

The Giessen Model for νA reactions

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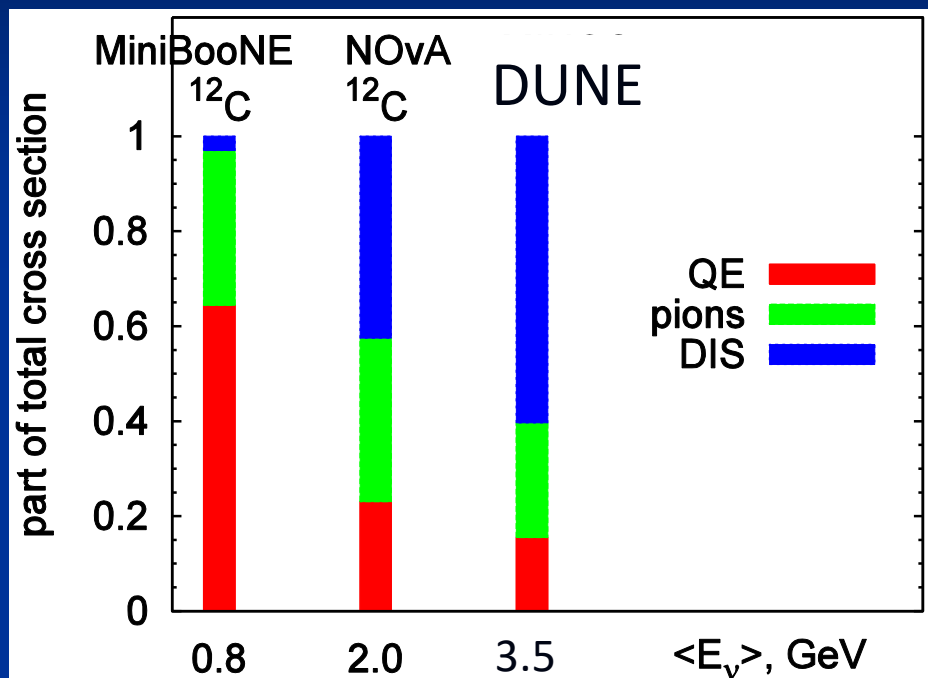


Intro

- Neutrino oscillation parameters require a reconstruction of the incoming neutrino energy
- Energy reconstruction requires generators
- The quality of the ultimate physics result (oscillation parameters, phases, neutrino mass ordering) depends on quality of the generator
- The generator must be as much state-of-the-art as the experimental equipment
- This talk concentrates on problems related to energy reconstruction and generators.



ν -A Processes



All these processes are entangled, cannot be separated experimentally.

For Mini/MicroBooNE, T2K:

physics is reasonably well described by QE and Δ resonance excitation

Both are entangled; pion reabsorption essential

For DUNE:

Must have explicit inelastic excitations and DIS

→ Need full final state, semi-inclusive

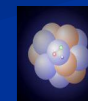
Giessen Model: Theory and Generator

■ Initial State Interactions

- Nucleons are bound in a momentum-dep mean-field potential
- Treats all ISI processes: QE, RES, 2p2h, DIS (switch to DIS = PYTHIA at $W \sim 2 - 3$ GeV)
- The low-energy part similar to Valencia model, but binds nuclei
- Contains large number of N^* resonances and mesons, up to charm
- Not restricted to the low energies of Valencia model

■ Final State Interactions: quantum-kinetic transport theory

- Contains elastic and inelastic FSI, tries to respect time-reversal invariance
- Fully relativistic transport in potential, trajectories numerically integrated
- Relativistically correct collision criteria for FSI
- Allows for off-shell transport of broad spectral functions
- Contains modelling of color transparency, formation times



Giessen model ingredients

- Baryon Resonances up to $W \sim 2$ GeV transported explicitly, with properties from PDG, *lifetime determined by widths*
- DIS Processes ($W > 2$ GeV) described by string fragmentation (PYTHIA), *lifetime determined by fragmentation time-scale, no external `formation times`:*

K. Gallmeister, U. Mosel

``Time Dependent Hadronization via HERMES and EMC Data Consistency''

Nucl. Phys. A **801**(2008) 68

K. Gallmeister, T. Falter

``Space-time picture of fragmentation in PYTHIA/JETSET for HERMES and RHIC''

Phys. Lett. B **630** (2005) 40

- **Problem:** Cross section development during these `formation times`, often taken to be 0, e.g. GENIE: no interactions within 0.342 fm/c!
Contradicts experiments!







- **Giessen Model implemented in the generator GiBUU**
- **GiBUU : Quantum-Kinetic Theory and Event Generator**
based on a BM solution of Kadanoff-Baym equations
- GiBUU propagates phase-space distributions, not particles
- Physics content and details of implementation in:
Buss et al, Phys. Rept. 512 (2012) 1- 124
- Code from gibuu.hepforge.org, new version **GiBUU 2021**, soon v 2022



CT identification needs reliable FSI description

- 
- 
- Kadanoff-Baym equation (1960s)
 - full equation not (yet) feasible for real world problems
 - Boltzmann-Uehling-Uhlenbeck (BUU) models: **GiBUU**
 - Boltzmann equation as gradient expansion of Kadanoff-Baym equations, in Botermans-Malfliet representation (1990s) with off-shell transport
 - Cascade models
(typical event generators, **GENIE, NEUT, NuWro, ...**)
 - Nuclei not bound, no mean-fields, primary interactions and FSI not consistent, frozen nuclear configuration,
 - Purely absorptive Cascade: Glauber

Quantum-kinetic Transport Theory

On-shell drift term

BM off-shell transport term

Collision term

$$\mathcal{D}F(x, p) - \text{tr} \left\{ \Gamma f, \text{Re} S^{\text{ret}}(x, p) \right\}_{\text{PB}} = C(x, p) .$$

$$\mathcal{D}F(x, p) = \{p_0 - H, F\}_{\text{PB}} = \frac{\partial(p_0 - H)}{\partial x} \frac{\partial F}{\partial p} - \frac{\partial(p_0 - H)}{\partial p} \frac{\partial F}{\partial x}$$

H contains
mean-field
potentials

Describes time-evolution of $F(x, p)$

$$F(x, p) = 2\pi g f(x, p) \mathcal{P}(x, p)$$

Spectral function

Phase space distribution

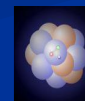
KB equations with BM offshell term

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GiBUU Tests

- Widely tested on
 - heavy-ion reactions (< 20 AGeV), $p + A$, $\pi + A$
 - mainly FSI tests
 - (e, A) reactions (JLAB: $E < 6$ GeV, HERMES: 28 GeV, EMC: 230 GeV)
 - (ν, A) reactions (MiniBooNE, MicroBooNE, T2K, MINERvA)

