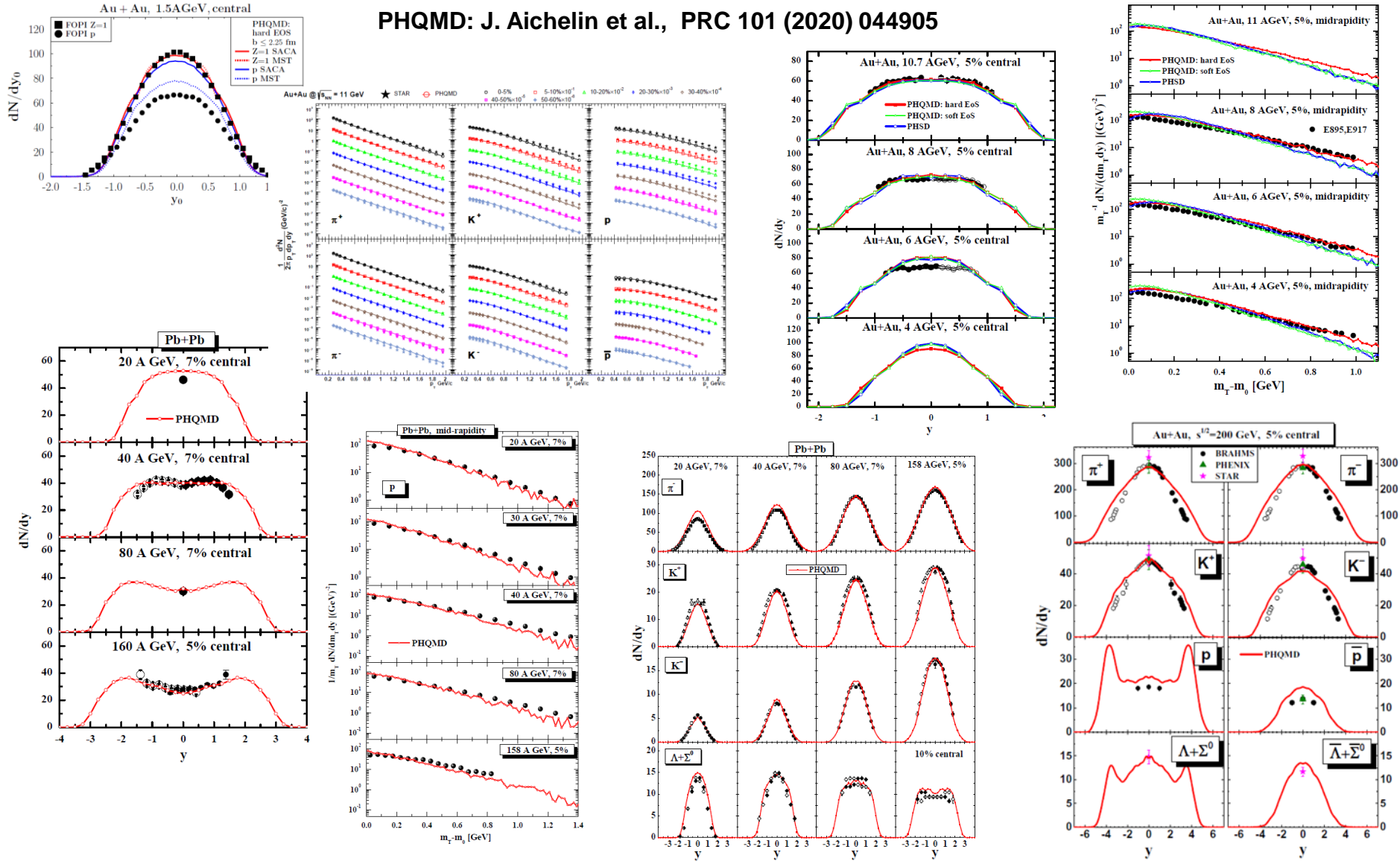
EoS for infinite matter at rest



* Work in progress: implementation of momentum dependent potential (M. Winn)

Highlights: PHQMD ,bulk' dynamics from SIS to RHIC

PHQMD: J. Aichelin et al., PRC 101 (2020) 044905



PHQMD provides a good description of hadronic 'bulk' observables from SIS to RHIC energies

Cluster recognition: Minimum Spanning Tree (MST)

R. K. Puri, J. Aichelin, J.Comp. Phys. 162 (2000) 245-266

The **Minimum Spanning Tree (MST)** is a **cluster recognition** method applicable for the (asymptotic) **final states** where coordinate space correlations may only survive for bound states.

The MST algorithm searches for **accumulations of particles in coordinate space**:

1. Two particles are **'bound'** if their **distance in the cluster rest frame** fulfills

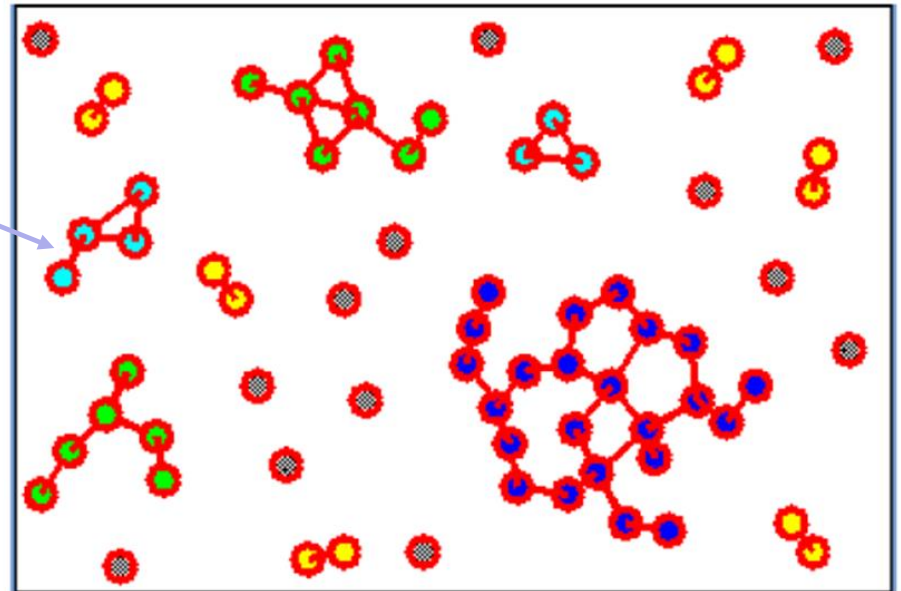
$$|\vec{r}_i - \vec{r}_j| \leq 4 \text{ fm}$$

2. Particle is **bound to a cluster** if it **bounds with at least one particle of the cluster**.

* Remark:

inclusion of an additional momentum cuts (coalescence) lead to a small changes: particles with large relative momentum are mostly not at the same position (V. Kireyeu, Phys.Rev.C 103 (2021) 5)

- **MST + extra condition:**
negative binding energy for identified clusters



Clusters in semi-classical QMD models

Limitation of semi-classical models (as QMD):

- ❑ Clusters in QMD are semiclassical bound objects (with a binding energy close to the Weizsäcker mass formula) but **not quantum system** with a defined ground state
- ❑ In bound QMD clusters kinetic energy can be therefore accumulated by one of the nucleons which may escape (what is not possible in a quantum cluster)
- ➔ We have therefore to **fix a time** at which we analyse the clusters. This choice influences the multiplicity. We verified that it does not influence the form of
 - the rapidity distribution
 - the p_T distribution
 - ratio of particles

➔ To compare the PHQMD results **at different rapidities** we have to chose the same **'physical time'** :

