

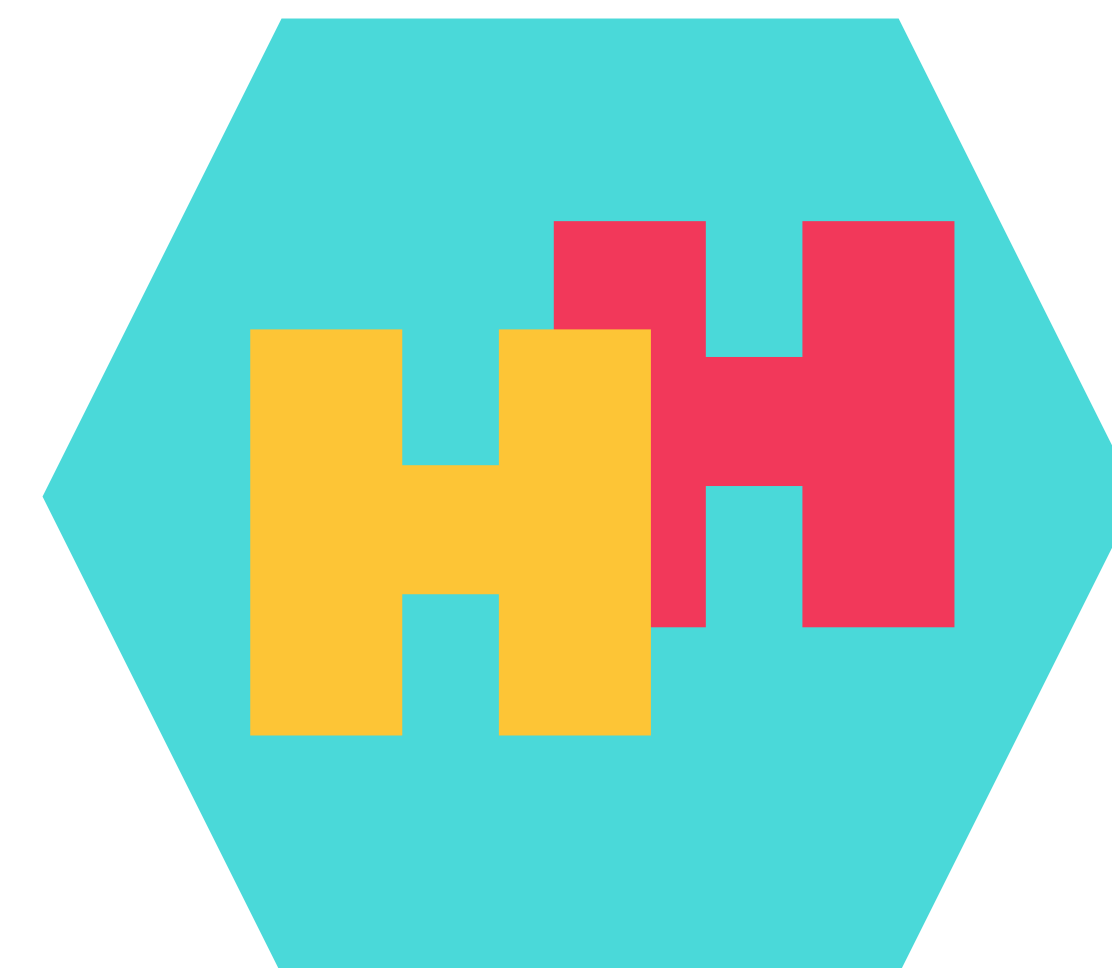


# ATLAS HH Overview

**Tülin Varol Mete**

**Academia Sinica**

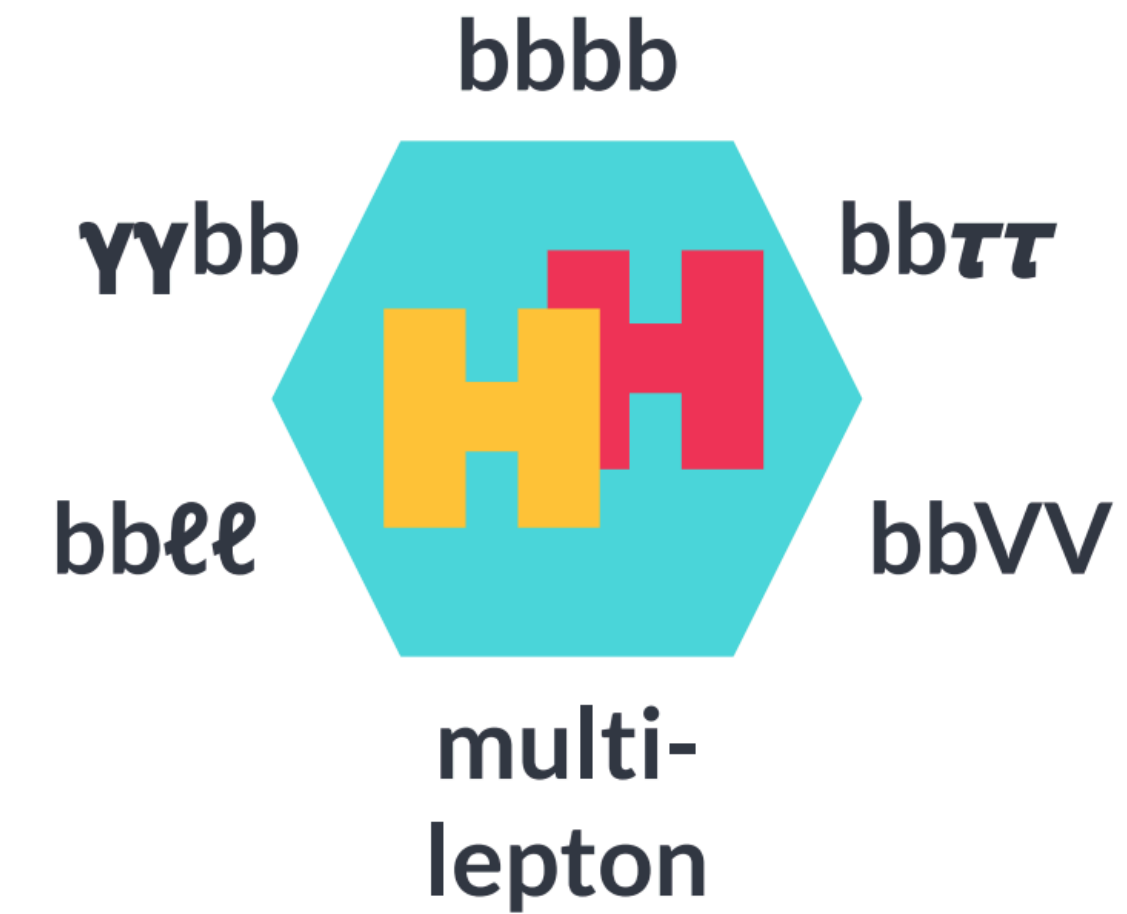
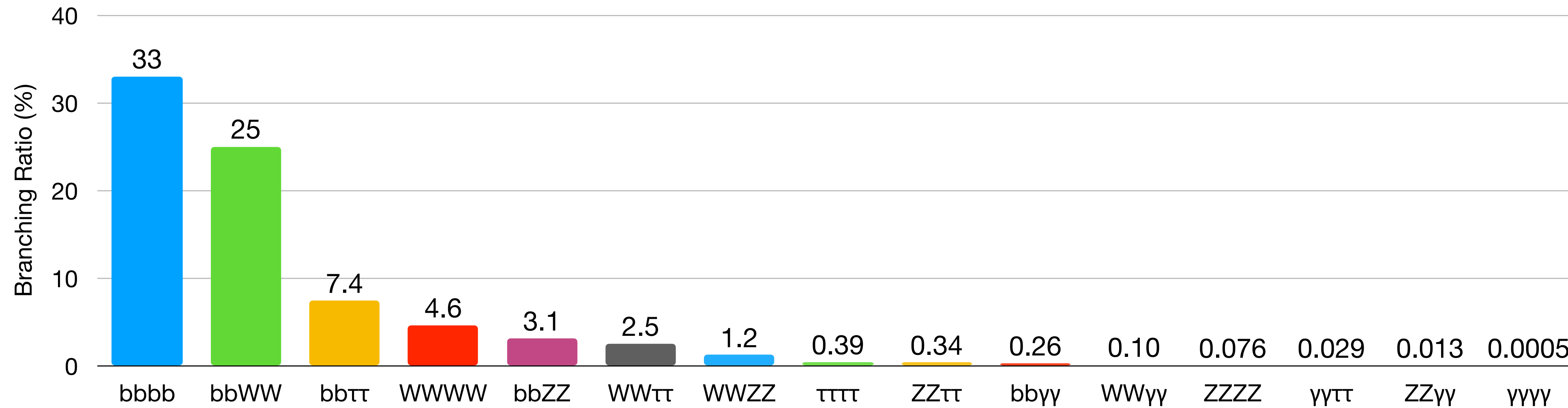
on behalf of the ATLAS HH analysis teams



Higgs Pairs Mini-Workshop

29/09/2021

# ATLAS HH Analyses



## With Run-II 2015 + 2016 datasets

### (36.1 fb<sup>-1</sup> of 13 TeV data)

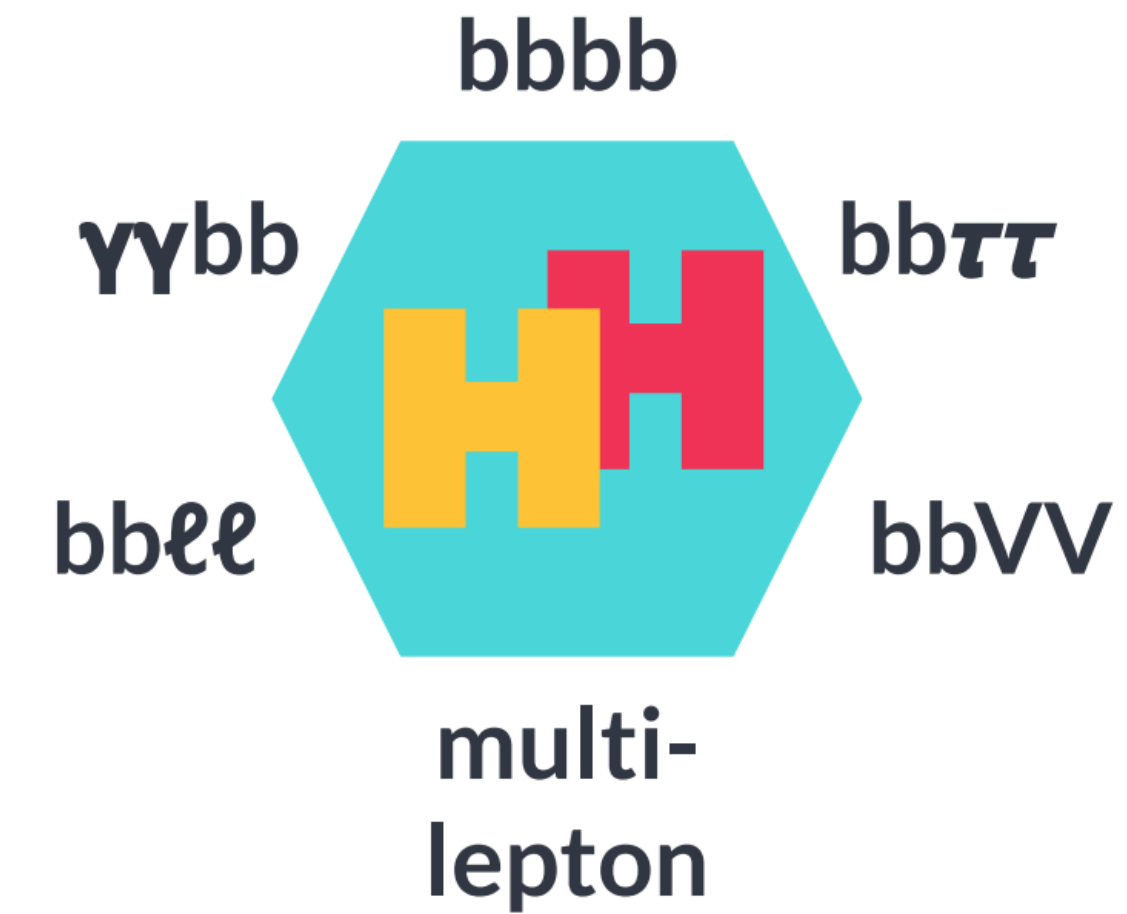
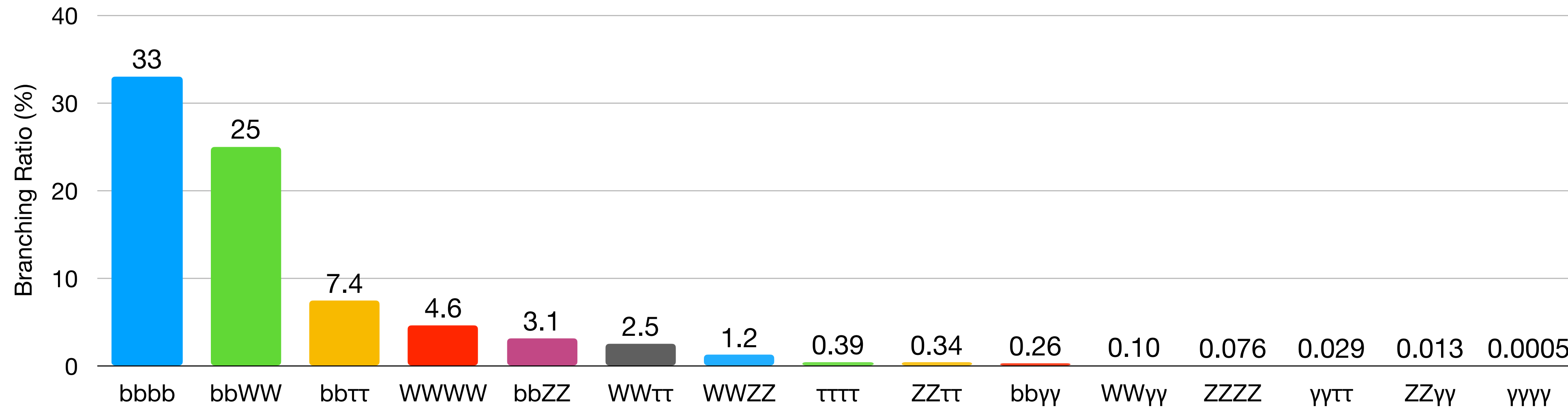
- $HH \rightarrow bbbb$  [1804.06174](#)
- $HH \rightarrow bb\gamma\gamma$  [1807.04873](#)
- $HH \rightarrow \gamma\gamma WW^*$  ( $\gamma\gamma lvjj$ ) [1807.08567](#)
- $HH \rightarrow bb\tau\tau$  [1808.00336](#)
- $HH \rightarrow bbWW^*$  ( $bb lvqq$ ) [1811.04671](#)
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- **HH Combination** [1906.02025](#)

## With full Run-II datasets

### (126-139 fb<sup>-1</sup> of 13 TeV data)

- $VBF HH \rightarrow bbbb$  [2001.05178](#)
- **Boosted**  $HH \rightarrow bb\tau\tau$  [2007.14811](#)
- $HH \rightarrow bblv lv$  ( $bb WW^*$ ,  $bb ZZ$ ,  $bb\tau\tau$ ) [1908.06765](#)
- **Resonant**  $HH \rightarrow bbbb$  [ATLAS-CONF-2021-035](#)
- $HH \rightarrow bb\tau\tau$  [ATLAS-CONF-2021-030](#)
- $HH \rightarrow bb\gamma\gamma$  [ATLAS-CONF-2021-016](#)

# ATLAS HH Analyses



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**Will cover the results with full Run-II data today!**

# HH $\rightarrow$ bb $\gamma\gamma$

**Publication:** ATLAS-CONF-2021-016

**Physics Briefing:** Twice the Higgs, twice the challenge

# HH→bbγγ: Analysis Overview

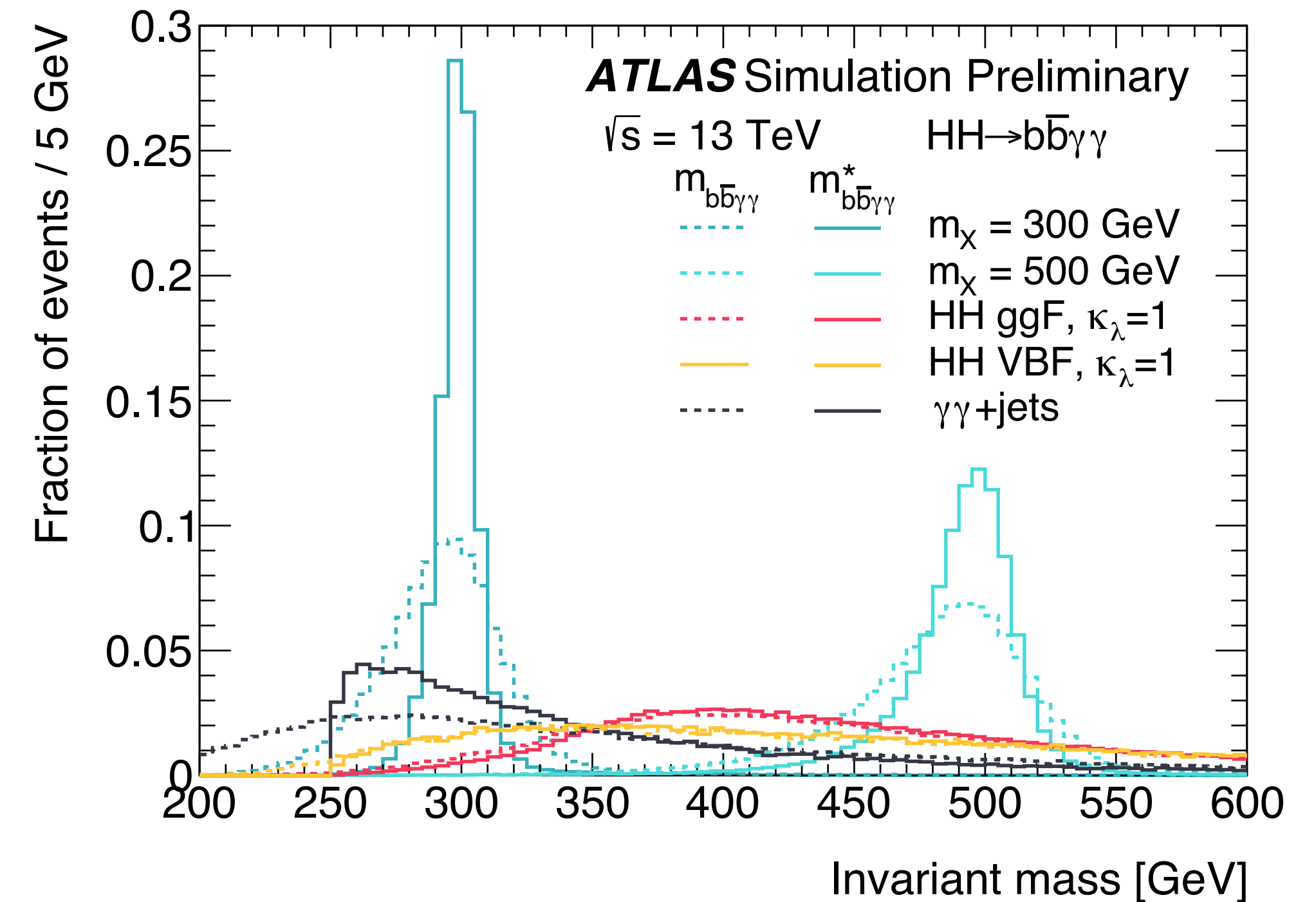
- Search for **non-resonant (ggF+VBF)** and **resonant HH production** using **139 fb<sup>-1</sup>** of pp data
  - Using **di-photon triggers**
  - Selecting events with **2 photons and 2 b-tagged jets** (with 77% b-tag efficiency)
    - 105 GeV < m<sub>γγ</sub> < 160 GeV
    - p<sub>T</sub><sup>γ</sup> lead. (sub-lead.) > 0.35 (0.25) \* m<sub>γγ</sub>

- Using **MVA** for the **signal/background discrimination**
- To improve the 4-object resolution, **m<sub>bbγγ</sub>\*** variable is defined:

$$m_{bb\bar{b}\gamma\gamma}^* = m_{bb\bar{b}\gamma\gamma} - (m_{bb} - 125 \text{ GeV}) - (m_{\gamma\gamma} - 125 \text{ GeV})$$

- Non-resonant **γγ+jets** background **fitted to the data sidebands** in m<sub>γγ</sub>
- **Single-H** background taken **from MC**

- **Simultaneous likelihood fit in m<sub>γγ</sub>** to all relevant categories
  - **Non-Resonant:** Limits on σ<sub>HH</sub> & σ<sub>HH</sub> vs κ<sub>λ</sub>
  - **Resonant:** Limits on σ<sub>HH</sub> vs m<sub>X</sub> (a heavy spin-0 resonance)



