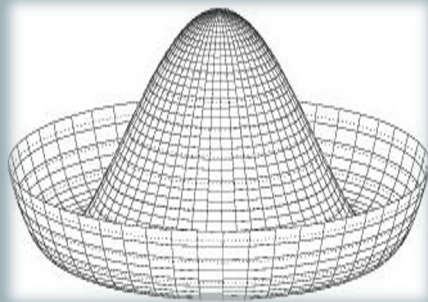


DOUBLE HIGGS AT FUTURE COLLIDERS



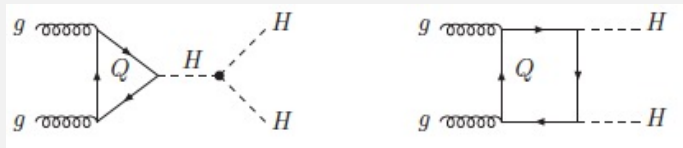
S. Dawson, BNL

Sept 30, 2021

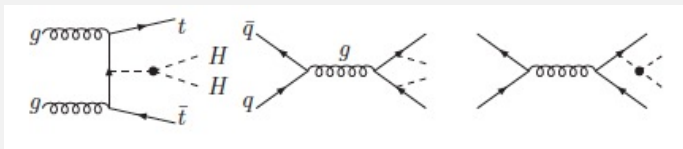
Future Colliders in a chart

Collider	Type	\sqrt{s}	\mathcal{P} [%] [e^-/e^+]	N(Det.)	$\mathcal{L}_{\text{inst}}$ [10^{34}] $\text{cm}^{-2}\text{s}^{-1}$	\mathcal{L} [ab^{-1}]	Time [years]	Refs.	Abbreviation
HL-LHC	pp	14 TeV	-	2	5	6.0	12	[10]	HL-LHC
HE-LHC	pp	27 TeV	-	2	16	15.0	20	[10]	HE-LHC
FCC-hh	pp	100 TeV	-	2	30	30.0	25	[1]	FCC-hh
FCC-ee	ee	M_Z	0/0	2	100/200	150	4	[1]	FCC-ee ₂₄₀ FCC-ee ₃₆₅ (1y SD before $2m_{\text{top}}$ run)
		$2M_W$	0/0	2	25	10	1-2		
		240 GeV	0/0	2	7	5	3		
		$2m_{\text{top}}$	0/0	2	0.8/1.4	1.5	5		
ILC	ee	250 GeV	$\pm 80/\pm 30$	1	1.35/2.7	2.0	11.5	[3, 11]	ILC ₂₅₀ ILC ₃₅₀ ILC ₅₀₀ (1y SD after 250 GeV run)
		350 GeV	$\pm 80/\pm 30$	1	1.6	0.2	1		
		500 GeV	$\pm 80/\pm 30$	1	1.8/3.6	4.0	8.5		
CEPC	ee	M_Z	0/0	2	17/32	16	2	[2]	CEPC
		$2M_W$	0/0	2	10	2.6	1		
		240 GeV	0/0	2	3	5.6	7		
CLIC	ee	380 GeV	$\pm 80/0$	1	1.5	1.0	8	[12]	CLIC ₃₈₀ CLIC ₁₅₀₀ CLIC ₃₀₀₀ (2y SDs between energy stages)
		1.5 TeV	$\pm 80/0$	1	3.7	2.5	7		
		3.0 TeV	$\pm 80/0$	1	6.0	5.0	8		
LHeC	ep	1.3 TeV	-	1	0.8	1.0	15	[9]	LHeC
HE-LHeC	ep	1.8 TeV	-	1	1.5	2.0	20	[1]	HE-LHeC
FCC-eh	ep	3.5 TeV	-	1	1.5	2.0	25	[1]	FCC-eh

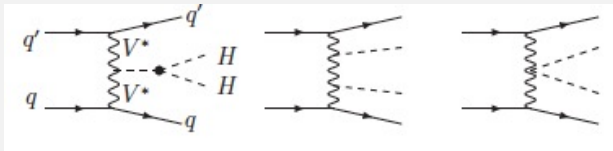
PRODUCTION OF HH



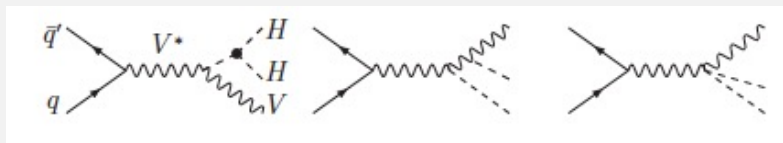
Sensitive to heavy colored particles (eg stops or top partners) and new resonances



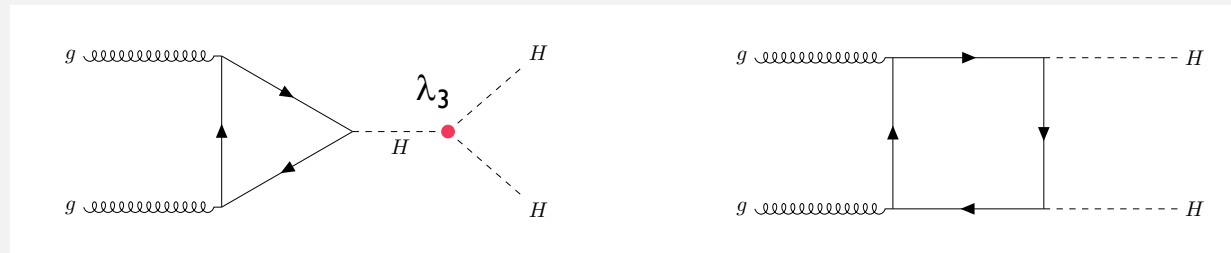
Sensitive to anomalous top-Higgs couplings



