

Axion Dark Matter in the Time of Primordial Black Holes

Based on:

NB, Fazlollah Hajkarim & Yong Xu [arXiv:2107.13575](https://arxiv.org/abs/2107.13575)



Nicolás BERNAL

UAN
UNIVERSIDAD
ANTONIO NARIÑO

CoCo 2021

September 8 – 10, 2021



El conocimiento
es de todos

Minciencias



Javier Humberto
Ordoñez



Julieth Ramirez
Meza

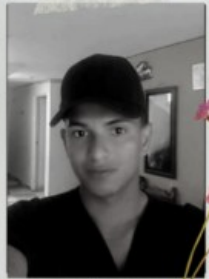


Lorwan Estiwen
Mendoza

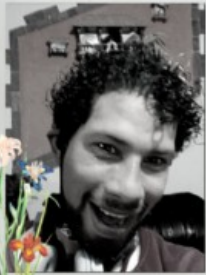
Julieth Ramirez
Meza



Julián Mauricio
González



Andrés Felipe
Rodríguez Ávila



Anthony Gabriel
Estrada Espinoza

Murdered by the Police September 2020



Freddy Alexander
Mahecha



Jaider Fonseca
Castillo



Angie Paola
Baquero Rojas



Christian Andrés
Hurtado Menecés



Cristian Camilo
Hernández Yara



Germán Smyth
Puentes Valero

Strong CP Problem

$$\mathcal{L}_{\text{QCD}} = \underbrace{-\frac{1}{4}G_{\mu\nu a}G_a^{\mu\nu} + \sum_q i\bar{q}\gamma^\mu D_\mu q - m_q\bar{q}q}_{\text{CP conserving}}$$

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Electric dipole moment of the neutron...

$$d_n = (2.4 \pm 1.0)\theta \times 10^{-3} e \text{ fm}$$

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Electric dipole moment of the neutron... *not observed!*

$$d_n = (2.4 \pm 1.0)\theta \times 10^{-3} e \text{ fm}$$

$$|\theta| < 1.3 \times 10^{-10}$$

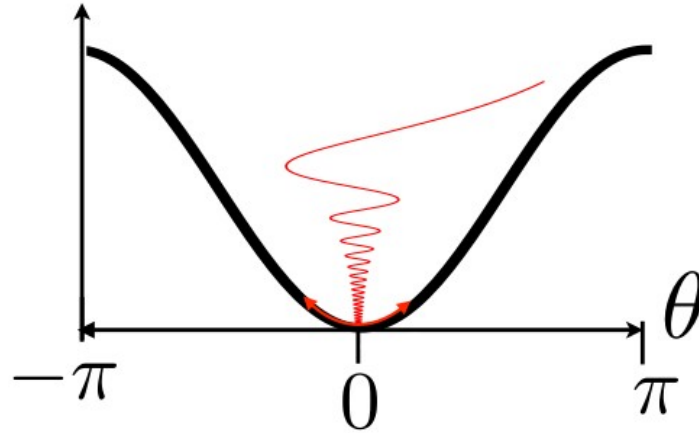
← **Strong CP problem!**

Axion

Talk by Moira

If θ is a *dynamical field*, QCD will relax it to its minimum...
→ Strong QCD problem explained!

Peccei & Quinn '77

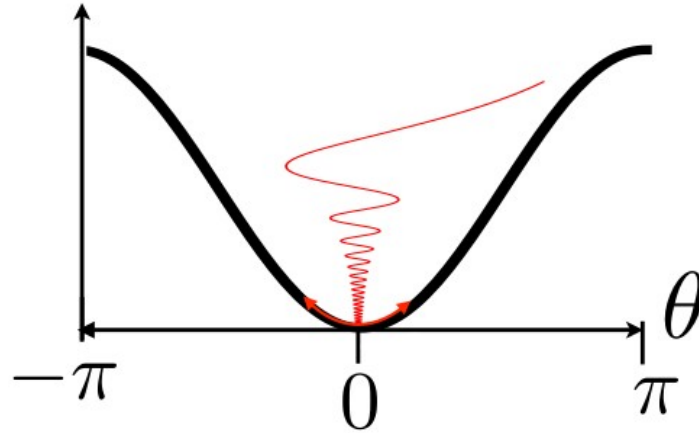


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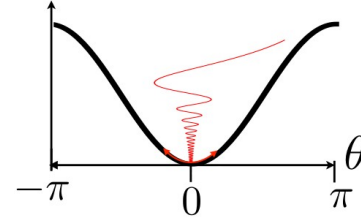


