

# Probing charged lepton flavor violation with axion-like particles at Belle II

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[arXiv:2108.11094](https://arxiv.org/abs/2108.11094)

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Tenth workshop of the LLP Community



**NTHU**



# Motivation

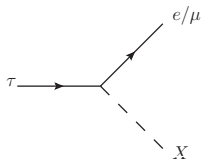
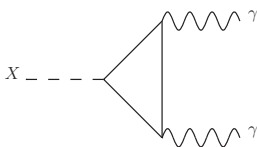
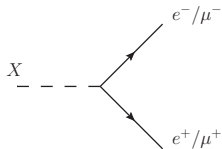
- Belle II:  $e^-$  and  $e^+$  beams at  $\Upsilon(4S)$
- A large number of  $\tau^+\tau^-$  events  $\Rightarrow$  study **rare  $\tau$  decays**
- Sensitive to **LFV** related to the third-generation leptons
- **Leptophilic axion-like particles**

# Model

- $X$ : axion-like particle

$$\begin{aligned}\mathcal{L}_X &= \frac{\partial_\mu X}{\Lambda} \bar{l}_\alpha G_{\alpha\beta} \gamma^\mu (1 + \gamma^5) l_\beta \\ &= -i \frac{X}{\Lambda} \bar{l}_\alpha G_{\alpha\beta} ((m_\alpha - m_\beta) + (m_\alpha + m_\beta) \gamma^5) l_\beta \\ g_{\alpha\beta} &\equiv G_{\alpha\beta} / \Lambda\end{aligned}$$

- *Sign. production*:  $\tau \rightarrow X e / \mu$
- *Sign. decay*:  $X \rightarrow e^- e^+ / \mu^- \mu^+$
- $X \rightarrow \gamma\gamma$  induced via a triangular loop



## Decay widths of $\tau$ and $X$

- $\tau \rightarrow X e/\mu$ :

$$\Gamma(l_\alpha \rightarrow l_\beta X) = \frac{m_\alpha^3}{8\pi} \sqrt{\left(1 - \left(\frac{m_\beta + m_X}{m_\alpha}\right)^2\right) \left(1 - \left(\frac{m_\beta - m_X}{m_\alpha}\right)^2\right)}$$
$$\times g_{\alpha\beta}^2 \left[ \left(1 - \frac{m_\beta^2}{m_\alpha^2}\right)^2 - \frac{m_X^2}{m_\alpha^2} \left(1 + \frac{m_\beta^2}{m_\alpha^2}\right) \right]$$

- ALP decays:

$$\Gamma(X \rightarrow l_\beta^- l_\beta^+) = \frac{m_X m_\beta^2}{2\pi} g_{\beta\beta}^2 \sqrt{1 - \frac{4m_\beta^2}{m_X^2}}$$

$$\Gamma(X \rightarrow \gamma\gamma) = 4\pi\alpha^2 m_X^3 |g_{\gamma\gamma}^{\text{eff}}|^2, \quad g_{\gamma\gamma}^{\text{eff}} = \frac{1}{8\pi^2} \sum_{\alpha=e,\mu,\tau} g_{\alpha\alpha} B_1(4m_\alpha^2/m_X^2)$$

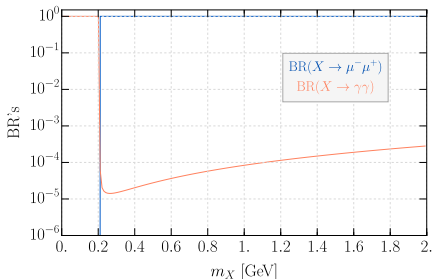
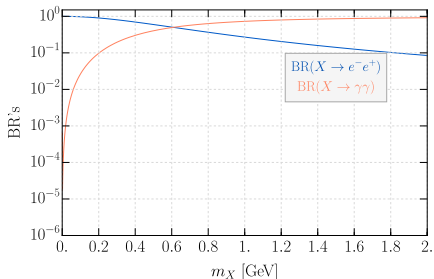
# Benchmark scenarios

|                                | Scenario 1   | Scenario 2   |
|--------------------------------|--|--|
| $g_{\tau\alpha}$<br>tau decays | $g_{\tau e}$<br>$\tau \rightarrow Xe$                        | $g_{\tau\mu}$<br>$\tau \rightarrow X\mu$                             |
| $g_{\beta\beta}$<br>X decays   | $g_{ee}$<br>$X \rightarrow e^-e^+(\text{sig.})/\gamma\gamma$ | $g_{\mu\mu}$<br>$X \rightarrow \mu^-\mu^+(\text{sig.})/\gamma\gamma$ |