# HH→bbγγ: Analysis Overview

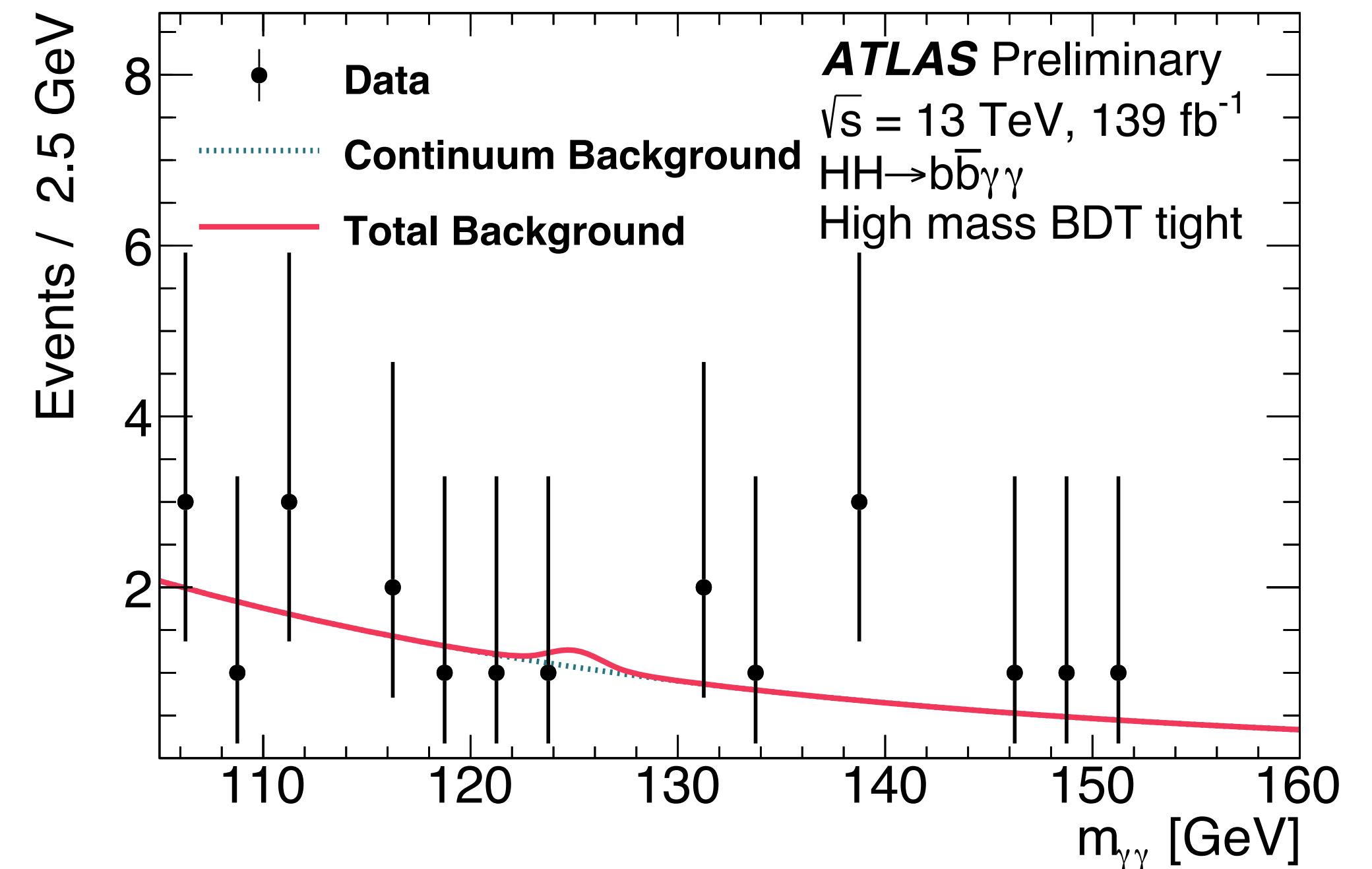
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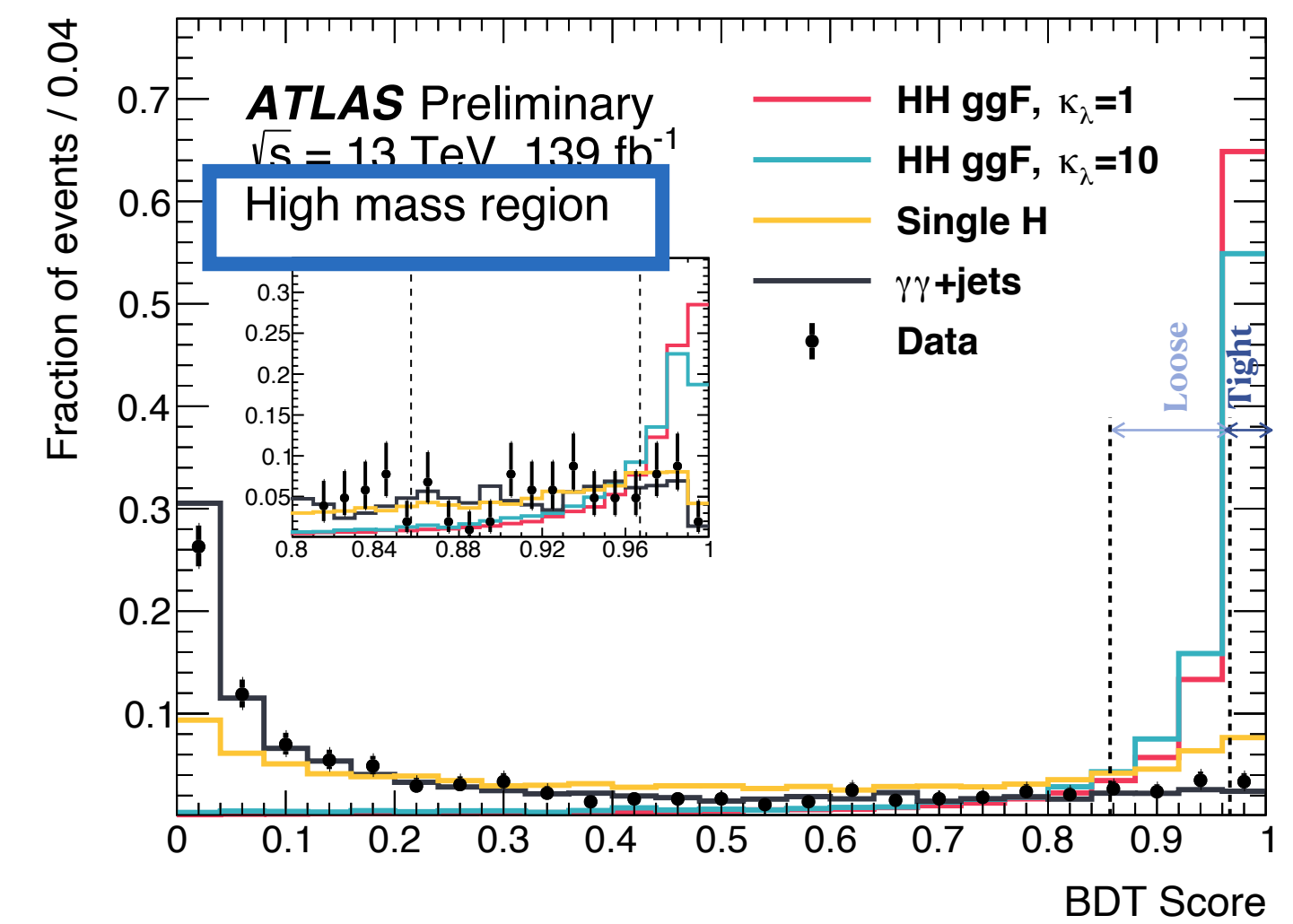
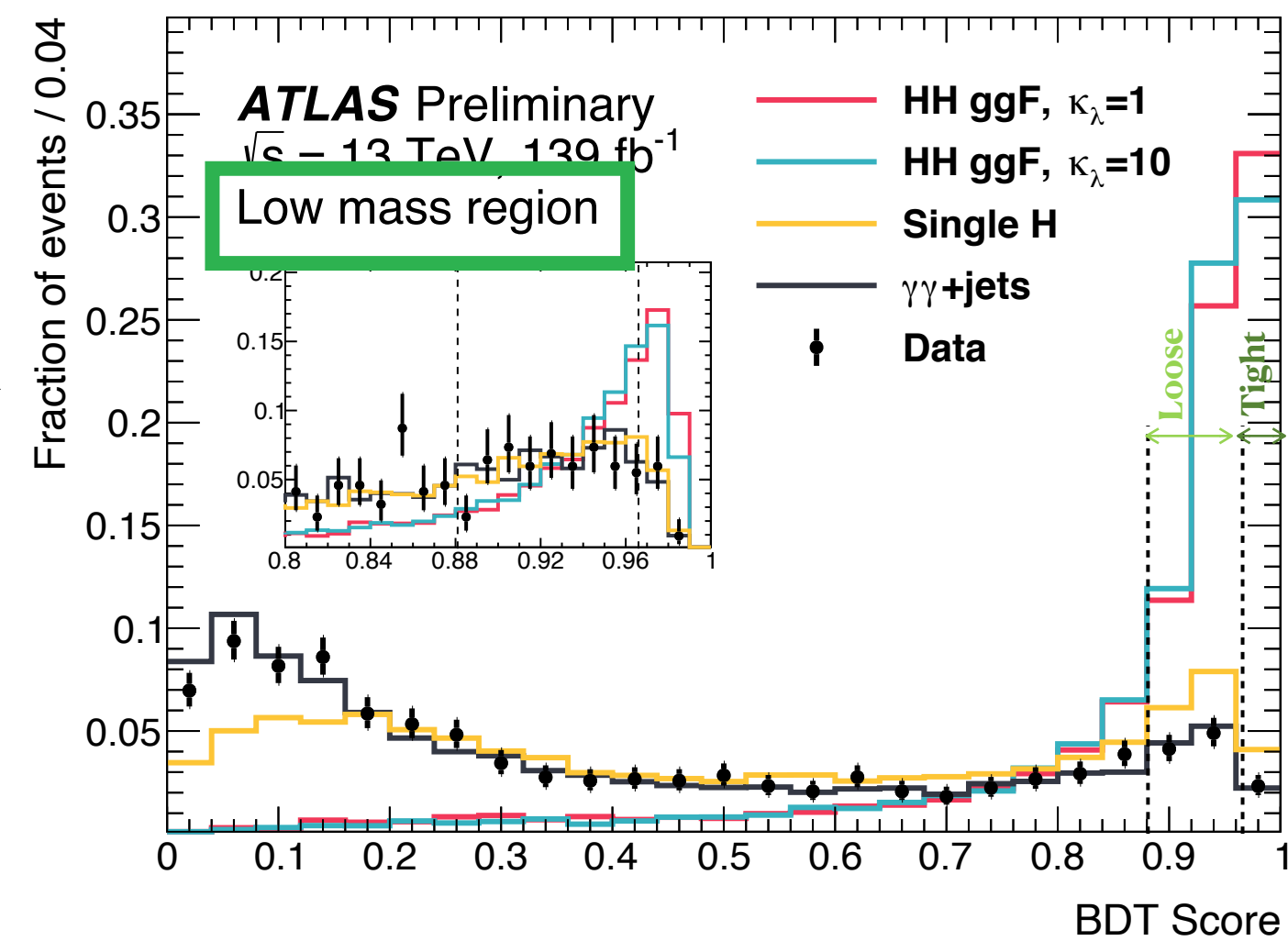
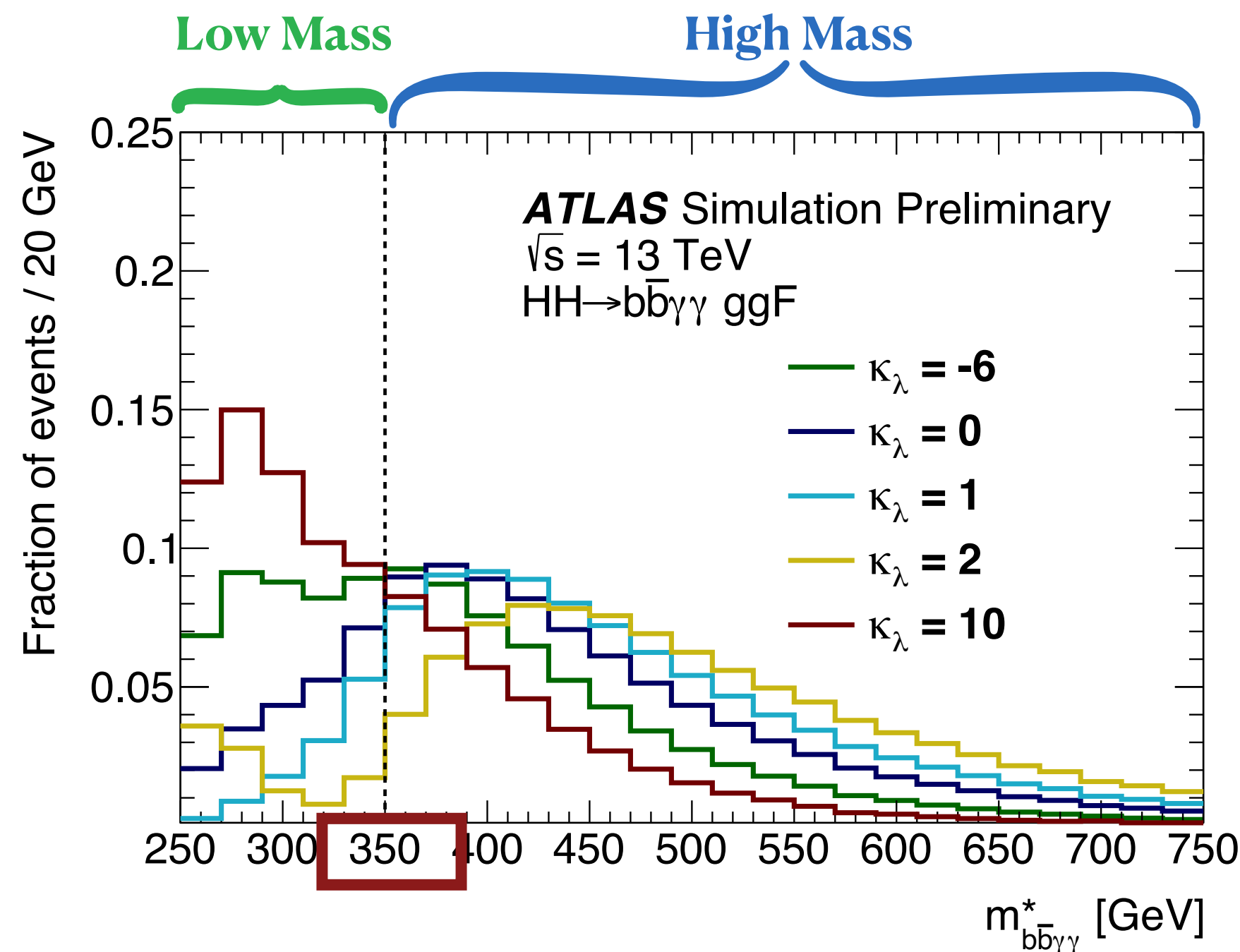
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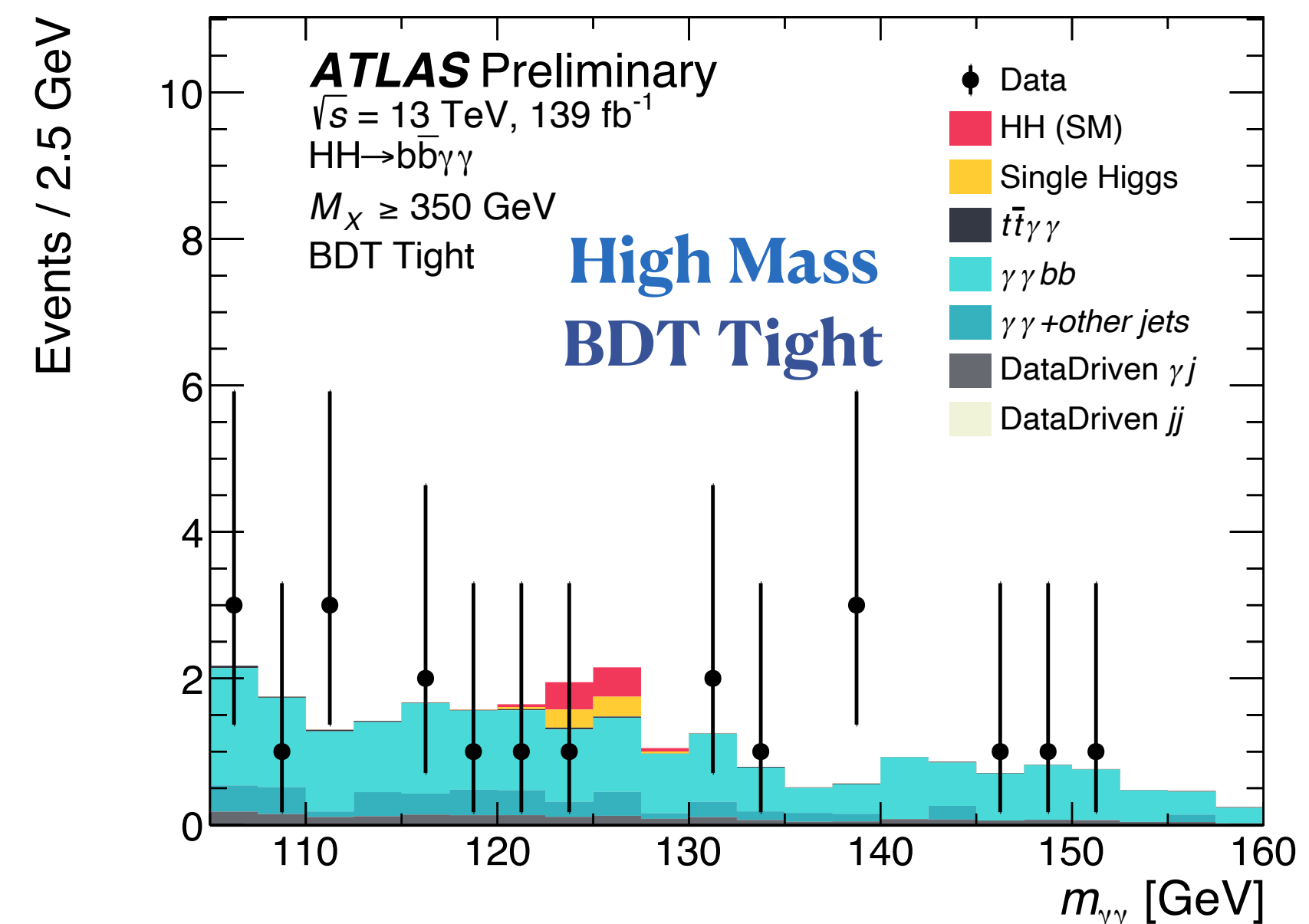
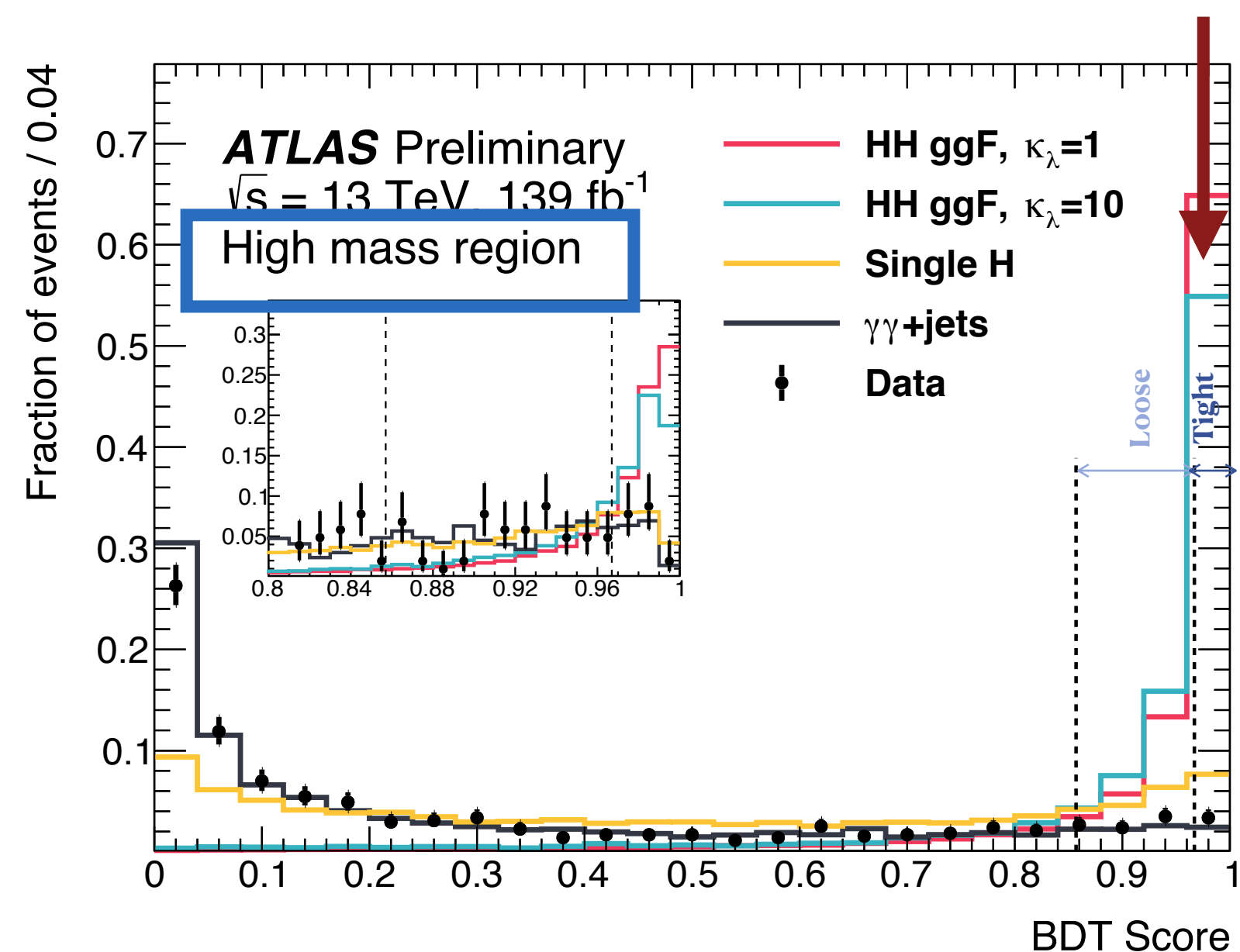
# HH $\rightarrow$ $b\bar{b}\gamma\gamma$ : Non-Resonant Analysis

