

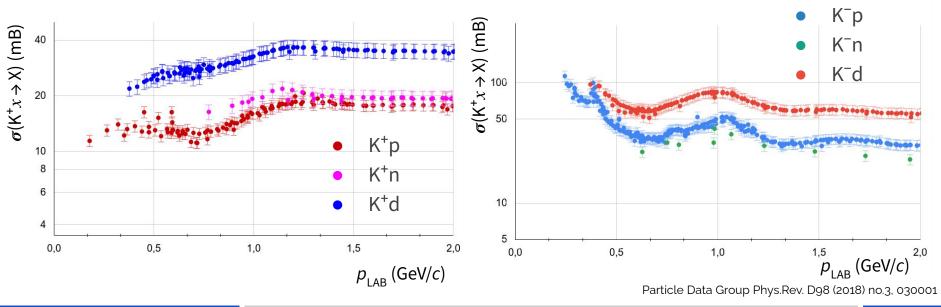
Two and three-body interactions among kaons and nucleons tested at the LHC

Ramona Lea University of Brescia and INFN Pavia

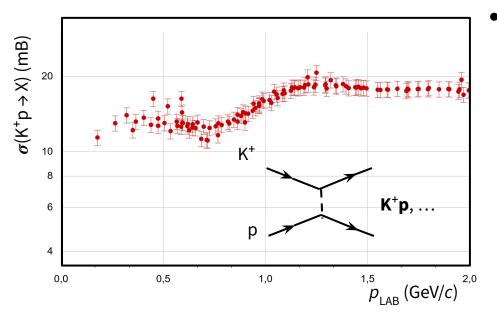
SQM 2022 - The 20th International Conference on Strangeness in Quark Matter

KN and $\overline{K}N$ interactions and how to study them

- Kaon (K) nucleon (N) and anti-Kaon K
 interactions are fundamental for the study of low-energy QCD
 K = K⁺ (u,s̄), K⁰(ds̄); K̄ = K⁻(sū), K̄⁰ (s,d̄)
- Traditionally, these interaction are studied by <u>scattering experiments</u> (K⁺(p,n,d) and K⁻(p,n,d)) at low energies
 - few experimental measurements with big uncertainties and not at low-energy p_{lab} < 50 MeV/c



K⁺p interaction



K⁺p interaction

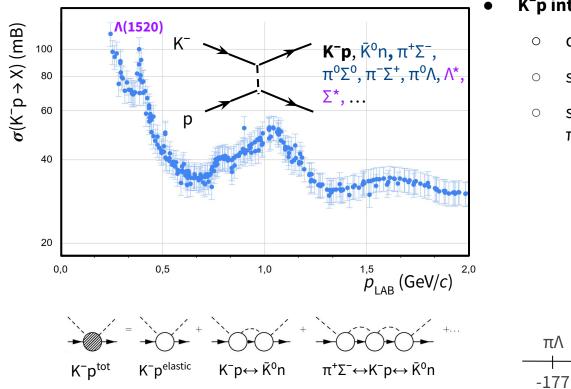
- Repulsive (due to Coulomb and strong interactions)
- No coupled channels
- No resonances
 - well known [1]

[1] K. Aoki and D. Jido, PTEP 2019 no. 1, (2019) 013D01 (arXiv:1806.00925 [nucl-th])

17/06/2022

K⁻p interaction

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K⁻p interaction

• deeply attractive

πΣ

-100

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- several resonances
- several **coupled-channels** (\bar{K}^0 n, $\pi^+\Sigma^-$, $\pi^0\Sigma^0$, $\pi^-\Sigma^+$, $\pi^0\Lambda$)

K⁻p

 systems close to the K⁻p threshold and with the same quantum numbers



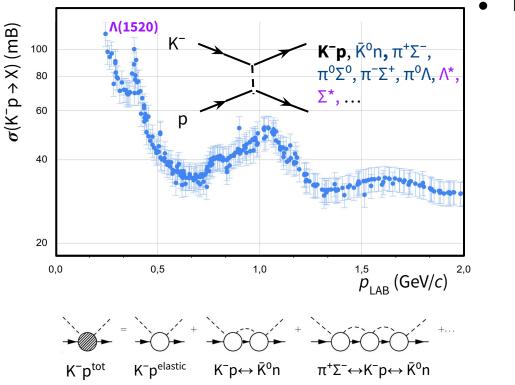
E(MeV/c)

3

Ē⁰n

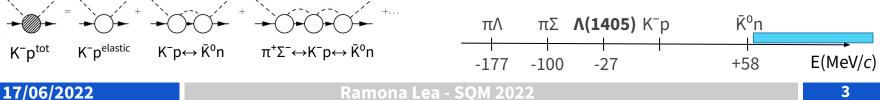
+58

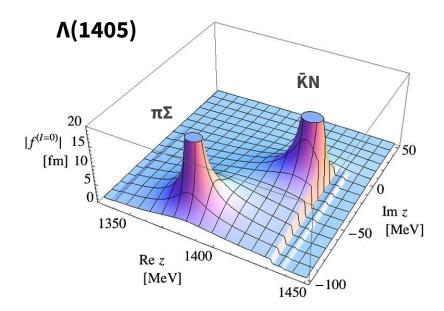
K⁻p interaction



K⁻**p** interaction

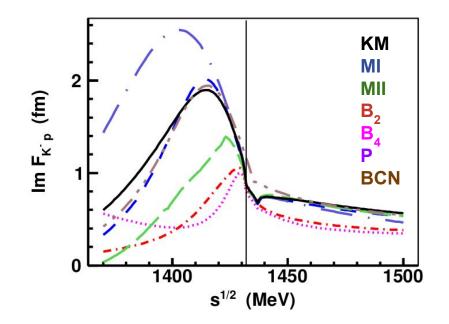
- deeply attractive Ο
- several resonances Ο
- several **coupled-channels** (\bar{K}^0 n, $\pi^+\Sigma^-$, $\pi^0\Sigma^0$, Ο $\pi^{-}\Sigma^{+},\pi^{0}\Lambda$
 - systems close to the K⁻p threshold and with the same quantum numbers
 - $\bar{K}N \leftrightarrow \pi\Sigma$ dynamics leads to the formation of the **Λ(1405)**, ~27 MeV below K⁻p threshold





- Nature of Λ(1405): dynamically generated resonance
 - Models based on below-threshold extrapolations
 - pole positions is model dependent (relative contributions not measured experimentally)

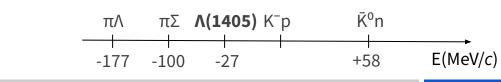


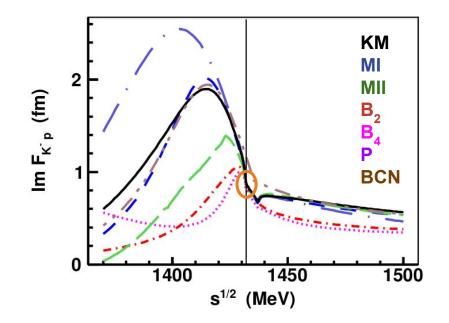


- Nature of Λ(1405): dynamically generated resonance
 - Models based on below-threshold extrapolations
 - pole positions is model dependent (relative contributions not measured experimentally)
 - State-of-the-art chiral models (*x*EFT) are in agreement above threshold
 - Large discrepancies in the region below threshold

A. Cieplý et al, arxiv:2001.08621

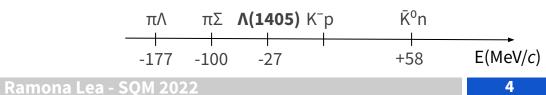
- KM Y. Ikeda, et al. NPA 881 (2012) 98
- MI , MII Z. H. Guo, et al. PRC 87 (2013) 035202
- B2 , B4 M. Mai, et al, EPJ A 51 (2015) 30
- P A. C., J. Smejkal, NPA 881 (2012) 115
- BCN A. Feijoo, et al, PRC 99 (2019) 035211