Sensitive to anomalous VVHH couplings



DOUBLE HIGGS IS GOAL OF HL-LHC AND FUTURE COLLIDERS

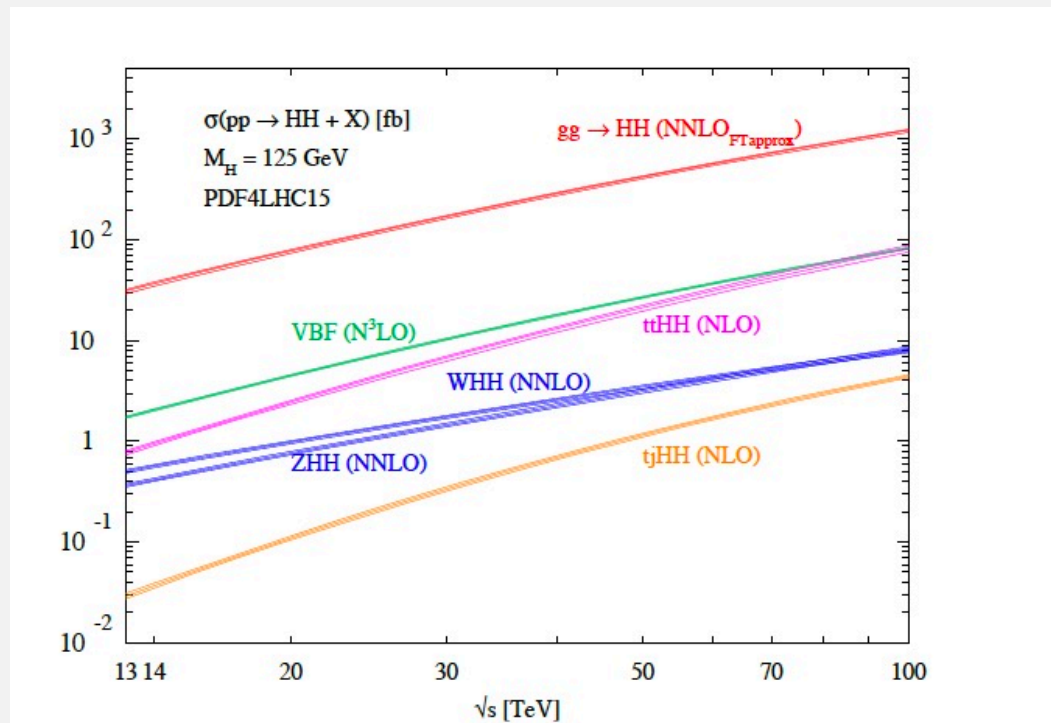


- $\lambda_3 = M_H^2/(2v)$ is SM HHH coupling
- In SM $\lambda_3=1$; any other value is a sign of new physics
- Contributions tend to cancel at threshold
- Theory includes NLO with all masses; NNLO with approximations

SMALL RATES AT pp COLLIDERS

$$\frac{\sigma_{100}^{ggF}}{\sigma_{14}^{ggF}} \sim 33$$

$$\frac{\sigma_{100}^{VBF}}{\sigma_{14}^{VBF}} \sim 41$$

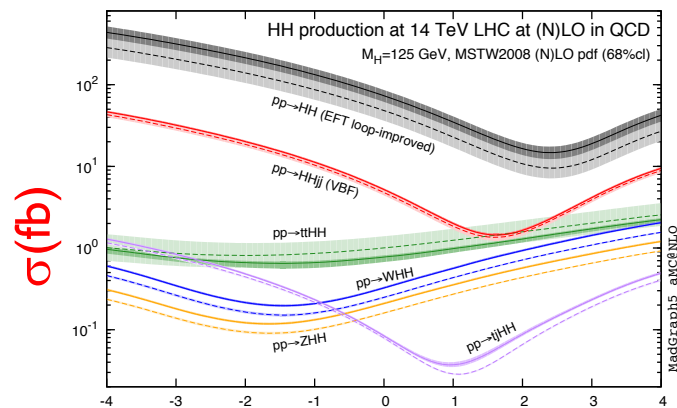


Most studies at HL-LHC consider gluon fusion or VBF only

ttHH+VBF \sim 15% of rate at 100 TeV

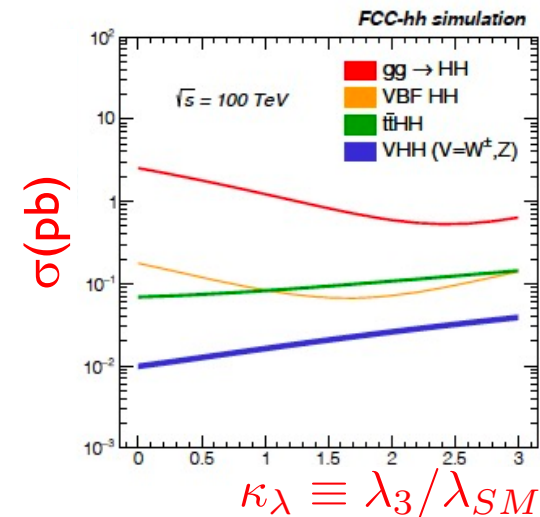
[1910.00012.pdf](#)

