

Probing the doubly magic shell closure at ^{132}Sn by Coulomb excitation of neutron-rich $^{130,134}\text{Sn}$ isotopes

- shell model results vs experiment
- experiment at HIE-ISOLDE
- beam time, rate estimates



Peter Reiter

Institute of Nuclear Physics, University of Cologne

INTC meeting, 23rd – 24th June 2021

Collaboration

Proposal to the ISOLDE and Neutron Time-of-Flight Committee

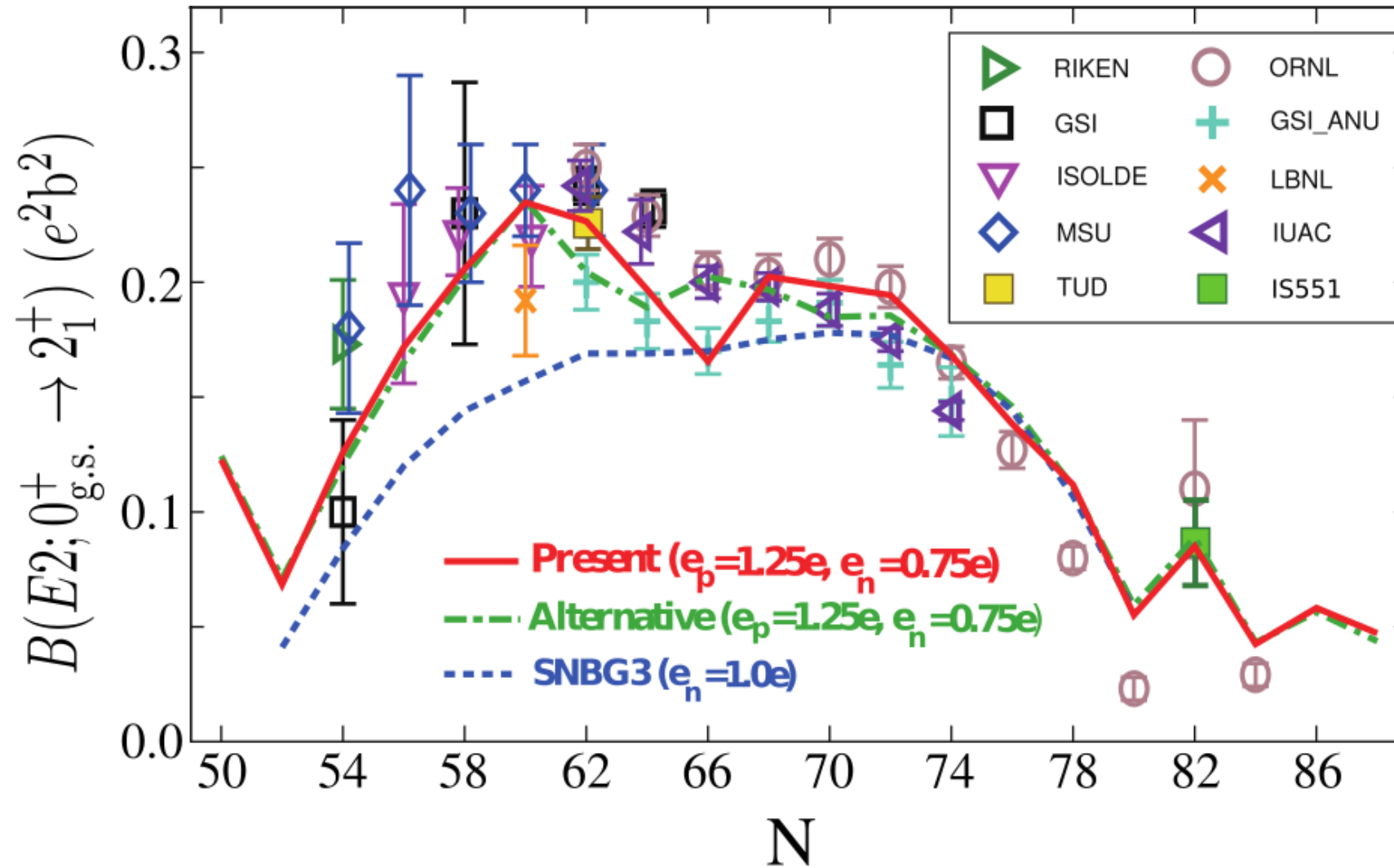
Probing the doubly magic shell closure at ^{132}Sn by Coulomb excitation of neutron-rich $^{130,134}\text{Sn}$ isotopes

P. Reiter, Th. Kröll, M. Droste, K. Arnsward, A. Blazhev, H. Hess, H. Kleis, N. Warr, C. Henrich, A.-L.Hartig, H.-B. Rhee, M. Rudigier, C. Sürder, I. Homm, N. Pietralla, M. Scheck, R. Gernhäuser, H. De Witte, M. Huyse, P. Van Duppen, P. Thioolf, L. P. Gaffney, A. Jungclaus, K. Wimmer, G. Georgiev, J. Cederkäll, G. Rainovski, D. Kocheva, K. Gladnishki, D. Bucurescu, N. Marginean, R. Marginean, D. Deleanu, A. Negret, D. Balabanski, K. Hadynska-Klek, K. Wrzosek-Lipska, P. J. Napiorkowski, M. Komorowska, D. Mücher, V. Bildstein, R. Chapman, T. Grahn, P. T. Greenlees, A. Illana, J. Pakarinen, P. Rahkila, R. Lozeva, A. Andreyev, L. M. Fraile, J. M. Allmond, A. Stuchbery and the MINIBALL and HIEISOLDE collaborations

Univ. of Cologne, Germany; TU Darmstadt, Germany; Univ. West of Scotland, Paisley, UK; TU München, Germany; KU Leuven, Belgium; LMU München, Germany; Univ. of Liverpool, UK; IEM CSIC, Madrid, Spain; Univ. of Tokyo, Japan; IJCLab, Orsay, France; Univ. of Lund, Sweden; Univ. of Sofia, Bulgaria; IFIN-HH, Bucharest, Romania; ELI-NP, Magurele, Romania; Heavy Ion Laboratory, Univ. of Warsaw, Poland; Univ. of Guelph, Canada; Univ. of Jyväskylä, Finland; Helsinki Institute of Physics, Finland; Univ. of York, UK; UC Madrid, Spain; Oak Ridge National Laboratory, USA; Australian National University, Canberra, Australia;

Spokespersons: P. Reiter [preiter@ikp.uni-koeln.de], Th. Kröll [tkroell@ikp.tu-darmstadt.de]
Contact person: B. Olaizola [Bruno.Olaizola@cern.ch]

Calculated and measured B(E2) values along Sn isotopic chain



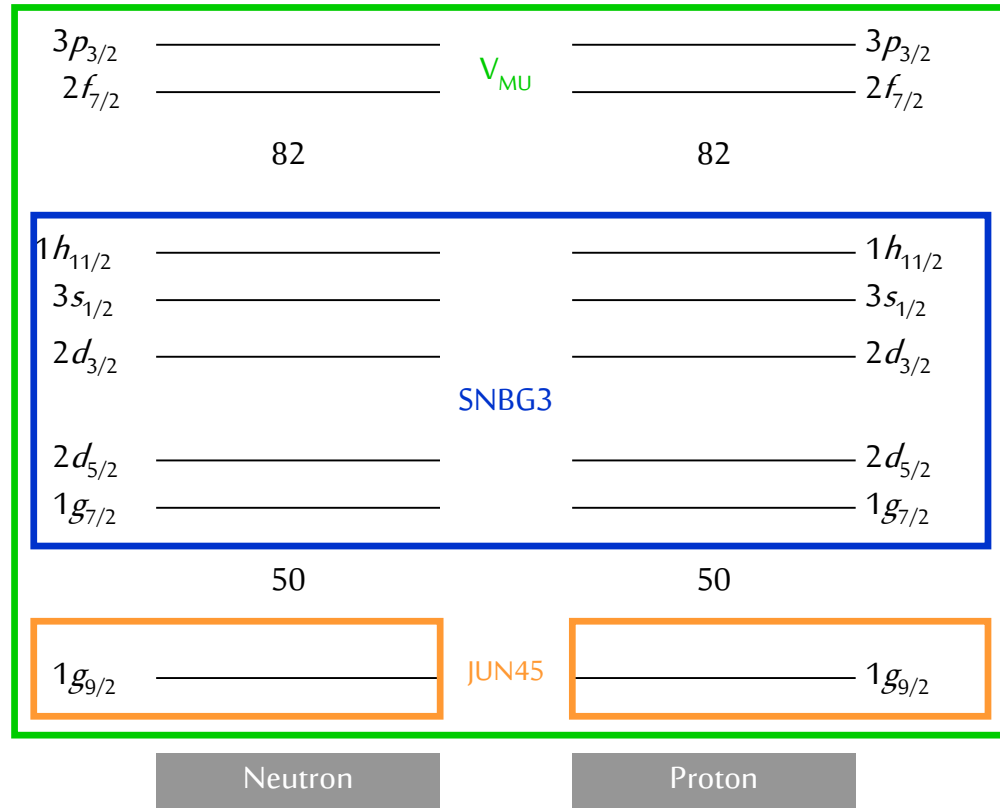
T. Togashi; Y. Tsunoda; T. Otsuka; N. Shimizu; M. Honma; Phys. Rev. Lett. 121, 062501 (2018)
 ^{132}Sn value by D. Rosiak et. al.; Phys. Rev. Lett. 121, 252501 (2018)

