

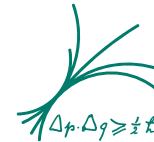
Introduction to



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Course material

Git-clone or download the course material:

<https://github.com/oschulz/julia-course>

Why Julia?

Science needs code - but how to write it?

- Choice of programming language(s) matter!
- Need to balance:
 - Learning time
 - Productivity
 - Performance
- Usually involves compromises

Programming Language Options

- C++:
 - Pro: Very fast (in expert hands)
 - Pro: Really cool new concepts (even literally) in C++11/14/17/...
 - Con: Complex, takes long time to learn and much longer to master
 - Con: Straightforward tasks often result in lengthy code
 - Con: No memory management (General protection faults)
 - Con: No universal package management
 - Con: Composability isn't great

Programming Language Options

- Python:
 - Pro: Broad user base, popular first programming language
 - Pro: Easy to learn, good standard library
 - Con: Can't write time-critical loops in Python, workarounds like Numba/Cython have [many limitations](#), don't compose well
 - Con: Language itself fairly primitive, not very expressive
 - Con: Duck-Typing necessitates lots of test code
 - Con: No effective multi-threading
 - Con: Composability isn't great

What else is there?

- Fortran:
 - Pro: Math can be really fast
 - Con: Old language, few modern concepts
 - Con: Shrinking user base
 - Con: Composability isn't great
 - Do you *really* want to ...?
- Scala, Go, Kotlin etc.:
 - Pro: Lots of individual strengths
 - Con: Math either fast *or* generic *or* complicated
 - Con: Calling C, Fortran or Python code often difficult
 - Con: Composability isn't great

The 97 and the 3 Percent

We should forget about small efficiencies, say about 97% of the time: premature optimization is the root of all evil. Yet we should not pass up our opportunities in that critical 3%.

Donald E. Knuth

- Some programming languages (e.g. Python) great for the 97% - but can't make the 3% fast.
- Some other languages (e.g. C/C++, Fortran) can handle the 3% - but makes the 97% complicated.

The Two-language Problem

- Common approach nowadays:
Write time critical code in C/C++, rest in Python
- Pro: End-user can code comfortably in Python, with good performance
- Con: Complexity of C/C++ **plus** complexity of Python
- Con: Need proficiency in **two** languages, barrier that prevents non-expert users from contributing to important parts of code
- Con: Limits generic implementation of algorithms
- Con: Severely limits metaprogramming, automatic differentiation, etc.

The Expression Problem

The expression problem is a new name for an old problem. The goal is to define a datatype by cases, where one can add new cases to the datatype and new functions over the datatype, without recompiling existing code, and while retaining static type safety (e.g., no casts).

Philip Wadler

- In other words: The capability to add both new subtypes and new functionality for a type defined in a package you don't own
- Object oriented languages typically can't do this (Ruby has a dirty way, Scala a clean workaround)
- If you have programming experience, you have felt this, even if you didn't name it
- Result: Packages tend not to compose well

We were looking for a language ...

- as fast as C/C++/Fortran
- as easy to learn and productive as Python
- with a solution for the expression problem
- with first class math support (vectors, matrices, etc.)
- with true functional programming
- with great Fortran/C/C++/Python integration
- with true metaprogramming (like Lisp or Scala)
- good at parallel and distributed programming
- suitable for interactive, small and large applications

Julia

- Designed for scientific/technical computing
- Originated at MIT, first public version 2012
- Covers the whole wish-list
- Clear focus on user productivity and software quality
- Rapid growth of user base and software packages
- Current version: Julia v1.5 (v1.6 will be out soon)

Julia Language Properties

- Fast: JAOT compilation to native CPU and GPU code
- Multiple-dispatch (more powerful than object-oriented): solves the expression problem
- Dynamically typed
- Very powerful type system, types are first-class values
- Functional programming and metaprogramming
- First-class math support (like Fortran or Matlab)
- ...

Julia Language Properties, cont.

- ...
- Local and distributed code execution
- State-of-the-art multi-threading: parallel code can call parallel code that can call parallel code, ..., without oversubscribing threads
- Software package management:
Trivial to create and install packages
- Excellent REPL (console)
- Easy to call Fortran, C/C++ and Python code

Julia large-scale use case examples

- Celeste: Variational Bayesian inference for astronomical images (doi:10.1214/19-AOAS1258), 1.54 petaflops using 1.3 million threads on 9,300 Knights Landing (KNL) nodes on Cori at NERSC
- Clima: Full-earth climate simulation, <https://clima.caltech.edu>, large team, uses everything from MPI to GPUs
- ...

When (not) to use Julia

- *Do* use Julia for computations, visualization, data processing ... pretty much anything scientific/technical
- *Do not* use Julia for scripts what will only run for a second (code gen overhead), use Python or shell scripts
- *Do not* use Julia for non-computing web apps, etc. (*at least not yet*), use Go or Node.js

Julia 101

Verbs and nouns - functions and types

- Julia is not Java: Verbs aren't owned by nouns
- Julia has: types, functions and methods
- Methods belong to *functions*, not to types!

Functions

Short one-liner function:

```
In [4]: f(x) = x^2
```

```
Out[4]: f (generic function with 1 method)
```

```
In [5]: f(3)
```

```
Out[5]: 9
```

Function that needs more than one line:

```
In [6]: function f(x)
        # ... something ...
        x^2
end
```

Out[6]: f (generic function with 1 method)

is equivalent to

```
In [7]: function f(x)
        # ... something ...
        return x^2
end
```

Out[7]: f (generic function with 1 method)

Note: `return` is optional, and often not used explicitly. Last expression in a function, block, etc. is automatically returned (like in Mathematica).

Types

An abstract type, must be empty:

```
abstract type MySuperType end
```

An immutable type, value of `i` can't change:

```
struct MySubType <: MySuperType  
  i::Int  
end
```

A mutable type, value of `i` can change:

```
mutable struct MyMutableSubType <: MySuperType  
  i::Int  
end
```

Type parameters

Julia has a powerful parametric type system, based on set theory:

```
struct MyRealArray{T<:Real,N} <: AbstractArray{T,N}
    # ...
end
```

defines an array type with real-valued elements.

```
foo(A::AbstractArray{<:Real}) = do_something_with(A)
```

is equivalent to

```
bar(A::AbstractArray{T,N}) where {T<:Real,N} = do_something_with(A)
```

defines a function covariant in the element type of `A`. Can also be contravariant:

```
baz(A::AbstractArray{>:Real}) = do_something_with(A)
```

Type aliases and union types

Type aliases are just const values:

```
const Abstract2DArray{T} = AbstractArray{T,2}  
rand(2, 2) isa Abstract2DArray == true
```

Type unions are unions of set of types.

```
const RealVecOrMat{T} where {T<:Real} = Union{AbstractArray{T,1},  
AbstractArray{T,2}}
```

is the union of a 1D and 2D array types with real-valued elements.

Syntax: Variables

```
# Global variables:  
const a = 42  
b = 24  
  
function foo(x)  
  # Local variables:  
  
  c = a * x  
  d = b * x # Avoid, type of b can change!  
  #...  
end
```


Loops

For loop:

```
for i in something_iterable
    # ...
end
```

`something_iterable` can be a range, an array, anything that implements the Julia [iterator API](#).

While loop:

```
while condition
    # do something
end
```

Control flow

If-else, evaluate only one branch:

```
if condition
  # do something
elseif condition
  # do something else
else
  # or something different
end
```

Ternary operator, evaluate only one branch:

```
condition ? result_if_true : result_if_false
```

`ifelse`, evaluate both results but return only one:

```
ifelse(condition, result_if_true, result_if_false)
```

Blocks and scoping

Begin/end-block:

```
begin  
  # *Not* a new scope in here  
  # ...  
end
```

Let-block:

```
b = 24  
  
let my_b = b  
  # New scope in here.  
  # If b is bound to new value, my_b won't change.  
  # ...  
end
```

Arrays

Vectors:

```
v = [1, 2, 3]
```

```
v = rand(5)
```

Matrices:

```
A = [1 2; 3 4]
```

```
A = rand(4, 5)
```

- Column-first memory layout!
- Almost anything array-like is subtype of `AbstractArray`.

Array indexing

Get `i`-th element of vector `v`:

```
v[i]
```

Most higher-dimensional array types support cartesian and linear indexing (usually faster):

```
A[i, j]  
A[lin_idx]
```

Use `eachindex(A)` to get indices of best type for given `A` (usually linear).

In Julia, anything array-like can usually be an index as well

```
A[2:3, [1, 4, 5]]
```

Array comprehension and generators

Returns an array:

```
[f(x) for x in some_collection]
```

Returns an iterable generator:

```
(f(x) for x in some_collection)
```

Hello World (and more) in Julia

In [8]:

```
println("Hello, World!")
```

```
Hello, World!
```

Hello World (and more) in Julia

```
In [8]: println("Hello, World!")
```

Hello, World!