- Train **two BDTs** for ggF in two  $m_{b\bar{b}\gamma\gamma}^*$  regions
  - High mass region ( $m_{b\bar{b}\gamma\gamma}^* > 350$  GeV), training with  $\kappa_\lambda = 1$  (SM HH) signal
  - Low mass region ( $m_{b\bar{b}\gamma\gamma}^* < 350$  GeV), training with  $\kappa_\lambda = 10$  (BSM HH) signal
- Further divide each mass region into **low and high BDT score regions**
- BDT trained with the ggF HH signal **used for both ggF and VBF**



# HH→bbγγ: Non-Resonant Analysis

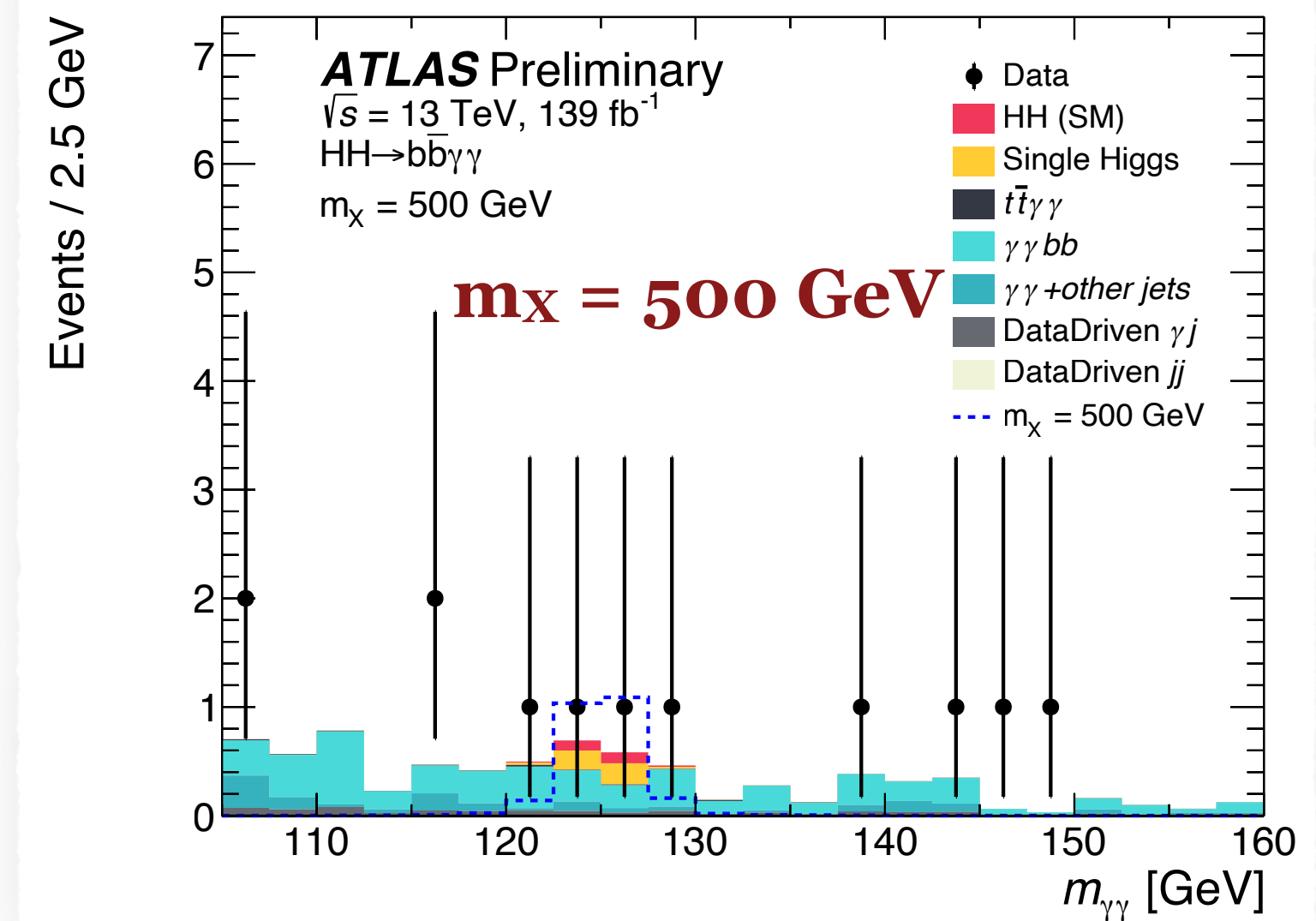
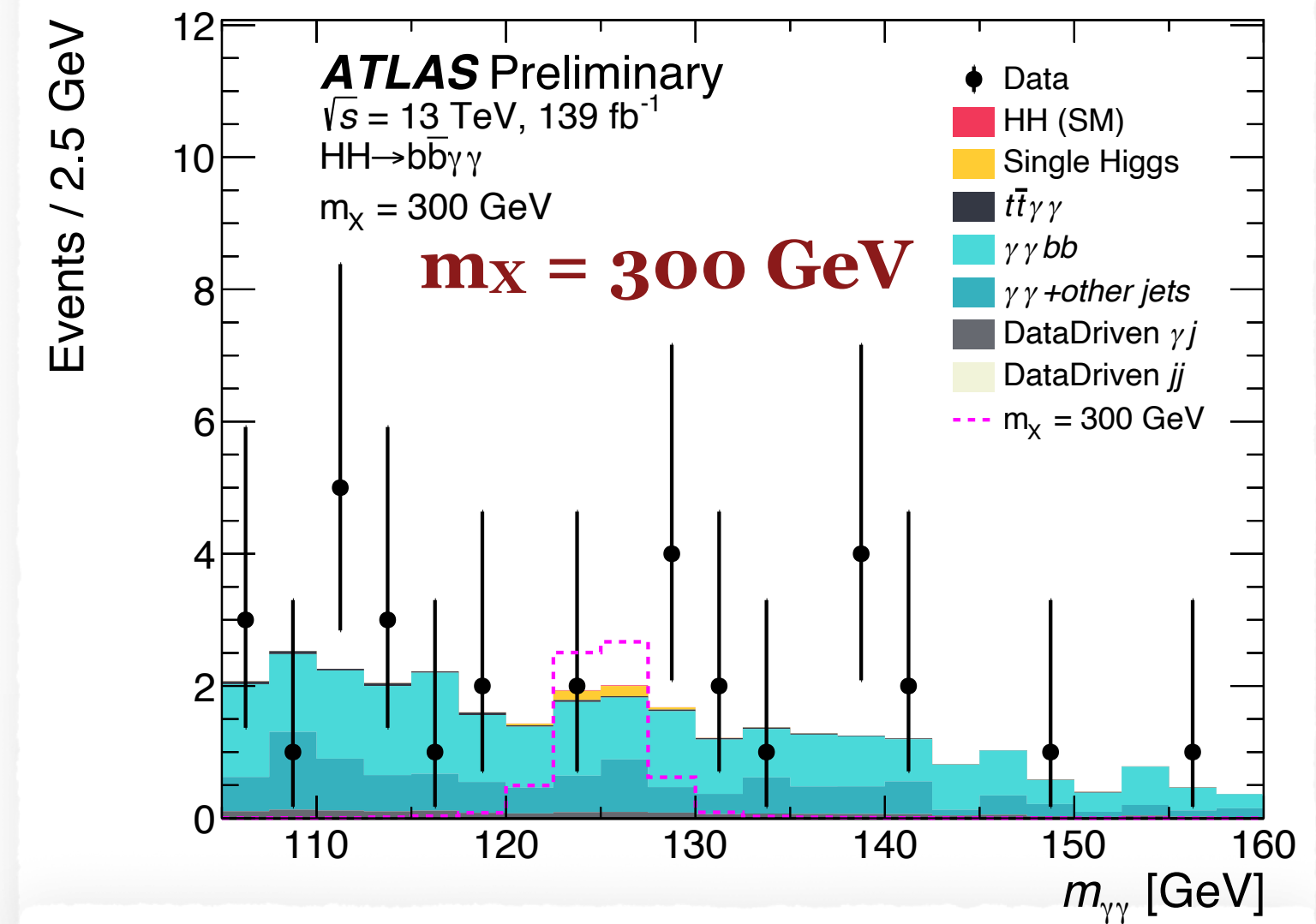
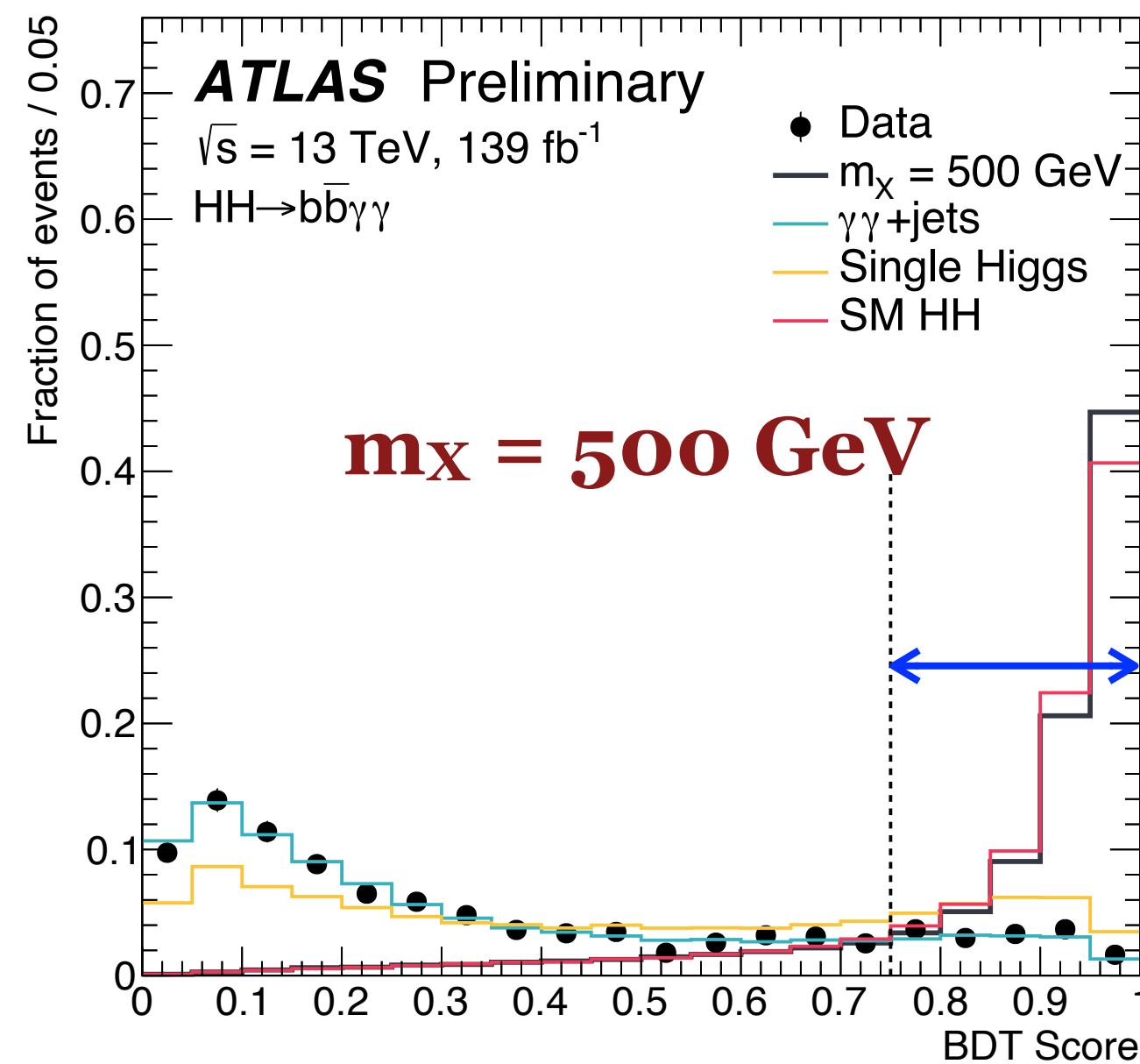
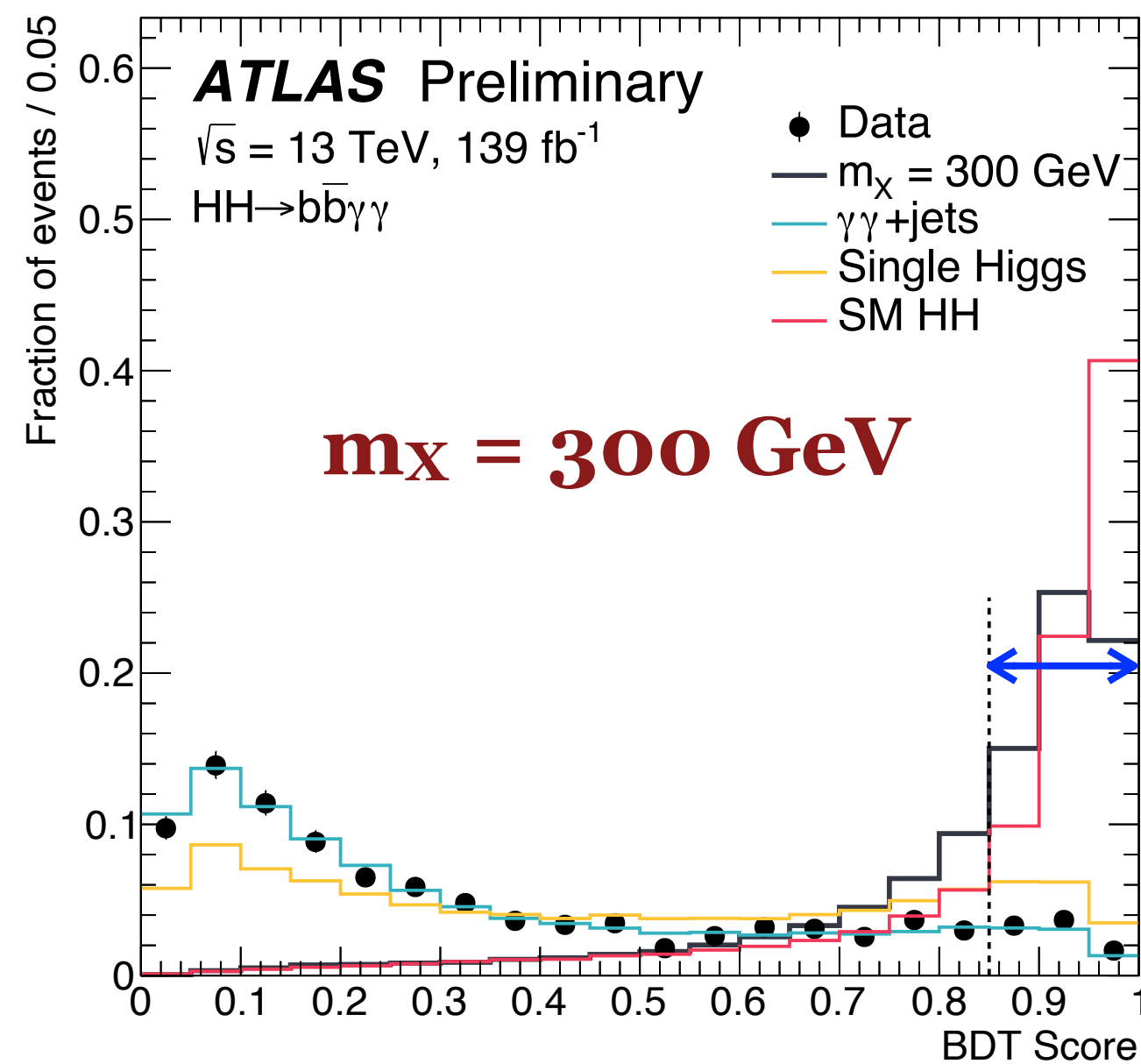
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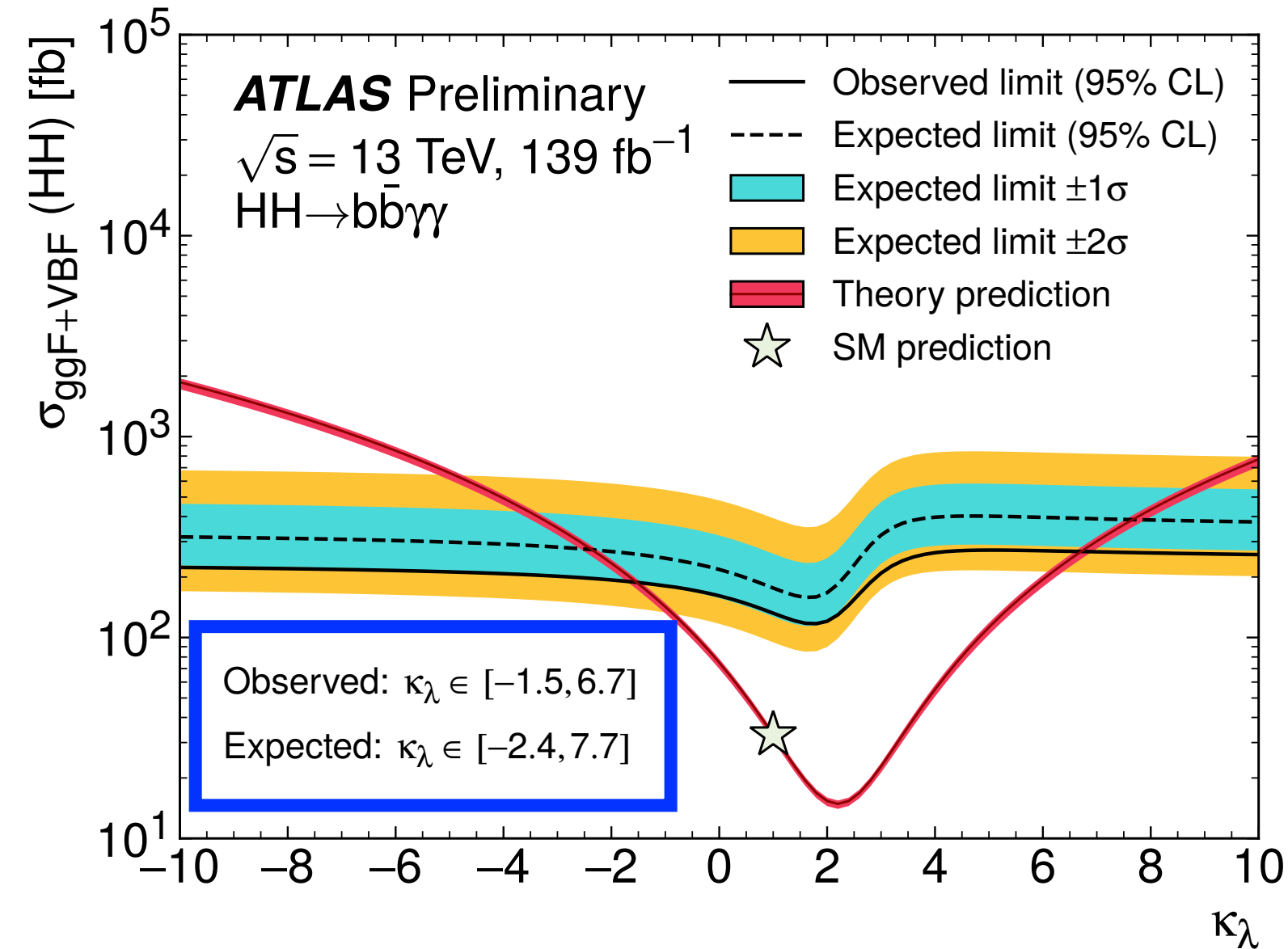
# HH→bbγγ: Resonant Analysis

- **Two BDTs trained** to better separate the signal from backgrounds of different nature:
  - **BDT<sub>γγ</sub>**: γγ + ttγγ background
  - **BDT<sub>singleH</sub>**: single-H backgrounds (ZH and ttH are the dominant bkg)
- **Two BDT scores** are combined in **BDT<sub>tot</sub>**
- **Mass-dependent cuts** are applied on **BDT<sub>tot</sub>** to define the SR for each mass



