

# Longitudinal beam dynamics & diagnostics

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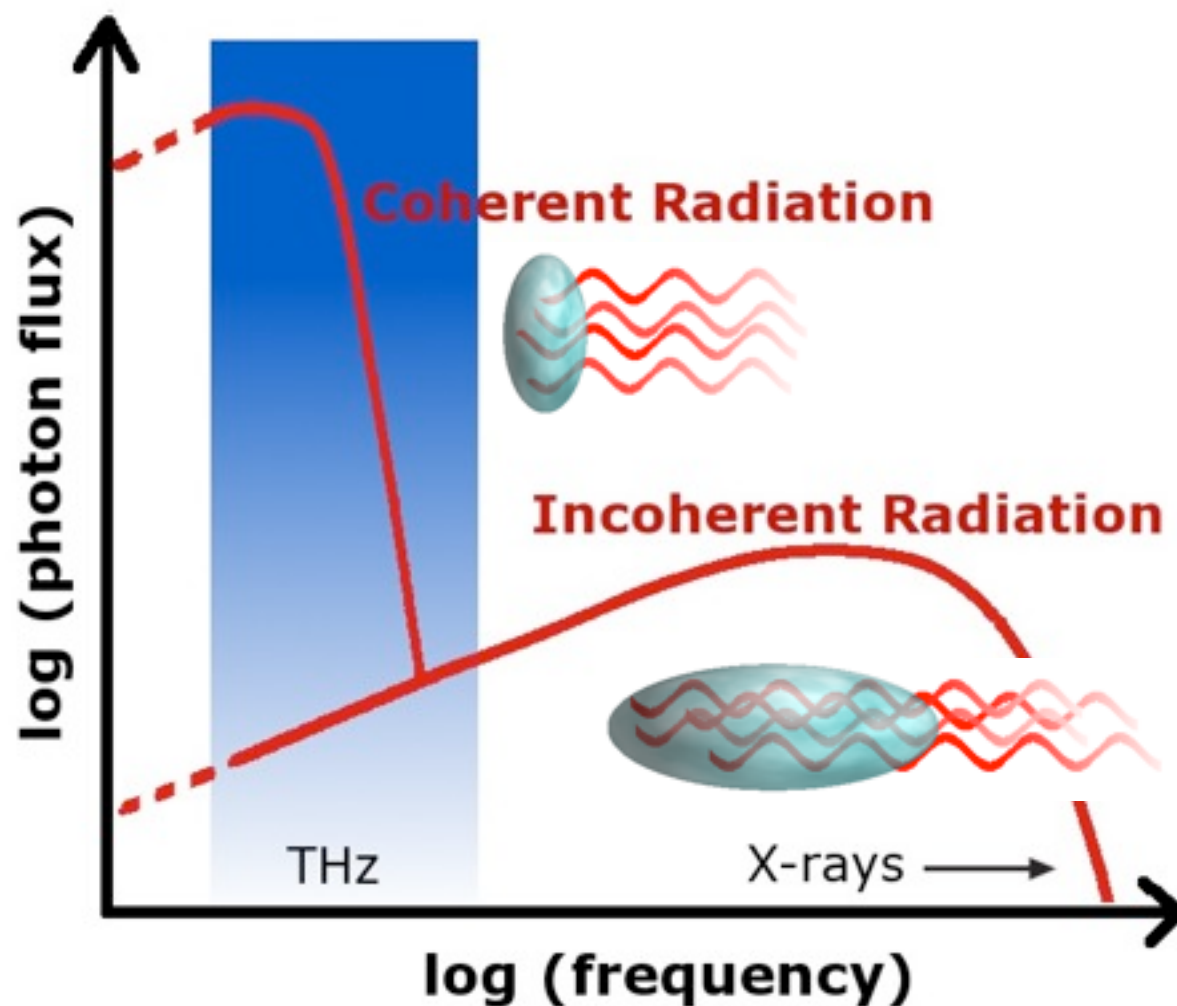
Institut für Synchrotronstrahlung (ISS) / Laboratorium für Applikationen der Synchrotronstrahlung (LAS) - Nicole Hiller



- Introduction
  - Coherent synchrotron radiation (CSR)
  - The low alpha mode
  - Time structures at ANKA
- Wake fields and impedances
  - Self fields
- Potential well distortion
  - Bunch shape
  - Bunch length → **Nicole's talk**
- Bursting stable threshold
  - Microbunching
  - Bursting behavior → **Vitali's talk**
- Power spectra of coherent radiation

# Coherent synchrotron radiation (CSR)

- Short bunches emit usable coherent synchrotron radiation
- Enormous increase in power in comparison to incoherent emission
- Dedicated optics with negative dispersion in the long and short straight sections for flexible bunch length tuning
  - ▶ Low- $\alpha_c$  optics



- Coherent radiation is produced in two regimes:
  - ▶ low power stable emission
  - ▶ high power radiation bursts

# The low-alpha mode

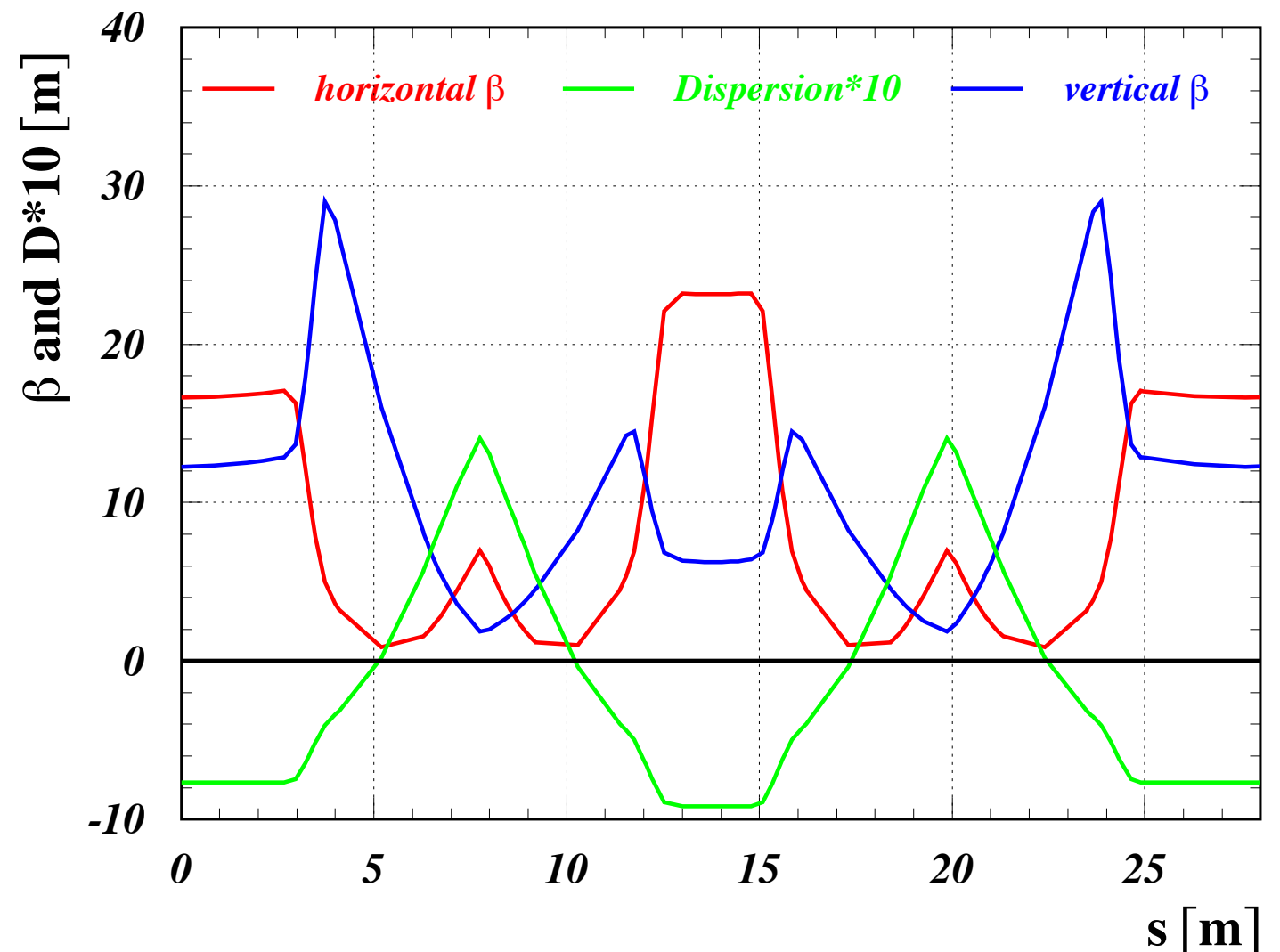
- Low-alpha user operation:  
12 days/year

