

SM HH THEORY OVERVIEW

Michael Spira (PSI)

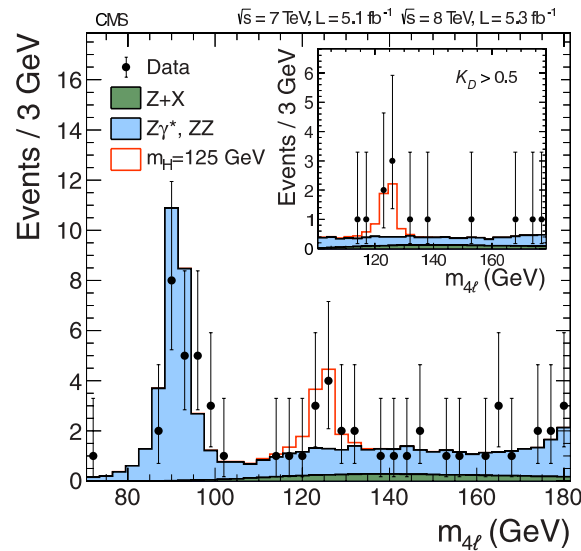
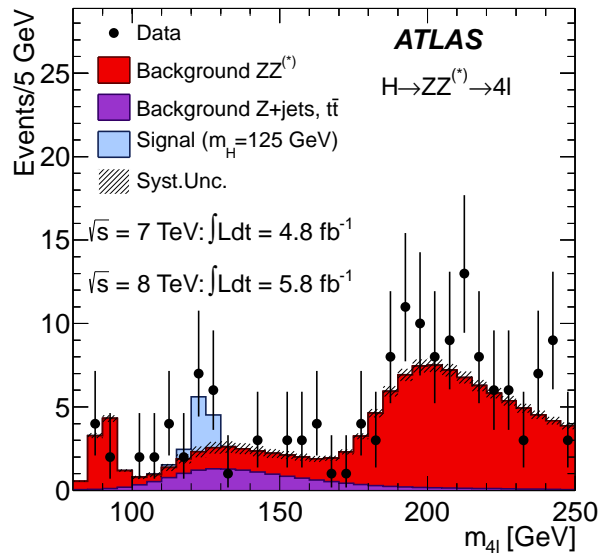
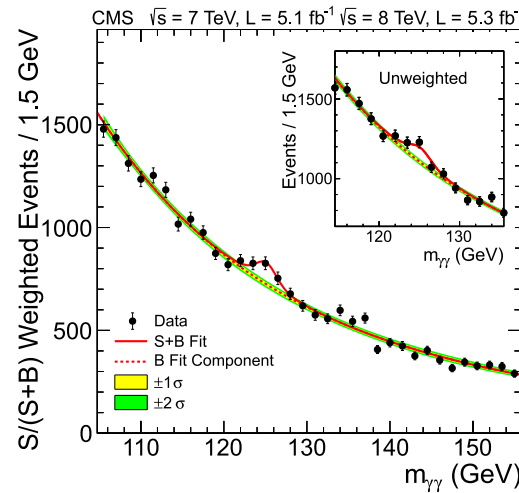
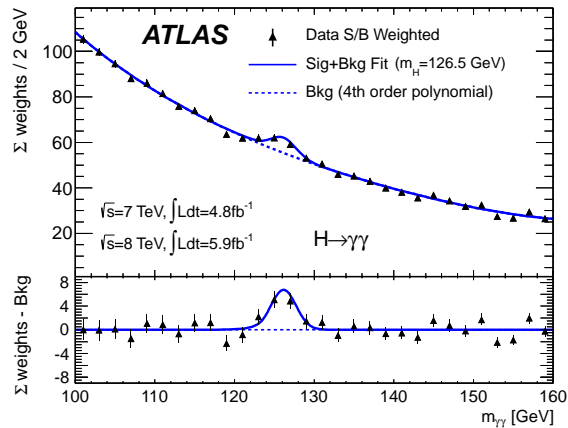
I Introduction

II Higgs Pair production

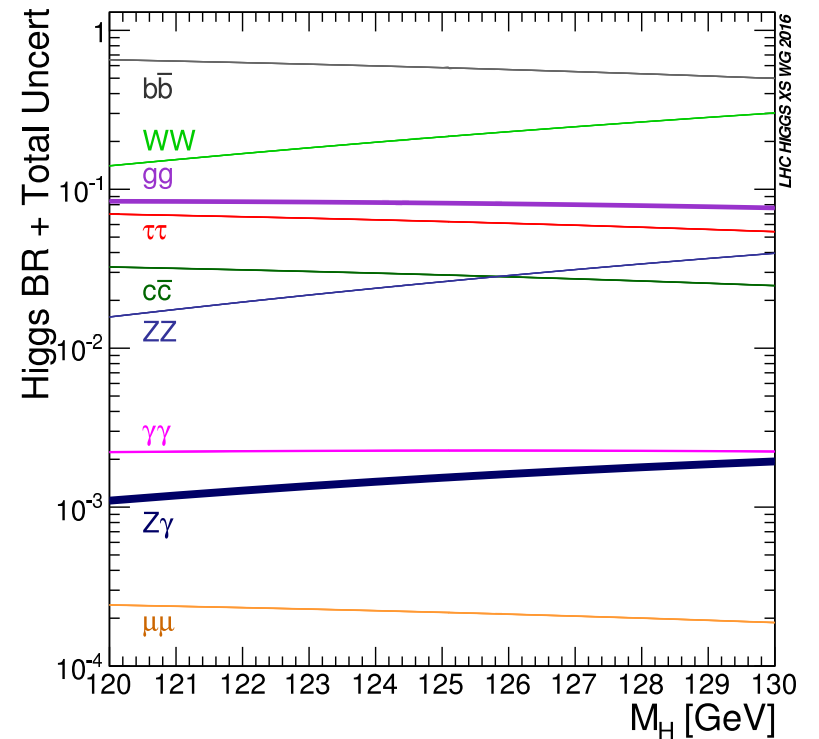
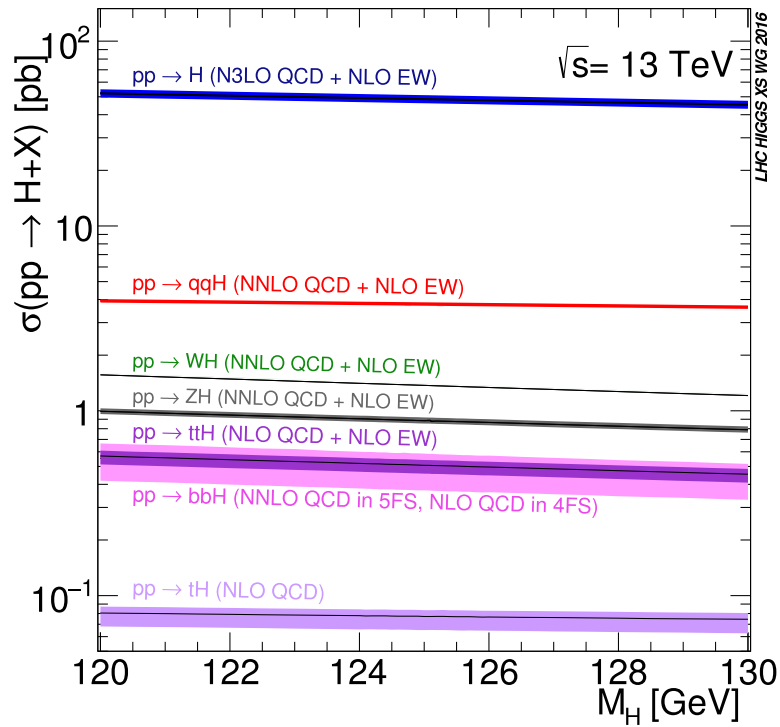
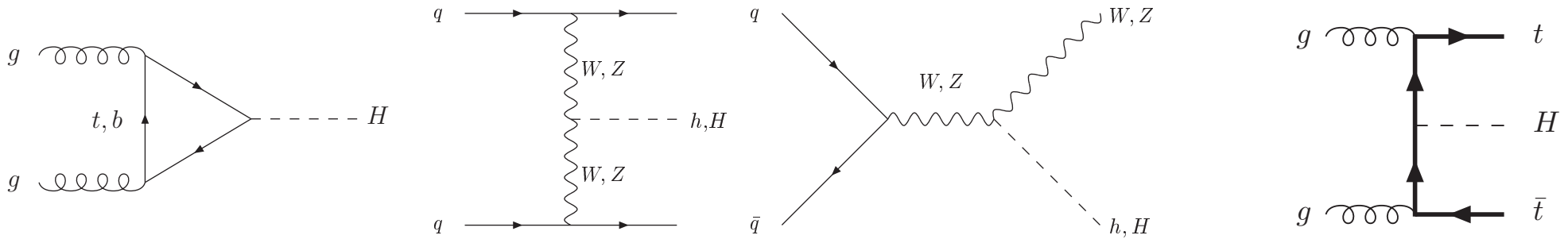
III Conclusions

