

LFV, LNV, LUV at Belle (II)



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Yonsei University

Muon Anomalies Workshop @ SNU, May 21, 2021

Belle & Belle II

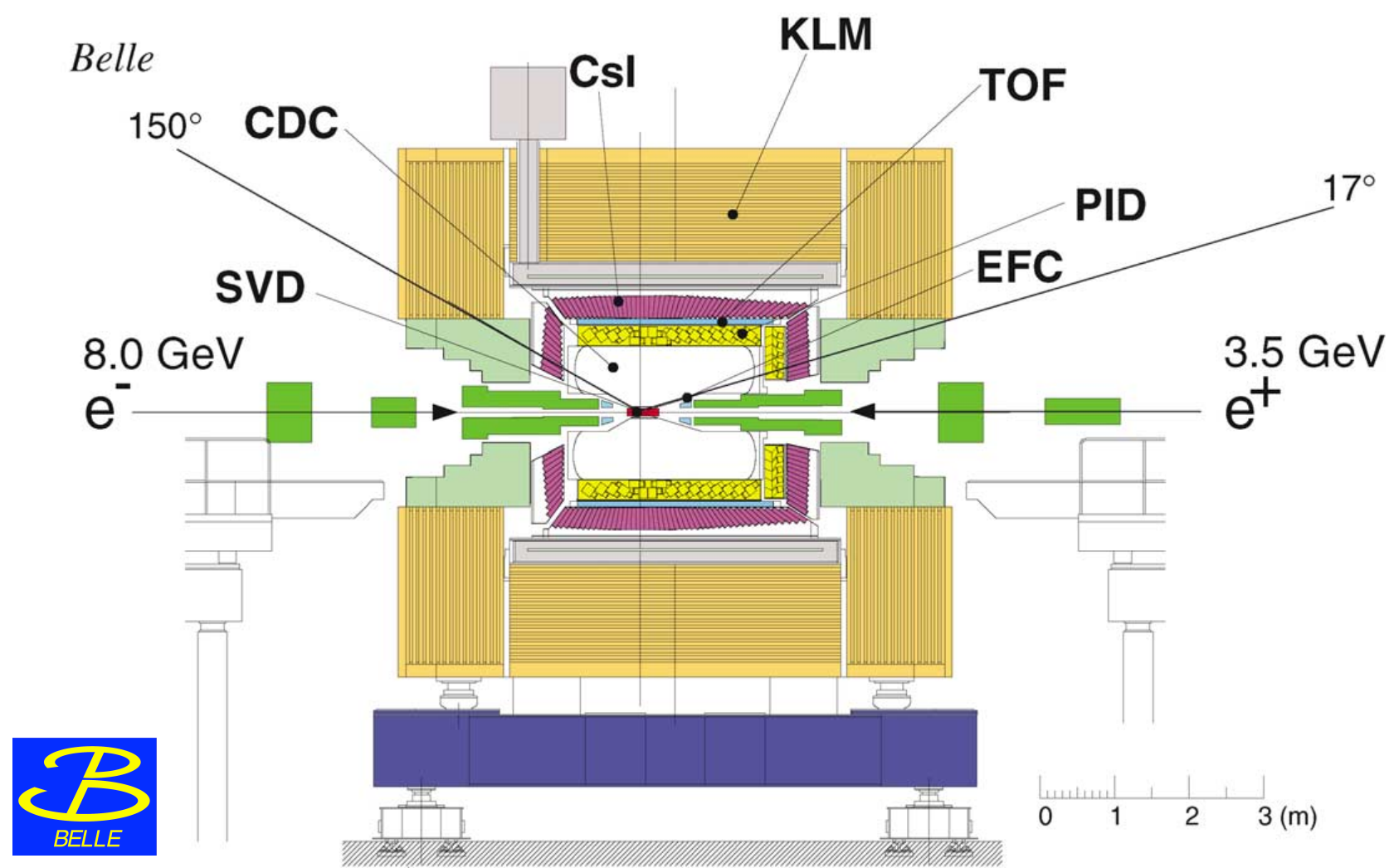
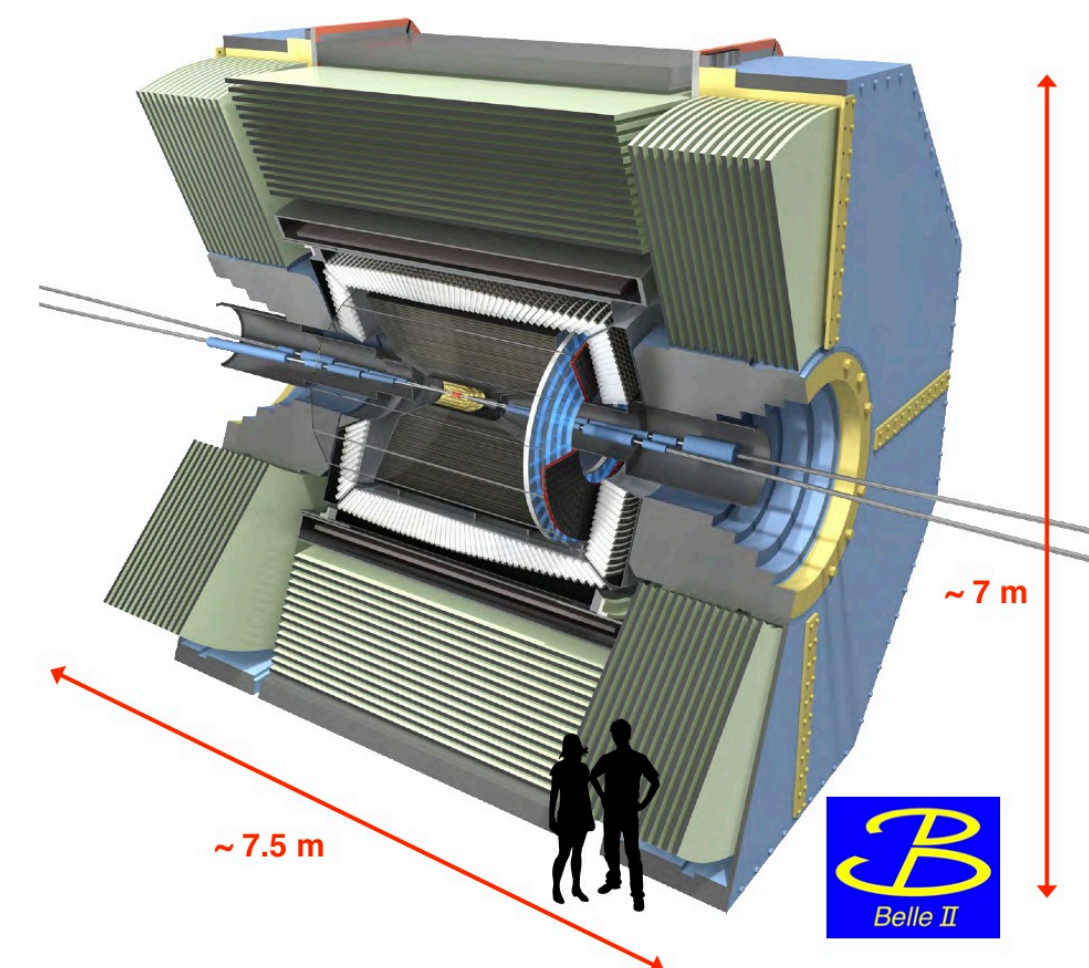
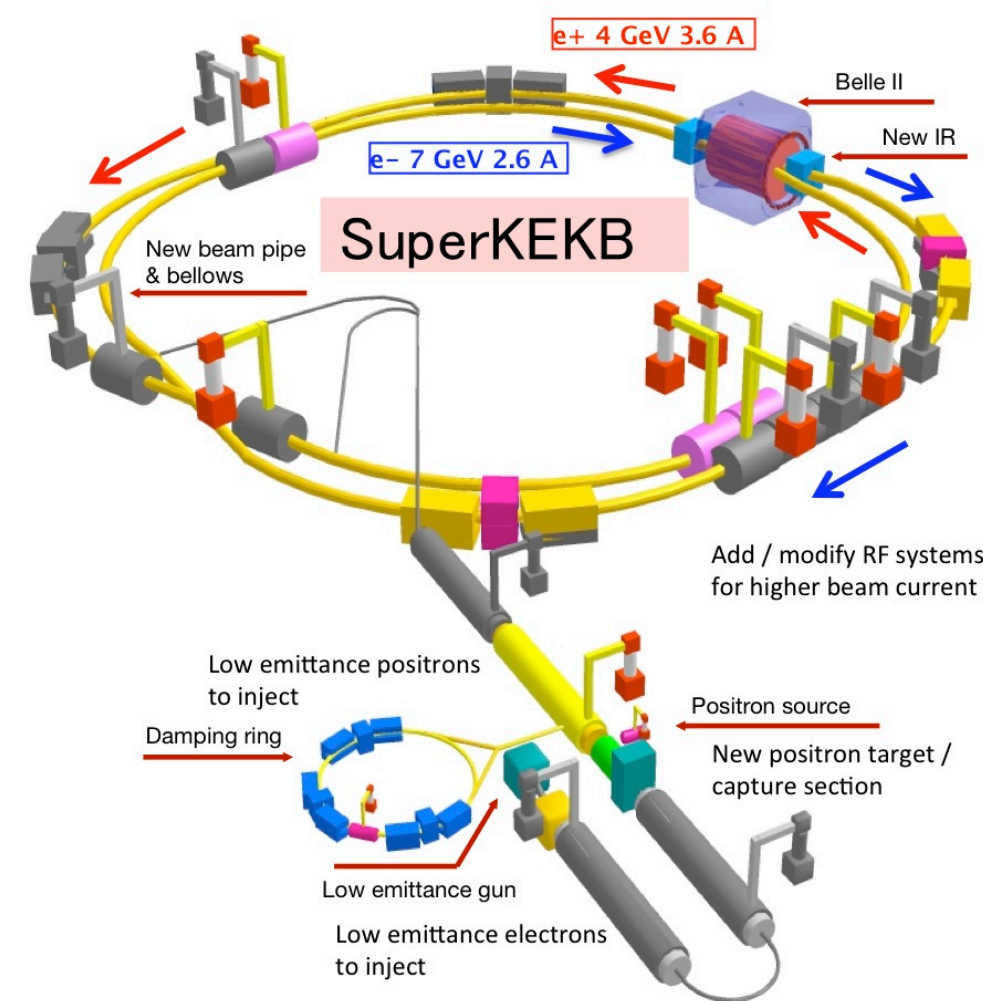


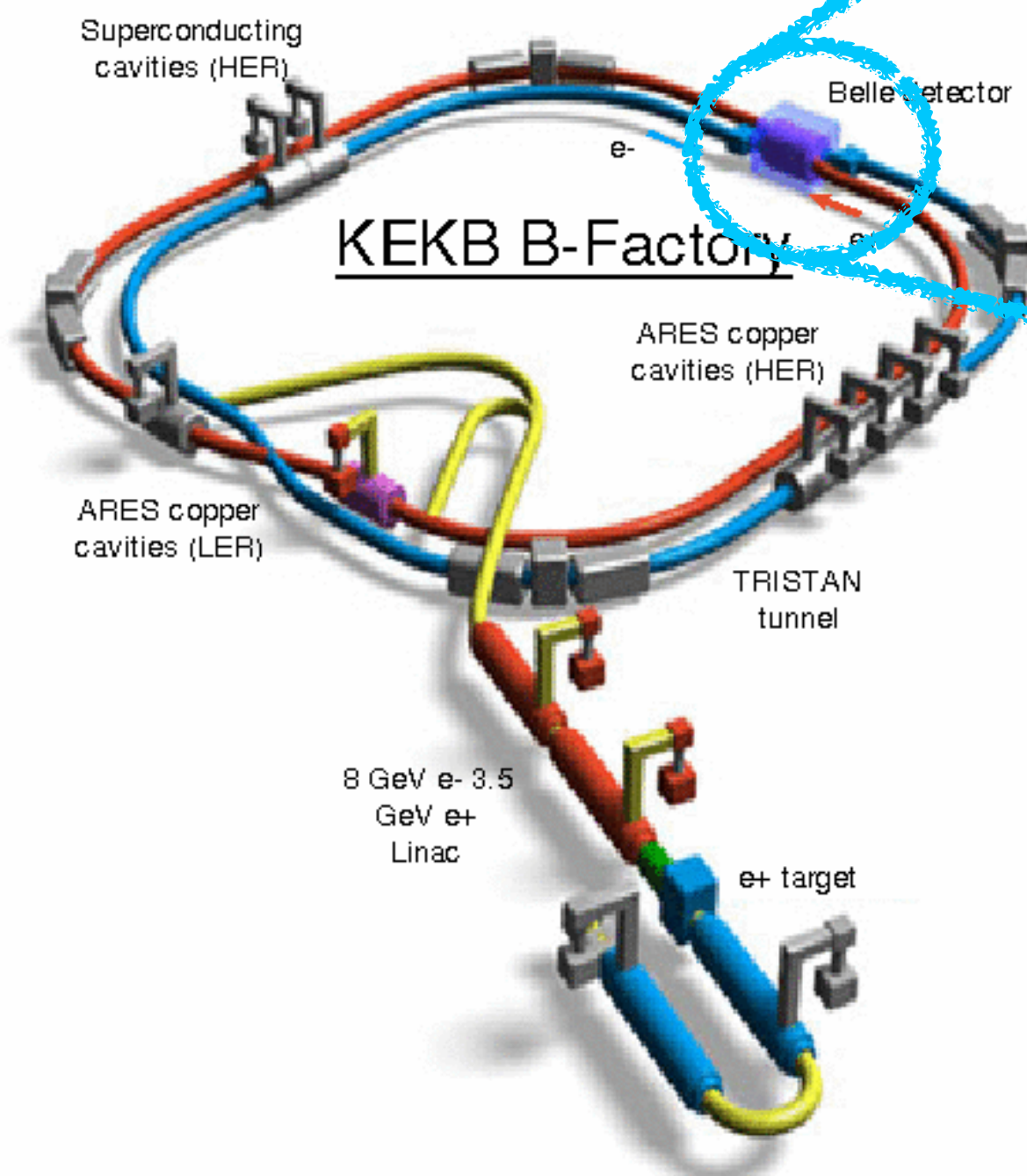
Fig. 1. Side view of the Belle detector.





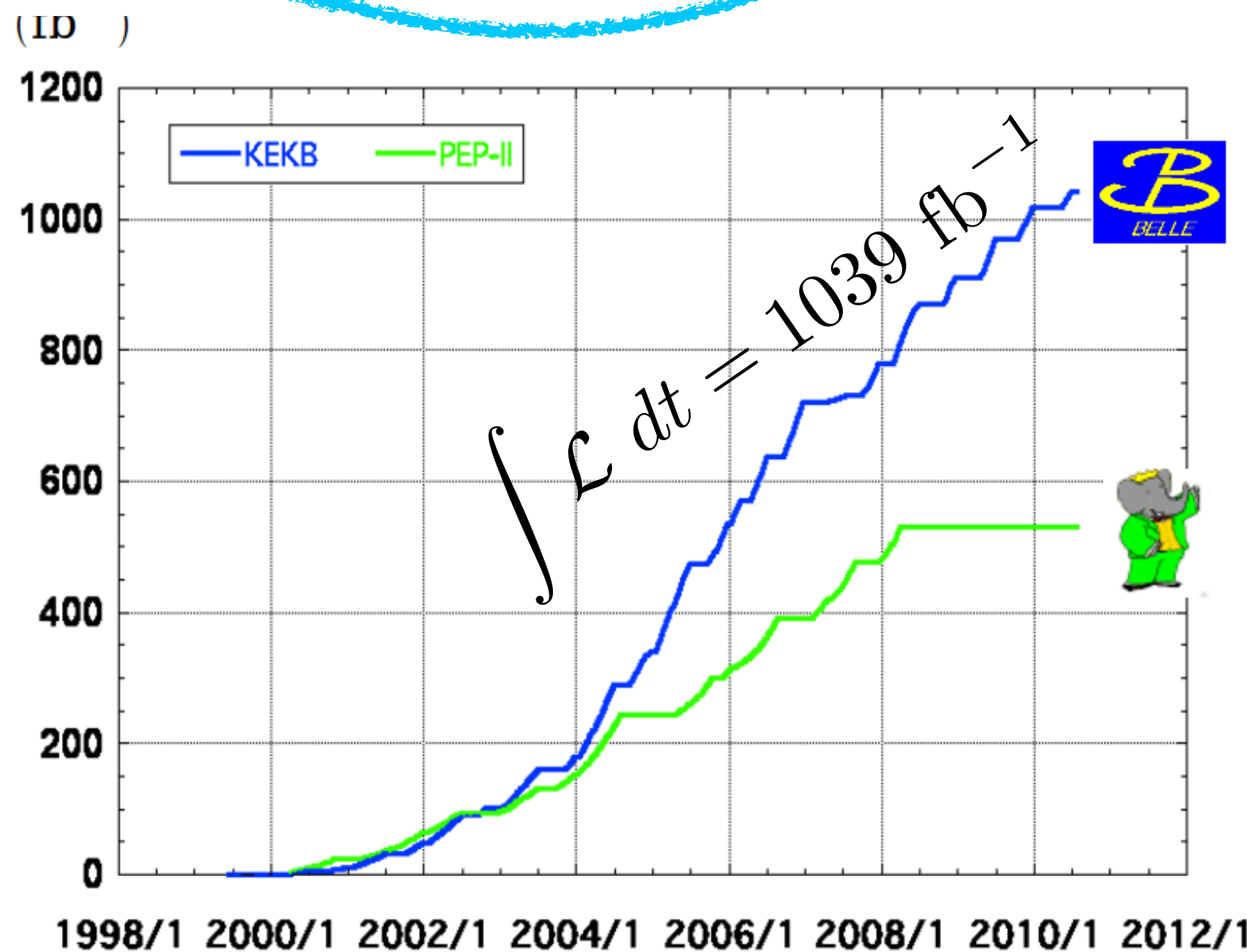
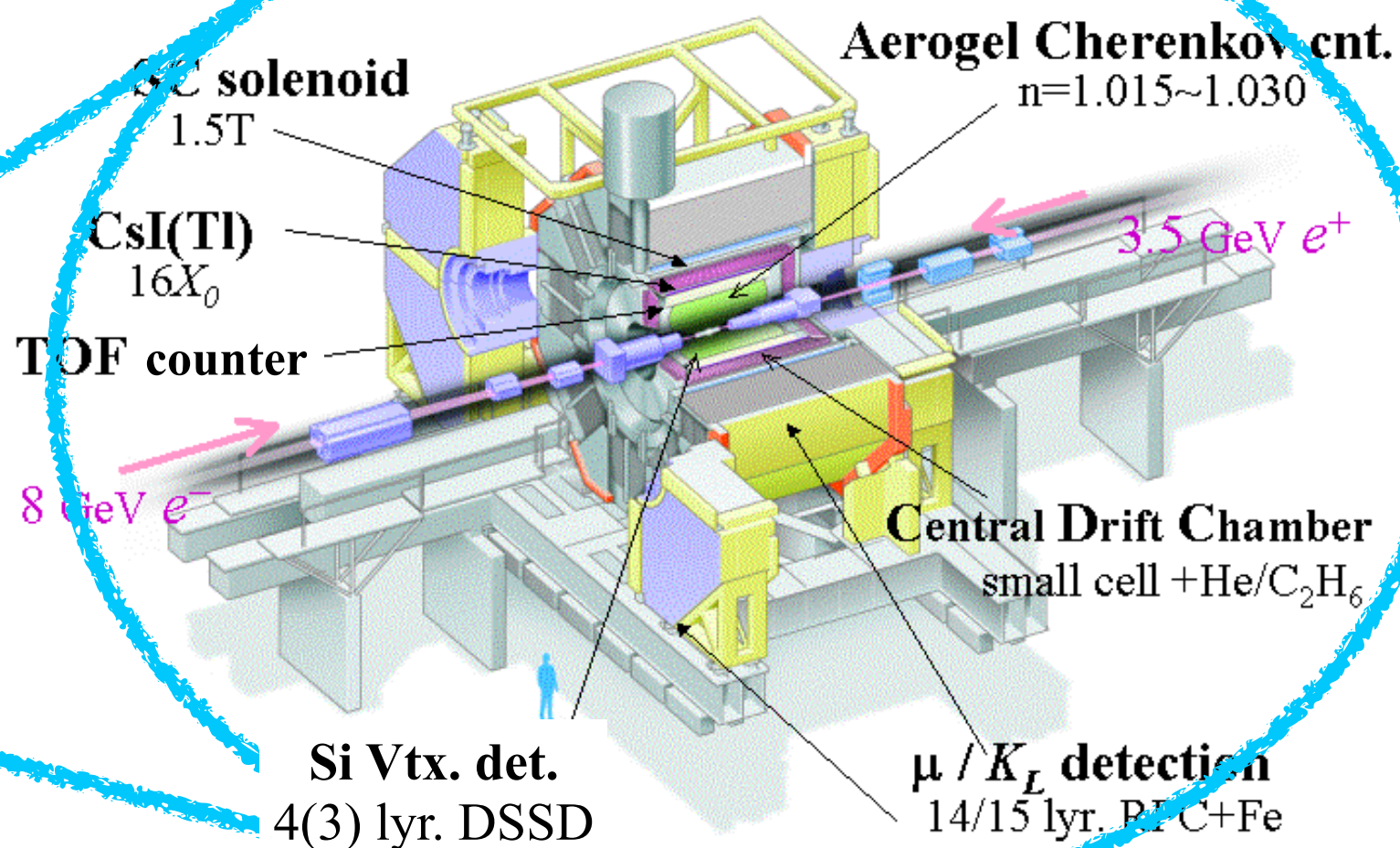
22 countries
100 institutions
~450 members

$$\mathcal{L}_{\text{peak}} = 21.1 \text{ nb}^{-1} \text{s}^{-1}$$



$$e^{-} \xrightarrow{8 \text{ GeV}} (\star) \xleftarrow{3.5 \text{ GeV}} e^{+}$$

Belle Detector



> 1 ab⁻¹

On resonance:

$\Upsilon(5S): 121 \text{ fb}^{-1}$

$\Upsilon(4S): 711 \text{ fb}^{-1}$

$\Upsilon(3S): 3 \text{ fb}^{-1}$

$\Upsilon(2S): 25 \text{ fb}^{-1}$

$\Upsilon(1S): 6 \text{ fb}^{-1}$

Off reson./scan:

$\sim 100 \text{ fb}^{-1}$

$\sim 550 \text{ fb}^{-1}$

On resonance:

$\Upsilon(4S): 433 \text{ fb}^{-1}$

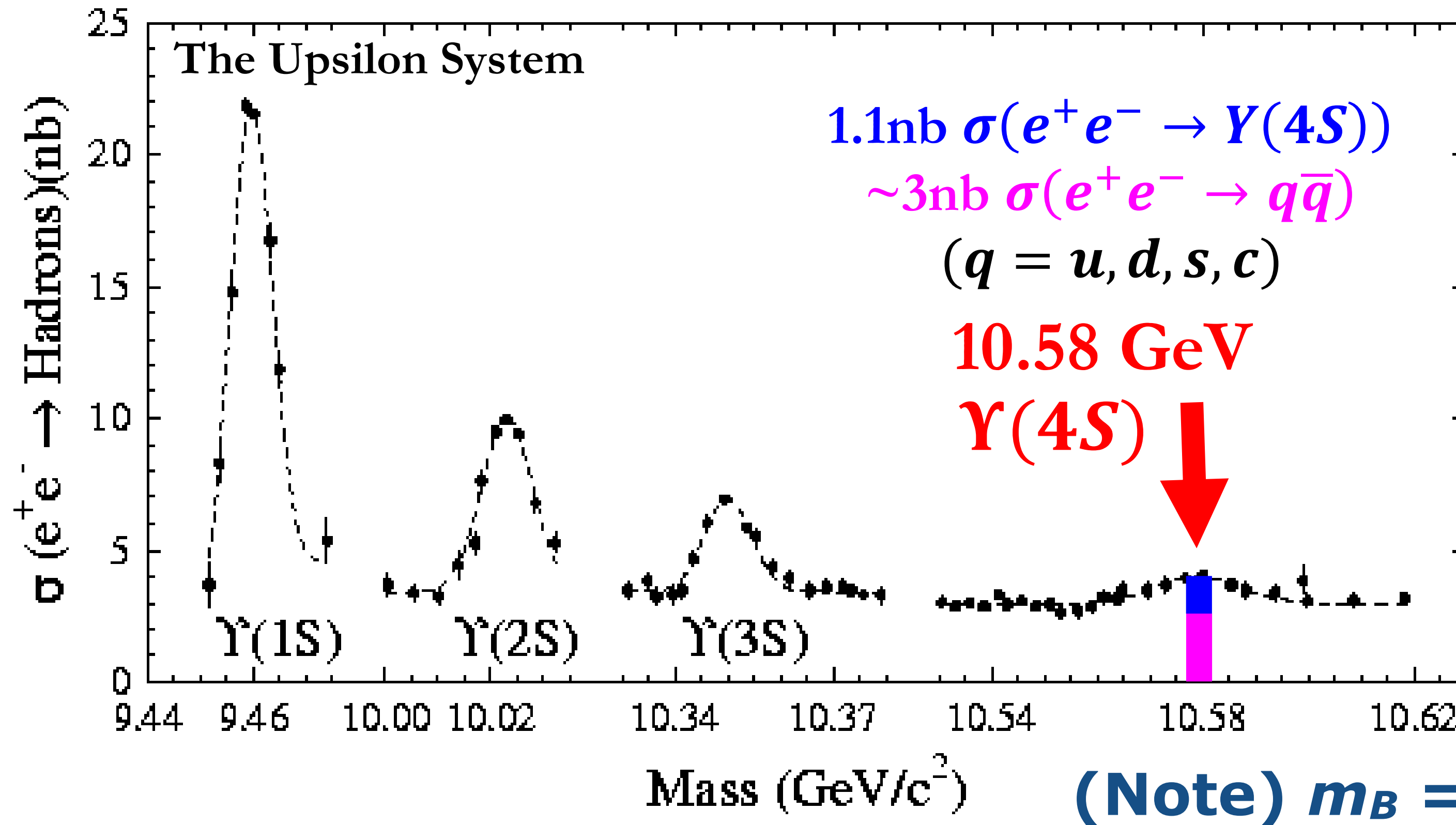
$\Upsilon(3S): 30 \text{ fb}^{-1}$

$\Upsilon(2S): 14 \text{ fb}^{-1}$

Off resonance:

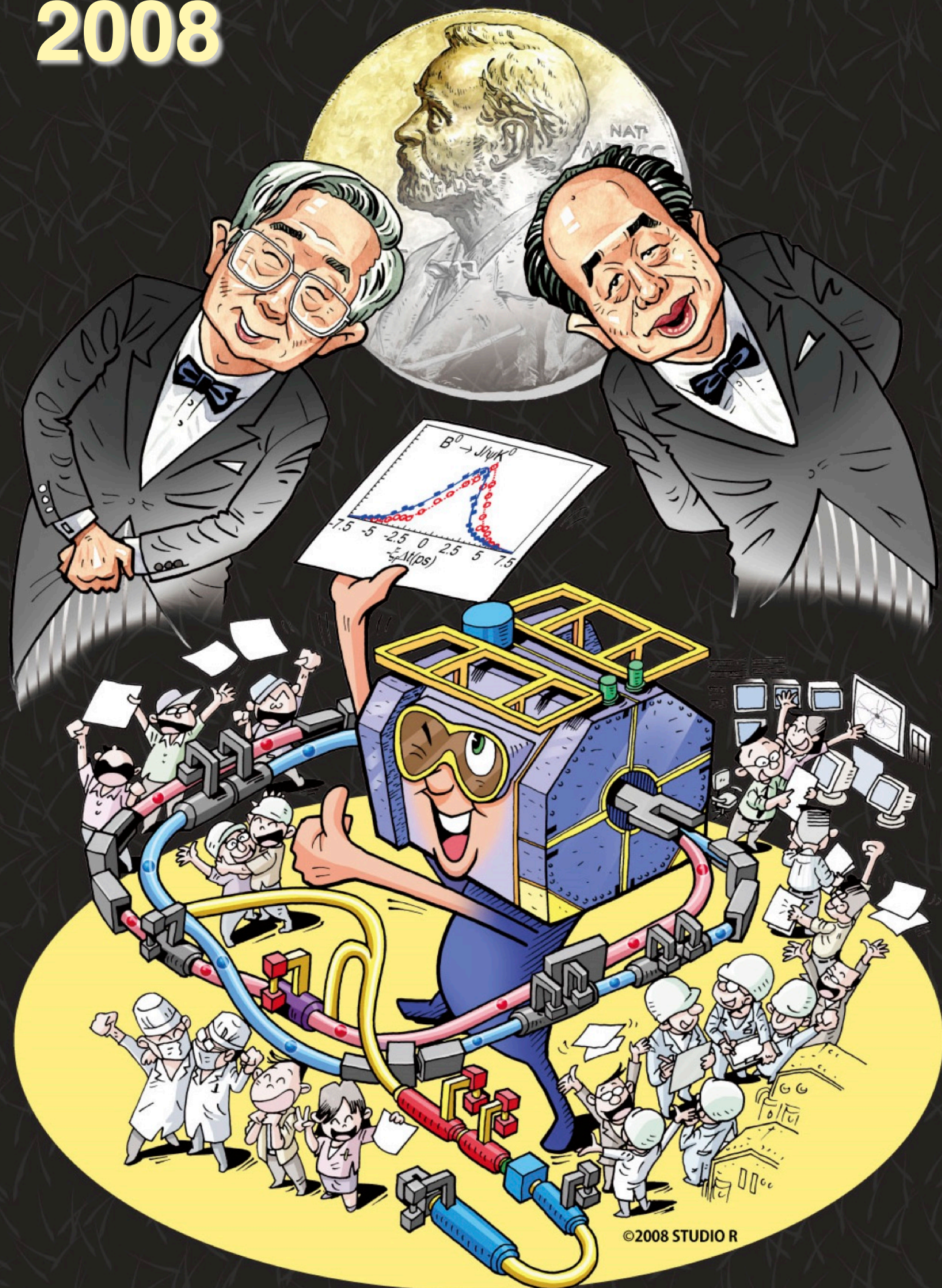
$\sim 54 \text{ fb}^{-1}$

$e^+e^- \rightarrow \Upsilon(4S)$ as a B -factory



- $\mathcal{B}(\Upsilon(4S) \rightarrow B\bar{B}) > 96\%$, with $p_B^{CM} \sim 0.35 \text{ GeV}/c$
- nothing else but $B\bar{B}$ in the final state
- \therefore if we know (E, \vec{p}) of one B , the other B is also constrained

2008



B ファクトリー実験に参加している研究教育機関

ブドカー研究所 チェンナイ数理論科学研 千葉大学
 チョナム大学 シンシナチ大学 イーファ女子大学
 ギーゼン大学 ギョンサン大学 ハワイ大学
 広島工業大学 北京 高能研
 モスクワ 高エネルギー研 モスクワ 理論実験物理研
 カールスルーエ大学 神奈川大学 コリア大学
 クラコウ原子核研 京都大学 キュンボック大学
 ローザンヌ大学 マックスプランク研究所
 ヨセフステファン研究所 メルボルン大学

名古屋大学 奈良女子大学 台湾 中央大学
 台湾 連合大学 台湾大学 日本歯科大学 新潟大学
 ノバゴリカ 科学技術学校 大阪大学 大阪市立大学
 パンジャブ大学 北京大学 ビッツバーク大学
 Belle グループ 高エネルギー加速器研究機構 KEKB グループ
<http://belle.kekb.jp> <http://www.kekb.jp> <http://kekb.jp>

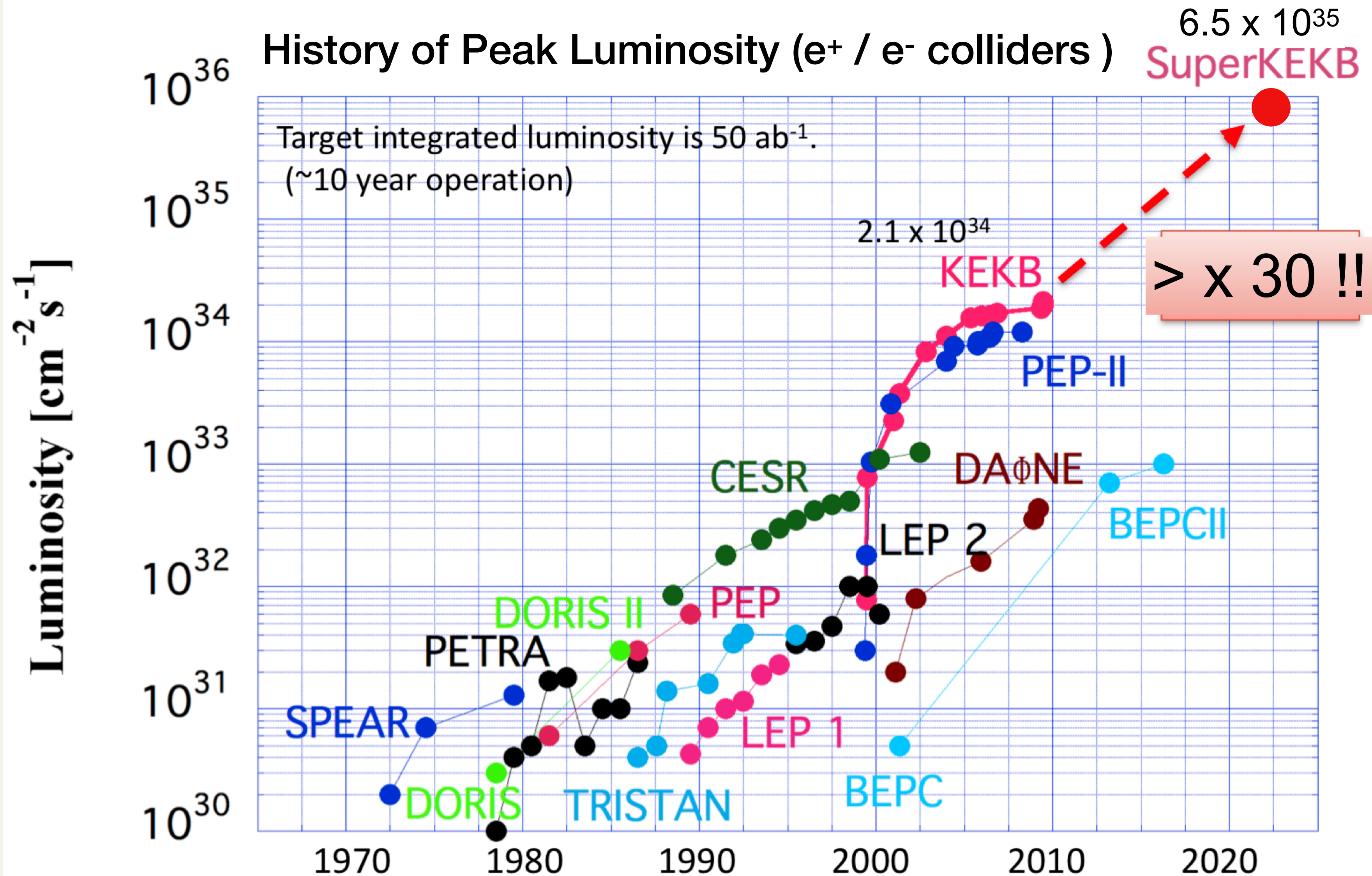
プリンストン大学 理化学研究所 佐賀大学
 中国科学技術大学 ソウル大学 信州大学
 サンキューカン大学 シドニー大学 首都大学東京
 タタ研究所 東邦大学 東北大学 東北学院大学
 東京大学 東京工業大学 東京農工大学
 トリノ 核物理研 富山商船高等専門学校
 ウェイン大学 ウィーン高エネルギー研
 パージニア工科大学 延世大学
 高エネルギー加速器研究機構

Belle (and BaBar, too) achievements include:

- CPV, CKM, and rare decays of B mesons (and B_s , too)
- Mixing, CP, and spectroscopy of charmed hadrons
- Quarkonium spectroscopy and discovery of (*many*) exotic states, e.g. $X(3872)$, $Z_c(4430)^+$
- Studies of τ and 2γ

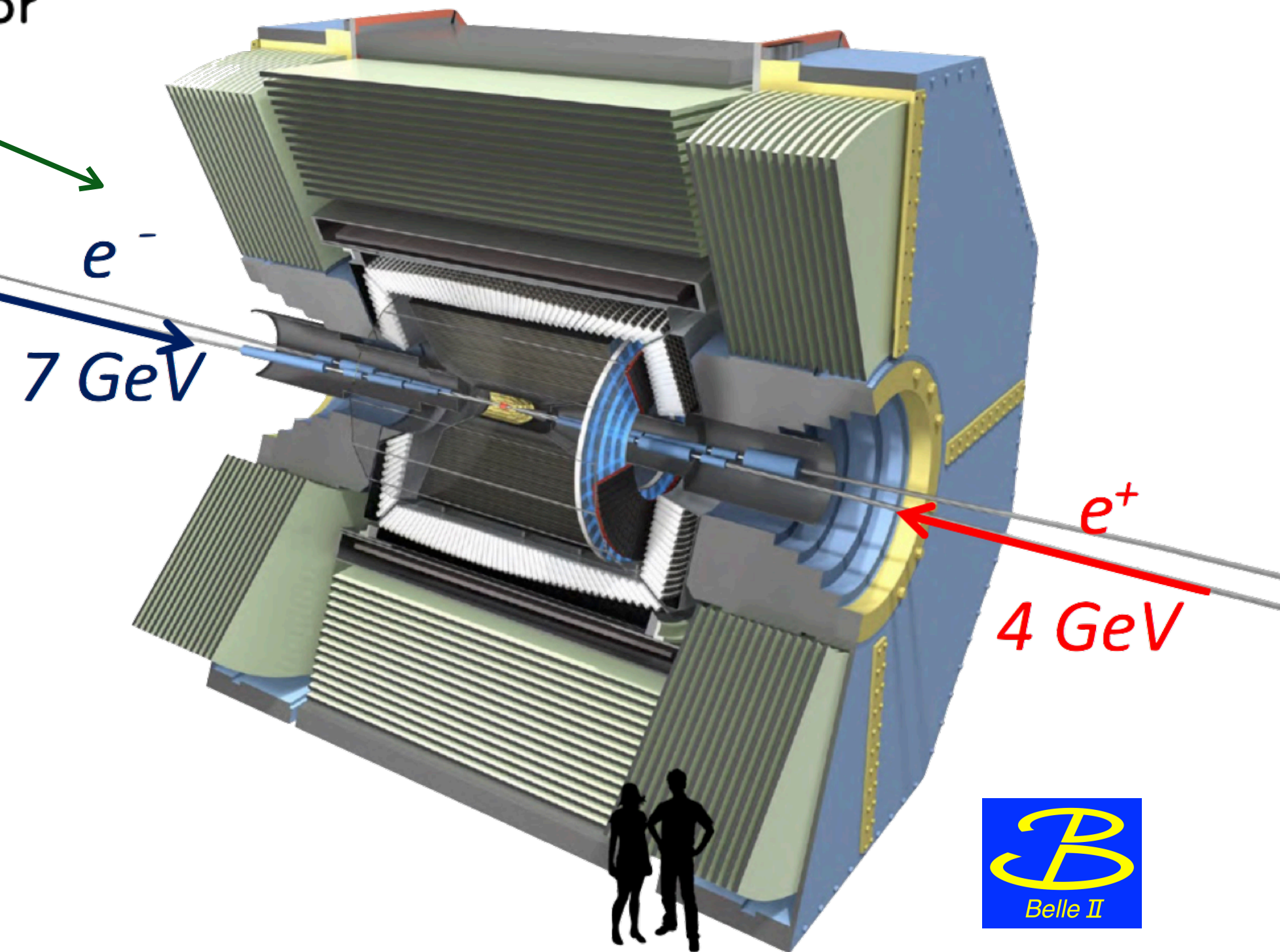
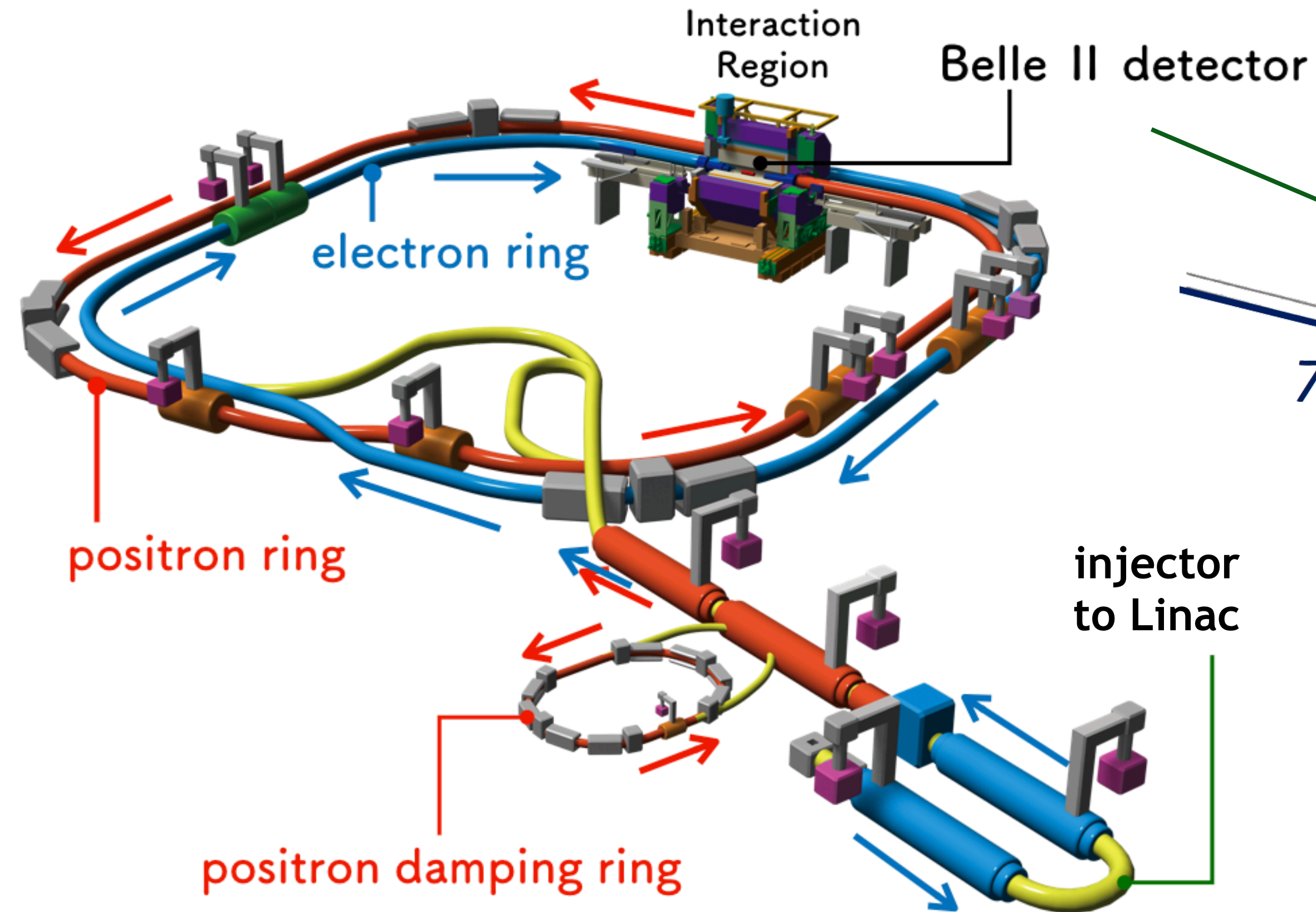


