

Dynamic mechanisms for shadowing



AoF CoE in
Quark Matter

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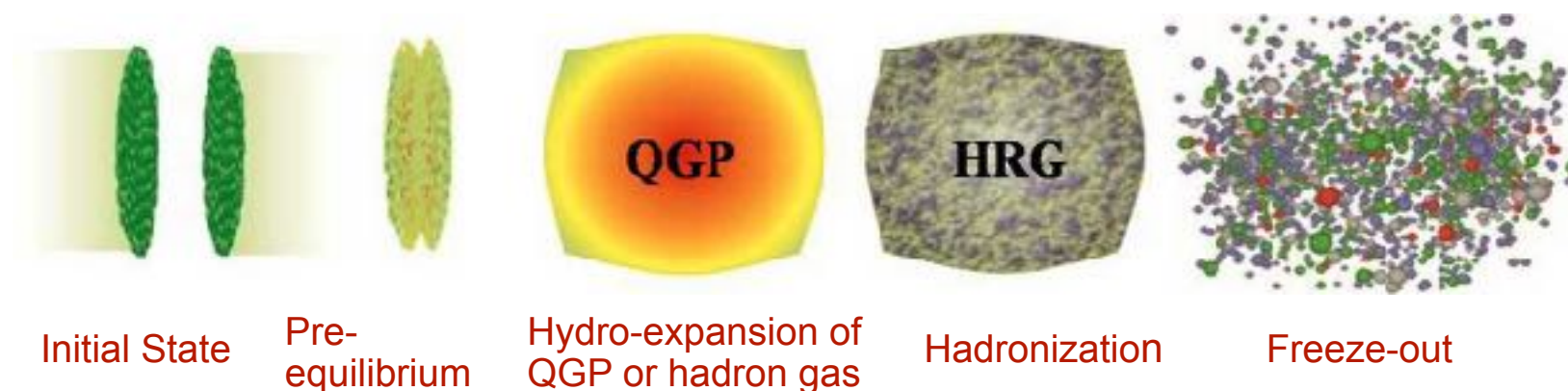
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Outline:

- Nuclear shadowing in scattering with nuclei
- Leading twist approximation for nuclear shadowing
- Nuclear shadowing in dipole picture
- Nuclear shadowing and saturation
- Summary and outlook

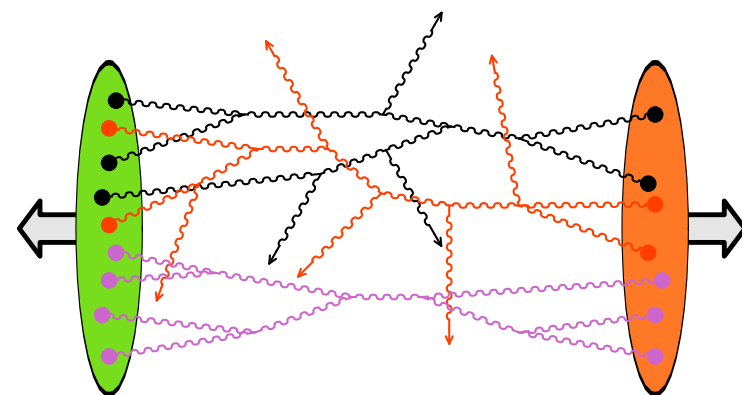
Nuclear shadowing in AA scattering

- **Nuclear shadowing (NS)** is general phenomenon of high-energy scattering → nuclear cross section $<$ sum of nucleon cross sections → nuclear parton distributions (nPDFs) $<$ sum of nucleon PDFs at small x .
- In context of nucleus-nucleus (AA) scattering → NS defines initial conditions (cold nuclear matter effects).



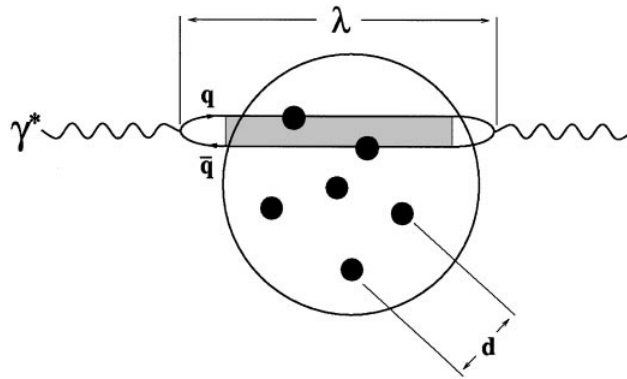
S. Bass,
Duke Univ.

- Fundamental in its own right (e.g. nPDFs) and also for description of onset of new states of matter → color glass condensate (CGC) and quark-gluon plasma (QGP).



Nuclear shadowing in $\gamma^{(*)}A$ scattering

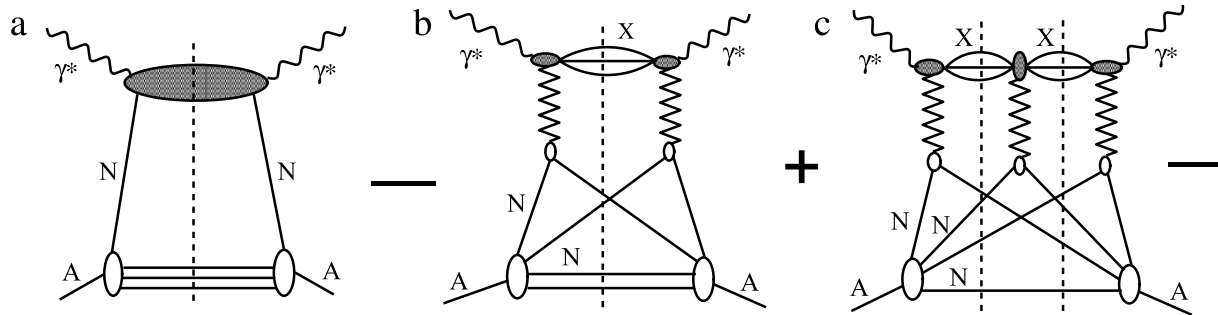
- Cleanest way to probe NS is using photons: real photons in UPCs at RHIC and LHC and virtual photons eA DIS with fixed targets and at EIC.
- In target rest frame, NS is due to multiple interactions of long-lived fluctuations of $\gamma^{(*)}$ with target nucleons \rightarrow destructive interference of amplitudes with $N=1,2,\dots,A$ nucleons \rightarrow nucleons geometrically shadow each other \rightarrow Gribov-Glauber (GG) theory of NS, [Glauber, PRD 50 \(1955\) 242](#); [Gribov, Sov. Phys. JETP 29 \(1969\) 483](#); [Frankfurt, Strikman, Phys. Rept. 160 \(1988\) 235](#); [Piller, Weise, Phys. Rept. 330 \(2000\) 1](#); [Armesto, J. Phys. G 32 \(2006\) R367](#).



