



Brookhaven[™]
National Laboratory



QIS for pdfs, saturation and non-equilibrium dynamics

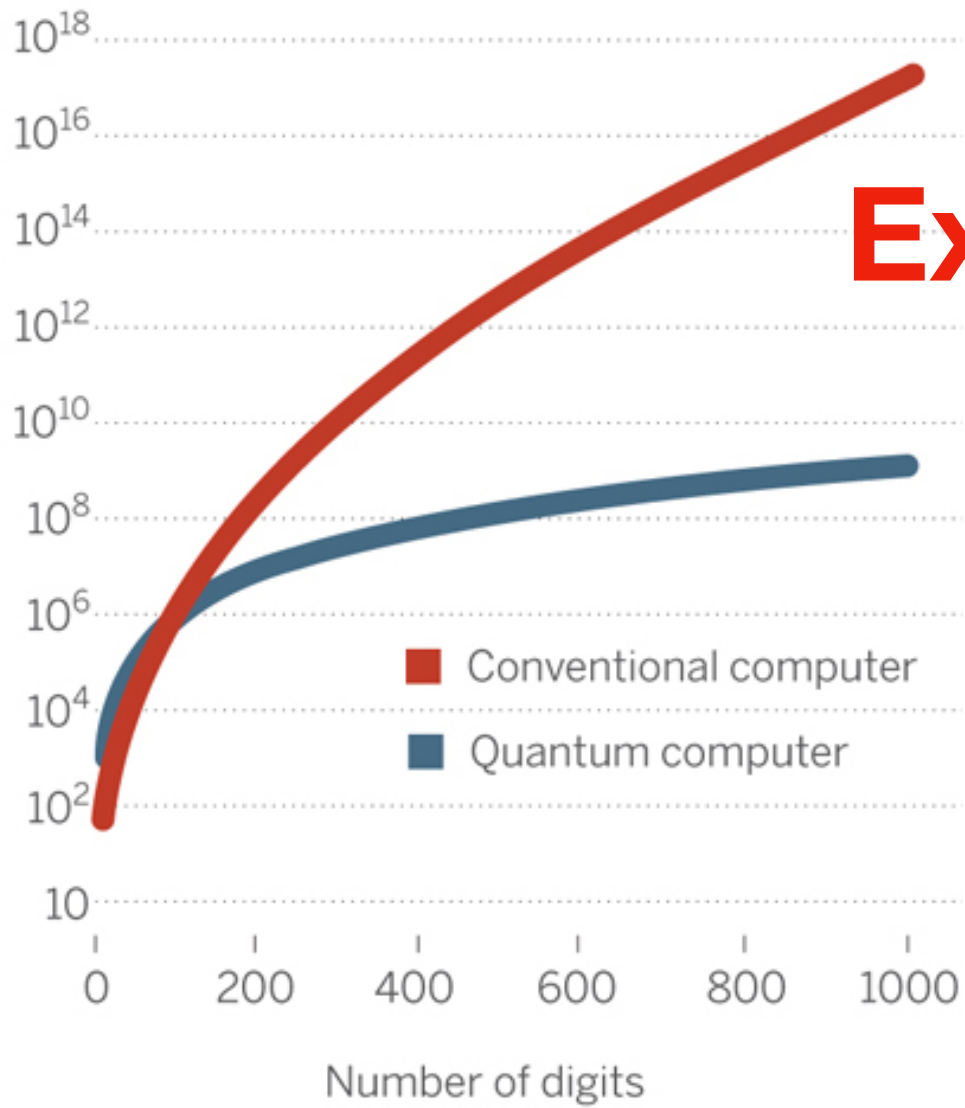


João Barata, BNL and C2QA

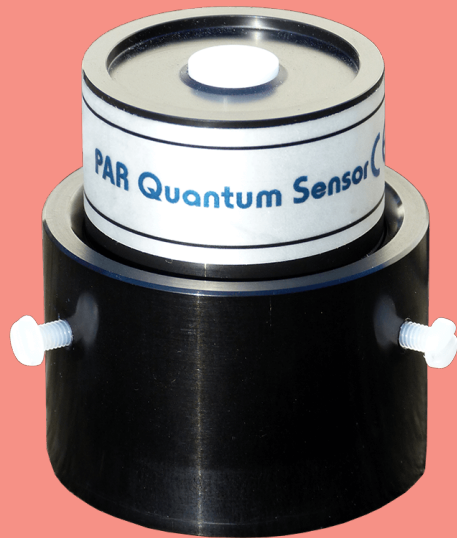
Why QIS for Nuclear Physics?

Quantum speedup

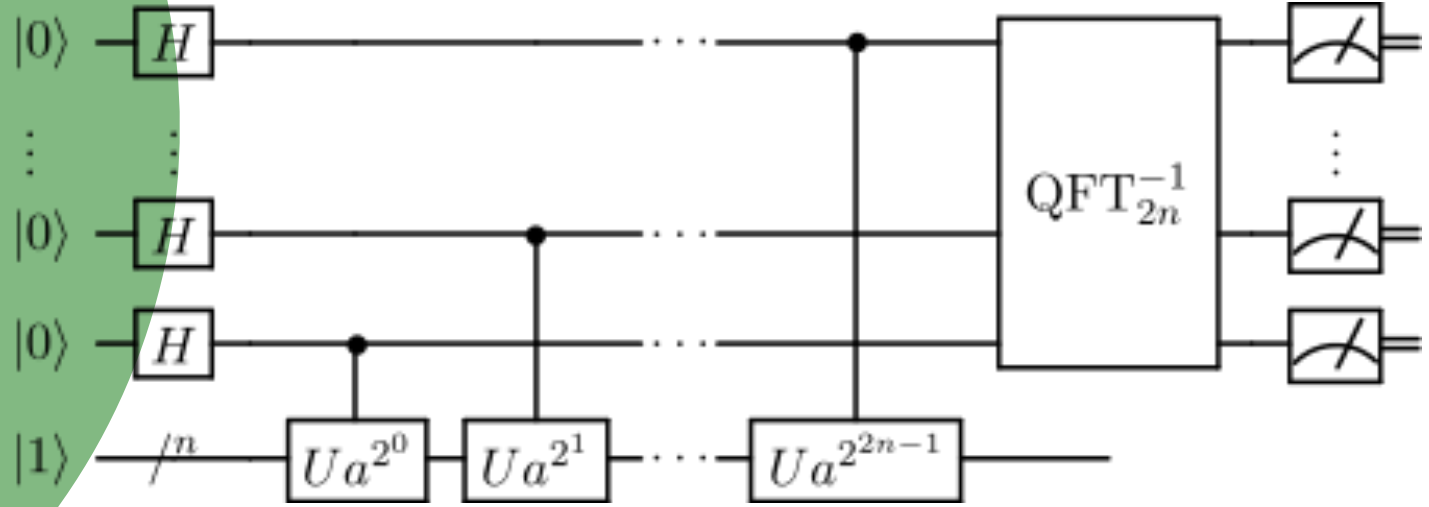
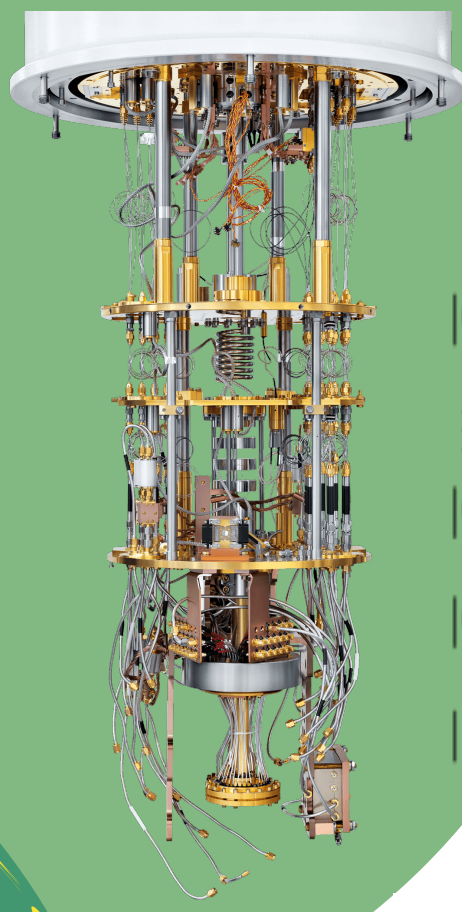
Computational steps to factor a number



Experimental needs



New Technologies



Today

New Theoretical ideas

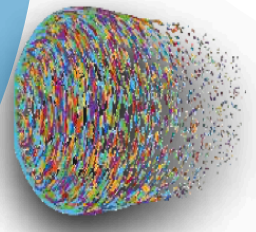
Entanglement

Confinement

Proton Structure

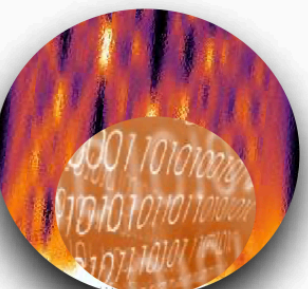
[Klebanov, Kutasov, Murugan, 0709.2140]
[Kharzeev, Levin, 1702.03489]

Chaos



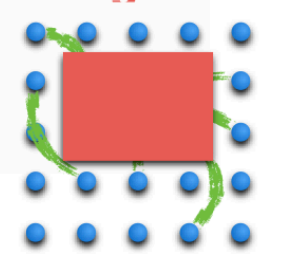
Lyapunov Exponents

Scrambling



Thermalization

Entanglement



Volume Law

[Berges et al, 2005.12299]
[Lewis-Swan, Safavi-Naini, Bollinger, Rey, 1808.07134]

① New Technologies

② Applications in experimental HEP

③ Theory and Pheno applications

→ Structure of matter

→ Fragmentation

→ Non-perturbative and out of equilibrium physics

1

New Technologies

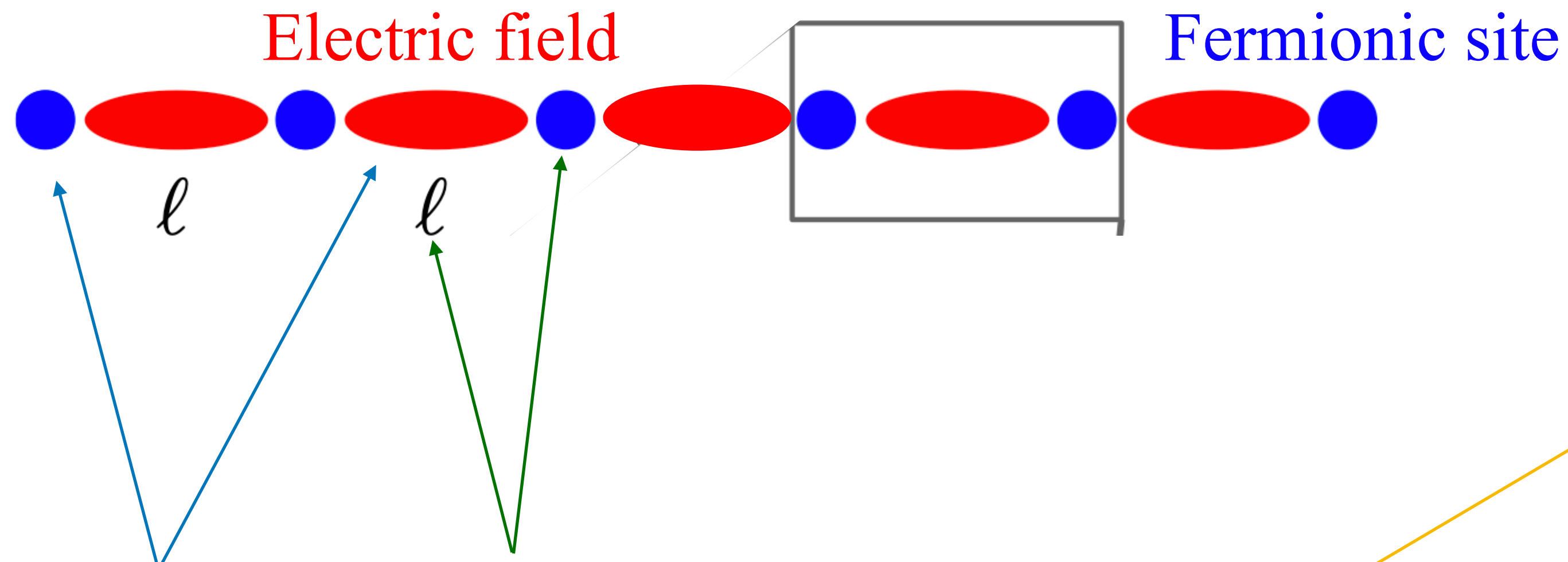
[Reviews in back up slides]

Analog quantum simulators

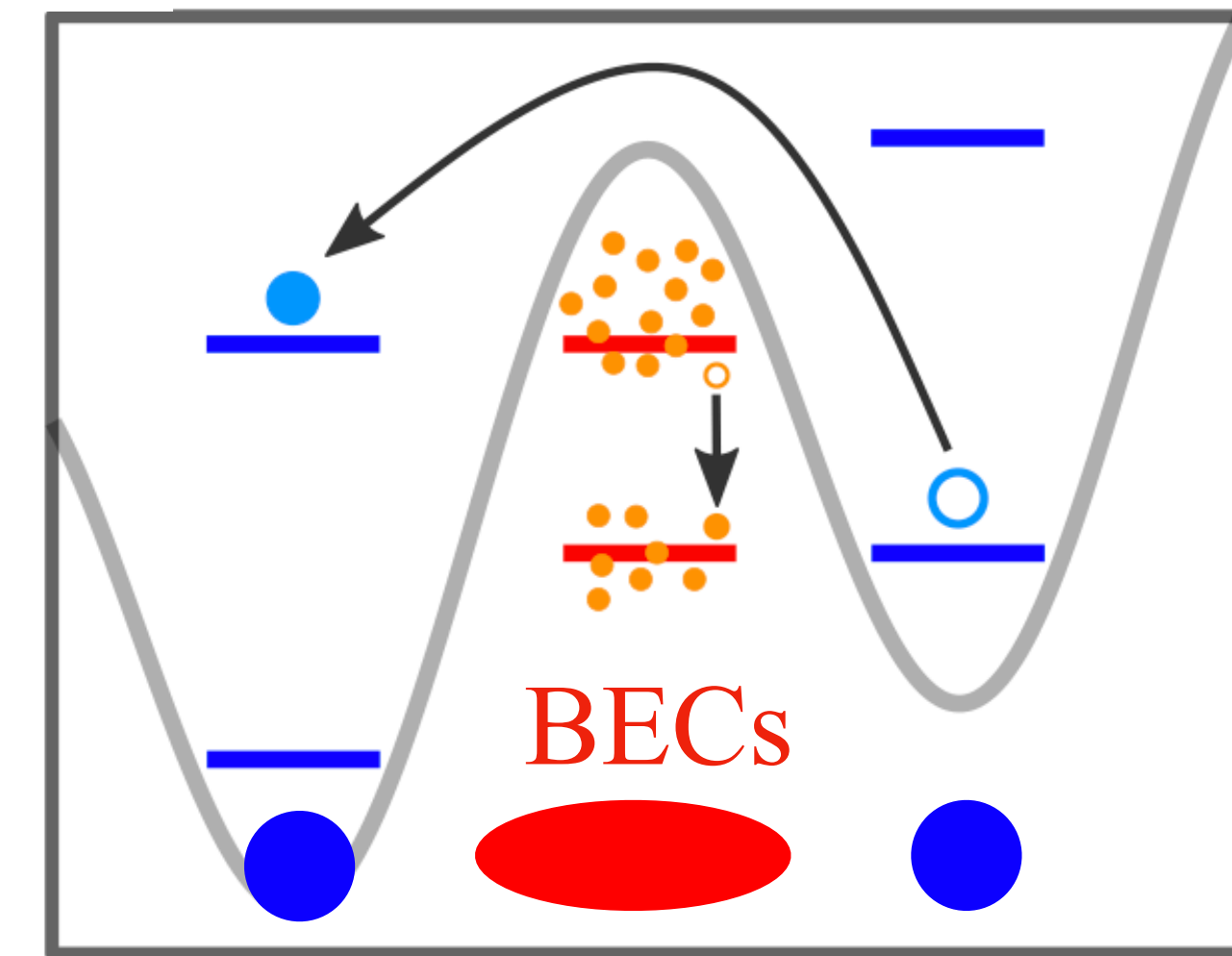
Basic idea: A controllable quantum system that can be engineered to mimic a physical system

An example: 1+1d lattice QED = Quantum Link model with truncated electric field; spin ℓ

QED/QLM



Cold atom Simulator



$$H_{\text{QED}} = H_{\text{QLM}} + \mathcal{O}(1/\ell) = H_{CA}$$

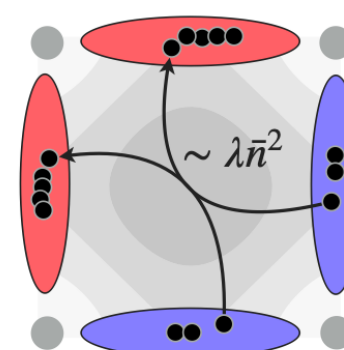
The most successful platform, but:

Non universal approach

Analog

New: 2+1d extensions

[Ott, Zache, Jendrzejewski, Berges, 2012.10432]

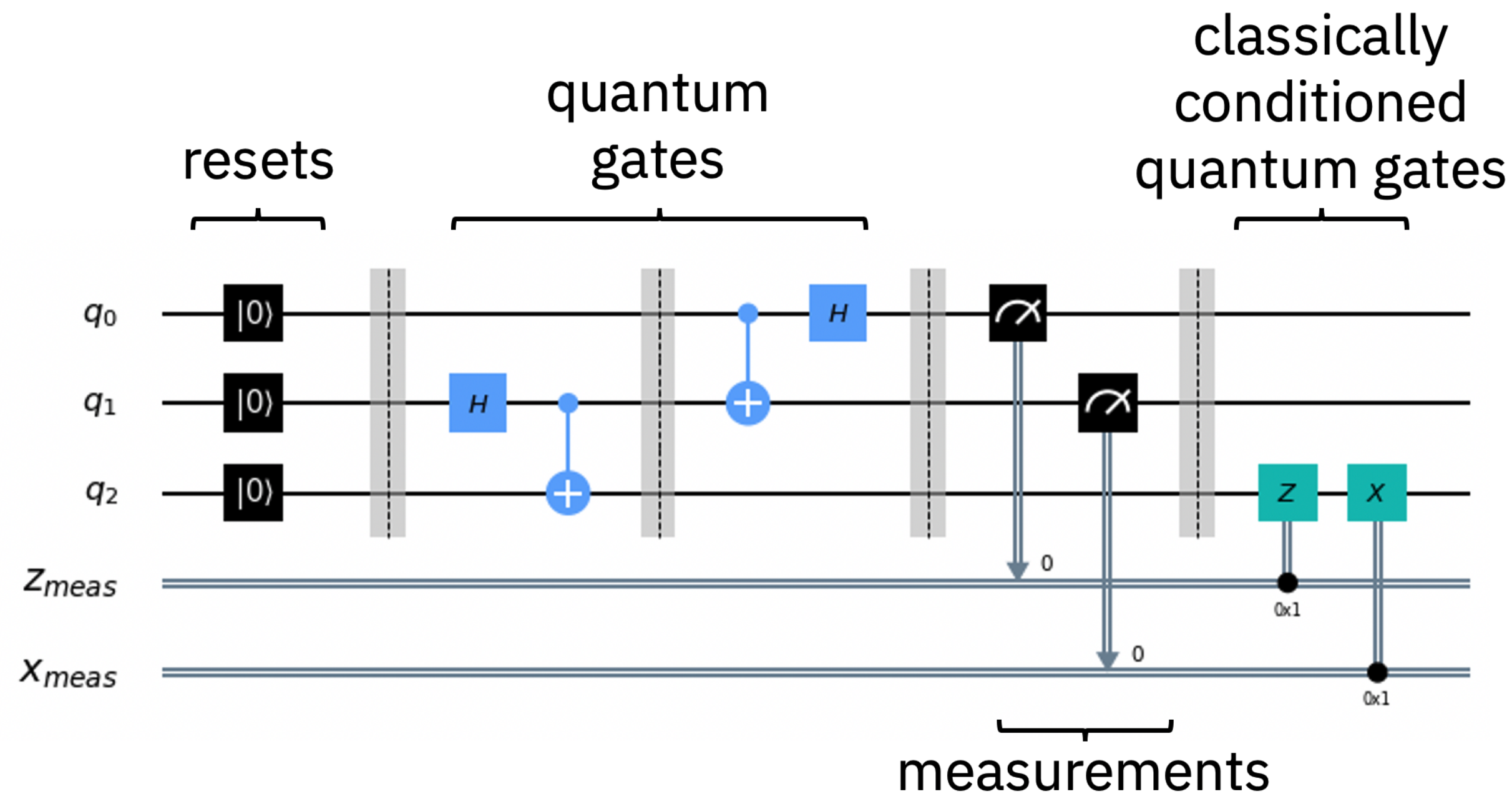


Digital quantum computers

Basic idea: A spin-chain where local operators can be applied

Computer = many qubits (lines) + unitary gates (operators)