The next Luminosity Frontier



SuperKEKB

Belle II



$$e^- \xrightarrow{7 \text{ GeV}} (\star) \xleftarrow{4 \text{ GeV}} e^+$$

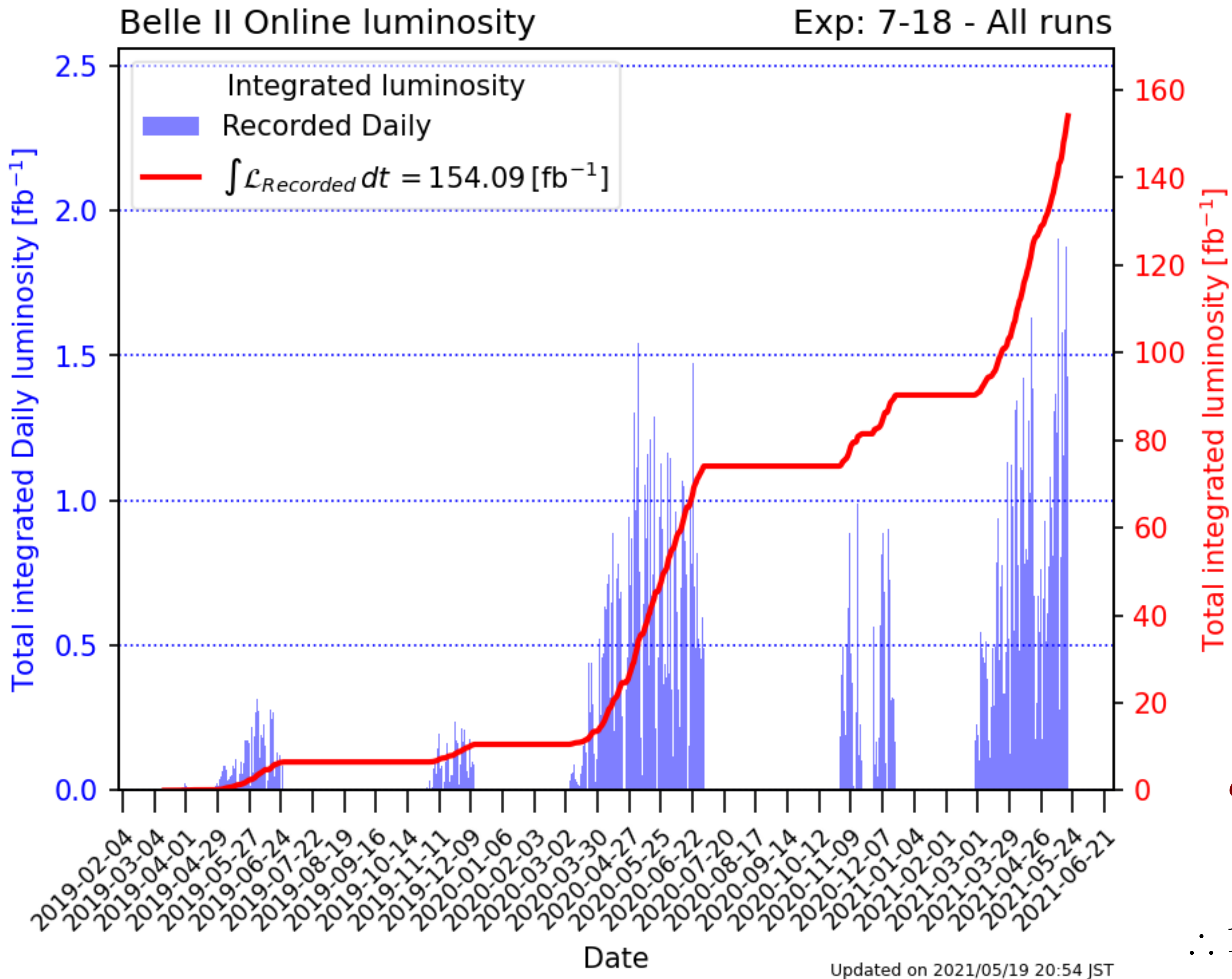
$$\mathcal{L} = 6.5 \times 10^{35} \text{ cm}^{-2} \text{ s}^{-1}$$

$$\int^{\text{goal}} \mathcal{L} dt = 50 \text{ ab}^{-1}$$

The Belle II Collaboration



26 countries/regions, ~120 institutions, ~1000 collaborators



$$\sigma \int \mathcal{L} dt = N(\text{events})$$

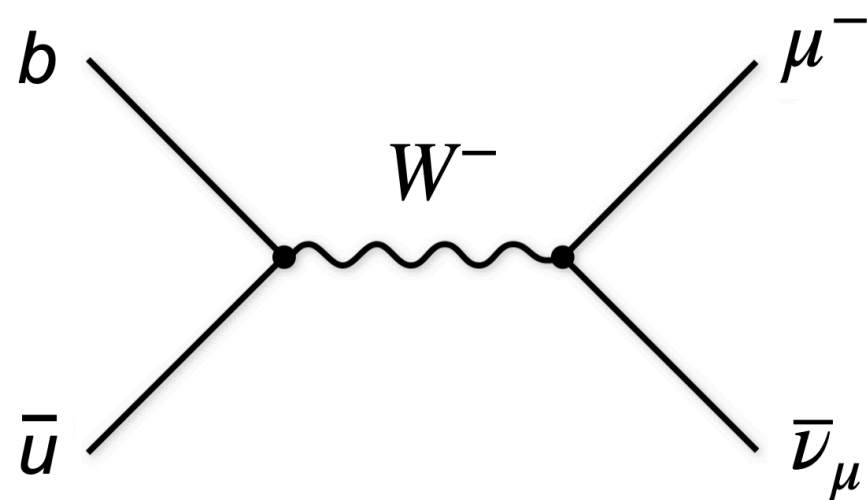
$$\sigma_{B\bar{B}} \simeq 1 \text{ nb}$$

$$\therefore 1 \text{ fb}^{-1} \sim 10^6 B\bar{B} \text{ events}$$

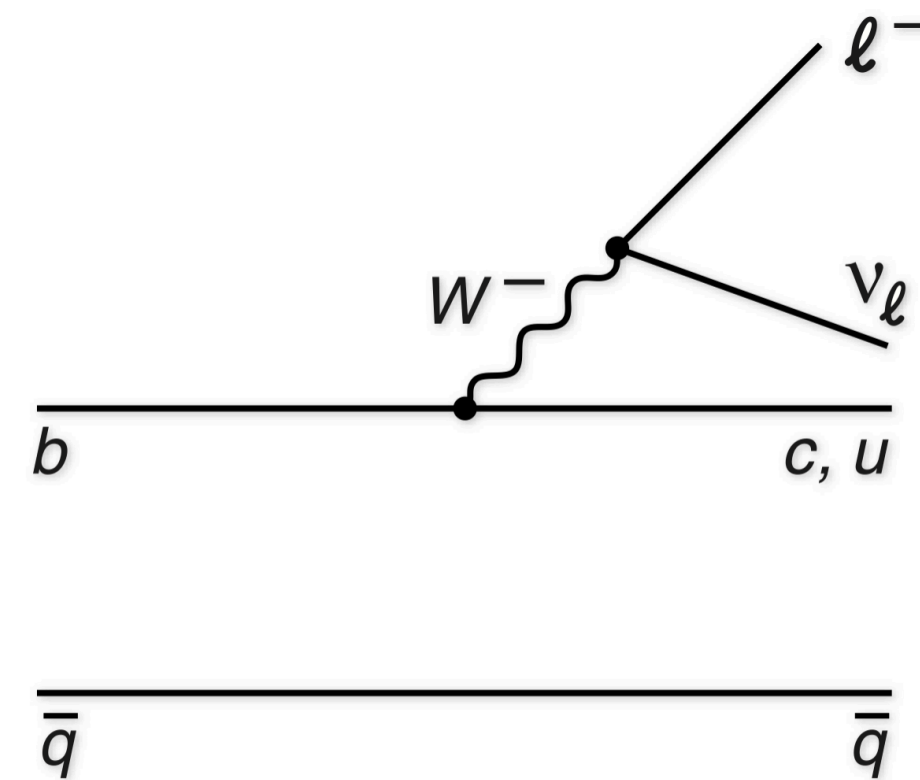
Processes with $W^+ \rightarrow \ell^+ \nu_\ell$

(a) $B^+ \rightarrow \ell^+ \nu_\ell$ and beyond (“leptonic”)

(b) $B^+ \rightarrow X_q \ell^+ \nu_\ell$ (“semileptonic”)



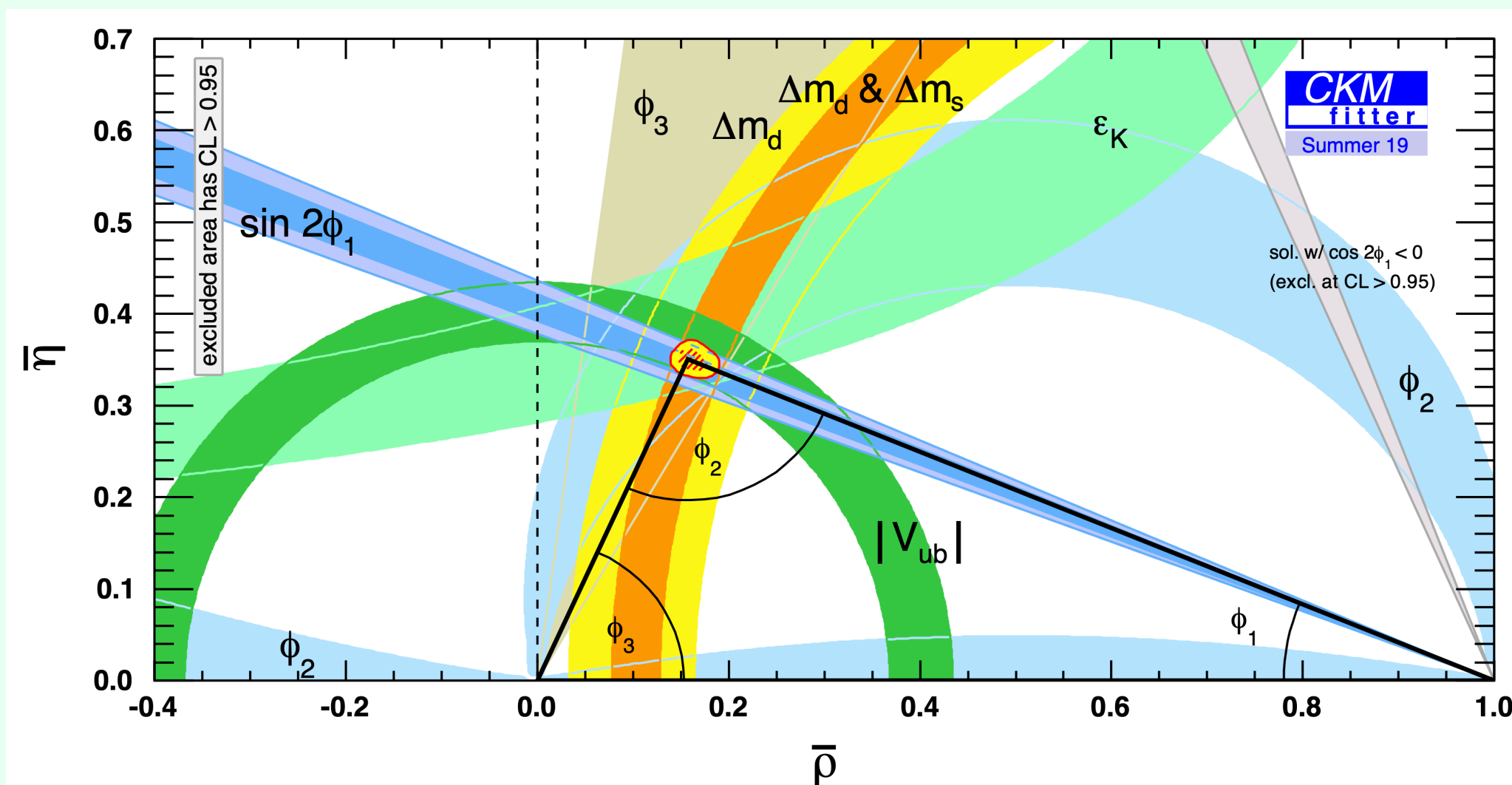
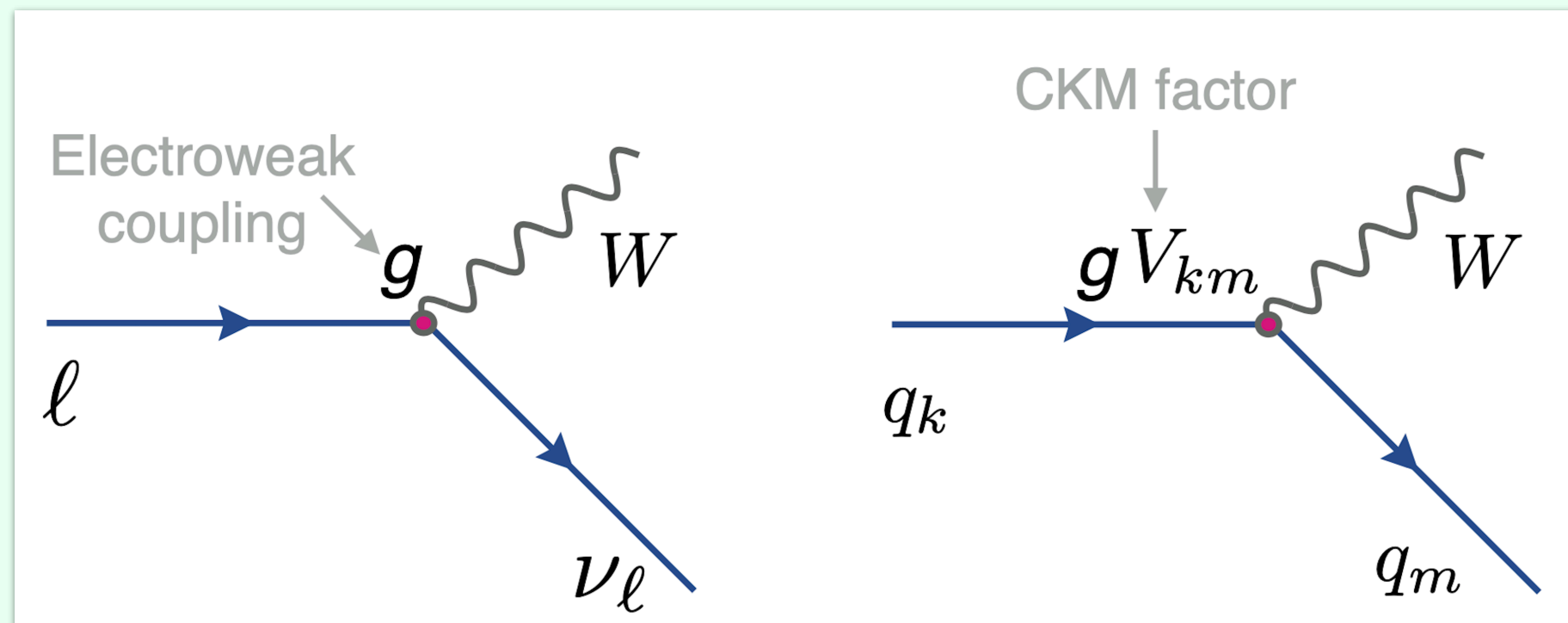
(a) Leptonic



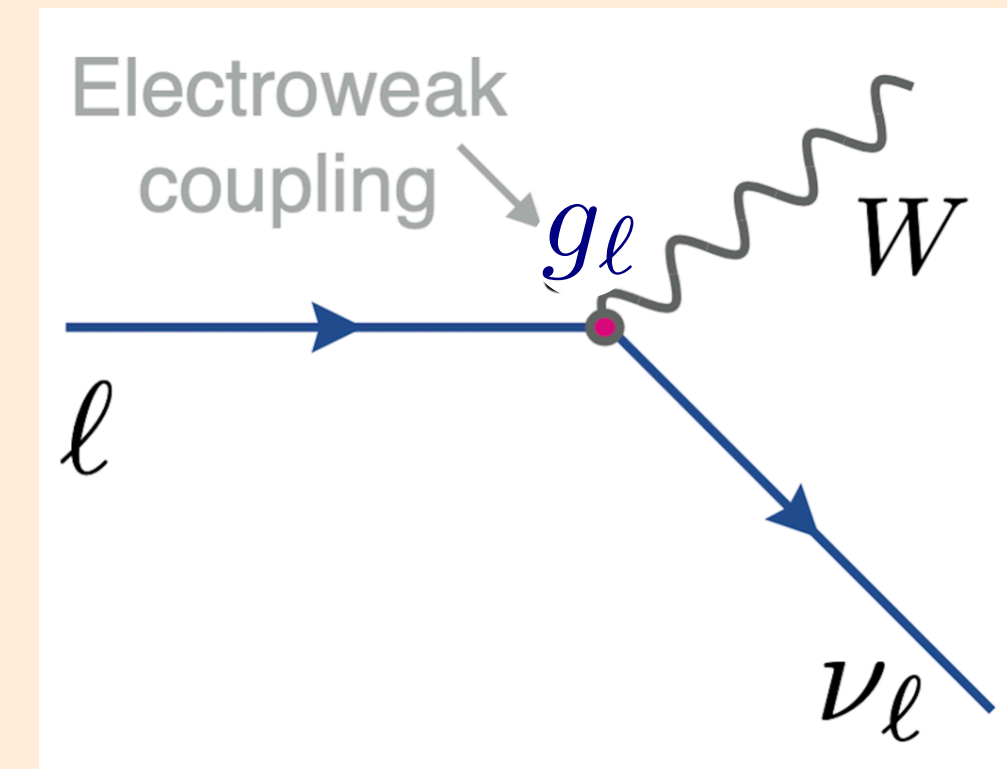
(b) Semileptonic

1-page summary of semileptonic decays

Precision measurements of CKM UT



Test of lepton universality in $R(D^{(*)})$



$$g_l \quad (\ell = e, \mu, \tau)$$

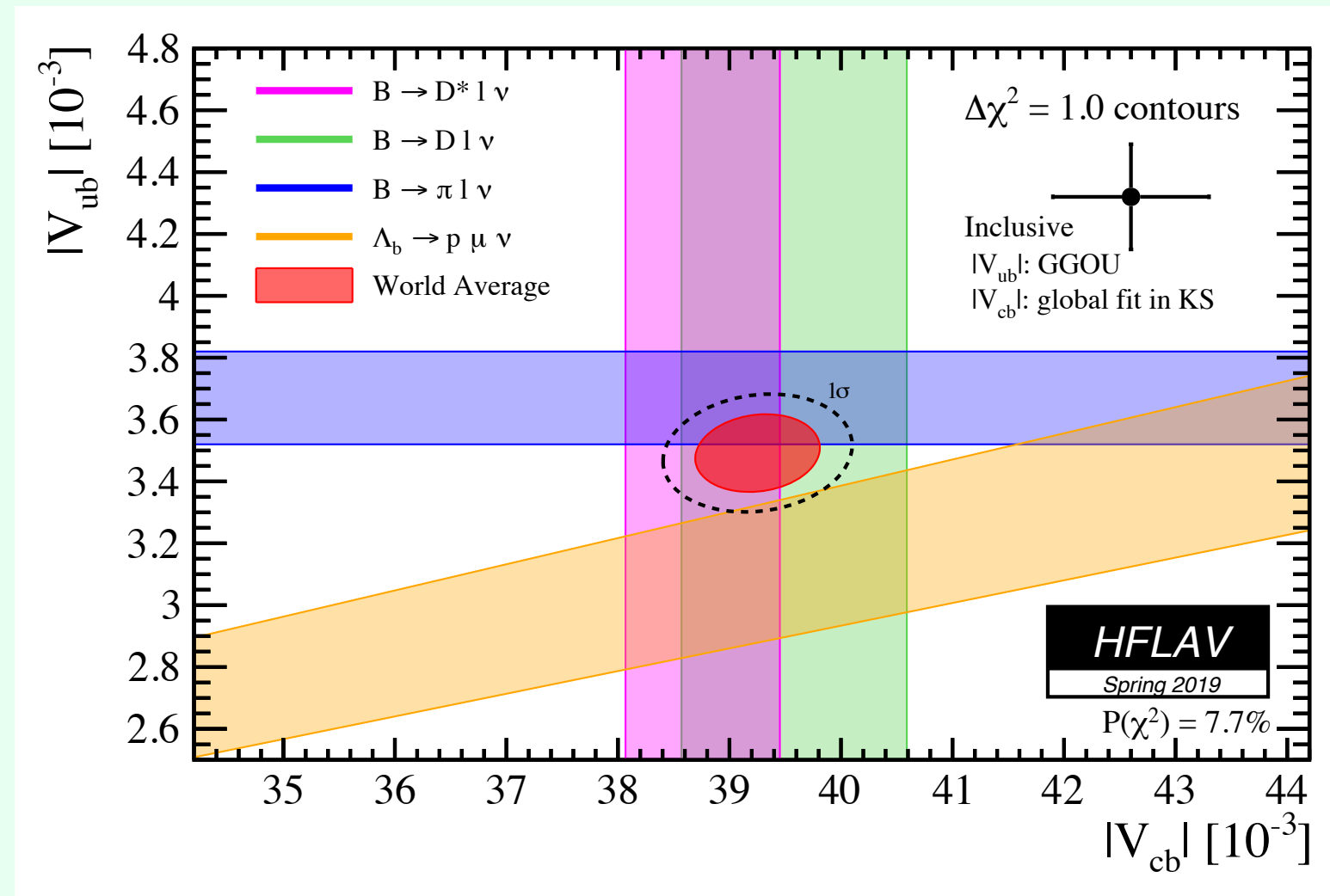
Is $g_\tau = g_\mu$, and/or g_e ?

$$R(D^{(*)}) \equiv \frac{\mathcal{B}(B \rightarrow D^{(*)} \tau^+ \nu)}{\mathcal{B}(B \rightarrow D^{(*)} \ell^+ \nu)}$$

1-page summary of semileptonic decays

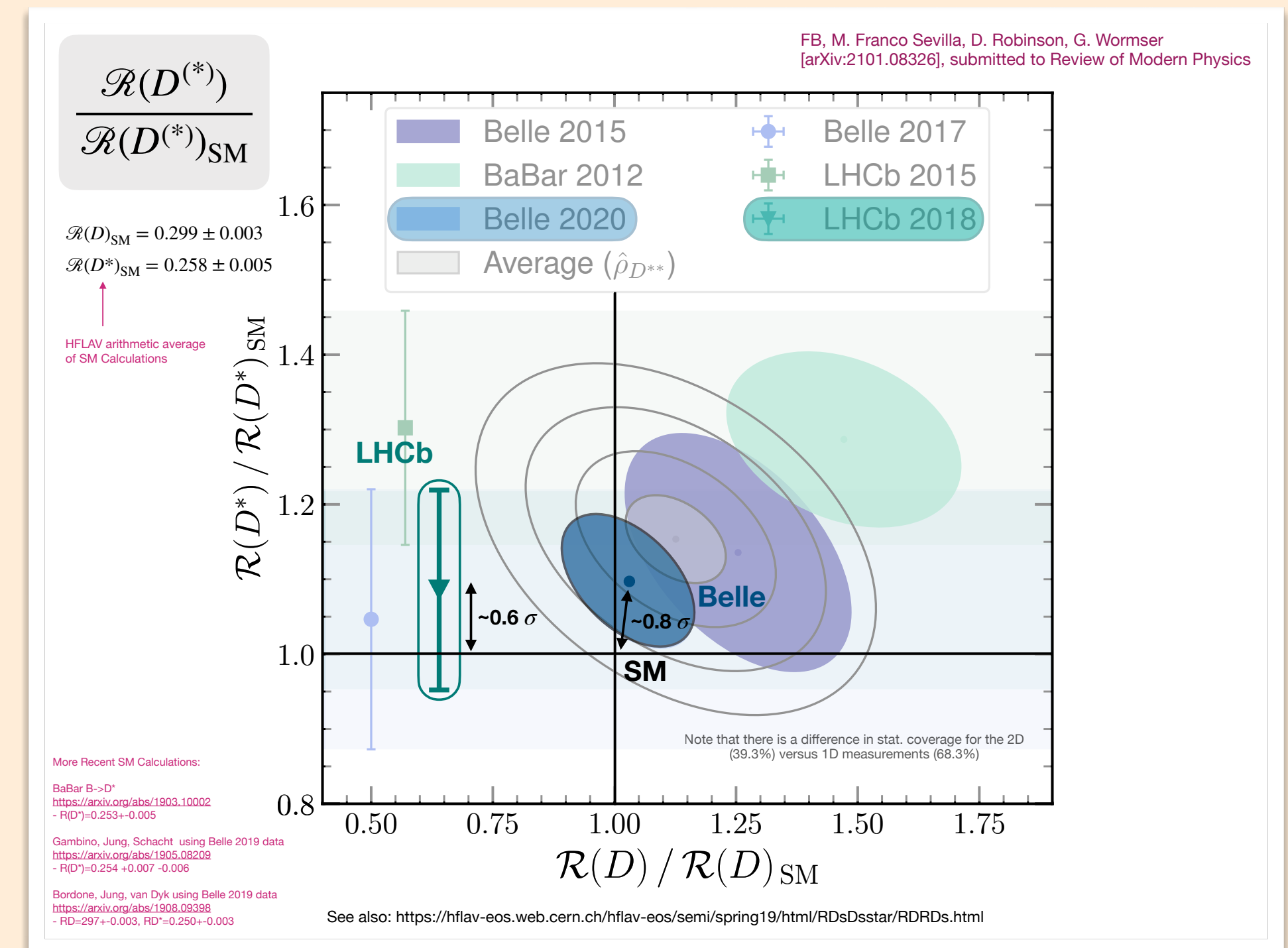
Precision measurements of CKM UT

- a tension of Inclusive vs. Exclusive?



- arXiv:2101.00020 for $|V_{ub}|$ inclusive
a “Belle masterpiece” by Uni. Bonn group

Test of lepton universality in $R(D^{(*)})$



from Florian Bernlochner's talk @ APS 2021

FB, M. Franco Sevilla, D. Robinson, G. Wormser
[arXiv:2101.08326], submitted to Review of Modern Physics



Youngjoon Kwon

February 19 · 👤

gave a journal club seminar @ KIAS today,
presenting a most recent Belle masterpiece by the respected
colleagues, Florian Bernlochner et al.
<https://arxiv.org/abs/2102.00020>

$B^+ \rightarrow \ell^+ \nu_\ell$, features & motivations

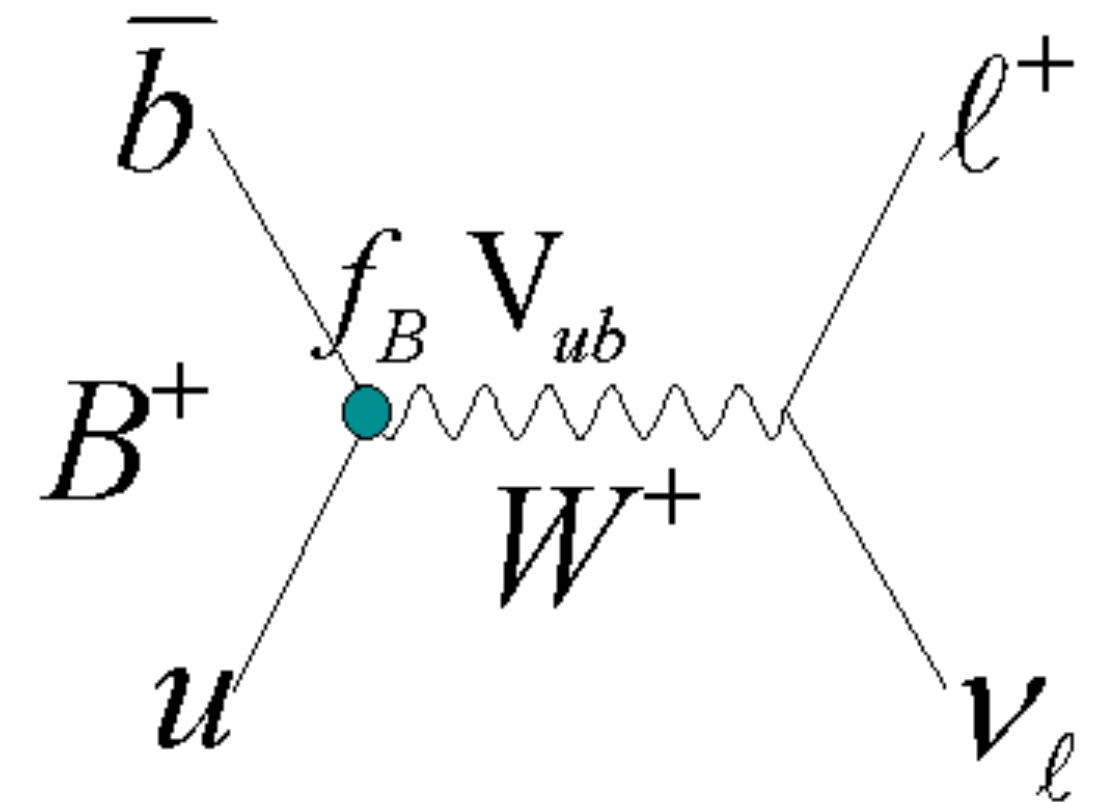
● SM predictions

$$\Gamma(B^+ \rightarrow \ell^+ \nu) = \frac{G_F^2 m_B m_\ell^2}{8\pi} \left(1 - \frac{m_\ell^2}{m_B^2}\right)^2 f_B^2 |V_{ub}|^2$$

$$\mathcal{B}(B^+ \rightarrow \tau^+ \nu) \sim 10^{-4}$$

$$\mathcal{B}(B^+ \rightarrow \mu^+ \nu) \sim \mathcal{B}(B^+ \rightarrow \tau^+ \nu)/300$$

$$\mathcal{B}(B^+ \rightarrow e^+ \nu) \sim \mathcal{B}(B^+ \rightarrow \tau^+ \nu)/10^7$$



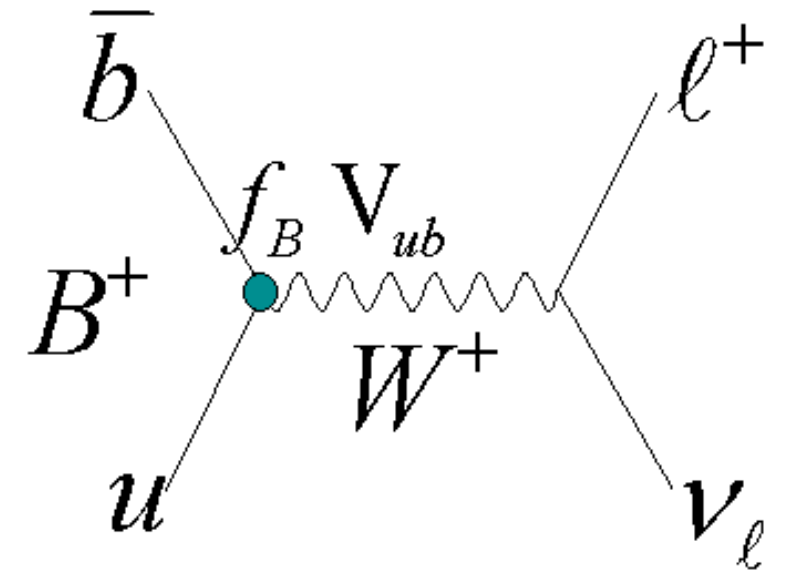
● Experimental features

- $B^+ \rightarrow \tau^+ \nu_\tau$ large BF, but multiple ν 's
- $B^+ \rightarrow \ell^+ \nu_\ell$ ($\ell \neq \tau$) $E_\ell \sim m_B/2$, but very small BF

$B^+ \rightarrow \ell^+ \nu_\ell$, features & motivations

● SM predictions

$$\Gamma(B^+ \rightarrow \ell^+ \nu) = \frac{G_F^2 m_B m_\ell^2}{8\pi} \left(1 - \frac{m_\ell^2}{m_B^2}\right)^2 f_B^2 |V_{ub}|^2$$



● Motivations

- very clean place to **measure** $f_B |V_{ub}|$, and/or **search for new physics** (e.g. H^+ or LQ)

- **ultimate test of LUV** $\frac{\Gamma(B^+ \rightarrow \ell^+ \nu)}{\Gamma(B^+ \rightarrow \tau^+ \nu)} = f(m_\ell^2, m_\tau^2)$ *and all other parameters cancel!*

- Belle has measured $B^+ \rightarrow e^+ \nu$, $\mu^+ \nu$ with both inclusive tag [PLB 647, 67 (2007)] and hadronic tag [PRD 91, 052016 (2015)] and updated $B^+ \rightarrow \mu^+ \nu$ with inclusive tagging [PRL 121, 031801 (2018), and PRD 101, 032007 (2020)].

$B^+ \rightarrow \ell^+ \nu_\ell$, ‘to Tag or not to Tag’

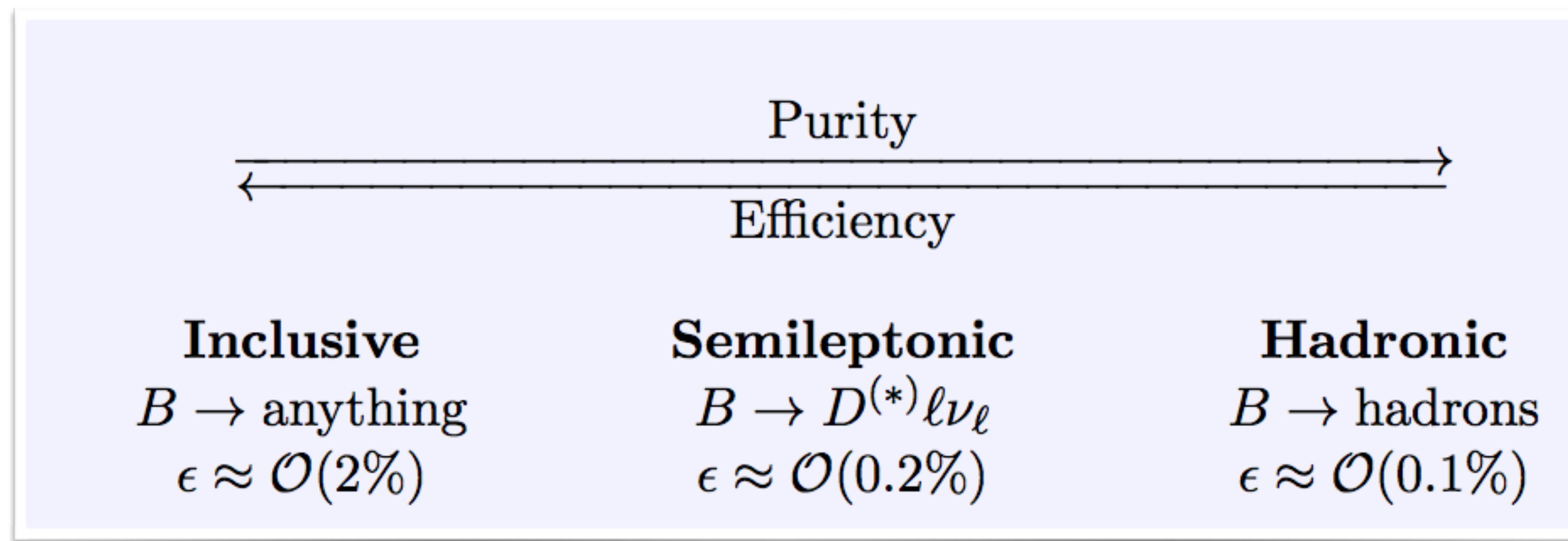
● Why bother?

- missing $\nu(s)$ in the final state
- need extra kinematic constraints to improve sensitivity
- exploit $\Upsilon(4S)$ producing $B\bar{B}$ and nothing else

$$e^+e^- \rightarrow \Upsilon(4S) \rightarrow B_{\text{sig}}\bar{B}_{\text{tag}}$$

● How to tag?