Standard Model

- we have found the Higgs: $M_H \sim 125$ GeV
- $gg \rightarrow H$ dominant



• Higgs Boson Production & Decay



- Discovery: LHC [Tevatron]

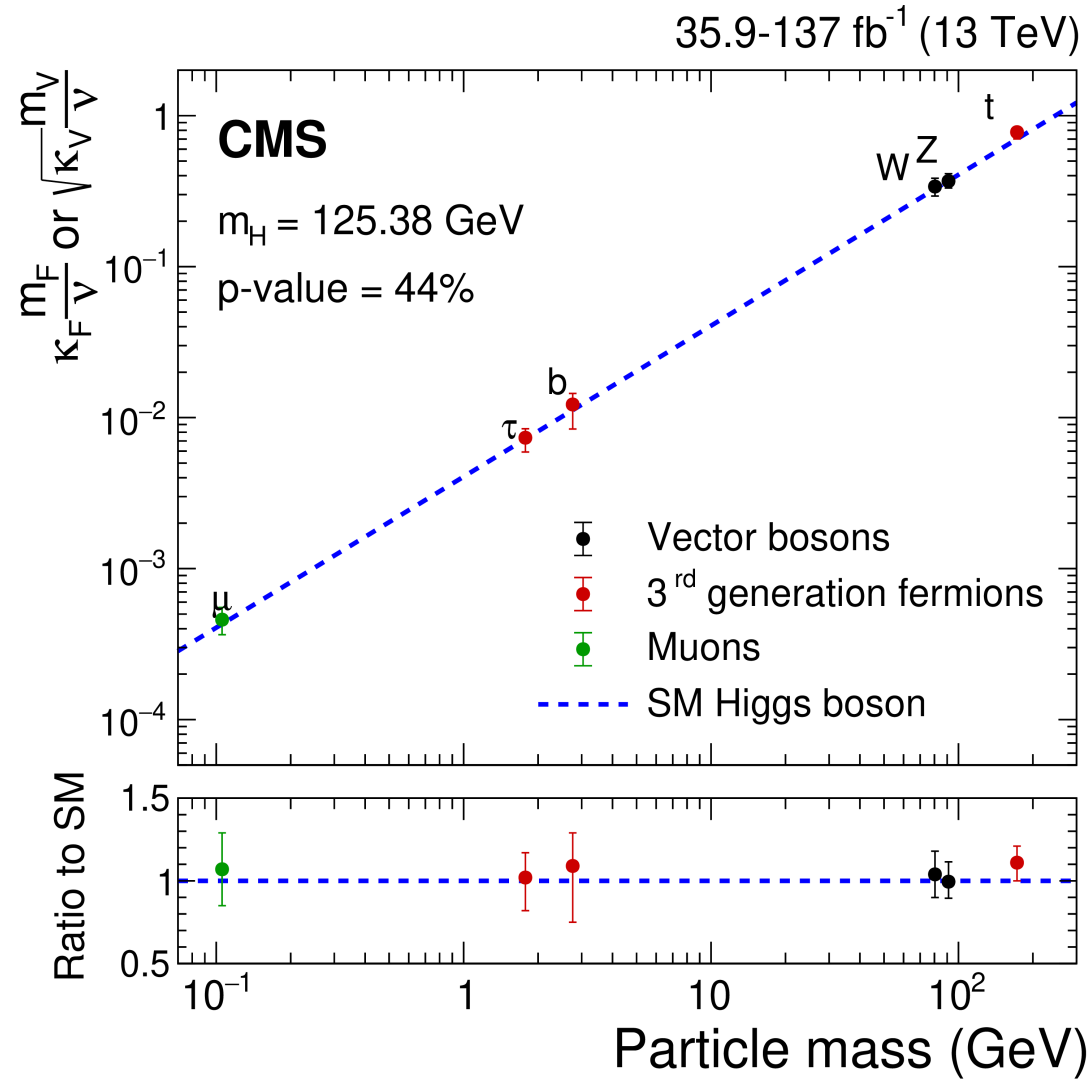
→ Higgs mass

couplings

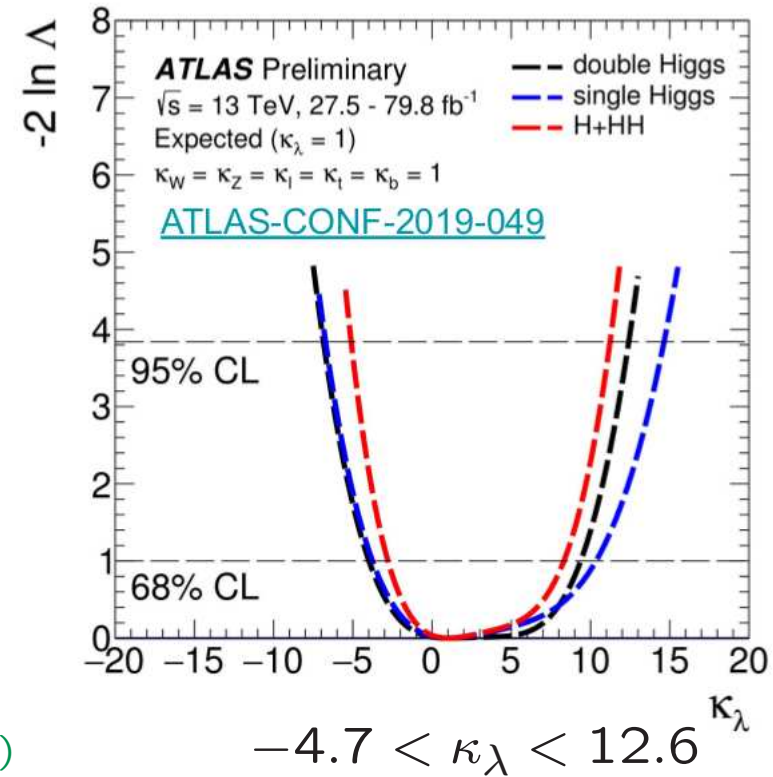
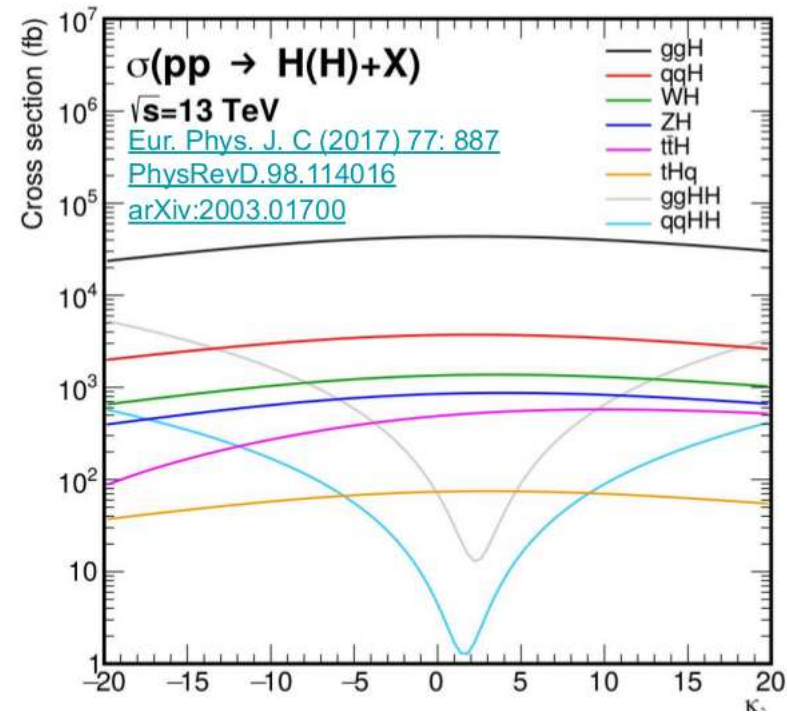
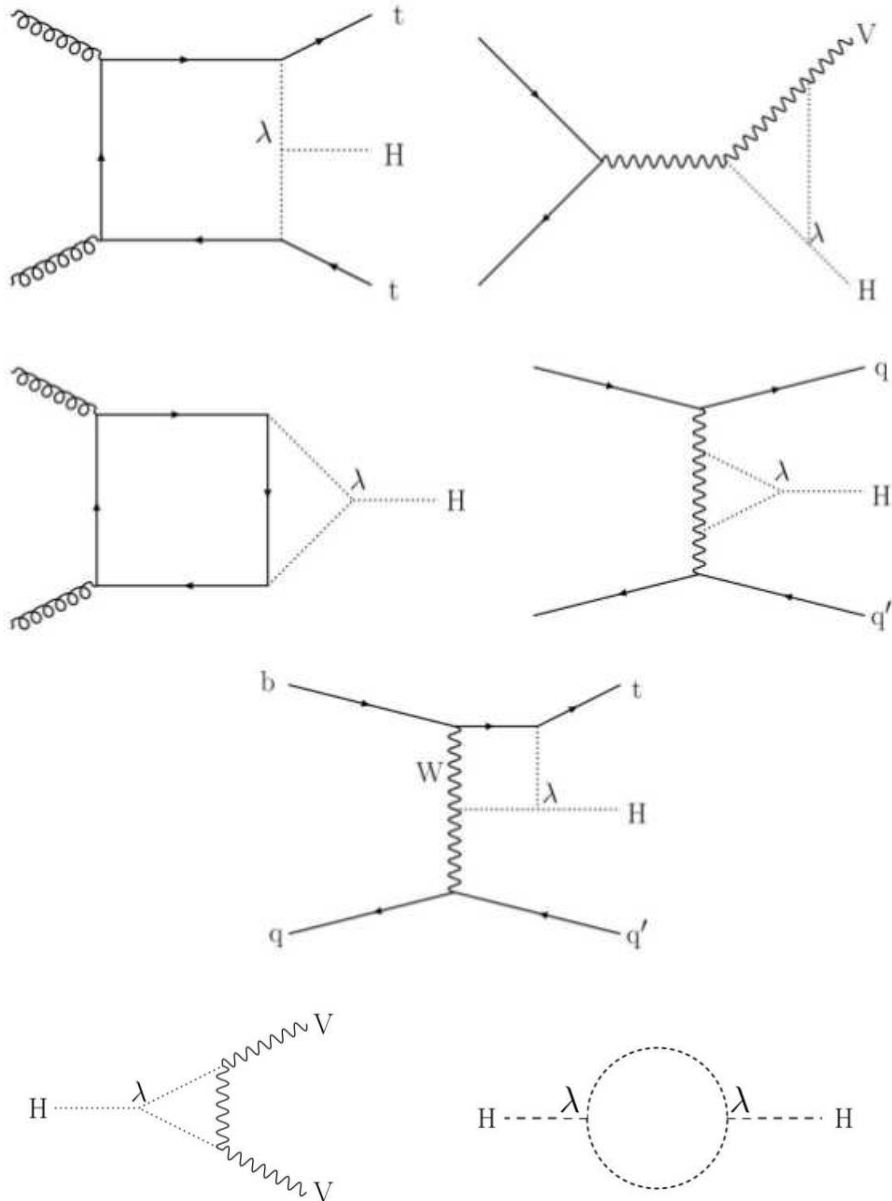
spin