DEPENDENCE ON λ_3



$$\kappa_\lambda \equiv \lambda_3/\lambda_{SM}$$

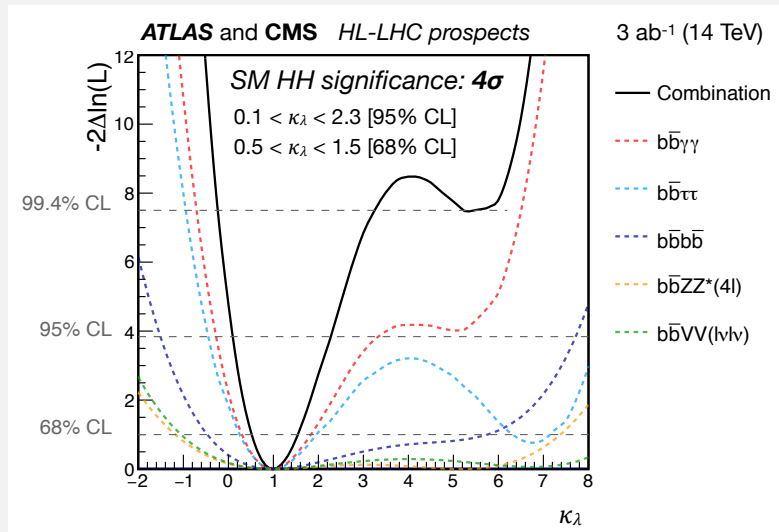
[1903.08137](#)



Everything SM **except** λ_3

S. Dawson

HIGGS TRI-LINEAR COUPLING IN THE FUTURE



Difficult measurement

[1902.00134](#) , [1905.03764](#)