Let's define a function

```
In [9]: f(x, y) = x * y  
f(20, 2.1)
```

```
Out[9]: 42.0
```

Multiplication is also defined for vectors, so this works, too:

```
In [10]: f(4.2, [1, 2, 3, 4])
```

```
Out[10]: 4-element Vector{Float64}:  
 4.2  
 8.4  
12.600000000000001  
16.8
```


Let's Look Under the Hood

```
In [11]: @code_llvm debuginfo=:none f(20, 2.1)
```

```
define double @julia_f_1769(i64 signext %0, double %1) {  
top:  
  %2 = sitofp i64 %0 to double  
  %3 = fmul double %2, %1  
  ret double %3  
}
```

```
In [12]: @code_native debuginfo=:none f(20, 2.1)
```

```
.text  
vcvtsi2sd    %rdi, %xmm1, %xmm1  
vmulsd      %xmm0, %xmm1, %xmm0  
retq  
nopw        (%rax,%rax)
```

Multiple Dispatch

```
In [13]: foo(x::Integer, y::Number) = x * y  
foo(x::Integer, y::AbstractString) = join(fill(y, x))
```

```
Out[13]: foo (generic function with 2 methods)
```

```
In [14]: foo(3, 4)
```

```
Out[14]: 12
```

```
In [15]: foo(3, "abc")
```

```
Out[15]: "abcabcabc"
```

```
In [16]: foo(4.5, 3)
```

```
MethodError: no method matching foo(::Float64, ::Int64)  
Closest candidates are:  
  foo(::Integer, ::Number) at In[13]:1
```

```
Stacktrace:
```

```
[1] top-level scope
```

```
  @ In[16]:1
```

```
[2] eval
```

```
  @ ./boot.jl:360 [inlined]
```

```
[3] include_string(mapexpr::typeof(REPL.softscope), mod::Module, code::St
```

```
ring, filename::String)  
@ Base ./loading.jl:1116
```

Functional Programming

```
In [17]: A = rand(10)
```

```
Out[17]: 10-element Vector{Float64}:  
 0.6371208023031867  
 0.6718241066725001  
 0.4748893050668026  
 0.42663698605676403  
 0.7906983796911875  
 0.12541113346976673  
 0.45340111998340027  
 0.47037648329103954  
 0.7763738096091002  
 0.8570304146388021
```

```
In [18]: idxs = findall(x -> 0.2 < x < 0.6, A)
```

```
Out[18]: 4-element Vector{Int64}:  
 3  
 4  
 7  
 8
```

```
In [19]: A[idxs]
```

```
Out[19]: 4-element Vector{Float64}:  
 0.4748893050668026  
 0.42663698605676403
```

0.45340111998340027
0.47037648329103954

Even types are first-class values:

```
In [20]: mytype = Number
```

```
Out[20]: Number
```

```
In [21]: subtypes(mytype)
```

```
Out[21]: 2-element Vector{Any}:  
          Complex  
          Real
```

Julia type hierarchy extends all the way down to primitive types:

```
In [22]: Float64 <: AbstractFloat <: Real <: Number <: Any
```

```
Out[22]: true
```

Broadcasting

```
In [23]: A = [1.1, 2.2, 3.3]
          B = [4.4, 5.5, 6.6]
          broadcast((x, y) -> (x + y)^2, A, B)
```

```
Out[23]: 3-element Vector{Float64}:
          30.25
          59.290000000000006
          98.009999999999998
```

Shorter broadcast syntax:

```
In [24]: (A .+ B) .^ 2
```

```
Out[24]: 3-element Vector{Float64}:
          30.25
          59.290000000000006
          98.009999999999998
```

Loop Fusion and SIMD Vectorization

In [25]:

```
foo(X, Y) = (X .+ Y) .^ 2
@code_llvm raw=false debuginfo=:none foo(A, B)
```

```
define nonnull {}* @japi1_foo_2441({}* %0, {}** %1, i32 %2) #0 {
top:
  %3 = alloca [4 x {}*], align 8
  %gcframe173 = alloca [4 x {}*], align 16
  %gcframe173.sub = getelementptr inbounds [4 x {}*], [4 x {}*]* %gcframe1
73, i64 0, i64 0
  %.sub = getelementptr inbounds [4 x {}*], [4 x {}*]* %3, i64 0, i64 0
  %4 = bitcast [4 x {}*]* %gcframe173 to i8*
  call void @llvm.memset.p0i8.i32(i8* nonnull align 16 dereferenceable(32)
%4, i8 0, i32 32, i1 false)
  %5 = alloca {}**, align 8
  store volatile {}** %1, {}*** %5, align 8
  %6 = alloca [1 x [1 x i64]], align 8
  %7 = alloca [1 x [1 x i64]], align 8
  %thread_ptr = call i8* asm "movq %fs:0, $0", "=r"() #8
  %ptls_i8 = getelementptr i8, i8* %thread_ptr, i64 -32768
  %8 = bitcast [4 x {}*]* %gcframe173 to i64*
  store i64 8, i64* %8, align 16
  %9 = getelementptr inbounds [4 x {}*], [4 x {}*]* %gcframe173, i64 0, i6
4 1
  %10 = bitcast i8* %ptls_i8 to i64*
  %11 = load i64, i64* %10, align 8
  %12 = bitcast {}** %9 to i64*
  store i64 %11, i64* %12, align 8
  %13 = bitcast i8* %ptls_i8 to {}***
  store {}** %gcframe173.sub, {}*** %13, align 8
  %14 = load {}*, {}** %1, align 8
```



```

%15 = getelementptr inbounds {}, {}, {}** %1, i64 1
%16 = load {}, {}, {}** %15, align 8
%17 = bitcast {}* %14 to {}**
%18 = getelementptr inbounds {}, {}, {}** %17, i64 3
%19 = bitcast {}** %18 to i64*
%20 = load i64, i64* %19, align 8
%21 = bitcast {}* %16 to {}**
%22 = getelementptr inbounds {}, {}, {}** %21, i64 3
%23 = bitcast {}** %22 to i64*
%24 = load i64, i64* %23, align 8
switch i64 %24, label %L20 [
  i64 0, label %L13
  i64 1, label %L17
]

```

```

L13:                                     ; preds = %top
%25 = icmp eq i64 %20, 0
br label %L23

```

```

L17:                                     ; preds = %top
%26 = icmp eq i64 %20, 1
br label %L23

```

```

L20:                                     ; preds = %top
%27 = icmp eq i64 %24, %20
br label %L23

```

```

L23:                                     ; preds = %L20, %L17, %L
13
%value_phi.in = phi i1 [ %25, %L13 ], [ %26, %L17 ], [ %27, %L20 ]
%28 = icmp eq i64 %20, 1
%value_phi1.v = or i1 %28, %value_phi.in
br i1 %value_phi1.v, label %L57, label %L31

```

```

L31:                                     ; preds = %L23
    switch i64 %20, label %L40 [
        i64 0, label %L33
        i64 1, label %L37
    ]

L33:                                     ; preds = %L31
    %29 = icmp eq i64 %24, 0
    br label %L43

L37:                                     ; preds = %L31
    %30 = icmp eq i64 %24, 1
    br label %L43

L40:                                     ; preds = %L31
    %31 = icmp eq i64 %20, %24
    br label %L43

L43:                                     ; preds = %L40, %L37, %L
33
    %value_phi20.in = phi i1 [ %29, %L33 ], [ %30, %L37 ], [ %31, %L40 ]
    %32 = icmp eq i64 %24, 1
    %value_phi21.v = or i1 %32, %value_phi20.in
    br i1 %value_phi21.v, label %L57, label %L51

L51:                                     ; preds = %L43
    %33 = call noalias nonnull {}* @jl_gc_pool_alloc(i8* %ptls_i8, i32 1400,
i32 16) #1
    %34 = bitcast {}* %33 to i64*
    %35 = getelementptr inbounds i64, i64* %34, i64 -1
    store atomic i64 140310350102144, i64* %35 unordered, align 8
    store i64 %20, i64* %34, align 8
    %36 = getelementptr inbounds [4 x {}*], [4 x {}*]* %gcframe173, i64 0, i
64 2