CP

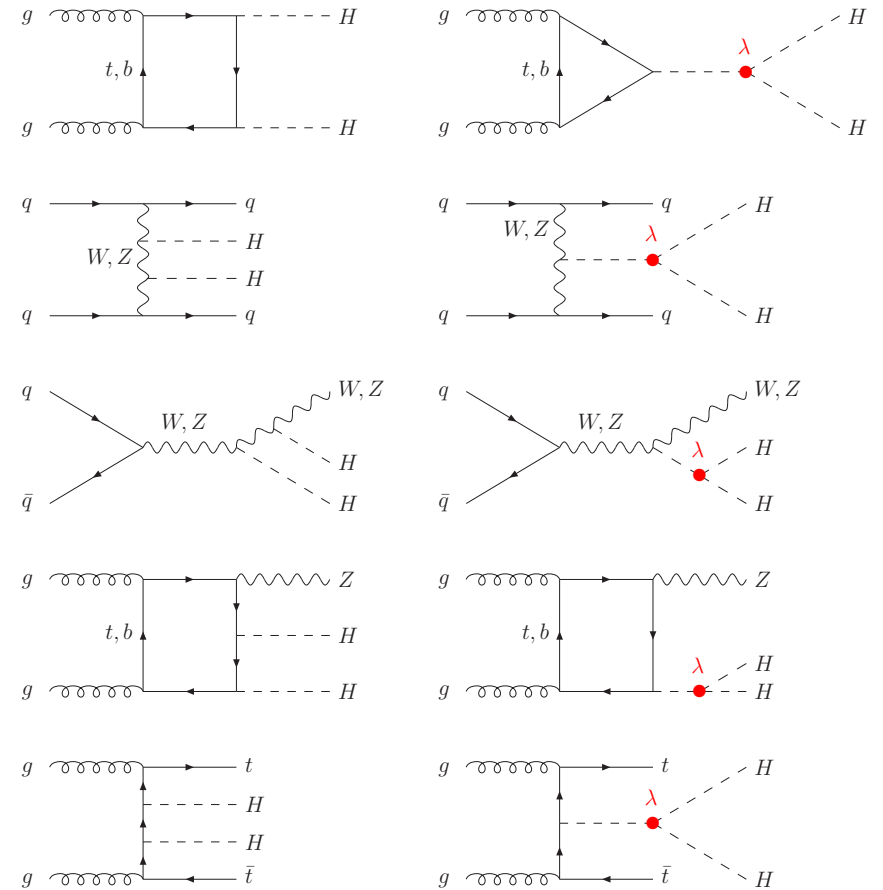
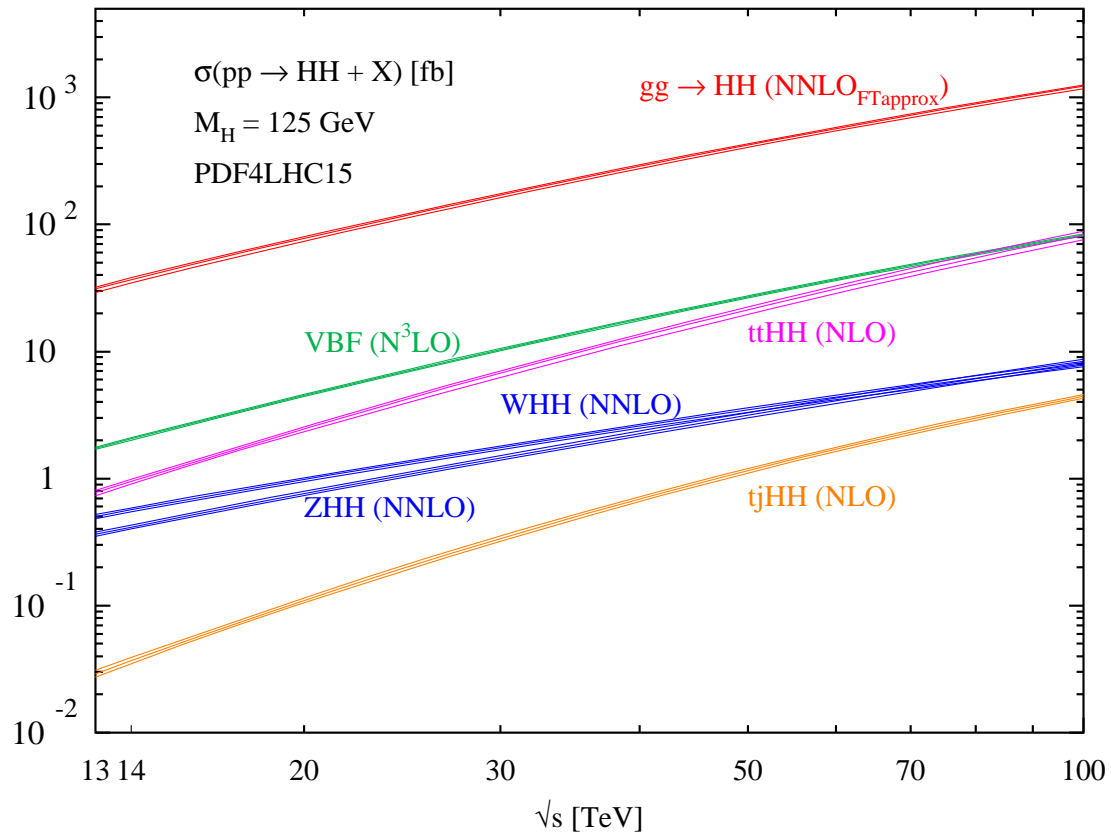
$\lambda ?$



● indirect effects:



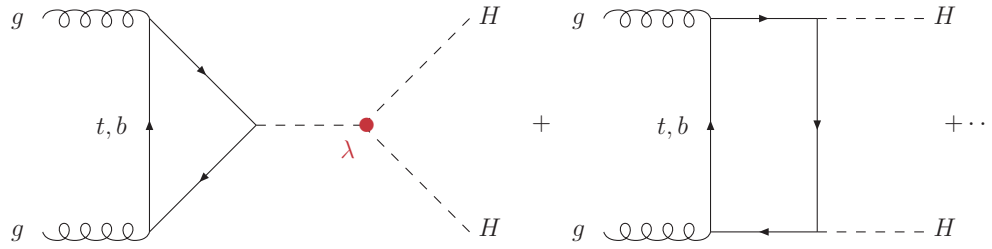
II HIGGS PAIR PRODUCTION



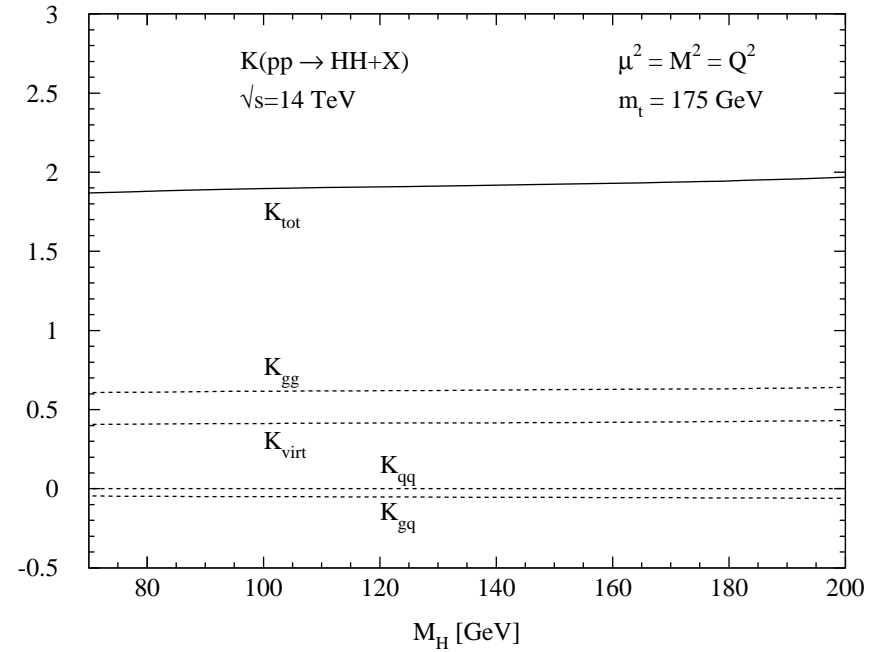
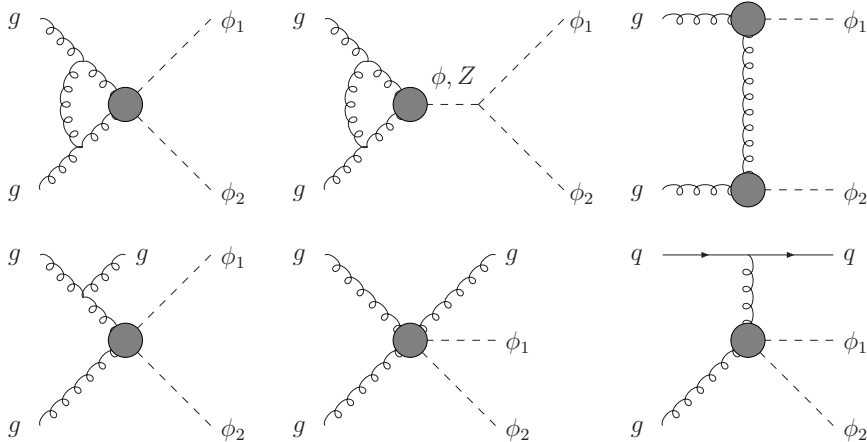
HH White Paper

(i) $gg \rightarrow HH$

SM



- third generation dominant $\rightarrow t, b$
- 2-loop QCD corrections: $\sim 90 - 100\%$
 $[M_H^2 \ll 4m_t^2, \quad \mu = M_{HH}]$



Dawson, Dittmaier, S.

$$\sigma_{\text{NLO}}(pp \rightarrow HH + X) = \sigma_{\text{LO}} + \Delta\sigma_{\text{virt}} + \Delta\sigma_{gg} + \Delta\sigma_{gq} + \Delta\sigma_{q\bar{q}}$$

$$\sigma_{\text{LO}} = \int_{\tau_0}^1 d\tau \frac{d\mathcal{L}^{gg}}{d\tau} \hat{\sigma}_{\text{LO}}(Q^2 = \tau s)$$

$$\Delta\sigma_{\text{virt}} = \frac{\alpha_s(\mu_R)}{\pi} \int_{\tau_0}^1 d\tau \frac{d\mathcal{L}^{gg}}{d\tau} \hat{\sigma}_{\text{LO}}(Q^2 = \tau s) C$$

$$\Delta\sigma_{gg} = \frac{\alpha_s(\mu_R)}{\pi} \int_{\tau_0}^1 d\tau \frac{d\mathcal{L}^{gg}}{d\tau} \int_{\tau_0/\tau}^1 \frac{dz}{z} \hat{\sigma}_{\text{LO}}(Q^2 = z\tau s) \left\{ -z P_{gg}(z) \log \frac{\mu_F^2}{\tau s} \right. \\ \left. + d_{gg}(z) + 6[1 + z^4 + (1 - z)^4] \left(\frac{\log(1 - z)}{1 - z} \right)_+ \right\}$$

$$\Delta\sigma_{gq} = \frac{\alpha_s(\mu_R)}{\pi} \int_{\tau_0}^1 d\tau \sum_{q, \bar{q}} \frac{d\mathcal{L}^{gq}}{d\tau} \int_{\tau_0/\tau}^1 \frac{dz}{z} \hat{\sigma}_{\text{LO}}(Q^2 = z\tau s) \left\{ -\frac{z}{2} P_{gq}(z) \log \frac{\mu_F^2}{\tau s(1 - z)^2} + d_{gq}(z) \right\}$$

$$\Delta\sigma_{q\bar{q}} = \frac{\alpha_s(\mu_R)}{\pi} \int_{\tau_0}^1 d\tau \sum_q \frac{d\mathcal{L}^{q\bar{q}}}{d\tau} \int_{\tau_0/\tau}^1 \frac{dz}{z} \hat{\sigma}_{\text{LO}}(Q^2 = z\tau s) d_{q\bar{q}}(z)$$

$$C \rightarrow \pi^2 + \frac{11}{2} + C_{\Delta\Delta}, \quad d_{gg} \rightarrow -\frac{11}{2}(1 - z)^3, \quad d_{gq} \rightarrow \frac{2}{3}z^2 - (1 - z)^2, \quad d_{q\bar{q}} \rightarrow \frac{32}{27}(1 - z)^3$$

- 2-loop QCD corrections:

$$\sigma = \sigma_0 + \frac{\sigma_1}{m_t^2} + \dots + \frac{\sigma_4}{m_t^8}$$

Grigo, Hoff, Melnikov, Steinhauser

[refinement: full LO at diff. level]