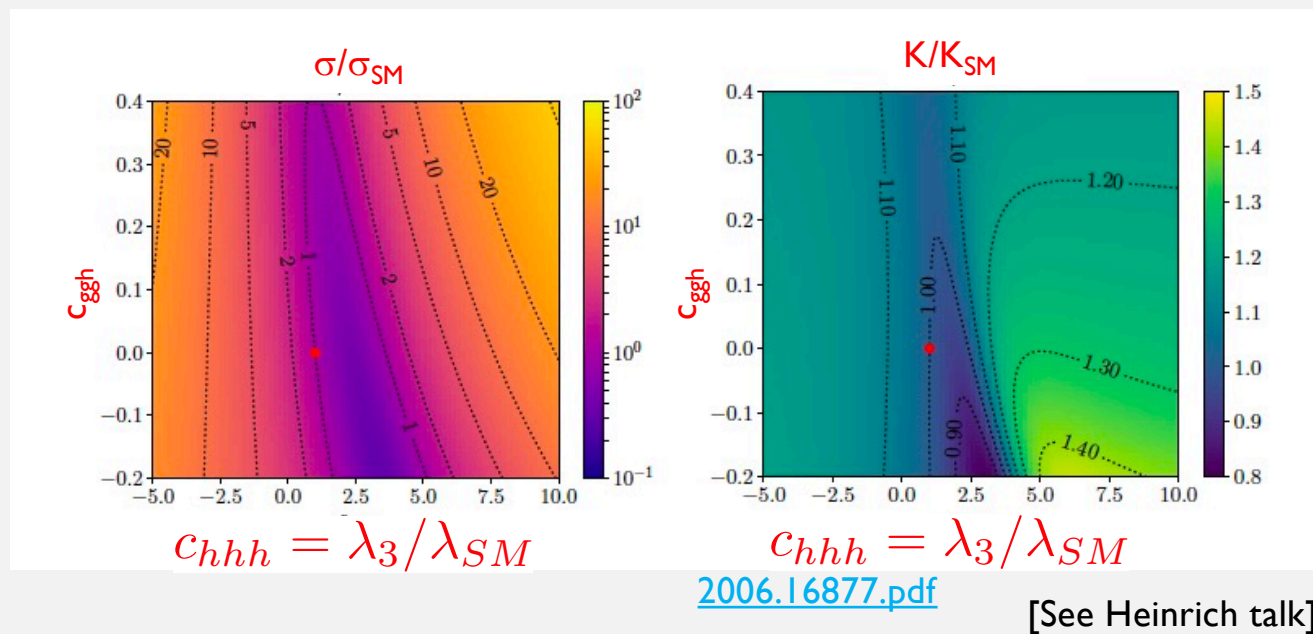
QCD EFFECTS

- NLO $gg \rightarrow HH$ with anomalous couplings implemented in POWHEG

NNLO' sensitivity
to anomalous
couplings

$$L \sim \frac{C_g}{\Lambda^2} |H^\dagger H| G_{\mu\nu}^A G^{\mu\nu,A}$$

$$c_{ggh} = \frac{8\pi}{\alpha_s} \frac{v^2}{\Lambda^2} C_g$$

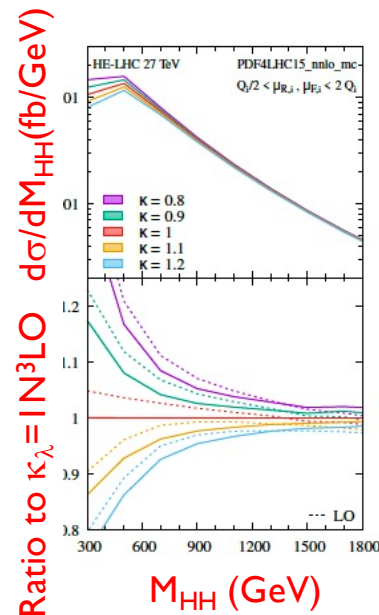
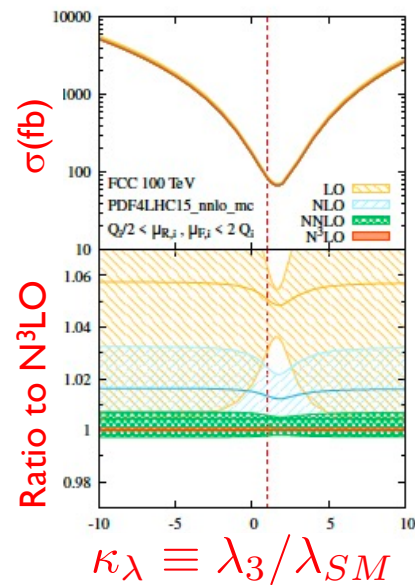


14 TeV

Red dot is SM

QCD EFFECTS

K factors @ 100 TeV



VBF HH production

- Total cross section K factor relatively flat in VBF HH
- NLO gets most of the effect
- Distributions sensitive to λ_3/λ_{SM}

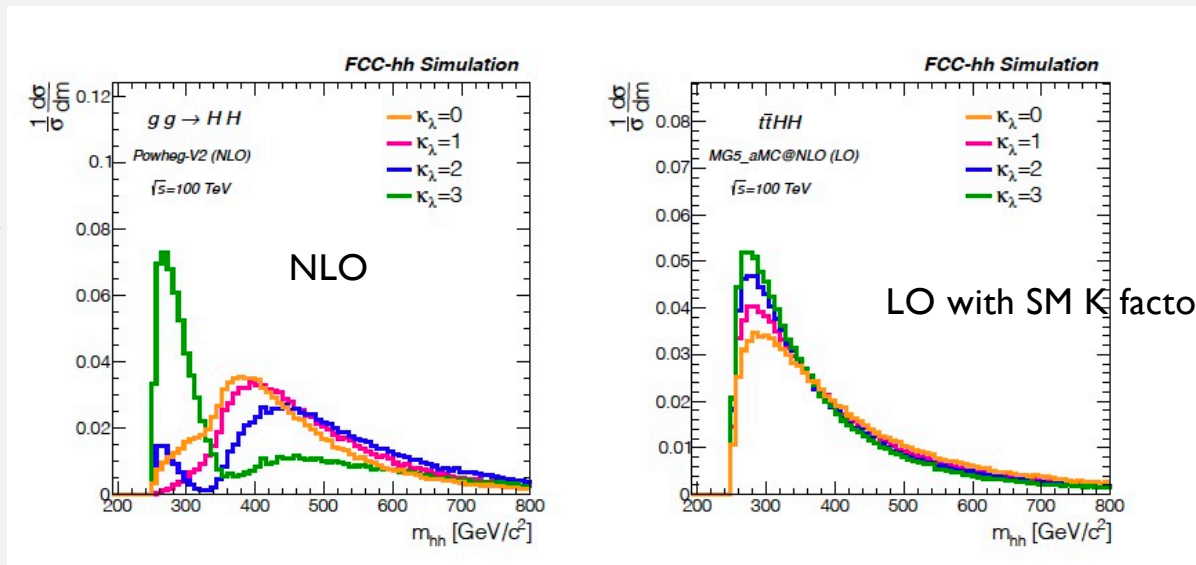
[1811.07906.pdf](#)

S. Dawson

DISCOVERY OF HH AT FCC-hh

- Tools exist to include higher order QCD effects

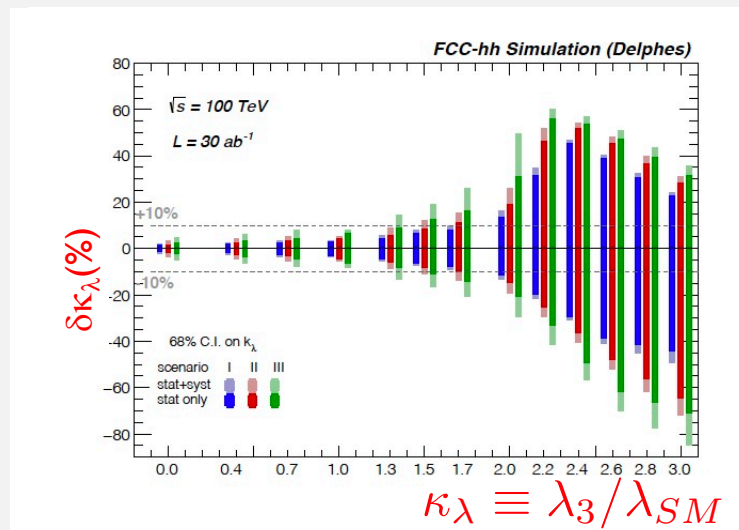
100 TeV



Include all
production
channels in study

FCC-hh PRECISION

- Combining $bb\gamma\gamma$, $bb\tau\tau$ and $bbbb$, precision on SM $\delta\kappa_\lambda \sim 3.4\text{-}7.8\%$
- Theory work needed: allow other couplings to vary