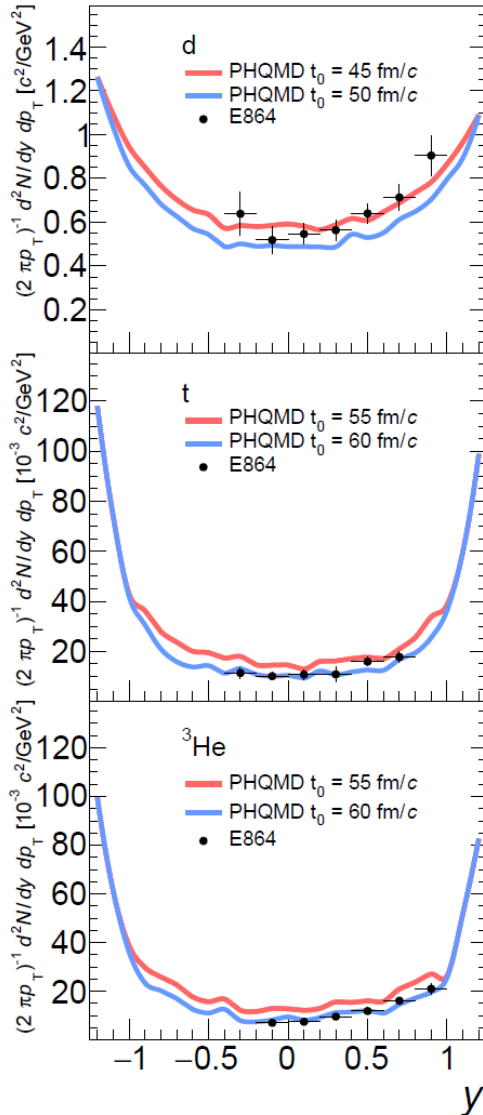
$$t = t_0 \cosh(y)$$

where t_0 is the time taken at $y=0$ (in the center-of-mass system) to compensate for the **time dilatation**

Cluster production in HIC at AGS energies

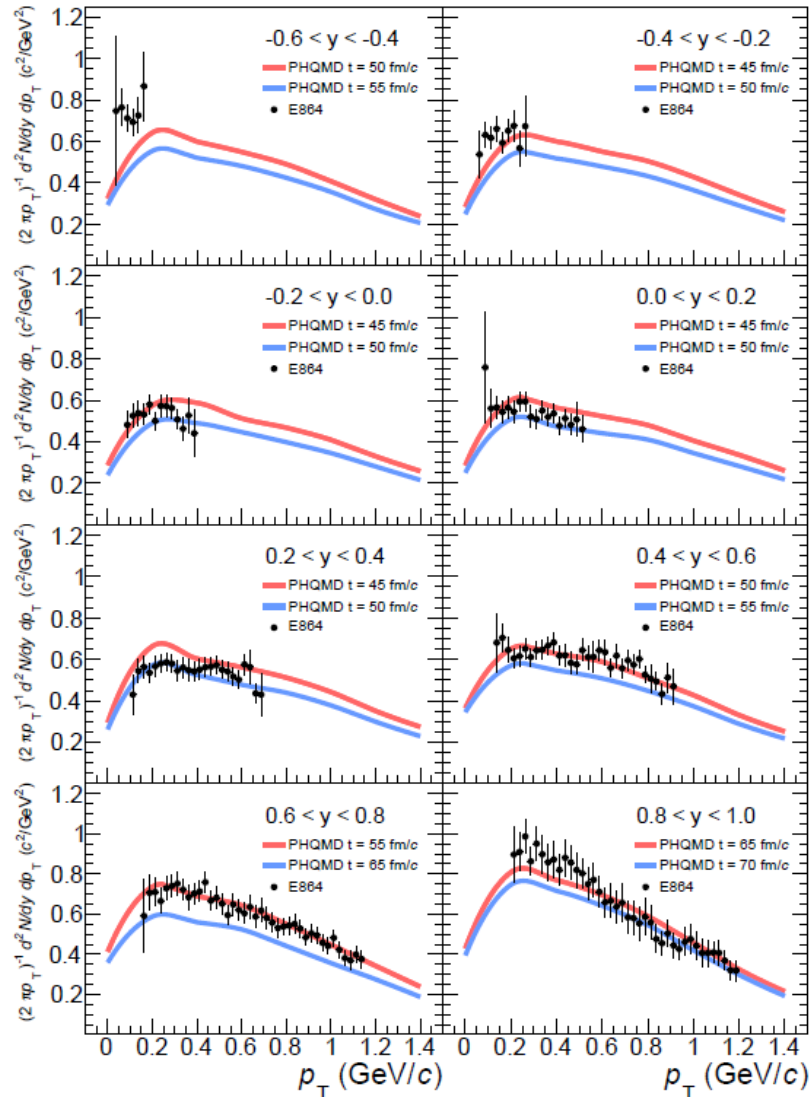
y- distributions of d, t, ^3He

Au+Pb@10.6 AGeV



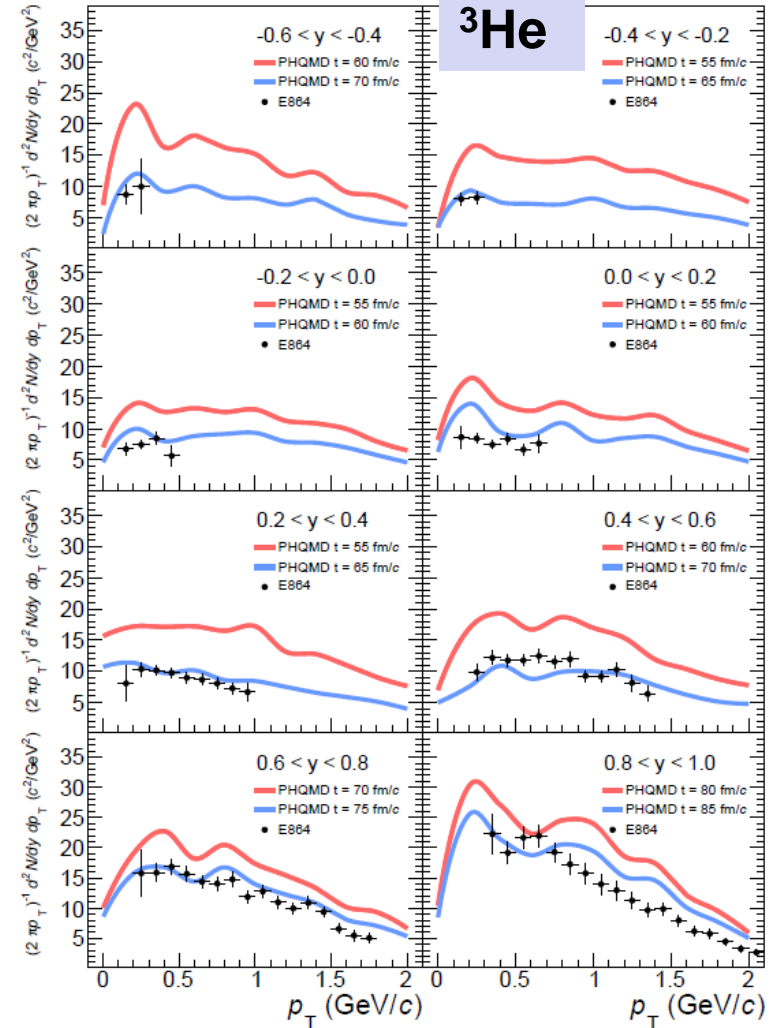
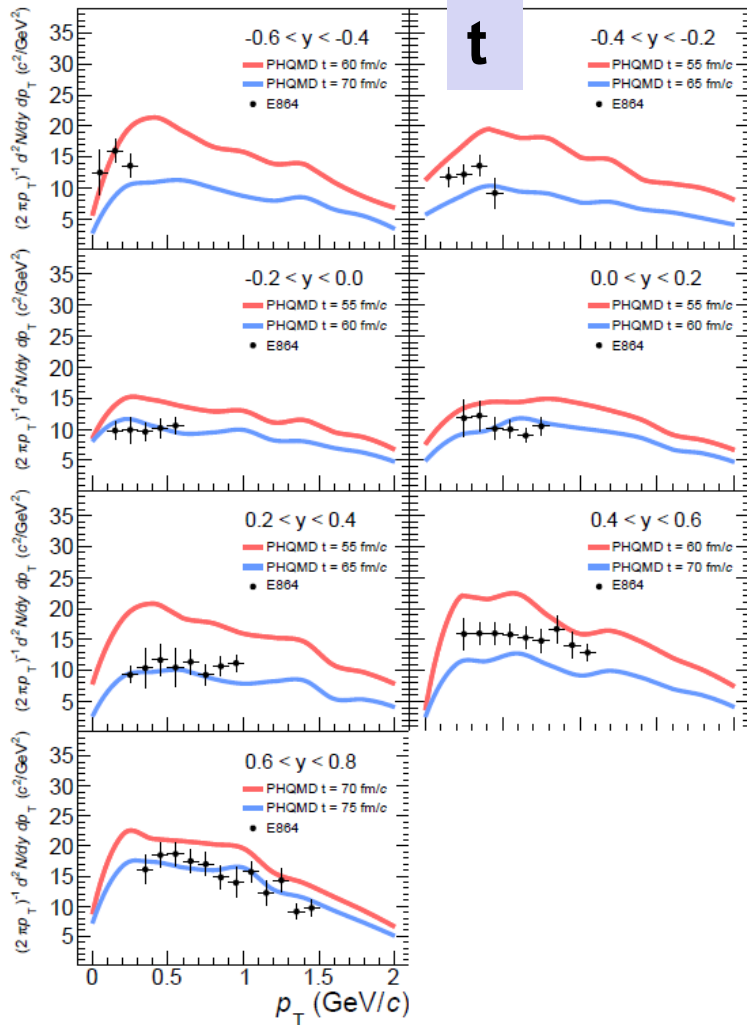
p_T - distribution of deuterons