```

```
store {}* %33, {}** %36, align 16
store {}* %33, {}** %.sub, align 8
%37 = call nonnull {}* @jl_apply_generic({}* inttoptr (i64 1403103688714
56 to {}*), {}** nonnull %.sub, i32 1)
%38 = getelementptr inbounds [4 x {}*], [4 x {}*]* %gcframe173, i64 0, i
64 3
store {}* %37, {}** %38, align 8
%39 = call noalias nonnull {}* @jl_gc_pool_alloc(i8* %ptls_i8, i32 1400,
i32 16) #1
%40 = bitcast {}* %39 to i64*
%41 = getelementptr inbounds i64, i64* %40, i64 -1
store atomic i64 140310350102144, i64* %41 unordered, align 8
store i64 %24, i64* %40, align 8
store {}* %39, {}** %36, align 16
store {}* %39, {}** %.sub, align 8
%42 = call nonnull {}* @jl_apply_generic({}* inttoptr (i64 1403103688714
56 to {}*), {}** nonnull %.sub, i32 1)
store {}* %42, {}** %36, align 16
store {}* inttoptr (i64 140310375323856 to {}*), {}** %.sub, align 8
%43 = getelementptr inbounds [4 x {}*], [4 x {}*]* %3, i64 0, i64 1
store {}* %37, {}** %43, align 8
%44 = getelementptr inbounds [4 x {}*], [4 x {}*]* %3, i64 0, i64 2
store {}* inttoptr (i64 140310375323952 to {}*), {}** %44, align 8
%45 = getelementptr inbounds [4 x {}*], [4 x {}*]* %3, i64 0, i64 3
store {}* %42, {}** %45, align 8
%46 = call nonnull {}* @jl_apply_generic({}* inttoptr (i64 1403103523589
76 to {}*), {}** nonnull %.sub, i32 4)
store {}* %46, {}** %36, align 16
store {}* %46, {}** %.sub, align 8
%47 = call nonnull {}* @jl_apply_generic({}* inttoptr (i64 1403104170782
40 to {}*), {}** nonnull %.sub, i32 1)
call void @jl_throw({}* %47)
unreachable
```

```

L57:                                     ; preds = %L43, %L23
    %.sroa.026.0 = phi i64 [ %24, %L23 ], [ %20, %L43 ]
    %48 = getelementptr inbounds [1 x [1 x i64]], [1 x [1 x i64]]* %6, i64 0
, i64 0, i64 0
    store i64 %.sroa.026.0, i64* %48, align 8
    %49 = call nonnull {}* inttoptr (i64 140310593210021 to {})* ({}*, i64)*
({}* inttoptr (i64 140310355132272 to {})*), i64 %.sroa.026.0)
    %50 = bitcast {}* %49 to {}**
    %51 = getelementptr inbounds {}*, {}** %50, i64 3
    %52 = bitcast {}** %51 to i64*
    %53 = load i64, i64* %52, align 8
    switch i64 %53, label %L90 [
        i64 0, label %L80
        i64 1, label %L84
    ]

```

```

L80:                                     ; preds = %L57
    %54 = icmp eq i64 %.sroa.026.0, 0
    br i1 %54, label %L98, label %L223

```

```

L84:                                     ; preds = %L57
    %55 = icmp eq i64 %.sroa.026.0, 1
    br i1 %55, label %L98, label %L223

```

```

L90:                                     ; preds = %L57
    %56 = icmp eq i64 %53, %.sroa.026.0
    br i1 %56, label %L98, label %L223

```

```

L98:                                     ; preds = %L90, %L84, %L80
    %.not34 = icmp eq {}* %49, %14
    br i1 %.not34, label %L124, label %L101

```

```

L101:                                    ; preds = %L98

```

```
%57 = load i8, i8* inttoptr (i64 140310355132345 to i8*), align 1
%58 = and i8 %57, 1
%.not42.not = icmp eq i8 %58, 0
br i1 %.not42.not, label %L107, label %L124
```

```
L107: ; preds = %L101
```

```
%59 = bitcast {}* %49 to i64*
%60 = load i64, i64* %59, align 8
%61 = bitcast {}* %14 to i64*
%62 = load i64, i64* %61, align 8
%.not58 = icmp eq i64 %60, %62
br i1 %.not58, label %L119, label %L124
```

```
L119: ; preds = %L107
```

```
%63 = getelementptr inbounds [4 x {}*], [4 x {}]* %gcframe173, i64 0, i64 3
store {}* %49, {}** %63, align 8
%64 = call nonnull {}* inttoptr (i64 140310593210237 to {}* ({}*)*)({}* nonnull %14)
%.pre166 = bitcast {}* %64 to {}**
br label %L124
```

```
L124: ; preds = %L119, %L107,
```

```
%L101, %L98
%.pre-phi168 = phi {}** [ %17, %L107 ], [ %17, %L101 ], [ %17, %L98 ], [ %.pre166, %L119 ]
%value_phi11 = phi {}* [ %14, %L107 ], [ %14, %L101 ], [ %14, %L98 ], [ %64, %L119 ]
%65 = getelementptr inbounds {}*, {}** %.pre-phi168, i64 3
%66 = bitcast {}** %65 to i64*
%67 = load i64, i64* %66, align 8
%.not38 = icmp eq i64 %67, 1
%.not35 = icmp eq {}* %49, %16
br i1 %.not35, label %L159, label %L136
```

```

L136:                                     ; preds = %L124
    %68 = load i8, i8* inttoptr (i64 140310355132345 to i8*), align 1
    %69 = and i8 %68, 1
    %.not40.not = icmp eq i8 %69, 0
    br i1 %.not40.not, label %L142, label %L159

```

```

L142:                                     ; preds = %L136
    %70 = bitcast {}* %49 to i64*
    %71 = load i64, i64* %70, align 8
    %72 = bitcast {}* %16 to i64*
    %73 = load i64, i64* %72, align 8
    %.not = icmp eq i64 %71, %73
    br i1 %.not, label %L154, label %L159

```

```

L154:                                     ; preds = %L142
    %74 = getelementptr inbounds [4 x {}*], [4 x {}]* %gcframe173, i64 0, i
64 3
    store {}* %49, {}** %74, align 8
    %75 = getelementptr inbounds [4 x {}*], [4 x {}]* %gcframe173, i64 0, i
64 2
    store {}* %value_phi11, {}** %75, align 16
    %76 = call nonnull {}* inttoptr (i64 140310593210237 to {}* ({}*)*)({}*
nonnull %16)
    %.pre169 = bitcast {}* %76 to {}**
    br label %L159

```

```

L159:                                     ; preds = %L154, %L142,
%L136, %L124
    %pre-phi172 = phi {}** [ %21, %L142 ], [ %21, %L136 ], [ %21, %L124 ],
[ %.pre169, %L154 ]
    %value_phi12 = phi {}* [ %16, %L142 ], [ %16, %L136 ], [ %16, %L124 ], [
%76, %L154 ]
    %77 = getelementptr inbounds {}*, {}** %pre-phi172, i64 3

```

```
%78 = bitcast {}** %77 to i64*
%79 = load i64, i64* %78, align 8
%.not39 = icmp eq i64 %79, 1
%.not36 = icmp eq i64 %.sroa.026.0, 0
br il %.not36, label %L233, label %L185.lr.ph
```

```
L185.lr.ph: ; preds = %L159
%80 = bitcast {}* %value_phi11 to double**
%81 = load double*, double** %80, align 8
%bc116 = bitcast double* %81 to i8*
%82 = bitcast {}* %value_phi12 to double**
%83 = load double*, double** %82, align 8
%bc = bitcast double* %83 to i8*
%84 = bitcast {}* %49 to double**
%85 = load double*, double** %84, align 8
%86 = bitcast double* %85 to i8*
%min.iters.check140 = icmp ult i64 %.sroa.026.0, 16
br il %.not38, label %L185.lr.ph.split.us, label %L185.lr.ph.L185.lr.ph.
split_crit_edge
```

```
L185.lr.ph.L185.lr.ph.split_crit_edge: ; preds = %L185.lr.ph
br il %.not39, label %L185.us52.preheader, label %L185.preheader
```

```
L185.preheader: ; preds = %L185.lr.ph.L1
85.lr.ph.split_crit_edge
br il %min.iters.check140, label %scalar.ph, label %vector.memcheck
```

```
vector.memcheck: ; preds = %L185.preheader
```

```
%scevgep = getelementptr double, double* %85, i64 %.sroa.026.0
%scevgep63 = getelementptr double, double* %81, i64 %.sroa.026.0
%scevgep65 = getelementptr double, double* %83, i64 %.sroa.026.0
%bound0 = icmp ult double* %85, %scevgep63
%bound1 = icmp ult double* %81, %scevgep
```

```
%found.conflict = and i1 %bound0, %bound1
%bound067 = icmp ult double* %85, %scevgep65
%bound168 = icmp ult double* %83, %scevgep
%found.conflict69 = and i1 %bound067, %bound168
%conflict.rdx = or i1 %found.conflict, %found.conflict69
br i1 %conflict.rdx, label %scalar.ph, label %vector.ph
```

```
vector.ph: ; preds = %vector.memcheck
```

```
%n.vec = and i64 %sroa.026.0, 9223372036854775792
br label %vector.body
```

```
vector.body: ; preds = %vector.body, %vector.ph
```

```
%index = phi i64 [ 0, %vector.ph ], [ %index.next, %vector.body ]
%87 = getelementptr inbounds double, double* %81, i64 %index
%88 = bitcast double* %87 to <4 x double>*
%wide.load = load <4 x double>, <4 x double>* %88, align 8
%89 = getelementptr inbounds double, double* %87, i64 4
%90 = bitcast double* %89 to <4 x double>*
%wide.load70 = load <4 x double>, <4 x double>* %90, align 8
%91 = getelementptr inbounds double, double* %87, i64 8
%92 = bitcast double* %91 to <4 x double>*
%wide.load71 = load <4 x double>, <4 x double>* %92, align 8
%93 = getelementptr inbounds double, double* %87, i64 12
%94 = bitcast double* %93 to <4 x double>*
%wide.load72 = load <4 x double>, <4 x double>* %94, align 8
%95 = getelementptr inbounds double, double* %83, i64 %index
%96 = bitcast double* %95 to <4 x double>*
%wide.load73 = load <4 x double>, <4 x double>* %96, align 8
%97 = getelementptr inbounds double, double* %95, i64 4
%98 = bitcast double* %97 to <4 x double>*
%wide.load74 = load <4 x double>, <4 x double>* %98, align 8
%99 = getelementptr inbounds double, double* %95, i64 8
```



```

%100 = bitcast double* %99 to <4 x double>*
%wide.load75 = load <4 x double>, <4 x double>* %100, align 8
%101 = getelementptr inbounds double, double* %95, i64 12
%102 = bitcast double* %101 to <4 x double>*
%wide.load76 = load <4 x double>, <4 x double>* %102, align 8
%103 = fadd <4 x double> %wide.load, %wide.load73
%104 = fadd <4 x double> %wide.load70, %wide.load74
%105 = fadd <4 x double> %wide.load71, %wide.load75
%106 = fadd <4 x double> %wide.load72, %wide.load76
%107 = fmul <4 x double> %103, %103
%108 = fmul <4 x double> %104, %104
%109 = fmul <4 x double> %105, %105
%110 = fmul <4 x double> %106, %106
%111 = getelementptr inbounds double, double* %85, i64 %index
%112 = bitcast double* %111 to <4 x double>*
store <4 x double> %107, <4 x double>* %112, align 8
%113 = getelementptr inbounds double, double* %111, i64 4
%114 = bitcast double* %113 to <4 x double>*
store <4 x double> %108, <4 x double>* %114, align 8
%115 = getelementptr inbounds double, double* %111, i64 8
%116 = bitcast double* %115 to <4 x double>*
store <4 x double> %109, <4 x double>* %116, align 8
%117 = getelementptr inbounds double, double* %111, i64 12
%118 = bitcast double* %117 to <4 x double>*
store <4 x double> %110, <4 x double>* %118, align 8
%index.next = add i64 %index, 16
%119 = icmp eq i64 %index.next, %n.vec
br il %119, label %middle.block, label %vector.body