Several implementations



$$|\psi\rangle = H^0 O_{+}^{01} O_{+}^{12} H^1 |q_0\rangle |q_1\rangle |q_2\rangle$$



Conceptually simple, but:

Few qubits

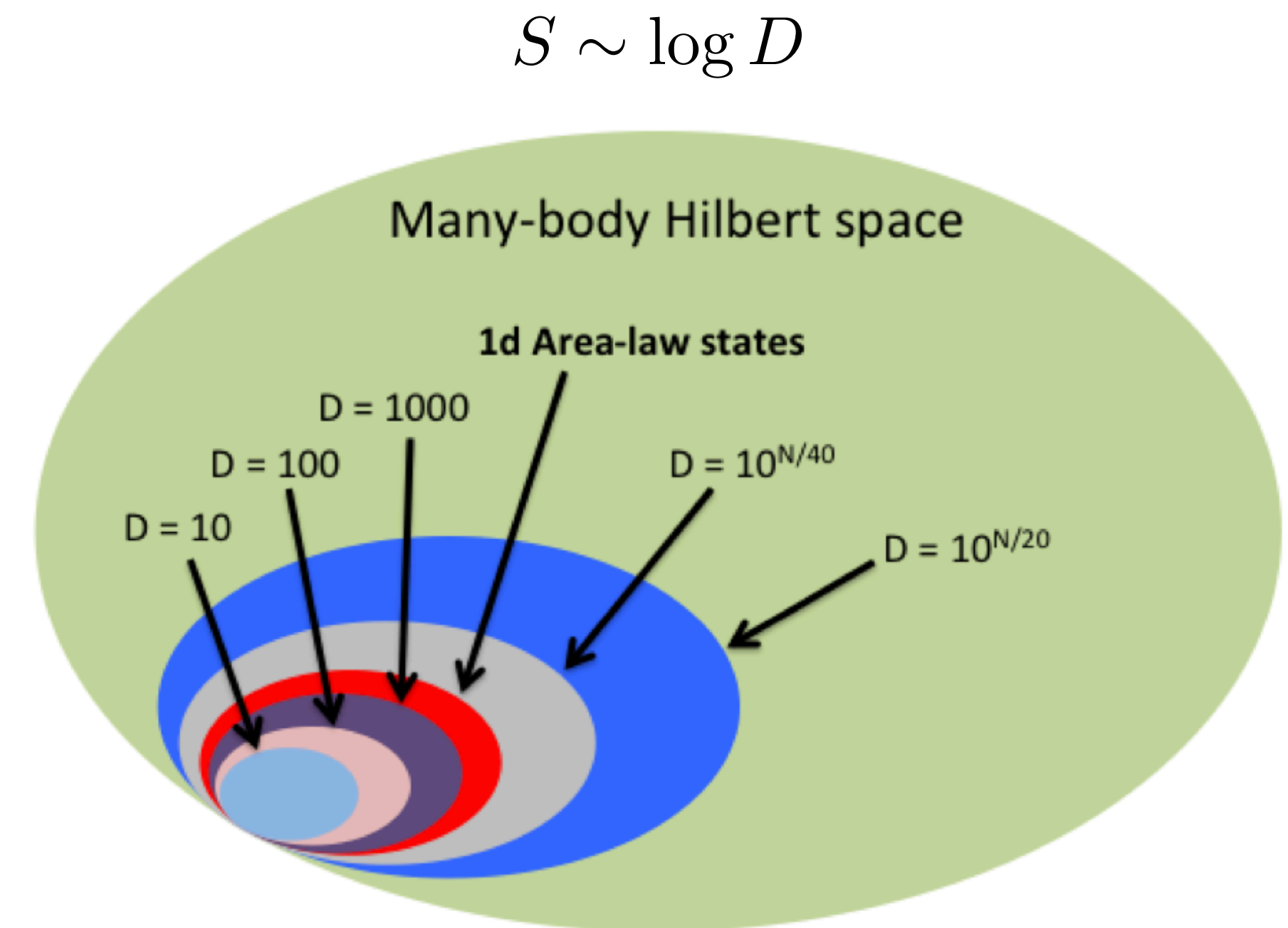
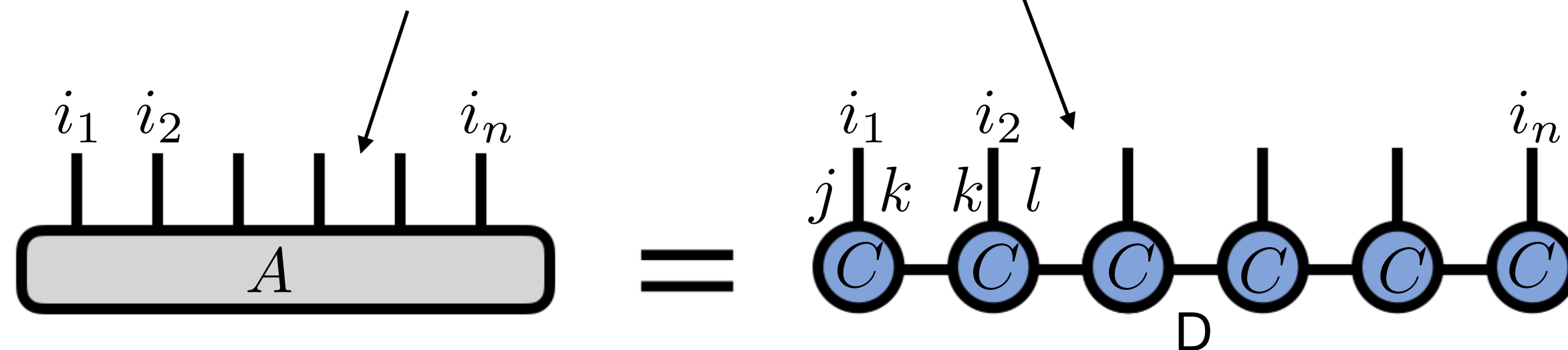
External noise

Tensor Networks (classical)

Basic idea: Lowest states of a gapped local Hamiltonian obey the area-law for entanglement entropy
 i.e. they are highly constrained by locality

$$|\psi\rangle = \sum_{i_j} A_{i_1 i_2 \dots i_n} |i_1\rangle |i_2\rangle |i_3\rangle \dots |i_n\rangle$$

$$A_{i_1 i_2 \dots i_n} = C_{i_1}^{jk} C_{i_2}^{kl} \dots$$



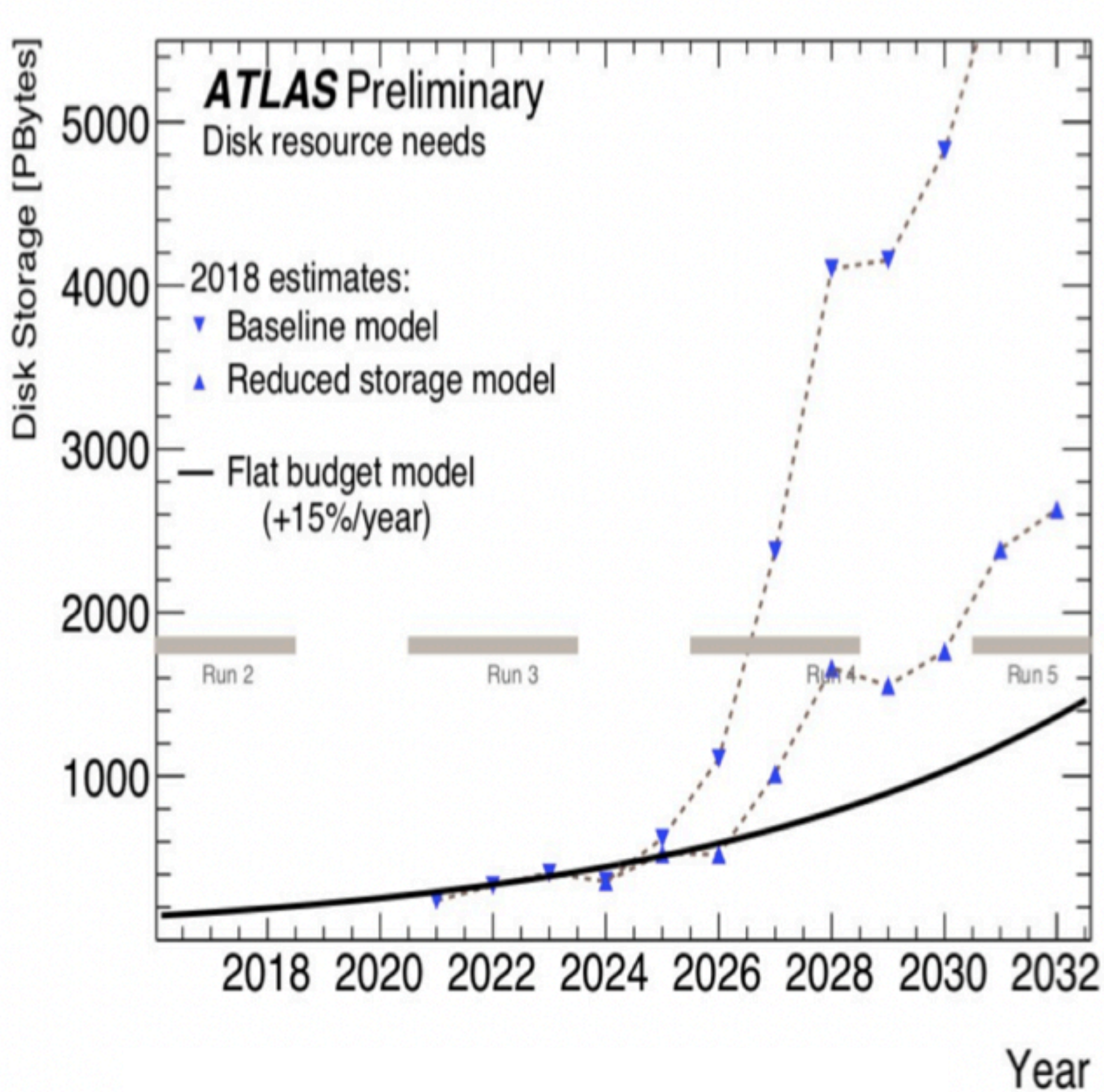
[Wilson] [White]

Very powerful in 1+1d ! Best example: density matrix renormalization group algorithm

Fails when: Long time evolution Near critical points

② Applications in experimental HEP

Motivated by large amounts of data...



... and optimization tasks

Several applications

Particle tracking

[Zlokapa et al, 1908.04475]
[Magano et al, 2104.11583]

Jet clustering

[Wei, Nail, Harrow, Thaler, 1908.08949]
[Pires, Bargassa, Seixas, Omar, 2101.05618]
[Delgado, Thaler, 2205.02814]

Detector simulation

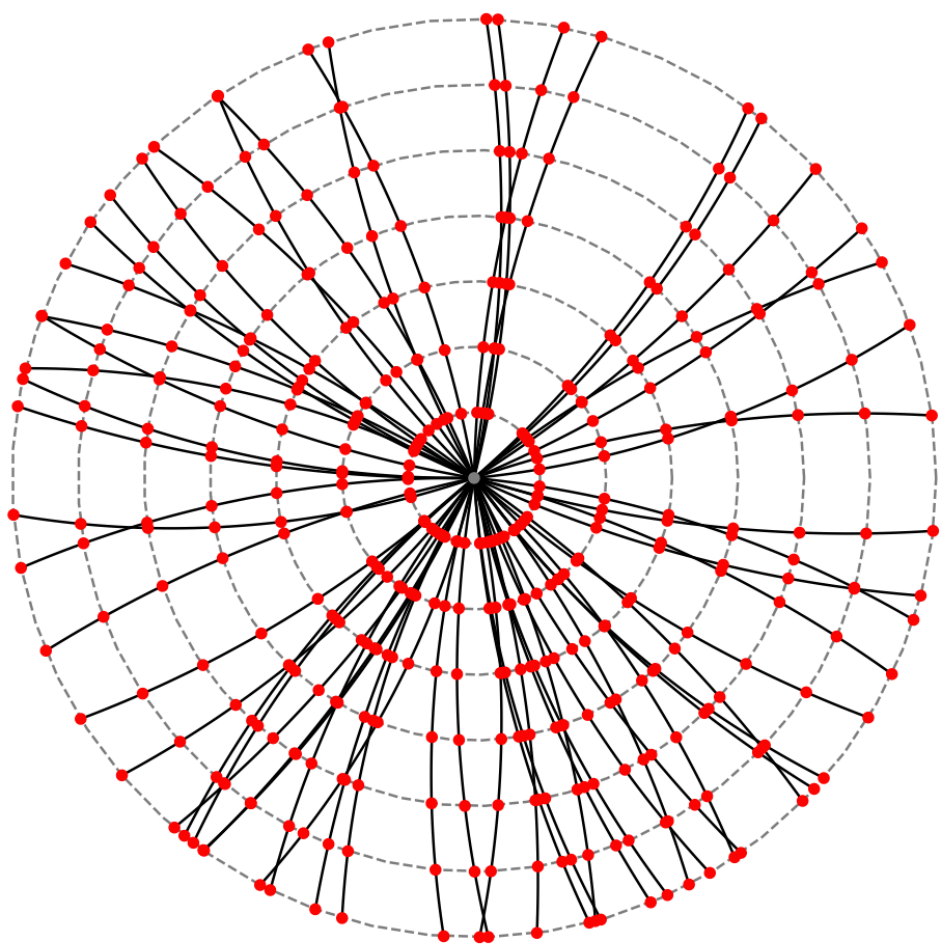
[Yeon Chang et al, 2101.11132]

Anomaly detection

[Alvi, Bauer, Nachman, 2206.08391]
[Ngairangbam, Spannowsky, Takeuchi, 2112.04958]

Quantum sensing

[Degen, Reinhard, Cappellaro, 1611.02427]



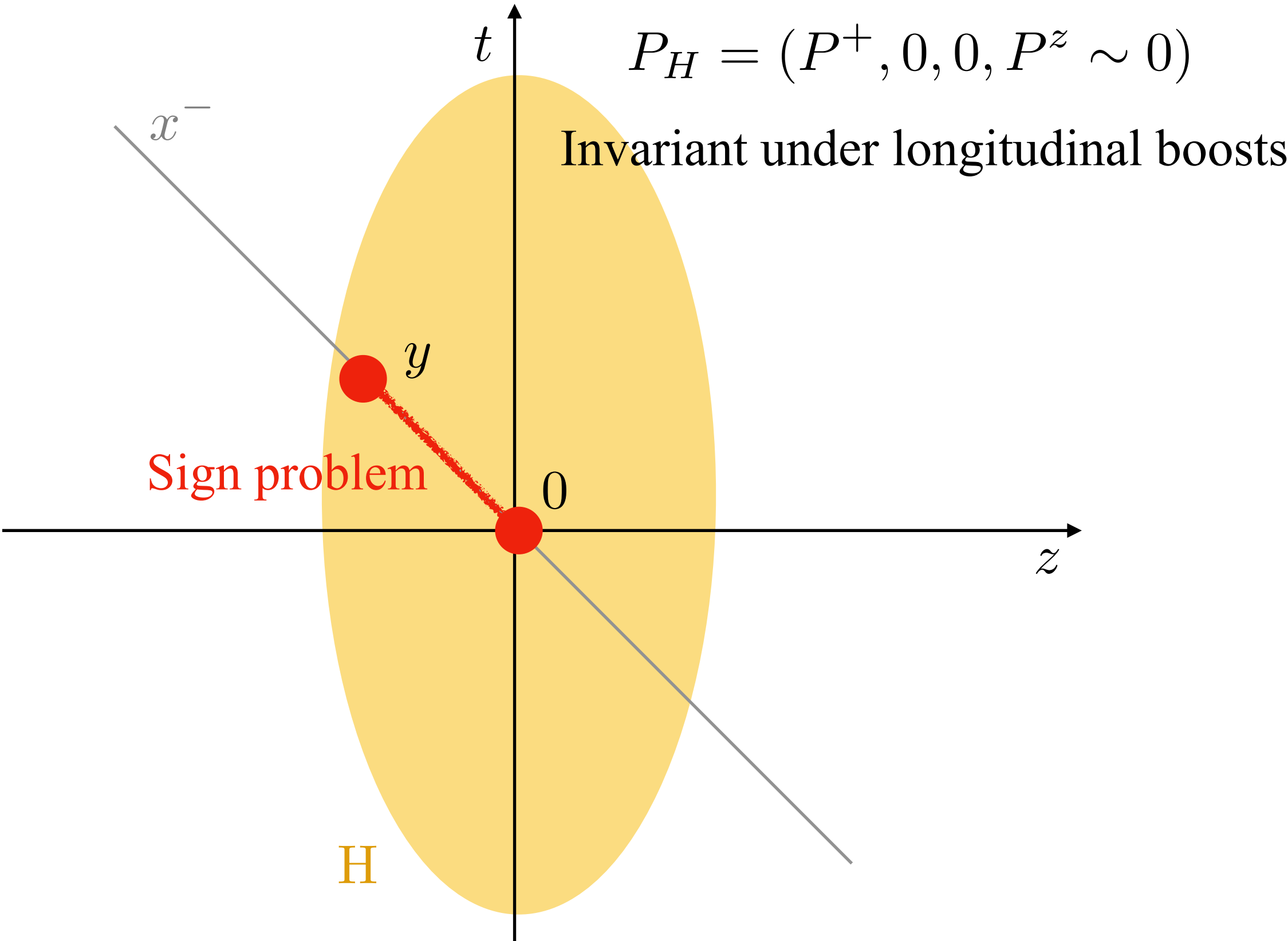
For recent review : [Delgado et al, 2203.08805]

