



# **MC Comparative Cost Analysis: *Part I – Phenomenological Model***

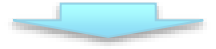
**Vladimir SHILTSEV (Fermilab)**

*MCC*

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# (Fast Forward) Summary Table

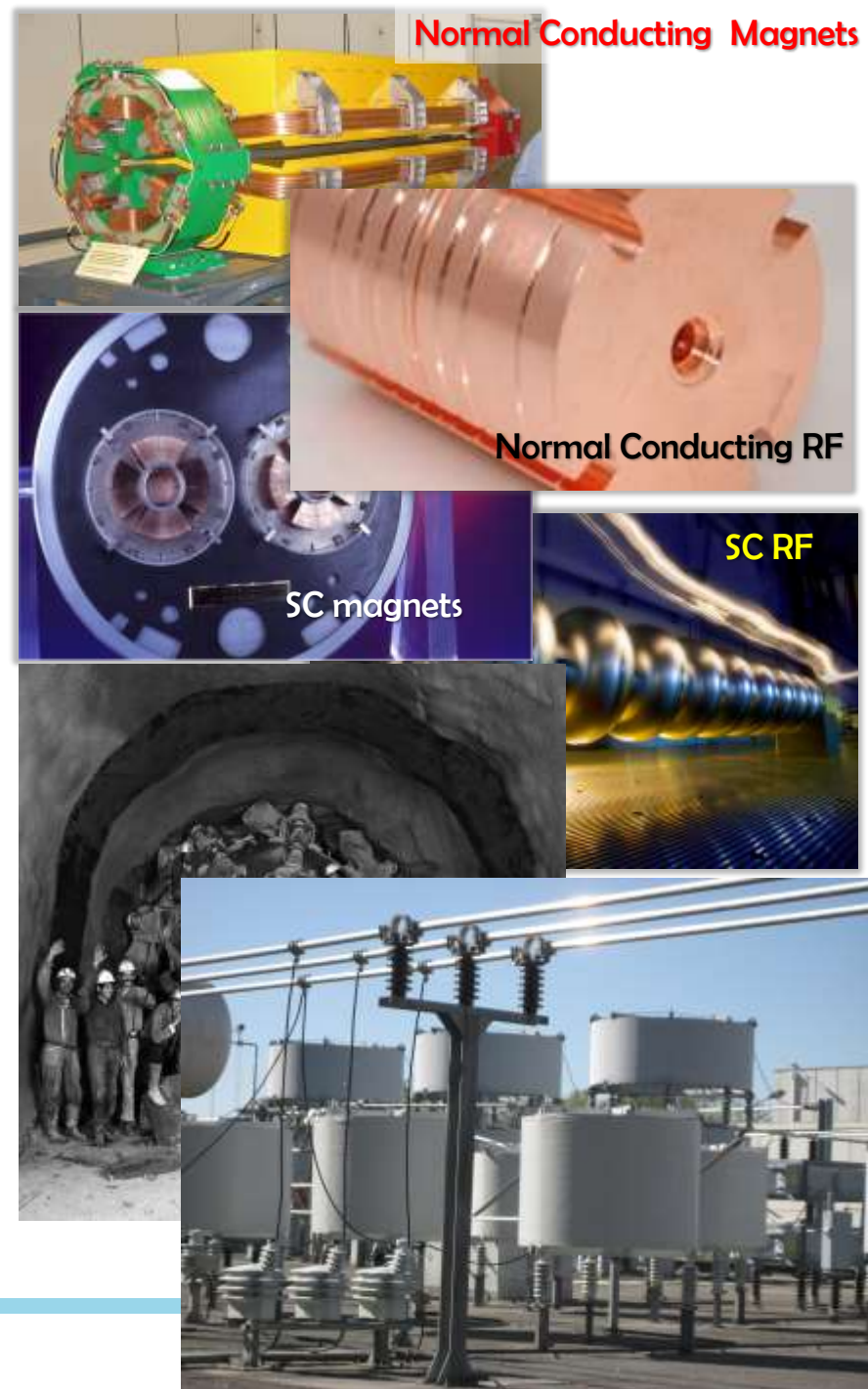
$\alpha\beta\gamma$  - Model



|                    | Civil (km)         | E_rf (TeV) | E_mag (TeV) | Site P (MW) | Cost* (LHCU) |
|--------------------|--------------------|------------|-------------|-------------|--------------|
| XFEL               | 3.3                | 0.017      | 0           | 15          | 0.25 ±0.1    |
| LHC* (green field) | 45                 | 0          | 14.5        | 230         | 1.4 ±0.4     |
| LHC project        | 0 <sub>+6</sub>    | 0          | 14          | 120         | <b>1.00</b>  |
| ILC-Higgs          | 21 <sub>+3</sub>   | 0.25       | 0           | 129         | 0.9 ±0.3     |
| CLIC - tt          | 11 <sub>+6</sub>   | 0.38       | 0           | 168         | 1.0 ±0.3     |
| CLIC-3             | 54 <sub>+6</sub>   | 3          | 0           | 580         | 2.9 ±0.9     |
| FCCee              | 100 <sub>+20</sub> | 0.016      | 0.24        | 282         | 1.3 ±0.4     |