- Soft processes: fluctuations are vector mesons (VMD model), [Bauer, Spital, Yennie, Pipkin, Rev. Mod. Phys. 50 \(1978\) 261](#) or generic hadronic states in Good-Walker picture, [Good, Walker, PR 120 \(1960\) 1857](#); [Blättet, Baym, Frankfurt, Heiselberg, Strikman, PRD 47 \(1992\) 2761](#).
- Hard processes: fluctuations are $q\bar{q}$, $q\bar{q}g, \dots$ QCD states (dipoles), [Nikolaev, Zakharov, Z. Phys. C 49 \(1991\) 607](#); [Mueller, NPB 415 \(1994\) 373](#).

Gribov-Glauber theory of nuclear shadowing

- Interactions with $N=1,2,3,..A$ target nucleons:

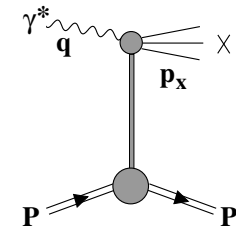


- Shadowing correction to total $\gamma^{(*)}A$ cross section, [Karmanov, Kondratyuk, JETP Lett. 18 \(1973\) 266](#); [Kaidalov et al, EPJ C 5 \(1998\) 111](#); [Piller, Weise, Phys. Rept. 330 \(2000\) 1](#)

$$\delta\sigma_{\gamma^*A} = -8\pi \int d^2b \int_{-\infty}^{+\infty} dz_1 \int_{z_1}^{+\infty} dz_2 \rho_A(\mathbf{b}, z_1) \rho_A(\mathbf{b}, z_2) \\ \times \int_{4m_\pi^2}^{W^2} dM_X^2 \cos[(z_2 - z_1)/\lambda] \left. \frac{d^2\sigma_{\gamma^*N}^{\text{diff}}}{dM_X^2 dt} \right|_{t \approx 0} \exp\left[-\frac{\sigma_{XN}}{2} \int_{z_1}^{z_2} dz \rho_A(\mathbf{b}, z) \right]$$

- Main feature: **$N=2$ contribution to NS in terms of diffraction on proton** \rightarrow consequence of unitarity (AGK cutting rules), [Abramovsky, Gribov, Kancheli, Sov. J. Nucl. Phys. 18 \(1974\) 308](#) \rightarrow elastic and inelastic intermediate states.

$$\sigma_{\text{eff}} = \frac{16\pi}{\sigma_{\gamma N}(1 + \eta^2)} \int_{4m_\pi^2}^{W^2} dM_X^2 \left. \frac{d^2\sigma_{\gamma^*N}^{\text{diff}}}{dM_X^2 dt} \right|_{t \approx 0}$$



GG shadowing in soft γA scattering

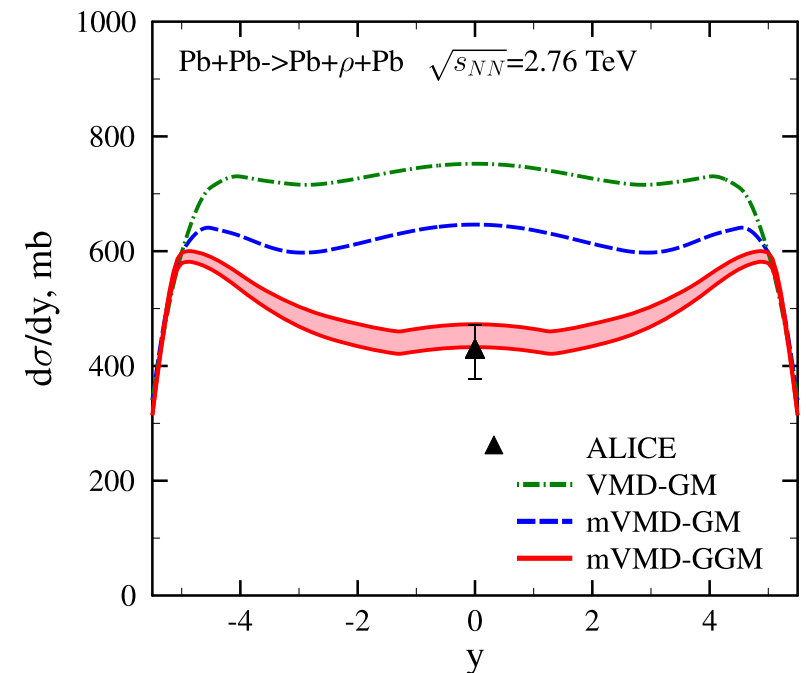
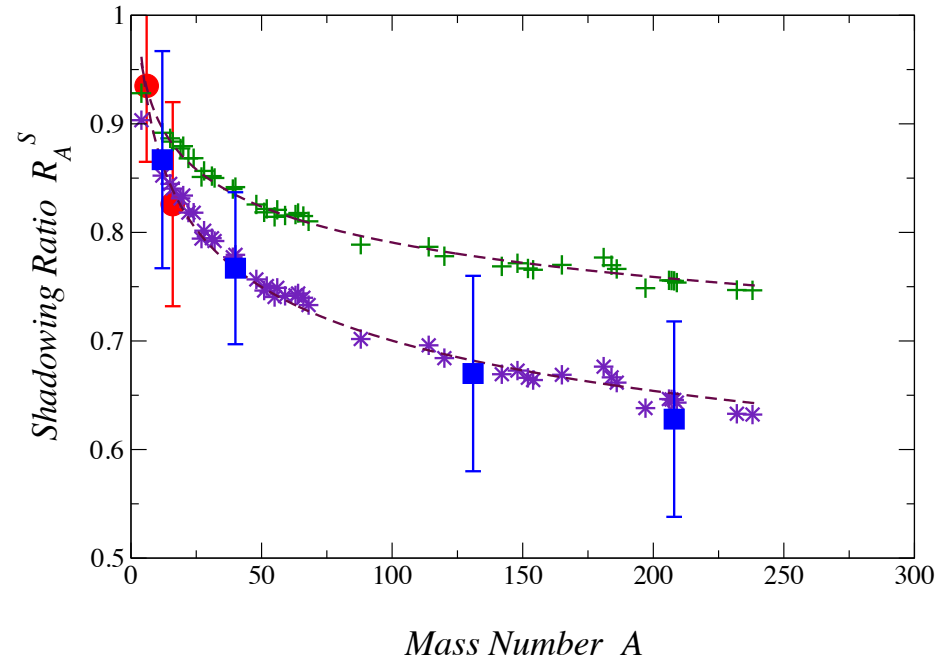
- Using data on diffraction of real photons to low and high diffractive masses $M_X \rightarrow$ good description of total γA cross section,