3 Theory and Pheno applications

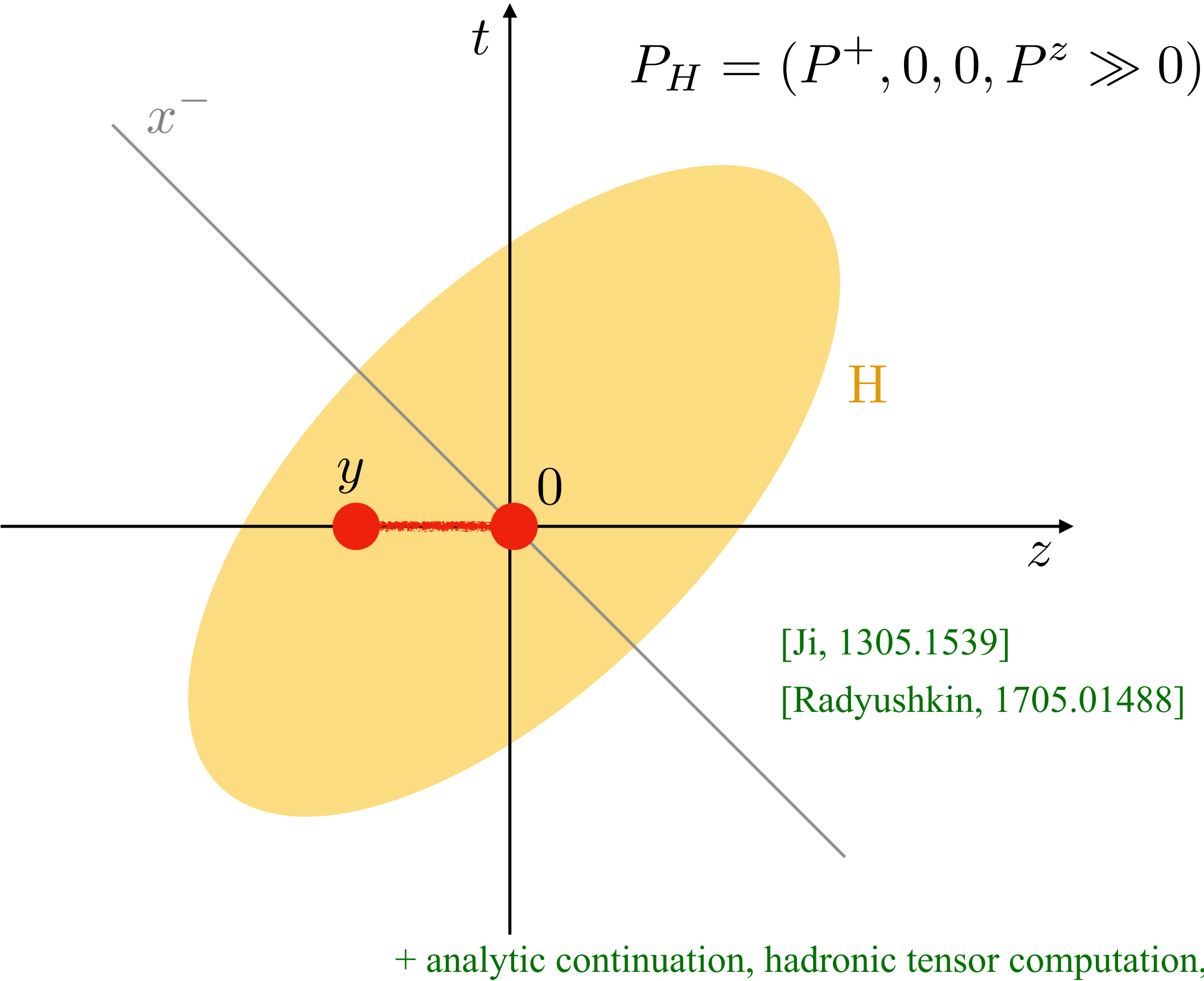
Extracting PDFs from quantum computers

$$f(x) = \int dy e^{ixP^+y} \langle \bar{\psi}(y) \gamma^+ W(y) \psi(0) \rangle_H$$

Boost to implement in euclidean lattice



Suitable for quantum calculation



Suitable for classical calculation

Extracting PDFs from quantum computers

Parton Physics on a Quantum Computer [\[1908.10439\]](#)

Henry Lamm,^{1,*} Scott Lawrence,^{1,†} and Yukari Yamauchi^{1,‡}

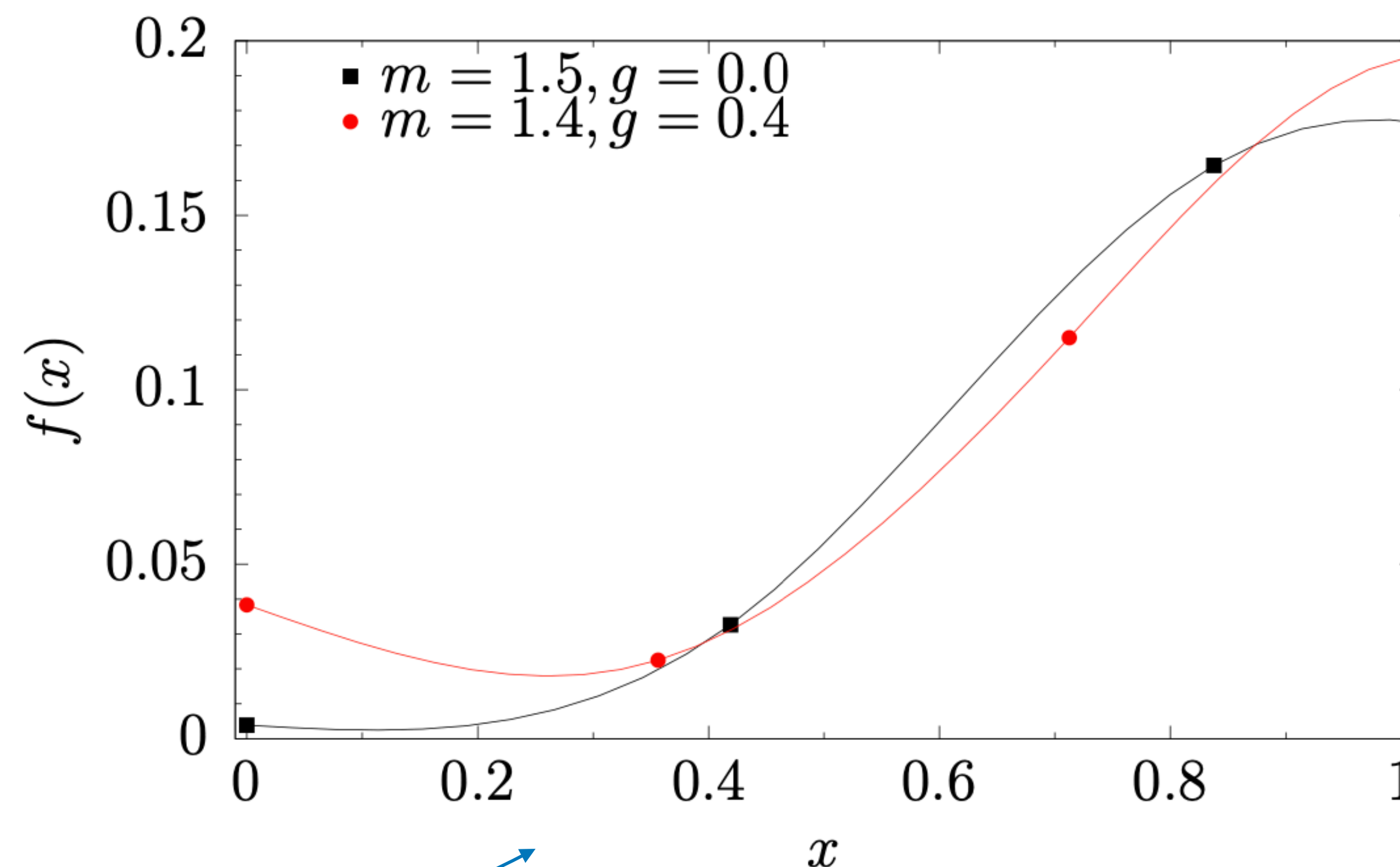
First exploratory calculation of quark distribution in 1+1d Thirring model

$$f(x) = \int dy e^{ixP^+ y} \langle \bar{\psi}(y) \gamma^+ W(y) \psi(0) \rangle_H$$

(1) Discretization + Kogut-Susskind prescription

[\[Kogut, Susskind, 1975\]](#)

$$f_{\text{stag}}(x) = \langle P | \sum_{y,z} e^{ixP(y-z)} \left[\delta_{|z|}^{|y|} + i(-1)^z \delta_{|z+1|}^{|y|} \right] \\ \times e^{iH(y-z)} \chi^\dagger(y) e^{-iH(y-z)} \chi(z) | P \rangle$$



(2) Map to spin chain system via Jordan-Wigner transform

Extracting PDFs from quantum computers

Challenges:

Including Wilson lines :

Compute hadronic tensor (no Wilson lines) [Lamm, Lawrence, Yamauchi, 1903.08807]

[Echevarria, Egusquia, Rico, Schnell, 2011.01275]

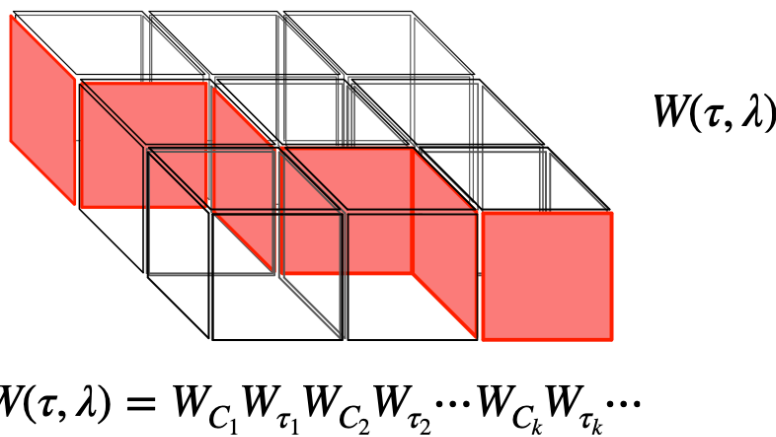
Several strategies for measuring Wilson loops, mesonic strings, ...

[Zohar, Cirac, Reznik, 1208.4299] [Brennen, 1512.06565] [Zohar, 1911.11156]

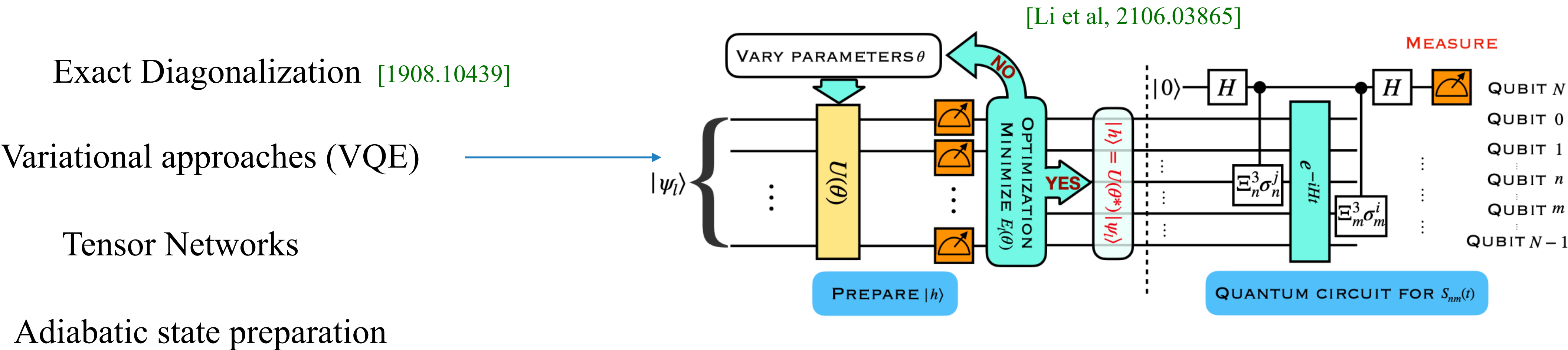
For DLCQ based approaches see:

[Kreshchuk et al, 2002.04016]

[Qian et al, 2112.01927]



Target state preparation : Hard and generic problem



Deeply inelastic scattering structure functions on a hybrid quantum computer [1908.07051]

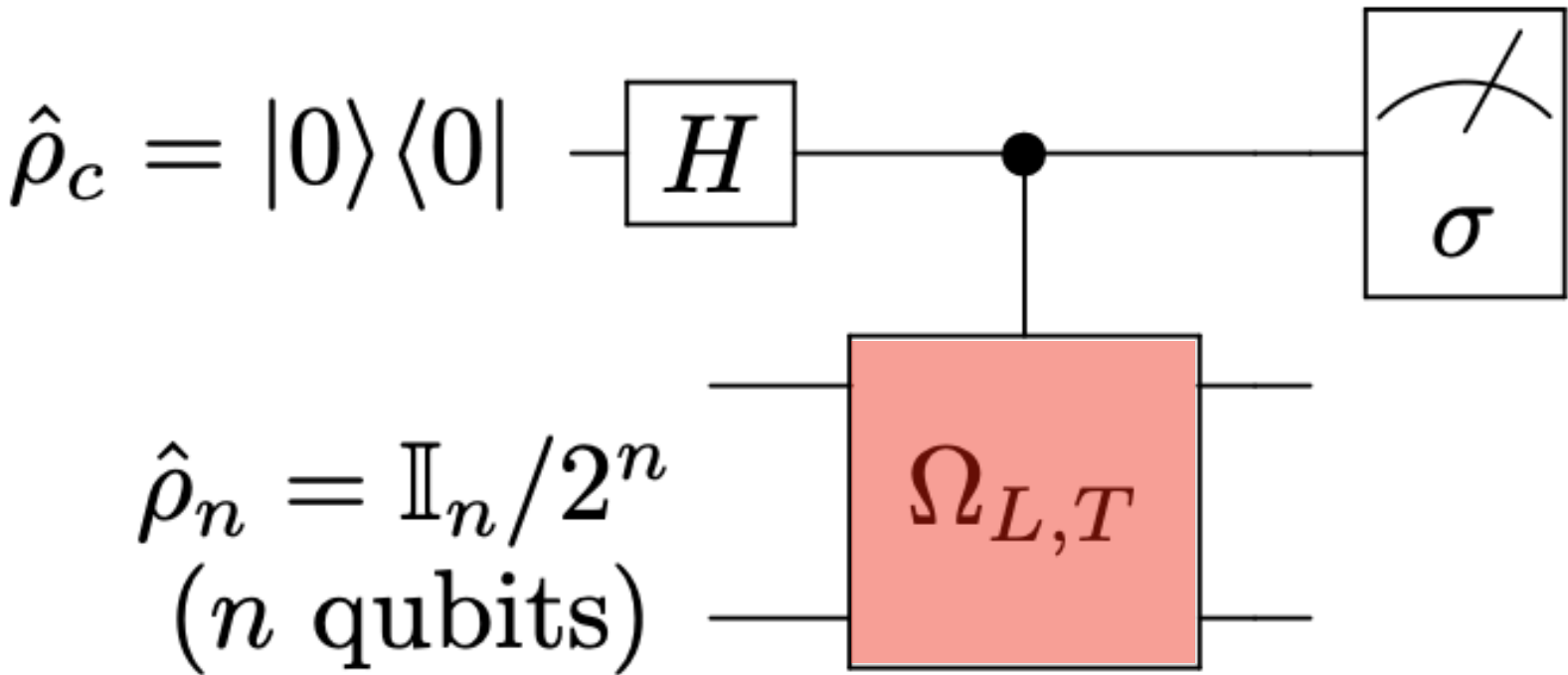
Niklas Mueller,^{1,*} Andrey Tarasov,^{1,2,3,†} and Raju Venugopalan^{1,‡}

Worldline formulation for QED (QCD) using CGC EFT

$$F_2(q, P) = \frac{\sigma Q^2}{2\pi e^2} \int \underbrace{[\mathcal{D}\rho] W[\rho]}_{x_\perp} \int \int_z \sum_{L,T; f} \underbrace{|\Psi_{L,T}^f(z, x_\perp)|^2}_{z} \times \underbrace{D_\rho(x_\perp)}_{x_\perp} i \int \underbrace{d^2\theta \langle -\theta | [\Omega_{L,T}(z, x_\perp)] | \theta \rangle}_{\theta}$$

easy to compute using standard methods

easy to compute in Qcomputer



Worldline formulation reduces problem to simple trace

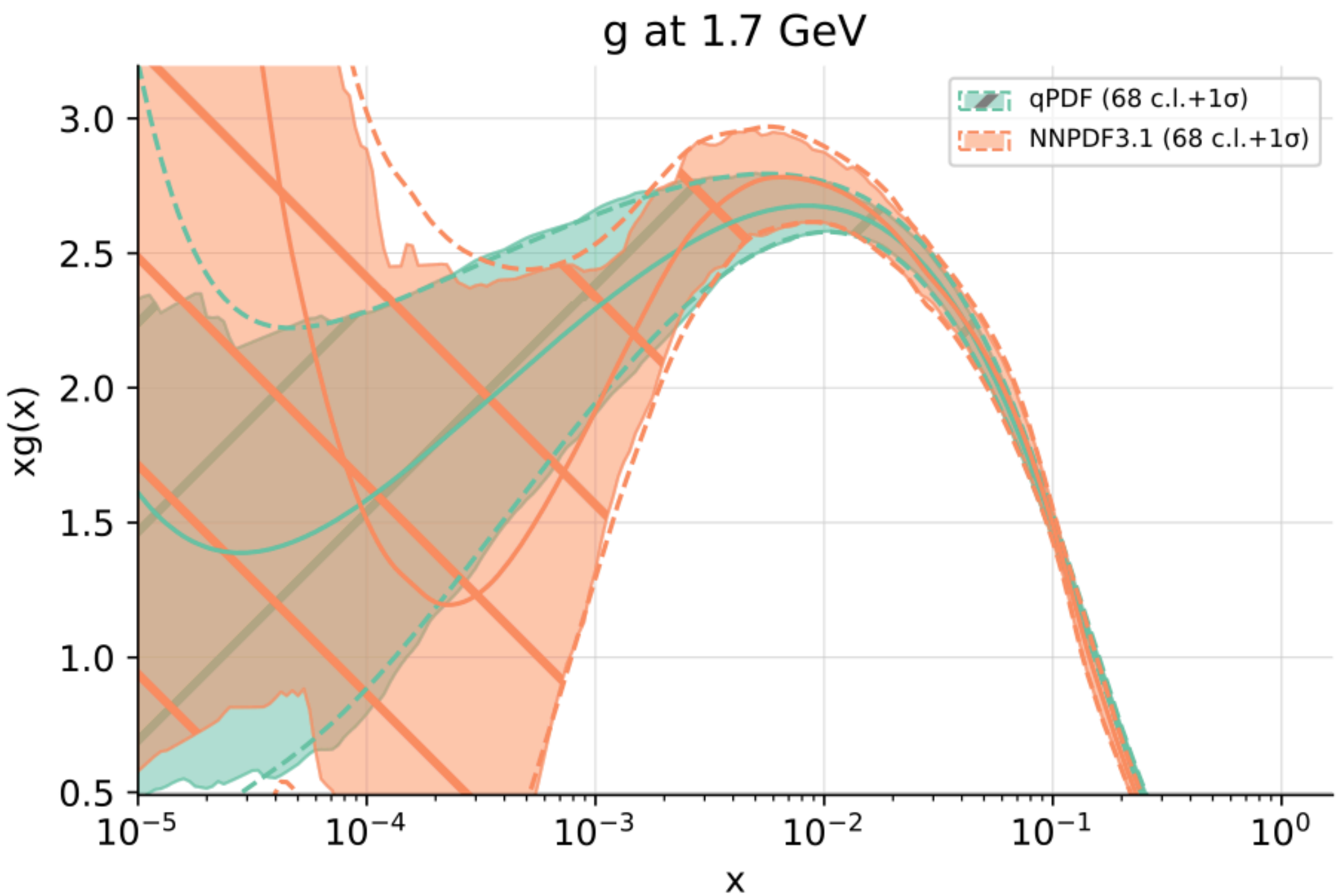
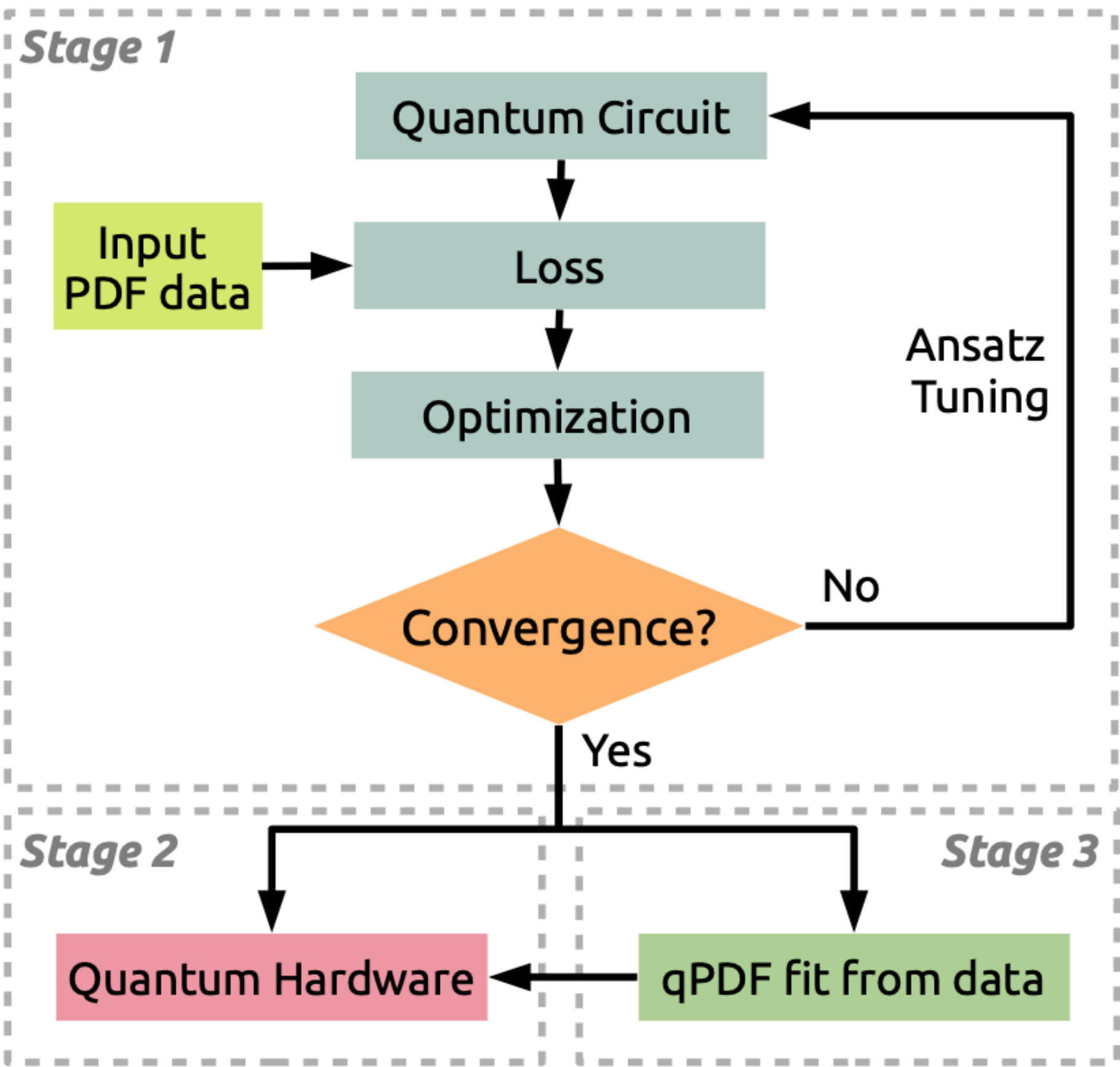
Quantum computers to leverage PDF Fits