# HH→bbγγ: Results

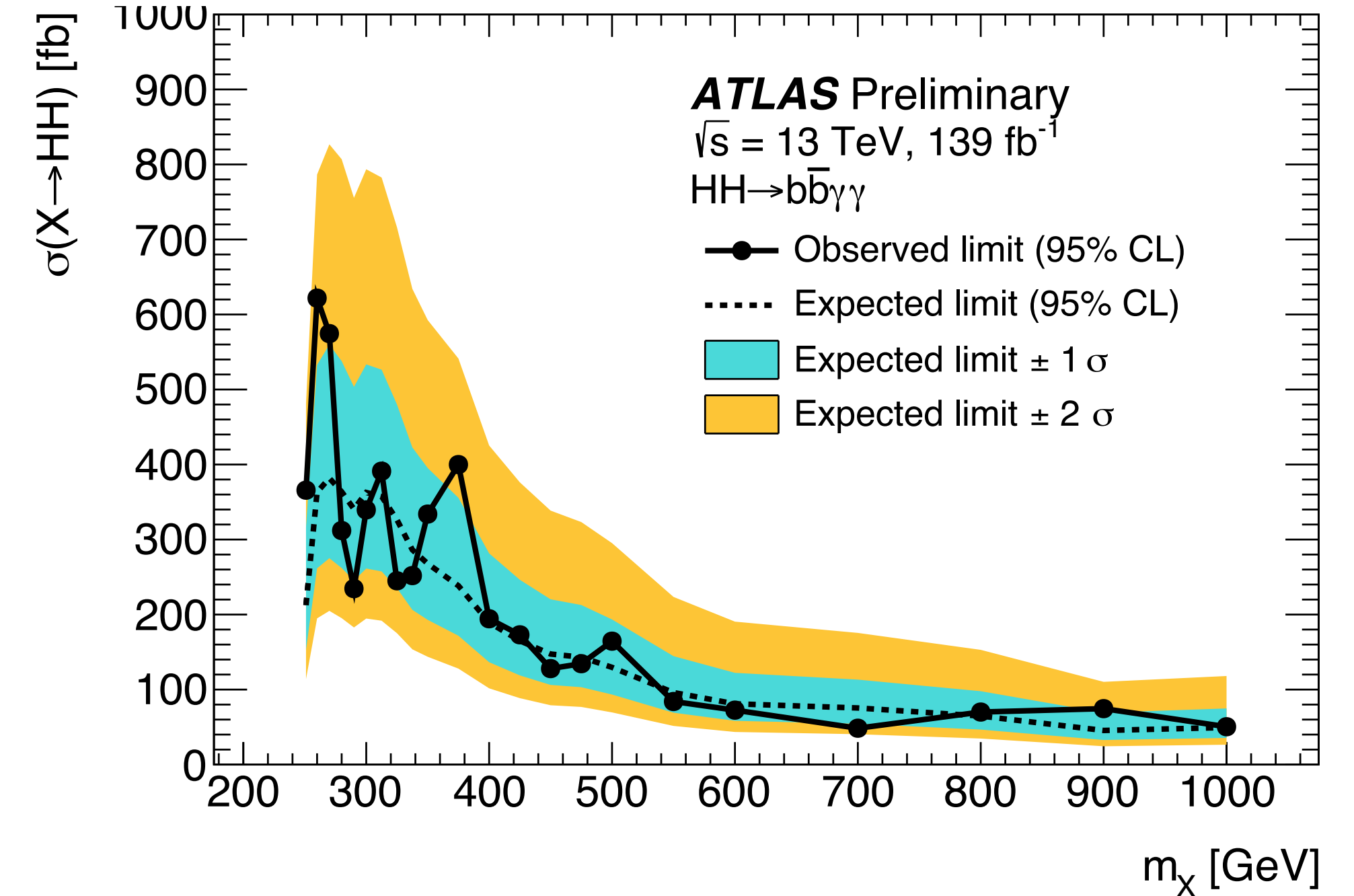
## Non-Resonant Results



ggF+VBF	Limit on $\sigma_{\text{HH}}$ [fb]	Limit on $\mu$ ( $\sigma/\sigma_{\text{SM}}$ )
Obs (Exp)	130 (180)	4.1 (5.5)

- No significant excess observed
- **5 x improvement** on the previous result ( $\sim 26 \times \text{SM}$ , with  $36 \text{ fb}^{-1}$ )
  - **3 x improvement** as a result of analysis improvements
- Statistically dominated, few % impact from systematics

## Resonant Results



- No significant excess observed
- Limits set on narrow width scalar resonances from 251 GeV to 1000 GeV
  - **Obs (exp)** varies between **610-47 fb (360-43 fb)**
  - **2 x-3 x improvement** depending on  $m_X$ 
    - **1/3 x improvement** from the BDT strategy

# $HH \rightarrow bb\tau\tau$

**Publication:** ATLAS-CONF-2021-030

**Physics Briefing:** Two Higgs bosons are better than one

# HH→bbττ: Analysis Overview

- Search for **non-resonant (ggF+VBF)** and **resonant HH production** using **139 fb<sup>-1</sup>** of pp data
  - 2 b-jets and 2 τ-leptons

- **Two initial categories** based on the di-τ decay mode:

- **τ<sub>lep</sub>τ<sub>had</sub>**: e/μ and oppositely charged τ<sub>had</sub>
- **τ<sub>had</sub>τ<sub>had</sub>**: two oppositely charge τ<sub>had</sub>

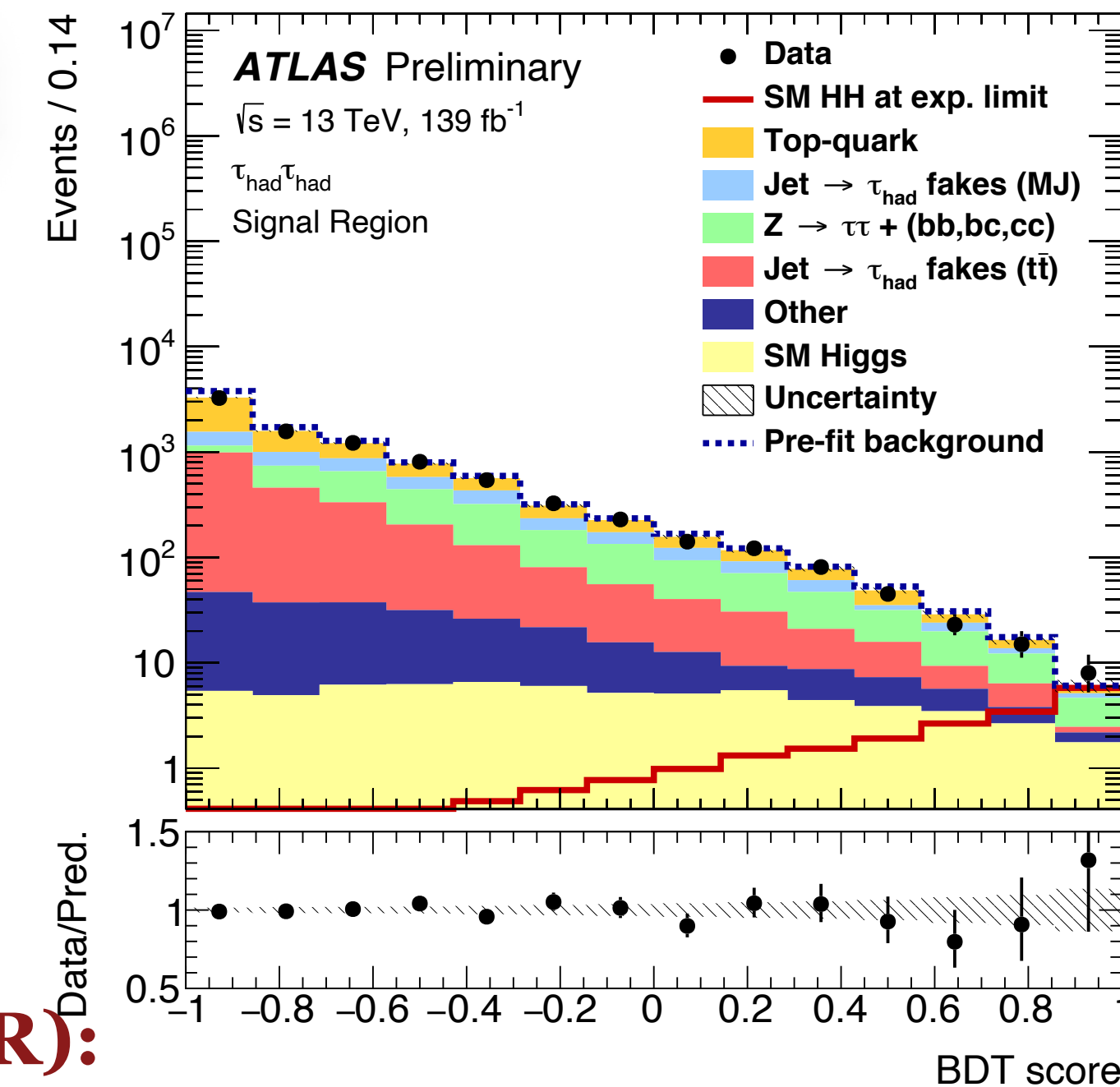
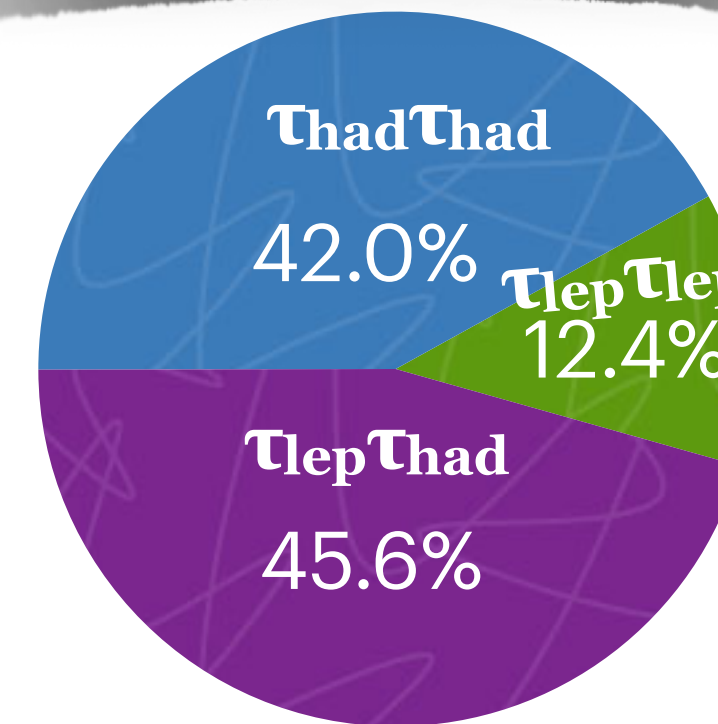
- **Backgrounds:**

- True τ<sub>had</sub> in ttbar and Z+HF (from MC, normalization from data)
- Fake τ<sub>had</sub> (jets faking τ<sub>had</sub>) in ttbar and multi-jet (data-driven)

- **Likelihood fits to MVA scores** in **3 signal regions (SRs)** and **1 control region (CR)**:

- τ<sub>lep</sub>τ<sub>had</sub> Single Lepton Trigger (SLT) SR - high acceptance, large ttbar contamination
- τ<sub>lep</sub>τ<sub>had</sub> Lepton Tau Trigger (LTT) SR - lowered p<sub>T</sub><sup>(l)</sup> improves low-mass sensitivity
- τ<sub>had</sub>τ<sub>had</sub> Single- and Di- Tau Triggers (STT/DTT) SR - high purity
- Z(→ll)+HF CR - measurement in bbll final state, m<sub>ll</sub> used as a discriminant

**Di-Tau Branching Ratio**



MVA	Resonant	Non-Resonant	
		τ <sub>had</sub> τ <sub>had</sub>	τ <sub>lep</sub> τ <sub>had</sub>
	PNN	BDT	NN

# HH→bbττ: Non-Resonant Results

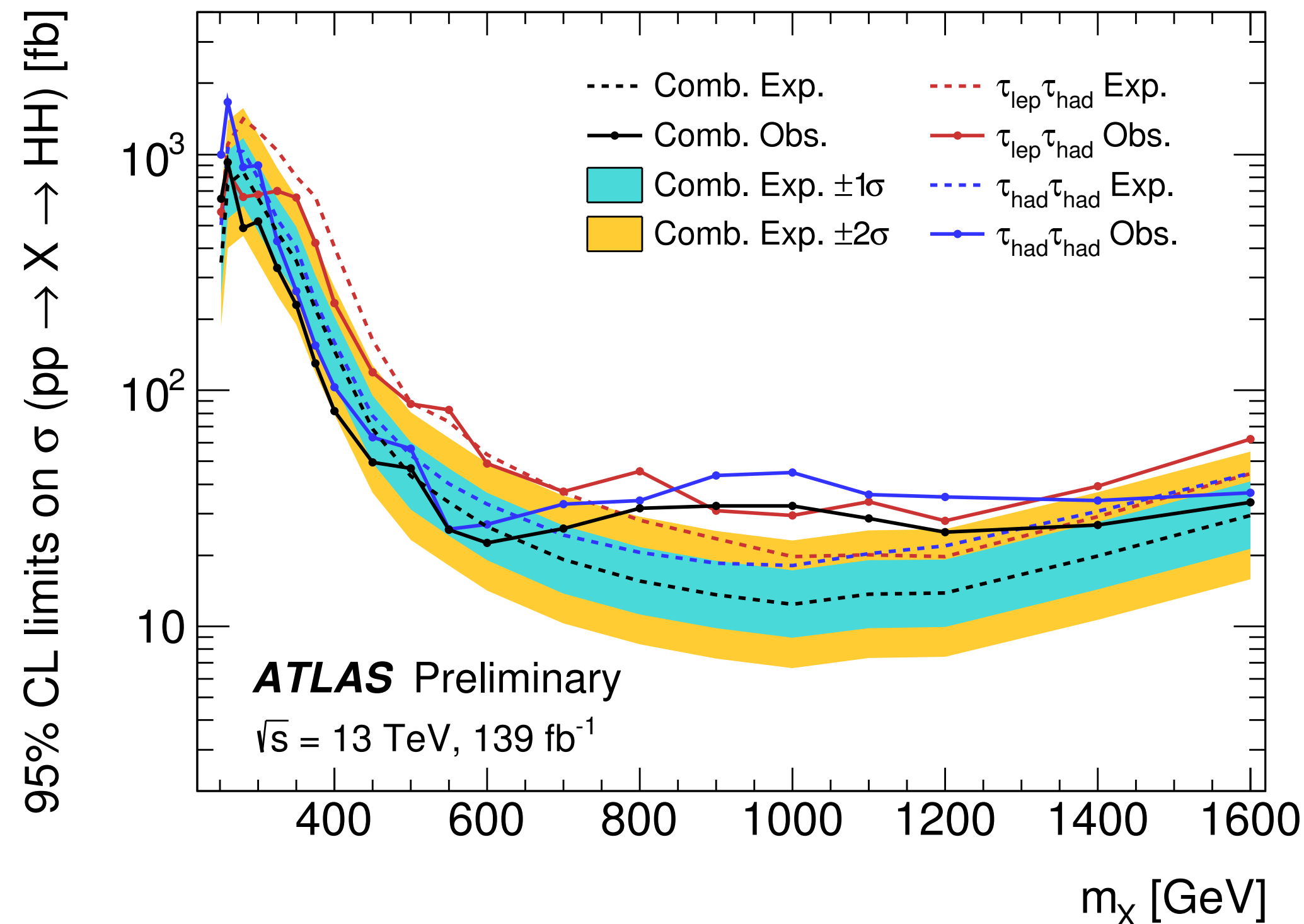
- **4 x improvement** wrt previous SM limits (with 36 fb<sup>-1</sup>)
  - **2 x** due to improvements in τ<sub>had</sub> and b-jet reconstruction/identification, and improvements in the MVA classification strategy and the fake estimation methods
- Statistically dominated, largest systematics from background modelling

		Observed	-2 σ	-1 σ	Expected	+1 σ	+2 σ
τ <sub>had</sub> τ <sub>had</sub>	σ <sub>ggF+VBF</sub> [fb]	145	70.5	94.6	131	183	245
	σ <sub>ggF+VBF</sub> /σ <sub>ggF+VBF</sub> <sup>SM</sup>	4.95	2.38	3.19	4.43	6.17	8.27
τ <sub>lep</sub> τ <sub>had</sub>	σ <sub>ggF+VBF</sub> [fb]	265	124	167	231	322	432
	σ <sub>ggF+VBF</sub> /σ <sub>ggF+VBF</sub> <sup>SM</sup>	9.16	4.22	5.66	7.86	10.9	14.7
<b>Combined</b>	σ <sub>ggF+VBF</sub> [fb]	135	61.3	82.3	114	159	213
	σ <sub>ggF+VBF</sub> /σ <sub>ggF+VBF</sub> <sup>SM</sup>	<b>4.65</b>	2.08	2.79	<b>3.87</b>	5.39	7.22

Limits on μ include the new cross-section uncertainties

**The highest expected sensitivity to non-resonant HH production to date**

# HH $\rightarrow$ bb $\tau\tau$ : Resonant Results



- The most significant excess for  $\tau_{had}\tau_{had}$  ( $\tau_{lep}\tau_{had}$ ) at 1 TeV (1.1 TeV), a local significance of  $2.8\sigma$  ( $1.5\sigma$ )
- The most significant **combined excess** is at  $m_X=1 \text{ TeV}$  with a local significance of  $3.0\sigma$  and a **global significance of  $2.0(+0.4, -0.2)\sigma$**

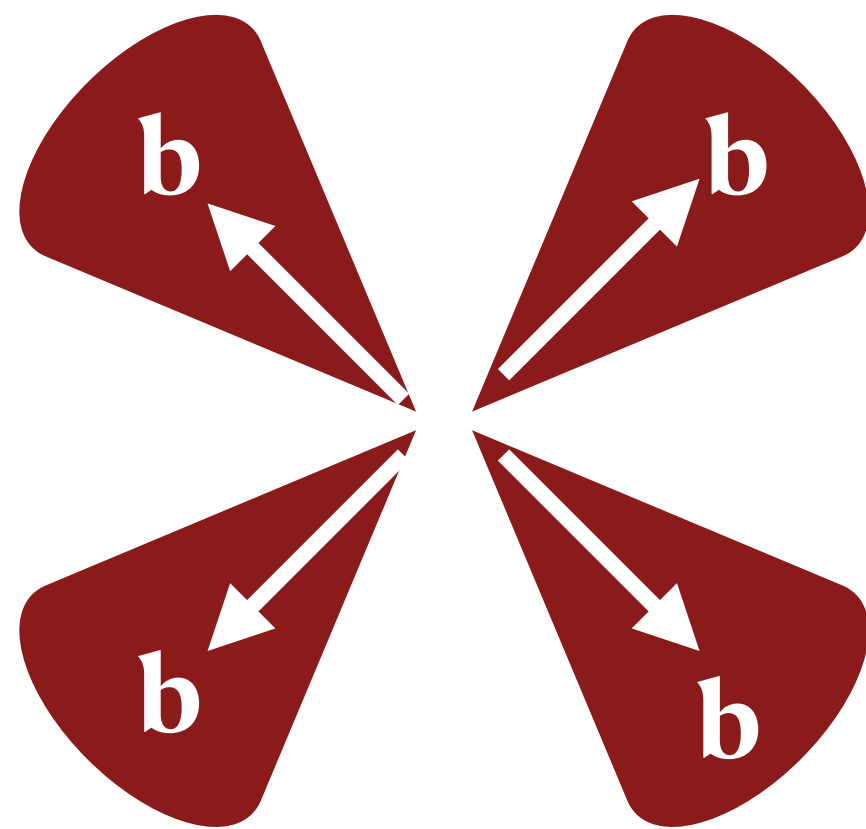
# HH $\rightarrow$ bbbb

**Publication:** ATLAS-CONF-2021-035

**Physics Briefing:** Probing new physics with pairs of Higgs bosons

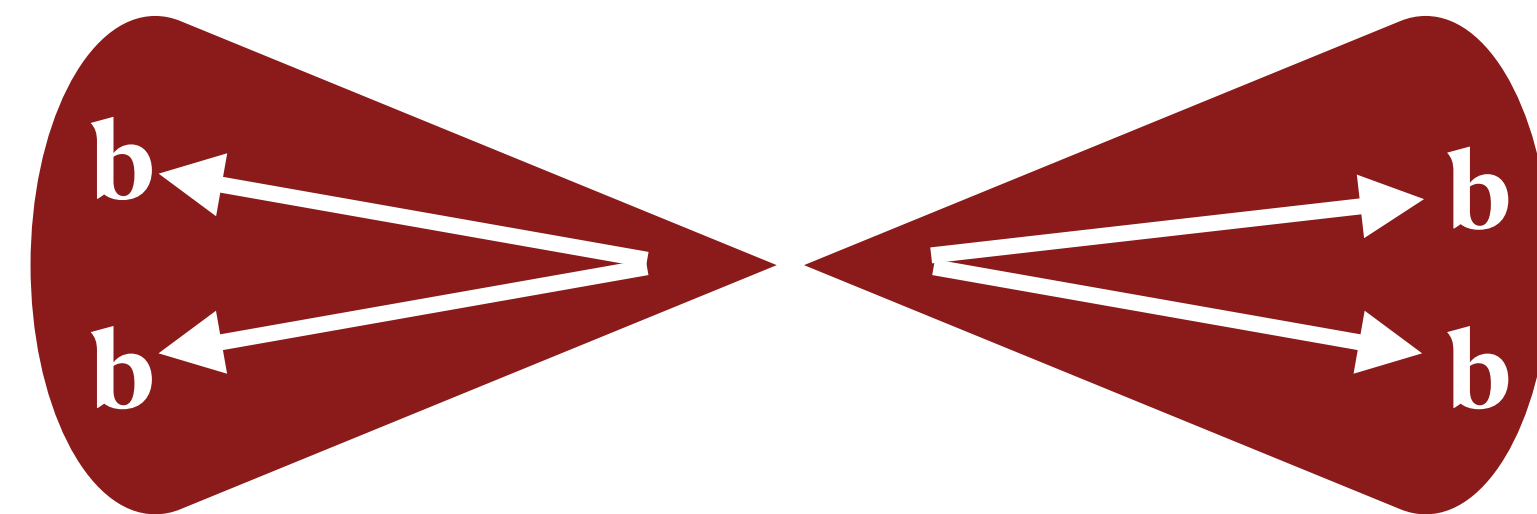
# HH $\rightarrow$ bbbb

- Search for **resonant HH production in resolved (boosted) channels** using **126 (139) fb<sup>-1</sup>** of pp data
  - Narrow-width **spin-0** resonance and **spin-2** Kaluza-Klein graviton



