

# A dynamically initialized hybrid approach with varying equations of state

Renan Hirayama<sup>12</sup>, Zuzana Paulínyová<sup>23</sup>, and Hannah Elfner<sup>124</sup>

<sup>1</sup>Helmholtz Research Academy Hesse (HFHF), GSI Helmholtz Center, Max-von-Laue-Str. 12, 60438 Frankfurt am Main

<sup>2</sup>Frankfurt Institute for Advanced Studies (FIAS), Ruth-Moufang-Straße 1, 60438 Frankfurt am Main

<sup>3</sup>Faculty of Science, P. J. Šafárik University, Košice, Slovakia

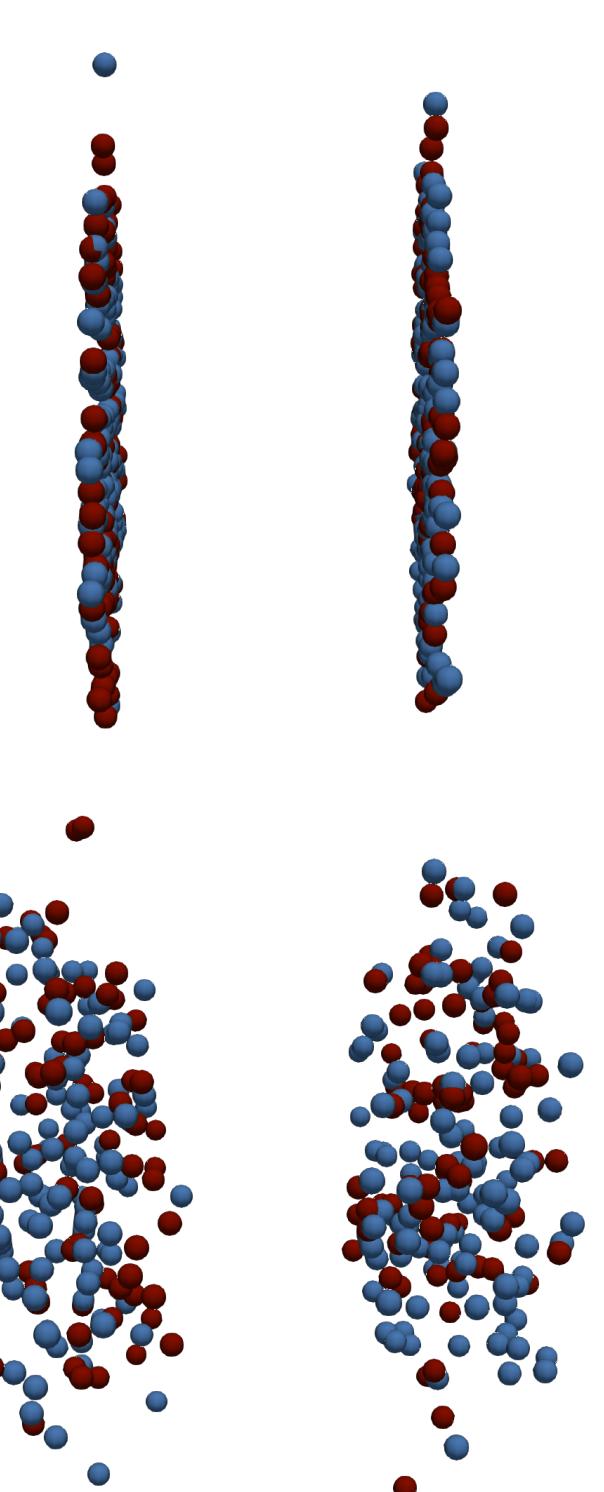
<sup>4</sup>GSI Helmholtzzentrum für Schwerionenforschung, Planckstraße 1, 64291 Darmstadt