## Operation procedure:

- Fill at 0.5 GeV
- Ramp energy (regular optics) to 1.3 GeV
- Low- $\alpha_c$  “squeeze”
  - ▶ change quadrupoles & sextupoles
  - ▶ orbit correction between steps

- Observed  $\alpha_c$  range as derived from  $Q_s$  measurements:

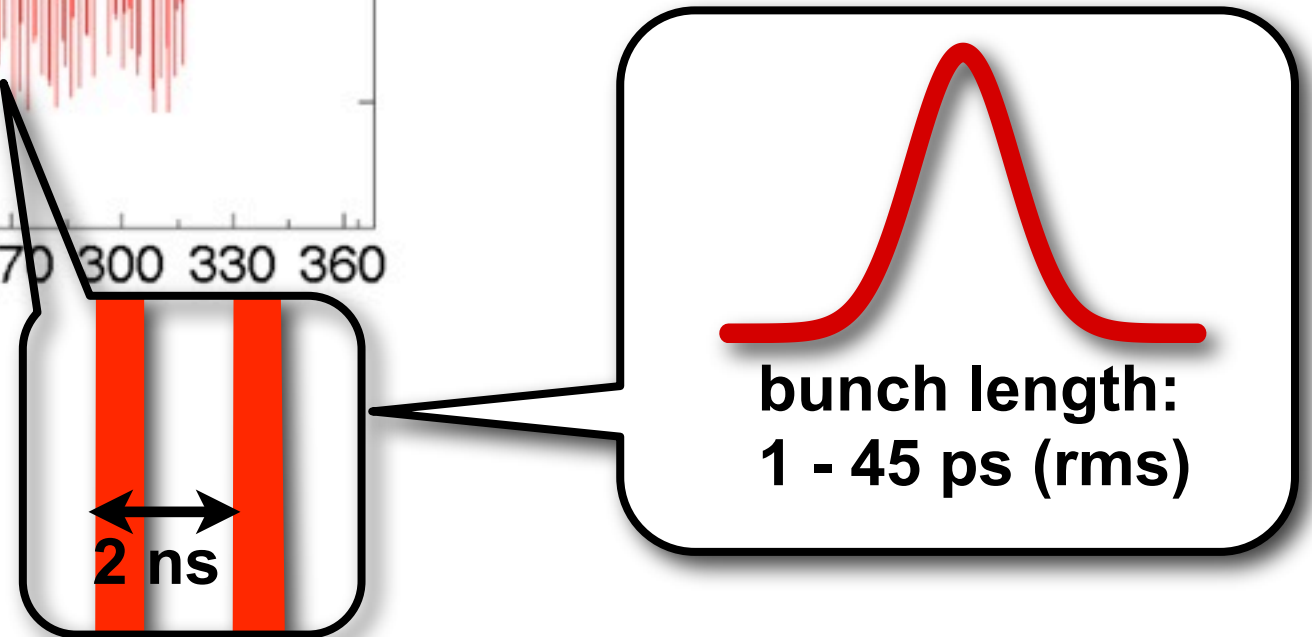
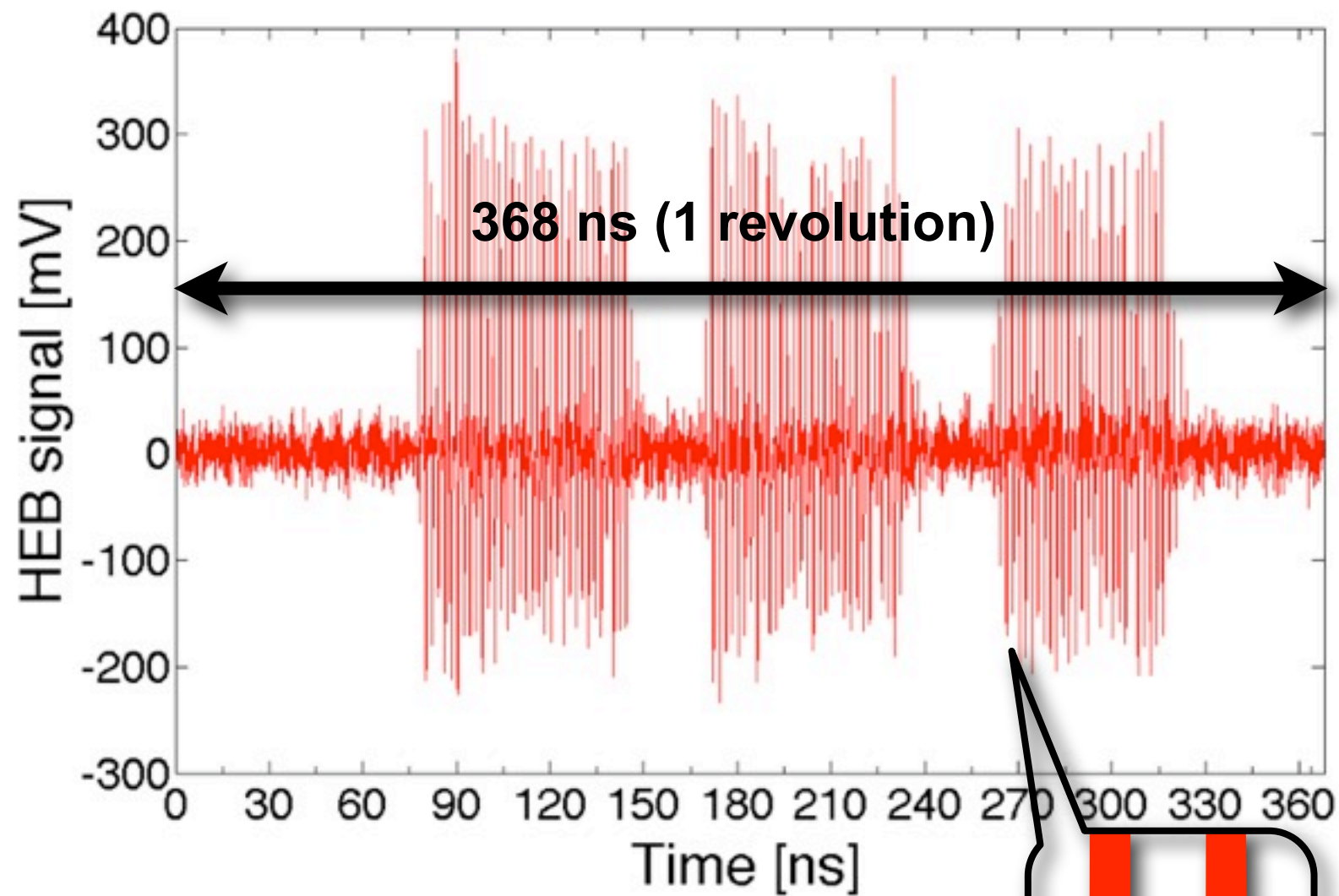
- ▶ from  $7.2 \cdot 10^{-3}$  to  $1.4 \cdot 10^{-4}$





