

Single-particle structure, effective proton charge, and emerging collectivity around ^{132}Sn

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E2 Strength (Coulex) of Odd-Z Nuclei Near ^{132}Sn : Effective charges and pn Interactions

Recently Published;
40% E2 enhancement

Beyond
particle-core

s.p. eff.
charges

Sb129 4.40 h 7/2+ * β^-	Sb130 39.5 m (8-) * β^-	Sb131 23.03 m (7/2+) * β^-	Sb132 2.79 m (4+) * β^-	Sb133 2.5 m (7/2+) * β^-	Sb134 0.85 s (0-) * β^-
Sn128 59.07 m 0+ * β^-	Sn129 2.23 m (3/2+) * β^-	Sn130 3.72 m 0+ * β^-	Sn131 56.0 s (3/2+) * β^-	Sn132 39.7 s 0+ * β^-	Sn133 1.44 s (7/2-) * β^-_n
In127 1.09 s (9/2+) * β^-_n	In128 0.84 s (3+) * β^-_n	In129 0.61 s (9/2+) * β^-_n	In130 0.32 s 1(-) * β^-_n	In131 0.282 s (9/2+) * β^-_n	In132 0.201 s (7-) * β^-_n

Proton +
neutron hole pairs

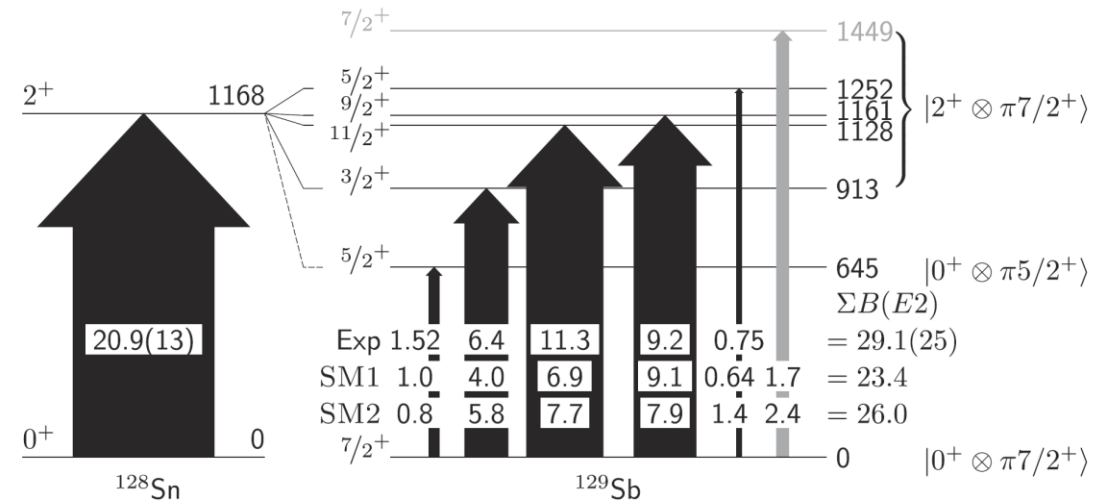
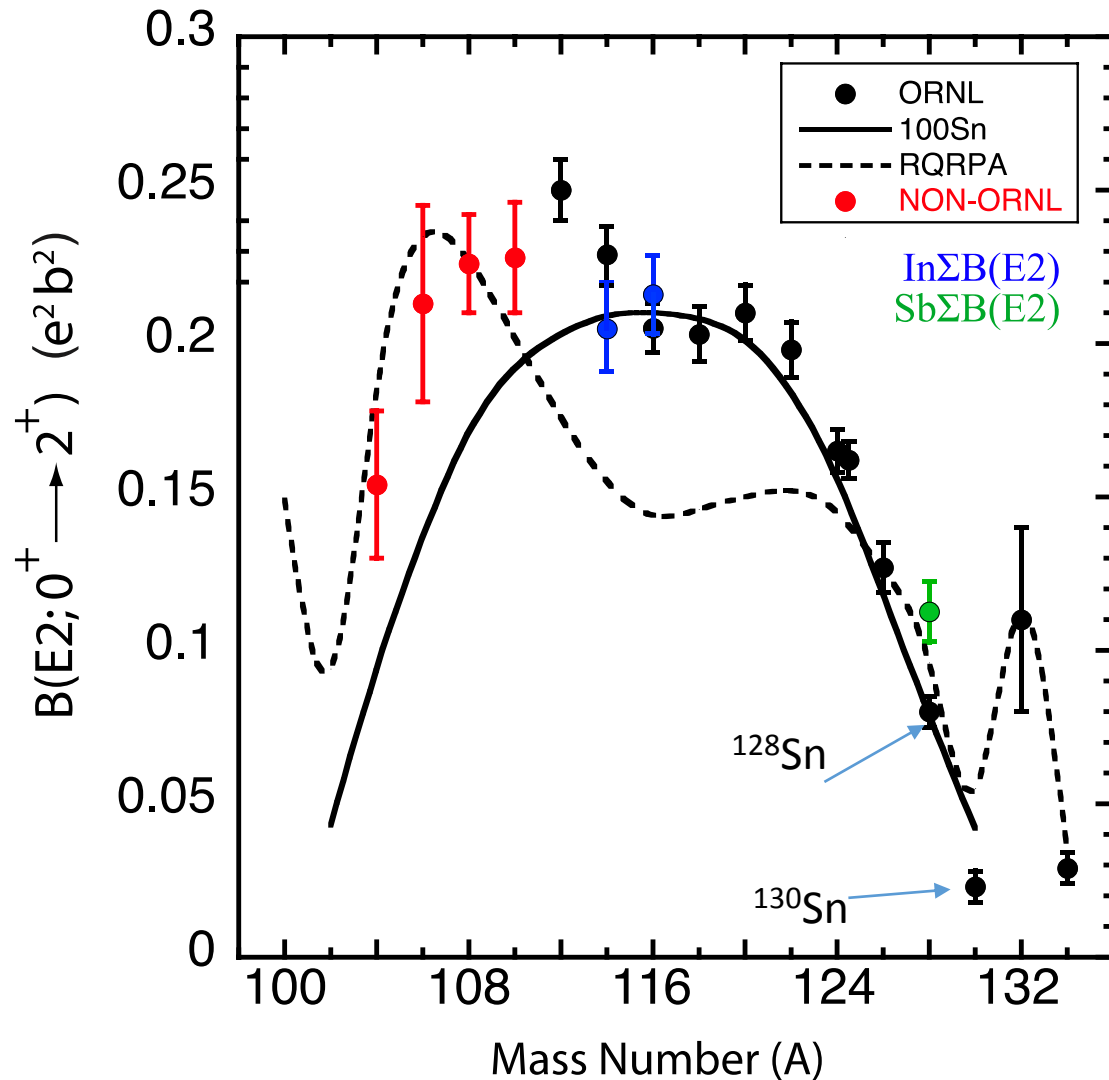
Proton hole +
neutron hole pairs