Au+Pb@10.6 AGeV



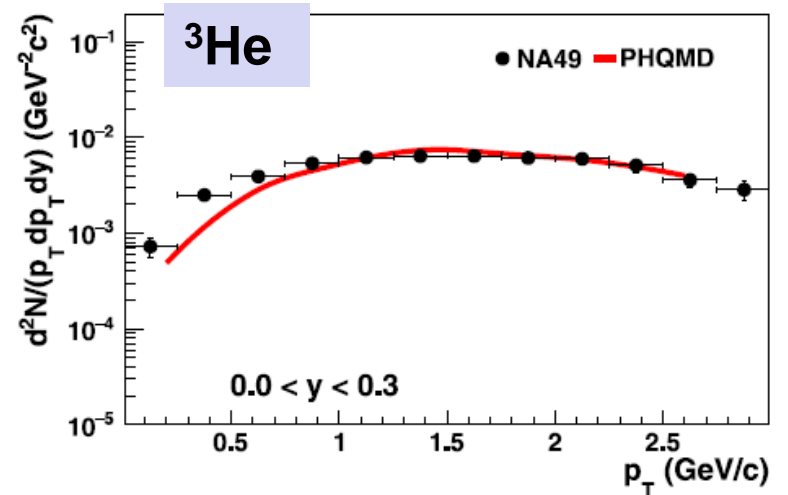
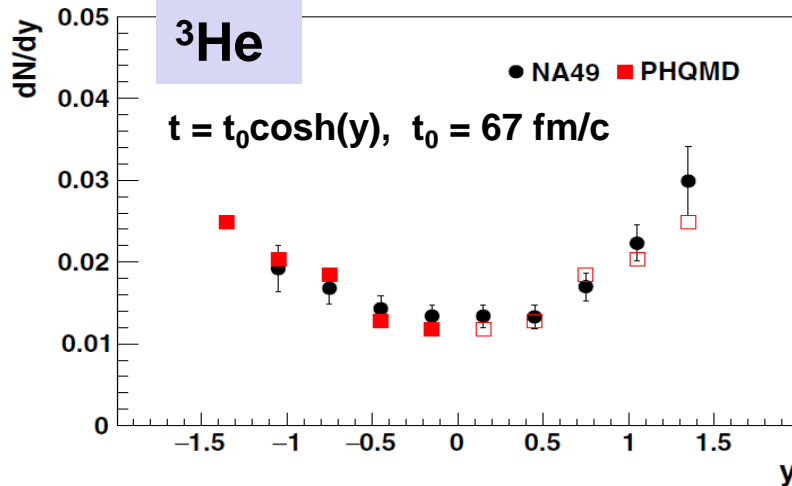
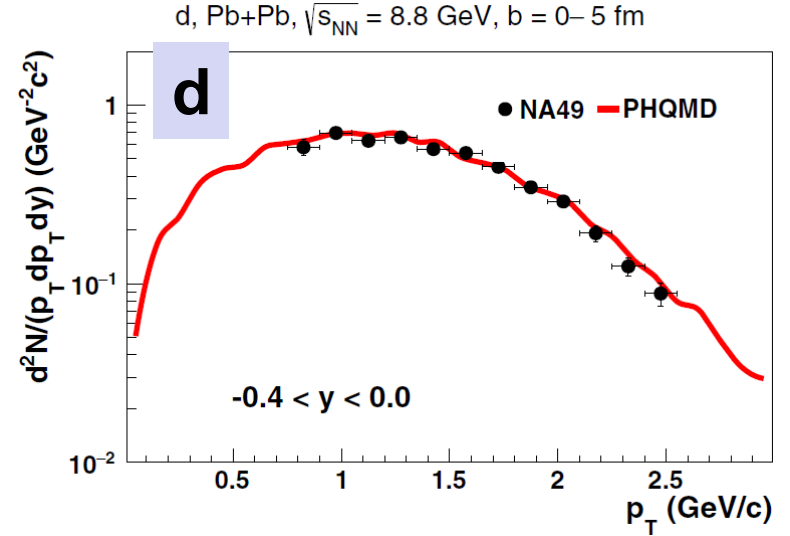
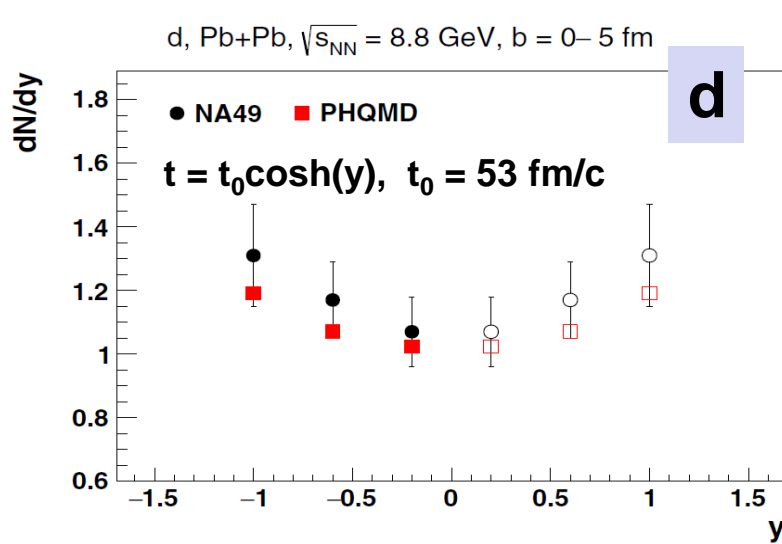
The PHQMD results are taken at $t = t_0 \cosh(y)$, where t_0 is the time at $y=0$