# Time scales at ANKA

measured fill pattern

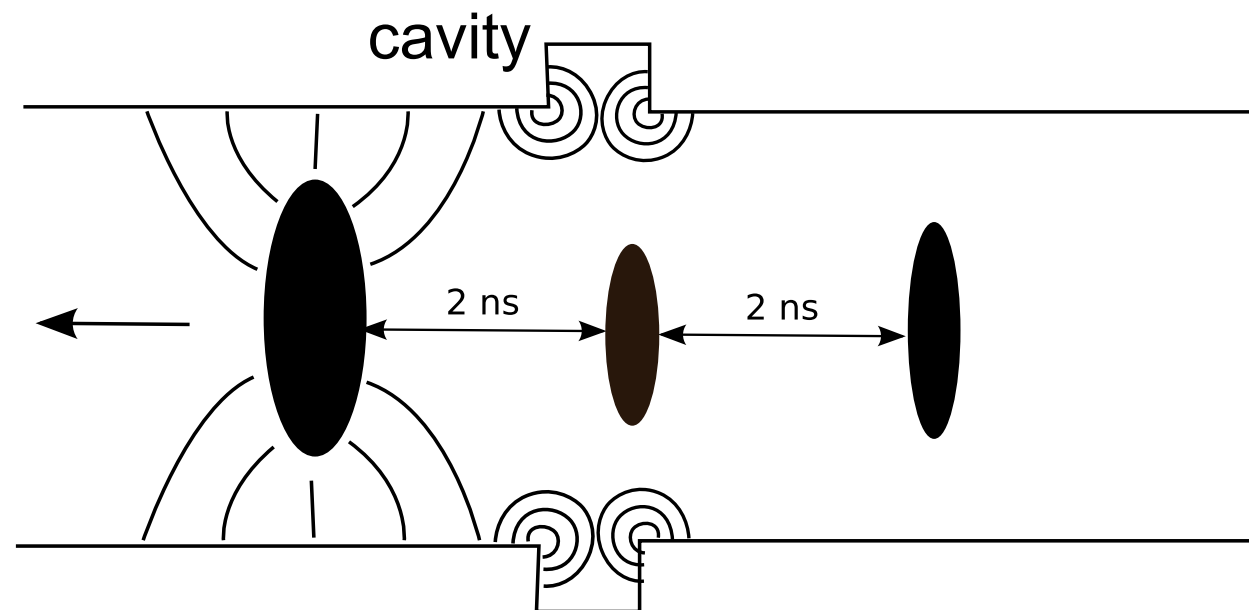
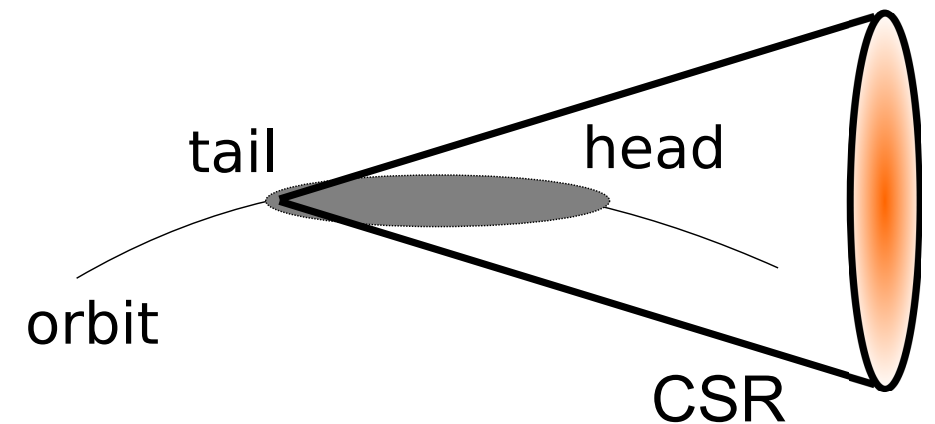


# Wake fields and impedances

- Wake fields are el.-mag. fields which are left behind by a particle
- They influence the motion of following particles
- The impedance is the fourier transform of the wake field
- Wake fields / impedances interact with the environment