- “hadronic tagging” — reconstruction of the full decay chain of B_{tag} in hadronic modes
- “semileptonic tagging” — use semileptonic B_{tag} decays, e.g. $B_{\text{tag}} \rightarrow \bar{D}^{(*)}\ell^+\nu$



$B^+ \rightarrow \ell^+ \nu_\ell$, ‘to Tag or not to Tag’

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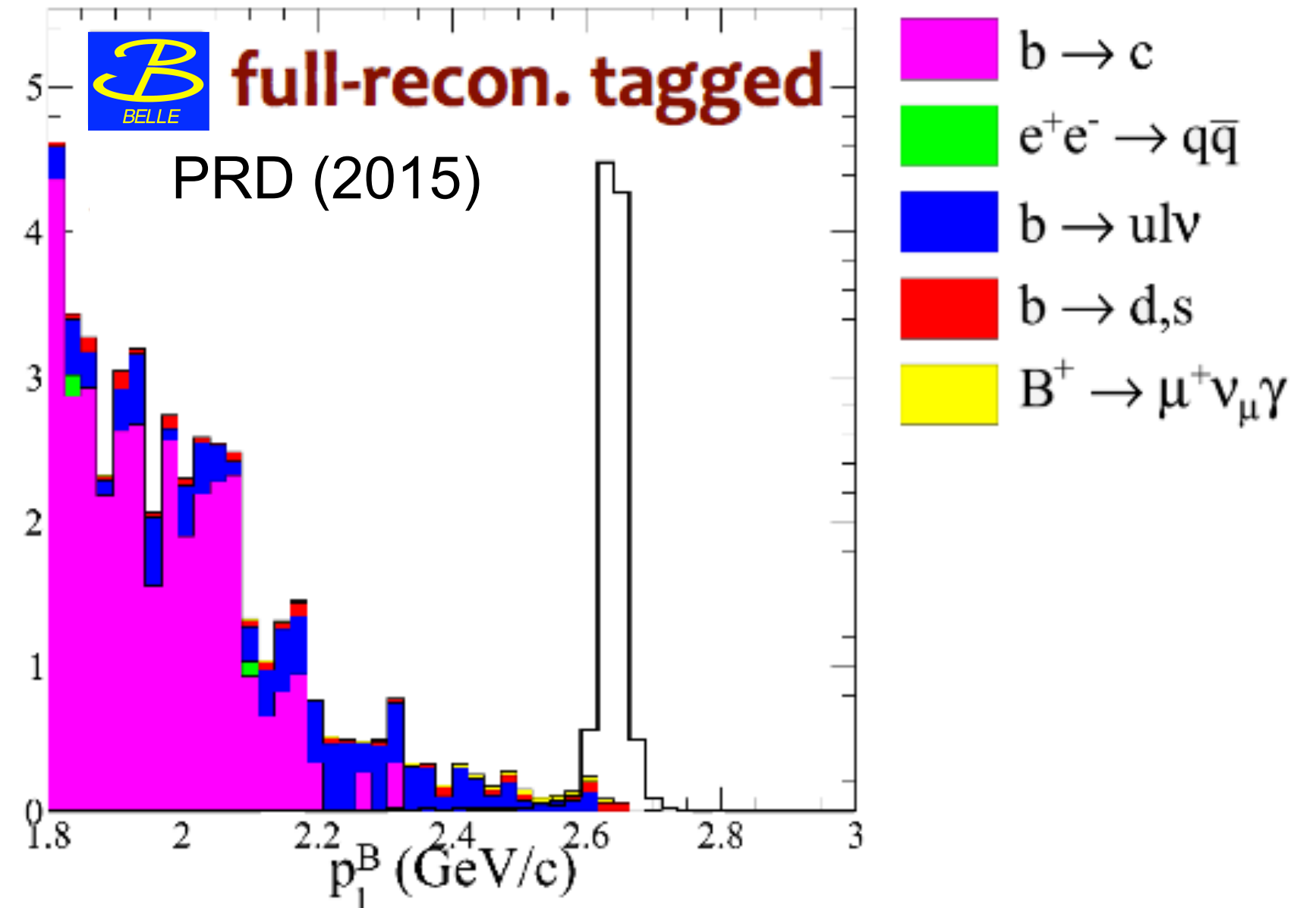
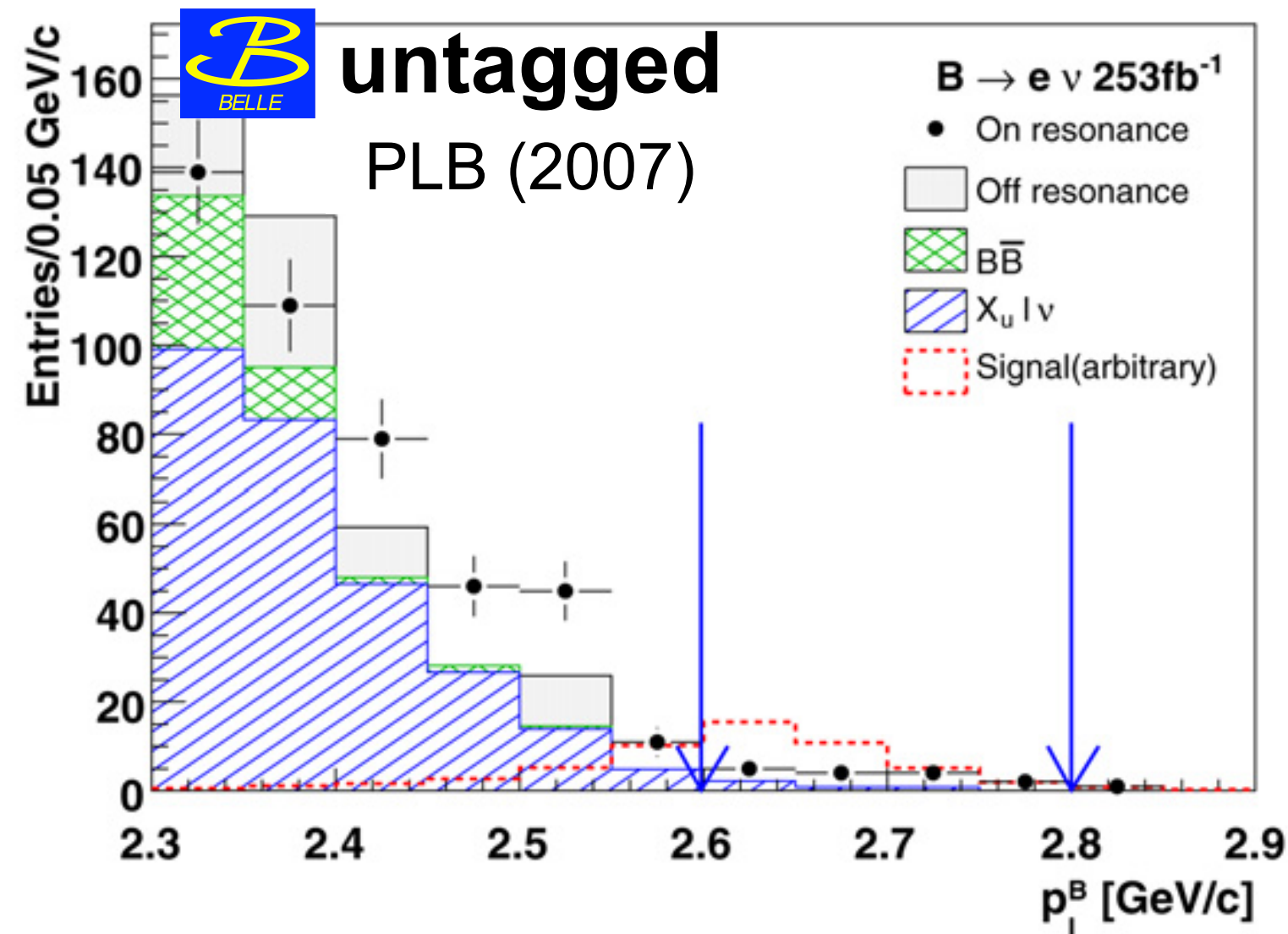
Tagged vs. Untagged for $B^+ \rightarrow \ell^+ \nu_\ell$ ($\ell \neq \tau$)

- tagging is not really necessary \because mono-energetic ℓ^+ in the final state
- Nonetheless, analyses with tagging have also been tried

<div> <div>← Purity →</div> <div>← Efficiency →</div> </div>		
Inclusive $B \rightarrow \text{anything}$ $\epsilon \approx \mathcal{O}(2\%)$	Semileptonic $B \rightarrow D^{(*)}\ell\nu_\ell$ $\epsilon \approx \mathcal{O}(0.2\%)$	Hadronic $B \rightarrow \text{hadrons}$ $\epsilon \approx \mathcal{O}(0.1\%)$

$B^+ \rightarrow \ell^+ \nu_\ell$, why bother with tagging?

signal lepton candidate's momentum in the B_{sig} rest frame



- much better resolution of p_ℓ^B with the full-recon. tagging
- But, does it make a case for ‘full-recon tagging’ analysis of $B^+ \rightarrow \ell^+ \nu_\ell$?

$B^+ \rightarrow \ell^+ \nu_\ell$, why bother with tagging?

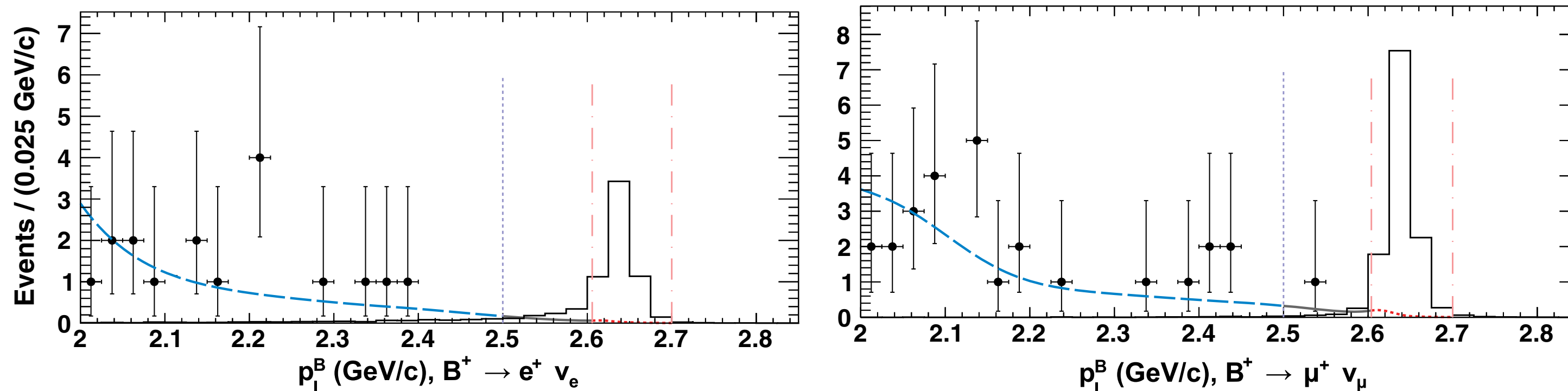
- Note: $\mathcal{B}_{\text{SM}}(B^+ \rightarrow e^+ \nu_e) \sim 10^{-11}$ and $\mathcal{B}_{\text{SM}}(B^+ \rightarrow \mu^+ \nu_\mu) \sim 3 \times 10^{-7}$
 \rightarrow any signal for $B^+ \rightarrow e^+ \nu_e$ at the Belle (II) sensitivity is way beyond the SM
- In that case, are we sure what we see is really $B^+ \rightarrow e^+ \nu_e$?
 What about $B^0 \rightarrow e^+ \tau^-$? Or, $B^+ \rightarrow e^+ X^0$ where X^0 is any invisible particle from NP, e.g. sterile ν ?
- With full-recon, we can use p_ℓ^B to discern many such cases

PHYSICAL REVIEW D **91**, 052016 (2015)

Search for $B^+ \rightarrow e^+ \nu_e$ and $B^+ \rightarrow \mu^+ \nu_\mu$ decays using hadronic tagging

Y. Yook,⁷⁰ Y.-J. Kwon,⁷⁰ A. Abdesselam,⁵⁸ I. Adachi,¹² S. Al Said,^{58,27} K. Arinstein,⁴ D. M. Asner,⁴⁹ V. Aulchenko,⁴
 T. Aushev,²² R. Avad,⁵⁸ S. Bahinipati,¹⁵ A. M. Bakich,⁵⁷ A. Bala,⁵⁰ V. Bansal,⁴⁹ V. Bhardwaj,⁴¹ R. Bhuvan,¹⁶ A. Bondar,⁴

Belle analysis with hadronic B -tagging

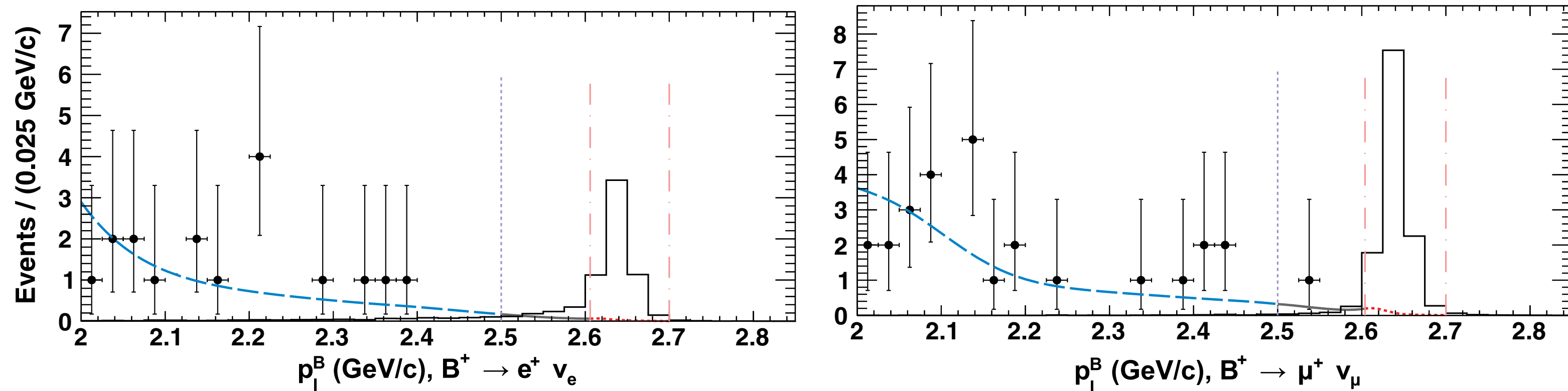


$B^+ \rightarrow \ell^+ \nu_\ell$, why bother with tagging?

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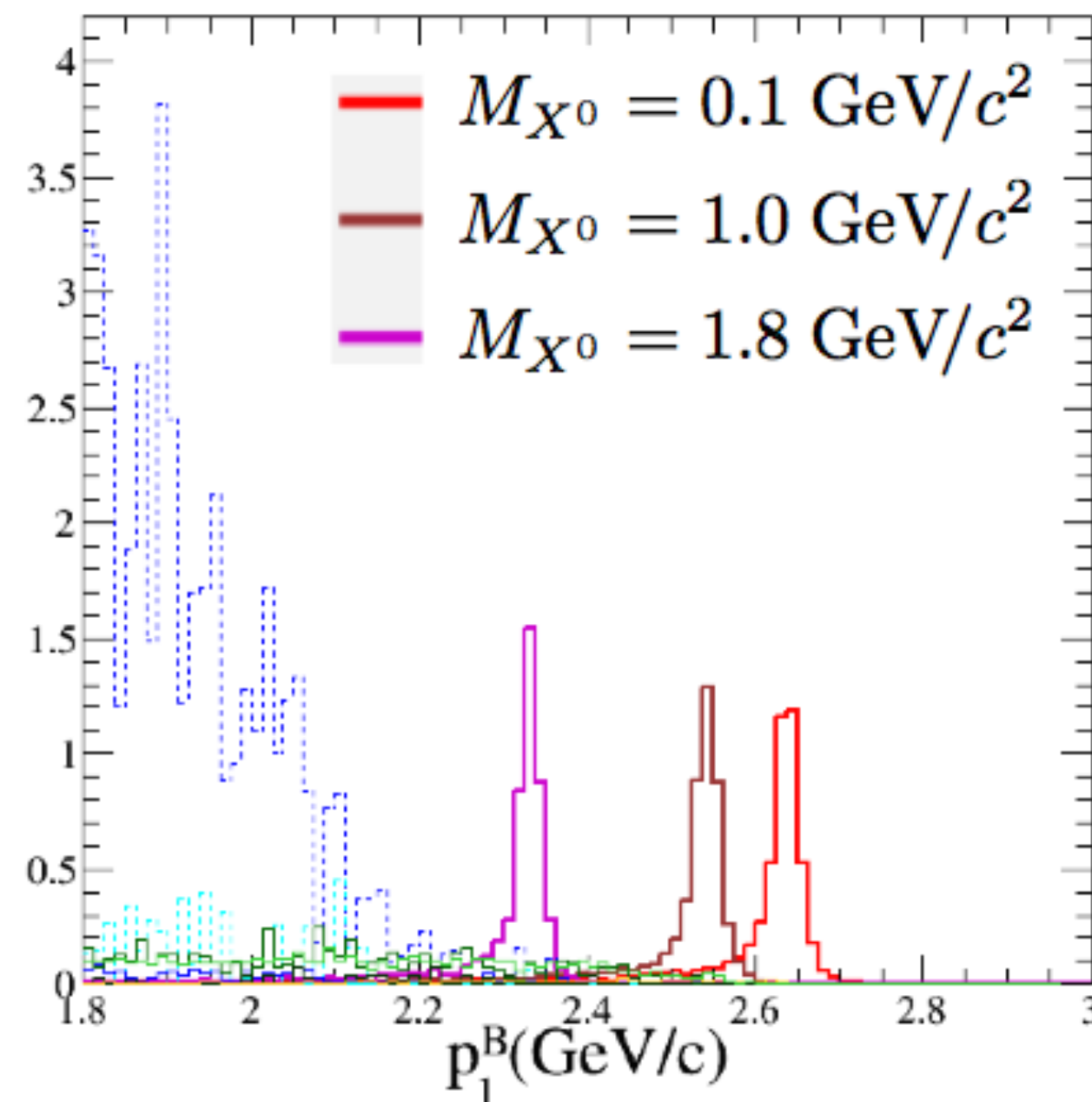
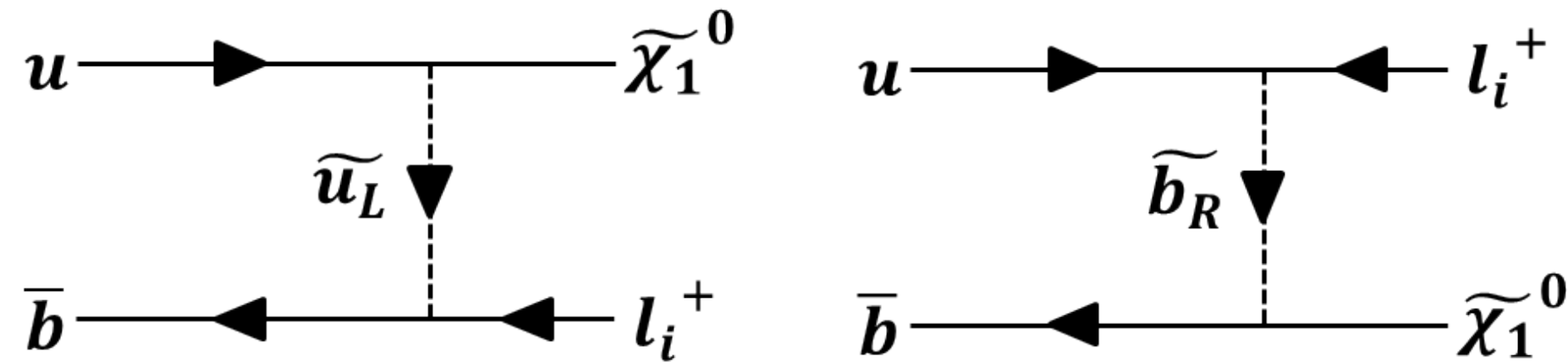
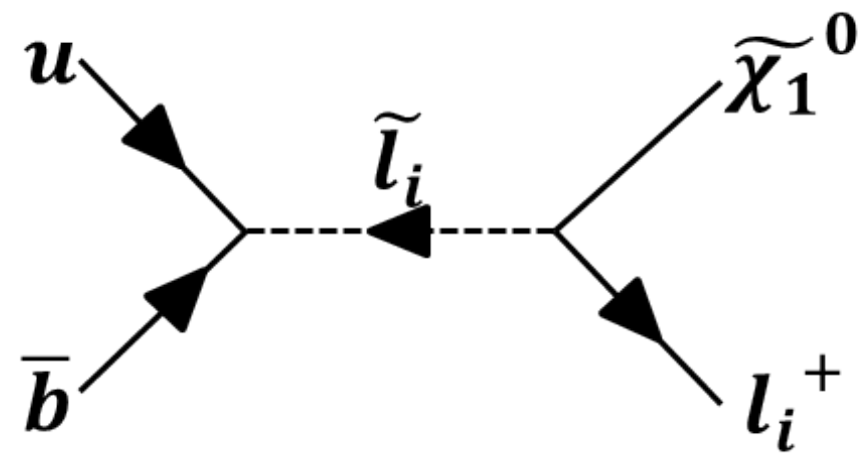
Belle analysis with hadronic B -tagging

PRD 91, 052016 (2015)



Mode	ϵ_s [%]	N_{obs}	$N_{\text{exp}}^{\text{bkg}}$	\mathcal{B} (in 10^{-6})
$B^+ \rightarrow e^+ \nu_e$	0.086 ± 0.007	0	0.10 ± 0.04	< 3.5
$B^+ \rightarrow \mu^+ \nu_\mu$	0.102 ± 0.008	0	$0.26^{+0.09}_{-0.08}$	< 2.7

$B^+ \rightarrow \ell^+ X^0$, why not?



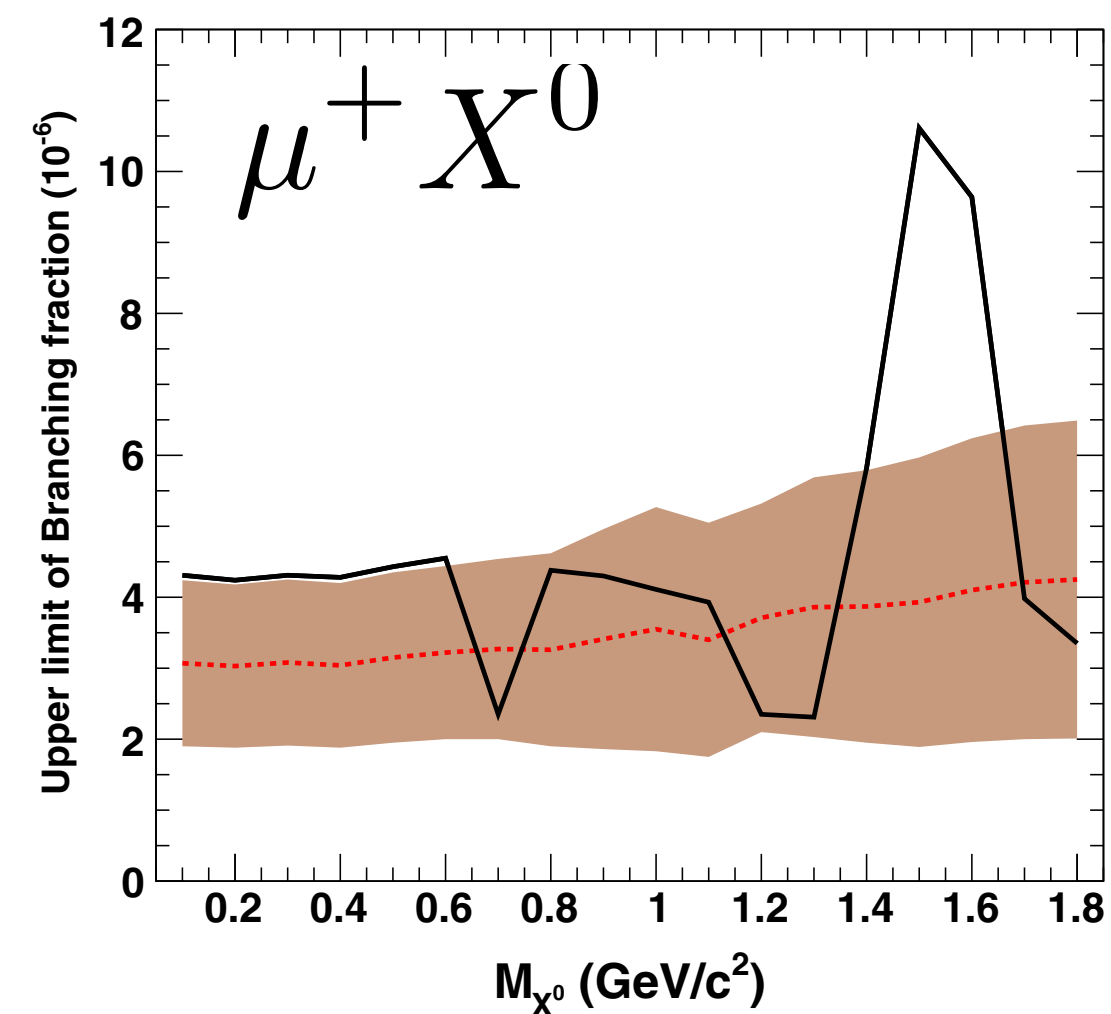
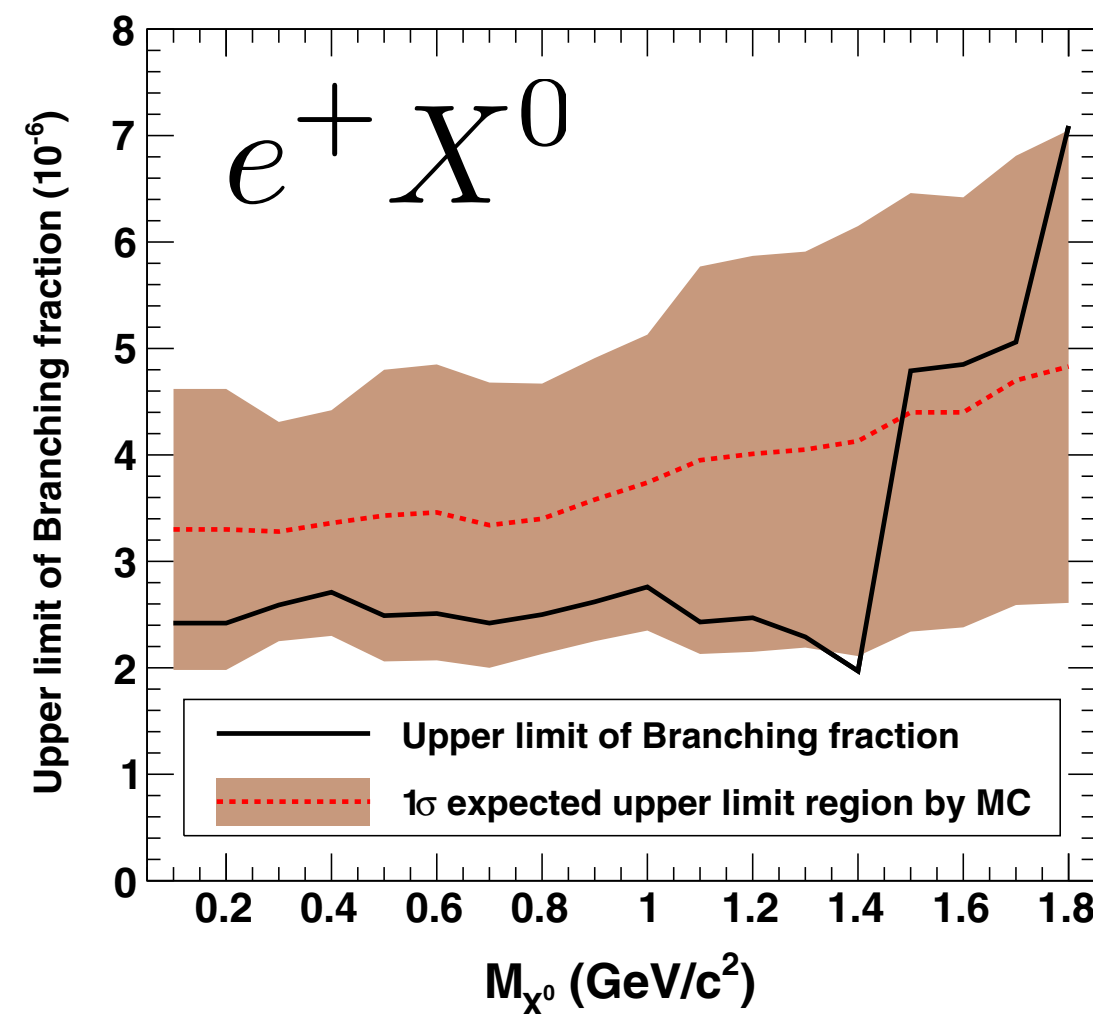
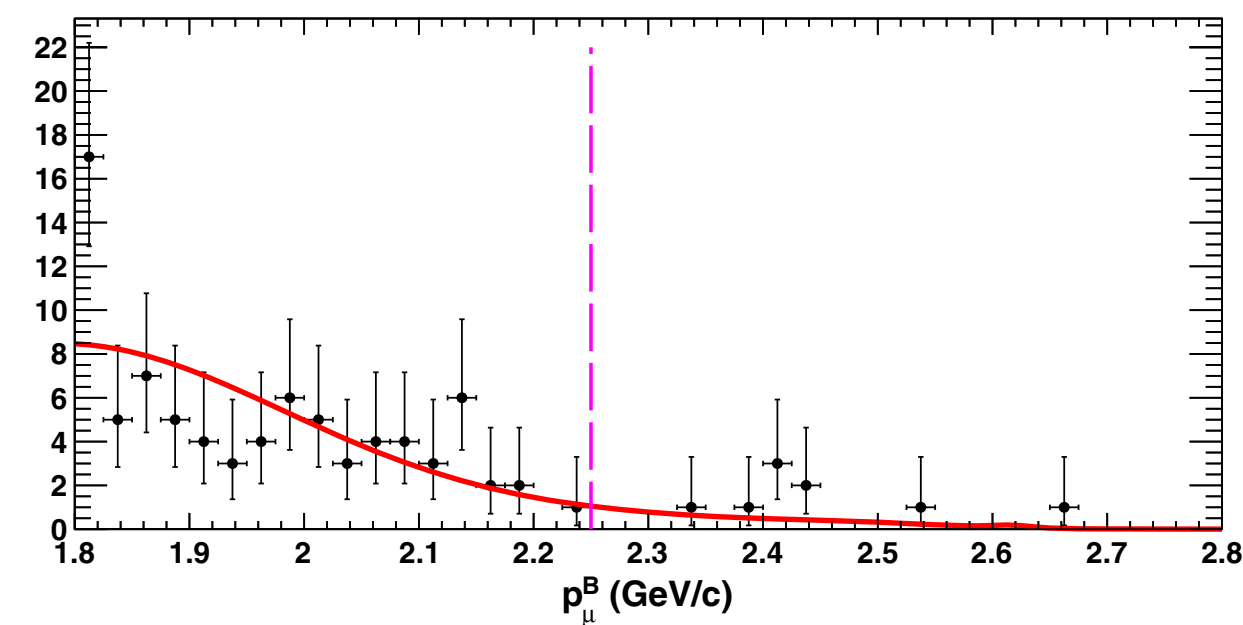
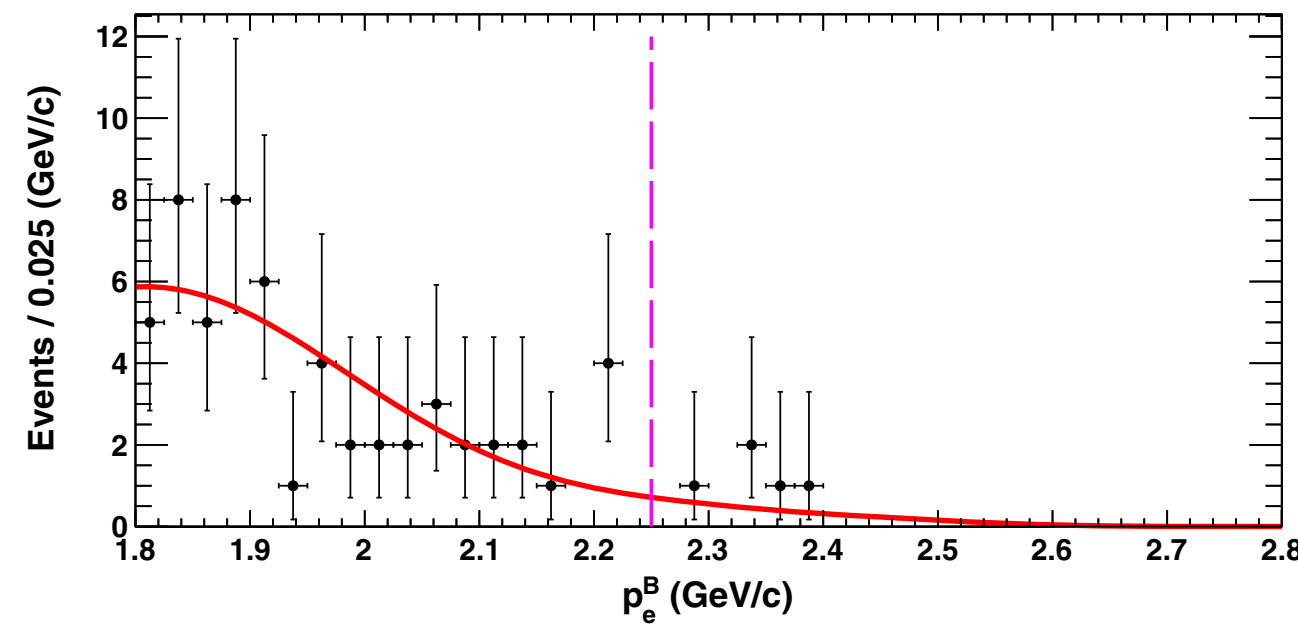
- Search for massive neutral invisible fermion “ X^0 ”
a heavy neutrino, or an LSP in RPV models, or whatever
- Experimental signature, very similar to $B^+ \rightarrow \ell^+ \nu_\ell$
- But, p_ℓ^B provides a handle on m_{X^0}

$B^+ \rightarrow \ell^+ X^0$ search at Belle

PHYSICAL REVIEW D **94**, 012003 (2016)

Search for a massive invisible particle X^0 in $B^+ \rightarrow e^+ X^0$ and $B^+ \rightarrow \mu^+ X^0$ decays

C.-S. Park,⁶⁹ Y.-J. Kwon,⁶⁹ I. Adachi,^{12,9} H. Aihara,⁶¹ D.M. Asner,⁴⁷ T. Aushev,³⁵ V. Babu,⁵⁵ I. Badhrees,^{54,24}
A. M. Rakich,⁵³ F. Barberio,³³ P. Behera,¹⁶ V. Bhardwaj,⁵¹ I. Biswal,²¹ G. Bonvicini,⁶⁷ A. Bozek,⁴² M. Bračkan,^{31,21}

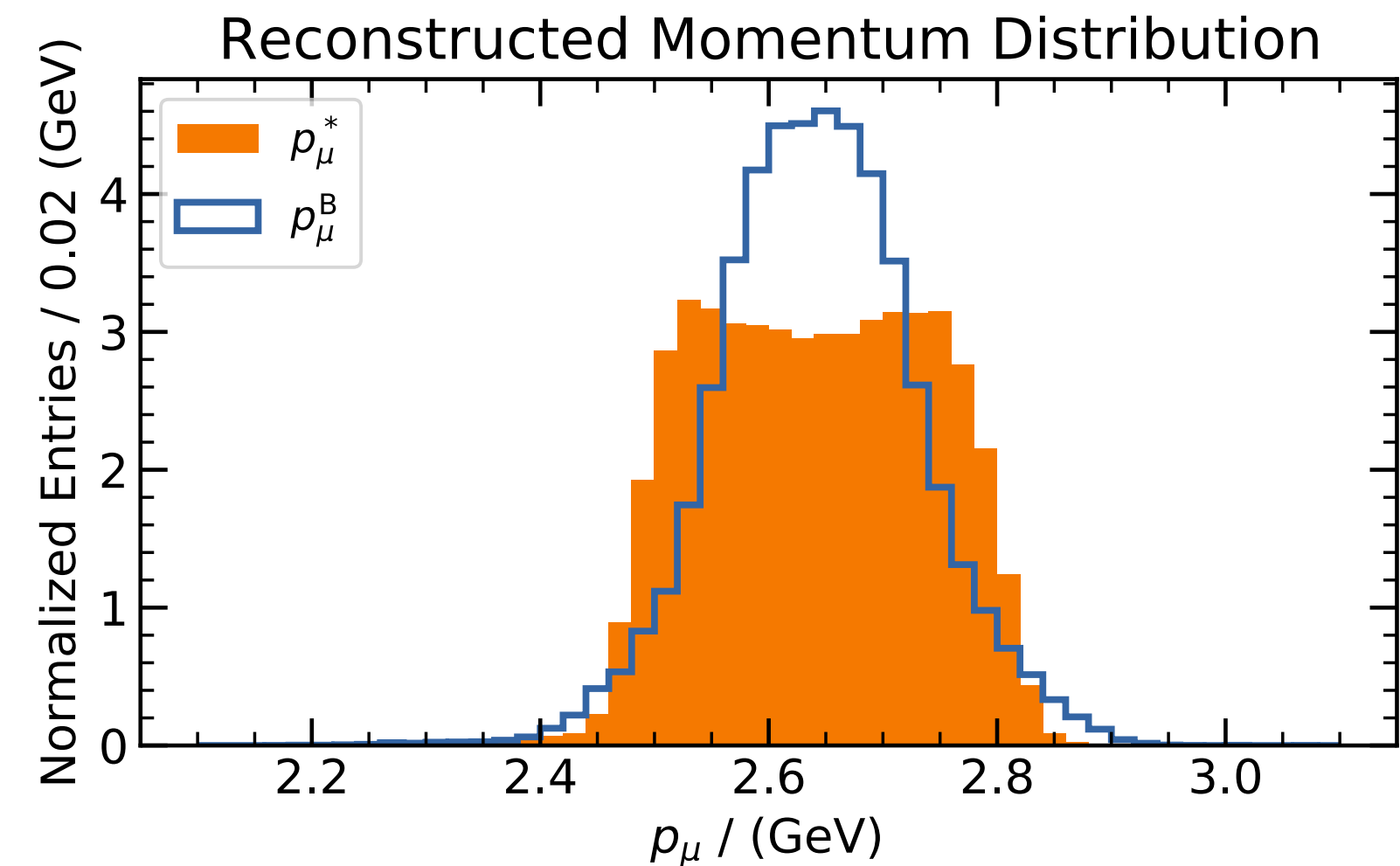


$$B^+ \rightarrow \mu^+ \nu_\mu \text{ and } B^+ \rightarrow \mu^+ N$$

N = an unknown neutral fermion (e.g. a sterile ν)