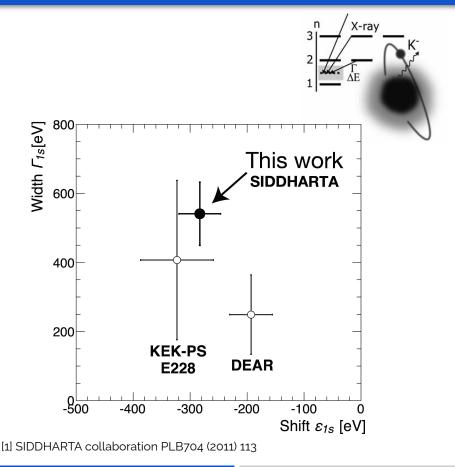




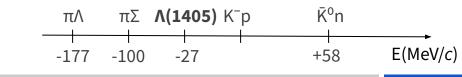
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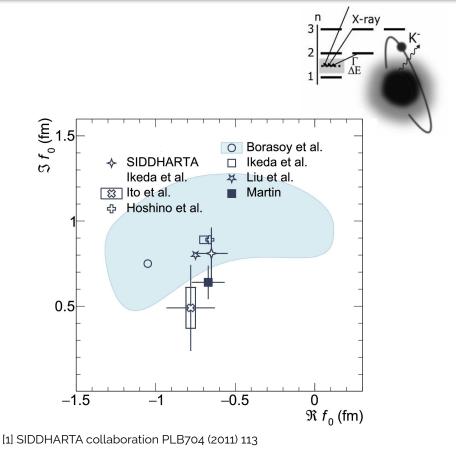
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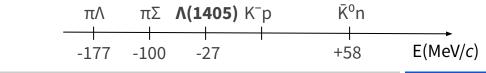


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 - Large discrepancies in the region below threshold
 - Constraint at threshold by SIDDARTHA measurement [1] of kaonic hydrogen 1s level shift and width
 - scattering length

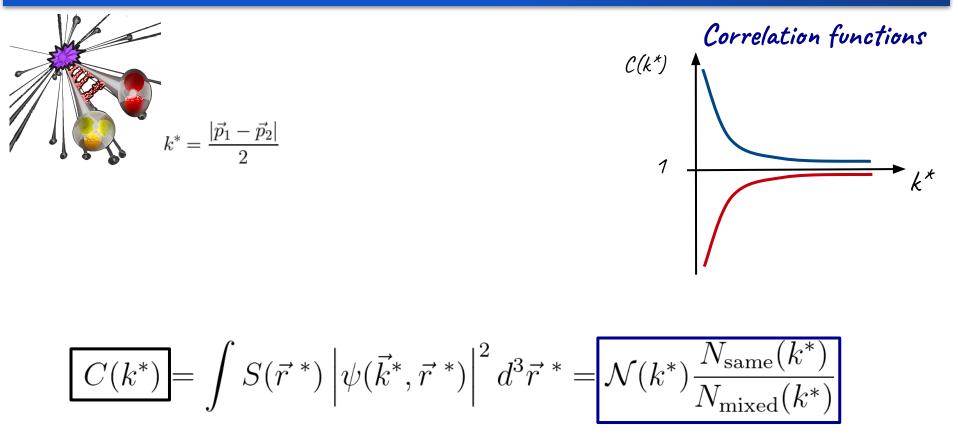


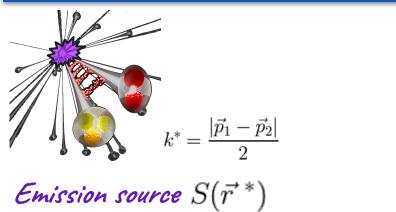
Two particle momentum correlation measured with ALICE at the LHC

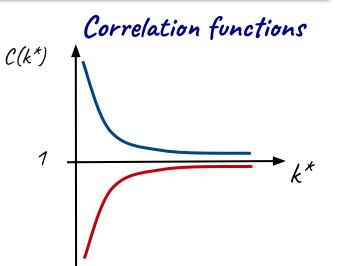
- KN and $\overline{K}N$ interaction
 - ALICE collaboration PRL 124 (2020) 9, 092301
 - ALICE collaboration PLB 822 (2021) 136708
 - ALICE collaboration arXiv: 2205.15176

• and other interactions:

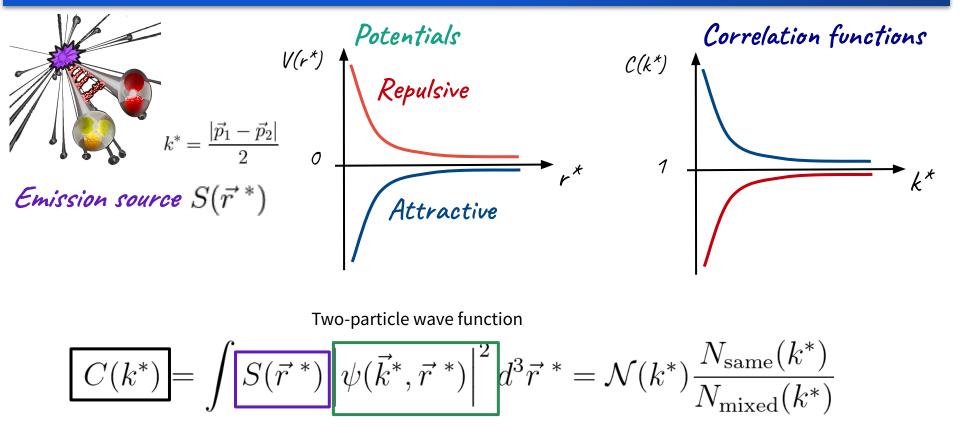
- pp, pA, AA: ALICE collaboration PRC 99(2019)
- ΛΛ: ALICE collaboration PLB 797 (2019) 134822
- o pE: ALICE collaboration PRL 123 (2019) 134822
- \circ p Σ° :ALICE collaboration PLB 805 (2020) 135419
- o pΩ: ALICE collaboration Nature 588 (2020) 232-238
- p**\$**: ALICE collaboration PRL 127 (2021) 172301
- B-**B**:ALICE collaboration PLB B 829 (2022) 137060
- pΛ: ALICE collaboration arXiv:2104.04427
- pD: ALICE collaboration arXiv:2201.05352
- ο ΛΞ: ALICE collaboration arXiv:2204.10258
- ppp and pp**Λ**: ALICE collaboration arXiv:2206.03344

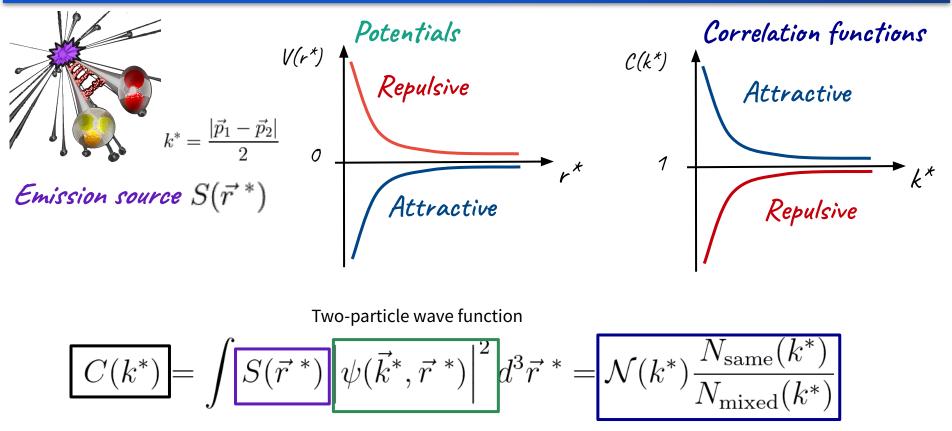






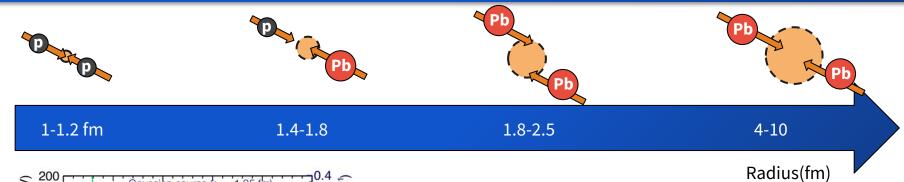
$$C(k^*) = \int S(\vec{r}^*) \left| \psi(\vec{k}^*, \vec{r}^*) \right|^2 d^3 \vec{r}^* = \mathcal{N}(k^*) \frac{N_{\text{same}}(k^*)}{N_{\text{mixed}}(k^*)}$$