The p_T - distributions of t and ${}^3\text{He}$ from Au+Pb at 10.6 A GeV



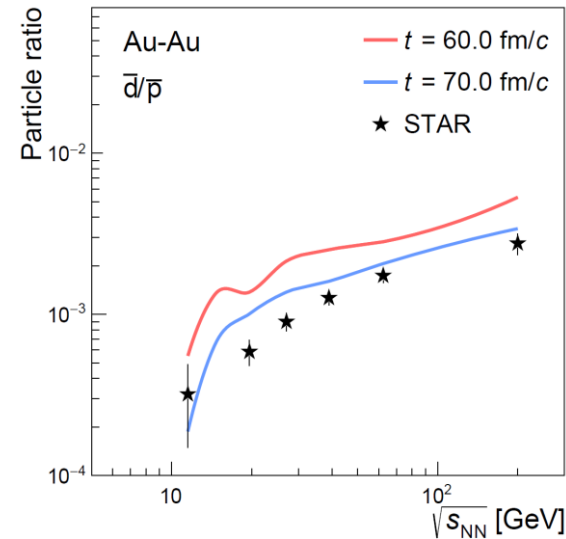
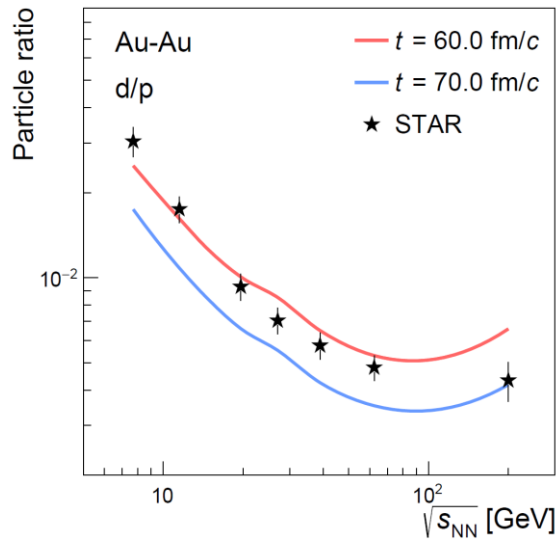
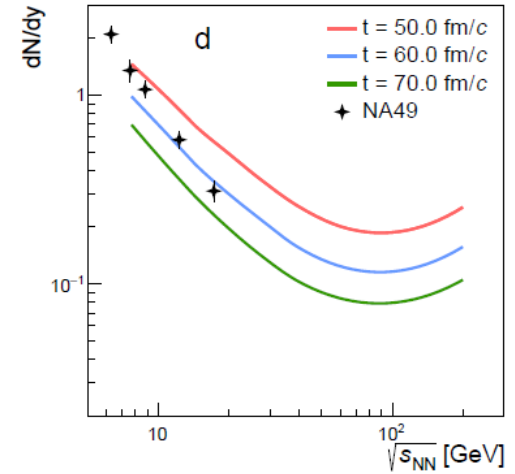
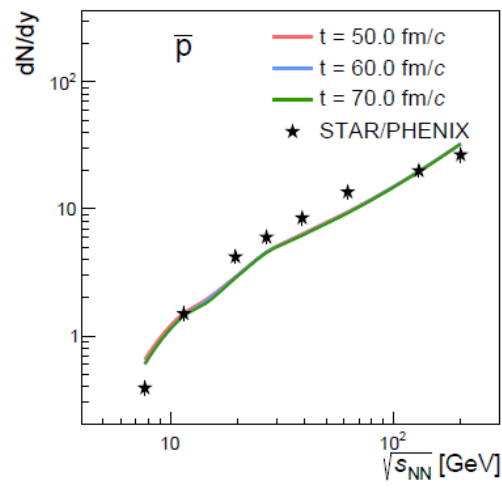
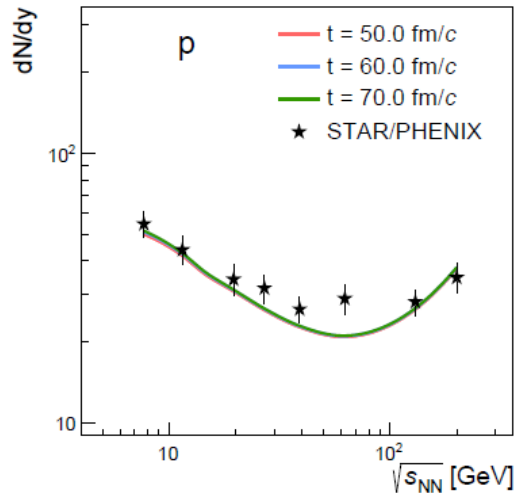
Cluster production in HIC at SPS energies

The rapidity and p_T -distributions of **d** and ${}^3\text{He}$ from Pb+Pb at 30 A GeV



The PHQMD results for **d** and ${}^3\text{He}$ agree with **NA49** data

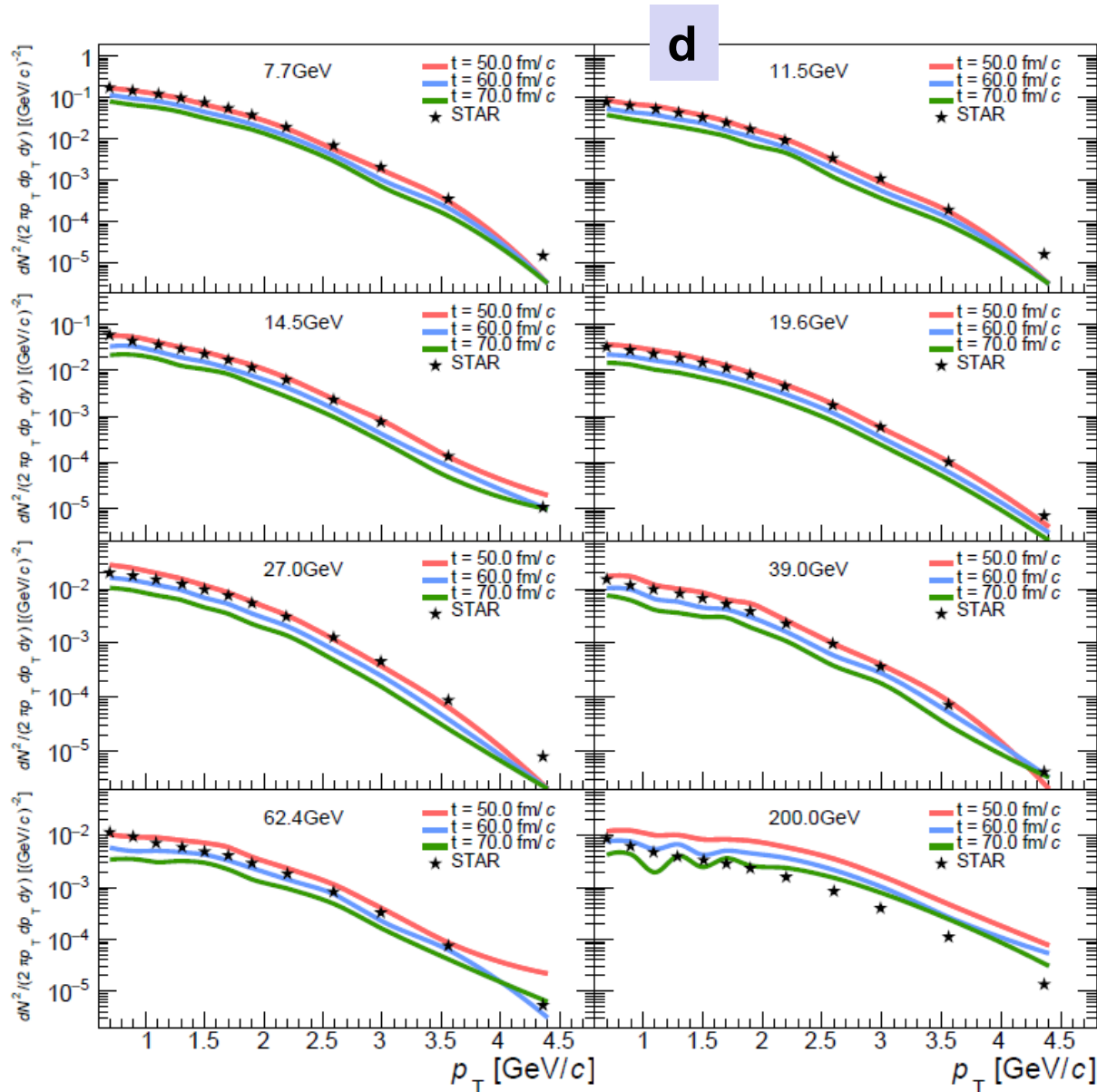
Excitation function of multiplicity of p, \bar{p}, d, \bar{d}



S. Gläsel et al.,
PRC 105 (2022) 1

The p, \bar{p} yields at $y \sim 0$ are stable, the d, \bar{d} yields are better described at $t = 60-70$ fm/c