- mass effects @ NLO in real corrections: $\sim -10\%$

Frederix, Frixione, Hirschi, Maltoni, Mattelaer, Torrielli, Vryonidou, Zaro

→ sizeable virtual mass effects

- NNLO QCD corrections: $\sim 20\%$

$$[M_H^2 \ll 4m_t^2]$$

de Florian, Mazzitelli

Grigo, Melnikov, Steinhauser

- soft gluon resummation: $\sim 10\%$

$$[M_H^2 \ll 4m_t^2]$$

Shao, Li, Li, Wang
de Florian, Mazzitelli

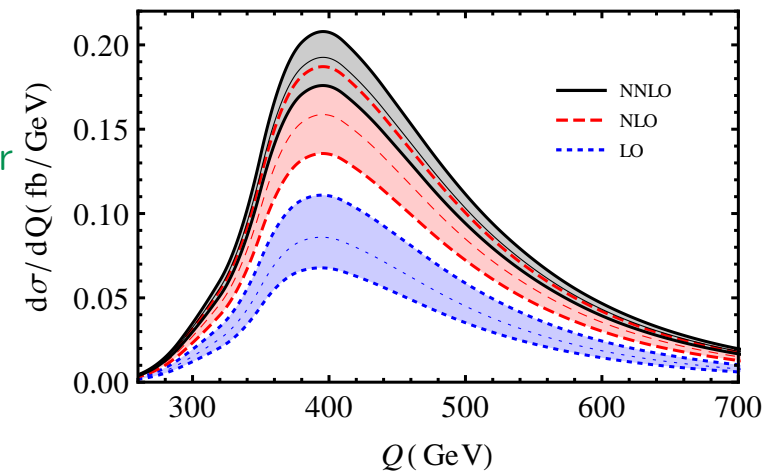
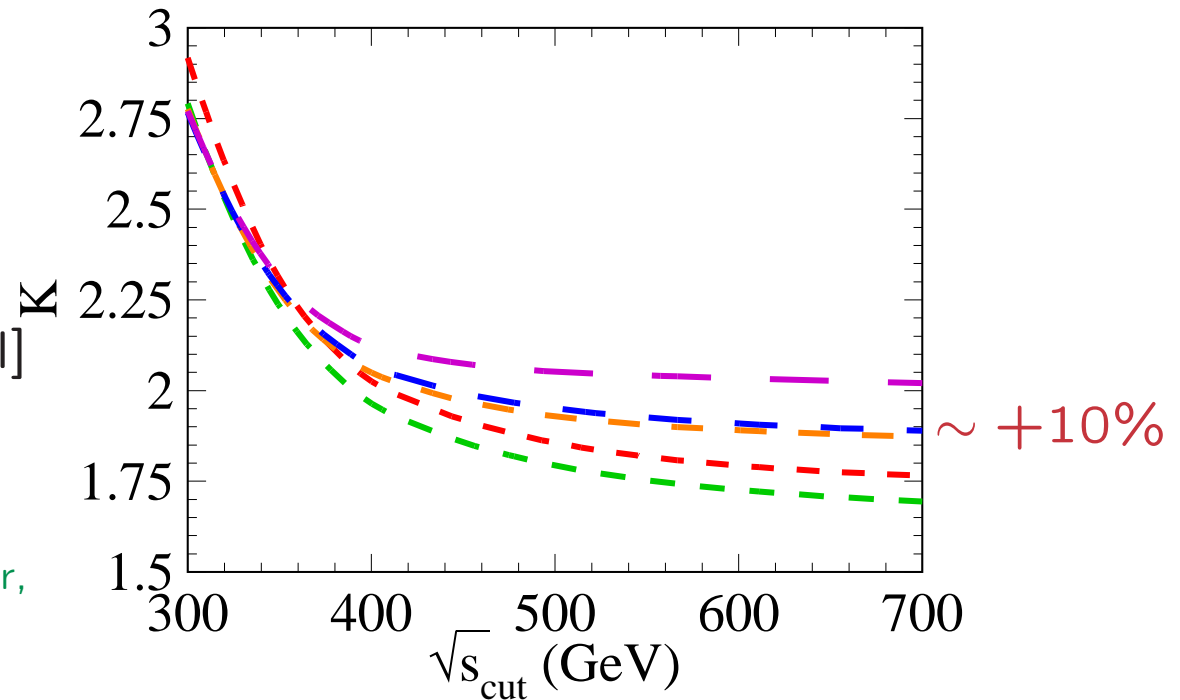
- N³LO QCD corrections: $\lesssim 3\%$

$$[M_H^2 \ll 4m_t^2]$$

Chen, Li, Shao, Wang

- NLO: small quark mass expansion

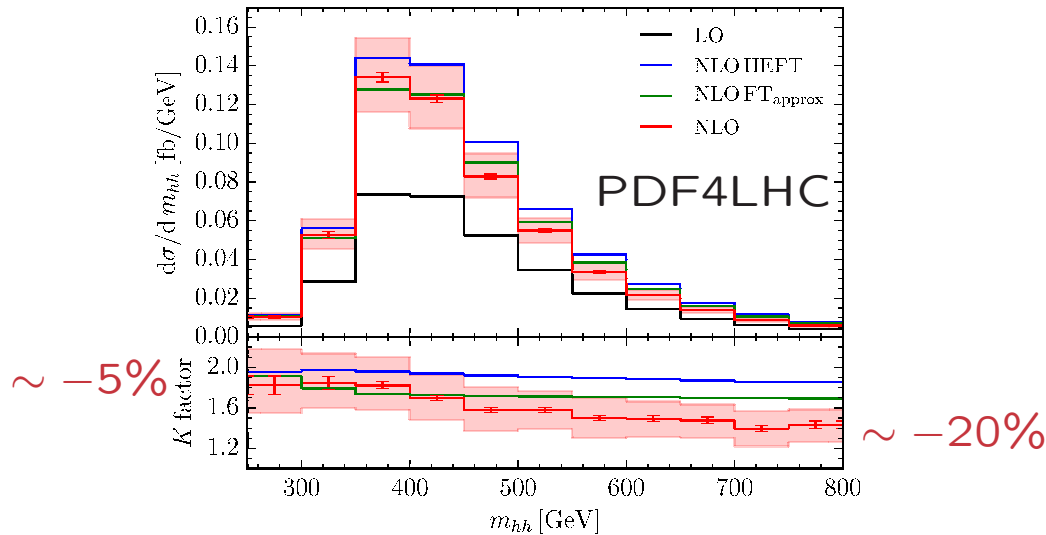
$$[Q^2 \gg m_t^2]$$



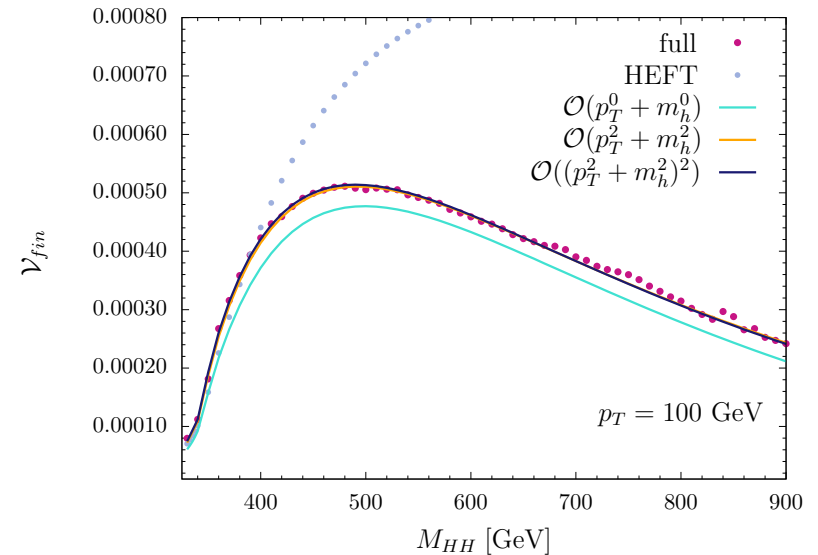
Davies, Mishima, Steinhauser, Wellmann

Full NLO calculation: top only [$\mu_R = \mu_F = M_{HH}/2$]

Numerical integration, sector decomposition, tensor reduction, contour deformation



Borowka, Greiner, Heinrich, Jones, Kerner
Schlenk, Schubert, Zirke



Boncianni, Degrassi, Giardino, Gröber

- 14 TeV: ($m_t = 173$ GeV) $\sigma_{NLO} = 32.91(10)_{-12.8\%}^{+13.8\%} fb$
 $\sigma_{NLO}^{HTL} = 38.75_{-15\%}^{+18\%} fb$ (\leftarrow HPAIR)

\Rightarrow -15% mass effects on top of LO

• new expansion/extrapolation methods:

(i) $1/m_t^2$ + thresh. expansion + conformal mapping + Padé approx.