## Resolved:

- Require 4 small R-jets ( $R=0.4$ )
- Targets low-medium mass resonances:
  - $m_X = 251-1500$  GeV



## Boosted:

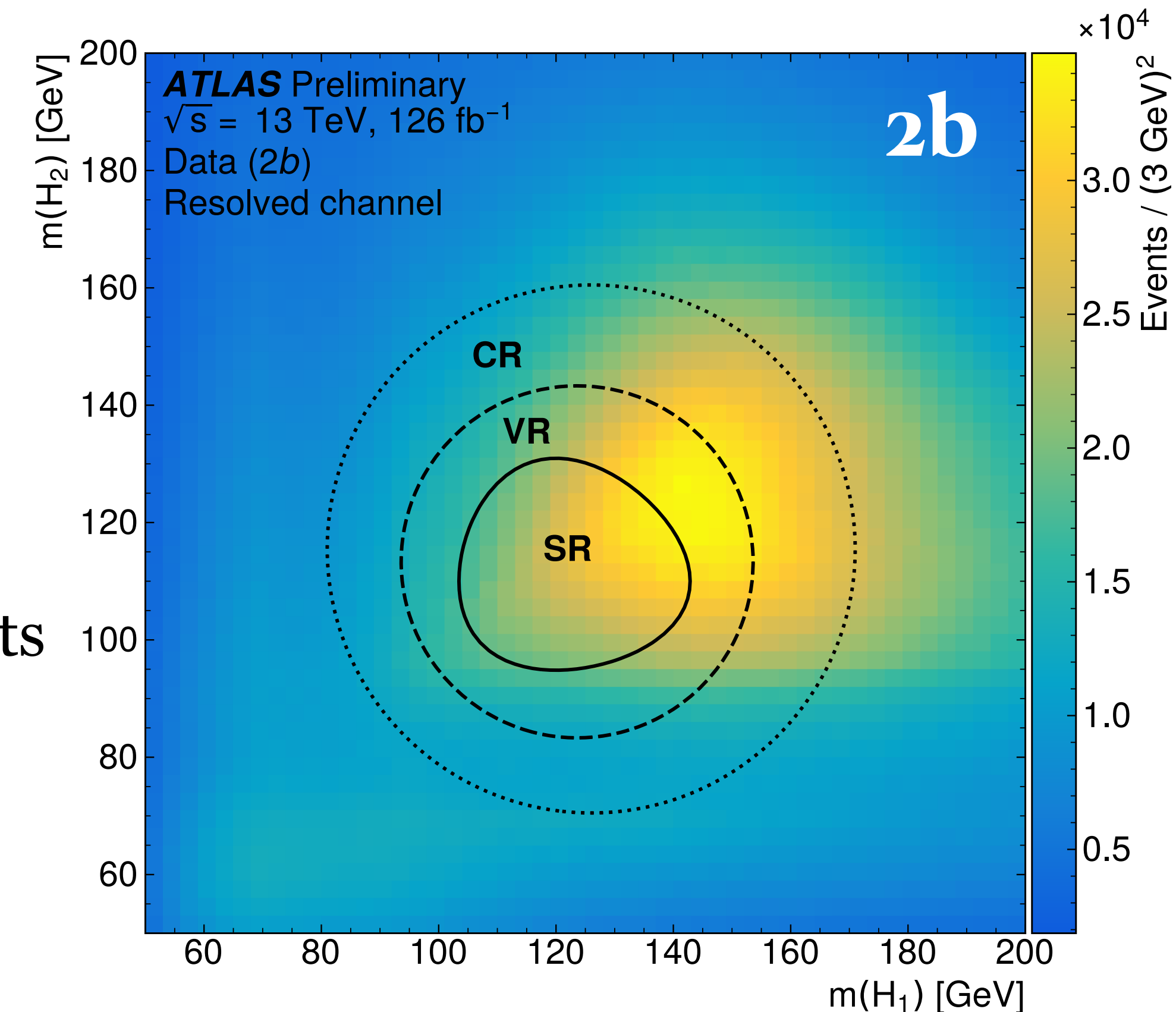
- Require 2 large R-jets ( $R=1.0$ )
  - Variable-radius track jets are used for b-tagging
- Targets high mass resonances:
  - $m_X = 900-3000$  GeV

**Two channels statistically combined in the overlap mass range**



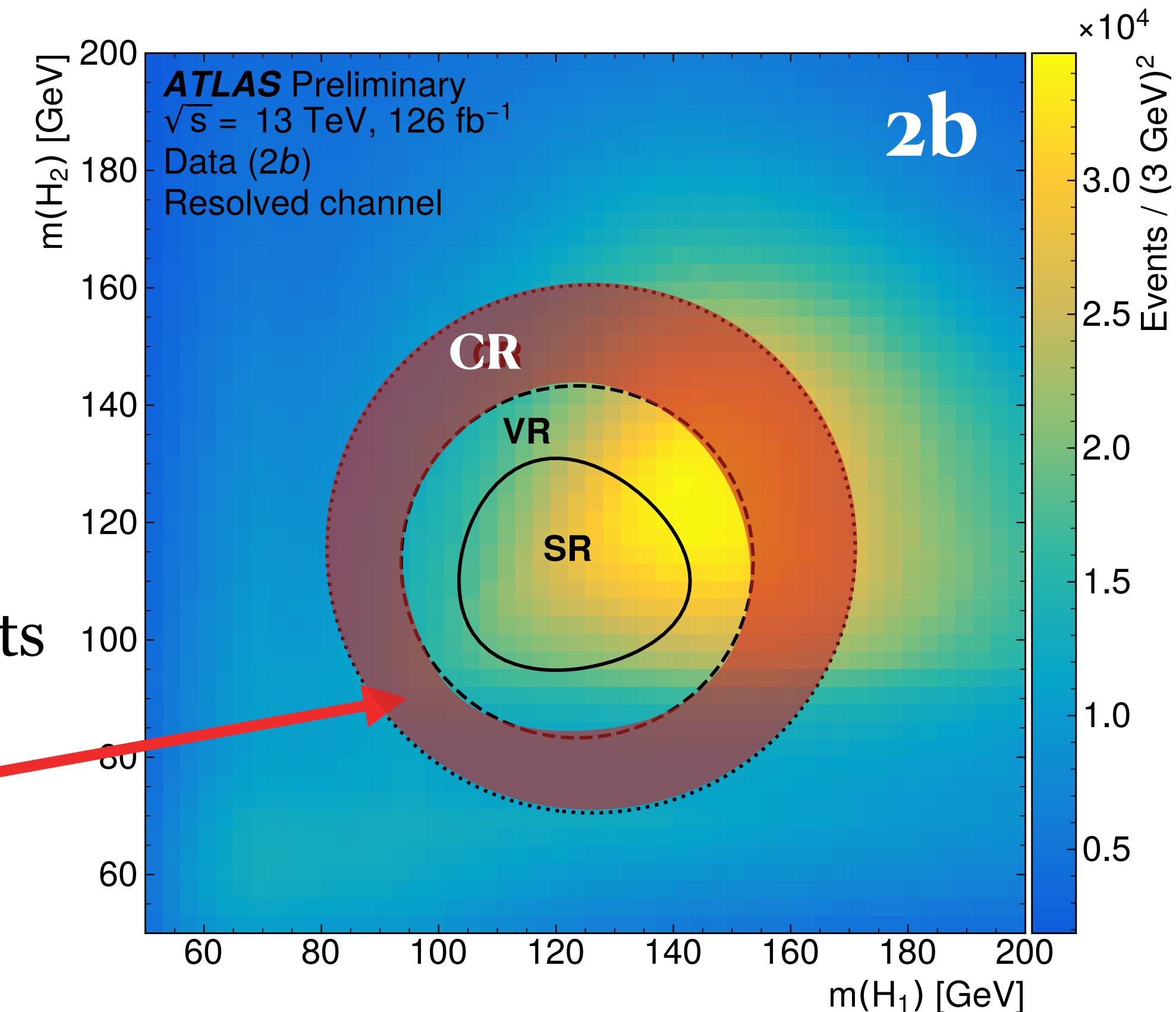
# HH→bbbb: Resolved Analysis Overview

- Uses a combination of b-jet, jet and  $H_T$  ( $\sum_{\text{jets}} |E_T|$ ) triggers
- **At least 4 small R-jets** is required in an event
- **BDT** is used to **pair the jets** into Higgs boson candidates
- **Two categories:**
  - **4b signal region:** 4 b-jets
  - **2b category for background estimate:** 2 b-jets + 2 untagged jets
    - Fully **data-driven background** estimation:
      - **~95% multijet**, **~5% from  $t\bar{t}$**
      - **Derive weights in the CR**, mapping from 2b to 4b
      - **Apply weights in 2b SR** to get a model of background in the 4b SR
- Likelihood fit in bins of “corrected  $m_{HH}$ ”



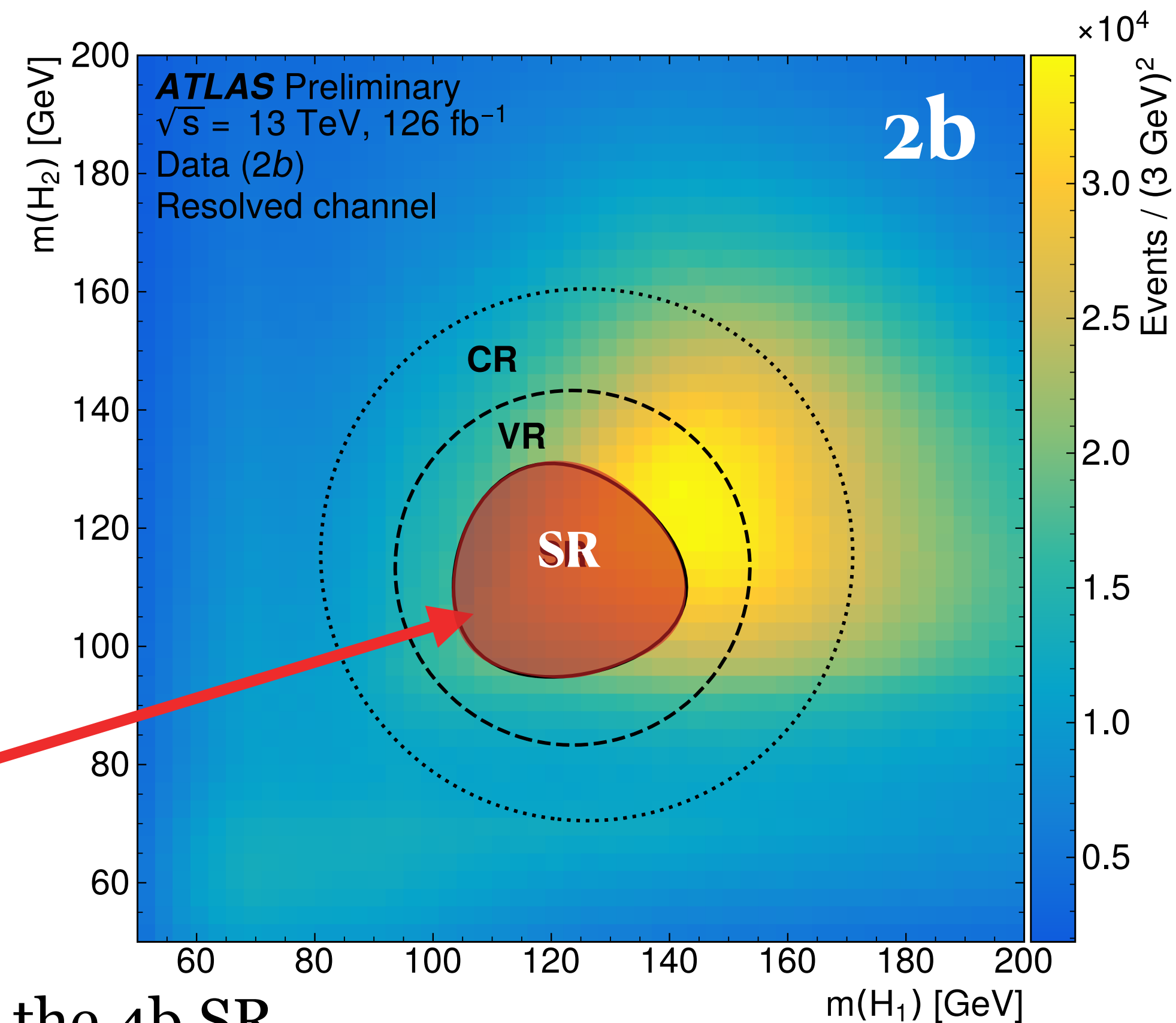
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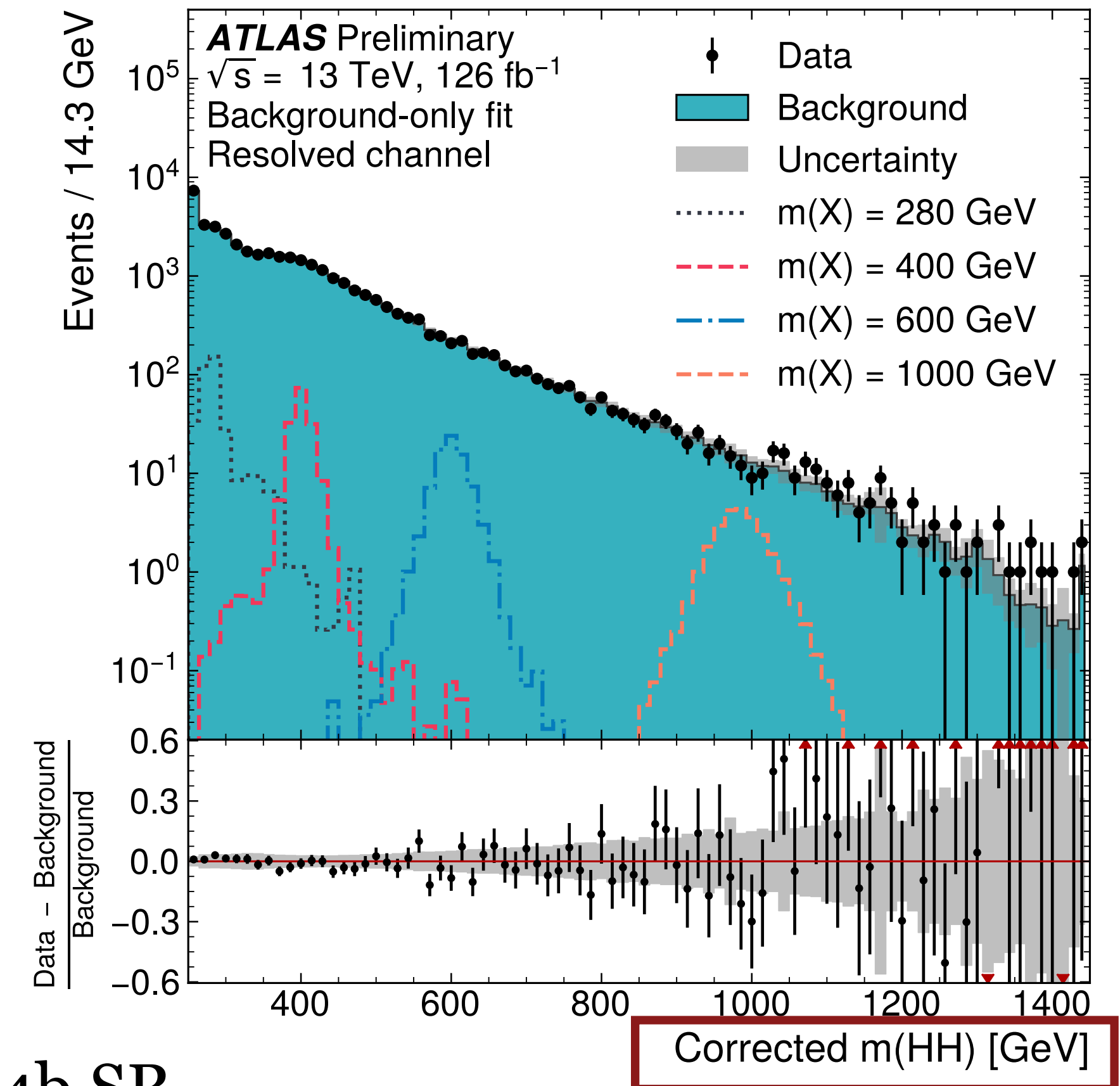
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- **Likelihood fit** in bins of **“corrected  $m_{HH}$ ”**



**“corrected  $m_{HH}$ ”** calculated by

- rescaling Higgs candidates' 4-vectors such that  $m(H_1)=m(H_2)=125 \text{ GeV}$
- sum the rescaled 4-vectors and take the invariant mass

# HH→bbbb: Boosted Analysis Overview

- Uses single large-R jet trigger
- At least two large-R jets required
- Fully data-driven multijet background estimation
- The remainder from  $t\bar{t}$ , from MC
  - Up to 30% contribution
  - Data-driven corrections applied in 2b and 3b categories
- 3 SRs are defined: 2b, 3b, 4b categories

4b background from 2b-2f

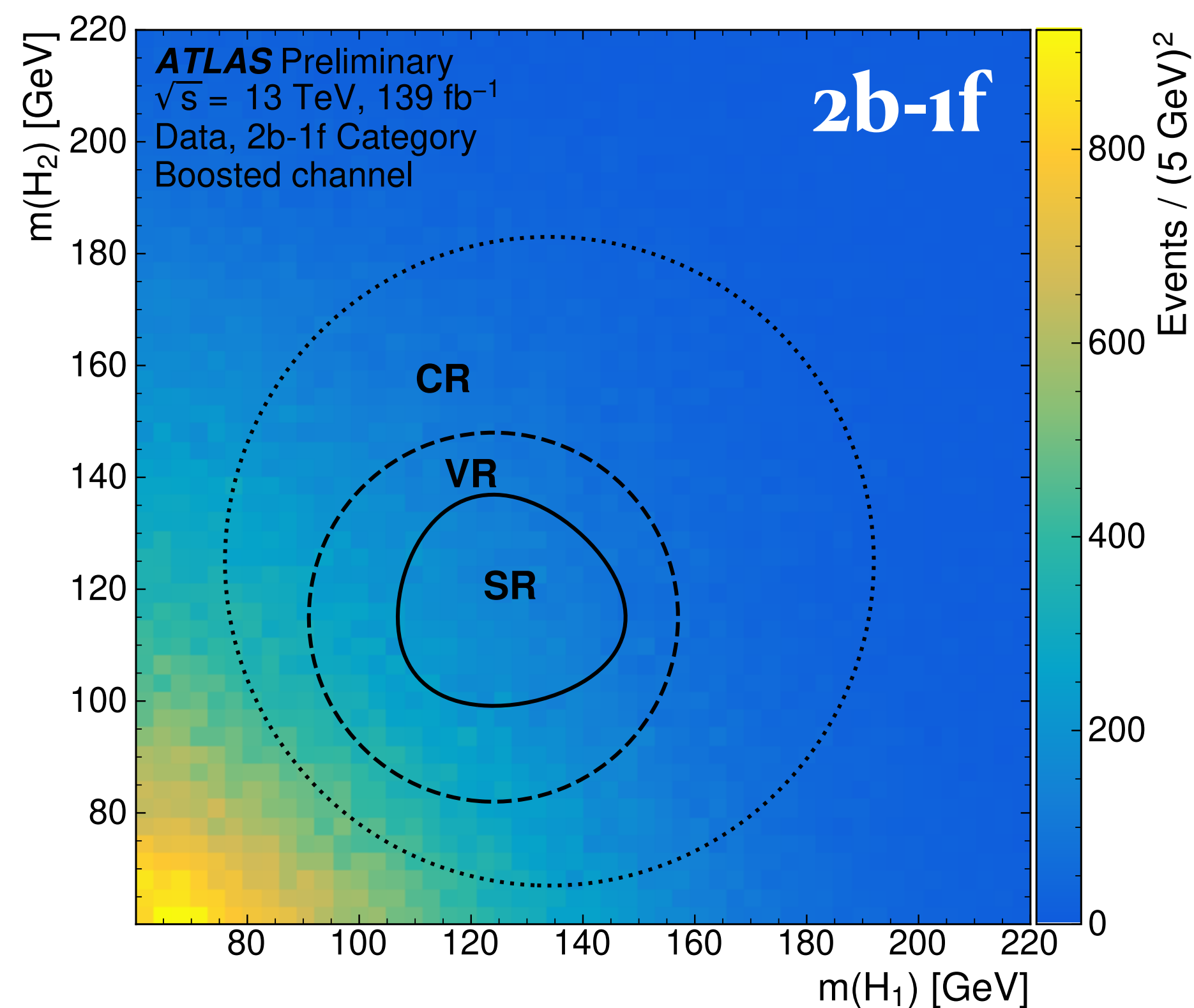
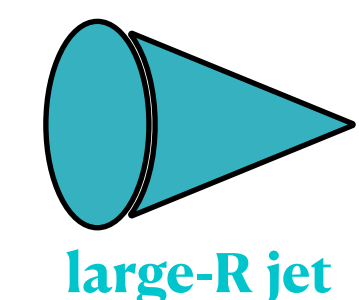
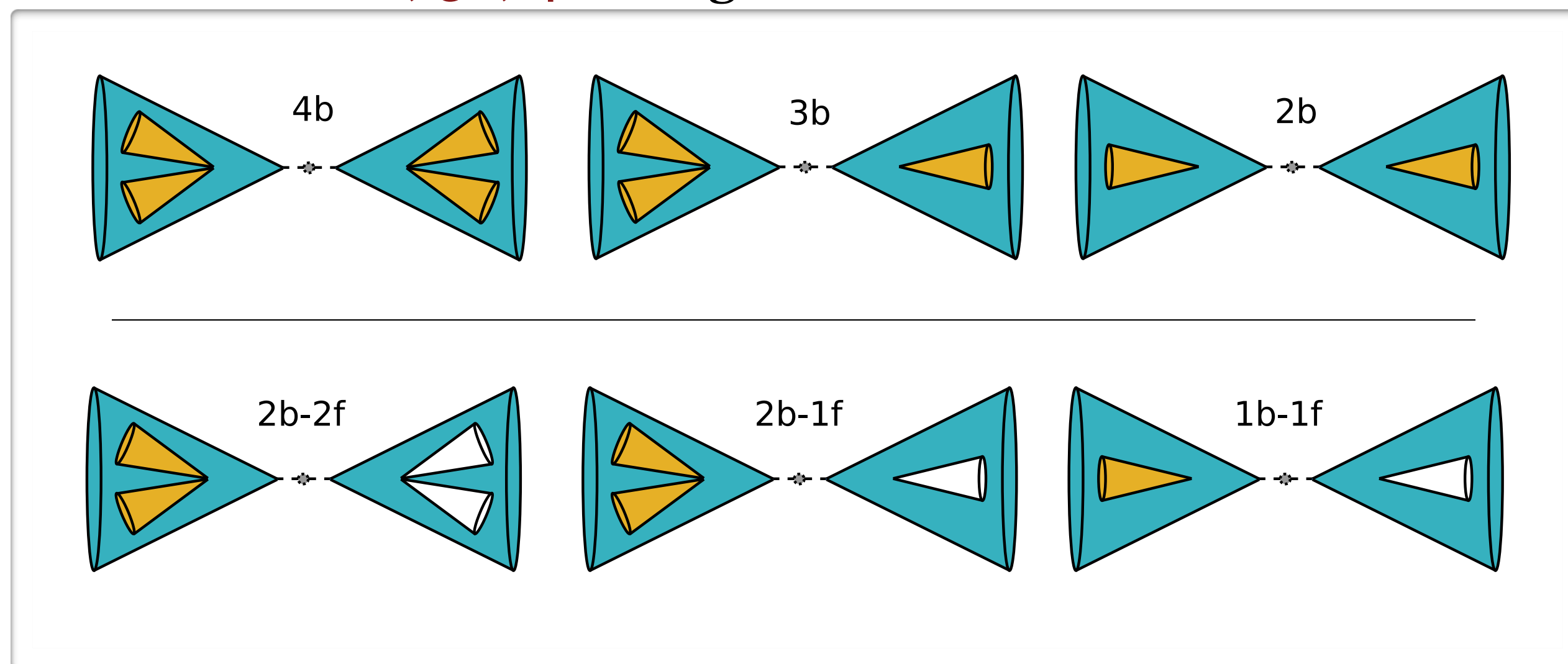
3b background from 2b-1f