New shell-model calculations

Closed proton/neutron shells

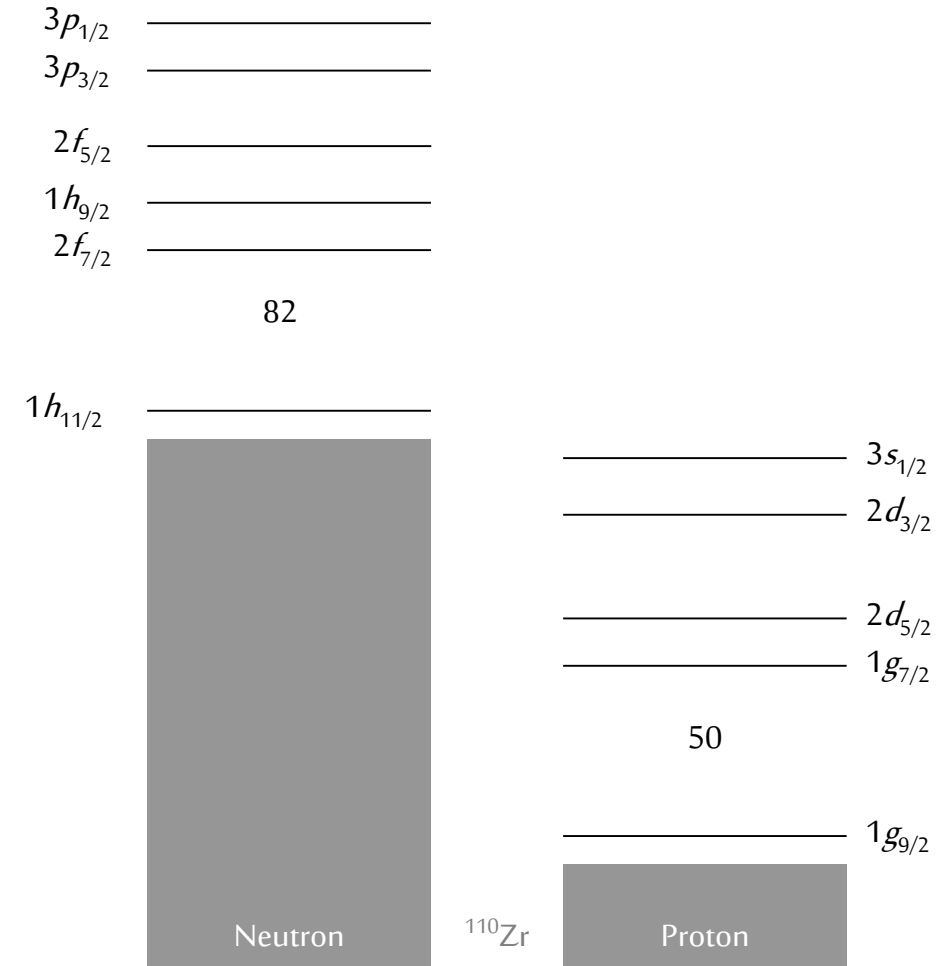
⇒ huge model space needed

Monte-Carlo shell model (MCSM)



T. Togashi, Y. Tsunoda, and T. Otsuka

Large-scale shell model (LSSM)



H. Naïdja and F. Nowacki

MCSM: T-plots – $^{130,132,134}\text{Sn}$

MCSM basis vectors and PES

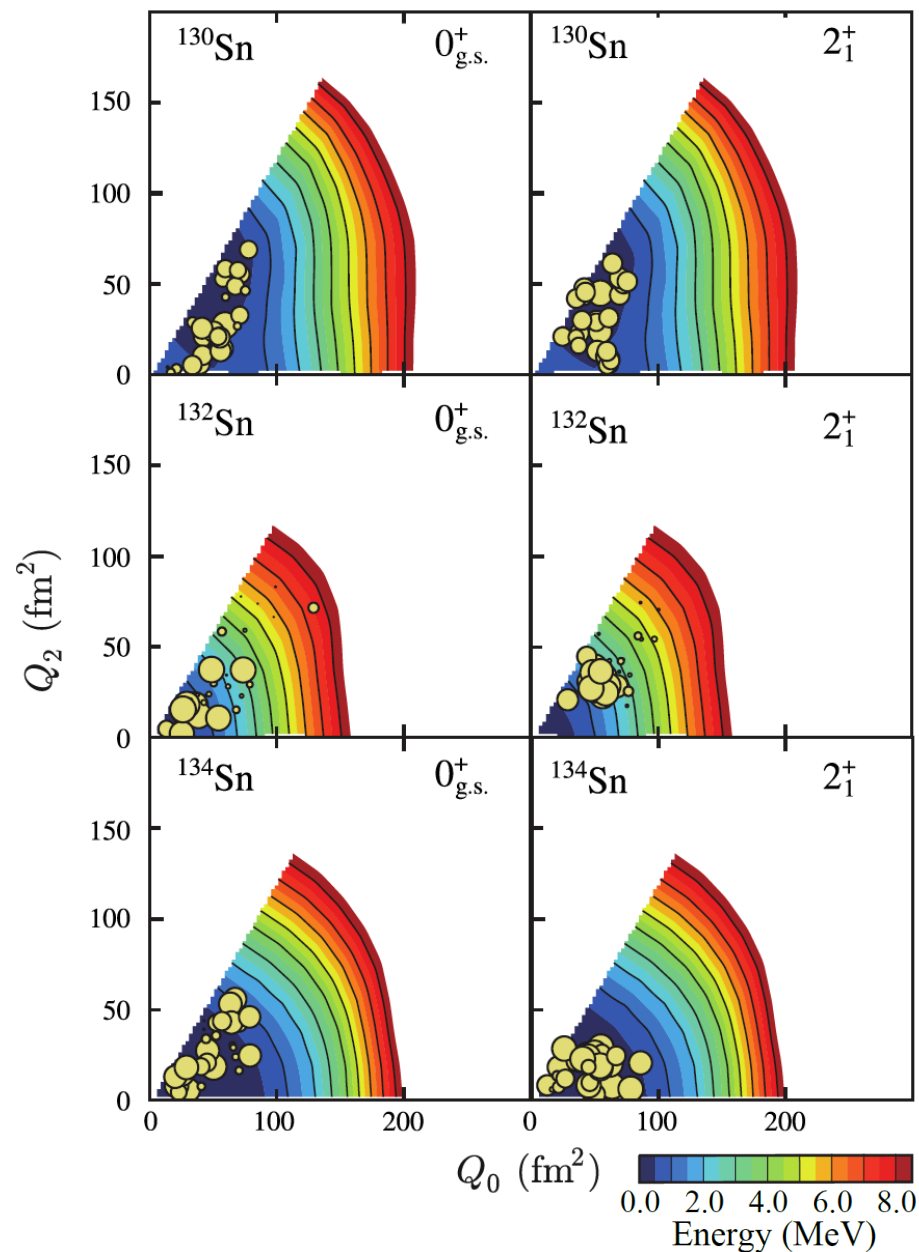
0^+ ground state:

- spherical minimum for $^{130,132,134}\text{Sn}$

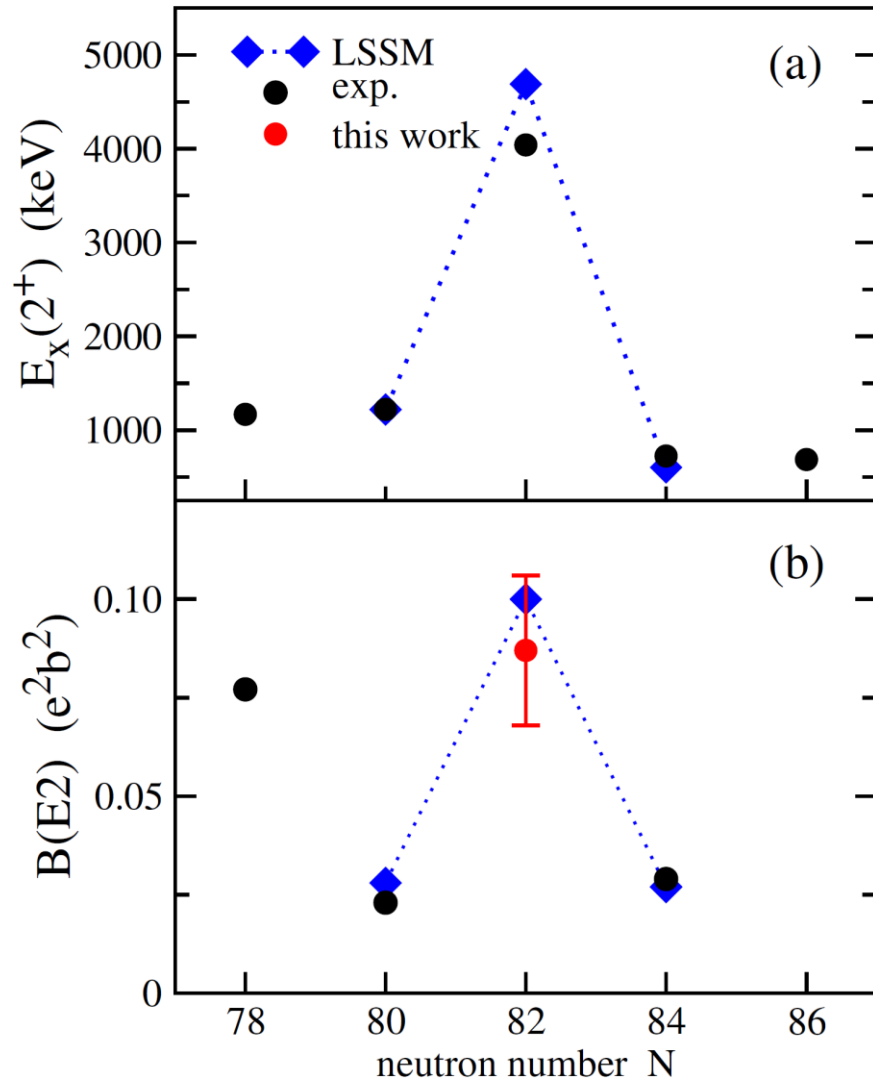
- Probability for spherical, doubly magic configuration of ^{132}Sn : 90%
(cf. $^{56,68,78}\text{Ni}$: 60%, 53%, 75%)