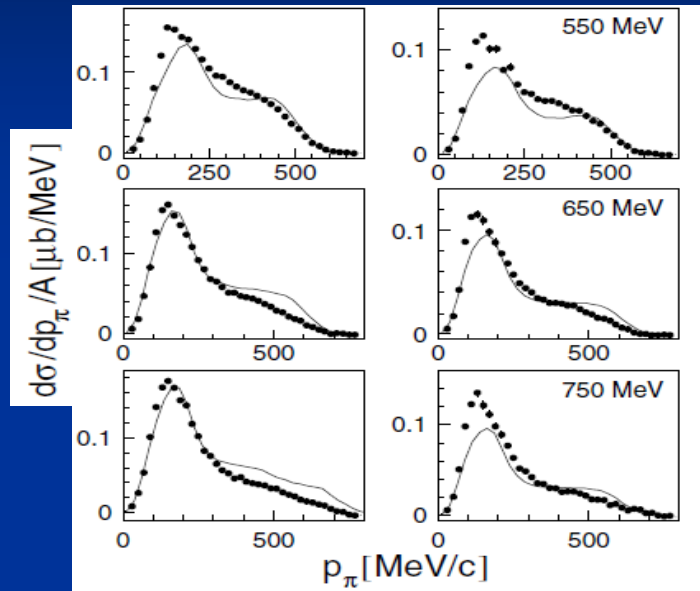


Check: pions, protons

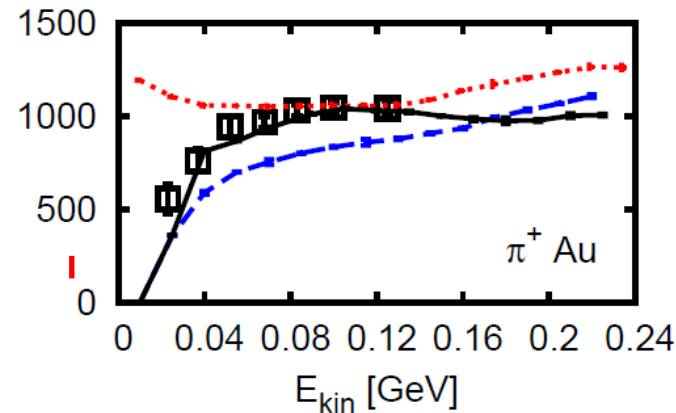
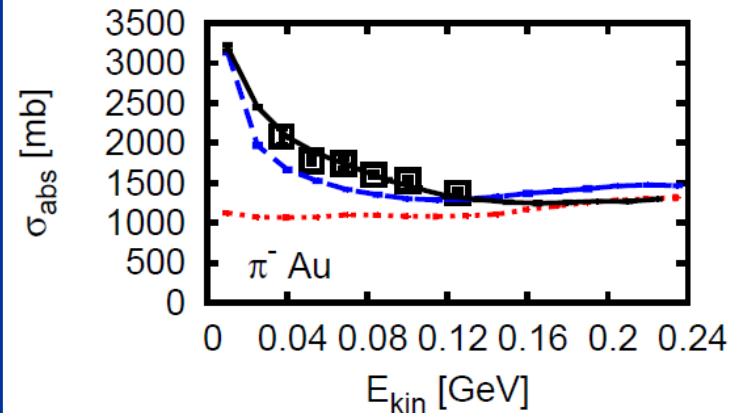
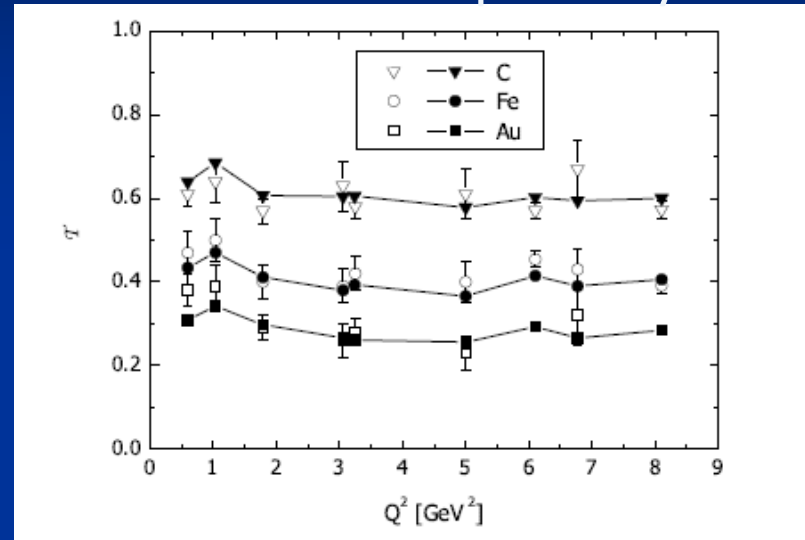
(Leitner et al, <https://inspirehep.net/literature/819969> (2009))

$\gamma \rightarrow \pi^0$ on Ca

Pb



Proton transparency



Pion reaction Xsect.

