

Seminar

18 May 2021

Institute of Nuclear  
and Particle Physics

**Demokritos**

# Pattern of Flavour Anomalies

(in light of recent results from LHCb)



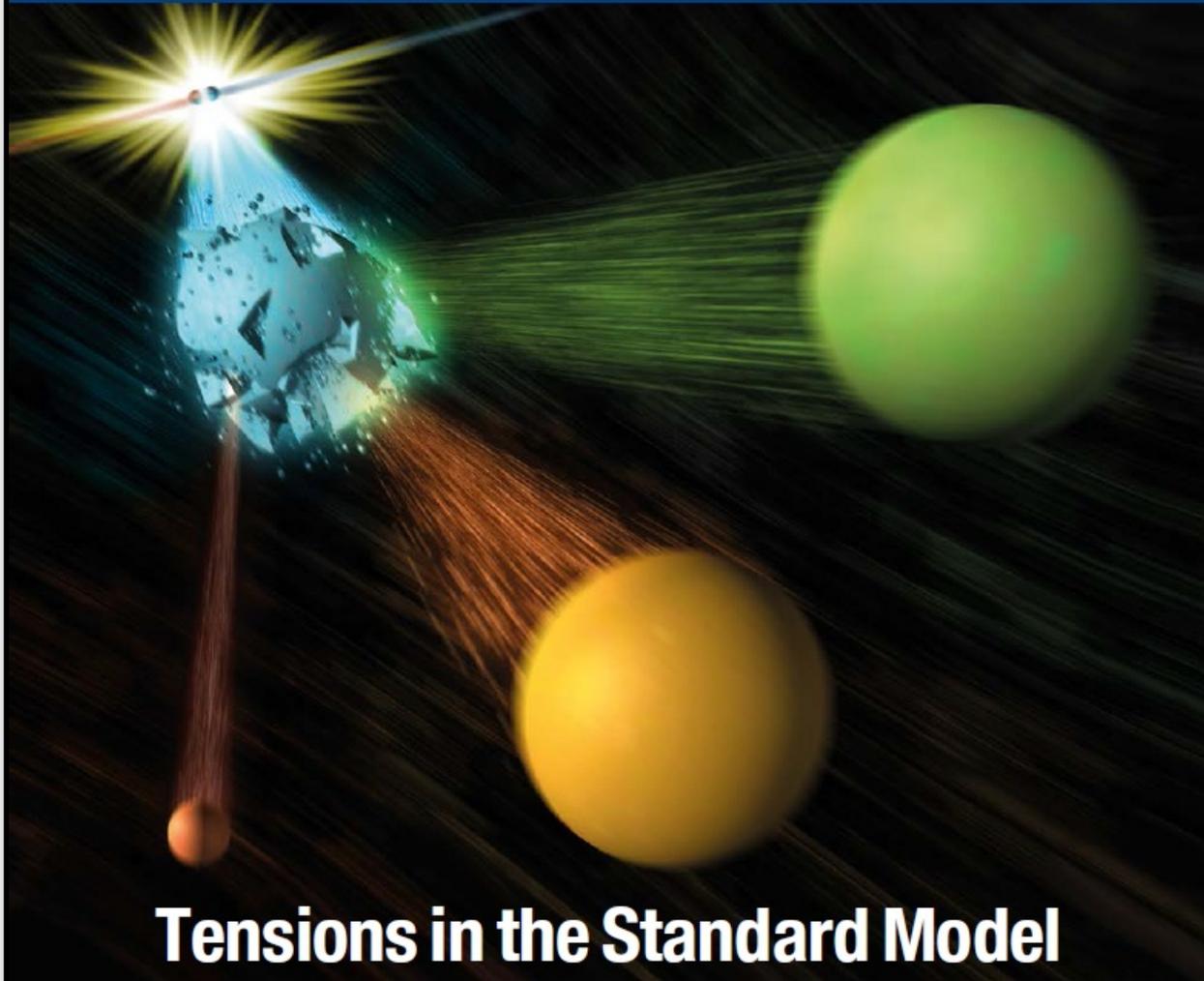
Niels Tuning



INTERNATIONAL JOURNAL OF HIGH-ENERGY PHYSICS

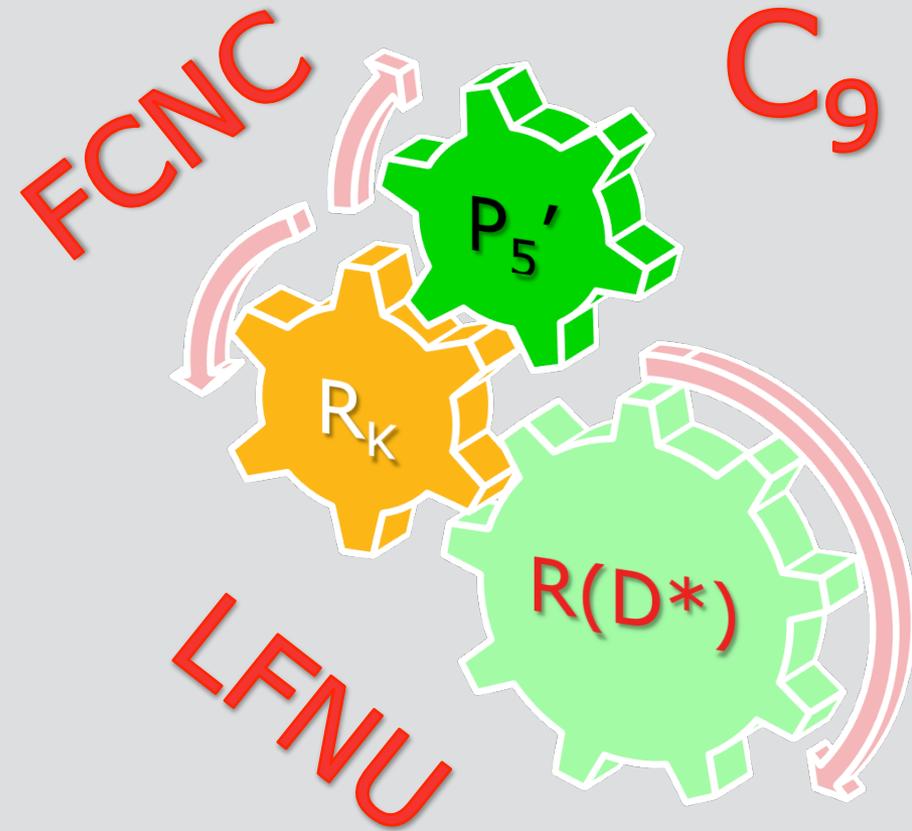
# CERN COURIER

VOLUME 55 NUMBER 9 NOVEMBER 2015



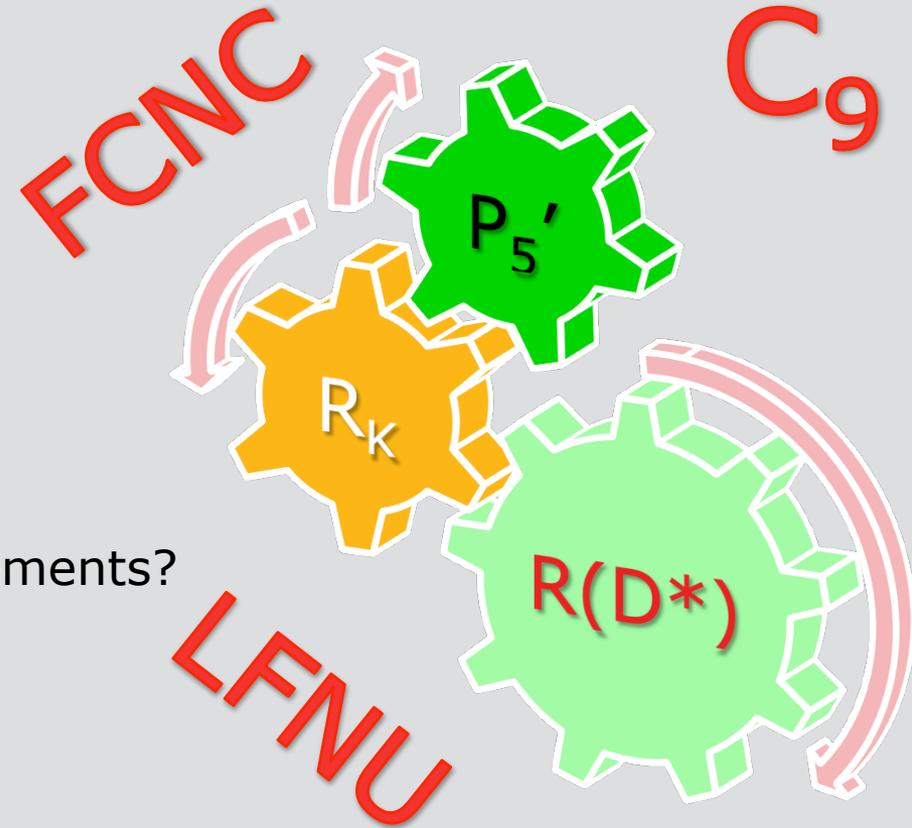
**Tensions in the Standard Model**

# Outline: the jargon



# Outline

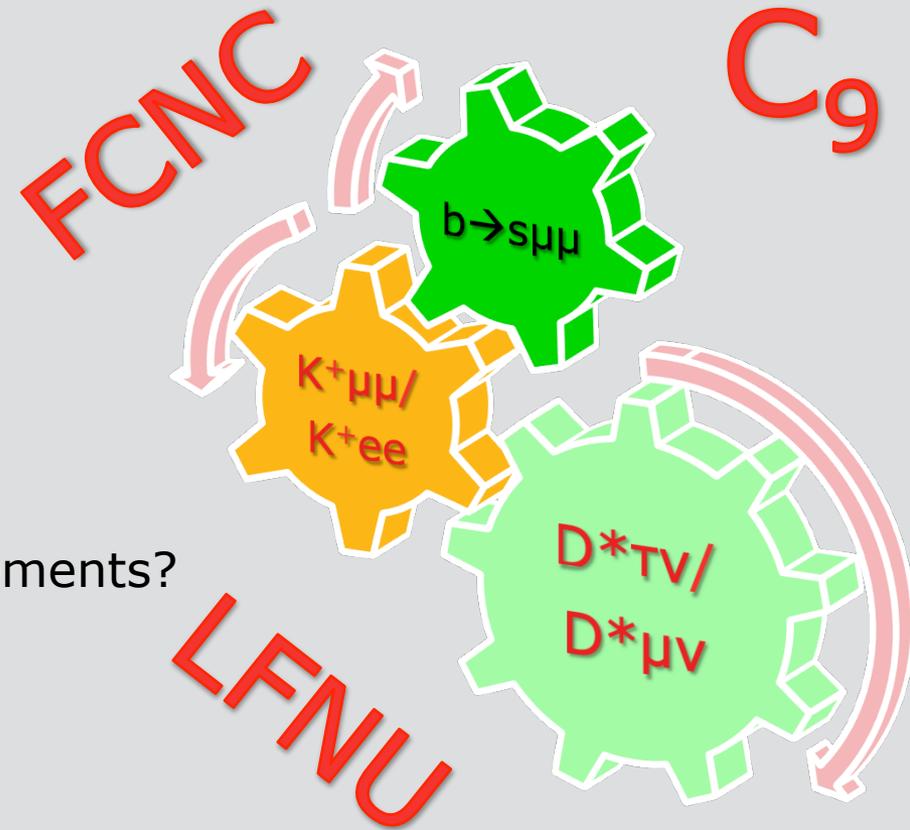
- Indirect measurements
- What are the (anomalous) measurements?
  - FCNC:  $b \rightarrow sll$
  - LFNU:  $b \rightarrow sll$  and  $b \rightarrow clv$
- What are the interpretations?



**New results**

# Outline

- Indirect measurements
- What are the (anomalous) measurements?
  - FCNC:  $b \rightarrow sll$
  - LFNU:  $b \rightarrow sll$  and  $b \rightarrow clv$
- What are the interpretations?



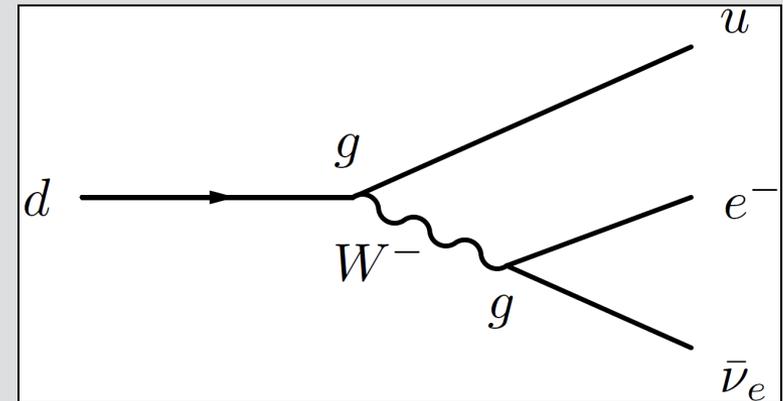
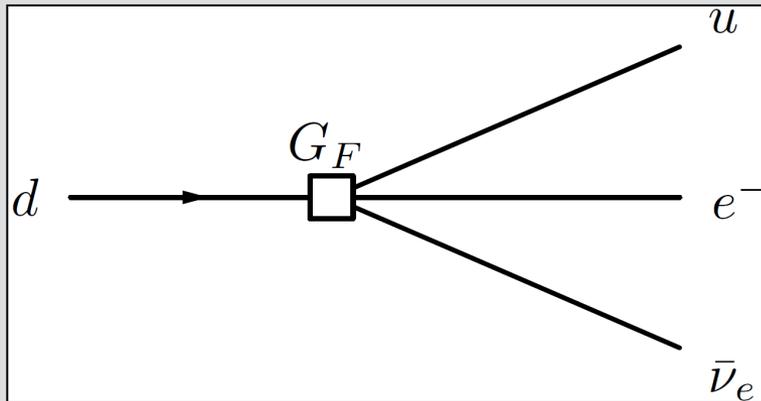
# Historical perspective

- The power of indirect measurements



# Historical perspective: W

- Radioactive decay was “discovery” of weak interaction?



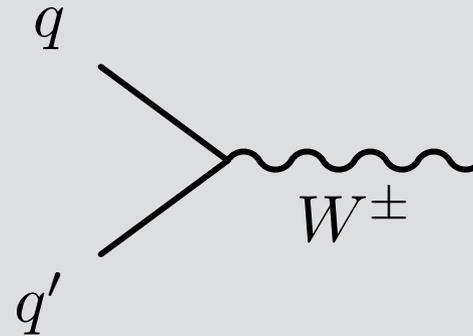
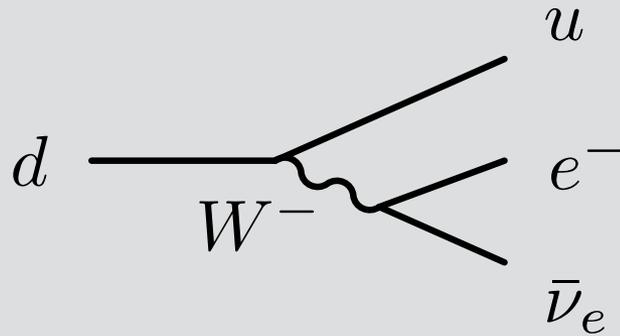
$$\frac{G_F}{\sqrt{2}} = \frac{g^2}{8M_W^2}$$



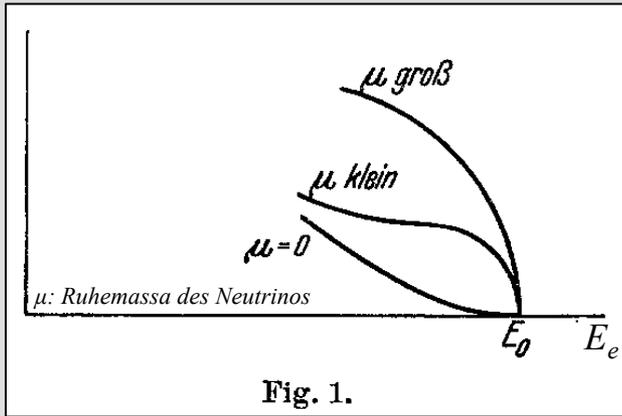
# Historical perspective: W

- Radioactive decay was "discovery" of weak interaction?

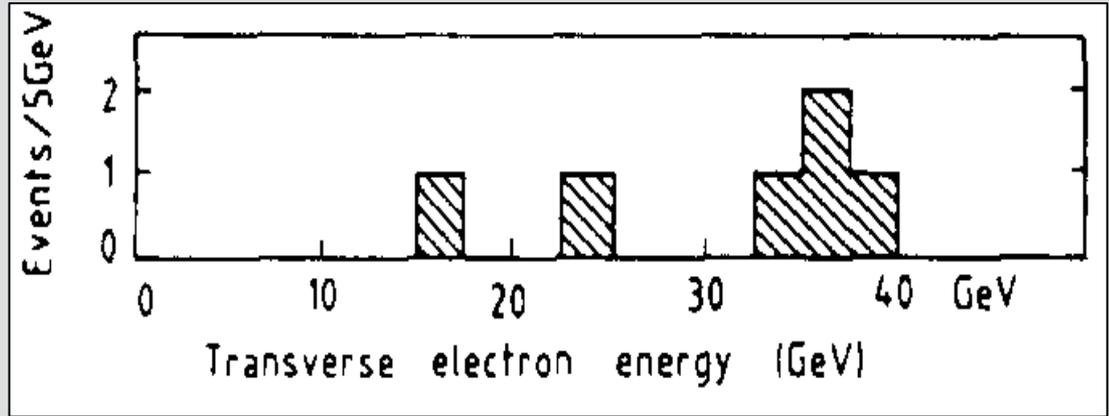
Indirect



Direct



E.Fermi, Z.Phys. 88 (1934) 161

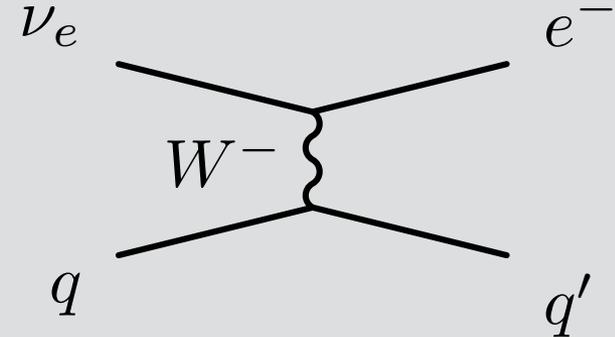
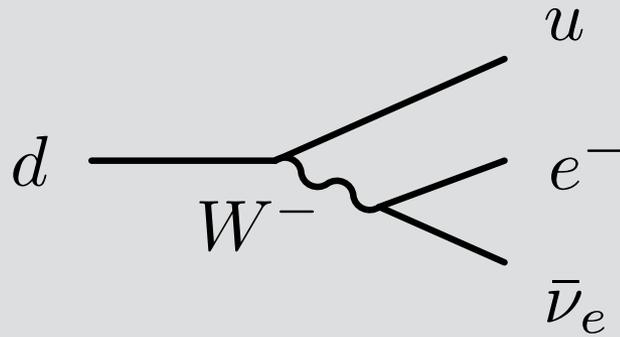


UA1 Coll., Phys.Lett. B122 (1983) 103

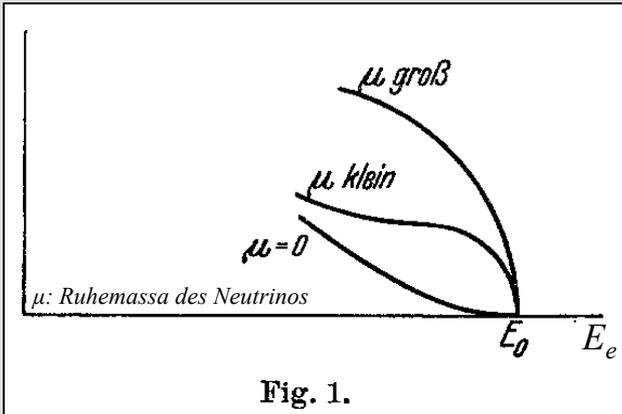
# Historical perspective: $\nu$

- Radioactive decay was "discovery" of neutrino?

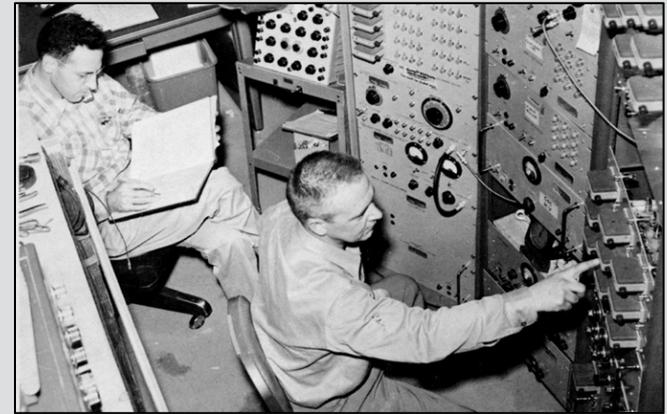
Indirect



Direct



E.Fermi, Z.Phys. 88 (1934) 161

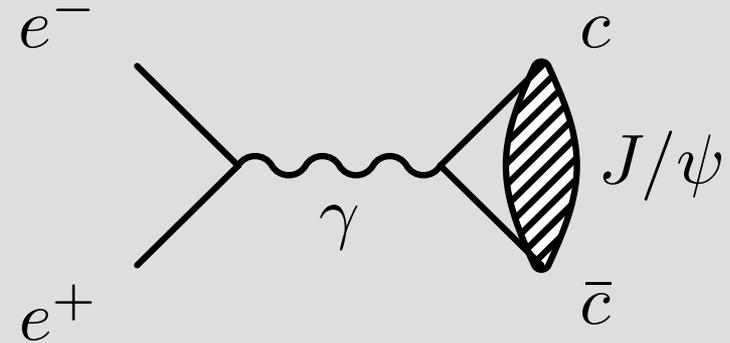
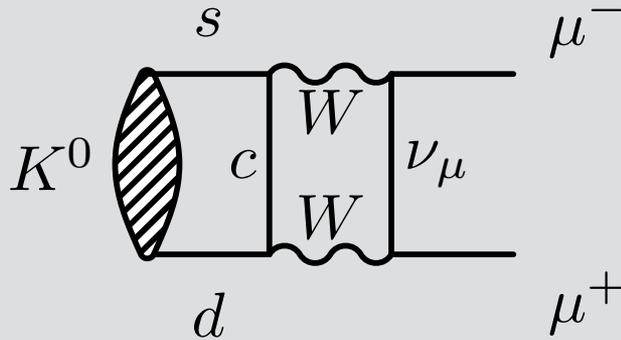


Cowan, Reines, et al., Science 124 (1956) 103-104



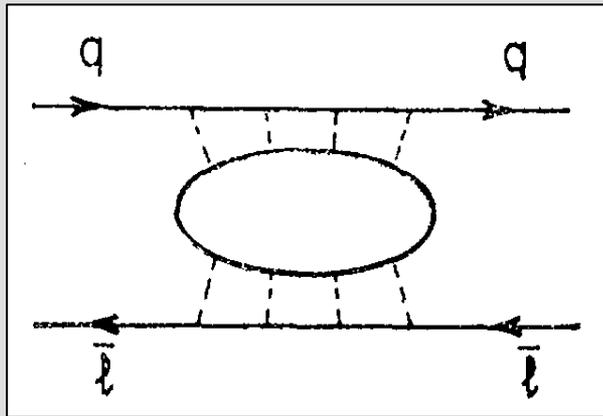
# Historical perspective: charm

- Kaon decay was “discovery” of charm quark?

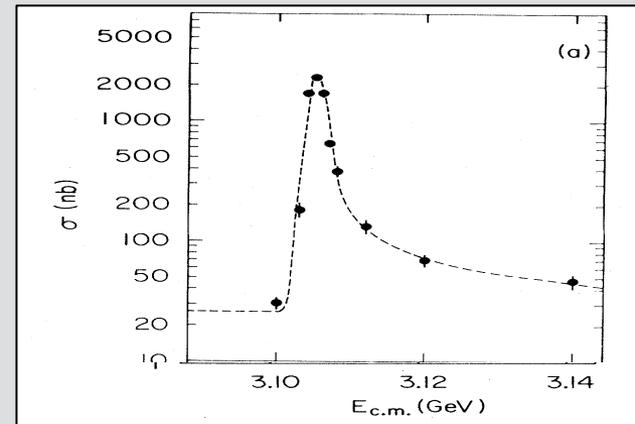


Indirect

Direct



GIM, Phys.Rev. D2 (1970) 1285



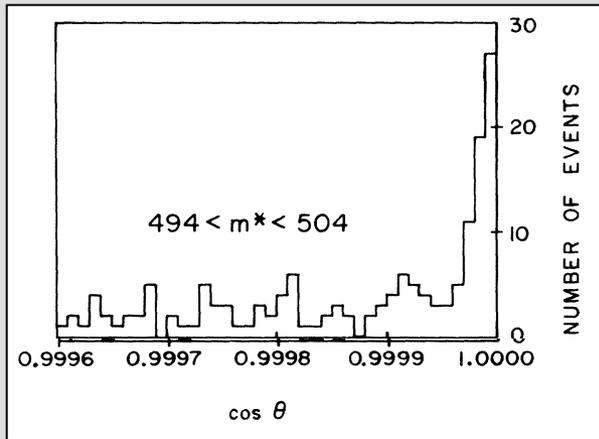
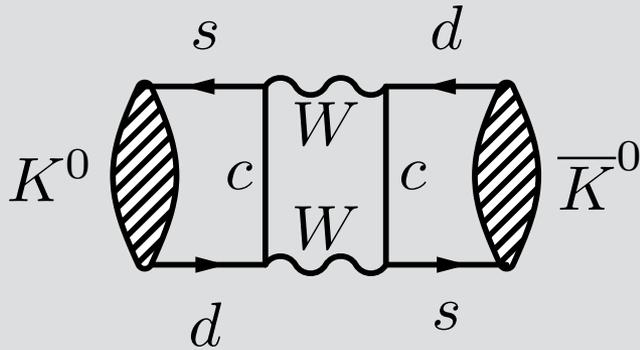
B.Richter et al, Phys.Rev.Lett. 33 (1974) 1406



# Historical perspective: bottom

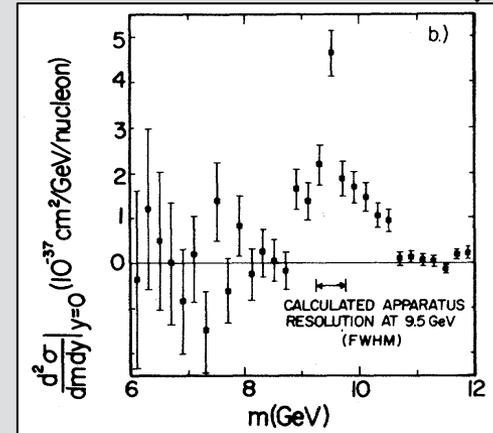
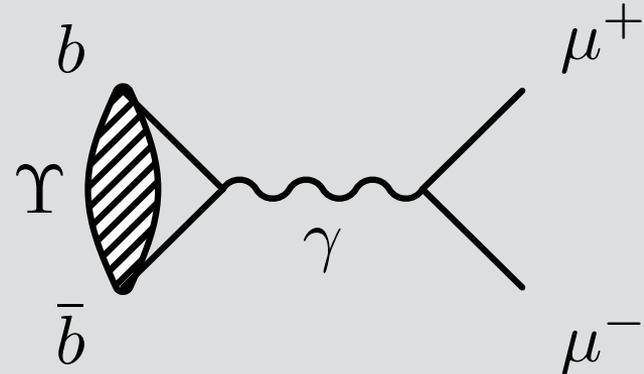
- CP violation was "discovery" of 3<sup>rd</sup> generation?

Indirect



Cronin and Fitch, Phys.Rev.Lett. 13 (1964) 138

Direct



L.Lederman et al., Phys.Rev.Lett. 39 (1977) 252



# Historical perspective: top

- Bottom mixing was "discovery" of top quark?

Indirect

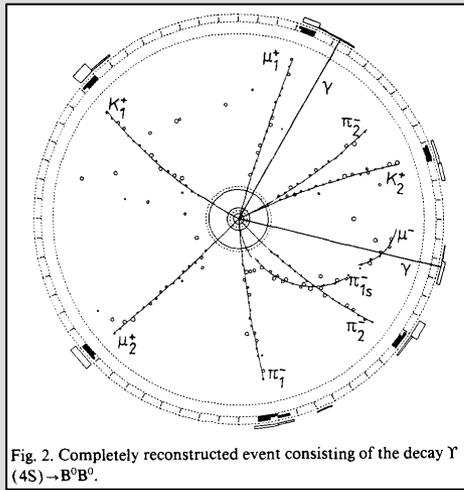
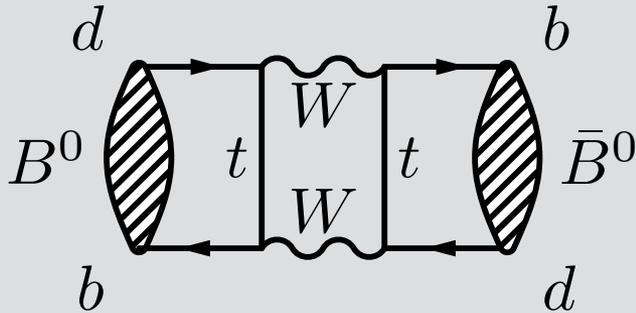
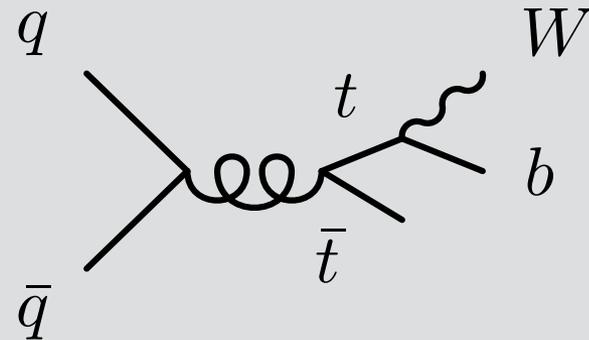
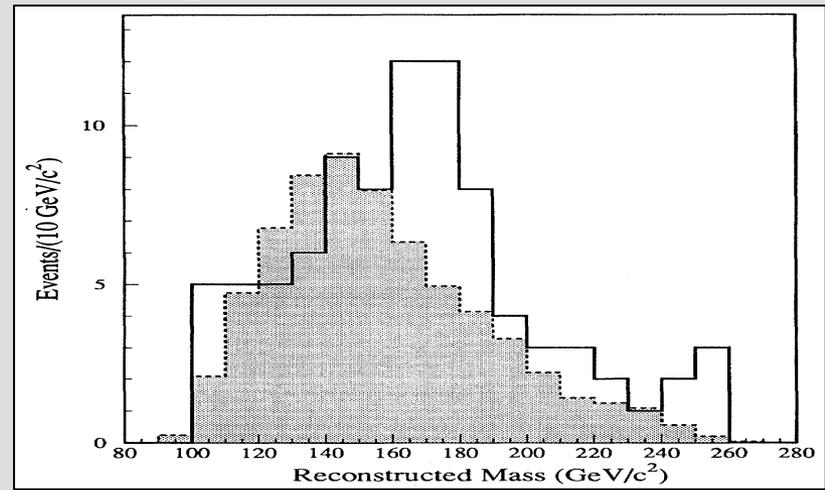


Fig. 2. Completely reconstructed event consisting of the decay  $\Upsilon(4S) \rightarrow B^0 \bar{B}^0$ .

ARGUS, Phys.Lett. B192 (1987) 245



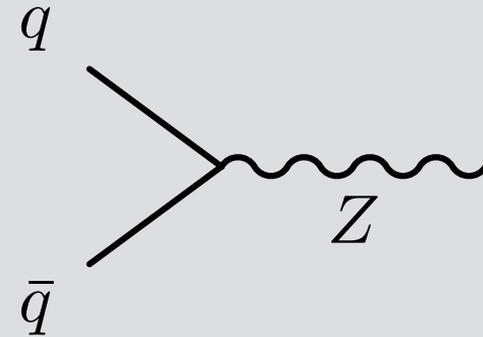
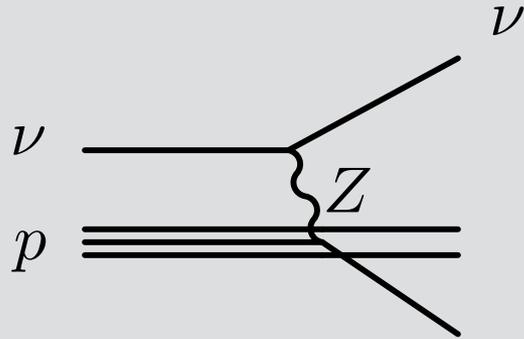
Direct



CDF Coll., Phys.Rev.Lett. 74 (1995) 2626

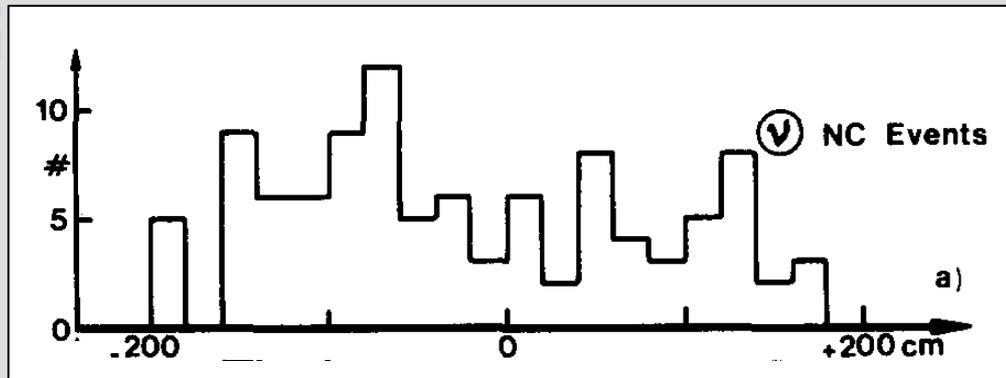
# Historical perspective: Z

- Neutral current interaction was "discovery" of Z?

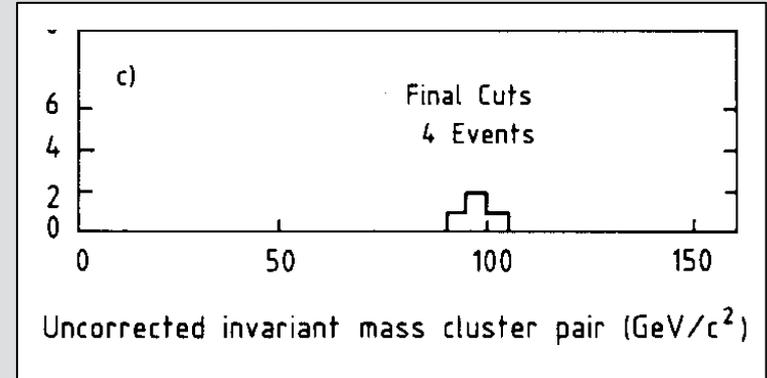


Indirect

Direct



Gargamelle Coll., Phys.Lett. B46 (1973) 138

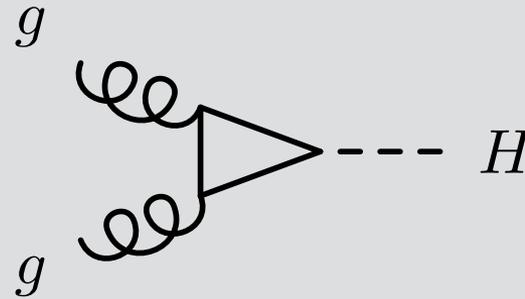
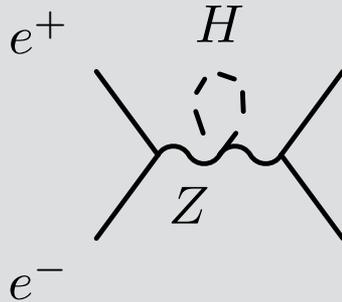


UA1 Coll., Phys.Lett. B126 (1983) 398

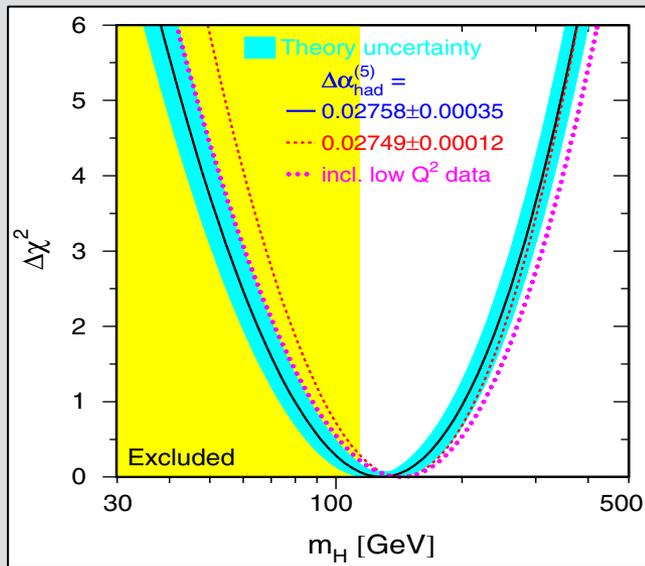


# Historical perspective: Higgs

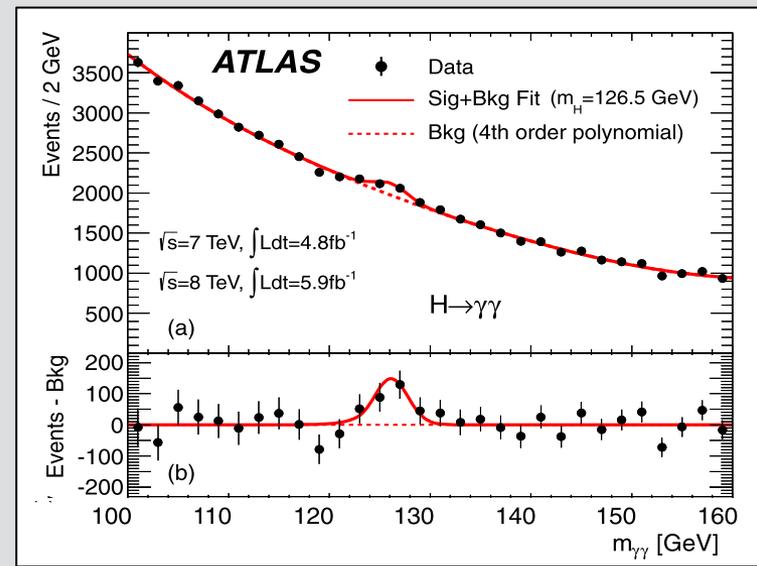
- Precision measurements at LEP were “discovery” of Higgs?