| FCChh*(no FCCee)   | 100 <sub>+20</sub> | 0.01       | 100         | 580         | 3.4 ± 1.1    |
| FCChh after FCCee  | 0                  | 0.01       | 100         | 580         | 2.8 ±0.9     |
| MC-HF              | 0.3 <sub>+3</sub>  | 0.02       | 0.13        | 200         | 0.6 ±0.2     |
| MC-3               | 4.5 <sub>+7</sub>  | 0.06       | 3           | 230         | 1.2 ±0.3     |
| MC-10 base         | 10 <sub>+7</sub>   | 0.07       | 10          | 310         | 1.5 ±0.5     |
| MC-10* max (M.P.)  | 10 <sub>+59</sub>  | 0.13       | 10          | 310         | 1.8 ±0.5     |
| MC-14* rcs-LHC tun | 0                  | 0.03       | 14          | 340         | 1.4 ±0.4     |

# Intro: Cost

- Cost is set by technology
  - *Accelerator technology* (magnets NC and SC, RF and SCRF)
  - *Civil construction technology*
  - *Power production, delivery and distribution technology*



# 2014 Cost analysis:

## 17 “Data Points” - Costs of Big Accelerators:

- Actually built:
  - RHIC, MI, SNS, LHC
- Under construction:
  - XFEL, FAIR, ESS
- Not built but costed:
  - SSC, VLHC, NLC
  - ILC, TESLA, CLIC, Project-X, Beta-Beam, SPL, v-Factory

## Wide range :

- 4 orders in Energy, >1 order in Power, >2 orders in Length
- Almost 2 orders in cost
  - (normalized to US TPC)