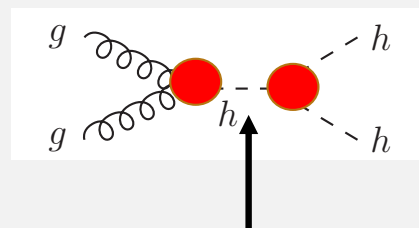
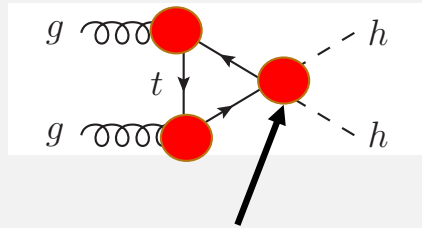
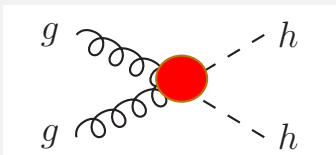
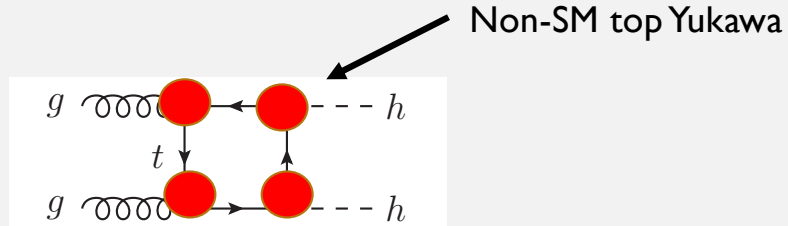
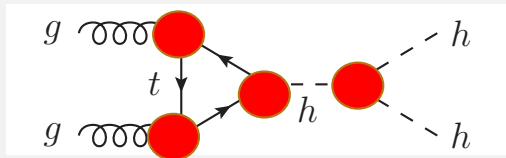


Precision depends on κ_λ
and assumptions about
systematics

[2004.03505.pdf](#)

IT'S NOT JUST HHH.....

- In any realistic model, interactions other than HHH are also changed
- Limits are correlated



$ttHH$ coupling in composite higgs models

Large resonant enhancement with new scalars

Different scaling with energy from different diagrams

POSSIBLE INTERACTIONS

- Quantify effects in terms of SMEFT
- Expect effects growing with energy to be significant at FCC-hh
- Effective field theory expansion in higher dimension operators

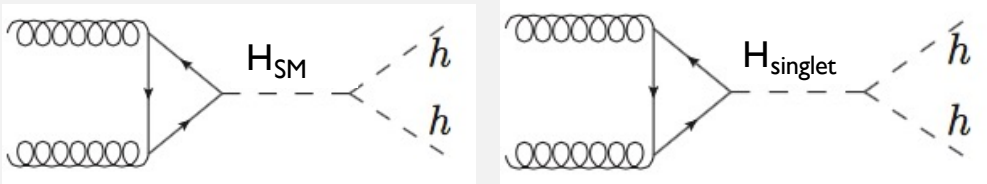
$$\begin{aligned}
 L \sim & \frac{C_H}{\Lambda^2} (H^\dagger \partial_\mu H)^2 + \frac{C_6}{\Lambda^2} |H|^6 + \frac{C_g}{\Lambda^2} |H|^2 G_{\mu\nu} G^{\mu\nu} \\
 & + \left(\frac{y_t C_Y}{\Lambda^2} \bar{Q}_L \tilde{H} t_R |H|^2 + \frac{C_{tG}}{\Lambda^2} \bar{Q}_L \sigma_{\mu\nu} T^A \tilde{H} t_R G_{\mu\nu}^A + h.c. \right)
 \end{aligned}$$

+ many more....

$$1 - \lambda_3/\lambda_{SM} \sim \frac{v^2}{\Lambda^2} \left(C_H + \frac{C_6}{\lambda_{SM}} \right)$$

THEORY MOTIVATION FOR ANOMALOUS COUPLINGS

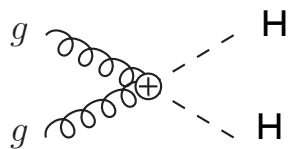
- Singlet model: Large resonant enhancements; interesting interference pattern
- Singlet model: new decay channels with $H_{SM} H_{\text{singlet}}$ in final state



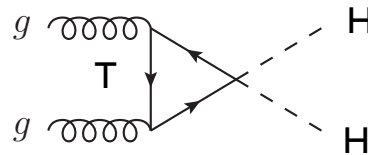
As the mass of $H_{\text{singlet}} \rightarrow \infty$, the model generates new effective interactions, C_6 and C_H

THEORY MOTIVATION FOR ANOMALOUS COUPLINGS

- Composite Higgs models have heavy top-like particle T which generates new interactions: C_g, C_Y, \dots