2^+ state:

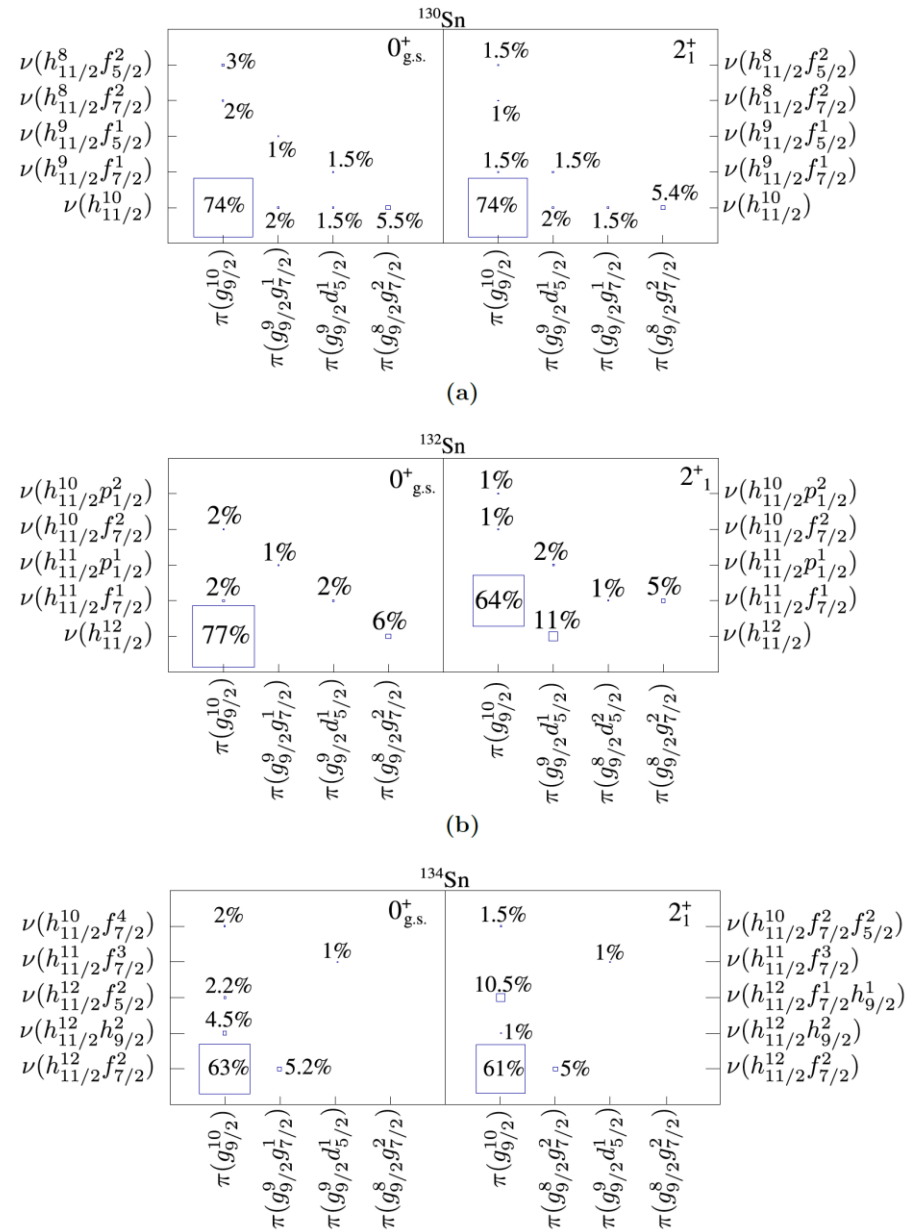
- Notable shift towards oblate for ^{130}Sn
and towards prolate for ^{134}Sn