Determining the proton content with a quantum computer [2011.13934]

Adrián Pérez-Salinas,^{1,2} Juan Cruz-Martinez,³ Abdulla A. Alhajri,⁴ and Stefano Carrazza^{3,5,4}

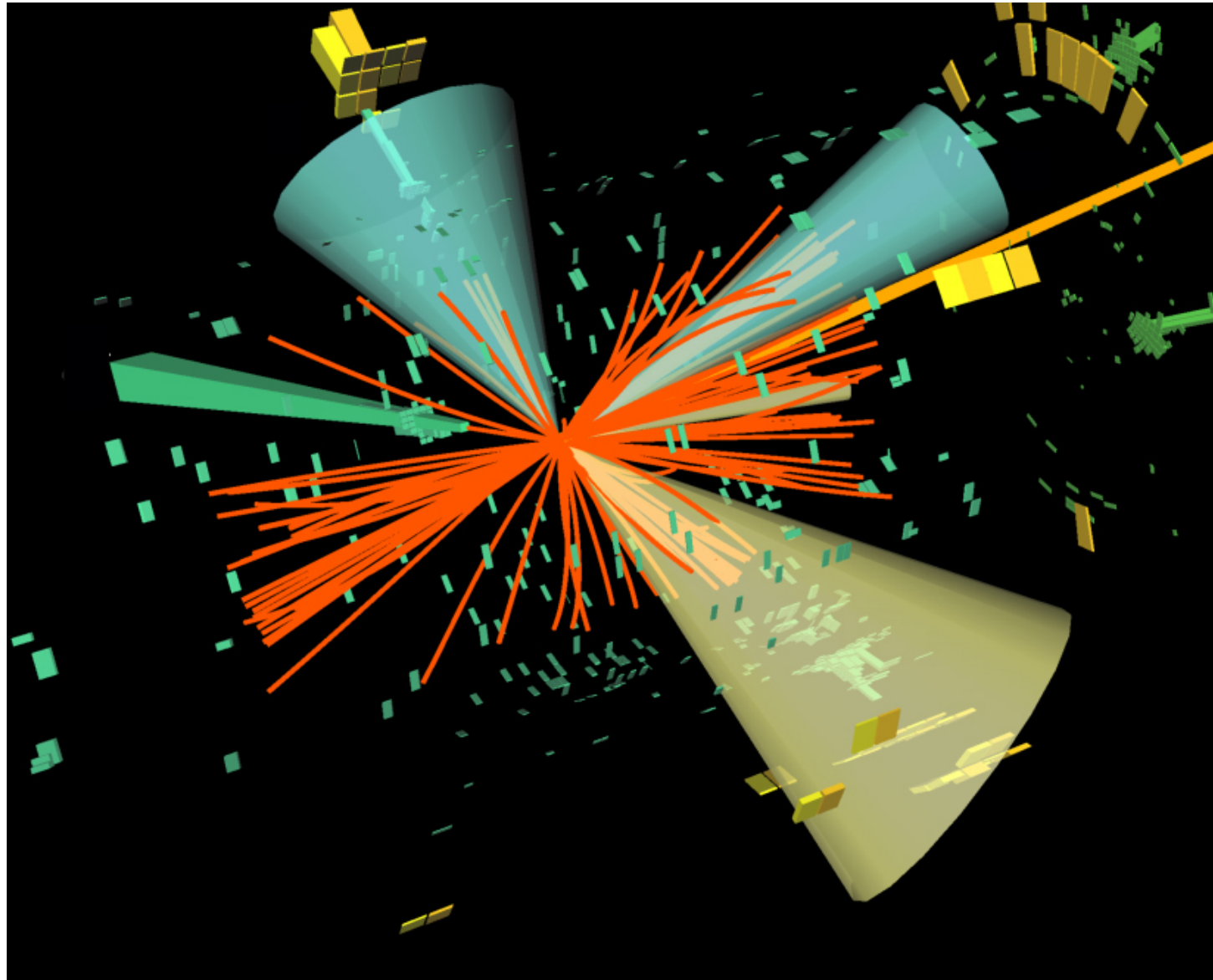
qPDF Workflow

VQE style approach

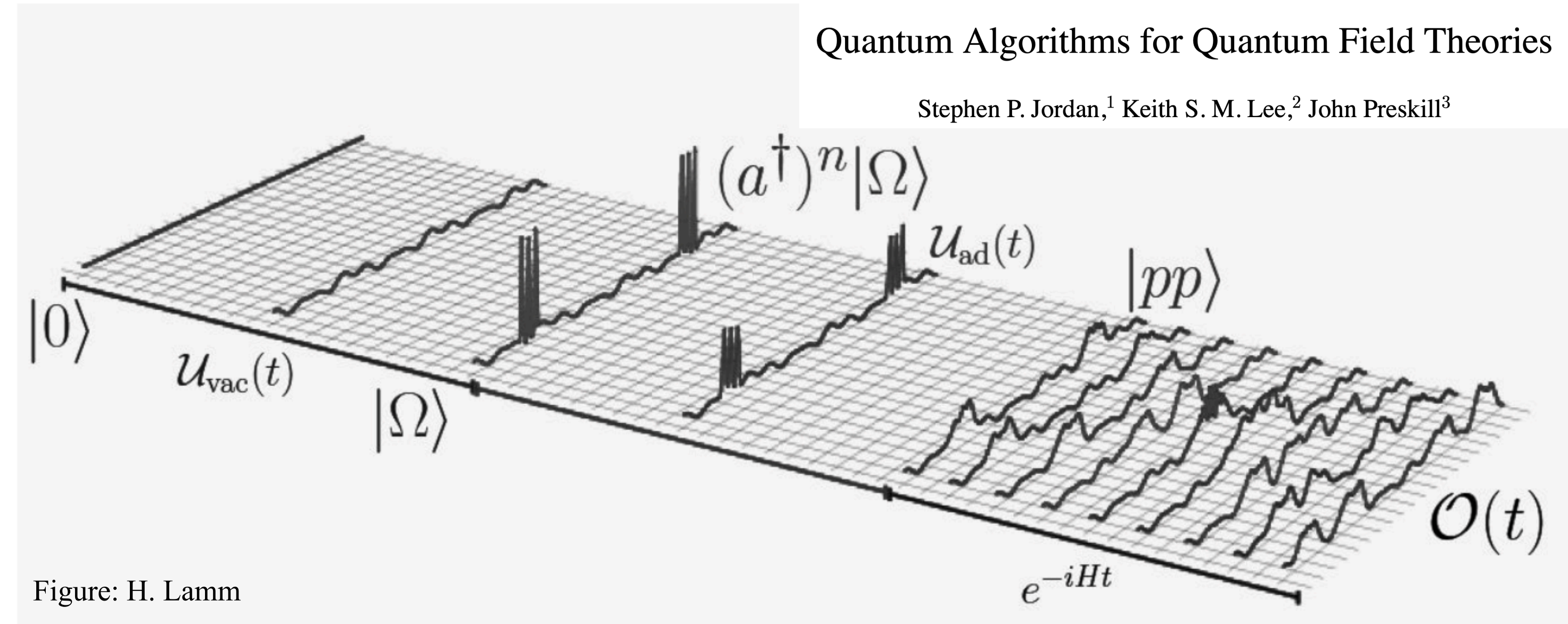


A master algorithm for scattering

[1111.3633] [1404.7115] [1112.4833]



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Other formulations for scalar theories

[Yeter-Aydeniz et al, 1811.12332]

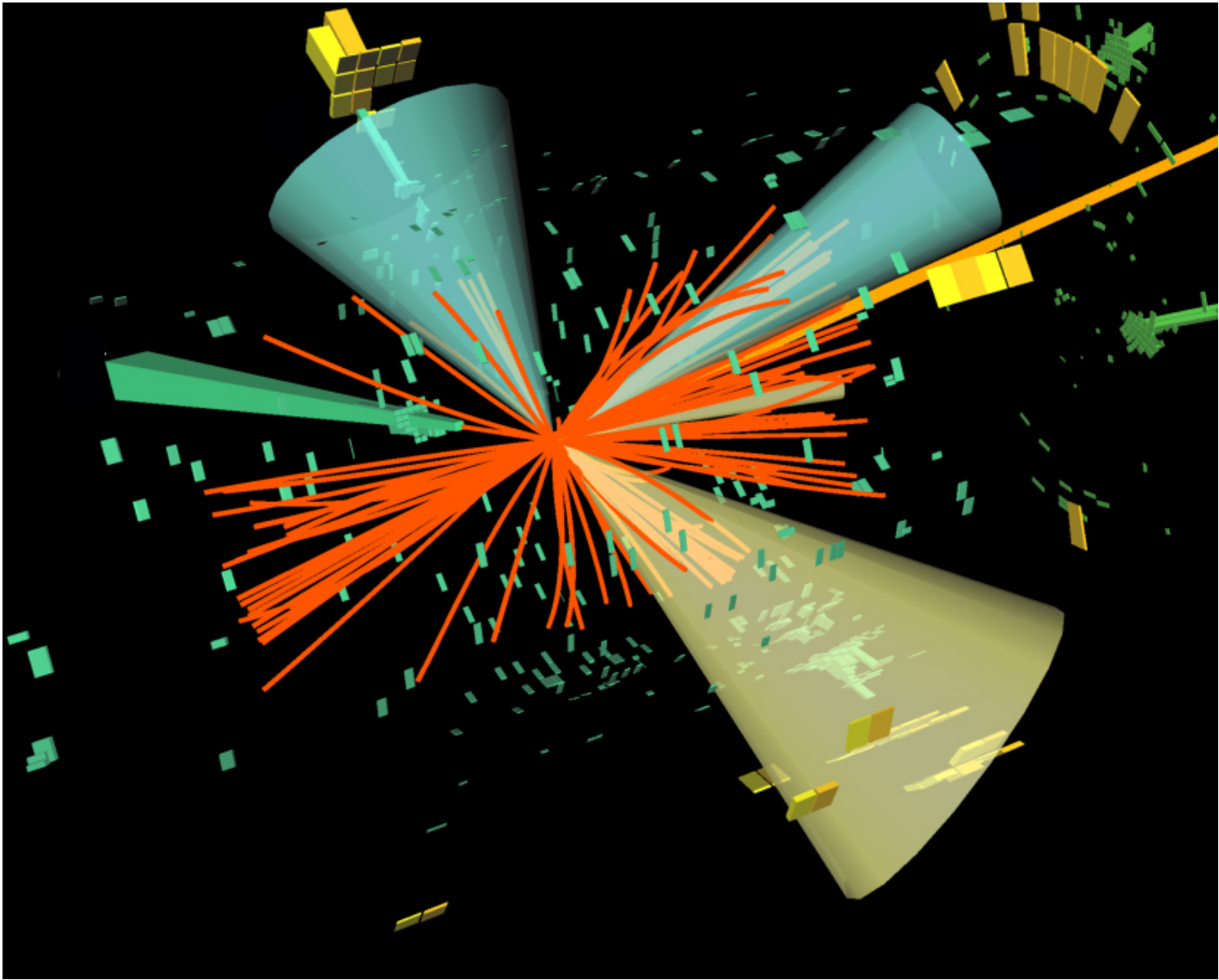
[Kloc, Savage, 1808.10378]

[Kreshchuk et al, 2002.04016]

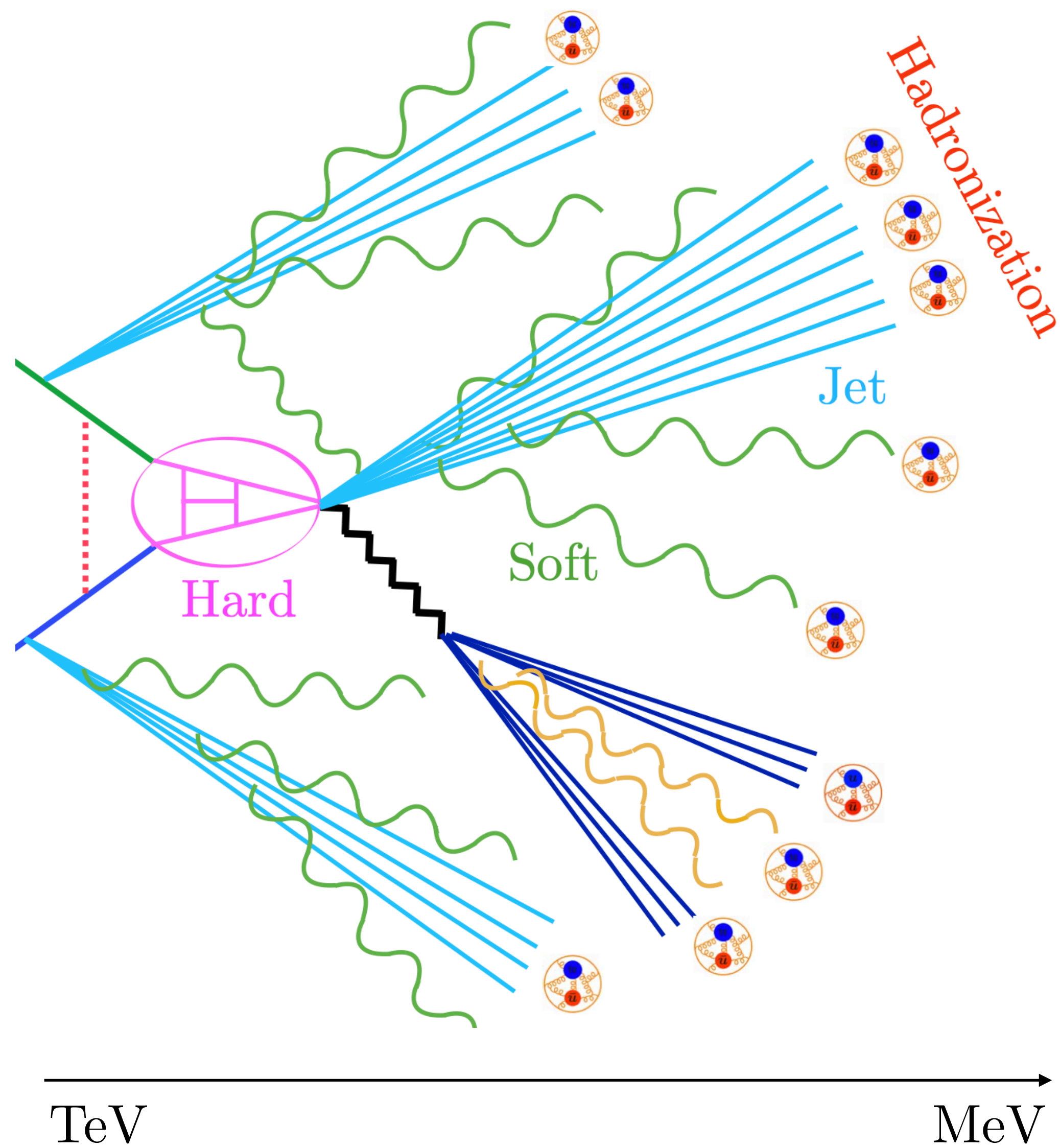
[JB, Mueller, Tarasov, Venugopalan, 2012.00020]

- Fundamentally hard problem: **physics from MeV to TeV !**
- Not guaranteed quantum methods can solve it efficiently

Divide and conquer



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Quantum computers for parton showers

[1904.03196]

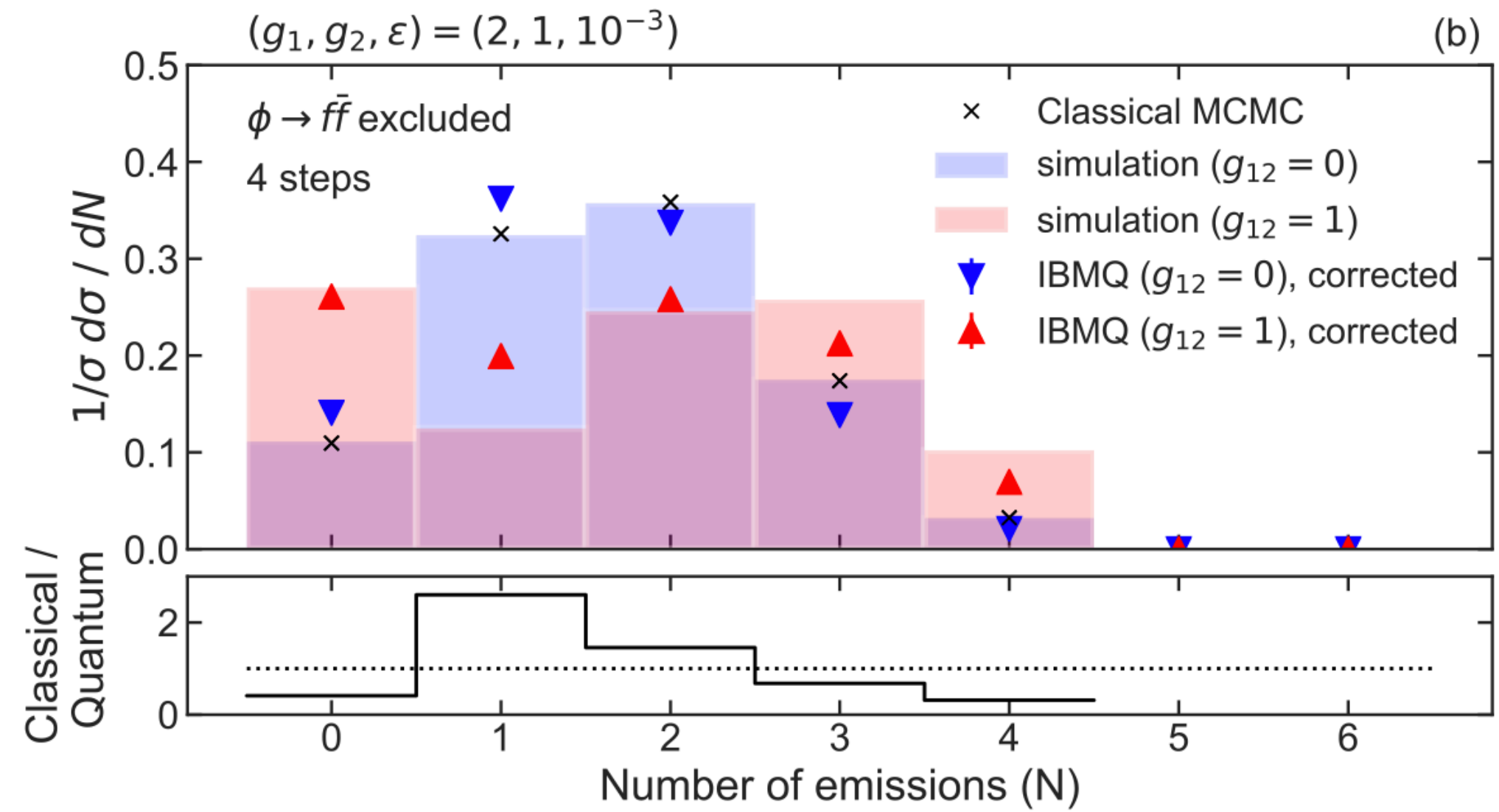
A quantum algorithm for high energy physics simulations