Features

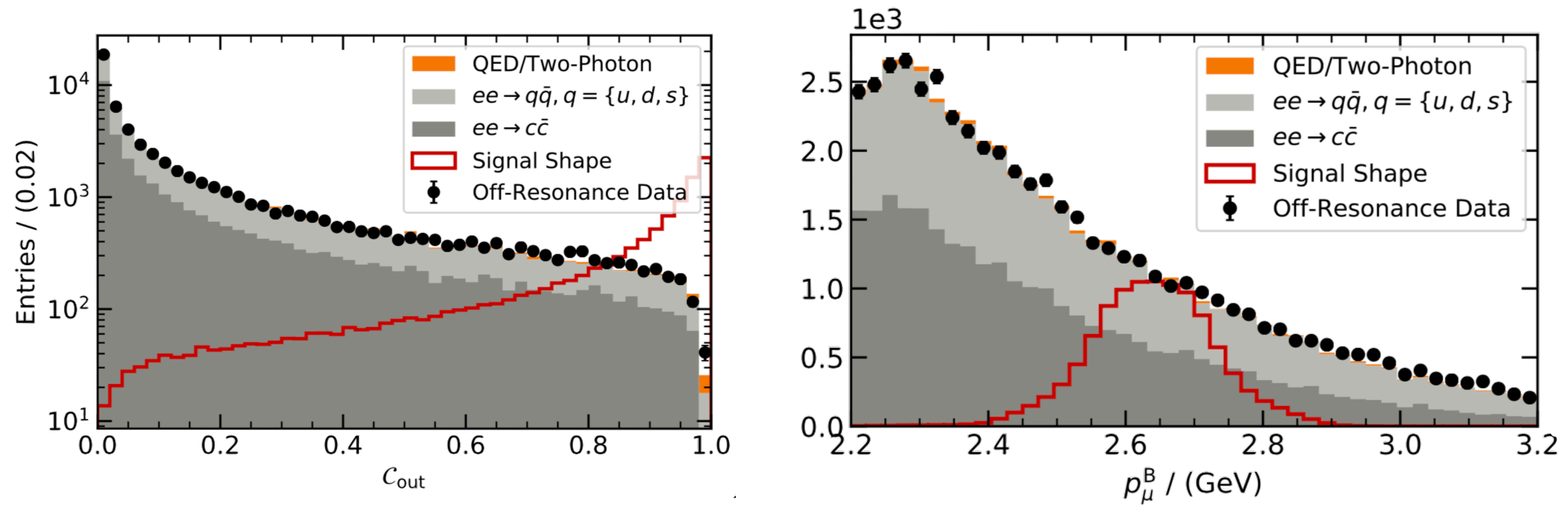
- an improved search over Belle's 2018 result ([PRL 121, 031801](#))
 - ✓ modeling of $b \rightarrow u \ell^+ \nu$ and continuum background
 - ✓ use inclusive B tagging to maximize signal selection efficiency ($\Leftarrow \text{BF}_{\text{SM}} \sim 4 \times 10^{-7}$)
- carry out the analysis in the signal B rest frame
 - ✓ exploit $p_\mu^B \simeq 2.64 \text{ GeV}$
 - ✓ achieve better resolution and sensitivity than using p_μ^* (CM frame)
 - ✓ sensitive to $B^+ \rightarrow \mu^+ N$ search, for $m_N \in [0, 1.5) \text{ GeV}$



$$B^+ \rightarrow \mu^+ \nu_\mu \text{ and } B^+ \rightarrow \mu^+ N$$

Signal extraction

✓ by binned max. likelihood fit to p_μ^B in kinematic/BDT categories

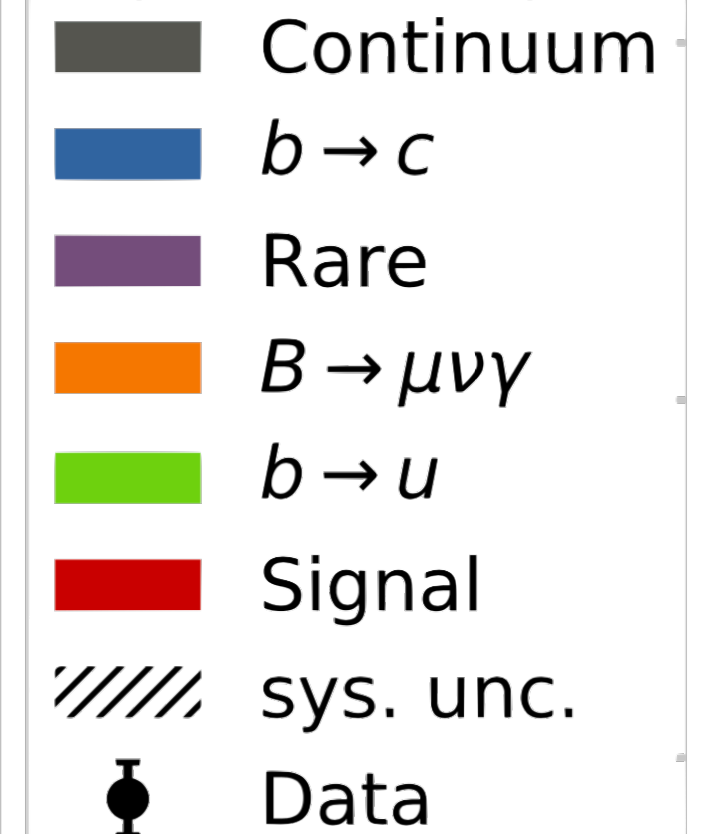
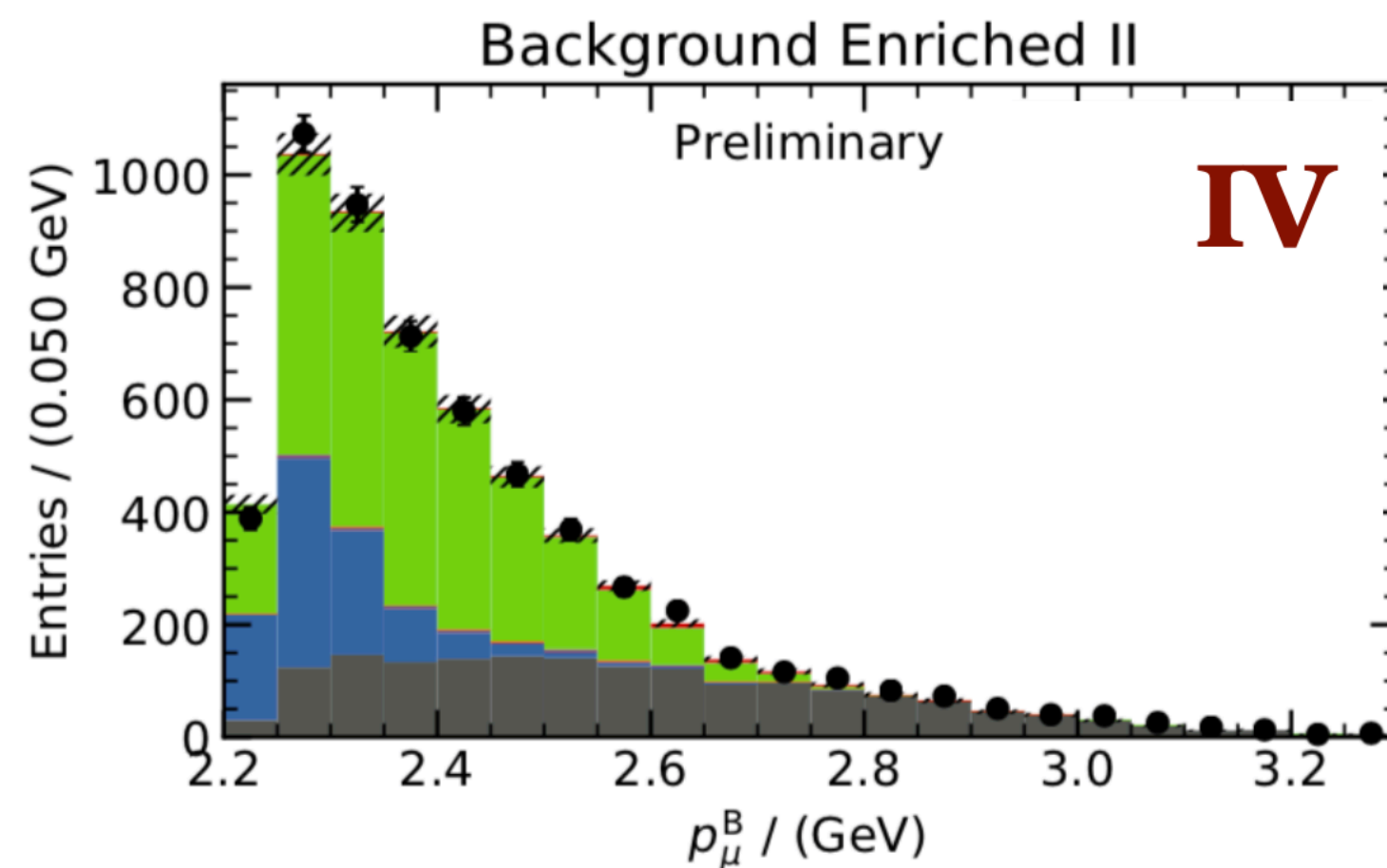
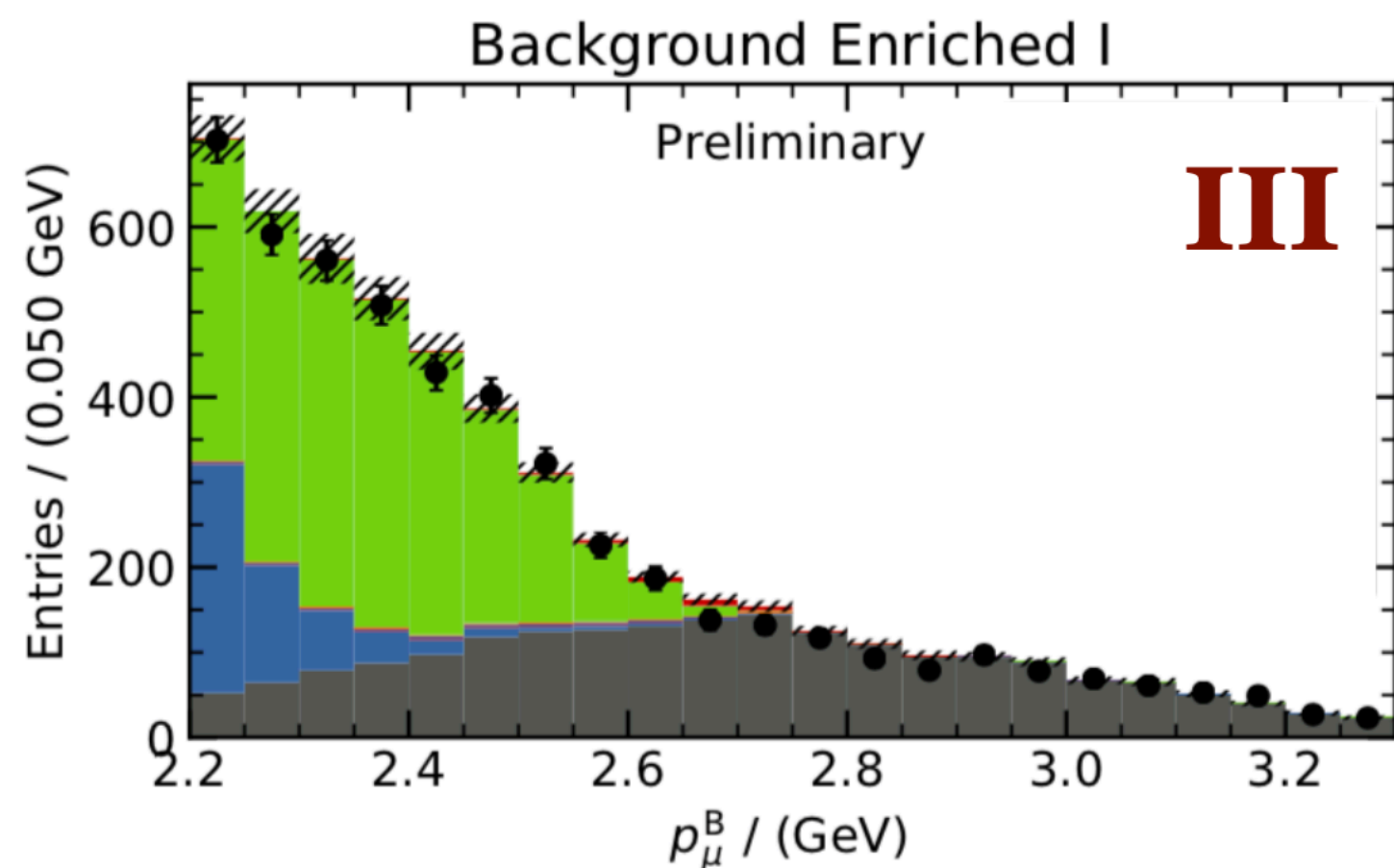
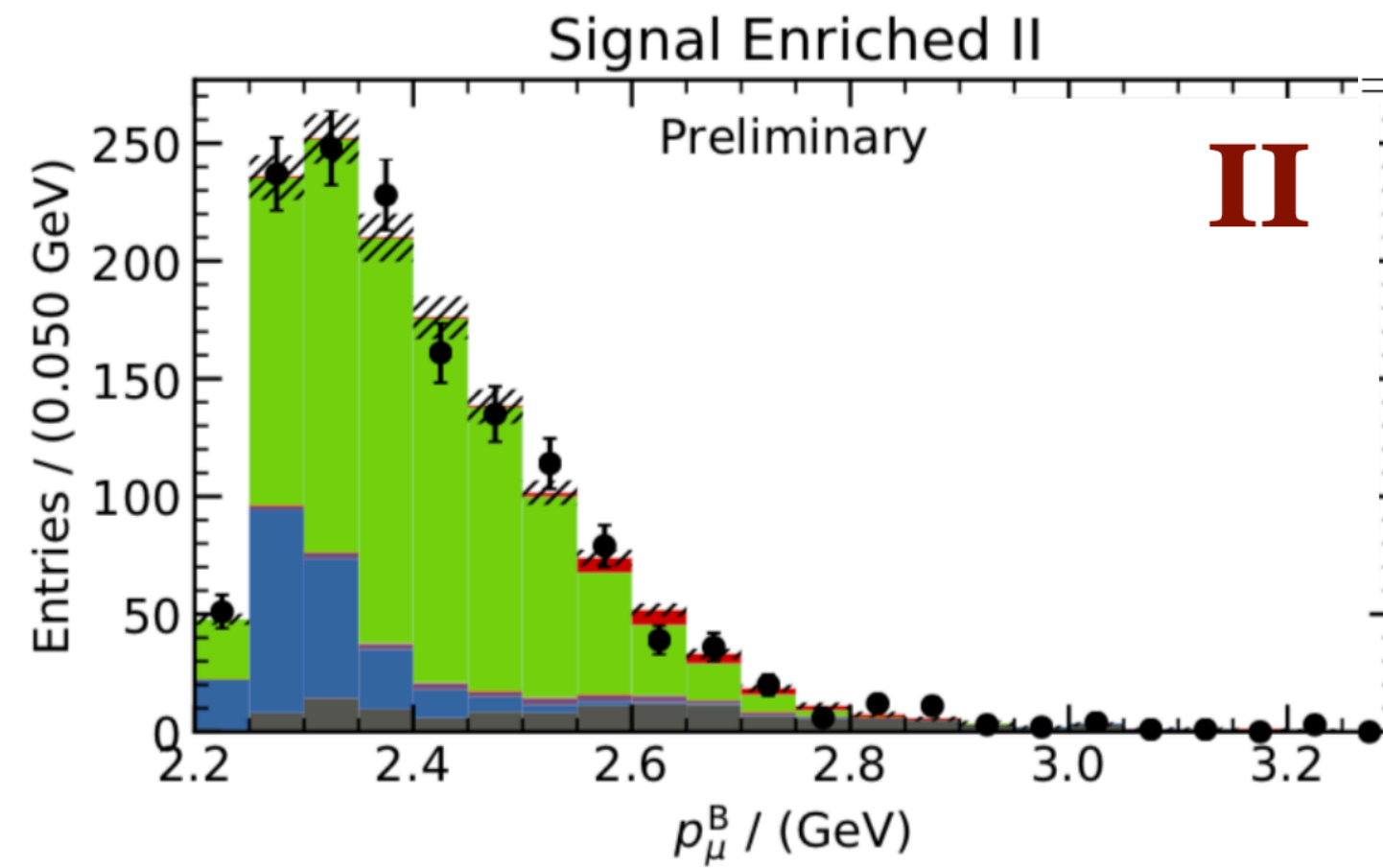
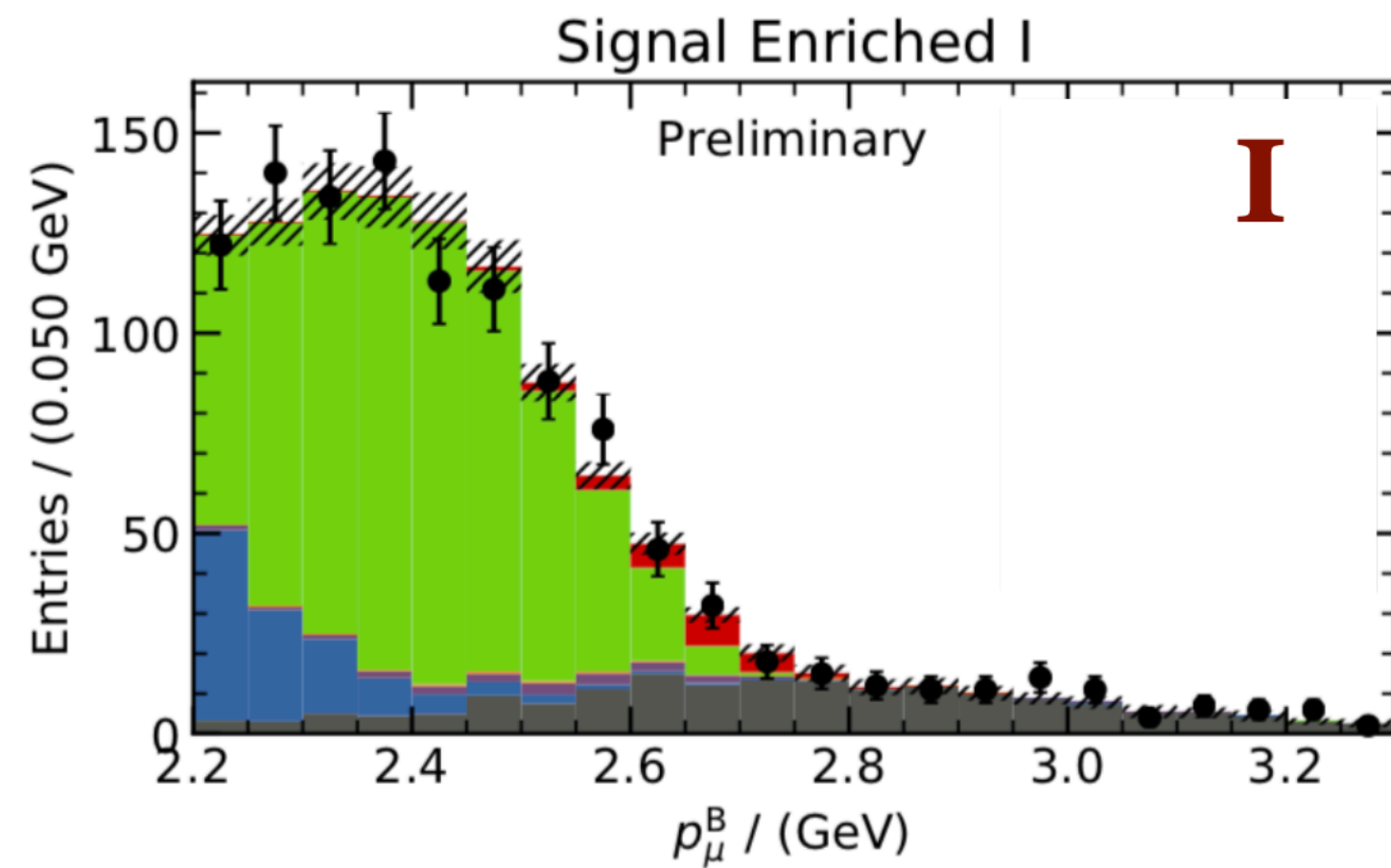


Category	C_{out}	$\cos \Theta_{B\mu}$	Signal Efficiency
I	[0.98,1.00)	[-0.13,1.00)	6.5 %
II	[0.98,1.00)	[-1.00,-0.13)	5.9 %
III	[0.93,0.98)	[0.04,1.00)	7.1 %
IV	[0.93,0.98)	[-1.00,0.04)	8.3 %

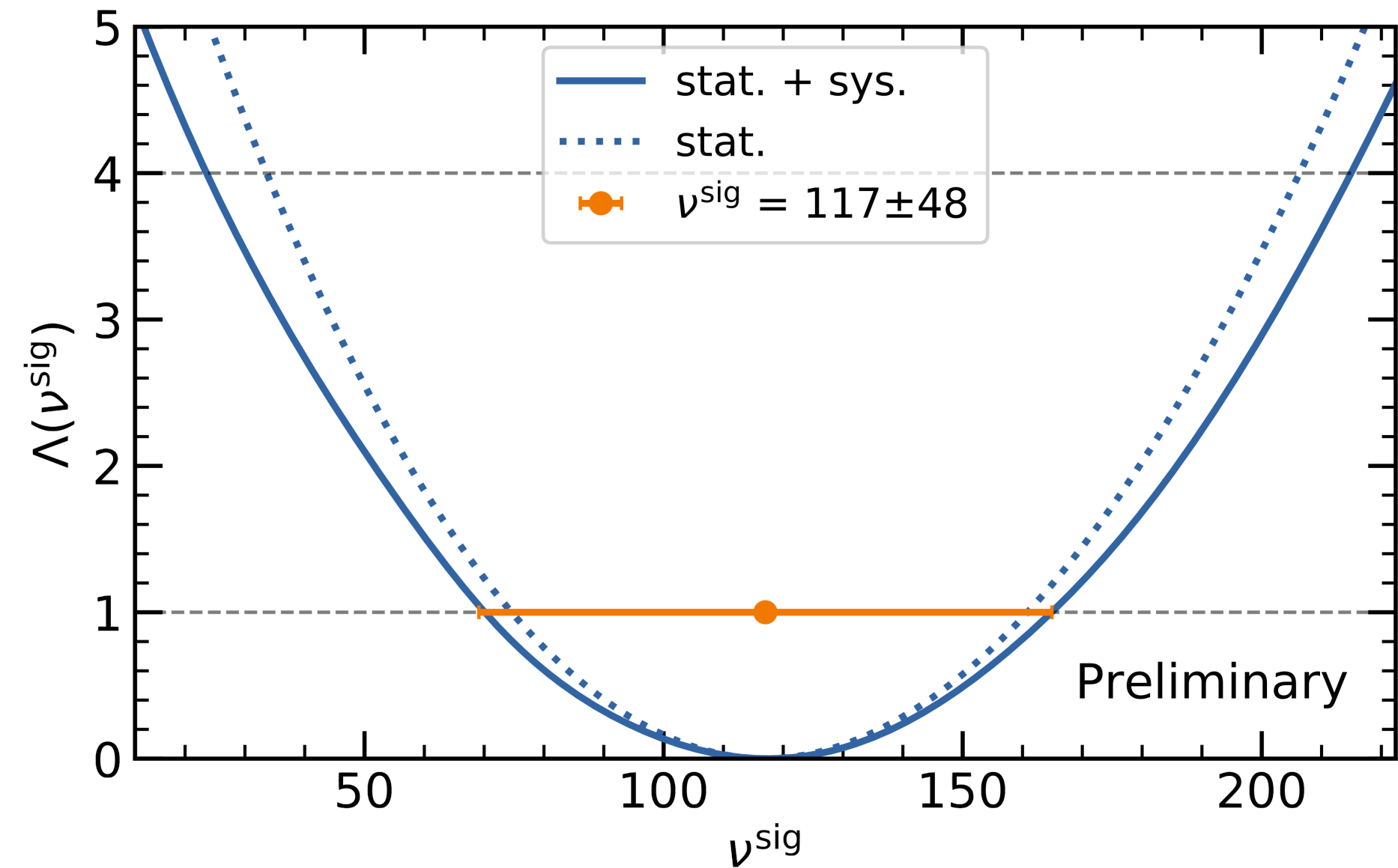
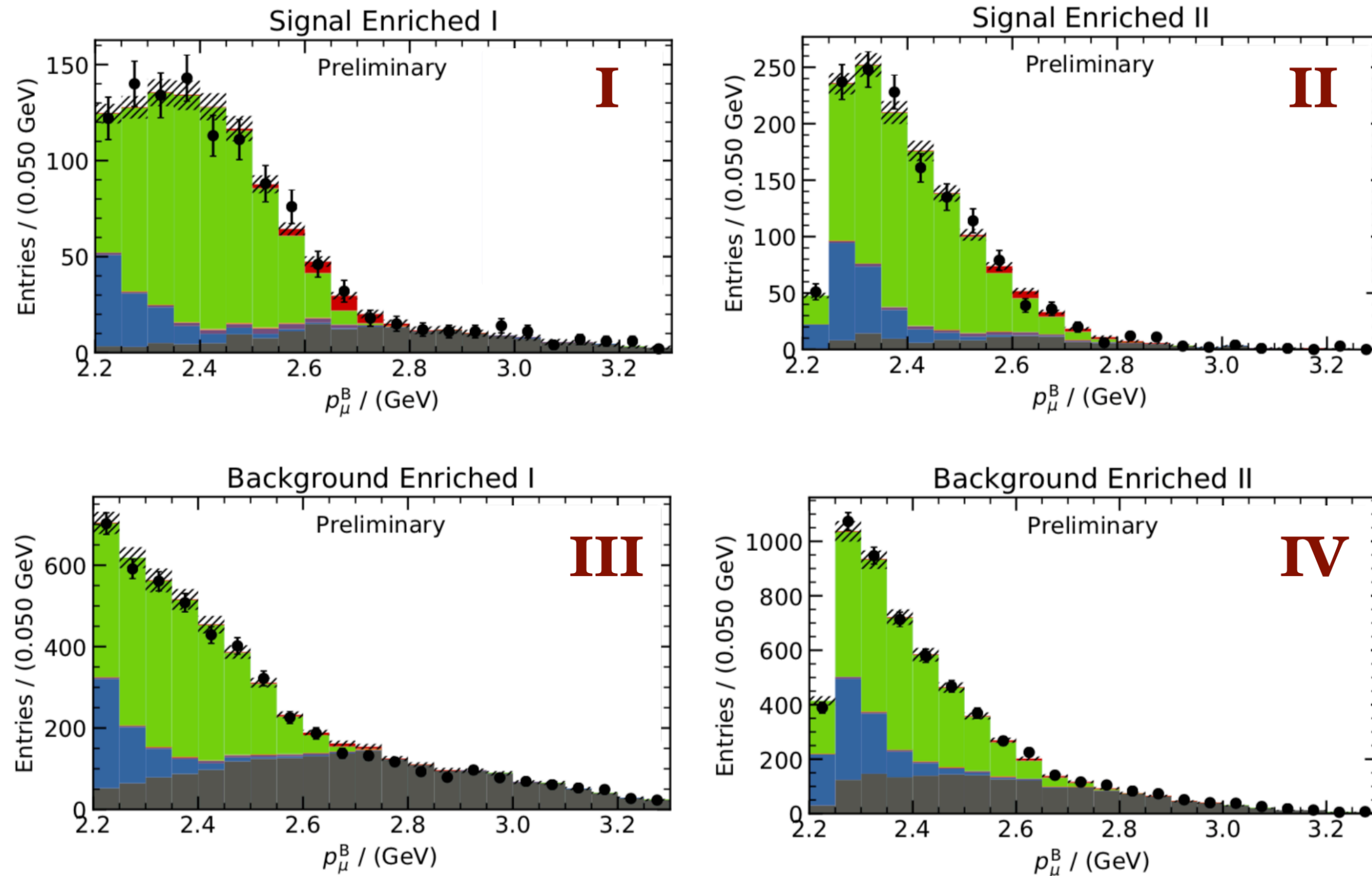
$$B^+ \rightarrow \mu^+ \nu_\mu \text{ and } B^+ \rightarrow \mu^+ N$$

Signal extraction

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IV	[0.93,0.98)	[-1.00,0.04)	8.3 %



$B^+ \rightarrow \mu^+ \nu$ Result



• $\mathcal{B}(B^+ \rightarrow \mu^+ \nu) = (5.3 \pm 2.0 \pm 0.9) \times 10^{-7} @ 2.8\sigma$

$\mathcal{B}(B^+ \rightarrow \mu^+ \nu) < 8.6 \times 10^{-7}$

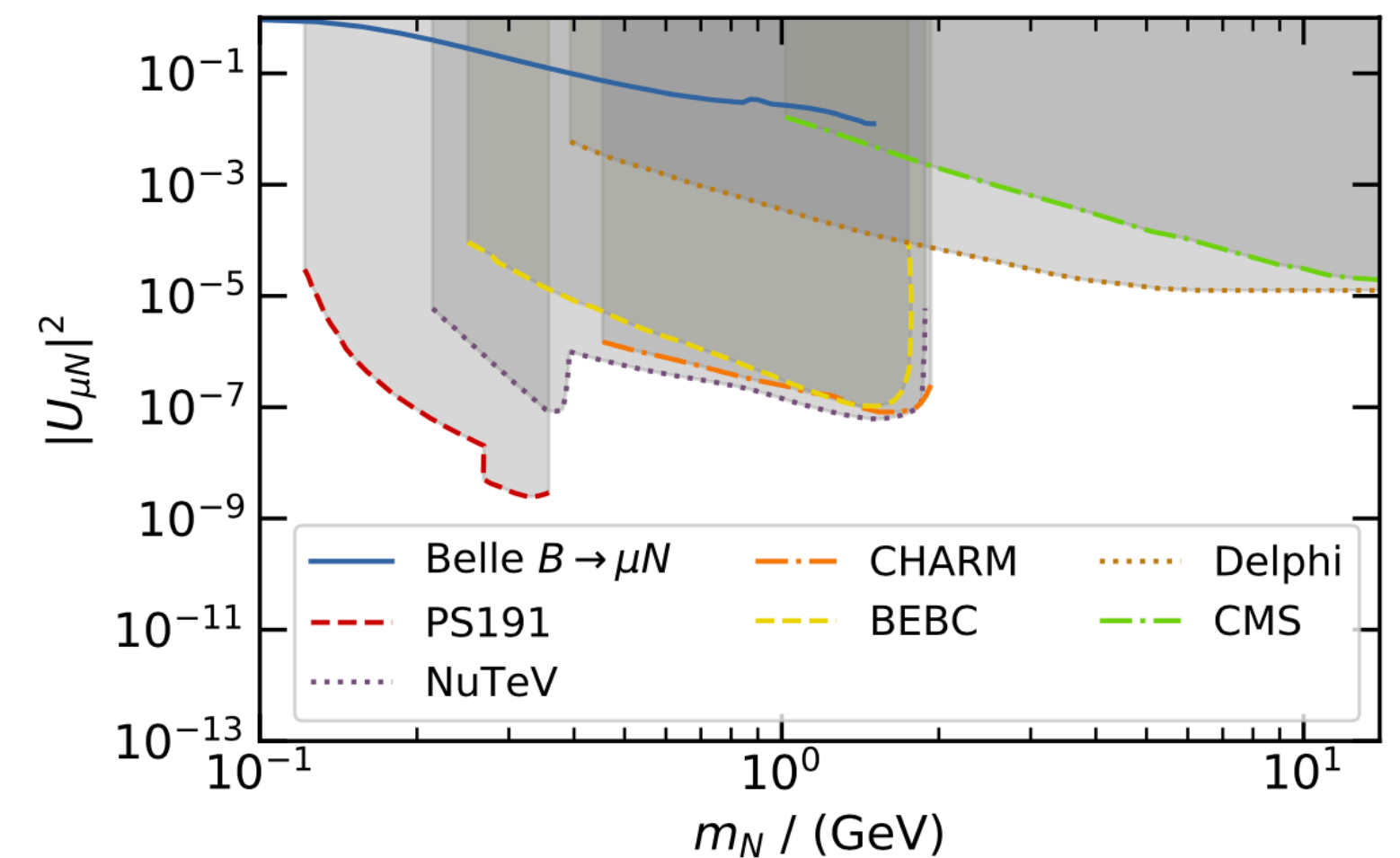
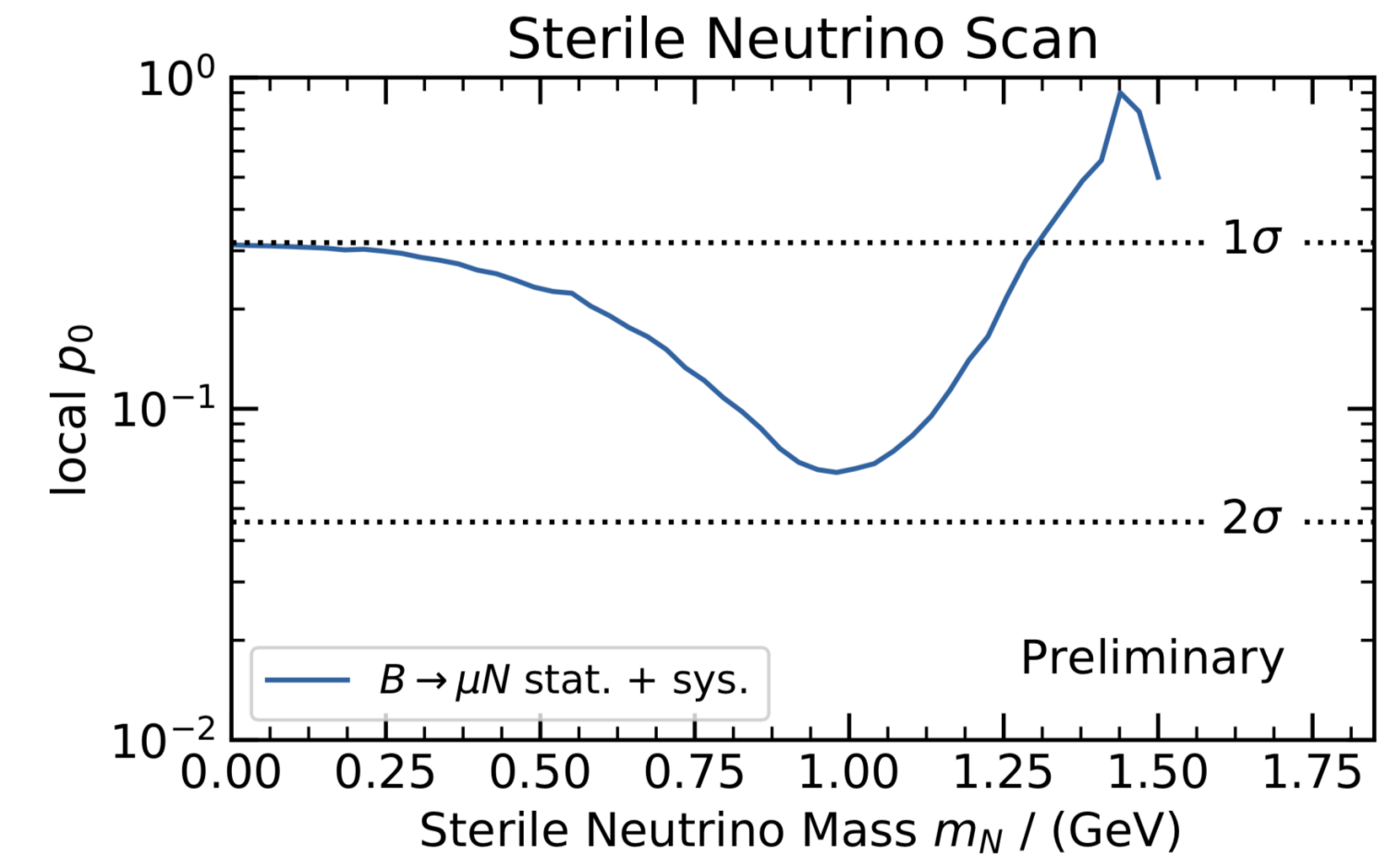
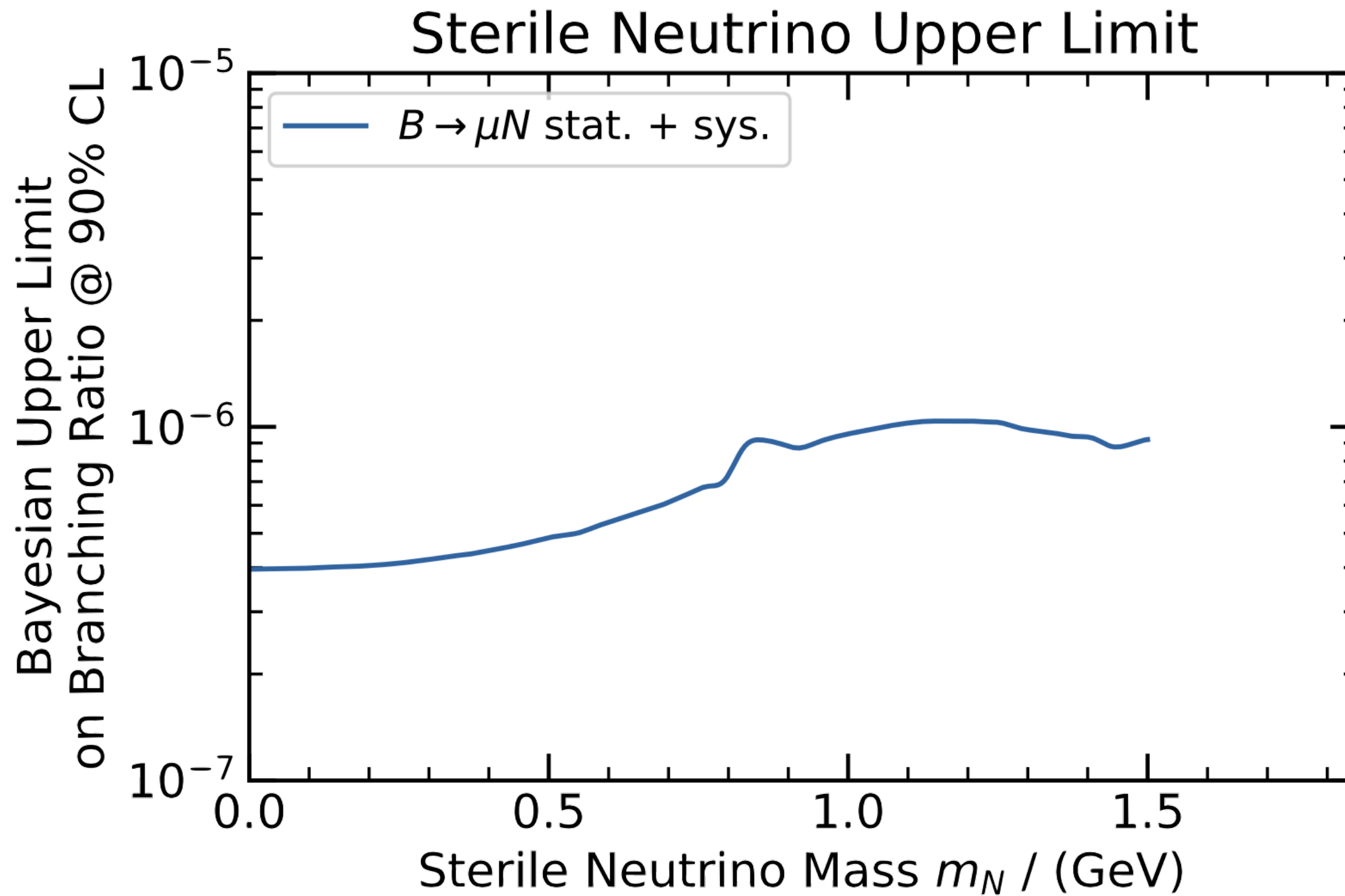
Frequentist

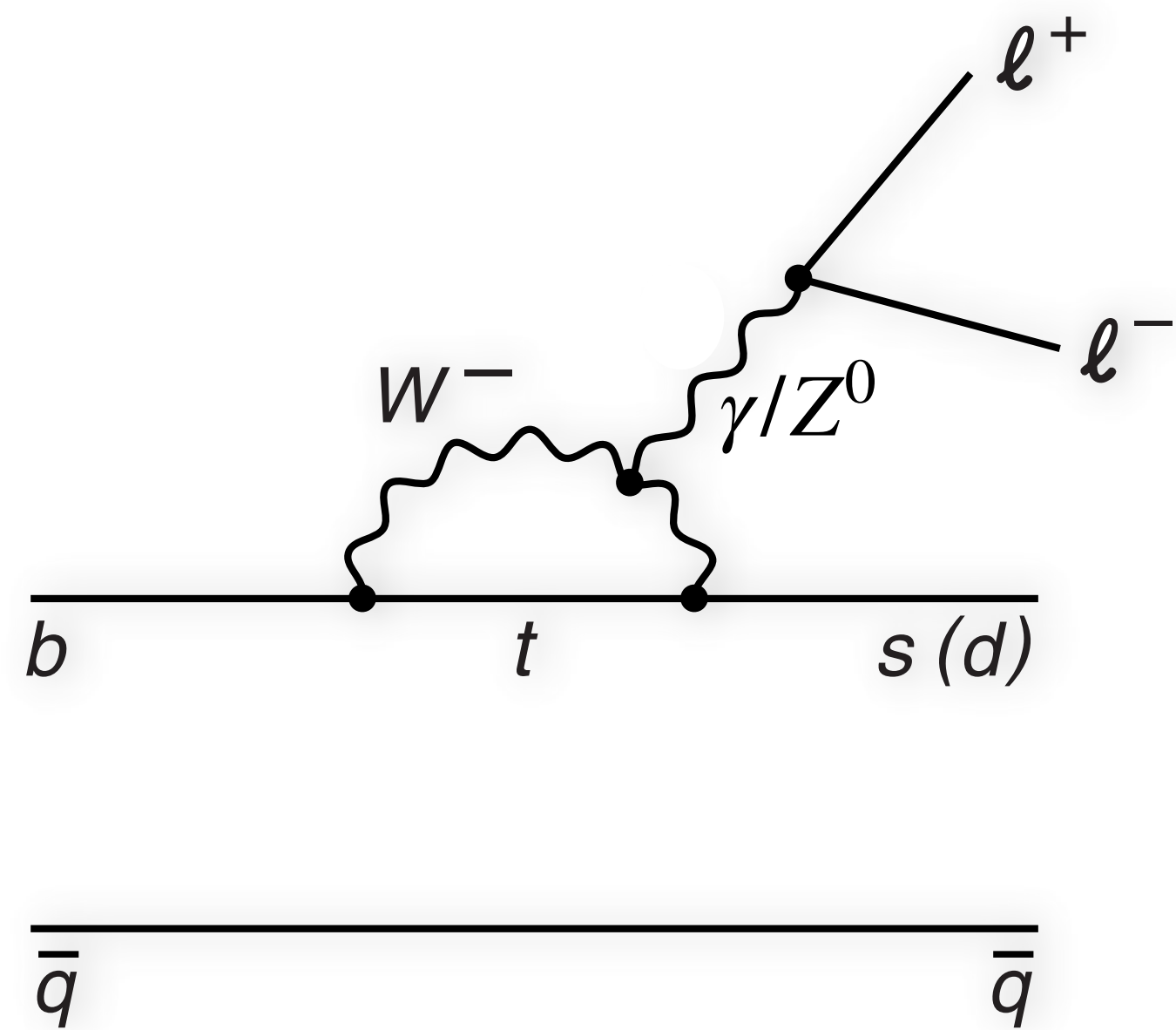
$< 8.9 \times 10^{-7}$

Bayesian

See back-up slide for New Physics implication!