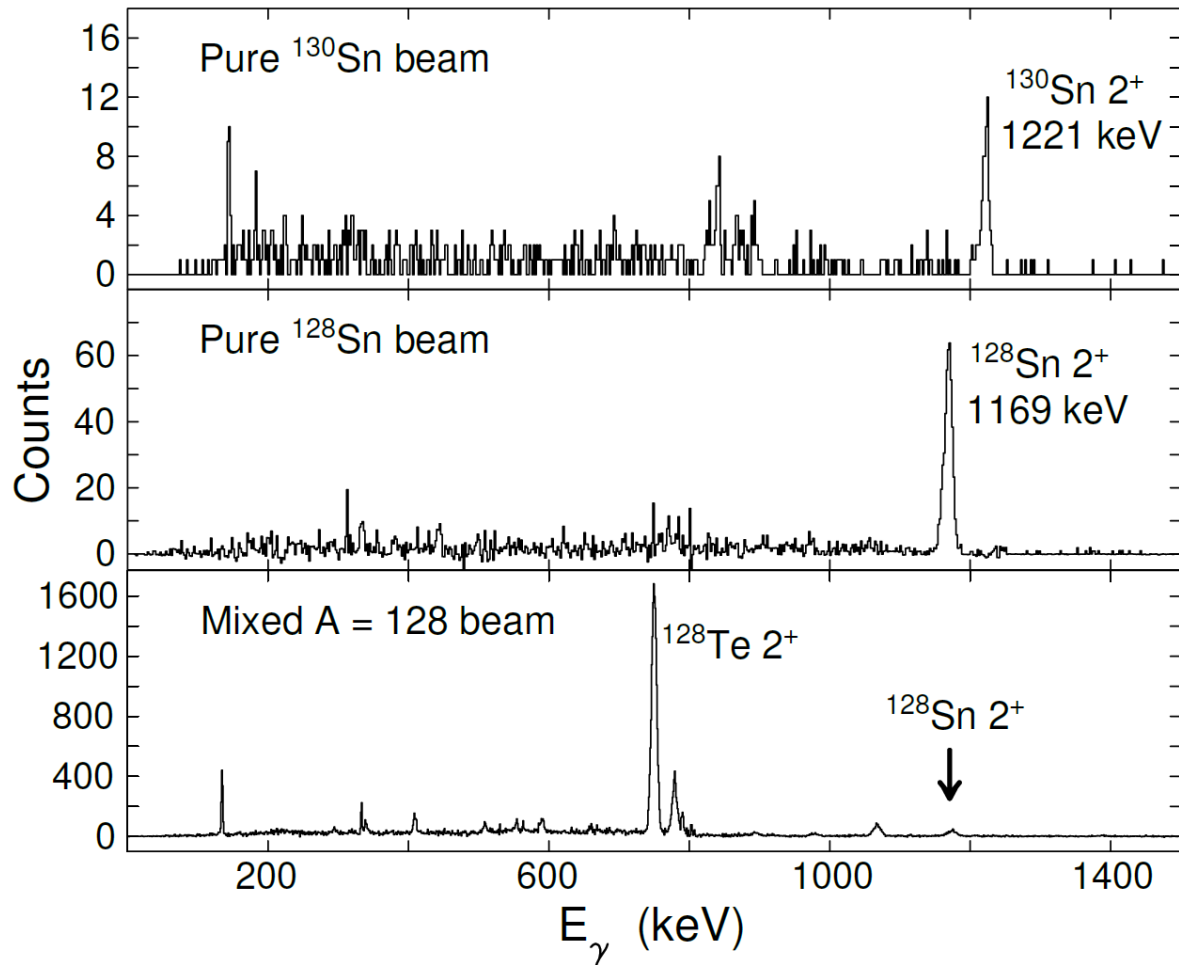
Large-scale shell-model calculations



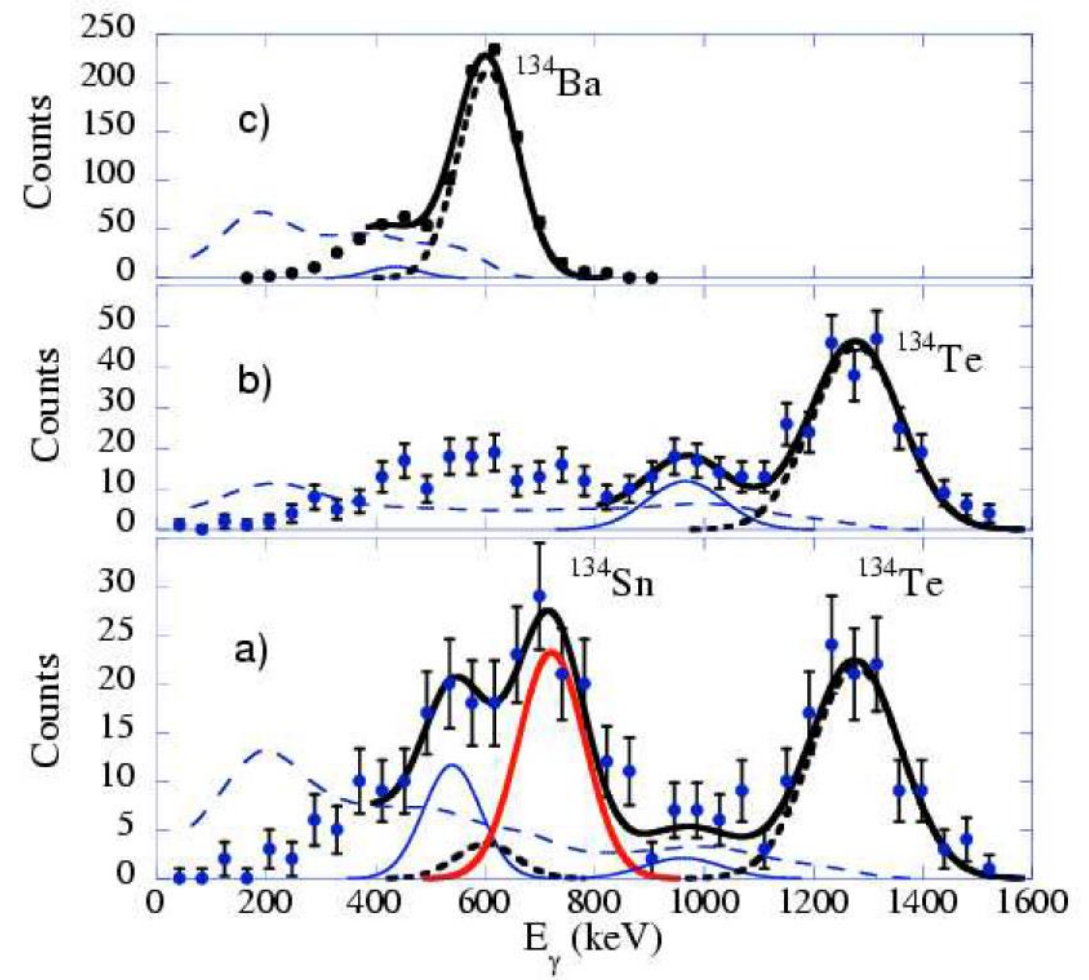
Proton excitation $g_{9/2}^{-1}d_{5/2}$ across shell gap crucial for $E2$ strength in ^{132}Sn



Coulomb excitation of $^{130,134}\text{Sn}$ at ORNL



γ -ray after Coulomb excitation of $^{128,130}\text{Sn}$ recorded by CLARION array. $2^+ \rightarrow 0^+$ transitions are labeled. Figure from Nuclear Physics A 752 (2005) 264c–272c



Coulomb excitation of ^{134}Sn . γ -ray spectrum from BaF_2 array TAMU. Contaminations: ^{134}Ba and ^{134}Te . Figure from Eur. Phys. J. A25, s01,391-394 (2005)

ISOLDE beam intensities

Element	A number	Half life	SC or PSB*	Yield at ISOLDE (ions/ μC)	Target material
Sn	123 - g	129.2 d	SC	5.0E+08	UC _x
Sn	125 - g	9.64 d	SC	1.3E+08	UC _x
Sn	127 - g	2.10 h	SC	6.0E+07	UC _x
Sn	129 - g	2.23 m	SC	5.0E+07	UC _x
Sn	131 - m	58.4 s	SC	1.5E+07	UC _x
Sn	132 - g	39.7 s	SC	3.0E+07	UC _x

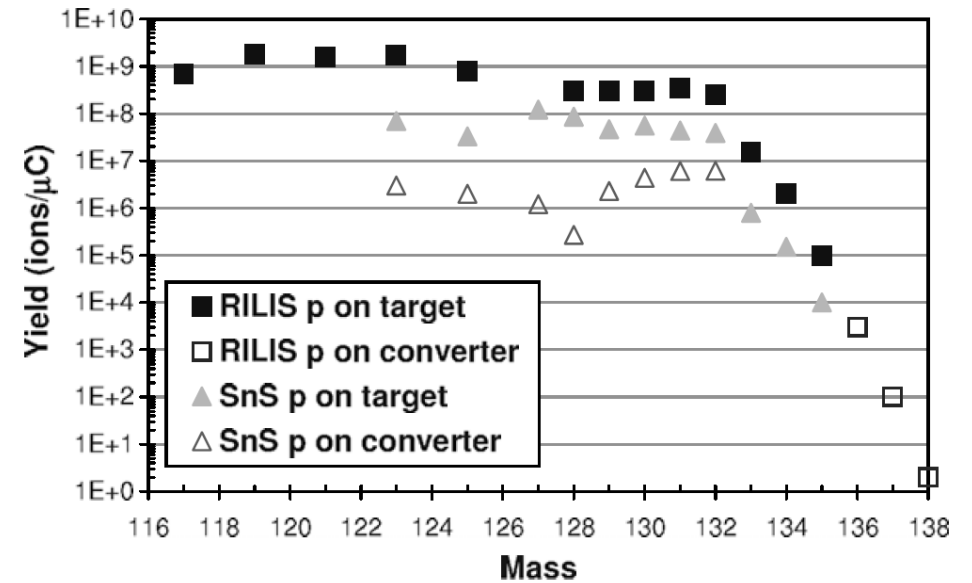
accelerator efficiency of HIE-ISOLDE for $^{130,134}\text{Sn}$ beams 5%
PSB proton beam current 2.0 μA

Beam intensities at MINIBALL:

- $I(^{130}\text{Sn}) = 1 \times 10^6$ ions/s
- $I(^{134}\text{Sn}) = 1 \times 10^4$ ions/s

Previous experiment in 2016:

- beam intensity at MINIBALL $I(^{132}\text{Sn}) = 3 \times 10^5$ ions/s
- PSB proton beam current 1.4 μA



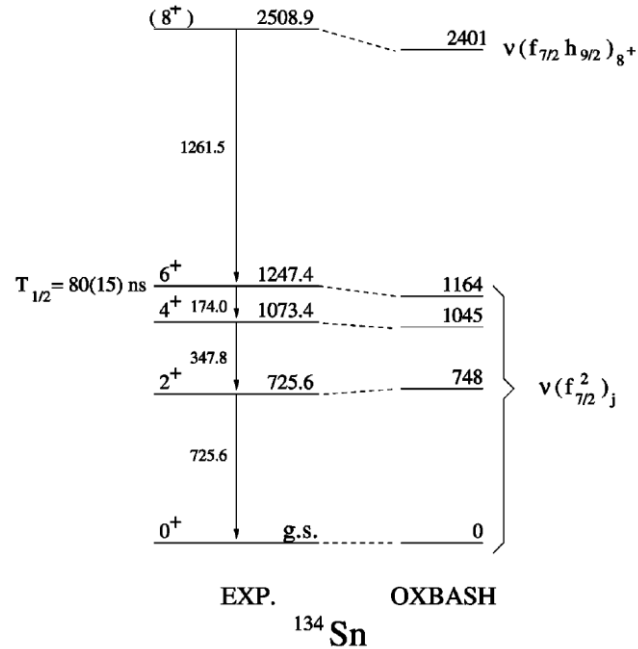
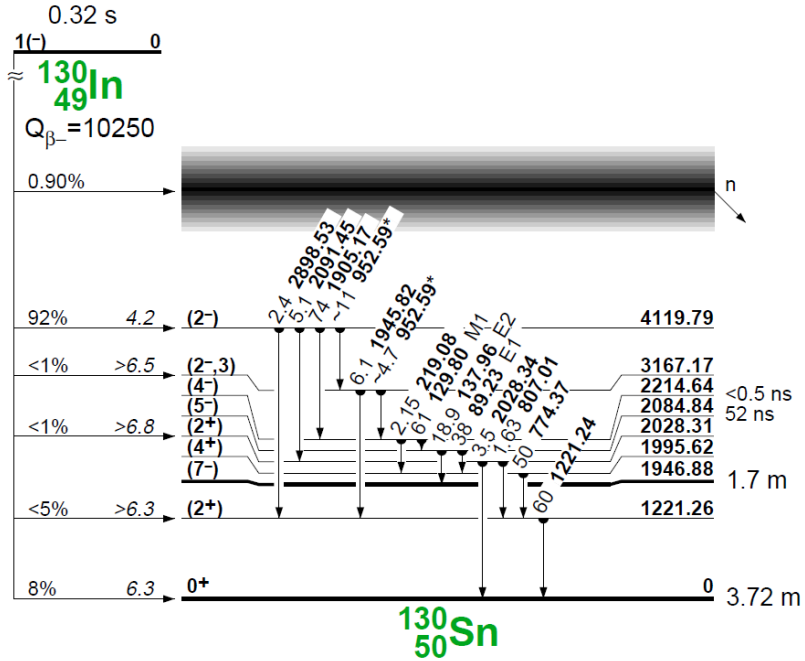
U. Köster et al. Nucl. Instr. and Meth. B 266 (2008) 4229