## Initialization of hybrid models

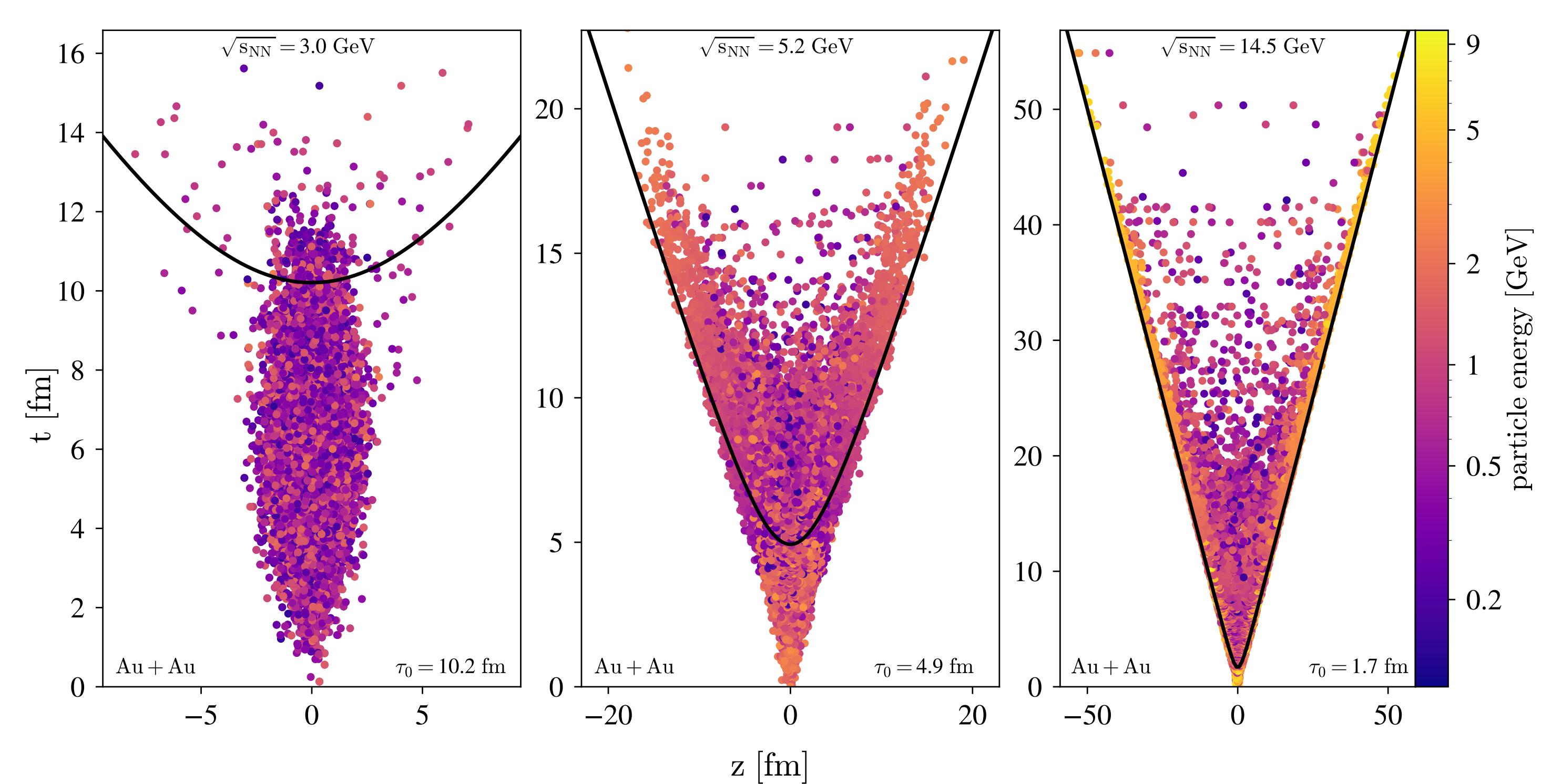
- In high beam energy heavy ion collisions, the traditional initialization for hydrodynamics is at the crossing of iso- $\tau_0$  hypersurface. A common choice is the passing time

$$\tau_0 = 2m_N \frac{R_{\text{proj}} + R_{\text{targ}}}{\sqrt{s_{\text{NN}} - 4m_N^2}}$$

- Centrality determination makes core-corona (dense-dilute) separation necessary
- Low energies  $\rightarrow$  nonequilibrium, secondary interactions, larger nuclei passing time
- Goal: dynamical condition for fluidization based on local energy density



## Dynamic fluidization



- At lower energies, fluidization happens way before  $\tau_0$  🤝
- As the beam energy increases, so does the energy of particles entering hydro; more important sources are closer to the iso- $\tau_0$  hypersurface 🤝
- Spread depends on threshold energy and formation time 😊

## SMASH

Simulating Many Strongly-interacting Hadrons

- Evolve hadrons according to the Boltzmann equation [1]
- Particle in energetic enough region  $\rightarrow$  fluidization
- Following [2], only hadronic or string decay products ?
- Threshold condition determined at production, but fluidization happens at formation time
- Background from fluid  $T^{00}$  not included yet !