```

```

middle.block: ; preds = %vector.body

```

```

    %cmp.n = icmp eq i64 %sroa.026.0, %n.vec
    br il %cmp.n, label %L233, label %scalar.ph

```

```

scalar.ph: ; preds = %middle.block,

```

```
%vector.memcheck, %L185.preheader  
%bc.resume.val = phi i64 [ %n.vec, %middle.block ], [ 0, %L185.preheader  
], [ 0, %vector.memcheck ]  
br label %L185
```

```
L185.us52.preheader: ; preds = %L185.lr.ph.L1  
85.lr.ph.split_crit_edge  
br il %min.iters.check140, label %scalar.ph78, label %vector.memcheck94
```

```
vector.memcheck94: ; preds = %L185.us52.pre  
header
```

```
%scevgep82 = getelementptr double, double* %85, i64 %sroa.026.0  
%scevgep84 = getelementptr double, double* %81, i64 %sroa.026.0  
%uglygep = getelementptr i8, i8* %bc, i64 1  
%bound086 = icmp ult double* %85, %scevgep84  
%bound187 = icmp ult double* %81, %scevgep82  
%found.conflict88 = and il %bound086, %bound187  
%bound089 = icmp ugt i8* %uglygep, %86  
%bound190 = icmp ult double* %83, %scevgep82  
%found.conflict91 = and il %bound089, %bound190  
%conflict.rdx92 = or il %found.conflict88, %found.conflict91  
br il %conflict.rdx92, label %scalar.ph78, label %vector.ph95
```

```
vector.ph95: ; preds = %vector.memche  
ck94
```

```
%n.vec97 = and i64 %sroa.026.0, 9223372036854775792  
%pre = load double, double* %83, align 8  
br label %vector.body79
```

```
vector.body79: ; preds = %vector.body7  
9, %vector.ph95
```

```
%index98 = phi i64 [ 0, %vector.ph95 ], [ %index.next99, %vector.body79  
]  
%120 = getelementptr inbounds double, double* %81, i64 %index98
```

```

%121 = bitcast double* %120 to <4 x double>*
%wide.load102 = load <4 x double>, <4 x double>* %121, align 8
%122 = getelementptr inbounds double, double* %120, i64 4
%123 = bitcast double* %122 to <4 x double>*
%wide.load103 = load <4 x double>, <4 x double>* %123, align 8
%124 = getelementptr inbounds double, double* %120, i64 8
%125 = bitcast double* %124 to <4 x double>*
%wide.load104 = load <4 x double>, <4 x double>* %125, align 8
%126 = getelementptr inbounds double, double* %120, i64 12
%127 = bitcast double* %126 to <4 x double>*
%wide.load105 = load <4 x double>, <4 x double>* %127, align 8
%128 = insertelement <4 x double> undef, double %.pre, i32 0
%129 = shufflevector <4 x double> %128, <4 x double> undef, <4 x i32> ze
roinitializer
%130 = fadd <4 x double> %wide.load102, %129
%131 = fadd <4 x double> %wide.load103, %129
%132 = fadd <4 x double> %wide.load104, %129
%133 = fadd <4 x double> %wide.load105, %129
%134 = fmul <4 x double> %130, %130
%135 = fmul <4 x double> %131, %131
%136 = fmul <4 x double> %132, %132
%137 = fmul <4 x double> %133, %133
%138 = getelementptr inbounds double, double* %85, i64 %index98
%139 = bitcast double* %138 to <4 x double>*
store <4 x double> %134, <4 x double>* %139, align 8
%140 = getelementptr inbounds double, double* %138, i64 4
%141 = bitcast double* %140 to <4 x double>*
store <4 x double> %135, <4 x double>* %141, align 8
%142 = getelementptr inbounds double, double* %138, i64 8
%143 = bitcast double* %142 to <4 x double>*
store <4 x double> %136, <4 x double>* %143, align 8
%144 = getelementptr inbounds double, double* %138, i64 12
%145 = bitcast double* %144 to <4 x double>*
store <4 x double> %137, <4 x double>* %145, align 8

```

```
%index.next99 = add i64 %index98, 16
%146 = icmp eq i64 %index.next99, %n.vec97
br i1 %146, label %middle.block77, label %vector.body79
```

```
middle.block77: ; preds = %vector.body79
%cmp.n101 = icmp eq i64 %.sroa.026.0, %n.vec97
br i1 %cmp.n101, label %L233, label %scalar.ph78
```

```
scalar.ph78: ; preds = %middle.block77
7, %vector.memcheck94, %L185.us52.preheader
%bc.resume.val100 = phi i64 [ %n.vec97, %middle.block77 ], [ 0, %L185.us52.preheader ], [ 0, %vector.memcheck94 ]
br label %L185.us52
```

```
L185.lr.ph.split.us: ; preds = %L185.lr.ph
br i1 %.not39, label %L185.us.us.preheader, label %L185.us.preheader
```

```
L185.us.preheader: ; preds = %L185.lr.ph.split.us
br i1 %min.iters.check140, label %scalar.ph107, label %vector.memcheck125
```

```
vector.memcheck125: ; preds = %L185.us.preheader
%scevgep111 = getelementptr double, double* %85, i64 %.sroa.026.0
%uglygep113 = getelementptr i8, i8* %bc116, i64 1
%scevgep114 = getelementptr double, double* %83, i64 %.sroa.026.0
%bound0117 = icmp ugt i8* %uglygep113, %86
%bound1118 = icmp ult double* %81, %scevgep111
%found.conflict119 = and i1 %bound0117, %bound1118
%bound0120 = icmp ult double* %85, %scevgep114
%bound1121 = icmp ult double* %83, %scevgep111
%found.conflict122 = and i1 %bound0120, %bound1121
%conflict.rdx123 = or i1 %found.conflict119, %found.conflict122
```

```
br i1 %conflict.rdx123, label %scalar.ph107, label %vector.ph126
```

```
vector.ph126: ; preds = %vector.memcheck125
```

```
%n.vec128 = and i64 %.sroa.026.0, 9223372036854775792
```

```
%pre165 = load double, double* %81, align 8
```

```
br label %vector.body108
```

```
vector.body108: ; preds = %vector.body108, %vector.ph126
```

```
%index129 = phi i64 [ 0, %vector.ph126 ], [ %index.next130, %vector.body108 ]
```

```
%147 = insertelement <4 x double> undef, double %pre165, i32 0
```

```
%148 = shufflevector <4 x double> %147, <4 x double> undef, <4 x i32> zero_initializer
```

```
%149 = getelementptr @inbounds double, double* %83, i64 %index129
```

```
%150 = bitcast double* %149 to <4 x double>*
```

```
%wide.load133 = load <4 x double>, <4 x double>* %150, align 8
```

```
%151 = getelementptr @inbounds double, double* %149, i64 4
```

```
%152 = bitcast double* %151 to <4 x double>*
```

```
%wide.load134 = load <4 x double>, <4 x double>* %152, align 8
```

```
%153 = getelementptr @inbounds double, double* %149, i64 8
```

```
%154 = bitcast double* %153 to <4 x double>*
```

```
%wide.load135 = load <4 x double>, <4 x double>* %154, align 8
```

```
%155 = getelementptr @inbounds double, double* %149, i64 12
```

```
%156 = bitcast double* %155 to <4 x double>*
```

```
%wide.load136 = load <4 x double>, <4 x double>* %156, align 8
```

```
%157 = fadd <4 x double> %148, %wide.load133
```

```
%158 = fadd <4 x double> %148, %wide.load134
```

```
%159 = fadd <4 x double> %148, %wide.load135
```

```
%160 = fadd <4 x double> %148, %wide.load136
```

```
%161 = fmul <4 x double> %157, %157
```

```
%162 = fmul <4 x double> %158, %158
```

```
%163 = fmul <4 x double> %159, %159
```

```

%164 = fmul <4 x double> %160, %160
%165 = getelementptr inbounds double, double* %85, i64 %index129
%166 = bitcast double* %165 to <4 x double>*
store <4 x double> %161, <4 x double>* %166, align 8
%167 = getelementptr inbounds double, double* %165, i64 4
%168 = bitcast double* %167 to <4 x double>*
store <4 x double> %162, <4 x double>* %168, align 8
%169 = getelementptr inbounds double, double* %165, i64 8
%170 = bitcast double* %169 to <4 x double>*
store <4 x double> %163, <4 x double>* %170, align 8
%171 = getelementptr inbounds double, double* %165, i64 12
%172 = bitcast double* %171 to <4 x double>*
store <4 x double> %164, <4 x double>* %172, align 8
%index.next130 = add i64 %index129, 16
%173 = icmp eq i64 %index.next130, %n.vec128
br i1 %173, label %middle.block106, label %vector.body108