- no potential
- Coulomb only
- Coulomb + nuclear



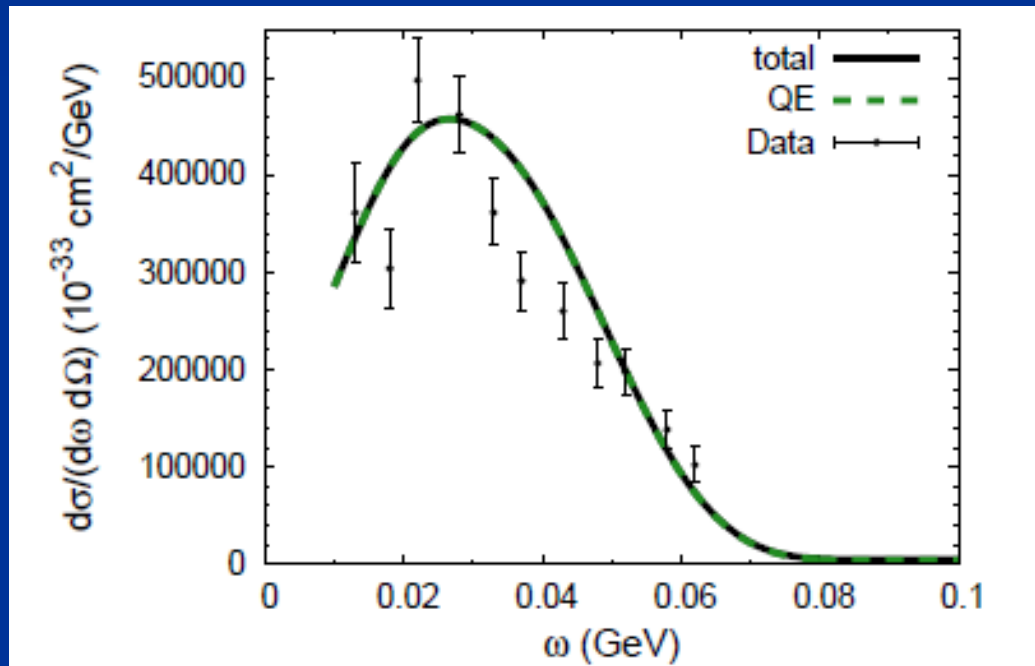
Inclusive Electron X-Sections

- Necessary (vector couplings),
but not sufficient (axial couplings) test
- Only indirect, weak test for FSI
- Not sufficient for energy-reconstruction



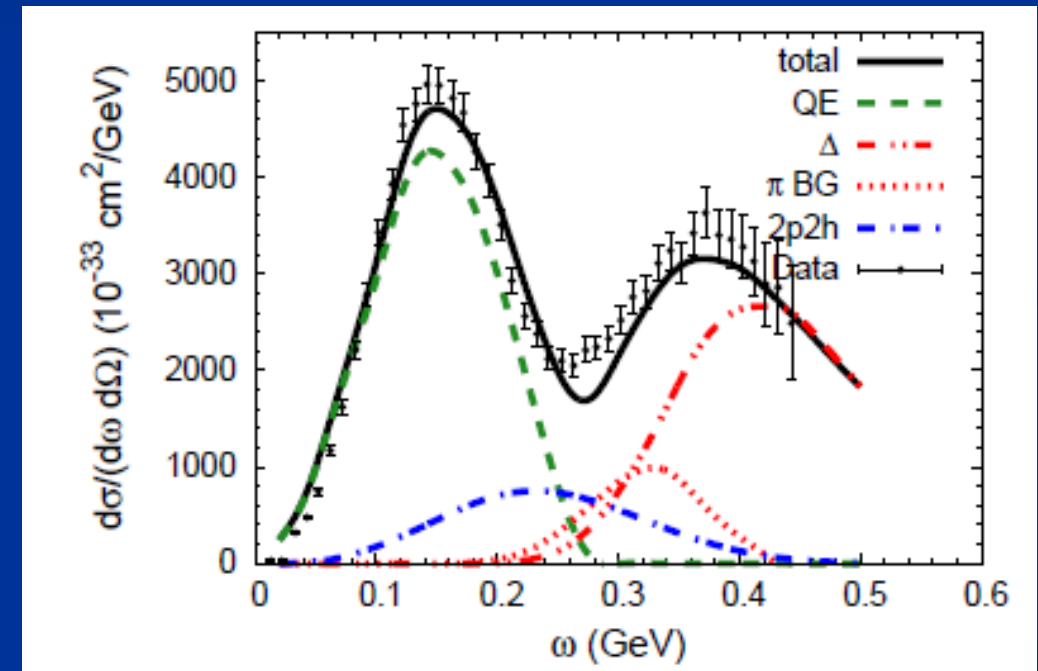
Inclusive QE Electron Scattering

- a **necessary check** for any generator development



0.24 GeV, 36 deg, $Q^2 = 0.02 \text{ GeV}^2$

Target: C



0.56 GeV, 60 deg, $Q^2 = 0.24 \text{ GeV}^2$

Uncertainties at lower energies

- At T2K, MicroBooNE energies:

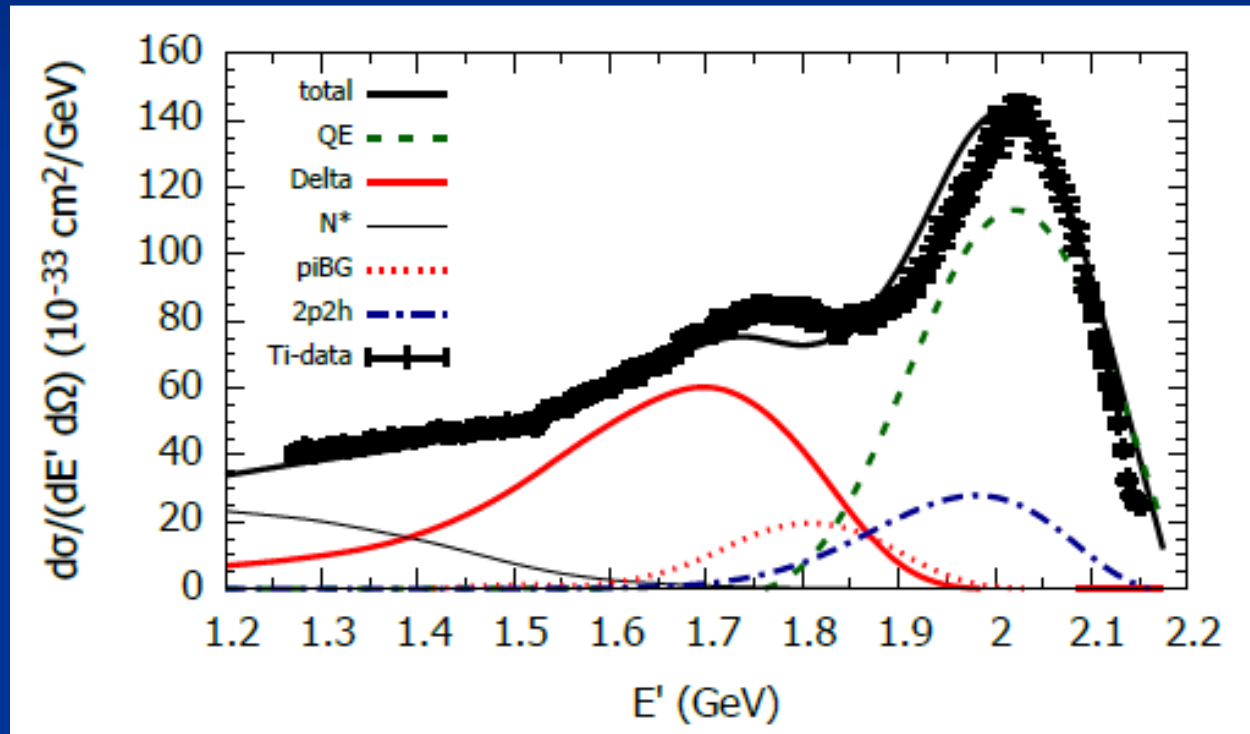
- Theory of QE and 2p2h reasonably well under control
- Δ resonance can be pinned down by simultaneous analysis of incl. X-sections and π -production