## vHLL

viscous Harten-Lax-van Leer-Einfeldt algorithm

- Israel-Stewart equations of motion with viscosity [3]
- Matching time steps with transport requires Cartesian coordinates
- Fluidized particles enter as smeared sources (Z. Paulínyová's poster)

$$J^\mu(\mathbf{r}) = \frac{1}{\Delta t} \sum_i p_i^\mu K(\mathbf{r} - \mathbf{r}_i)$$

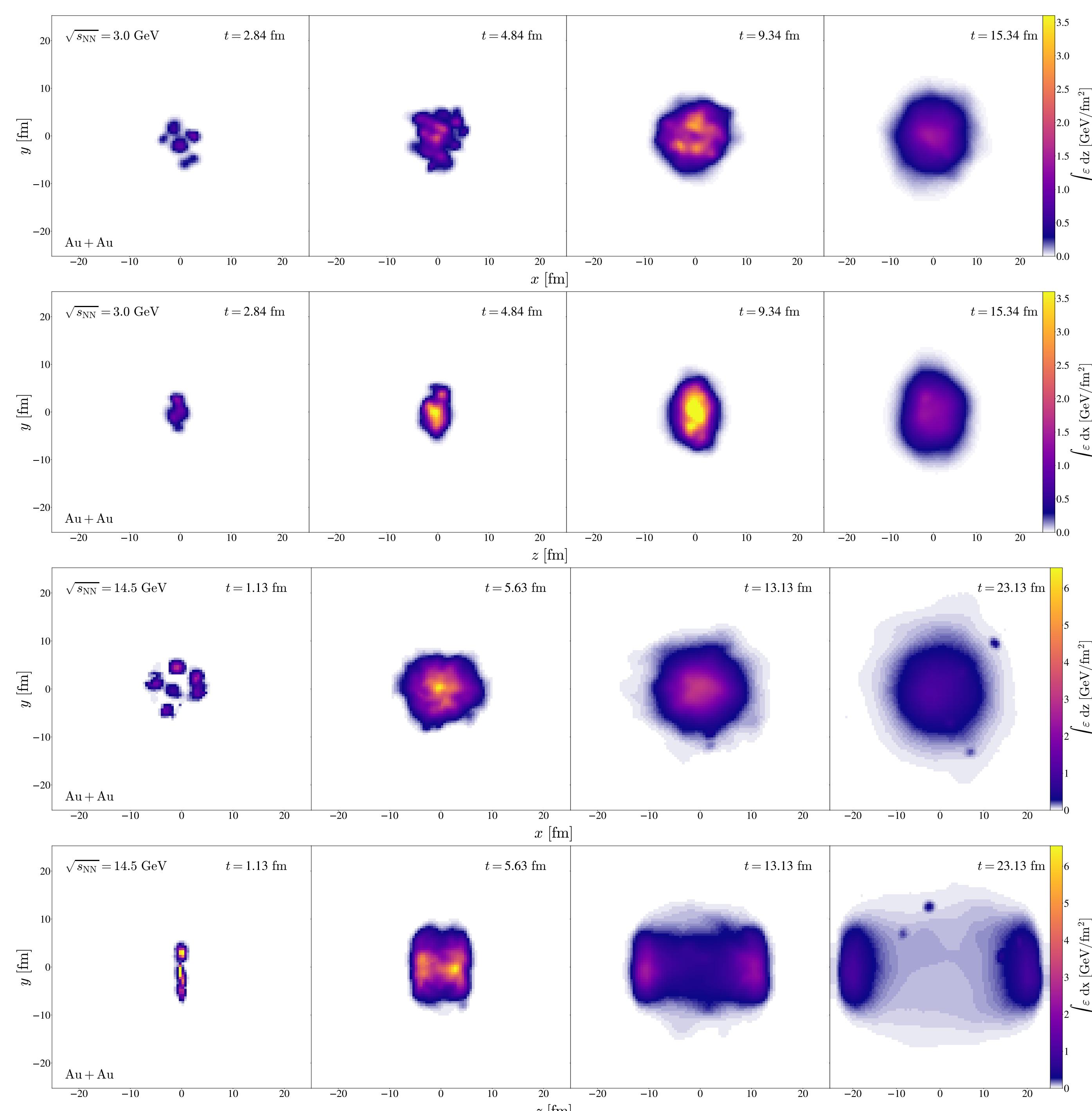
$$T^{\mu\nu}(\mathbf{r}) = \sum_i \frac{p_i^\mu p_i^\nu}{p_i^0} K(\mathbf{r} - \mathbf{r}_i)$$

No particlization yet !