|           | Cost (B\$)<br>Year    | Energy<br>(TeV) | Accelerator<br>technology | Comments  | Length<br>(km) | Site<br>power<br>(MW) | TPC<br>range<br>(Y14 B\$) |
|-----------|-----------------------|-----------------|---------------------------|---|----------------|-----------------------|---------------------------|
| SSC       | 11.8 B\$<br>(1993)    | 40              | SC Mag                    | Estimates changed many times [6–8]                                    | 87             | ~ 100                 | 19–25                     |
| FNAL MI   | 260M\$<br>(1994)      | 0.12            | NC Mag                    | “old rules”, no OH, existing injector [9]                             | 3.3            | ~ 20                  | 0.4–0.54                  |
| RHIC      | 660M\$<br>(1999)      | 0.5             | SC Mag                    | Tunnel, some infrastructure, injector re-used [10]                    | 3.8            | ~ 40                  | 0.8–1.2                   |
| TESLA     | 3.14 B€<br>(2000)     | 0.5             | SC RF                     | “European accounting” [11]  | 39             | ~ 130                 | 11–14                     |
| VLHC-I    | 4.1 B\$<br>(2001)     | 40              | SC Mag                    | “European accounting”, existing injector [12]                         | 233            | ~ 60                  | 10–18                     |
| NLC       | ~ 7.5 B\$<br>(2001)   | 1               | NC RF                     | ~ 6 B\$ for 0.5 TeV collider. [13]                                    | 30             | 250                   | 9–15                      |
| SNS       | 1.4 B\$<br>(2006)     | 0.001           | SC RF                     | [14]  | 0.4            | 20                    | 1.6–1.7                   |
| LHC       | 6.5 BCHF<br>(2009)    | 14              | SC Mag                    | collider only — existing injector, tunnel & infrstr., no OH, R&D [15] | 27             | ~ 40                  | 7–11                      |
| CLIC      | 7.4–8.3B<br>CHF(2012) | 0.5             | NC RF                     | “European accounting” [16]  | 18             | 250                   | 12–18                     |
| Project X | 1.5 B\$<br>(2009)     | 0.008           | SC RF                     | [17]  | 0.4            | 37                    | 1.2–1.8                   |
| XFEL      | 1.2 B€<br>(2012)      | 0.014           | SC RF                     | in 2005 prices, “European accounting” [18]                            | 3.4            | ~ 10                  | 2.9–4.0                   |
| NuFactory | 4.7–6.5 B€<br>(2012)  | 0.012           | NC RF                     | Mixed accounting, w. contingency [19]                                 | 6              | ~ 90                  | 7–11                      |
| Beta-Beam | 1.4–2.3 B€<br>(2012)  | 0.1             | SC RF                     | Mixed accounting, w. contingency [19]                                 | 9.5            | ~ 30                  | 3.7–5.4                   |
| SPL       | 1.2–1.6 B€<br>(2012)  | 0.005           | SC RF                     | Mixed accounting, w. contingency [19]                                 | 0.6            | ~ 70                  | 2.6–4.6                   |
| FAIR      | 1.2 B€<br>(2012)      | 0.003–0.08      | SC Mag                    | “European accounting” [20], 6 rings, existing injector                | ~ 3            | ~ 30                  | 1.8–3.0                   |
| ILC       | 7.8 B\$<br>(2013)     | 0.5             | SC RF                     | “European accounting” [21]  | 34             | 230                   | 13–19                     |
| ESS       | 1.84 B€<br>(2013)     | 0.0025          | SC RF                     | “European accounting” [22, 23]  | 0.4            | 37                    | 2.5–3.8                   |



# Methodology of the $\alpha\beta\gamma$ – Model

- **Adjust all costs to TPC (US accounting)**
  - usually, btw 1.9 to 2.4 x European Accounting
- **Break TPC in just three parts (with sum = total)**
  - “Tunnels” (civil construction and siting)
  - “Accelerator systems” (SC and/or NC RF, Magnets)
  - “Power” (site, cryo, generators/converters/distribution, etc)
- **Scale each part with two parameters:  $a_{L,E,P}$  and  $b_{L,E,P}$** 
  - $L$  (in 10 km units),  $E$  (in TeV of cme),  $P$  (in 100 MW)