Beyond
particle-core

Sn B(E2) Systematics – moving to odd-proton neighbours

Total electric quadrupole strength of ^{129}Sb is enhanced compared to the Sn systematics

^{129}Sb PRL 124, 032502 (2020)



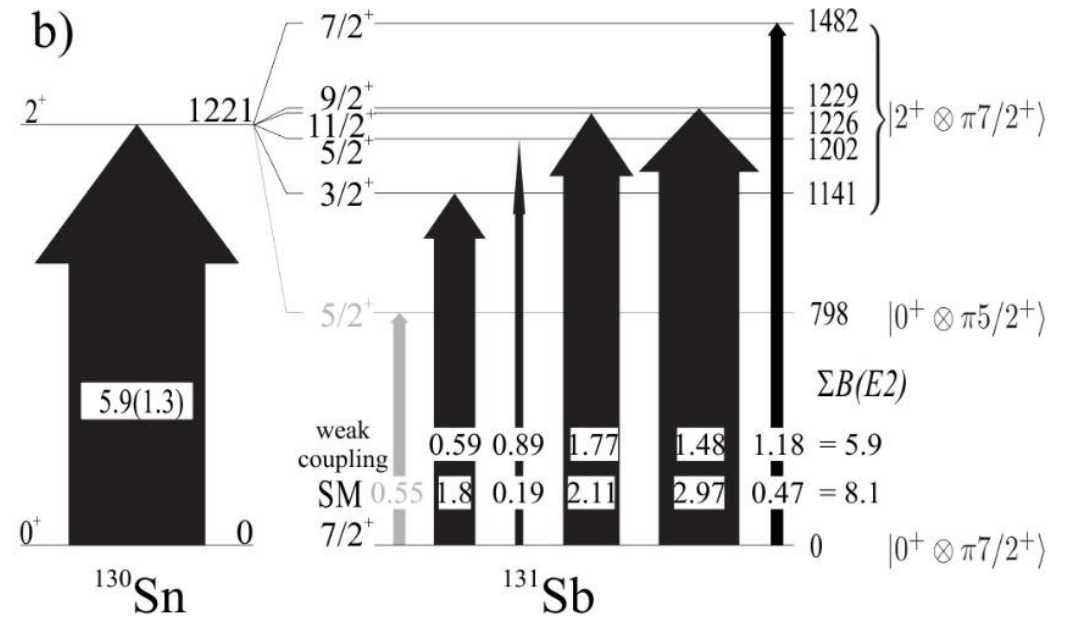
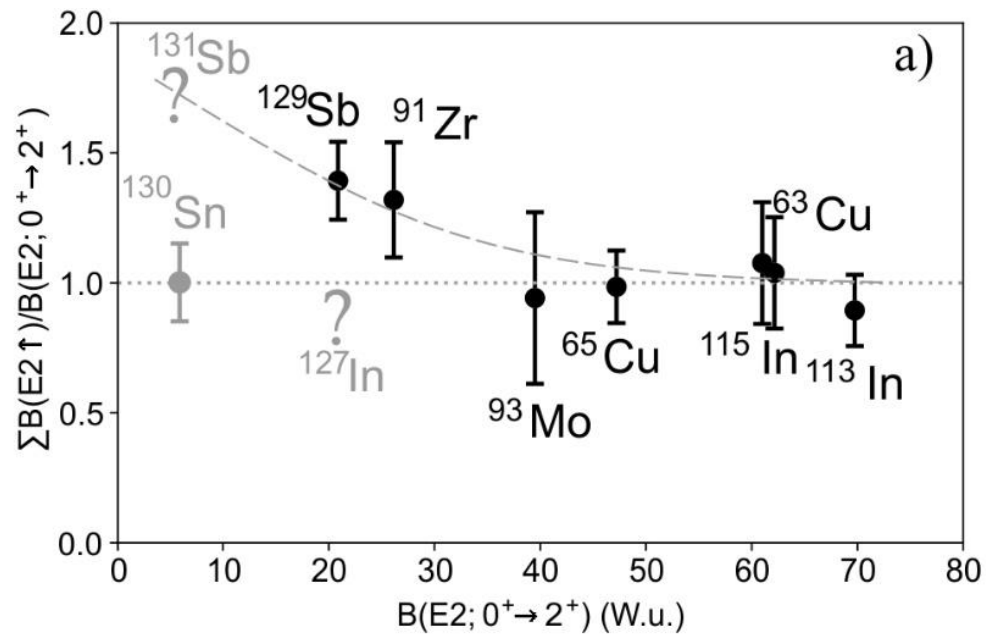
$$B(E2; 0^+ \rightarrow 2^+)_{core} = \sum_i B(E2; I_{gs} \rightarrow I_i)_i$$