```

```

middle.block106:                                ; preds = %vector.body108
8

```

```

%cmp.n132 = icmp eq i64 %.sroa.026.0, %n.vec128
br i1 %cmp.n132, label %L233, label %scalar.ph107

```

```

scalar.ph107:                                   ; preds = %middle.block106
06, %vector.memcheck125, %L185.us.preheader
%bc.resume.val131 = phi i64 [ %n.vec128, %middle.block106 ], [ 0, %L185.us.preheader ], [ 0, %vector.memcheck125 ]
br label %L185.us

```

```

L185.us.us.preheader:                          ; preds = %L185.lr.ph.sp
lit.us
br i1 %min.iters.check140, label %scalar.ph138, label %vector.memcheck156
6

```

```

vector.memcheck156:                            ; preds = %L185.us.us.pr

```

ehheader

```
%scevgep142 = getelementptr double, double* %85, i64 %s.roa.026.0
%uglygep144 = getelementptr i8, i8* %bc116, i64 1
%uglygep145 = getelementptr i8, i8* %bc, i64 1
%bound0147 = icmp ugt i8* %uglygep144, %86
%bound1148 = icmp ult double* %81, %scevgep142
%found.conflict149 = and i1 %bound0147, %bound1148
%bound0151 = icmp ugt i8* %uglygep145, %86
%bound1152 = icmp ult double* %83, %scevgep142
%found.conflict153 = and i1 %bound0151, %bound1152
%conflict.rdx154 = or i1 %found.conflict149, %found.conflict153
br i1 %conflict.rdx154, label %scalar.ph138, label %vector.ph157
```

```
vector.ph157: ; preds = %vector.memche
ck156
```

```
%n.vec159 = and i64 %s.roa.026.0, 9223372036854775792
br label %vector.body139
```

```
vector.body139: ; preds = %vector.body13
9, %vector.ph157
```

```
%index160 = phi i64 [ 0, %vector.ph157 ], [ %index.next161, %vector.body
139 ]
```

```
%174 = load double, double* %81, align 8
%175 = insertelement <4 x double> undef, double %174, i32 0
%176 = load double, double* %83, align 8
%177 = insertelement <4 x double> undef, double %176, i32 0
%178 = fadd <4 x double> %175, %177
%179 = fmul <4 x double> %178, %178
%180 = shufflevector <4 x double> %179, <4 x double> undef, <4 x i32> ze
```

roinitializer

```
%181 = getelementptr inbounds double, double* %85, i64 %index160
%182 = bitcast double* %181 to <4 x double>*
store <4 x double> %180, <4 x double>* %182, align 8
%183 = getelementptr inbounds double, double* %181, i64 4
```



```

%184 = bitcast double* %183 to <4 x double>*
store <4 x double> %180, <4 x double>* %184, align 8
%185 = getelementptr inbounds double, double* %181, i64 8
%186 = bitcast double* %185 to <4 x double>*
store <4 x double> %180, <4 x double>* %186, align 8
%187 = getelementptr inbounds double, double* %181, i64 12
%188 = bitcast double* %187 to <4 x double>*
store <4 x double> %180, <4 x double>* %188, align 8
%index.next161 = add i64 %index160, 16
%189 = icmp eq i64 %index.next161, %n.vec159
br il %189, label %middle.block137, label %vector.body139

```

```

middle.block137:                                     ; preds = %vector.body139
9

```

```

%cmp.n163 = icmp eq i64 %s.roa.026.0, %n.vec159
br il %cmp.n163, label %L233, label %scalar.ph138

```

```

scalar.ph138:                                       ; preds = %middle.block137, %vector.memcheck156, %L185.us.us.preheader
%bc.resume.val162 = phi i64 [ %n.vec159, %middle.block137 ], [ 0, %L185.us.us.preheader ], [ 0, %vector.memcheck156 ]
br label %L185.us.us

```

```

L185.us.us:                                         ; preds = %L185.us.us, %scalar.ph138
%value_phi1351.us.us = phi i64 [ %195, %L185.us.us ], [ %bc.resume.val162, %scalar.ph138 ]

```

```

%190 = load double, double* %81, align 8
%191 = load double, double* %83, align 8
%192 = fadd double %190, %191
%193 = fmul double %192, %192
%194 = getelementptr inbounds double, double* %85, i64 %value_phi1351.us.us
store double %193, double* %194, align 8

```



```
%195 = add nuw nsw i64 %value_phi1351.us.us, 1
%exitcond57.not = icmp eq i64 %195, %.sroa.026.0
br i1 %exitcond57.not, label %L233, label %L185.us.us
```

```
L185.us: ; preds = %L185.us, %scalar.ph107
%value_phi1351.us = phi i64 [ %202, %L185.us ], [ %bc.resume.val131, %scalar.ph107 ]
%196 = load double, double* %81, align 8
%197 = getelementptr inbounds double, double* %83, i64 %value_phi1351.us
%198 = load double, double* %197, align 8
%199 = fadd double %196, %198
%200 = fmul double %199, %199
%201 = getelementptr inbounds double, double* %85, i64 %value_phi1351.us
store double %200, double* %201, align 8
%202 = add nuw nsw i64 %value_phi1351.us, 1
%exitcond55.not = icmp eq i64 %202, %.sroa.026.0
br i1 %exitcond55.not, label %L233, label %L185.us
```

```
L185.us52: ; preds = %L185.us52, %scalar.ph78
%value_phi1351.us53 = phi i64 [ %209, %L185.us52 ], [ %bc.resume.val100, %scalar.ph78 ]
%203 = getelementptr inbounds double, double* %81, i64 %value_phi1351.us53
%204 = load double, double* %203, align 8
%205 = load double, double* %83, align 8
%206 = fadd double %204, %205
%207 = fmul double %206, %206
%208 = getelementptr inbounds double, double* %85, i64 %value_phi1351.us53
store double %207, double* %208, align 8
%209 = add nuw nsw i64 %value_phi1351.us53, 1
%exitcond56.not = icmp eq i64 %209, %.sroa.026.0
```

```
In [26]: @code_native debuginfo=:none foo(A, B)
```

```
.text
pushq   %rbp
movq    %rsp, %rbp
pushq   %r15
pushq   %r14
pushq   %r13
pushq   %r12
pushq   %rbx
andq    $-32, %rsp
subq    $128, %rsp
vxorpd  %xmm0, %xmm0, %xmm0
vmovapd %ymm0, (%rsp)
movq    %rsi, 96(%rsp)
movq    %fs:0, %rdi
movq    $8, (%rsp)
movq    -32768(%rdi), %rax
movq    %rax, 8(%rsp)
movq    %rsp, %rax
movq    %rax, -32768(%rdi)
movq    (%rsi), %r12
movq    8(%rsi), %r13
movq    24(%r12), %r15
movq    24(%r13), %rbx
cmpq    $1, %rbx
je      L112
testq   %rbx, %rbx
jne     L121
testq   %r15, %r15
sete    %al
jmp     L127
```

```

L112:      cmpq    $1, %r15
           sete   %al
           jmp    L127

L121:      cmpq    %r15, %rbx
           sete   %al

L127:      addq    $-32768, %rdi                # imm = 0x8000
           movabsq $jl_system_image_data, %r14
           cmpq    $1, %r15
           movq    %rdi, 40(%rsp)
           je     L225
           testb   %al, %al
           jne    L225
           cmpq    $1, %r15
           je     L184
           testq   %r15, %r15
           jne    L202
           testq   %rbx, %rbx
           sete   %al
           cmpq    $1, %rbx
           jne    L214
           jmp    L197

L184:      cmpq    $1, %rbx
           sete   %al
           cmpq    $1, %rbx
           jne    L214

L197:      movq    %r15, %rbx
           jmp    L225

L202:      cmpq    %rbx, %r15