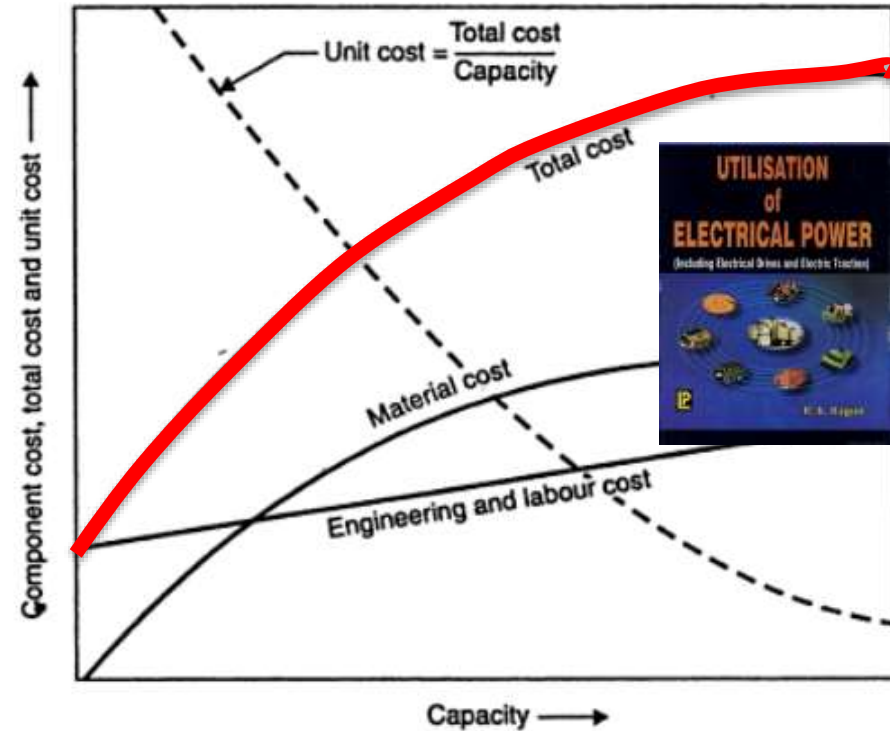
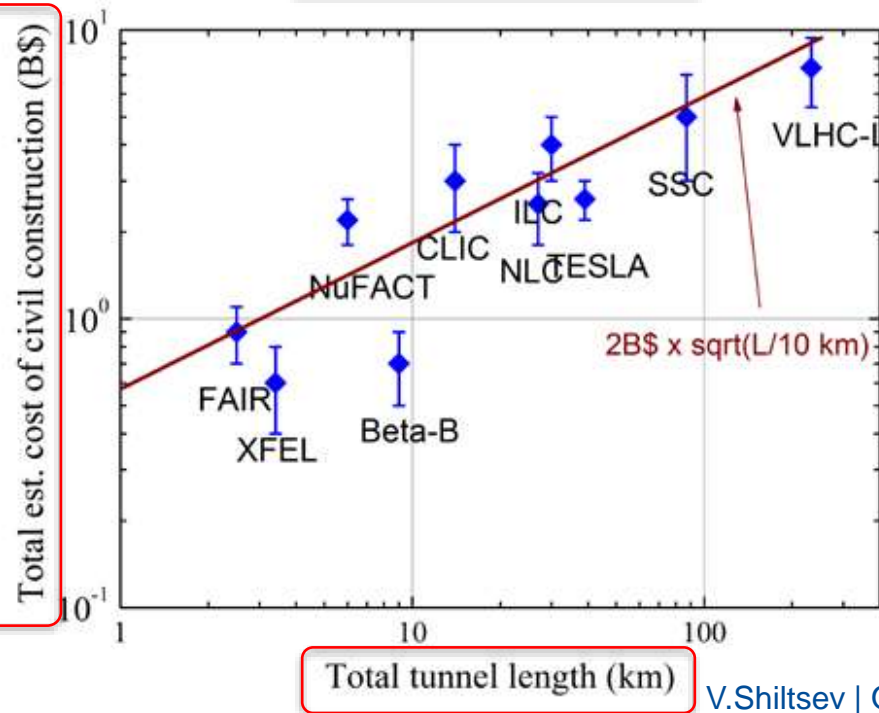
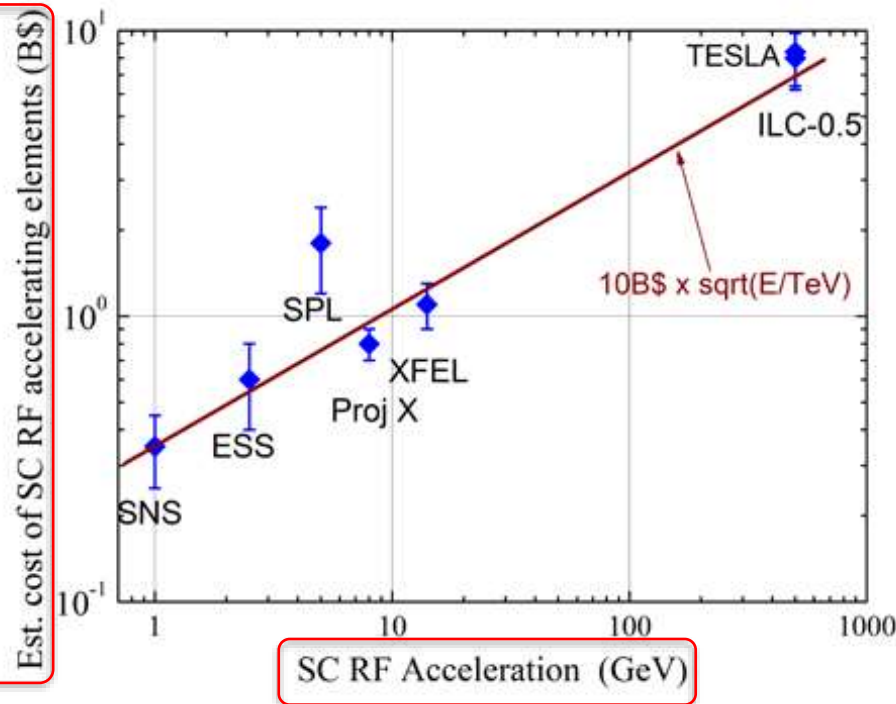
$$TPC = a_L \left( \frac{L}{10\text{km}} \right)^{b_L} + a_E \left( \frac{E}{1\text{TeV}} \right)^{b_E} + a_P \left( \frac{P}{100\text{MW}} \right)^{b_P}$$