2b background from 1b-1f

Region definitions slightly different from the resolved analysis

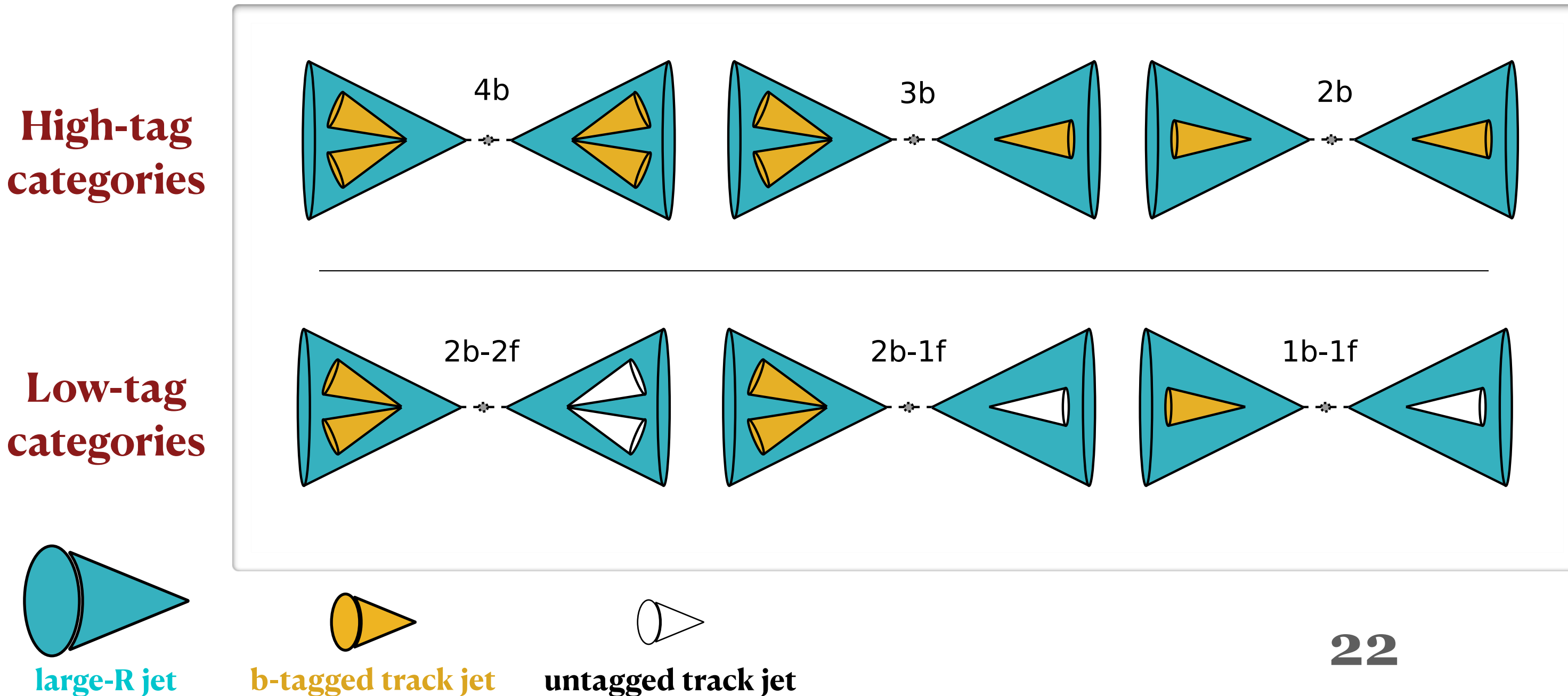
High-tag categories

Low-tag categories

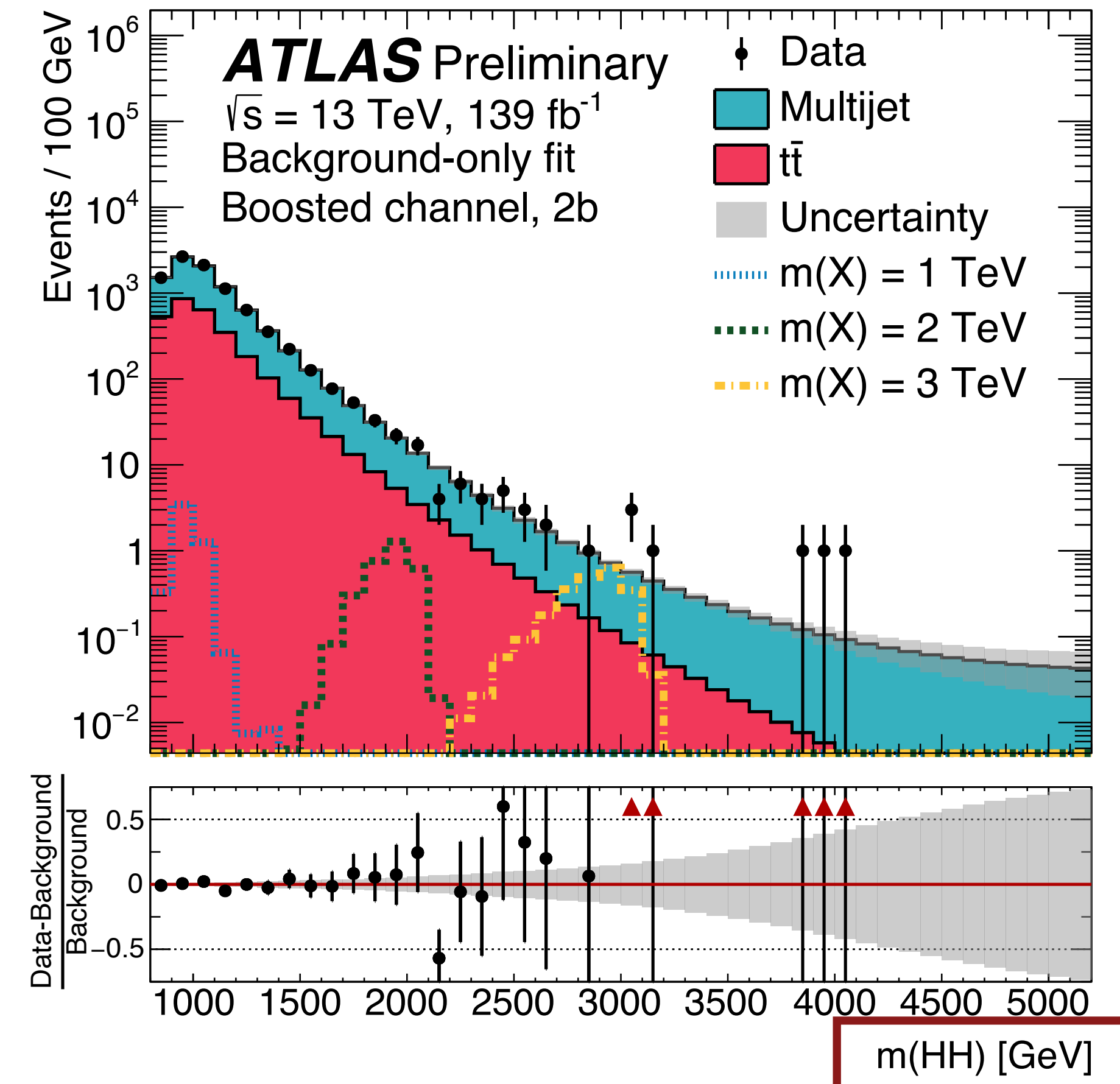


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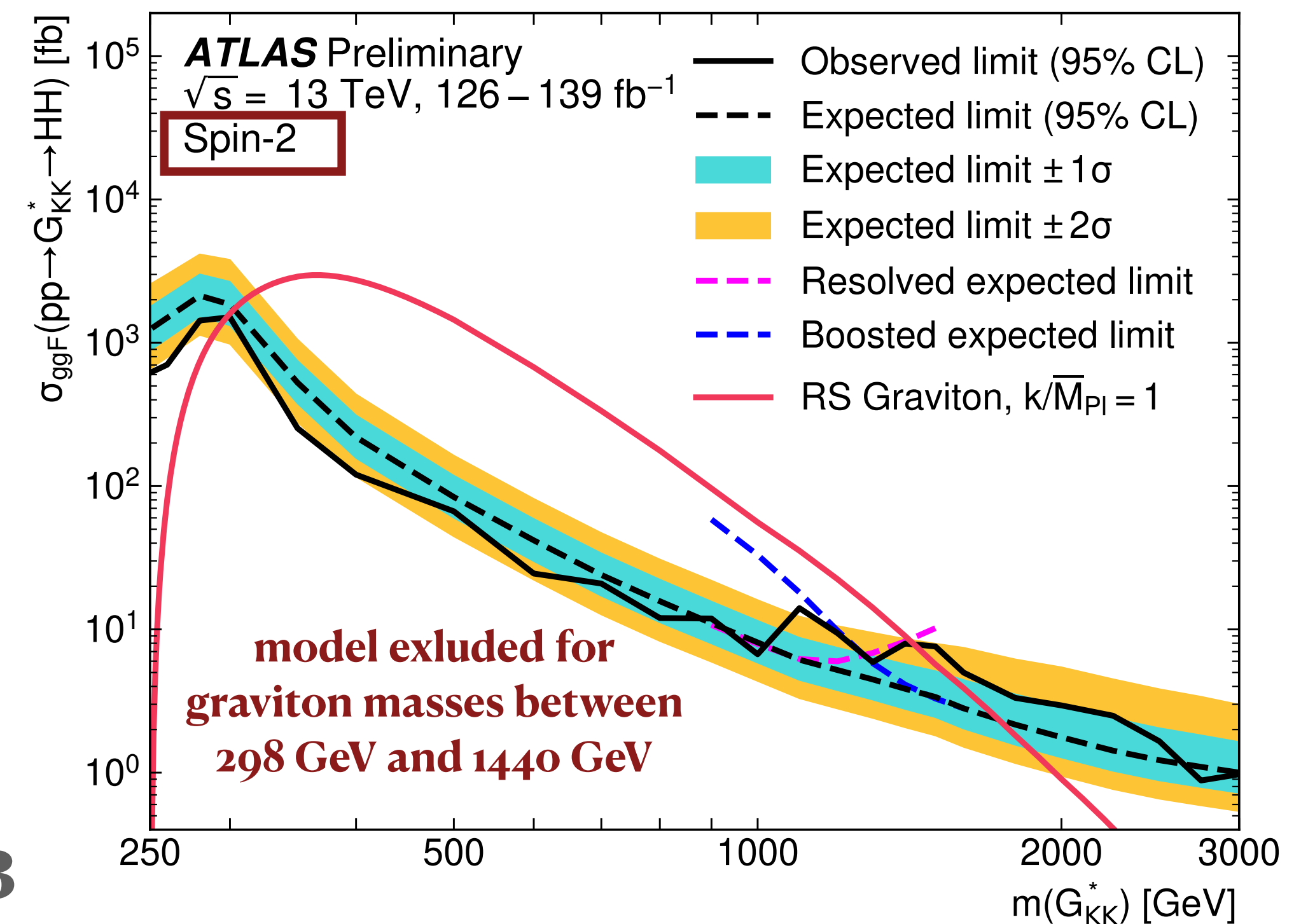
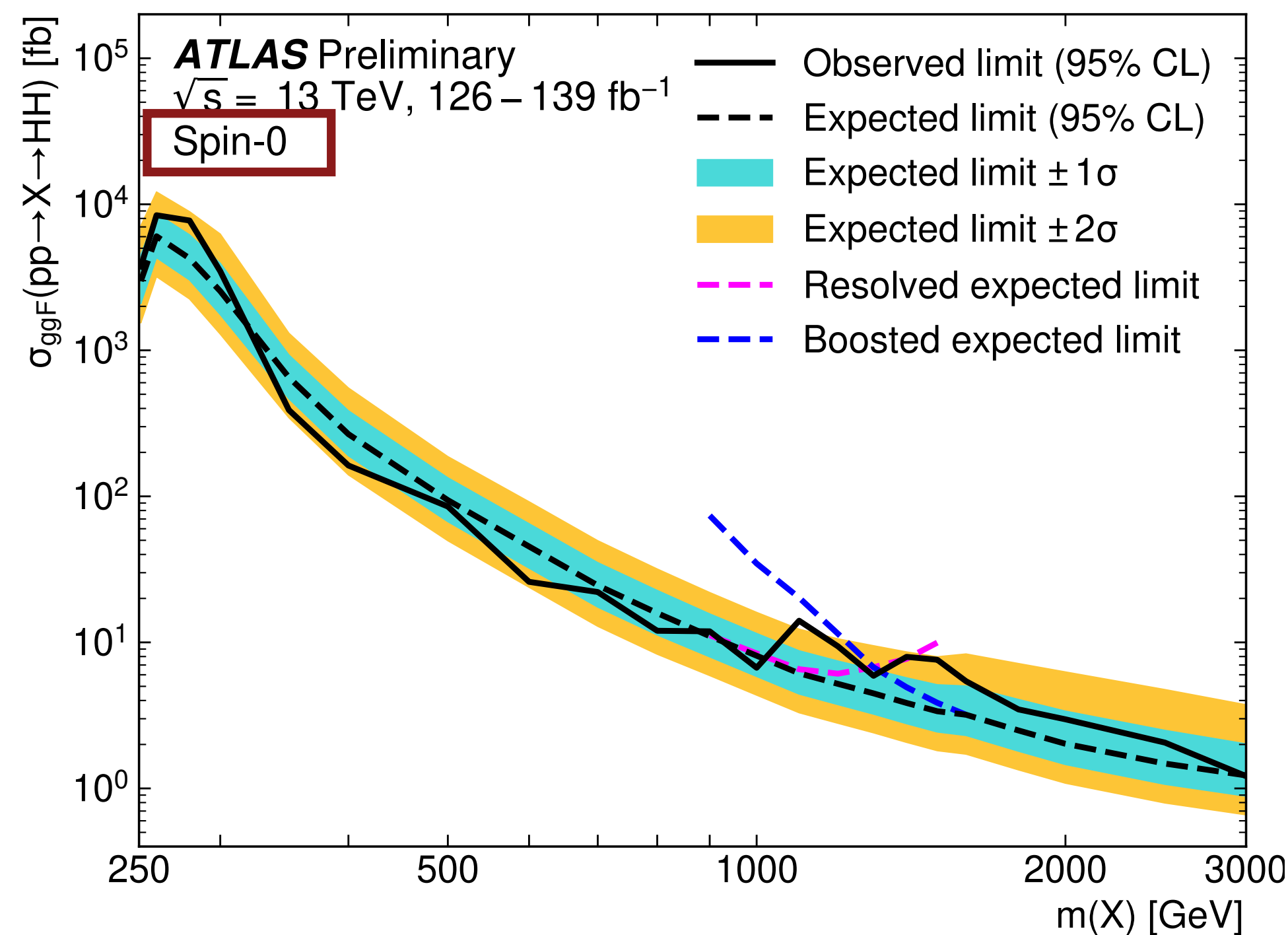


## Likelihood fit in bins of $m_{HH}$



# HH → bbb: Results

- Set upper limits at 95% CL on  $\sigma \times \text{BR}$  of **resonant  $X/G_{KK}^* \rightarrow \text{HH}$**  production
- The most significant excess **at 1.1 TeV**
  - **Local significance  $2.6\sigma$  ( $2.7\sigma$ )** for the spin-0 (spin-2) model
  - **Global significance  $1.0\sigma$  ( $1.2\sigma$ )** for the spin-0 (spin-2) model
- **Statistically dominated**, the **impact of systematic uncertainties up to  $\sim 16\%$** , mainly from the background modelling