Problem is energy reconstruction via QE-like processes, because QE and pion production with subsequent pion absorption are entangled:

exp $|p0\pi$ is not QE!!! Problem for e4nu, SUSA

- Tuning generator to e-data (e-GENIE) does not help, entanglement is physics, not generator problem, need to describe consistently QE, 2p2h and Δ resonance excitation

Inclusive Electron X-section



$E = 2.22 \text{ GeV}, \theta = 15.5 \text{ deg}$

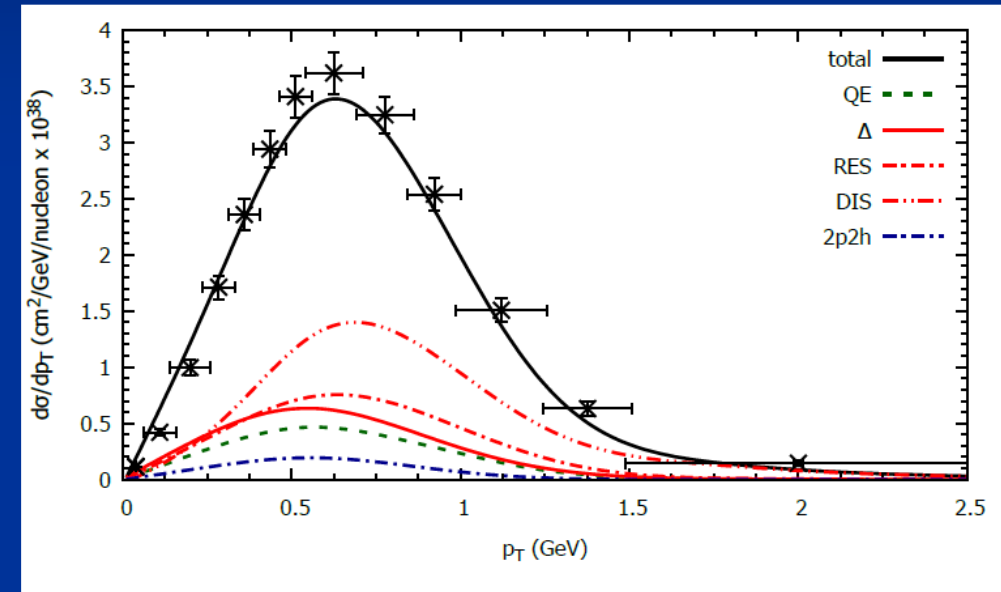
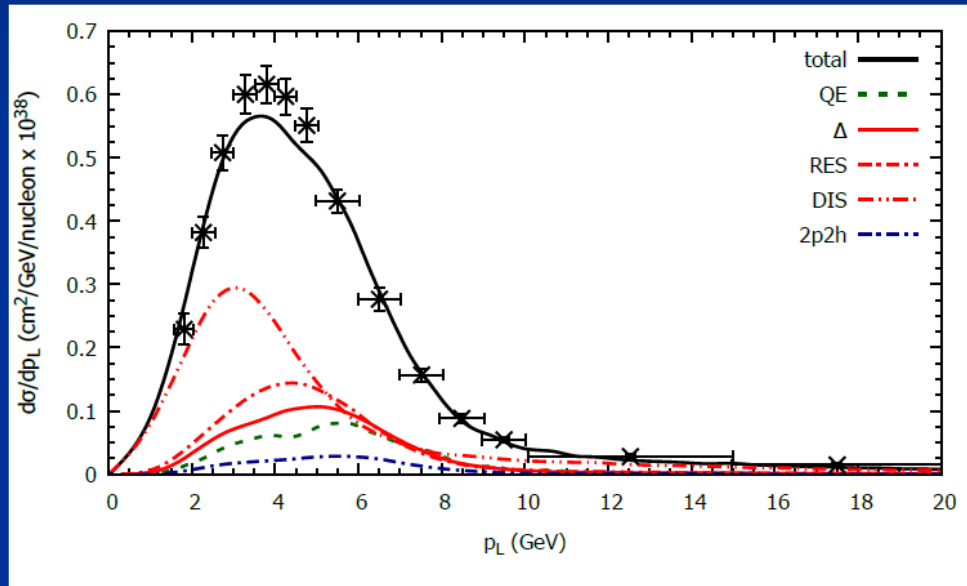
Data: Dai et al,
PRC98 (2018) 014617

GiBUU theory:
Mosel et al, PRC 99 (2019) 6

Inclusive ν X-section at $E_\nu \sim 6$ GeV

Data: MINERvA ME, Ruterbories et al, PRC 104 (2021) 9

GiBUU preliminary



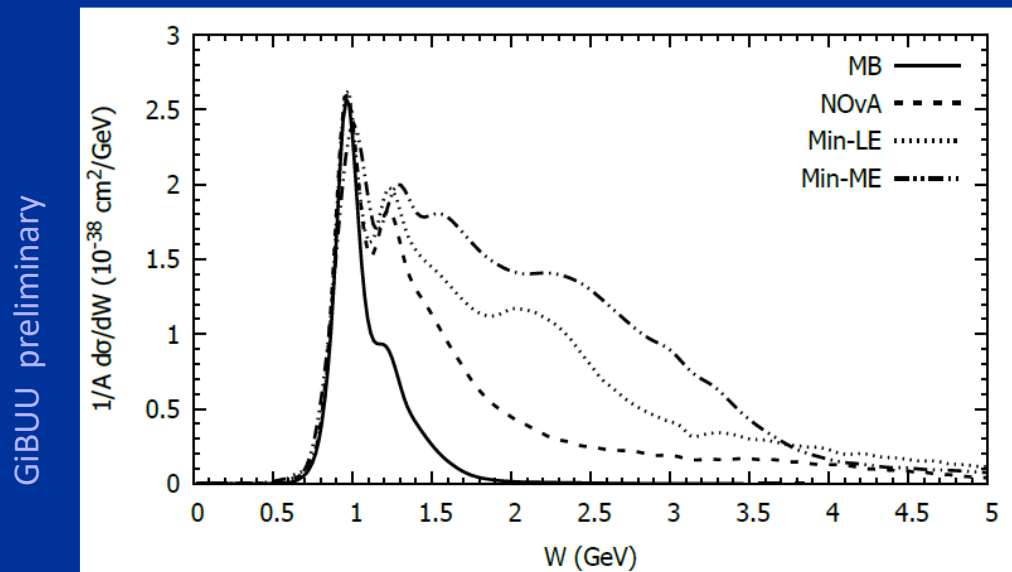
DIS and RES dominate:

DIS is uncertain at these (for pQCD) relatively low energies

RES is uncertain because of axial couplings to resonances

Uncertainties at higher energies (SIS)

- At NOvA, MINERvA and DUNE energies:
 - Higher resonances ($> \Delta$, SIS region) explored by present experiments



No info from e-A reactions
axial coupling to resonances is uncertain

Axial coupling of spin 3/2 resonances:
Up to 100% uncertainty in X-section
(Lalakulich and Paschos, PR D74 (2006) 014009)

Difference of MINERvA and NOvA is nearly pure RES and SIS

Neutrinos: Uncertainties in SIS

- From Lalakulich, Paschos, Piranishvili (PR D74 (2006) 014009)
Transition operator to spin-3/2 resonances:

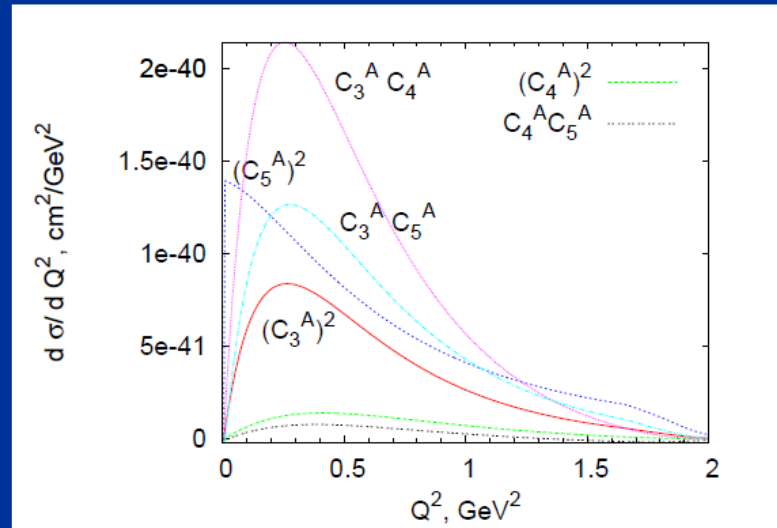
$$d_{D13}^{\lambda\nu} = g^{\lambda\nu} \left[\frac{C_3^V}{m_N} \not{q} + \frac{C_4^V}{m_N^2} (p'q) + \frac{C_5^V}{m_N^2} (pq) + C_6^V \right] - q^\lambda \left[\frac{C_3^V}{m_N} \gamma^\nu + \frac{C_4^V}{m_N^2} p'^{\nu} + \frac{C_5^V}{m_N^2} p^\nu \right]$$

$$+ g^{\lambda\nu} \left[\frac{C_3^A}{m_N} \not{q} + \frac{C_4^A}{m_N^2} (p'q) \right] \gamma_5 - q^\lambda \left[\frac{C_3^A}{m_N} \gamma^\nu + \frac{C_4^A}{m_N^2} p'^{\nu} \right] \gamma_5 + \left[g^{\lambda\nu} C_5^A + q^\lambda q^\nu \frac{C_6^A}{m_N^2} \right] \gamma_5.$$

known

not known

E = 2 GeV
C3A = 1,
C4A = 1



Interference terms between various axial formfactors can double the cross section!

Info obtainable only from inclusive neutrino X-sections

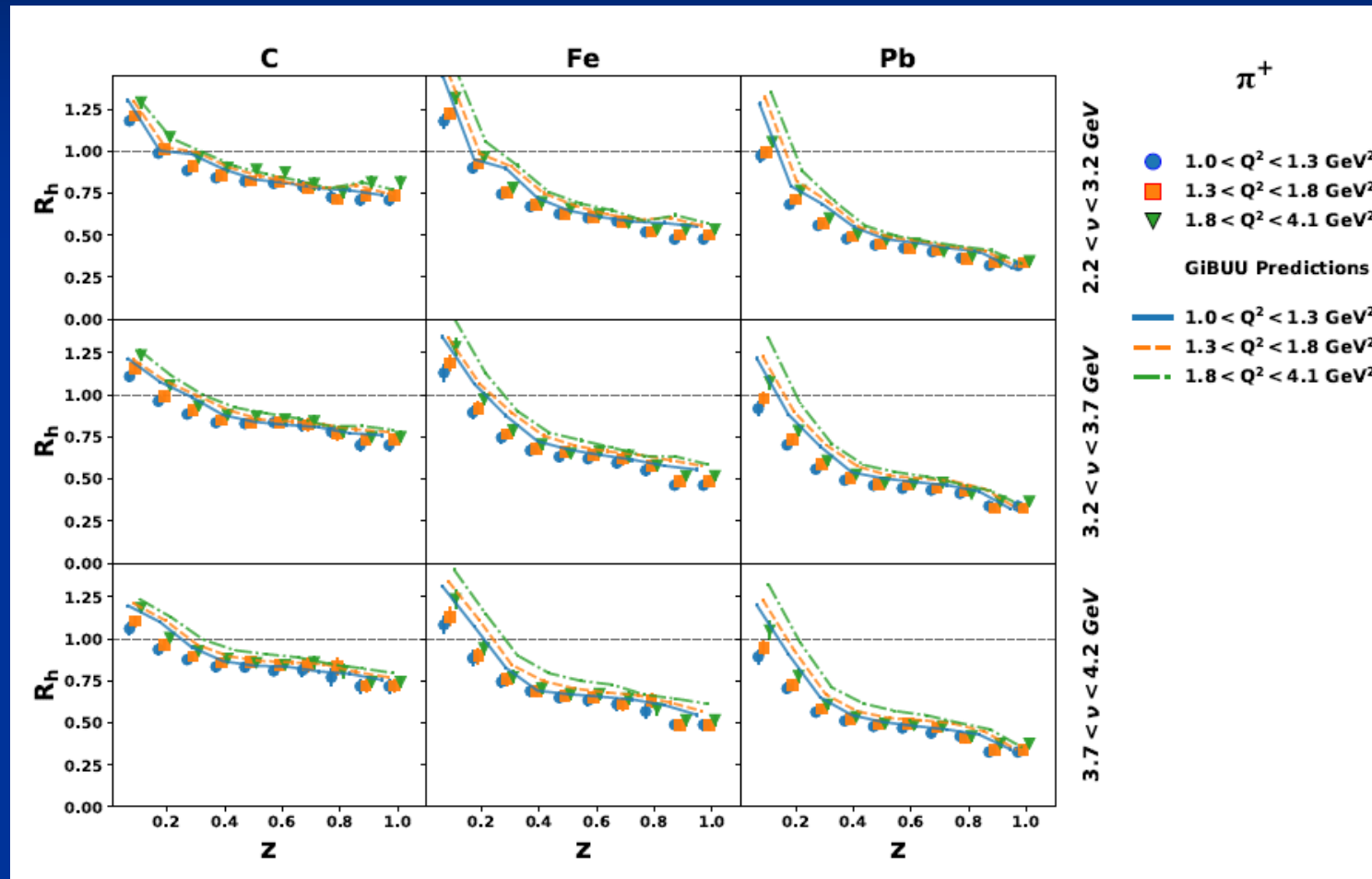
Energy Reconstruction at Higher Energies