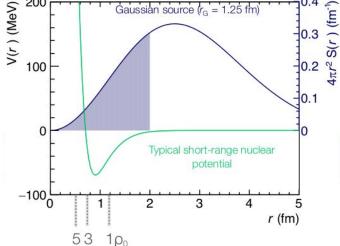




Measure $C(k^*) \rightarrow$ fixing the source $S(r^*)$, study the interaction

... from small to large systems

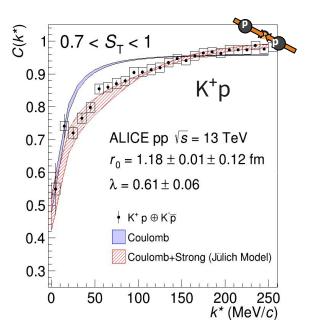




• By changing the colliding system it is possible to probe interaction distances ranging from ~1 fm up to ~10 fm

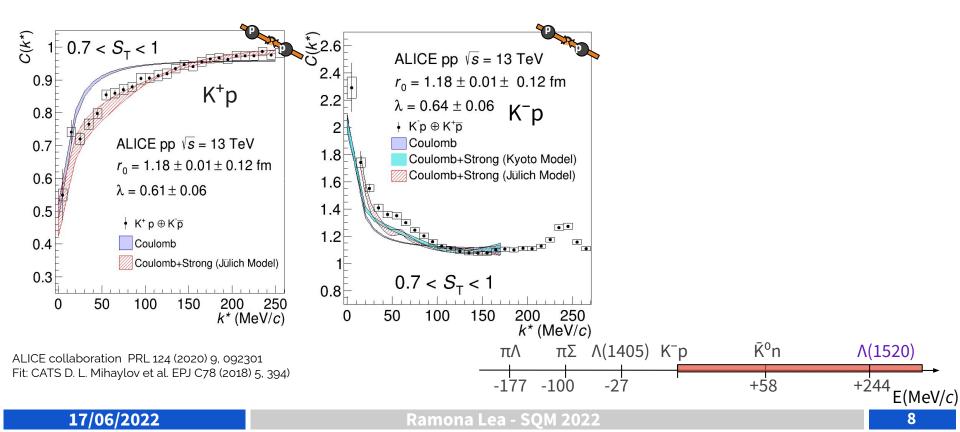
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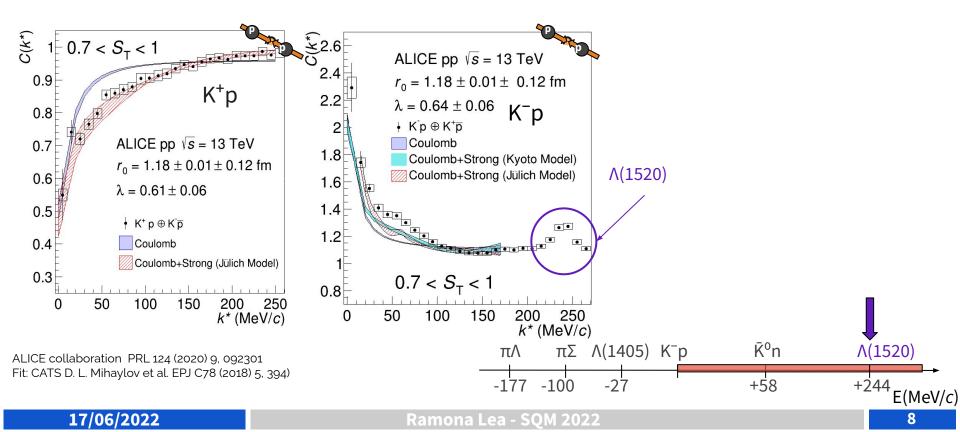
Two particle momentum correlation measured with ALICE at the LHC

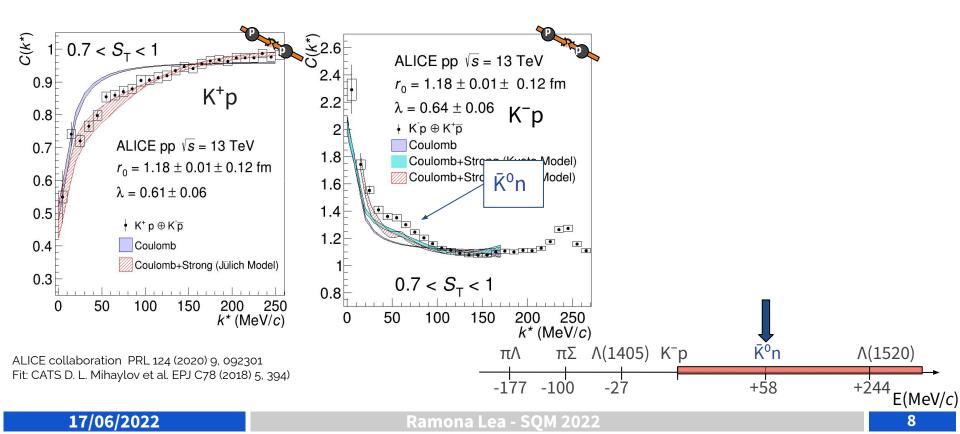


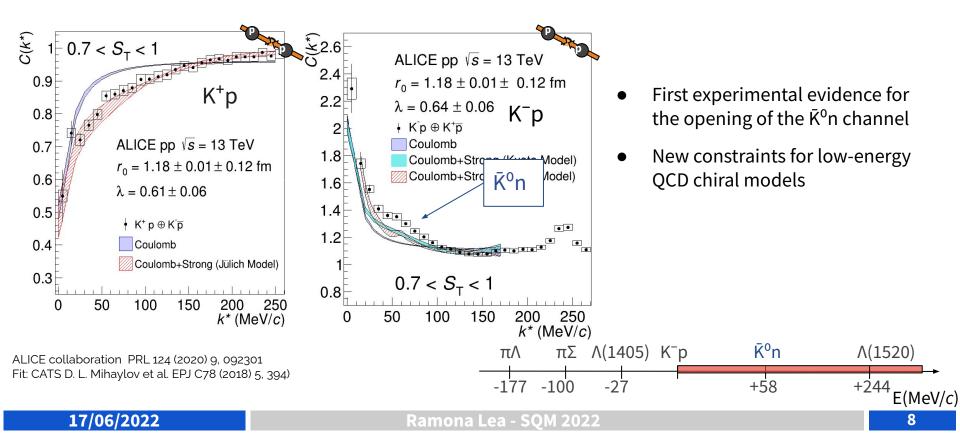
ALICE collaboration PRL 124 (2020) 9, 092301 Fit: CATS D. L. Mihaylov et al. EPJ C78 (2018) 5, 394)

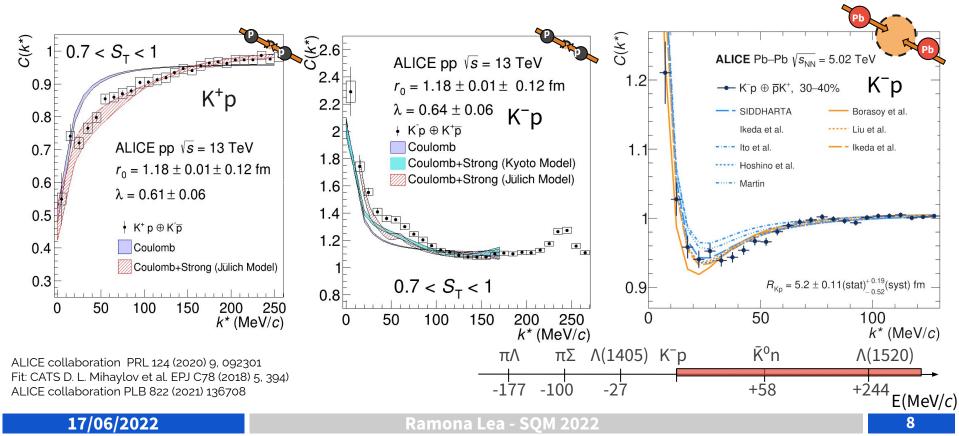
- The Coulomb-only potential is not able to describe K⁺p interaction and the introduction of the strong potential is needed to fit the data:
 - CFs are sensitive to the strong interaction