Axion oscillates in a \sim quadratic potential
→ natural *cold dark matter* candidate

Misalignment: Producing Axion DM

Effective axion potential

$$V(\theta) = \chi(T) (1 - \cos \theta)$$



Evolution of the axion field

$$\ddot{\theta} + 3H(T)\dot{\theta} + m_a^2(T) \sin \theta = 0$$

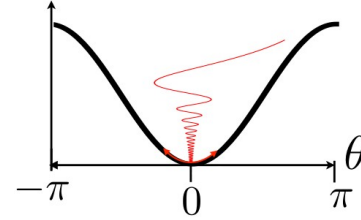
Axion energy density

$$\rho_a(T) = \frac{1}{2} f_a^2 \dot{\theta}^2 + m_a^2(T) f_a^2 (1 - \cos \theta)$$

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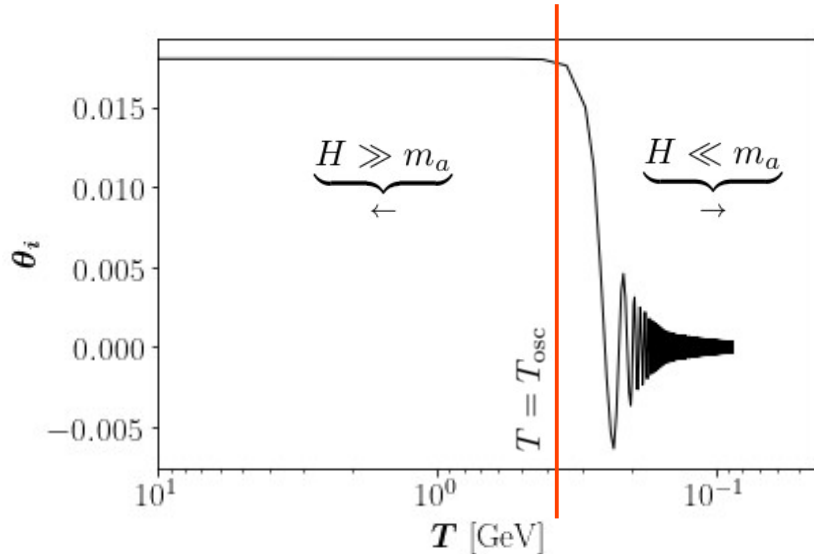