Adeluyi, Fai, PRC 74 (2006) 054904

- Account of hadronic fluctuations of real photons \rightarrow elastic (ρ) and inelastic intermediate states \rightarrow good description of Run 1,2 data on coherent ρ photoproduction in Pb-Pb UPCs@LHC,

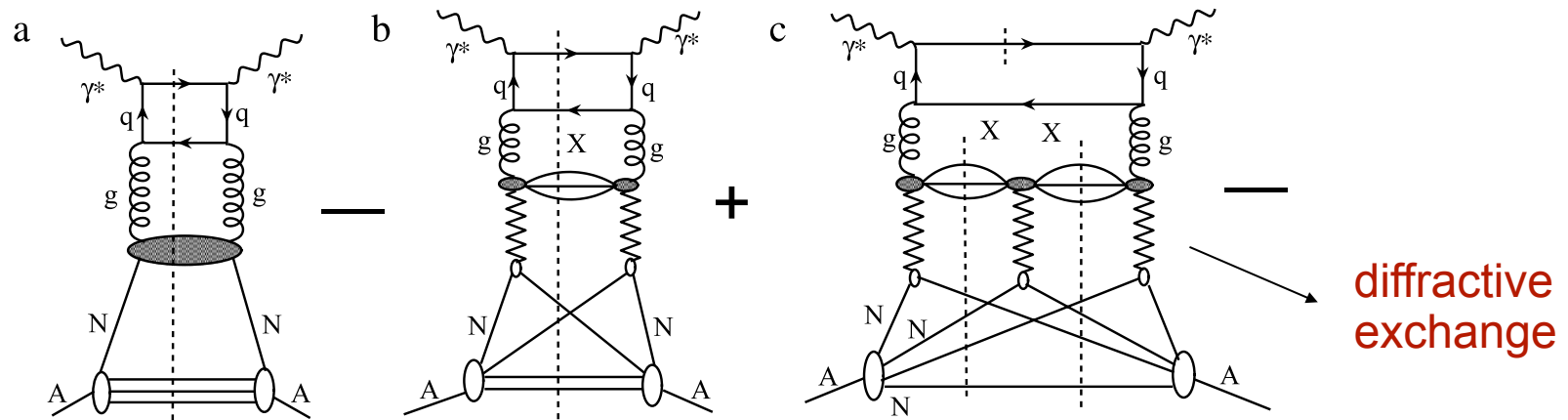
Frankfurt, Guzey, Strikman, Zhalov, PLB 752 (2016) 51; Guzey, Kryshen, Zhalov, PRC 102 (2020) 1, 015208

- Gribov (inelastic) shadowing correction is small for pA , noticeable for γA , and dominant (leading twist) for $\gamma^* A$.



Leading twist model of nuclear shadowing

- Combination of Gribov-Glauber theory with QCD factorization theorems for inclusive and diffractive DIS \rightarrow prediction for small- x nPDFs at input scale Q_0 , Frankfurt, Strikman, EPJ A5 (1999) 293; Frankfurt, Guzey, Strikman, Phys. Rept. 512 (2012) 255



$$xf_{j/A}(x, Q_0^2) = Axf_{j/N}(x, Q_0^2) - 8\pi A(A-1) \Re e \frac{(1-i\eta)^2}{1+\eta^2} B_{\text{diff}} \int_x^{0.1} dx_{\mathbb{P}} \beta f_j^{D(3)}(\beta, Q_0^2, x_{\mathbb{P}})$$

$j=q$ or g

$$\times \int d^2b \int_{-\infty}^{\infty} dz_1 \int_{z_1}^{\infty} dz_2 \rho_A(\vec{b}, z_1) \rho_A(\vec{b}, z_2) e^{i(z_1-z_2)x_{\mathbb{P}}m_N} e^{-\frac{A}{2}(1-i\eta)\sigma_{\text{soft}}^j(x, Q_0^2) \int_{z_1}^{z_2} dz' \rho_A(\vec{b}, z')}$$

nuclear density

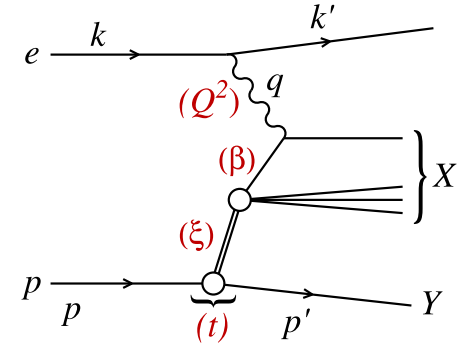
$N=2$ term: proton diffractive PDFs from HERA

$N \geq 3$ terms: model-dependent effective cross section

- Alternative to extraction of nPDFs using global QCD fits, Plenary talk on nPDFs, 23.06.

