

Measurement of the changes in the mean-square charge radii of aluminium isotopes across $N = 20$

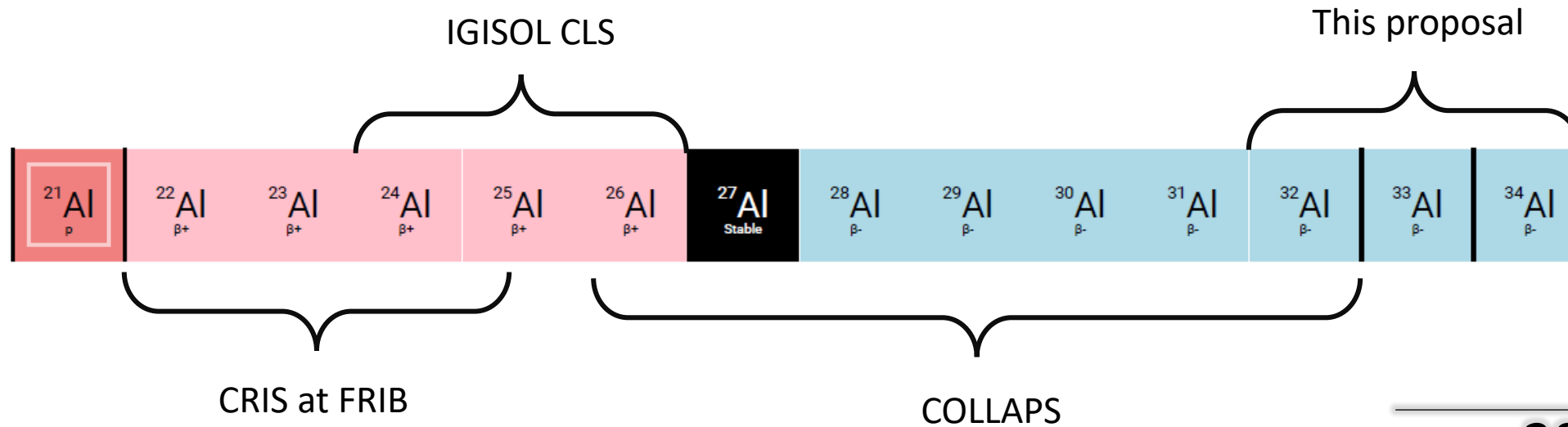
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On behalf of the CRIS collaboration

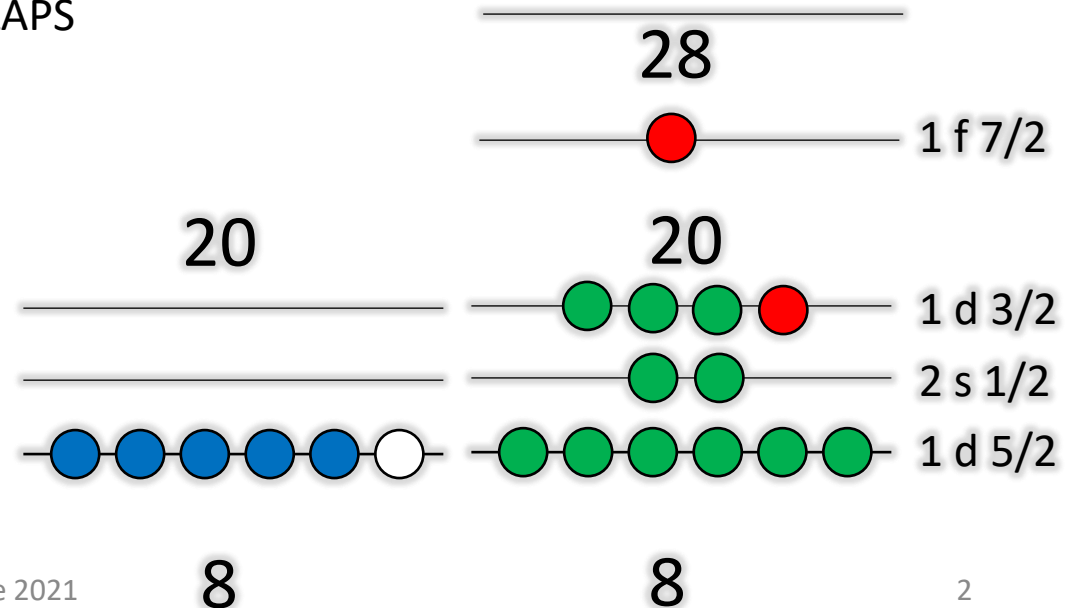
21.06.2021

Interest in the Al isotopes

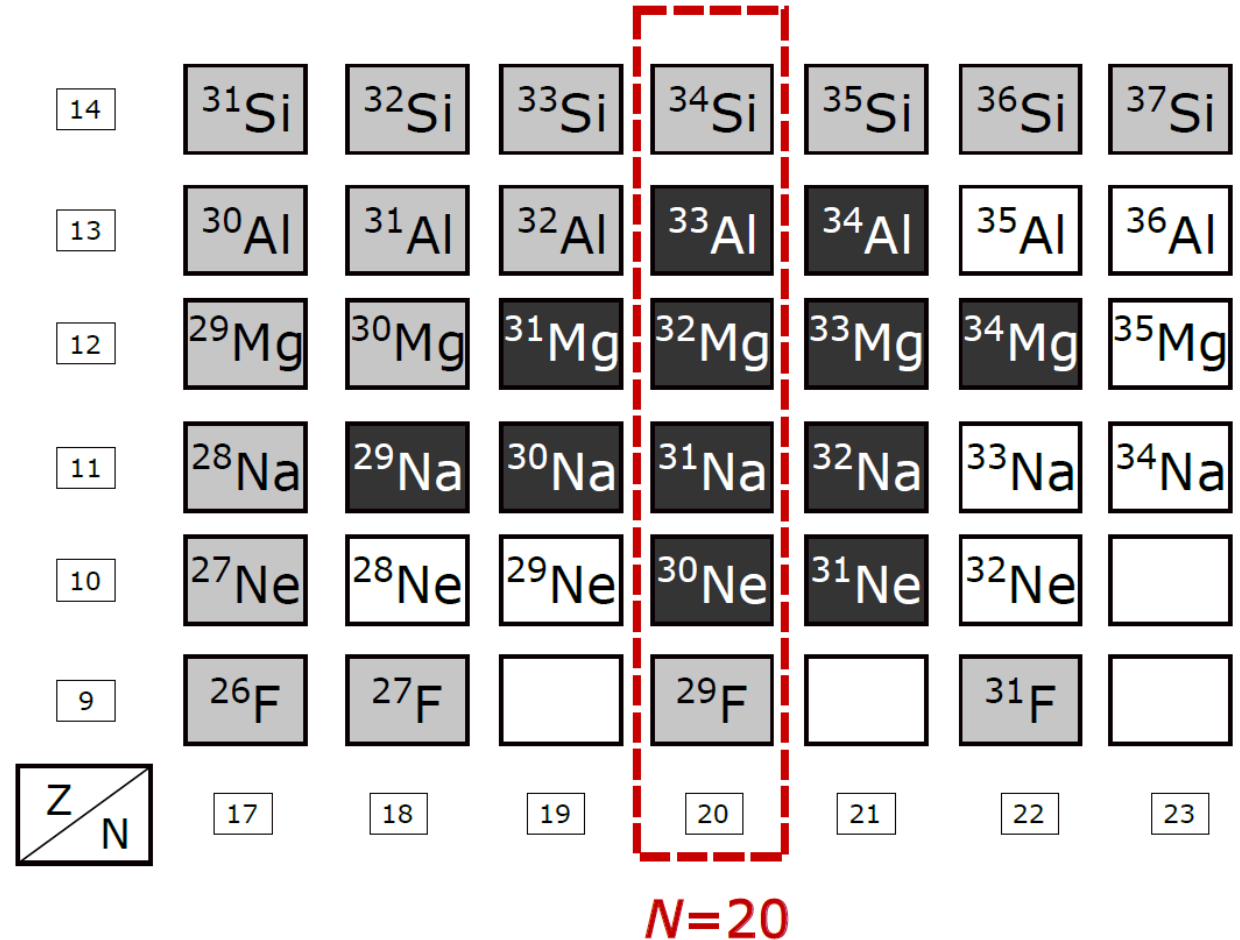
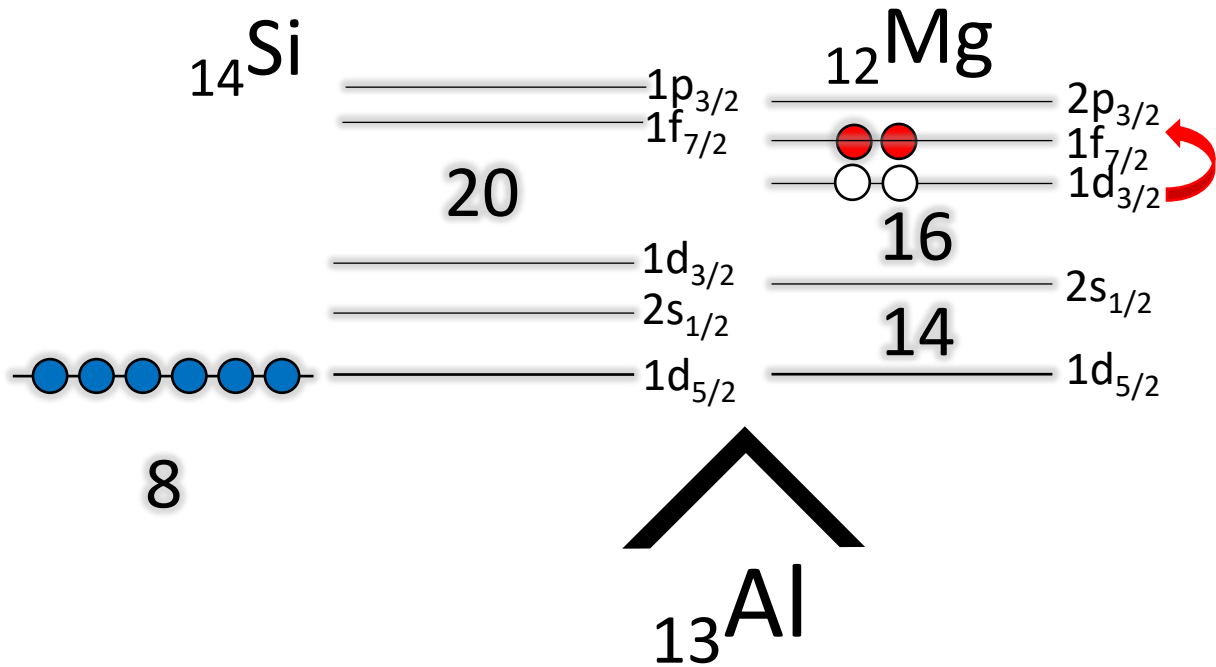