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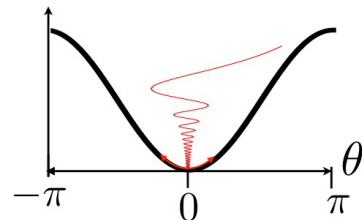
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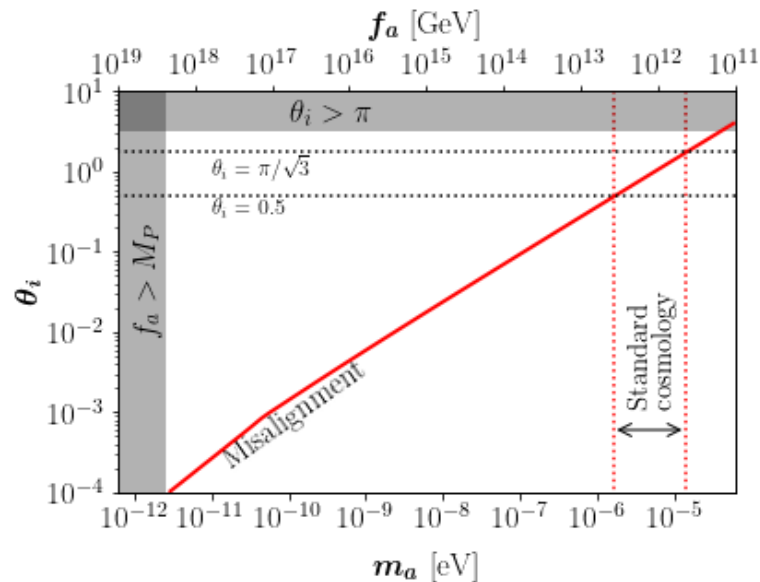
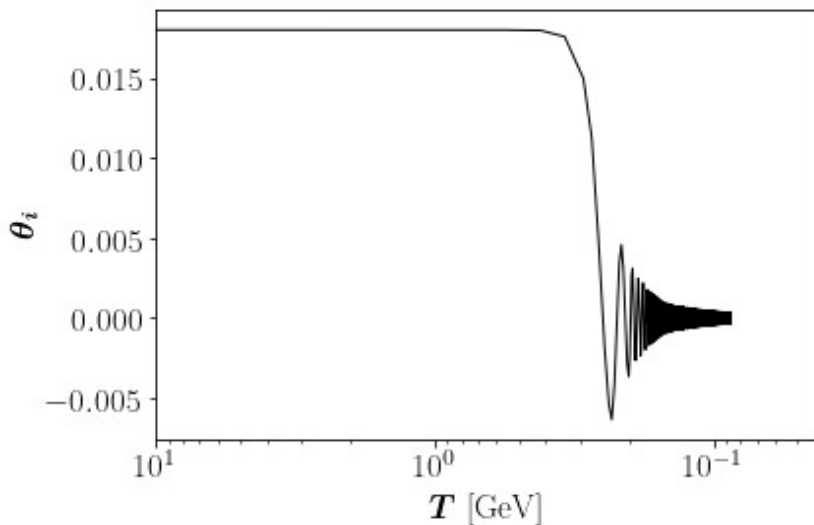


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Misalignment in the Time of Primordial Black Holes

Primordial Black Holes

Talks by
Ashadul &
Satyabrata

- * Density fluctuations can collapse into a PBH in the early universe
- * Lose mass by emitting *all* particles via Hawking evaporation
 - PBH have a ~black body spectrum, with temperature $T_{\text{BH}} \sim 1/M_{\text{BH}}$
 - PBHs unavoidable radiate DM!
- * If $M_{\text{in}} < 10^9$ g, PBH completely evaporate before BBN
 - poorly constrained

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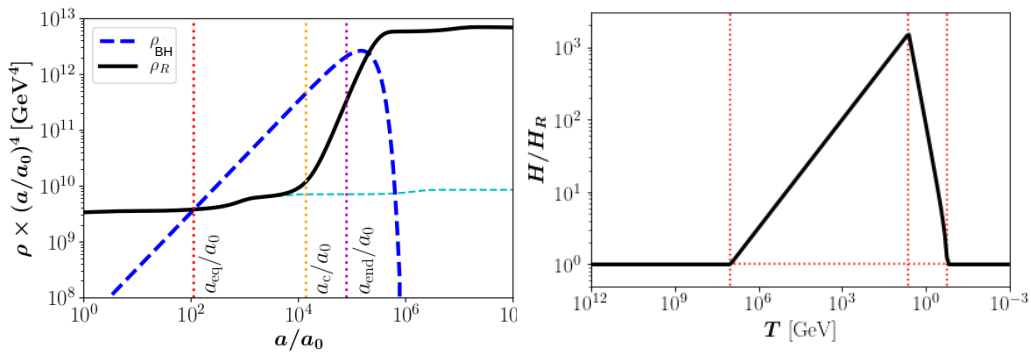
Effective theory: Two free parameters

- * A single PBH characterized by its mass at formation M_{in}
(or equivalently, by the SM temperature T_{in} at formation)
- * Initial PBH energy density $\beta = \rho_{\text{BH}}/\rho_{\text{SM}}$