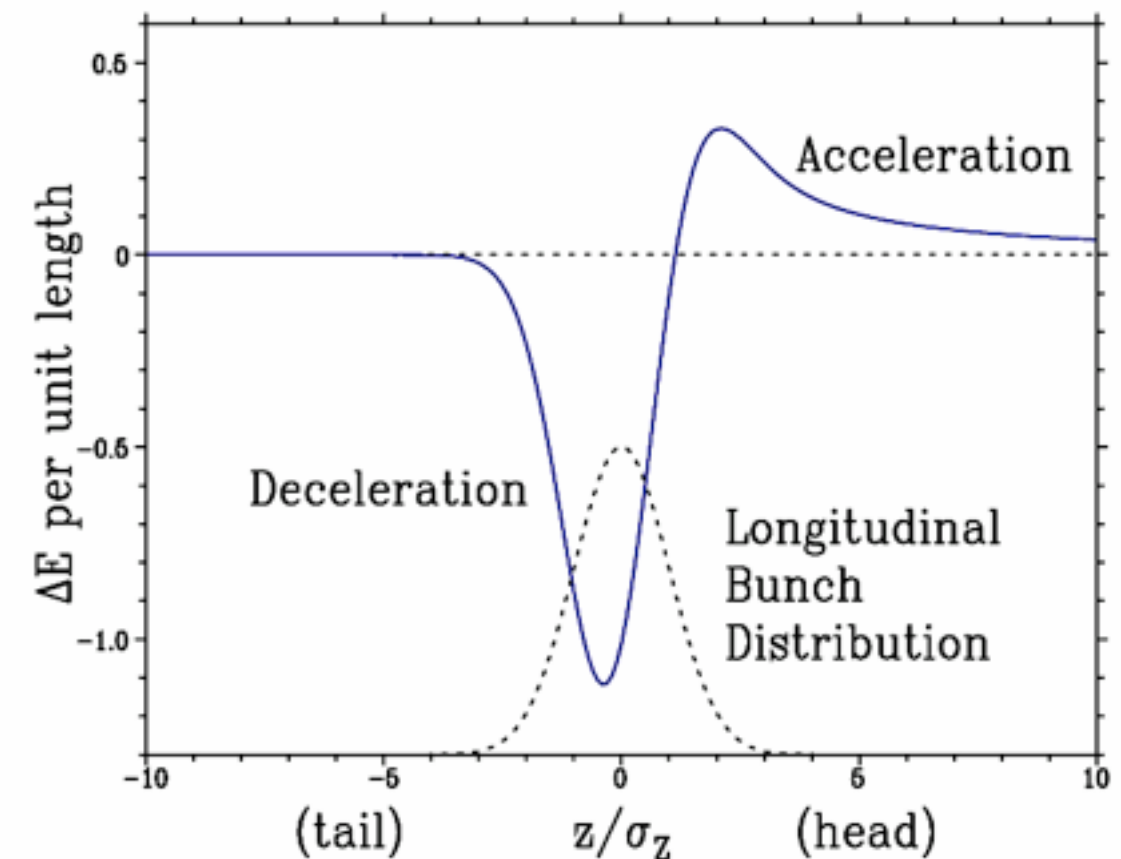
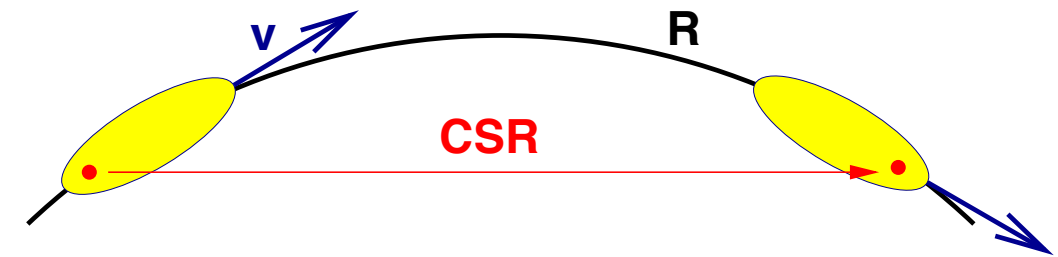
- Superposition of different impedances:

- Broad band impedance  
(inductive + reactive + resistive part)
- Synchrotron radiation impedance
- CSR impedance
- ...



# Self fields

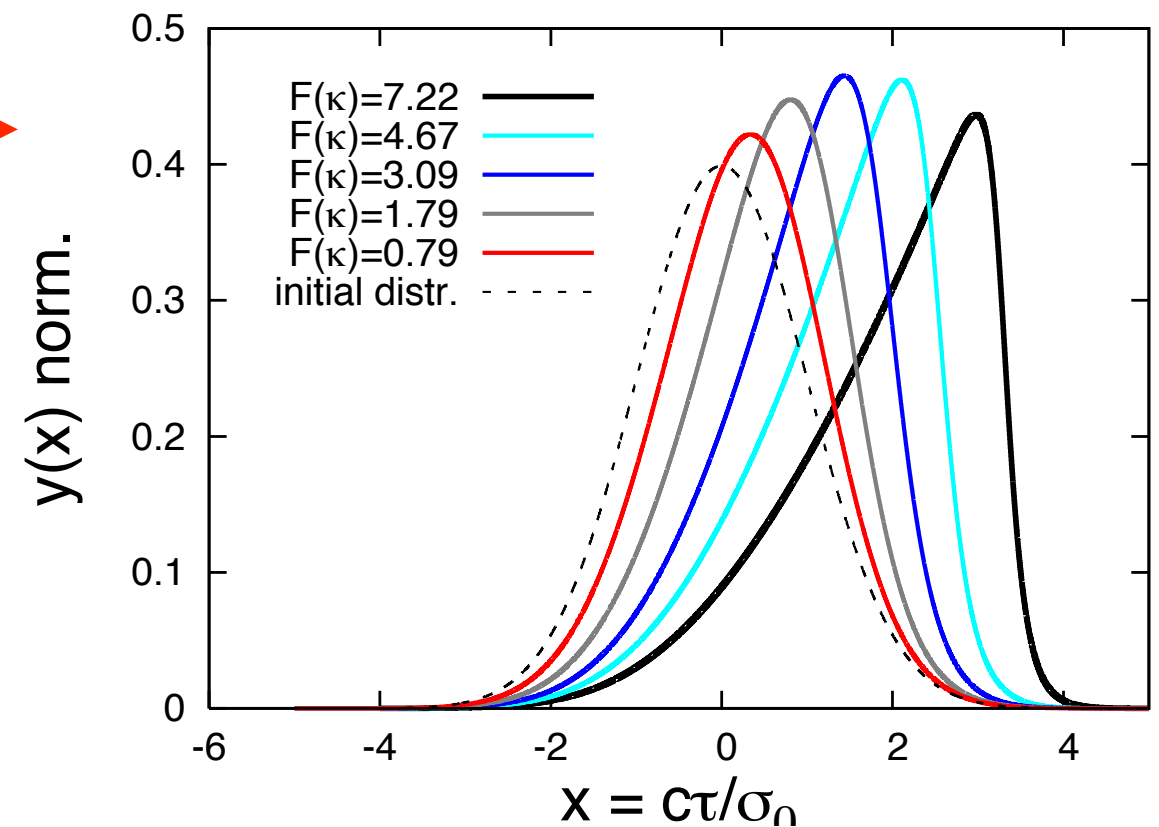
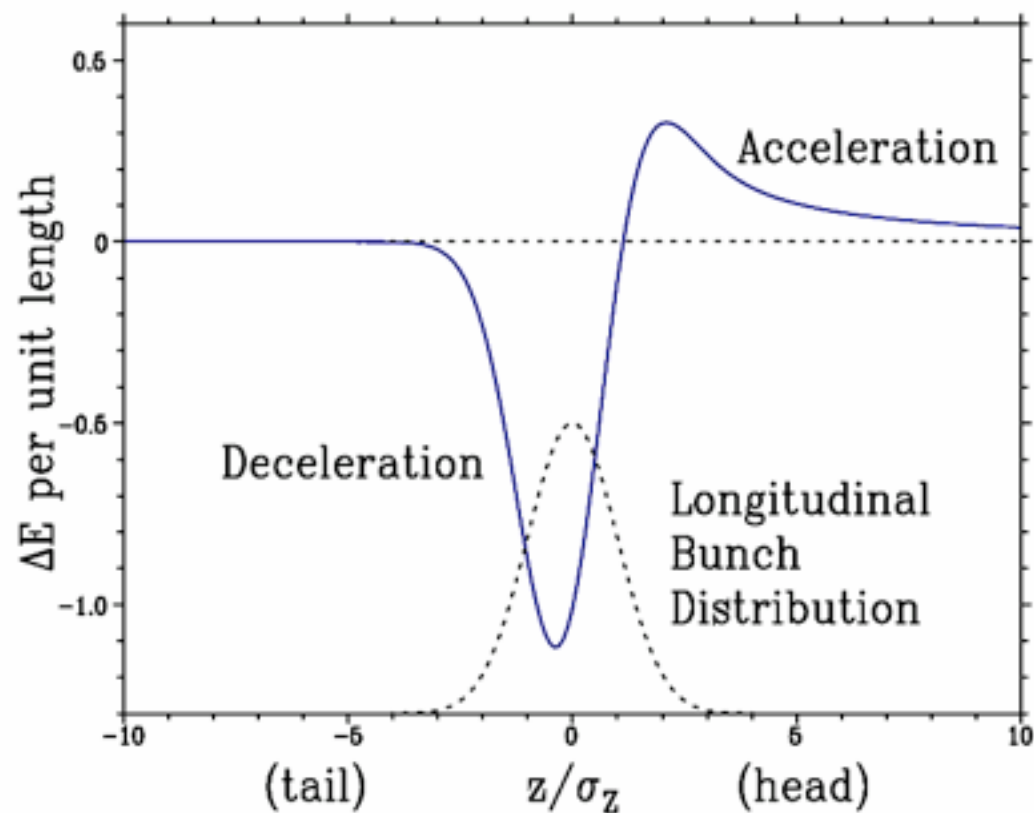
- The CSR wake field can act back on the same bunch
- Different ways to model the CSR wake / impedance:
  - free space, no shielding
  - shielding by ideal conducting parallel plates
  - shielding by rectangular beam pipe
  - ...
- Electrons in the head of the bunch are accelerated, electrons in the tail of the bunch are decelerated.