$^{26-32}\text{Al}$ have been measured at **ISOLDE** by COLLAPS
 $^{24-26}\text{Al}$ proposed at **IGISOL** (collinear laser spectroscopy)
 $^{22-23}\text{Al}$ will be proposed at **FRIB** (CRIS)

We propose to measure the neutron-rich isotopes $^{32-34}\text{Al}$ using the CRIS technique.



Island of inversion and $N=20$



$^{33-34}\text{Al}$ at the border of the island of inversion.
 ^{33}Al has a magic number of neutrons $N=20$.

Figure: The island of inversion at $N=20$.

Charge radii along $N=20$

No shell effect at the magic $N=20$ for Ar, K and Ca.

The study of Cl, S, P and Si is extremely challenging.

The charge radius of ^{32}Al was extracted with large uncertainties (7 MHz). However, the relatively low value may be an indication of the $N=20$ shell closure. [1]

Al is the next isotope which can be measured across $N=20$ without technical developments.

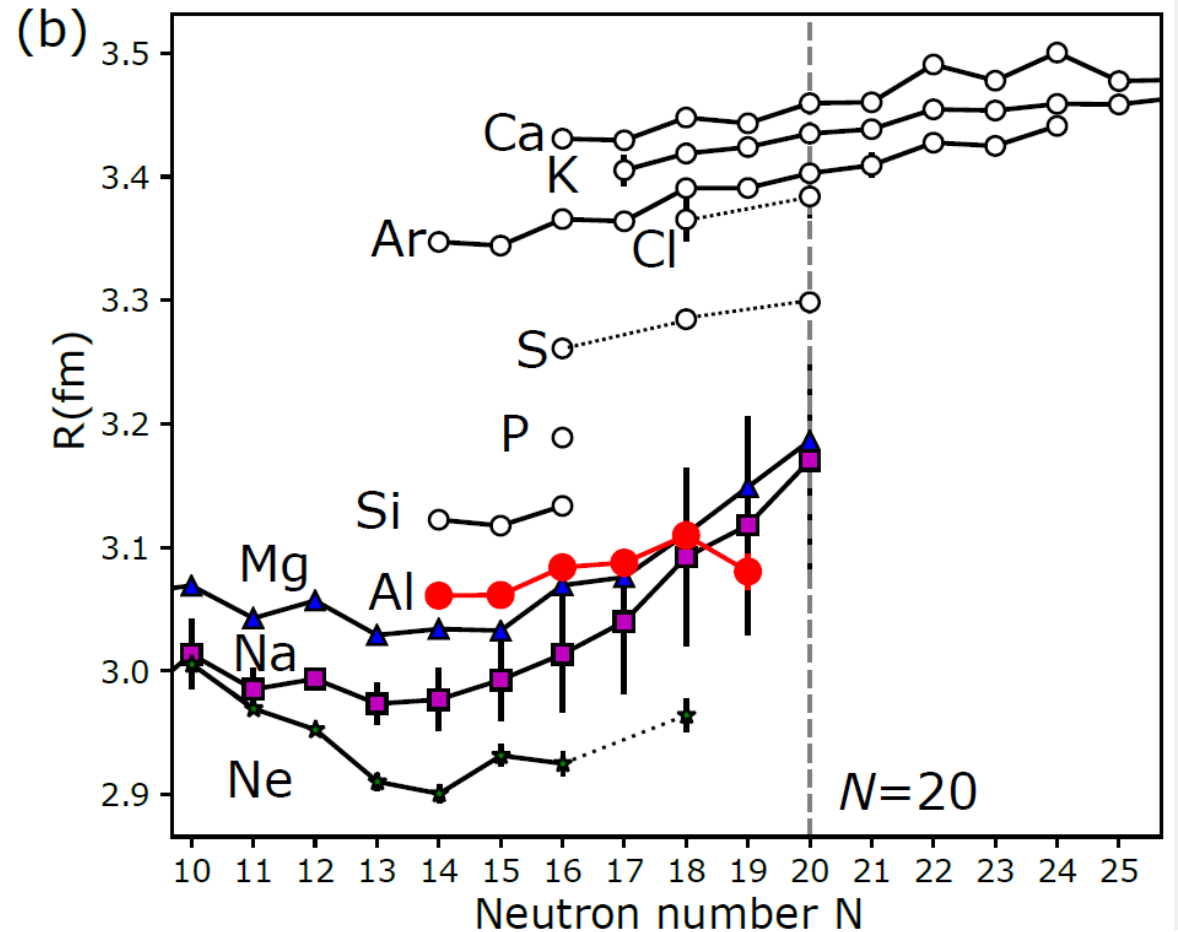


Figure: The charge radii around $N=20$.

Charge radii in the island of inversion

The charge radii are sensitive to structural changes in the Island of inversion and shell closures.

A striking correspondence is found between the nuclear charge radius and the neutron shell structure [1].

The onset of deformation is clear at $N=19$ in the Mg chain [1].

The radius of ^{32}Al is unexpectedly small [2].