Leading twist model of nuclear shadowing (2)

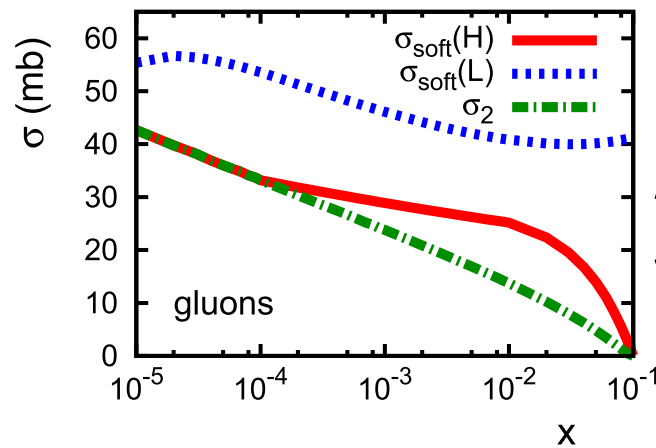
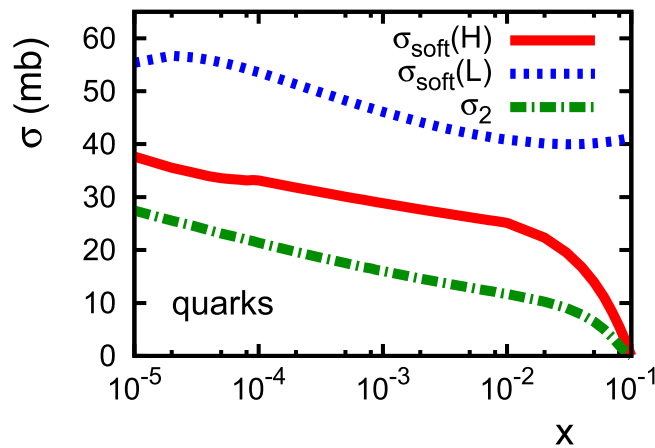
- Essential input: universal, leading twist (LT) diffractive PDFs of proton, [Collins, PRD 57, 3051 \(1998\); PRD 61, 019902 \(2000\)](#)
- Extracted from HERA data on diffraction in ep DIS, [Aktas et al \[H1\], EPJ C48, 715 \(2006\), EPJC 48, 749 \(2006\); Chekanov et al \[ZEUS\], NPB 831, 1 \(2010\)](#)



- Interaction with 2 nucleons model- independently in terms of diffractive (Pomeron) PDFs:

$$\sigma_2^j(x, Q^2) = \frac{16\pi}{(1 + \eta^2)x f_{j/N}(x, Q^2)} \int_x^{0.1} dx_{\mathbb{P}} \beta f_j^{D(4)}(\beta, Q^2, x_{\mathbb{P}}, t_{\min}).$$

- Interaction with $N \geq 3$ nucleons modeled using hadronic fluctuations of photon

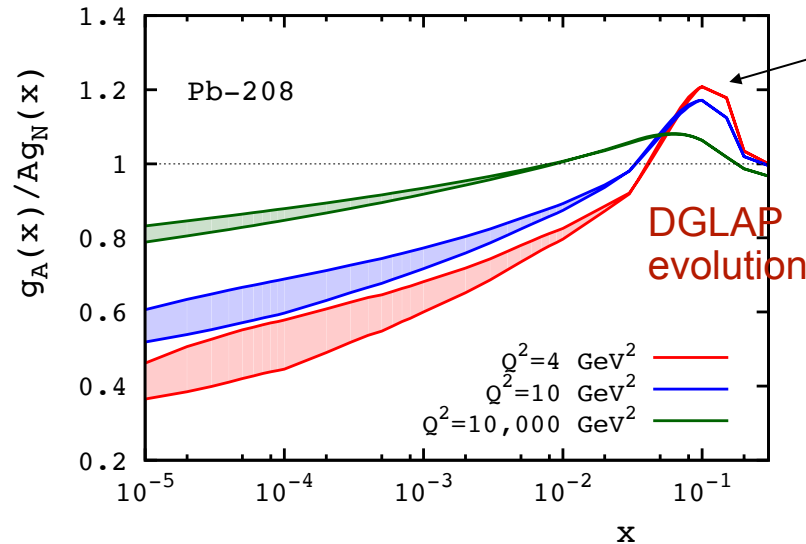
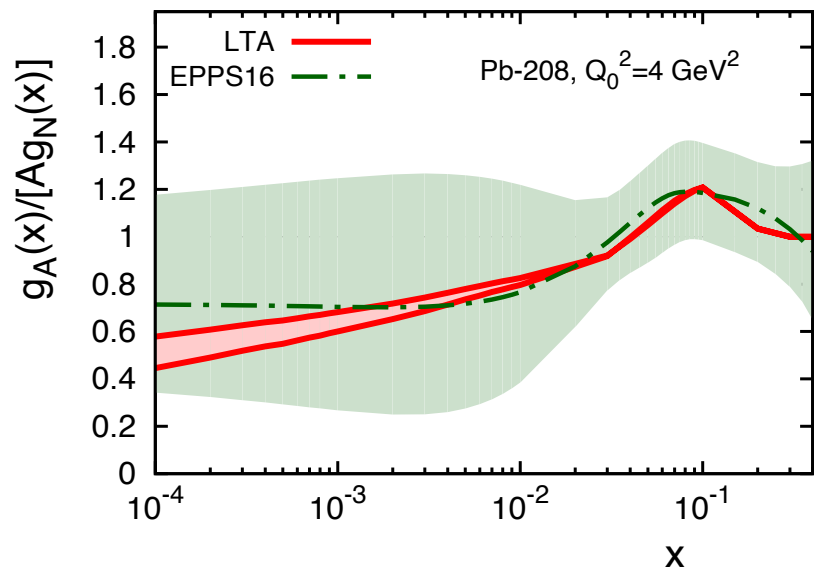