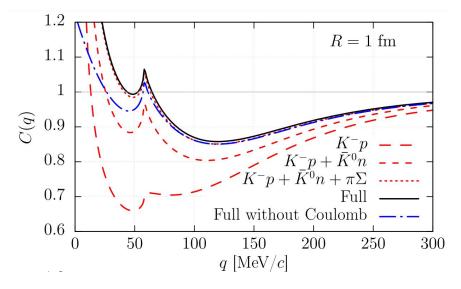






K⁻p interaction: improved chiral model

Koonin-Prat formula for coupled channels (CC) $C_{\mathrm{K^{-}p}}(k^{*}) = \int d^{3}\vec{r} \,^{*}S_{\mathrm{K^{-}p}}(\vec{r}^{*}) \left| \psi_{\mathrm{K^{-}p}}(\vec{k}^{*},\vec{r}^{*}) \right|^{2} + \sum_{j} \omega_{j} \int d^{3}\vec{r} \,^{*}S_{j}(\vec{r}^{*}) \left| \psi_{j}(\vec{k}^{*},\vec{r}^{*}) \right|^{2}_{j=\bar{\mathrm{K}}^{0}\mathrm{n}, \pi^{0}\Sigma^{0}, \pi^{+}\Sigma^{-}, \pi^{-}\Sigma^{+}, \pi^{0}\Lambda}$

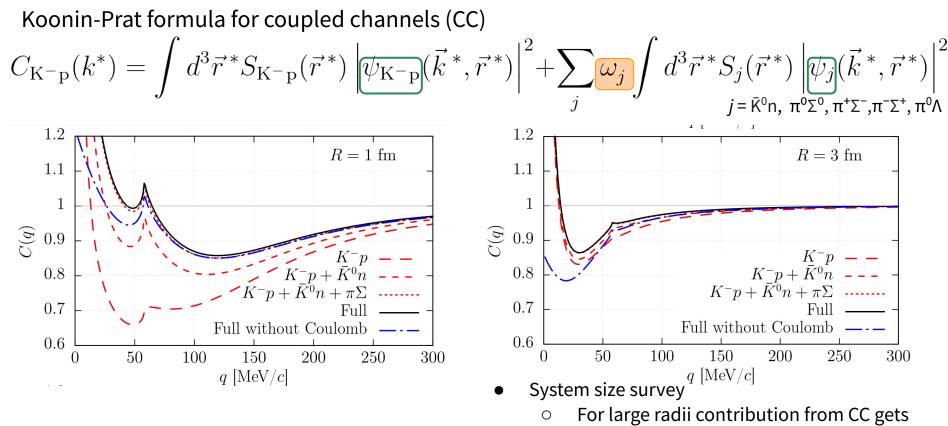


- Coupled-channel are short-range features of the strong interaction
 - the shape and strength of the correlation function are modified at small distances
 - Improved Kyoto chiral model to describe CC potential V_i
- Conversion weights (ω_i)
 - control CC contribution
 - depend on primary yield and kinematics

Y. Kamiya et al, PRL 124 (2020) 132501, arXiv:1911.01041



K⁻p interaction: improved chiral model



Y. Kamiya et al, PRL 124 (2020) 132501, arXiv:1911.01041

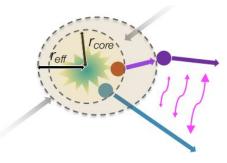
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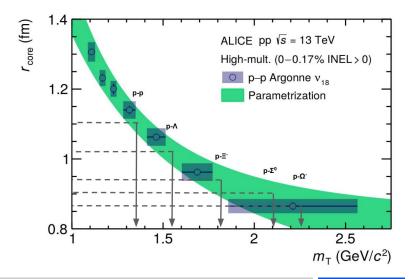
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negligible \rightarrow elastic scattering

The emitting source in small colliding systems

- Data-driven analysis on p-p and p-Λ pairs
 - Possible presence of collective effects $\rightarrow m_{\tau}$ scaling of the core radius
 - \circ Contribution of strongly decaying resonances with ct ~1 fm (*)
- Common universal core source for baryons



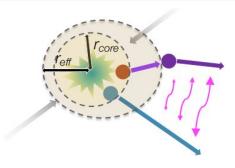


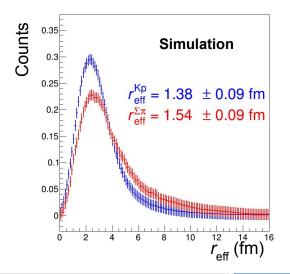
ALICE Collaboration PLB 811 (2020) 135849

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The emitting source in small colliding systems

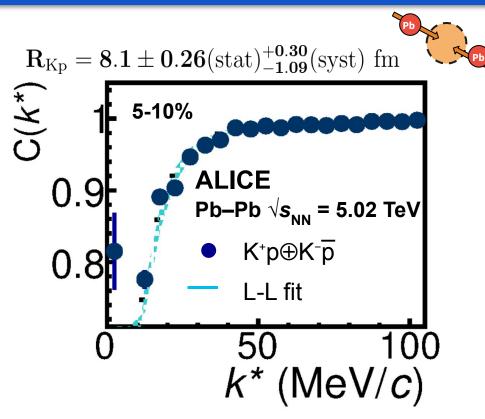
- Data-driven analysis on p–p and p–Λ pairs
 - Possible presence of collective effects $\rightarrow m_{\tau}$ scaling of the core radius
 - Contribution of strongly decaying resonances with cτ ~1 fm (*)
- Common universal core source for baryons
- What about meson-baryon pairs?
 - K⁺p interaction is well known \rightarrow extract r_{core} for Kp pairs
 - For small systems:
 - build effective sources for Kp(K
 ⁰n) and one for πΣ (πΛ) pairs using different resonances





ALICE Collaboration arXiv: 2205.15176

K⁻p in large systems

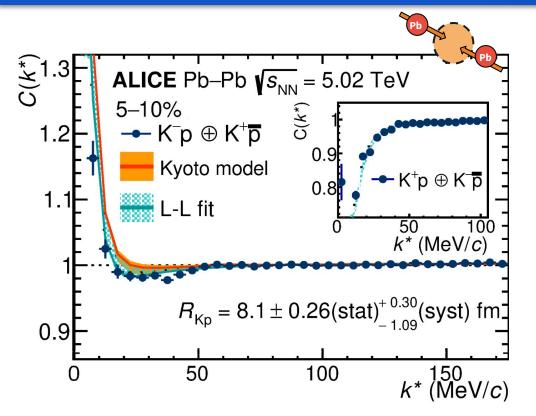


- K⁺p used to extract source size
 - Gaussian source
 - Lednický-Lyuboshitz (LL) fit to extract r_{eff}

ALICE collaboration PLB 822 (2021) 136708



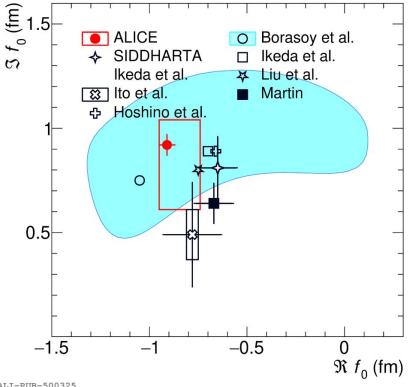
K⁻p in large systems



- K⁺p used to extract source size
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 - Lednický-Lyuboshitz (LL) fit to extract r_{eff}
- Large system: no coupled channels (as in Kyoto model)
- Use Lednický-Lyuboshitz (LL) fit to extract $\Re f_0$ and $\Im f_0$

ALICE collaboration PLB 822 (2021) 136708

K⁻p in large systems



- K⁺p used to extract source size
 - Gaussian source Ο
 - Lednický-Lyuboshitz (LL) fit to Ο extract r_{eff}
- Large system: no coupled channels (as in Kyoto model)
- Use Lednický-Lyuboshitz (LL) fit to extract $\Re f_0$ and $\Im f_0$
- $\Re f_0$ and $\Im f_0$ in agreement with available data and calculations
 - Alternative to exotic atoms \cap and scattering experiments!