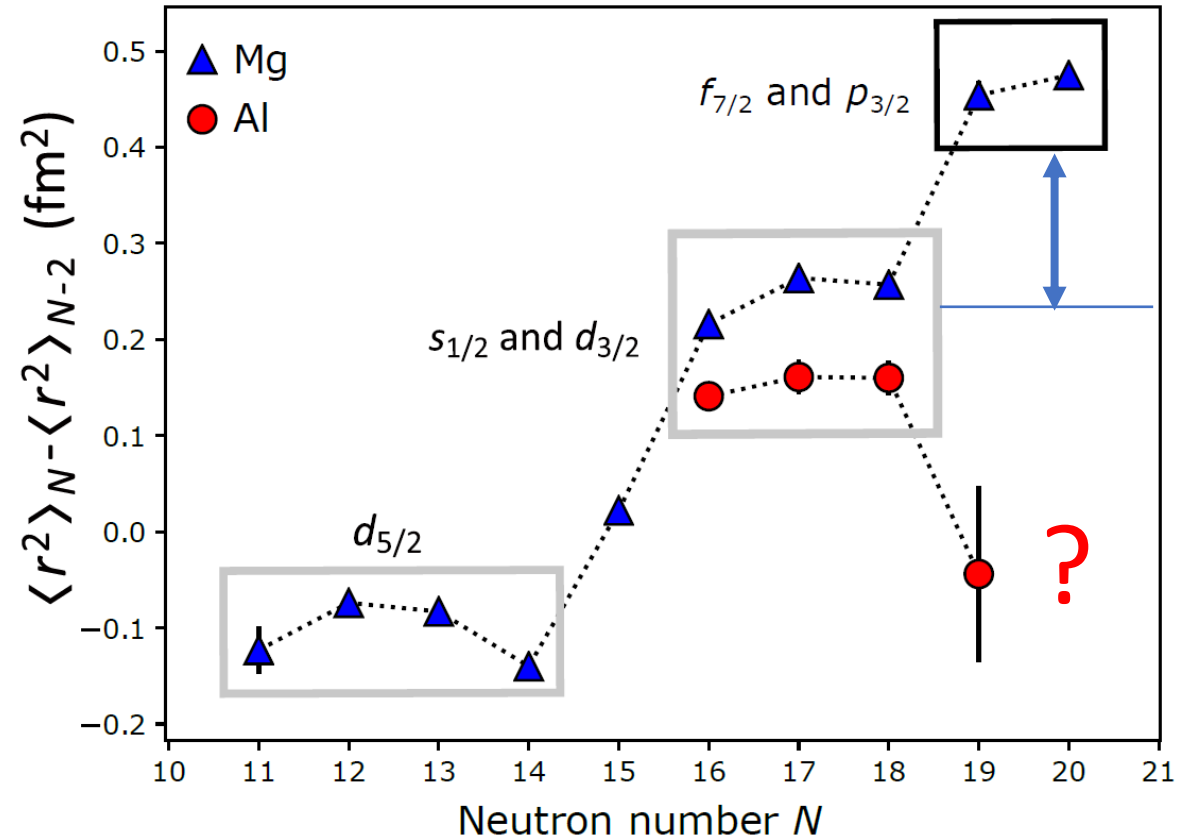
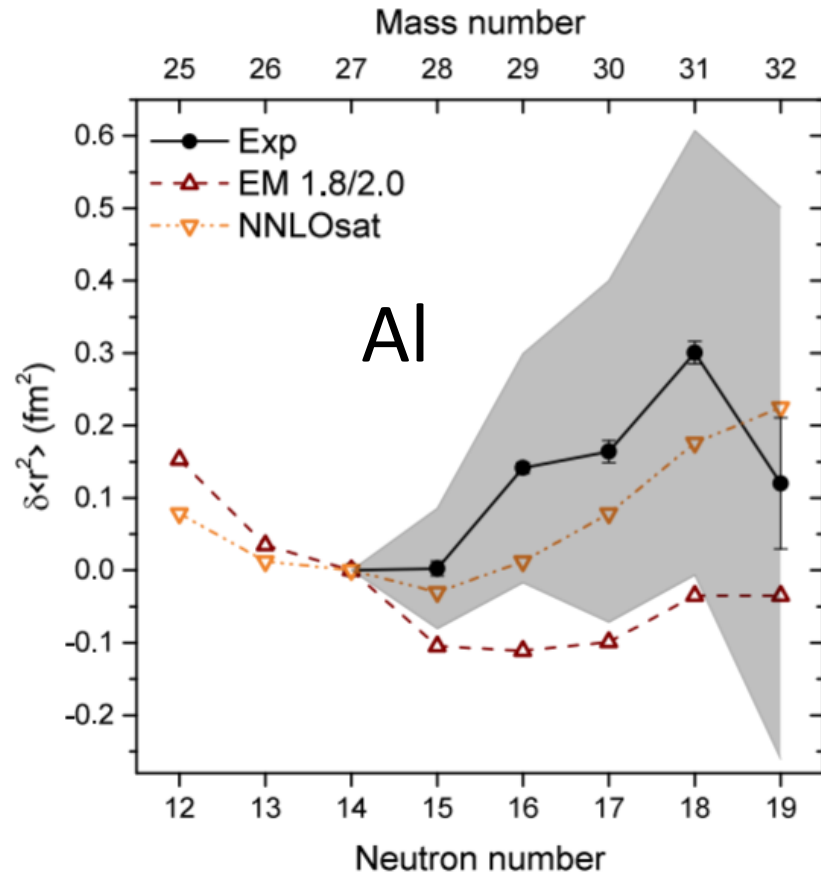


Figure: Differential charge radii of Mg and Al. Clear evidence for the onset of deformation at $N=19$ for Mg [1].

[1] D.T. Yordanov et al. Phys. Rev. Lett. 108, 042504

[2] H. Heylen et al. Phys. Rev. C 103, 014318

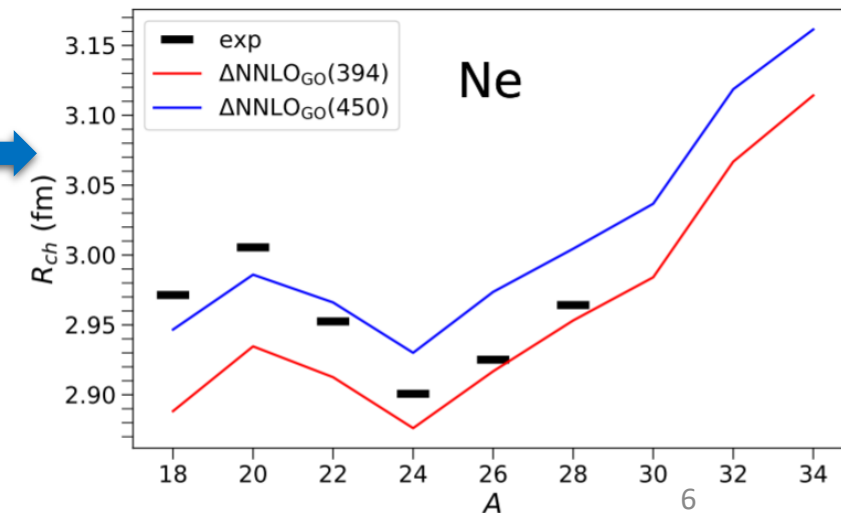
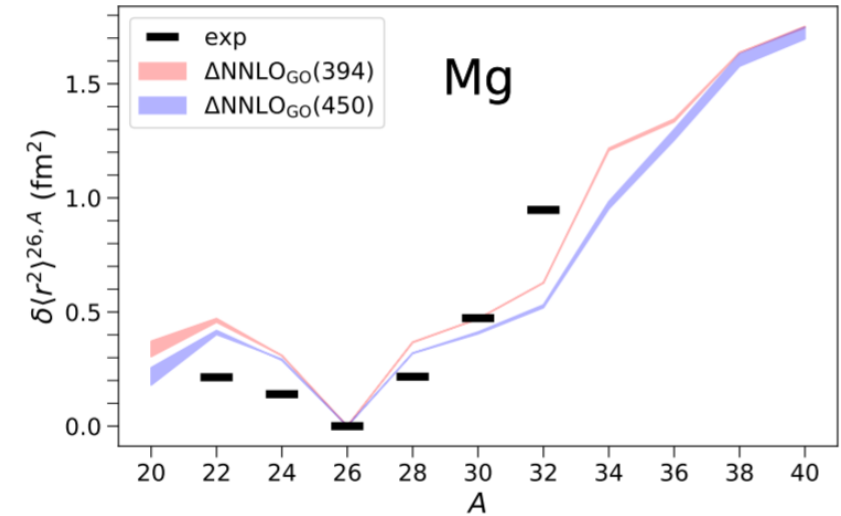
Theoretical models: VS-IMSRG and Coupled Cluster method



Both methods have been used in the region of the island of inversion.

VS-IMSRG calculations are readily available for Al. [1]

The CC [2] methods can be used to calculate Al charge radii to the same approximation as in the K chain. [3,4]



[1] H. Heylen et al. Phys. Rev. C 103, 014318

[2] S.J. Novario et al., Phys. Rev. C 102, 051303(R)

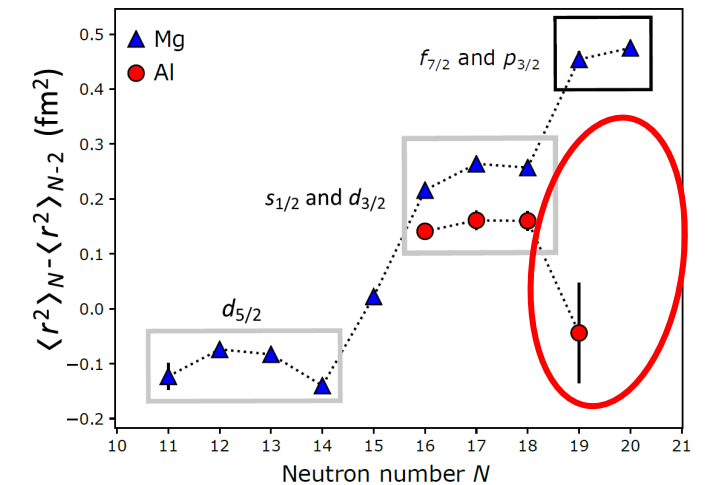
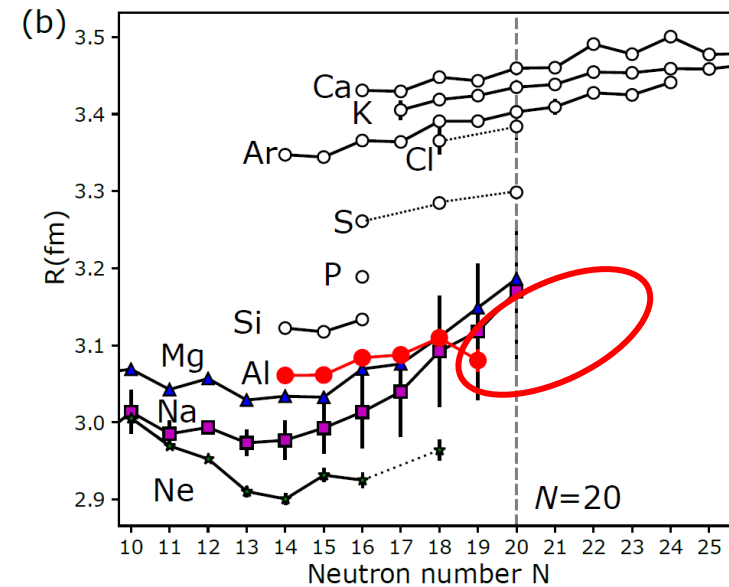
[3] A. Koszorus et al., Nature Physics 17, 439–443 (2021)