T. Agh, „Dynamics of Coherent Synchrotron Radiation by Paraxial Approximation“, Doctoral Thesis

# Potential well distortion

- The CSR wake can distort the longitudinal potential well
- The equilibrium bunch distribution of the distorted bunch can be calculated iteratively
- The integral over the bunch distribution  $F(\kappa)$  connects the bunch shapes with accelerator parameters

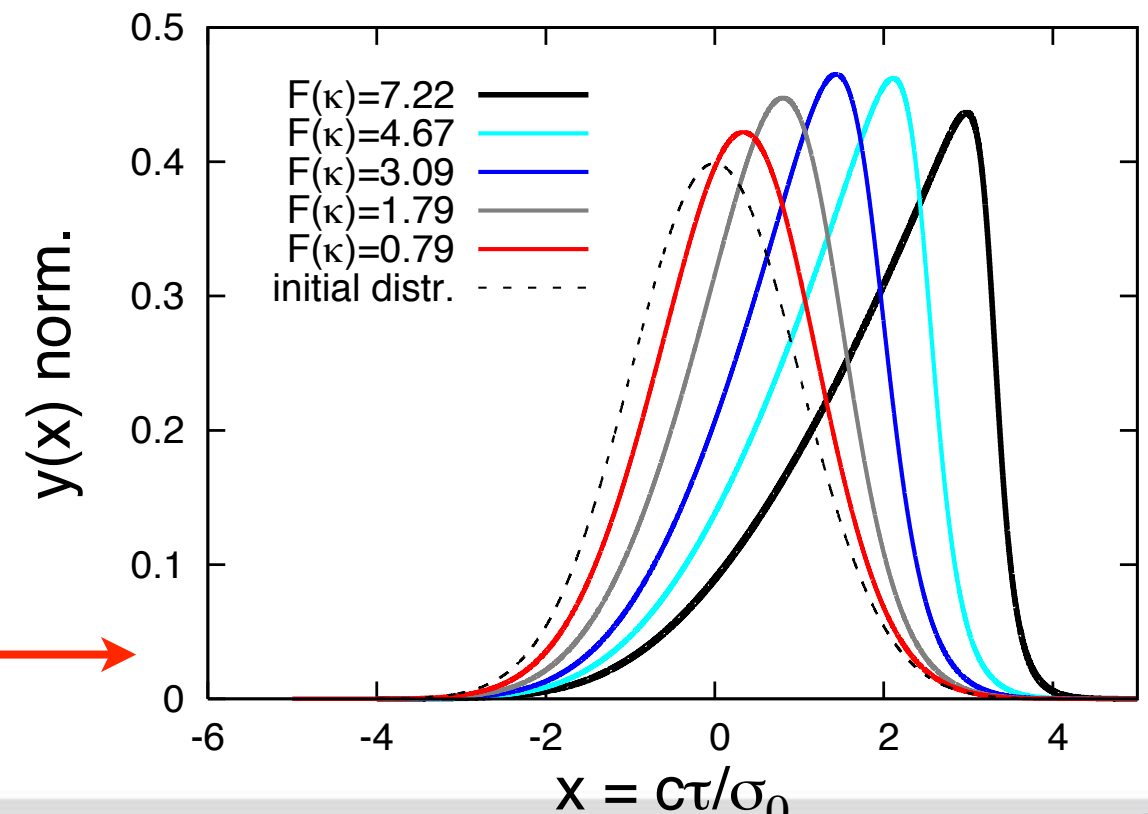
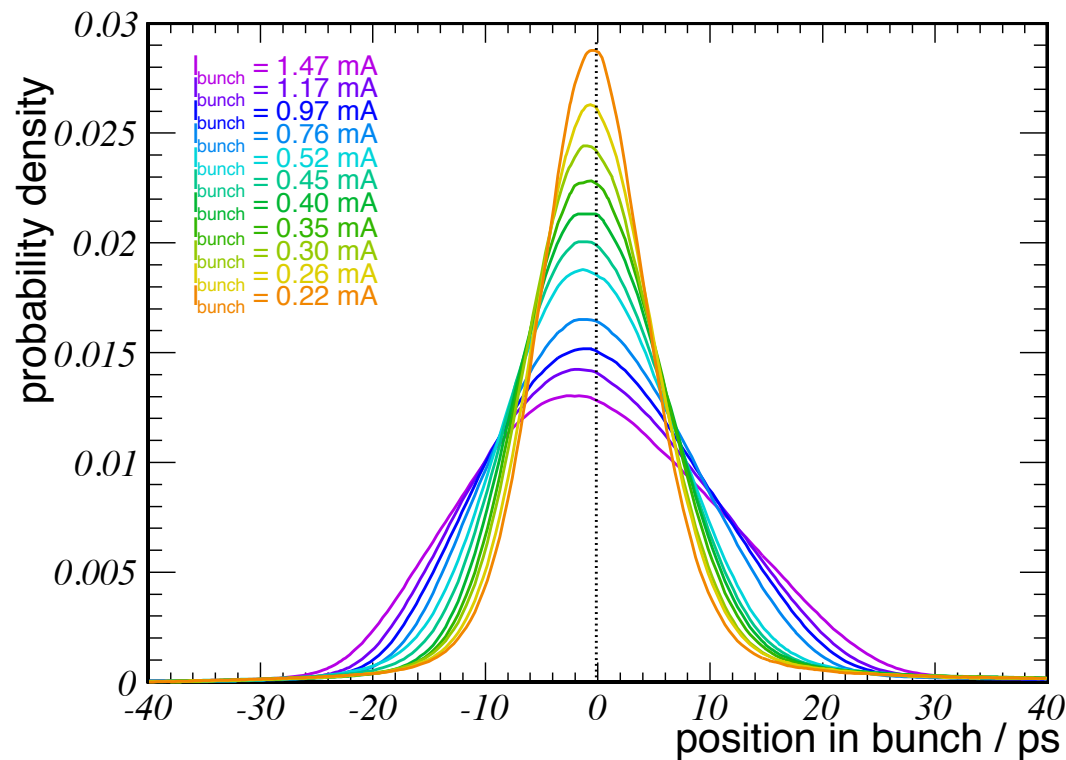
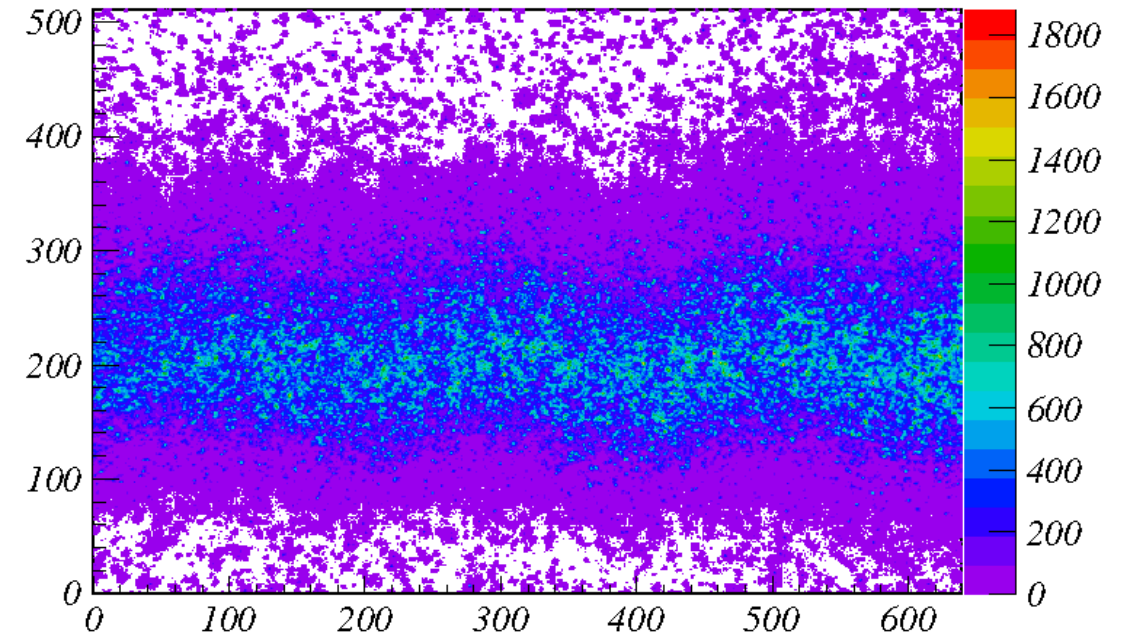