# VBF $HH \rightarrow bbbb$

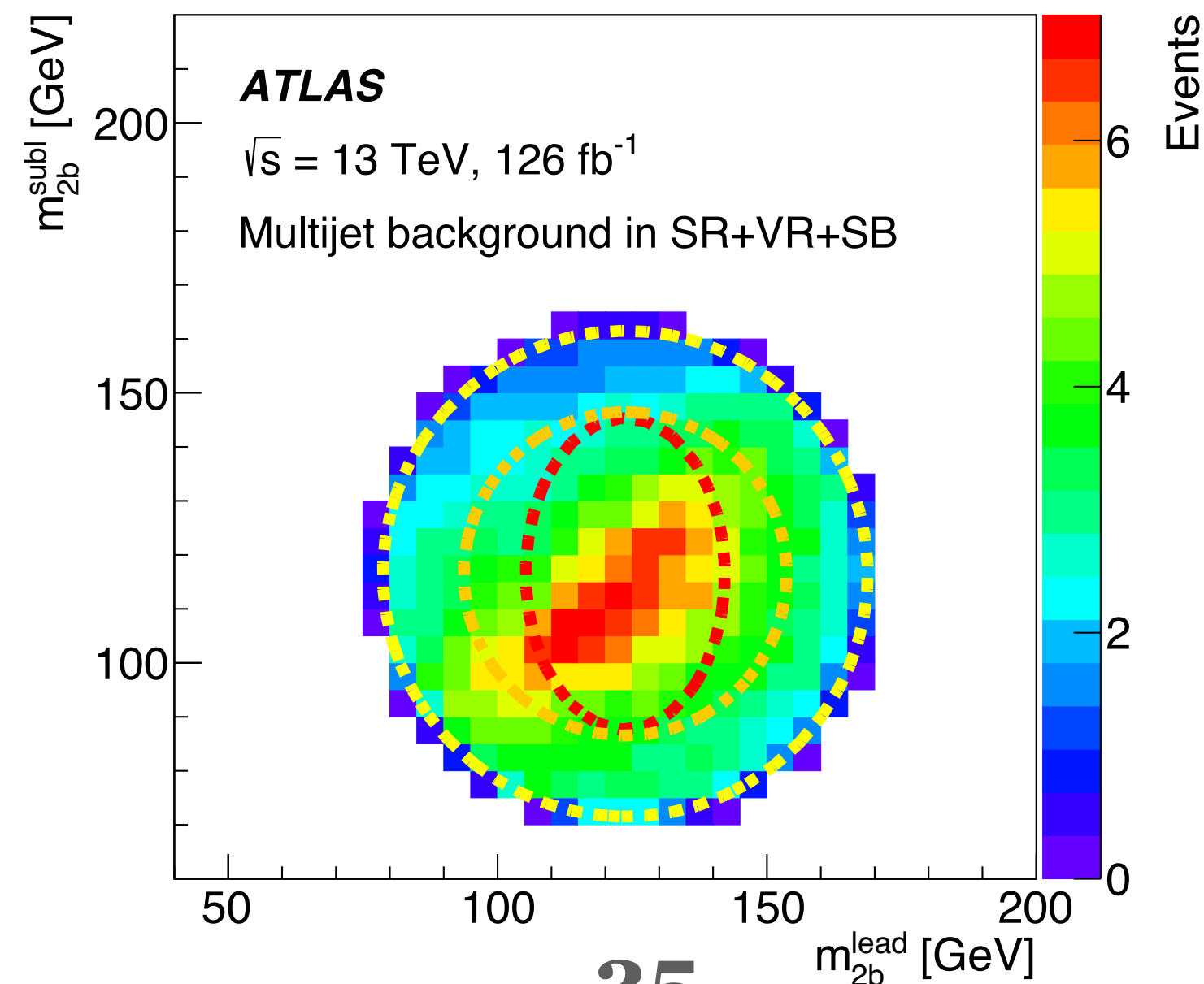
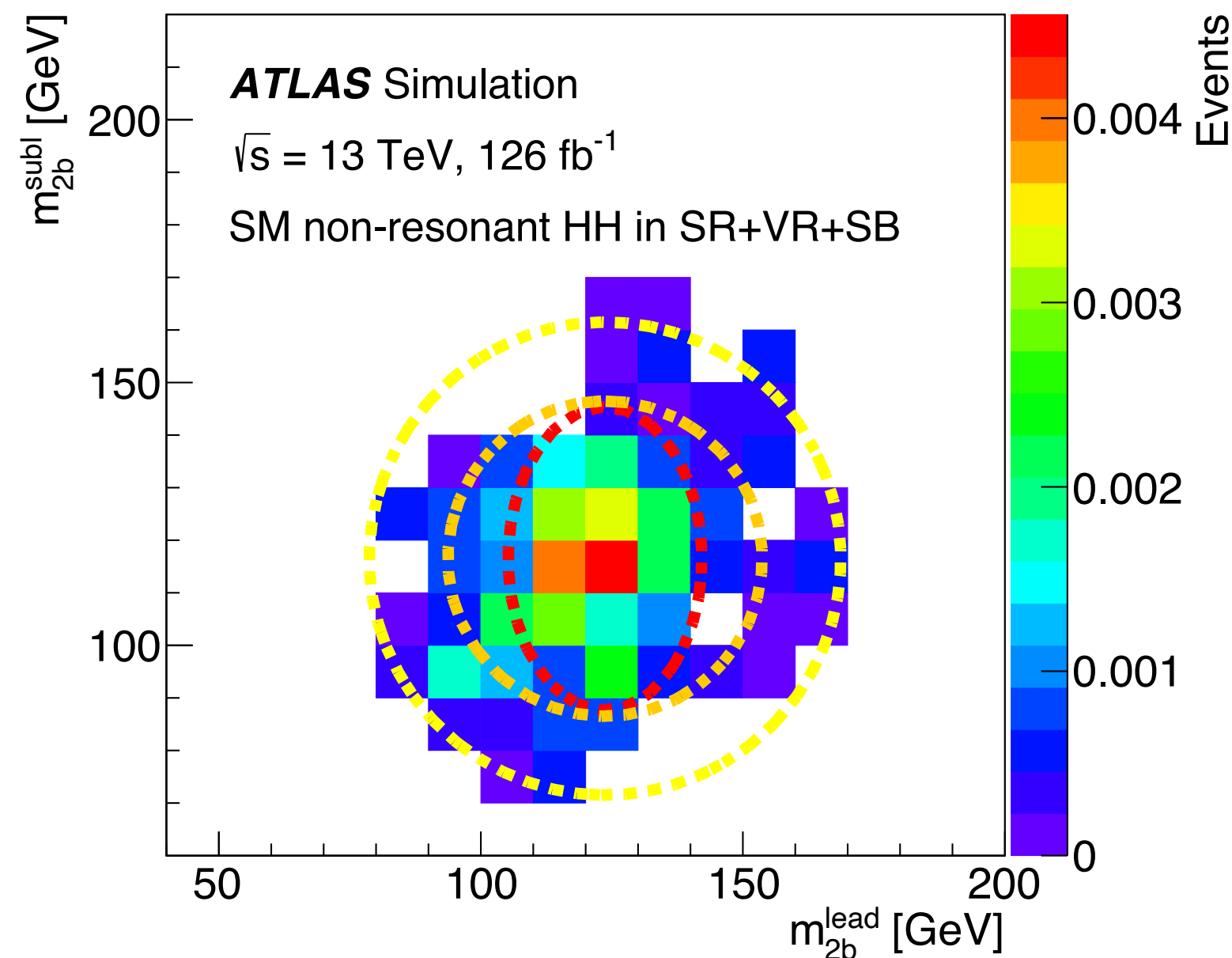
**Publication:** JHEP 07 (2020) 108

**Physics Briefing:** Double the Higgs for double the difficulty



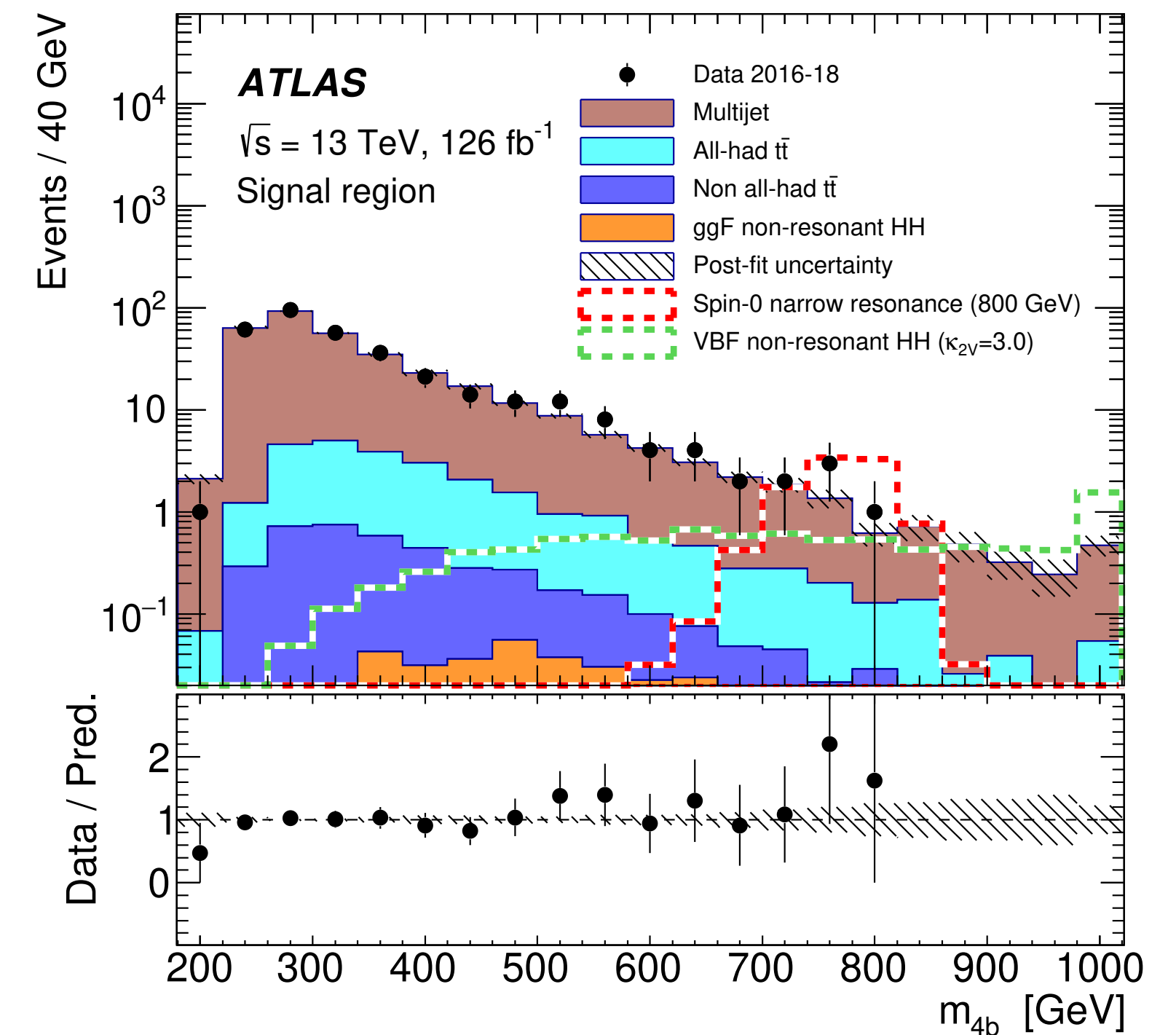
# VBF HH $\rightarrow$ bbbb: Analysis Overview

- Search for **resonant** and **non-resonant VBF HH production** using **126 fb<sup>-1</sup>** of pp data
  - Use a combination of **b-jet triggers**
  - **Distinct VBF signature**: two high p<sub>T</sub> jets with a large rapidity gap and invariant mass
- Based on early Run-2 ggF resolved analysis strategy, with **optimizations for the VBF HH process**
- **95% multijet background** (data-driven), **5% ttbar** (simulation)
- ggF HH process treated as a **background**, normalised to the SM expectation



25

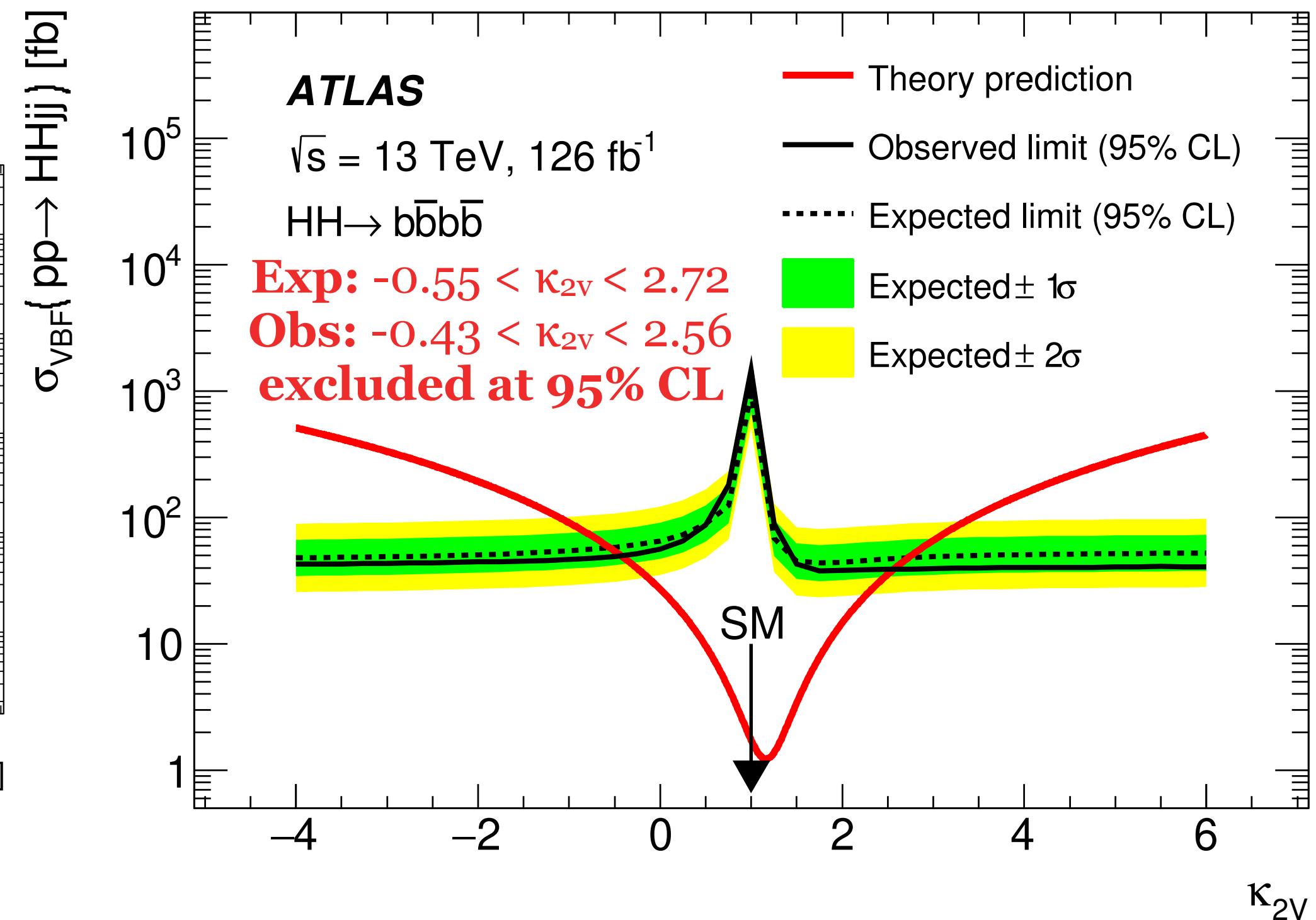
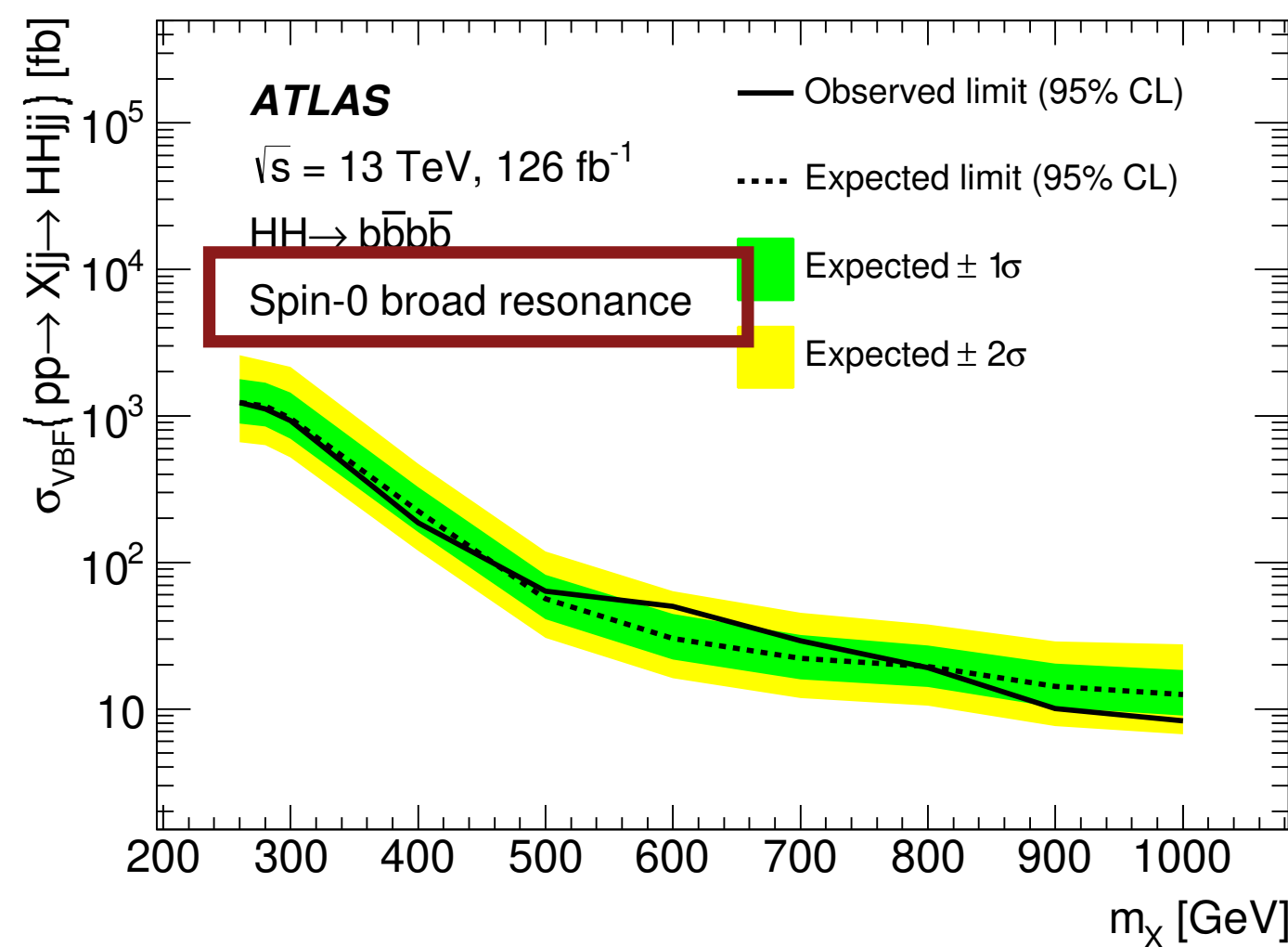
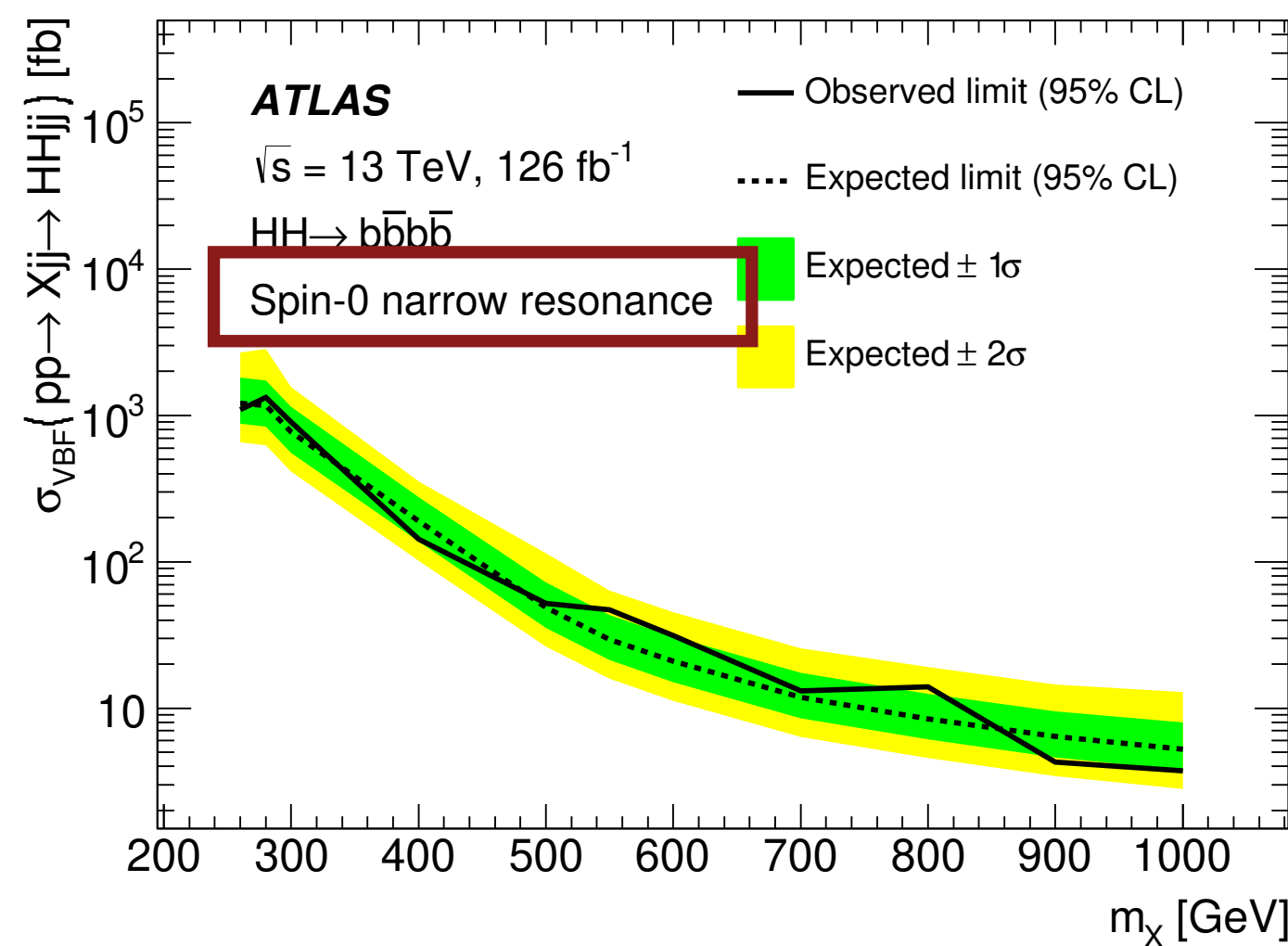
**$m_{4b}$  used as a final discriminant**



# VBF $HH \rightarrow b\bar{b}b\bar{b}$ : Results

- No significant excess observed
- Limits set on:
  - Spin-0 narrow and broad width resonances
  - SM  $\sigma_{HH}$  and  $\kappa_{2V}$
- Statistically limited, followed by systematics on the multijet background