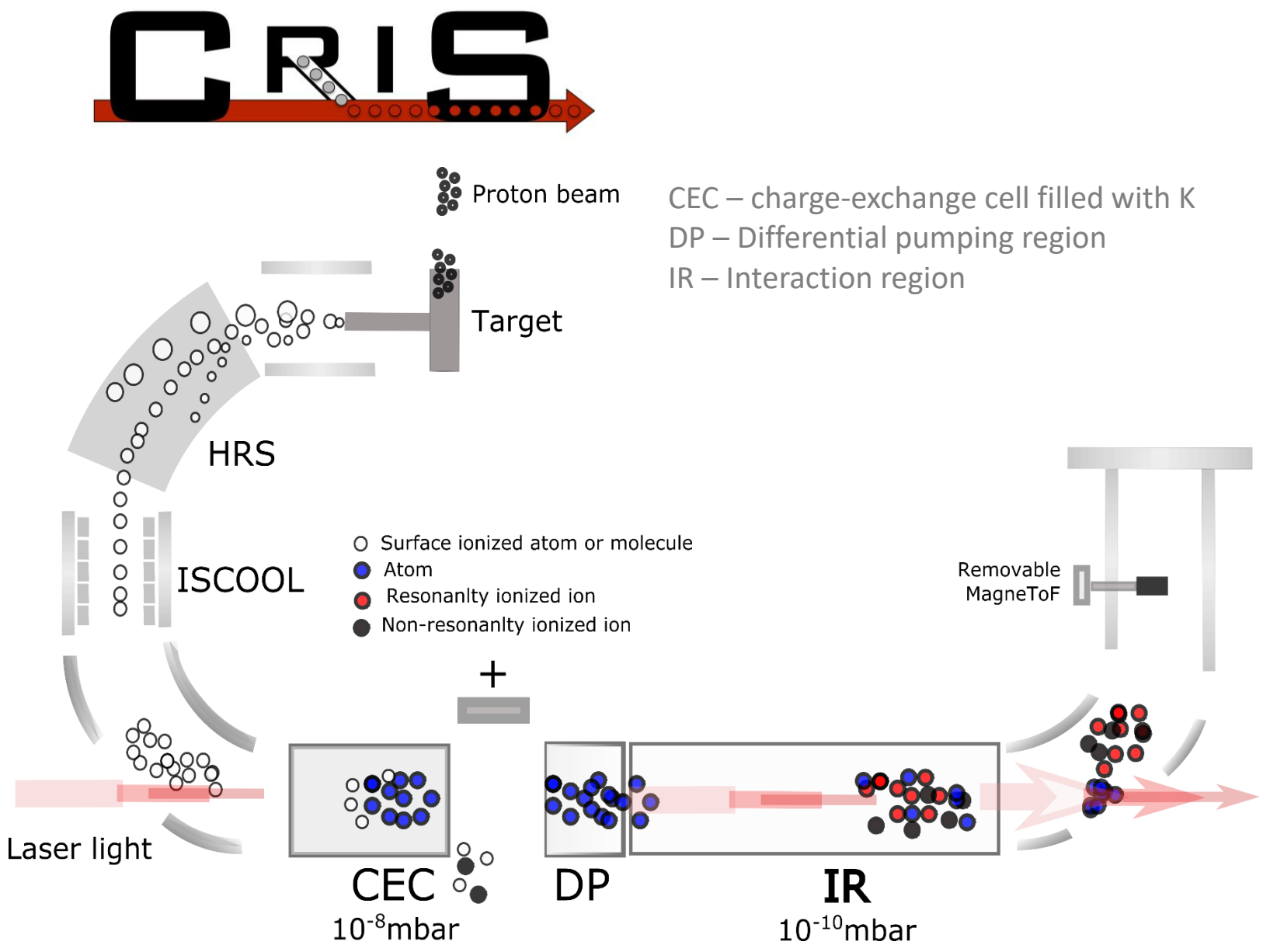
[4] G. Hagen, private communication

Open questions

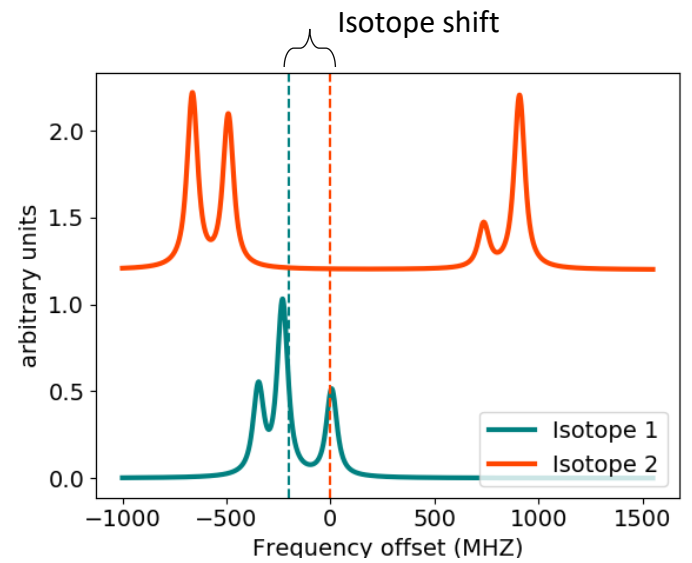
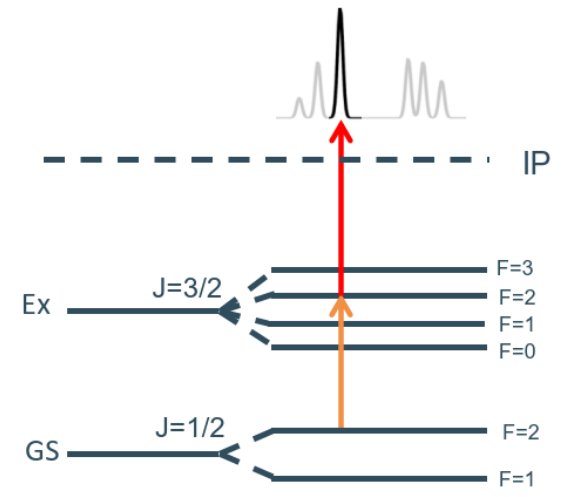
1. Investigate how the nuclear **charge distribution evolves beyond $N=20$** in this uncharted territory?
2. Is there a signature of deformation in the charge radii of $^{32-34}\text{Al}$ isotopes? – Better **understanding of the border of the island of inversion.**
3. How do the experimental results **compare to theoretical calculation?**

The precision measurement of the changes in the mean-square charge radius of $^{32-34}\text{Al}$ provides answers to these questions.