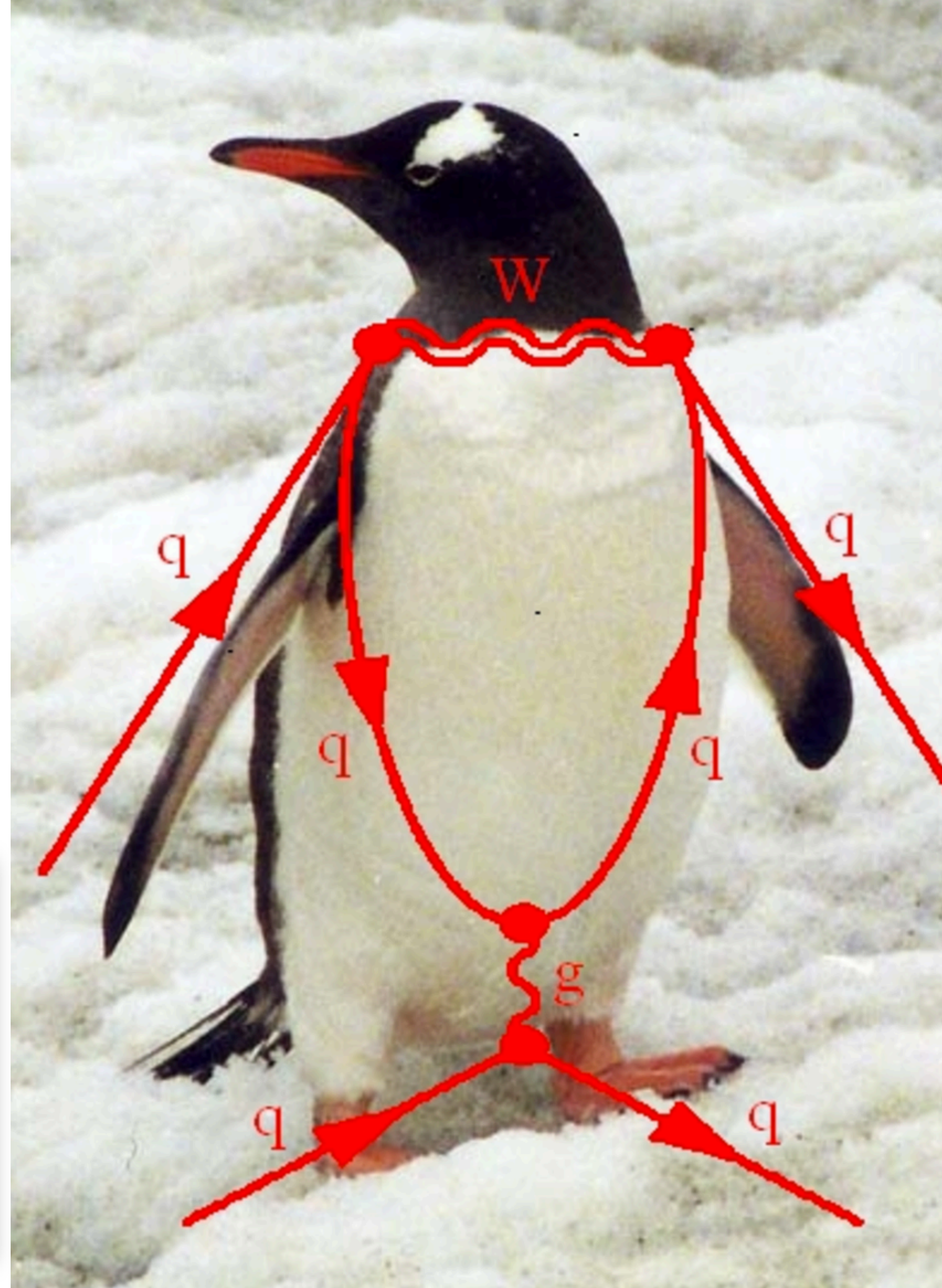
$B^+ \rightarrow \mu^+ N$ search





EW penguin

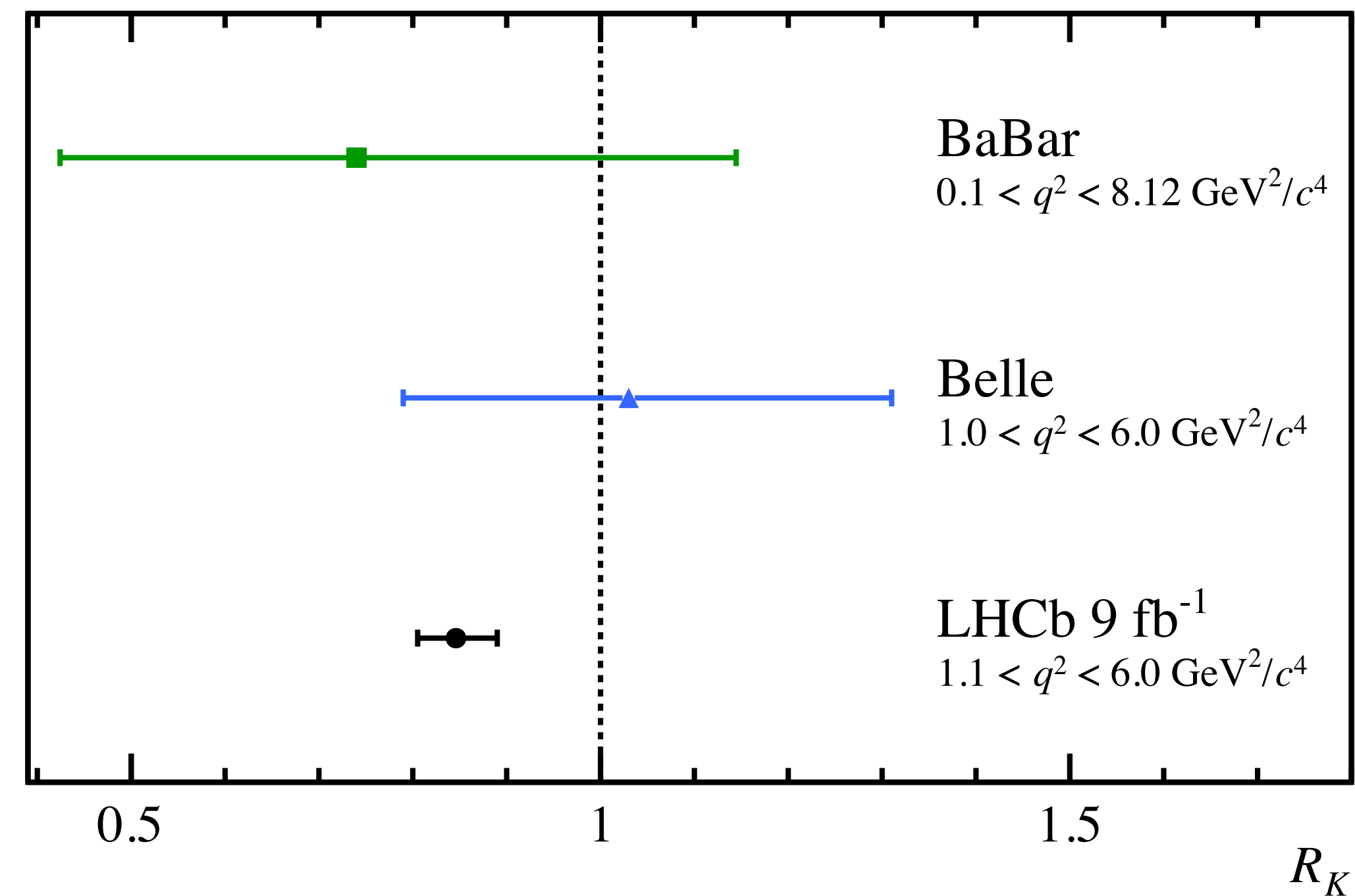
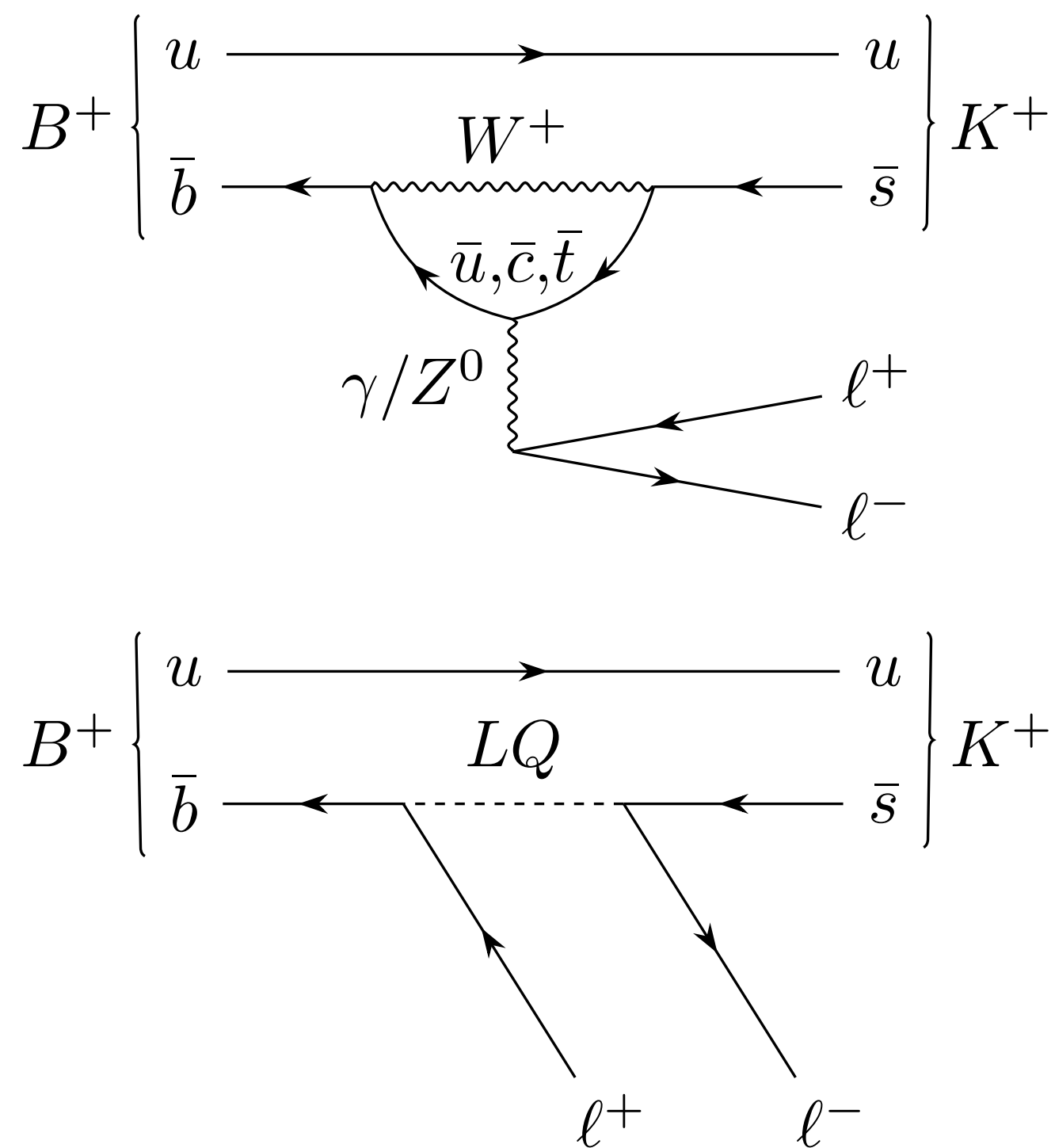
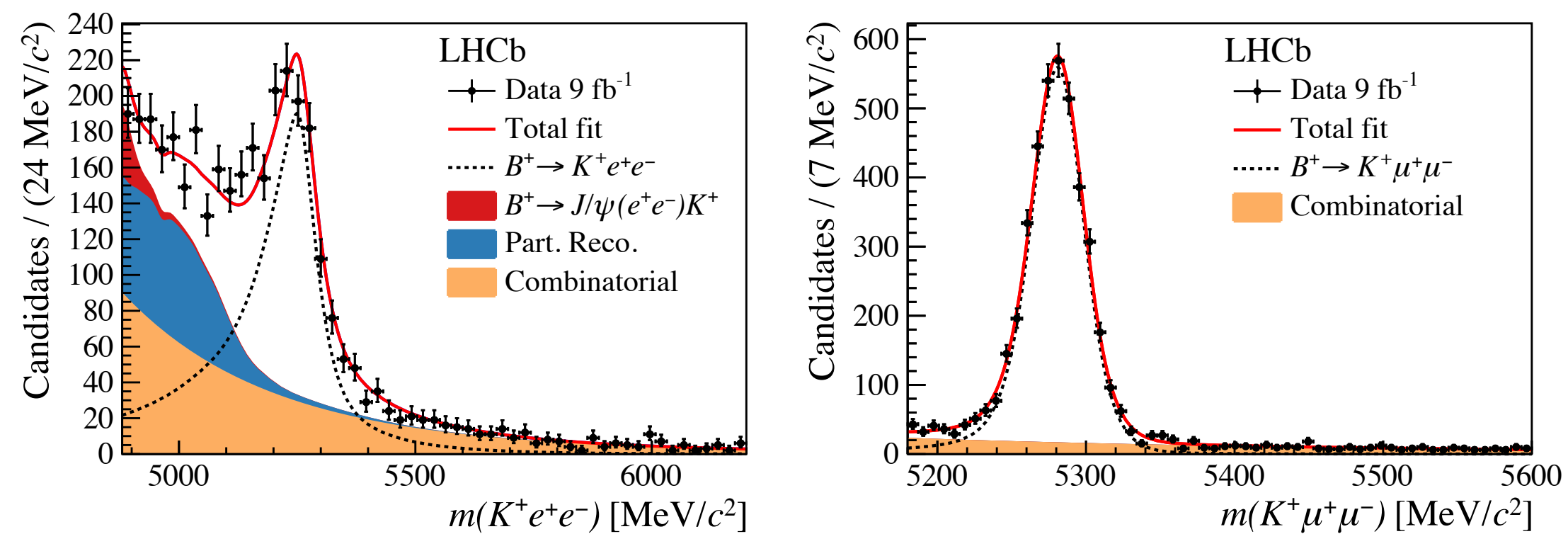
$$R_{K^{(*)}}$$



Belle's legacy on EW penguins

- First observation of $B \rightarrow K\ell^+\ell^-$ PRL **88**, 021801 (2002)
- First observation of $B \rightarrow K^*\ell^+\ell^-$ PRL **91**, 261601 (2003)
- First observation of $B \rightarrow X_s\ell^+\ell^-$ PRL **90**, 021801 (2003)
- First measurement of A_{FB} of $B \rightarrow K^*\ell^+\ell^-$ PRL **96**, 251801 (2006)
- First observations of several radiative modes, $\phi K\gamma$, $K_1\gamma$, etc.
- First observation of $B \rightarrow (\rho, \omega)\gamma$ PRL **96**, 221601 (2006)
- Most precise measurement of $B \rightarrow X_s\gamma$
covering the widest E_γ range PRL **103**, 241801 (2009)
- *and many more published results*

$$R_H \equiv \frac{\int_{q_{\min}^2}^{q_{\max}^2} \frac{d\mathcal{B}(B \rightarrow H \mu^+ \mu^-)}{dq^2} dq^2}{\int_{q_{\min}^2}^{q_{\max}^2} \frac{d\mathcal{B}(B \rightarrow H e^+ e^-)}{dq^2} dq^2}$$

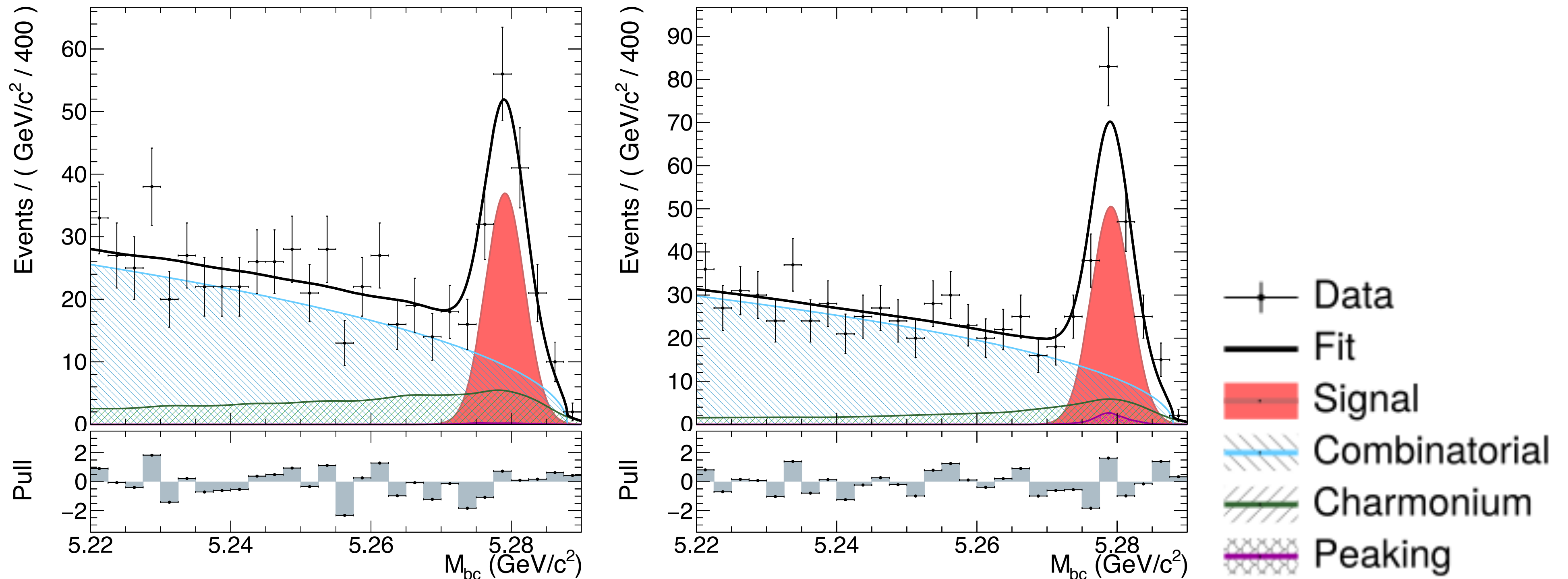


$$R_K(1.1 < q^2 < 6.0 \text{ GeV}^2/c^4) = 0.846^{+0.042}_{-0.039} + {}^{+0.013}_{-0.012}$$

R_{K^*} from Belle

● Use both B^0 and B^+ modes

- K^* modes: $K^+\pi^-$, $K^+\pi^0$, $K_S^0\pi^+$

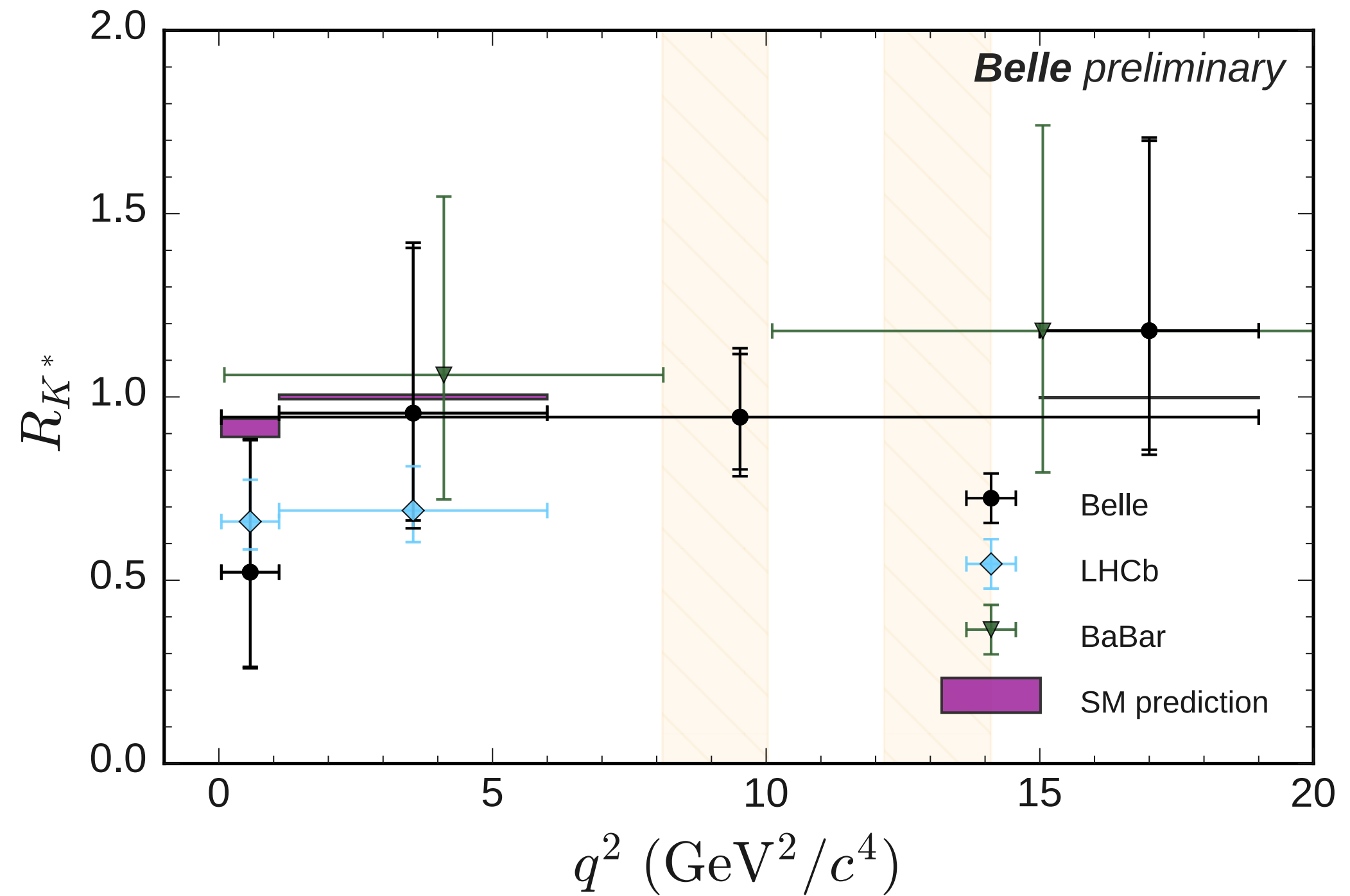
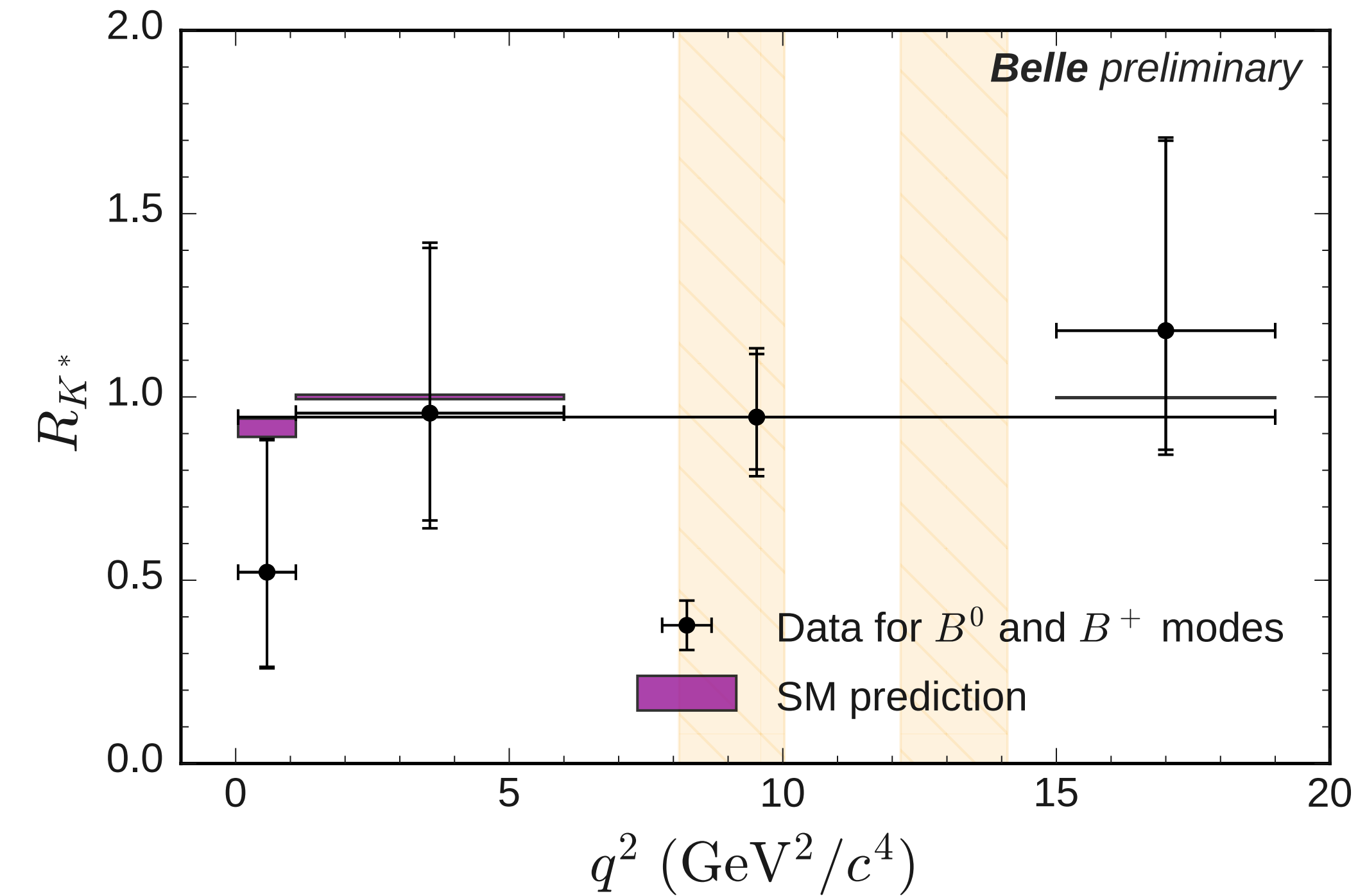


- example fit for $q^2 > 0.045$ GeV²
- $103.0^{+13.4}_{-12.7}$ ($139.0^{+16.0}_{-15.4}$) events in the e (μ) modes

R_{K^*} from Belle

R_{K^*} (Belle)

R_{K^*} (all)

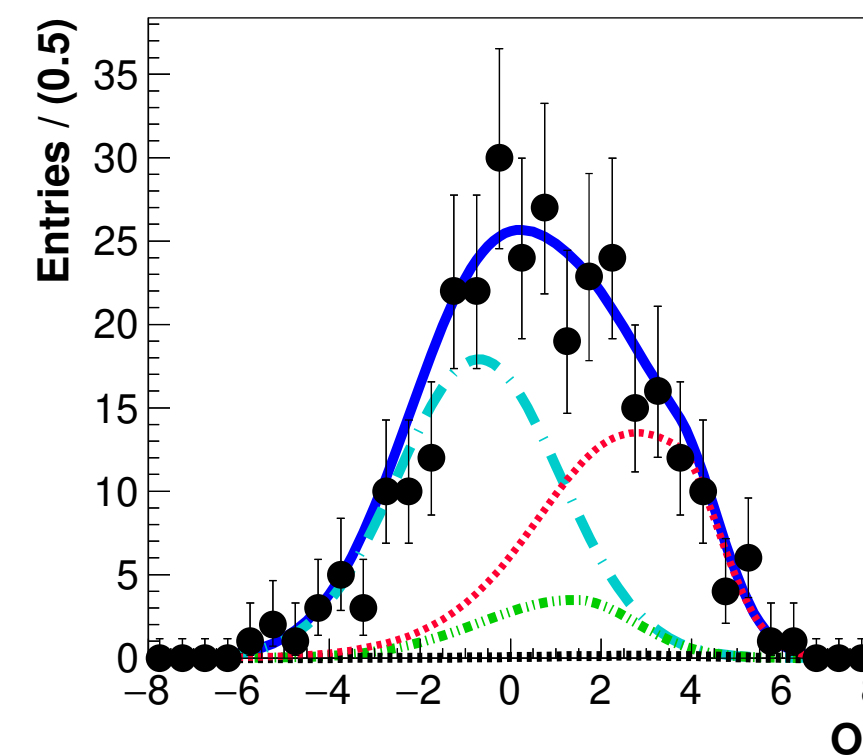
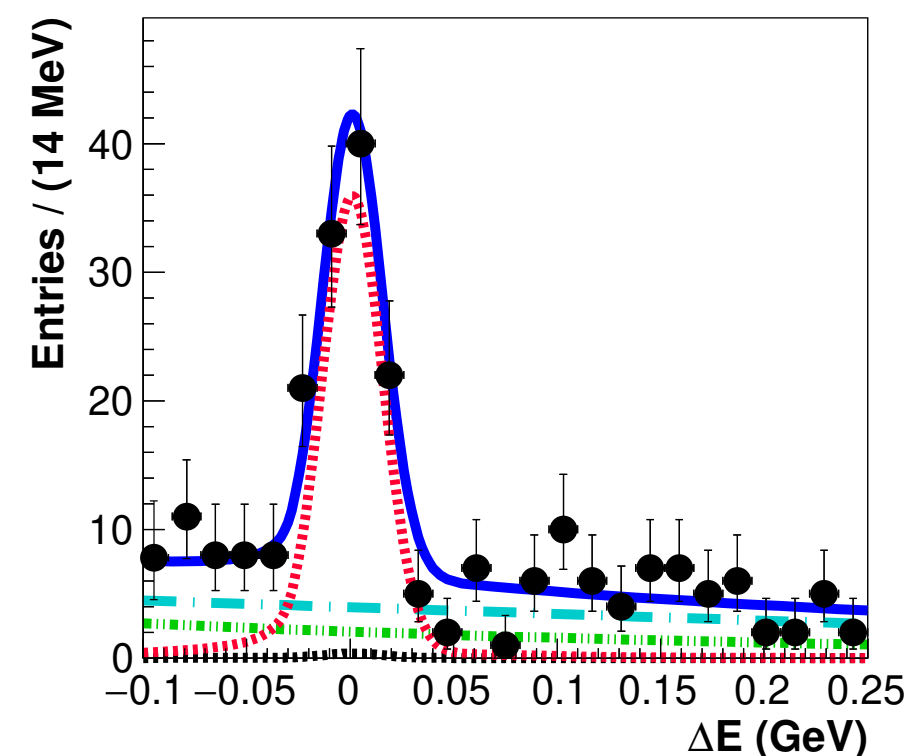
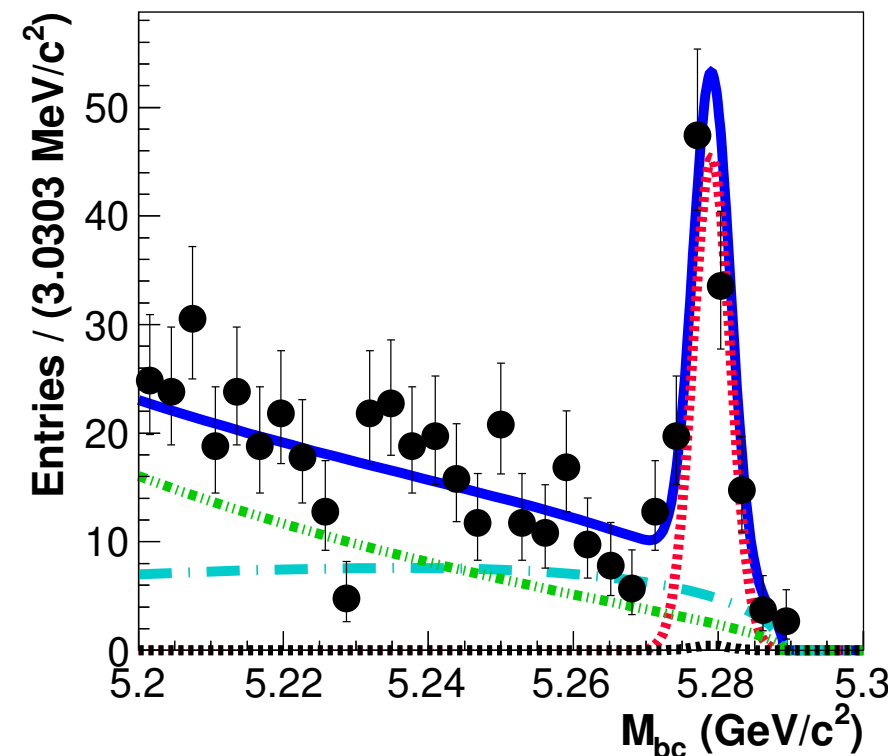


R_K from Belle

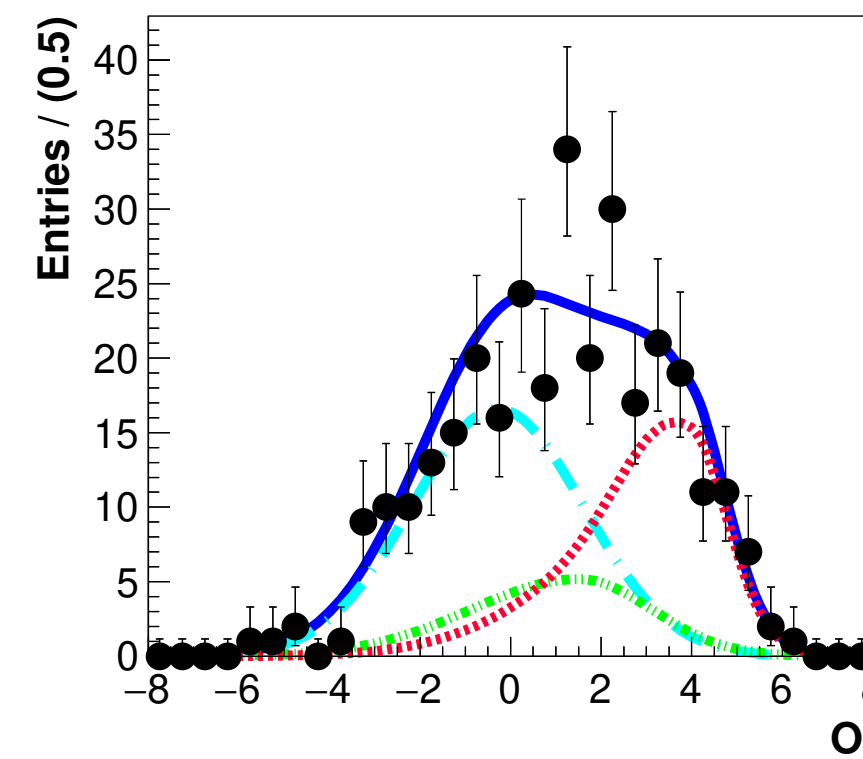
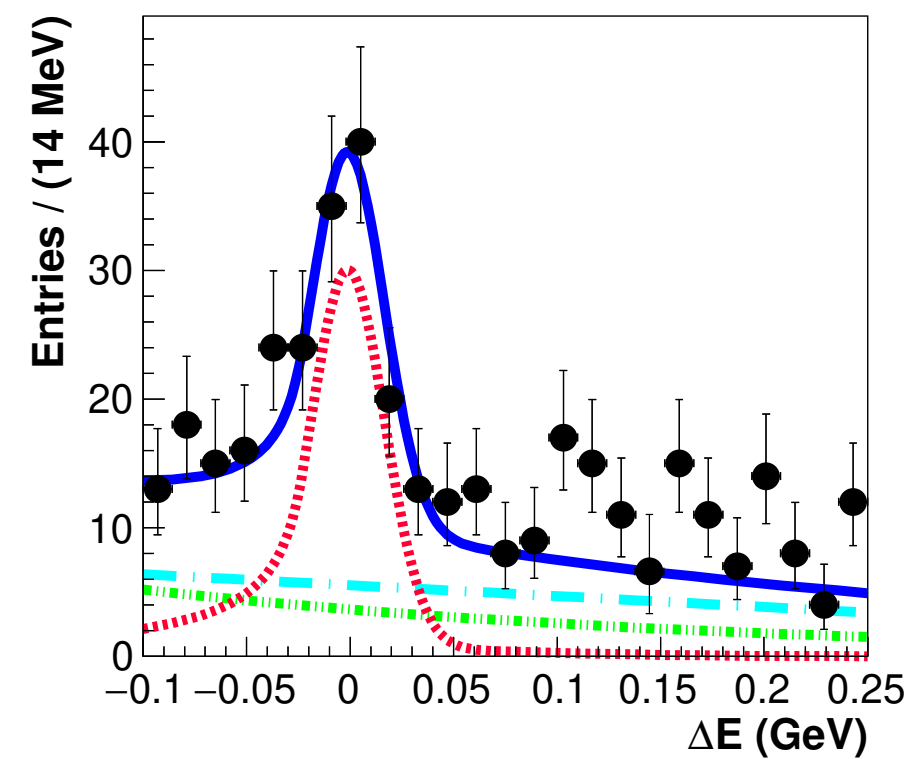
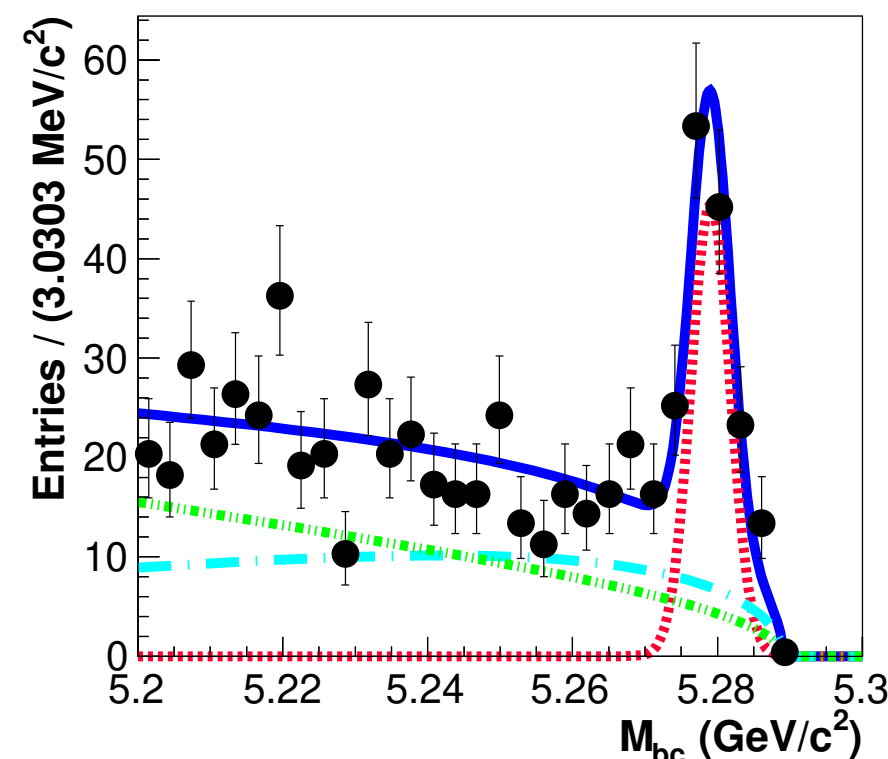