Indirect



LEP, Phys.Rept. 427 (2006) 257



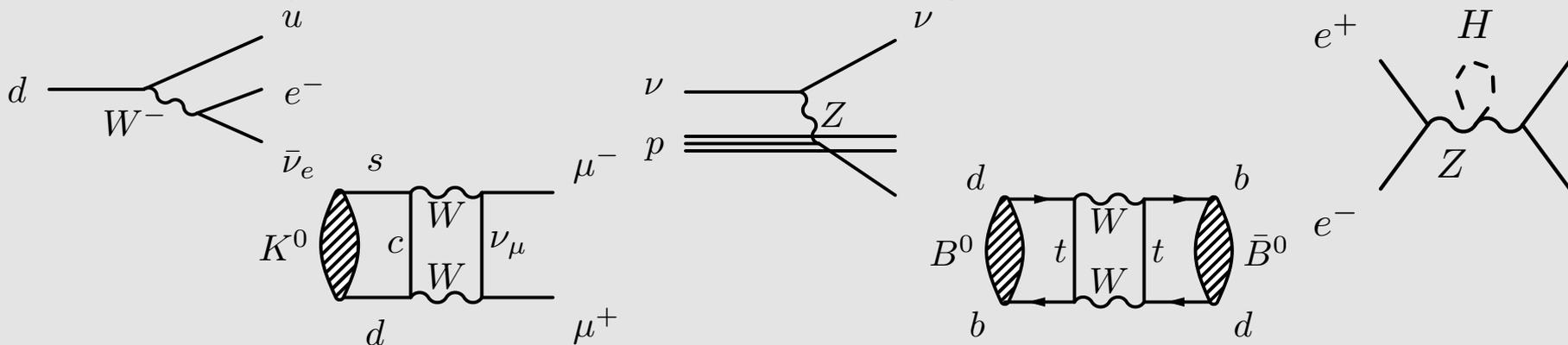
ATLAS Coll., Phys.Lett. B716 (2012) 1

Direct

# Heavy Flavour = Precision search for NP

- Historical record of indirect discoveries:

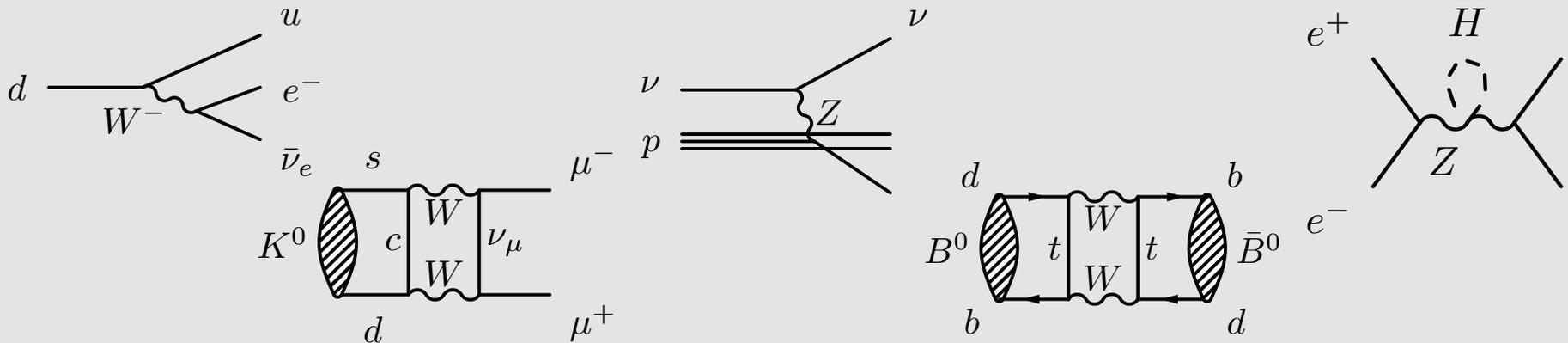
Particle	Indirect			Direct		
$\nu$	$\beta$ decay	Fermi	1932	Reactor $\nu$ -CC	Cowan, Reines	1956
$W$	$\beta$ decay	Fermi	1932	$W \rightarrow e\nu$	UA1, UA2	1983
$c$	$K^0 \rightarrow \mu\mu$	GIM	1970	$J/\psi$	Richter, Ting	1974
$b$	CPV $K^0 \rightarrow \pi\pi$	CKM, 3 <sup>rd</sup> gen	1964/72	$\Upsilon$	Ledermann	1977
$Z$	$\nu$ -NC	Gargamelle	1973	$Z \rightarrow e^+e^-$	UA1	1983
$t$	B mixing	ARGUS	1987	$t \rightarrow Wb$	D0, CDF	1995
$H$	$e^+e^-$	EW fit, LEP	2000	$H \rightarrow 4\mu/\gamma\gamma$	CMS, ATLAS	2012
?	<b>What's next ?</b>					?



# Heavy Flavour = Precision search for NP

- Direct discoveries rightfully higher valued:

Particle	Indirect			Direct		
$\nu$	$\beta$ decay	Fermi	1932 	Reactor $\nu$ -CC	Cowan, Reines	1956 
W	$\beta$ decay	Fermi	1932	$W \rightarrow e\nu$	UA1, UA2	1983 
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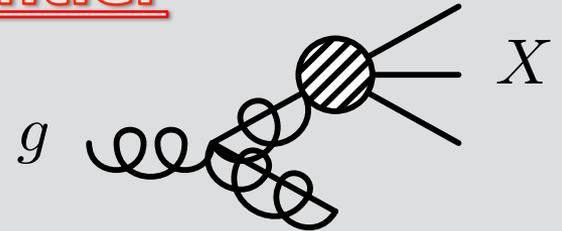
# Precision measurements point to new phenomena



Quantum fluctuations at precision frontier

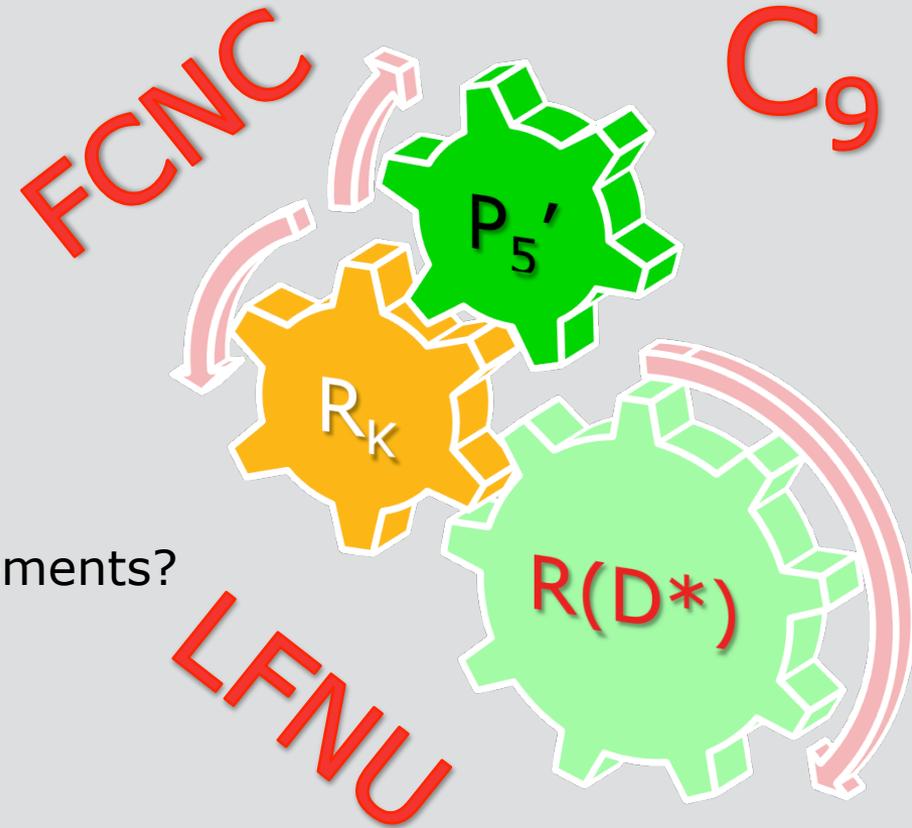
complement

direct production at energy frontier



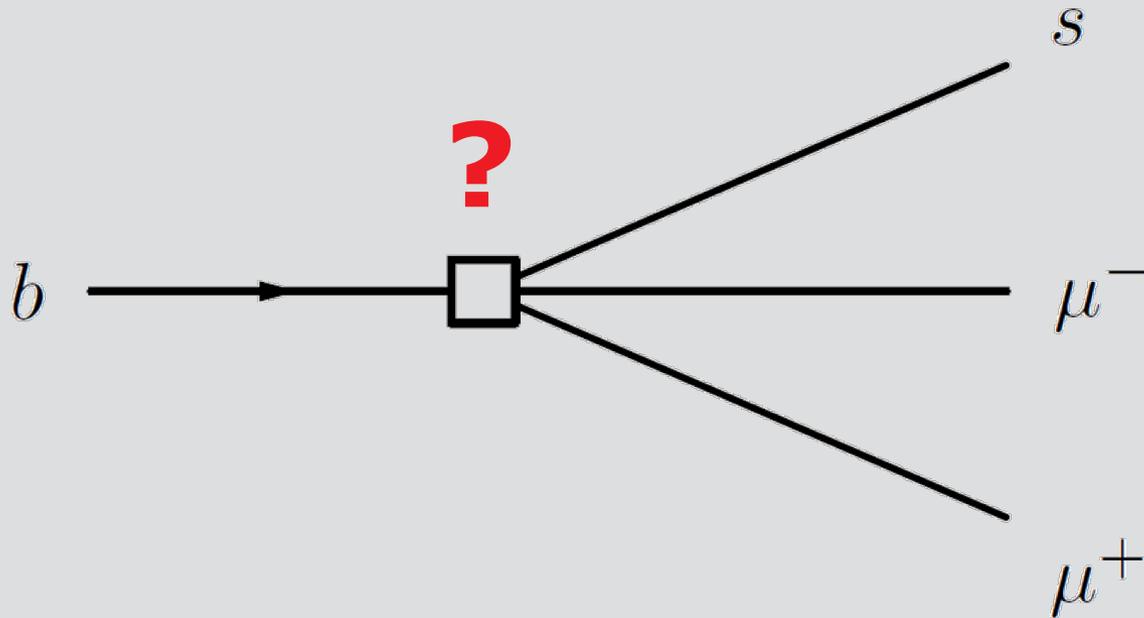
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- Indirect measurements
- What are the (anomalous) measurements?
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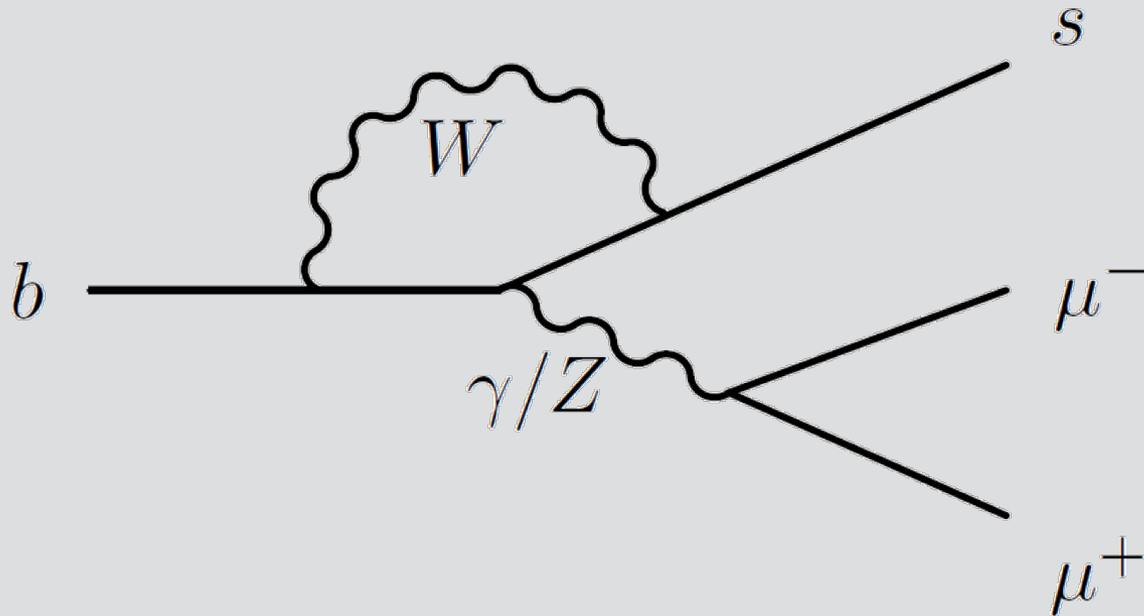
# FCNC: $b \rightarrow sll$

- $b \rightarrow s$  transition forbidden at tree level in SM



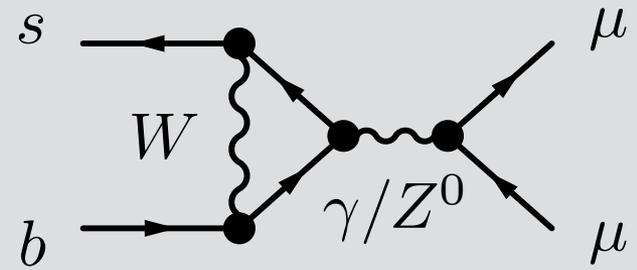
# FCNC: $b \rightarrow sll$

- $b \rightarrow s$  transition occurs at loop level
  - Suppressed in SM
  - NP can compete with SM



# $B_s^0 \rightarrow \mu^+ \mu^-$

- Famous example of  $b \rightarrow sll$  process
- Very, very rare in the SM
- Sensitive to small effects beyond the SM



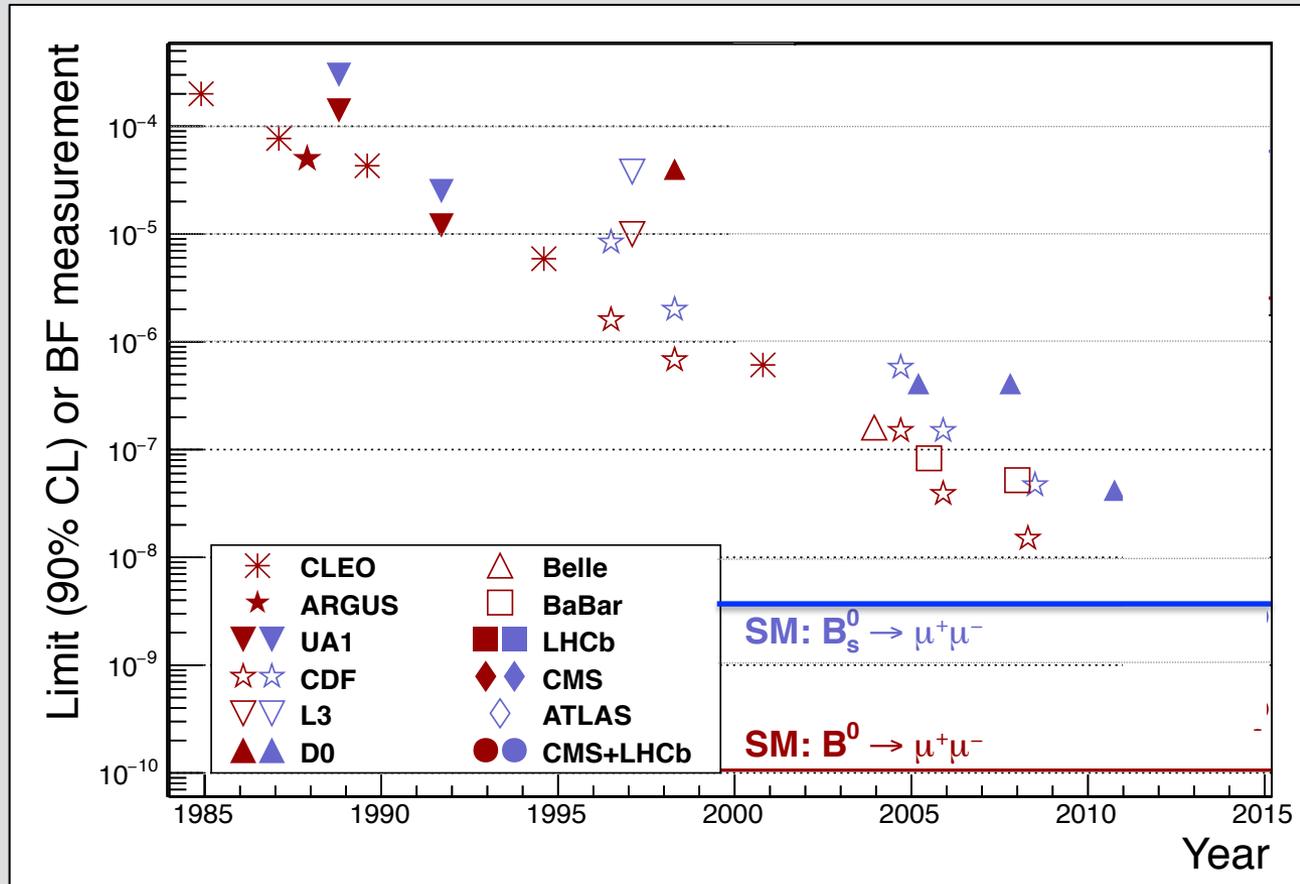
$$N(B_s^0 \rightarrow \mu^+ \mu^-) = C \left| \begin{array}{l} \begin{array}{c} s \rightarrow \mu^+ \\ b \rightarrow \mu^- \end{array} \begin{array}{c} W \\ W \\ \nu \end{array} \begin{array}{c} \mu^+ \\ \mu^- \end{array} + \begin{array}{c} s \rightarrow \mu^+ \\ b \rightarrow \mu^- \end{array} \begin{array}{c} W \\ \gamma/Z^0 \end{array} \begin{array}{c} \mu^+ \\ \mu^- \end{array} + \dots \end{array} \right|^2$$

The equation shows the branching ratio  $N(B_s^0 \rightarrow \mu^+ \mu^-) = C$  multiplied by the square of the sum of several Feynman diagrams. The first row shows two diagrams: one with two  $W$  bosons and a neutrino  $\nu$  loop, and another with one  $W$  boson and a  $\gamma/Z^0$  boson exchange. The second row shows two diagrams: one with a  $\chi$  particle and a  $Z^0$  boson exchange, and another with a  $\chi$  particle and an  $A^0/H^0$  boson exchange. The entire sum is enclosed in large vertical bars with a superscript 2.



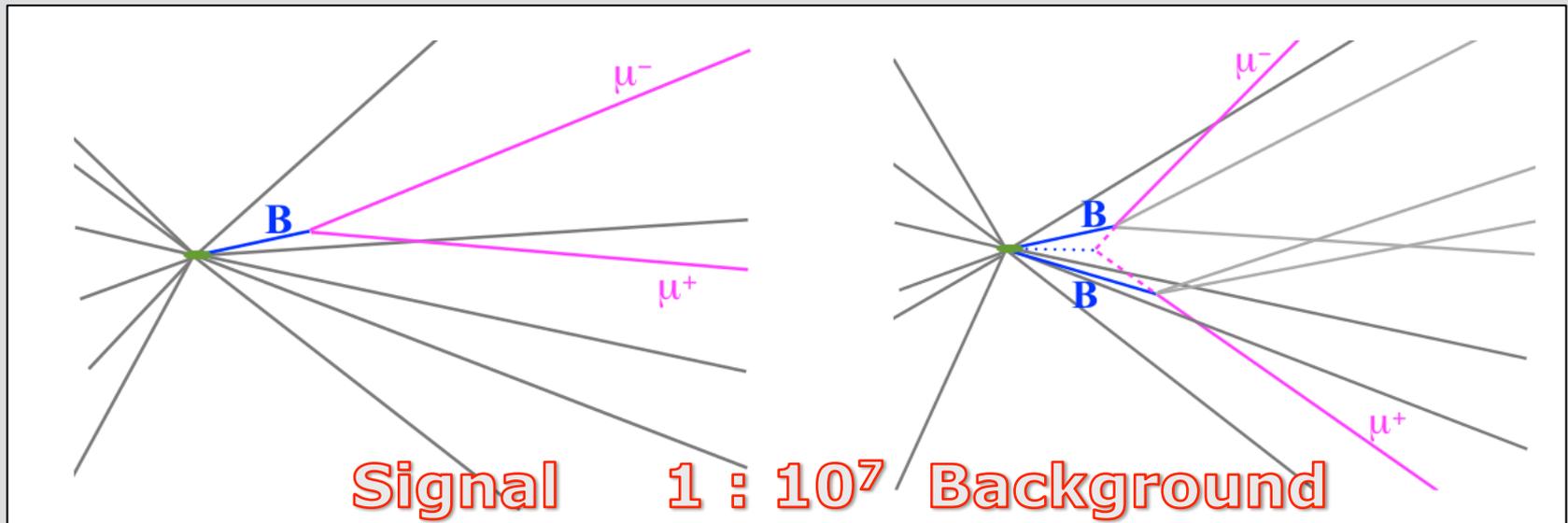
# $B_s^0 \rightarrow \mu^+ \mu^-$

- Historical endeavour!



# $B_s^0 \rightarrow \mu^+ \mu^-$

- Challenge: huge amount of events with two muons!
  - Background:  $BR(B \rightarrow X\mu^+) = 10^{-1}$
  - Signal:  $BR(B_s^0 \rightarrow \mu^+ \mu^-) < 10^{-8}$
- $10^{12}$   $B$  produced; probability of  $\mu\mu$  decay  $10^{-9}$ ; eff  $\sim 5\%$ 
  - Expect  $\sim 50$  events



# $B_s^0 \rightarrow \mu^+ \mu^-$

## Challenge: huge amount of events with two muons!

- Background:  $BR(B \rightarrow X\mu^+) = 10^{-1}$
- Signal:  $BR(B_s^0 \rightarrow \mu^+ \mu^-) < 10^{-8}$

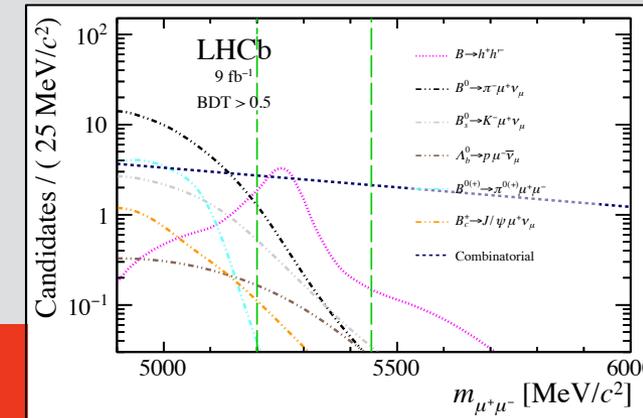
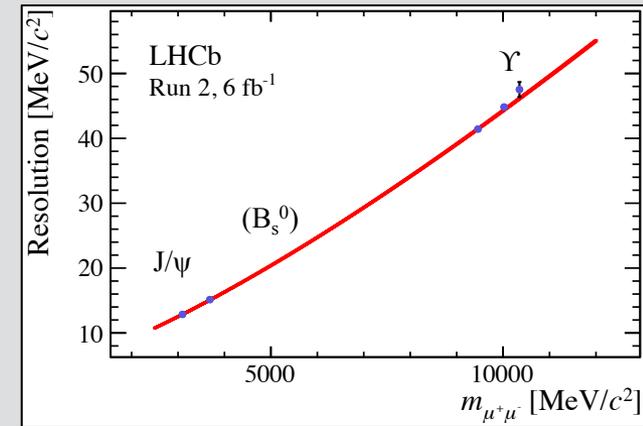
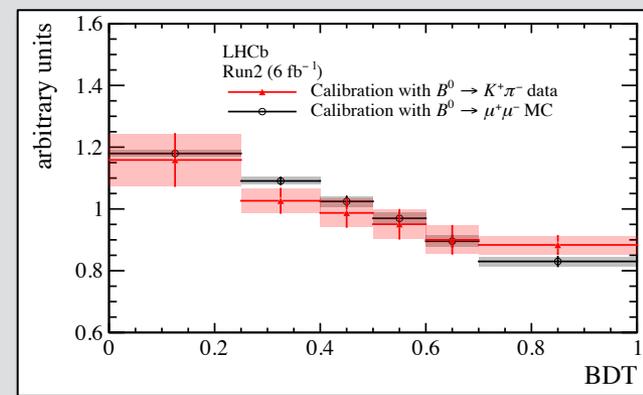
## Analysis:

- BDT event selection
  - Mainly lifetime
  - Calibrate efficiency on data with  $B \rightarrow \pi\pi\pi$  decays
- Mass resolution
  - Interpolate between  $J/\psi \rightarrow \mu\mu$  and  $Y \rightarrow \mu\mu$
- Backgrounds
  - $b \rightarrow \mu + b \rightarrow \mu$
  - Semileptonic  $B^0, B_s^0, B_c^+$  and  $\Lambda_b^0$  decays
  - Misidentified  $B \rightarrow \pi\pi$

## Largest systematic uncertainty:

- Relative production of  $B_s^0$  wrt  $B^0$  mesons,  $f_s/f_d$

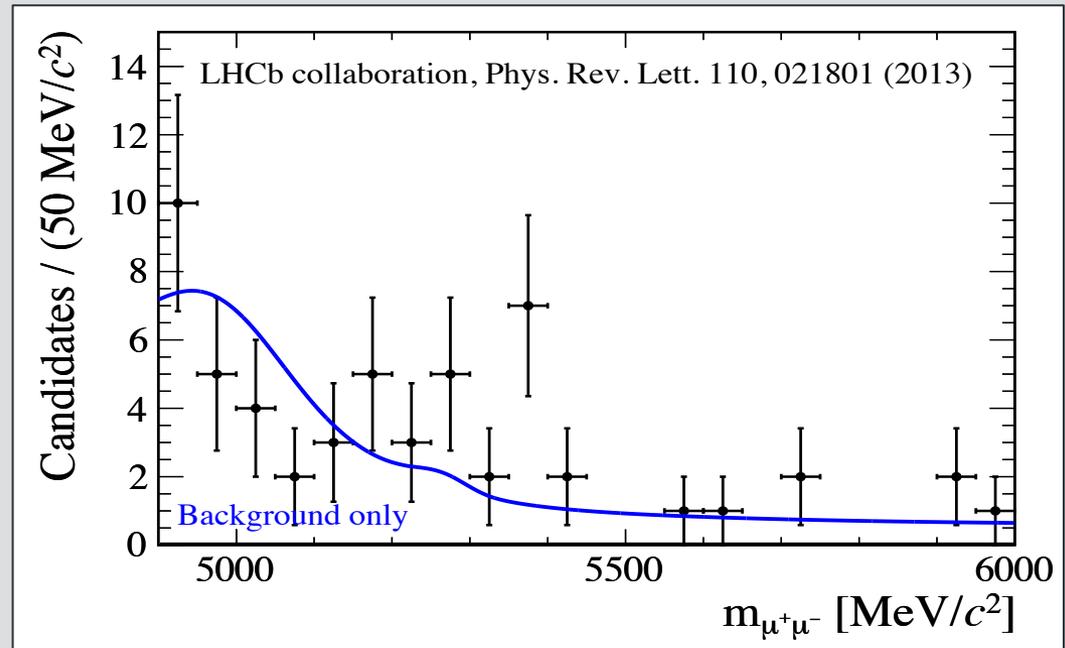
LHCb coll., [arXiv:2103.06810](https://arxiv.org/abs/2103.06810)



LHCb coll., PAPER-2021-007



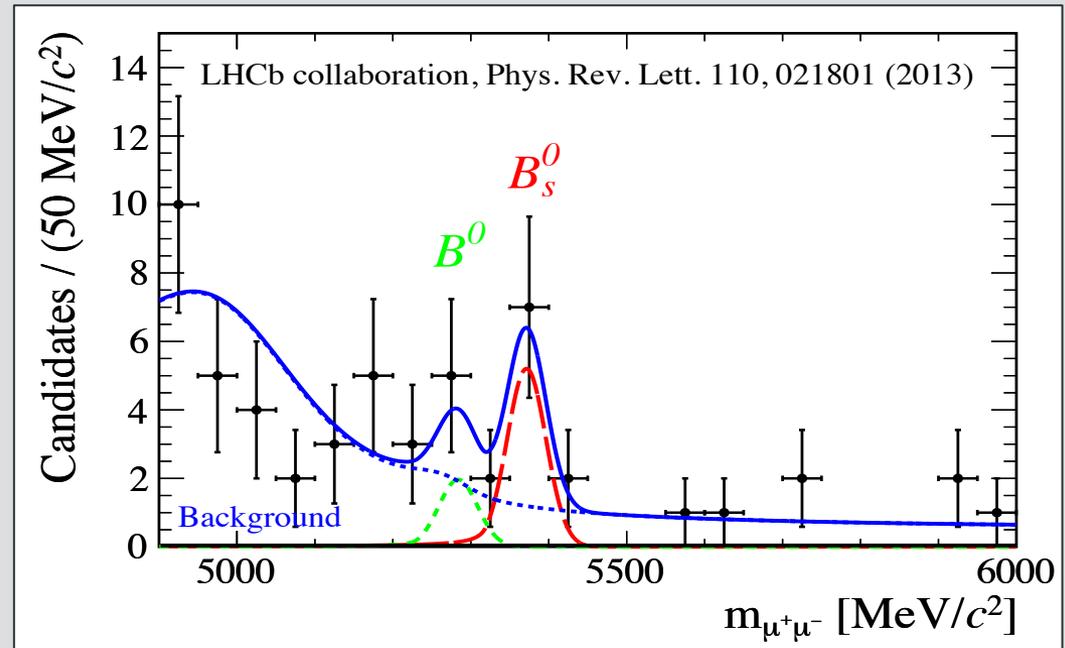
$$B_s^0 \rightarrow \mu^+ \mu^-$$



LHCb Coll. Phys.Rev.Lett. 110, 021801 (2013)

# $B_s^0 \rightarrow \mu^+ \mu^-$

- First evidence,  $3.5\sigma$ 
  - '11, part '12
  - $2.1 \text{ fb}^{-1}$

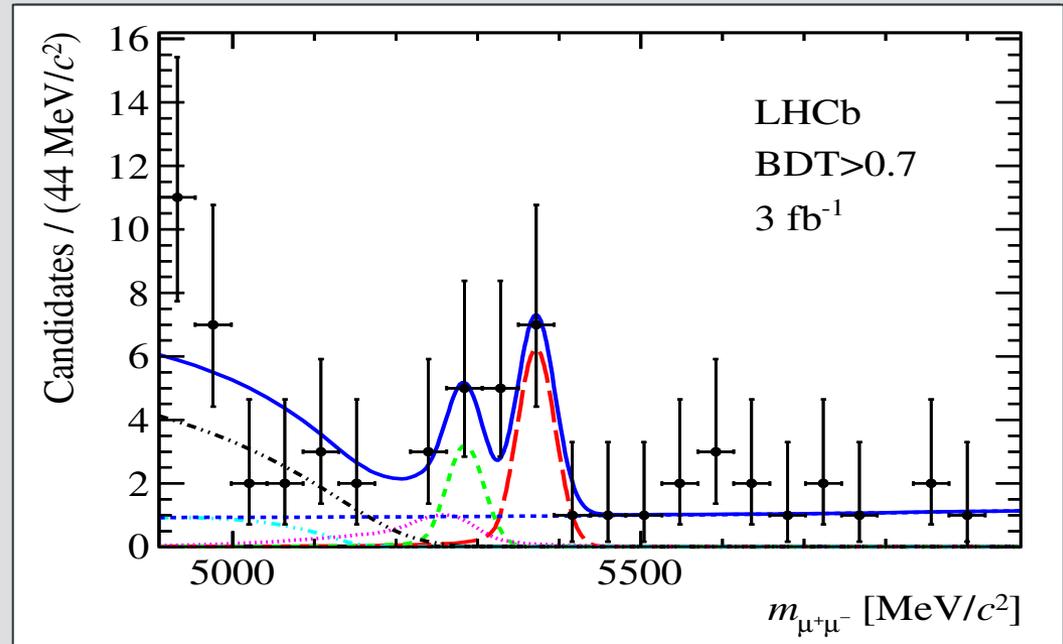


LHCb Coll. Phys.Rev.Lett. 110, 021801 (2013)

# $B_s^0 \rightarrow \mu^+ \mu^-$

4.0 $\sigma$

- '11 and '12
- 3.0 fb<sup>-1</sup>

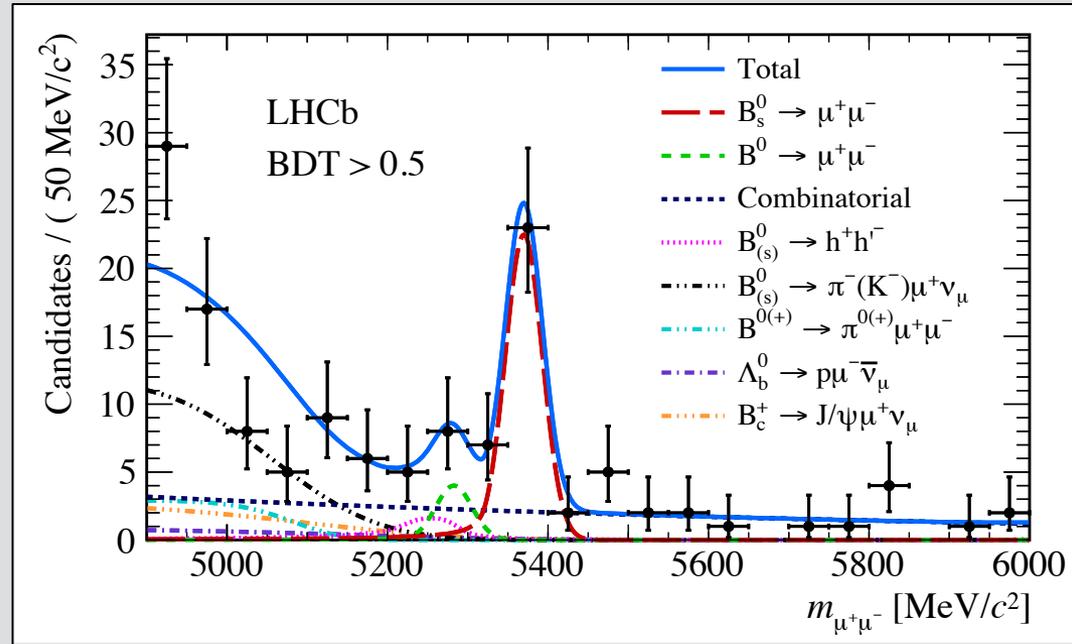


LHCb Coll. Phys.Rev.Lett. 111, 101805 (2013)