HIE-ISOLDE beam energy: 4.4 MeV/u

'safe' Coulex $^{130,134}\text{Sn}$ (@ 4.4 MeV/u) + ^{206}Pb

'safe' criterion $d > R_p + R_t + 5 \text{ fm} = 18.8 \text{ fm}$
fulfilled for target projectile distance at $\theta_{\text{Lab}} = 180^\circ$

Beam composition and isomers

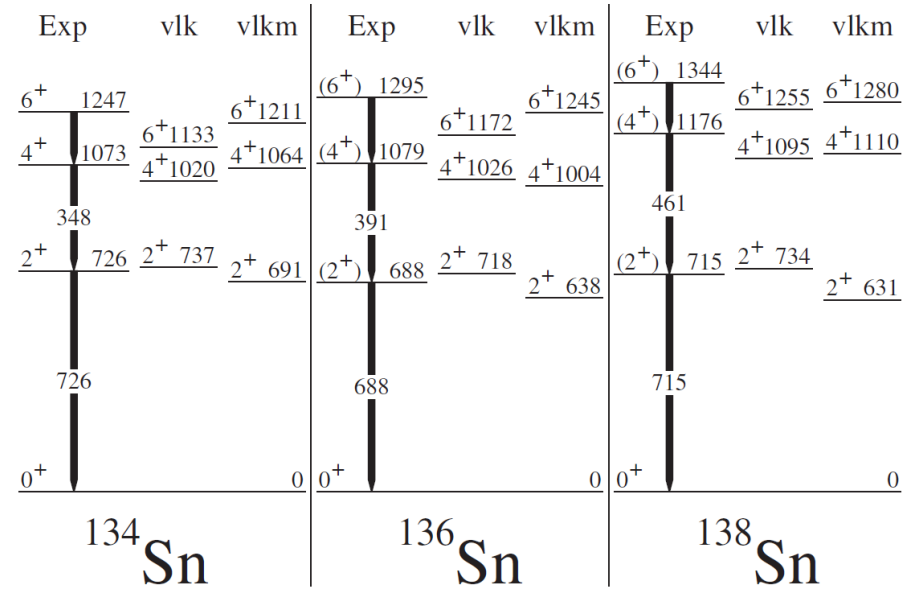


A. Korgul et al, EPJ A 7, 167 (2000)

G.S. Simpson, et al,

PRL 113, 132502 (2014)

PHYSICAL REV



Only short lived isomers in ^{134}Sn
 6^+ isomer (E=1247.4 keV, $T_{1/2} = 80$ ns)

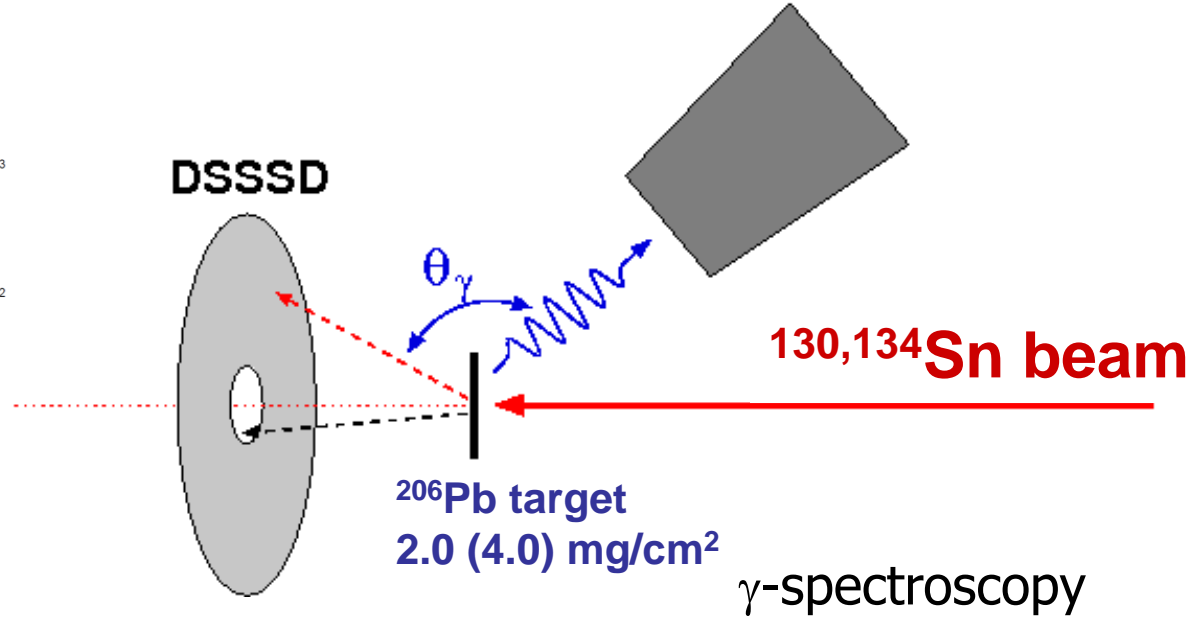
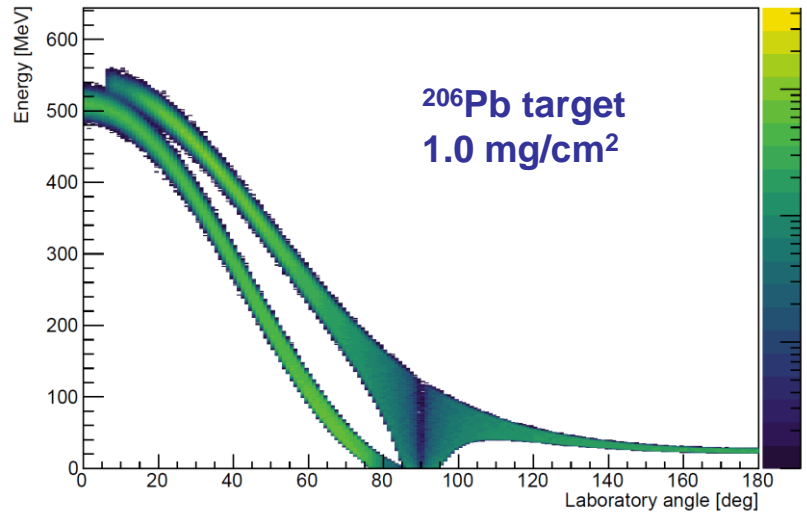
Fraction of ^{130}Sn beam is expected to be produced as 7^- isomer (E=1946.88 keV, $T_{1/2} = 1.7$ m)

Different β decay paths of ^{130}Sn 0^+_{gs} and 7^- isomer

- γ -spectroscopy of β decay products
- request of additional 3 shifts for decay spectroscopy, longest half life is 39.5 m of ^{130}Sb ground state decay