E2 sum as a tool & a measure of developing collectivity:

- Empirical comparison of E2 strengths
- *Detailed shell-model comparisons*

Core vs Particle-Core (fragmented) E2 Strength

- E2 Sum is invariant in particle-core model for all coupling strengths
- Breakdown of particle-core observed for $B(E2) < 40$ W.u. [Gray et al., PRL (2021)]
- Shell-model calculations predict different breakdowns for particles and holes; **breakdown not understood, limited data**

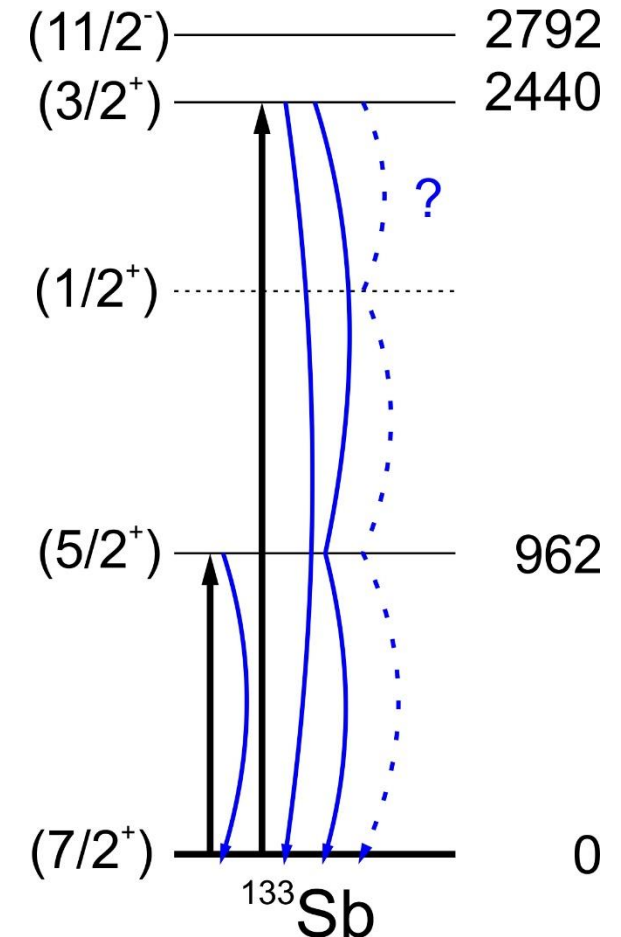


Breakdown pattern may not be monotonic

^{133}Sb : Effective charges next to ^{132}Sn

s.p. eff. charges

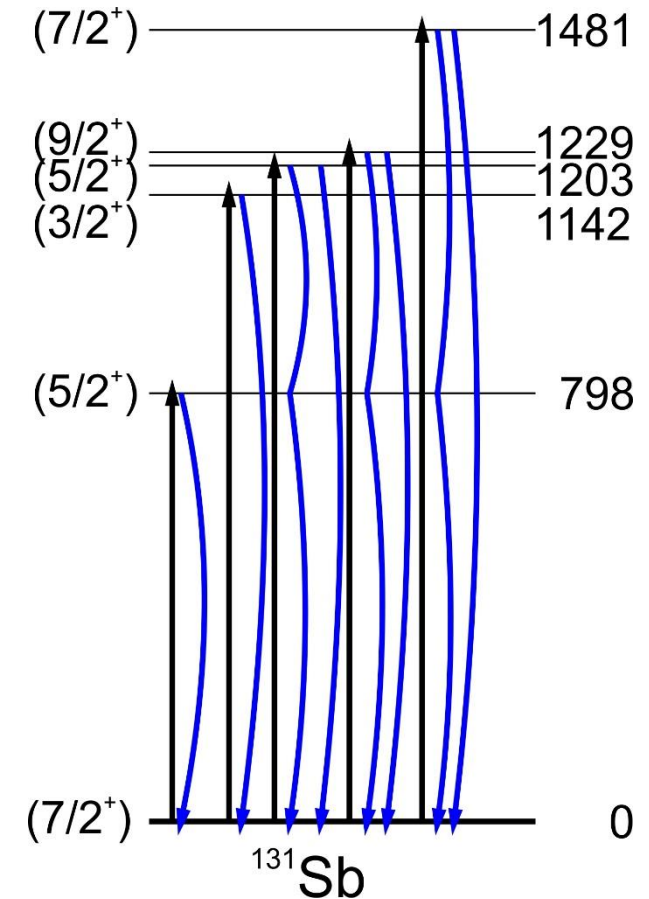
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^{131}Sb : particle-core structure, pn interactions, developing collectivity

Beyond
particle-core

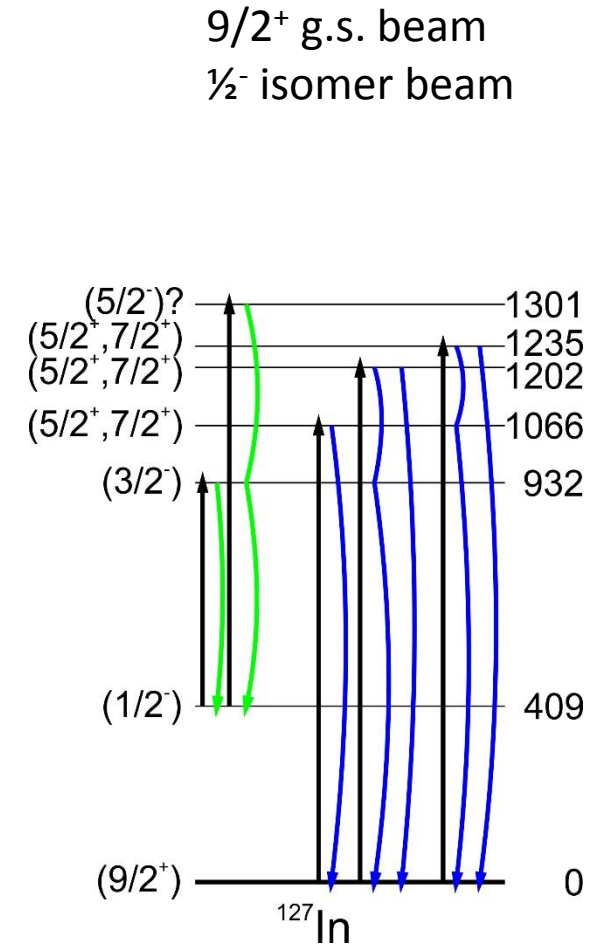
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^{127}In : particle-core structure, $p^{-1}n$ interactions, developing collectivity

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Sn128 59.07 m 0+ β^- *	Sn129 2.23 m (3/2+) β^- *	Sn130 3.72 m 0+ β^- *	Sn131 56.0 s (3/2+) β^- *	Sn132 39.7 s 0+ β^- *	Sn133 1.44 s (7/2-) β^-_n
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Beyond
particle-core



What we aim for and what the experiment will provide?

^{133}Sb

- transition probabilities; purity of single-particle states; proton effective charge; single particle energies around ^{132}Sn

^{131}Sb

- probe the sum rule at ^{130}Sn - very sensitive test case; stringent test of shell model calculations; emergence of collectivity around shell closures; *distinguish between core modification and proton-neutron correlations*