- $g_{\tau\alpha}$  and  $m_X \Rightarrow$  prod. rates
- $g_{\beta\beta}$  and  $m_X \Rightarrow c\tau_X$

# X decays

- $\Gamma(X \rightarrow l_{\beta}^{-} l_{\beta}^{+}) \sim m_X m_{\beta}^2, \Gamma(X \rightarrow \gamma\gamma) \sim m_X^3$



# Tightest current constraint

- Belle results on tau LFV decays which we recast:

| Decay modes                            | Upper bounds on BR [ $10^{-8}$ ] |
|--|----------------------------------|
| $\tau^- \rightarrow e^- e^+ e^-$       | 2.7                              |
| $\tau^- \rightarrow \mu^- \mu^+ \mu^-$ | 2.1                              |
| $\tau^- \rightarrow e^- \mu^+ \mu^-$   | 2.7                              |
| $\tau^- \rightarrow \mu^- e^+ e^-$     | 1.8                              |
| $\tau^- \rightarrow e^+ \mu^- \mu^-$   | 1.7                              |
| $\tau^- \rightarrow \mu^+ e^- e^-$     | 1.5                              |

[arXiv:1001.3221](https://arxiv.org/abs/1001.3221)

## Second-tightest current constraint

Lepton flavor universality from BaBar, for long-lived  $X$  ( $c\tau_X \gtrsim 1$  m)

- $$R_{\mu e} = \frac{\Gamma_{\tau \rightarrow \mu \nu \bar{\nu}}}{\Gamma_{\tau \rightarrow e \nu \bar{\nu}}}, R_{\mu e}^{\text{SM}} = 0.972559 \pm 0.000005, R_{\mu e}^{\text{BaBar}} = 0.9796 \pm 0.0039$$

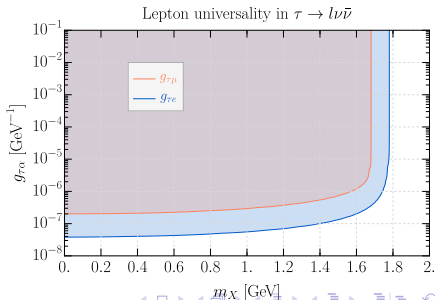
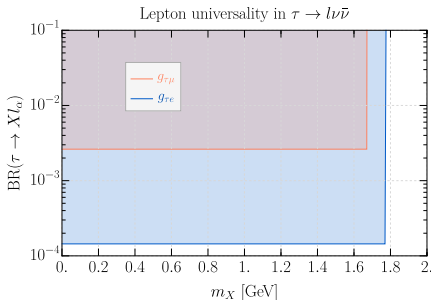
$$\Delta R_{\mu e} \equiv R_{\mu e}^{\text{BaBar}} / R_{\mu e}^{\text{SM}} - 1 = 0.0072 \pm 0.0040$$

$$R_{\mu e}^{\text{SM}+X} = R_{\mu e}^{\text{SM}} + \Gamma(\tau \rightarrow X \mu) / \Gamma_{\tau \rightarrow e \nu \bar{\nu}}^{\text{SM}}$$

$$R_{\mu e}^{\text{SM}+X} / R_{\mu e}^{\text{SM}} - 1 < 0.0072 + 2 \times 0.0040$$

$\Rightarrow$  bounds on  $g_{\tau\mu}$  and  $\text{BR}(\tau \rightarrow X\mu)$

- Similarly for the  $e$  scenario, where  $\Delta R_{e\mu} < 0 \Rightarrow$  particularly stringent bounds