Benjamin Nachman,^{*} Davide Provasoli,[†] and Christian W. Bauer[‡]
Physics Division, Lawrence Berkeley National Laboratory, Berkeley, CA 94720, USA

Wibe A. de Jong[§]

Consider theory with non-diagonal flavor operator

$$\mathcal{L} = \bar{f}_1(i\partial + m_1)f_1 + \bar{f}_2(i\partial + m_2)f_2 + (\partial_\mu\phi)^2 + g_1\bar{f}_1f_1\phi + g_2\bar{f}_2f_2\phi + g_{12}[\bar{f}_1f_2 + \bar{f}_2f_1]\phi$$



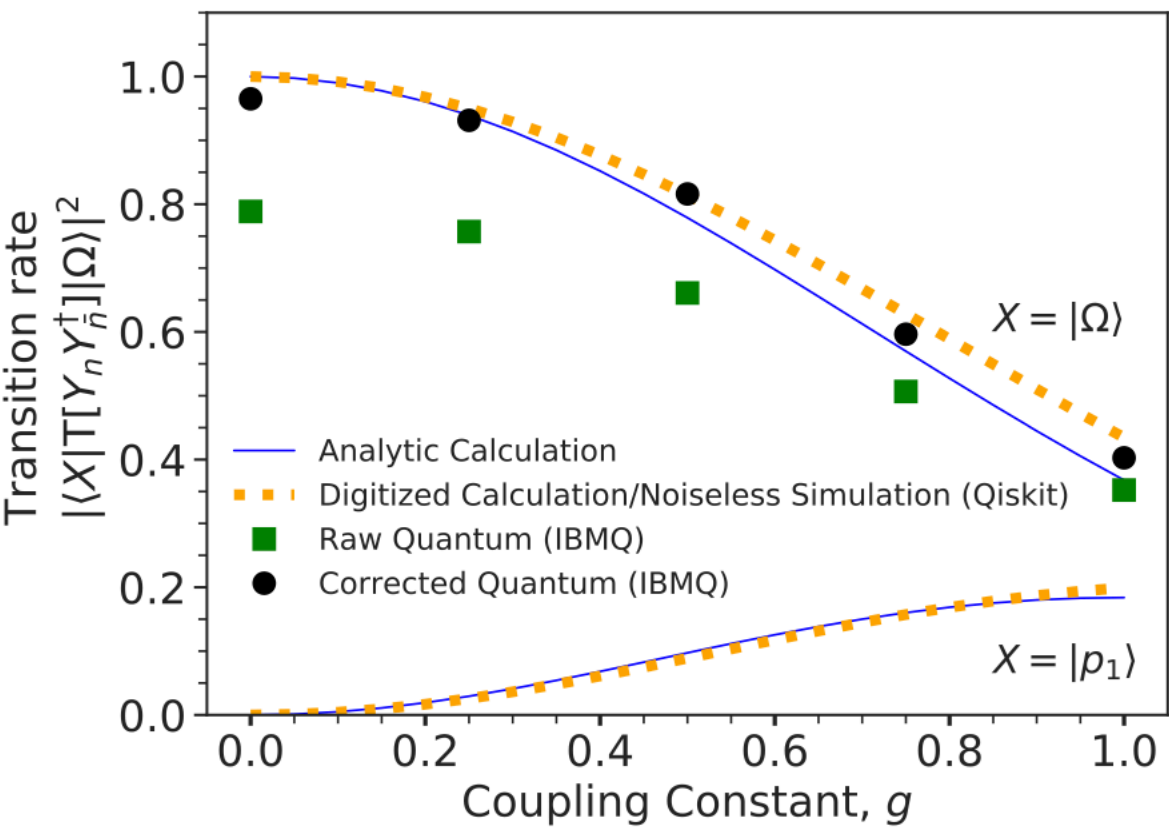
[2102.05044]

Simulating collider physics on quantum computers using effective field theories

Christian W. Bauer^{*} and Benjamin Nachman[†] Marat Freytsis[‡]

$$\sigma = H \otimes J_1 \otimes \cdots \otimes J_n \otimes S$$

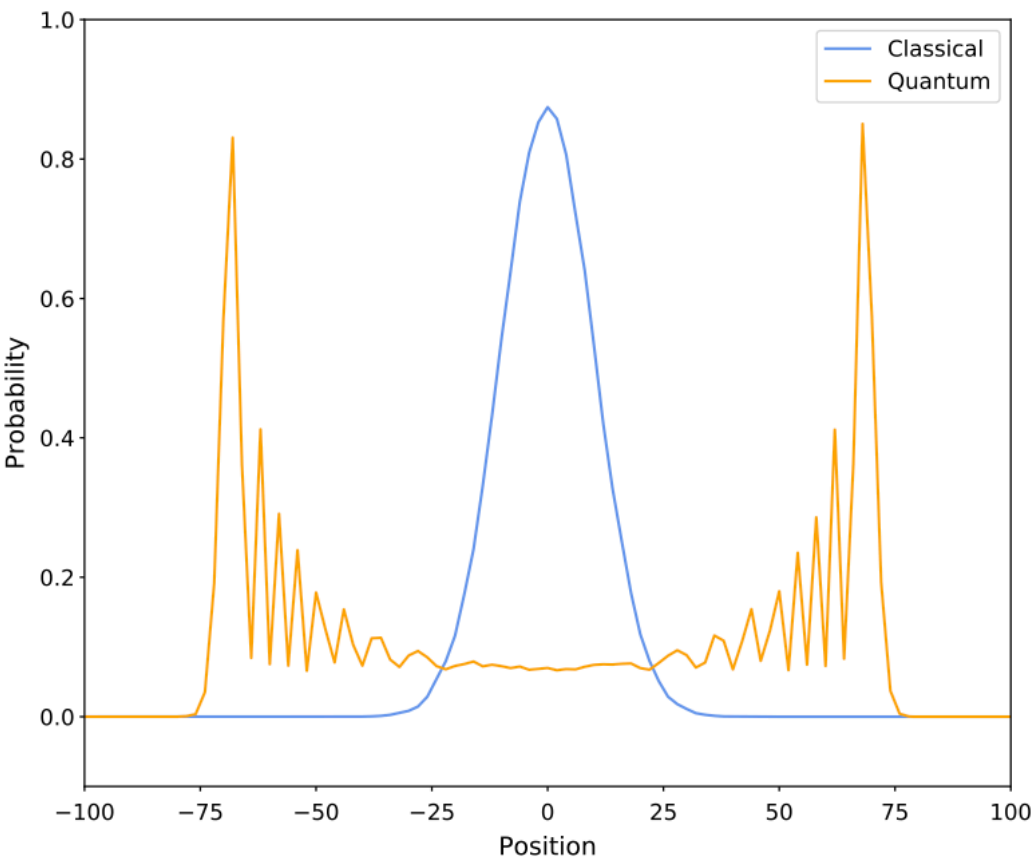
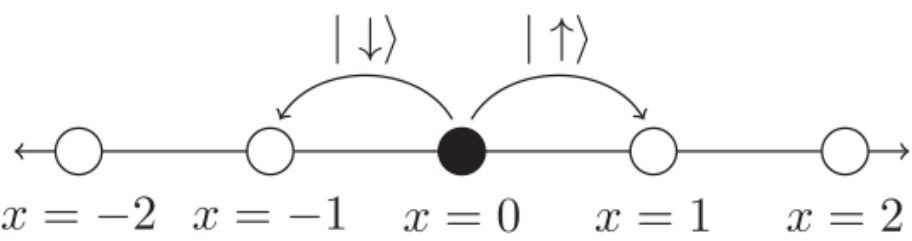
$$\langle X | T[Y_n Y_{\bar{n}}^\dagger] | \Omega \rangle$$



[2109.13975]

Quantum walk approach to simulating parton showers

Khadeejah Bepari,^a Sarah Malik,^b Michael Spannowsky^a and Simon Williams^c



[2010.03571] [2106.08394]

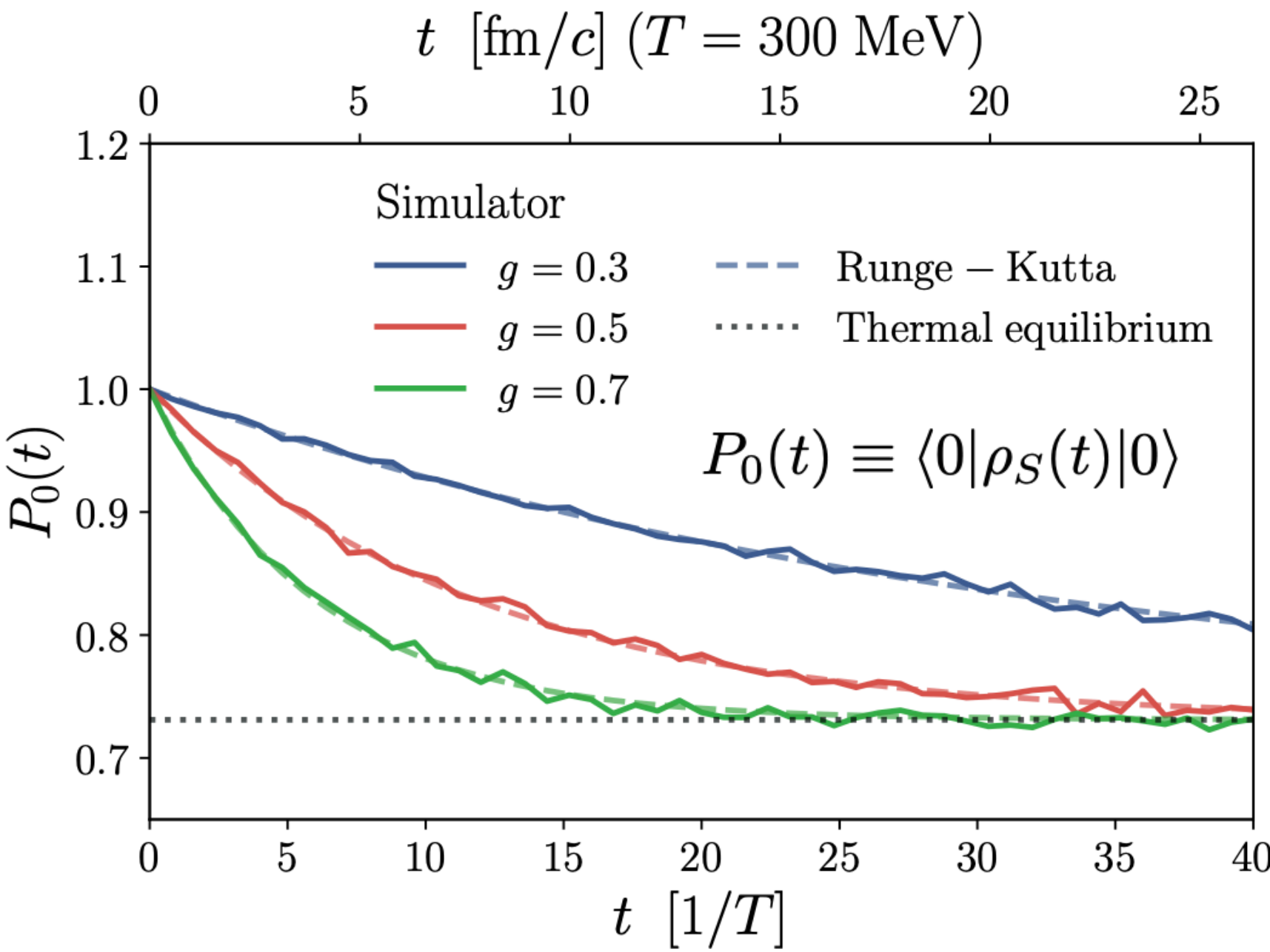
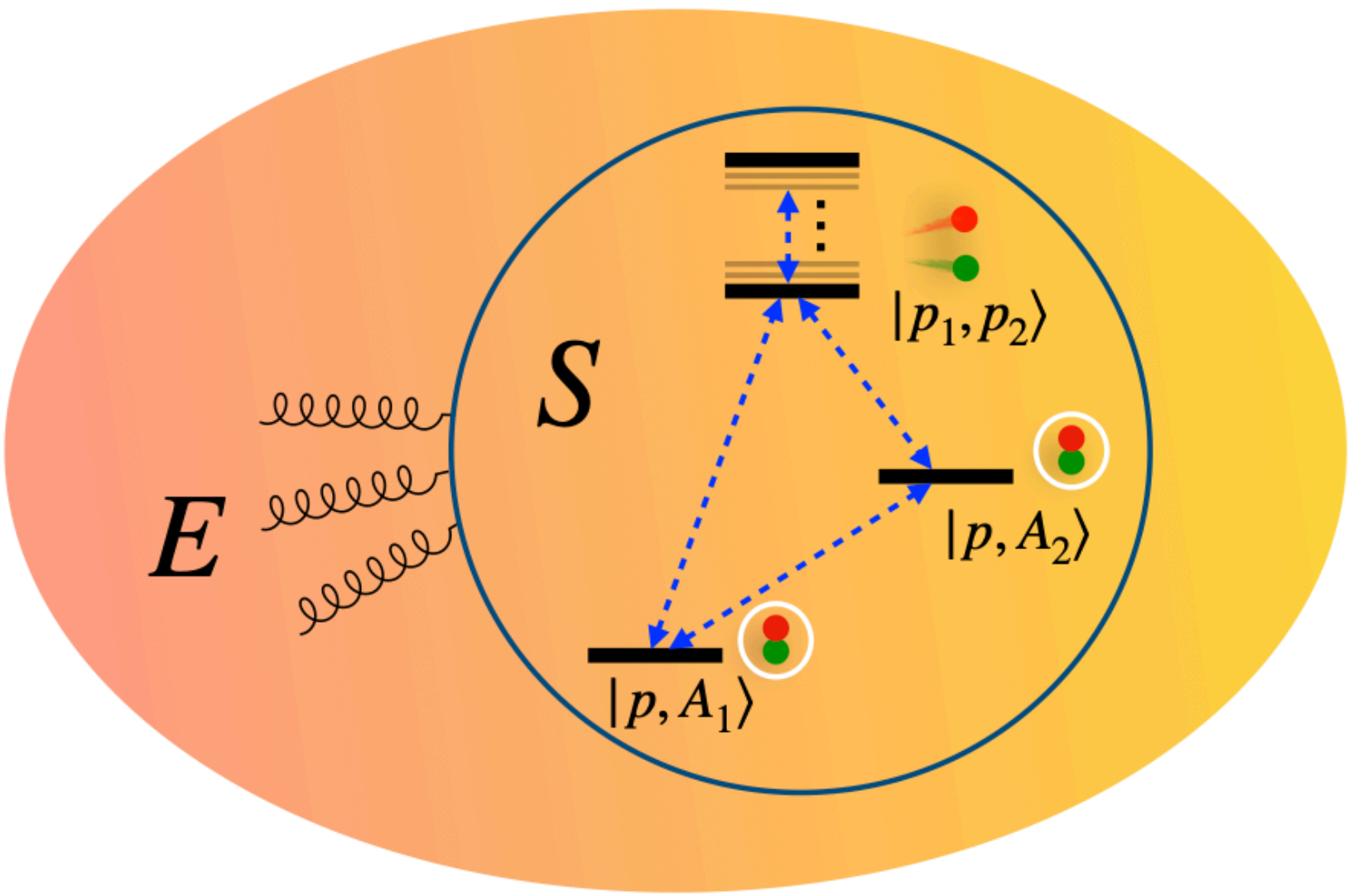
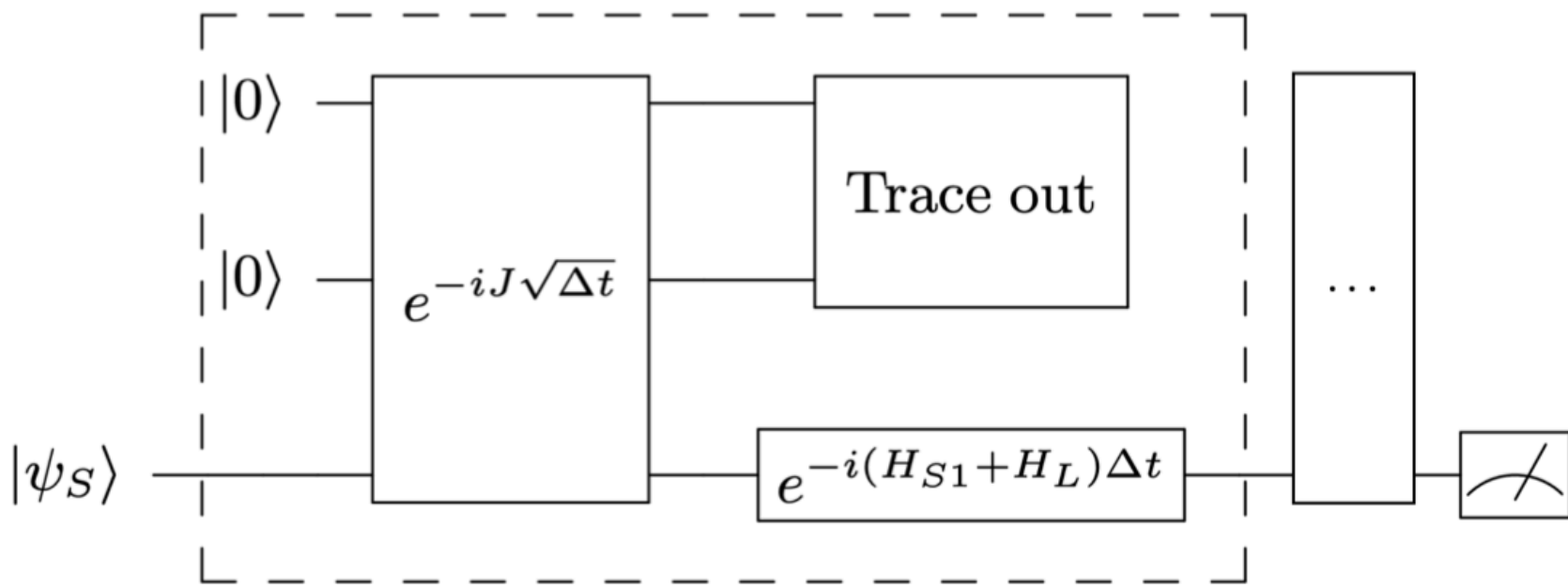
Quantum simulation of open quantum systems in heavy-ion collisions

Wibe A. de Jong,^{1,*} Mekena Metcalf,^{1,†} James Mulligan,^{2,3,‡}
Mateusz Płoskoń,^{2,§} Felix Ringer,^{2,¶} and Xiaojun Yao^{4,**}

Open quantum systems formulation for quarkonia, jets, ...