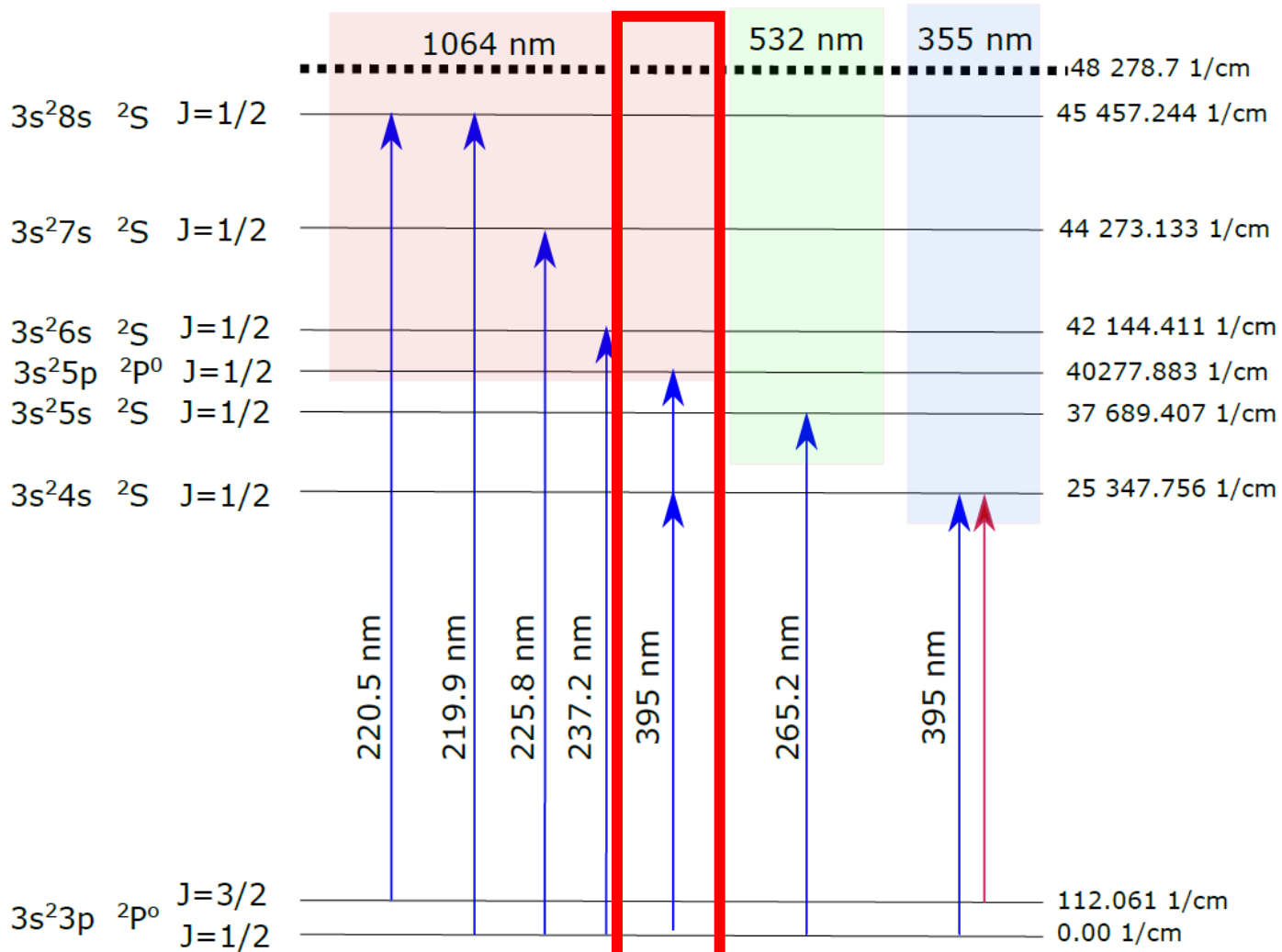
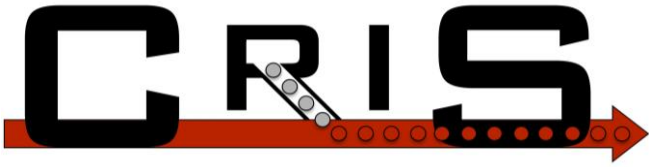




CEC – charge-exchange cell filled with K
 DP – Differential pumping region
 IR – Interaction region

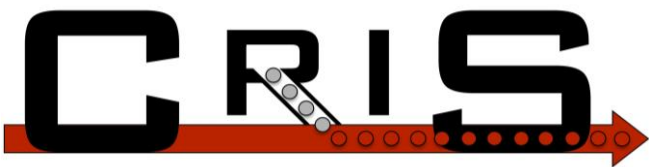


Isotope shift requires the precise measurement of the hfs of two isotopes.

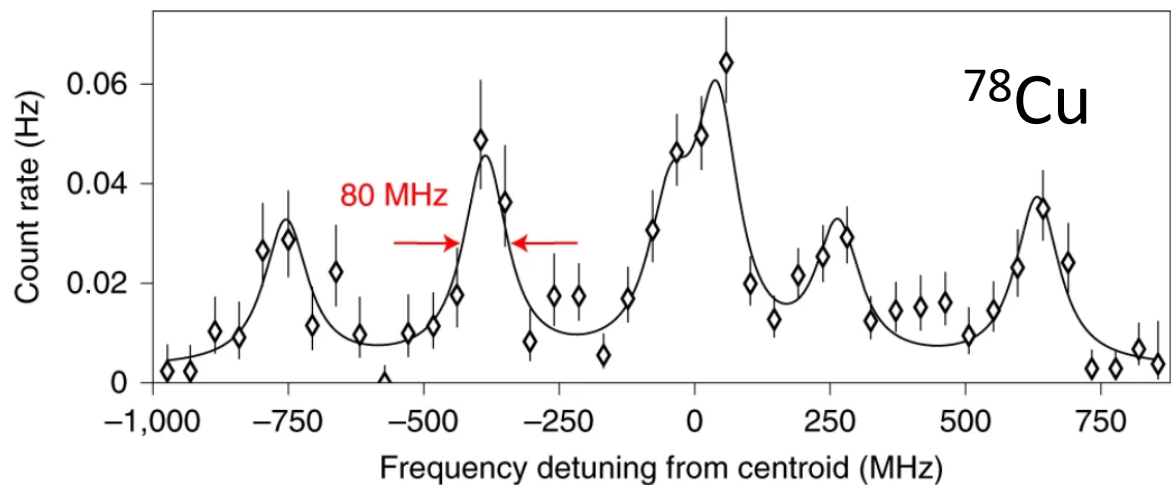


3 step resonance ionization scheme
 395 nm + 670 nm + 1064 nm

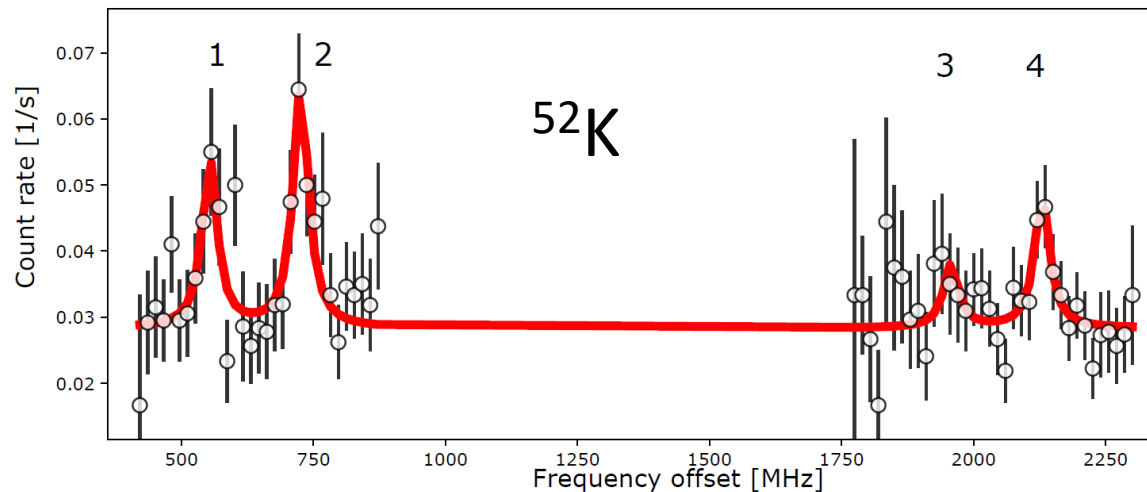
All wavelengths can be produced
 by the existing lasers.



11 shifts requested for $^{33-34}\text{Al}$ with yields of ~ 500 ions/s and >10 ions/s



20 ion/s produced [1]

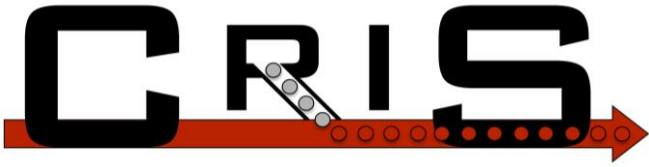


360 ion/s produced [2]