- **(Simplify to SQRT and round up... set all  $b_{L,E,P} = 1/2$  )**
  - as they were typically found btw 0.4 and 0.6

# Illustrations

## Comment:

*Sqrt*-functions are quite accurate over wide range because such dependence well approximates the “initial cost” – effect :



# ! WARNING !

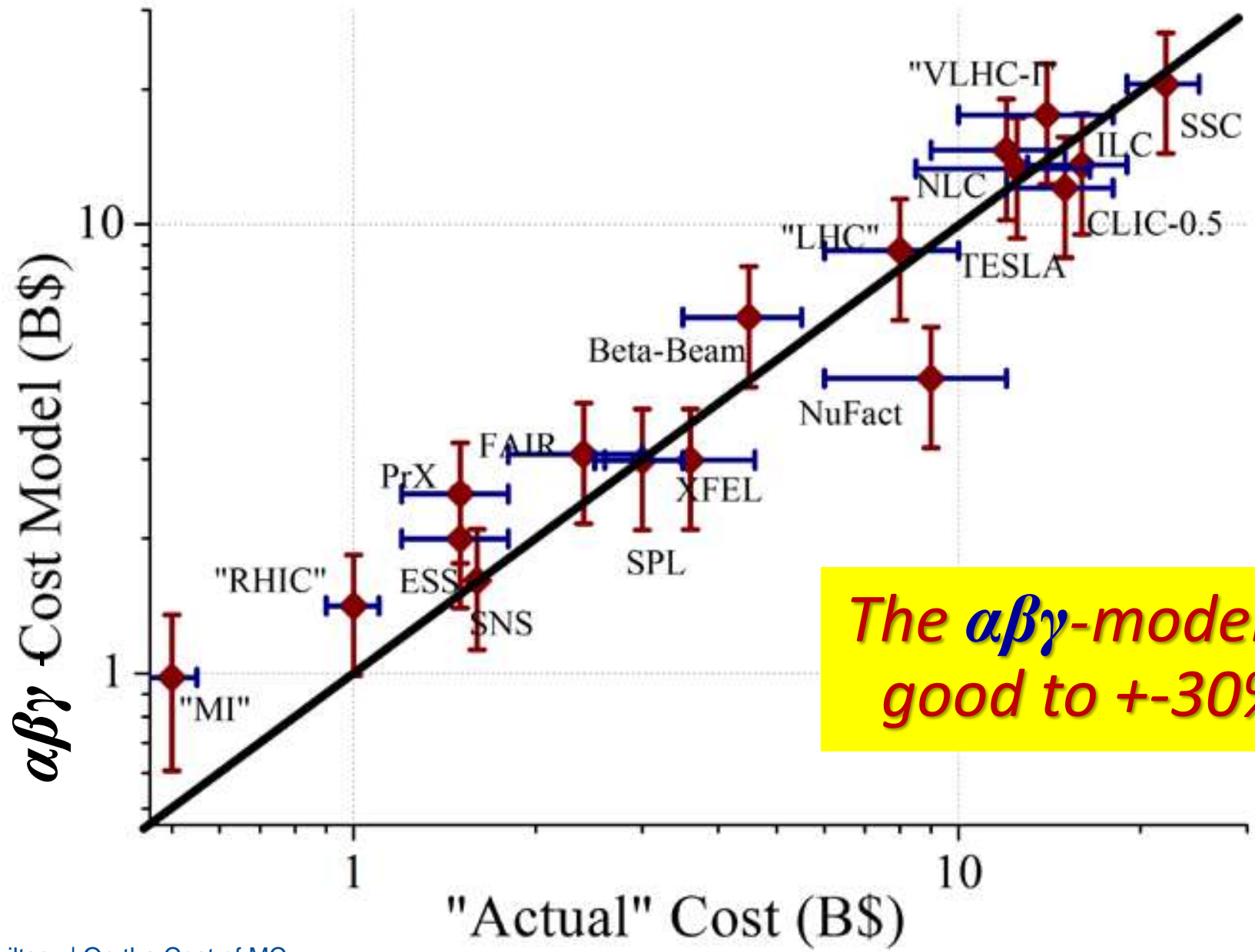
The  $\alpha\beta\gamma$  cost model:

$$\text{Cost(TPC)} = \alpha L^{1/2} + \beta E^{1/2} + \gamma P^{1/2}$$

- a) Is for a “green field” facility !
- b) US-Accounting !
- c) There is hidden correlation btw  $E$  and technology progress
- d) Pay attention to units (10 km for  $L$ , 1 TeV for  $E$ , 100 MW for  $P$ )
  - $\alpha \approx 2\text{B}\$/\text{sqrt}(L/10 \text{ km})$
  - $\beta \approx 10\text{B}\$/\text{sqrt}(E/\text{TeV})$  for SC/NC RF
  - $\beta \approx 2\text{B}\$ /\text{sqrt}(E/\text{TeV})$  for SC magnets
  - $\beta \approx 1\text{B}\$ /\text{sqrt}(E/\text{TeV})$  for NC magnets
  - $\gamma \approx 2\text{B}\$/\text{sqrt}(P/100 \text{ MW})$

# USE AT YOUR OWN RISK!

# Total Cost vs $\alpha\beta\gamma$ -Model (Log-Log)



*The  $\alpha\beta\gamma$ -model is good to +/-30%*



# Take LHC as an Example:

- **$\alpha\beta\gamma$  – Model:**

- 40 km of tunnels
- 14 TeV c.o.m SC magnets
- ~150 MW of site power

$$2\sqrt{40/10} = 4$$

$$2\sqrt{14} = 7.5$$

$$2\sqrt{150/100} = 2.5$$

TOTAL PROJECT COST : **14B\$ ± 4.5B\$**

- **ITF T.Roser talk @ PLUB-II (USD 2021):**

- existing injector complex **4.6 B\$**
- new accelerator systems **4.06 B\$**
- new infrastructure and civil **2.75 B\$**
- explicit labor **~1.4 B\$**