Use both B^0 and B^+ modes

$$q^2(\mu\mu) \in [(0.1, 8.75), (10.2, 13), (> 14.18)]$$



$$B^+ \rightarrow K^+ \mu^+ \mu^-$$

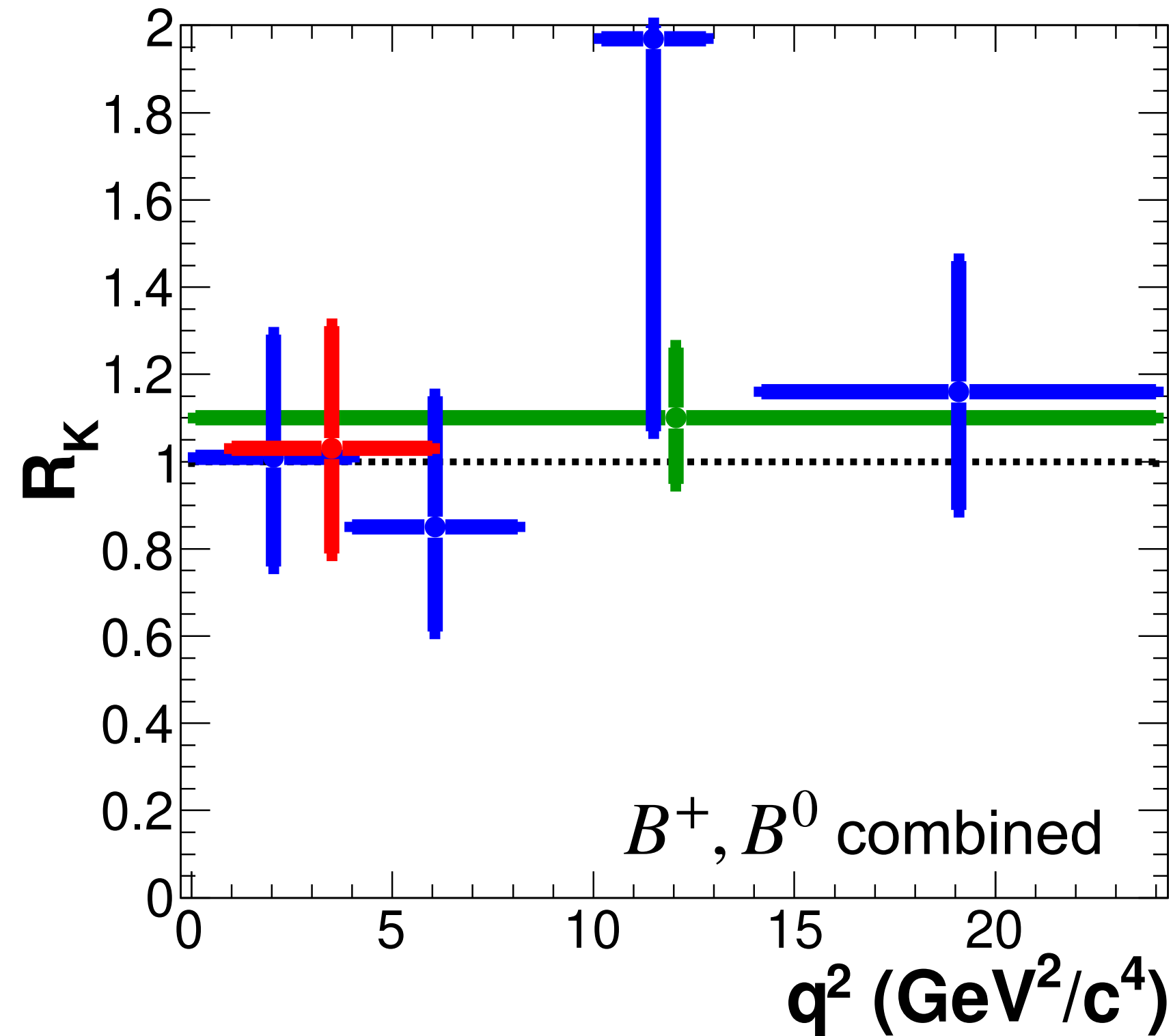


$$B^+ \rightarrow K^+ e^+ e^-$$

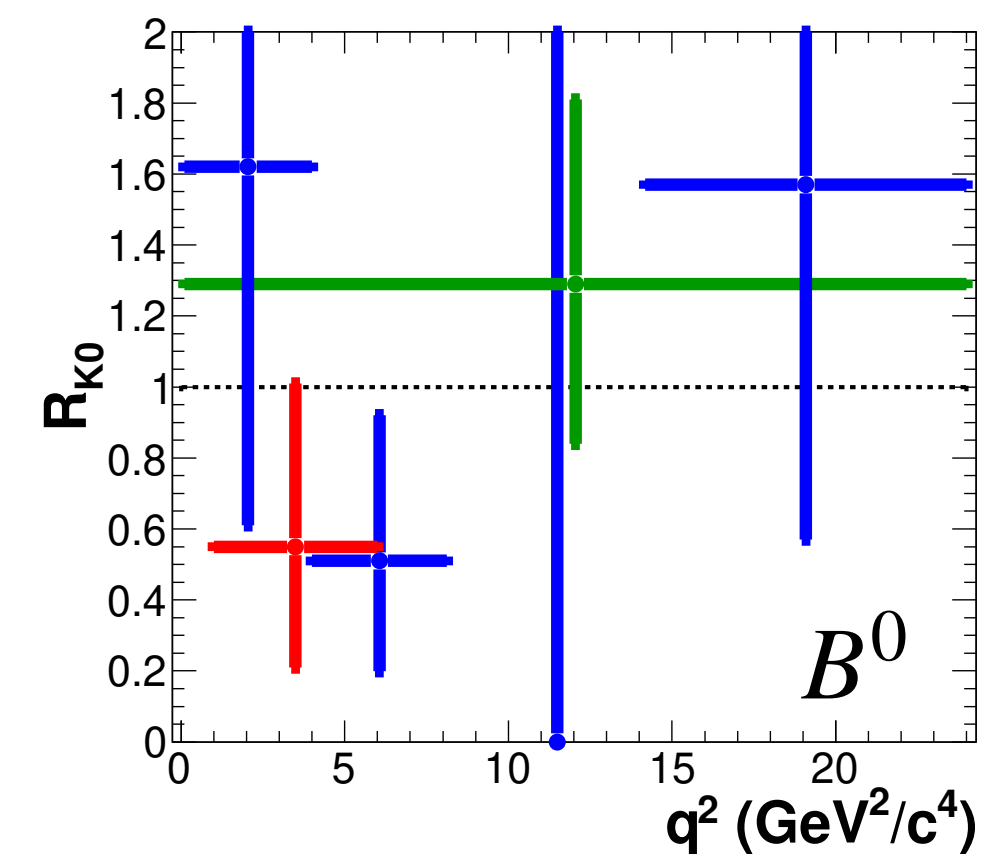
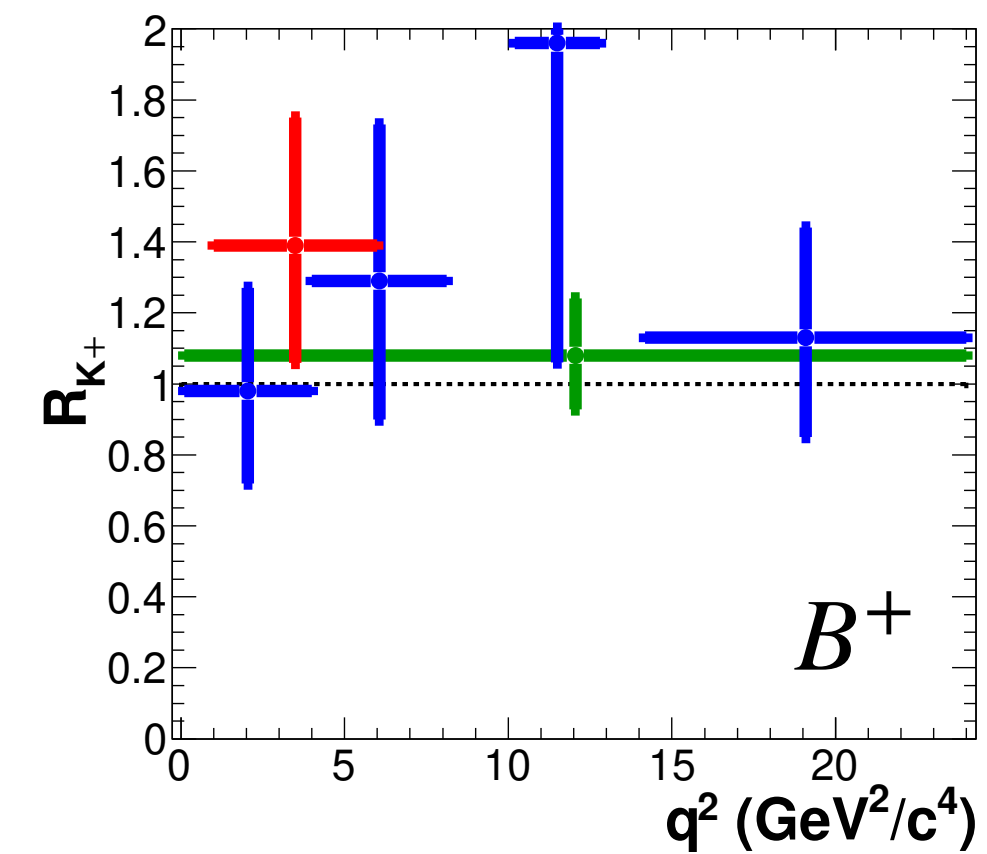
$$q^2(ee) \in [(0.1, 8.12), (10.2, 12.8), (> 14.18)]$$

- $137 \pm 14 (138 \pm 15)$ events in the $B^+ \rightarrow K^+ \mu^+ \mu^-$ ($K^+ e^+ e^-$)
- $27.3^{+6.6}_{-5.8}$ ($21.8^{+7.0}_{-6.1}$) events in the $B^0 \rightarrow K_S^0 \mu^+ \mu^-$ ($K_S^0 e^+ e^-$)

R_K from Belle



$$R_K = \begin{cases} 1.01^{+0.28}_{-0.25} \pm 0.02 & q^2 \in (0.1, 4.0) \text{ GeV}^2/c^4, \\ 0.85^{+0.30}_{-0.24} \pm 0.01 & q^2 \in (4.00, 8.12) \text{ GeV}^2/c^4, \\ 1.03^{+0.28}_{-0.24} \pm 0.01 & q^2 \in (1.0, 6.0) \text{ GeV}^2/c^4, \\ 1.97^{+1.03}_{-0.89} \pm 0.02 & q^2 \in (10.2, 12.8) \text{ GeV}^2/c^4, \\ 1.16^{+0.30}_{-0.27} \pm 0.01 & q^2 > 14.18 \text{ GeV}^2/c^4. \end{cases}$$



LFV in $B \rightarrow K^{(*)} \ell^+ \ell^-$

- Much renewed interests in $B \rightarrow K^{(*)} \ell^+ \ell^-$ for $R_{K^{(*)}}$ anomalies and potential interpretations in LUV

- LUV accompanied by LFV

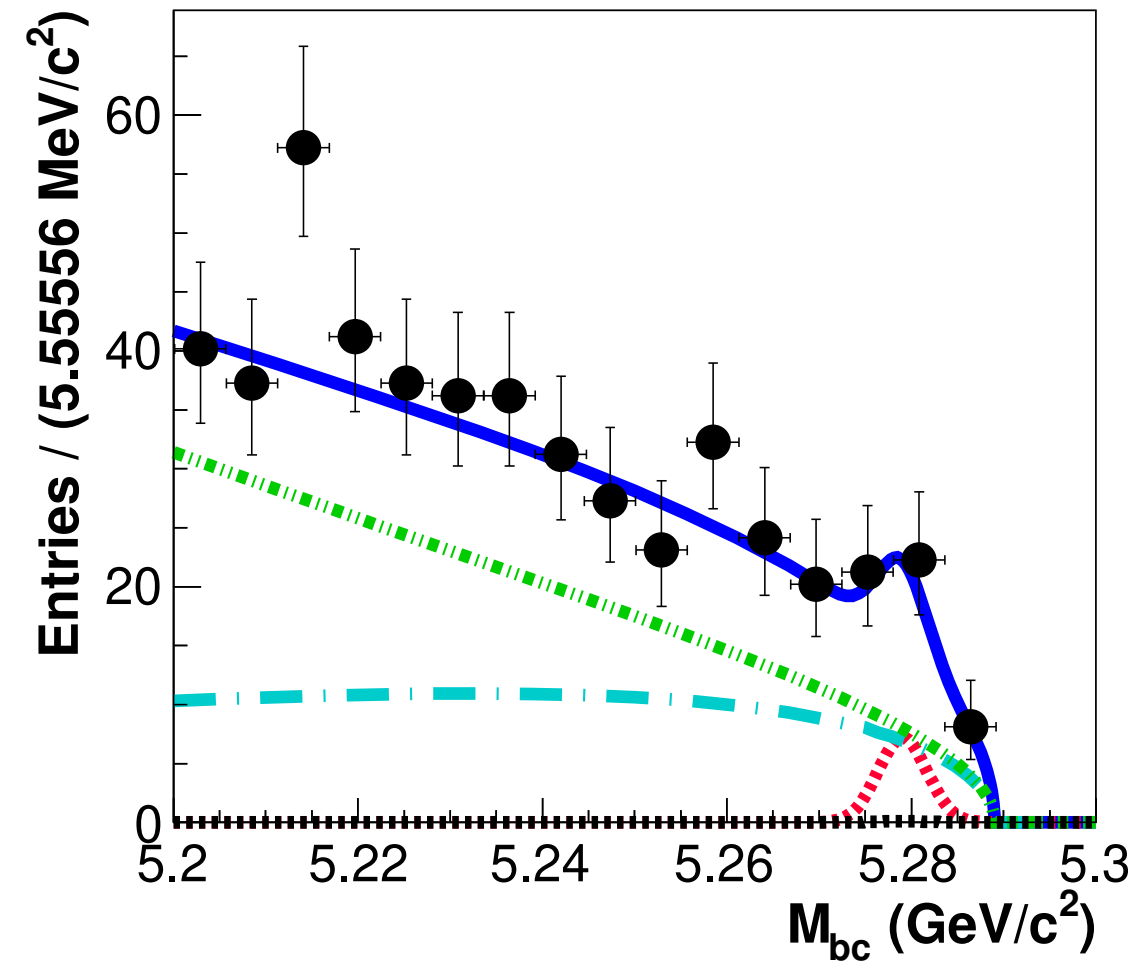
“However, any departure from lepton universality is necessarily associated with the violation of lepton flavor conservation. *No known symmetry principle can protect the one in the absence of the other.*”*

- So, why not search for $B \rightarrow K^{(*)} \ell^+ \ell'^- \ (\ell' \neq \ell)$?

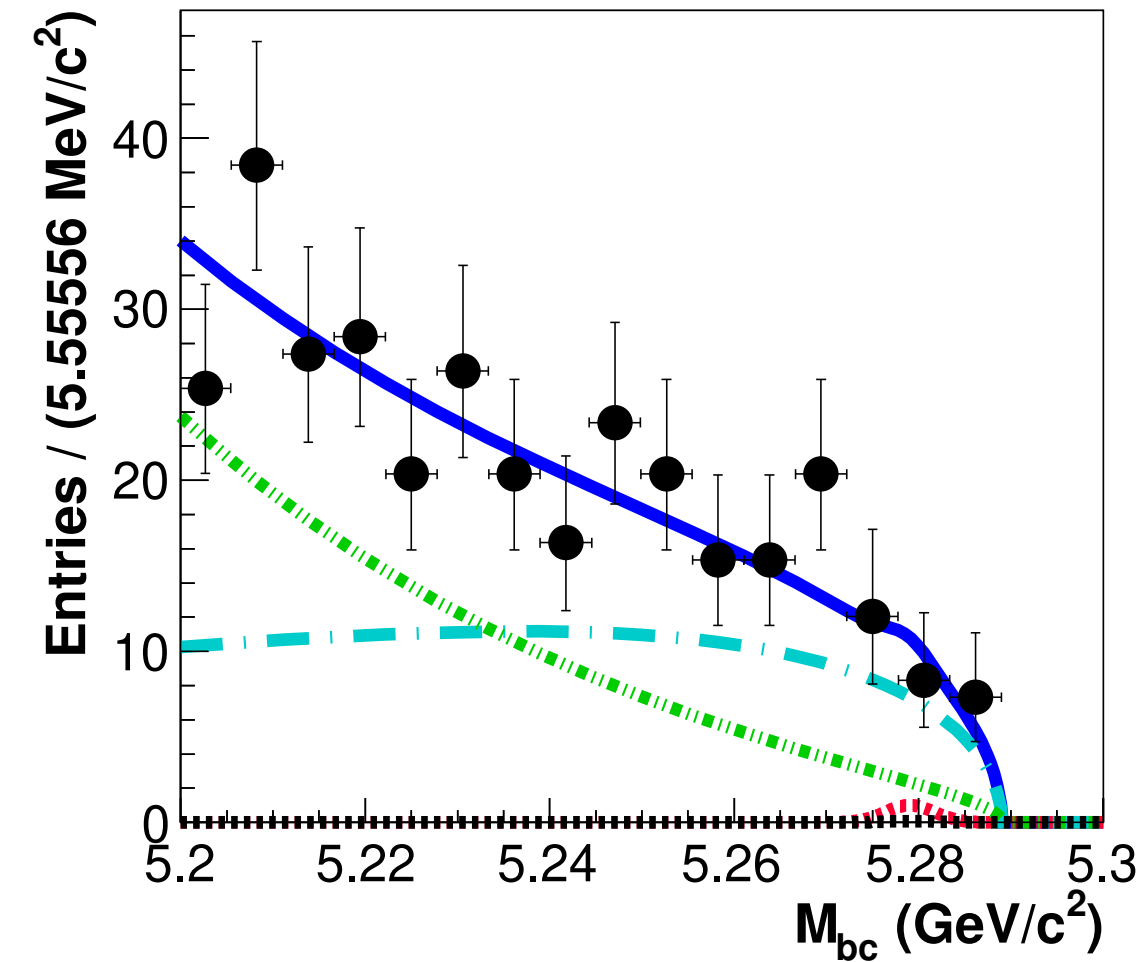
* *Lepton Flavor Violation in B Decays?* Glashow, Guadagnoli, Lane, PRL 114, 091801 (2015)

LFV in $B \rightarrow K \ell^+ \ell^-$

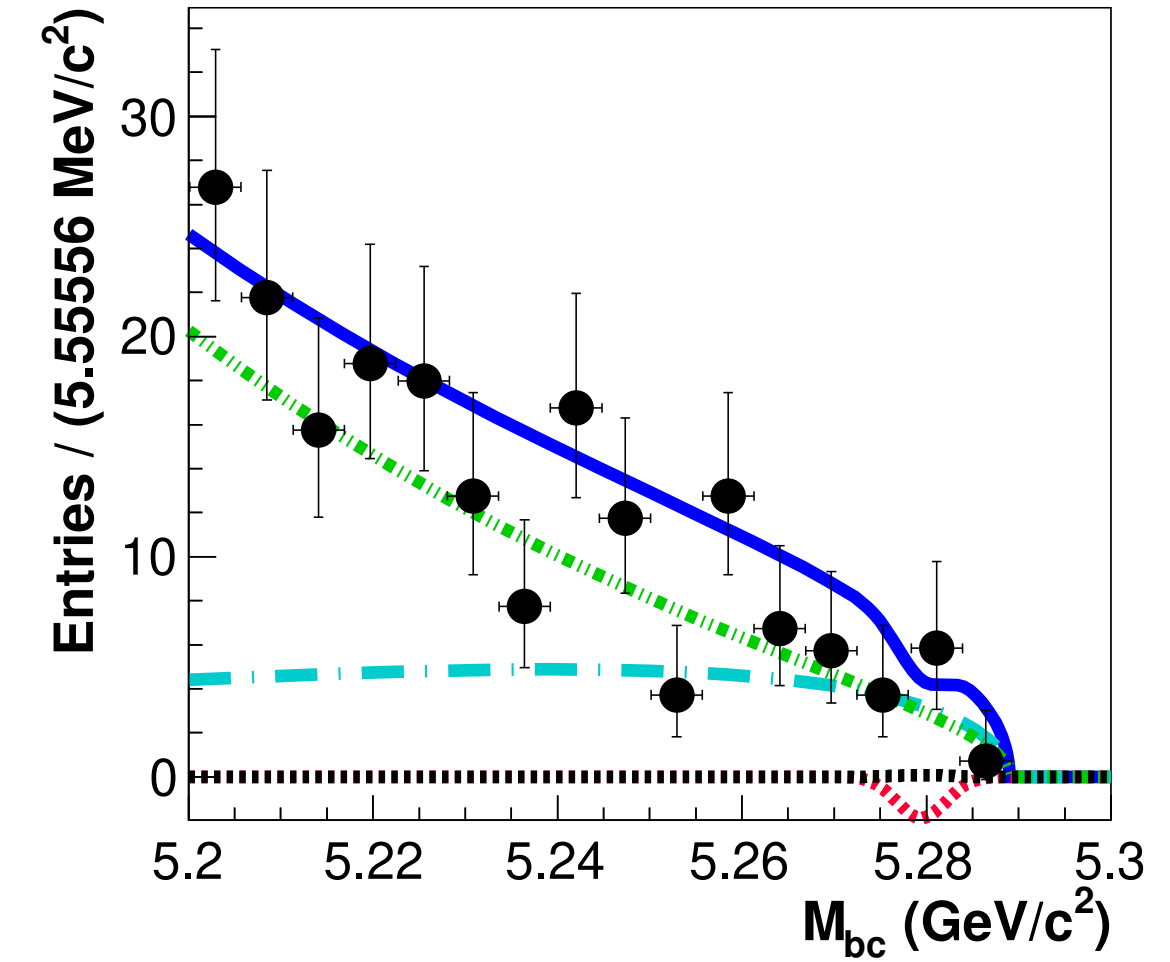
$$B^+ \rightarrow K^+ \mu^+ e^-$$



$$B^+ \rightarrow K^+ \mu^- e^+$$



$$B^0 \rightarrow K_S^0 \mu^- e^+$$



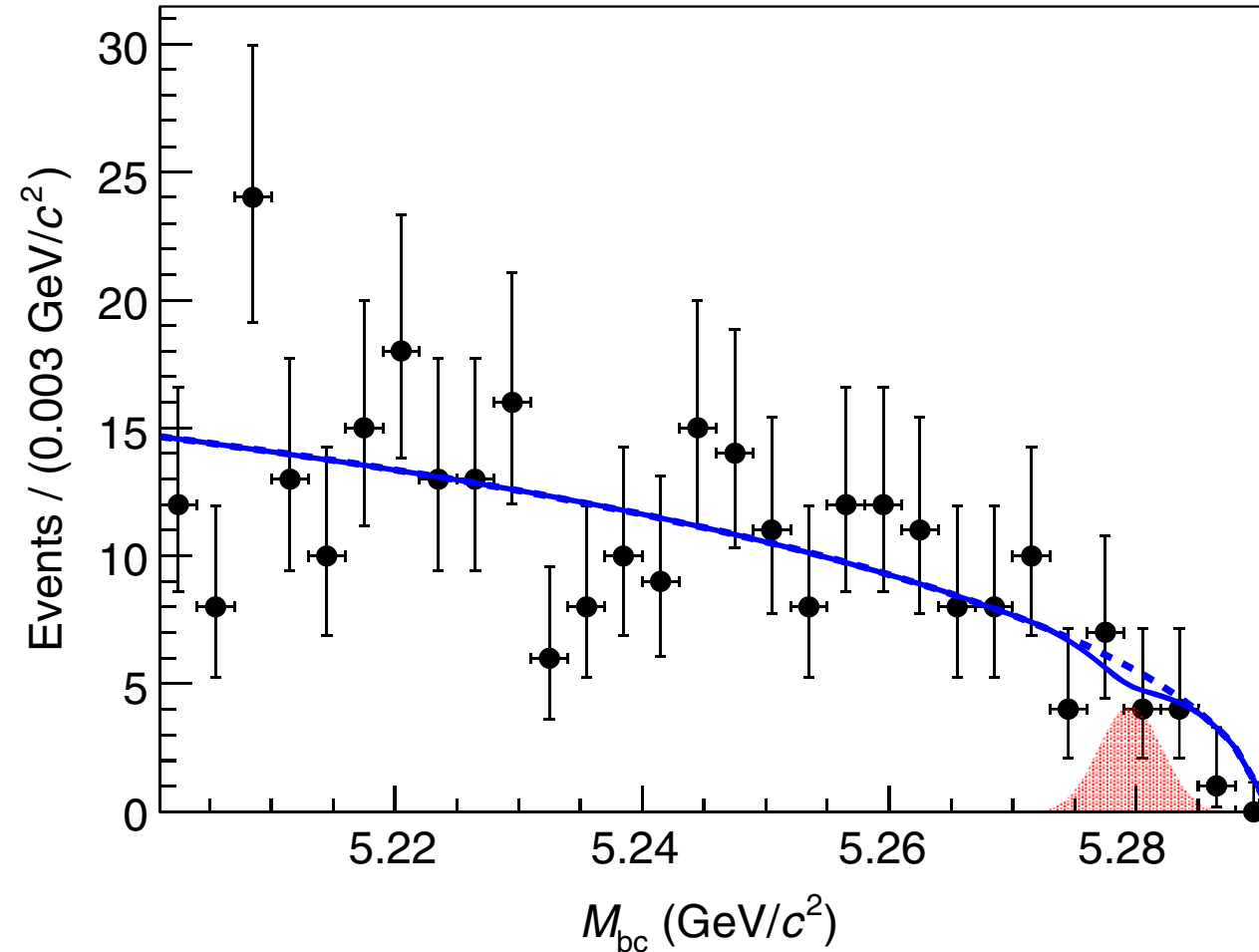
$$\mathcal{B}(B^+ \rightarrow K^+ \mu^+ e^-) < 8.5 \times 10^{-8}$$

$$\mathcal{B}(B^+ \rightarrow K^+ \mu^- e^+) < 3.0 \times 10^{-8}$$

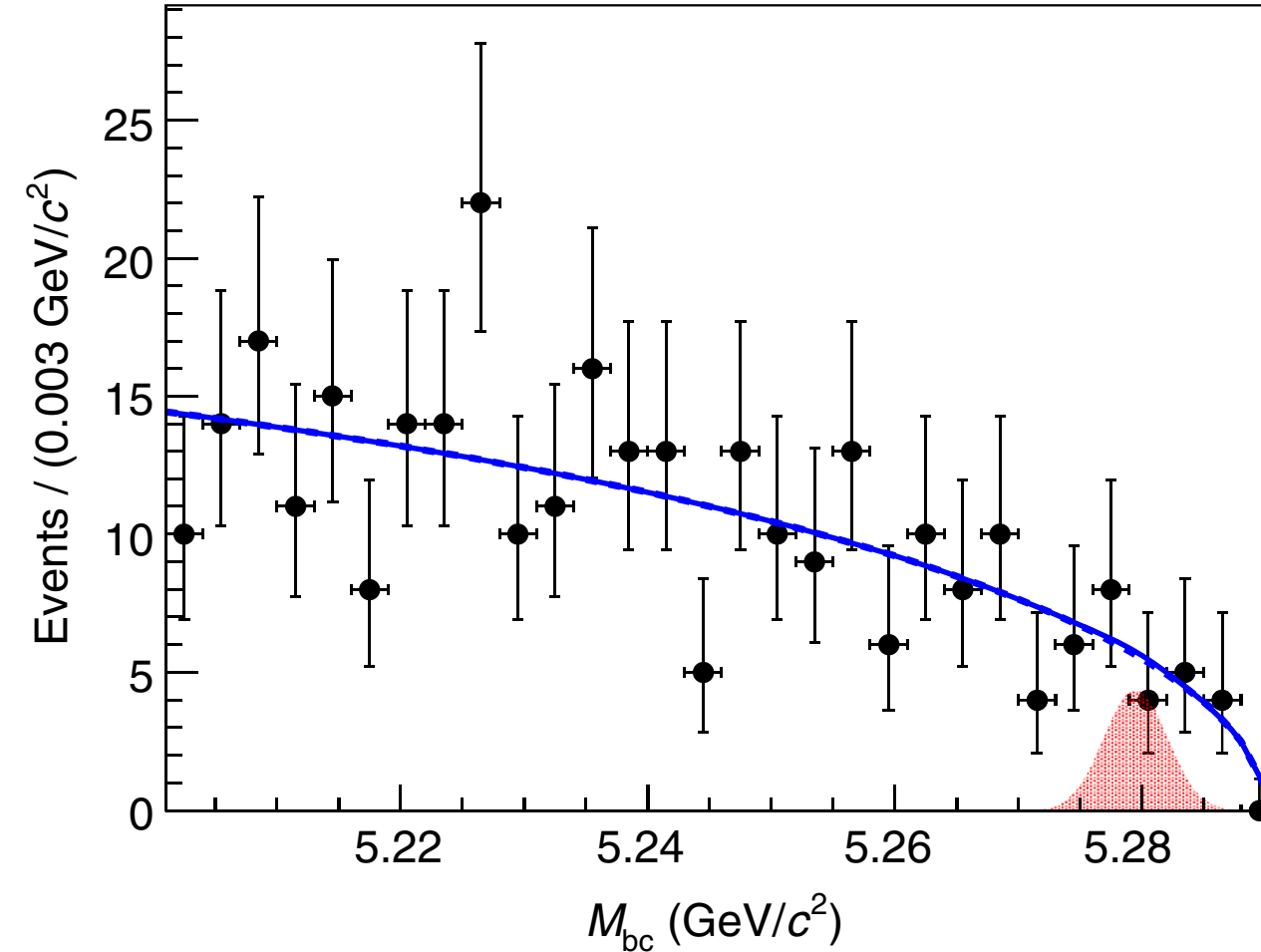
$$\mathcal{B}(B^0 \rightarrow K_S^0 \mu^- e^+) < 3.8 \times 10^{-8}$$

Search for the lepton-flavor-violating decay $B^0 \rightarrow K^{*0} \mu^\pm e^\mp$

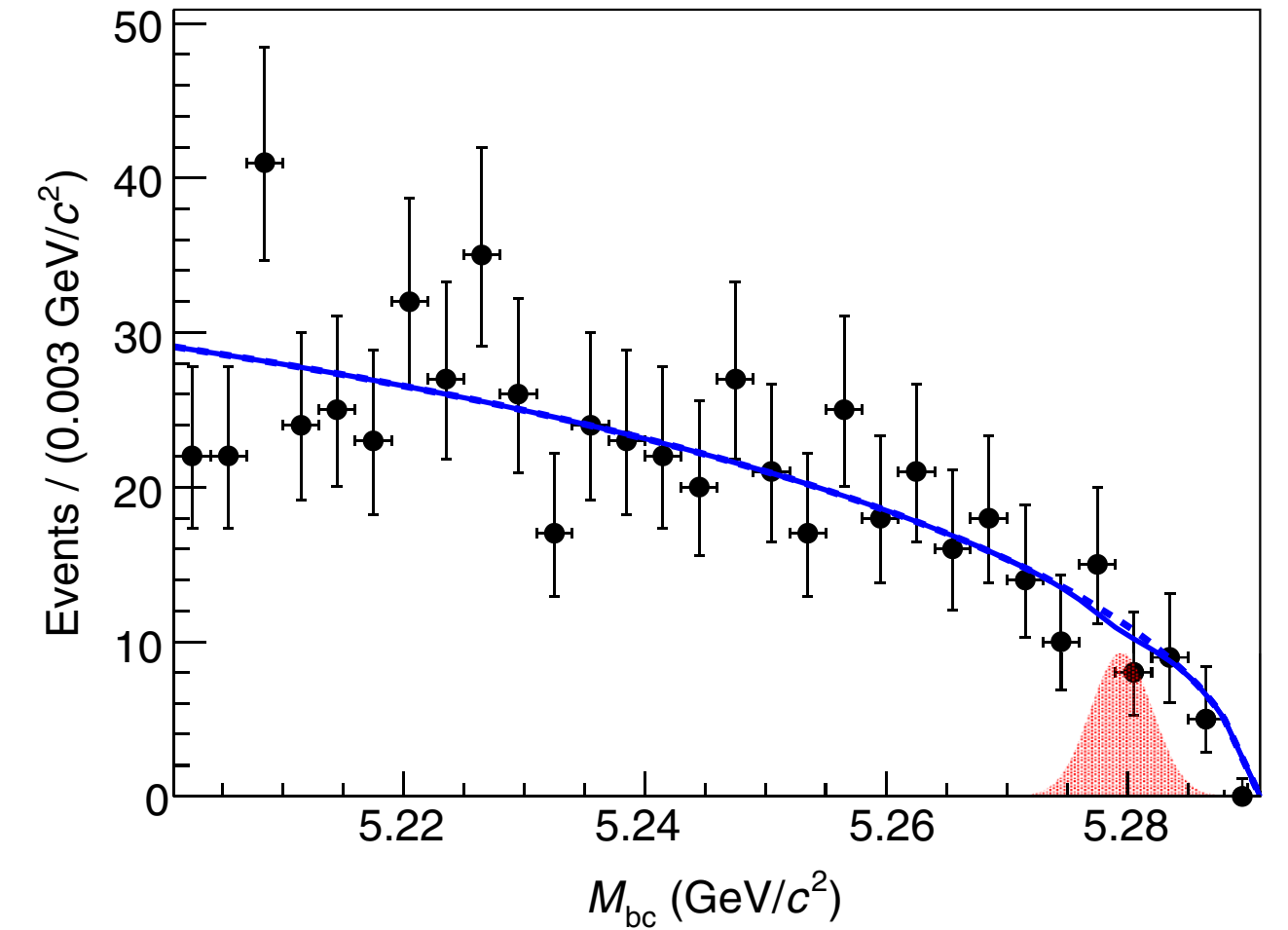
$$B^0 \rightarrow K^{*0} \mu^+ e^-$$



$$B^0 \rightarrow K^{*0} \mu^- e^+$$



$$B^0 \rightarrow K^{*0} \mu^\pm e^\mp$$



Mode	ϵ (%)	N_{sig}	$N_{\text{sig}}^{\text{UL}}$	\mathcal{B}^{UL} (10^{-7})
$B^0 \rightarrow K^{*0} \mu^+ e^-$	8.8	$-1.5^{+4.7}_{-4.1}$	5.2	1.2
$B^0 \rightarrow K^{*0} \mu^- e^+$	9.3	$0.4^{+4.8}_{-4.5}$	7.4	1.6
$B^0 \rightarrow K^{*0} \mu^\pm e^\mp$ (combined)	9.0	$-1.2^{+6.8}_{-6.2}$	8.0	1.8

BaBar
(2006)

5.3

3.4

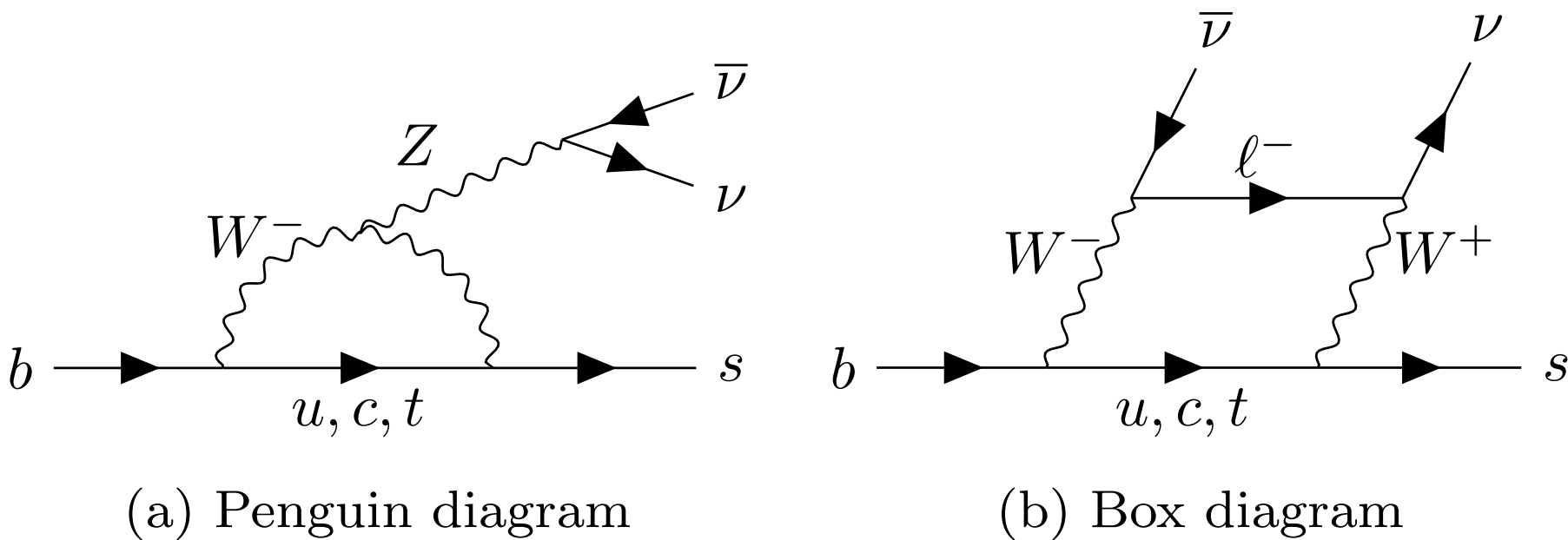
5.8

Invisible final states

- $B^+ \rightarrow K^+ \nu \bar{\nu}$ (Belle II)
- $B^0 \rightarrow \nu \bar{\nu}(\gamma)$

Search for $B^+ \rightarrow K^+ \nu \bar{\nu}$ at Belle II

- In the SM,
 - $\mathcal{B}(B^+ \rightarrow K^+ \nu \bar{\nu}) = (4.6 \pm 0.5) \times 10^{-6}$ [4]
- sensitive to new physics BSM, e.g.
 - leptoquarks,
 - axions,
 - DM particles, etc.



[4] T. Blake, G. Lanfranchi, and D. M. Straub, Prog. Part. Nucl. Phys. **92**, 50 (2017).

existing measurements (upper limits)

$B^+ \rightarrow K^+ \bar{\nu} \nu$					
$\Gamma(B^+ \rightarrow K^+ \bar{\nu} \nu) / \Gamma_{\text{total}}$					
Test for $\Delta B=1$ weak neutral current. Allowed by higher-order electroweak interactions.					
VALUE	CL%	DOCUMENT ID	TECN	COMMENT	
$< 1.6 \times 10^{-5}$	90	1, 2 LEES	2013	BABR	$e^+ e^- \rightarrow Y(4S)$
... We do not use the following data for averages, fits, limits, etc. ...					
$< 1.9 \times 10^{-5}$	90	3, 1 GRYGIER	2017	BELL	$e^+ e^- \rightarrow Y(4S)$
$< 5.5 \times 10^{-5}$	90	1 LUTZ	2013	BELL	$e^+ e^- \rightarrow Y(4S)$

Tagging

hadronic + SL

semileptonic
hadronic

$B^+ \rightarrow K^+ \nu \bar{\nu}$ at Belle II

1. signal K^+ — track of highest p_T w/ at least 1 PXD hit ($\varepsilon \sim 80\%$)

2. all other tracks & clusters \Rightarrow “ROE” (rest of event)

3. BDT for signal discrimination

use event-shape, ROE dynamics, B_{sig} kinematics, v_{sig}

4. BDT₁ & BDT₂ (consecutive applications)

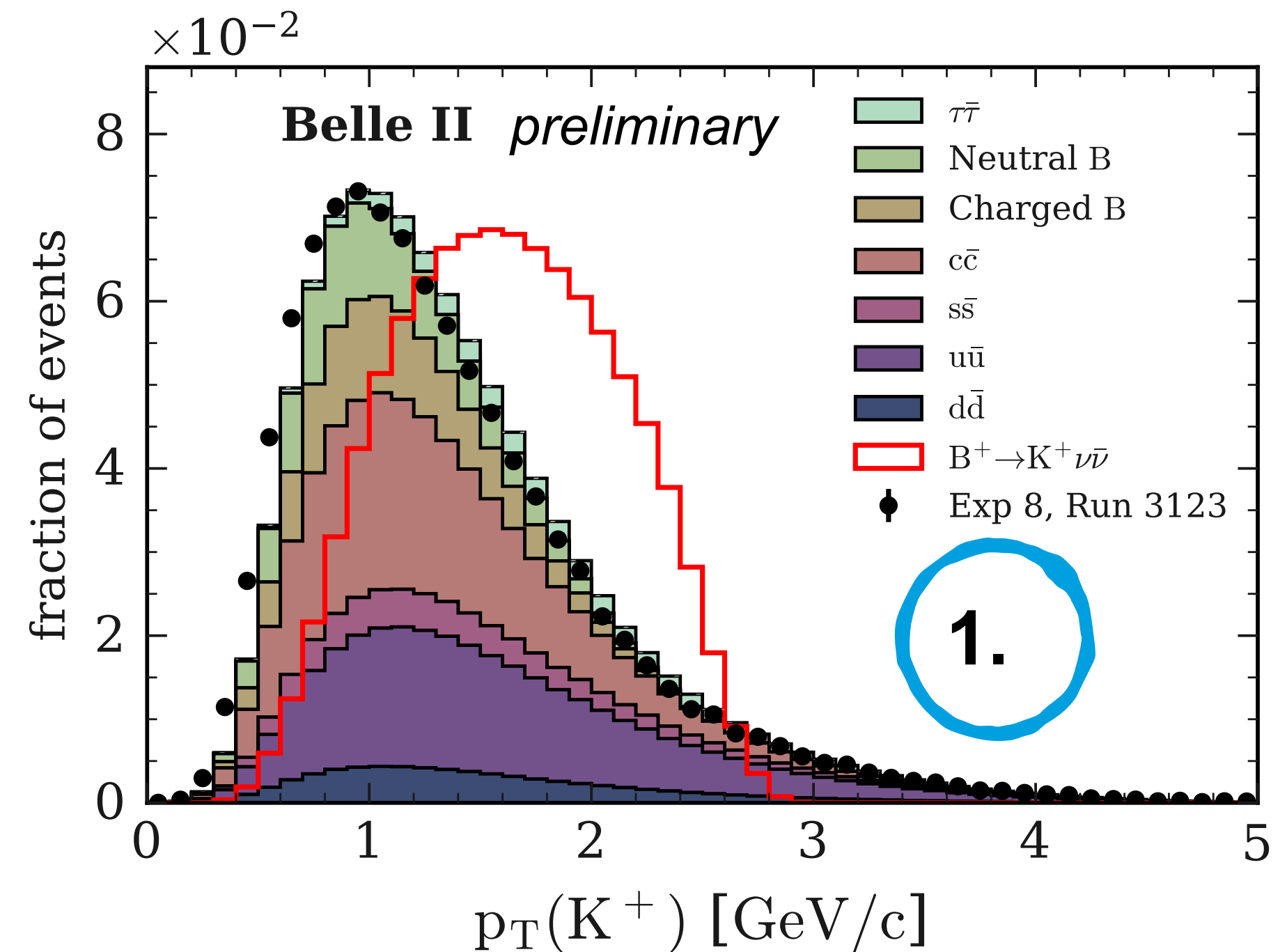
\therefore to suppress two different bkgds : BB and continuum

5. signal region in 2D (BDT₂ vs. $p_T(K^+)$)

6. check BDT output with $B^+ \rightarrow J/\psi K^+$ sample

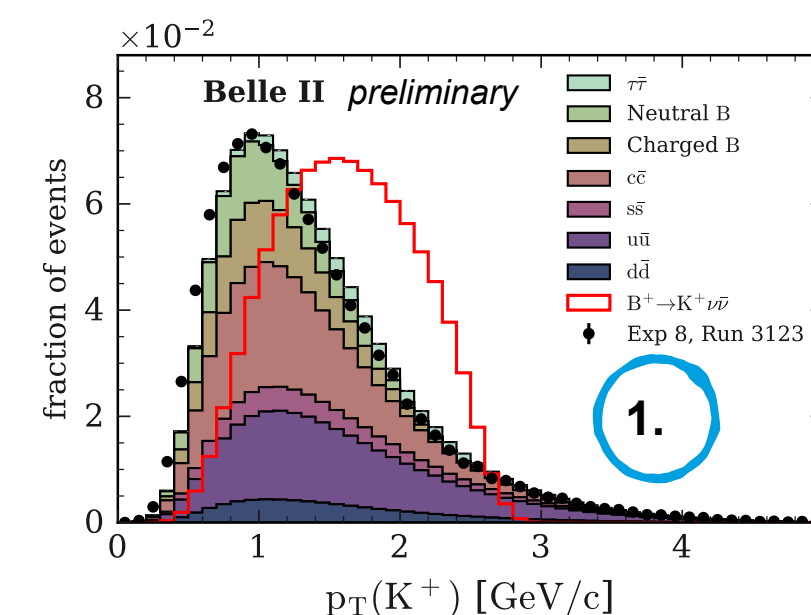
for both signal and bkgd (see *back-up slide for details*)

7. check Data/MC agreement using Off-resonance data

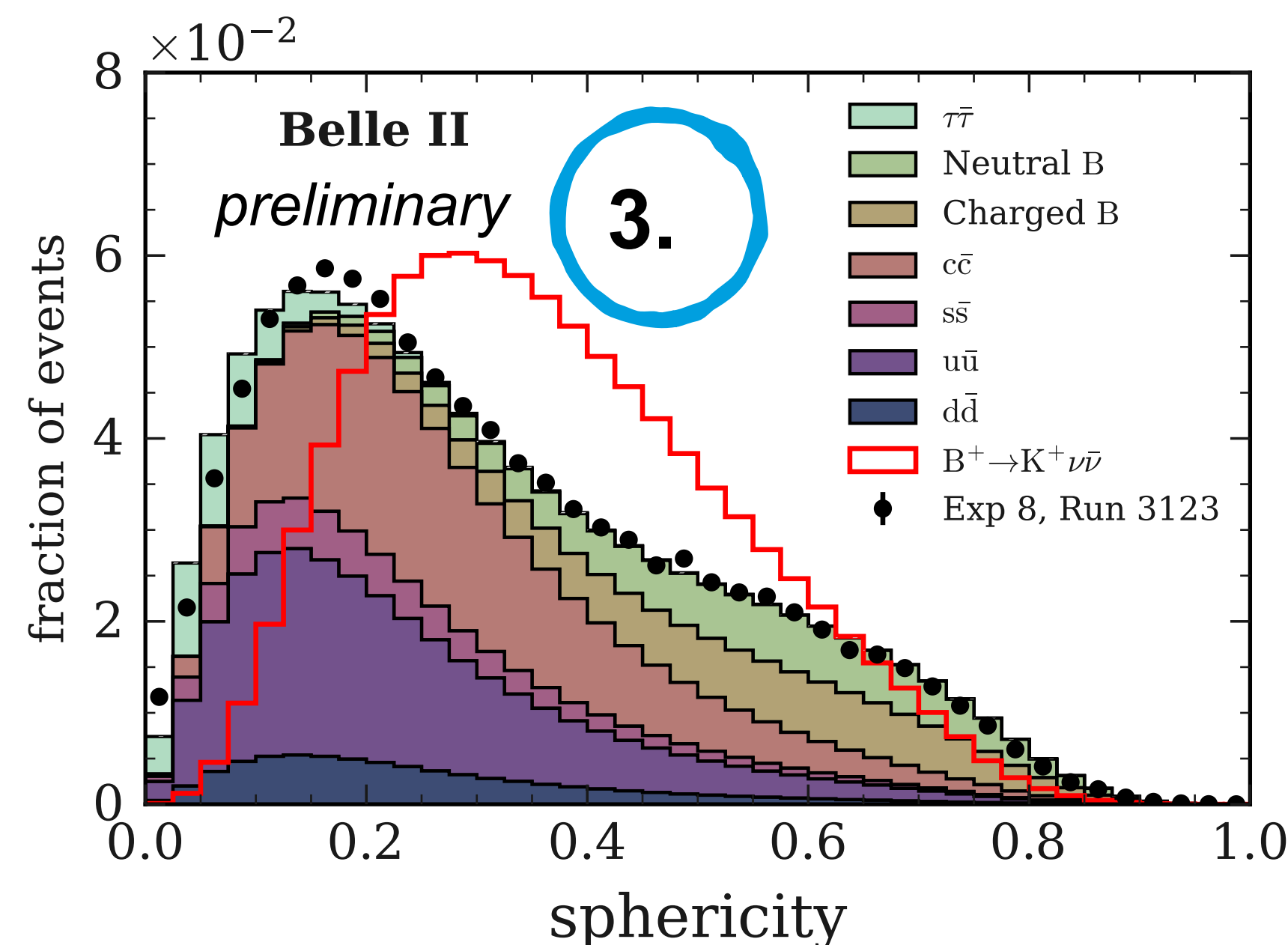


$B^+ \rightarrow K^+ \nu \bar{\nu}$ at Belle II

1. signal K^+ — track of highest p_T w/ at least 1 PXD hit ($\varepsilon \sim 80\%$)
2. all other tracks & clusters \Rightarrow “ROE” (rest of the event)
3. BDT for signal discrimination
use event-shape, ROE dynamics, B_{sig} kinematics, vertexing info.