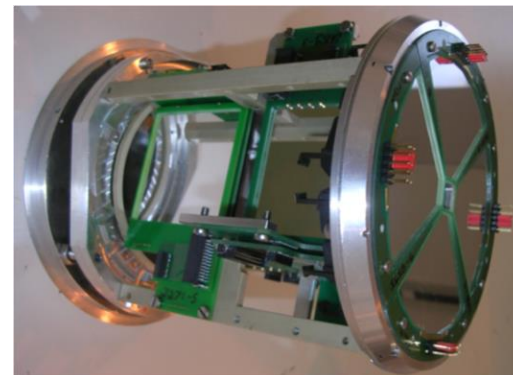
MINIBALL setup & particle kinematics

Kinematics in the lab frame for ^{130}Sn on ^{206}Pb at 4.4 MeV/u

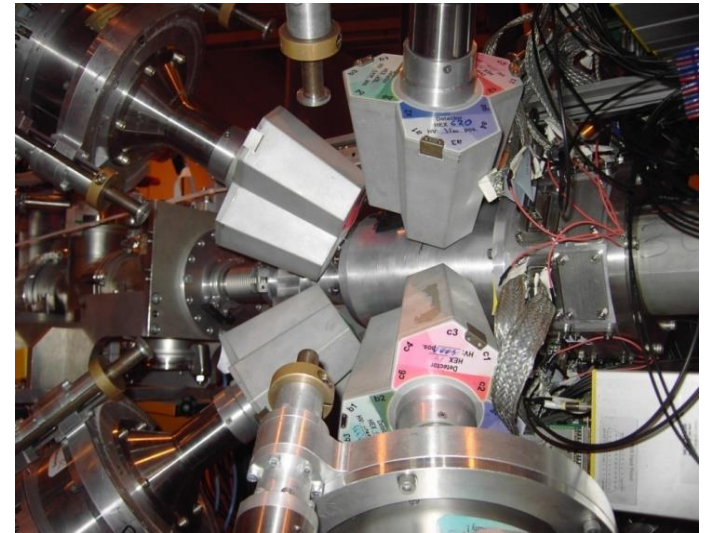


Particle detection

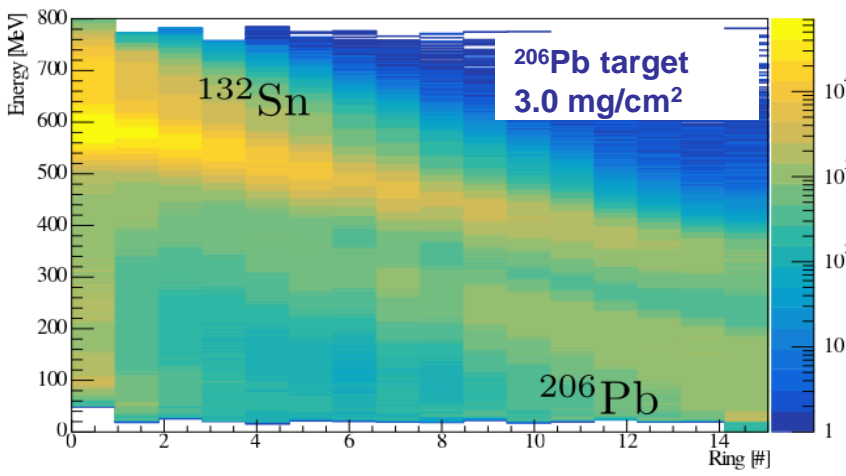
- scattering angle
- energy



TU München, K.U. Leuven



Uni Köln, K.U. Leuven



Cross sections & count rate estimate

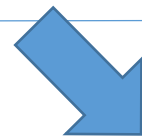
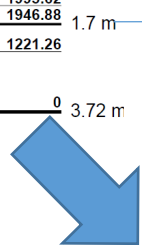
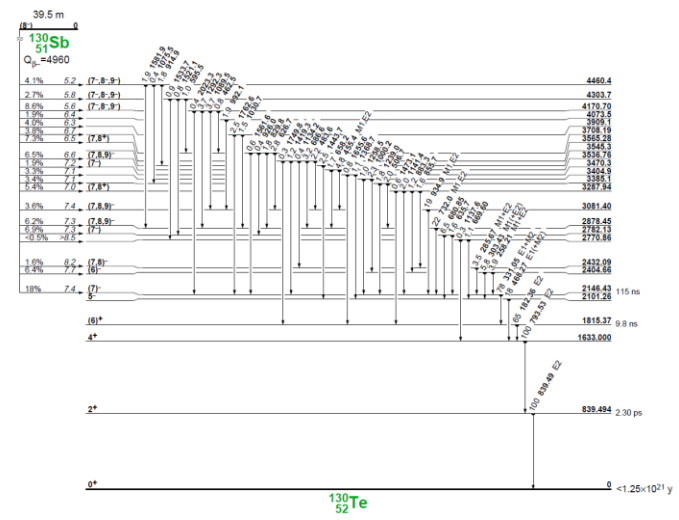
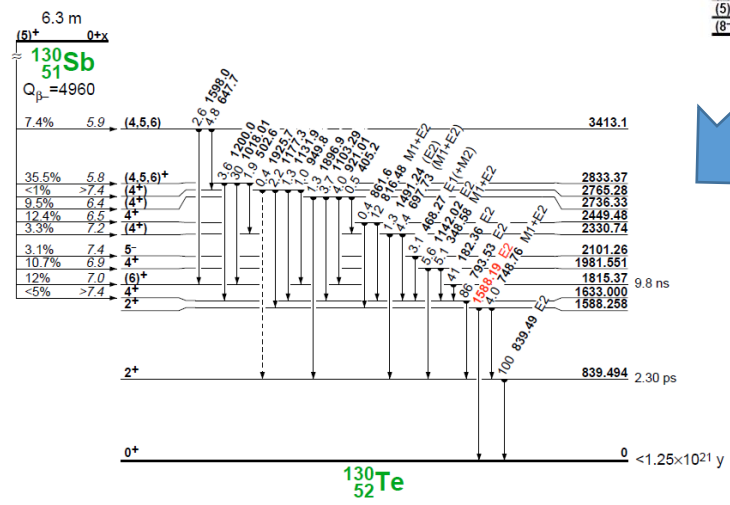
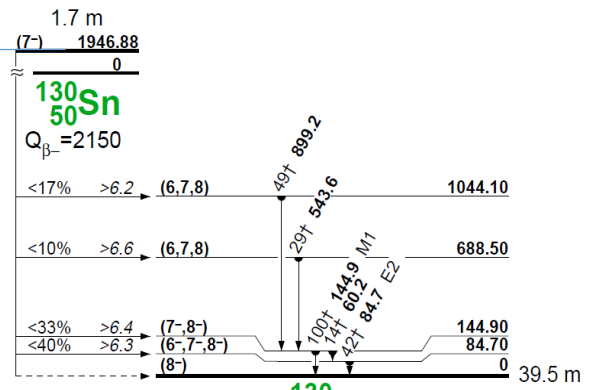
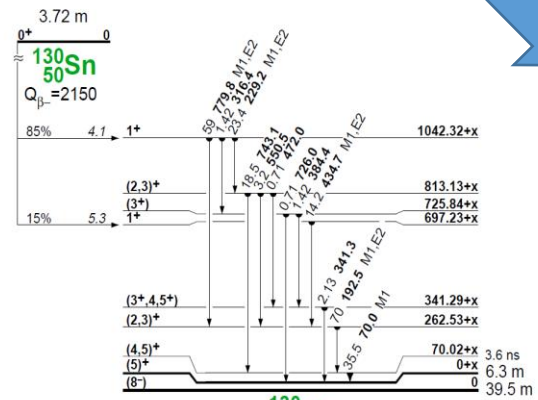
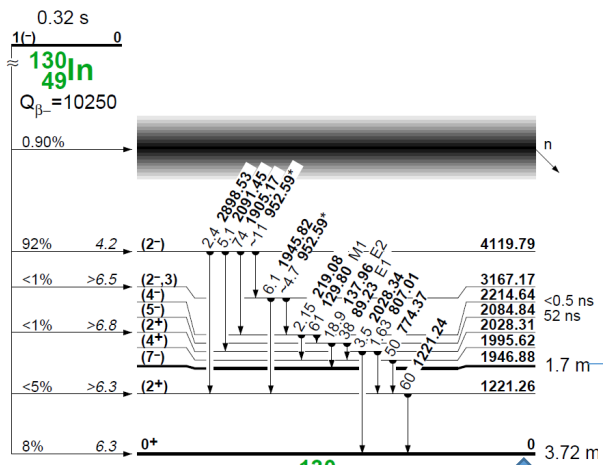
Transition, energy	Transition strength	Integr. CLX cross-section $15^\circ < \theta_{\text{Lab}} < 50^\circ$ DSSSD	Integr. CLX cross-section $105^\circ < \theta_{\text{Lab}} < 172^\circ$ C-REX	cts/h	cts/ run	statistical error		isotope
$0_1^+ \rightarrow 2_1^+$ 1221.2 keV ^{130}Sn	$B(E2, 0_1^+ \rightarrow 2_1^+)$ $0.023 e^2b^2$ <i>Nucl. Phys. A</i> <i>752 (2005) 264c</i>	$\sigma(2_1^+)$ 130 mb	$\sigma(2_1^+)$ 90 mb	370	35000 <i>12 shifts</i>	<2%		^{130}Sn
$2_1^+ \rightarrow 4_1^+$ 774 keV ^{130}Sn	$B(E2, 2_1^+ \rightarrow 4_1^+)$ $0.024 e^2b^2$	$\sigma(4_1^+)$ 0.19 mb	$\sigma(4_1^+)$ 0.46 mb	2	200 <i>12 shifts</i>	~7%		^{130}Sn
$0_1^+ \rightarrow 2_1^+$ 725.6 keV ^{134}Sn	$B(E2, 0_1^+ \rightarrow 2_1^+)$ $0.029 e^2b^2$ <i>Eur. Phys. J. A</i> <i>25, s01, 391 (2005)</i>	$\sigma(2_1^+)$ 400 mb	$\sigma(2_1^+)$ 320 mb	15	3530 <i>15 shifts</i>	<2%		^{134}Sn
$2_1^+ \rightarrow 4_1^+$ 347.8 keV ^{134}Sn	$B(E2, 2_1^+ \rightarrow 4_1^+)$ $0.031 e^2b^2$ <i>Phys. Rev. C</i> <i>76, 024313 (2007)</i>	$\sigma(4_1^+)$ 2.6 mb	$\sigma(4_1^+)$ 10 mb	0.3	73 <i>15 shifts</i>	~12%		^{134}Sn