ALI-PUB-500325

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ALICE collaboration PLB 822 (2021) 136708

K⁻p from small to large systems

$$C_{\rm K^-p}(k^*) = \int d^3 \vec{r} \, {}^*S_{\rm K^-p}(\vec{r}^*) \left| \psi_{\rm K^-p}(\vec{k}^*, \vec{r}^*) \right|^2 + \sum_j \omega_j \int d^3 \vec{r} \, {}^*S_j(\vec{r}^*) \left| \psi_j(\vec{k}^*, \vec{r}^*) \right|^2$$

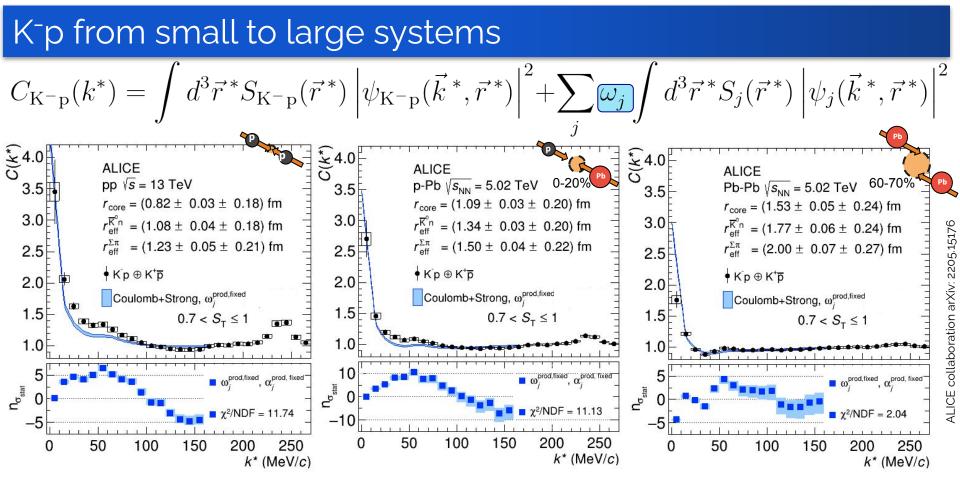
Each coupled channels is accounted in the ω_i weights

- primary production yields fixed from thermal model (Thermal-FIST) [1]
- estimate amount of pairs in FSI sensitive kinematic region
- distribute particles according to blast-wave model [2,3,4]
- normalize to expected yield of K⁻p

V. Vovchenko et al. PRC 100 no. 5 (2019)
 E. Schnedermann et al. PRC 48 (1993)
 ALICE Collaboration, PLB 728 (2014)
 ALICE Collaboration, PRC 101 no. 4 (2020)

Maximilian Korwieser, PA-Light-flavor and Strangeness 14/06/22

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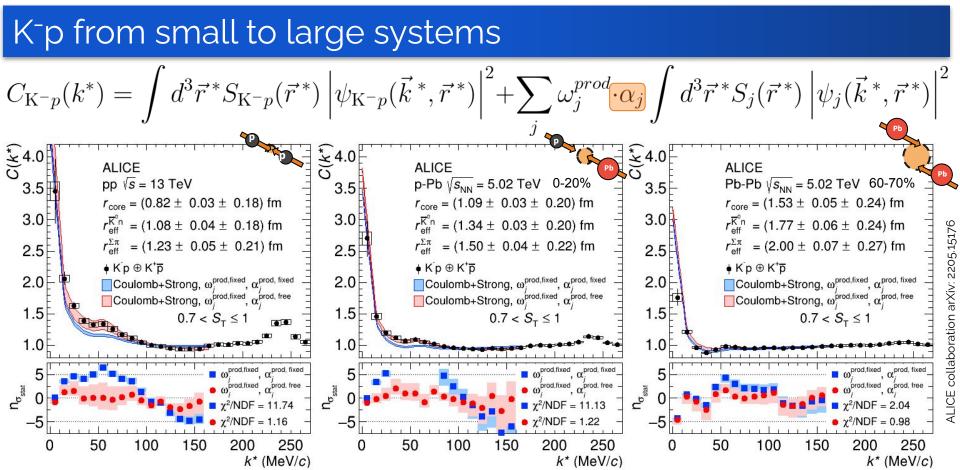


State-of-the art Kyoto Model is not able to describe the data from small to large source size

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K⁻p from small to large systems

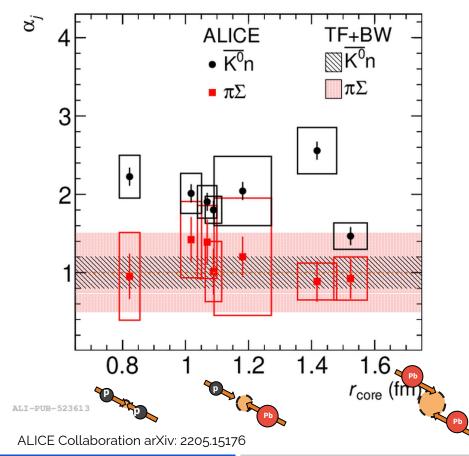
$$C_{\mathrm{K}^{-}p}(k^{*}) = \int d^{3}\vec{r}^{*}S_{\mathrm{K}^{-}p}(\vec{r}^{*}) \left| \psi_{\mathrm{K}^{-}p}(\vec{k}^{*},\vec{r}^{*}) \right|^{2} + \sum_{j} \omega_{j}^{prod} \alpha_{j} \int d^{3}\vec{r}^{*}S_{j}(\vec{r}^{*}) \left| \psi_{j}(\vec{k}^{*},\vec{r}^{*}) \right|^{2}$$



A correction factor α_i is introduced to quantify the model-to-data deviation

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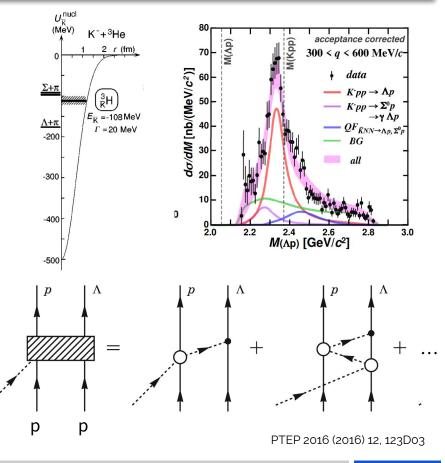
K⁻p from small to large systems



- Unique constraint and direct access to $K^-p \leftrightarrow \overline{K}^0n$ and $K^-p \leftrightarrow \pi\Sigma$ dynamics
- $\alpha_{\bar{K}^0-n}$ deviates from unity:
 - $K^-p \leftrightarrow \bar{K}^0$ n currently implemented in Kyoto χ EFT is too weak
 - fine tuning of Kyoto χEFT is needed and data from hadron-hadron collisions have to be taken into account

What about many-body systems?

- K
 NN: exotic bound states of anti-kaon with nucleons predicted more than 30 years ago [1,2] due to the strongly attractive K
 N interaction in I = 0 channel
- First positive experimental evidence of the p-p-K⁻ bound state by the E15 Collaboration [3]
- Next experimental challenge: genuine three-body interaction measurements

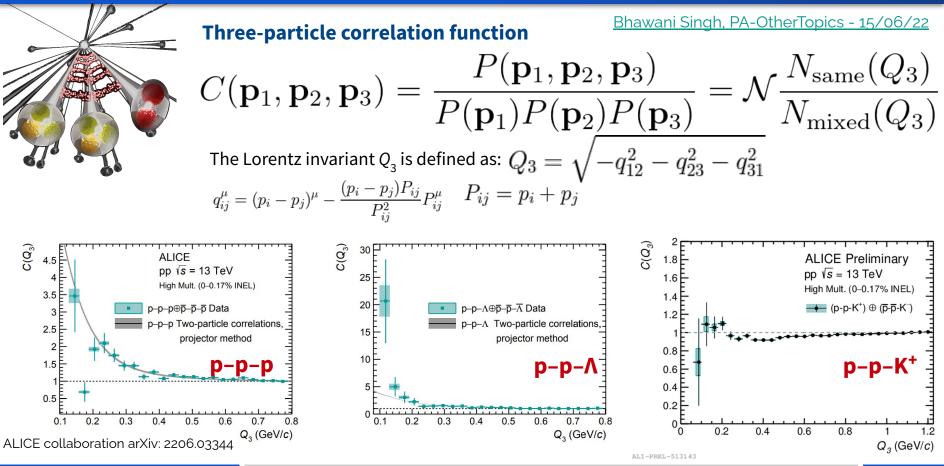


[1]S. Wycech, NPA 450 (1986) 399c;
[2]Y. Akaishi, T. Yamazaki, PRC 65 (2002) 044005
[3]J-PARC E15 Collaboration PRC 102, 044002 (2020)