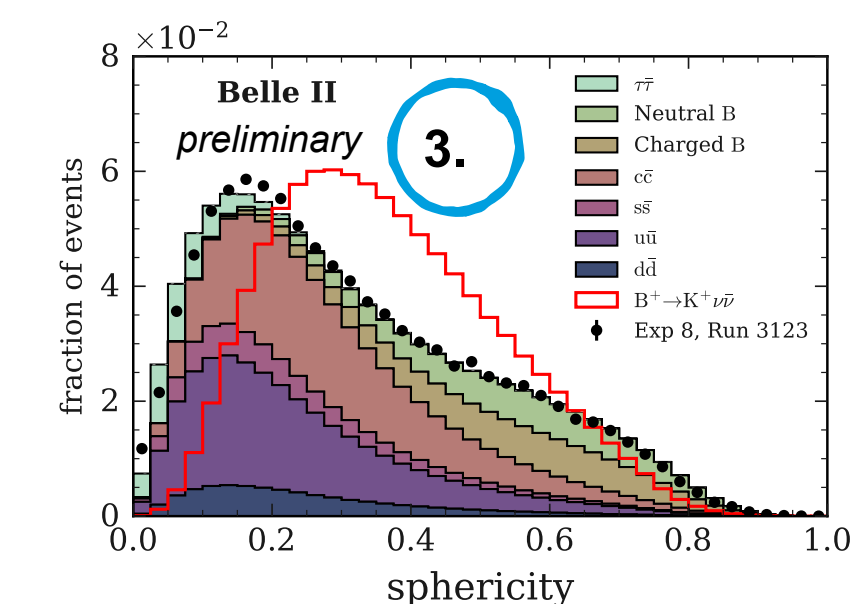
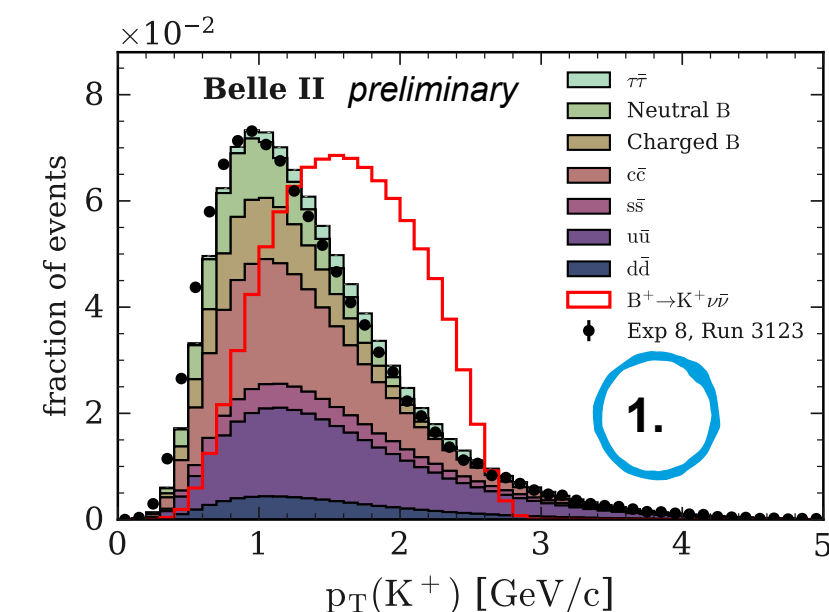


4. BDT₁ & BDT₂ (consecutive applications)
 \because to suppress two different bkgds : BB and continuum
5. signal region in 2D (BDT₂ vs. $p_T(K^+)$)
6. check BDT output with $B^+ \rightarrow J/\psi K^+$ samples
for both signal and bkgd (see *back-up slide for details*)
7. check Data/MC agreement using Off-resonance

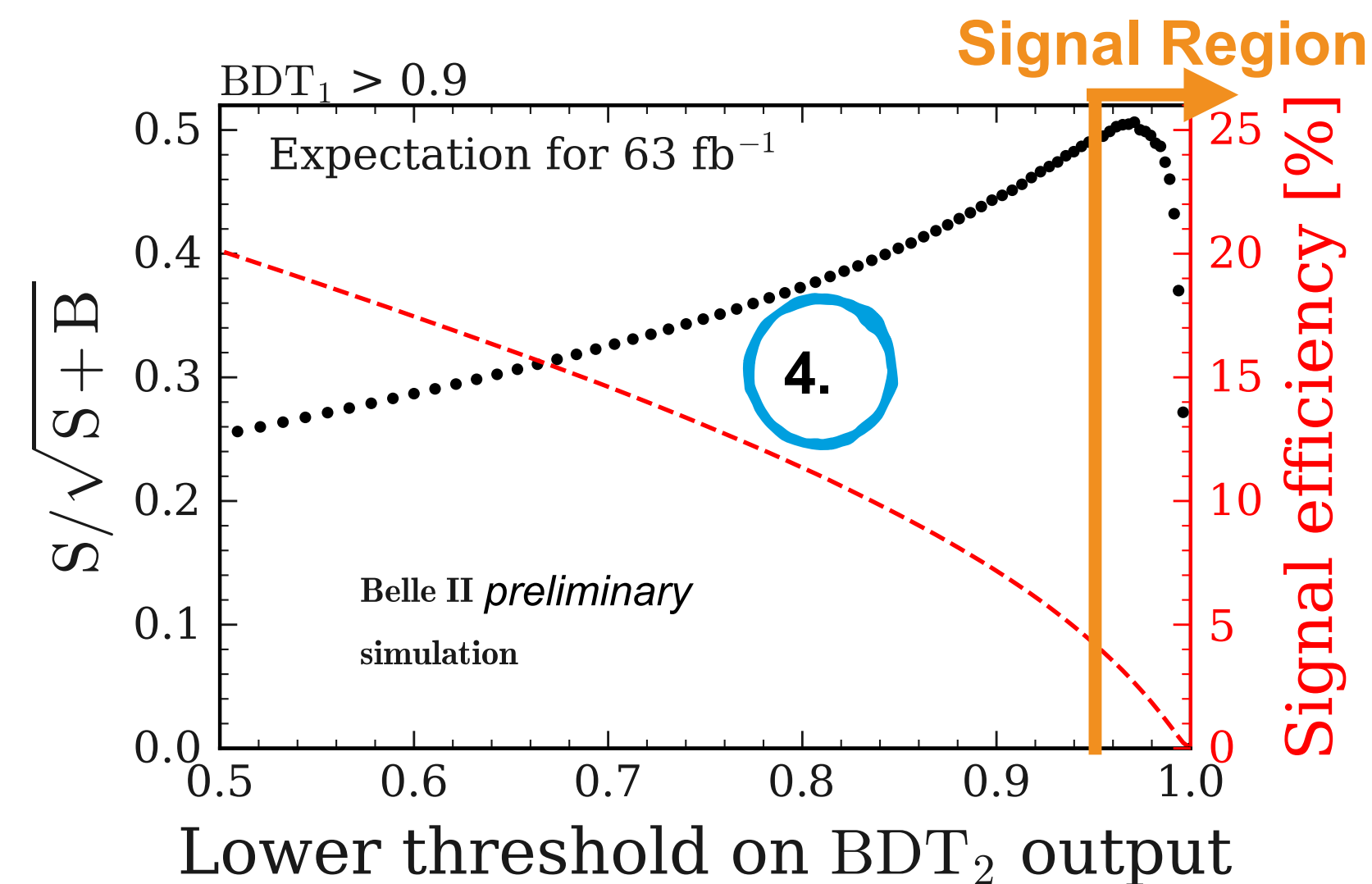


$B^+ \rightarrow K^+ \nu \bar{\nu}$ at Belle II

1. signal K^+ — track of highest p_T w/ at least 1 PXD hit ($\varepsilon \sim 80\%$)
2. all other tracks & clusters \Rightarrow “ROE” (rest of the event)
3. BDT for signal discrimination
use event-shape, ROE dynamics, B_{sig} kinematics, vertexing info.
4. BDT₁ & BDT₂ (consecutive applications)
 \because to suppress two different bkgds : BB and continuum



5. signal region in 2D (BDT₂ vs. $p_T(K^+)$)
6. check BDT output with $B^+ \rightarrow J/\psi K^+$ samples
for both signal and bkgd (see *back-up slide for details*)
7. check Data/MC agreement using Off-resonance d



$B^+ \rightarrow K^+ \nu \bar{\nu}$ at Belle II

1. signal K^+ — track of highest p_T w/ at least 1 PXD hit ($\varepsilon \sim 80\%$)

2. all other tracks & clusters \Rightarrow “ROE” (rest of the event)

3. BDT for signal discrimination

use event-shape, ROE dynamics, B_{sig} kinematics, vertexing info.

4. BDT₁ & BDT₂ (consecutive applications)

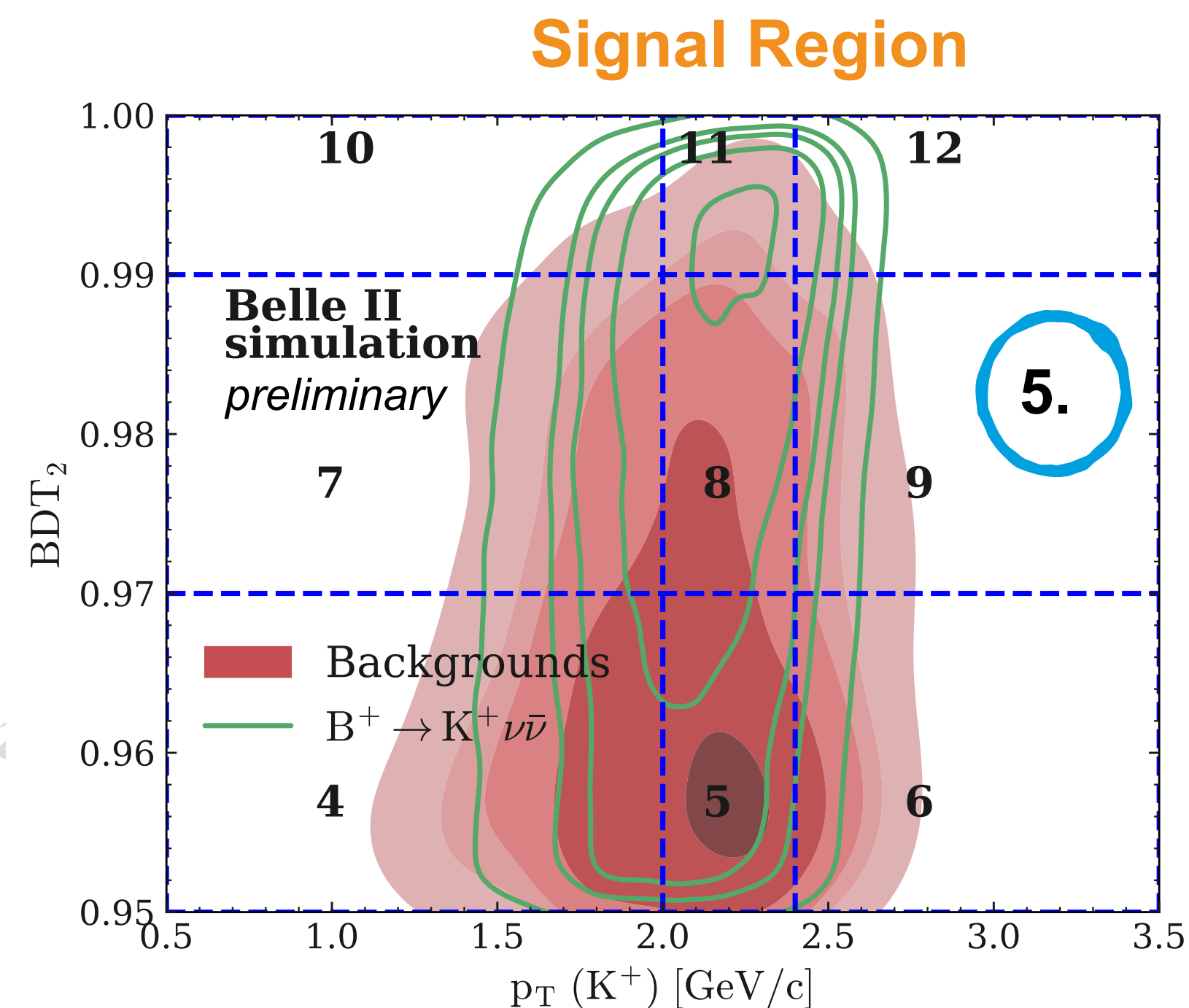
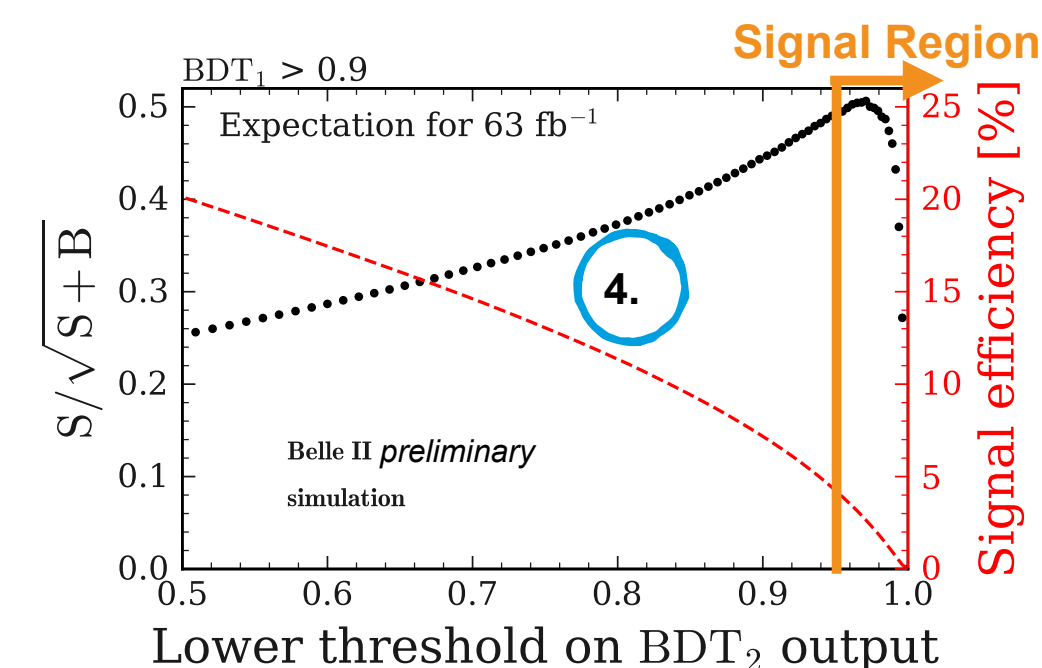
\because to suppress two different bkgds : BB and continuum

5. signal region in 2D (BDT₂ vs. $p_T(K^+)$)

6. check BDT output with $B^+ \rightarrow J/\psi K^+$ samples

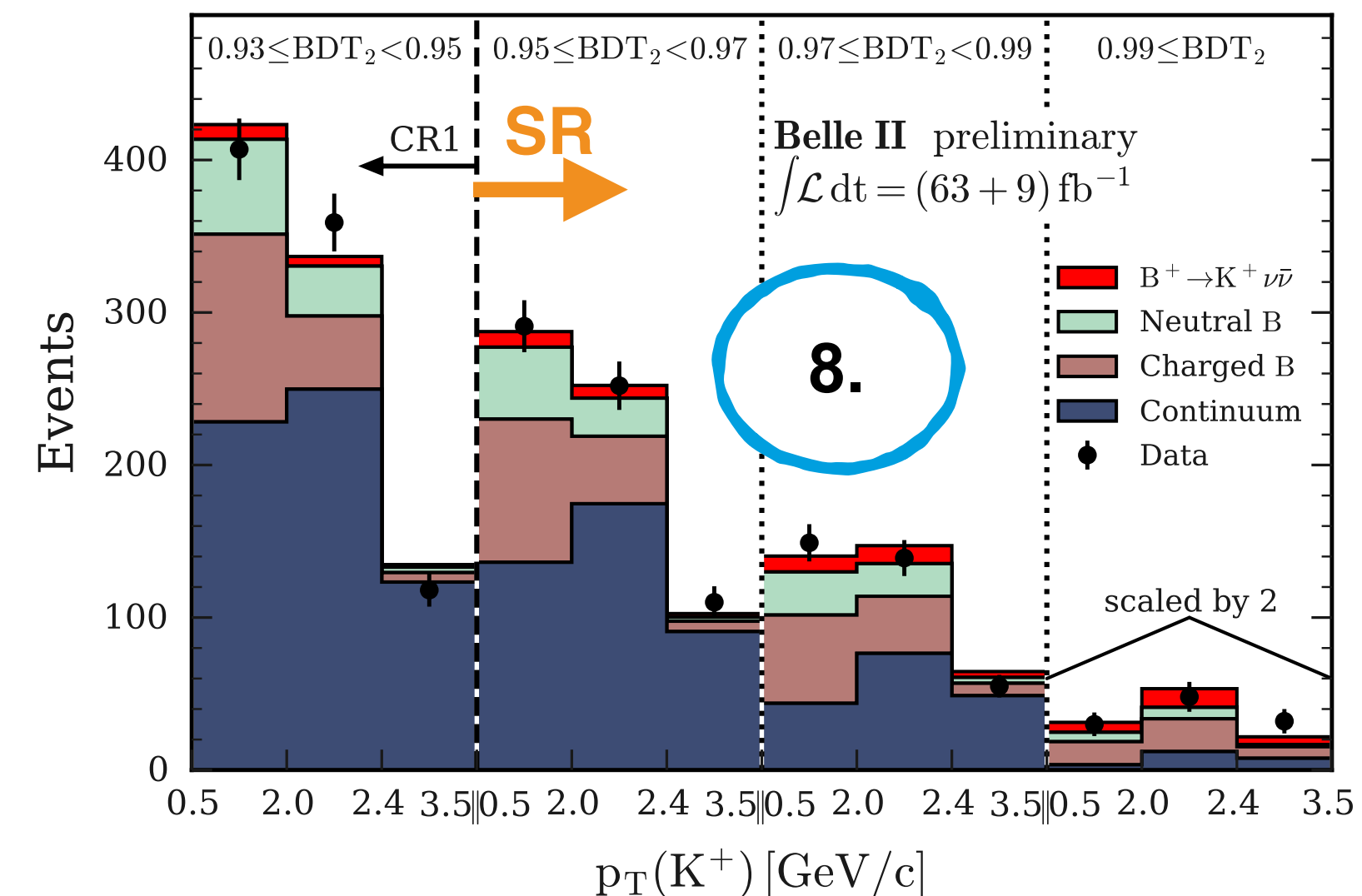
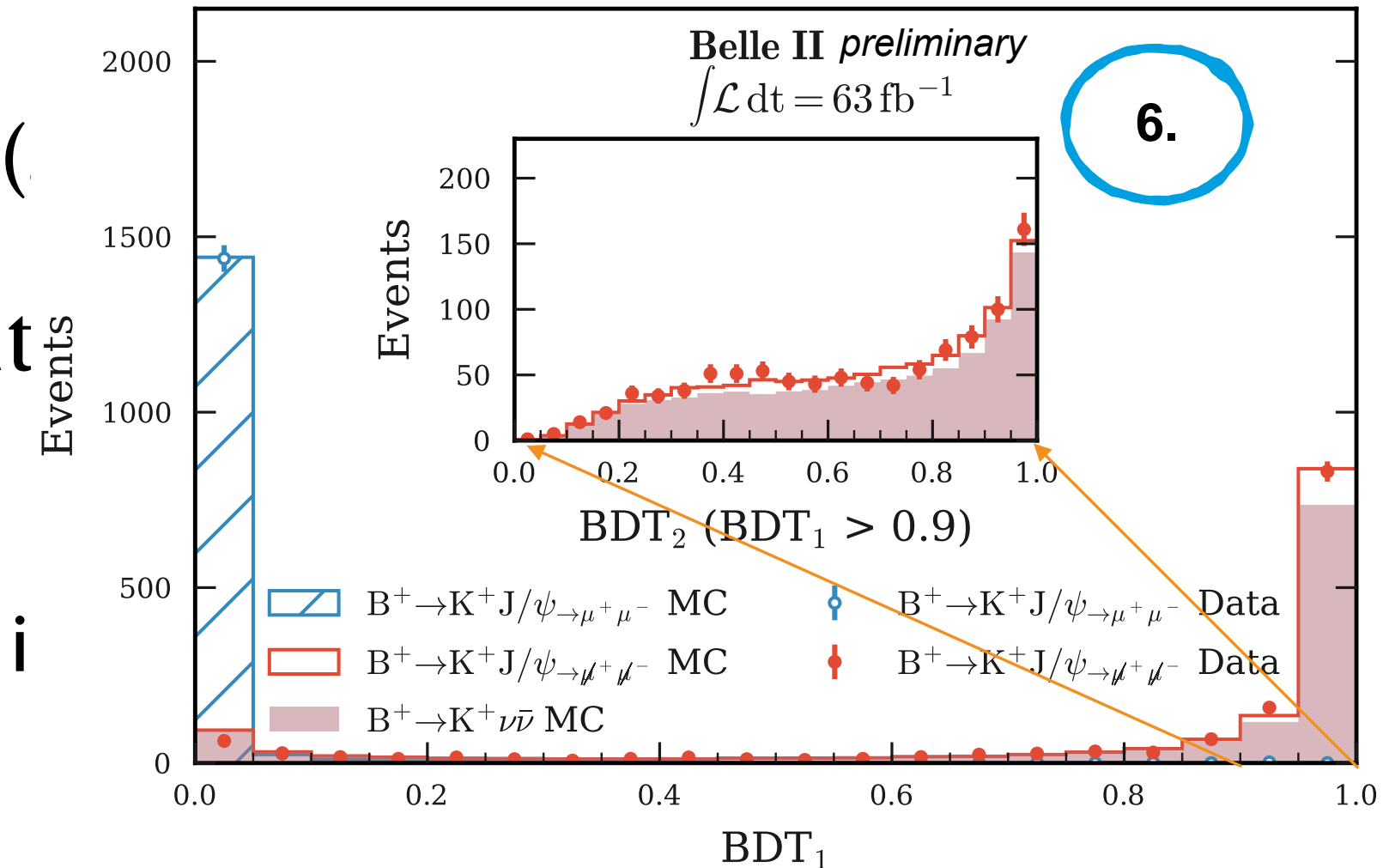
for both signal and bkgd (see *back-up slide for details*)

7. check Data/MC agreement using Off-resonance data

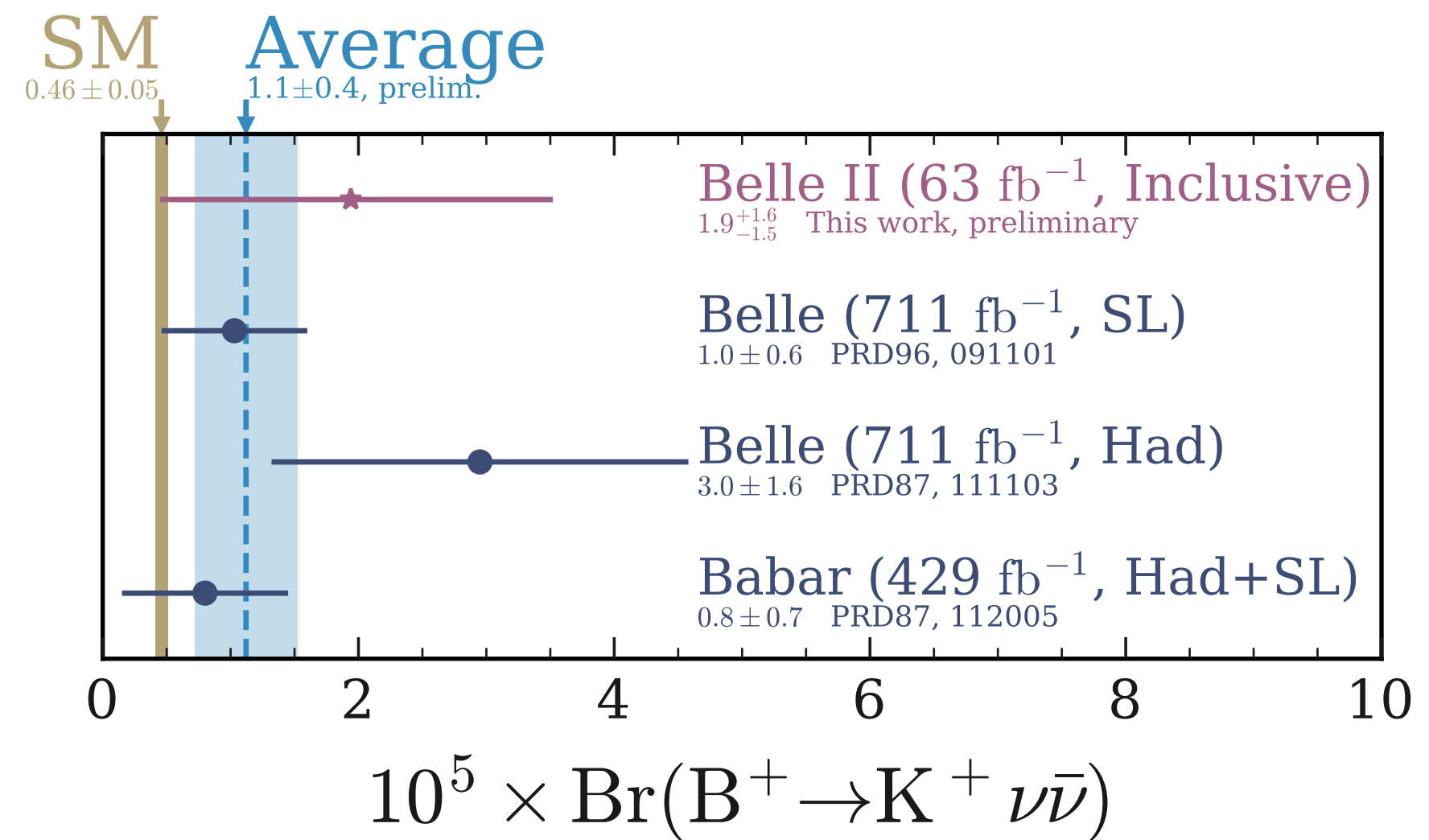
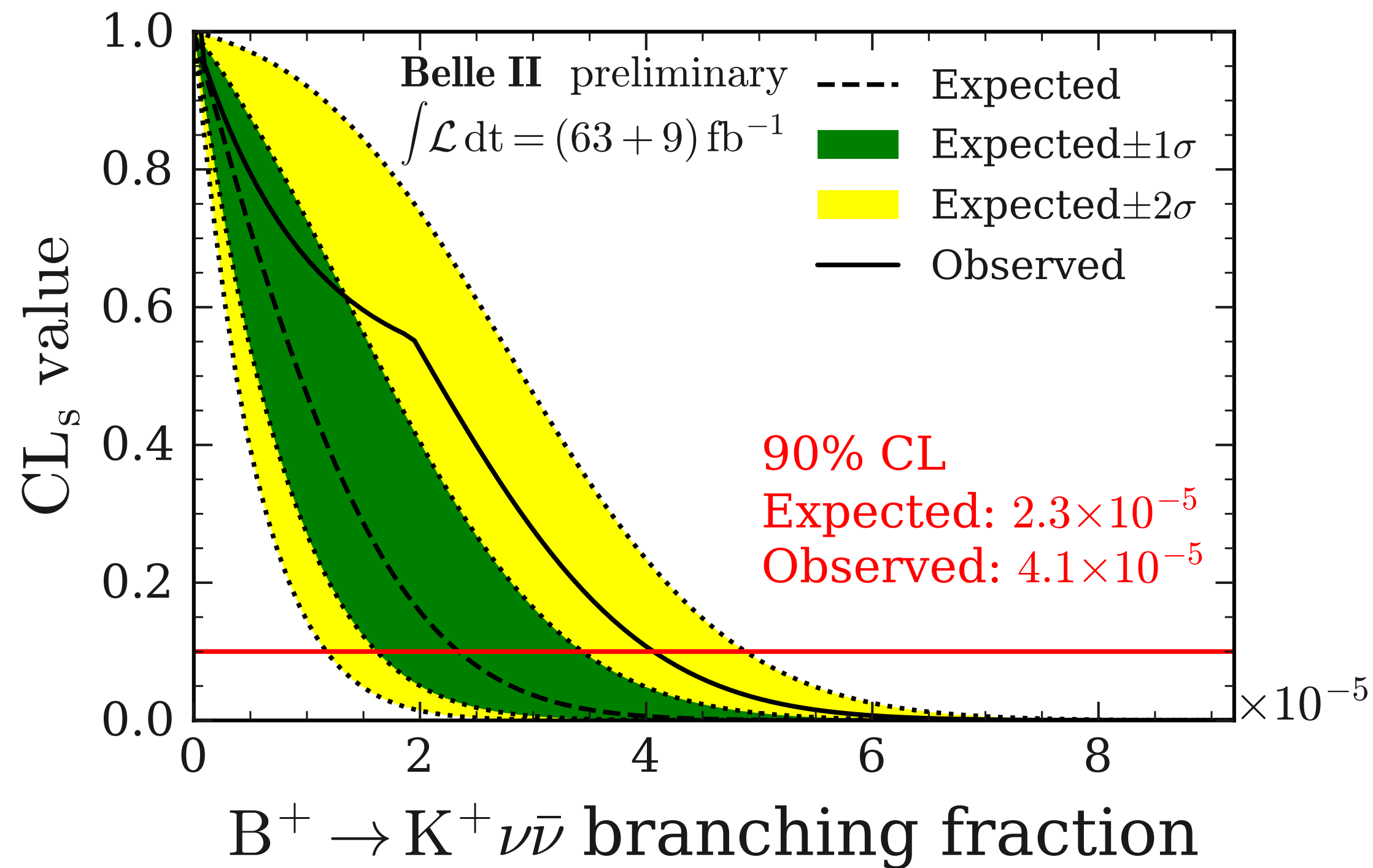


$B^+ \rightarrow K^+ \nu \bar{\nu}$ at Belle II

1. signal K^+ — track of highest p_T w/ at least 1 PXD hit (
2. all other tracks & clusters \Rightarrow “ROE” (rest of the event
3. BDT for signal discrimination
use event-shape, ROE dynamics, B_{sig} kinematics, vertexing i
4. BDT₁ & BDT₂ (consecutive applications)
 \because to suppress two different bkgds : BB and continuum
5. signal region in 2D (BDT₂ vs. $p_T(K^+)$)
6. check BDT output with $B^+ \rightarrow J/\psi K^+$ samples
for both signal and bkgd (see *the paper for details*)
7. Data/MC agreement using OFF-resonance data
8. simultaneous ML fit to ON- & OFF-resonance data



$B^+ \rightarrow K^+ \nu \bar{\nu}$ at Belle II



$$\mathcal{B}(B^+ \rightarrow K^+ \nu \bar{\nu}) = (1.9^{+1.3+0.8}_{-1.3-0.7}) \times 10^{-5}$$

$$< 4.1 \times 10^{-5} \quad @ 90\% \text{ CL}$$

$B^0 \rightarrow \textit{invisible} (+\gamma)$



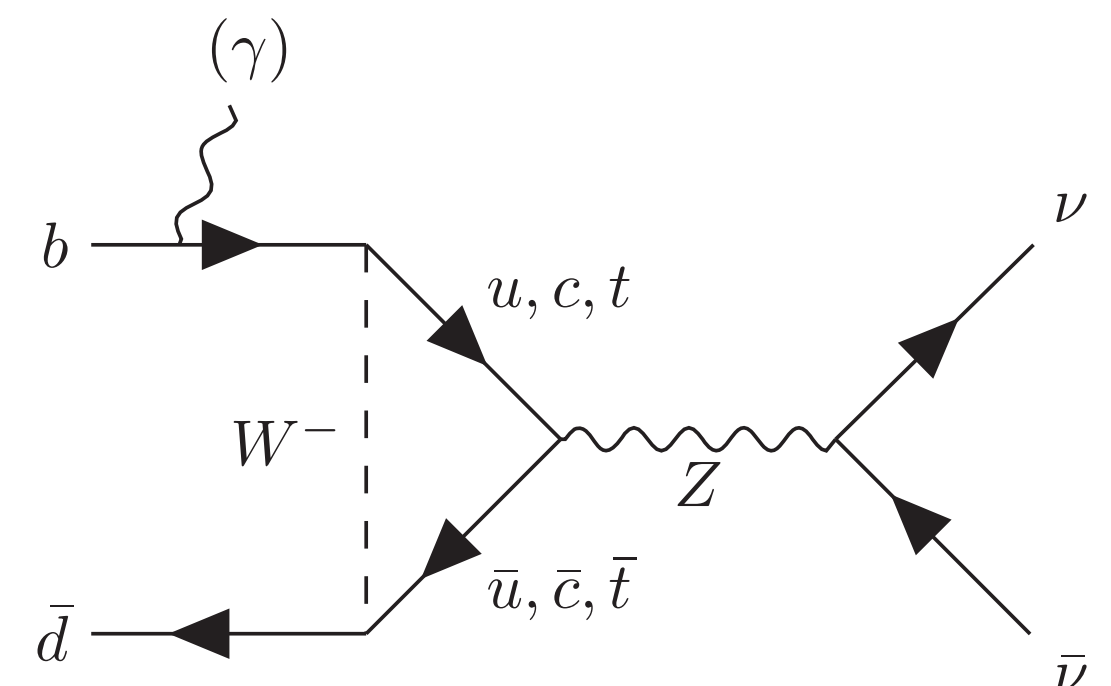
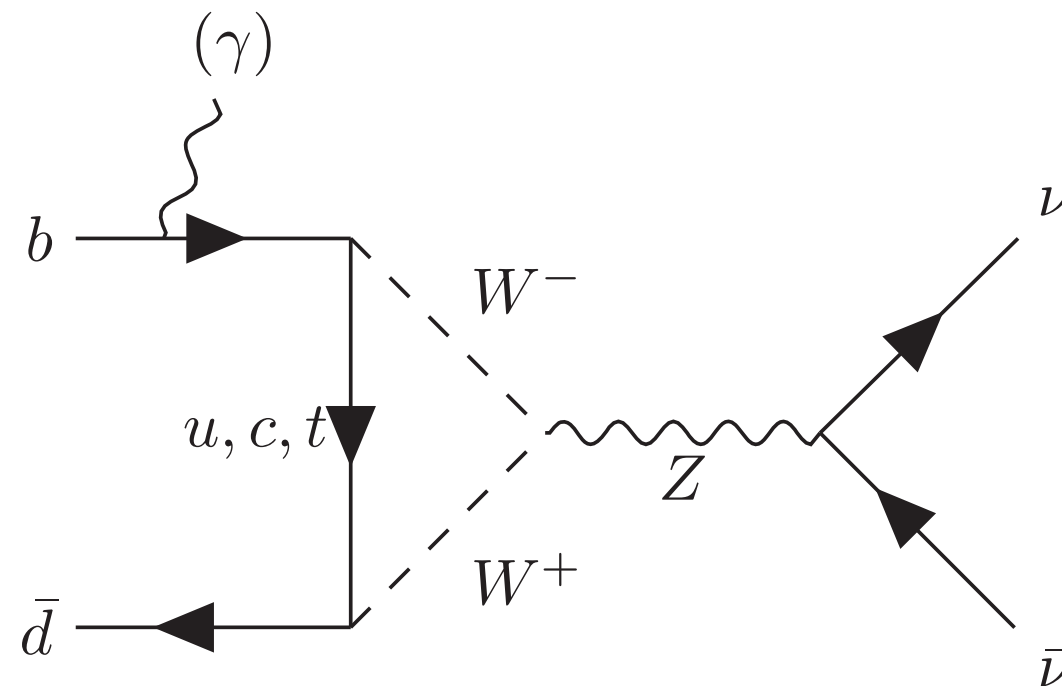
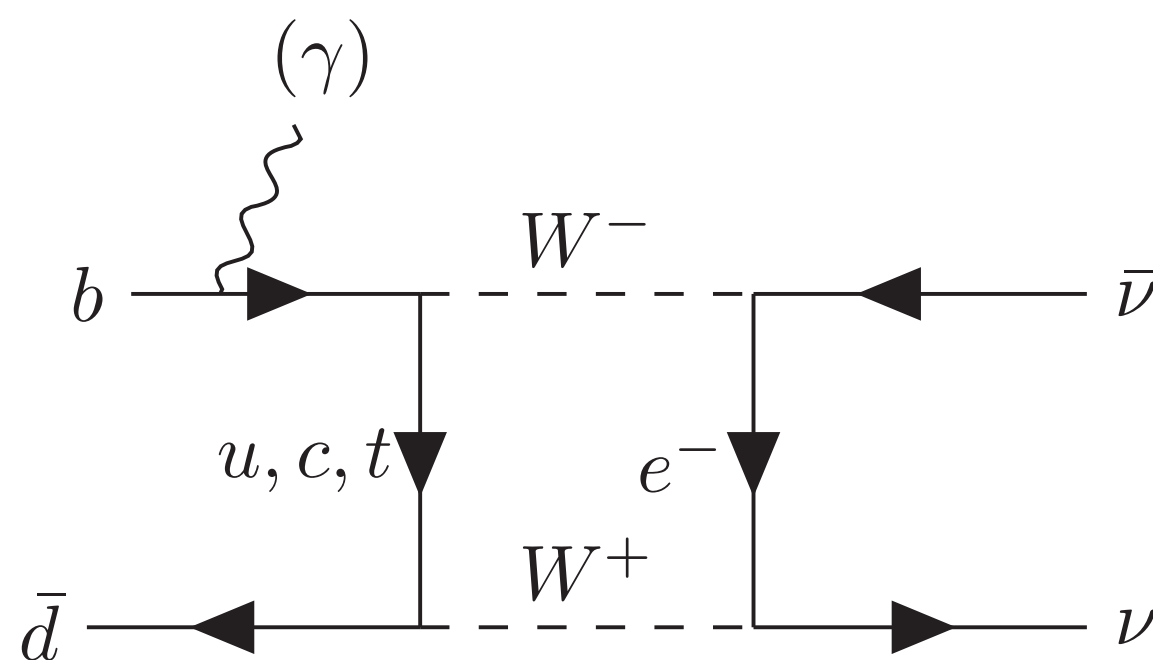
In the SM