PBHs can dominate the total energy density: Non-standard cosmology

Talk by Moira

Hubble expansion rate modified

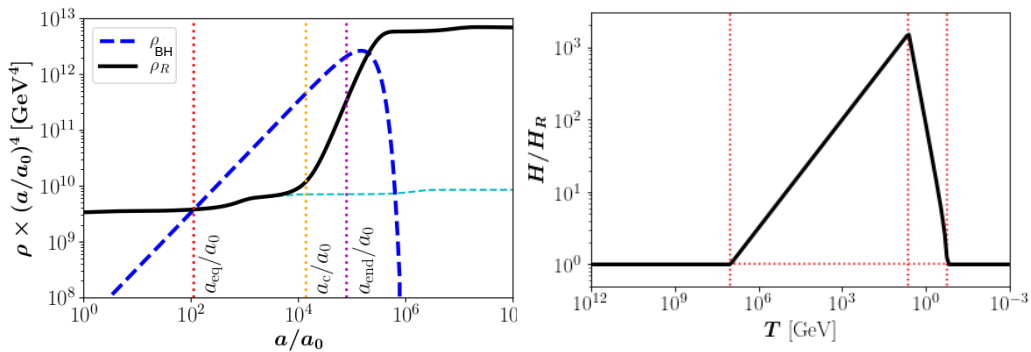


$$H(T) \simeq \begin{cases} H_R(T) & \text{for } T \geq T_{\text{eq}}, \\ H_R(T_{\text{eq}}) \left[\frac{g_{\star s}(T)}{g_{\star s}(T_{\text{eq}})} \left(\frac{T}{T_{\text{eq}}} \right)^3 \right]^{1/2} & \text{for } T_{\text{eq}} \geq T \geq T_c, \\ H_R(T_{\text{ev}}) \left[1 - \frac{720}{\pi} \frac{M_{\text{in}}^3}{g_{\star}(T_{\text{in}})} \frac{M_{\text{P}}^4}{M_{\text{P}}^4} \frac{H_R^2(T_{\text{ev}}) - H_R^2(T)}{H_R(T_{\text{ev}})} \right] & \text{for } T_c \geq T \geq T_{\text{ev}}, \\ H_R(T) & \text{for } T_{\text{ev}} \geq T, \end{cases}$$