Deuteron p_T spectra from 7.7 GeV to 200 GeV



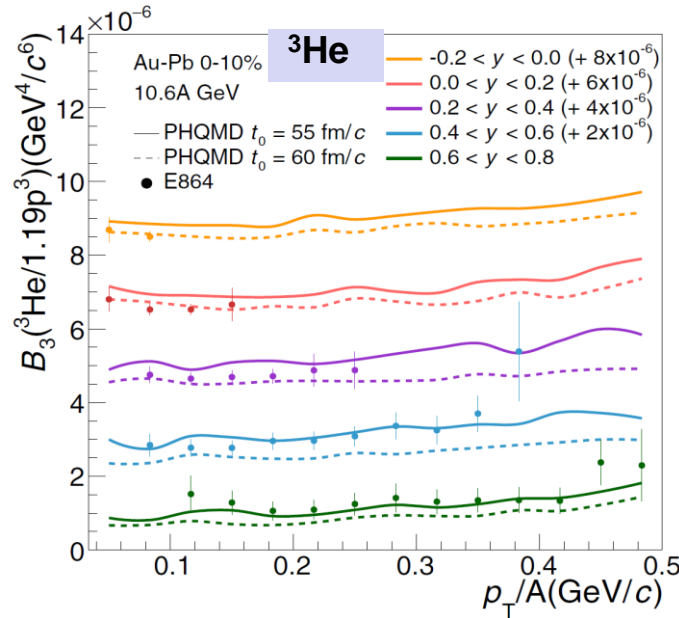
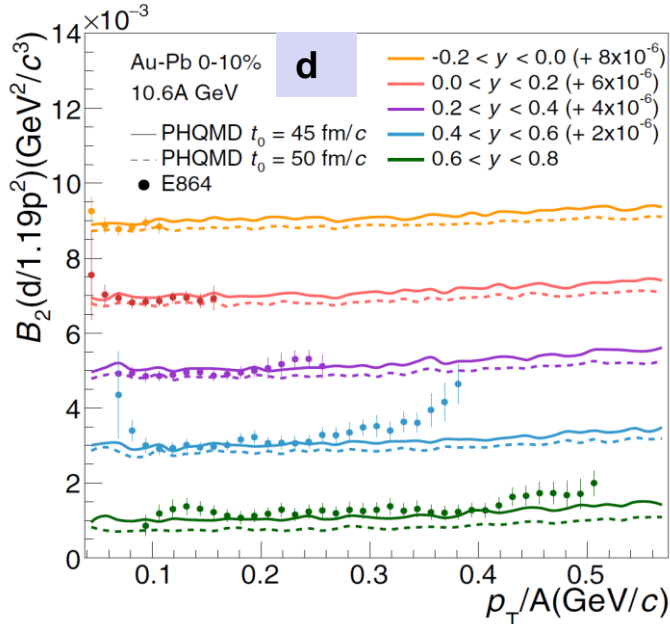
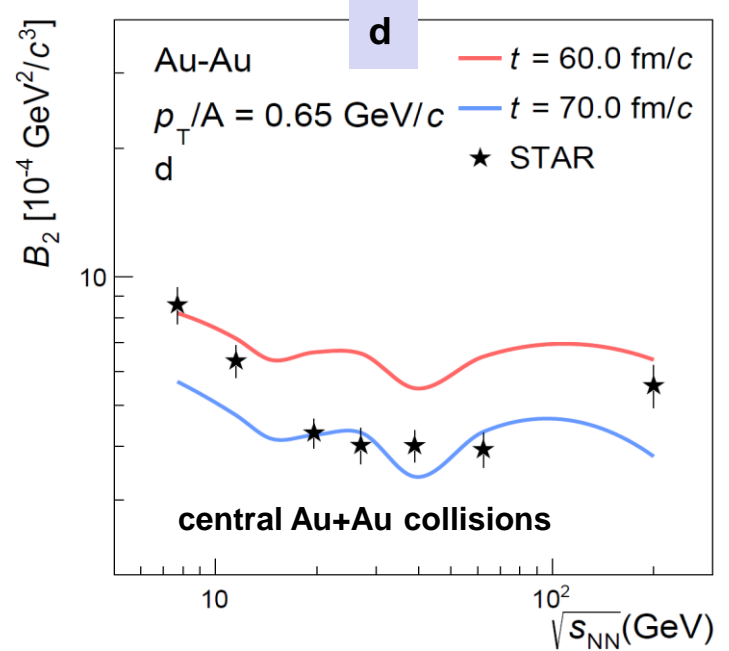
Comparison of the PHQMD results for the **deuteron** p_T -spectra at midrapidity with STAR data

S. Gläsel et al., Phys. Rev. C 105 (2022) 1

Coalescence parameter B_2 :

$$B_2 = \frac{E_d \frac{d^3 N_d}{d^3 P_d}}{\left(E_p \frac{d^3 N_p}{d^3 p_p} \Big|_{p_p = P_d/2} \right)^2}$$

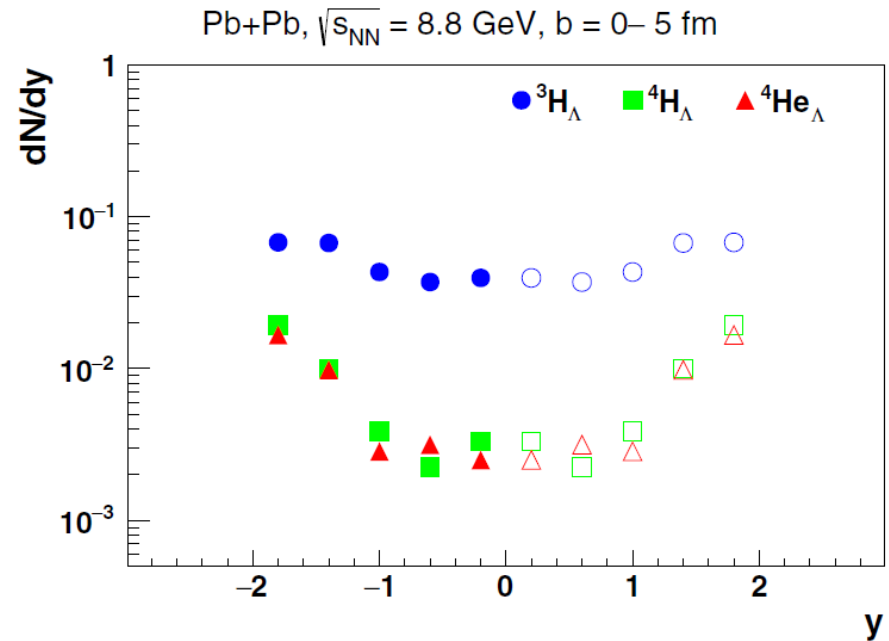
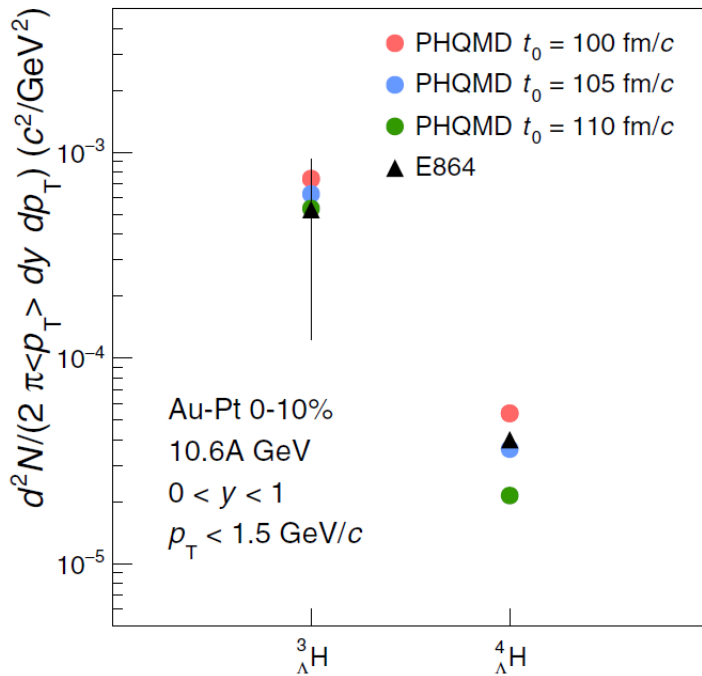
S. Gläsel et al., Phys. Rev. C 105 (2022) 1



$t = t_0 \cosh(y)$

The PHQMD results for **hypernuclei** production in Au+Pt central collisions at 10.6 A GeV

The PHQMD **predictions** for dN/dy of ${}^3\text{H}_\Lambda$, ${}^4\text{H}_\Lambda$ and ${}^4\text{He}_\Lambda$ from central Pb+Pb collisions at 30 A GeV ($\sqrt{s}^{1/2} = 8.8$ GeV)