```

```

sete    %al
cmpq    $1, %rbx
je      L197
L214:
testb   %al, %al
je      L1357
movq    %r15, %rbx
L225:
movq    %rbx, 56(%rsp)
leaq    243107877(%r14), %rax
movabsq $jl_system_image_data, %rdi
movq    %rbx, %rsi
vzeroupper
callq   *%rax
movq    %rax, %r11
movq    24(%rax), %rax
cmpq    $1, %rax
je      L450
testq   %rax, %rax
jne     L489
testq   %rbx, %rbx
jne     L460
L290:
cmpq    %r12, %r11
je      L340
testb   $1, 5030201(%r14)
jne     L340
movq    (%r11), %rax
cmpq    (%r12), %rax
jne     L340
movq    %r11, 24(%rsp)
leaq    243108093(%r14), %rax
movq    %r12, %rdi
movq    %r11, %r15

```

```

    callq    *%rax
    movq    %r15, %r11
    movq    %rax, %r12
L340:
    movq    24(%r12), %r15
    cmpq    %r13, %r11
    je      L401
    testb   $1, 5030201(%r14)
    jne     L401
    movq    (%r11), %rax
    cmpq    (%r13), %rax
    jne     L401
    movq    %r11, 24(%rsp)
    movq    %r12, 16(%rsp)
    addq    $243108093, %r14           # imm = 0xE7D88FD
    movq    %r13, %rdi
    movq    %r11, %r13
    callq   *%r14
    movq    %r13, %r11
    movq    %rax, %r13
L401:
    testq   %rbx, %rbx
    je      L1323
    movq    24(%r13), %rsi
    movq    (%r12), %rax
    movq    (%r13), %rcx
    movq    (%r11), %rdx
    cmpq    $1, %r15
    jne     L500
    cmpq    $1, %rsi
    jne     L523
    cmpq    $16, %rbx
    jae     L557
    xorl   %esi, %esi

```

```
    jmp      L688
L450:
    cmpq    $1, %rbx
    je      L290
L460:
    movq    %rax, 48(%rsp)
    movabsq $throwdm, %rax
    leaq   48(%rsp), %rdi
    leaq   56(%rsp), %rsi
    callq  *%rax
    ud2
L489:
    cmpq    %rbx, %rax
    je      L290
    jmp     L460
L500:
    cmpq    $1, %rsi
    jne     L540
    cmpq    $16, %rbx
    jae     L718
    xorl    %esi, %esi
    jmp     L880
L523:
    cmpq    $16, %rbx
    jae     L911
    xorl    %esi, %esi
    jmp     L1072
L540:
    cmpq    $16, %rbx
    jae     L1103
    xorl    %esi, %esi
    jmp     L1296
L557:
    leaq   (%rdx,%rbx,8), %rsi
```

```

leaq    1(%rax), %rdi
leaq    1(%rcx), %r8
cmpq    %rdx, %rdi
seta    %r9b
cmpq    %rsi, %rax
setb    %r10b
cmpq    %rdx, %r8
seta    %dil
cmpq    %rsi, %rcx
setb    %r8b
xorl    %esi, %esi
testb   %r10b, %r9b
jne     L688
andb    %r8b, %dil
jne     L688
movq    %rbx, %rsi
andq    $-16, %rsi
xorl    %edi, %edi
nop

```

L624:

```

vmovsd  (%rax), %xmm0
vaddsd  (%rcx), %xmm0, %xmm0
vmulsd  %xmm0, %xmm0, %xmm0
vbroadcastsd %xmm0, %ymm0
vmovupd %ymm0, (%rdx,%rdi,8)
vmovupd %ymm0, 32(%rdx,%rdi,8)
vmovupd %ymm0, 64(%rdx,%rdi,8)
vmovupd %ymm0, 96(%rdx,%rdi,8)
addq    $16, %rdi
cmpq    %rdi, %rsi
jne     L624
cmpq    %rsi, %rbx
je      L1323
nopw    (%rax,%rax)

```

xmm0 = mem[0],zero

L688:

```
vmovsd    (%rax), %xmm0
vaddsd    (%rcx), %xmm0, %xmm0
vmulsd    %xmm0, %xmm0, %xmm0
vmovsd    %xmm0, (%rdx,%rsi,8)
incq      %rsi
cmpq      %rsi, %rbx
jne       L688
jmp       L1323
```

xmm0 = mem[0],zero

L718:

```
leaq      (%rdx,%rbx,8), %rsi
leaq      (%rax,%rbx,8), %rdi
leaq      1(%rcx), %r8
cmpq      %rdi, %rdx
setb      %r9b
cmpq      %rsi, %rax
setb      %r10b
cmpq      %rdx, %r8
seta      %dil
cmpq      %rsi, %rcx
setb      %r8b
xorl      %esi, %esi
testb     %r10b, %r9b
jne       L880
andb      %r8b, %dil
jne       L880
movq      %rbx, %rsi
andq      $-16, %rsi
vmovsd    (%rcx), %xmm0
xorl      %edi, %edi
vbroadcastsd %xmm0, %ymm0
nopw      %cs:(%rax,%rax)
```

xmm0 = mem[0],zero

L800:

```
vaddpd    (%rax,%rdi,8), %ymm0, %ymm1
```



```

vaddpd 32(%rax,%rdi,8), %ymm0, %ymm2
vaddpd 64(%rax,%rdi,8), %ymm0, %ymm3
vaddpd 96(%rax,%rdi,8), %ymm0, %ymm4
vmulpd %ymm1, %ymm1, %ymm1
vmulpd %ymm2, %ymm2, %ymm2
vmulpd %ymm3, %ymm3, %ymm3
vmulpd %ymm4, %ymm4, %ymm4
vmovupd %ymm1, (%rdx,%rdi,8)
vmovupd %ymm2, 32(%rdx,%rdi,8)
vmovupd %ymm3, 64(%rdx,%rdi,8)
vmovupd %ymm4, 96(%rdx,%rdi,8)
addq $16, %rdi
cmpq %rdi, %rsi
jne L800
cmpq %rsi, %rbx
je L1323

```

L880:

```

vmovsd (%rax,%rsi,8), %xmm0
vaddsd (%rcx), %xmm0, %xmm0
vmulsd %xmm0, %xmm0, %xmm0
vmovsd %xmm0, (%rdx,%rsi,8)
incq %rsi
cmpq %rsi, %rbx
jne L880
jmp L1323

```

xmm0 = mem[0],zero

L911:

```

leaq (%rdx,%rbx,8), %rsi
leaq 1(%rax), %rdi
leaq (%rcx,%rbx,8), %r8
cmpq %rdx, %rdi
seta %r9b
cmpq %rsi, %rax
setb %r10b
cmpq %r8, %rdx

```

```

setb    %dil
cmpq    %rsi, %rcx
setb    %r8b
xorl    %esi, %esi
testb   %r10b, %r9b
jne     L1072
andb    %r8b, %dil
jne     L1072
movq    %rbx, %rsi
andq    $-16, %rsi
vmovsd  (%rax), %xmm0           # xmm0 = mem[0],zero
xorl    %edi, %edi
vbroadcastsd %xmm0, %ymm0
nopw    %cs:(%rax,%rax)

```

L992:

```

vaddpd  (%rcx,%rdi,8), %ymm0, %ymm1
vaddpd  32(%rcx,%rdi,8), %ymm0, %ymm2
vaddpd  64(%rcx,%rdi,8), %ymm0, %ymm3
vaddpd  96(%rcx,%rdi,8), %ymm0, %ymm4
vmulpd  %ymm1, %ymm1, %ymm1
vmulpd  %ymm2, %ymm2, %ymm2
vmulpd  %ymm3, %ymm3, %ymm3
vmulpd  %ymm4, %ymm4, %ymm4
vmovupd %ymm1, (%rdx,%rdi,8)
vmovupd %ymm2, 32(%rdx,%rdi,8)
vmovupd %ymm3, 64(%rdx,%rdi,8)
vmovupd %ymm4, 96(%rdx,%rdi,8)
addq    $16, %rdi
cmpq    %rdi, %rsi
jne     L992
cmpq    %rsi, %rbx
je      L1323

```

L1072:

```

vmovsd  (%rax), %xmm0           # xmm0 = mem[0],zero

```

```
vaddsd (%rcx,%rsi,8), %xmm0, %xmm0
vmulsd %xmm0, %xmm0, %xmm0
vmovsd %xmm0, (%rdx,%rsi,8)
incq %rsi
cmpq %rsi, %rbx
jne L1072
jmp L1323
```

L1103:

```
leaq (%rdx,%rbx,8), %rsi
leaq (%rax,%rbx,8), %rdi
leaq (%rcx,%rbx,8), %r8
cmpq %rdi, %rdx
setb %r9b
cmpq %rsi, %rax
setb %r10b
cmpq %r8, %rdx
setb %dil
cmpq %rsi, %rcx
setb %r8b
xorl %esi, %esi
testb %r10b, %r9b
jne L1296
andb %r8b, %dil
jne L1296
movq %rbx, %rsi
andq $-16, %rsi
xorl %edi, %edi
nopw %cs:(%rax,%rax)
```