- At NOvA, MINERvA and DUNE need calorimetric method to reconstruct incoming energy → need full final state information, inclusive is not enough!
- Final State Interactions are identical for electrons and neutrinos:
final state particles do not remember how they were initially produced
→ no uncertainty stemming from axial coupling
→ semi-inclusive **electron data can give relevant (and necessary) info on FSI**
- Baryon spectra and multiplicities to fix and check FSI treatment are needed, for NOvA, MINERvA, DUNE semi-inclusive DIS (SIDIS) is relevant



SIDIS: Pions at 5 GeV@JLAB

Attenuation ratios



Data:
Moran et al,
Phys.Rev.C 105 (2022) 1
Theory:
GiBUU

$$z = E_{\pi}/\nu$$

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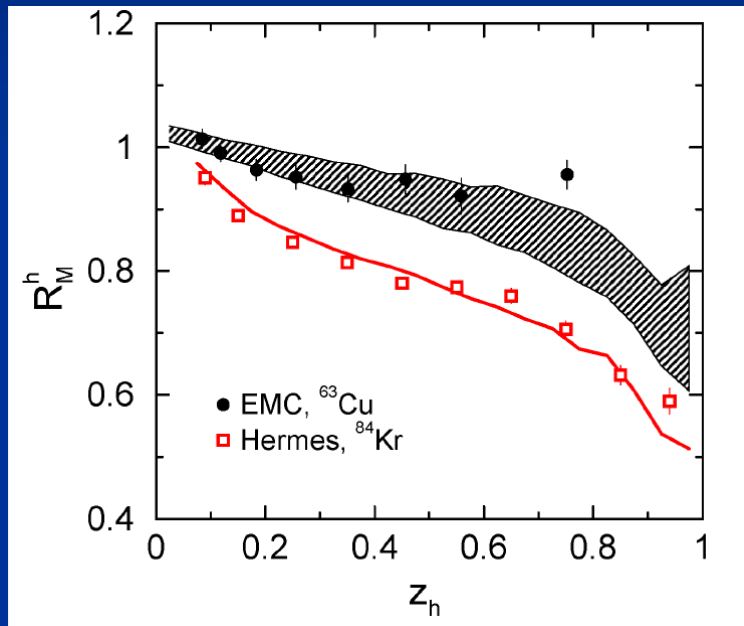
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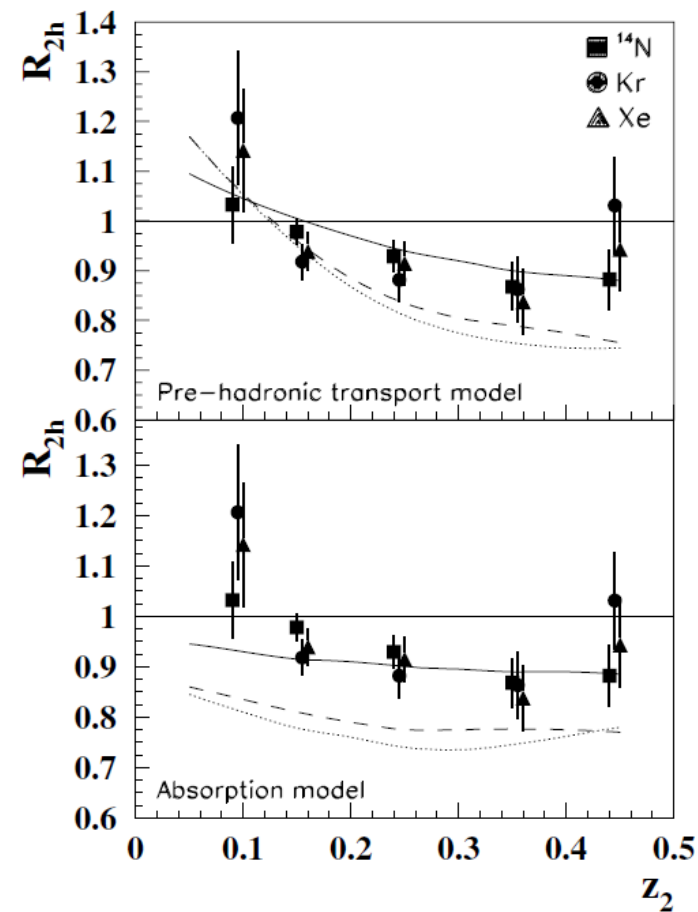
SIDIS at higher energies