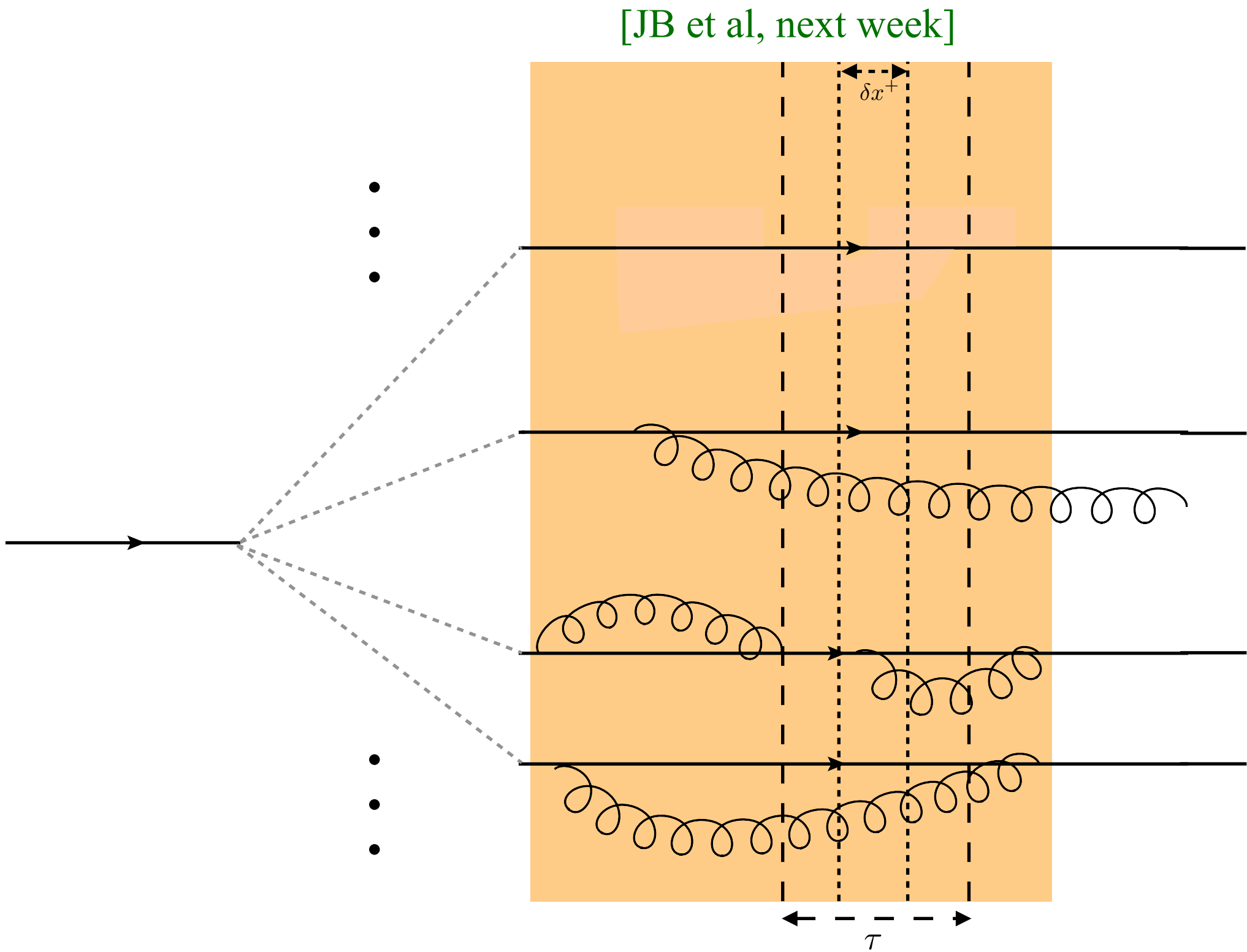
[Blaizot, Escobedo, 1711.10812, 1803.07996]
+ [Akamatsu, 2009.10559]

Quantum circuit for Lindbladian evolution



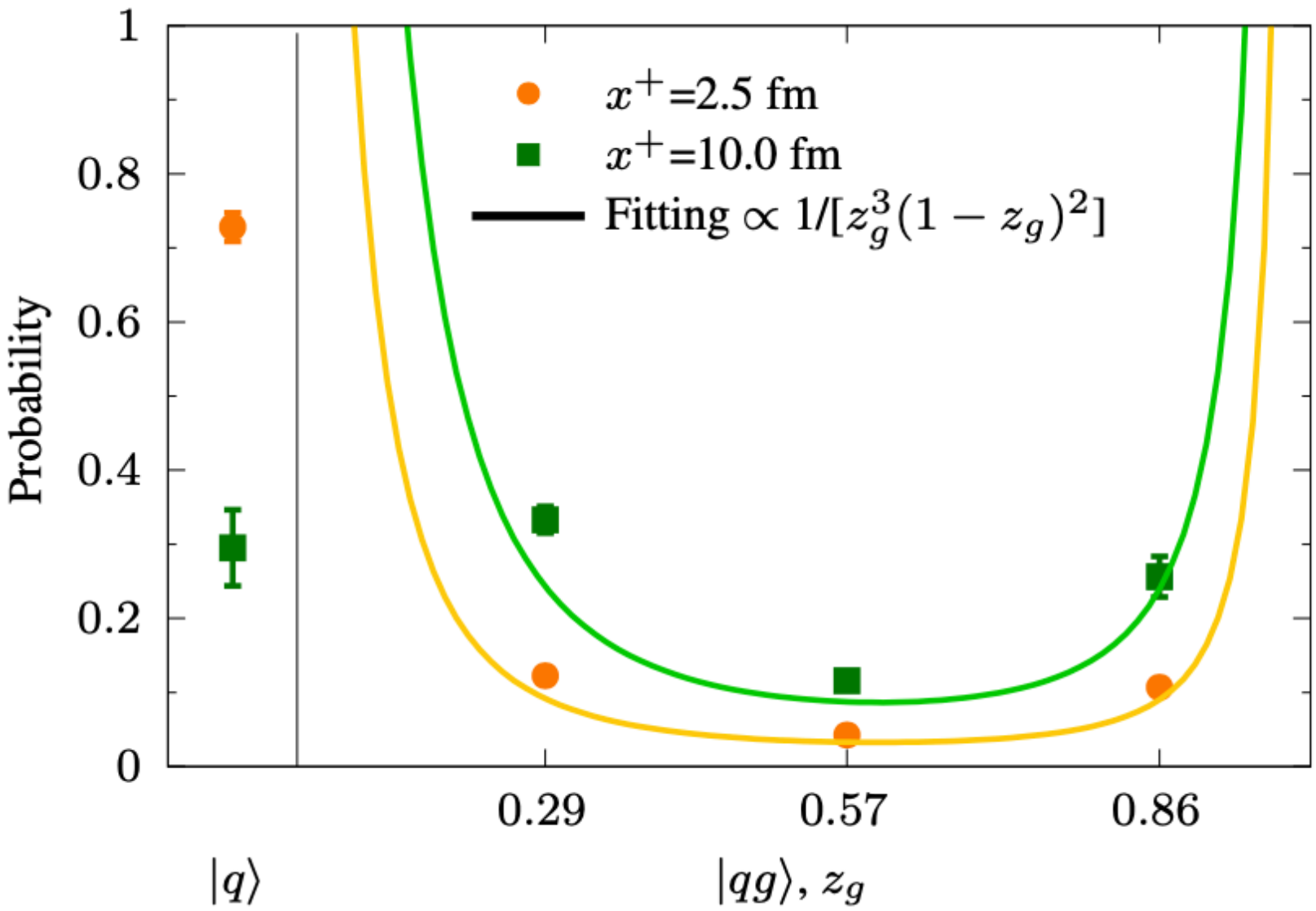
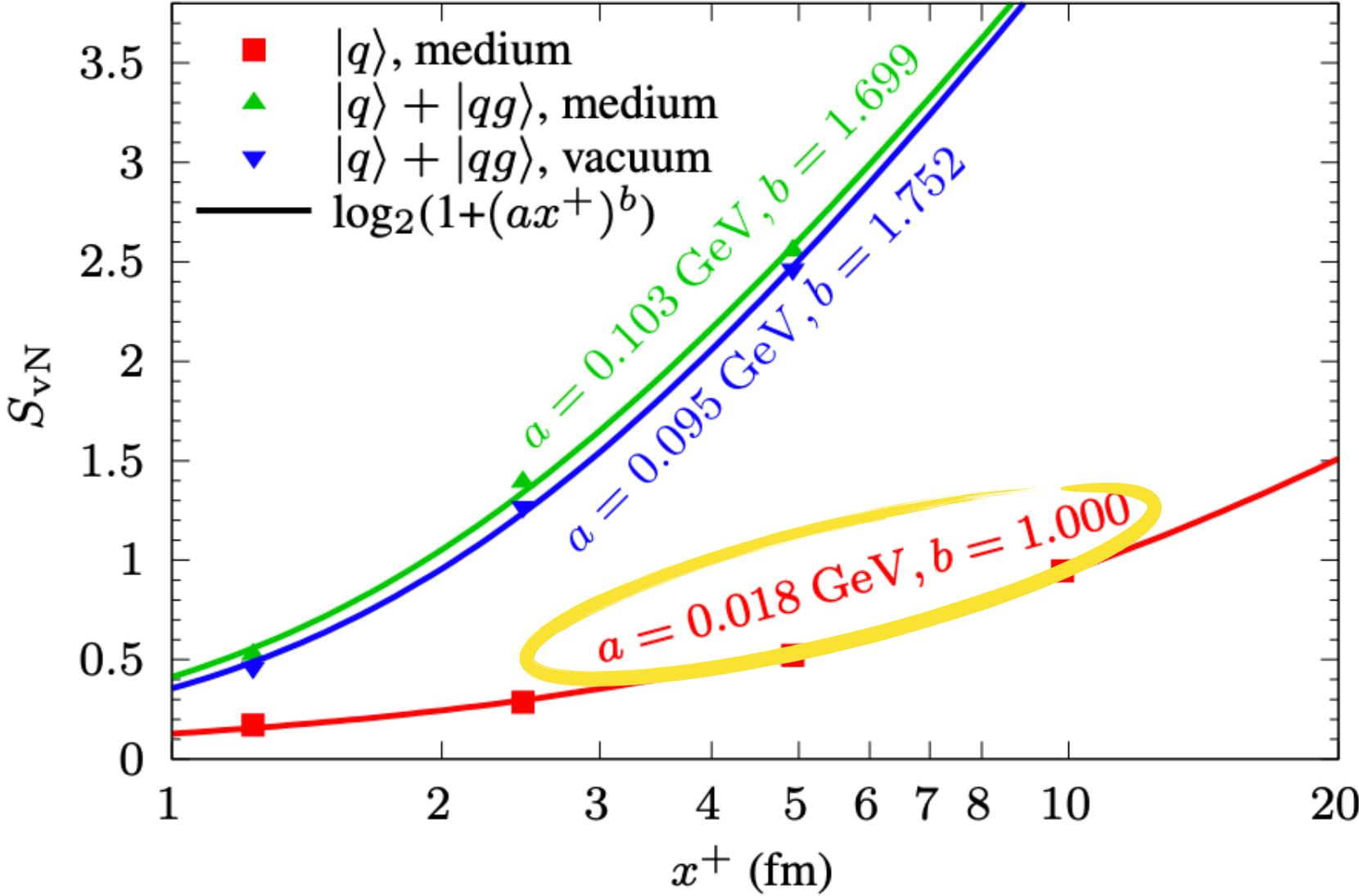
QIS for probes of nuclear matter

Light Front approach using CGC picture



See also: [JB, Salgado, 2104.04661]
[Li, Lappi, Zhao, 2107.02225]
[JB et al, 2208.06750]
[Yao, 2205.07902]

[JB, Blaizot, Mehtar-Tani, 2305.10476]



Pair production

Schwinger effect: intense electric fields can lead to proliferation of particle pairs out of the vacuum

Pair-production rate computed in the semi-classical limit (no back-reaction) [Schwinger, 1951]

Atomic Quantum Simulation of Dynamical Gauge Fields coupled to Fermionic Matter:
From String Breaking to Evolution after a Quench

D. Banerjee¹, M. Dalmonte^{2,3}, M. Müller⁴, E. Rico^{2,3}, P. Stebler¹, U.-J. Wiese¹, and P. Zoller^{2,3,5}

Real-time Dynamics in U(1) Lattice Gauge Theories with Tensor Networks

T. Pichler,¹ M. Dalmonte,^{2,3} E. Rico,^{4,5,6} P. Zoller,^{2,3} and S. Montangero¹

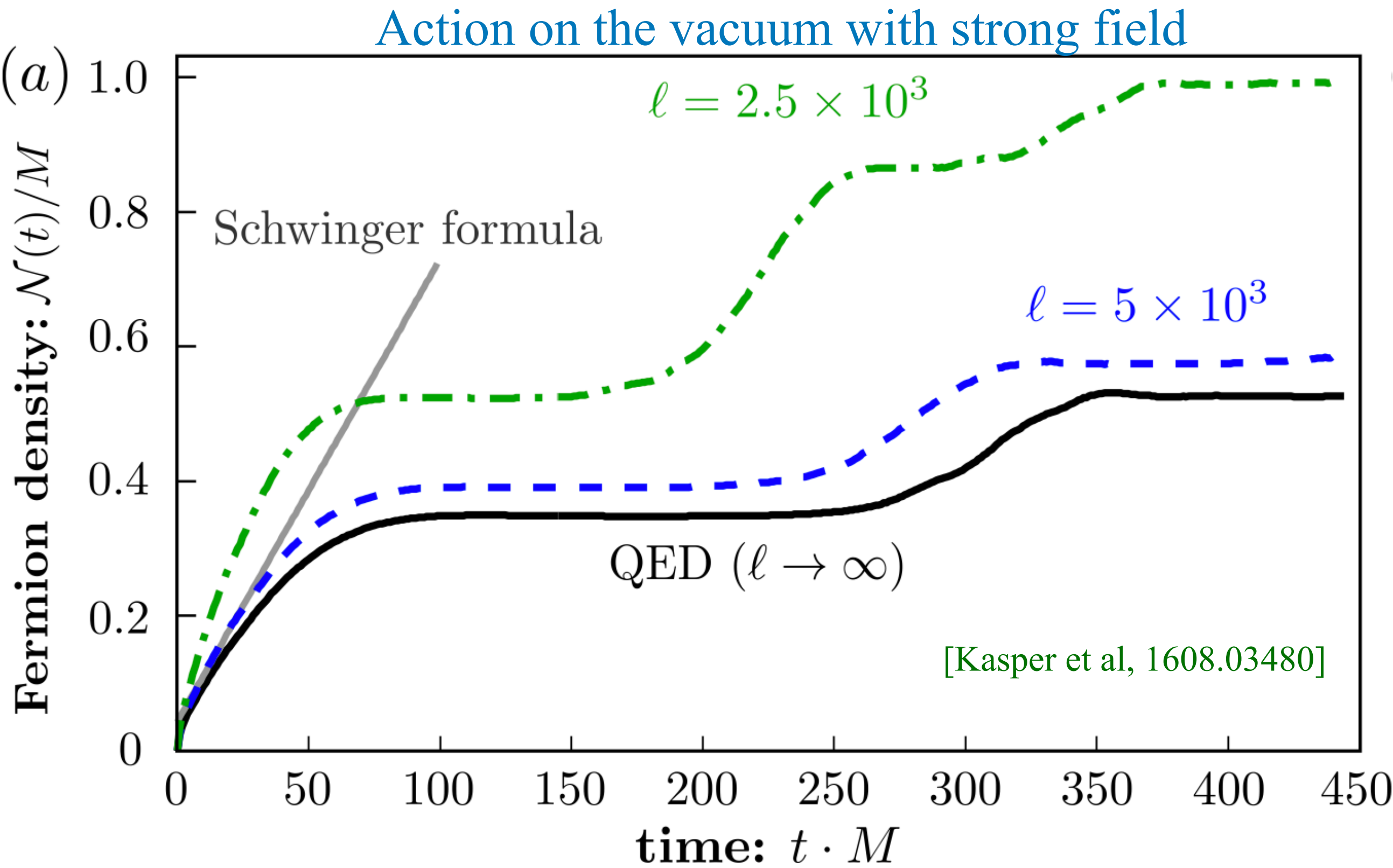
Schwinger pair production with ultracold atoms

V. Kasper^{a,*}, F. Hebenstreit^b, M. K. Oberthaler^c, J. Berges^a

Implementing quantum electrodynamics with ultracold atomic systems

V. Kasper,^{1,2,*} F. Hebenstreit,³ F. Jendrzejewski,⁴ M. K. Oberthaler,⁴ and J. Berges¹

...

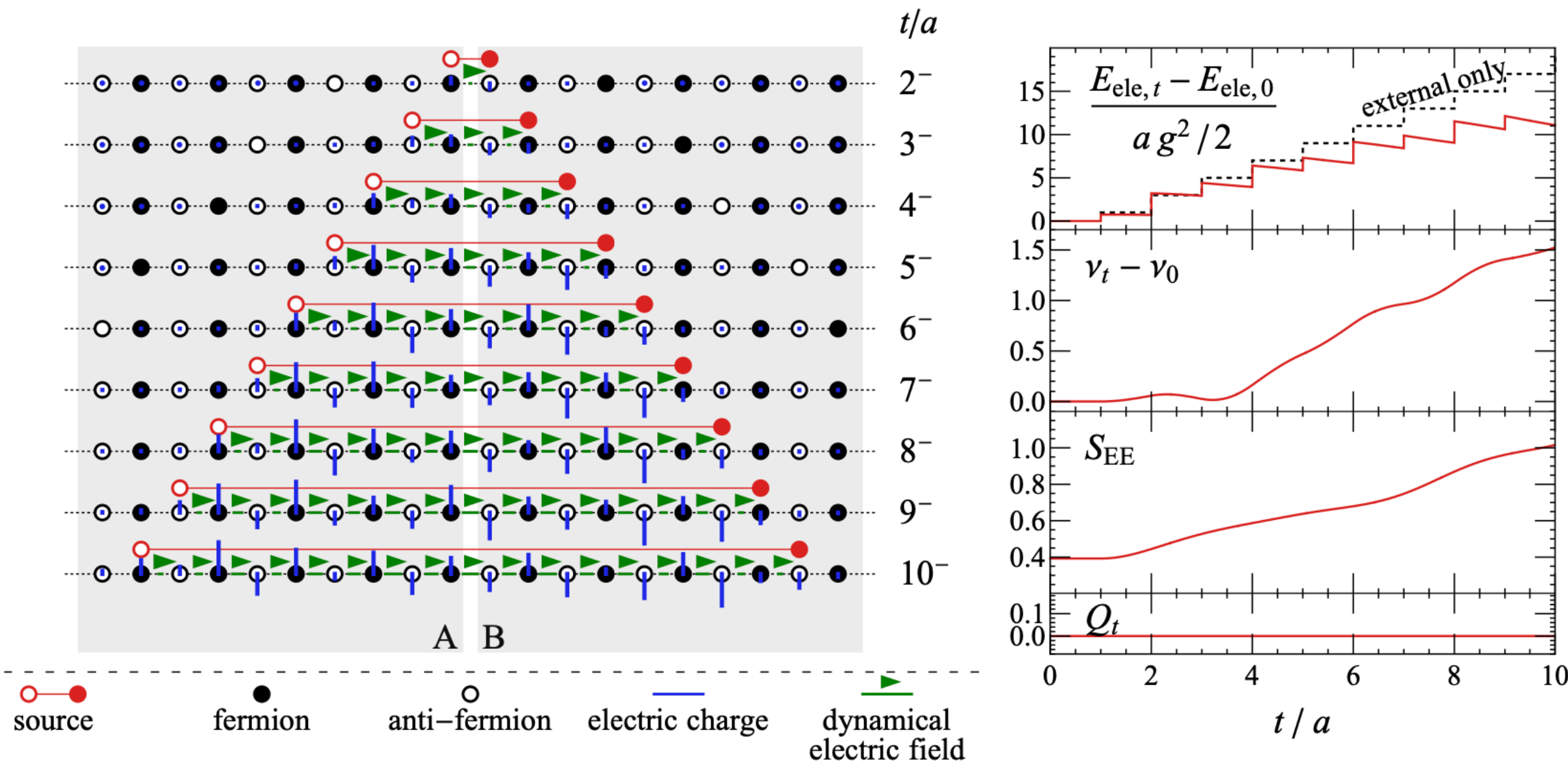


From pair production to QCD string breaking

In QCD: Schwinger effect drives hadronization models, it is responsible for string breaking