L1184:

```
vmovupd (%rax,%rdi,8), %ymm0
vmovupd 32(%rax,%rdi,8), %ymm1
vmovupd 64(%rax,%rdi,8), %ymm2
vmovupd 96(%rax,%rdi,8), %ymm3
vaddpd (%rcx,%rdi,8), %ymm0, %ymm0
```

```

vaddpd 32(%rcx,%rdi,8), %ymm1, %ymm1
vaddpd 64(%rcx,%rdi,8), %ymm2, %ymm2
vaddpd 96(%rcx,%rdi,8), %ymm3, %ymm3
vmulpd %ymm0, %ymm0, %ymm0
vmulpd %ymm1, %ymm1, %ymm1
vmulpd %ymm2, %ymm2, %ymm2
vmulpd %ymm3, %ymm3, %ymm3
vmovupd %ymm0, (%rdx,%rdi,8)
vmovupd %ymm1, 32(%rdx,%rdi,8)
vmovupd %ymm2, 64(%rdx,%rdi,8)
vmovupd %ymm3, 96(%rdx,%rdi,8)
addq $16, %rdi
cmpq %rdi, %rsi
jne L1184
cmpq %rsi, %rbx
je L1323
nopw (%rax,%rax)

```

L1296:

```

vmovsd (%rax,%rsi,8), %xmm0
vaddsd (%rcx,%rsi,8), %xmm0, %xmm0
vmsd %xmm0, %xmm0, %xmm0
vmovsd %xmm0, (%rdx,%rsi,8)
incq %rsi
cmpq %rsi, %rbx
jne L1296

```

xmm0 = mem[0],zero

L1323:

```

movq 8(%rsp), %rax
movq 40(%rsp), %rcx
movq %rax, (%rcx)
movq %r11, %rax
leaq -40(%rbp), %rsp
popq %rbx
popq %r12
popq %r13

```

```
popq    %r14
popq    %r15
popq    %rbp
vzeroupper
retq
```

L1357:

```
movabsq $140310593213369, %rax      # imm = 0x7F9C9B1113B9
movl    $1400, %esi                # imm = 0x578
movl    $16, %edx
movq    %rdi, %r12
vzeroupper
callq   *%rax
movq    %r14, -8(%rax)
movq    %r15, (%rax)
movq    %rax, 16(%rsp)
movq    %rax, 64(%rsp)
movabsq $j_l_apply_generic, %rax
movabsq $j_l_system_image_data, %rdi
leaq    64(%rsp), %r15
movq    %r15, %rsi
movl    $1, %edx
callq   *%rax
movq    %rax, %r13
movq    %rax, 24(%rsp)
movq    %r12, %rdi
movl    $1400, %esi                # imm = 0x578
movl    $16, %edx
movabsq $140310593213369, %rax      # imm = 0x7F9C9B1113B9
callq   *%rax
movq    %r14, -8(%rax)
movq    %rbx, (%rax)
movq    %rax, 16(%rsp)
movq    %rax, 64(%rsp)
movabsq $j_l_system_image_data, %rdi
```

```
movq    %r15, %rsi
movl    $1, %edx
movabsq $jll_apply_generic, %rbx
callq   *%rbx
movq    %rax, 16(%rsp)
movabsq $jll_system_image_data, %rcx
movq    %rcx, 64(%rsp)
movq    %r13, 72(%rsp)
movabsq $jll_system_image_data, %rcx
movq    %rcx, 80(%rsp)
movq    %rax, 88(%rsp)
movabsq $jll_system_image_data, %rdi
movq    %r15, %rsi
movl    $4, %edx
callq   *%rbx
movq    %rax, 16(%rsp)
movq    %rax, 64(%rsp)
movabsq $jll_system_image_data, %rdi
movq    %r15, %rsi
movl    $1, %edx
callq   *%rbx
movabsq $jll_throw, %rcx
movq    %rax, %rdi
callq   *%rcx
```

Package management

- Julia probably has the best package management to date
- Press "]" to enter package management console
- Typically `add PACKAGE_NAME` is sufficient, can also do `add PACKAGE_NAME@VERSION`
- To get an unreleased version, use `add PACKAGE_NAME#BRANCH_NAME`
- Easy to start modifying a package via `dev PACKAGE_NAME`
- Multiple package versions can be installed, selection via [Pkg.jl environments](#).
- Also useful: `julia> using Pkg; pkg"<Pkg console command>"`

Package creation

- A Julia package needs:
 - A "Project.toml" file
 - A "src/PackageName.jl" file
- That's it: Push to GitHub, and package is installable via `add PACKAGE_URL`
- Use [Documenter.jl](#) to document your package
- To enable `add PACKAGE_NAME`, package must be [registered](#), there are [some rules](#)
- Use [PkgTemplates.jl](#) to generate new package with CI config (Travis, Appveyor, ...), docs generation, etc.

No free lunch

- Package loading and code-gen can sometime take a long time, but mitigations available:
- [Revise.jl](#): Hot code-reloading at runtime
- [\[PackageCompiler.jl\]\(https://github.com/JuliaLang/PackageCompiler.jl\)](https://github.com/JuliaLang/PackageCompiler.jl): Ahead-of-time compilation, producing custom Julia system images

Performance tips

- Read the [official Julia performance tips](#)!
- Do *not* call on (non-const) global variables from time-critical code
- Type-stable code is fast code. Use `@code_warntype` and `Test.@inferred` to check!
- In some situations, closures [can be troublesome](#), using `let` can help the compiler

This is efficient (not runtime reflection):

```
In [27]: half_dynrange(T::Type{<:Number}) = (Int(typemax(T)) - Int(typemin(T))) / 2  
half_dynrange(Int16)
```

```
Out[27]: 32767.5
```

```
In [28]: @code_llvm half_dynrange(Int16)  
  
; @ In[27]:1 within `half_dynrange'  
define double @julia_half_dynrange_2449() {  
top:  
    ret double 3.276750e+04  
}
```

SIMD

Demo

Shared-memory parallelism

- Julia has native multithreading support
- Simple cases: Use `@threads` macro
- Since Julia v1.3: Cache-efficient [composable multi-threaded parallelism](#)

Processes, Clusters, MPI

- Julia brings a full API for remote processes and compute clusters
- Native support for local processes and remote processes via SSH
- MPI support via [MPI.jl](#) and [MPIClusterManagers.jl](#)

Benchmarking and profiling, digging deeper

Demo

Docs and help

- [Official Julia docs](#)
- [Julia Cheat Sheet](#)
- [ThinkJulia](#)
- <https://julialang.org/learning/>
- [Julia Discourse](#)
- [Julia Slack](#)
- [Julia Gitter](#)
- [Julia on Youtube](#)
- [JuliaCon 2020](#)

Statistics

Demo

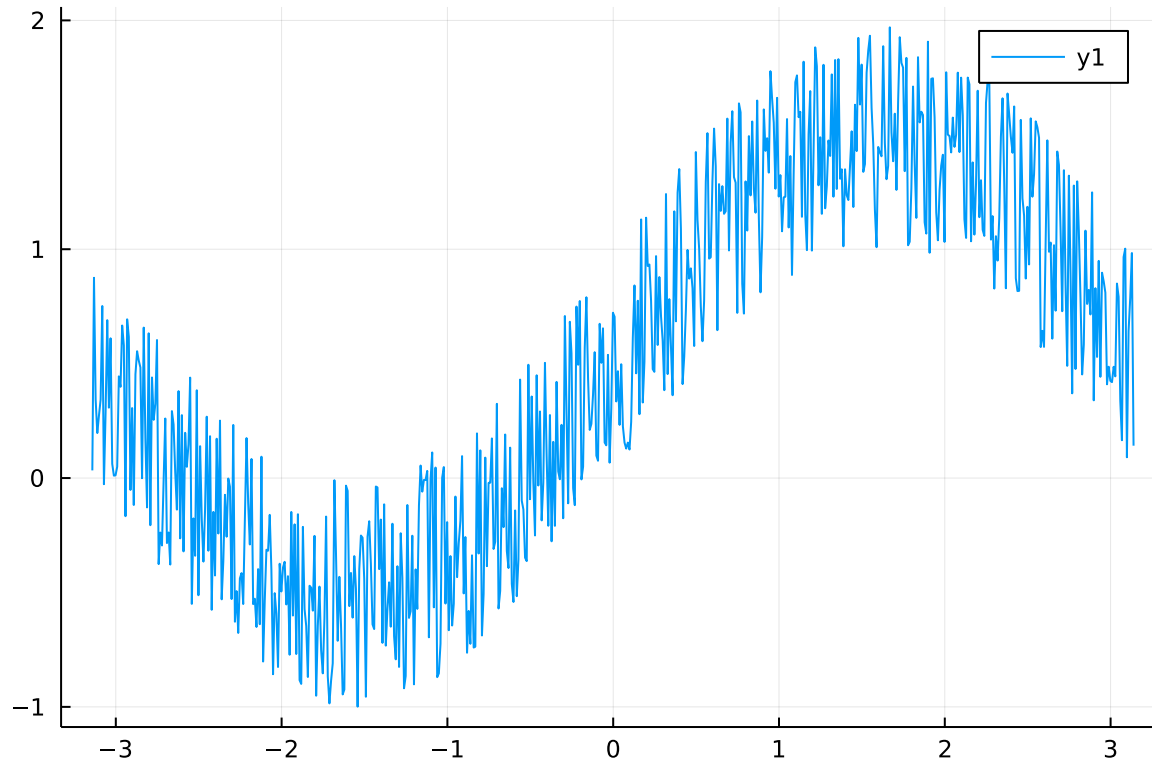
Visualization/Plotting: Plots, Makie, plotting recipes