Summary and beam time request

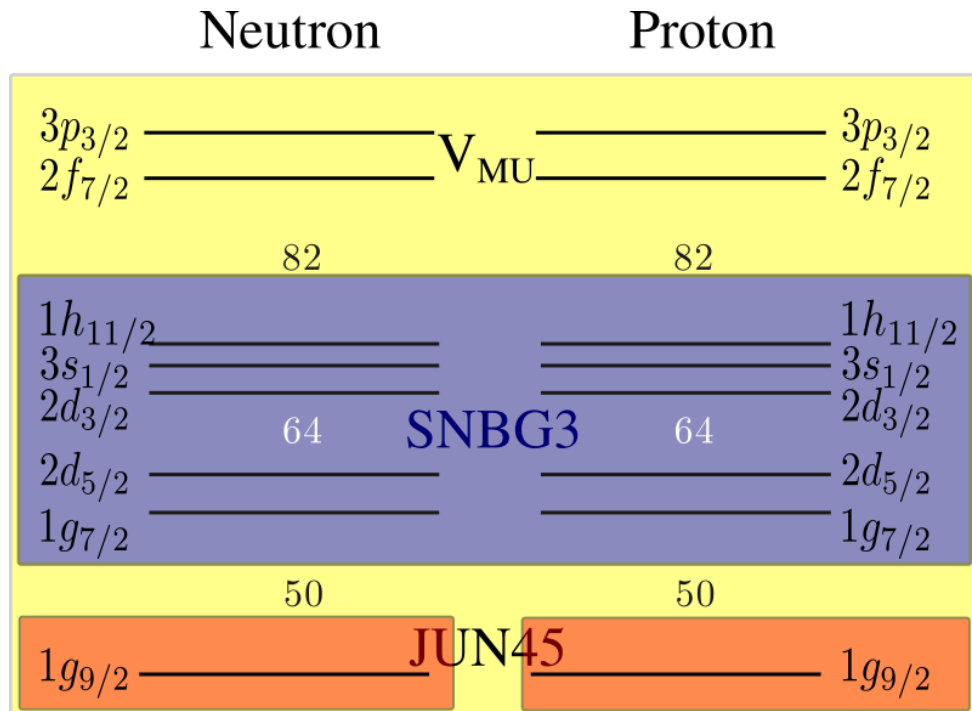
- Measurements of the $B(E2, 2_1^+ \rightarrow 0^+)$ - and $B(E2, 4_1^+ \rightarrow 2_1^+)$ values for the neutron-rich isotopes $^{130,134}\text{Sn}$ are proposed.
- $B(E2, 2_1^+ \rightarrow 0^+)$ values will be improved significantly and will allow for crucial test of MCSM- and large scale SM calculations.
- $B(E2, 4_1^+ \rightarrow 2_1^+)$ values will be accessible in this region for the first time.
- Electric quadrupole moments Q_2 will be extracted from data. For short-lived states, this quantity is only accessible by safe Coulomb excitation via the reorientation effect.
- Beam time request:
 - 12 shifts in beam spectroscopy + 3 shifts decay spectroscopy for ^{130}Sn
 - 15 shifts for ^{134}Sn

Backup slides

^{130}Sn beam composition



Monte-Carlo Shell Model



→ V_{MU} No $T=0$ interaction adjustments;
 $T=1$ reduced by a factor of 0.75

Dimension and calculation:

→ realistic interactions JUN45 (CD-Bonn),
 SNBG3 (N3LO) and V_{MU} (central Gaussian part +
 meson exchange)

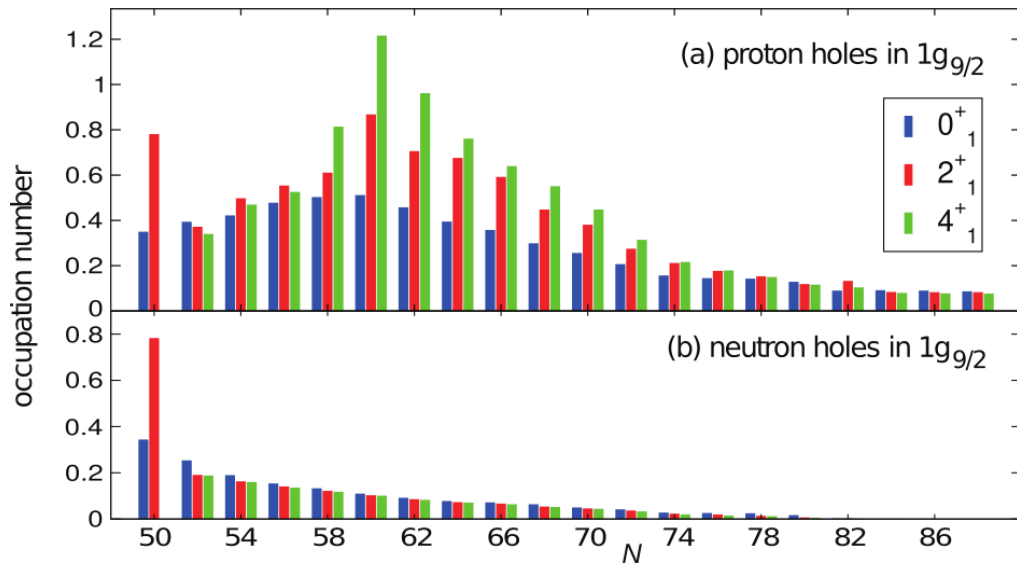
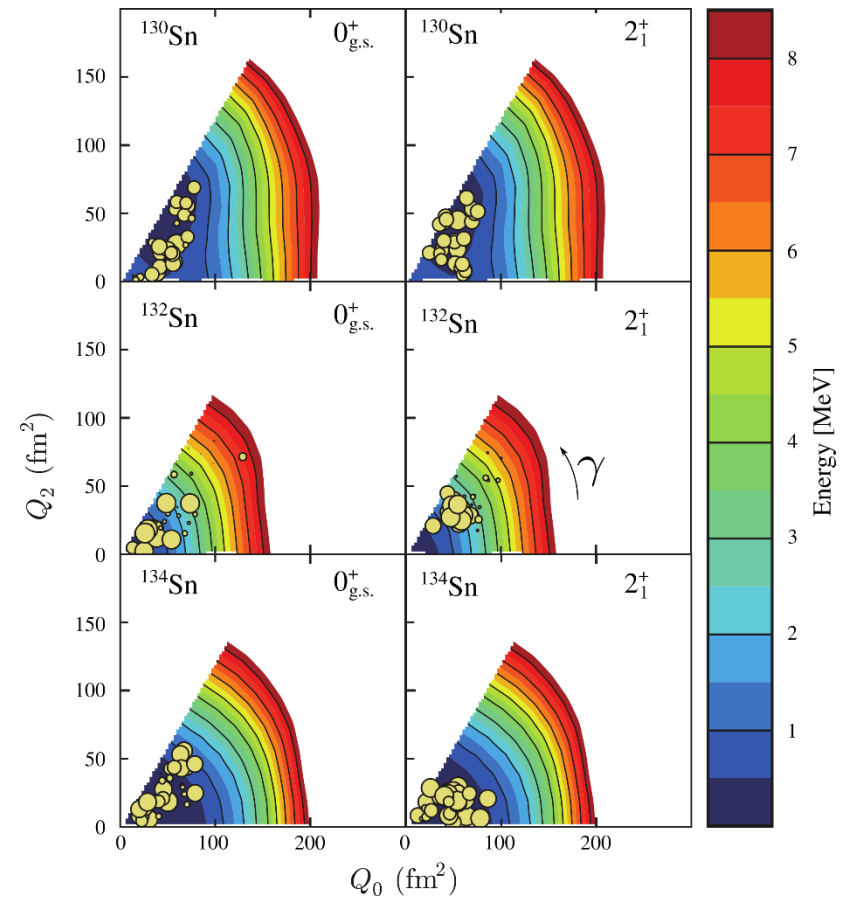
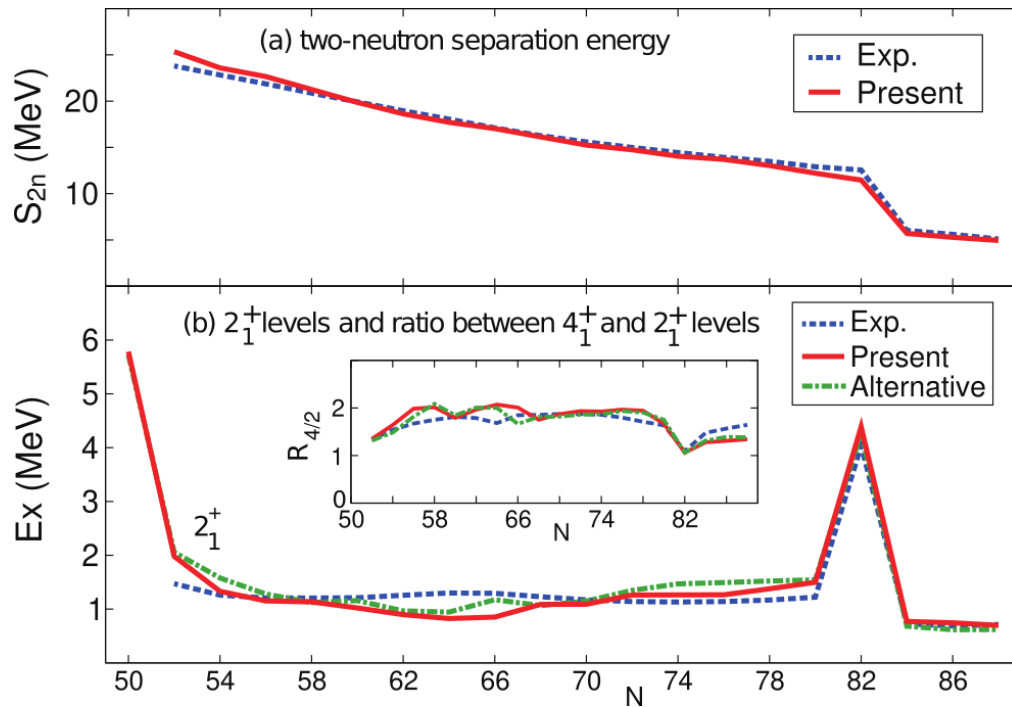
→ Fine tuning to reproduce 2^+_{11} and 4^+_{11} levels of
 $^{102-138}\text{Sn}$ (TBME scaled to $A^{-1/3}$)