## Event selections

- $E_{e^-} = 7 \text{ GeV}$ ,  $E_{e^+} = 4 \text{ GeV} \Rightarrow \sqrt{s} = 10.58 \text{ GeV}$
- $\mathcal{L}_{\text{Belle}}^{\text{int}} = 1 \text{ ab}^{-1}$ ,  $\mathcal{L}_{\text{Belle II}}^{\text{int}} = 50 \text{ ab}^{-1}$
- $4.6 \times 10^{10}$  tau pair production events at Belle II
- **Prompt** search, **recast** [arXiv:1001.3221](https://arxiv.org/abs/1001.3221):

① Baseline efficiency:

| Decay modes  | Baseline efficiency |
|--|---------------------|
| $\tau \rightarrow Xe, X \rightarrow e^- e^+$       | 6.0 %               |
| $\tau \rightarrow X\mu, X \rightarrow \mu^- \mu^+$ | 7.6 %               |

- ②  $d_0 < 5 \text{ mm}$  (includ. track curvature in the  $B$  field) and  $z_0 < 30 \text{ mm}$
- ③ Small transverse distance:  $r < 10 \text{ cm}$
- **Propose** a **displaced-vertex** search:

- ① Baseline efficiency, same as above
- ② Fiducial volume:  $1 \text{ cm} < r < 80 \text{ cm}$ ,  $-40 \text{ cm} < z < 120 \text{ cm}$
- ③ Linear displaced-tracking efficiency:

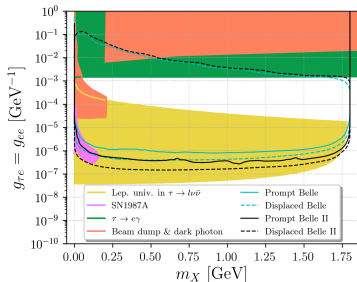
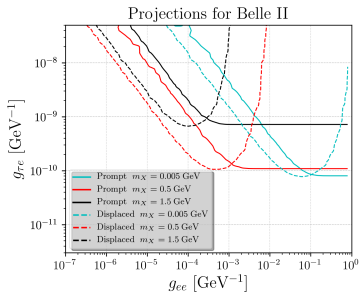
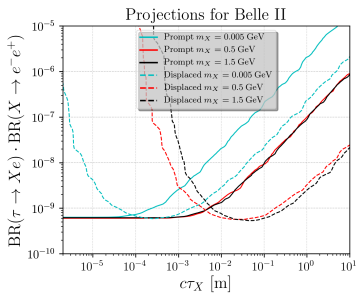
$$\epsilon^{\text{track}}(r = 1 \text{ cm}) = 100\%, \quad \epsilon^{\text{track}}(r = 80 \text{ cm}) = 0\%$$

# Sensitivity computation

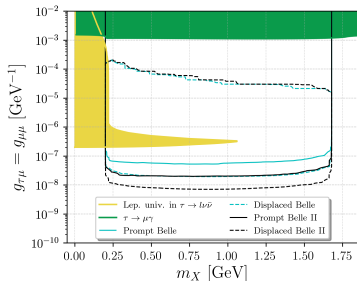
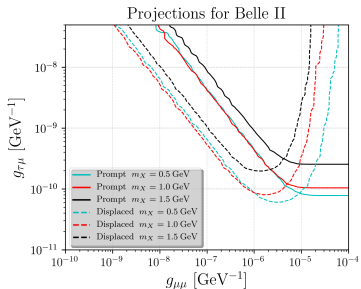
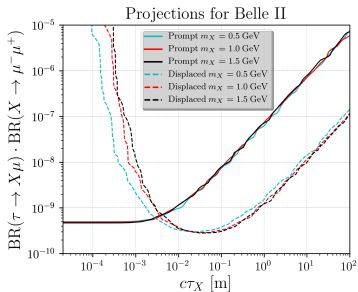
$$N_5^{\text{Belle II}} = 2 \cdot N_{\tau^- \tau^+} \cdot \text{BR}(\tau \rightarrow 1 \text{ prong}) \cdot \text{BR}(\tau \rightarrow X l_\alpha) \cdot \epsilon \cdot \text{BR}(X \rightarrow l_\alpha^- l_\alpha^+)$$