$$\sim C_g \frac{s}{\Lambda^2}$$

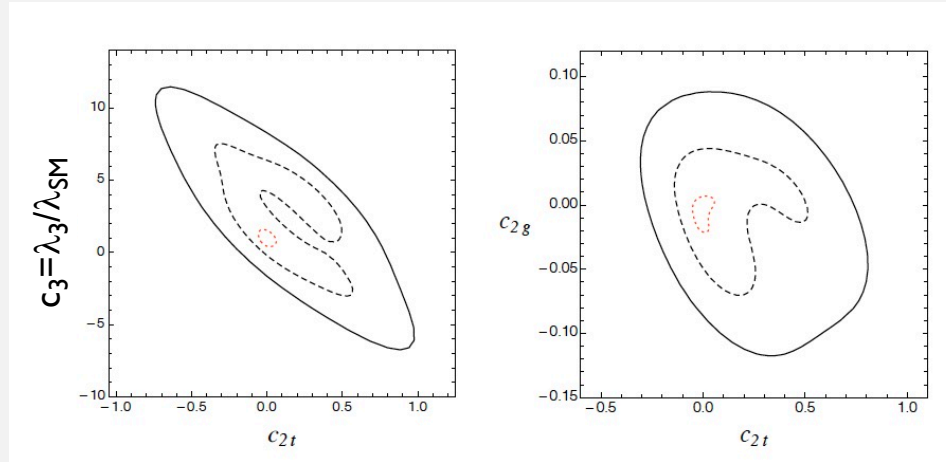


$$\sim C_Y \log^2 \left(\frac{s}{M_T^2} \right)$$

NOT JUST λ_3

$HH \rightarrow bb\gamma\gamma$

68% exclusion contours

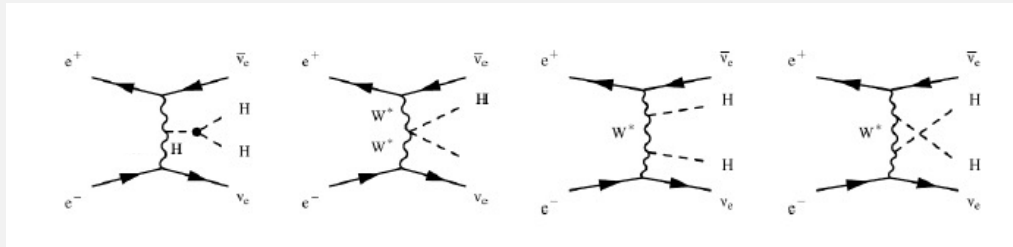


- FCC-hh 3 ab⁻¹
- HL-LHC, 3 ab⁻¹
- LHC, 300 fb⁻¹

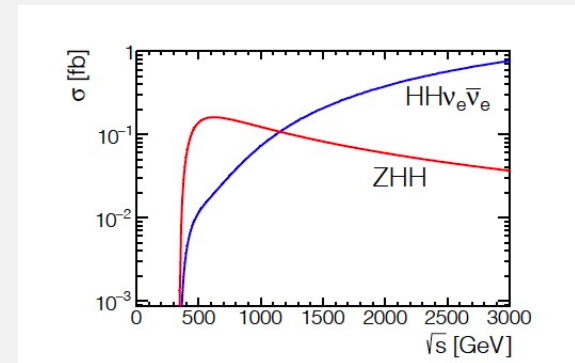
$$c_{2t} = -\frac{v^2}{\Lambda^2} \left(C_H + \frac{3}{2} C_Y \right) \quad (\text{ttHH vertex})$$

DOUBLE HIGGS PRODUCTION AT e^+e^- COLLIDERS

- Very small cross sections
- Not possible at 240 GeV e^+e^- colliders



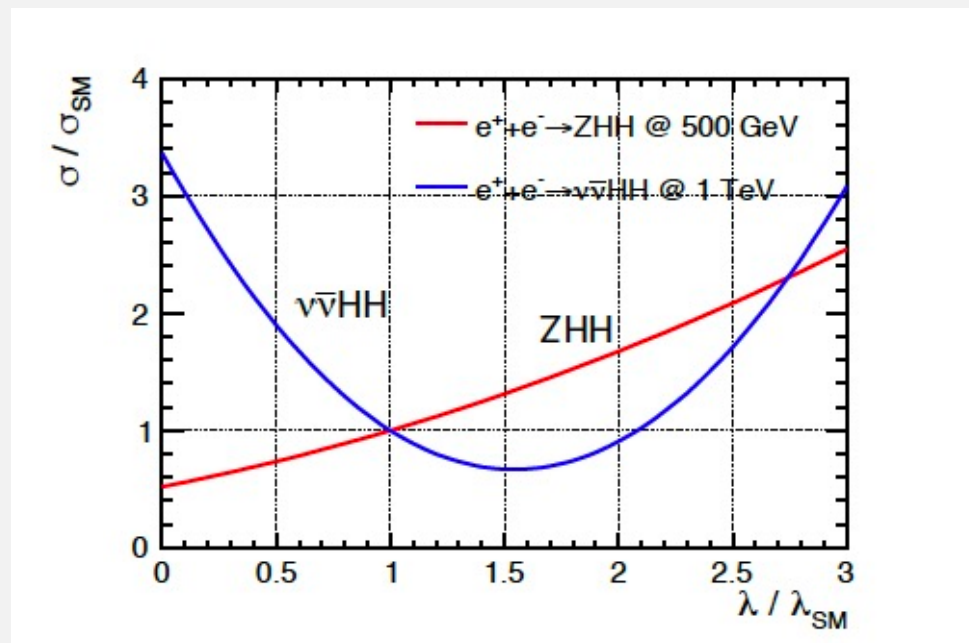
- Depends on HHH coupling and on $WWH, WWHH$ couplings



LH polarization increases HH $v\nu$ rate

HHH COUPLING IN e^+e^-

- Either ZHH or HH $\nu\nu$ is greater than SM rate for anomalous HHH couplings



Only allow λ_3 to vary

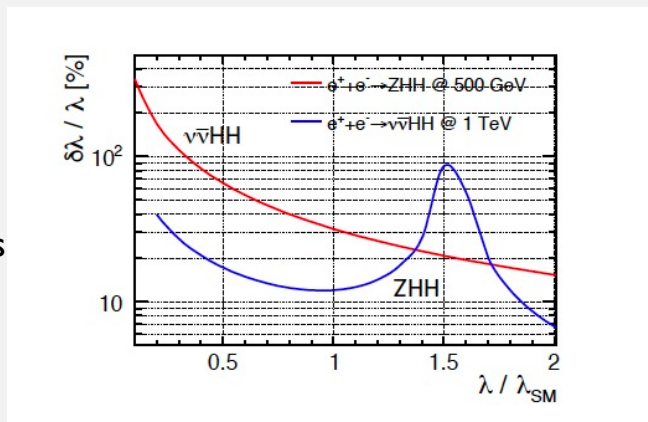
[1908.11299.pdf](#)