Spread in $\sigma_{\text{soft}} \rightarrow$ uncertainty of LTA predictions

- “LT” in the name comes from HERA analysis, but higher twist effects in diffraction at low Q_0 could be significant, [Motyka, Sadzikowski, Slominski, PRD 86 \(2012\) 111501; Maktoubian, Mehraban, Khanpour, Goharipour, PRD 100 \(2019\) 054020.](#)

LTA predictions for nPDFs

- HERA analysis: perturbative Pomeron is made mostly of gluons → LTA model naturally predicts large gluon nuclear shadowing, [Frankfurt, Guzey, Strikman, Phys. Rept. 512 \(2012\) 255](#)



Antishadowing from momentum sum rule.

Alternative: dynamic model, [Frankfurt, Guzey, Strikman, PRC 95 \(2017\) 1, 055208](#)

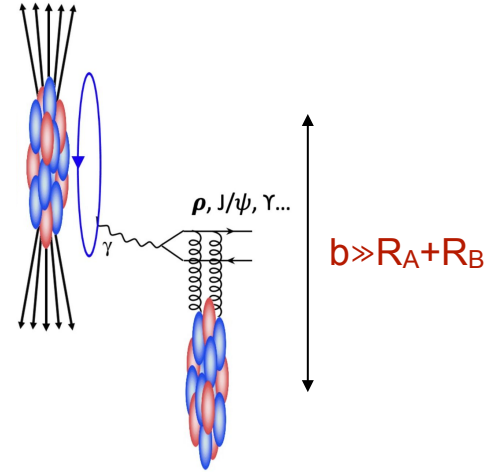
- Alternative, complementary point of view: shadowing is mixture of leading and higher twist (HT) effects in dipole picture with saturation, [Kowalski, Lappi, Venugopalan, PRL 100 \(2008\) 022303](#), or a purely HT effect, [Qiu, Vitev, PRL 93 \(2004\) 262301](#).

- Electron-Ion Collider has potential to discriminate models of NS due to:
 - wide x - Q^2 coverage
 - measurements of the longitudinal structure function $F_L^A(x, Q^2)$ sensitive to gluons
 - measurements of diffraction in eA DIS

Plenary talks on EIC, 23.06.

Nuclear shadowing in UPC at LHC

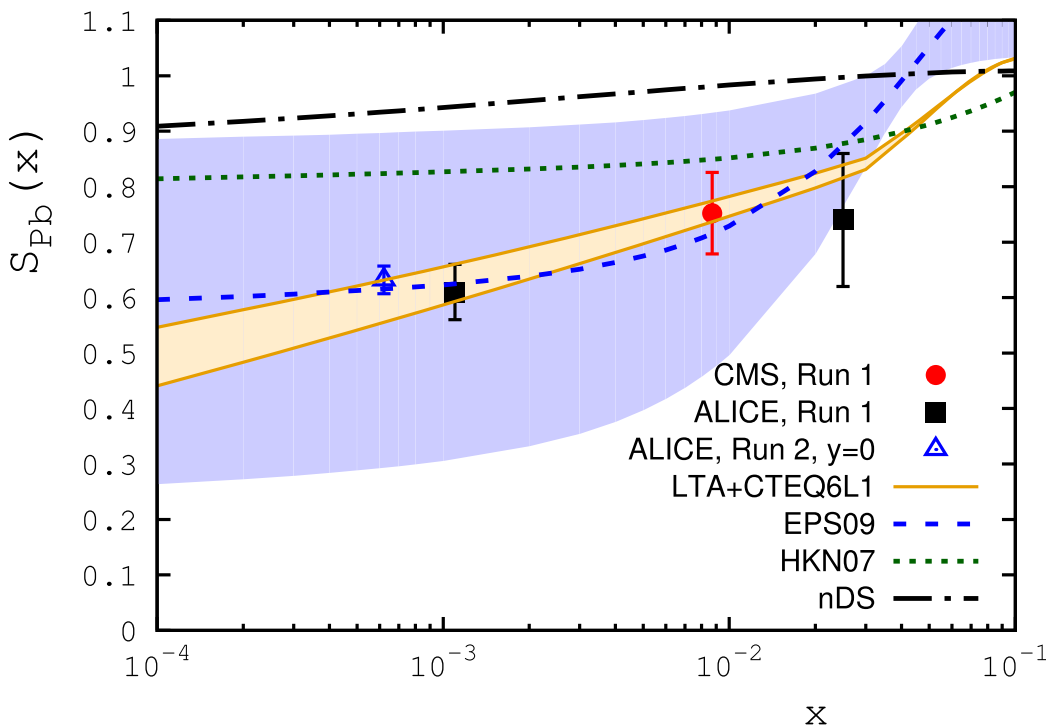
- Before EIC, models of NS can be tested in ultraperipheral collisions (UPCs) of heavy ions at LHC and RHIC, [Plenary talks on UPCs, 21.06](#); [Nystrand, 20.06](#)



- Measured cross section converted nuclear suppression factor S_{Pb} , [Abelev et al. \[ALICE\], PLB718 \(2013\) 1273](#); [Abbas et al. \[ALICE\], EPJ C 73 \(2013\) 2617](#); [\[CMS\] PLB 772 \(2017\) 489](#); [Acharya et al \[ALICE\], EPJC 81 \(2021\) 8, 712](#)

$$S_{Pb}(W) = \left[\frac{\sigma^{\gamma A \rightarrow J/\psi A}(W)}{\sigma^{\gamma p \rightarrow J/\psi p}(W)} \right]^{1/2} = \frac{g_A(x, \mu^2)}{A g_p(x, \mu^2)}$$