# $B_s^0 \rightarrow \mu^+ \mu^-$

7.8 $\sigma$

- '11, '12, '15, part '16
- 4.4 fb<sup>-1</sup>

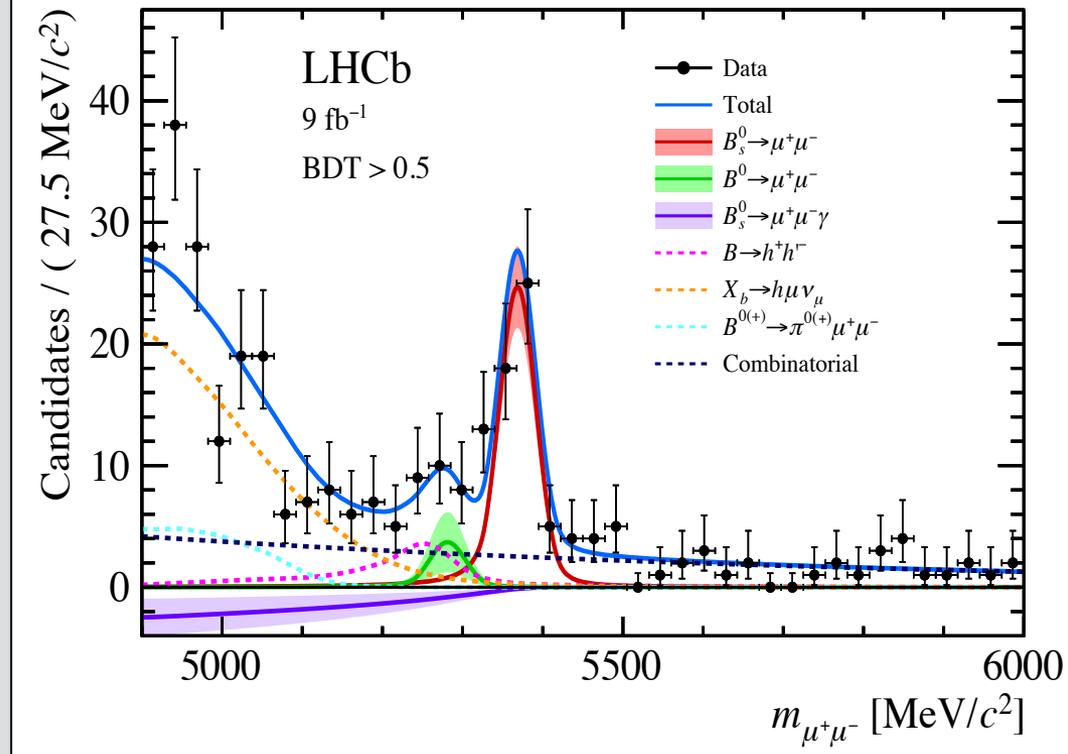


LHCb Coll. Phys.Rev.Lett. 118, 191801 (2017)

# $B_s^0 \rightarrow \mu^+ \mu^-$

10  $\sigma$

- Full data set
- 9 fb<sup>-1</sup>



LHCb Coll. PAPER-2021-007

$$\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-) = (3.09^{+0.46+0.15}_{-0.43-0.11}) \times 10^{-9}$$

New result



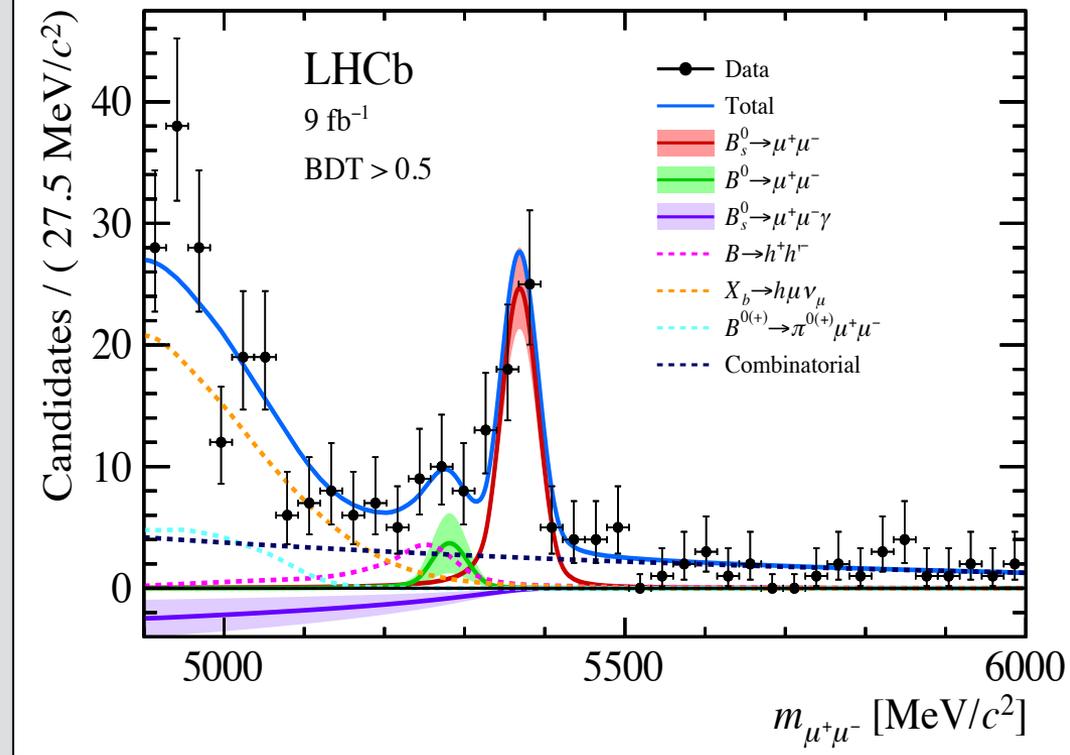
$$B_s^0 \rightarrow \mu^+ \mu^-$$

10  $\sigma$

- Full data set
- 9 fb<sup>-1</sup>

$$B^0 \rightarrow \mu^+ \mu^- ?$$

$$B_s^0 \rightarrow \mu^+ \mu^- \gamma ?$$



LHCb Coll. PAPER-2021-007

Theory:

$$\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-) = (3.66 \pm 0.14) \times 10^{-9}$$

$$\mathcal{B}(B^0 \rightarrow \mu^+ \mu^-) = (1.03 \pm 0.05) \times 10^{-10}$$

$$\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-) = (3.09^{+0.46+0.15}_{-0.43-0.11}) \times 10^{-9}$$

$$\mathcal{B}(B^0 \rightarrow \mu^+ \mu^-) < 2.6 \times 10^{-10}$$

$$\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^- \gamma)_{m_{\mu\mu} > 4.9 \text{ GeV}/c^2} < 2.0 \times 10^{-9}$$

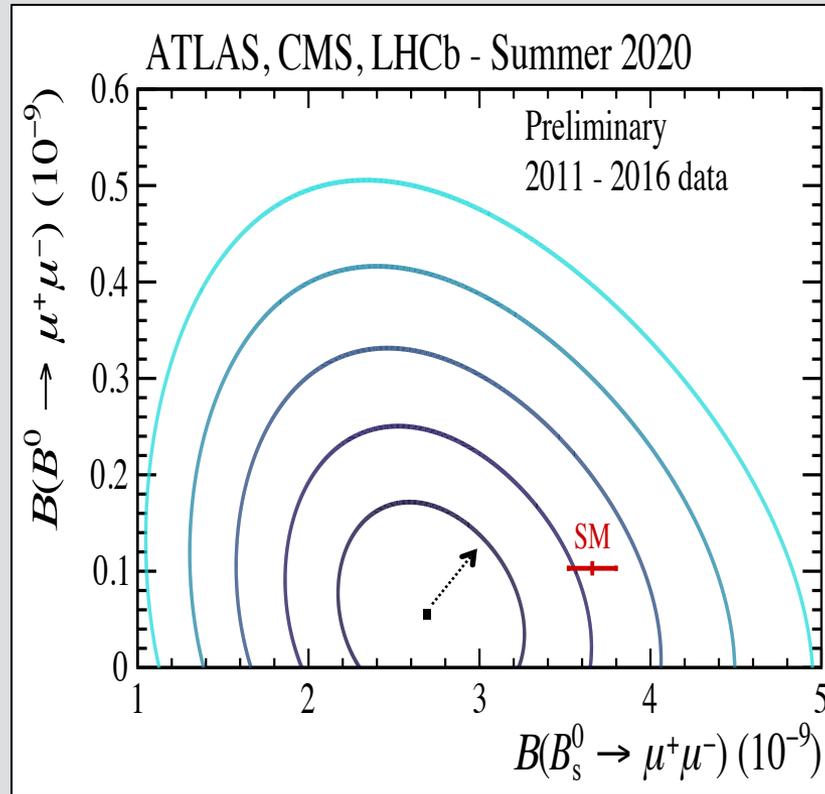
Beneke, Bobeth, Szafron, arXiv:1908.07011

$$B_s^0 \rightarrow \mu^+ \mu^-$$

■  $10 \sigma$

- Full data set
- $9 \text{ fb}^{-1}$

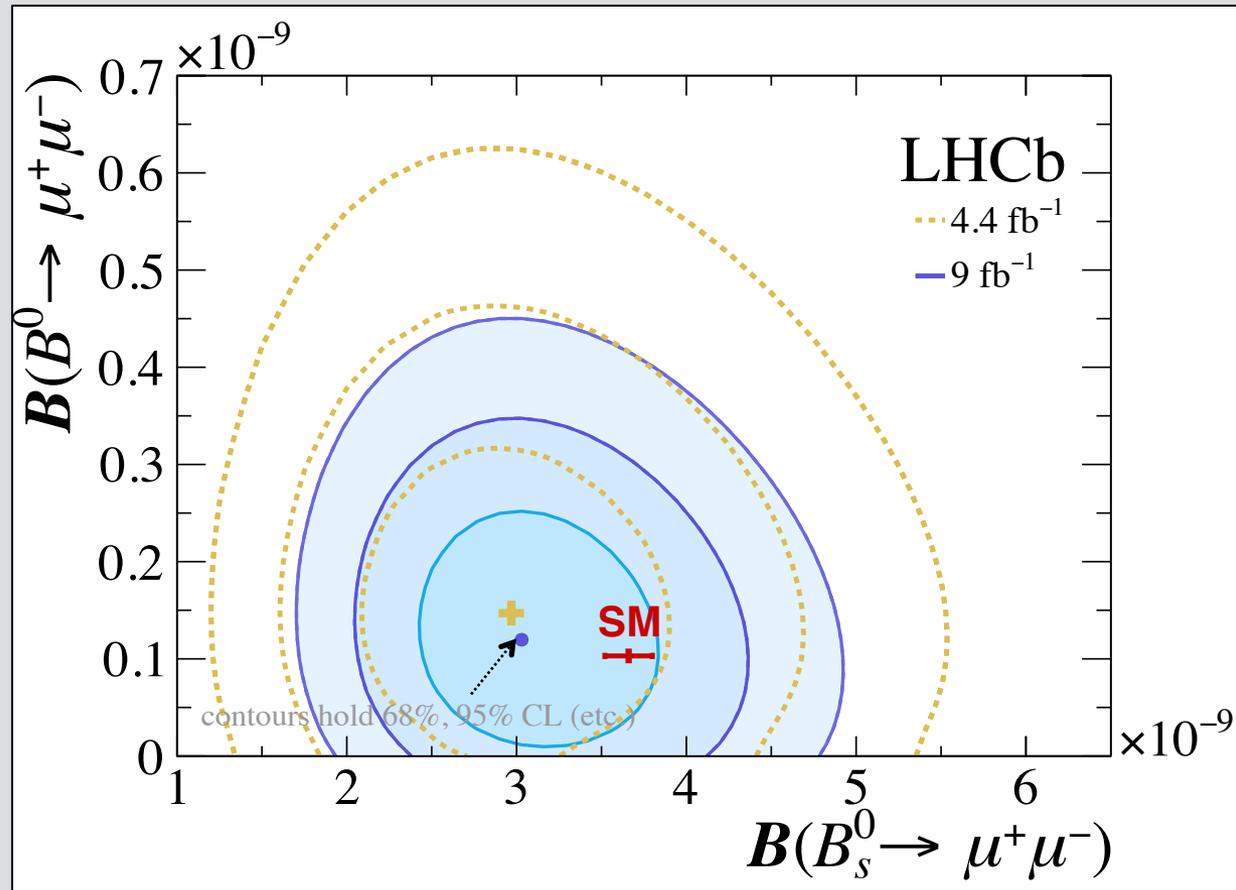
$$B^0 \rightarrow \mu^+ \mu^-$$



# $B_s^0 \rightarrow \mu^+ \mu^-$

- $10 \sigma$
- Full data set
- $9 \text{ fb}^{-1}$

# $B^0 \rightarrow \mu^+ \mu^-$



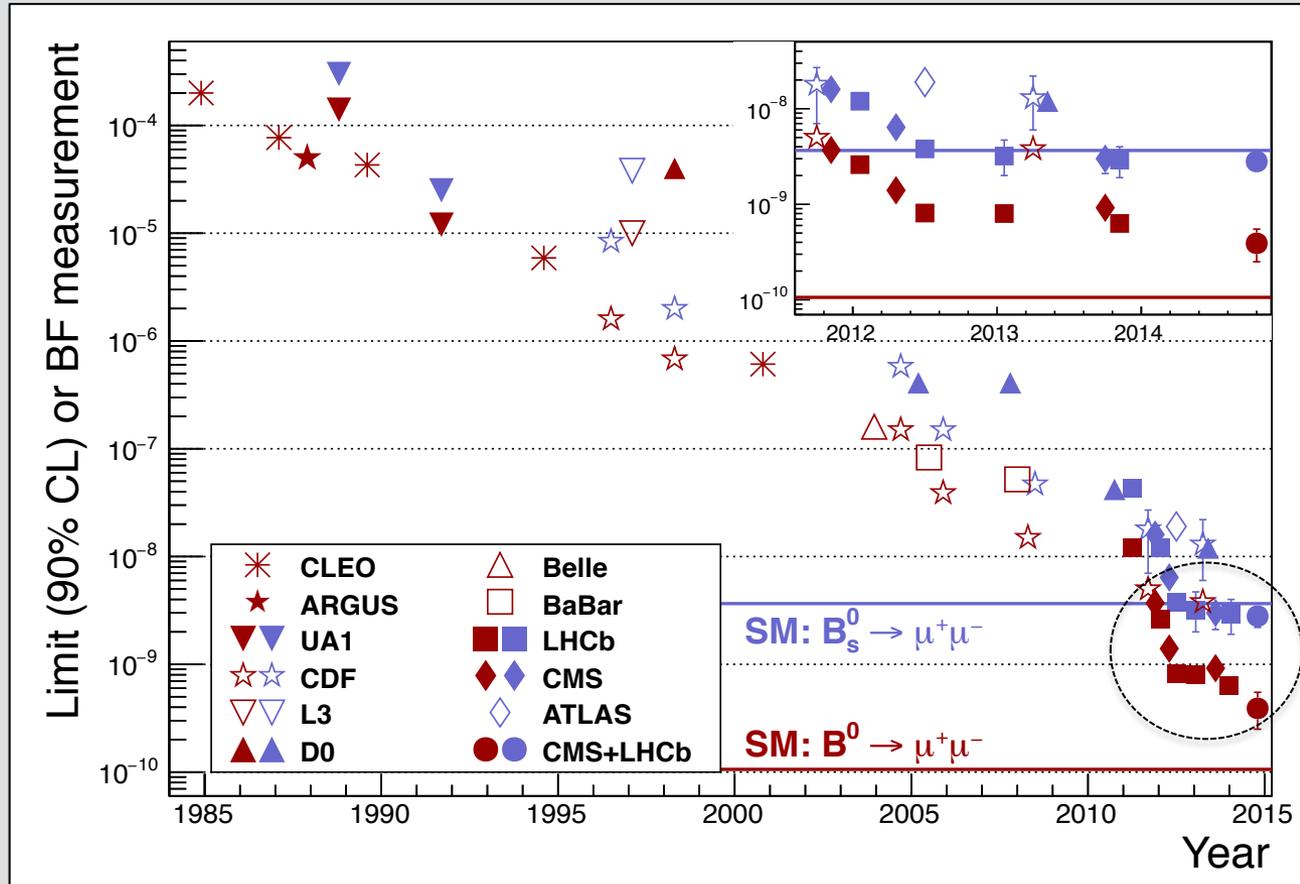
- Relative production of  $B_s^0$  wrt  $B^0$  mesons,  $f_s/f_d$  :
- updated average recently!

$$\begin{aligned} f_s/f_d (7 \text{ TeV}) &= 0.2390 \pm 0.0076 \\ f_s/f_d (8 \text{ TeV}) &= 0.2385 \pm 0.0075 \\ f_s/f_d (13 \text{ TeV}) &= 0.2539 \pm 0.0079 \end{aligned}$$

LHCb coll., [arXiv:2103.06810](https://arxiv.org/abs/2103.06810)

# $B_s^0 \rightarrow \mu^+ \mu^-$

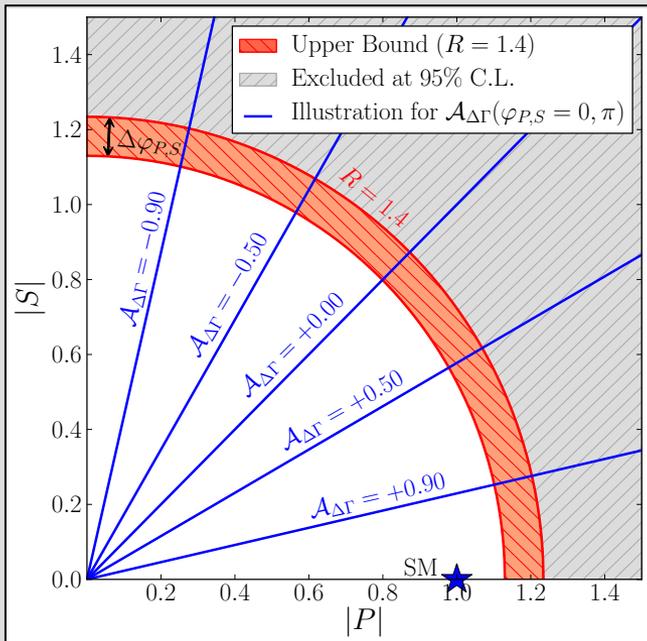
- Historical endeavour!



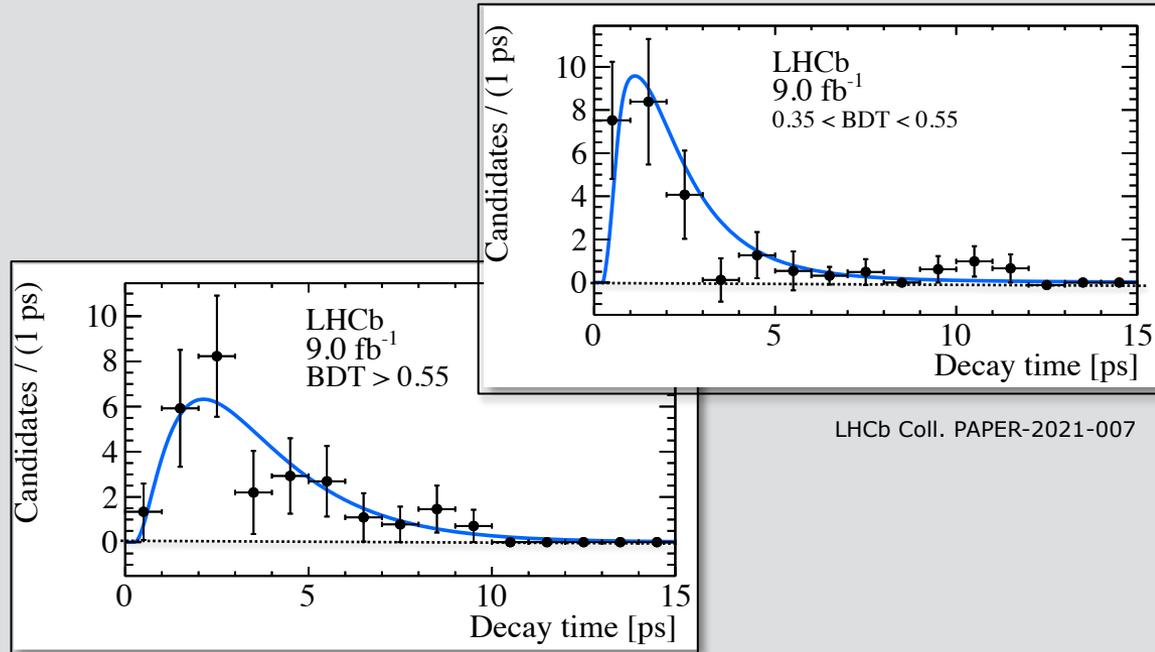
# $B_s^0 \rightarrow \mu^+ \mu^-$

New result

- More observables accessible
- New Physics can lead to different CP structure of final state
  - Affects the mix of long and short-living  $B_s^0$  mesons



De Bruyn, Fleischer, NT, et al., PRL109 (2012) 041801

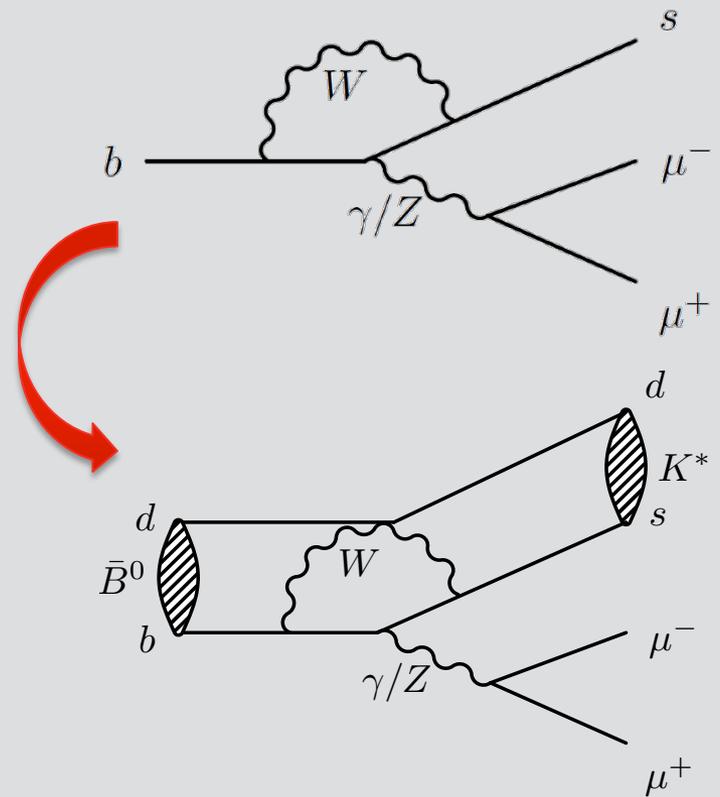


LHCb Coll. PAPER-2021-007

$$\tau(B_s^0 \rightarrow \mu^+ \mu^-) = 2.07 \pm 0.29 \pm 0.03 \text{ ps}$$

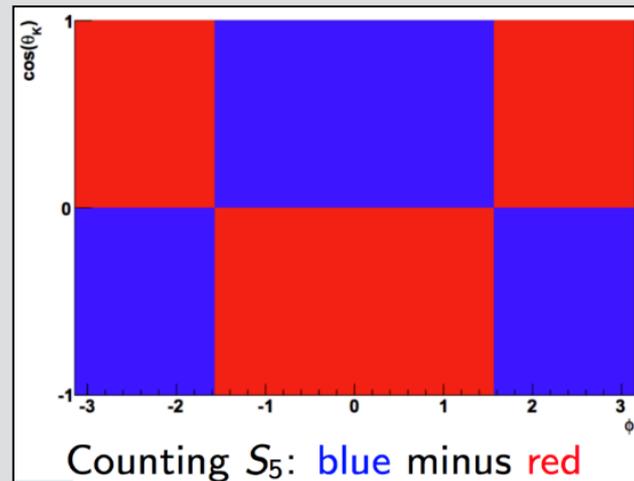
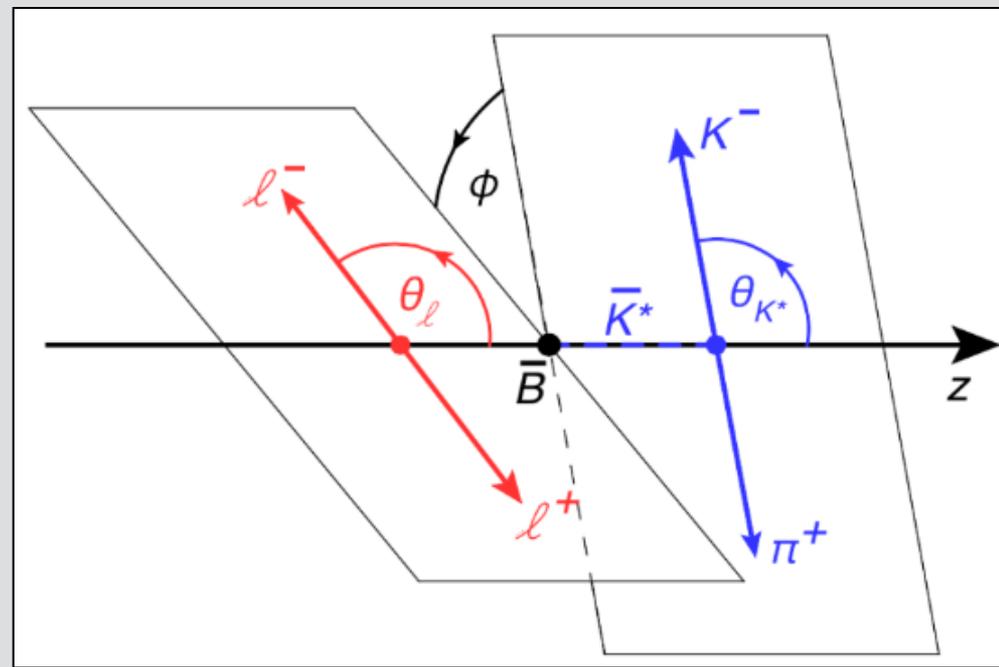
# FCNC: $B^0 \rightarrow K^{*0} \mu \mu$

- Similar loop diagram!
- More observables
  - Invariant mass of  $\mu\mu$ -pair
  - Angles of  $K$  and  $\mu$



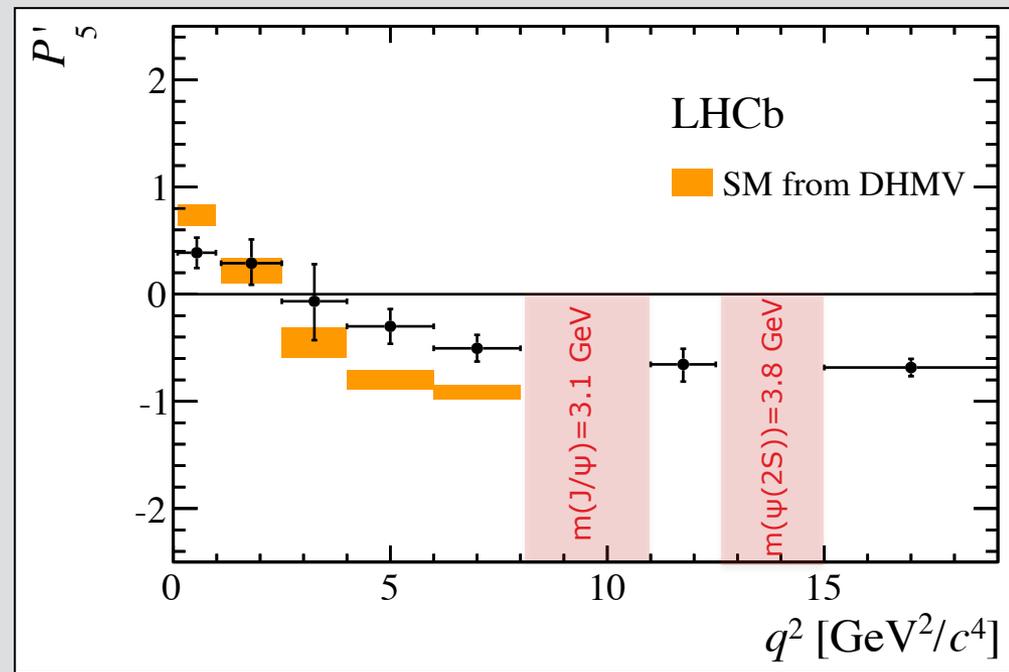
# $B^0 \rightarrow K^{*0} \mu^+ \mu^-$

- Similar loop diagram!
- More observables
  - Invariant mass of  $\mu\mu$ -pair
  - Angles of  $K$  and  $\mu$
- For example,
  - asymmetry of red and blue:



# $B^0 \rightarrow K^{*0} \mu^+ \mu^-$

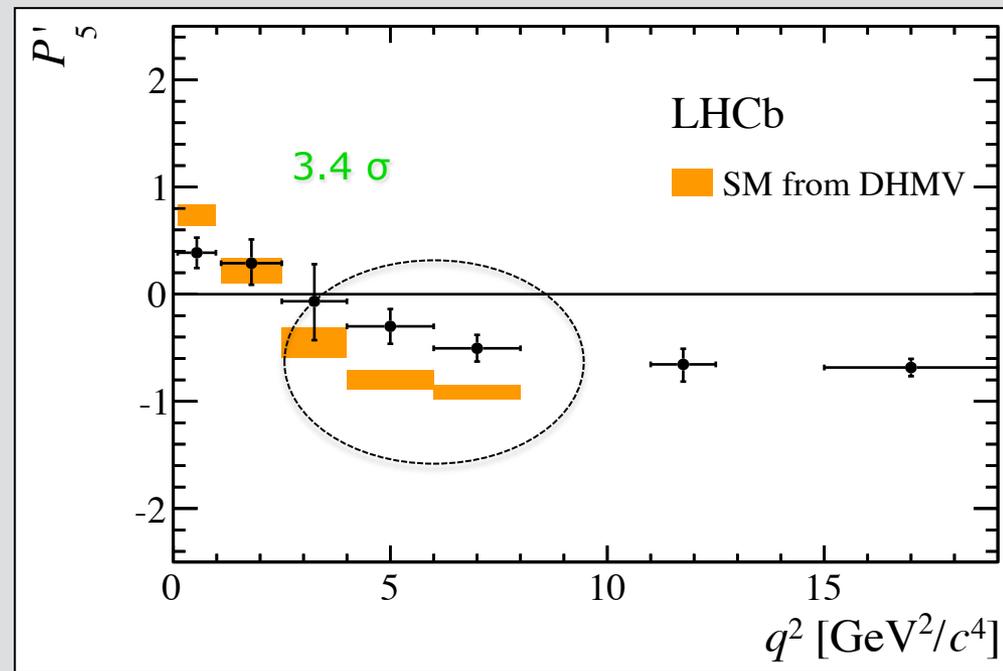
- Similar loop diagram!
- More observables
  - Invariant mass of  $\mu\mu$ -pair
  - Angles of  $K$  and  $\mu$



LHCb, arXiv:1512.04442

# $B^0 \rightarrow K^{*0} \mu^+ \mu^-$

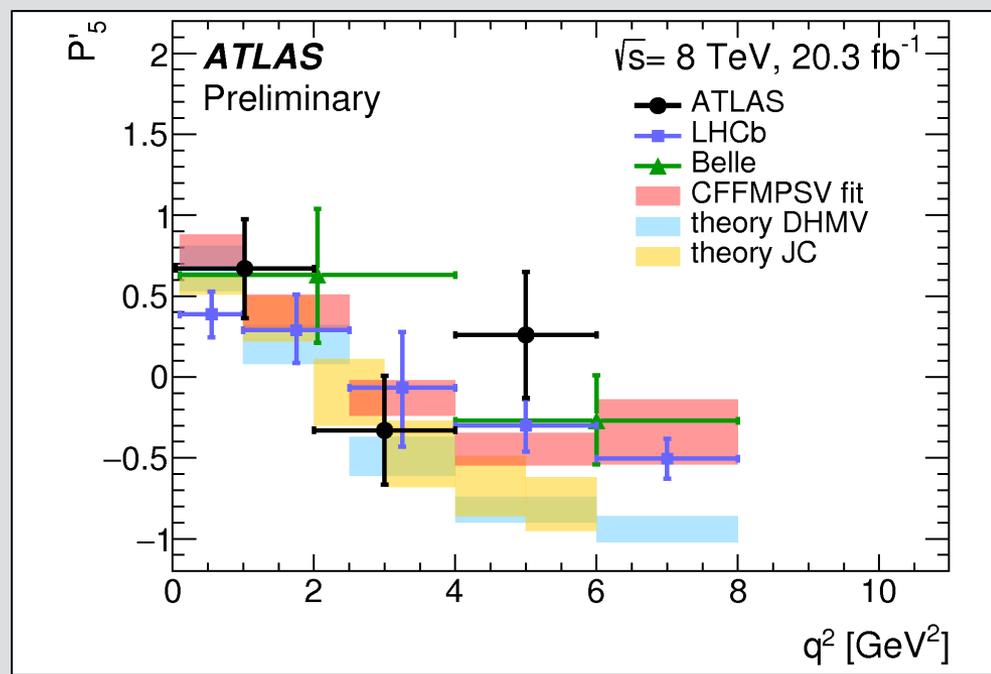
- Similar loop diagram!
- More observables
  - Invariant mass of  $\mu\mu$ -pair
  - Angles of  $K$  and  $\mu$
- Debate on SM calculation
  - Non-perturbative "charm loop" effects?



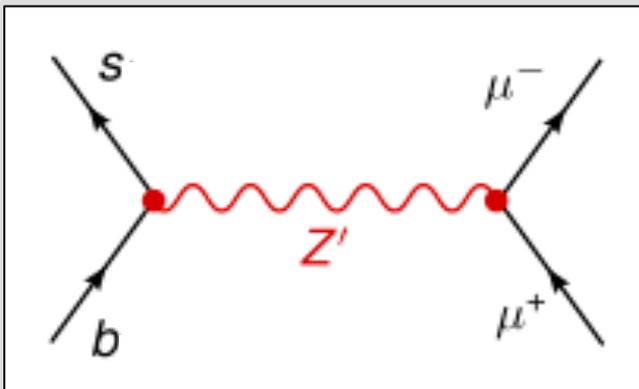
LHCb, arXiv:1512.04442

# $B^0 \rightarrow K^{*0} \mu^+ \mu^-$

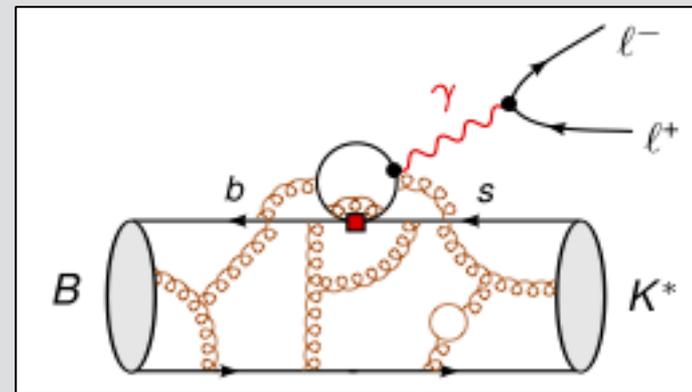
- Similar loop diagram!
- More observables
  - Invariant mass of  $\mu\mu$ -pair
  - Angles of  $K$  and  $\mu$
- Debate on SM calculation
  - Non-perturbative "charm loop" effects?



ATLAS-CONF-2017-023



or

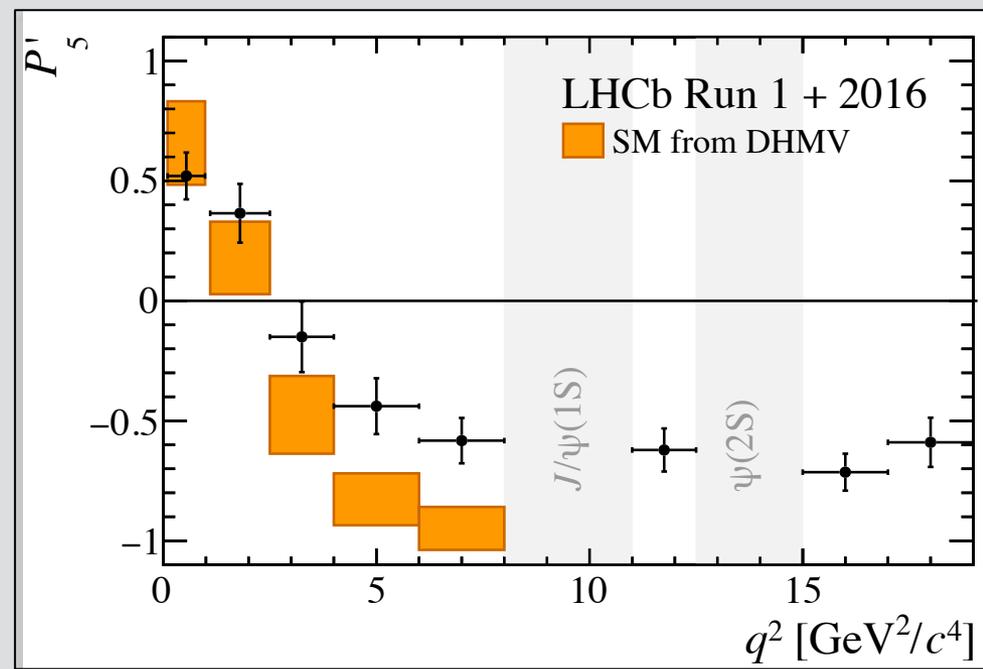


?