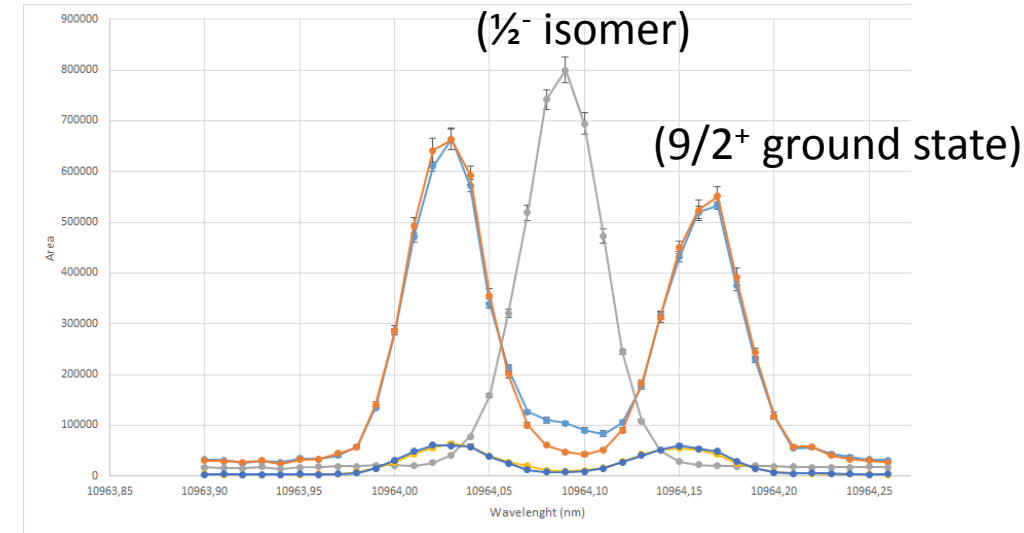
^{127}In (**$1/2^-$ isomer and $9/2^+$ g.s. beams accelerated**)

- measure $B(E2)$ strengths
- excitation on $1/2^-$ isomer should give $B(E2)$ s and angular correlations
- spins and configuration assignment of the 'known' candidate multiplet states and search for other strongly Coulomb-excited states, which might be missing multiplet members
- identify other low-lying states (possibly with both positive and negative parities, when structures on top of the two isomeric states are excited) to be compared to shell-model calculations and E2 sum rule.

RIB production from ISOLDE and experimental details

- Use of a neutron-converter for reducing the surface-ionized spallation products (Cs, Ba etc.)
- **Narrow-band RILIS for isomer selection in ^{127}In**

isotopes	yield [p/ μC]	surface contamination	rate @ Miniball [pps]
^{131}Sb	7.2×10^7	25%	3×10^6
^{133}Sb	4.7×10^7	50%	2×10^6
^{127}In	5.5×10^6	25%	2.5×10^5



Coulomb excitation measurement at Miniball (CD-only configuration)

- Beams – ^{133}Sb , ^{131}Sb ; ^{127g}In , ^{127m}In
- Energy – 4 MeV/u
- Targets – ^{196}Pt : 1 mg/cm² for ^{133}Sb and ^{131}Sb ; 2 mg/cm² for ^{127}In
- Standard Miniball Coulex configuration

beam energy and the **target** (composition and thickness) were **optimized** aiming at:

- **safe (single-step) Coulomb excitation** (within the angular coverage of the CD detector)
- **precise B(E2) values** - considering the influence of the *Q moment* on the B(E2)

Beam-time request

- **3 shifts** of beam on target with ^{131}Sb beam;
- **3 shifts** of beam on target with ^{133}Sb beam;
- **3 shifts** of beam on target with ^{127}In ($9/2^+$) using a narrow-band RILIS ionization;
- **3 shifts** of beam on target with ^{127}In ($1/2^-$) using a narrow-band RILIS ionization.
- **2 shifts** for changes between isotopes/isomers

A total of **14 shifts requested**.

(Technical Advisory Committee has OK'ed proposal: "The yields in the proposal are properly discussed and have been recently measured. " etc.)

What we aim for and what the experiment will provide?