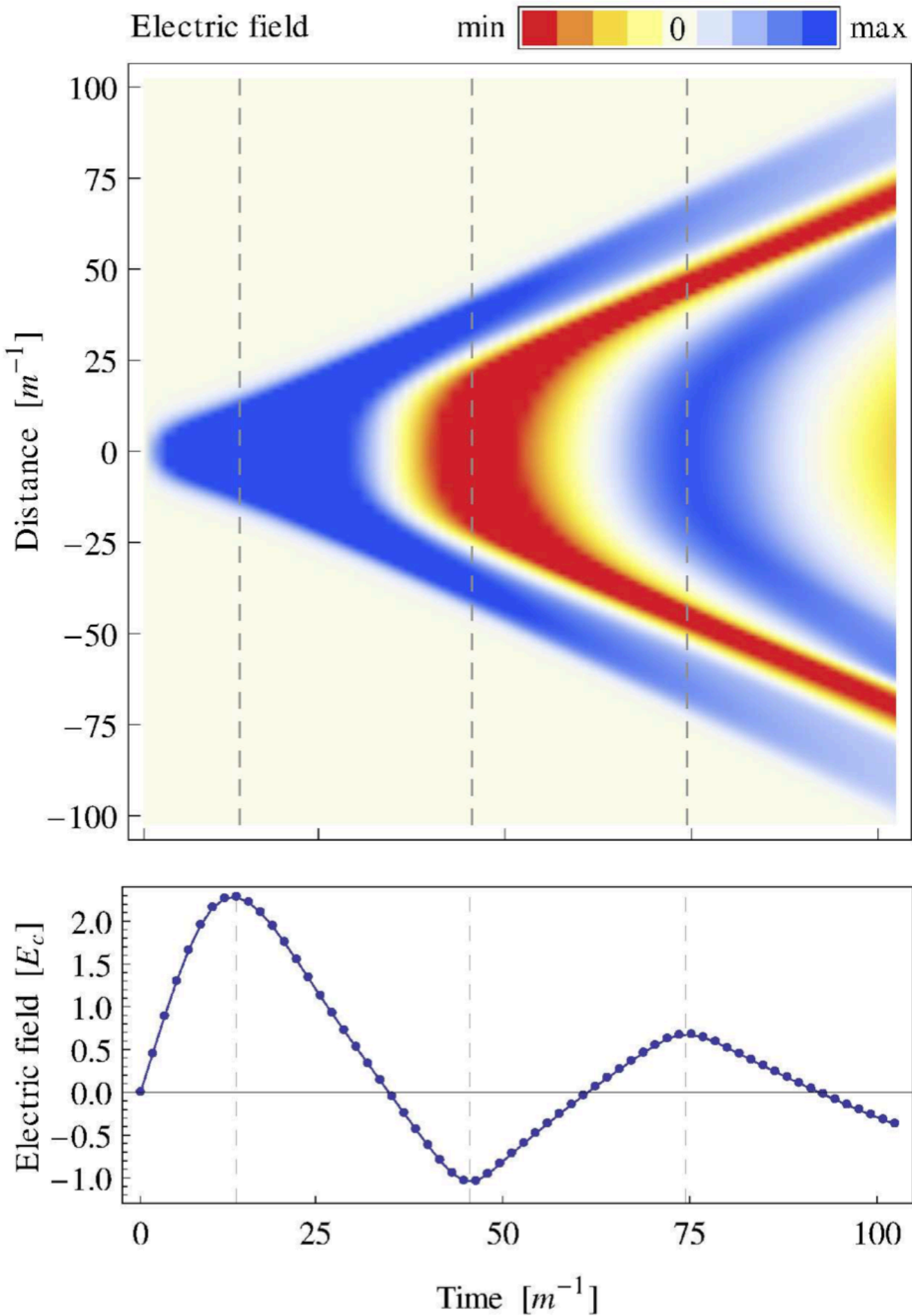
Fully dynamical simulations exhibit multiple strings

Pair production modifies the vacuum in between fast moving charges



[Florio et al, 2301.11991]

A simple model for jet induced modifications to the soft sector (?)



[Hebenstreit, Berges, Gelfand, 1307.4619]

Spin correlations as probes of QCD strings

Hyperon spin correlations might give access to QCD string evolution and entanglement spectrum

[Gong, Parida, Tu, Venugopalan, 2107.13007]

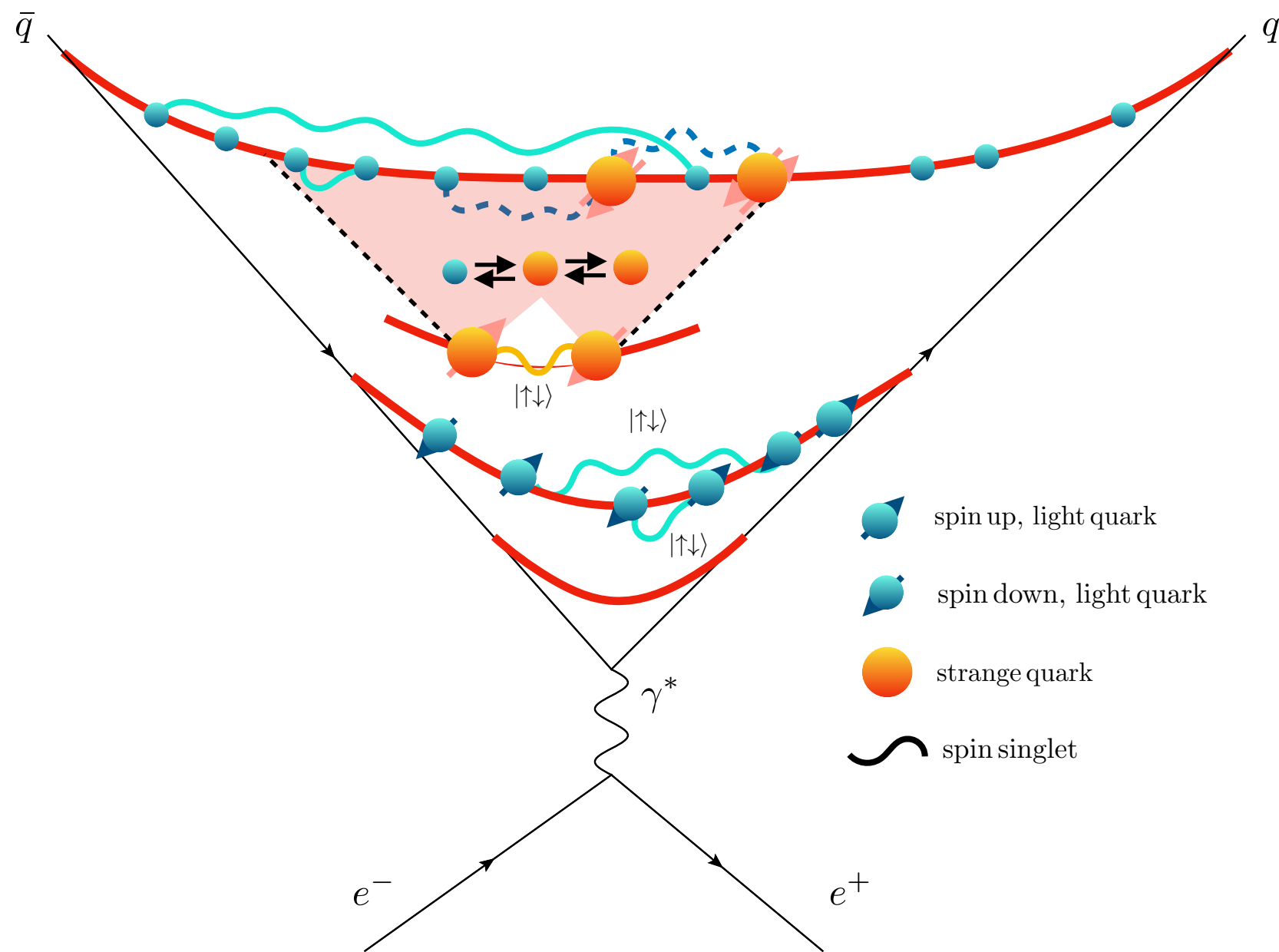
Entanglement in static string configurations

$$\frac{P(|\hat{n}_1\rangle, |\hat{n}_2\rangle)}{P(|\hat{n}_1\rangle)P(|\hat{n}_2\rangle)} = 1 - \frac{a}{(a + b/2)^2} \cos(\theta_2 - \theta_1)$$

a= # strange pairs b= # light quarks

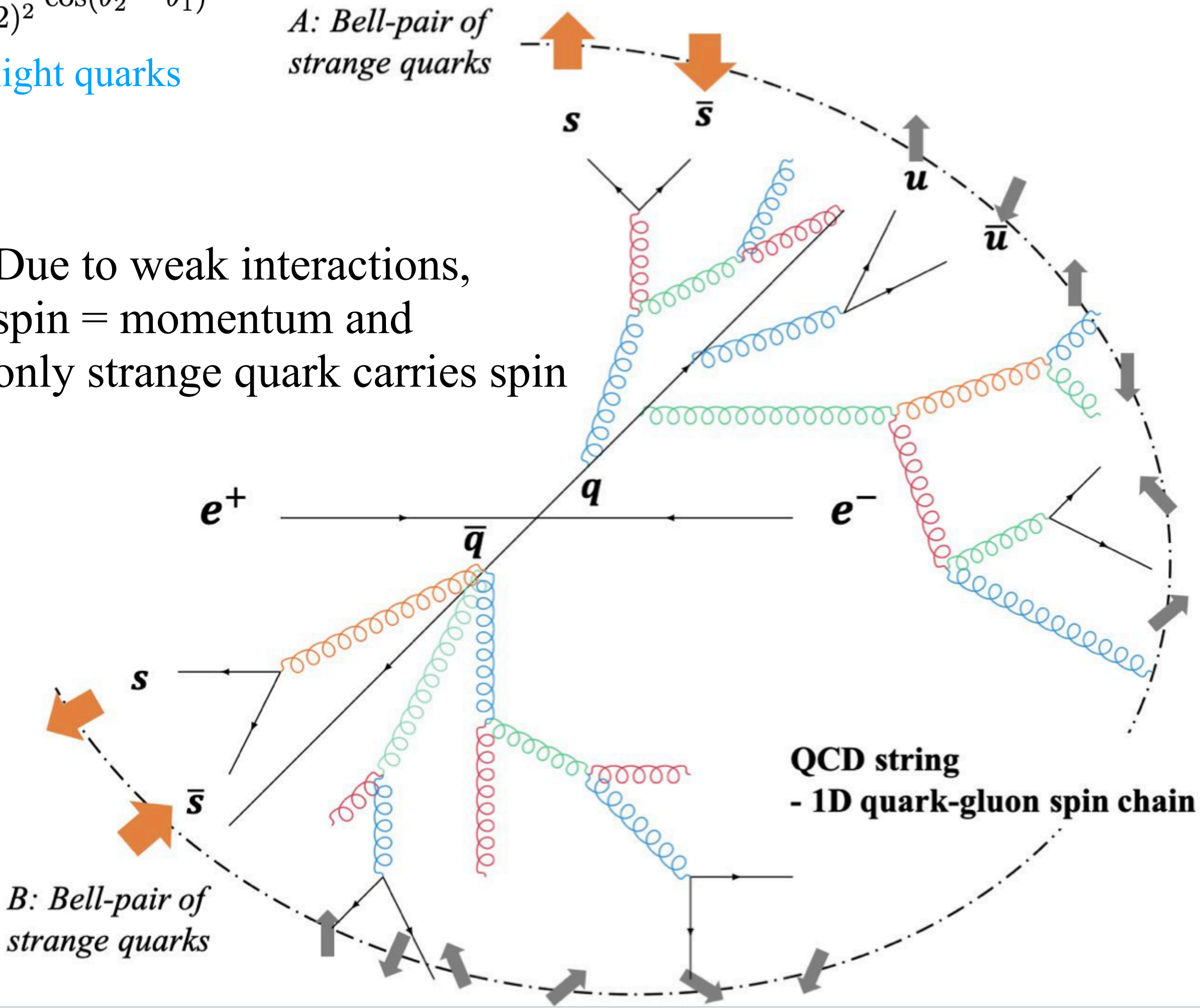
Corollary 2. If the magnitude of the coefficient of $\cos(\theta_{ab})$ in a symmetric rotationally invariant correlation function is $> \frac{1}{2}$, then the measured state ρ_{ab} is entangled.

Extended to 1+1d QFT with spin degrees of freedom



[JB, Gong, Venugopalan, 2306.xxxxx]

Due to weak interactions, spin = momentum and only strange quark carries spin



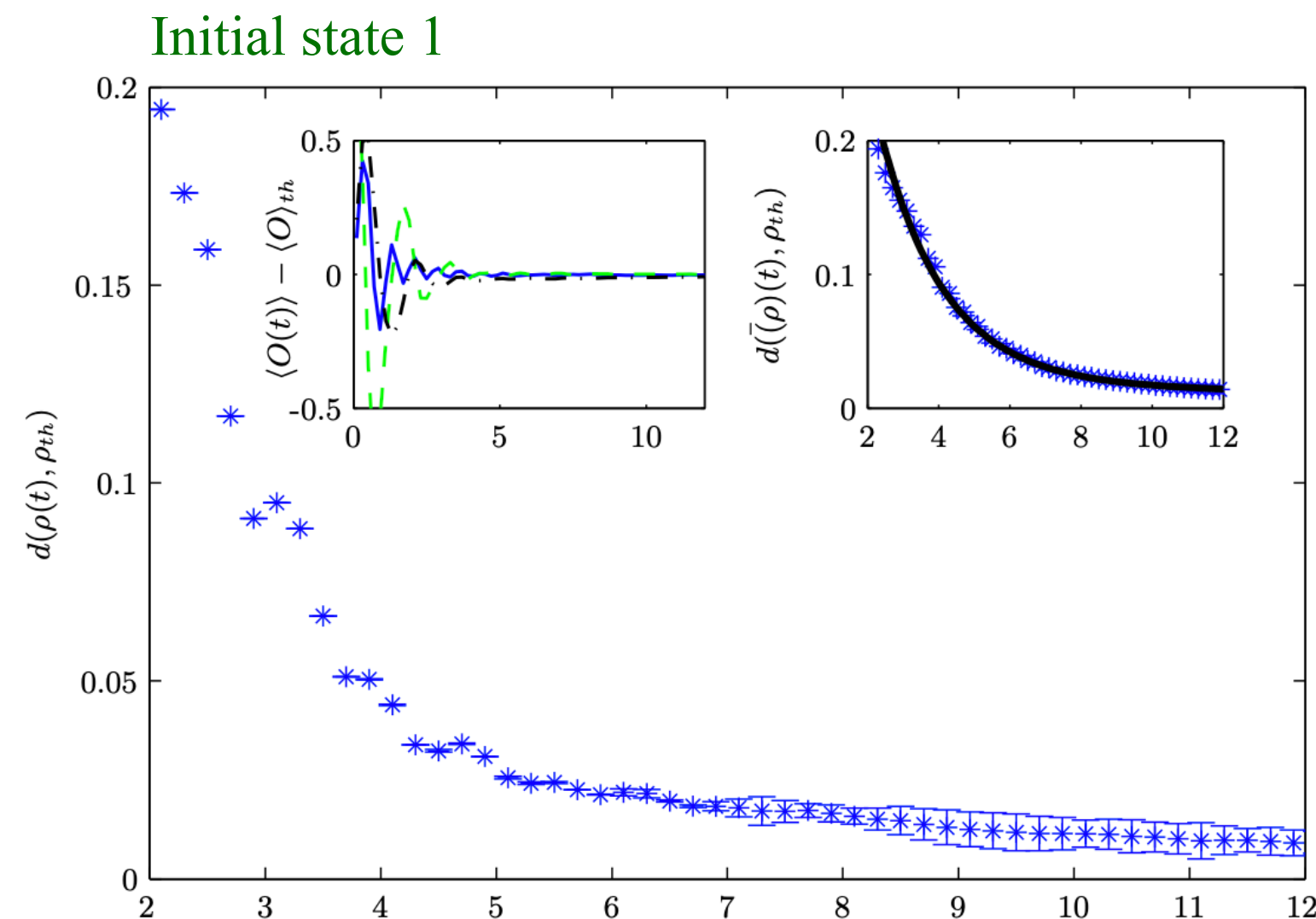
Thermalization in gauge theories

[Kinoshita, Wenger, Weiss, Nature 440, 2006]

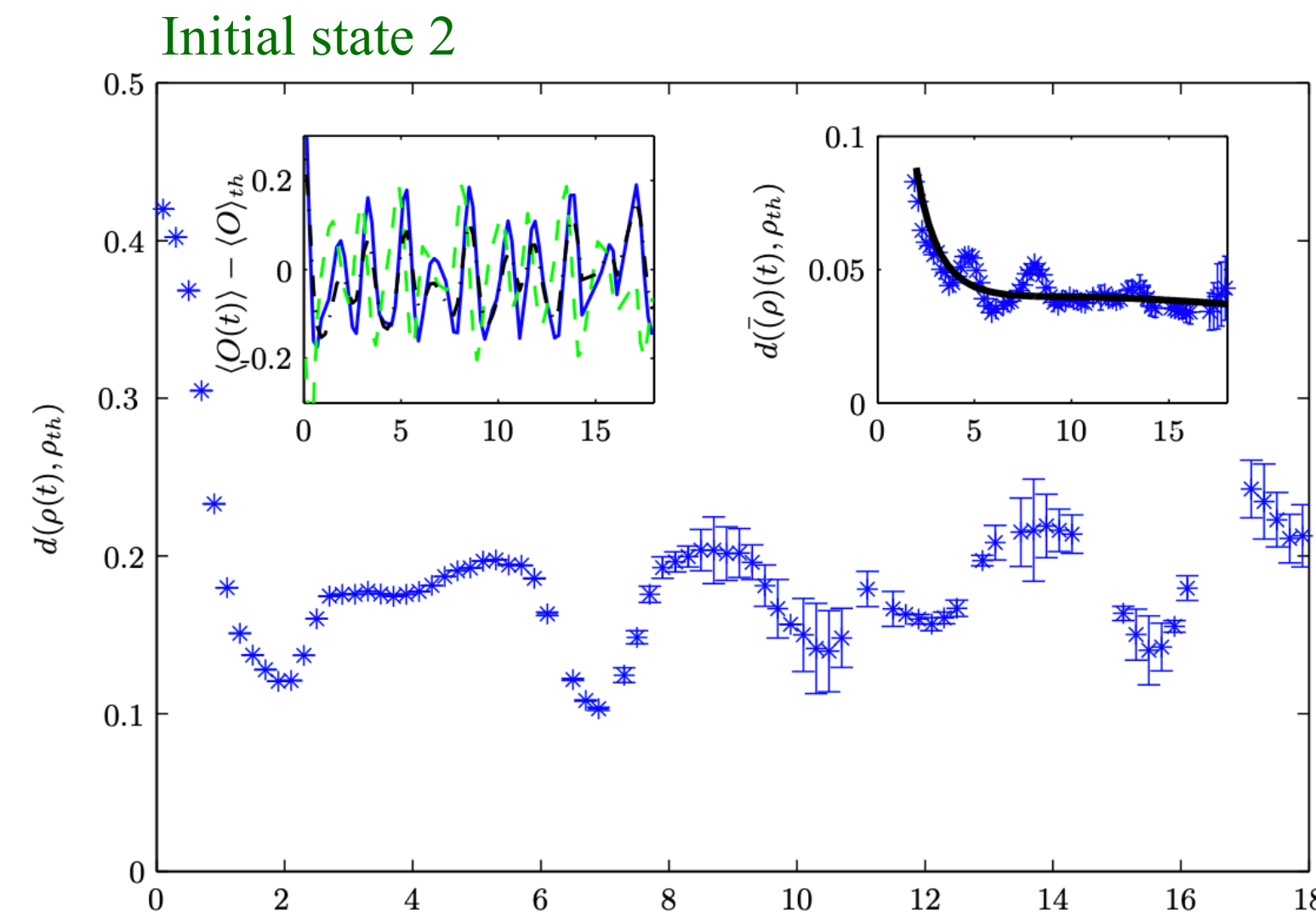
Early studies driven by surprising experimental results for nearly integrable systems