# $B^0 \rightarrow K^{*0} \mu^+ \mu^-$

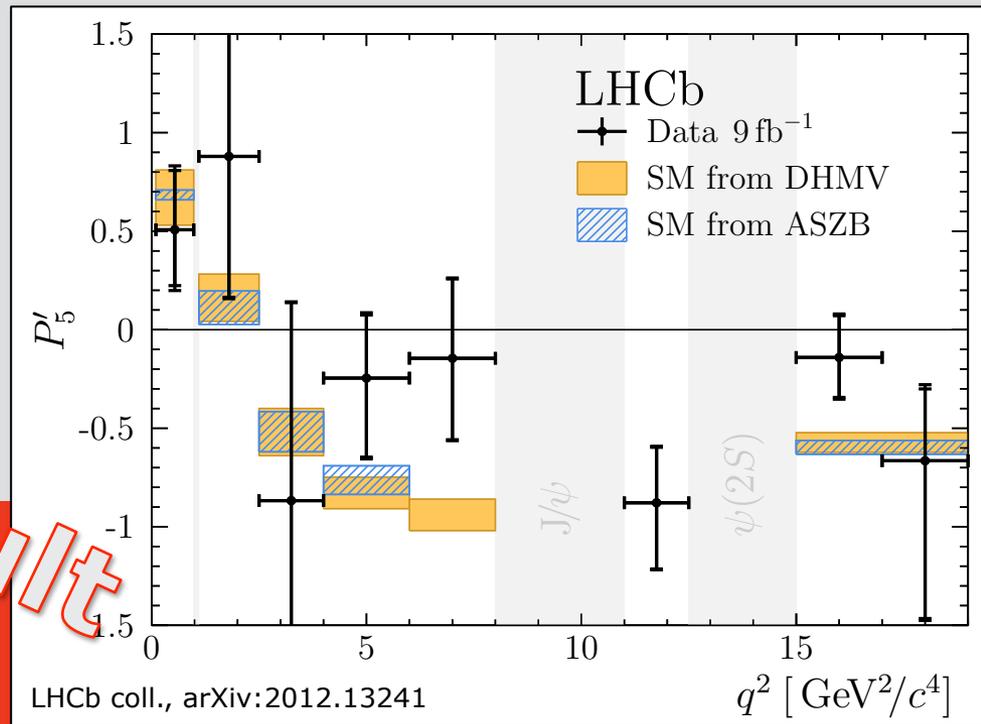
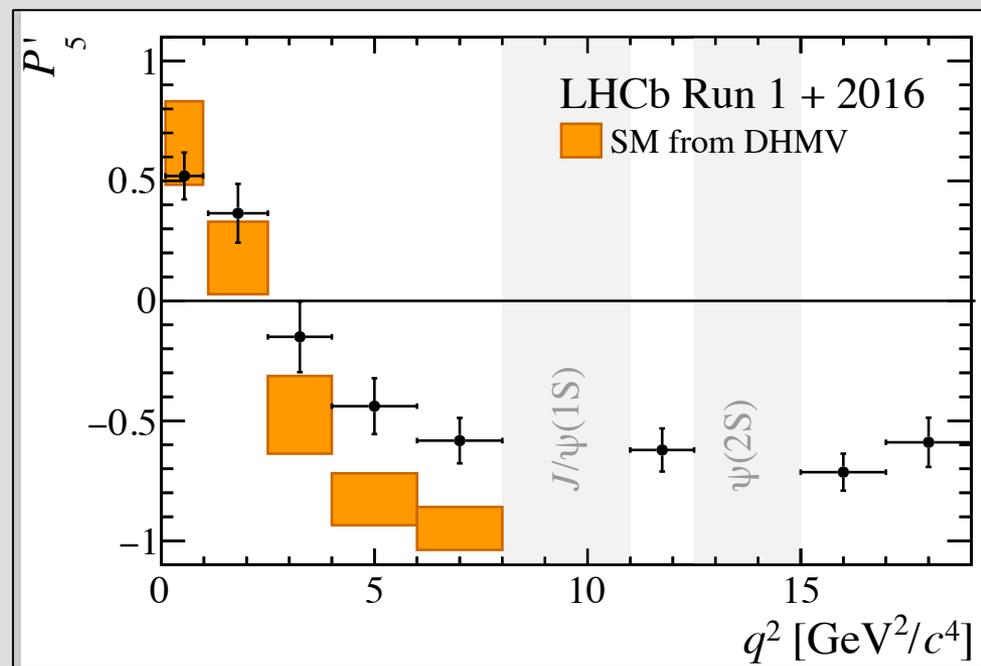
- Similar loop diagram!
- More observables
  - Invariant mass of  $\mu\mu$ -pair
  - Angles of  $K$  and  $\mu$
- Debate on SM calculation
  - Non-perturbative "charm loop" effects?



LHCb coll., arXiv:2003.04831

# $B^+ \rightarrow K^{*+} \mu^+ \mu^-$

- Similar loop diagram!
- More observables
  - Invariant mass of  $\mu\mu$ -pair
  - Angles of  $K$  and  $\mu$
- Recently, the charged  $B^+$  confirmed the same trend:

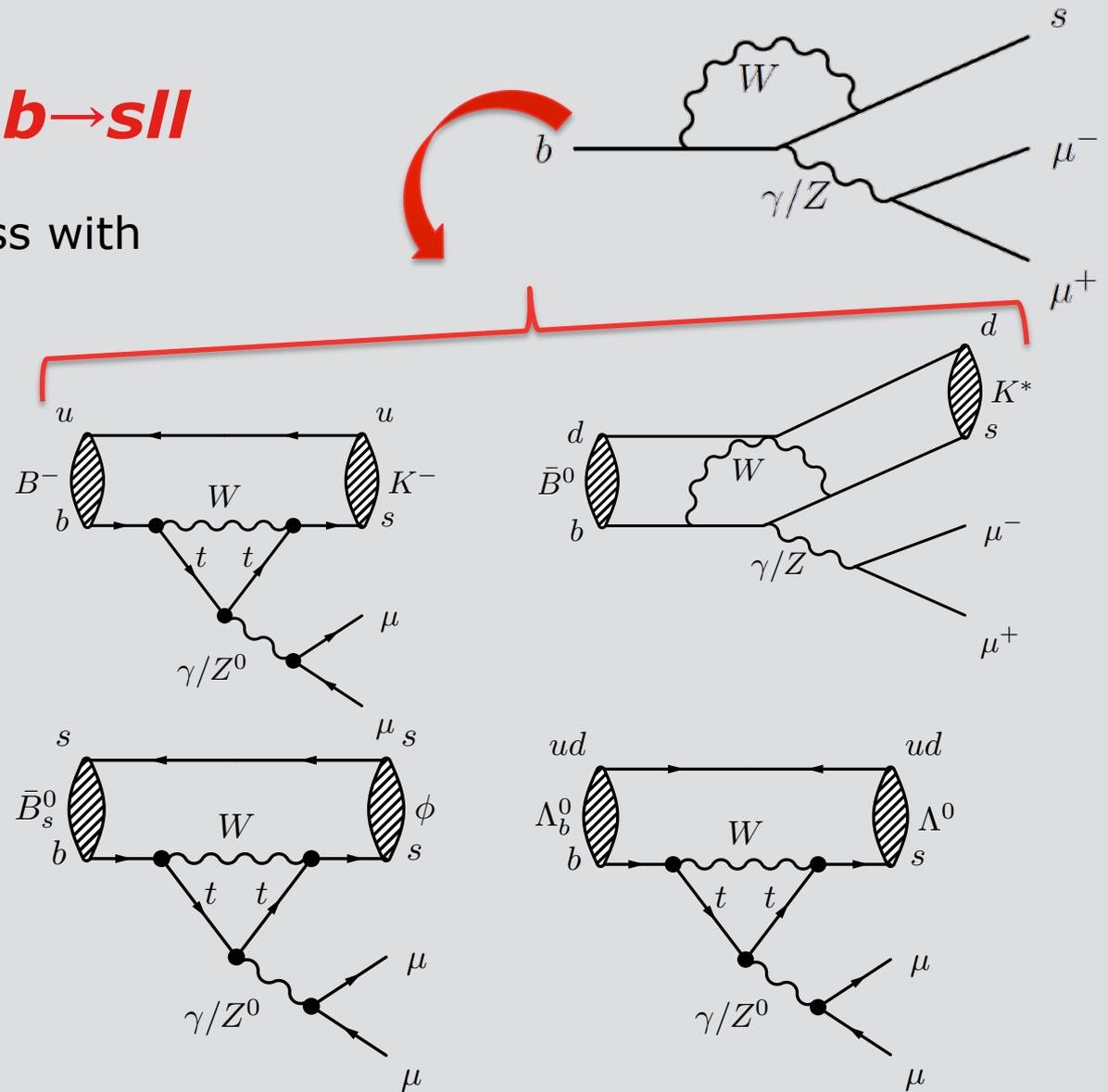


New result



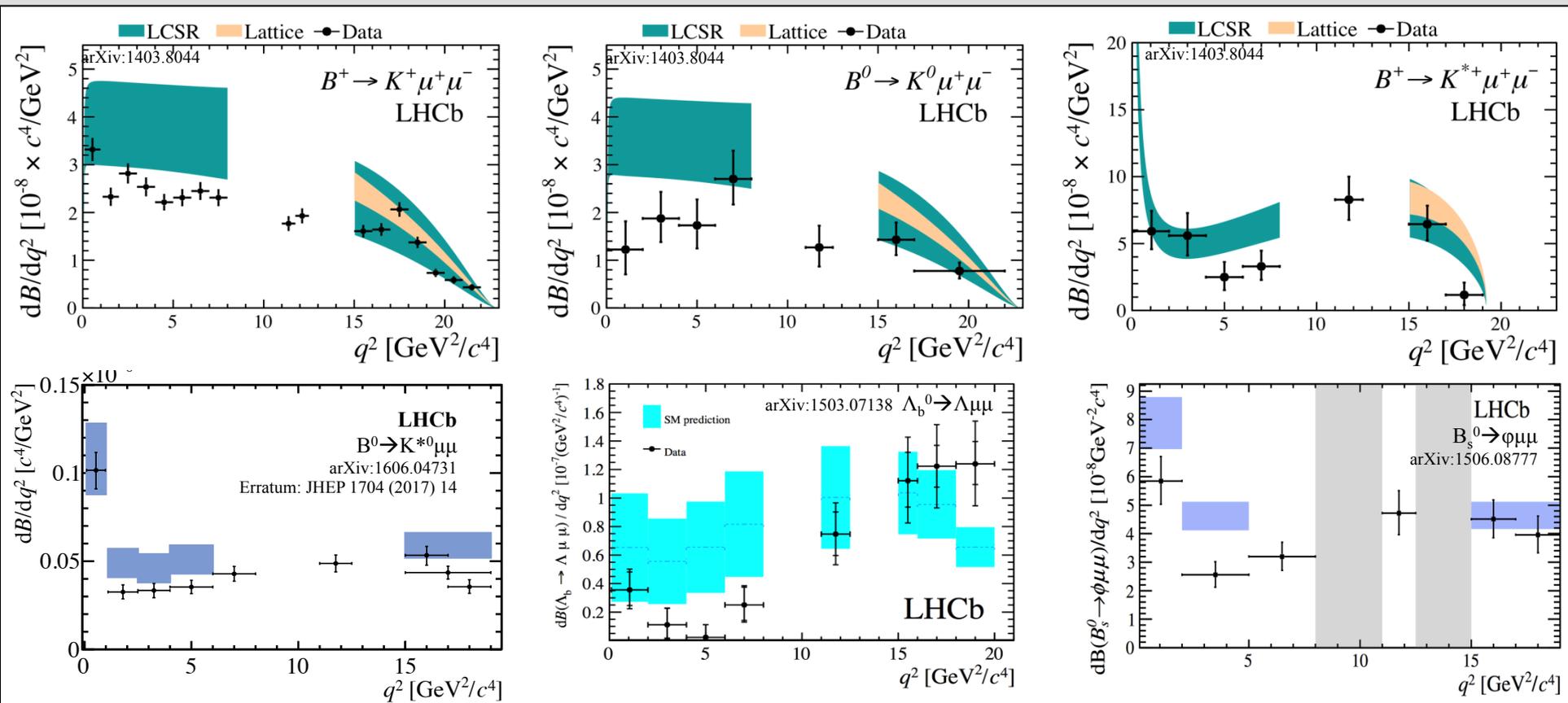
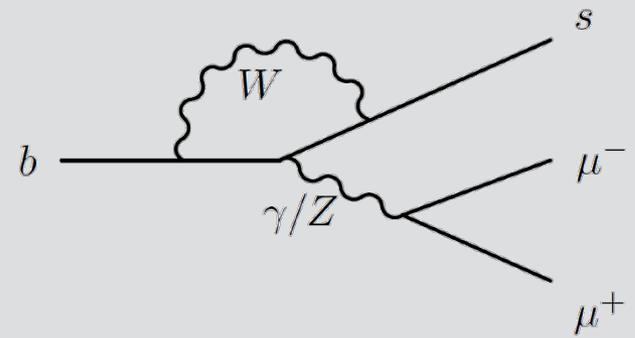
# Decay rates: $b \rightarrow sll$

- Study **same** process with **different** hadrons:



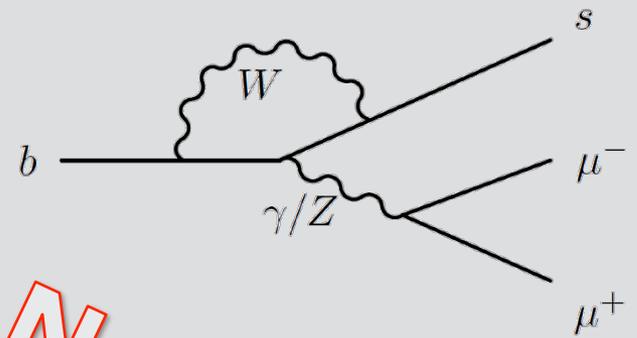
# Decay rates: $b \rightarrow sll$

- Decay rate is consistently low:

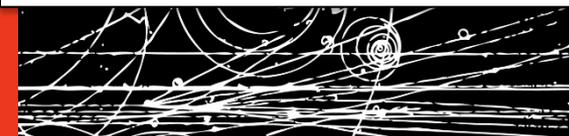
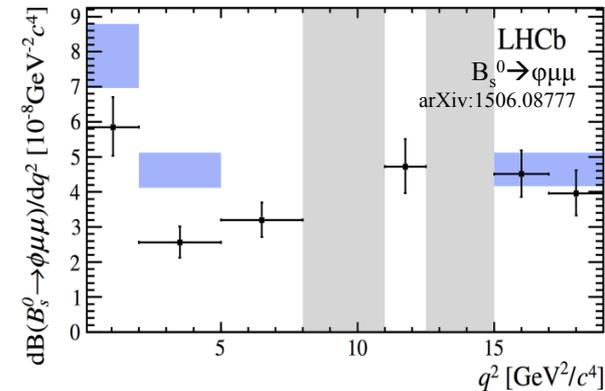
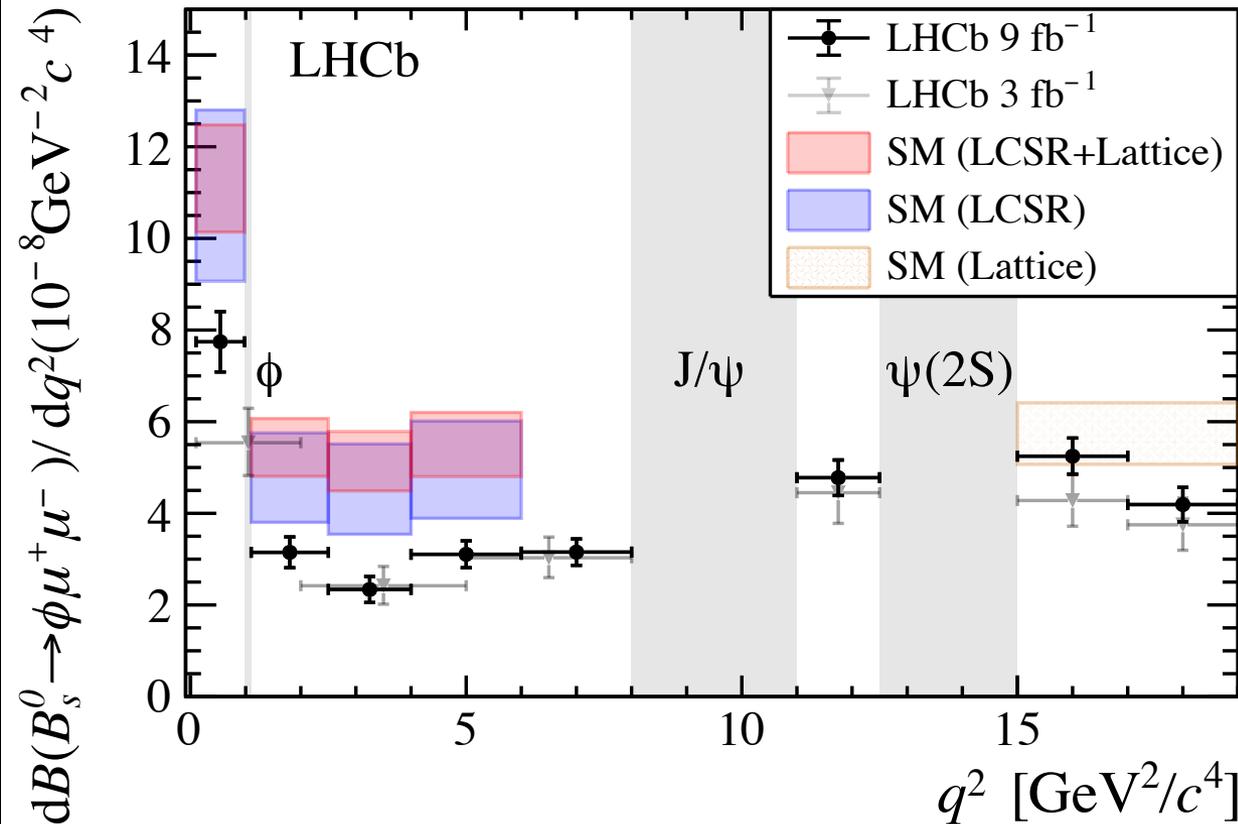


# Decay rates: $b \rightarrow sll$

- Decay rate is consistently low:
  - 3.6 (1.8)  $\sigma$  below LCSR+Lattice (LCSR)

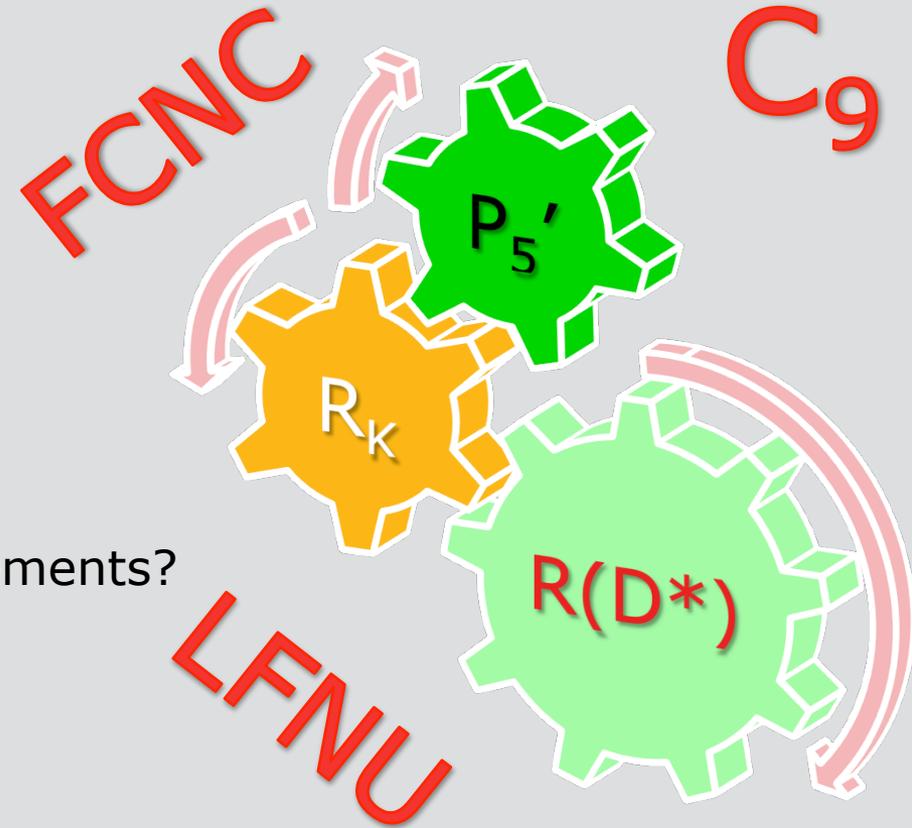


**New result**



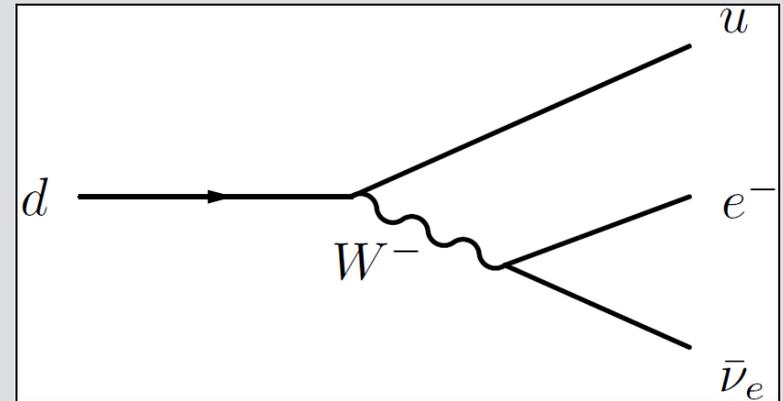
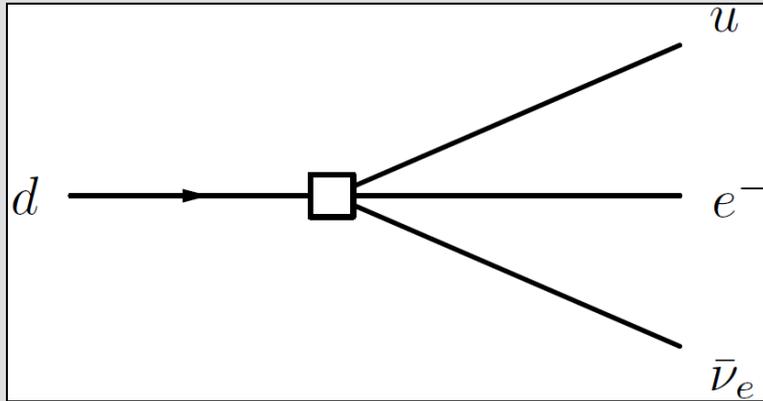
# Outline

- Indirect measurements
- What are the (anomalous) measurements?
  - FCNC:  $b \rightarrow sll$
  - LFNU:  $b \rightarrow sll$  and  $b \rightarrow clv$
- What are the interpretations?



# Effective couplings

- Historical example

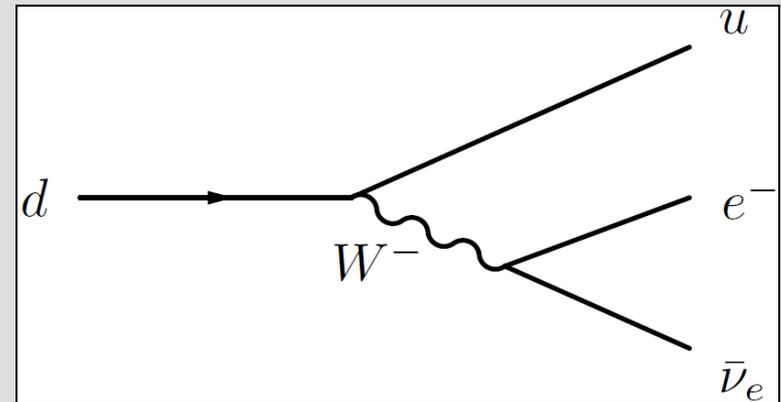
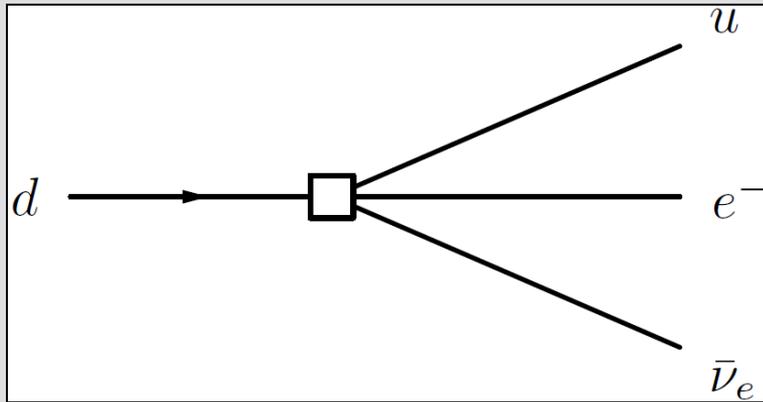


$$\frac{G_F}{\sqrt{2}} = \frac{g^2}{8M_W^2}$$

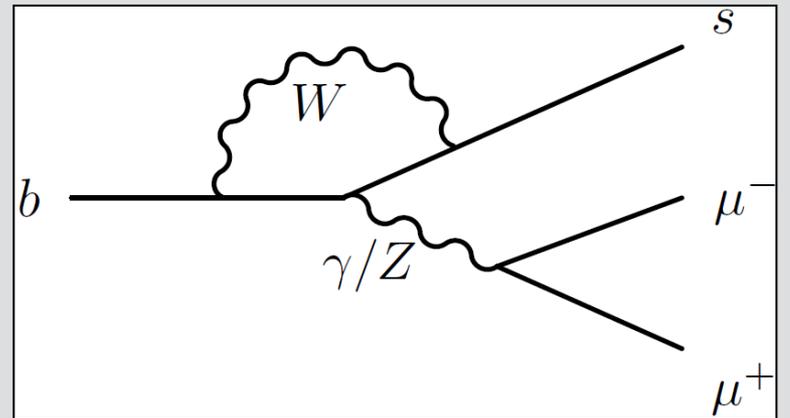
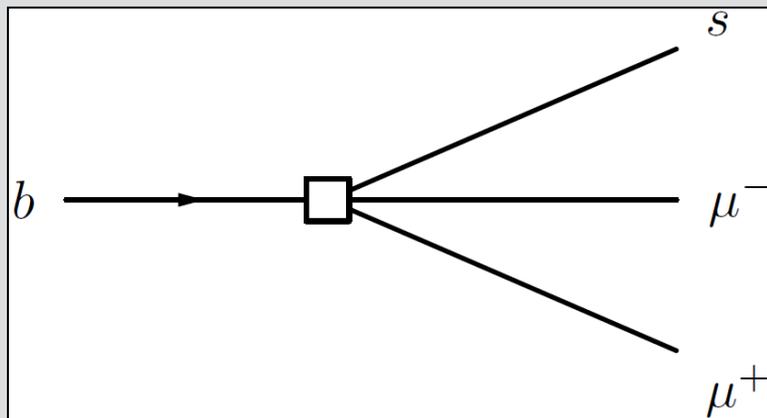
- Both are correct, depending on the energy scale you consider

# Effective couplings

- Historical example



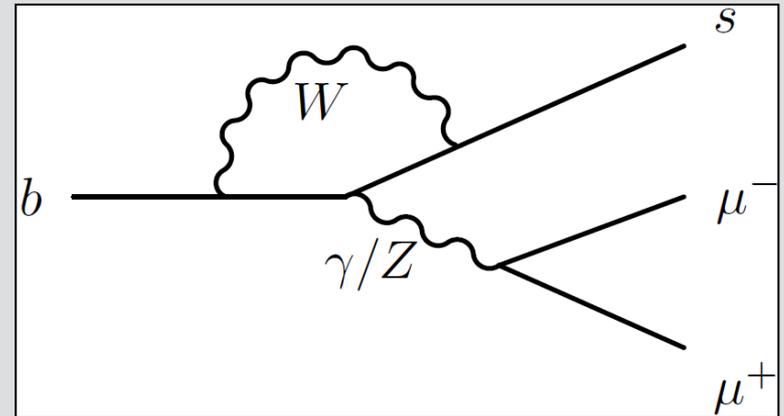
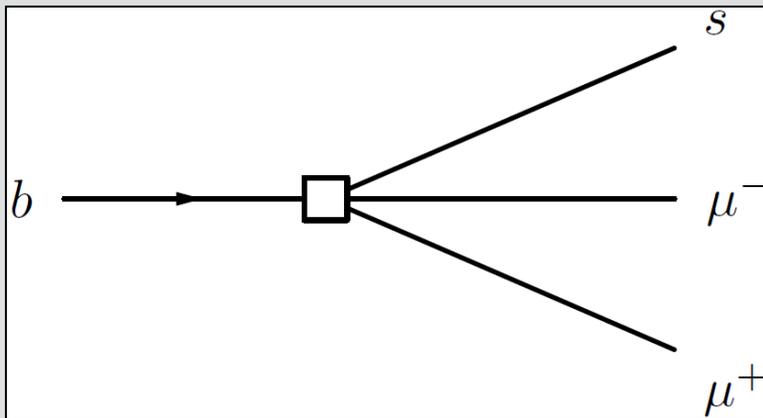
- Analog: Flavour-changing neutral current



# Effective couplings

- Effective coupling can be of various “kinds”
  - Vector coupling
  - Axial coupling
  - Left-handed coupling (V-A)
  - Right-handed (to quarks)
  - ...

$$\mathcal{H}_{\text{eff}} = \frac{G_F}{\sqrt{2}} V_{\text{CKM}} \sum_i C_i(\mu) Q_i$$



# Effective couplings

- Effective coupling can be of various “kinds”

- Vector coupling:  $C_9$
- Axial coupling:  $C_{10}$
- Left-handed coupling (V-A):  $C_9$ - $C_{10}$
- Right-handed (to quarks):  $C_9', C_{10}', \dots$
- ...

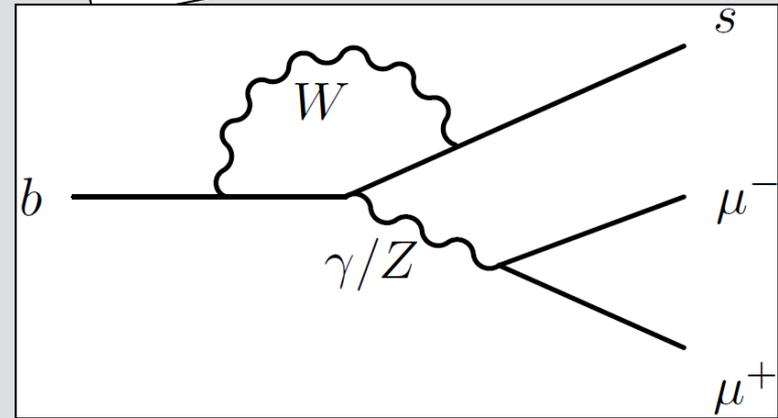
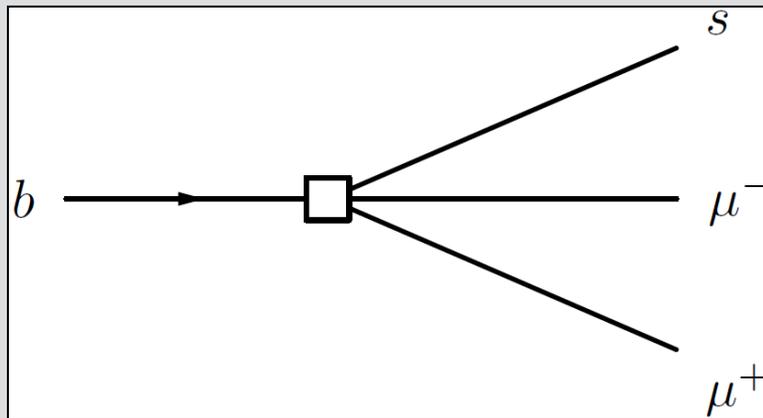
$$\mathcal{H}_{\text{eff}} = \frac{G_F}{\sqrt{2}} V_{\text{CKM}} \sum_i C_i(\mu) Q_i$$

See e.g. Buras & Fleischer, [hep-ph/9704376](https://arxiv.org/abs/hep-ph/9704376)

Semi-Leptonic Operators (fig. 11f):

$$Q_{9V} = (\bar{s}b)_{V-A}(\bar{\mu}\mu)_V$$

$$Q_{10A} = (\bar{s}b)_{V-A}(\bar{\mu}\mu)_A$$



At this stage it should be mentioned that the usual Feynman diagram drawings of the type shown in fig. 11 containing full  $W$ -propagators,  $Z^0$ -propagators and top-quark propagators represent really the happening at scales  $\mathcal{O}(M_W)$  whereas the true picture of a decaying hadron is more correctly described by the local operators in question. Thus, whereas at scales  $\mathcal{O}(M_W)$  we have to deal with the full six-quark theory containing the photon, weak gauge bosons and gluons, at scales  $\mathcal{O}(1\text{ GeV})$  the relevant effective theory contains only three light quarks  $u, d$  and  $s$ , gluons and the photon. At intermediate energy scales  $\mu = \mathcal{O}(m_b)$  and  $\mu = \mathcal{O}(m_c)$  relevant for beauty and charm decays, effective five-quark and effective four-quark theories have to be considered, respectively.

From Buras & Fleischer, [hep-ph/9704376](https://arxiv.org/abs/hep-ph/9704376)

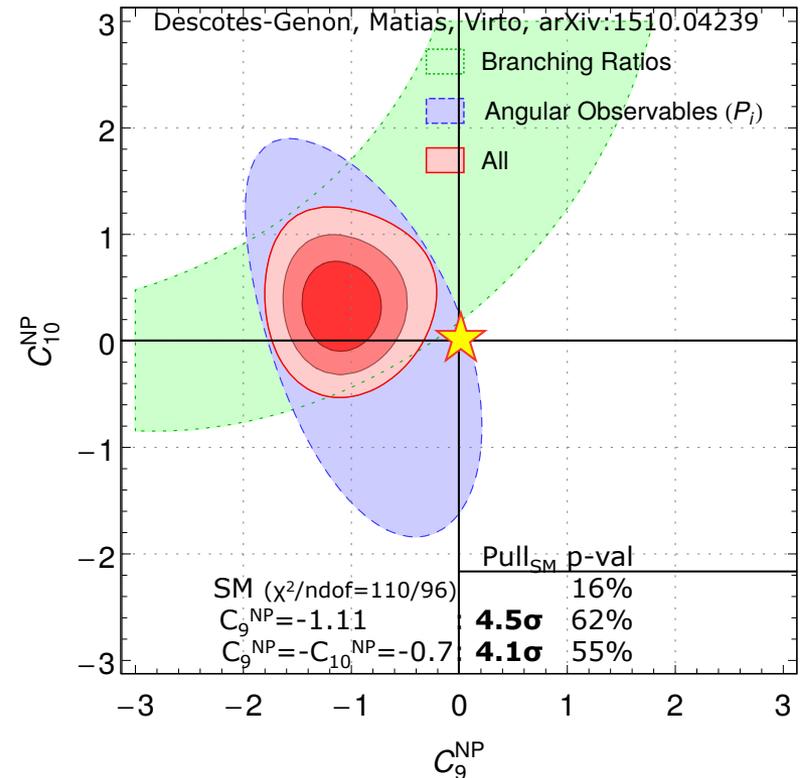
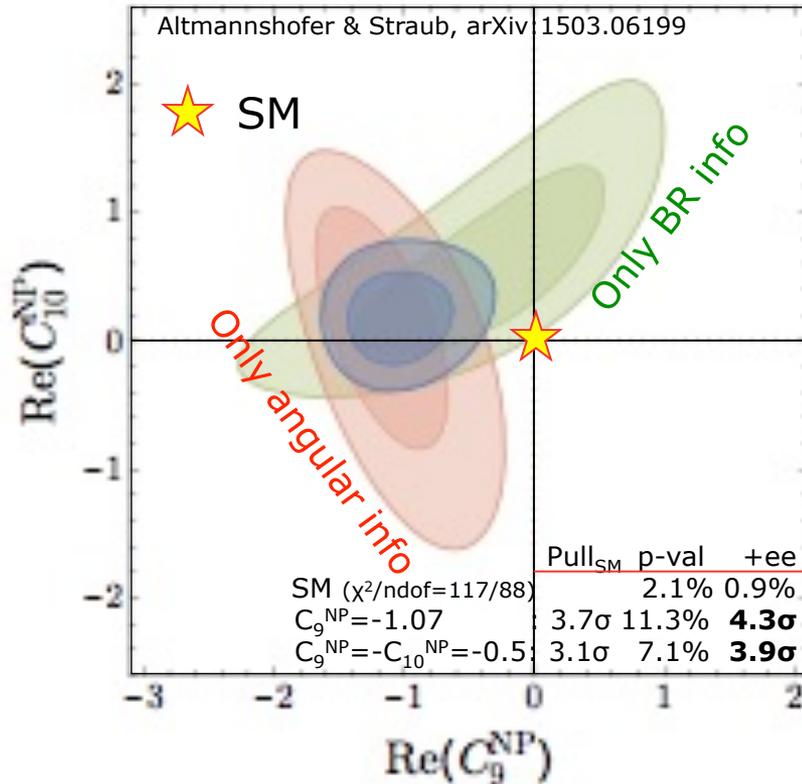
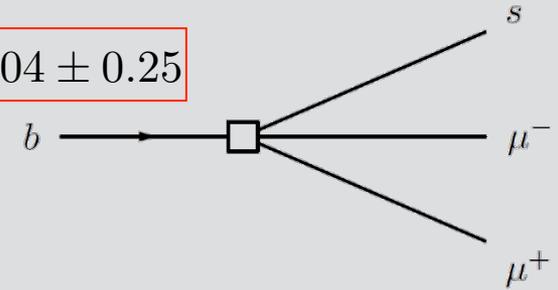
“the true picture of a decaying hadron is more correctly described by the local operators”

# Model independent fits to $b \rightarrow sll$ processes

- $C_9^{\text{NP}}$  deviates from 0 by  $>4\sigma$
- Independent fits by more groups
  - $C_9^{\text{NP}} = -1$  or
  - $C_9^{\text{NP}} = -C_{10}^{\text{NP}}$
- Caveat: debate on charm-loop effects...