PBHs can dominate the total energy density: Non-standard cosmology

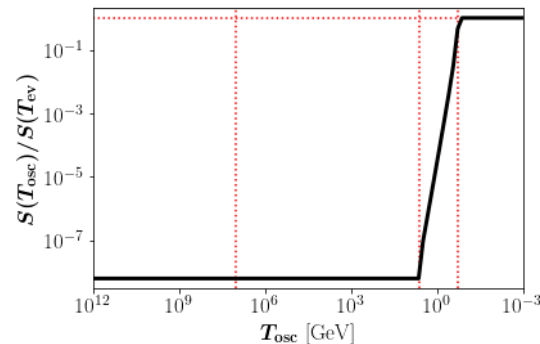
Talk by Moira

Hubble expansion rate modified



Entropy injection

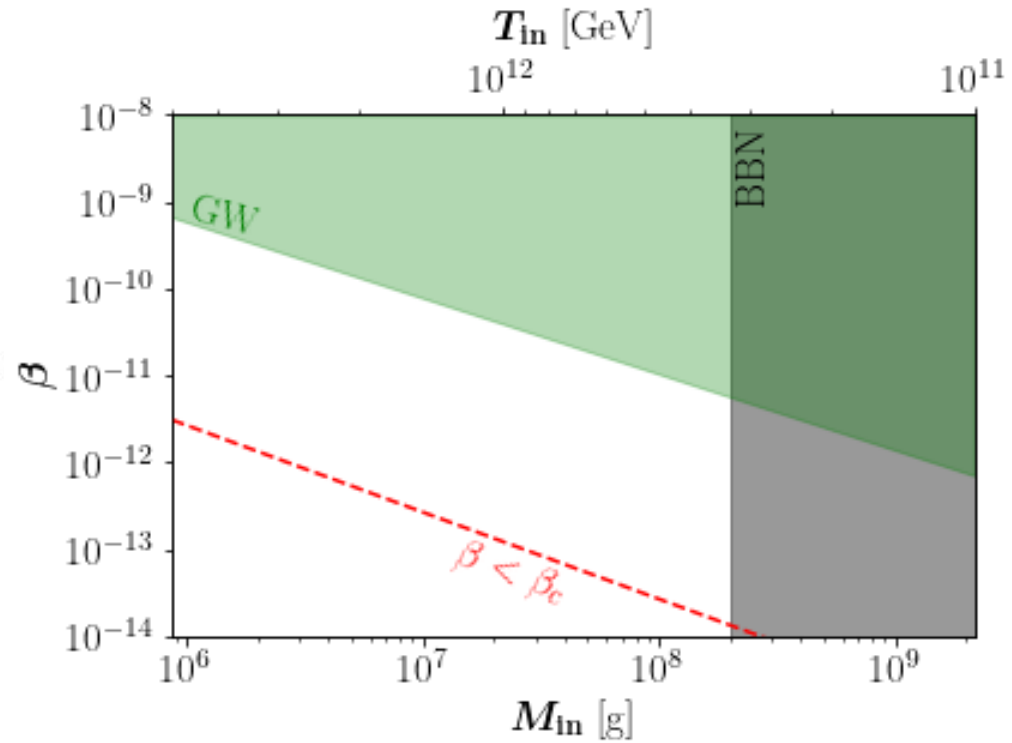
PBHs evaporate,
Hawking radiating all SM particles...



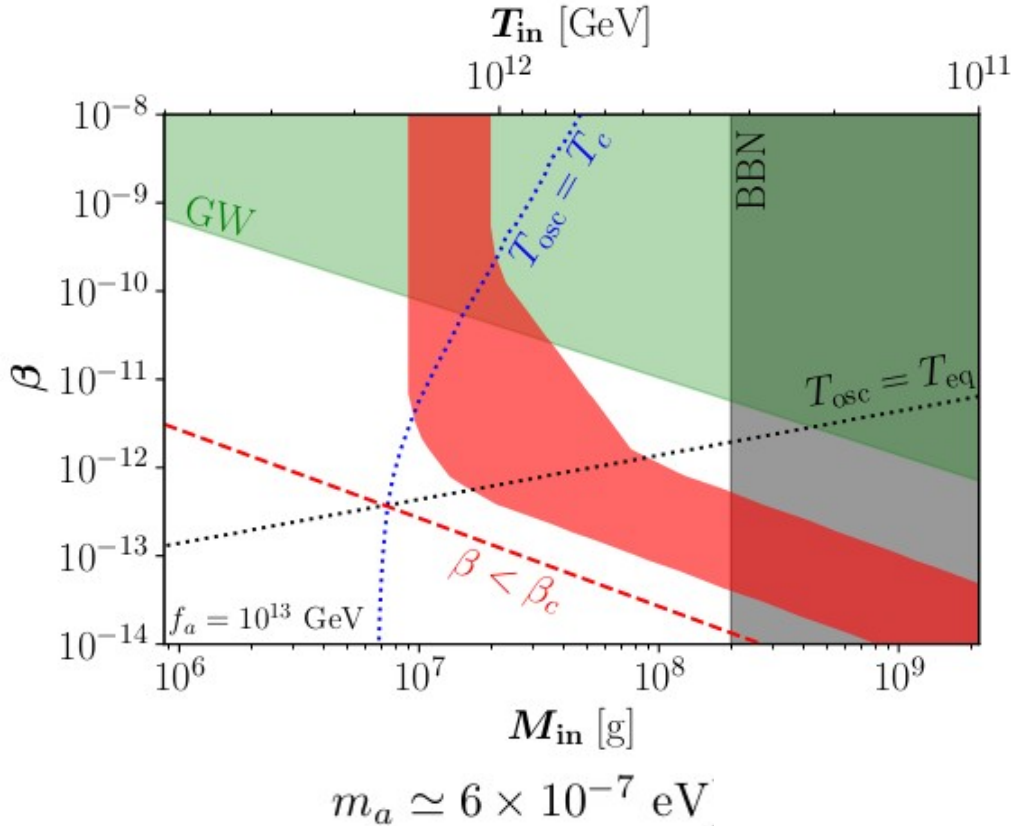
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$$\frac{S(T)}{S(T_{\text{ev}})} \simeq \begin{cases} \frac{g_{\star s}(T_{\text{eq}})}{g_{\star s}(T_{\text{ev}})} \frac{g_{\star}(T_{\text{ev}})}{g_{\star}(T_{\text{eq}})} \frac{T_{\text{ev}}}{T_{\text{eq}}} & \text{for } T \geq T_c, \\ \frac{g_{\star s}(T)}{g_{\star s}(T_{\text{ev}})} \left(\frac{T}{T_{\text{ev}}} \right)^3 \left[1 - \frac{720}{\pi} \frac{M_{\text{in}}^3}{g_{\star}(T_{\text{in}}) M_P^4} \frac{H_R^2(T_{\text{ev}}) - H_R^2(T)}{H_R(T_{\text{ev}})} \right]^{-2} & \text{for } T_c \geq T \geq T_{\text{ev}}, \\ 1 & \text{for } T_{\text{ev}} \geq T. \end{cases}$$