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^{131}Sb

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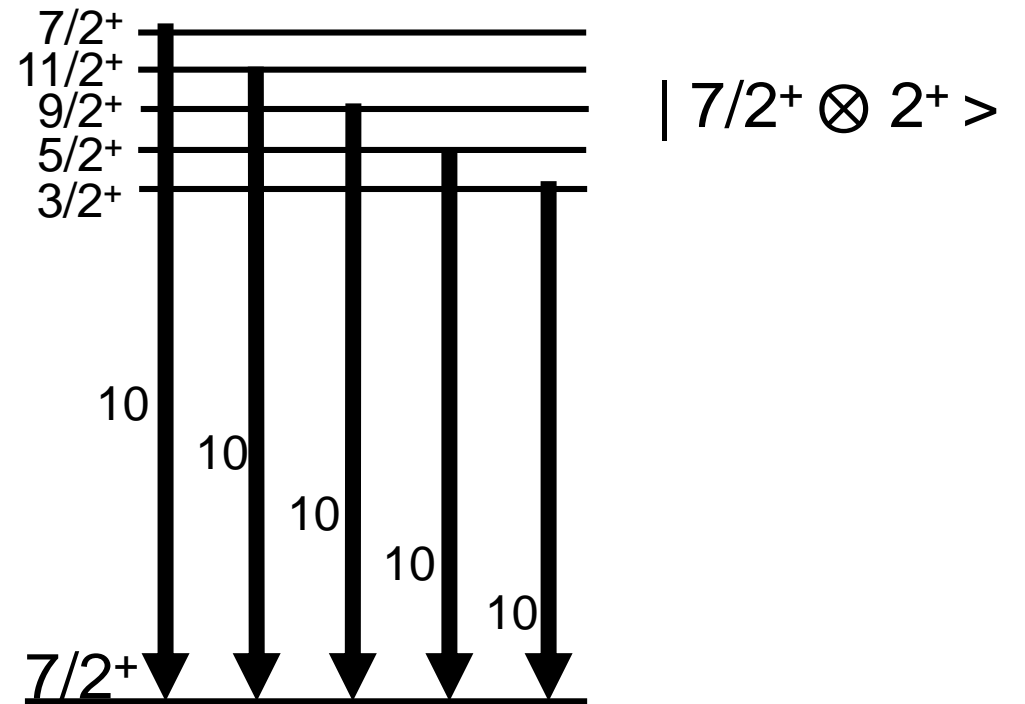
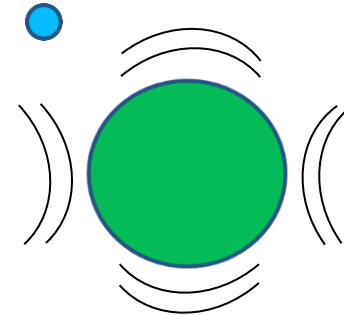
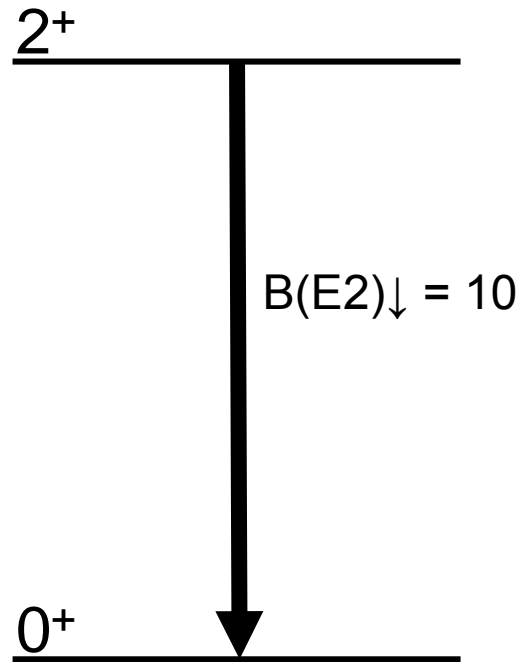
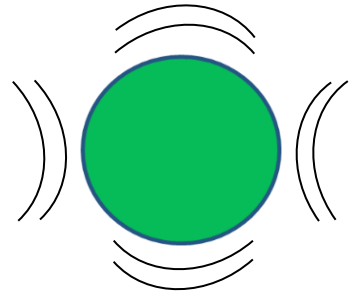
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End

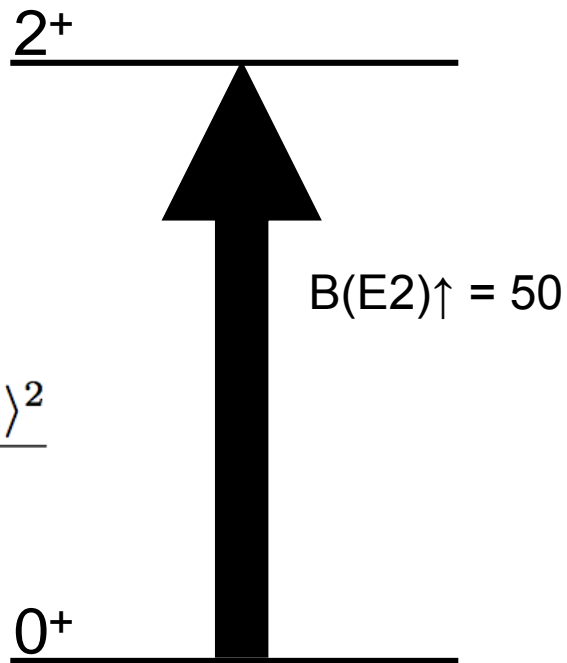
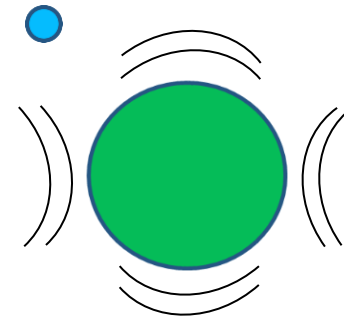
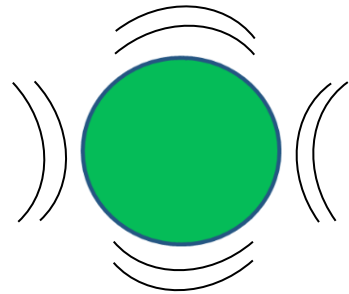
Particle-Core Coupling