N. Bianchi / Nuclear Physics A 783 (2007) 93c-100c

All hadron attenuation



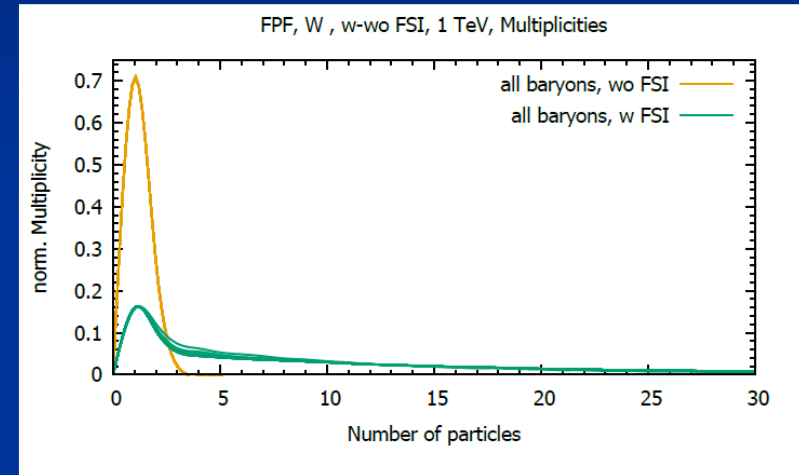
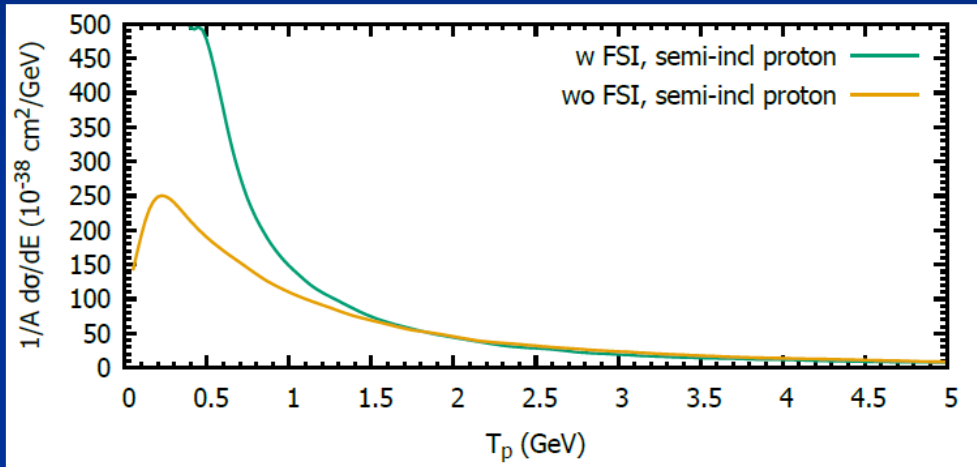
K. Gallmeister, U.M.
Nucl.Phys.A 801 (2008) 68-79



HERMES Experiment:
28 GeV positrons or electrons,
2N attenuation

Curves: GiBUU

FSI effects in energy spectra

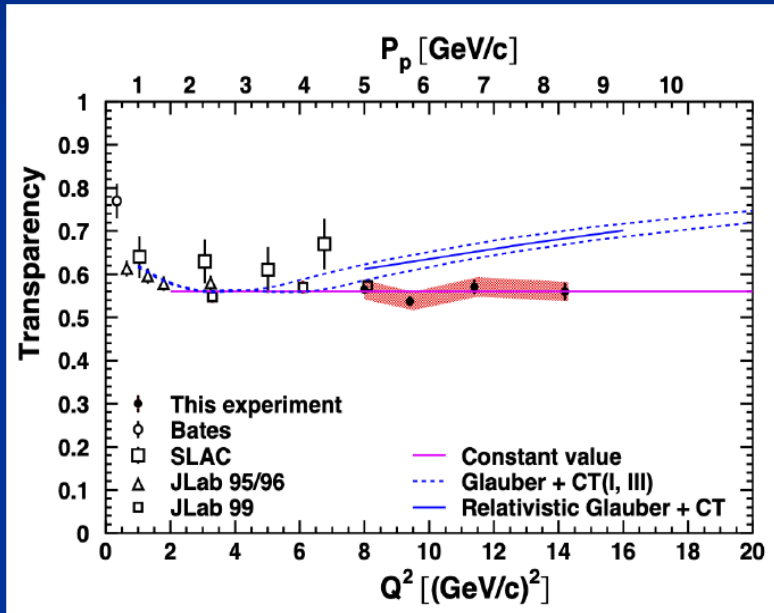


Strong avalanche effect: pileup of baryons at low energies
strong rise sets in below ~ 1.5 GeV kinetic energy,
reflects strong rise of NN X-sections at this energy

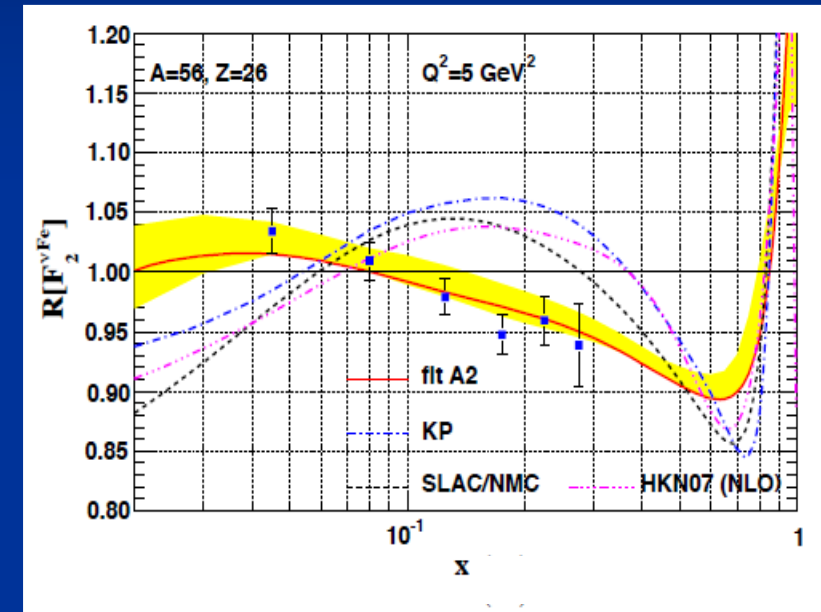
Target: W, 1 TeV
for FPF project

Fundamental open problems

JLAB 2021



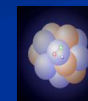
Where is Color Transparency ???
Needs generator to follow struck hadrons through nuclear target



EMC effect for neutrinos,
tension with electrons:
needs generator to reconstruct Bjorken x

Summary

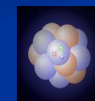
- ‚Low-energy‘ experiments are dominated by QE, 2p2h, Δ . Energy reconstruction can rely on QE-like processes, but needs generator to separate out true QE. Even there the generator must go beyond models for inclusive Xsections (also for experimental analyses of semi-inclusive electron data).
- ‚High-energy‘ experiments have large contributions from SIS and DIS. Energy reconstruction needs calorimetric method and needs reliable generators for semi-inclusive X-sections in SIS/DIS regime
 - Axial properties of N^* resonances are quite uncertain, inclusive X-sections can give info on SIS region.
 - Semi-inclusive electron data are dominated by FSI, i.e. independent of axial uncertainties -> crucial tests for generators are final state particle spectra and multiplicities. Few electron-SIDIS data are available in the DUNE energy regime (few GeV) and so far no neutrino data.