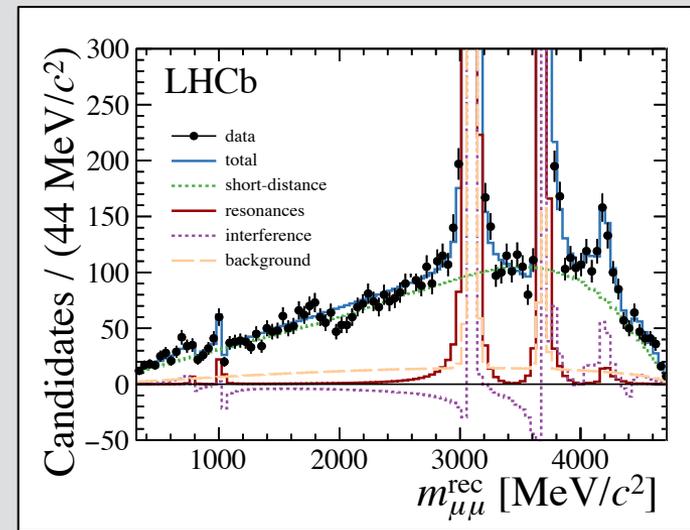
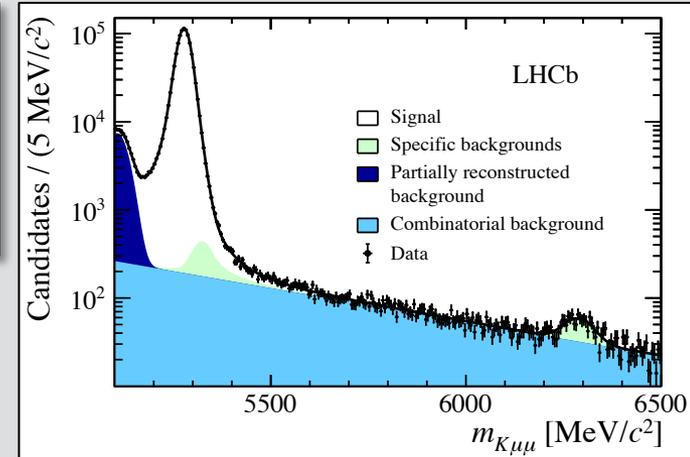
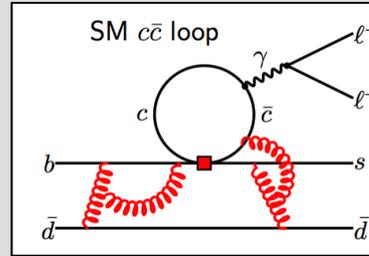
LHCb-PAPER-2015-051

$$\Delta\text{Re}(C_9) = -1.04 \pm 0.25$$



# $B^+ \rightarrow K^+ \mu^+ \mu^-$ in detail

- Contributions from  $b \rightarrow sll$ 
  - $B^+ \rightarrow K^+ \mu^+ \mu^-$
- Contributions from  $b \rightarrow scc$ 
  - e.g.  $B^+ \rightarrow K^+ \phi$ ,  $B^+ \rightarrow K^+ J/\psi$ ,  $B^+ \rightarrow K^+ \psi(2S)$ , ...
- Understand interference
  - Positive or negative?
  - More general: phase difference?
  - $\pm 90^\circ$
  - Small interference



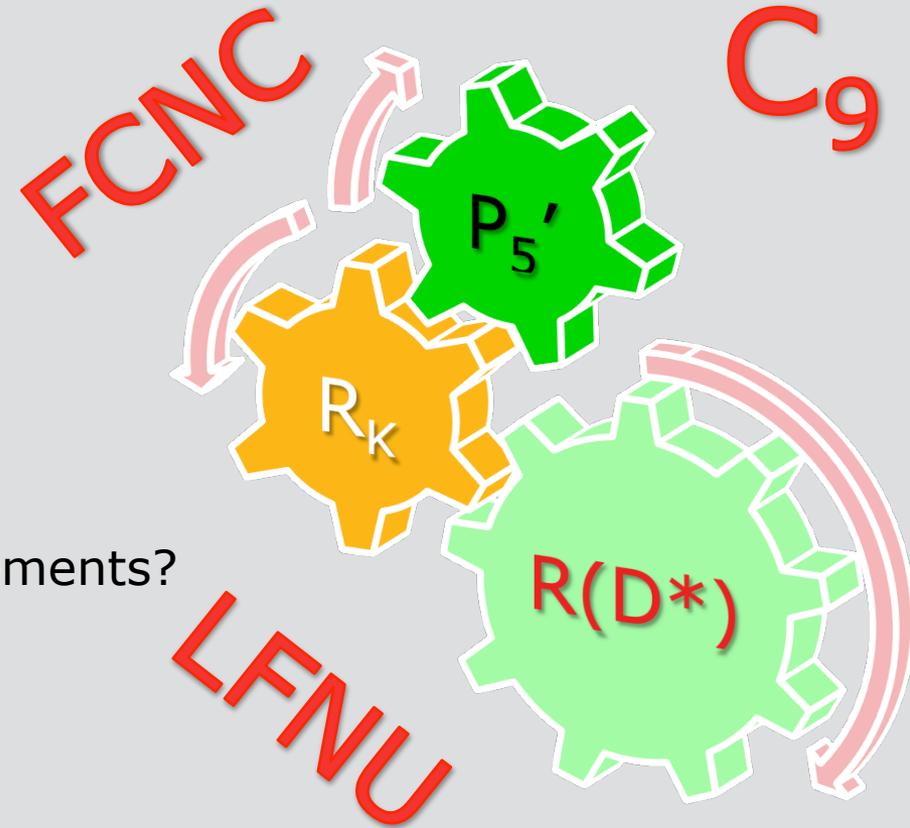
Resonance	Phase [rad]
$J/\psi$	$-1.66 \pm 0.05$
$\psi(2S)$	$-1.93 \pm 0.10$

$$\mathcal{B}(B^+ \rightarrow K^+ \mu^+ \mu^-) = (4.37 \pm 0.15 \text{ (stat)} \pm 0.23 \text{ (syst)}) \times 10^{-7}$$



# Outline

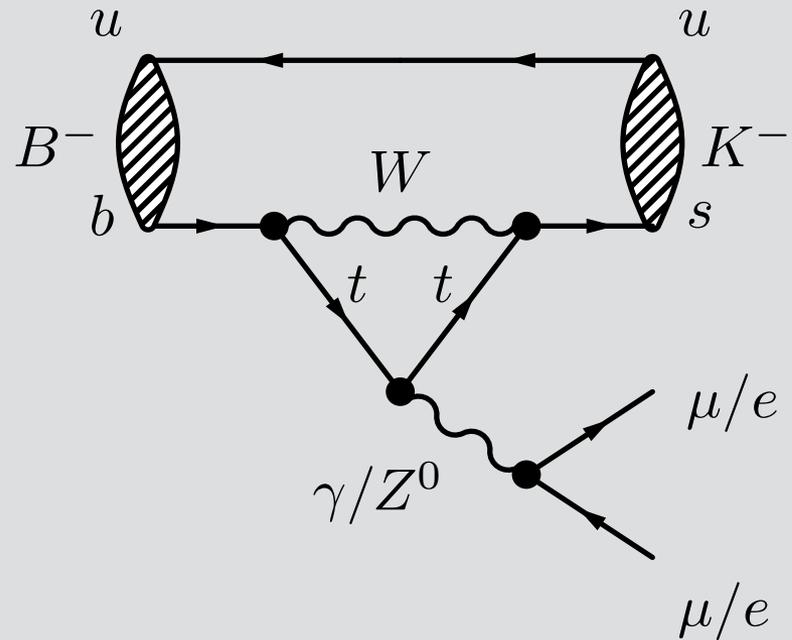
- Indirect measurements
- What are the (anomalous) measurements?
  - FCNC:  $b \rightarrow sll$
  - LFNU:  $b \rightarrow sll$  and  $b \rightarrow clv$
- What are the interpretations?



# $B \rightarrow K \mu^+ \mu^-$

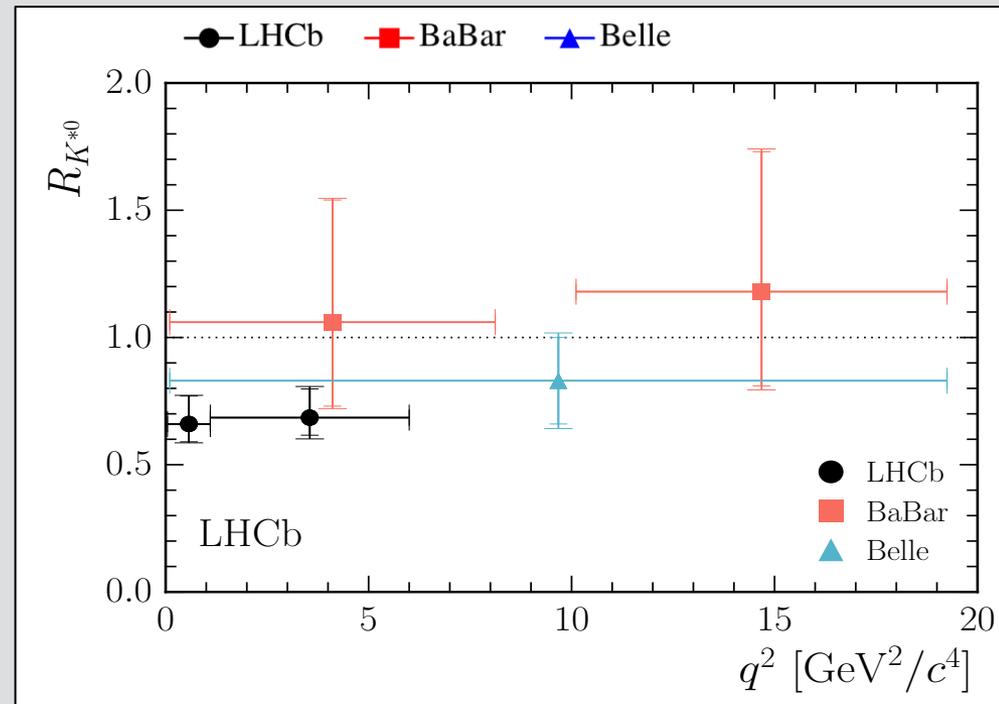
- Similar loop diagram!
- Measure ratio  $\mu/e$
- SM expectation:  $R_K=1$

$$R_K = \frac{\Gamma(B^+ \rightarrow K^+ \mu^+ \mu^-)}{\Gamma(B^+ \rightarrow K^+ e^+ e^-)}$$



# $B^0 \rightarrow K^{*0} \mu^+ \mu^-$

- Similar loop diagram!
- Measure ratio  $\mu/e$
- SM expectation:  $R_{K^*} = 1$
- Extra bin at low  $q^2$ ...
  - $q^2 \sim 0$  not helicity suppressed



LHCb Coll., JHEP 1708 (2017) 055

$$R_{K^{*0}} = \begin{cases} 0.66 \pm_{-0.07}^{+0.11} (\text{stat}) \pm 0.03 (\text{syst}) & \text{for } 0.045 < q^2 < 1.1 \text{ GeV}^2/c^4 \\ 0.69 \pm_{-0.07}^{+0.11} (\text{stat}) \pm 0.05 (\text{syst}) & \text{for } 1.1 < q^2 < 6.0 \text{ GeV}^2/c^4 \end{cases}$$

- **Lepton flavour “non-universal” ?**



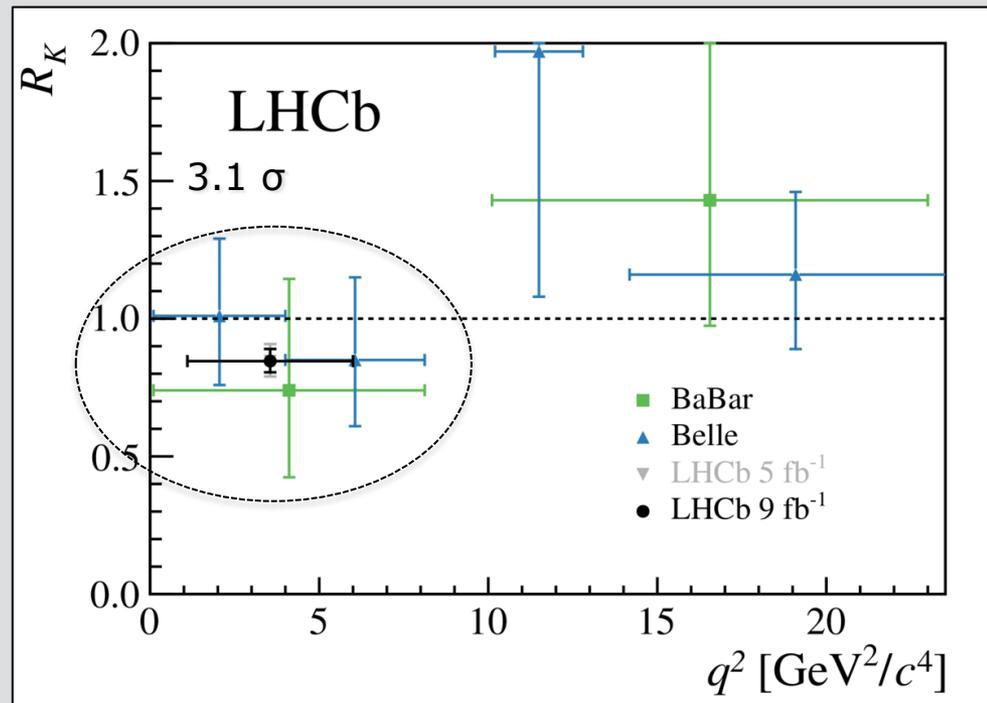
# $B^+ \rightarrow K^+ \mu^+ \mu^-$

- Similar loop diagram!
- Measure ratio  $\mu/e$
- SM expectation:  $R_K=1$

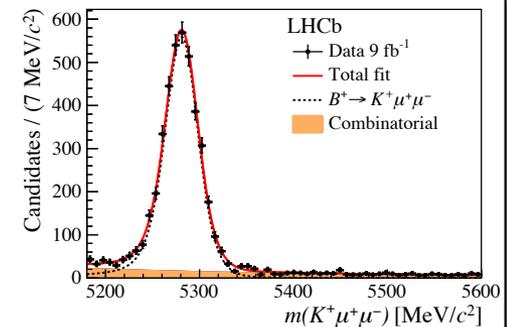
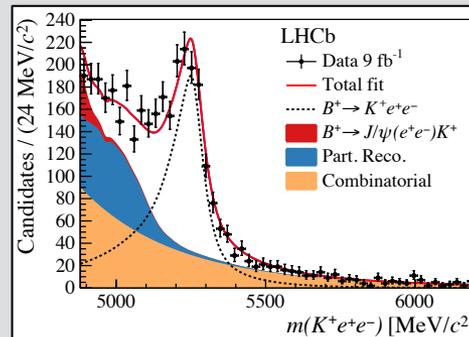
$$R_K = \frac{\Gamma(B^+ \rightarrow K^+ \mu^+ \mu^-)}{\Gamma(B^+ \rightarrow K^+ e^+ e^-)}$$

$$R_K = 0.846^{+0.044}_{-0.041}$$

➤ **Lepton flavour  
"non-universal" ?**



LHCb Coll., arXiv:2103.11769



# New result

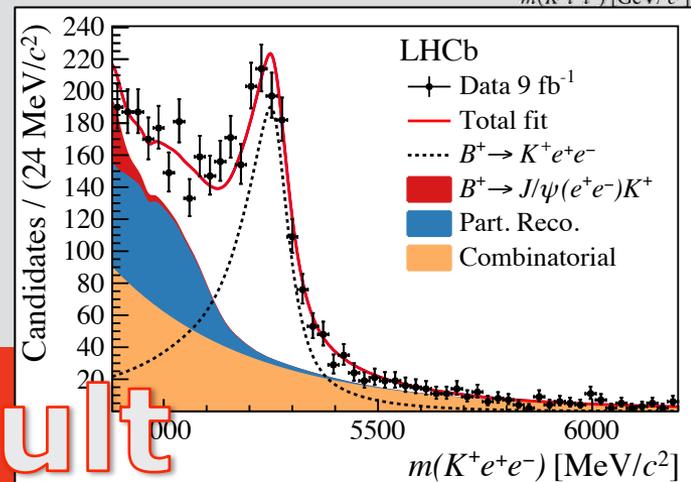
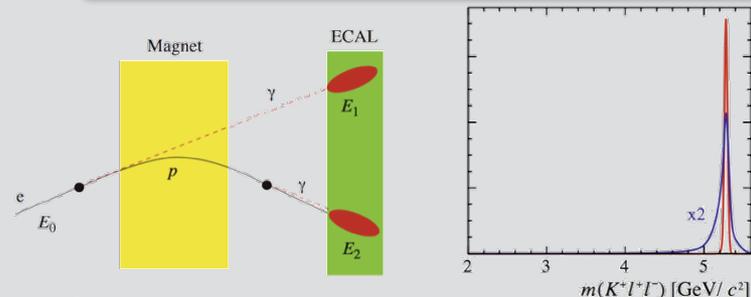
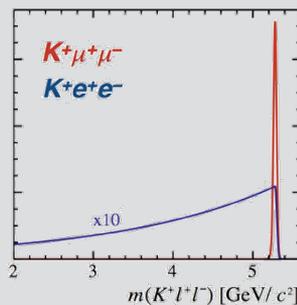
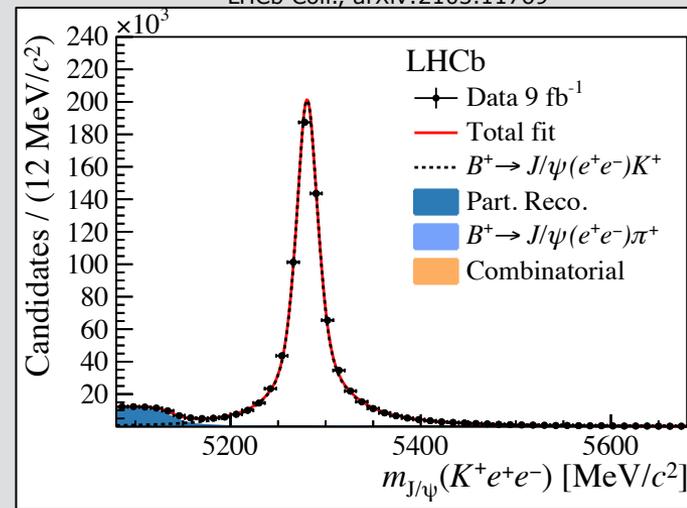
# $R_K$ - Analysis

Double ratio:

$$R_K = \frac{\mathcal{B}(B^+ \rightarrow K^+ \mu^+ \mu^-)}{\mathcal{B}(B^+ \rightarrow J/\psi(\rightarrow \mu^+ \mu^-) K^+)} \bigg/ \frac{\mathcal{B}(B^+ \rightarrow K^+ e^+ e^-)}{\mathcal{B}(B^+ \rightarrow J/\psi(\rightarrow e^+ e^-) K^+)}$$

Bremstrahlung correction

Statistically dominated by  $B^+ \rightarrow K^+ ee$



# New result

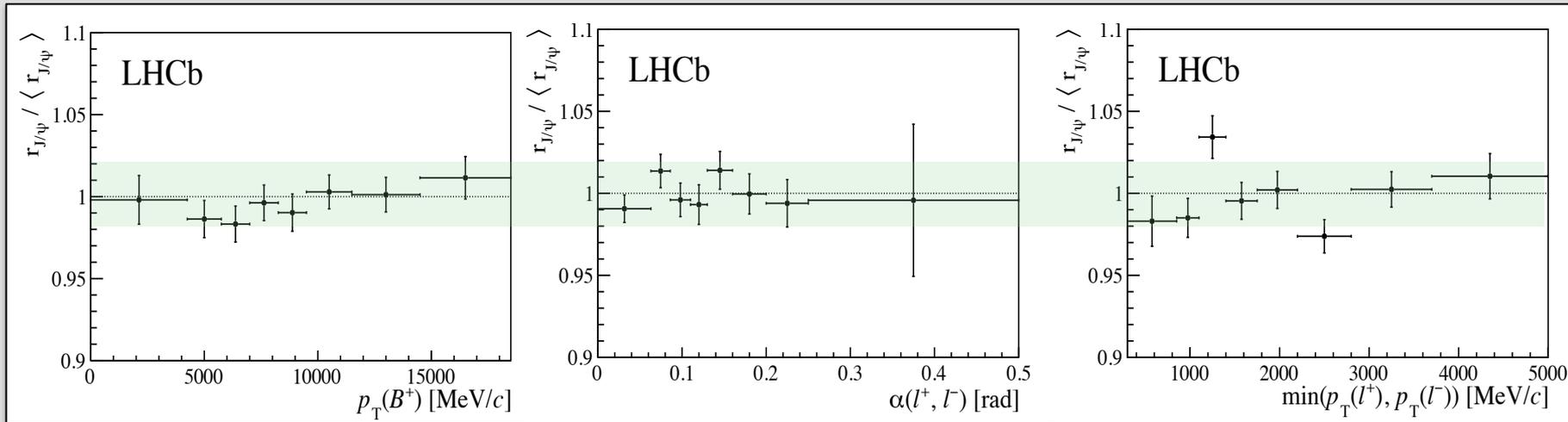
# R<sub>K</sub> - Analysis

- Event yields:

Decay mode	Yield
$B^+ \rightarrow K^+ e^+ e^-$	$1\,640 \pm 70$
$B^+ \rightarrow K^+ \mu^+ \mu^-$	$3\,850 \pm 70$
$B^+ \rightarrow J/\psi (\rightarrow e^+ e^-) K^+$	$743\,300 \pm 900$
$B^+ \rightarrow J/\psi (\rightarrow \mu^+ \mu^-) K^+$	$2\,288\,500 \pm 1\,500$

- $r_{J/\psi}$ : control across phase space!  $\langle r_{J/\psi} \rangle = 0.981 \pm 0.020$

$$r_{J/\psi} = \mathcal{B}(B^+ \rightarrow J/\psi (\rightarrow \mu^+ \mu^-) K^+) / \mathcal{B}(B^+ \rightarrow J/\psi (\rightarrow e^+ e^-) K^+)$$



- $R_{\psi(2S)}$ : 
$$R_{\psi(2S)} = \frac{\mathcal{B}(B^+ \rightarrow \psi(2S) (\rightarrow \mu^+ \mu^-) K^+)}{\mathcal{B}(B^+ \rightarrow J/\psi (\rightarrow \mu^+ \mu^-) K^+)} \bigg/ \frac{\mathcal{B}(B^+ \rightarrow \psi(2S) (\rightarrow e^+ e^-) K^+)}{\mathcal{B}(B^+ \rightarrow J/\psi (\rightarrow e^+ e^-) K^+)} = 0.997 \pm 0.011$$

# New result

# $R_{K^*}$ - Cross checks

- Check with  $J/\psi$ 
  - Unity with 4.5% at  $1\sigma$
- Check with  $\psi(2S)$ 
  - Unity within 2% at  $1\sigma$
- Check  $\text{BR}(B^0 \rightarrow K^* \gamma (\rightarrow ee))$ 
  - Agrees within 15% at  $2\sigma$

$$r_{J/\psi} = \frac{\mathcal{B}(B^0 \rightarrow K^{*0} J/\psi (\rightarrow \mu^+ \mu^-))}{\mathcal{B}(B^0 \rightarrow K^{*0} J/\psi (\rightarrow e^+ e^-))} = 1.043 \pm 0.006(\text{stat}) \pm 0.045(\text{syst})$$

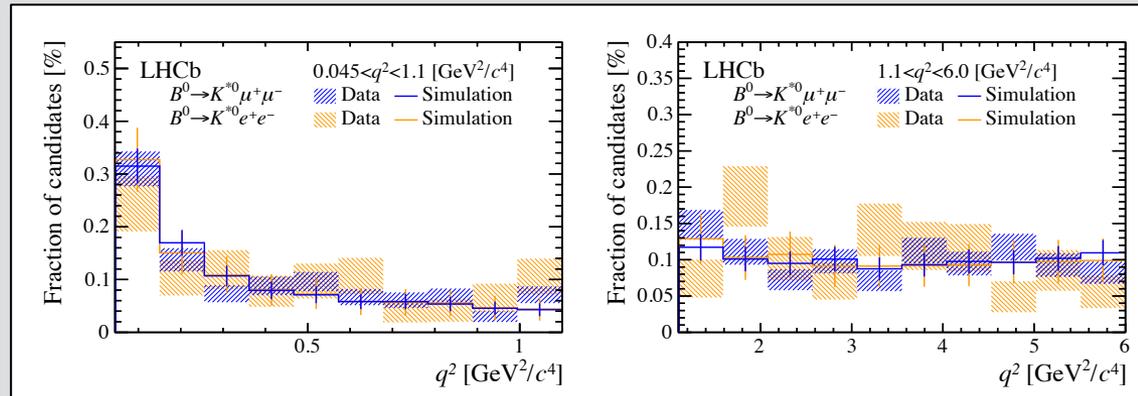
$$R_{\psi(2S)} = \frac{\mathcal{B}(B^0 \rightarrow K^{*0} \psi(2S) (\rightarrow \mu^+ \mu^-))}{\mathcal{B}(B^0 \rightarrow K^{*0} J/\psi (\rightarrow \mu^+ \mu^-))} \bigg/ \frac{\mathcal{B}(B^0 \rightarrow K^{*0} \psi(2S) (\rightarrow e^+ e^-))}{\mathcal{B}(B^0 \rightarrow K^{*0} J/\psi (\rightarrow e^+ e^-))}$$

$$r_\gamma = \frac{\mathcal{B}(B^0 \rightarrow K^{*0} \gamma)}{\mathcal{B}(B^0 \rightarrow K^{*0} J/\psi (\rightarrow e^+ e^-))}$$

- Cross checked with earlier  $d\Gamma/dq^2(B^0 \rightarrow K^* \mu\mu)$ 
  - Consistent

LHCb Coll., JHEP 1611 (2016) 47  
Erratum: JHEP 1704 (2017) 14

- Data vs simulation:

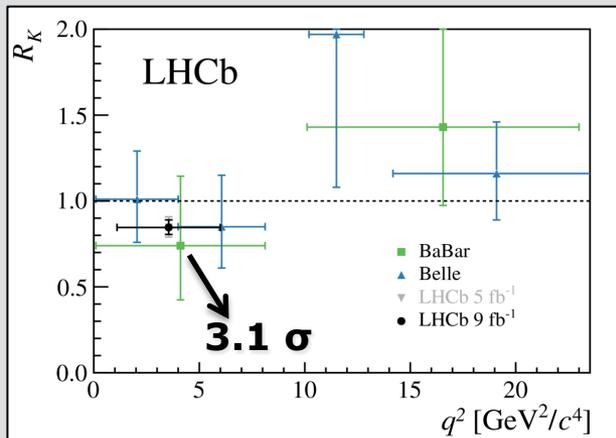
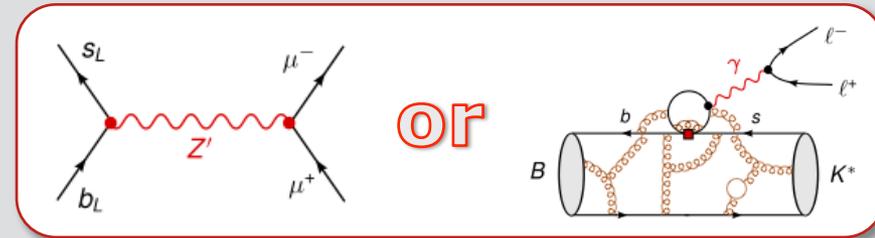
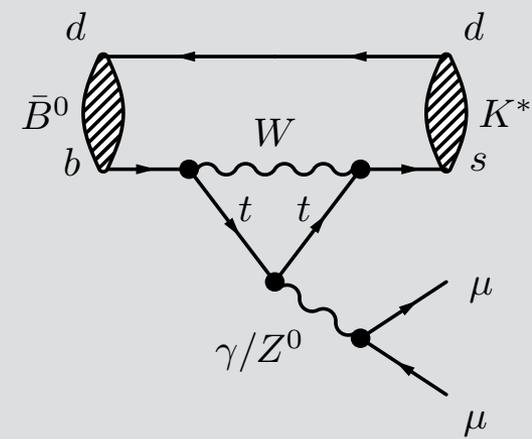


# Summary $b \rightarrow sll$

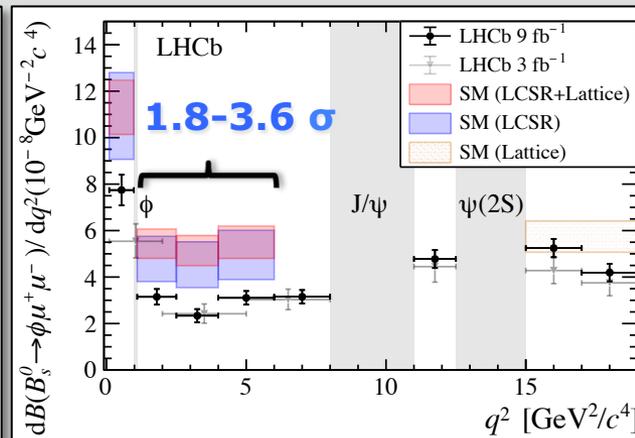
➤ FCNC: EW penguin

■ Curious tensions:

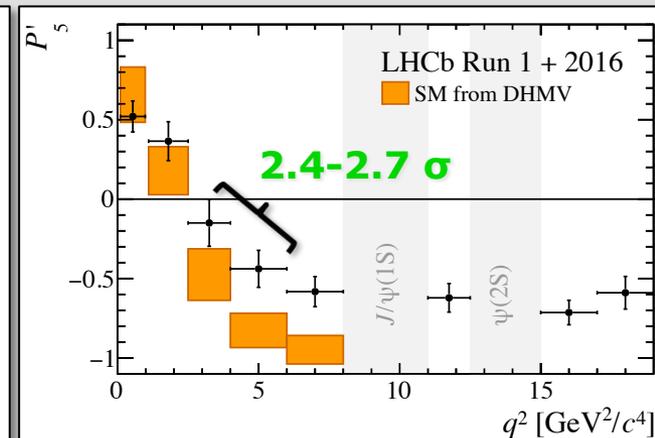
- Lepton flavour universality
- Decay rates
- Angular distributions,  $P_5'$



LHCb, PAPER-2021-004



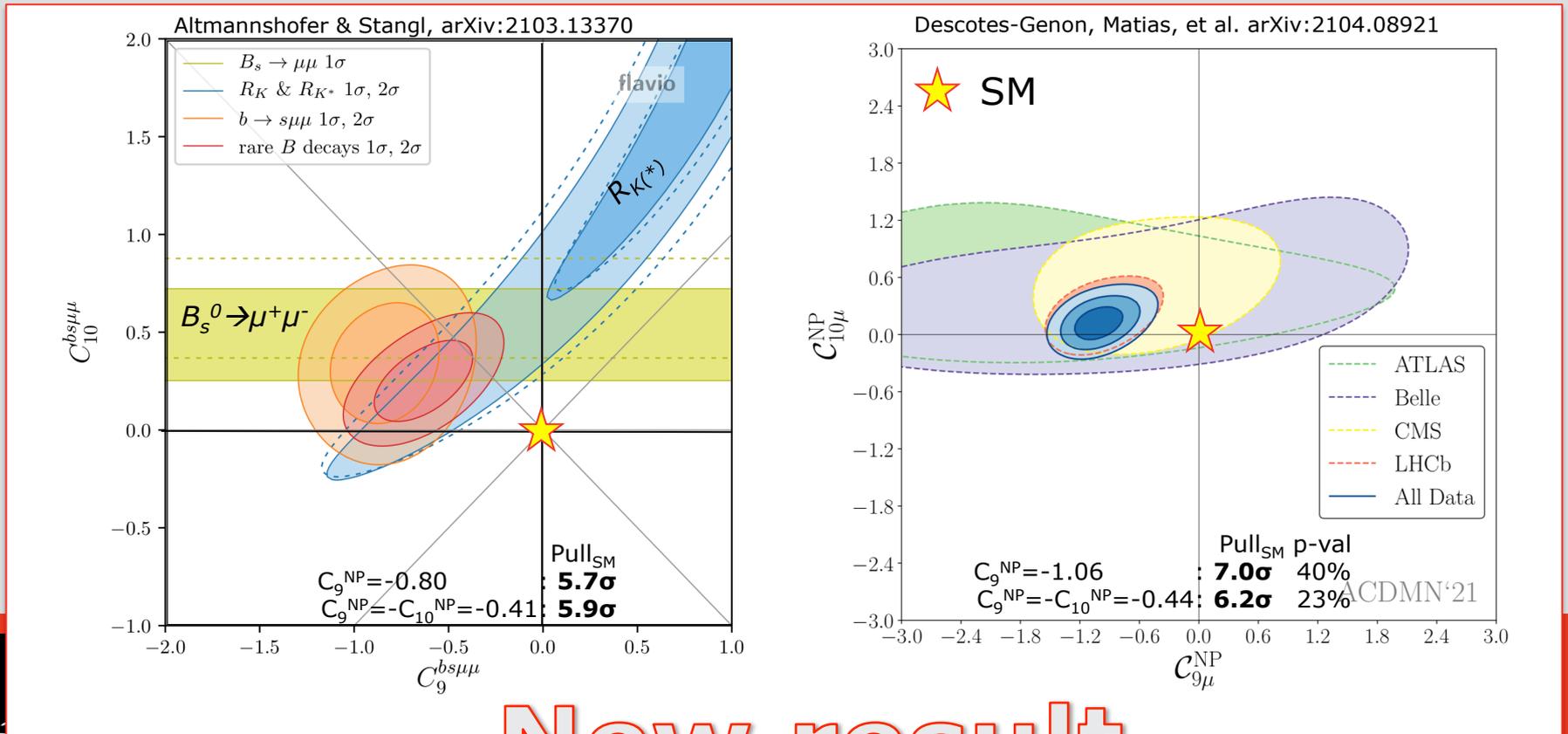
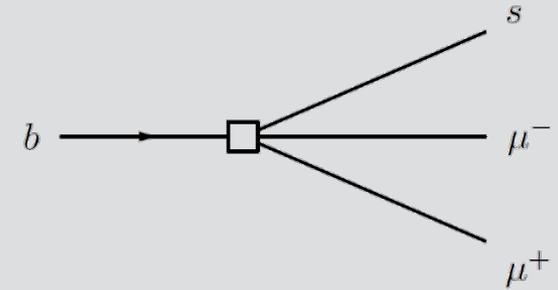
LHCb, PAPER-2021-014



LHCb, arXiv:2003.04831

# Model independent fits to $b \rightarrow sll$ processes

- $C_9^{\text{NP}}$  deviates from 0 by  $>4\sigma$
- Independent fits by more groups
  - 1D:  $C_9^{\text{NP}} = -1$  or  $C_9^{\text{NP}} = -C_{10}^{\text{NP}}$  ??
  - NB: Many possibilities (2D, RH, ...) !
- **Caveat: debate on charm-loop effects...**



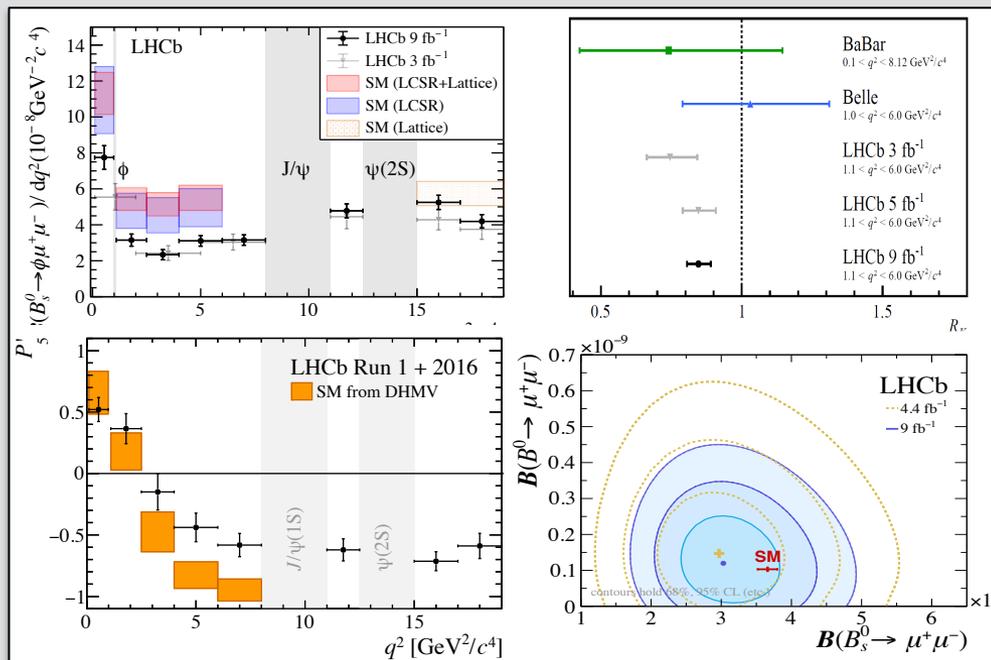
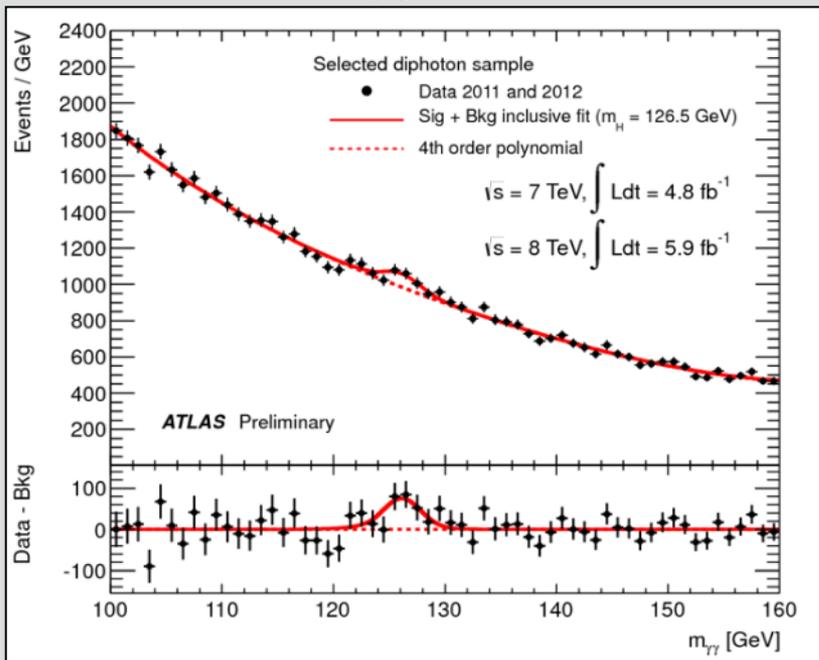
# New result

# Quantifying significance ?

Higgs

vs

$b \rightarrow s l^+ l^-$



$\chi^2$  of null hypothesis?