Let's Make a Plot

In [29]:

```
using Plots
range = -π:0.01:π
plot(range, sin.(range) + rand(length(range)))
```

Out[29]:

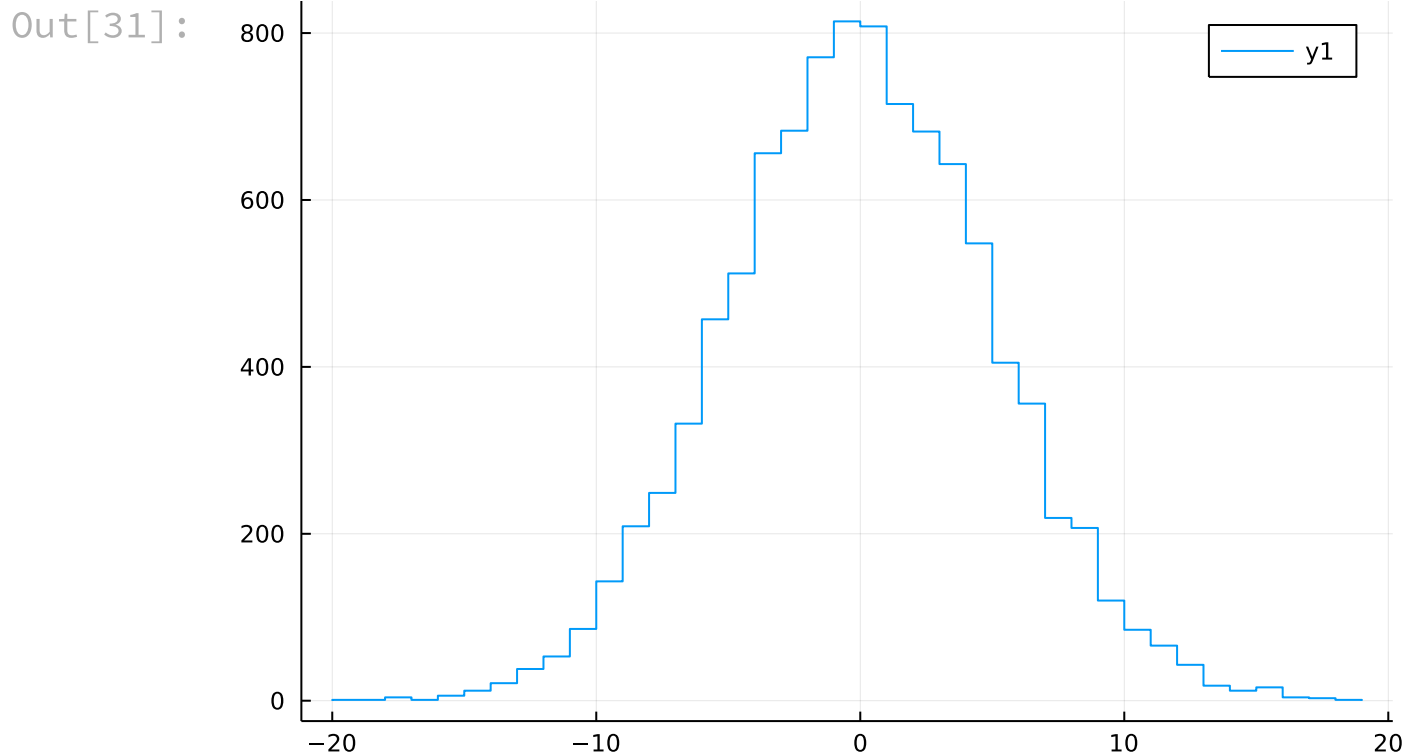


Histograms are easy, too

```
In [30]: using Distributions  
         dist = Normal(0.0, 5.0)
```

```
Out[30]: Normal{Float64}(μ=0.0, σ=5.0)
```

```
In [31]: stephist(rand(dist, 10000))
```



Automatic differentiation

Let's define a simple neural network layer and loss function and auto-differentiate through it.

```
In [32]: struct DenseLayer{M::AbstractMatrix{<:Real},V::AbstractVector{<:Real},F::Function} <: Function
          A::M
          b::V
          f::F
        end

        (l::DenseLayer)(x::AbstractVector{<:Real}) = (l.f).(l.A * x + l.b)

        f_loss(y) = sum(y .^ 2);
```

```
In [33]: mylayer = DenseLayer(rand(5,5), rand(5), x -> ifelse(x > zero(x), x, zero(x)));
```

```
In [34]: x = rand(5)
          mylayer(x)
```

```
Out[34]: 5-element Vector{Float64}:
          1.7041810782876734
          1.163826388903705
          1.682990185750071
          2.6543044638188427
          2.161791402654909
```

```
In [35]: f_loss(mylayer(x))
```

```
Out[35]: 18.809855231674746
```

```
In [36]: using Zygote
g = Zygote.gradient((mylayer, x) -> f_loss(mylayer(x)), mylayer, x)
g[1].A
```

```
Out[36]: 5×5 Matrix{Float64}:
 2.78885  1.12708  3.20878  1.92882  1.42191
 1.90457  0.769712  2.19135  1.31724  0.971056
 2.75417  1.11307  3.16888  1.90484  1.40423
 4.3437   1.75546  4.99775  3.00419  2.21466
 3.53772  1.42973  4.07041  2.44675  1.80372
```

```
In [37]: g[1].b
```

```
Out[37]: 5-element Vector{Float64}:
 3.408362156575347
 2.32765277780741
 3.365980371500142
 5.308608927637685
 4.323582805309818
```

Calling code written in other language, REPL modes

Shell REPL mode

- The Julia shell is multi-language
- Press "!" for a system shell

PyCall, RCall

Calling Python from Julia is easy, can even use inline Python code:

```
using PyCall
numpy = pyimport("numpy")
numpy.zeros(5) isa Array

A = rand(5)
py"""type($A)""" isa PyObject
```


An incomplete tour of the Julia package ecosystem

Math

- [ApproxFun.jl](#): Powerful function approximations
- [FFTW.jl](#): Fast fourier transforms via [FFTW](#)
- [DifferentialEquations.jl](#): A suite for numerically solving differential equations
- ...

Optimization

- [JuMP.jl](#): Modeling language for Mathematical Optimization
- [NLOpt.jl](#): Optimization via [NLOpt](#)
- [Optim](#): Julia native nonlinear optimization

TypedTables and DataFrames

- [Tables.jl](#): Abstract API for tabular data
- [DataFrames.jl](#): Python/R-like dataframes
- [TypedTables.jl](#): Type-stable tables
- [Query.jl](#) LINQ-inspired data query and transformation

Plotting and Visualization

- [IJulia.jl](#): Julia Jupyter kernel
- [Images.jl](#): Image processing
- [PyPlot.jl](#): Use matplotlib/PyPlot from Julia
- [Makie.jl](#): Hardware-accelerated plotting
- [Plots.jl](#): Plotting with generic recipes and multiple backends

Statistics

- [Distributions.jl](#): Probability distributions and associated functions
- [StatsBase.jl](#): Statistics, histograms, etc.
- Many specialized packages

Automatic Differentiation

- [ForwardDiff.jl](#): Forward-mode automatic differentiation
- [Zyote.jl](#): Source-level reverse-mode automatic differentiation
- [Enzyme.jl](#): LLVM-level reverse-mode automatic differentiation
- Several other packages available ([ReverseDiff.jl](#), [Nabla.jl](#), [Yota.jl](#), ...)
- Exciting developments to come with new Julia Compiler features

Bayesian analysis and probabilistic programming

- [BAT.jl](#): Bayesian analysis toolkit
- [Gen.jl](#): General-Purpose Probabilistic Programming System
- [Mamba.jl](#): MCMC for Bayesian analysis
- [Turing.jl](#): Probabilistic machine learning and Bayesian statistics
- ...

Machine learning

- [Flux.jl](#): Julia native deep learning library
- [Knet.jl](#): Koc University deep learning framework
- [MXNet.jl](#): MXNet Julia API
- ...

Calling code in other languages

- [Cxx.jl](#): Call C++ from Julia
- [PyCall.jl](#): Call Python from Julia
- [RCall.jl](#): Call R from Julia
- ...

Efficient memory layout

- [ArraysOfArrays.jl](#): Duality of flat and nested arrays
- [StructArrays.jl](#), [TypedTables.jl](#): AoS and SoA duality
- [ValueShapes.jl](#): Duality of flat and nested structures
- ...

GPU Programming

- [AMDGPU.jl](#): Julia on AMD GPUs (WIP)
- [CUDA.jl](#): Julia on NVIDIA GPUs
- [GPUArrays.jl](#): Generic CPU programming API
- [XLA.jl](#): Julia on Google TPUs
- Maybe more architectures in the future?

IDEs

- [julia-vscode](#): Visual Studio Code based Julia IDE
- [Juno](#): Atom based Julia IDE (now deprecated in favor of VS code)

Final Remarks

- Julia is productive, fast and fun - give it a chance!
- Multiple dispatch opens up powerful ways of combining code