**Total: 12.8B\$**

# Future Colliders w.r.t. LHC

$\alpha\beta\gamma$  - Model



|                    | Civil (km)         | E_rf (TeV) | E_mag (TeV) | Site P (MW) | Cost* (LHCU)   | Cost Reported |
|--------------------|--------------------|------------|-------------|-------------|----------------|---------------|
| XFEL               | 3.3                | 0.017      | 0           | 15          | $0.25 \pm 0.1$ | 1.7 BEUR      |
| LHC* (green field) | 27 <sub>+28</sub>  | 0          | 14.5        | 230         | $1.4 \pm 0.4$  | 13-15 B?      |
| LHC project        | 0 <sub>+6</sub>    | 0          | 14          | 120         | <b>1.00</b>    | 8-10 B?       |
| ILC-Higgs          | 21 <sub>+3</sub>   | 0.25       | 0           | 129         | $0.9 \pm 0.3$  | 7 kOKU        |
| CLIC - tt          | 11 <sub>+6</sub>   | 0.38       | 0           | 168         | $1.0 \pm 0.3$  | 5.9 BCHF      |
| CLIC-3             | 54 <sub>+6</sub>   | 3          | 0           | 580         | $2.9 \pm 0.9$  | 18.9 BCHF     |
| FCCee              | 100 <sub>+20</sub> | 0.016      | 0.24        | 282         | $1.3 \pm 0.4$  | 10.8 BCHF     |
| FCChh*(no FCCee)   | 100 <sub>+20</sub> | 0.01       | 100         | 580         | $3.4 \pm 1.1$  | 24 BCHF       |
| FCChh after FCCee  | 0                  | 0.01       | 100         | 580         | $2.8 \pm 0.9$  | 17 BCHF       |
| MC-HF              | 0.3 <sub>+3</sub>  | 0.02       | 0.13        | 200         | $0.6 \pm 0.2$  | ?             |
| MC-3               | 4.5 <sub>+7</sub>  | 0.06       | 3           | 230         | $1.2 \pm 0.3$  | ?             |
| MC-10 base         | 10 <sub>+7</sub>   | 0.07       | 10          | 310         | $1.5 \pm 0.5$  | ?             |
| MC-10 max M.P.     | 10 <sub>+59</sub>  | 0.13       | 10          | 310         | $1.8 \pm 0.5$  | ?             |
| MC-14* rcs-LHC tun | 0                  | 0.03       | 14          | 340         | $1.4 \pm 0.4$  | ?             |

# “ $\alpha\beta\gamma$ – Model” : Notes

- Costs of future technologies are not well known:
  - plasma, lasers, crystals, “magic cheap” magnets, tunnels, HTS, etc
- Costs of civil construction and power systems are driven by larger economy (not by us)... “stable”
- Having injector/reuse infrastructure helps a lot (~1/3 of cost)
- Follows from the model:
  - Cost is weak function of luminosity (see next slide)
    - Also, LHC 10B\$, HL-LHC 1B\$ with x5 increase in luminosity
    - It’s OK to start high  $E$ , low  $L$ ...CESR, Tevatron increased  $L$  >100x, LHC >10x
  - Cost is moderate function of length/circumference
  - Cost is strong function of  $E$ nergy and technology
- Of course, the model error bars are large (range of ~2) but at least allows approximately sort proposals in categories
  - E.g., “Less than LHCU”, “1-2 LHCU”, “More than 3 LHCU”, etc