Misalignment with PBHs

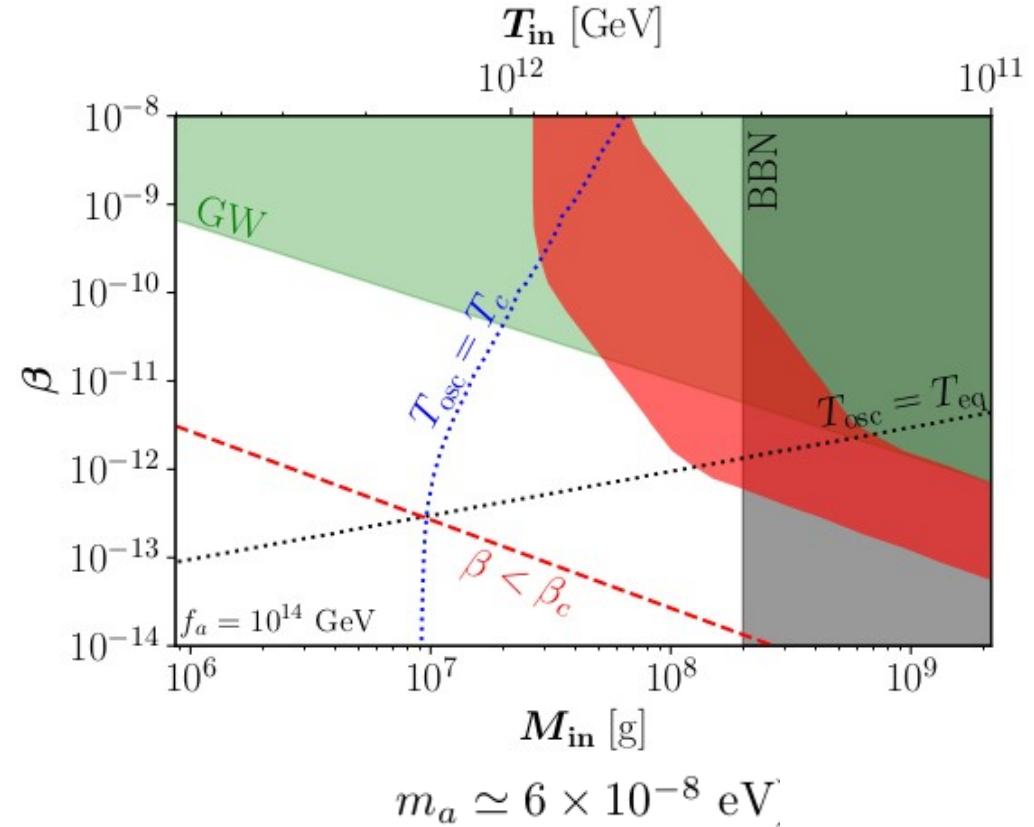
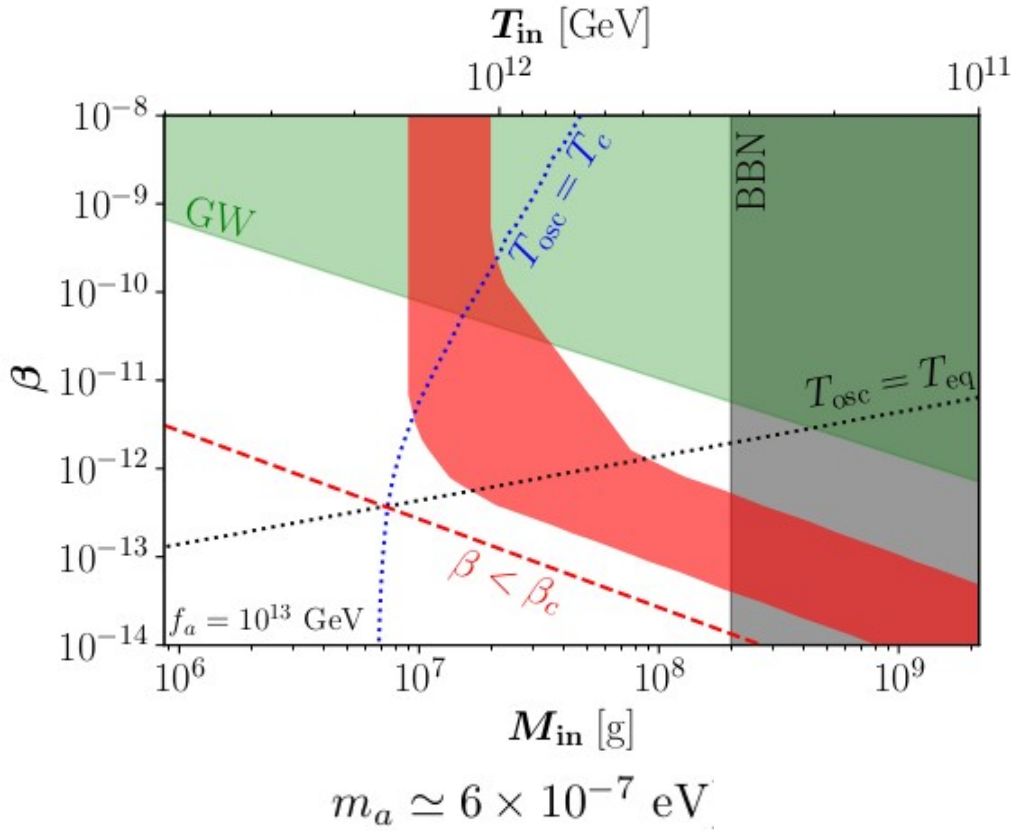