A. Stahl, LPCC CERN Seminar, 6.12.2022



- Direct evidence of large gluon shadowing, $R_g(x=6 \times 10^{-4} - 0.001) \approx 0.6$ in agreement with LTA model and EPS09/EPPS16 nPDFs, [Guzey, Kryshen, Strikman, Zhalov, PLB 726 \(2013\) 290](#), [Guzey, Zhalov, JHEP 1310 \(2013\) 207](#)

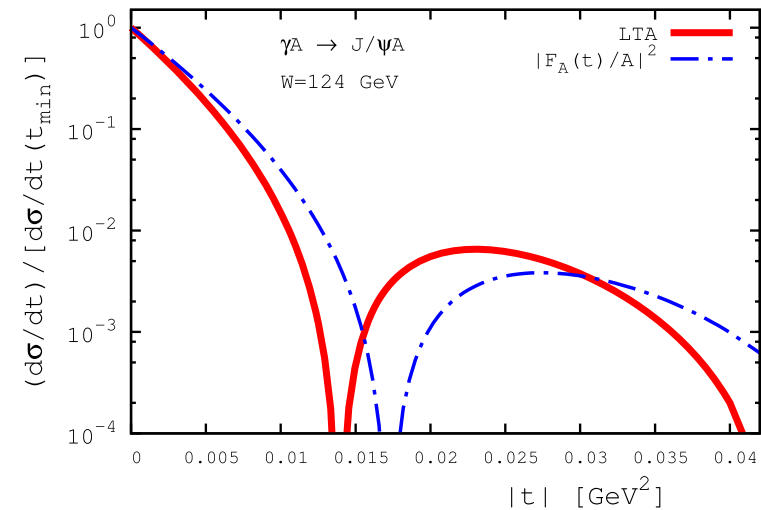
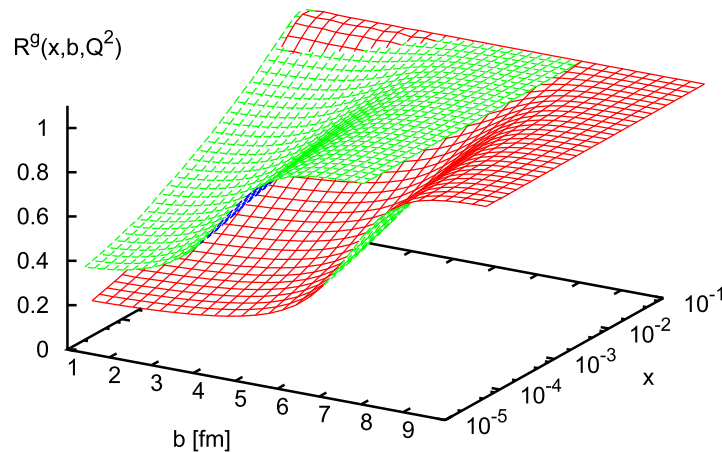
- NLO pQCD challenges this interpretation due strong cancellation between LO and NLO gluon terms, [Eskola, plenary talk on 21.06](#).

Impact parameter dependence of NS

- Leading twist models predicts dependence of nPDFs on the **impact parameter b** (transverse position of partons in nucleus):

$$xf_{j/A}(x, Q_0^2, b) = AT_A(b)xf_{j/N}(x, Q_0^2) - 8\pi A(A-1)B_{\text{diff}} \Re e \frac{(1-i\eta)^2}{1+\eta^2} \int_x^{0.1} dx_{\mathbb{P}} \beta f_j^{D(3)}(\beta, Q_0^2, x_{\mathbb{P}}) \\ \times \int_{-\infty}^{\infty} dz_1 \int_{z_1}^{\infty} dz_2 \rho_A(\vec{b}, z_1) \rho_A(\vec{b}, z_2) e^{i(z_1-z_2)x_{\mathbb{P}}m_N} e^{-\frac{A}{2}(1-i\eta)\sigma_{\text{soft}}^j(x, Q_0^2) \int_{z_1}^{z_2} dz' \rho_A(\vec{b}, z')}$$

- Shadowing is stronger at small $b \rightarrow$ broadening of nPDFs in b -space \rightarrow shift of t -dependence of $\gamma A \rightarrow J/\psi A$ cross section, [Guzey, Strikman, Zhalov, PRC 95 \(2017\) 2, 025204](#) \rightarrow confirmed by [ALICE](#), [Acharya et al., PLB 817 \(2021\) 1, 136280](#)



- Similar effect is caused by saturation in dipole picture, [Bendova, Cepila, Contreras, Matas, PLB 817 \(2021\) 136306](#)
- With additional assumptions, b -dependence of nPDFs can be extracted from data using global QCD fits, [EPS09s](#), [Helenius, Eskola, Honkanen, Salgado, JHEP 07 \(2012\) 073](#).

Nuclear shadowing in dipole picture

- Space-time picture of strong interaction at high energies in target rest frame
→ photon is a superposition of long-lived $q\bar{q}$, $q\bar{q}g$,... dipoles.