Good

Good

$\Delta\chi^2$  wrt discovery hypothesis (*coherent pattern*) ?

Favour Gauss

Favour  $(C_9, C_{10})^{\text{NP}}$

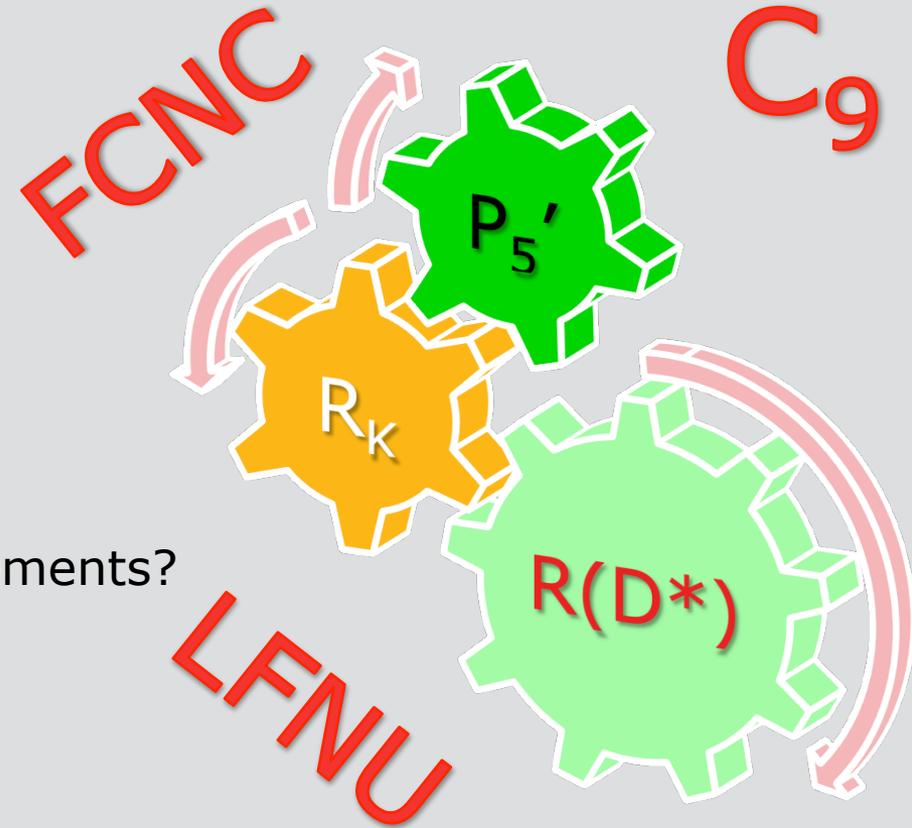
Look-elsewhere effect (*eg. arXiv:2104.05631*) ?

1-dim Mass range

n-dim Wilson space

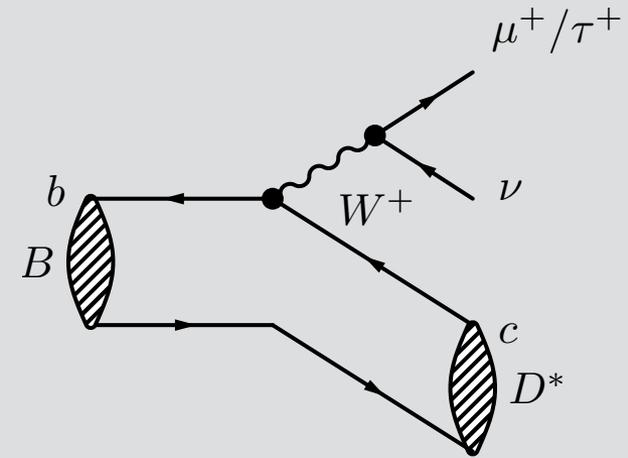
# Outline

- Indirect measurements
- What are the (anomalous) measurements?
  - FCNC:  $b \rightarrow sll$
  - LFNU:  $b \rightarrow sll$  and  $b \rightarrow clv$
- What are the interpretations?



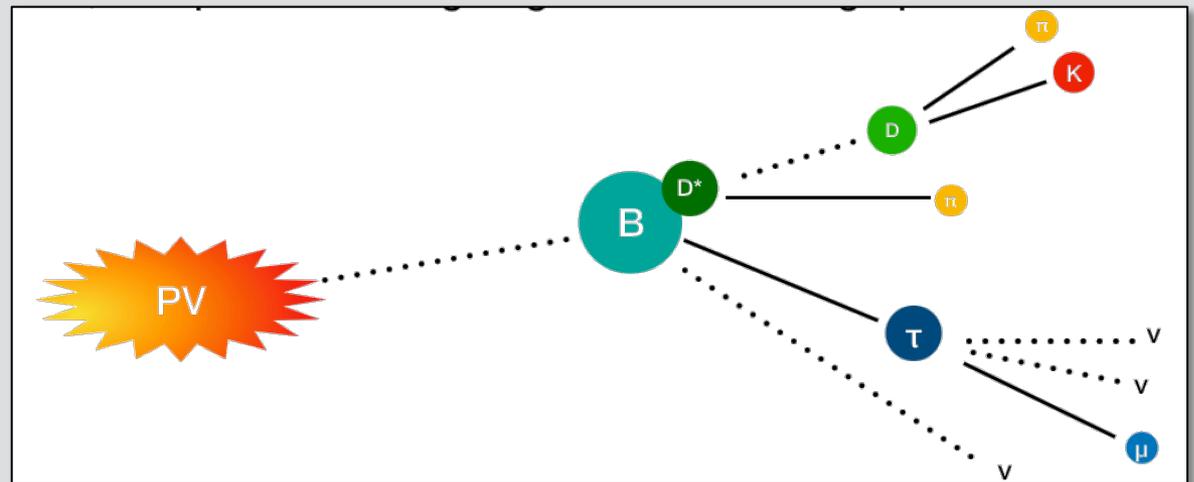
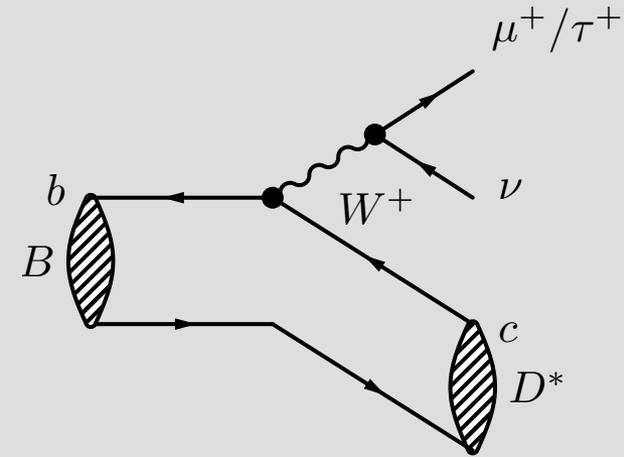
# More LFNU ?!

- Surprises possible in tree-level decays?



# More LFNU: $b \rightarrow cl\nu$

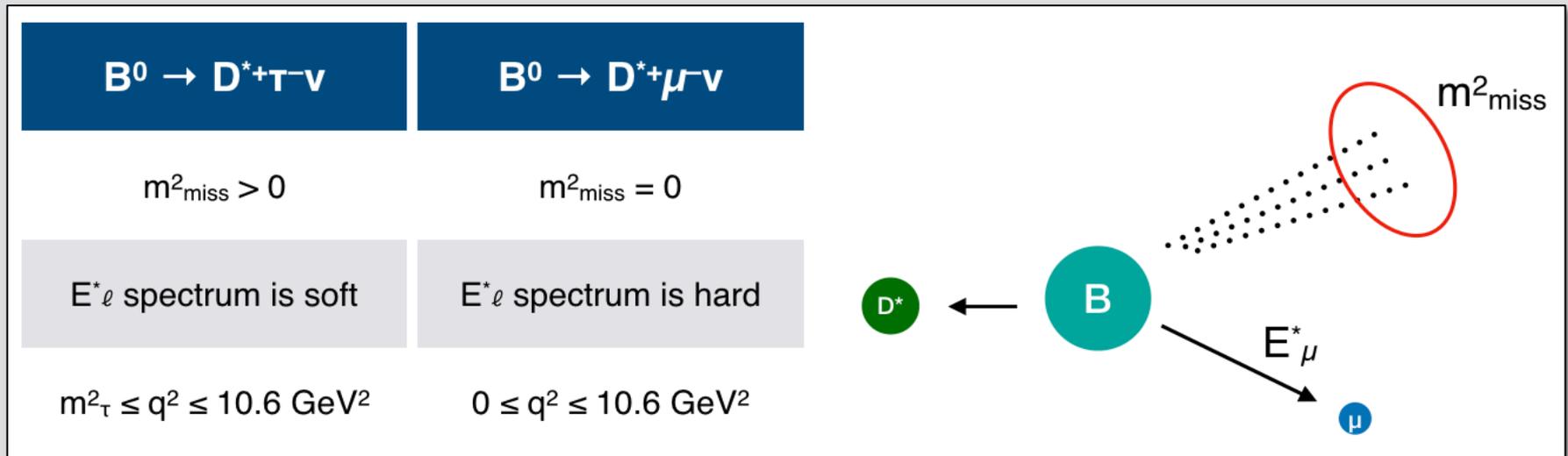
- Surprises possible in tree-level decays?
- Challenging analysis:
  - Missing neutrino
  - Background from  $B \rightarrow D^{**}\mu$
- Compare  $B \rightarrow D^*\mu\nu$  with  $B \rightarrow D^*\tau(\rightarrow\mu\nu\nu)\nu$  : similar final state!



# Semileptonic $B \rightarrow D^* \nu \mu(\tau)$ decays: $b \rightarrow c l \nu$

## Discriminating variables:

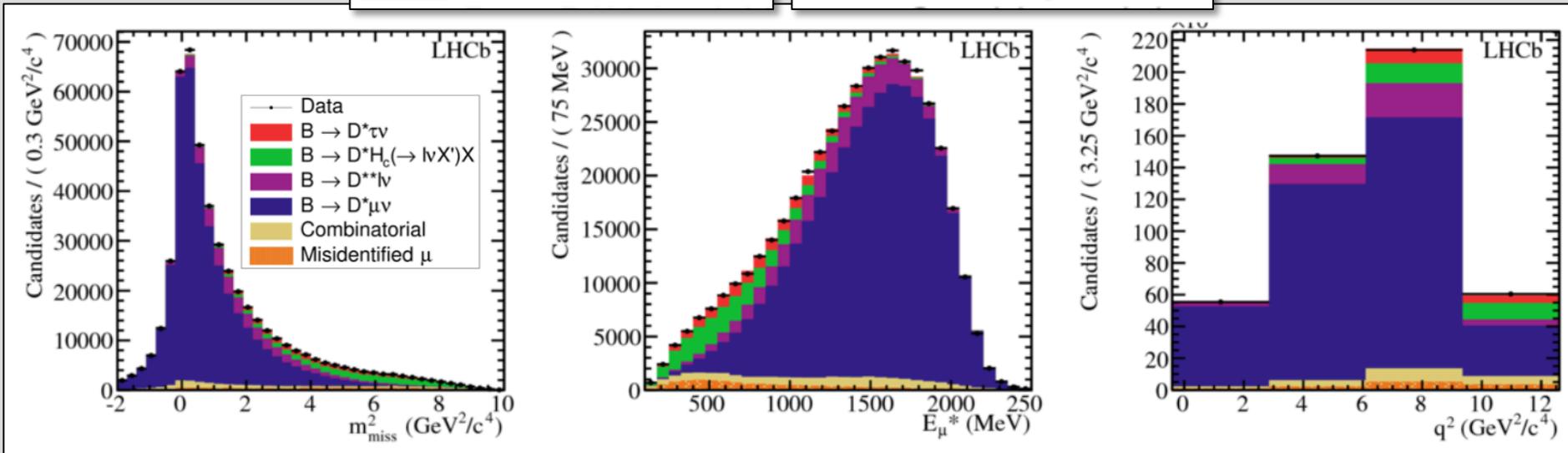
- $m^2_{\text{miss}}$ : Missing mass (neutrino + ?)
- $E^*_\mu$ : Energy of muon in  $B$  rest frame
- $q^2$ : Invariant mass of lepton-pair



# Semileptonic $B \rightarrow D^* \nu \mu(\tau)$ decays: $b \rightarrow c l \nu$

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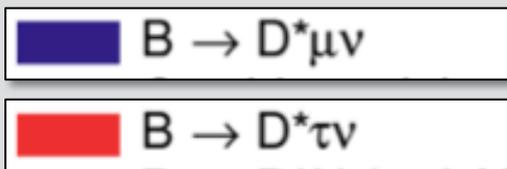


LHCb Coll., Phys. Rev. Lett. 115 (2015) 159901

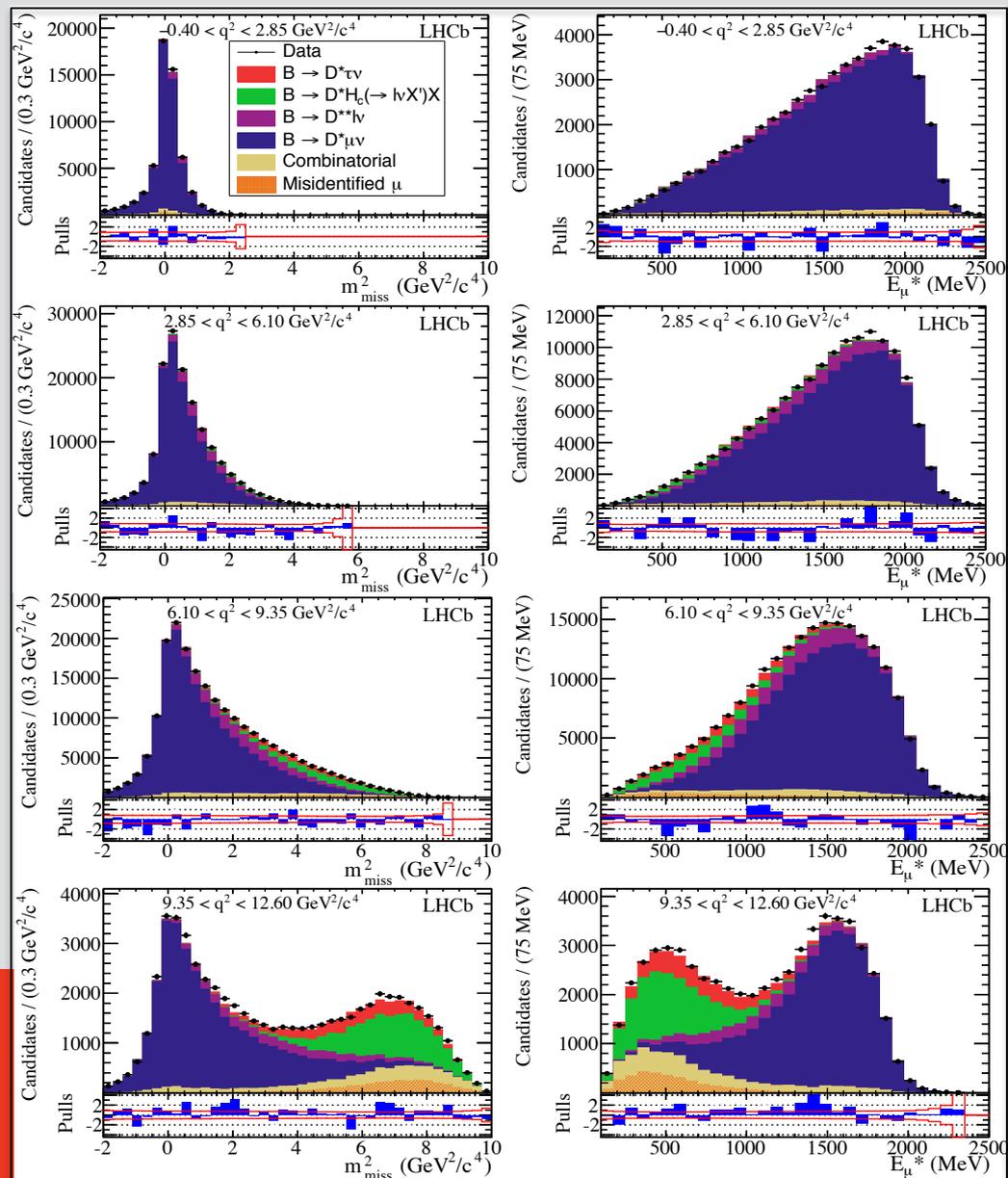
# Semileptonic $B \rightarrow D^* \nu \mu(\tau)$ decays: $b \rightarrow cl\nu$

Discriminating variables:

- $m_{\text{miss}}^2$
- $E_{\mu}^*$
- in bins of  $q^2$ :



$q^2$



LHCb Coll., PRL115 (2015) 111803



# Semileptonic $B \rightarrow D^* \nu \mu(\tau)$ decays: $b \rightarrow c l \nu$

- Surprises possible in tree-level decays?

$$\mathcal{R}(D^*) \equiv \mathcal{B}(\bar{B}^0 \rightarrow D^{*+} \tau^- \bar{\nu}_\tau) / \mathcal{B}(\bar{B}^0 \rightarrow D^{*+} \mu^- \bar{\nu}_\mu)$$

- $B^0 \rightarrow D^* l \nu$

- Measured ratio  $\tau/\mu$  :

$$\mathcal{R}(D^*) = 0.336 \pm 0.027 \text{ (stat)} \pm 0.030 \text{ (syst)}$$

- SM:  $R(D^*) = 0.252 \pm 0.003$

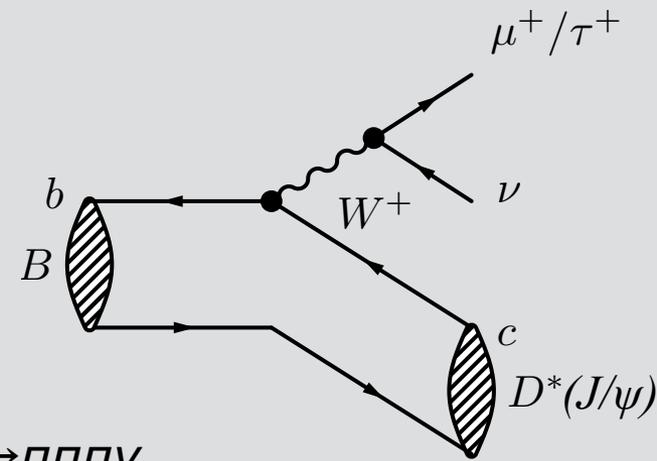
- Different from unity due to smaller phase space for tau decays

Fajfer, Kamenik, Nisandzic PRD 85, 094025 (2012)



# More measurements!

- $R(D^*)$  from Babar and Belle
- $R(D)$  from Babar and Belle
- $R(D^*)$  from LHCb with hadronic tau decays,  $\tau \rightarrow \pi\pi\pi\nu$



$$\mathcal{B}(B^0 \rightarrow D^{*-}\tau^+\nu_\tau) / \mathcal{B}(B^0 \rightarrow D^{*-}\pi^+\pi^-\pi^+) = 1.93 \pm 0.13 \pm 0.18$$

$$\mathcal{R}(D^{*-}) = 0.286 \pm 0.019 \pm 0.025 \pm 0.021$$

$$\mathcal{B}(B^0 \rightarrow D^{*-}3\pi) = (7.23 \pm 0.51) \times 10^{-3}$$

$$\mathcal{B}(B^0 \rightarrow D^{*-}\mu^+\nu_\mu) = (4.88 \pm 0.10) \times 10^{-2}$$

- $R(J/\psi)$  from LHCb ( $< 2\sigma$ )

$$\mathcal{R}(J/\psi) = \frac{\mathcal{B}(B_c^+ \rightarrow J/\psi\tau^+\nu_\tau)}{\mathcal{B}(B_c^+ \rightarrow J/\psi\mu^+\nu_\mu)}$$

$$\mathcal{R}(J/\psi) = 0.71 \pm 0.17 \text{ (stat)} \pm 0.18 \text{ (syst)}$$

LHCb Coll. arXiv:1711.02505

LHCb Coll. arXiv:1711.05623

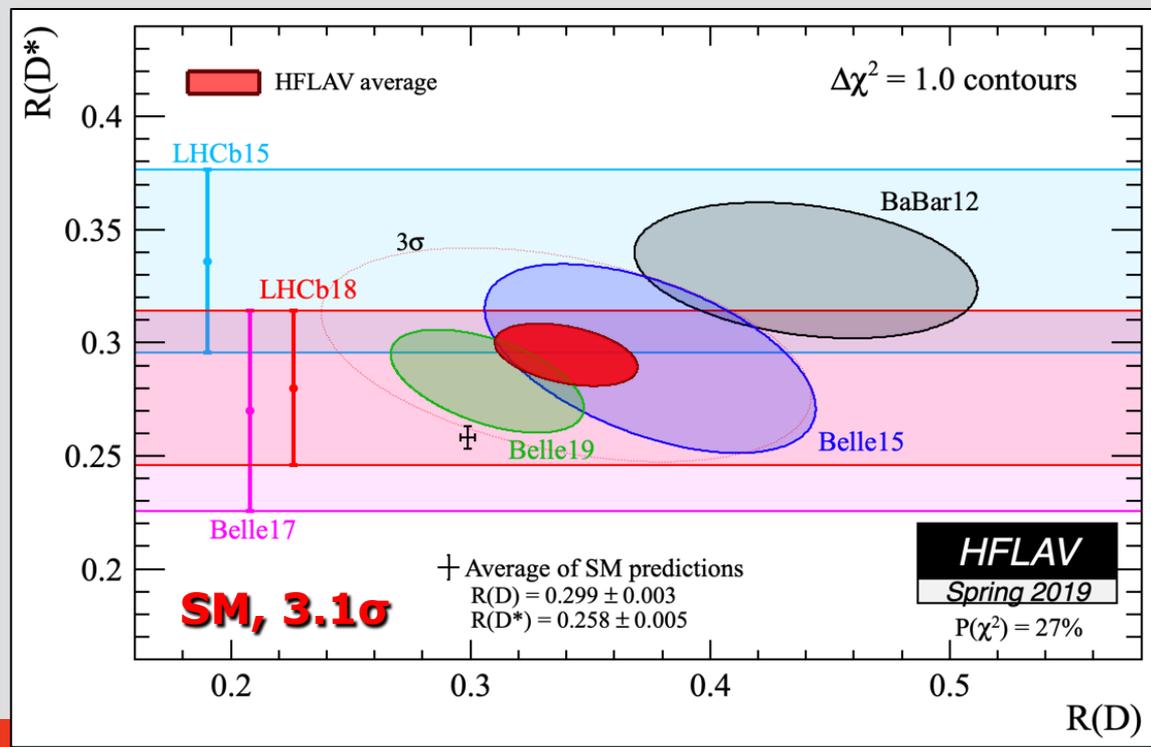
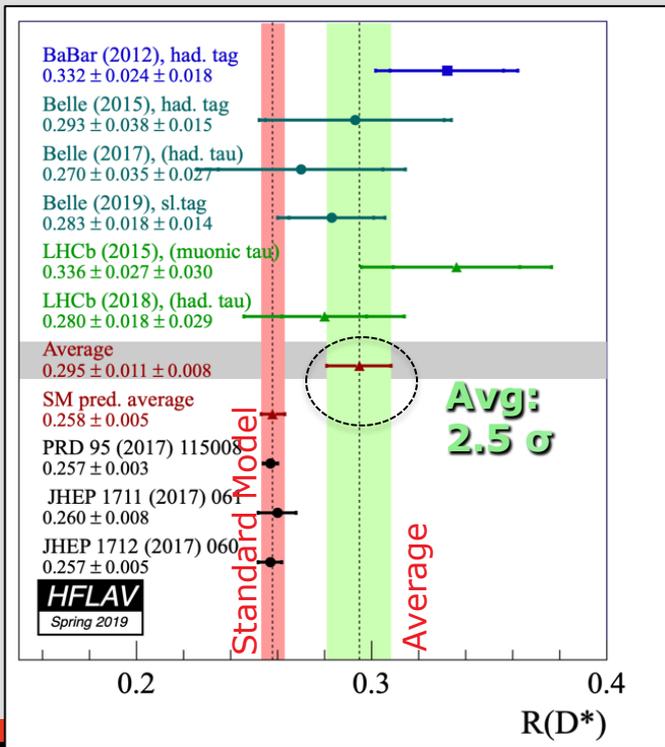
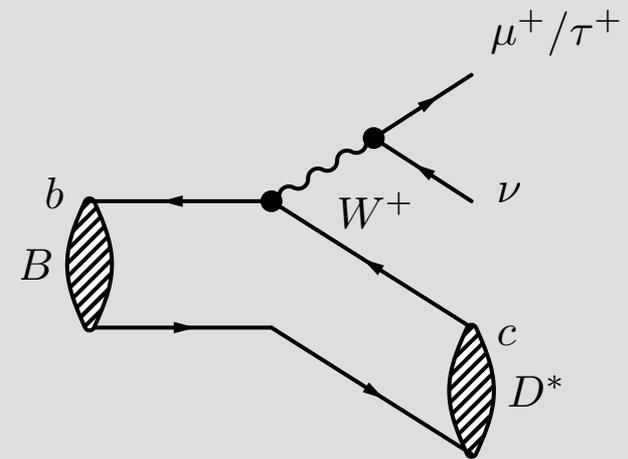
- $R(\Lambda_c)$ ,  $R(D)$ ,  $R(D_s)$  being analyzed
- Run-2 data on the shelves!

# More LFNU

- Surprises possible in tree-level decays

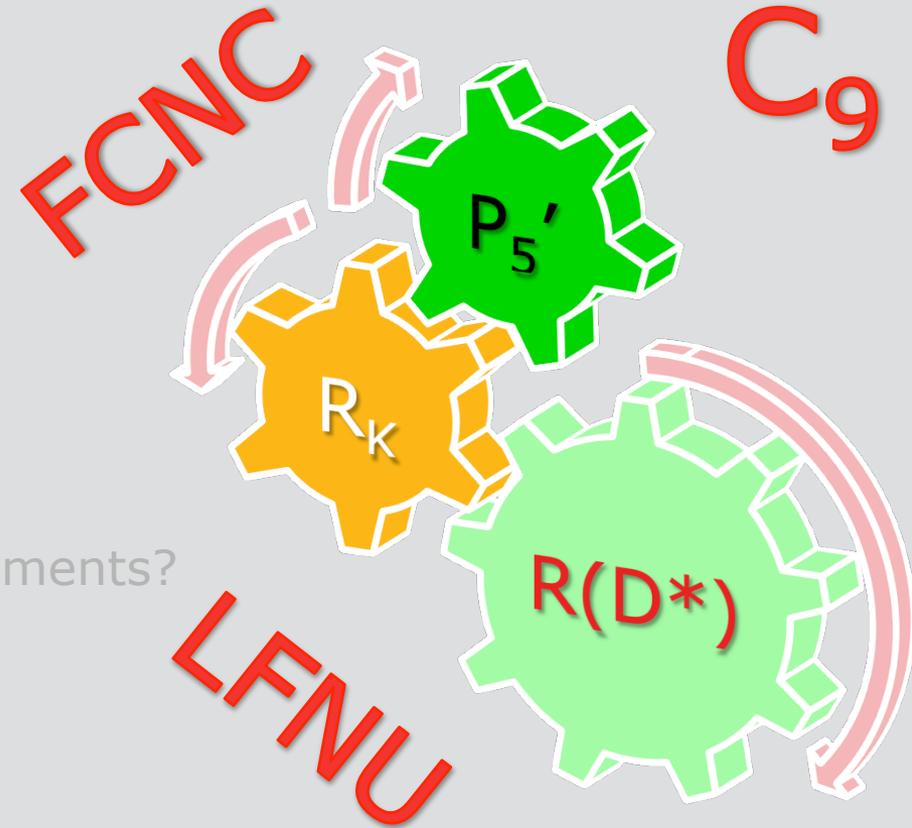
- $B \rightarrow D^{(*)} l \nu$

-  $R(D)$  and  $R(D^*)$  combined:  $3.1 \sigma$



# Outline

- Indirect measurements
- What are the (anomalous) measurements?
  - FCNC:  $b \rightarrow sll$
  - LFNU:  $b \rightarrow sll$  and  $b \rightarrow clv$
- What are the interpretations?



# What NP could it be?

- If interpreted as NP signals, both set of anomalies are not in contradiction among themselves & with existing low- & high-energy data.  
Taken together, they point out to NP coupled mainly to 3<sup>rd</sup> generation, with a flavor structure connected to that appearing in the SM Yukawa couplings

G. Isidori, *Implications workshop*, CERN, 10 Nov 2017  
<https://indico.cern.ch/event/646856/timetable/>

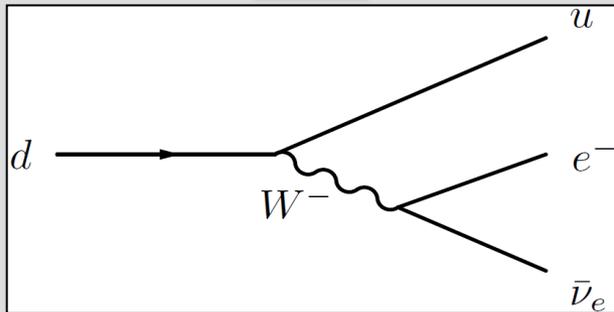
- Indirect measurements
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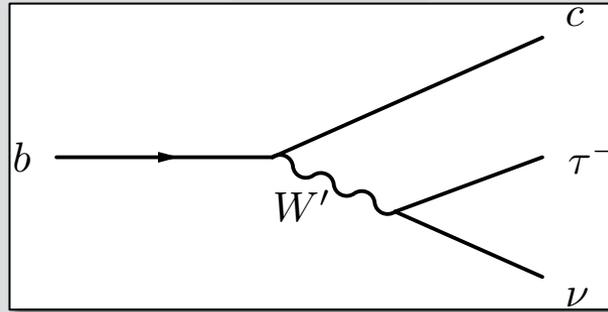
# Model building

- Most popular models:  $Z'$  or Leptoquark

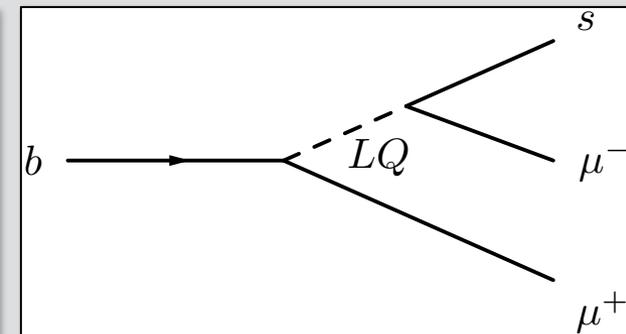
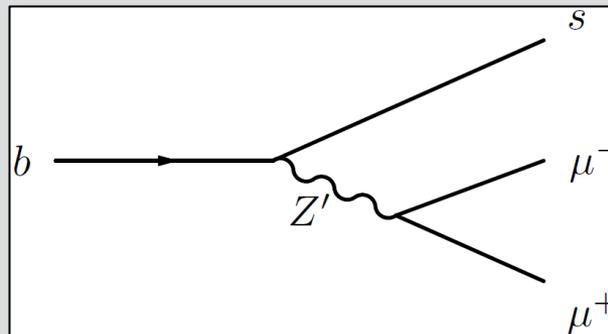
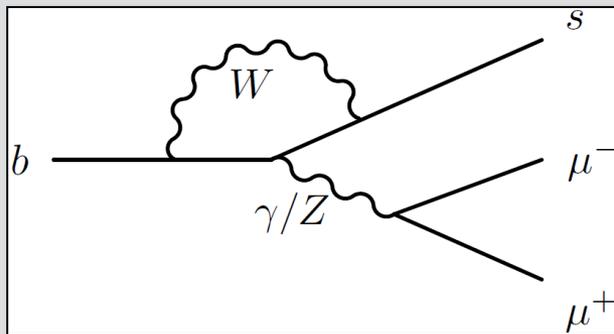
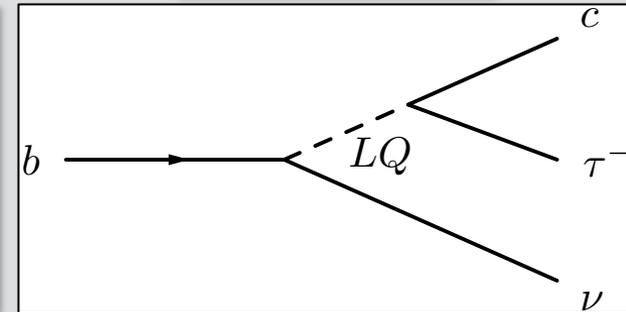
SM



$SU(2)'$

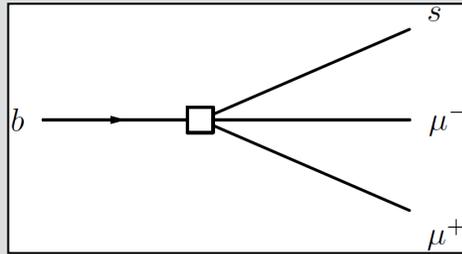


Leptoquark



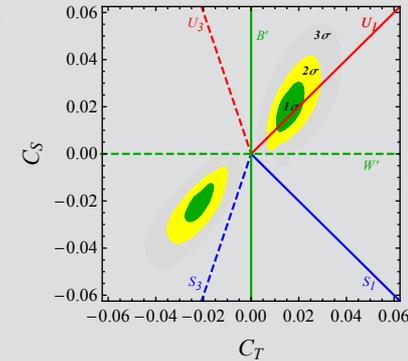
# Model building

## Step 1: Effective theory

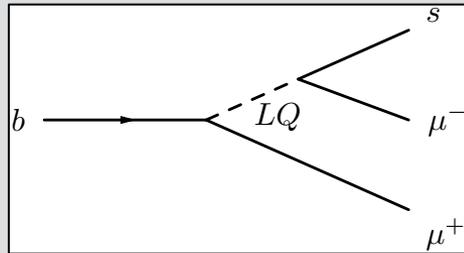


$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{SM}} - \frac{1}{v^2} \lambda_{ij}^q \lambda_{\alpha\beta}^\ell \left[ C_T (\bar{Q}_L^i \gamma_\mu \sigma^a Q_L^j) (\bar{L}_L^\alpha \gamma^\mu \sigma^a L_L^\beta) + C_S (\bar{Q}_L^i \gamma_\mu Q_L^j) (\bar{L}_L^\alpha \gamma^\mu L_L^\beta) \right]$$

Observable	Experimental bound	Linearised expression
$R_{D^{(*)}}^\ell$	$1.237 \pm 0.053$	$1 + 2C_T(1 - \lambda_{sb}^q V_{tb}^*/V_{ts}^*)(1 - \lambda_{\mu\mu}^\ell/2)$
$\Delta C_9^\mu = -\Delta C_{10}^\mu$	$-0.61 \pm 0.12$ [36]	$-\frac{\pi}{\alpha_{\text{em}} V_{tb} V_{ts}^*} \lambda_{\mu\mu}^\ell \lambda_{sb}^q (C_T + C_S)$
$R_{b \rightarrow c}^{\mu e} - 1$	$0.00 \pm 0.02$	$2C_T(1 - \lambda_{sb}^q V_{tb}^*/V_{ts}^*) \lambda_{\mu\mu}^\ell$
$B_{K^{(*)} \nu \bar{\nu}}$	$0.0 \pm 2.6$	$1 + \frac{2}{3} \frac{\pi}{\alpha_{\text{em}} V_{tb} V_{ts}^*} C_S^{\text{SM}} (C_T - C_S) \lambda_{sb}^q (1 + \lambda_{\mu\mu}^\ell)$
$\delta g_{\tau L}^Z$	$-0.0002 \pm 0.0006$	$0.033C_T - 0.043C_S$
$\delta g_{\nu\tau}^Z$	$-0.0040 \pm 0.0021$	$-0.033C_T - 0.043C_S$
$ g_\tau^W/g_\ell^W $	$1.00097 \pm 0.00098$	$1 - 0.084C_T$
$\mathcal{B}(\tau \rightarrow 3\mu)$	$(0.0 \pm 0.6) \times 10^{-8}$	$2.5 \times 10^{-4} (C_S - C_T)^2 (\lambda_{\tau\mu}^\ell)^2$



## Step 2: Simplified models



$SU(2)_L$ -singlet vector leptoquark,  $U_1^\mu \equiv (\mathbf{3}, \mathbf{1}, 2/3)$

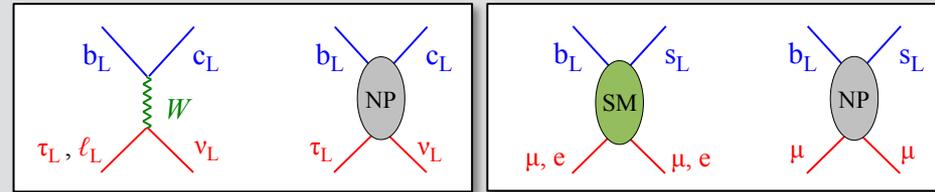
$$\mathcal{L}_U = -\frac{1}{2} U_{1,\mu\nu}^\dagger U^{1,\mu\nu} + M_U^2 U_{1,\mu}^\dagger U_1^\mu + g_U (J_U^\mu U_{1,\mu} + \text{h.c.})$$

$$J_U^\mu \equiv \beta_{i\alpha} \bar{Q}_i \gamma^\mu L_\alpha .$$

# Model building

## Ingredients

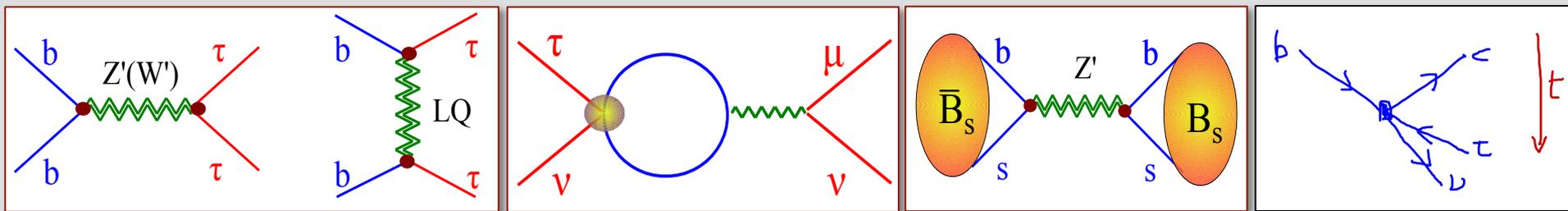
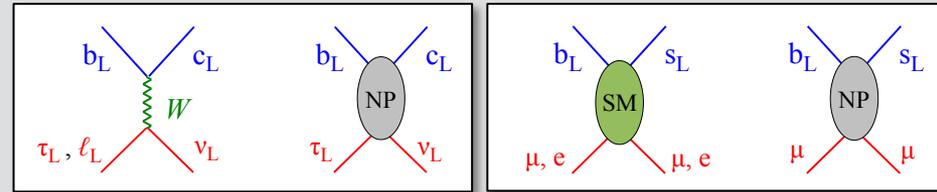
- NP: large coupling  $b \rightarrow c \tau \nu$ 
  - Large coupling to 3<sup>rd</sup> gen leptons
  - Left-handed coupling (no RH neutrino)
- NP: small (non-vanishing) coupling  $b \rightarrow s \mu \mu$ 
  - Small coupling to 2<sup>nd</sup> gen leptons
  - Left-handed coupling (from  $C_9$ )



# Model building

## Ingredients

- NP: large coupling  $b \rightarrow c \tau \nu$ 
  - Large coupling to 3<sup>rd</sup> gen leptons
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  - Small coupling to 2<sup>nd</sup> gen leptons
  - Left-handed coupling (from  $C_9$ )



G.Isidori

J.M.Camalich

## Experimental constraints

- High  $p_T$  searches (No  $\tau\tau$  resonance: no s-channel  $Z'$ )
- Radiative constr.  $\tau \rightarrow \mu \nu \nu$
- $B_s^0$  mixing (No tree level NP: small  $b_s$  implies large  $\tau\nu$ )
- $B_c^+$  lifetime (Scalar LQ increases  $BR(B_c^+ \rightarrow \tau^+ \nu)$ )

Vector LQ favoured over Scalar LQ or  $Z'$



# Model building

- Many more experimental handles; predictions can be checked!