- $\text{BR}(\tau \rightarrow 1 \text{ prong}) \sim 85\%$
- Simulate kinematics with Pythia8
- Expected zero background  $\rightarrow$  3 signal-event isocurves as 95% C.L. exclusion limits

# Results: Scenario 1



# Results: Scenario 2



# Summary

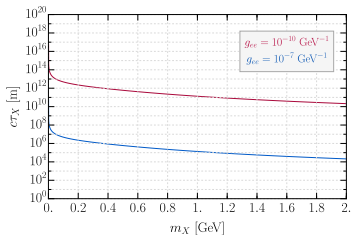
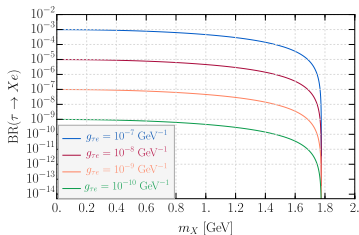
- Recast a Belle prompt search and proposed a DV search, for studying LFV with leptophilic ALPs at Belle II
- Estimated the search efficiencies with Monte-Carlo simulation
- DV/prompt searches better sensitivity at long/short decay lengths
- For long decay lengths, the DV search extends the prompt search's sensitivity to the branching-fraction product by a factor of 40

# Thank You!

# Back-up slides

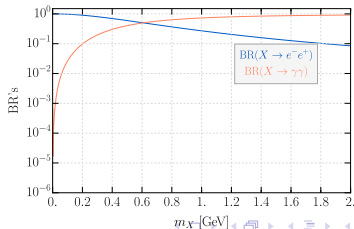
# Scenario 1

- Signature:  $\tau \rightarrow Xe, X \rightarrow e^-e^+$



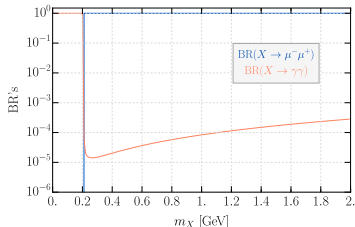
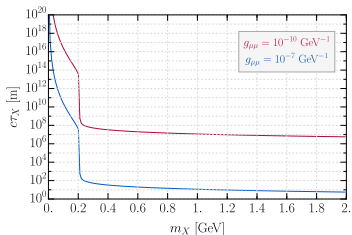
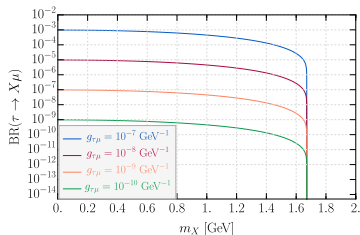
- $\text{BR}(X \rightarrow \gamma\gamma) > \text{BR}(X \rightarrow e^-e^+)$  for  $m_X \gtrsim 0.6$  GeV

- $\Gamma(X \rightarrow l_\beta^- l_\beta^+) \sim m_X m_\beta^2$
- $\Gamma(X \rightarrow \gamma\gamma) \sim m_X^3$



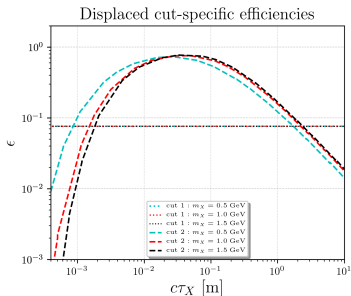
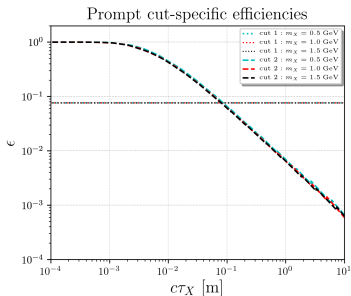
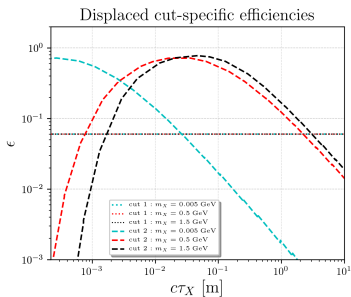
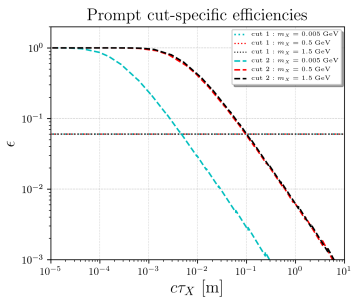
# Scenario 2