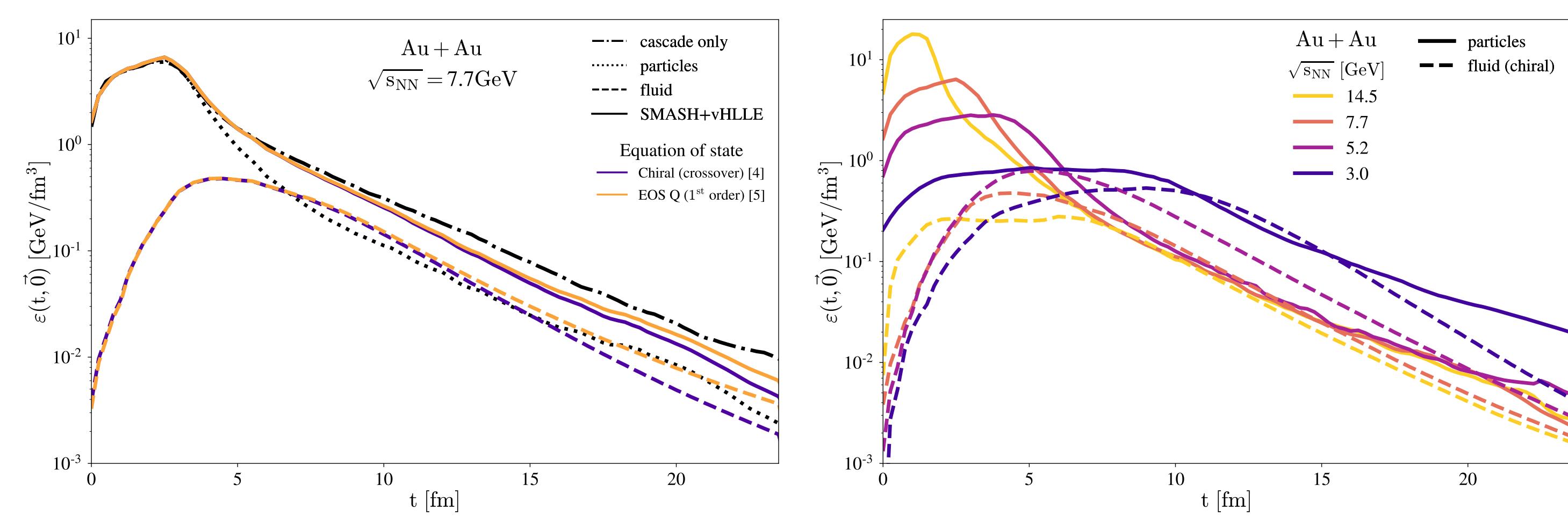
## Energy density profiles

- Au+Au collisions with  $b = 0$
- Threshold  $\epsilon_f = 0.5 \text{ GeV}/\text{fm}^3$

- Viscosity  $\eta/s = 0.2$ ,  $\zeta/s = 0$
- Smearing parameter  $\sigma = 1 \text{ fm}$