→ Model space dimension 7.5×10^{23}
 (current calculation limit 10^{12})

→ MCSM with no truncations

→ single Hamiltonian with active p and n
 representation by TBME of effective
 N-N interaction (coupled to J and T)

→ $\pi g_{9/2}$ prolate shape + $\nu h_{11/2}$ oblate shape +
 enhanced shell gap → magic



→ Occupation numbers $^{132}\text{Sn } 2_1^+$

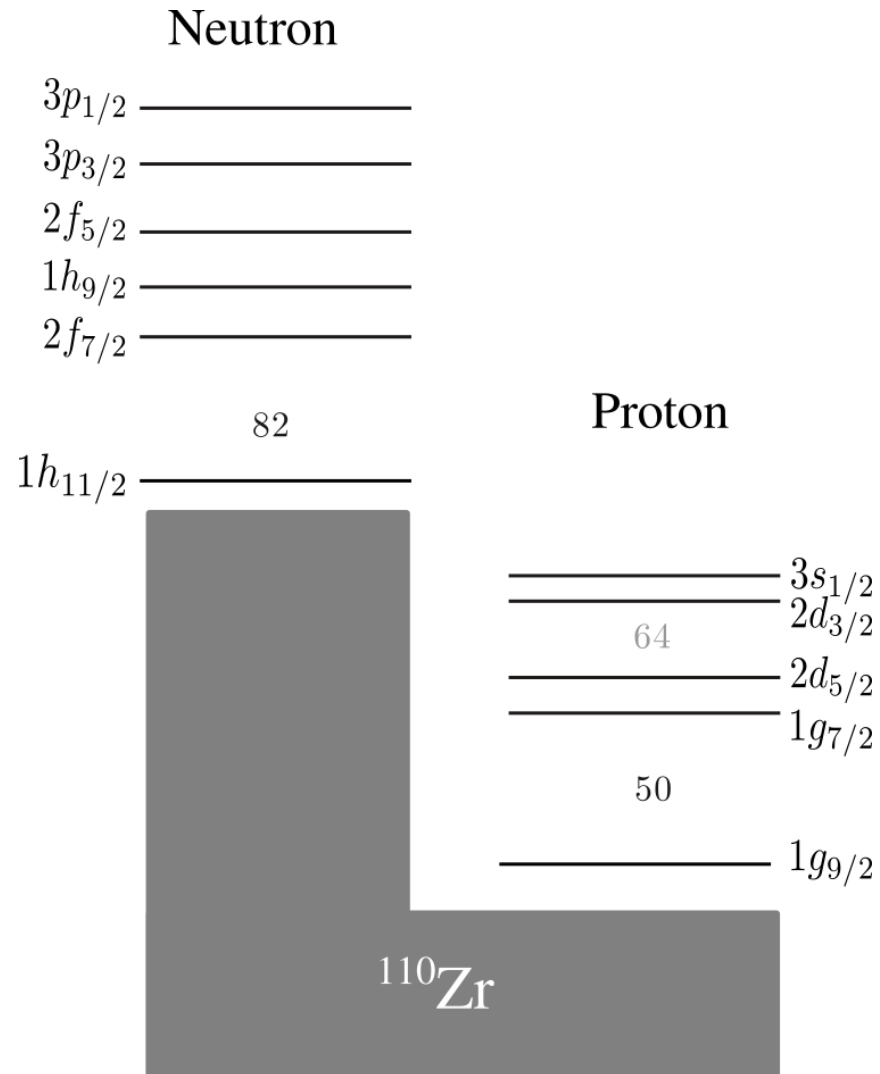
$\pi g_{9/2} \rightarrow 0.09$

$\nu h_{11/2} \rightarrow 0.13$

→ Proton contributes with $\frac{1}{4}$ to total E2 strength

→ Protons in $g_{9/2}$ prolate – Neutrons in $h_{11/2}$ oblate shape + enhanced shell gap → MAGIC

Large-scale shell-model calculation with ^{110}Zr



Dimension and conditions:

- realistic interactions NNS100 derived from CD-Bonn
- renormalized by $V_{\text{low-k}}$ (G-Matrix) to exclude repulsive short range (cutoff = 2.2 fm^{-1})
- many-body perturbation up to second order
 - monopole adjustments to get SPE of $^{133}\text{Sn} + ^{133}\text{Sb}$
 - p-p and n-p monopole matrix elements to get SPE for N=82 and N=83 isotones
- fixed neutron gap of ^{132}Sn and proton gap of ^{120}Sn
- Dimension 2×10^{19}
- truncation scheme by limiting 7p7h excitation (ANTOINE)

N. Houda^{1,2}, F. Nowacki¹

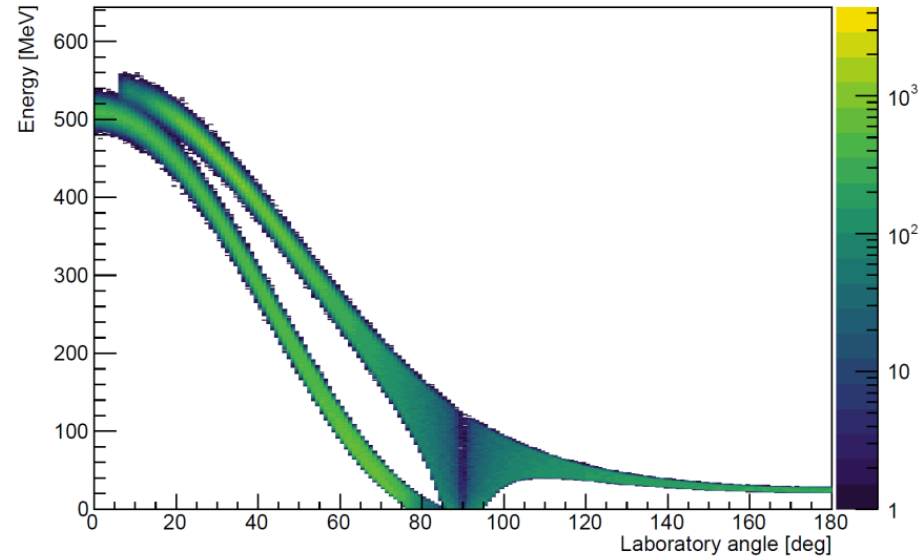
1) IPHC Strasbourg, France

2) LPMS, Université Constantine 1, Algeria.

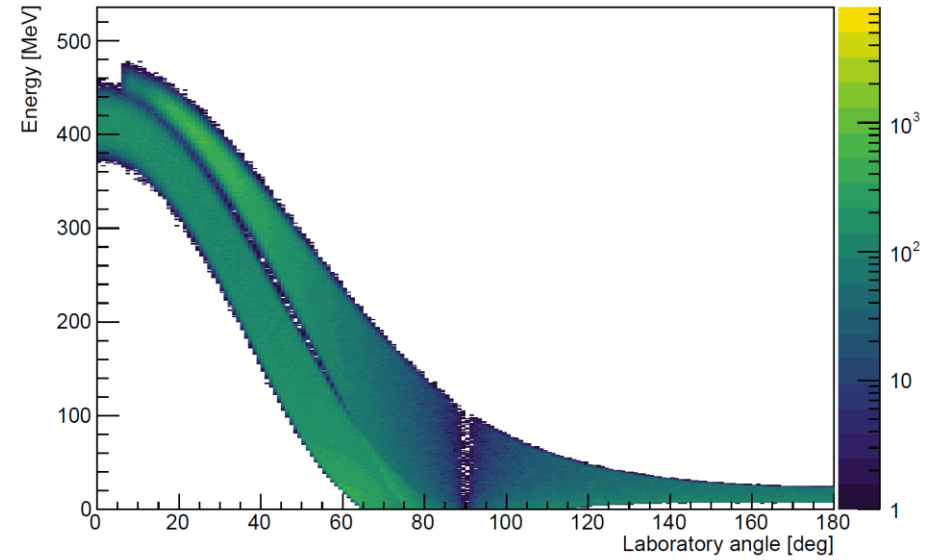
priv. comm. January 2018

Backup: Experimental considerations

Kinematics in the lab frame for ^{130}Sn on ^{206}Pb at 4.4 MeV/u



Kinematics in the lab frame for ^{130}Sn on ^{206}Pb at 4.4 MeV/u



Kinematics in the lab frame for ^{130}Sn on ^{206}Pb at 4.4 MeV/u