S. Dawson

* Polarized beams as in ILC

~10% MEASUREMENTS

- Many models have enhanced HHH couplings
- Shape of distributions change with λ_3



ILC with 4 ab^{-1} with 80% e^- and 30% e^+ polarizations in $bbbb$ and $bbWW$ channels

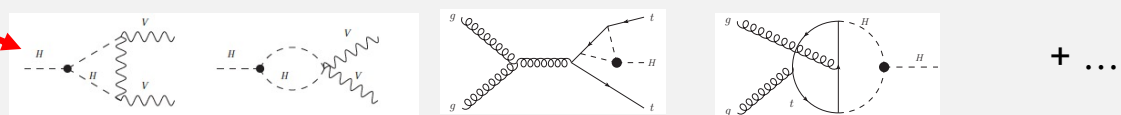
- CLIC at 1.4 TeV expects 5.9σ evidence for ZHH observation with 68%cl measurement

$$0.93 < \lambda / \lambda_{SM} < 1.11$$

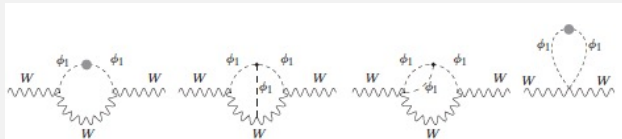
COMPLEMENTARITY WITH PRECISION MEASUREMENTS

- Indirect constraints from Higgs measurements

Contributes to $e^+e^- \rightarrow ZH$



- Indirect constraints from precision observables



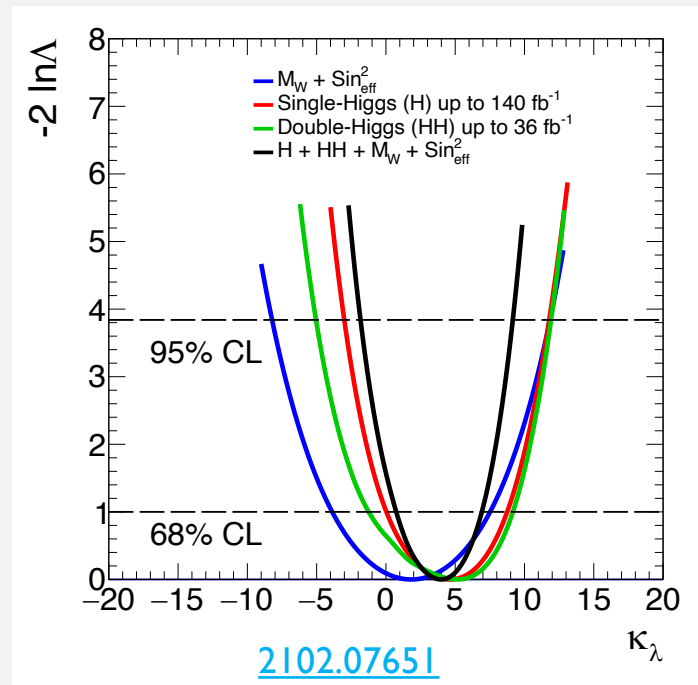
- Single H production sensitive to loops
- If you consider loops you get many more operators

Precision on κ_λ similar to that from direct measurements of HH

➔ Include in global fits

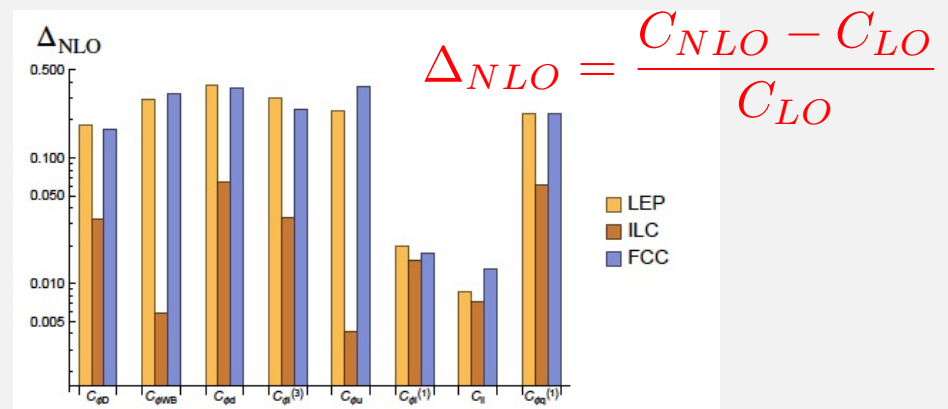
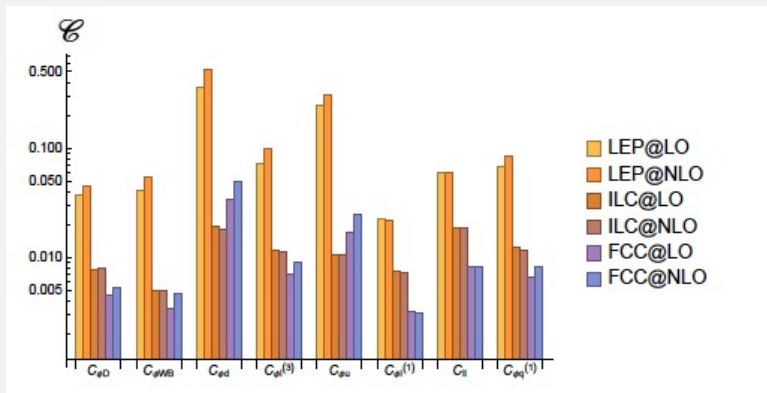
κ_λ IN SINGLE HIGGS PRODUCTION