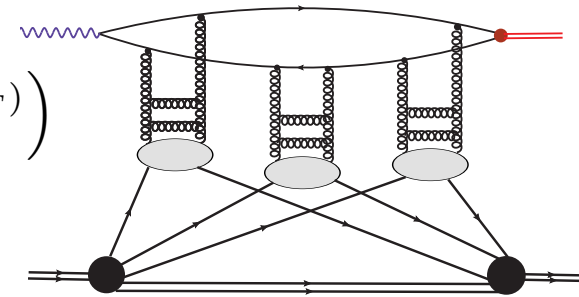
- Dipoles successively, elastically scatter on target nucleons → high-energy factorization for, e.g., $\gamma + A \rightarrow J/\psi + A$ amplitude:

$$\mathcal{M}^{\gamma A \rightarrow J/\psi A} = \int d^2 \mathbf{r}_T \int \frac{dz}{4\pi} \int d^2 \mathbf{b}_T [\Psi_{J/\psi}^* \Phi_\gamma] 2 \left(1 - e^{-\frac{1}{2} \sigma_{\text{dip}}(\mathbf{r}_T) T_A(\mathbf{b}_T)} \right)$$

Overlap of photon (QED) and J/ψ (model) wf's

Dipole cross section from fits to HERA

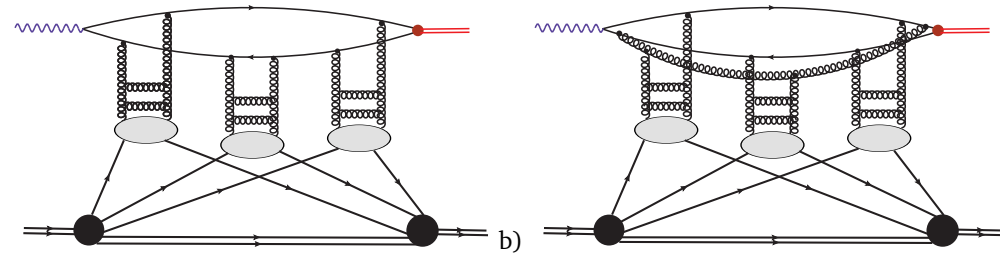
Nuclear density



- Describes data on $F_{2A}(x, Q^2)$ in eA DIS, [Kowalski, Lappi, Venugopalan, PRL 100 \(2008\) 022303](#)
- But overestimates coherent J/ψ photoproduction in Pb-Pb UPCs, [Lappi, Mäntysaari, PRC 87 \(2013\) 3, 032201](#); [Luszczak, Schäfer, PRC 99 \(2019\) 4, 044905](#)
- Weak shadowing is general property of eikonal scattering of small-size dipoles, e.g. longitudinal structure function $F_L^A(x, Q^2)$, [Frankfurt, Guzey, McDermott, Strikman, JHEP 02 \(2002\) 027](#)
- Need to include higher $q\bar{q}g$ Fock states (dipoles) to better describe diffraction on proton driving NS, [Buchmüller, McDermott, Hebecker, NPB 487 \(1997\) 283](#); [Kowalski, Lappi, Marquet, Venugopalan, PRC 78 \(2008\) 045201](#); [Golek-Biernat, Luszczak, PRD 79 \(2009\) 114010](#)

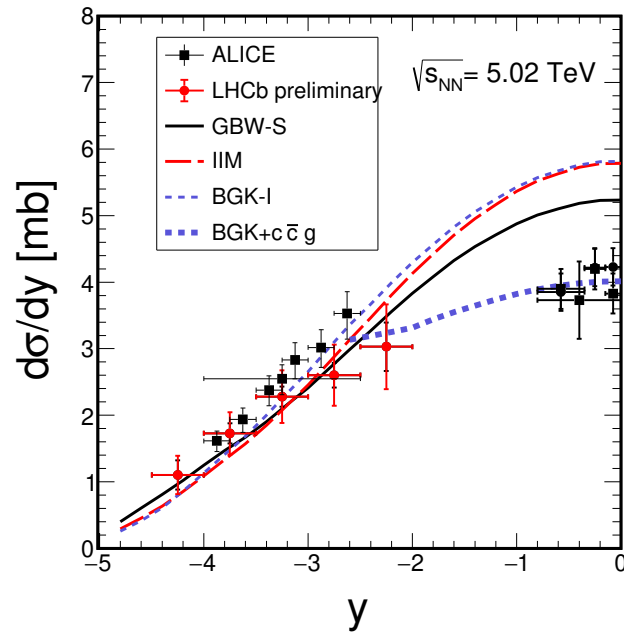
Dipole picture: role of $q\bar{q}g$ dipoles

- Higher $q\bar{q}g$ Fock states contribute to inelastic shadowing \rightarrow bridge gap between dipole picture and LT model.

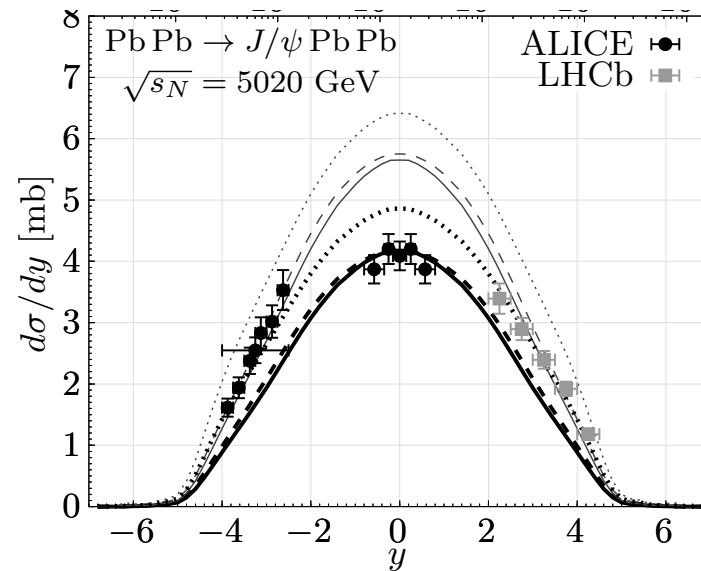


- Provide good description of coherent J/ψ photoproduction in Pb-Pb UPCs

Luszczak, Schäfer, SciPost Phys.Proc. 8 (2022) 109, arXiv:2108.06788 [hep-ph]



Kopeliovich, Krelina, Nemchik, Potashnikova, PRD 107 (2023) 5, 054005



- Depends on details of dipole cross section and photon and J/ψ wave functions.
- Alternatively, good description using BK equations with nuclear geometry,