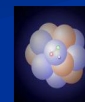
Fundamental open problems

- Construct a generator that is theoretically as much state-of-the-art as the experimental equipment.
- Use state-of-the-art nuclear structure and reaction theory to get away from tuning unphysical parameters.
- Ultimate problem: obtain sufficient funding (and long-range jobs for younger scientists) for such a development which has to start now to be ready for the start of DUNE

One possible solution: bring generator-theory into the CERN neutrino platform, needs transatlantic funding scheme between CERN and FNAL



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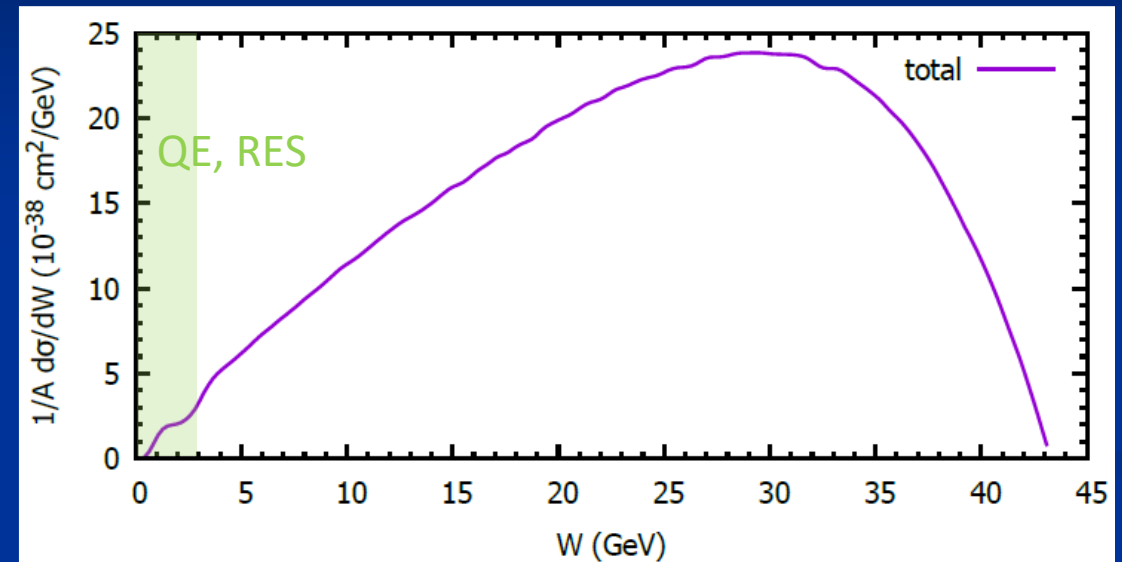
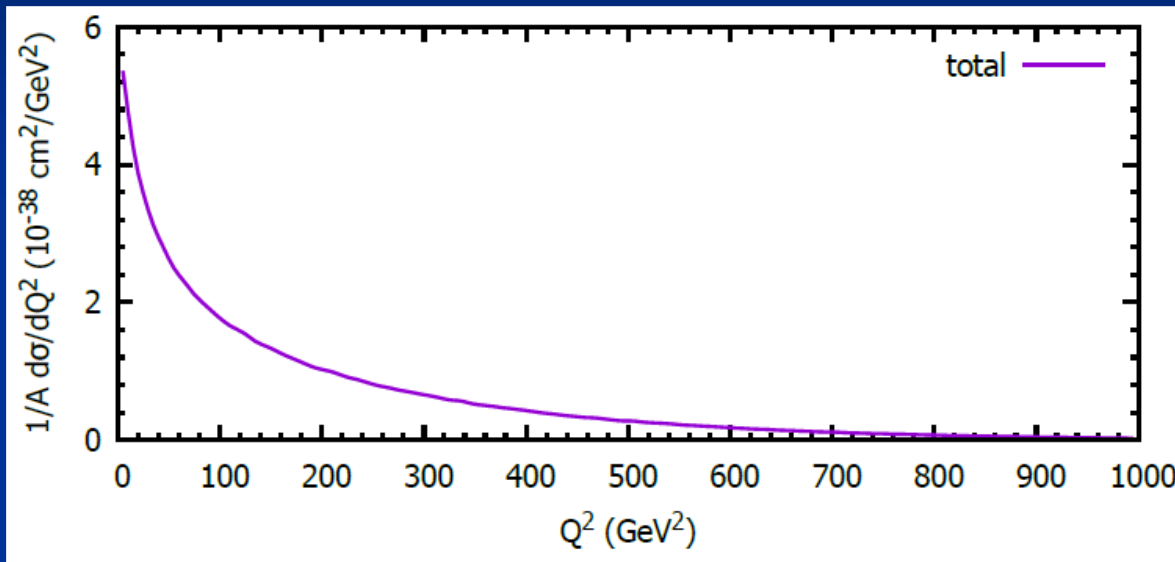
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Time Course of a (γ, ν) A Reaction

- First, initial state (IS) interaction of incoming boson (γ, W, Z) with Fermi-moving nucleon bound in a groundstate potential
-> initially produced *final state hadrons are affected by that potential*
- Initial starting points for hadron FS transport are anywhere within the nuclear volume; photons and neutrinos illuminate the whole nucleus.
- Second, *final state (FS) interaction of the produced hadrons in that same potential*, move out through the nucleus to detector
 - \rightarrow IS and FS do not factorize!

FPF, 1 TeV, incl. distributions



Dominated by DIS, have to worry about Color Transparency in FSI:

$$\frac{\sigma^*(t)}{\sigma} = X_0 + (1 - X_0) \cdot \left(\frac{t - t_P}{t_F - t_P} \right), \quad X_0 = r_{\text{lead}} \frac{\text{const}}{Q^2},$$

Farrar, Strikman et al

describes JLAB and HERMES hadronization data, also EMC