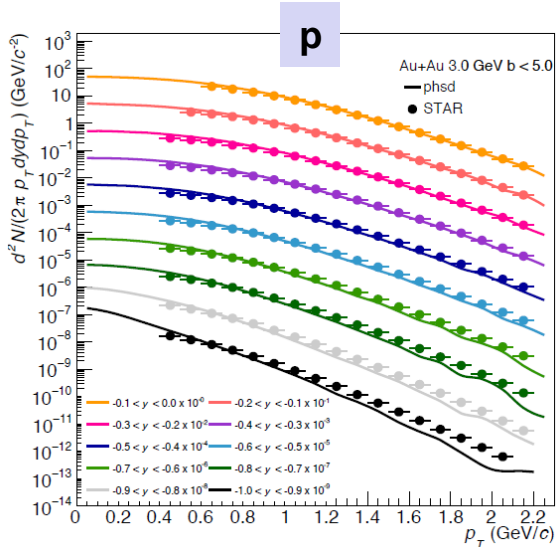


- Assumption on nucleon-hyperon potential: $V_{N\Lambda} = 2/3 V_{NN}$

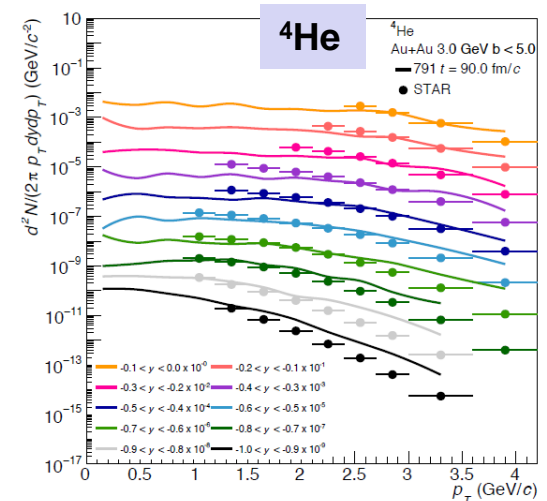
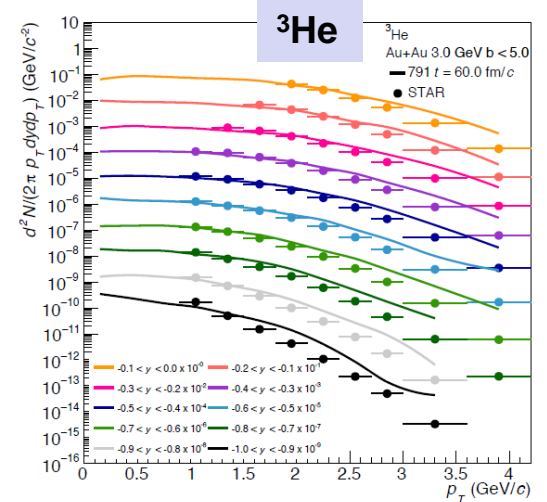
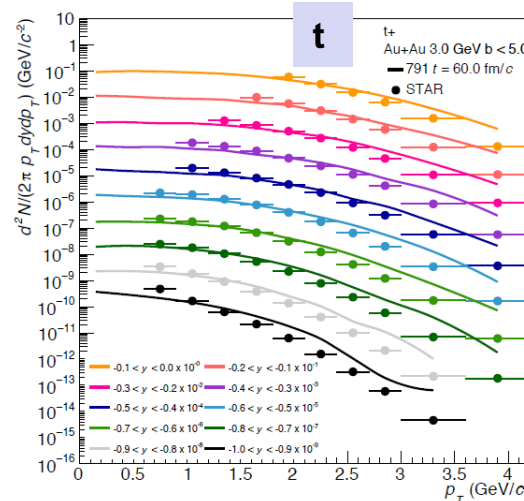
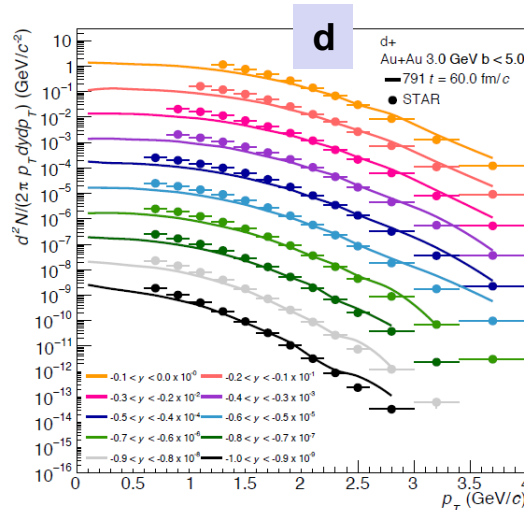
Light cluster production at $s^{1/2} = 3$ GeV

The PHQMD comparison with recent (preliminary) STAR fixed target p_T distribution of p , d , t , ${}^3\text{H}$, ${}^4\text{H}$ from Au+Au central collisions at $\sqrt{s} = 3$ GeV

PHQMD: $t = 60$ fm/c



(preliminary) STAR data – talk by Hui Liu at QM'2022



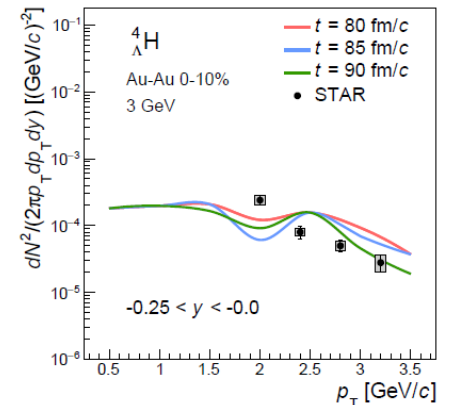
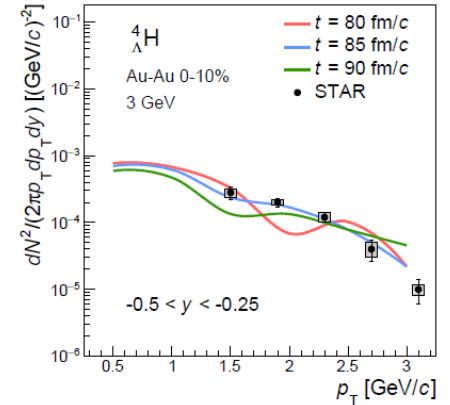
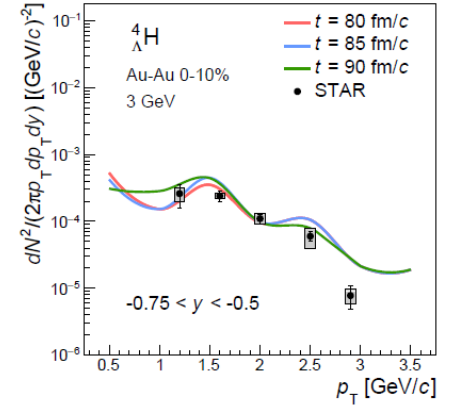
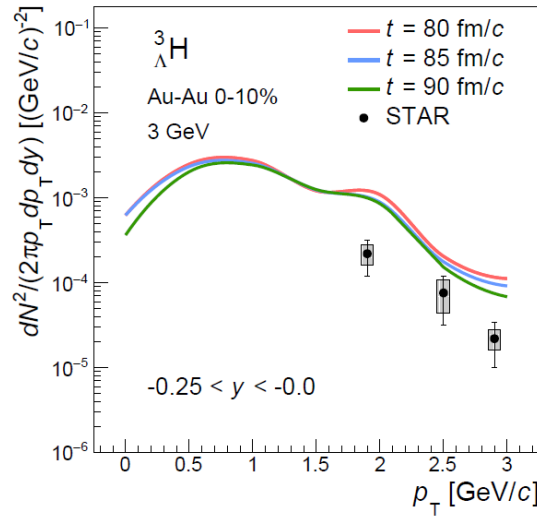
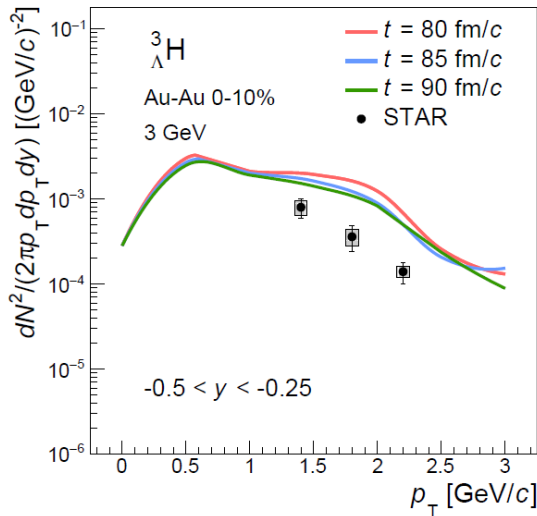
➔ Good description of cluster production

Hypernuclei production at $s^{1/2} = 3$ GeV

The PHQMD comparison with recent STAR fixed target p_T distribution of ${}^3\text{H}_\Lambda$, ${}^4\text{H}_\Lambda$ from Au+Au central collisions at $\sqrt{s} = 3$ GeV

STAR: Phys. Rev. Lett. 128, 202301 (2022)