Misalignment with PBHs

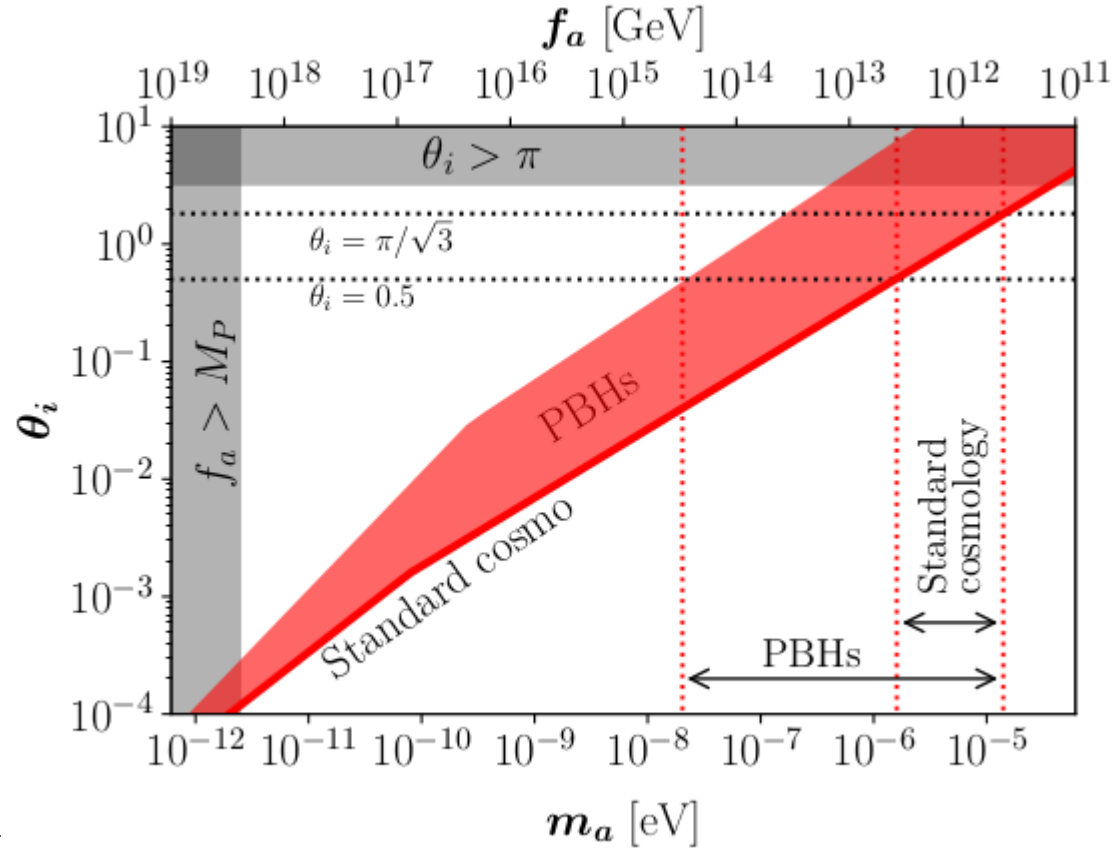


$$\frac{\Omega_a h^2}{0.12} \simeq \begin{cases} \left(\frac{\theta_i}{1}\right)^2 \left(\frac{m_a}{10^{-7} \text{ eV}}\right)^{-\frac{3}{2}} \left(\frac{\beta}{10^{-13}}\right)^{-1} \left(\frac{M_{\text{in}}}{10^8 \text{ g}}\right)^{-1} & \text{for } T_{\text{osc}} \geq T_{\text{eq}}, \\ \left(\frac{\theta_i}{1}\right)^2 \left(\frac{m_a}{10^{-8} \text{ eV}}\right)^{-2} \left(\frac{M_{\text{in}}}{10^8 \text{ g}}\right)^{-\frac{3}{2}} & \text{for } T_{\text{eq}} \geq T_{\text{osc}} \geq T_c, \\ \left(\frac{\theta_i}{1}\right)^2 \left(\frac{m_a}{10^{-8} \text{ eV}}\right)^{-2} \left(\frac{M_{\text{in}}}{10^8 \text{ g}}\right)^{-\frac{3}{2}} & \text{for } T_c \geq T_{\text{osc}} \geq T_{\text{ev}}, \\ \left(\frac{\theta_i}{10^{-3}}\right)^2 \left(\frac{m_a}{m_{\text{QCD}}}\right)^{-\frac{3}{2}} & \text{for } T_{\text{ev}} \geq T_{\text{osc}}. \end{cases}$$

Misalignment with PBHs



Misalignment with PBHs



Axions radiated by PBHs

PBHs *inevitably* radiate axions during their Hawking evaporation

As these axions are ultra-relativistic:

→ can't be the cold DM

→ contribute to dark radiation $\Delta N_{\text{eff}} \simeq 0.04$

within the reach of future CMB-S4 experiment!

Conclusions

- QCD axion solved the strong CP problem
- QCD axion is a viable DM candidate
- PBHs formed in the early universe
- $0.1 \text{ g} < M_{\text{in}} < 10^9 \text{ g}$ evaporate before BBN
- PBHs Hawking radiate ultra-relativistic axions (dark radiation) → tested by CMB-S4
- PBHs could generate a period of non-standard cosmology
- Strong impact on axion production by misalignment
- Hubble expansion enhanced → oscillation gets delayed
- Entropy injection → axion density gets diluted
- Standard axion window is enlarged: *lighter axion allowed* → $m_a > 10^{-8} \text{ eV}$
→ could be tested by ABRACADABRA, KLASH, and ADMX



**¡Muchas
gracias!**