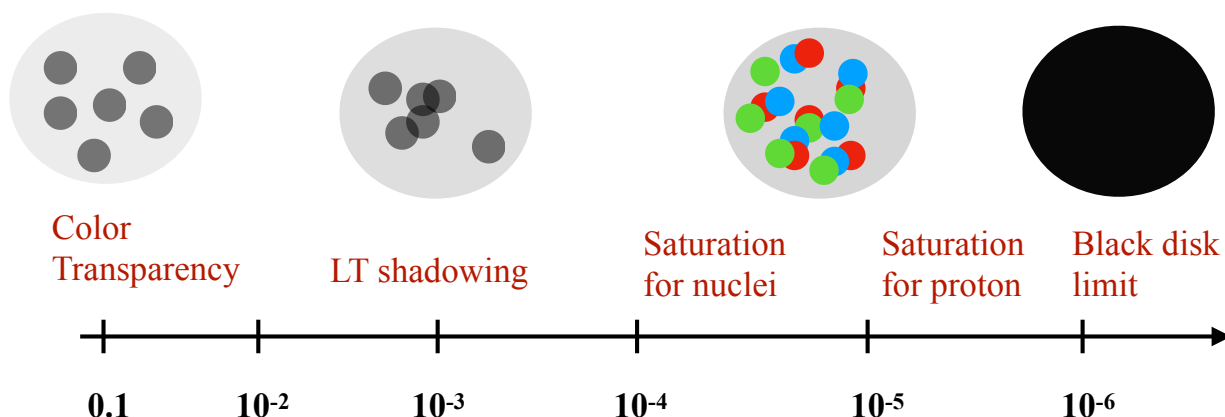
Bendova, Cepila, Contreras, Matas, PLB 817 (2021) 136306

Nuclear shadowing and saturation

- Many questions on connection between shadowing and saturation:

- ★ Are they the same thing or capture the same physics?
- ★ If not, how should one combine them together?
- ★ What are their distinctive signatures?
- ★ ...

- Possible stages of high-energy scattering off nuclei :



- LT shadowing is linear regime, not the same as non-linear saturation, but it lowers saturation scale Q_s , Frankfurt, Guzey, Stasto, Strikman, Rept. Prog. Phys. 85 (2022) 12, 126301

- Q_s controls onset of non-linear parton recombination, Gribov, Levin, Ryskin, Phys. Rep. 100 (1983) 1; Muller, Qiu, NPB 268 (1986) 427 → delayed by NS and dilute nuclear density:

$$Q_s^2 \sim \frac{\alpha_s(Q_s^2)}{\pi R_{gN}^2} xg(x, Q_s^2) \rightarrow \frac{Q_{sA}^2}{Q_{sN}^2} = A \frac{R_{gN}^2}{R_A^2} \frac{g_A(x, Q^2)}{Ag_N(x, Q^2)} \rightarrow \frac{Q_{sA}^2}{Q_{sN}^2} = 0.3A^{1/3} \approx 1.75$$

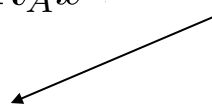
Nuclear shadowing and black disk limit (BDL)

- LT approximation breaks down at sufficiently low x .
- Estimated using BDL limit $\sigma_{\text{diff}}/\sigma_{\text{tot}} \leq 1/2 \rightarrow \sigma_2 \leq 8\pi B_{2g} \approx 50 \text{ mb}$ at $x \sim 10^{-5} \rightarrow$ lower limit on NS $g_A(x, Q^2)/Ag_p(x, Q^2) \geq 0.3 \rightarrow$ compare to [Kopeliovich, et al PRC79 \(2009\) 064906](#)
- In BDL, photon fluctuations interact with maximal cross section $2\pi R^2$, but their masses grow \rightarrow Bjorken scaling of DIS structure functions violated, [Gribov, Sov. Phys. JETP 30 \(1970\) 709; McDermott, Frankfurt, Guzey, Strikman, EPJC 16 \(2000\) 641](#)

$$F_2^A(x, Q^2) = \sum_i e_i^2 Q^2 \frac{2\pi R_A^2}{12\pi^3} \ln 1/4m_N R_A x$$

$$F_2^p(x, Q^2) \propto \sum_i e_i^2 Q^2 \frac{2\pi R_N^2}{12\pi^3} \left(1 + \frac{4c_N^2}{R_N^2} \ln^2 x_0/x\right) \ln 1/x$$

additional logs from interaction range



- Shadowing continues to decrease:

$$\frac{F_2^A(x, Q^2)}{AF_2^N(x, Q^2)} \propto \frac{R_A^2}{AR_N^2} \frac{1}{1 + 4c_N^2 R_A^2 \ln^2 1/x}$$

- Signals of saturation/BDL more pronounced in diffractive final states: vector mesons, [Frankfurt, Guzey, McDermott, Strikman, PRL 87 \(2001\) 192301](#), structure functions, [Kowalski, Lappi, Venugopalan, PRL 100 \(2008\) 022303](#), dijets, [E. Iancu, parallel session talk, 20.06.](#)

Summary and Outlook

- Leading twist model and dipole picture are two competing dynamic mechanisms for nuclear shadowing.
- They are best discriminated by nuclear longitudinal F_L^A and diffractive F_{2A}^D structure functions in the EIC kinematics.
- Real photon-nucleus scattering in UPCs at the LHC and RHIC has provided new information on dynamics of nuclear shadowing in small- x QCD.
- The UPC data at the LHC — including the recent measurements of energy dependence of NS — challenge both LT and dipole models.
- The LT model would benefit from better treatment of antishadowing and a possible symbiosis with nPDFs from global QCD fits.
- Important to apply recent progress in NLO calculations in the dipole model to UPC phenomenology.
- LT shadowing \neq saturation, but slows down its onset.
- Nuclear shadowing does not saturate even in BDL.
- I didn't have time to discuss large LT shadowing in incoherent scattering.