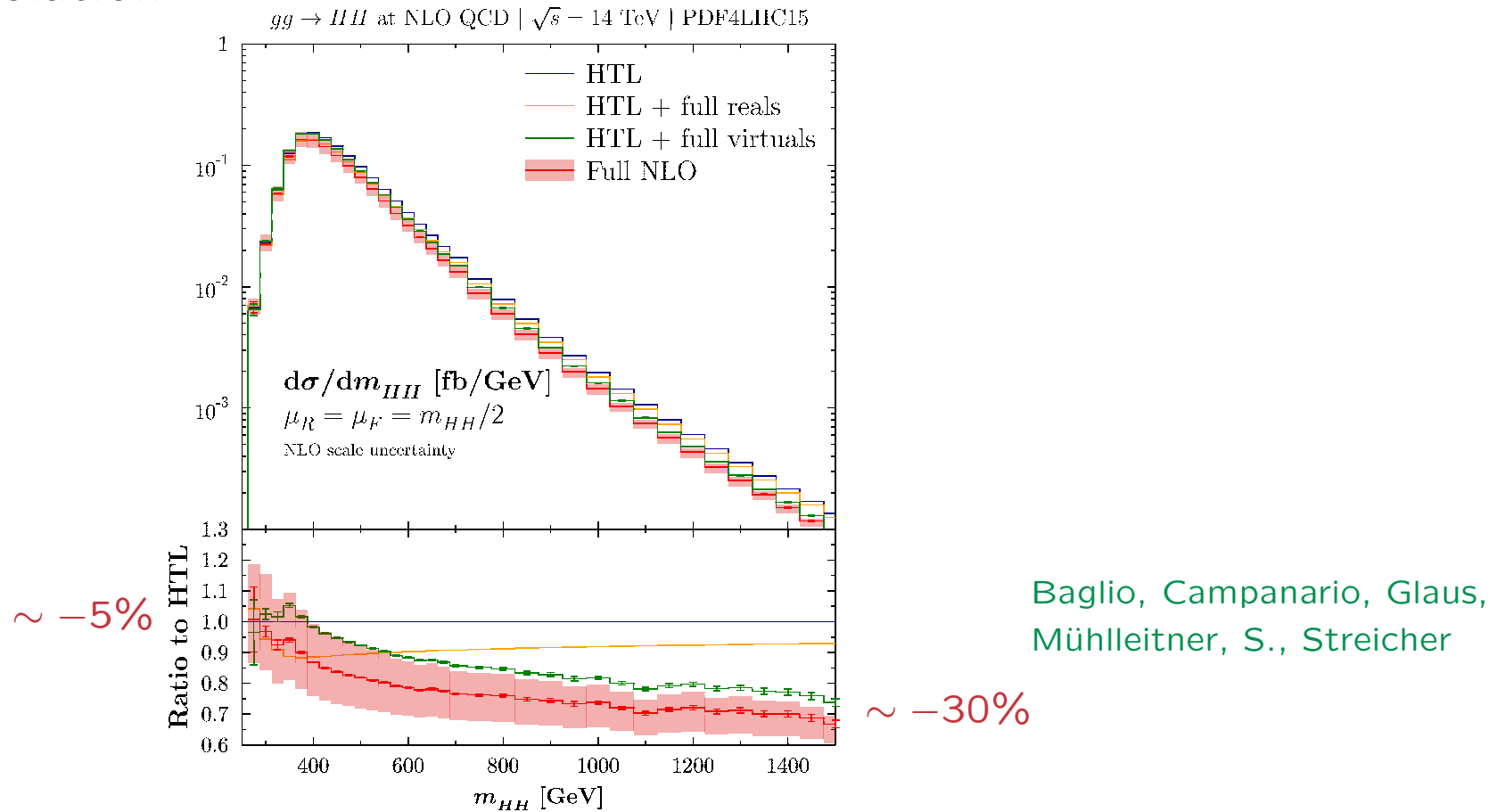
Gröber, Maier, Rauh

(ii) M_T^2 expansion

Boncianni, Degrassi, Giardino, Gröber

Full NLO calculation: top only [$\mu_R = \mu_F = M_{HH}/2$]

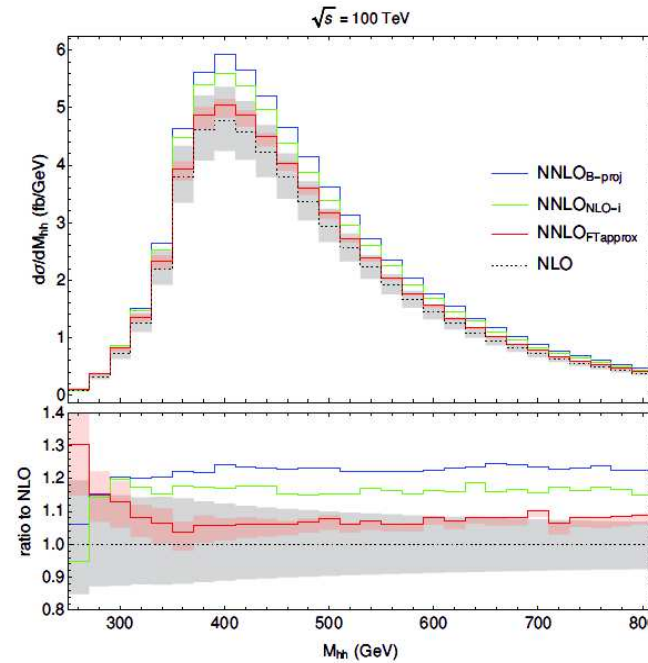
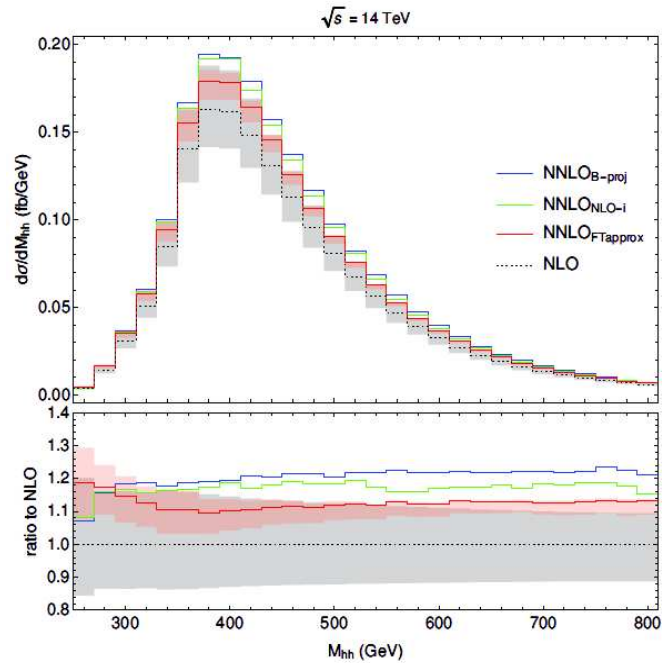
Numerical integration, IR subtraction, no tensor reduction, Richardson extrapolation



- 14 TeV: ($m_t = 172.5$ GeV) $\sigma_{NLO} = 32.81(7)_{-12.5\%}^{+13.5\%}$ fb
 $\sigma_{NLO}^{HTL} = 38.66_{-15\%}^{+18\%}$ fb (← HPAIR)

$\Rightarrow -15\%$ mass effects on top of LO

- NNLO Monte Carlo: inclusion of full top-mass effects @ NLO



Grazzini, Heinrich, Jones, Kallweit, Kerner, Lindert, Mazzitelli

⇒ 20% effects beyond NLO

- NLO: matching to parton showers Heinrich, Jones, Kerner, Luisoni, Vryonidou

- combination of full NLO and small mass expansion Davies, Heinrich, Jones, Kerner, Mishima, Steinhauser, Wellmann

uncertainties due to m_t

- transform $m_t \rightarrow \overline{m}_t(\mu)$ ($\overline{\text{MS}}$)

→ modification of mass CT

- use $m_t, \overline{m}_t(\overline{m}_t)$ and scan $Q/4 < \mu < Q \rightarrow$ uncertainty = envelope:

$$\left. \frac{d\sigma(gg \rightarrow HH)}{dQ} \right|_{Q=300 \text{ GeV}} = 0.02978(7)_{-34\%}^{+6\%} \text{ fb/GeV},$$

$$\left. \frac{d\sigma(gg \rightarrow HH)}{dQ} \right|_{Q=400 \text{ GeV}} = 0.1609(4)_{-13\%}^{+0\%} \text{ fb/GeV},$$

$$\left. \frac{d\sigma(gg \rightarrow HH)}{dQ} \right|_{Q=600 \text{ GeV}} = 0.03204(9)_{-30\%}^{+0\%} \text{ fb/GeV},$$

$$\left. \frac{d\sigma(gg \rightarrow HH)}{dQ} \right|_{Q=1200 \text{ GeV}} = 0.000435(4)_{-35\%}^{+0\%} \text{ fb/GeV}$$

- bin-by-bin interpolation:

$$\sigma(gg \rightarrow HH) = 32.81(7)_{-18\%}^{+4\%} \text{ fb}$$

- why a dynamical scale $\sim Q$?

large momentum expansion ($\hat{s} = Q^2 \gg m_t^2$), two FF:

← Davies, Mishima, Steinhauser, Wellmann

pole mass m_t :

$$\Delta F_{1,mass} \rightarrow \frac{\alpha_s}{\pi} \left\{ 2F_{1,LO} \log \frac{m_t^2}{\hat{s}} + \frac{m_t^2}{\hat{s}} G_1(\hat{s}, \hat{t}) \right\},$$

$$\Delta F_{2,mass} \rightarrow \frac{\alpha_s}{\pi} \left\{ 2F_{2,LO} \log \frac{m_t^2}{\hat{s}} + \frac{m_t^2}{\hat{s}} G_2(\hat{s}, \hat{t}) \right\}$$