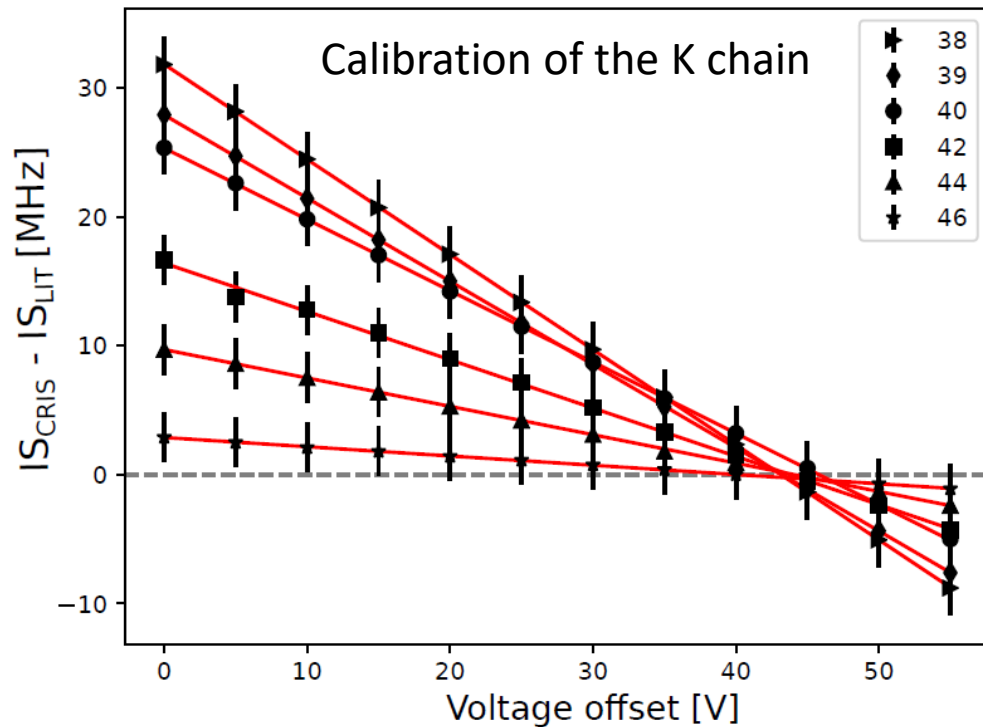
For the successful extraction of the changes in the mean-square charge radii of Al, a precision better than 2 MHz is required.

[1] R.P. de Groote et al., Nature Physics 16, 620–624 (2020)

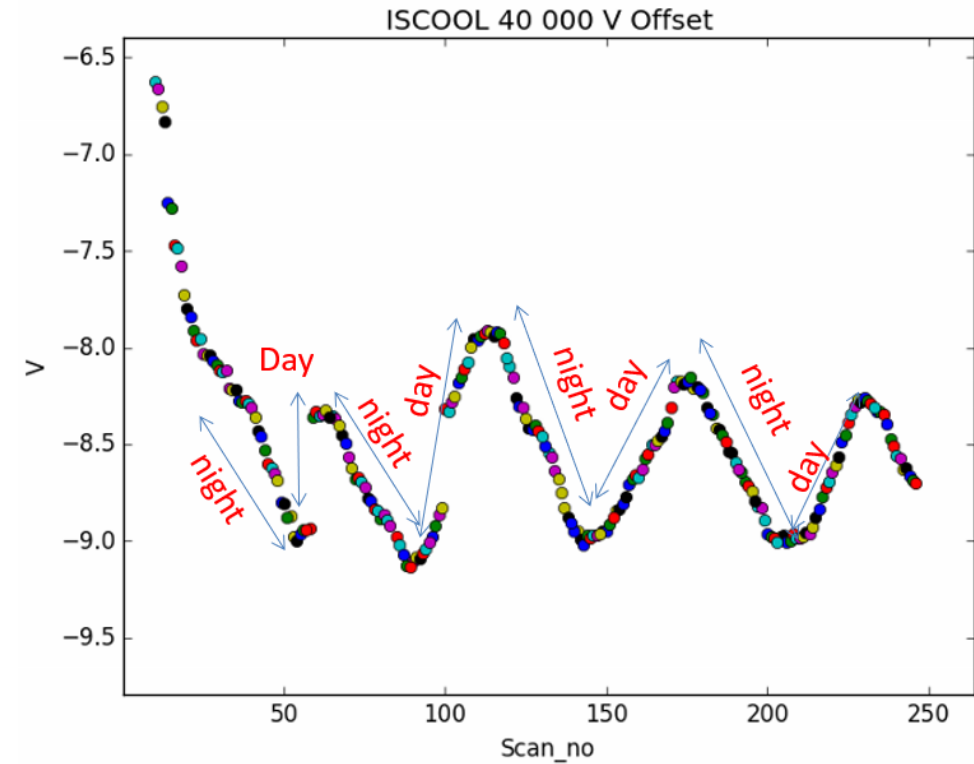
[2] A. Koszorus et al., Nature Physics 17 439–443 (2021)



- Remeasure the $^{27-31}\text{Al}$ to calibrate the beam energy.
- Frequent reference measurements to monitor drifts.



2 shifts requested for $^{27-31}\text{Al}$ to get the systematics under control!



Shift request

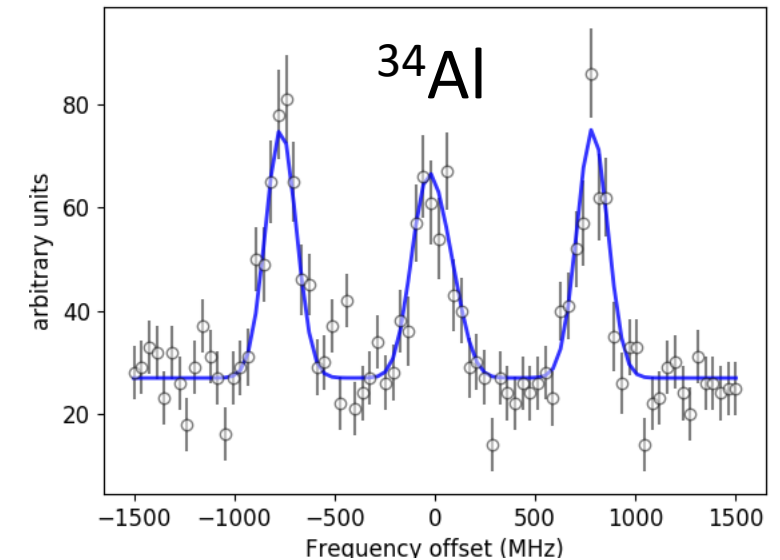
Isotope	Predicted yields (ion/s)	Shifts
^{27}Al	Stable	0.5
$^{28-31}\text{Al}$	$>10^5$	2
^{32}Al	Not listed	1.5
^{33}Al	4.9×10^2	2
^{34}Al	>10	9
Beam tuning		1

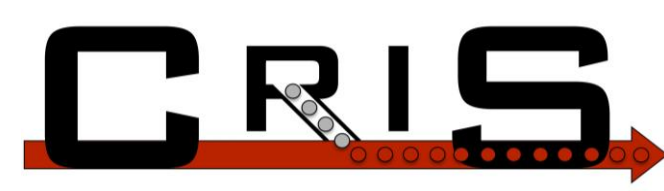
In total 16 shifts.

TAC comments:

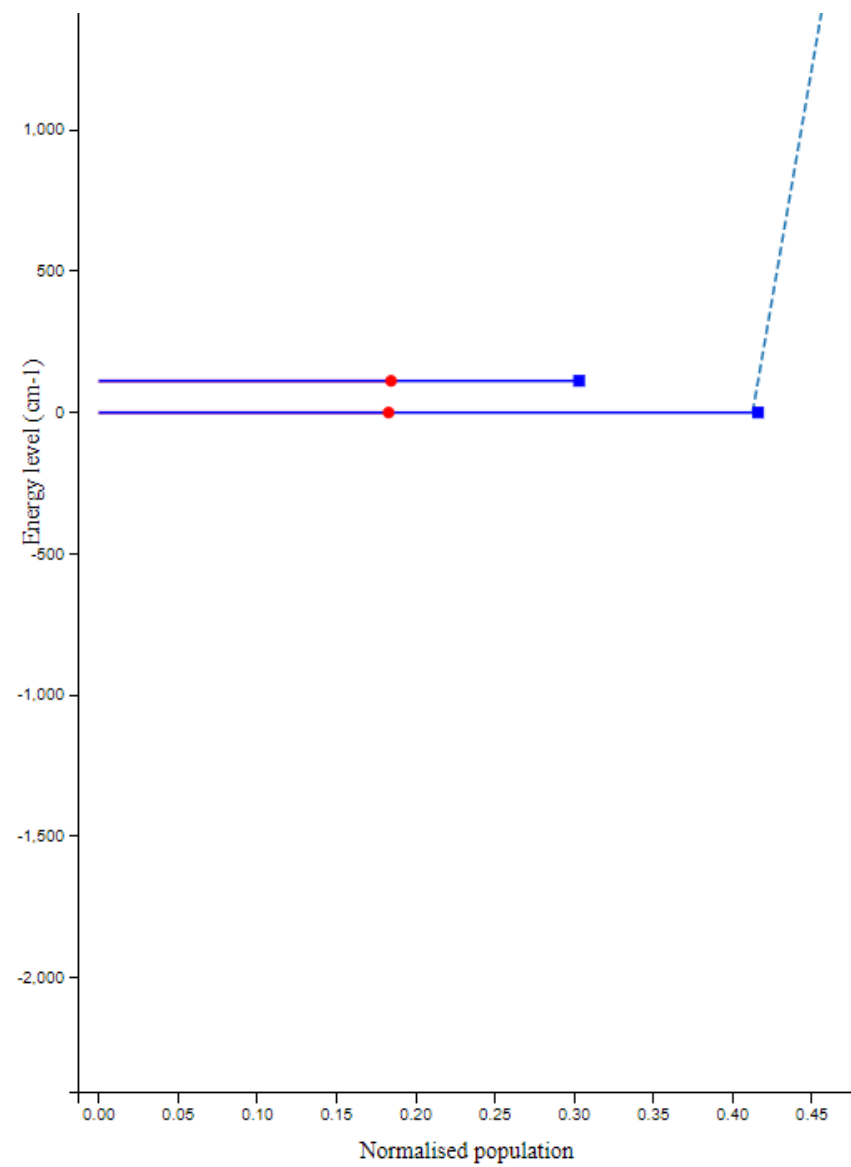
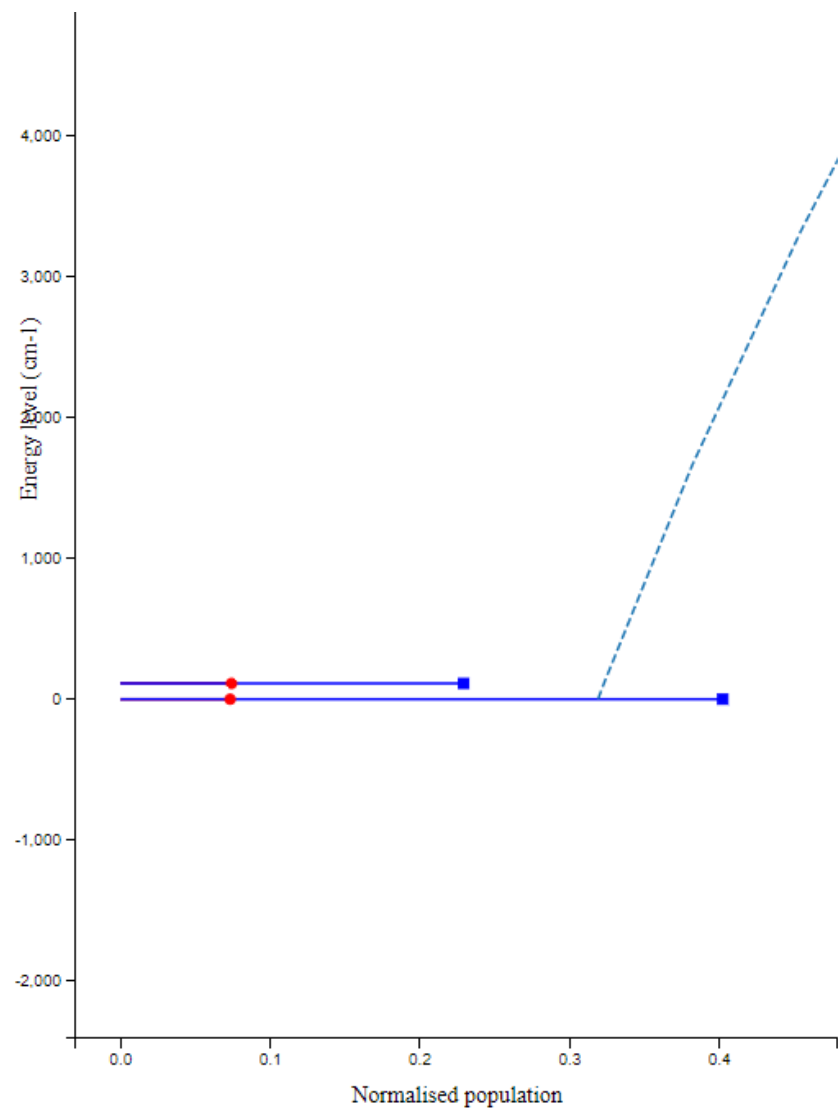
The TAC does not foresee any issues with this proposal other than that the isotopes of concern are difficult to produce but this is well understood.

3 shifts \rightarrow 5.3 MHz uncertainty





Thank you for your attention!



Charge radii of Al isotopes

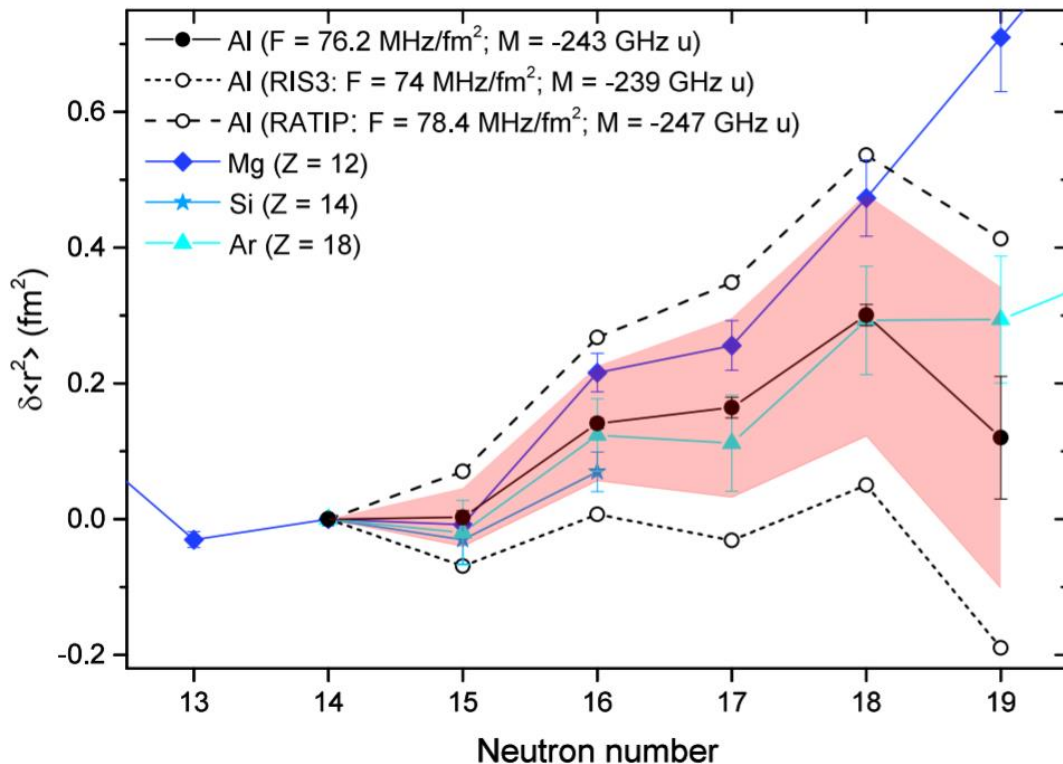


Figure: The charge radii of $^{27-32}\text{Al}$ and the neighboring chains.

$^{26-32}\text{Al}$ have been measured at **ISOLDE** by COLLAPS

The charge radius of ^{32}Al was extracted with large uncertainties (7 MHz). However, the relatively low value may be an indication of the $N=20$ shell closure. [1]

Measurements with higher experimental precision are required.

CRIS technique

Changes in the mean-square charge radii

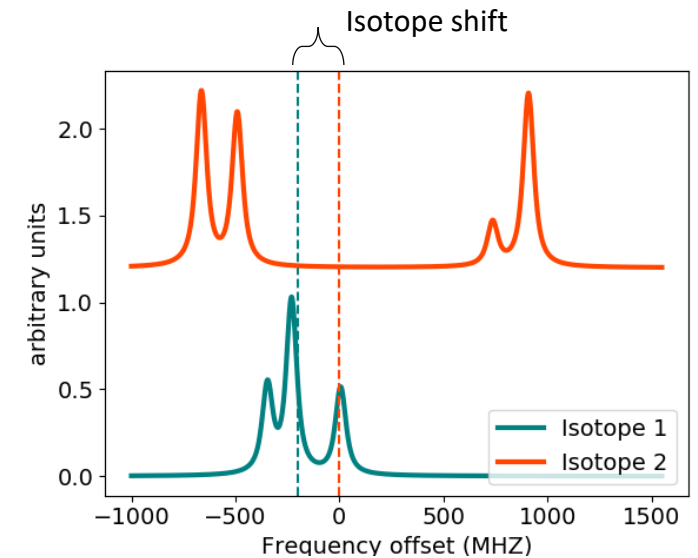
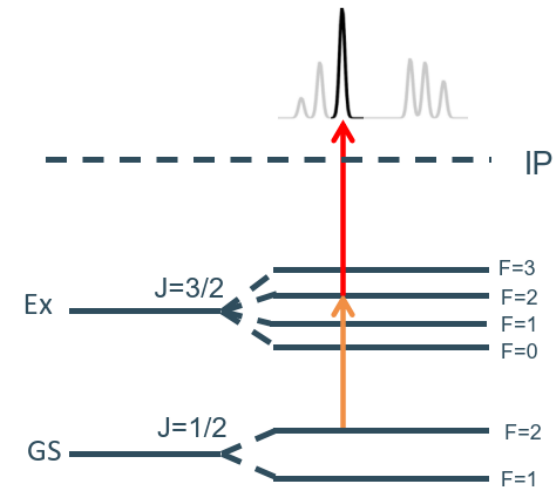
Isotope shift

$$\delta \langle r^2 \rangle = \frac{1}{F} \left(\frac{m_A - m_{A'}}{m_A m_{A'}} K - \delta\nu \right)$$