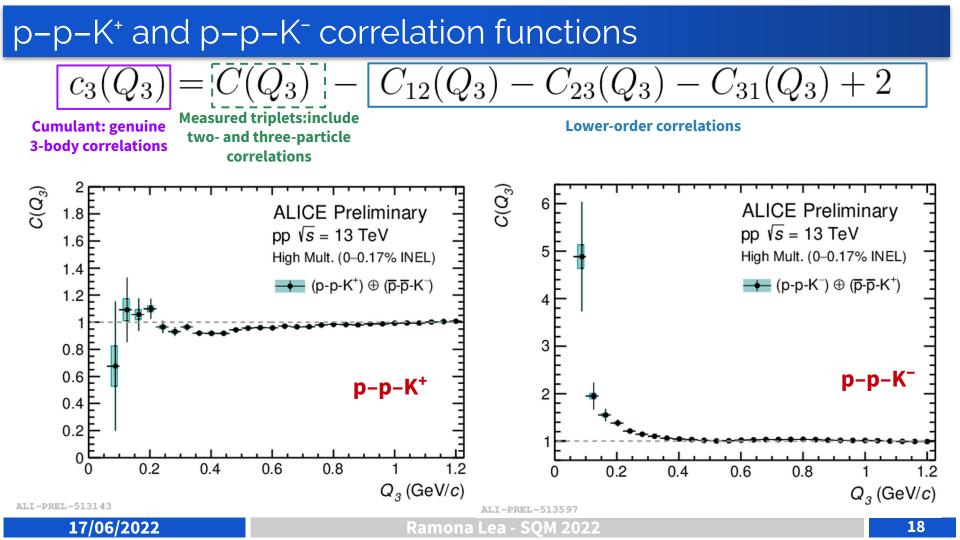
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K

Investigating three-hadron hadronic interactions at LHC

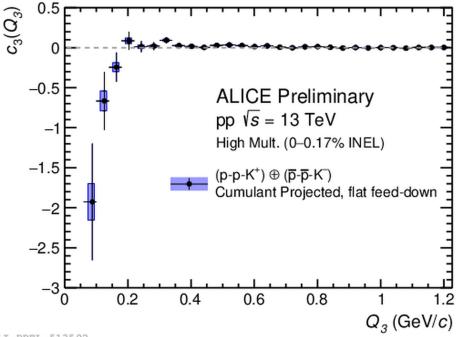


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p–p–K⁺ cumulant

Genuine 3-body correlations



• $n_{\sigma} = 2.3 \text{ for } Q_3 < 0.4 \text{ GeV/}c$

• Conclusions:

- The measured cumulant is compatible with zero within the uncertainties
- Above 180 MeV/c, the genuine three-body effects do to not contribute significantly in the dynamics of the p-p-K⁺ system

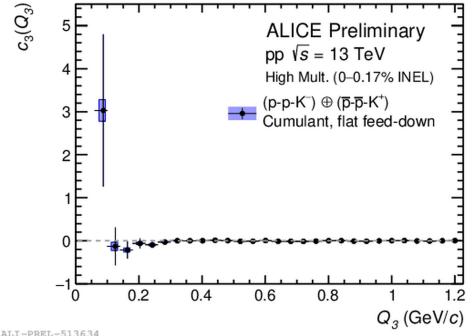
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[•] Statistical significance:

ALI-PREL-513592

p-p-K⁻ cumulant

Genuine 3-body correlations



Statistical significance: $n_{g} = 0.5$ for $Q_{3} < 0.4$ GeV/c 0

Conclusion:

- The measured cumulant is consistent Ο with zero within uncertainties
- Genuine three-body effects are not significant in p-p-K⁻ systems
 - The measurement confirms that Ο three-body strong interaction is not relevant in the formation of the exotic kaonic bound states

Conclusions

- Momentum correlation technique applied to data collected at the LHC in different collision systems
 - Unique way to access KN and KN interaction: New constraints for low-energy QCD chiral models
 - First experimental access to coupled channels dynamics ($K^-p \leftrightarrow \bar{K}^0n$, $K^-p \leftrightarrow \pi\Sigma$, $K^-p \leftrightarrow \pi\Lambda$)
 - Data-model tension in description of K⁻p interaction:
 - $K^-p \leftrightarrow \bar{K}^0$ n currently implemented in state-of-the-art Kyoto χ EFT is too weak
 - First direct measurement of p-p-K⁺ and p-p-K⁻ interaction
 - cumulants compatible with 0, no evidence of a genuine three-body force
 - kaonic bound state formation driven by two-body forces
- More precision studies within reach with large statistics in LHC Run 3 & 4
 - Unique way to access coupled-channels dynamics in the meson-baryon sector: open a new era in the charm sector!

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BACKUP

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Conclusions

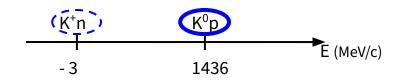
- Momentum correlation technique applied to data collected at the LHC in different collision systems
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 - Data-model tension in description of K⁻p interaction:
 - $K^-p \leftrightarrow \bar{K}^0$ n currently implemented in state-of-the-art Kyoto χ EFT is too weak
 - **Direct** access to $K^0_{c}p(Kp + \bar{K}p)$ interaction:
 - state-of-the-art theory Kyoto χ EFT well describes the experimental data
 - First direct measurement of $p-p-K^+$ and $p-p-K^-$ interaction
 - cumulants compatible with 0, no evidence of a genuine three-body force
 - kaonic bound state formation driven by two-body forces
- More precision studies within reach with large statistics in Run 3 & 4!

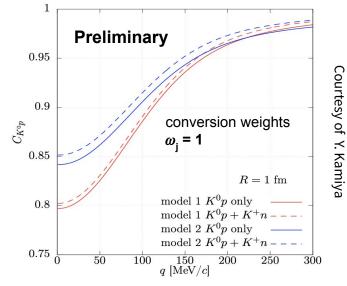
Accessing KN and $\overline{K}N$ interaction with K^o

• K⁰_s –p system is a combination of strong eigenstates

$$|K_s^0 p\rangle = \frac{1}{\sqrt{2}} \left[\overline{|K^0 p\rangle} - \overline{|\bar{K}^0 p\rangle} \right] \implies C_{K_s^0 p} = \frac{1}{2} \left[C_{K^0 p} + C_{\bar{K}^0 p} \right]$$

- Weak strong repulsion
- 1 CC below threshold: K⁺n
 - predicted to be a weak coupling
- Calculations from **A**oki-**J**ido χEFT model for KN[1]





[1] K. Aoki and D. Jido, PTEP 2019, 013D01 (2019), 1806.00925.

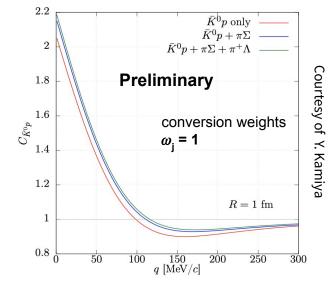
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Accessing KN and $\overline{K}N$ interaction with K^o

• K^o_s –p system is a combination of strong eigenstates

$$|K_s^0 p\rangle = \frac{1}{\sqrt{2}} \left[|K^0 p\rangle - \left[\bar{K}^0 p \right] \right] \implies C_{K_s^0 p} = \frac{1}{2} \left[C_{K^0 p} + C_{\bar{K}^0 p} \right]$$

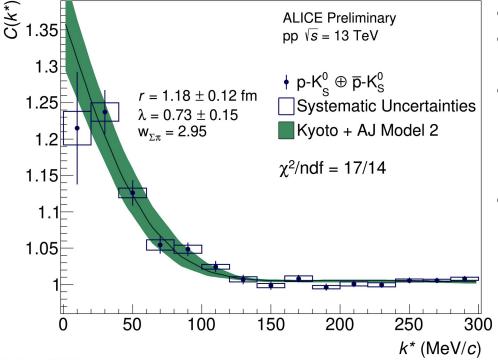
- Moderate attraction
- 3 CC below threshold: $\pi^0 \Sigma^+$, $\pi^+ \Sigma^0$, $\pi^+ \Lambda$
 - large $\pi\Sigma$ coupling (as in K⁻-p)
- Calculations from Kyoto χEFT model for K⁻p [1,2]



[1] K. Miyahara, et al. PRC98, 025201 (2018), arXiv: 1804.08269 [2] Y.Kamiya, et al PRL124 (2020) 132501

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K^o_s-p interaction



ALI-PREL-487651

[1] ALICE Collaboration, PRL 124, 092301 (2020)[2] Y.Kamiya, et al. PRL 124 132501 (2020)

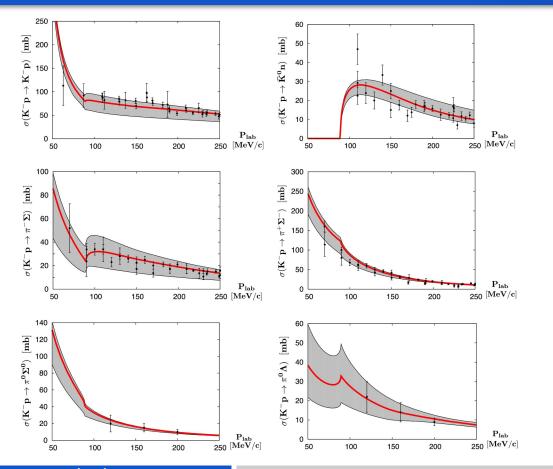
• Gaussian source function with r=1.18±0.12 fm [1]