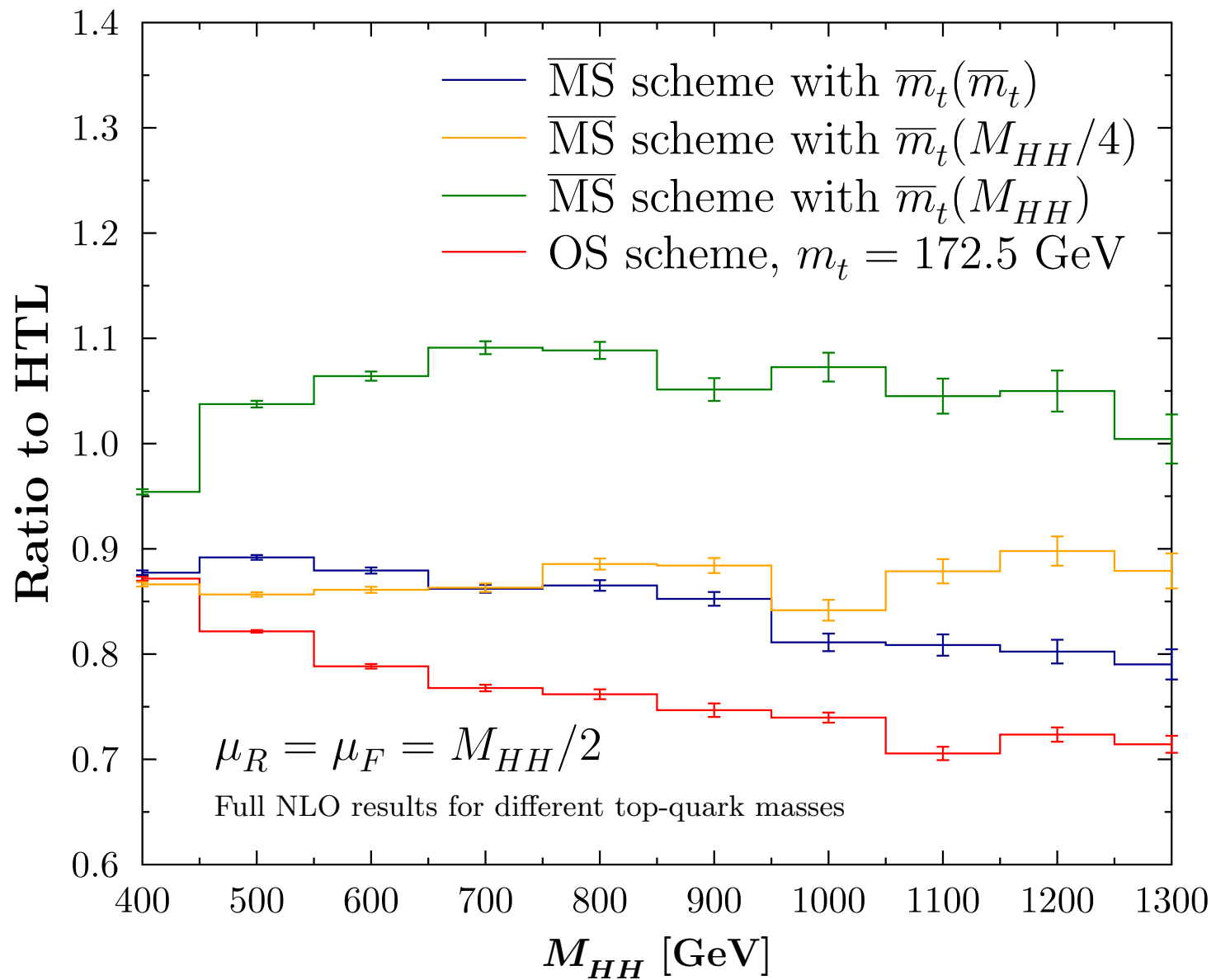
MS mass $\bar{m}_t(\mu_t)$:

$$\Delta F_{1,mass} \rightarrow \frac{\alpha_s}{\pi} \left\{ 2F_{1,LO} \left[\log \frac{\mu_t^2}{\hat{s}} + \frac{4}{3} \right] + \frac{\bar{m}_t^2(\mu_t)}{\hat{s}} G_1(\hat{s}, \hat{t}) \right\},$$

$$\Delta F_{2,mass} \rightarrow \frac{\alpha_s}{\pi} \left\{ 2F_{2,LO} \left[\log \frac{\mu_t^2}{\hat{s}} + \frac{4}{3} \right] + \frac{\bar{m}_t^2(\mu_t)}{\hat{s}} G_2(\hat{s}, \hat{t}) \right\}$$

\Rightarrow scale $\mu_t \sim Q$ preferred at large Q

$gg \rightarrow HH$ at NLO QCD | $\sqrt{s} = 13$ TeV | PDF4LHC15



Baglio, Campanario, Glaus, Mühlleitner, Ronca, S.

- renormalization/factorization scale uncertainties @ NNLO_{FTapprox}:

$$\sqrt{s} = 13 \text{ TeV} : \quad \sigma_{tot} = 31.05^{+2.2\%}_{-5.0\%} \text{ fb}$$

$$\sqrt{s} = 14 \text{ TeV} : \quad \sigma_{tot} = 36.69^{+2.1\%}_{-4.9\%} \text{ fb}$$

$$\sqrt{s} = 27 \text{ TeV} : \quad \sigma_{tot} = 139.9^{+1.3\%}_{-3.9\%} \text{ fb}$$

$$\sqrt{s} = 100 \text{ TeV} : \quad \sigma_{tot} = 1224^{+0.9\%}_{-3.2\%} \text{ fb}$$

- m_t scale/scheme uncertainties @ NLO:

$$\sqrt{s} = 13 \text{ TeV} : \quad \sigma_{tot} = 27.73(7)^{+4\%}_{-18\%} \text{ fb}$$

$$\sqrt{s} = 14 \text{ TeV} : \quad \sigma_{tot} = 32.81(7)^{+4\%}_{-18\%} \text{ fb}$$

$$\sqrt{s} = 27 \text{ TeV} : \quad \sigma_{tot} = 127.8(2)^{+4\%}_{-18\%} \text{ fb}$$

$$\sqrt{s} = 100 \text{ TeV} : \quad \sigma_{tot} = 1140(2)^{+3\%}_{-18\%} \text{ fb}$$

- how to combine them? → envelope → \sim linear sum (rel. err.)

- combined ren./fac. scale and m_t scale/scheme unc. @ NNLO_{FTapprox}:

$$\sqrt{s} = 13 \text{ TeV} : \quad \sigma_{tot} = 31.05^{+6\%}_{-23\%} \text{ fb}$$

$$\sqrt{s} = 14 \text{ TeV} : \quad \sigma_{tot} = 36.69^{+6\%}_{-23\%} \text{ fb}$$

$$\sqrt{s} = 27 \text{ TeV} : \quad \sigma_{tot} = 139.9^{+5\%}_{-22\%} \text{ fb}$$

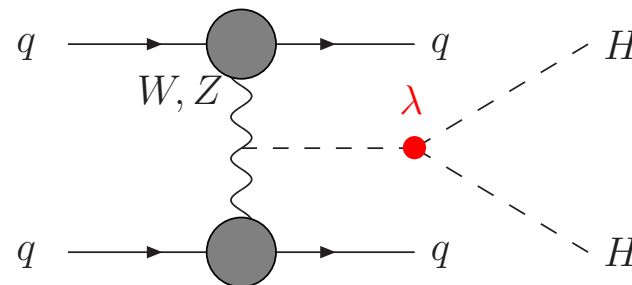
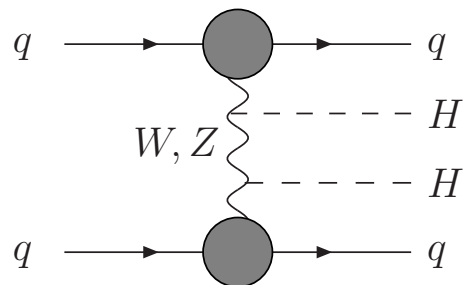
$$\sqrt{s} = 100 \text{ TeV} : \quad \sigma_{tot} = 1224^{+4\%}_{-21\%} \text{ fb}$$

$$[\mu_R = \mu_F = M_{HH}/2]$$

- combined uncertainties @ NNLO_{FTapprox} [$\mu_R = \mu_F = M_{HH}/2$]:

$\kappa_\lambda = -10$:	σ_{tot}	=	$1680^{+13\%}_{-14\%}$	fb
$\kappa_\lambda = -5$:	σ_{tot}	=	$598.9^{+13\%}_{-15\%}$	fb
$\kappa_\lambda = -1$:	σ_{tot}	=	$131.9^{+11\%}_{-16\%}$	fb
$\kappa_\lambda = 0$:	σ_{tot}	=	$70.38^{+8\%}_{-18\%}$	fb
$\kappa_\lambda = 1$:	σ_{tot}	=	$31.05^{+6\%}_{-23\%}$	fb
$\kappa_\lambda = 2$:	σ_{tot}	=	$13.81^{+3\%}_{-28\%}$	fb
$\kappa_\lambda = 2.4$:	σ_{tot}	=	$13.10^{+6\%}_{-27\%}$	fb
$\kappa_\lambda = 3$:	σ_{tot}	=	$18.67^{+12\%}_{-22\%}$	fb
$\kappa_\lambda = 5$:	σ_{tot}	=	$94.82^{+18\%}_{-13\%}$	fb
$\kappa_\lambda = 10$:	σ_{tot}	=	$672.2^{+16\%}_{-13\%}$	fb