	Observed	$-2\sigma$	$-1\sigma$	Expected	$+1\sigma$	$+2\sigma$
$\sigma_{\text{VBF}}$ [fb]	1460	510	690	950	1330	1780
$\sigma_{\text{VBF}}/\sigma_{\text{VBF}}^{\text{SM}}$	840	290	400	550	770	1030



**$HH \rightarrow bb\bar{v}v$**

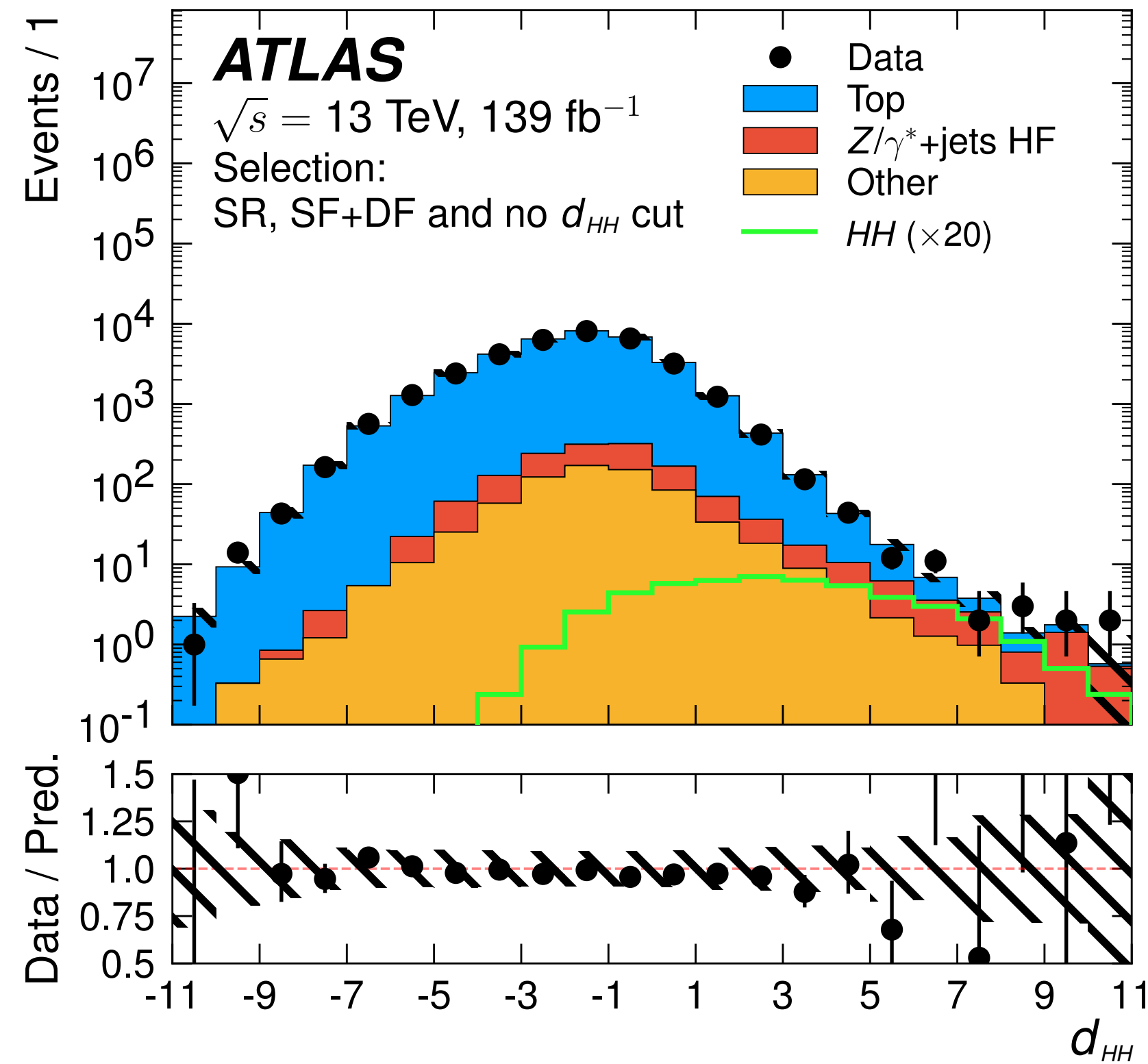
**Publication:** Phys. Lett. B 801 (2020) 135145

# HH→bbllv: Analysis Overview

- Search for **non-resonant (ggF) HH production** using **139 fb<sup>-1</sup>** of pp data
  - Contributions from **HH→bbWW\*** (90% of the total signal yield), **HH→bbττ** (9%), **HH→bbZZ\*** (1%)
  - At least **2 b-jets** and exactly **2 opposite-sign leptons** (e or μ)
- **Main backgrounds** from Top production and Z/γ\* + HF
- **A multi-class deep neural network (DNN)** used to discriminate signal and the SM background
  - Trained only with the HH→bbWW\* signal, due to its larger BR
  - **Final discriminant** defined using the DNN outputs
    - **$d_{HH} = \ln[p_{HH}/(p_{Top} + p_{Z-H} + p_{Z-\tau\tau})]$** , ( $p_i=[0-1]$ , where 1 indicates the event likely belongs to class i)
- Perform **a counting experiment with a likelihood fit** simultaneously across:
  - Top and Z+HF CRs
  - The same flavour (SF) and different flavour (DF) SRs

# HH→bbllv: Results

- Dominant uncertainties from Top and Z+HF background modelling

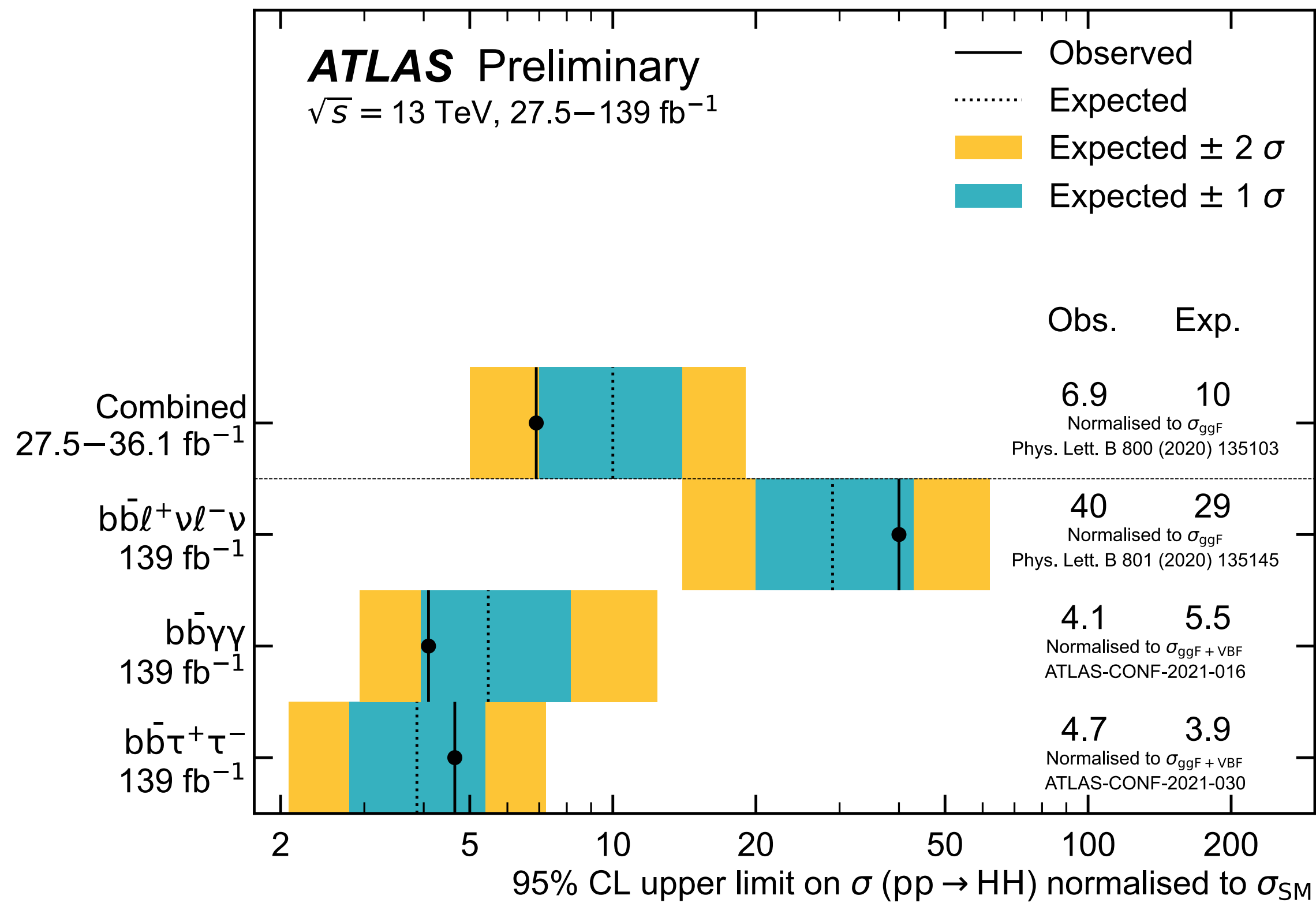


	$-2\sigma$	$-1\sigma$	<b>Expected</b>	$+1\sigma$	$+2\sigma$	<b>Observed</b>
$\sigma (gg \rightarrow HH) [\text{pb}]$	0.5	0.6	0.9	1.3	1.9	1.2
$\sigma (gg \rightarrow HH) / \sigma^{\text{SM}} (gg \rightarrow HH)$	14	20	29	43	62	40

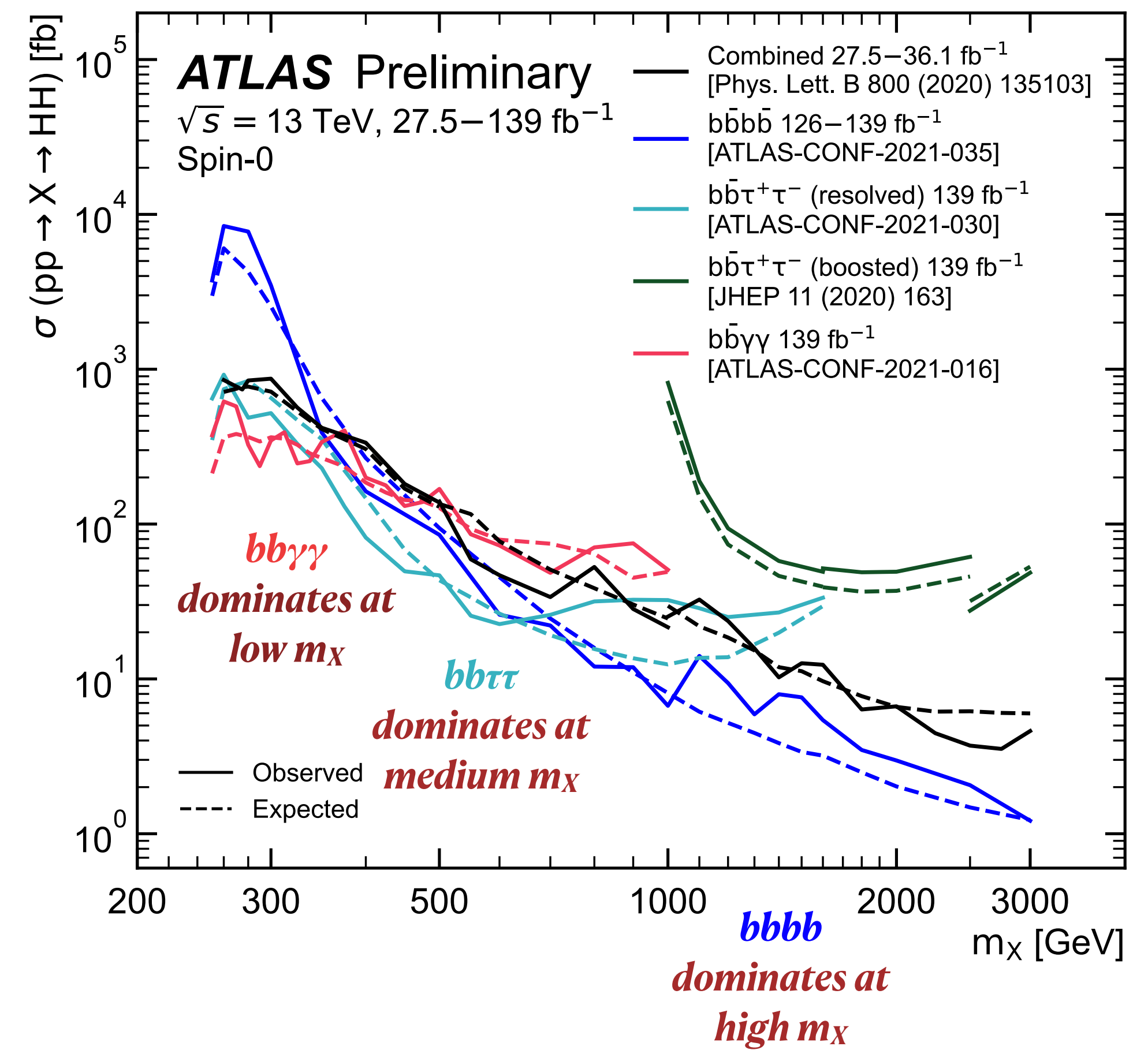
# Summary

# Summary of Results

## Non-Resonant - SM HH



## Resonant - Spin-0



**Even better results from the individual channels compared to the 36 fb<sup>-1</sup> HH combination!**

# Projections for HL-LHC

- **Prospects study for the non-resonant HH production at the HL-LHC**
  - **3 ab<sup>-1</sup> of data assumed** → ~21 x full Run-2 dataset
  - **Based on analysis performed with 36 fb<sup>-1</sup> of data**
    - Except bbyγ prospects are from a dedicated analysis on 14 TeV simulation

Channel	Statistical-only	Statistical + Systematic
$HH \rightarrow b\bar{b}b\bar{b}$	1.2	0.5
$HH \rightarrow b\bar{b}\tau^+\tau^-$	2.3	2.0
$HH \rightarrow b\bar{b}\gamma\gamma$	2.1	2.0
Combined	3.3 $\sigma$	2.9 $\sigma$



# Conclusion

- Searches for **Higgs pair production** performed in **multiple final states** with the **ATLAS detector**
- **Results include:**
  - Limits on  $\sigma_{HH}$
  - Constraints on  $\kappa_\lambda, \kappa_{2V}$
  - Limits on  $\sigma_{HH}$  vs  $m_X$ , for a spin-0 heavy resonance
  - Limits on  $\sigma_{HH}$  vs  $m(G_{KK})$ , for a spin-2 graviton
- Large **improvements in sensitivity** compared to the previous iterations

**BACK UP**

# HH $\rightarrow$ bby $\gamma$ : BDT Input Variables (Non-Res)

Variable	Definition
Photon-related kinematic variables	
$p_T/m_{\gamma\gamma}$	Transverse momentum of the two photons scaled by their invariant mass $m_{\gamma\gamma}$
$\eta$ and $\phi$	Pseudo-rapidity and azimuthal angle of the leading and sub-leading photon
Jet-related kinematic variables	
$b$ -tag status	Highest fixed $b$ -tag working point that the jet passes
$p_T, \eta$ and $\phi$	Transverse momentum, pseudo-rapidity and azimuthal angle of the two jets with the highest $b$ -tagging score
$p_T^{b\bar{b}}, \eta_{b\bar{b}}$ and $\phi_{b\bar{b}}$	Transverse momentum, pseudo-rapidity and azimuthal angle of $b$ -tagged jets system
$m_{b\bar{b}}$	Invariant mass built with the two jets with the highest $b$ -tagging score
$H_T$	Scalar sum of the $p_T$ of the jets in the event
Single topness	For the definition, see Eq. (1)
Missing transverse momentum-related variables	
$E_T^{\text{miss}}$ and $\phi^{\text{miss}}$	Missing transverse momentum and its azimuthal angle

Category	Selection criteria
High mass BDT tight	$m_{b\bar{b}\gamma\gamma}^* \geq 350$ GeV, BDT score $\in [0.967, 1]$
High mass BDT loose	$m_{b\bar{b}\gamma\gamma}^* \geq 350$ GeV, BDT score $\in [0.857, 0.967]$
Low mass BDT tight	$m_{b\bar{b}\gamma\gamma}^* < 350$ GeV, BDT score $\in [0.966, 1]$
Low mass BDT loose	$m_{b\bar{b}\gamma\gamma}^* < 350$ GeV, BDT score $\in [0.881, 0.966]$

**Highest discriminating power against the  $\gamma\gamma$ +jets continuum background**

# HH $\rightarrow$ bby $\gamma$ : BDT Input Variables (Resonant)

Variable	Definition
<b>Photon-related kinematic variables</b>	
$p_T^{\gamma\gamma}, y^{\gamma\gamma}$	Transverse momentum and rapidity of the di-photon system
$\Delta\phi_{\gamma\gamma}$ and $\Delta R_{\gamma\gamma}$	Azimuthal angular distance and $\Delta R$ between the two photons
<b>Jet-related kinematic variables</b>	
$m_{b\bar{b}}, p_T^{b\bar{b}}$ and $y_{b\bar{b}}$	Invariant mass, transverse momentum and rapidity of the $b$ -tagged jets system
$\Delta\phi_{b\bar{b}}$ and $\Delta R_{b\bar{b}}$	Azimuthal angular distance and $\Delta R$ between the two $b$ -tagged jets
$N_{\text{jets}}$ and $N_{b\text{-jets}}$	Number of jets and number of $b$ -tagged jets
$H_T$	Scalar sum of the $p_T$ of the jets in the event
<b>Photons and jets-related kinematic variables</b>	
$m_{b\bar{b}\gamma\gamma}$	Invariant mass built with the di-photon and $b$ -tagged jets system
$\Delta y_{\gamma\gamma, b\bar{b}}, \Delta\phi_{\gamma\gamma, b\bar{b}}$ and $\Delta R_{\gamma\gamma, b\bar{b}}$	Distance in rapidity, azimuthal angle and $\Delta R$ between the di-photon and the $b$ -tagged jets system

$$\text{BDT}_{\text{tot}} = \frac{1}{\sqrt{C_1^2 + C_2^2}} \sqrt{C_1^2 \left( \frac{\text{BDT}_{\gamma\gamma} + 1}{2} \right)^2 + C_2^2 \left( \frac{\text{BDT}_{\text{Single}H} + 1}{2} \right)^2}$$

# HH $\rightarrow$ bb $\tau\tau$ : Event Selection

<b><math>\tau_{\text{had}}\tau_{\text{had}}</math> category</b>		<b><math>\tau_{\text{lep}}\tau_{\text{had}}</math> categories</b>	
STT	DTT	SLT	LTT
<b><math>e/\mu</math> selection</b>			
No loose $e/\mu$ with $p_T > 7$ GeV		Exactly one tight $e$ or medium $\mu$	
		$p_T^e > 25, 27$ GeV	$18 \text{ GeV} < p_T^e < \text{SLT cut}$
		$p_T^\mu > 21, 27$ GeV	$15 \text{ GeV} < p_T^\mu < \text{SLT cut}$
		$ \eta^e  < 2.47$ , not $1.37 <  \eta^e  < 1.52$	
		$ \eta^\mu  < 2.7$	
<b><math>\tau_{\text{had-vis}}</math> selection</b>			
Two loose $\tau_{\text{had-vis}}$ $ \eta  < 2.5$		One loose $\tau_{\text{had-vis}}$ $ \eta  < 2.3$	
$p_T > 100, 140, 180$ (25) GeV	$p_T > 40$ (30) GeV	$p_T > 20$ GeV	$p_T > 30$ GeV
<b>Jet selection</b>			
$\geq 2$ jets with $ \eta  < 2.5$			
$p_T > 45$ (20) GeV	Trigger dependent	$p_T > 45$ (20) GeV	Trigger dependent
<b>Event-level selection</b>			
Trigger requirements passed			
Collision vertex reconstructed			
$m_{\tau\tau}^{\text{MMC}} > 60$ GeV			
Opposite-sign electric charges of $e/\mu/\tau_{\text{had-vis}}$ and $\tau_{\text{had-vis}}$			
Exactly two $b$ -tagged jets			
$m_{bb} < 150$ GeV			

# HH $\rightarrow$ bb $\tau\tau$ : Input Parameters in MVA

Variable	$\tau_{\text{had}}\tau_{\text{had}}$	$\tau_{\text{lep}}\tau_{\text{had}}$	SLT	$\tau_{\text{lep}}\tau_{\text{had}}$	LTT
$m_{HH}$	✓		✓		✓
$m_{\tau\tau}^{\text{MMC}}$	✓		✓		✓
$m_{bb}$	✓		✓		✓
$\Delta R(\tau, \tau)$	✓		✓		✓
$\Delta R(b, b)$	✓		✓		
$\Delta p_{\text{T}}(\ell, \tau)$			✓		✓
Sub-leading $b$ -tagged jet $p_{\text{T}}$			✓		
$m_{\text{T}}^{\text{W}}$			✓		
$E_{\text{T}}^{\text{miss}}$			✓		
$\mathbf{p}_{\text{T}}^{\text{miss}}$ $\phi$ centrality			✓		
$\Delta\phi(\ell\tau, bb)$			✓		
$\Delta\phi(\ell, \mathbf{p}_{\text{T}}^{\text{miss}})$					✓
$\Delta\phi(\ell\tau, \mathbf{p}_{\text{T}}^{\text{miss}})$					✓
$S_{\text{T}}$					✓