- $K^{o}p(\bar{p})$ and $\bar{K}^{o}(\bar{p}) \psi$ with CC provided by Kyoto χ EFT
- Conversions weights $\omega = 1$ for K°p, K+n, and $\pi^+\Lambda$; $\omega_{\Sigma\pi} = 2.95$ [2]

- Model describes data within 2σ between 0 and 300 MeV/c
 - State-of-the-art theory well describes the experimental data
 - Small caveat: source not (yet) studied in details

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Best fit of K⁻p observables: cross section data



Y. Ikeda et al, PLB Volume 706, (2011),63-67

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KN scattering lengths

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• Deser-type relation connects shift ε_{1s} and width Γ_{1s} to the real and imaginary part of α_{K^-p} and α_{K^-d} :

$$\varepsilon + \frac{i\Gamma}{2} = 2\alpha^{3}\mu^{2}a_{K^{-}p} = 412 \frac{eV}{fm}a_{K^{-}p} \qquad \text{done by SIDDHARTA}$$
$$\varepsilon + \frac{i\Gamma}{2} = 2\alpha^{3}\mu^{2}a_{K^{-}d} = 601 \frac{eV}{fm}a_{K^{-}d} \qquad \text{aim of SIDDHARTA-2}$$

• one can obtain the isospin dependent antikaon-nucleon scattering lengths

$$a_{K^{-}p} = \frac{a_0(I=0) + a_1(I=1)}{2}$$
$$a_{K^{-}d} = \frac{1}{2} \frac{m_N + m_K}{m_N + \frac{m_K}{2}} (3a_1 + a_0) + C$$

Fundamental inputs of low-energy QCD effective field theories

Resonances used for $\pi\Sigma(\Lambda)$ source (π)

 For modeling the source every resonance with a cτ > 8 fm is taken out and the yields properly renormalized. These resonance are used to determine the decay-kinematics with EPOS.

Primordial fraction	Resonance fractions			
	ст < 1 fm	1 <i>< c1</i> < 2 fm	2 < c 7 < 5 fm	c t > 5 fm
28 %	15 %	35 %	10 %	12 %

$$< m(\pi) > = 1124 \text{ MeV}/c^2$$

$$< c\tau(\pi) > = 1.5 \text{ fm}$$

Resonance	ρο	ρ⁺	ω	K(892)**
Yield (in %)	9.01	8.71	7.67	2.29

Only resonances which contribute more then 2% to total yield are shown

Resonances used for $\pi\Sigma(\Lambda)$ source ($\Sigma\Lambda$)

 For modeling the source every resonance with a cτ > 8 fm is taken out and the yields properly renormalized. These resonance are used to determine the decay-kinematics with EPOS.

Primordial fraction	Resonance fractions			
	<i>c1</i> < 1 fm	1 <i>< c7</i> < 2 fm	2 < c 7 < 5 fm	c t > 5 fm
26 %	0 %	5 %	5 %	64 %

$$< m(\Sigma) > = 1463 \text{ MeV/c}^2$$

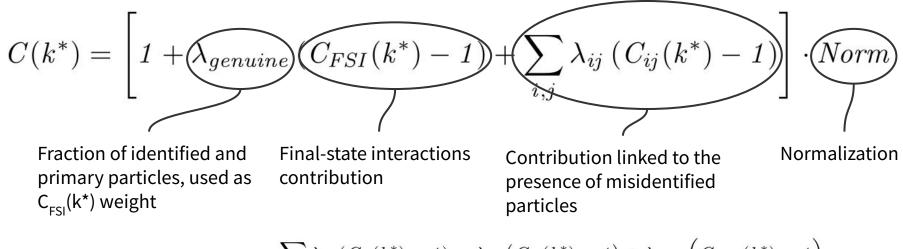
 $< c\tau(\Sigma) > = 4.7 \text{ fm}$

Resonance	Σο	Σ*0	Σ**	Σ*-
Yield (in %)	27	12	12	12

Only resonances which contribute more then 2% to total yield are shown

Contributions to the experimental correlation function

• Fit of the $C(k^*) = C_{data}(k^*)/C_{baseline}(k^*)$ to obtain the parameters of the strong interaction between K_{s}^{0} and $p(\bar{p})$ is performed with the function:



$$\sum_{i,j} \lambda_{ij} \left(C_{ij}(k^*) - 1 \right) = \lambda_{\tilde{K}} \left(C_{\tilde{K}}(k^*) - 1 \right) + \lambda_{\tilde{p}(\tilde{p})} \left(C_{\tilde{p}(\tilde{p})}(k^*) - 1 \right)$$

K°_s-p correlation function fit with Lednický-Lyuboshitz

$$C_{FSI}(k^*) = \sum_{S} \rho_S \left[\frac{1}{2} \left| \frac{f(k^*)}{R} \right|^2 \left(1 - \frac{d_0}{2\sqrt{\pi R}} \right) + \frac{2\Re f(k^*)}{\sqrt{\pi R}} F_1(2k^*R) - \frac{\Im f(k^*)}{R} F_2(2k^*R) \right]$$

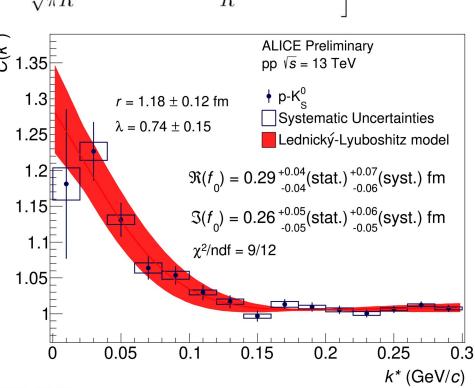
$$C_{Lednicky}(k^*) = 1 + C_{FSI}(k^*)$$

$$\overset{\text{ALICE Preliminary}}{\underbrace{\textcircled{S}}} 1.35$$

Scattering amplitude:

$$f(k^*) = \left(\frac{1}{f_0} + \frac{1}{2}d_0k^{*2} - ik^*\right)^{-1}$$

- f_0 scattering length, d_0 effective range of interaction
 - \circ $\Re f_0, \Im f_0$ estimated parameters
- $\Re f_0 > 0$: attractive interaction
- ℑf₀ ≠0 : presence of annihilation processes



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Kaon-proton interaction - Large systems

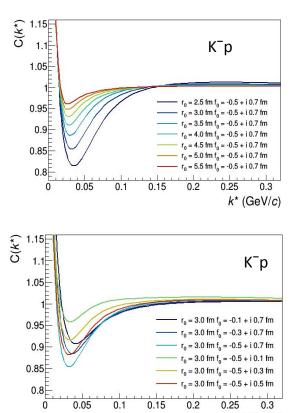
Lednický-Lyuboshitz model

$$C(\mathbf{k}^*) = rac{\int S(\mathbf{r}^*, \mathbf{k}^*) |\psi(\mathbf{r}^*, \mathbf{k}^*)|^2}{\int S(\mathbf{r}^*, \mathbf{k}^*)} \mathrm{d}^4 r^*$$

$$|\psi(r^*,k^*)| = \sqrt{A_C(\eta)} \left[\exp(-ik^*r^*)F(-i\eta,1,i\xi) + f_c(k^*)\frac{G}{r^*} \right]$$

$$f_{c}(k^{*}) = \left(\frac{1}{f_{0}} + \frac{d_{0} \cdot k^{*2}}{2} - \frac{-2h(k^{*}a_{c})}{s_{c}} - ik^{*}A_{c}(k^{*})\right)^{-1}$$