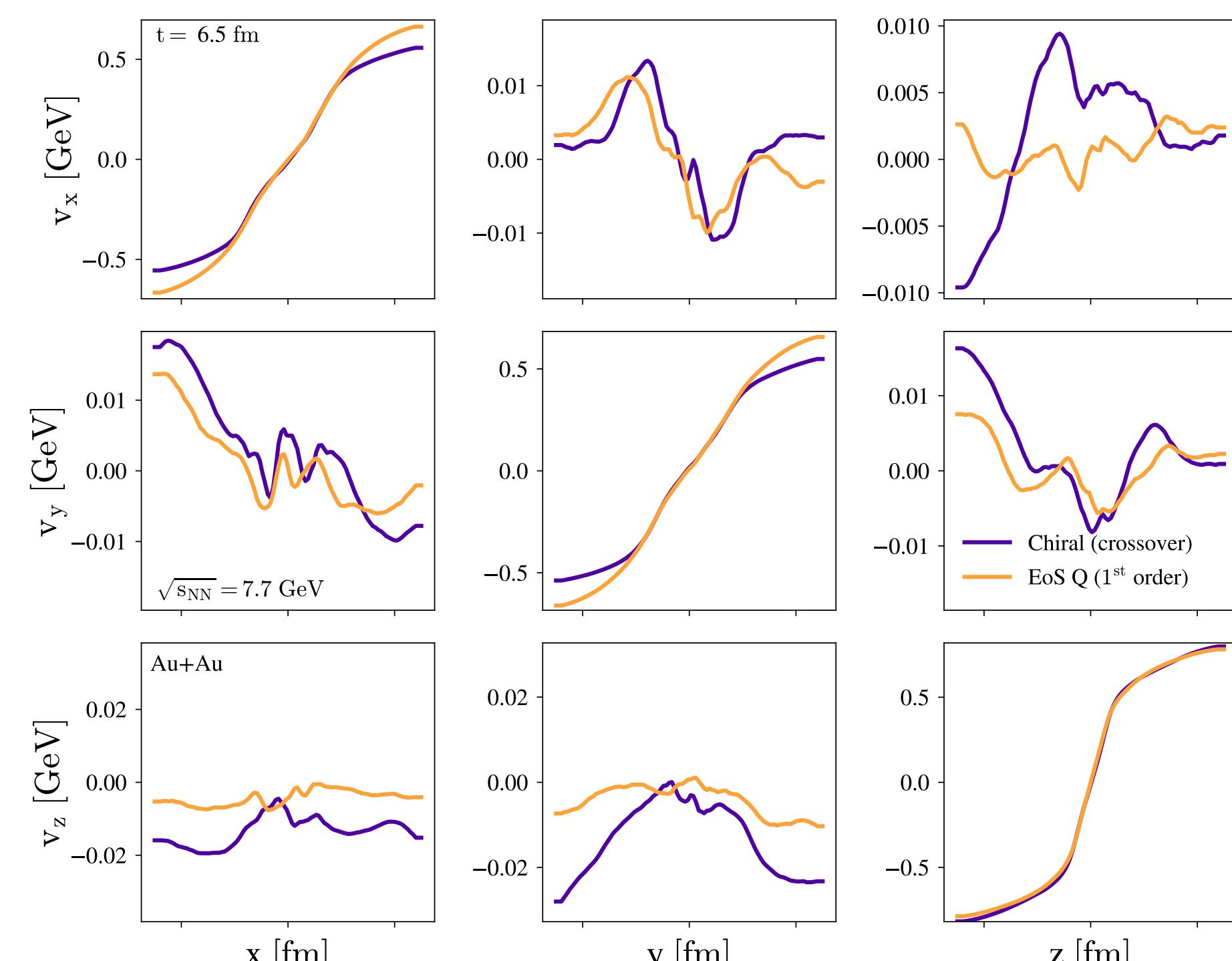


## Central cell evolution



- Less  $\varepsilon$  at center than cascade mode ↴ faster expansion?
- Small difference between EoS:  $\varepsilon$  includes compression energy
- Higher  $\sqrt{s_{\text{NN}}}$   $\Rightarrow$  faster fluidization
- Fast beams expand away quickly
- Contribution depends on which particles are chosen to fluidize

## Fluid velocities



## Outlook

- Allow different particles to fluidize
- Vary threshold energy and formation time
- Communication between energy density backgrounds for concurrent evolution
- Particle sampling to compute observables
- Radial and anisotropic flow may be sensitive to EoS and phase transition

## References

- [1] J. Weil, et al., PRC 94.5 (2016) 054905.
- [2] Y. Akamatsu, et al., PRC 98.2 (2018) 024909.
- [3] Iu. Karpenko, P. Huovinen, and M. Bleicher, Comput. Phys. Commun. 185.11 (2014) 3016-3027.
- [4] J. Steinheimer, S. Schramm, and H. Stöcker, J. Phys. G 38.3 (2011) 035001.
- [5] P.F. Kolb, J. Sollfrank, and U. Heinz, PRC 62.5 (2000) 054909.