Strong and weak thermalization of infinite non-integrable quantum systems

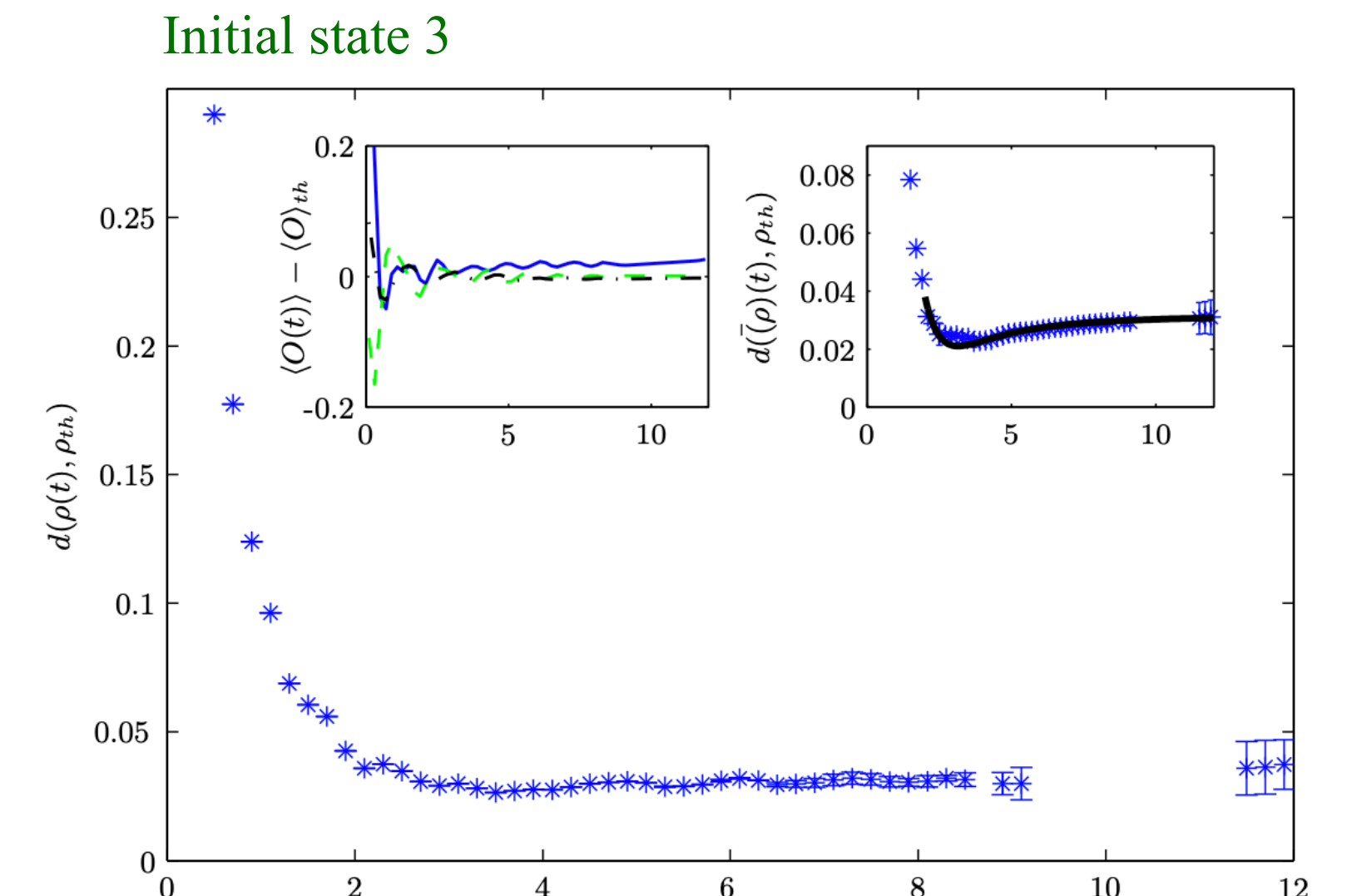
M. C. Bañuls,^{1,*} J. I. Cirac,¹ and M. B. Hastings²



Strong thermalization



Weak thermalization



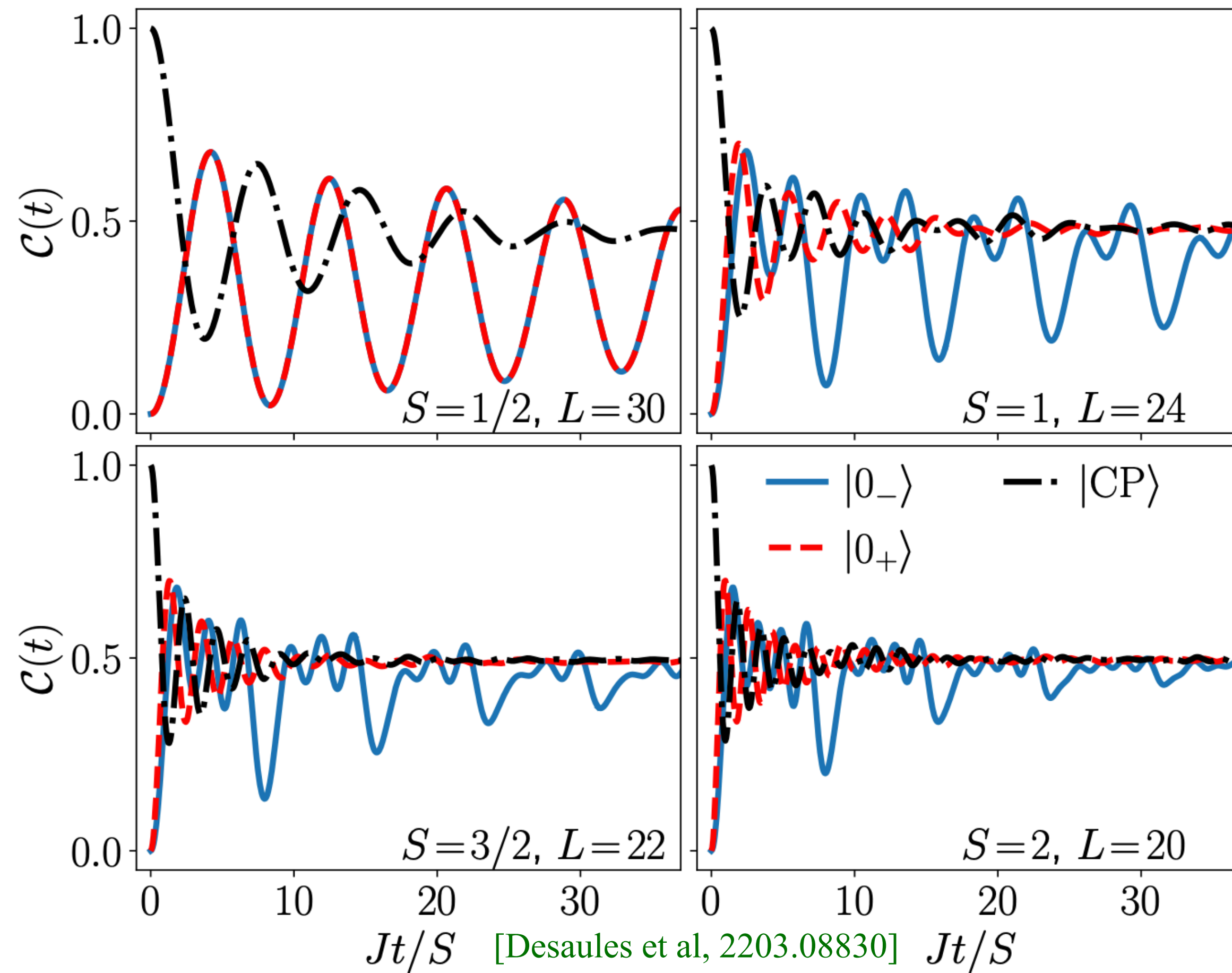
No thermalization

$$H = - \sum_i \sigma_z^{[i]} \otimes \sigma_z^{[i+1]} - g \sum_i \sigma_x^{[i]} - h \sum_i \sigma_z^{[i]} \quad (\text{in general non-integrable})$$

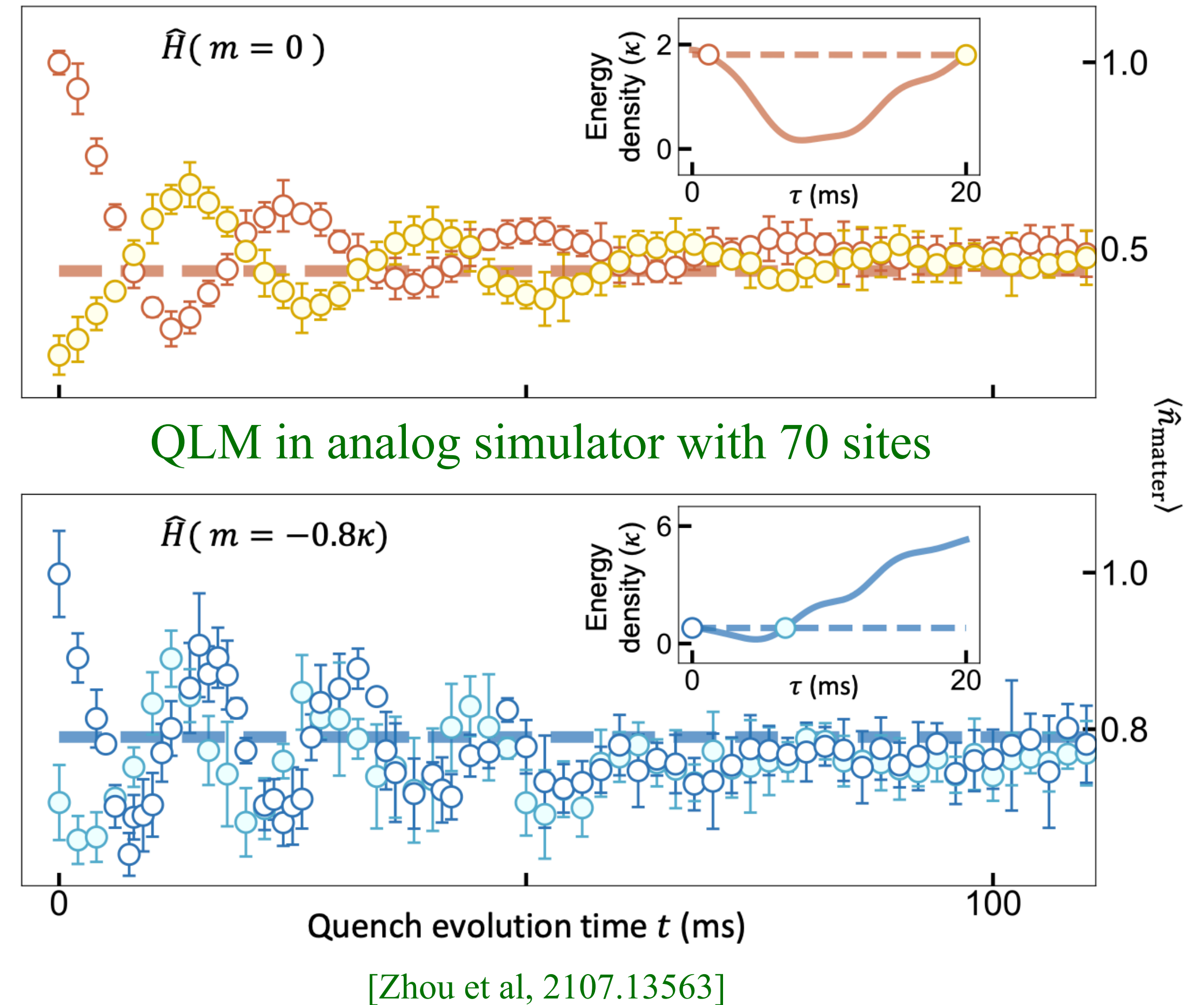
Thermalization in gauge theories

The same occurs in QLMs !

Chiral condensate for several initial conditions



For generic initial conditions = thermalization

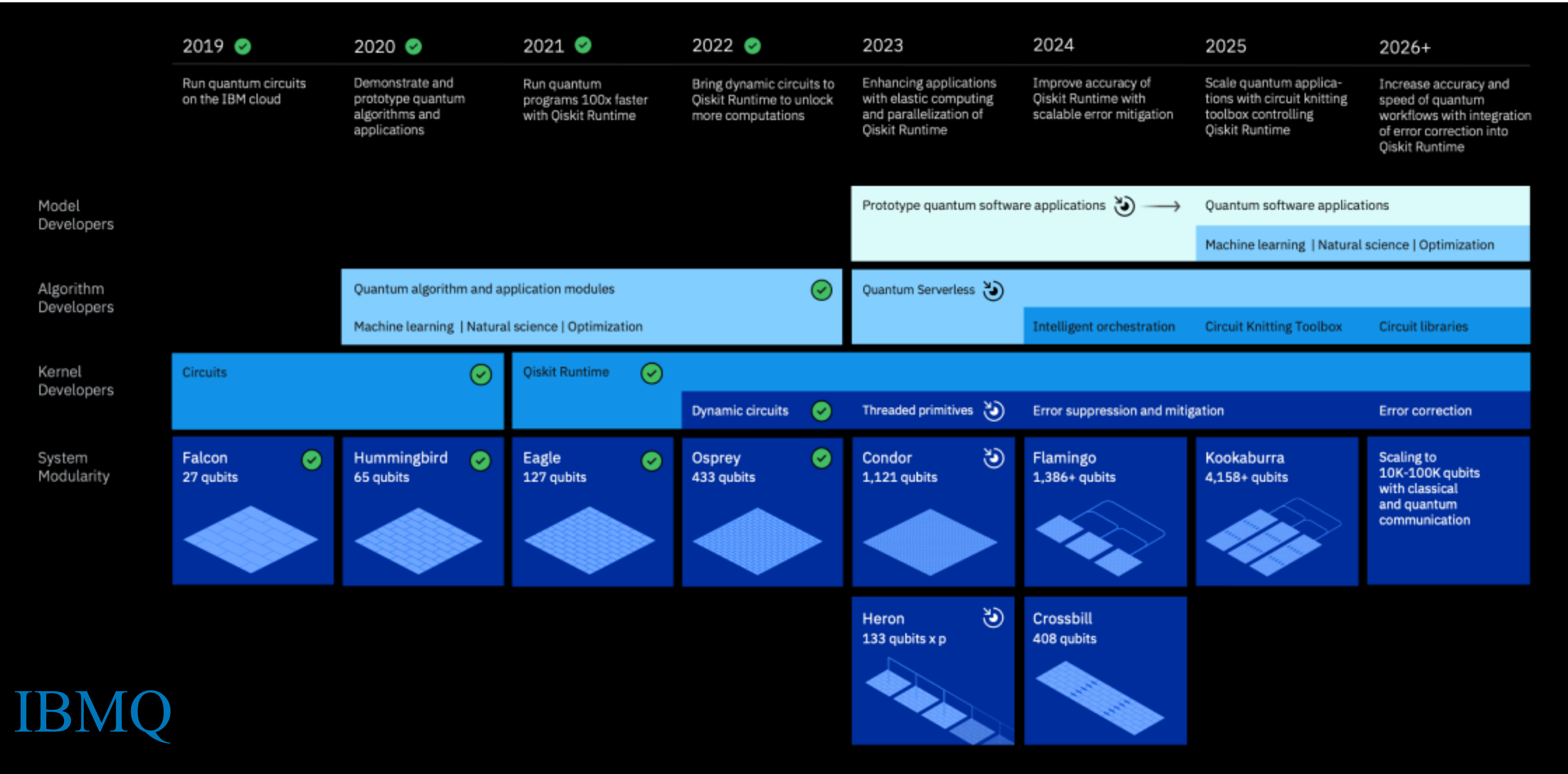


Connection to many interesting concepts in QFT: quantum scars, quantum chaos, out of time correlations, ETH, ...

Some key ideas

1

QIS technologies are growing at a fast pace



2

Resurgence of old ideas under a new light

PHYSICAL REVIEW D VOLUME 13, NUMBER 4 15 FEBRUARY 1976

Strong-coupling calculations of lattice gauge theories: (1 + 1)-dimensional exercises

T. Banks and Leonard Susskind*
Tel Aviv University, Tel Aviv, Israel

John Kogut†
Laboratory of Nuclear Studies, Cornell University, Ithaca, New York 14853
(Received 25 August 1975)

1975

MORE ABOUT THE MASSIVE SCHWINGER MODEL*

Sidney Coleman

Lyman Laboratory of Physics
Harvard University
Cambridge, Mass. 02138

1976

**Atomic Quantum Simulation of Dynamical Gauge Fields coupled to Fermionic Matter:
From String Breaking to Evolution after a Quench**

D. Banerjee¹, M. Dalmonte^{2,3}, M. Müller⁴, E. Rico^{2,3}, P. Stebler¹, U.-J. Wiese¹, and P. Zoller^{2,3,5}

2012

Implementing quantum electrodynamics with ultracold atomic systems

V. Kasper,^{1,2,*} F. Hebenstreit,³ F. Jendrzejewski,⁴ M. K. Oberthaler,⁴ and J. Berges¹

2016

3

There is a wealth of other works I did not cover

Lattice Gauge Theory applications

Entanglement measures and non-pert. QCD

Foundations of QM in the LHC era

Phase structure of Gauge Theories

Chiral dynamics

Back ups

Quantum Simulation for HEP 2204.03381

Submitted to the Proceedings of the US Community Study
on the Future of Particle Physics (Snowmass 2021)

Quantum Simulation for High Energy Physics

Quantum Computers and Simulators for Lattice 1911.00003

Simulating Lattice Gauge Theories within Quantum Technologies

M.C. Bañuls^{1,2}, R. Blatt^{3,4}, J. Catani^{5,6,7}, A. Celi^{3,8}, J.I. Cirac^{1,2}, M. Dalmonte^{9,10}, L. Fallani^{5,6,7}, K. Jansen¹¹,
M. Lewenstein^{8,12,13}, S. Montangero^{7,14} ^a, C.A. Muschik³, B. Reznik¹⁵, E. Rico^{16,17} ^b, L. Tagliacozzo¹⁸, K. Van
Acoleyen¹⁹, F. Verstraete^{19,20}, U.-J. Wiese²¹, M. Wingate²², J. Zakrzewski^{23,24}, and P. Zoller³

Introduction to Tensor Networks 1306.2164

A Practical Introduction to Tensor Networks:
Matrix Product States and Projected Entangled Pair States

Román Orús *

Thermalization in QCD and applications of quantum technologies 2005.12299

QCD thermalization: *Ab initio* approaches and interdisciplinary connections

Jürgen Berges*

*Institute for Theoretical Physics, Heidelberg University,
Philosophenweg 16, D-69120 Heidelberg, Germany*

Michal P. Heller[†]

*Max Planck Institute for Gravitational Physics
(Albert Einstein Institute),
Am Mühlenberg 1, D-14476 Potsdam, Germany*

Aleksas Mazeliauskas[‡]

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Review papers

Quantum computing resources and references



qiskit 0.37.0
[see release notes](#)

<https://qiskit.org>

Open-Source Quantum Development