The weak-coupling limit yields equivalent $B(E2)_{\downarrow}$ values; strong coupling would repartition strength

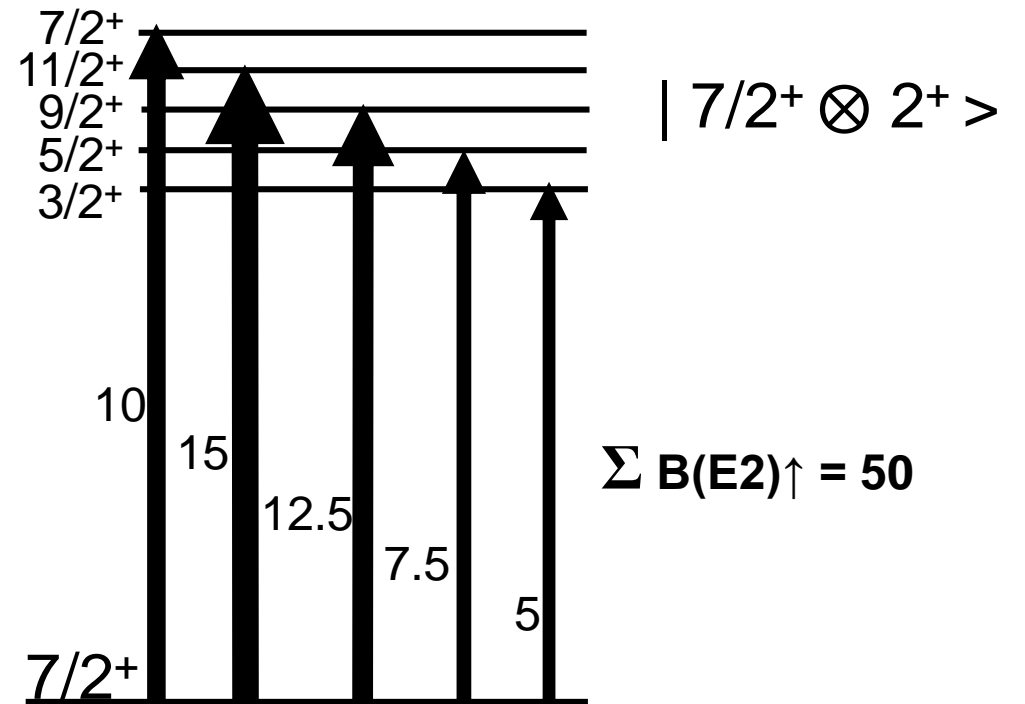


Particle-Core Coupling

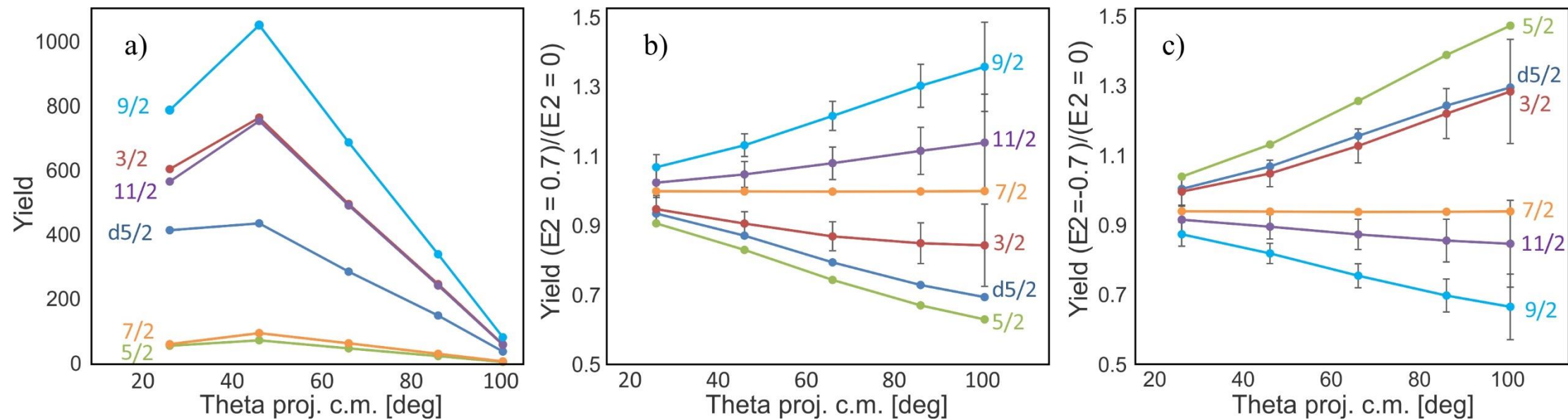
All particle-core coupling schemes (e.g., weak and strong) preserve the total strength up, $\langle Q^2 \rangle_{\text{core}} = \sum B(E2) \uparrow$