- Include HH limits in global fits
- Theory is scenario where **only** new physics is scalar modification of HHH vertex
- EFT approach will have other contributions to HH production



FIT TO PRECISION EW OBSERVABLES

- At NLO EW, dependence on many coefficients that don't arise at tree level when computing Z pole observables
- These effects can be numerically significant



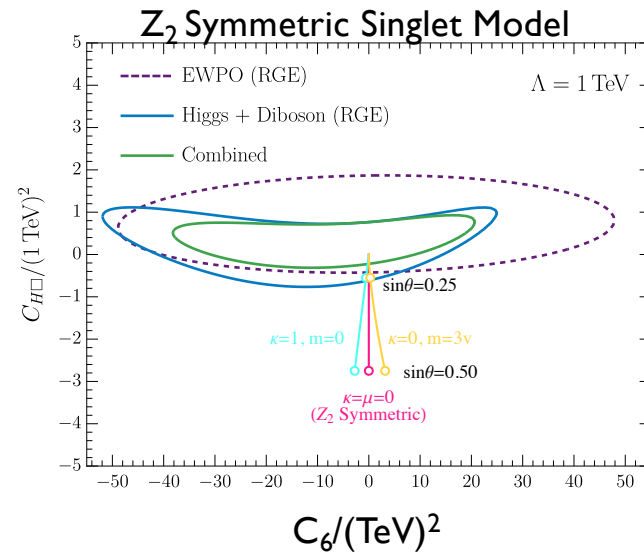
TARGET FOR PRECISION?

- Z_2 symmetric singlet model fit to single Higgs, VV data, electroweak precision observables
- Target measurement of λ_3/λ_{SM} to improve on current limit

$$-.27 < \frac{\lambda_3}{\lambda_{SM}} < .82$$

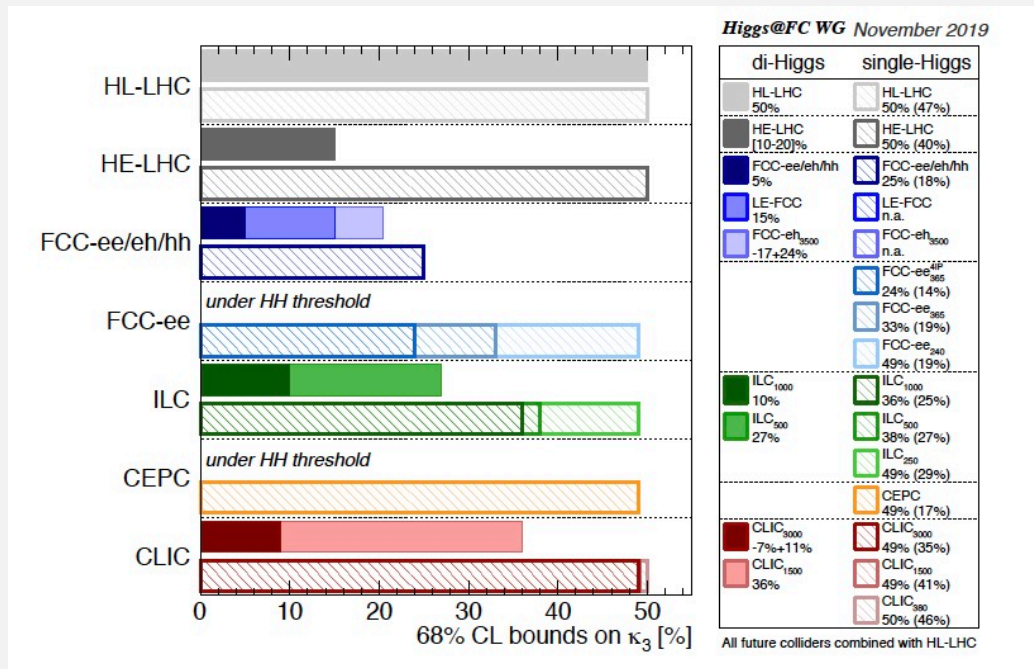
$C_{H\Box} = 0$ in Z_2 symmetric singlet model

[2007.01296.pdf](#)



$$\frac{\lambda_3}{\lambda_{SM}} = \frac{v^2}{\Lambda^2} C_6$$

CONCLUSION



Single Higgs numbers have multi-parameter SMEFT fit with 1 parameter fit in ().

2 years later, we have better handles on SMEFT theory predictions (both QCD and EW)

Combine di-Higgs and single Higgs sensitivities

CONCLUSIONS

- Theory has advanced so that we have the tools to do NLO QCD studies for FCC-hh for HH production with anomalous couplings
 - SMEFT EW loop calculations not complete (and our understanding of when they are needed is also inadequate)
- Need to include more than just the HHH coupling in projections for HH sensitivities
 - This effort is taking hold
 - Models motivate choice of anomalous couplings
- Global fits (both e^+e^- and pp) sensitive to anomalous couplings in HH production