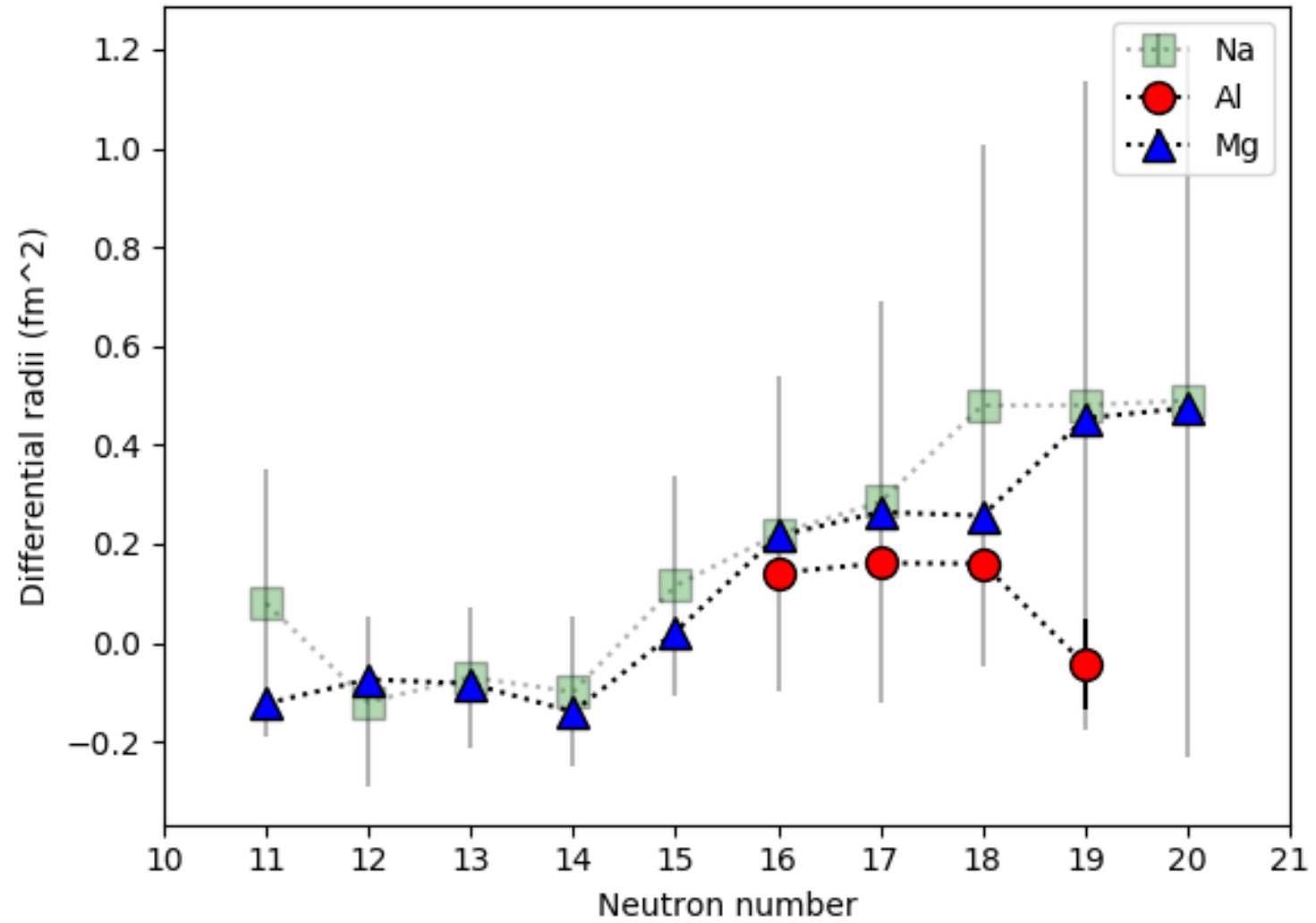
F and K and atomic parameters.

F is sensitive to the charge radius!

Light isotopes have small F . ~ 70 MHz/fm² for Al
 \rightarrow High experimental precision is required for $\delta\nu$ to extraction of the $\delta \langle r^2 \rangle$.



Isotope shift requires the precise measurement of the hfs of two isotopes.



CRIS scheme

219.9150 1.75e+06 0.000 45 457.244 $3s^23p$ $^2P^\circ$ $1/2$ $3s^28s$ 2S $1/2$

220.4590 3.49e+06 112.061 45 457.244 $3s^23p$ $^2P^\circ$ $3/2$ $3s^28s$ 2S $1/2$

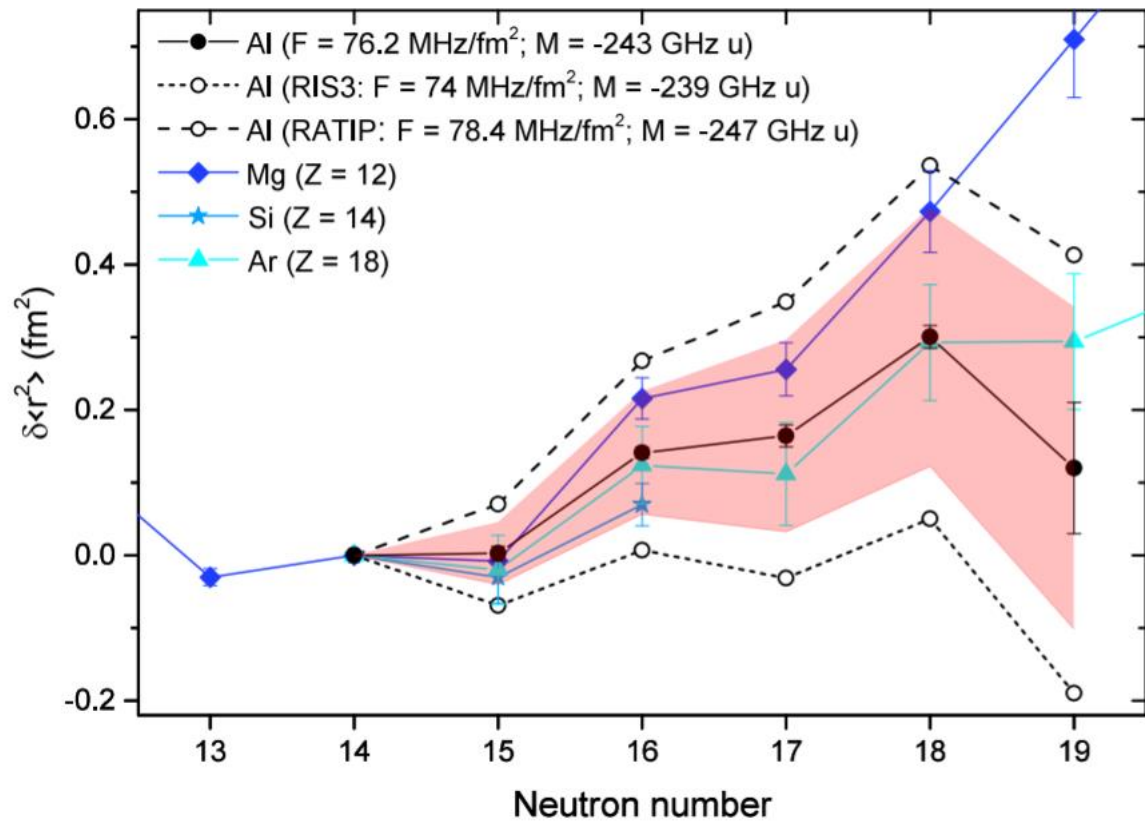
225.7999 3.77e+06 0.000 44 273.133 $3s^23p$ $^2P^\circ$ $1/2$ $3s^27s$ 2S $1/2$

237.2070 5.76e+06 0.000 42 144.411 $3s^23p$ $^2P^\circ$ $1/2$ $3s^26s$ 2S $1/2$

265.2484 1.42e+07 0.000 37 689.407 $3s^23p$ $^2P^\circ$ $1/2$ $3s^25s$ 2S $1/2$

394.40058 4.99e+07 0.000 25 347.756 $3s^23p$ $^2P^\circ$ $1/2$ $3s^24s$ 2S $1/2$

396.15200 9.85e+07 112.061 25 347.756 $3s^23p$ $^2P^\circ$ $3/2$ $3s^24s$ 2S $1/2$



multiconfiguration DiracHartree-Fock framework for the atomic parameters

Ab initio atomic calculations are now possible with coupled-cluster theory.

This will result in more accurate atomic parameters.