- Universal for all  $b \rightarrow c \tau \nu$ :
  - Accurate  $R(D^*)$ ,  $R(J/\psi)$ , ...

$$\frac{R_D}{(R_D)_{SM}} = \frac{\Gamma(B \rightarrow D^* \tau \nu) / \Gamma_{SM}}{\Gamma(B \rightarrow D^* \mu \nu) / \Gamma_{SM}} = \frac{\Gamma(B_c \rightarrow \psi \tau \nu) / \Gamma_{SM}}{\Gamma(B_c \rightarrow \psi \mu \nu) / \Gamma_{SM}} = \frac{\Gamma(\Lambda_b \rightarrow \Lambda_c \tau \nu) / \Gamma_{SM}}{\Gamma(\Lambda_b \rightarrow \Lambda_c \mu \nu) / \Gamma_{SM}} = \dots$$

- Strong coupling to  $\tau$ ’s:
  - Measure e.g.  $B^0 \rightarrow K^* \tau \tau$

	$\mu\mu$ (ee)	$\tau\tau$	$\nu\nu$	$\tau\mu$	$\mu e$
$b \rightarrow s$	$R_K, R_{K^*}$ O(20%)	$B \rightarrow K^{(*)} \tau\tau$ → 100×SM	$B \rightarrow K^{(*)} \nu\nu$ O(1)	$B \rightarrow K \tau\mu$ → ~10 <sup>-6</sup>	$B \rightarrow K \mu e$ ???
$b \rightarrow d$	$B_d \rightarrow \mu\mu$ $B \rightarrow \pi \mu\mu$ $B_s \rightarrow K^{(*)} \mu\mu$ O(20%) [ $R_K=R_\pi$ ]	$B \rightarrow \pi \tau\tau$ → 100×SM	$B \rightarrow \pi \nu\nu$ O(1)	$B \rightarrow \pi \tau\mu$ → ~10 <sup>-7</sup>	$B \rightarrow \pi \mu e$ ???

- LFNU linked with LFV:
  - Look for e.g.  $B^0 \rightarrow K^* \tau \mu$
  - $BR(\tau \rightarrow \mu \mu \mu) \sim 10^{-9}$

- c, u symmetry:
  - Study suppressed semileptonic

$$\frac{\Gamma(B \rightarrow \pi \tau \nu) / \Gamma_{SM}}{\Gamma(B \rightarrow \pi \mu \nu) / \Gamma_{SM}} = \frac{\Gamma(\Lambda_b \rightarrow p \tau \nu) / \Gamma_{SM}}{\Gamma(\Lambda_b \rightarrow p \mu \nu) / \Gamma_{SM}} = \frac{\Gamma(B_s \rightarrow K^* \tau \nu) / \Gamma_{SM}}{\Gamma(B_s \rightarrow K^* \mu \nu) / \Gamma_{SM}} = \dots = \frac{R_D}{(R_D)_{SM}}$$

- $B_s$  mixing
  - O(1-10%) effect on  $\Delta m_s$

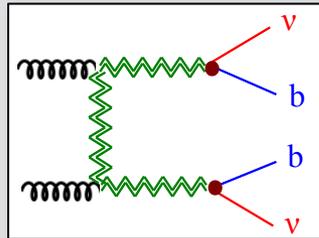
Buttazzo, Greife, Isidori, Marzocca, B-physics anomalies: a guide to combined explanations. JHEP 1711 (2017) 044



# Model building

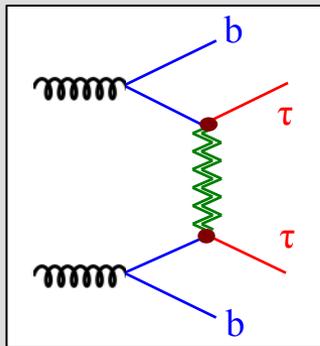
- Many more experimental handles; predictions can be checked!
- High  $p_T$  signatures?

- LQ pairs

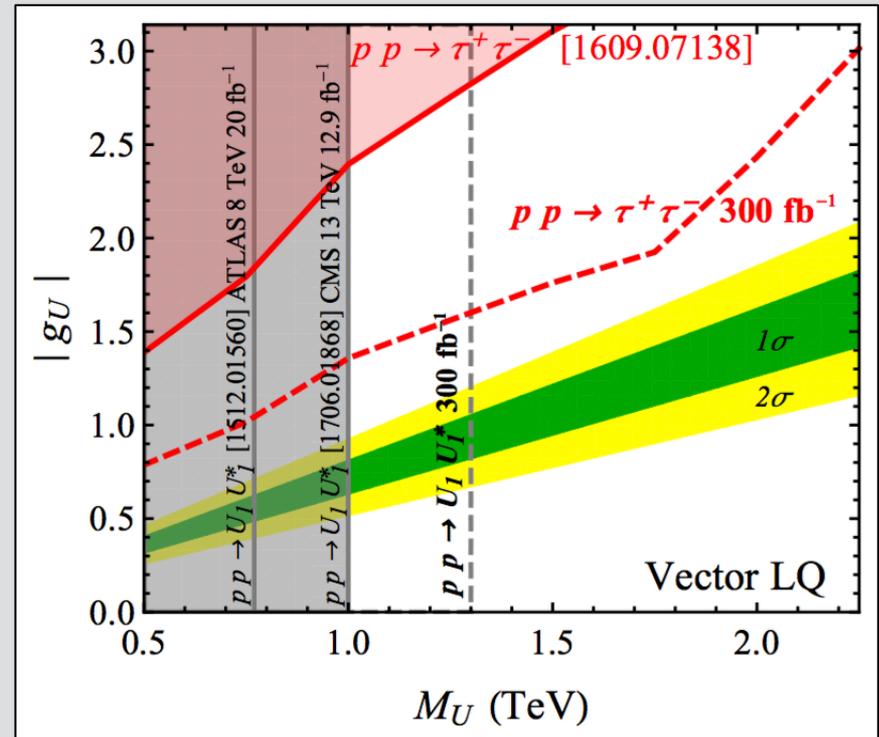
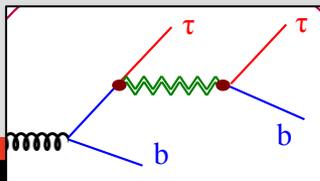


- LQ t-channel in  $bb \rightarrow \tau\tau$

Reachable during HL-LHC



- Single production channel (dominant?)



# Outlook

2020	2021	2022	2023	2024	2025	2026	2027	2028	2029	2030	2031	2032	2033	203+
		Run III					Run IV						Run V	
<b>LS2</b>					<b>LS3</b>						<b>LS4</b>			
<b>LHCb 40 MHz UPGRADE I</b>	$L = 2 \times 10^{33}$			<b>LHCb Consolidate: UPGRADE Ib</b>		$L = 2 \times 10^{33}$ $50 \text{ fb}^{-1}$				<b>LHCb UPGRADE II</b>		$L = 1-2 \times 10^{34}$ $300 \text{ fb}^{-1}$		
<b>ATLAS Phase I Upgr</b>	$L = 2 \times 10^{34}$			<b>ATLAS Phase II UPGRADE</b>		<b>HL-LHC</b> $L = 5 \times 10^{34}$						<b>HL-LHC</b> $L = 5 \times 10^{34}$		
<b>CMS Phase I Upgr</b>	$300 \text{ fb}^{-1}$			<b>CMS Phase II UPGRADE</b>								$3000 \text{ fb}^{-1}$		
<b>Belle II</b>	$5 \text{ ab}^{-1}$			$L = 6 \times 10^{35}$		$50 \text{ ab}^{-1}$								

LHC schedule:

<https://lhc-commissioning.web.cern.ch/schedule/LHC-long-term.htm>

## ■ LHCb Upgrade

- Upgrade to 40 MHz readout
- New VELO: strips → pixel
- New SciFi tracker

## ■ LHCb Upgrade II

- Add timing for 4D tracking

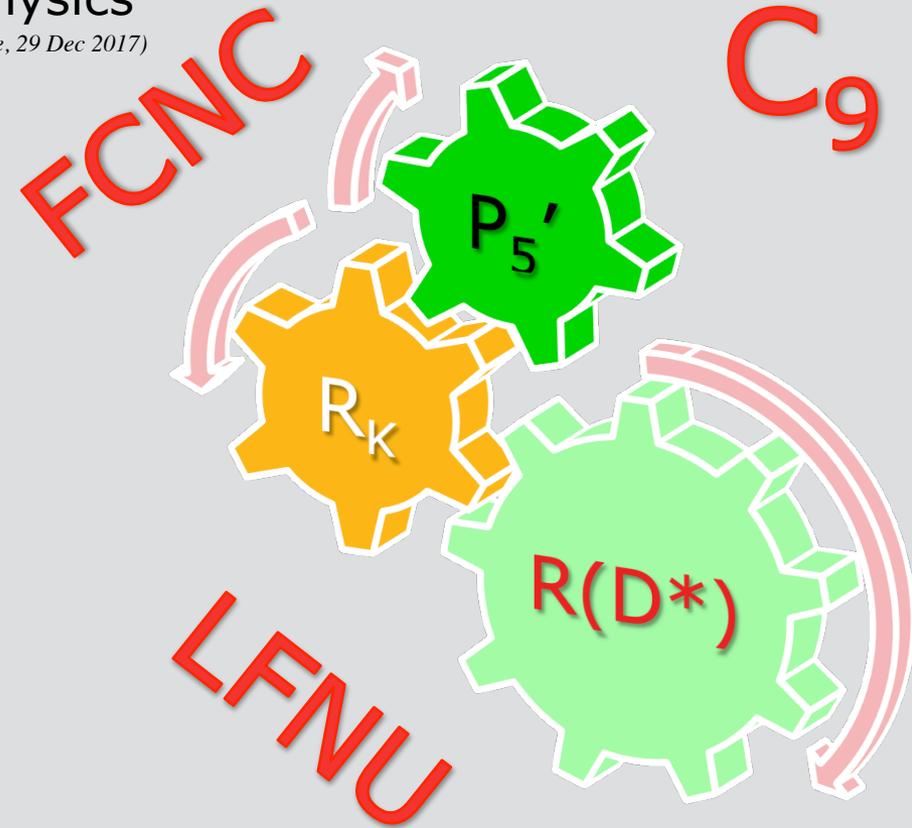
# Summary

- Many “unresolved issues in flavor physics”

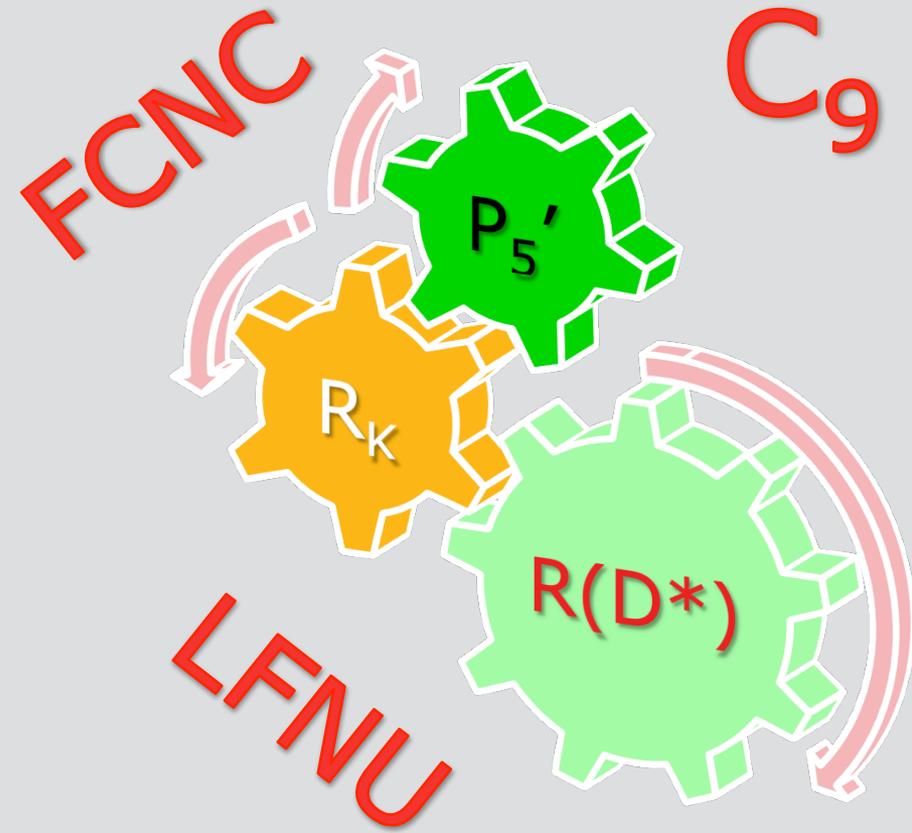
*(F. Gianotti, Jot Down Magazine, 29 Dec 2017)*

- Individually not so exciting...  
... but combined they are!

Stay tuned!



Thanks!



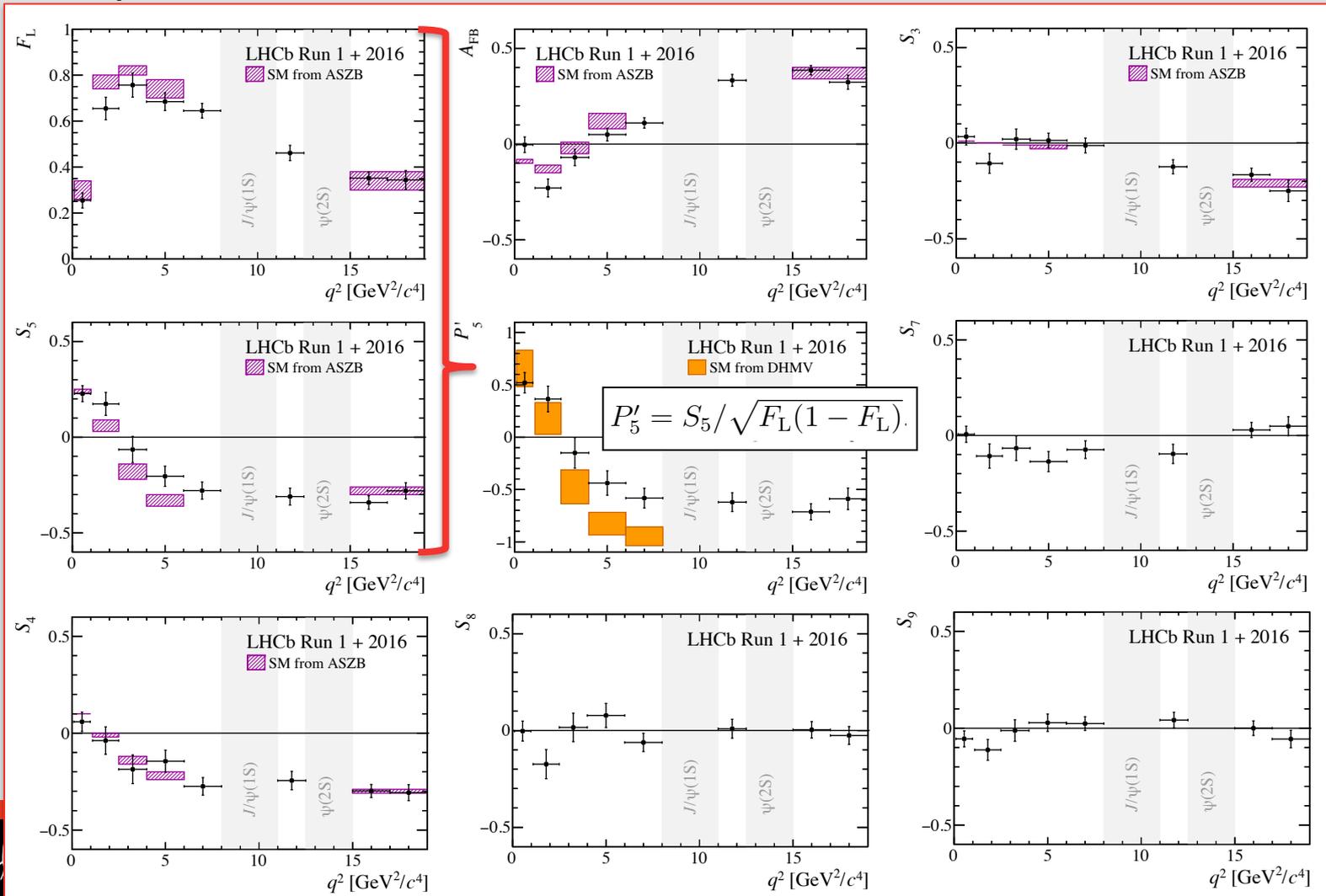
# Backup slides



# $B^0 \rightarrow K^0 \mu^+ \mu^-$ : more than just $P_5'$

- Many measurements:

LHCb coll., arXiv:2003.04831



# Many variables; all sensitive to effective couplings:

- $C_7$  (photon),  $C_9$  (vector) and  $C_{10}$  (axial) couplings hide everywhere:

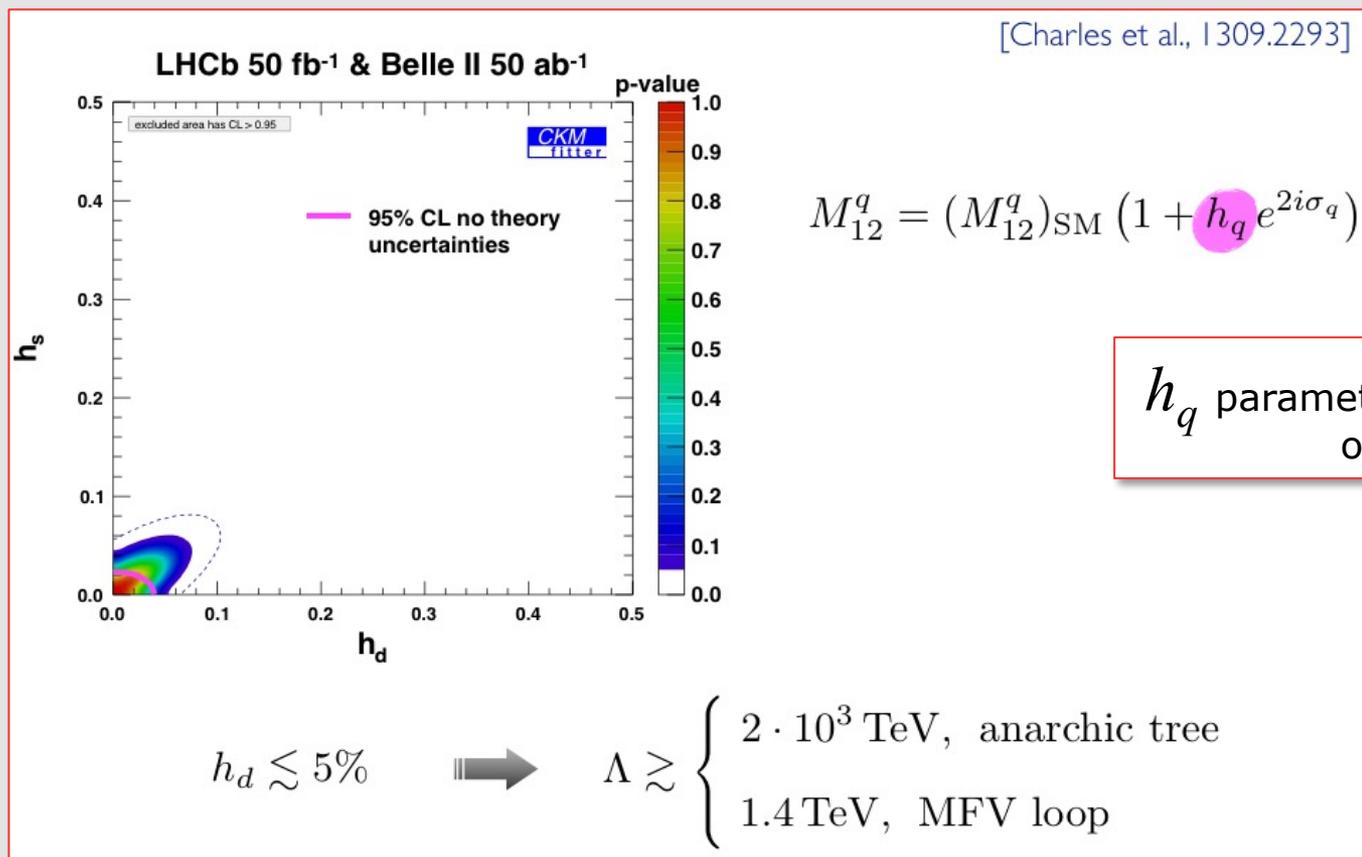
$$\begin{aligned}
 A_{\perp}^{L,R} &\propto (C_9^{eff} + C_9^{eff'}) \mp (C_{10}^{eff} + C_{10}^{eff'}) \frac{V(q^2)}{m_B + m_{K^*}} + \frac{2m_l}{q^2} (C_7^{eff} + C_7^{eff'}) T_1(q^2) \\
 A_{\parallel}^{L,R} &\propto (C_9^{eff} - C_9^{eff'}) \mp (C_{10}^{eff} - C_{10}^{eff'}) \frac{A_1(q^2)}{m_B + m_{K^*}} + \frac{2m_l}{q^2} (C_7^{eff} - C_7^{eff'}) T_2(q^2) \\
 A_0^{L,R} &\propto (C_9^{eff} - C_9^{eff'}) \mp (C_{10}^{eff} - C_{10}^{eff'}) \times [(m_B^2 - m_{K^*}^2 - q^2)(m_B + m_{K^*} A_1(q^2) - \lambda \frac{A_2(q^2)}{m_B + m_{K^*}})] + \\
 &\quad 2m_l (C_7^{eff} - C_7^{eff'}) [(m_B^2 + 3m_{K^*}^2 - q^2) T_2(q^2) - \frac{\lambda}{m_B^2 - m_{K^*}^2} T_3(q^2)]
 \end{aligned}$$

$$\begin{aligned}
 F_L &= \frac{A_0^2}{A_{\parallel}^2 + A_{\perp}^2 + A_0^2} \\
 S_3 &= \frac{A_{\perp}^{L2} - A_{\parallel}^{L2}}{A_{\perp}^{L2} + A_{\parallel}^{L2} + A_0^{L2}} + L \rightarrow R \\
 S_4 &= \frac{\Re(A_0^{L*} A_{\parallel}^L)}{|A_0^L|^2 |A_{\parallel}^L|^2 + |A_0^L|^2} + L \rightarrow R \\
 S_5 &= \frac{\Re(A_0^{L*} A_{\perp}^L)}{|A_0^L|^2 + |A_{\perp}^L|^2 + |A_0^L|^2} - L \rightarrow R \\
 S_6 &= \frac{\Re(A_{\perp}^{L*} A_{\parallel}^L)}{|A_{\perp}^L|^2 + |A_{\parallel}^L|^2 + |A_0^L|^2} - L \rightarrow R = \frac{4}{3} A_{FB} \\
 S_7 &= \frac{\Im(A_0^{L*} A_{\parallel}^L)}{|A_0^L|^2 + |A_{\parallel}^L|^2 + |A_0^L|^2} + L \rightarrow R \\
 S_8 &= \frac{\Im(A_0^{L*} A_{\perp}^L)}{|A_0^L|^2 + |A_{\parallel}^L|^2 + |A_0^L|^2} + L \rightarrow R \\
 S_9 &= \frac{\Im(A_{\perp}^{L*} A_{\parallel}^L)}{|A_{\perp}^L|^2 + |A_{\parallel}^L|^2 + |A_0^L|^2} - L \rightarrow R
 \end{aligned}$$

$$\begin{aligned}
 \frac{1}{\Gamma} \frac{d^3(\Gamma + \bar{\Gamma})}{d \cos \theta_{\ell} d \cos \theta_K d \phi} &= \frac{9}{32\pi} \left[ \frac{3}{4} (1 - F_L) \sin^2 \theta_K + F_L \cos^2 \theta_K + \frac{1}{4} (1 - F_L) \sin^2 \theta_K \cos 2\theta_{\ell} \right. \\
 &\quad \left. - F_L \cos^2 \theta_K \cos 2\theta_{\ell} + \right. \\
 &\quad S_3 \sin^2 \theta_K \sin^2 \theta_{\ell} \cos 2\phi + S_4 \sin 2\theta_K \sin 2\theta_{\ell} \cos \phi + \\
 &\quad S_5 \sin 2\theta_K \sin \theta_{\ell} \cos \phi + S_6 \sin^2 \theta_K \cos \theta_{\ell} + \\
 &\quad S_7 \sin 2\theta_K \sin \theta_{\ell} \sin \phi + \\
 &\quad \left. S_8 \sin 2\theta_K \sin 2\theta_{\ell} \sin \phi + S_9 \sin^2 \theta_K \sin^2 \theta_{\ell} \sin 2\phi \right]
 \end{aligned}$$

# Heavy Flavour = Precision search for NP

- Depending on your model, sensitive to multi-TeV scales, eg:



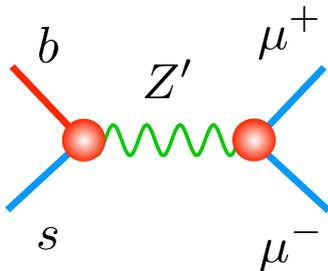
$$M_{12}^q = (M_{12}^q)_{\text{SM}} (1 + h_q e^{2i\sigma_q})$$

$h_q$  parametrizes magnitude of NP in  $B_q$  mixing

From Uli Haisch, [31 Aug 2016](#)

# Heavy Flavour = Precision search for NP

- Depending on your model, sensitive to multi-TeV scales, eg:



$$\mu_{B_s \rightarrow \mu^+ \mu^-} \simeq 1 \pm \frac{4\pi}{g^2 |V_{tb}^* V_{ts}|^2} \frac{v^2}{\Lambda^2}$$

$\mu_{B \rightarrow \mu\mu}$  is ratio  $BR^{\text{exp}}/BR^{\text{SM}}$

$$\Lambda \gtrsim \frac{v}{\sqrt{0.2}} \times \begin{cases} \frac{\sqrt{4\pi}}{g |V_{tb}^* V_{ts}|} \\ 1 \end{cases} \simeq \begin{cases} 50 \text{ TeV}, & \text{anarchic tree} \\ 0.6 \text{ TeV}, & \text{MFV loop} \end{cases}$$

From Uli Haisch, [31 Aug 2016](#)

# $B^0_{(s)} \rightarrow \mu\mu$ : projections

## Statistics

(3  $ab^{-1}$ )

	CMS	LHCb (50fb <sup>-1</sup> )	LHCb (300fb <sup>-1</sup> )
N(B <sub>d</sub> )	271	40	240
N(B <sub>s</sub> )	2250	400	2400

From: CMS-PAS-FTR-14-015

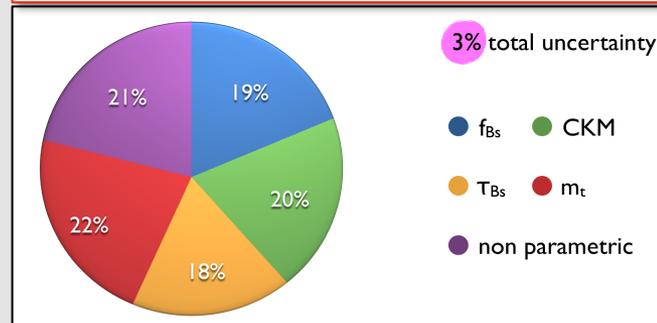
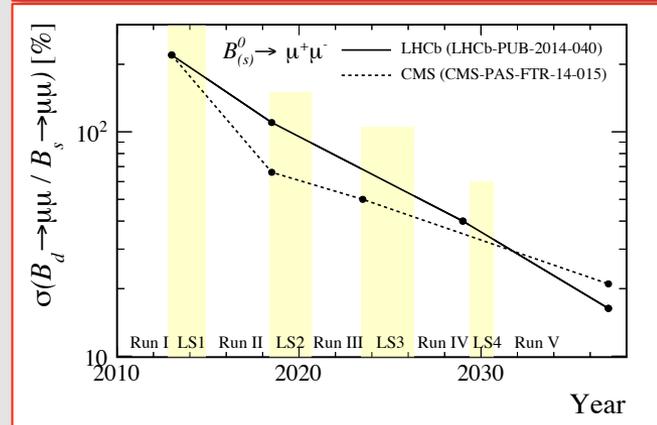
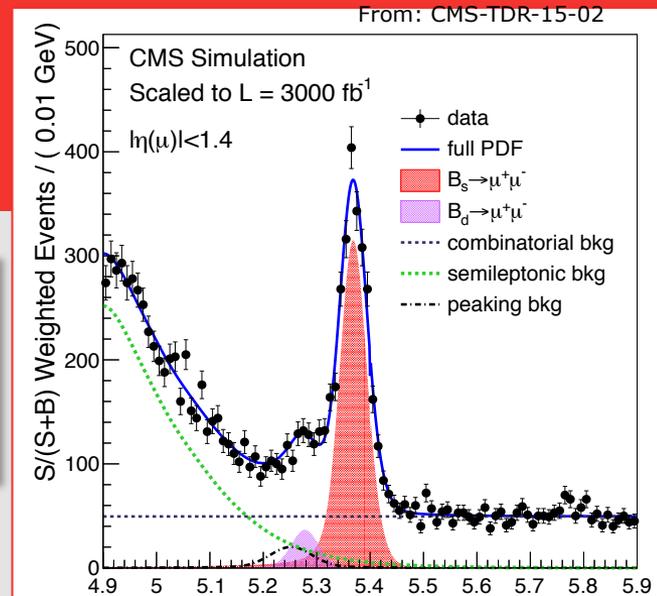
## Systematics

- ATLAS+CMS: improved mass resolution
- Limiting:  $f_s/f_d$

## Theoretical prediction $BR(B^0_{(s)} \rightarrow \mu\mu)$

- CKM elements, B decay constants
  - Accuracy expected to increase with improved lattice
  - Future unc. might reach  $\sim 3\%$  :

- Exp. uncertainty will probably not decrease to theoretical uncertainty



# $B^0_{(s)} \rightarrow \mu\mu$ : dominant systematic : $f_s/f_d$

- Dominant systematic uncertainty for  $\text{BR}(B_s^0 \rightarrow \mu\mu)$
- Relies on theoretical knowledge of ratio of BRs:

- Semileptonic:  $\Gamma(B_s^0 \rightarrow \mu X) = \Gamma(B \rightarrow \mu X)$

- Hadronic:

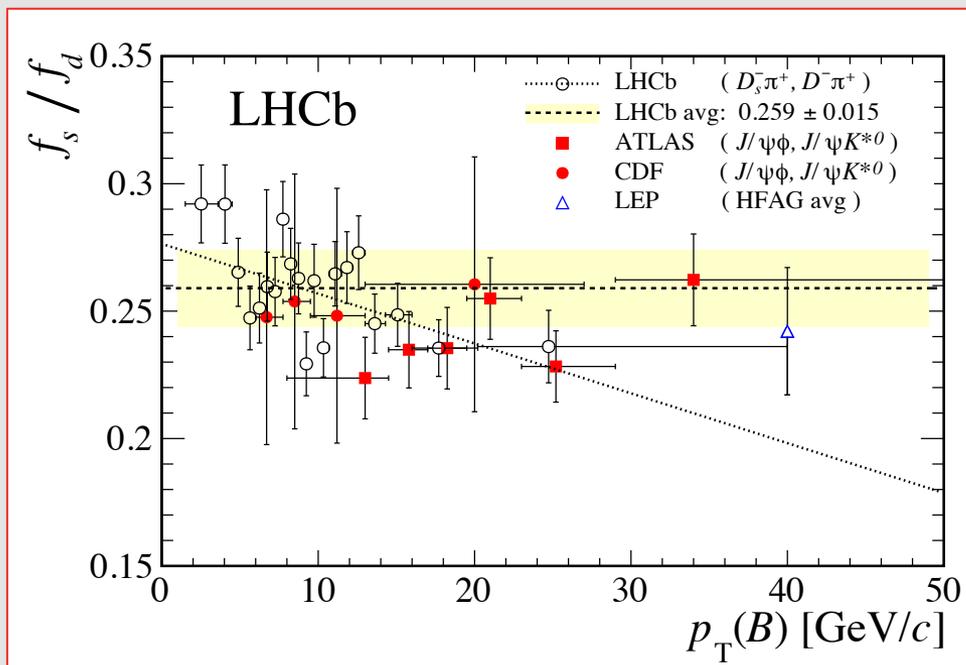
$$\frac{\text{BR}(\bar{B}_s^0 \rightarrow D_s^+ \pi^-)}{\text{BR}(\bar{B}_d^0 \rightarrow D^+ K^-)} = \frac{\Phi(D_s \pi) \tau_{B_s}}{\Phi(DK) \tau_{B_d}} \left| \frac{V_{ud}}{V_{us}} \right|^2 \left( \frac{f_\pi}{f_K} \right)^2 \left[ \frac{F_0^{(s)}(m_\pi^2)}{F_0^{(d)}(m_K^2)} \right]^2 \left| \frac{a_1(D_s \pi)}{a_1(D_d K)} \right|^2 = 14.2 \pm 1.3(\text{FF})$$