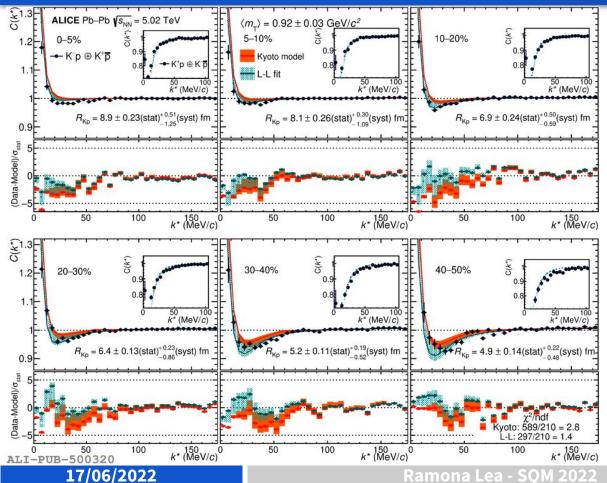
- Numerically solvable (strong+Coulomb)
- **3 parameters:** $\Re f_0$, $\Im f_0$ and source r define the correlation function.
- d₀ = 0 (zero effective range approx.)



k* (GeV/c)

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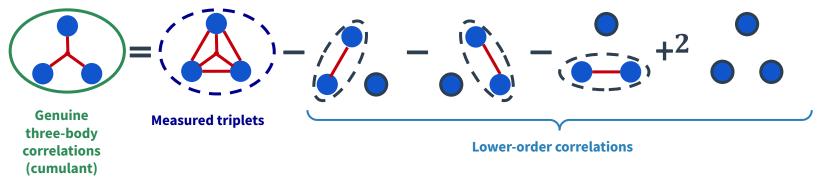
Kaon-proton in Pb-Pb



- No K⁰n structure
- Simultaneous description (and fit) of the correlation functions for 6 centralities (0-50%) with two parameters and 6 radii
- Radii constrained from K⁺p

Kubo's cumulant expansion method

• Genuine three-particle correlations isolated using the Kubo's cumulant expansion method:



R. Kubo, J. Phys. Soc. Jpn. 17(7), 1100-1120 (1962)

• In terms of correlation functions:

$$c_3(Q_3) = C(Q_3) - C_{12}(Q_3) - C_{23}(Q_3) - C_{31}(Q_3) + 2$$

Lower-order contributions evaluation

Data-driven approach

• Using the **same** and **mixed-events** distributions:

 $C\left(\left[\mathbf{p}_{1}, \mathbf{p}_{2}\right], \mathbf{p}_{3}\right) = \frac{N_{2}\left(\mathbf{p}_{1}, \mathbf{p}_{2}\right) N_{1}\left(\mathbf{p}_{3}\right)}{N_{1}\left(\mathbf{p}_{1}\right) N_{1}\left(\mathbf{p}_{2}\right) N_{1}\left(\mathbf{p}_{3}\right)}$

• The scalar Q₃ is calculated from the measured single-particle momenta

$$(\mathbf{p}_1,\mathbf{p}_2,\mathbf{p}_3) \to Q_3$$

Projector method

R. Del Grande, L. Šerkšnytė et al, Eur.Phys.J.C 82 (2022) 3, 244

- Using the two-body correlation function of the pair (1,2).
- A kinematic transformation from

 $k_{12}^*(\text{pair}) \rightarrow Q_3(\text{triplet})$ $C_2(k_{12}^*) \rightarrow C_3(Q_3)$

is performed.

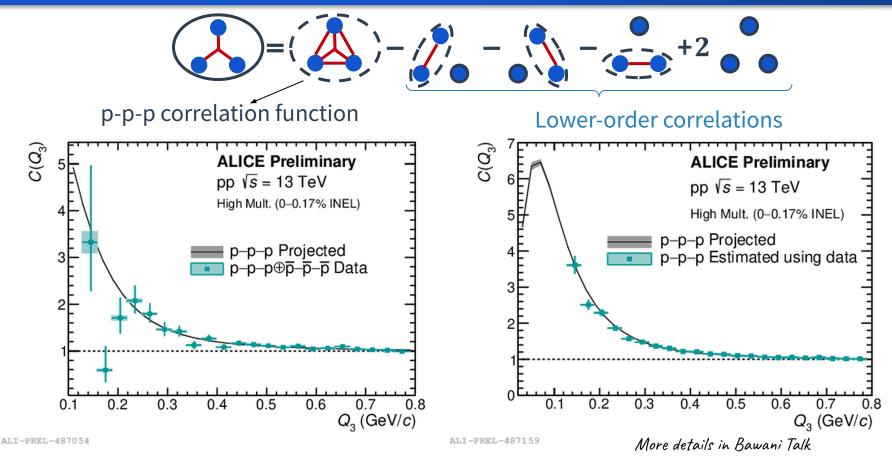
• For the pair (*i, j*) we have

$$C_3^{ij}(Q_3) = \int C_2(k_{ij}^*) W_{ij}(k_{ij}^*, Q_3) dk_{ij}^*$$

two-body correlation function

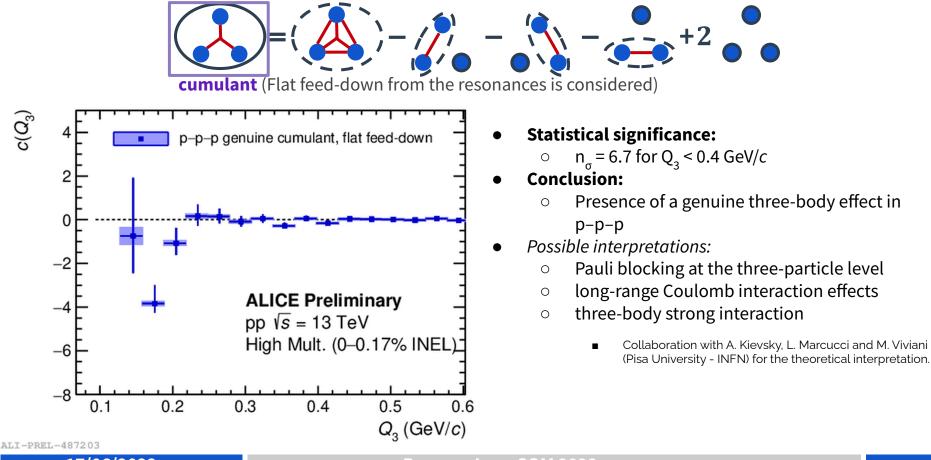
projector

p-p-p correlation function

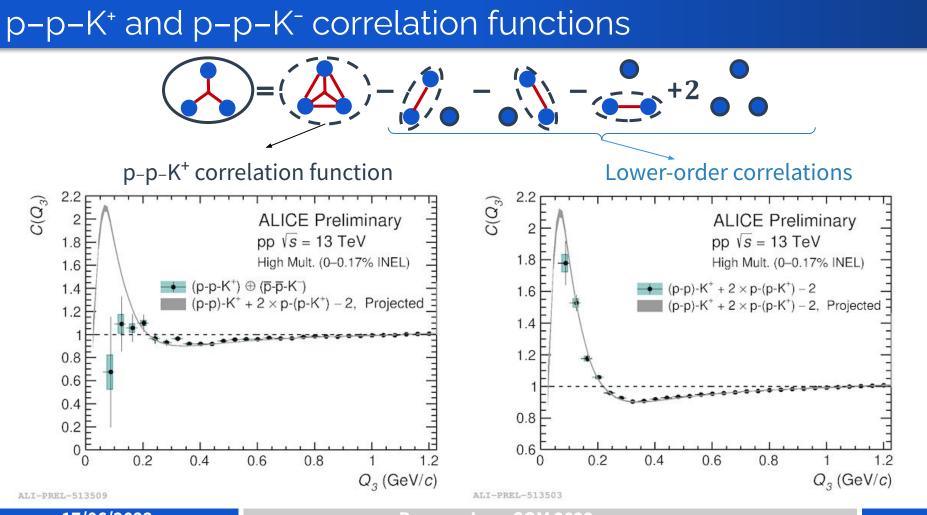


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p-p-p cumulant

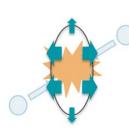


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Small Sources: Collective Effects and Strong Resonances



Elliptic flow

Anisotropic pressure gradients within the source

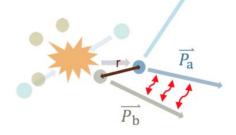


Radial flow

- Expanding source with constant velocity
- Different effect on different
 masses

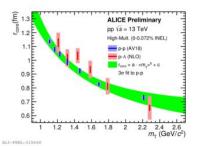
Strong decays of broad resonances

U. A. Wiedemann, U. W. Heinz, Phys.Rept. 319, 145-230 (1999)



- Resonances with $c\tau \sim r_0 \sim 1$ fm (Δ^* , N^{*}, Σ^*) introduce an exponential tail to the source
- Different for each particle species

Core Radius





Strong decays of specific resonances

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