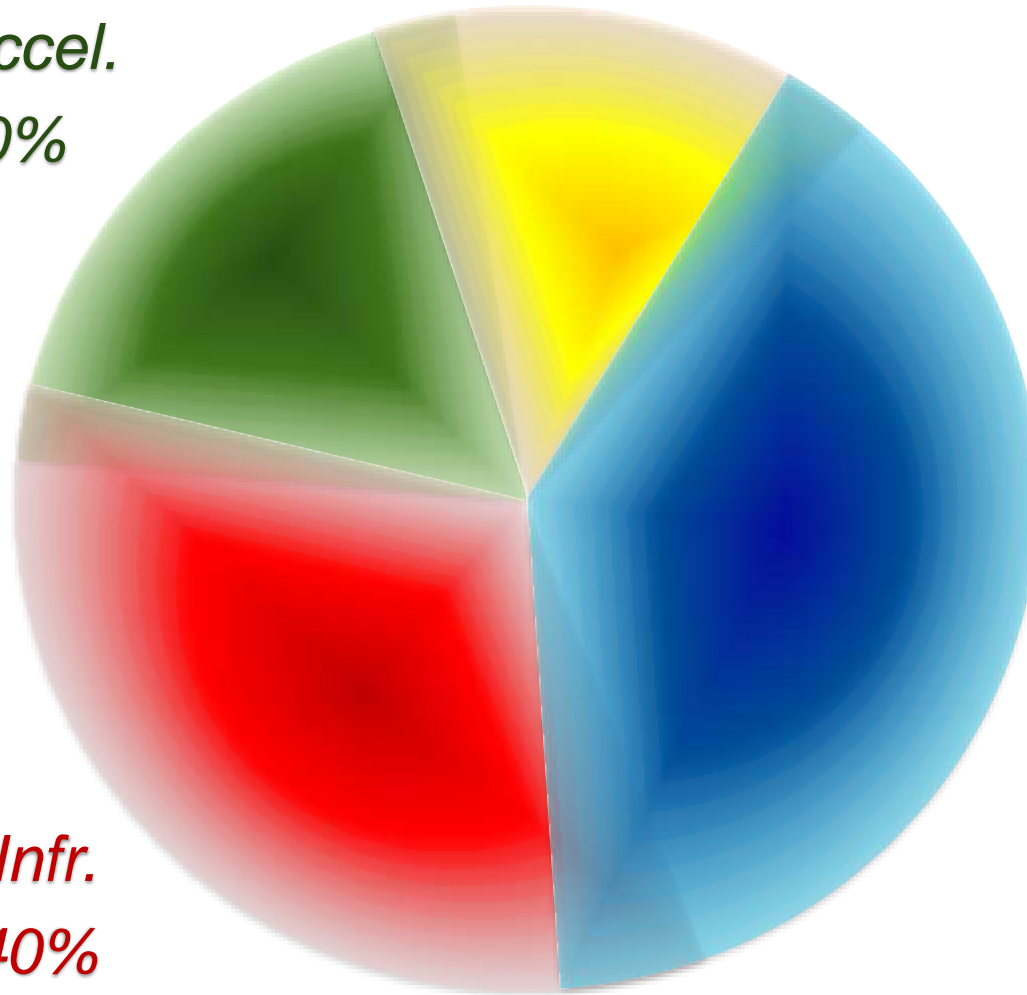
# “ $\alpha\beta\gamma$ – Model” : 10 TeV Muon Collider

*Civil 10-16%*

*RF Accel.  
15-20%*

*Magnets  
30-45%*

*Power Infr.  
25-40%*





# “ $\alpha\beta\gamma$ – Model” : Caveats

- “*Non-uniformity*”: machine costs estimated by proponents and in variable methodologies
- Analysis was done in 2013:
  - *many more projects have been costed since then*: FCCee, FCChh, CepC, SPPC, LHeC, NICA, PIP-II, EIC, LCLS-II & HE, HL-LHC
  - *others updated or finished*: XFEL, SwissFEL, FRIB, ESS, FAIR, ILC, CLIC
  - *inflation 7yrs x 3% = 21%... varies by region*
- Analysis to be updated for the *Snowmass’21*:
  - *As part of the* AF Implementation Task Force
  - Scaling *and* relative weights of cost factors

**BACK UP SLIDES**