(ii) VBF



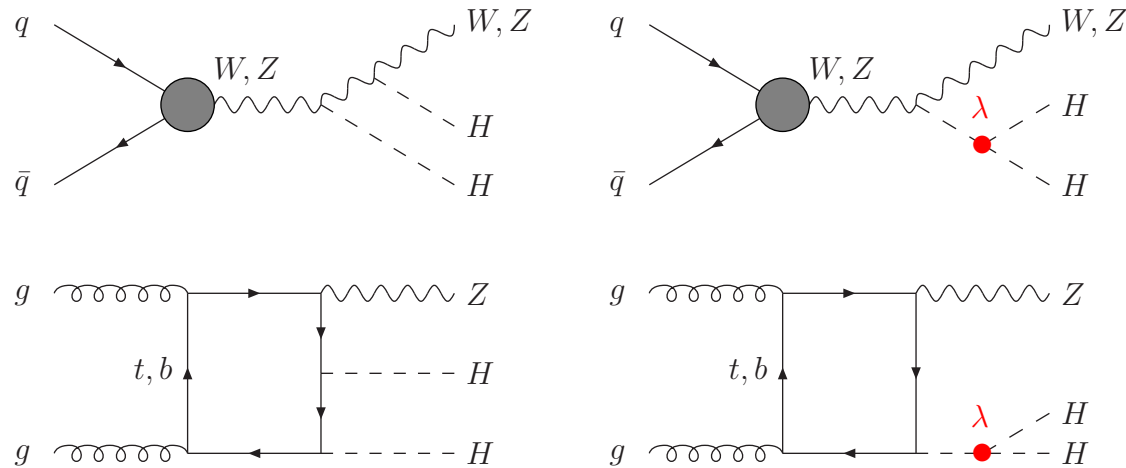
- QCD corrections \leftarrow DIS (STFU approach)
- NLO $\sim 10\%$, NNLO+N³LO $\lesssim 1\%$ [$\mu_R = \mu_F = \sqrt{-q_{1,2}^2}$ (≥ 1 GeV)]

Baglio, Djouadi, Gröber, Mühlleitner, Quevillon, S.
Ling, Zhang, Ma, Guo, Li, Li
Dreyer, Karlberg

- differential @ NNLO

Dreyer, Karlberg

(iii) Double Higgs-strahlung



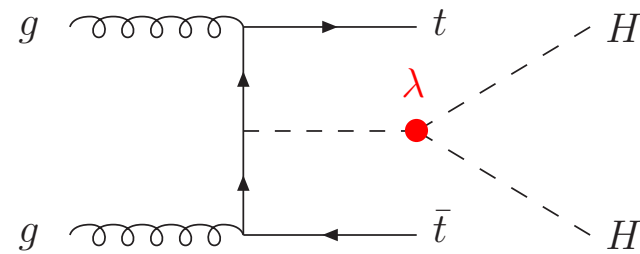
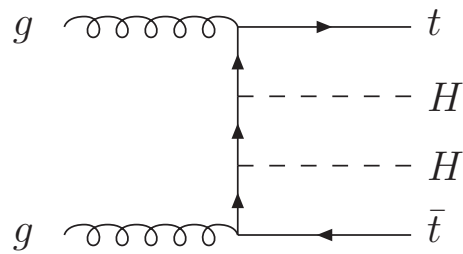
- QCD corrections \leftarrow DY
- $gg \rightarrow ZHH$: $\sim 30\%$ (LO \rightarrow NNLO)
- NLO+NNLO $\sim 30\%$ [$\mu_R = \mu_F = M_{HHV}$]

Baglio, Djouadi, Gröber, Mühlleitner, Quevillon, S.
Li, Wang
Li, Li, Wang

- differential @ NNLO

Li, Wang
Li, Li, Wang

(iv) $t\bar{t}HH$

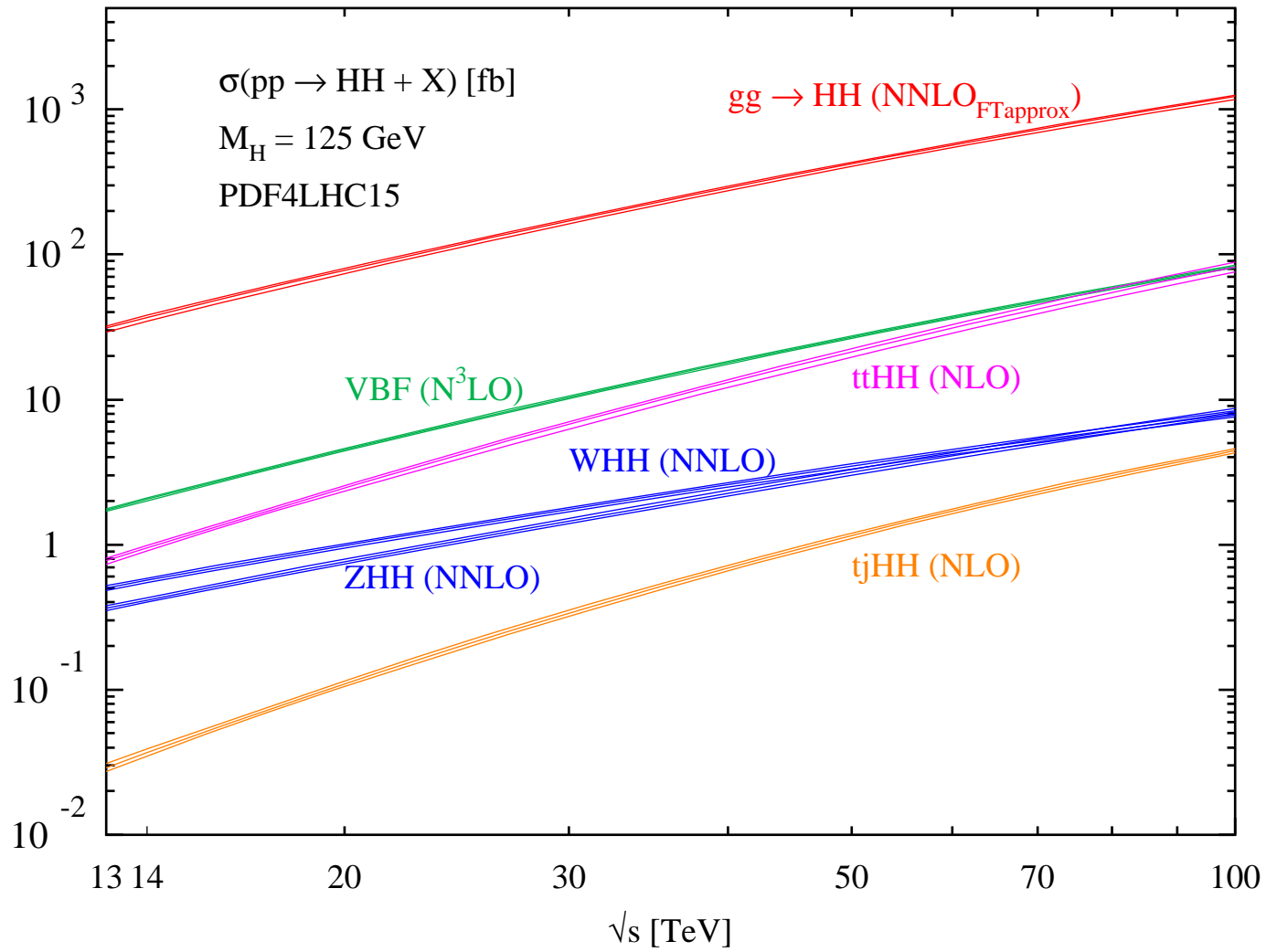


- QCD corrections: MG5_aMC@NLO
- $t\bar{t}HH$: $\sim -20\%$ moderate (\leftarrow single H) [$\mu_R = \mu_F = M_{t\bar{t}}/2$]
- $tjHH$: $\sim +20\%$ moderate [$\mu_R = \mu_F = M_{HH}/2$]

Frederix, Frixione, Hirschi, Maltoni, Mattelaer, Torrielli, Vryonidou, Zaro

III CONCLUSIONS

- Higgs pair production at full NLO...N³LO
⇒ THU $\lesssim 25 \dots 1\%$
- gg → HH: NLO top mass effects on top of LO sizeable
factorization/renormalization scale uncertainties $\sim 15\%$
uncertainties due to scale/scheme choice of m_t sizeable $\lesssim 30\%$
recommended scheme to comb. fac./ren. scale and m_t uncertainties



BACKUP SLIDES

- pole mass \leftrightarrow $\overline{\text{MS}}$ mass:

$$\overline{m}_t(M_t) = \frac{M_t}{1 + \frac{4\alpha_s(M_t)}{3\pi} + 10.9 \left(\frac{\alpha_s(M_t)}{\pi}\right)^2}$$

$$\overline{m}_t(\mu) = \overline{m}_t(M_t) \frac{c[\alpha_s(\mu)/\pi]}{c[\alpha_s(M_t)/\pi]}$$

$$c(x) = \left(\frac{7}{2}x\right)^{\frac{4}{7}} [1 + 1.398x + 1.793x^2 - 0.6834x^3]$$

$$M_t = 172.5 \text{ GeV}$$

$$\overline{m}_t(\overline{m}_t) = 163.0 \text{ GeV}$$