- $\mathcal{B}(B^0 \rightarrow \nu\bar{\nu}) \sim 10^{-25}$, $\mathcal{B}(B^0 \rightarrow \nu\bar{\nu}\nu\bar{\nu}) \sim 10^{-16}$, $\mathcal{B}(B^0 \rightarrow \gamma\nu\bar{\nu}) \sim 10^{-9}$



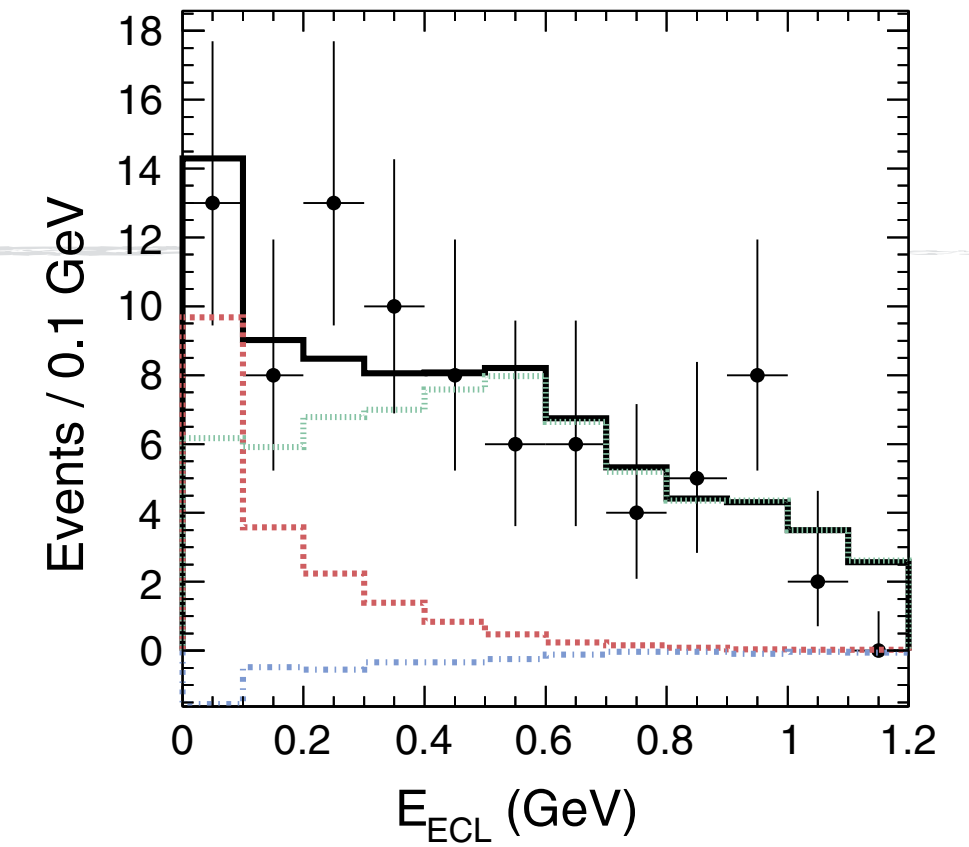
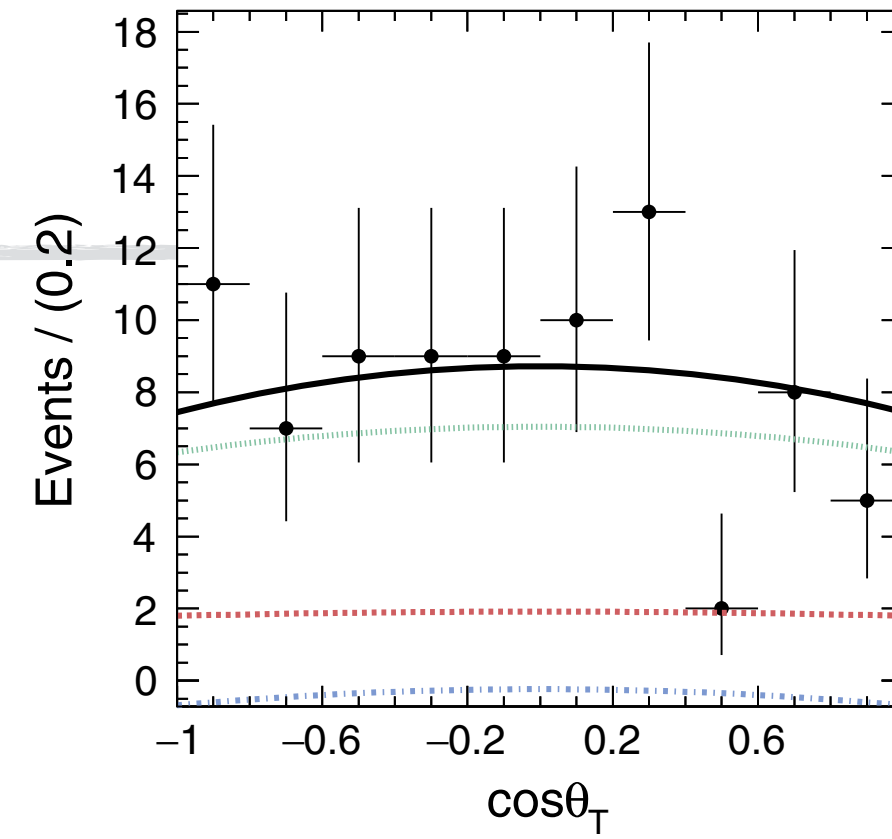
sensitive to new physics BSM, e.g.

- R-parity-violating models
- dark matter contributions
- some models predict $\mathcal{B} \lesssim \mathcal{O}(10^{-6} - 10^{-7})$

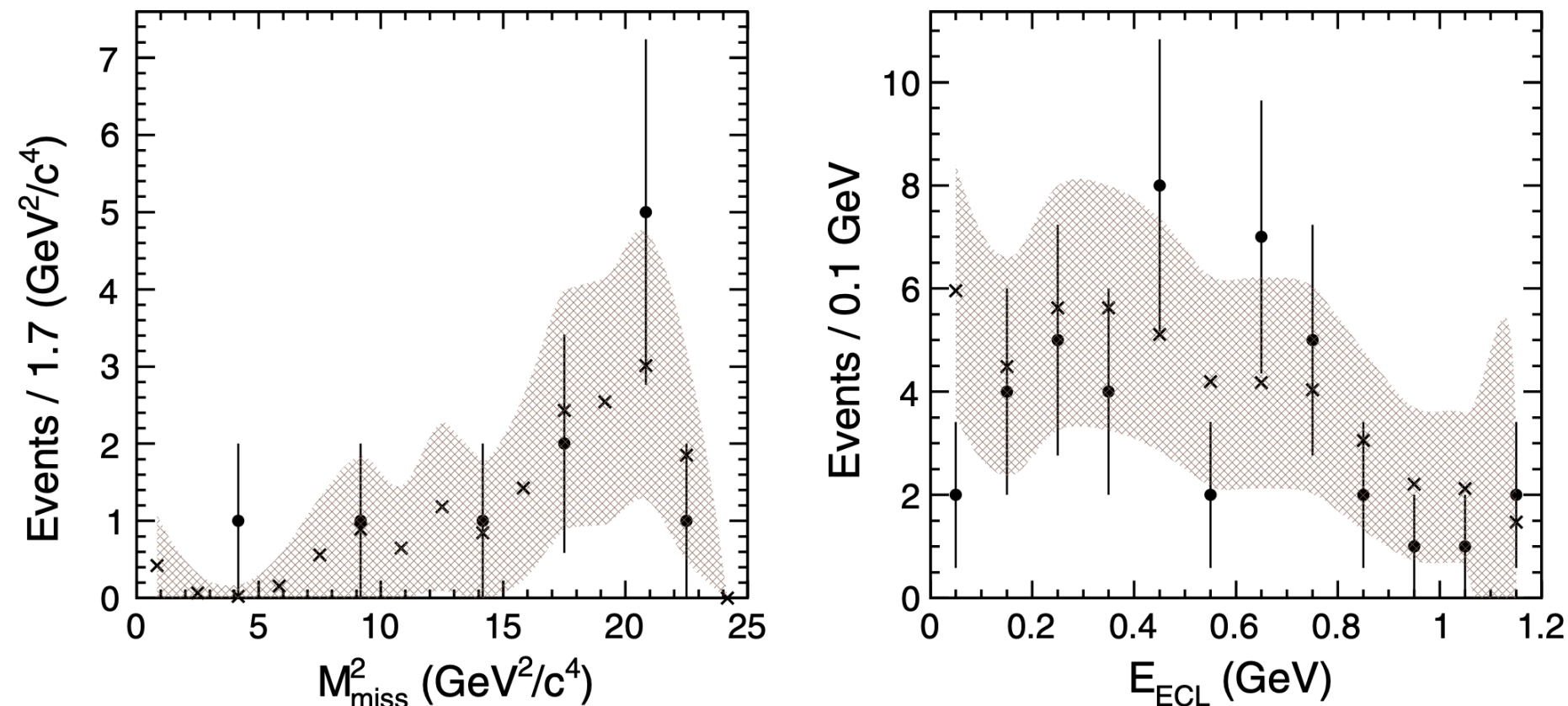


$B^0 \rightarrow \text{invisible} (+\gamma)$

- $B^0 \rightarrow \text{inv.}$ signal extraction
 - by 2D fit to $(E_{\text{ECL}}, \cos \theta_T)$
 - $N_{\text{sig}} = 18.8^{+15.3}_{-14.5}$
- $B^0 \rightarrow \text{inv.} + \gamma$ signal extraction
 - counting in E_{ECL} with bkgd. subtraction
 - study M_{miss}^2 for bkgd. evaluation using control mode, $B^0 \rightarrow D^- \ell^+ \nu$



$$\mathcal{B}(B^0 \rightarrow \text{invisible}) < 7.8 \times 10^{-5} @ 90\% \text{ CL}$$



$$\mathcal{B}(B^0 \rightarrow \text{invisible} + \gamma) < 1.6 \times 10^{-5} @ 90\% \text{ CL}$$

LFV, LNV & BNV searches in τ decays

$$\tau^- \rightarrow \mu^- \gamma$$

$$\tau^- \rightarrow e^- \gamma$$

preliminary, to be submitted to JHEP

$$\tau^- \rightarrow \bar{p} e^+ e^-$$

$$\tau^- \rightarrow \bar{p} e^+ \mu^-$$

PRD 102, 111101 (2020)

$$\tau^- \rightarrow p \mu^- \mu^-$$




$$\tau^- \rightarrow p e^- e^-$$

$$\tau^- \rightarrow \bar{p} e^- \mu^+$$

$$\tau^- \rightarrow \bar{p} \mu^- \mu^+$$

New physics (NP) search with τ

- the τ lepton
 - the heaviest charged lepton
 - highly sensitive to NP
- Unique lab to look for NP
 - **LFV**
 - EDM, $g-2$, CPV
 - B (D) decays to τ
 - BNV, too ($m_\tau > m_\Lambda, m_p, \dots$)

	electron	muon	tau
			
Gen.	I	II	III
Mass [MeV]	0.511	106	1780
Life	∞	$2.20\mu\text{s}$	0.291ps

Lepton-flavor-violating (LFV) τ decay

- In the Standard Model with non-zero ν mass, τ LFV can happen, but the rate is really tiny.

$$\mathcal{B}(\tau \rightarrow l\gamma) = \frac{3\alpha}{32\pi} \left| \sum_i U_{\tau i}^* U_{\mu i} \frac{\Delta_{3i}^2}{m_W^2} \right|^2 \leq 10^{-53} \sim 10^{-49}$$

- However, in many new physics models it can become large enough to be within sensitivity of Belle (or Belle-II)

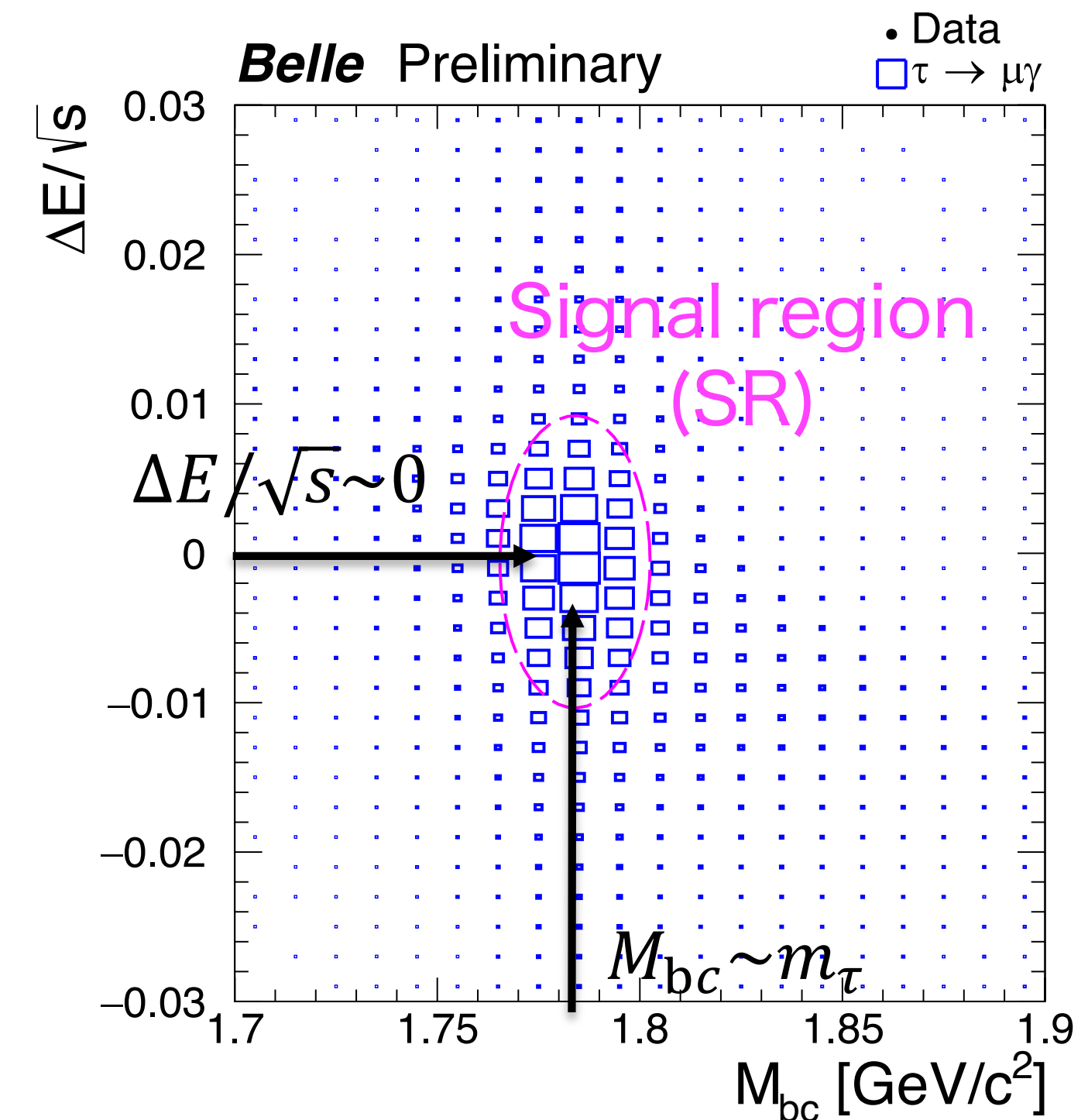
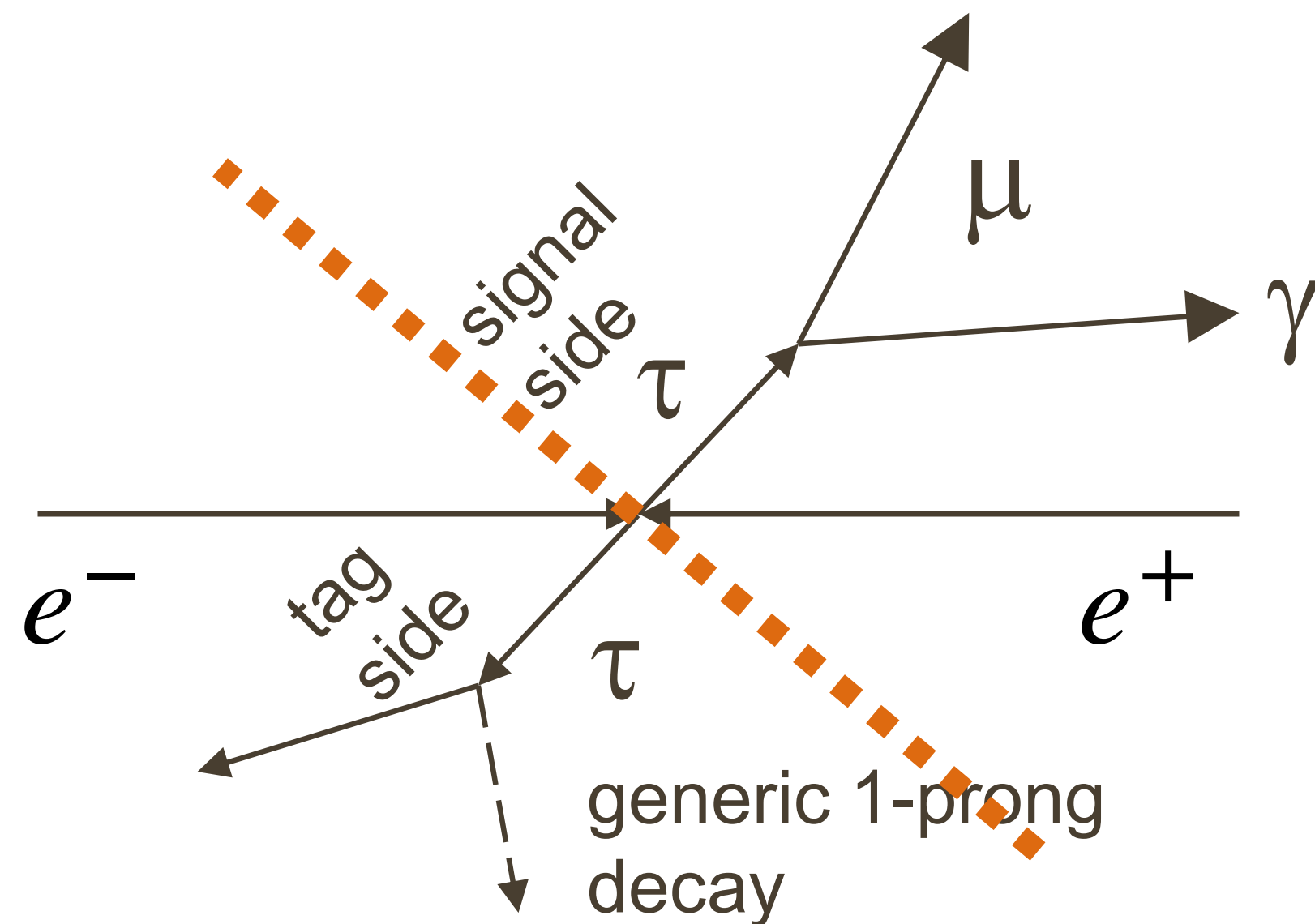
- For example, with SUSY-GUT,

Calibbi et al.,
PRD 74, 116002 (2006)

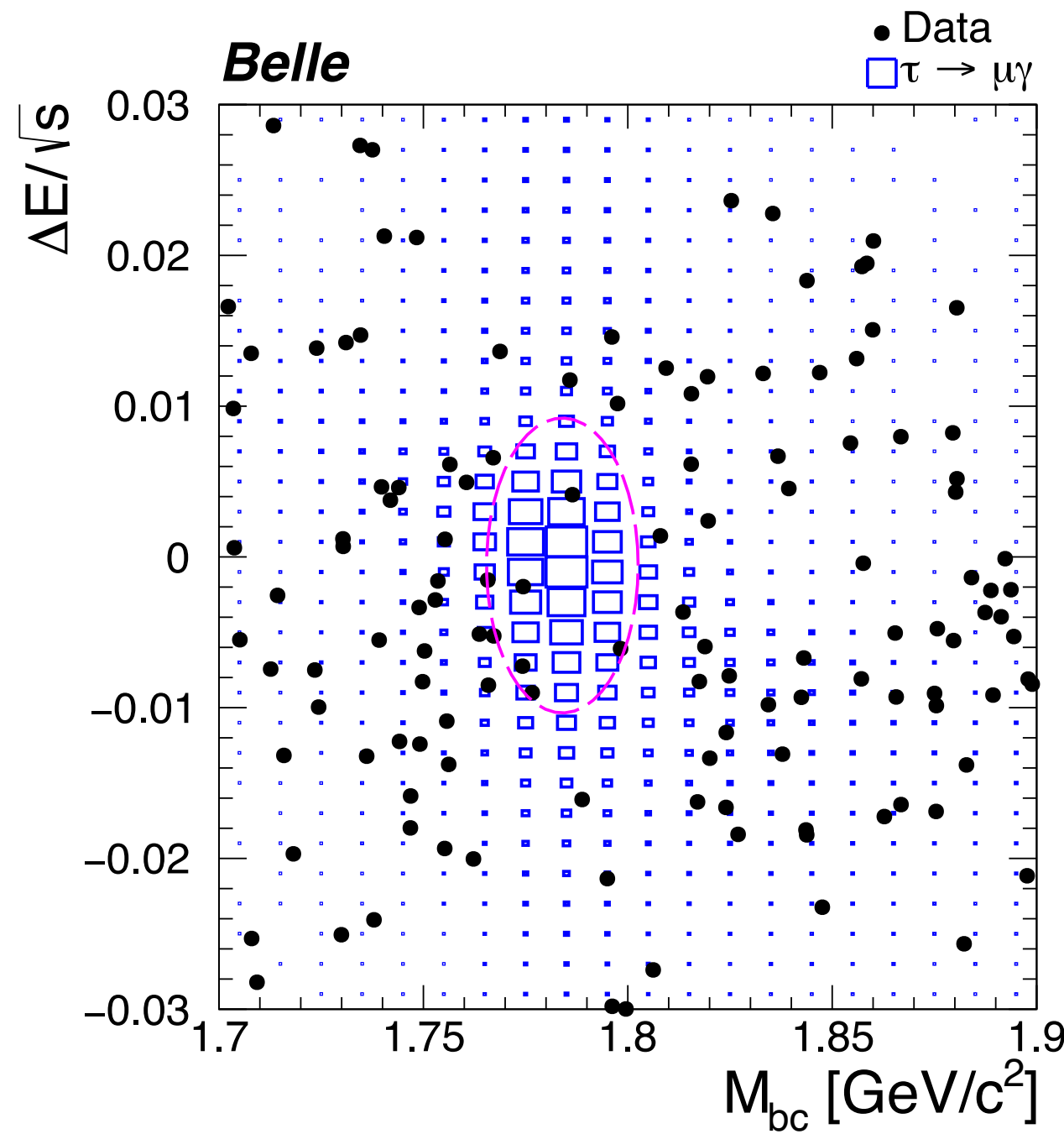
$$\mathcal{B}(\tau \rightarrow \mu\gamma) \simeq (4.5 \times 10^{-6}) |(\delta_{LL})_{32}|^2 \left(\frac{500 \text{ GeV}}{m_{\text{SUSY}}} \right)^4 \left(\frac{\tan \beta}{10} \right)^2$$

Search for $\tau^+ \rightarrow \ell^+ \gamma$

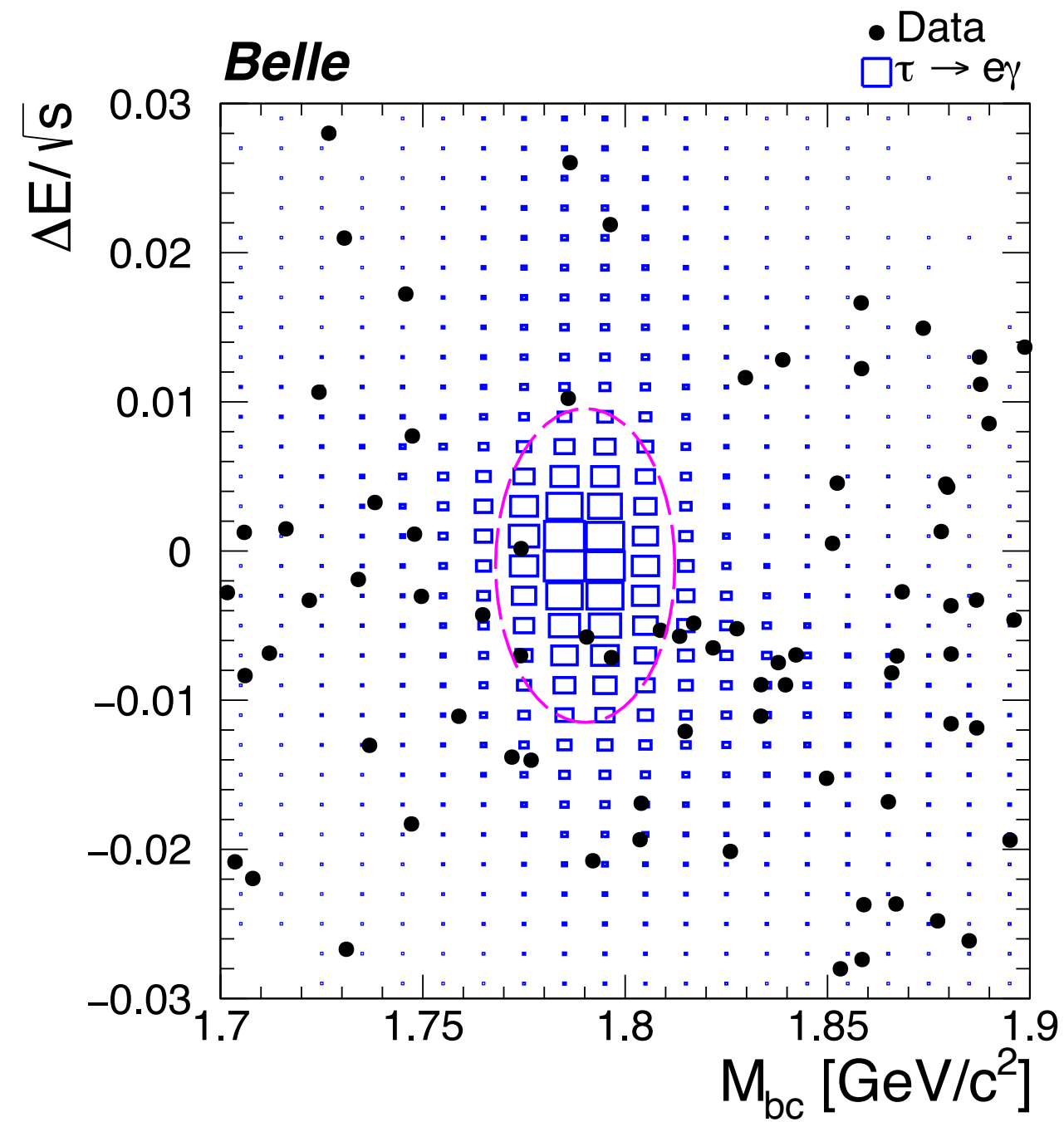
- $\sigma(e^+e^- \rightarrow \tau^+\tau^-) = (0.919 \pm 0.003) \text{ nb} \approx \sigma_{b\bar{b}}$, at $\sqrt{s} \approx 10.58 \text{ GeV}$
 $\therefore e^+e^-$ B -factory is, at the same time, a τ -factory, too!
- tag-side and signal-side τ decays are cleanly separated
- signal extraction by M_{bc} and $\Delta E/\sqrt{s}$



Search for $\tau^+ \rightarrow \ell^+ \gamma$



(a) $\tau^\pm \rightarrow \mu^\pm \gamma$



(b) $\tau^\pm \rightarrow e^\pm \gamma$

$$\mathcal{B}(\tau^\pm \rightarrow \mu^\pm \gamma) < \frac{\tilde{s}_{90}}{2\epsilon N_{\tau\tau}} = 4.2 \times 10^{-8}$$

$$\mathcal{B}(\tau^\pm \rightarrow e^\pm \gamma) < \frac{\tilde{s}_{90}}{2\epsilon N_{\tau\tau}} = 5.6 \times 10^{-8}$$

- use $\int \mathcal{L} dt = 988 \text{ fb}^{-1}$ Belle data
 $\Rightarrow N_{\tau\tau} = 912 \times 10^6$

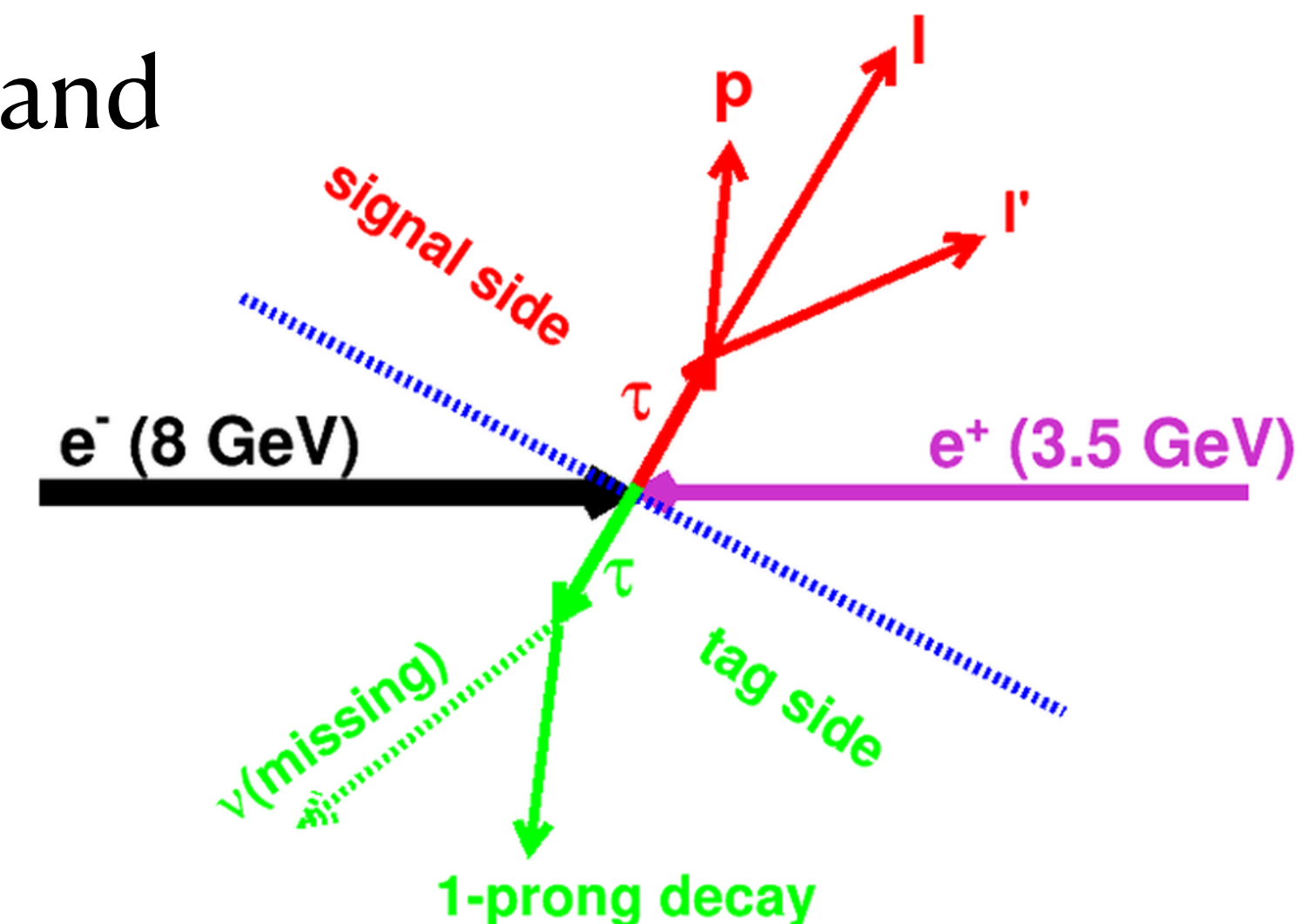
UL (90% CL)	Luminosity	Reference	$\tau \rightarrow \mu \gamma$	$\tau \rightarrow e \gamma$
Belle	535 fb ⁻¹	PLB 666, 16 (2008)	4.5 x 10 ⁻⁸	12.0 x 10 ⁻⁸
BaBar	515 fb ⁻¹	PRL 104, 021802 (2010)	4.4 x 10 ⁻⁸	3.3 x 10 ⁻⁸

τ LNV, BNV search — motivations

- Baryogenesis of our Universe has been unknown
- Lepton #, Baryon # — accidental symmetries of SM
- Baryon number violation — a crucial element of baryogenesis
- Signals of LNV, BNV could be a clear signal of BSM
- Selection rules : $|\Delta(B - L)| = 0$ or 2
 - $\Delta B = \Delta L = 0$ for standard β -decay
 - $\Delta B = \Delta L = \pm 1$
 - $\Delta B = -\Delta L = 1$, e.g. p decay
 - $\Delta B = 2$ ($n\bar{n}$ oscil.) or $\Delta L = 2$ ($0\nu 2\beta$), etc.

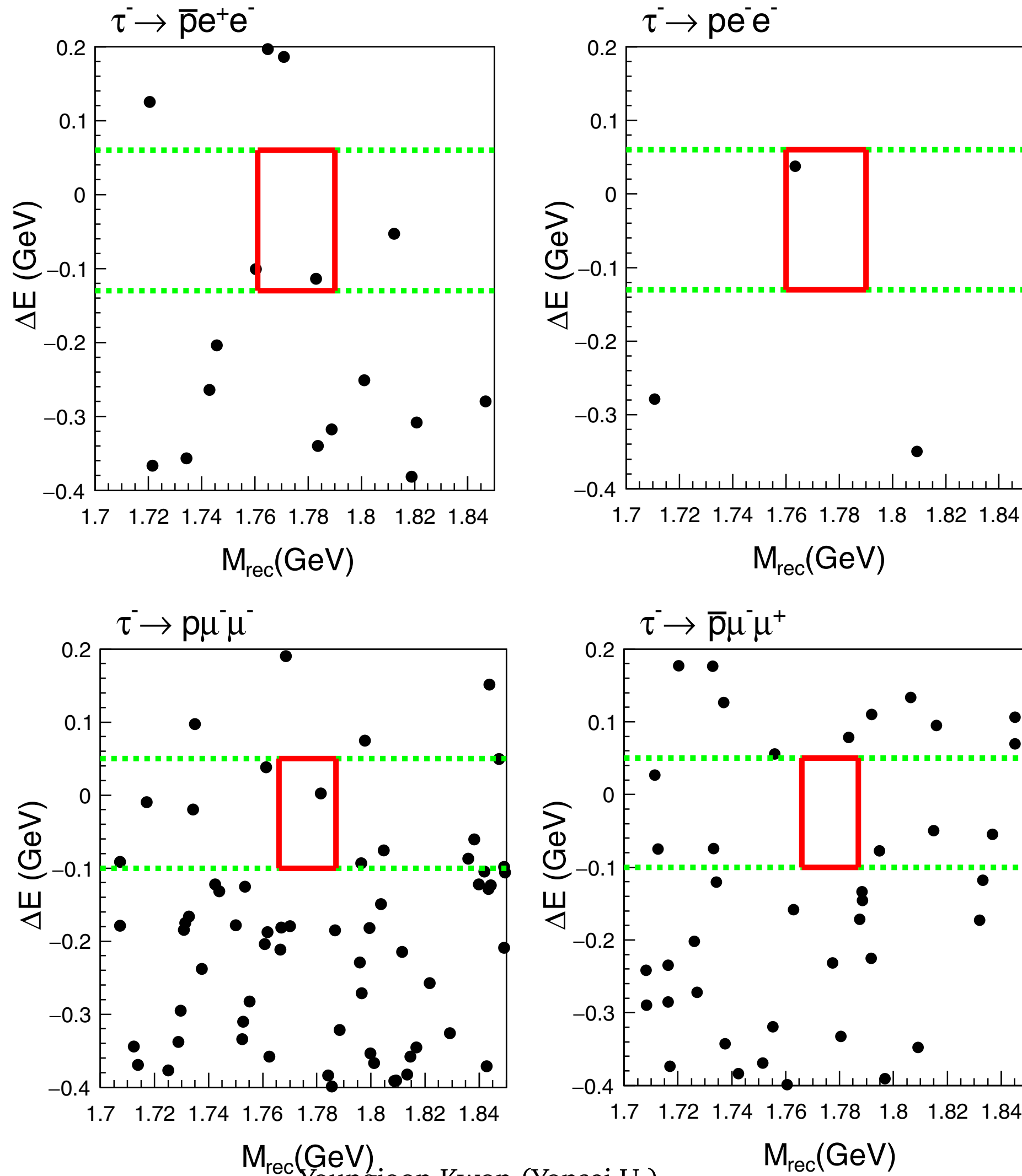
τ LNV, BNV search at Belle

- We search for various LNV, BNV τ decays
- \exists LHCb limits for $\tau^- \rightarrow \bar{p}\mu^+\mu^-, p\mu^-\mu^- : \mathcal{B} < \mathcal{O}(10^{-7})$
- Theory calculations using p lifetime bound:
 $\mathcal{B} \lesssim 10^{-30} - 10^{-48}$
- Search using full $\Upsilon(4S)$ (**on**- and **off**-resonance) and $\Upsilon(5S)$ data from Belle



τ LNV, BNV

● Signal yield in $(M_{\text{rec}}, \Delta E)$



Channel	$\epsilon(\%)$	N_{bkg}	N_{obs}	$N_{\text{sig}}^{\text{UL}}$	$\mathcal{B}(\times 10^{-8})$
$\tau^- \rightarrow \bar{p}e^+e^-$	7.8	0.50 ± 0.35	1	3.9	< 3.0
$\tau^- \rightarrow pe^-e^-$	8.0	0.23 ± 0.07	1	4.1	< 3.0
$\tau^- \rightarrow \bar{p}e^+\mu^-$	6.5	0.22 ± 0.06	0	2.2	< 2.0
$\tau^- \rightarrow \bar{p}e^-\mu^+$	6.9	0.40 ± 0.28	0	2.1	< 1.8
$\tau^- \rightarrow p\mu^-\mu^-$	4.6	1.30 ± 0.46	1	3.1	< 4.0
$\tau^- \rightarrow \bar{p}\mu^-\mu^+$	5.0	1.14 ± 0.43	0	1.5	< 1.8

- an order-of-mag. improvement from LHCb in $p\mu^-\mu^-$, $\bar{p}\mu^+\mu^-$
- first limits in the other four modes

Epilogue

- Ever since the B -factories (Belle & BaBar) started taking data in 1999, we have learned a lot, e.g. CP violations in B systems and confirmation of CKM mechanism, discoveries of many rare decays, and many exotic hadrons.
- But we have not found answers to fundamental questions of ‘flavor’ in the SM. Moreover, we are most sure that SM is not a complete description of the Nature, and we definitely need New Physics beyond the SM.
- In this talk, we went through a few examples of such on-going efforts, searching for LFV, LNV, and LUV with Belle (II).

*“There must be something in the flavors. We just don’t know where we can find it and what its scale is.”**

“We shall not cease from exploration”†

* In a private conversation with Tao Han

† T. S. Eliot

Thank you!