Fleischer, Serra, NT, PRD82 (2010) 034038

-  $B \rightarrow J/\psi X$ :

$$R_{s/d}^{\text{th},J} \equiv \frac{\text{BR}(B_s \rightarrow J/\psi \phi)}{\text{BR}(B_d \rightarrow J/\psi K^{*0})} \approx 0.83_{-0.02}^{+0.03} (\omega_B)_{-0.00}^{+0.01} (f_M)_{-0.02}^{+0.01} (a_i)_{-0.02}^{+0.01} (m_c) [0.83_{-0.03}^{+0.03}]$$

Liu, Wang, Xie, PRD89 (2014) 094010



# $B^0_{(s)} \rightarrow \mu\mu$ : dominant systematic : $f_s/f_d$

- Dominant systematic uncertainty for  $\text{BR}(B_s^0 \rightarrow \mu\mu)$
- Relies on theoretical knowledge of ratio of BRs:

$$\left[ \frac{F_0^{(s)}(m_\pi^2)}{F_0^{(d)}(m_K^2)} \right] = 1.046 \pm 0.044(\text{stat}) \pm 0.015(\text{sys})$$

Bailey et al, PRD.85(2012)114502

- Semileptonic:  $\Gamma(B_s^0 \rightarrow \mu X) = \Gamma(B \rightarrow \mu X)$

- Hadronic:

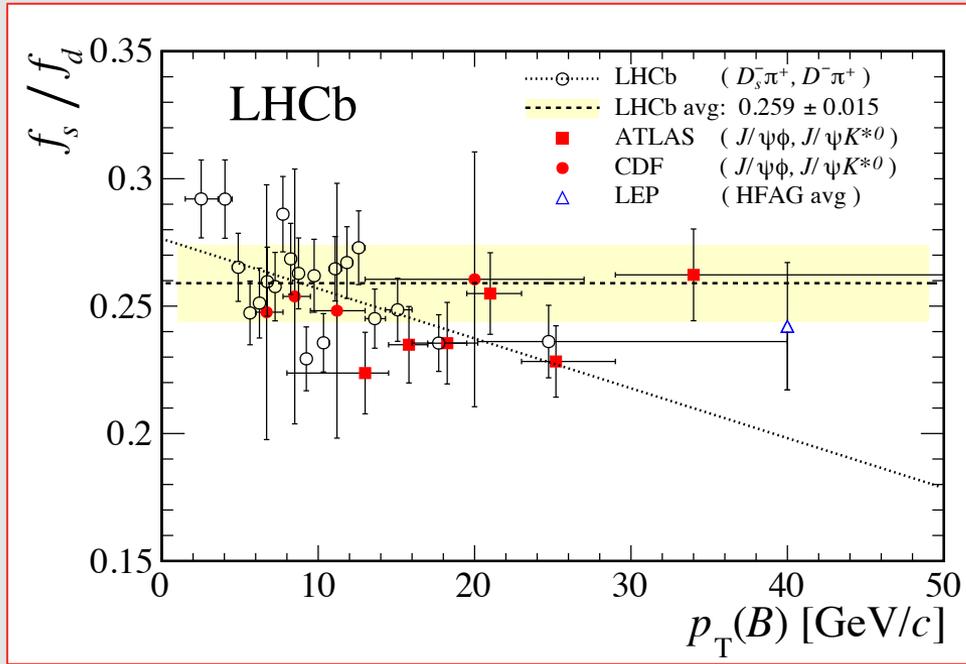
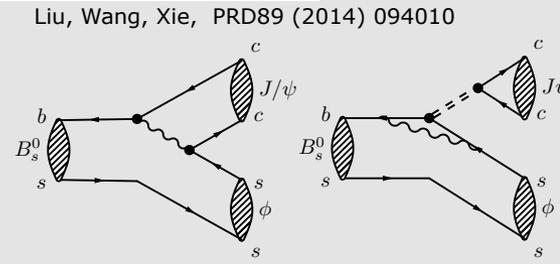
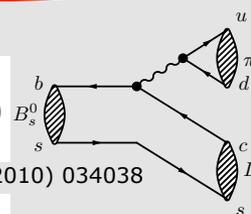
$$\frac{\text{BR}(\bar{B}_s^0 \rightarrow D_s^+ \pi^-)}{\text{BR}(\bar{B}_d^0 \rightarrow D^+ K^-)} = \frac{\Phi(D_s \pi) \tau_{B_s}}{\Phi(DK) \tau_{B_d}} \left| \frac{V_{ud}}{V_{us}} \right|^2 \left( \frac{f_\pi}{f_K} \right)^2 \left[ \frac{F_0^{(s)}(m_\pi^2)}{F_0^{(d)}(m_K^2)} \right]^2 \left| \frac{a_1(D_s \pi)}{a_1(D_d K)} \right|^2 = 14.2 \pm 1.3(\text{FF})$$

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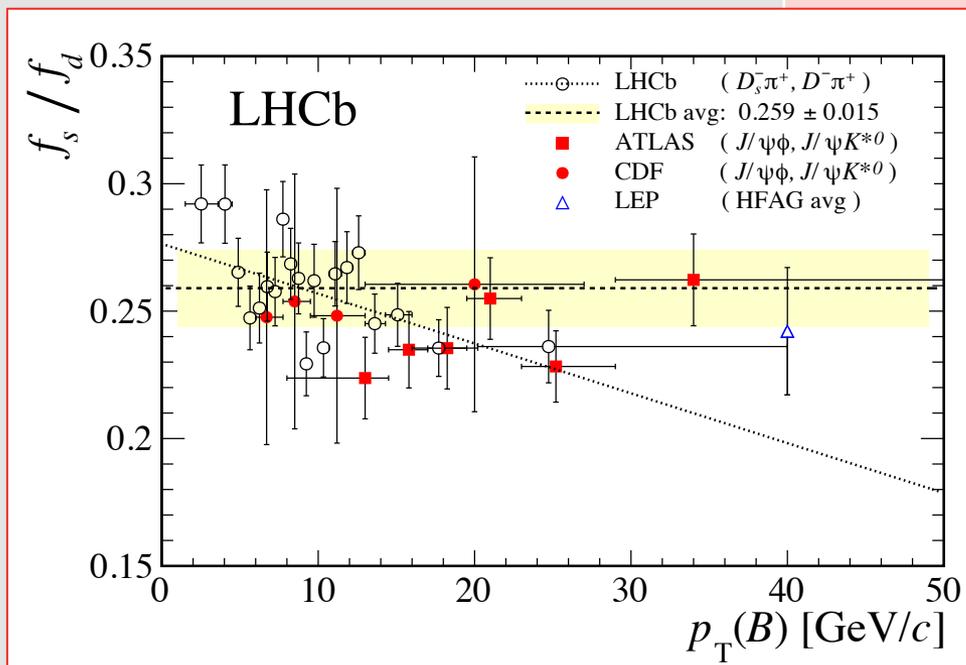
Liu, Wang, Xie, PRD89 (2014) 094010



# $B^0_{(s)} \rightarrow \mu\mu$ : dominant systematic : $f_s/f_d$

- Dominant systematic uncertainty for  $\text{BR}(B_s^0 \rightarrow \mu\mu)$
- Measurements:

	Normalization	Dependence
LHCb	Semileptonic <a href="#">Phys. Rev. D 85 (2012) 032008</a> $B \rightarrow Dh$ <a href="#">Phys. Rev. Lett. 107 (2011) 211801</a> LHCb-CONF-2013-011	$B \rightarrow Dh$ <a href="#">JHEP 04 (2013) 001</a>
CDF	Semileptonic <a href="#">Phys. Rev. D 77, 072003 (2008)</a> .	$B \rightarrow J/\psi X$ <a href="#">Public Note 10795</a>
ATLAS	$B \rightarrow J/\psi X$	$B \rightarrow J/\psi X$ <a href="#">Phys.Rev.Lett. 115 (2015) 262001</a>

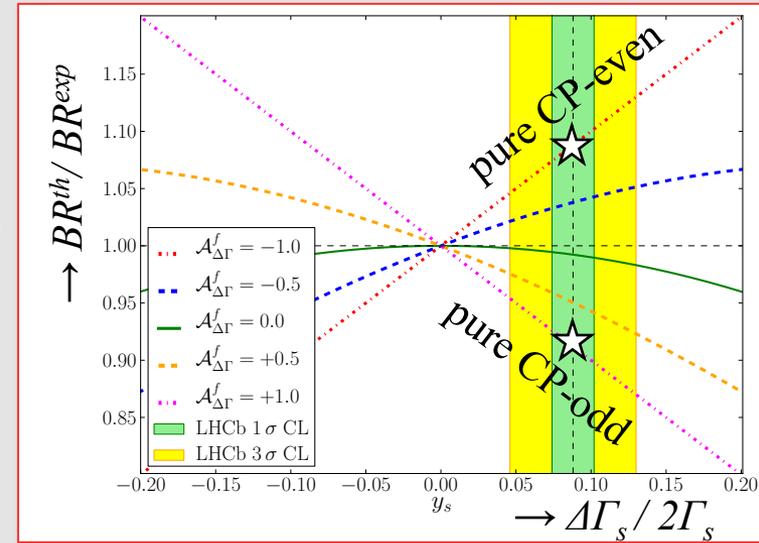
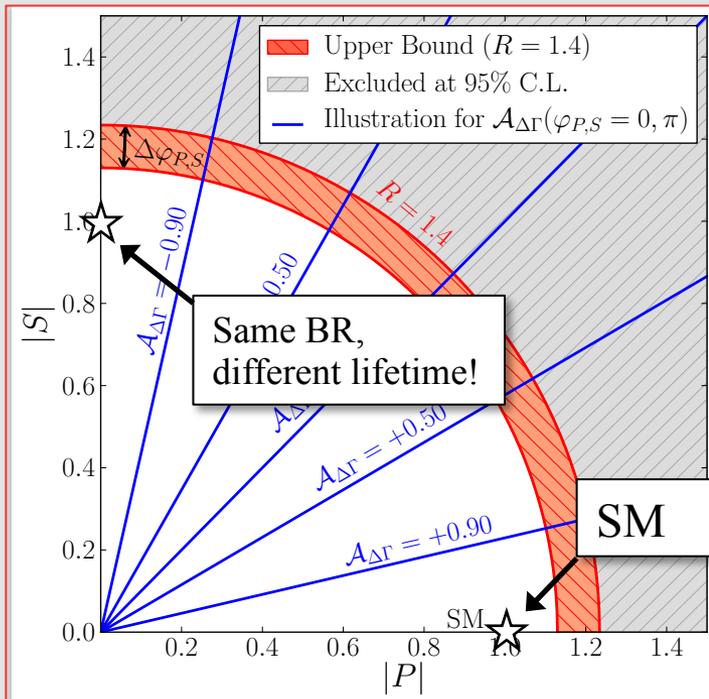


## ■ Possible improvements:

- $B_{(s)} \rightarrow D_{(s)}$  form factors: Lattice
- $B_s \rightarrow D_s$  form factors: LHCb
- $\text{BR}(B \rightarrow DX\mu\nu)$ : BelleII
- $\text{BR}(D_{(s)})$ : BESIII

# $B^0_{(s)} \rightarrow \mu\mu$ : effective lifetime

- Lifetime difference  $B_S^0_H$  (CP-) and  $B_S^0_L$  (CP+):
- SM: P-amplitude dominates, selecting CP-odd
- Different CP admixture affects effective lifetime
  - possibly not affecting the BR, when  $|S|$  and  $A_{\Delta\Gamma}$  compensate...
- Could be due to scalar amplitude  $|S|$  from NP



De Bruyn, Fleischer, NT, et al. Phys.Rev. D86 (2012) 014027

$$R \equiv \frac{\text{BR}(B_s \rightarrow \mu^+ \mu^-)_{\text{exp}}}{\text{BR}(B_s \rightarrow \mu^+ \mu^-)_{\text{SM}}} = \left[ \frac{1 + \mathcal{A}_{\Delta\Gamma} y_s}{1 - y_s^2} \right] (|P|^2 + |S|^2)$$

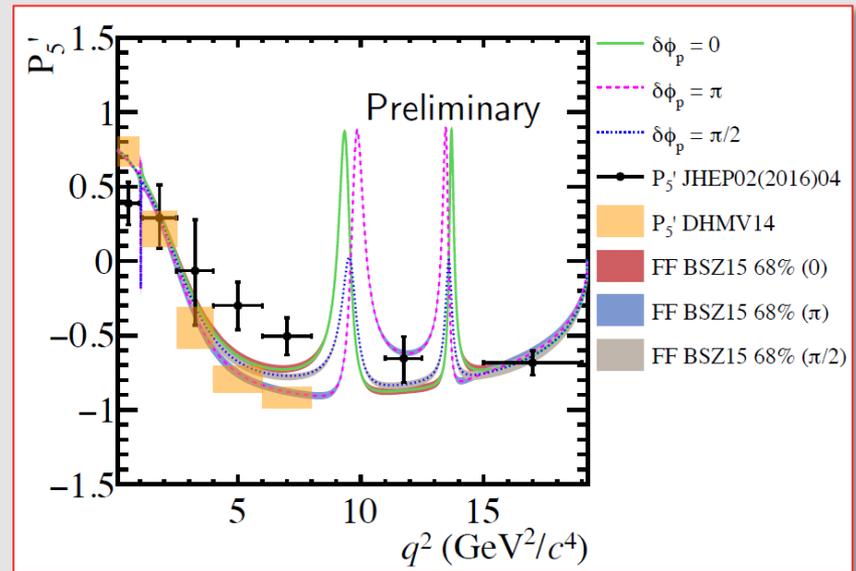
# $B^0 \rightarrow K^* \mu\mu$ : Projections

- Statistics for  $B^0 \rightarrow K^* \mu\mu$  :
- Understand theory:
  - Measure  $q^2$  dependence
    - To disentangle charm loop effects!
  - Factorisable power corrections
  - Form factors

For  $P_5'$  in [4, 6]  $\text{GeV}^2$  bin:

$-0.82^{+0.01}_{-0.01} \quad +0.02^{+0.02}_{-0.02} \quad +0.03^{+0.03}_{-0.06} \quad +0.06^{+0.06}_{-0.06} \quad +0.07^{+0.07}_{-0.08}$

	Run 1	Run 1-3(4)	Run 1-5
LHCb JHEP 02 (2016) 104	600	20,000	120,000*
CMS Phys. Lett. B 753 (2016) 424	300	10,000	100,000
		(naïve scaling with lumi)	



Pomery, Egde, Owen, Petrides, Blake

# $b \rightarrow sll$ : Projections

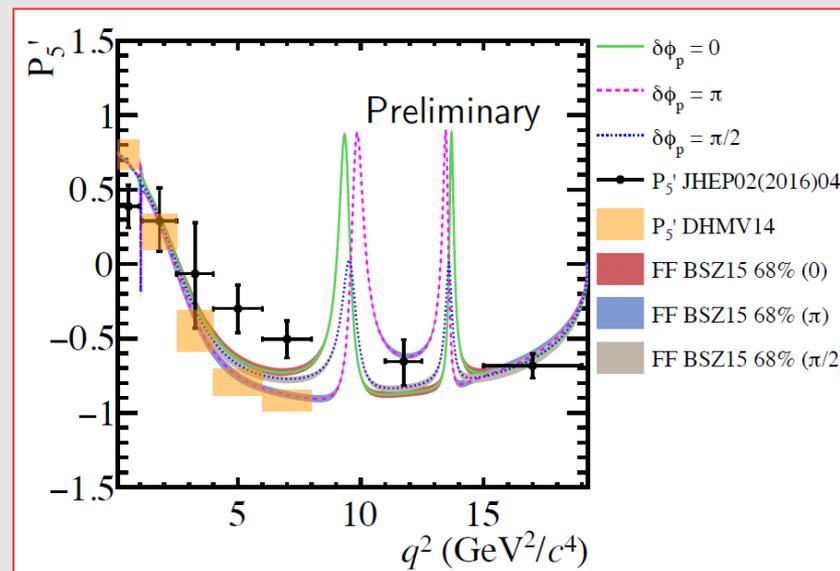
- Statistics for  $B^0 \rightarrow K^* \mu \mu$  :
- Understand theory for  $B^0 \rightarrow K^* \mu \mu$  :
  - Measure  $q^2$  dependence
    - To disentangle charm loop effects!
  - Factorisable power corrections
  - Form factors

For  $P_5'$  in [4, 6]  $\text{GeV}^2$  bin:

$$-0.82^{+0.01}_{-0.01} \quad +0.02^{+0.02}_{-0.02} \quad +0.03^{+0.03}_{-0.06} \quad +0.06^{+0.06}_{-0.06} \quad +0.07^{+0.07}_{-0.08}$$

- Many more observables!
  - Lepton-flavour universality,  $R_{K^*}$
  - Lepton-flavour violation searches
  - BR's
  - $A_{\text{FB}}(S_6)$ ,  $A_9$ , ...
  - $B^0 \rightarrow K^* ee$
  - ...

	Run 1	Run 1-3(4)	Run 1-5
LHCb JHEP 02 (2016) 104	600	20,000	120,000*
CMS Phys. Lett. B 753 (2016) 424	300	10,000	100,000
		(naïve scaling with lumi)	



Pomery, Egde, Owen, Petrides, Blake

	Decay	Run 1	Run 2	50 $\text{fb}^{-1}$	300 $\text{fb}^{-1}$
$R_K$	$B^+ \rightarrow K^+ \mu^+ \mu^-$	11%	5%	2%	1%
$R_{K^*}$	$B^0 \rightarrow K^{*0} \mu^+ \mu^-$	18%	8%	3%	1%
$R_\phi$	$B_s^0 \rightarrow \phi \mu^+ \mu^-$	36%	15%	8%	3%

# Experiment vs Theory

- For very long, flavour observables will stay statistically limited!

	LHCb up to LS2		LHCb upgrade		Theory
	Run 1	Run 2	Run 3	Run 4	Theory uncertainty
Integrated lumi	$3 \text{ fb}^{-1}$	$8 \text{ fb}^{-1}$	$23 \text{ fb}^{-1}$	$46 \text{ fb}^{-1}$	
$\frac{Br(B_d \rightarrow \mu\mu)}{Br(B_s \rightarrow \mu\mu)}$	-	110 %	60%	40%	5%
$q_0^2 A_{FB}(B_d \rightarrow K^{*0} \mu\mu)$	10%	5%	2.8%	1.9%	7%
$\phi_s(B_s \rightarrow J/\psi\phi, B_s \rightarrow J/\psi\pi\pi)$	0.05	0.025	0.013	0.009	0.003
$\phi_s(B_s \rightarrow \phi\phi)$	0.18	0.12	0.04	0.026	0.02
$\gamma$	$7^\circ$	$4^\circ$	$1.7^\circ$	$1.1^\circ$	negl.
$A_\Gamma(D^0 \rightarrow KK)$	$3.4 \cdot 10^{-4}$	$2.2 \cdot 10^{-4}$	$0.9 \cdot 10^{-4}$	$0.5 \cdot 10^{-4}$	-

LHCb-PUB-2014-040

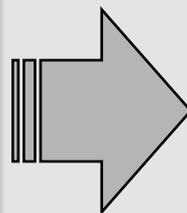
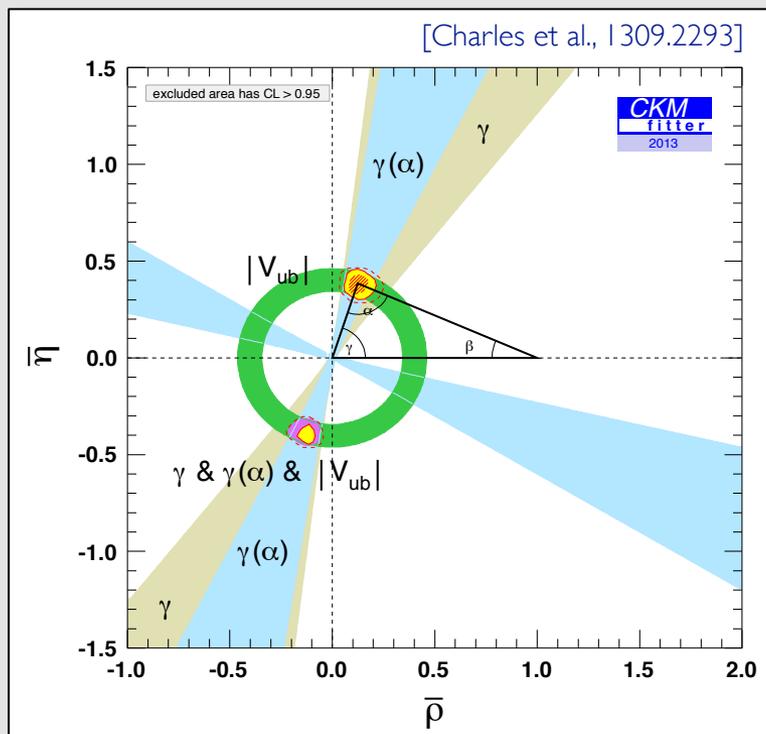
$\delta\gamma$	$\mathcal{O}(10^{-7})$	[Brod & Zupan, 1308.5663]
$\delta\beta$	$\mathcal{O}(1\%)$	[Ciuchini et al, hep-ph/0507290]
$\delta R_{D^*}$	$\mathcal{O}(1\%)$	[Fajfer et al., 1203.2654]
$\delta R_K, \delta R_{K^*}, \dots$	$\mathcal{O}(1\%)$	[Bordone et al., 1605.07633]

From Ull Haisch, 31 Aug 2016

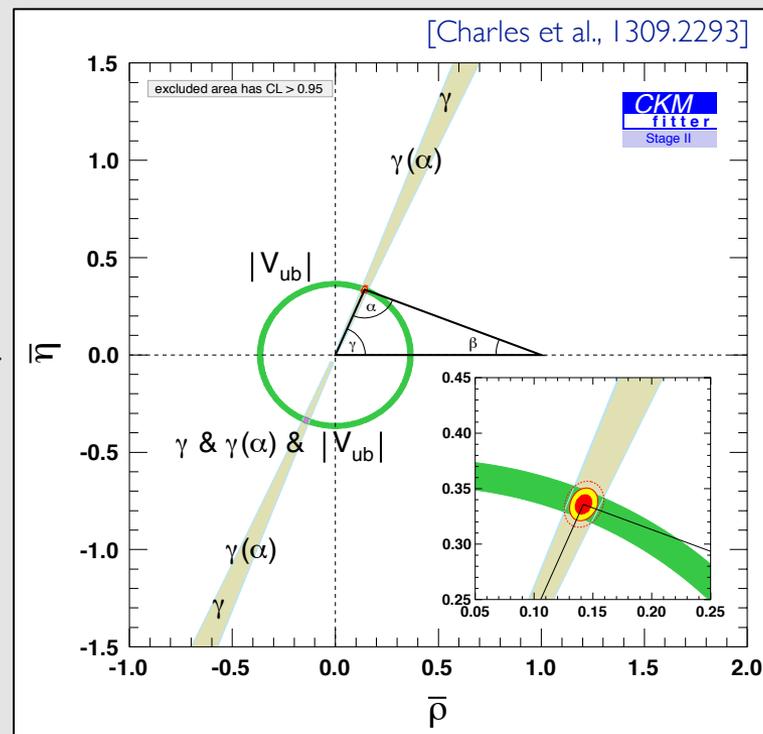
# CKM unitarity triangle: test consistency

- Precision measurements to scrutinize the Standard Model
- Precision measurements only way to reach very high mass scales
- Precision measurements are not yet precise enough

2013



2030



# The need for more precision

Imagine if Fitch and Cronin had stopped at the 1% level, how much physics would have been missed”

– A.Soni

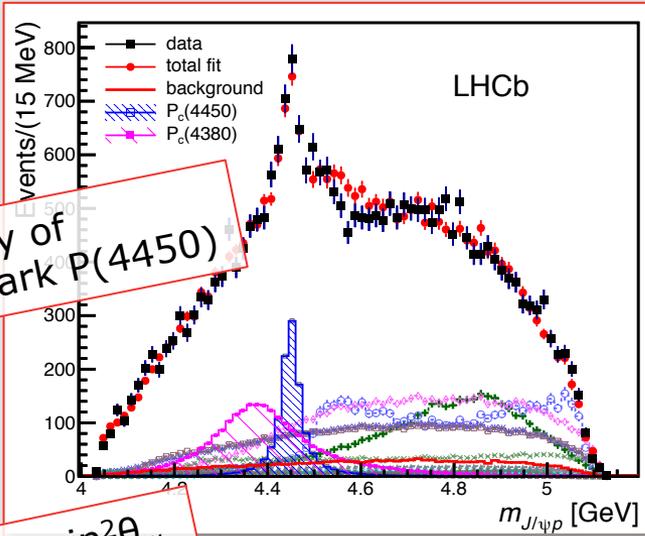
- “A special search at Dubna was carried out by Okonov and his group. They did not find a single  $K_L^0 \rightarrow \pi^+ \pi^-$  event among 600 decays into charged particles (Anikira et al., JETP 1962). At that stage the search was terminated by the administration of the lab. The group was unlucky.”

– L.Okun

(remember:  $B(K_L^0 \rightarrow \pi^+ \pi^-) \sim 2 \cdot 10^{-3}$ )

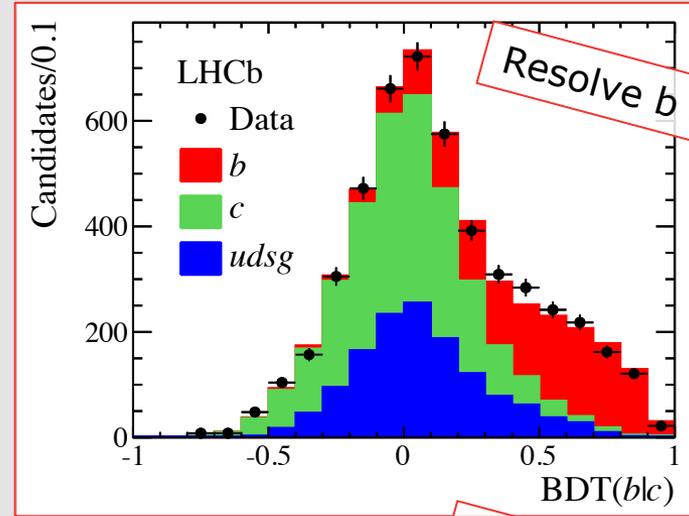
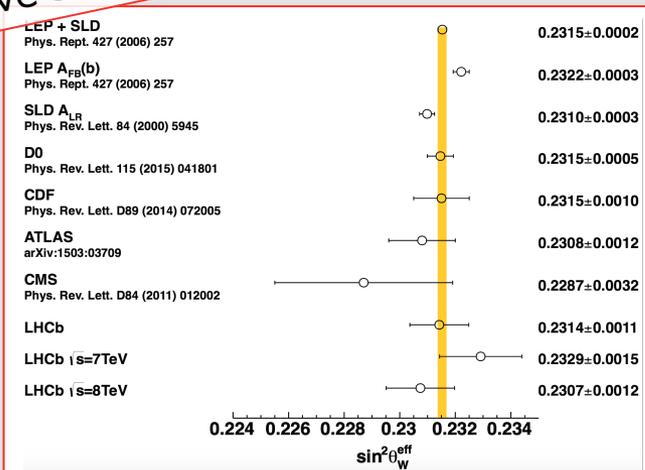
# LHCb = more than flavour

pdfs, jets, heavy-ion, EW, exotic states...

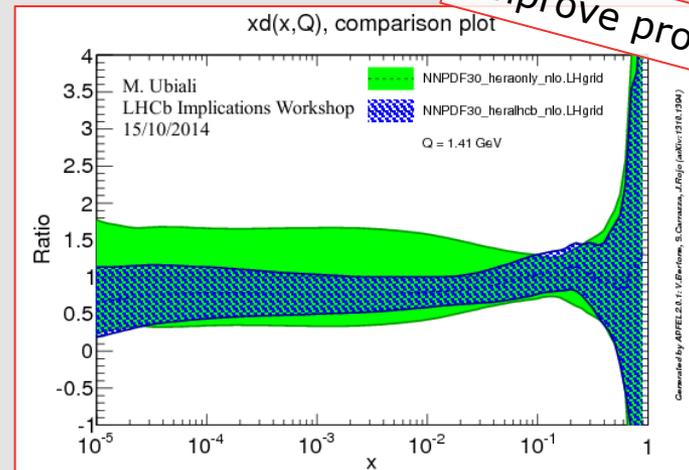


Discovery of pentaquark P(4450)

Impressive  $\sin^2\theta_W$

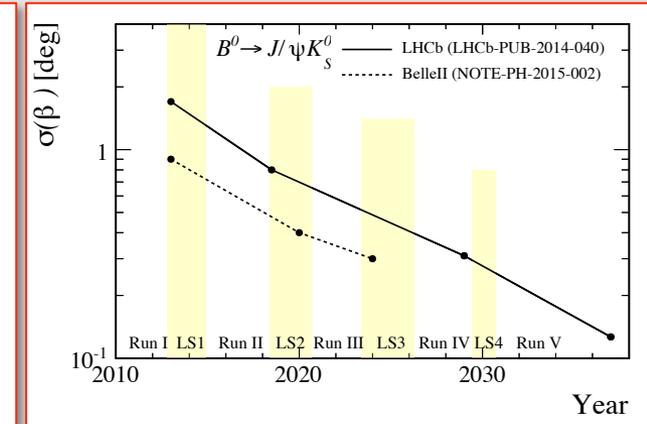
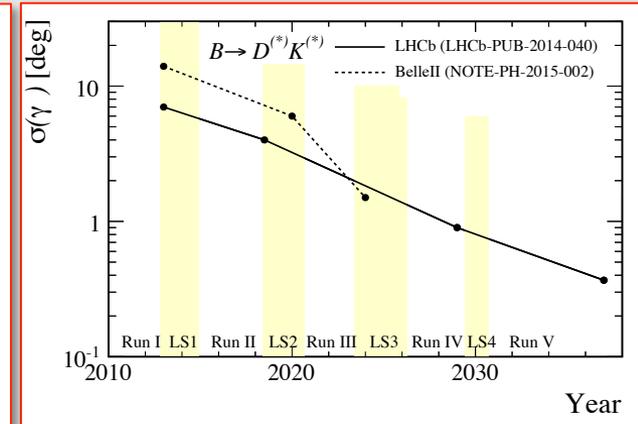
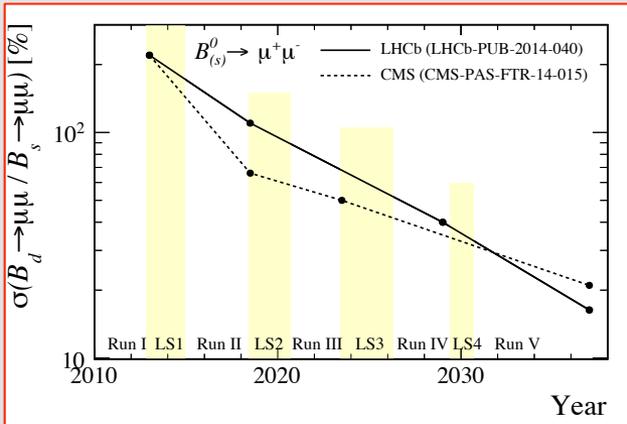
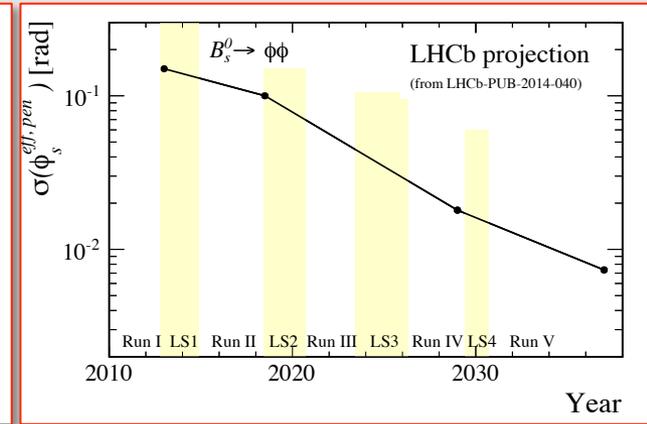
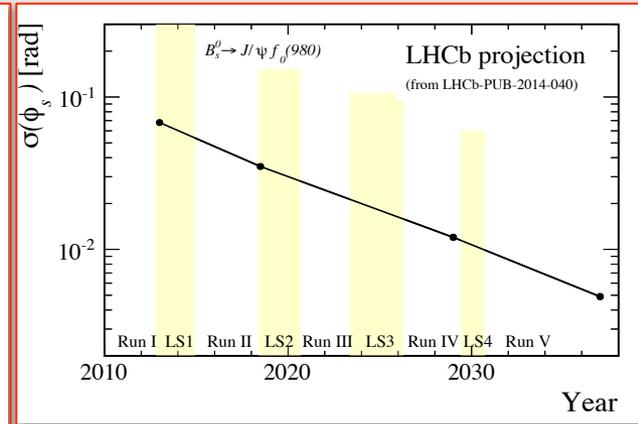
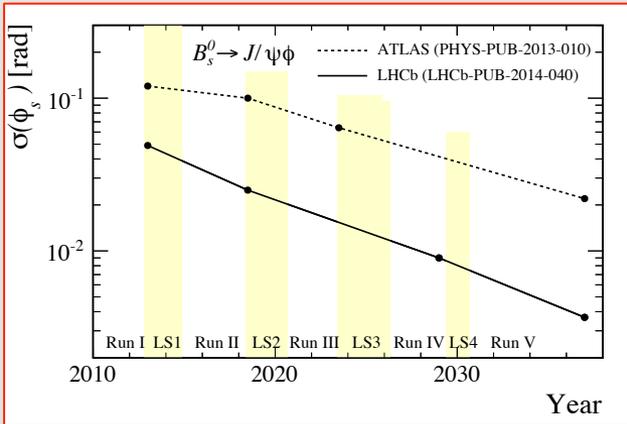


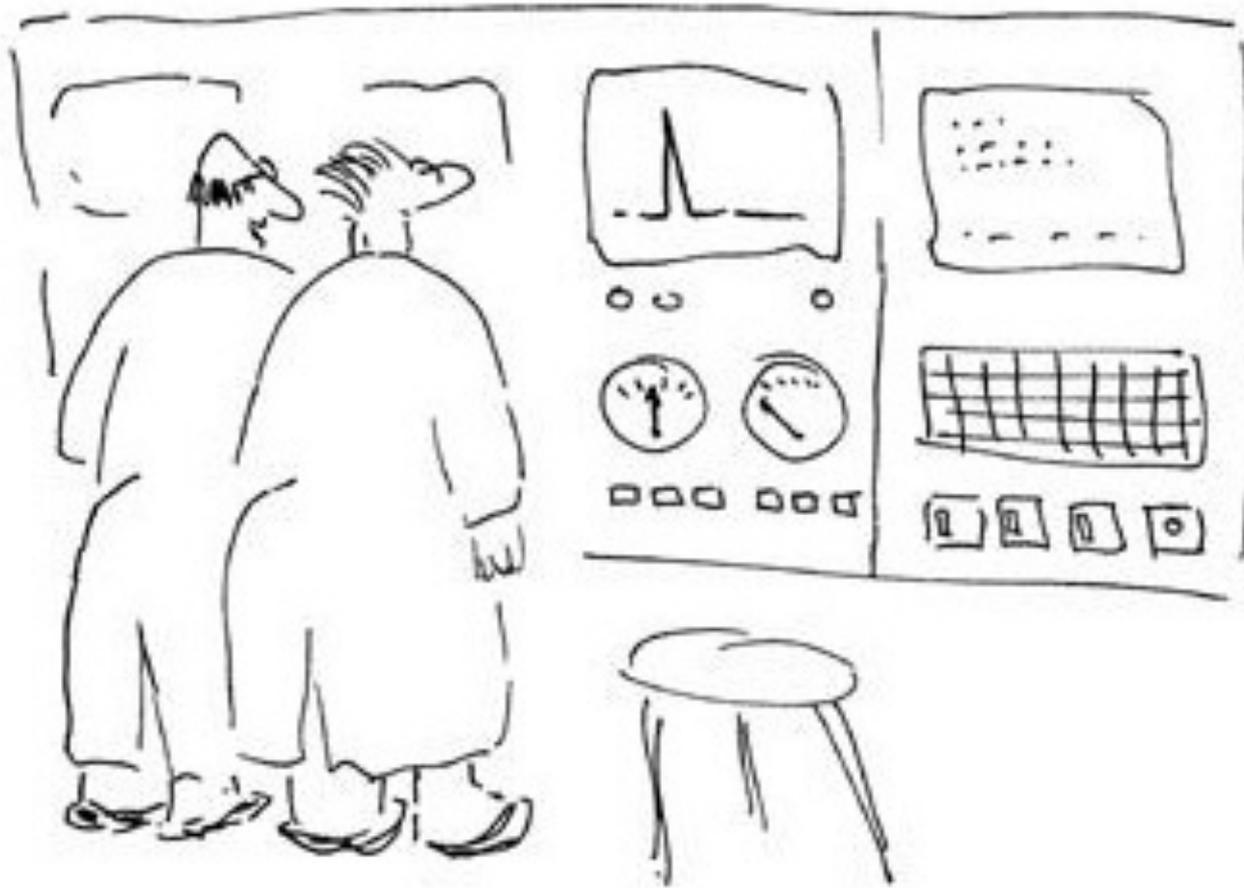
Resolve b and c jets



Improve proton pdf's

# Projected sensitivities





WELL, EITHER WE'VE FOUND A LEPTOQUARK,  
OR GEORGIOS'S JUST PUT THE KETTLE ON