- Signature:  $\tau \rightarrow X\mu$ ,  $X \rightarrow \mu^- \mu^+$



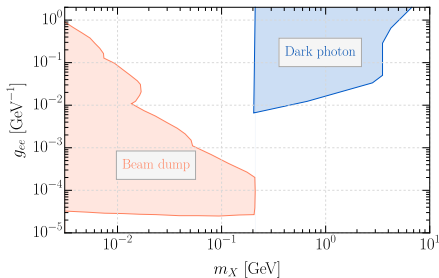
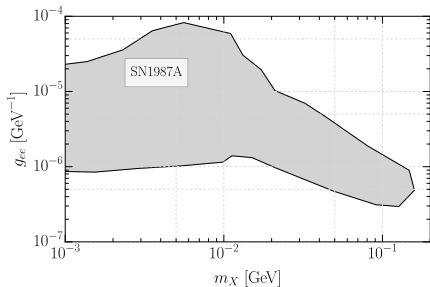


# Efficiencies



## Less important constraints – I

- **LEP ALEPH:**  $\sigma(e^-e^+ \rightarrow \tau^-\tau^+) = 6.02 \pm 0.39(\text{stat} \pm 0.09(\text{syst}))$  pb at  $\sqrt{s} = 209$  GeV  $\Rightarrow g_{\tau e} < 0.078$  GeV $^{-1}$
- $X$  coupled to leptons enhances cooling rate of **supernova** ([arXiv:2107.12393](https://arxiv.org/abs/2107.12393)):



- **Beam-dump** experiments ([arXiv:1008.0636](https://arxiv.org/abs/1008.0636), [arXiv:1005.3978](https://arxiv.org/abs/1005.3978))
  - **BaBar dark photon** search ([arXiv:1708.00443](https://arxiv.org/abs/1708.00443))
  - $\text{BR}(\tau \rightarrow e\gamma) < 3.3 \times 10^{-8}$  and  $\text{BR}(\tau \rightarrow \mu\gamma) < 4.4 \times 10^{-8}$  ([arXiv:0908.2381](https://arxiv.org/abs/0908.2381))
- $\Rightarrow g_{\tau e}g_{ee}$  and  $g_{\tau\mu}g_{\mu\mu} \lesssim 10^{-6}$  GeV $^{-2}$  for  $m_X \lesssim m_\tau$

## Less important constraints – II

- **Leptonic decays of  $\mu$** :  $\mu \rightarrow e\gamma$ ,  $\mu \rightarrow 3e$ ,  $\mu \rightarrow e\gamma\gamma$ ,  $\mu \rightarrow e + \text{missing}$ , strong bounds on coupling combinations or couplings, **irrelevant to Scenarios 1 or 2**
- Muonium-antimuonium oscillations with  $g_{\mu e}$ : not considered
- $\mu^- \rightarrow e^-$  conversion in nuclei with  $g_{\mu e}$ : not considered
- Leptonic  $g - 2$ 's:

$$\Delta a_e = a_e^{\text{exp}} - a_e^{\text{SM}} = (4.8 \pm 3.0) \times 10^{-13}$$

$$\Delta a_\mu \equiv a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = (25.1 \pm 5.9) \times 10^{-10}$$

$(g - 2)_e$ : the leptophilic  $X$  considered in Scenario 1 can bring the theoretical prediction to reach the 95% lower limit of  $\Delta a_e$  but not up to the central value

$(g - 2)_\mu$ : the ALPs in Scenario 2 cannot even bring the theoretical prediction to the edge of the 95% lower limit of the experimental value