# Bunch shape

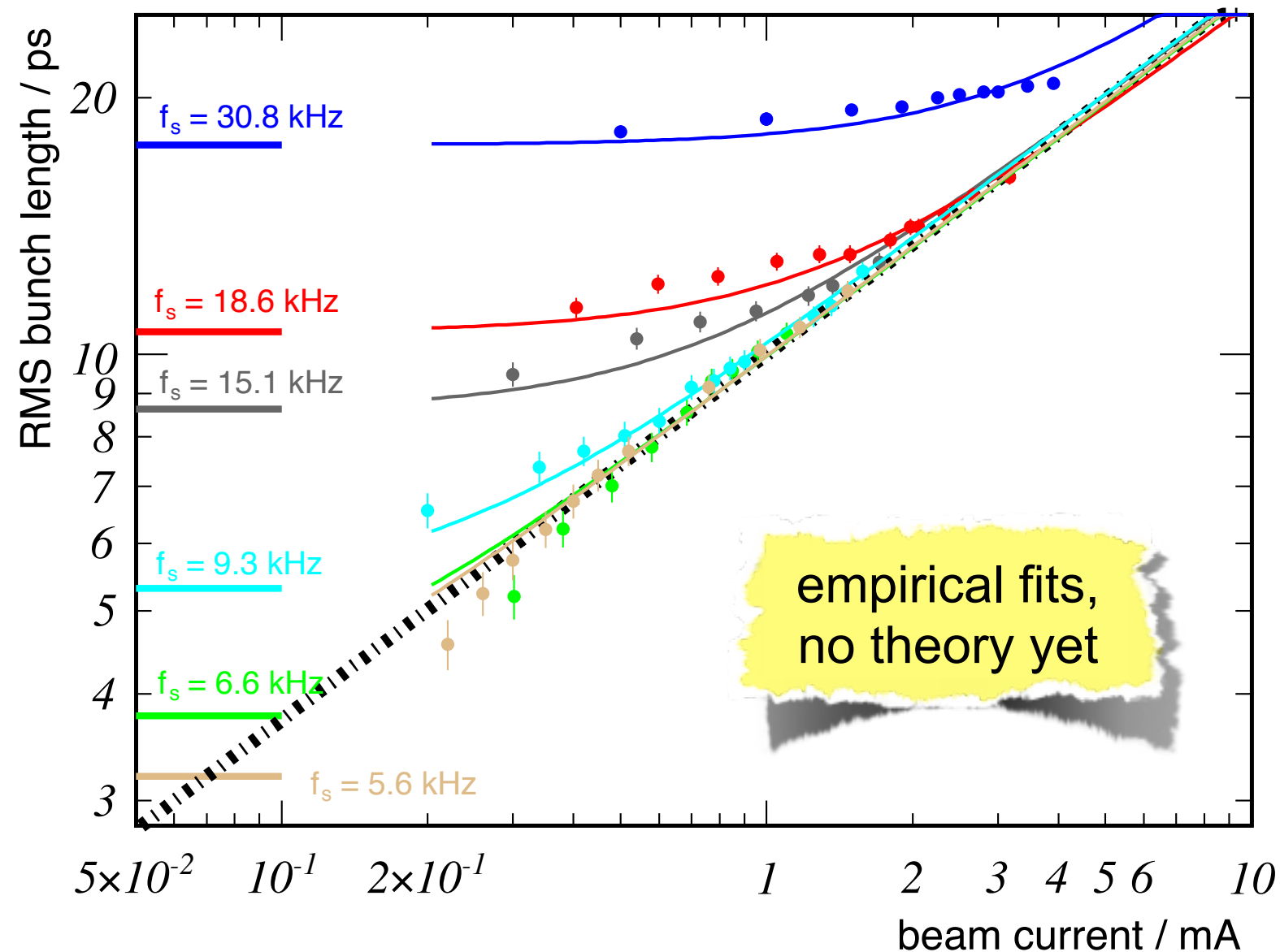
- Measurements with a streak camera
- Subtraction of oscillations
- Comparison with calculations

## ► Nicole's talk



# Bunch length

- Low currents: Converging to the zero current bunch length
- Above bursting stable threshold: Turbulent bunch lengthening