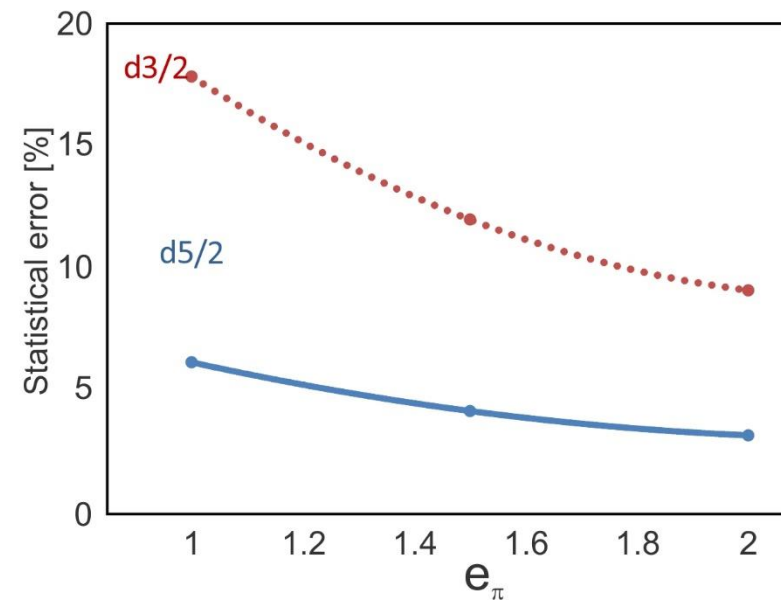
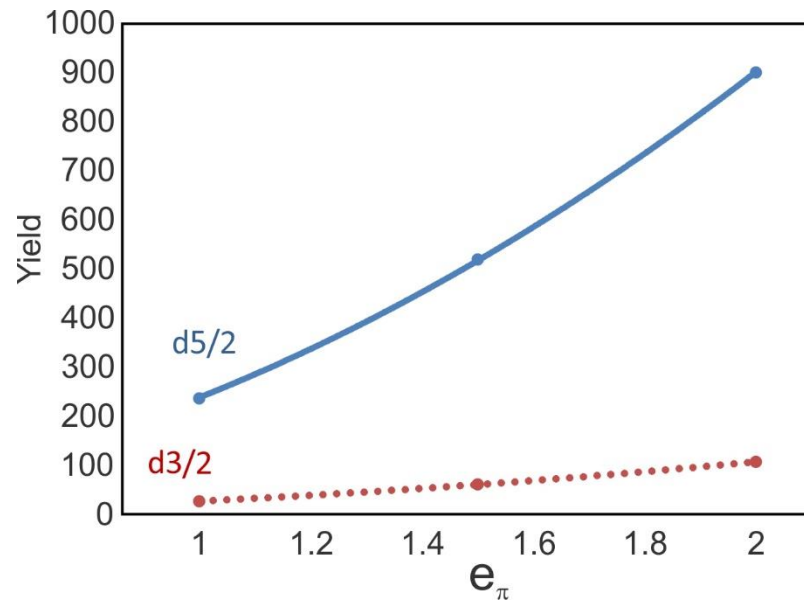
$$B(E2; I_i^+ \rightarrow I_f^+) = \frac{\langle I_f || E2 || I_i \rangle^2}{2I_i + 1}$$



High-accuracy B(E2)'s from Coulex – the pitfalls



Proton effective charges from ^{133}Sb



Expected γ -yields at Miniball

isotope	I_i	I_f	E_x [MeV]	$B(E2)$ [W.u.]	p-g yields	$B(E2)$ stat. err. [W.u.]	stat. err. [%]
¹³¹ Sb	7/2	5/2 _{d5/2}	0.798	0.55	1325	0.015	2.7
		3/2	1.141	1.8	2174	0.039	2.1
		5/2	1.202	0.19	205	0.014	7.0
		11/2	1.226	2.11	2114	0.046	2.2
		9/2	1.229	2.97	2951	0.055	1.8
		7/2	1.482	0.47	257	0.029	6.2
¹³³ Sb	7/2	5/2 _{d5/2}	0.962	0.31	520	0.014	4.4
		3/2 _{d3/2}	2.439	2.79	62	0.35	13
¹²⁷ In	9/2	11/2	1.066	7.1	921	0.20	3.3
		13/2	1.235	7.2	458	0.34	4.7
		5/2	~1.1	3.8	658	0.15	3.9
		7/2	~1.6	0.34	14	0.09	27
		9/2	~1.6	0.2	8	0.07	35
¹²⁷ In	1/2	3/2	0.524	2.5	2948	0.04	4.0
		5/2	~1	1.5	1905	0.03	2.8