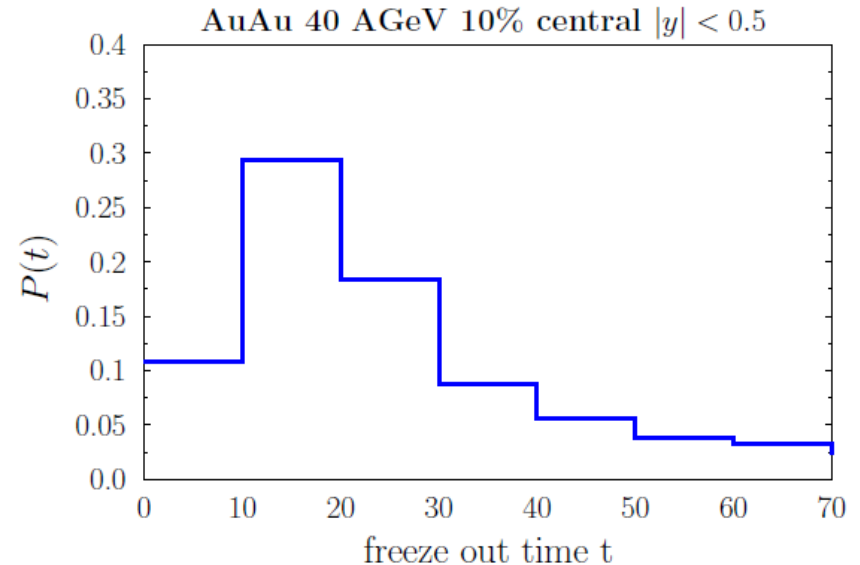
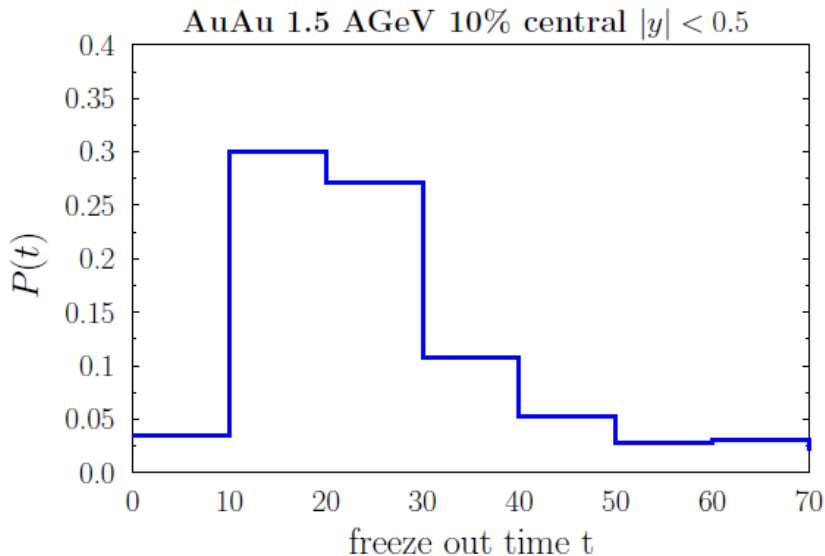
- Assumption for nucleon-hyperon potential: $V_{N\Lambda} = 2/3 V_{NN}$



→ Reasonable description of hypernuclei production at $\sqrt{s} = 3$ GeV

When does the system freeze out?

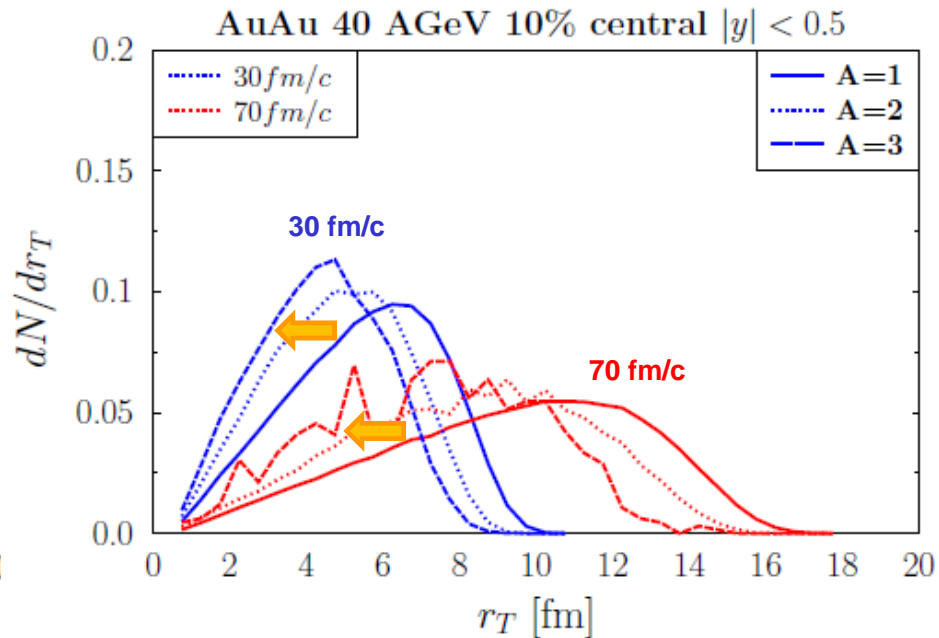
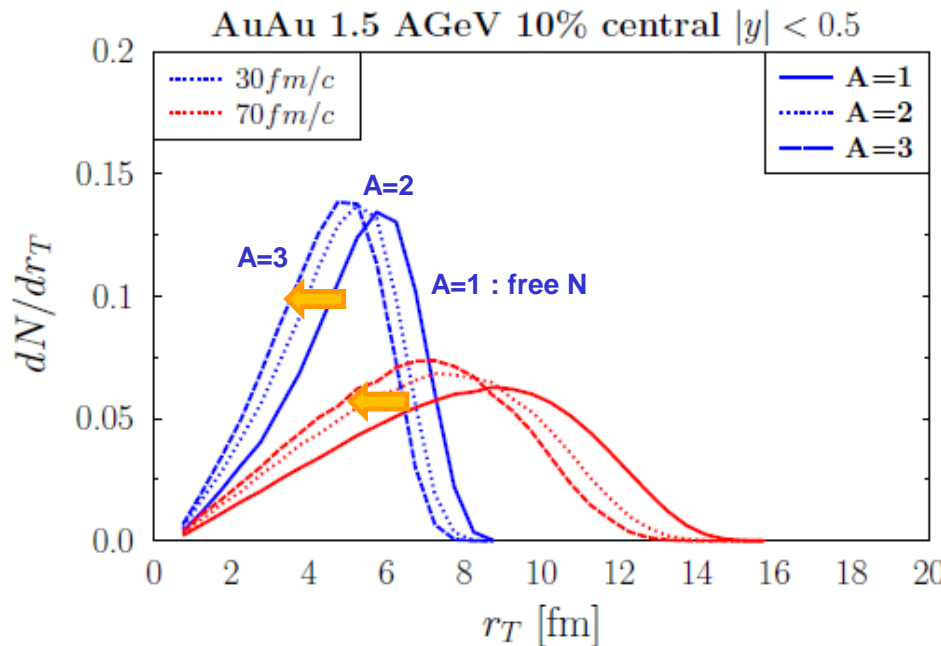
- The normalized distribution of the **freeze-out time of baryons** (nucleons and hyperons) which are finally observed at mid-rapidity $|y| < 0.5$
 - * Here freeze-out time as defined as a **last elastic or inelastic collision**, after that **only potential interaction** between baryons occurs



- ➔ Freeze-out time of baryons in Au+Au at 1.5 AGeV and 40 AGeV:
 - **similar profile** since expansion velocity of mid-rapidity fireball is roughly independent of the beam energy

Where are the clusters formed?

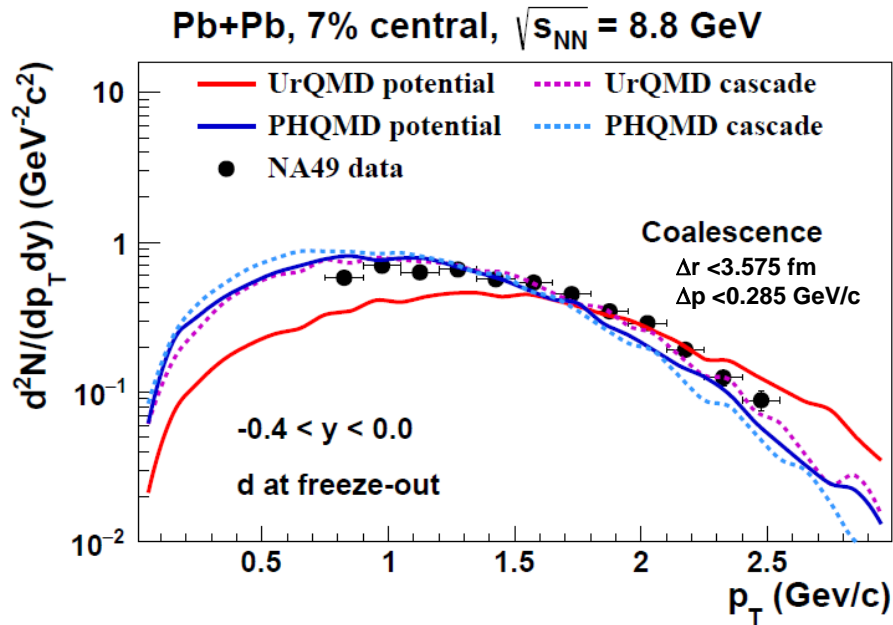
- The snapshot (taken at time 30 and 70 fm/c) of the **normalized distribution of the transverse distance r_T of the nucleons to the center of the fireball.**
- It is shown for $A=1$ (free nucleons) and for the nucleons in $A=2$ and $A=3$ clusters



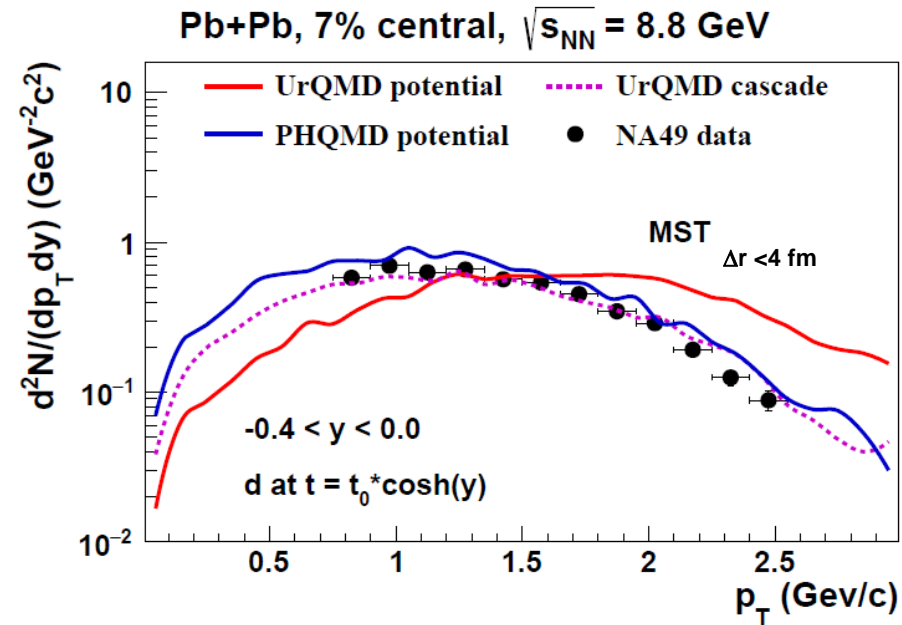
→ **Transverse distance profile** of free nucleons and clusters are different!
 Clusters are mainly formed behind the “front” of free nucleons of the expanding fireball

Comparison of the coalescence and MST for d

Coalescence



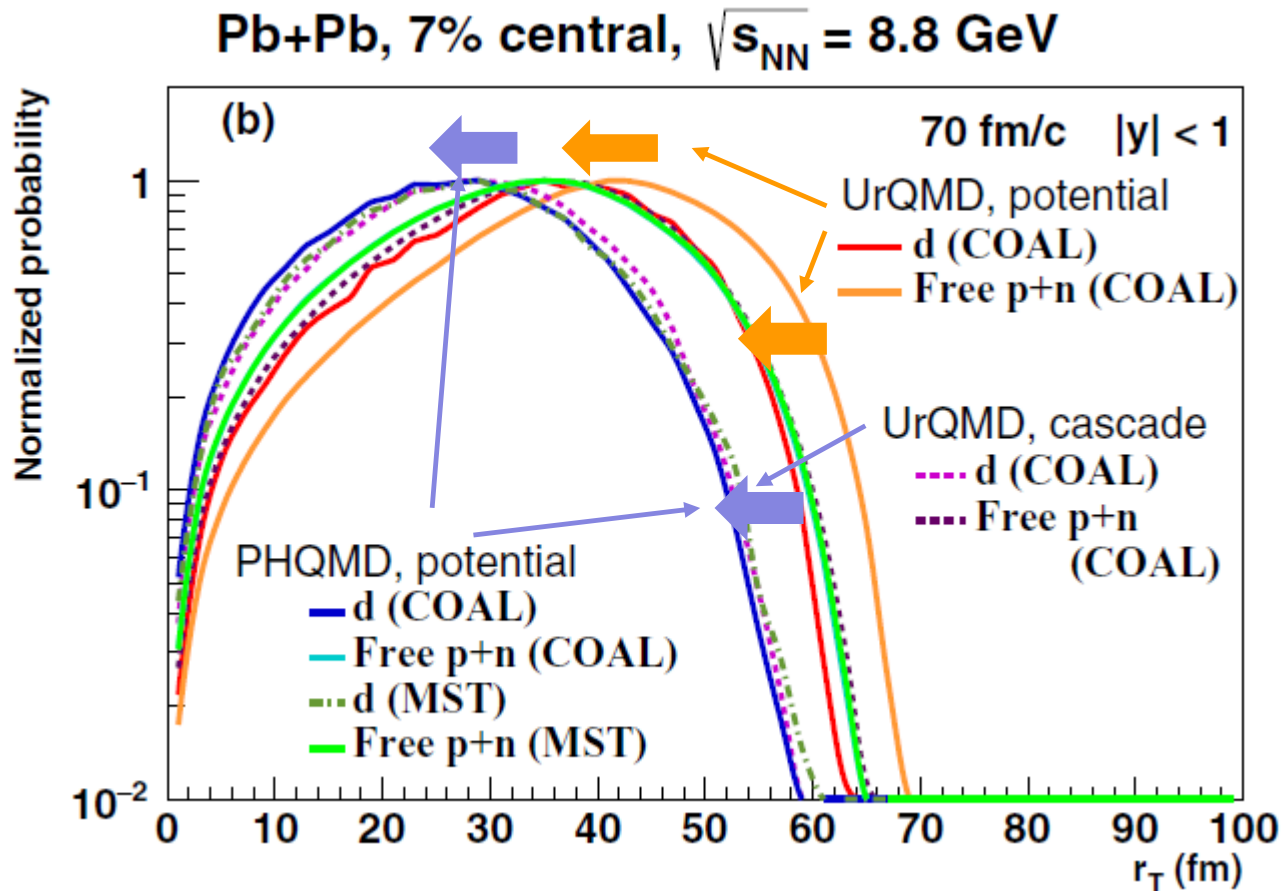
MST



- **Coalescence and MST** give very **similar** multiplicities and y - and p_T -distributions
- PHQMD and UrQMD results in the cascade mode are very similar
- Deuteron production is sensitive to the realization of potential in transport approaches

Coalescence in UrQMD – cf. talk by Tom Reichert (PA-RES, 14.04.22)

Comparison of the coalescence and MST for d



➔ Coalescence as well as the MST procedure show that the deuterons remain in transverse direction closer to the center of the heavy-ion collision than free nucleons.

Summary

- ❑ The **PHQMD** is a **microscopic n-body transport approach** for the description of heavy-ion dynamics and cluster formation
- ❑ Clusters are identified by **Minimum Spanning Tree** model

combined model **PHQMD** = (PHSD & **QMD**) & (**MST** | **SACA**)

- predicts the **dynamical formation of clusters** from SIS to RHIC energies due to the **interactions** among the nucleons
- reproduces cluster data on dN/dy and dN/dp_T as well as **ratios d/p** and \bar{d}/\bar{p} for HI collisions from AGS to top RHIC energies.

A detailed analysis reveals that stable **clusters are formed**

- shortly after elastic and inelastic collisions have ceased
- behind the front of the expanding energetic hadrons
- **since the 'fire' is not at the same place as the 'ice', cluster can survive.**

- ❑ **Coalescence and MST** give very similar deuteron distributions within the PHQMD and UrQMD transport approaches

- ❖ **In progress:** PHQMD with **potential + kinetic mechanisms** for deuteron production

POS-RES-08: PHQMD – Gabriele Coci

Thank you for your attention !

Thanks to the Organizers !