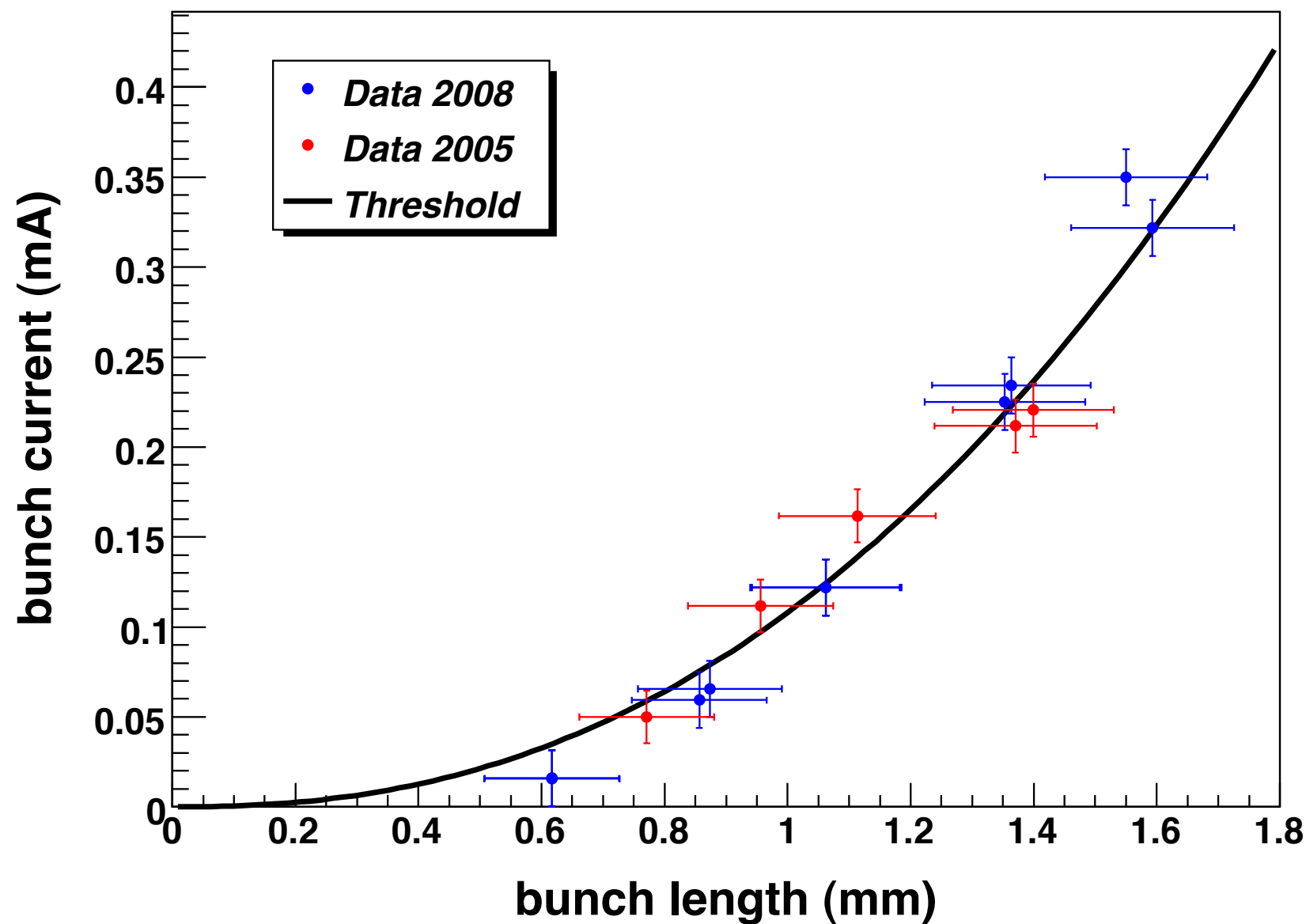


$$\sigma_z \propto I^{7/3}$$

► Nicole's talk

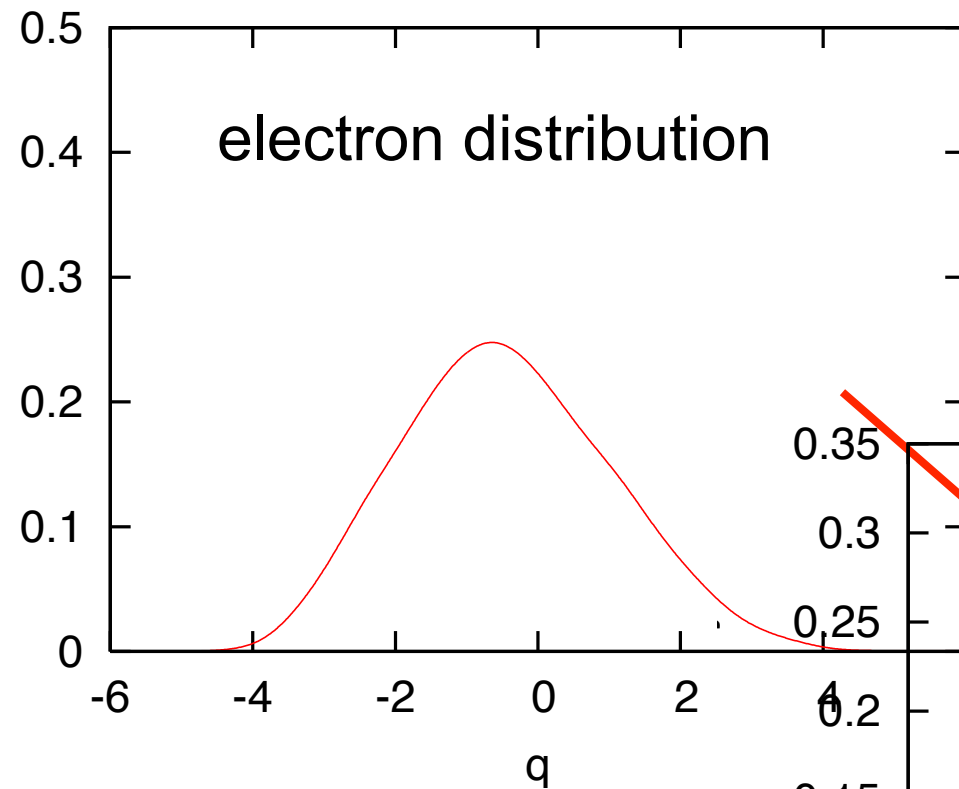
# The bursting stable threshold

- Measured bursting stable threshold with Si bolometer
- Good agreement with theoretical prediction:

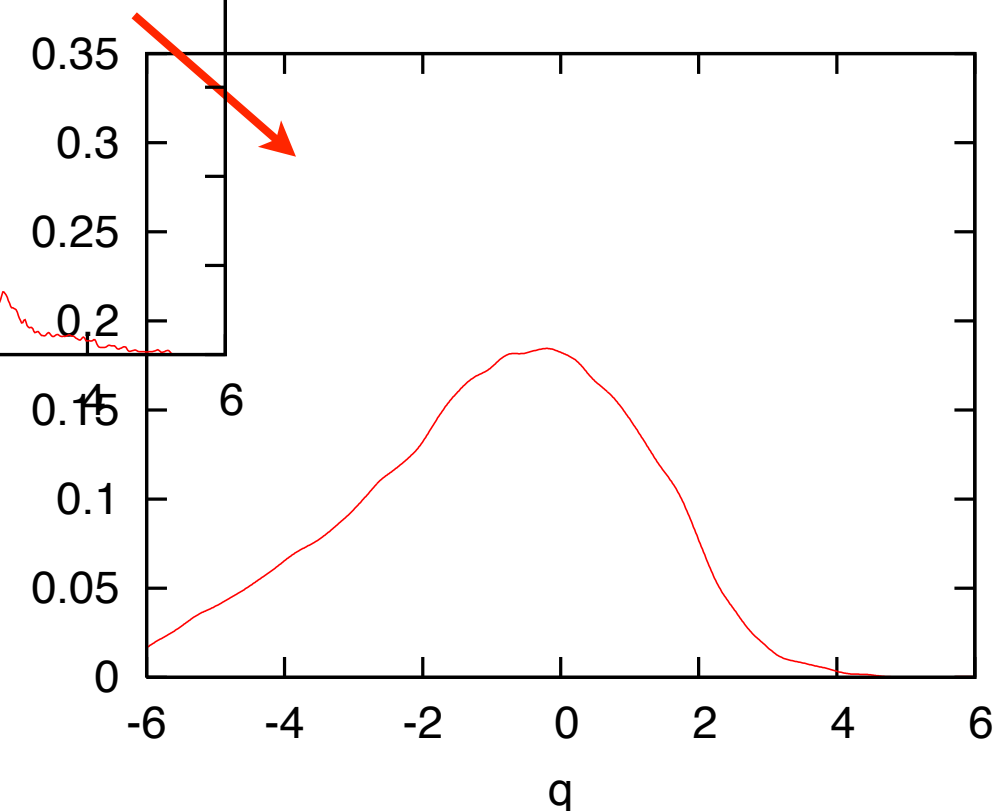
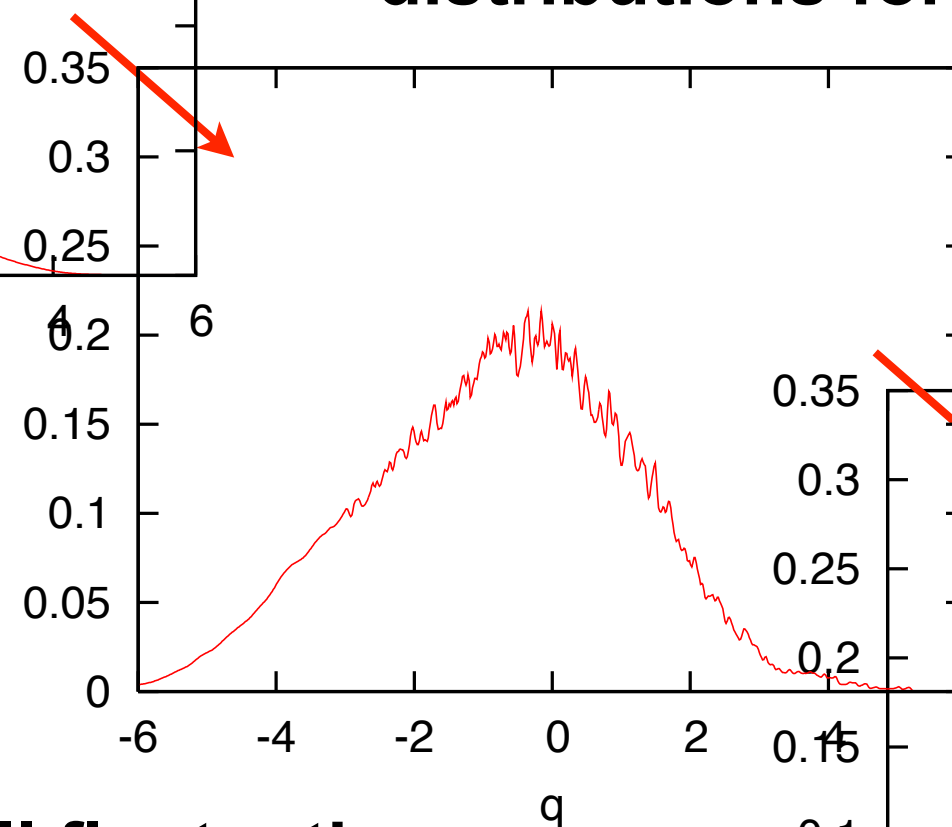


$$I_{threshold} \propto \sigma_s^{7/3}$$

# Microbunching



- Longitudinal dynamics described by the Vlasov-Focke-Planck equation
- A Vlasov solver calculates electron distributions for advancing time

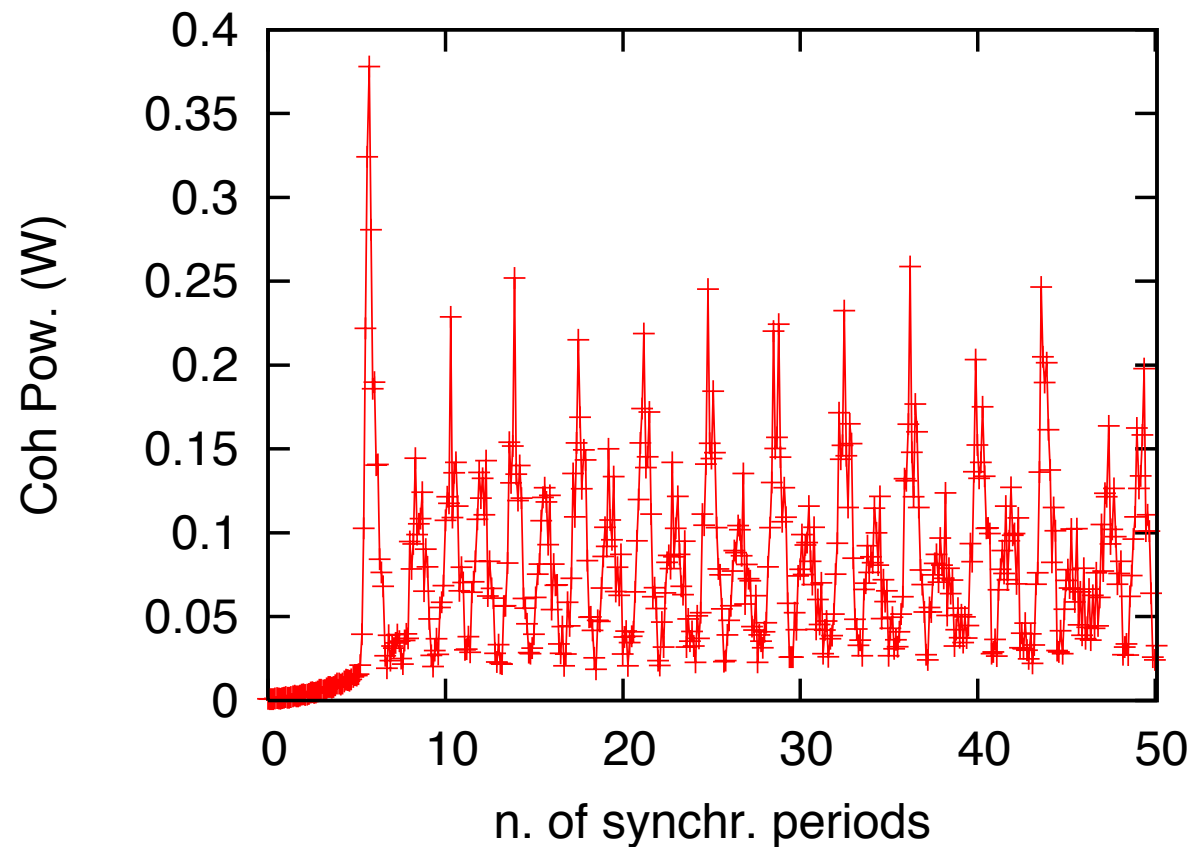


- In the beginning small fluctuations grow under the influence of self fields

## ▶ Microbunching



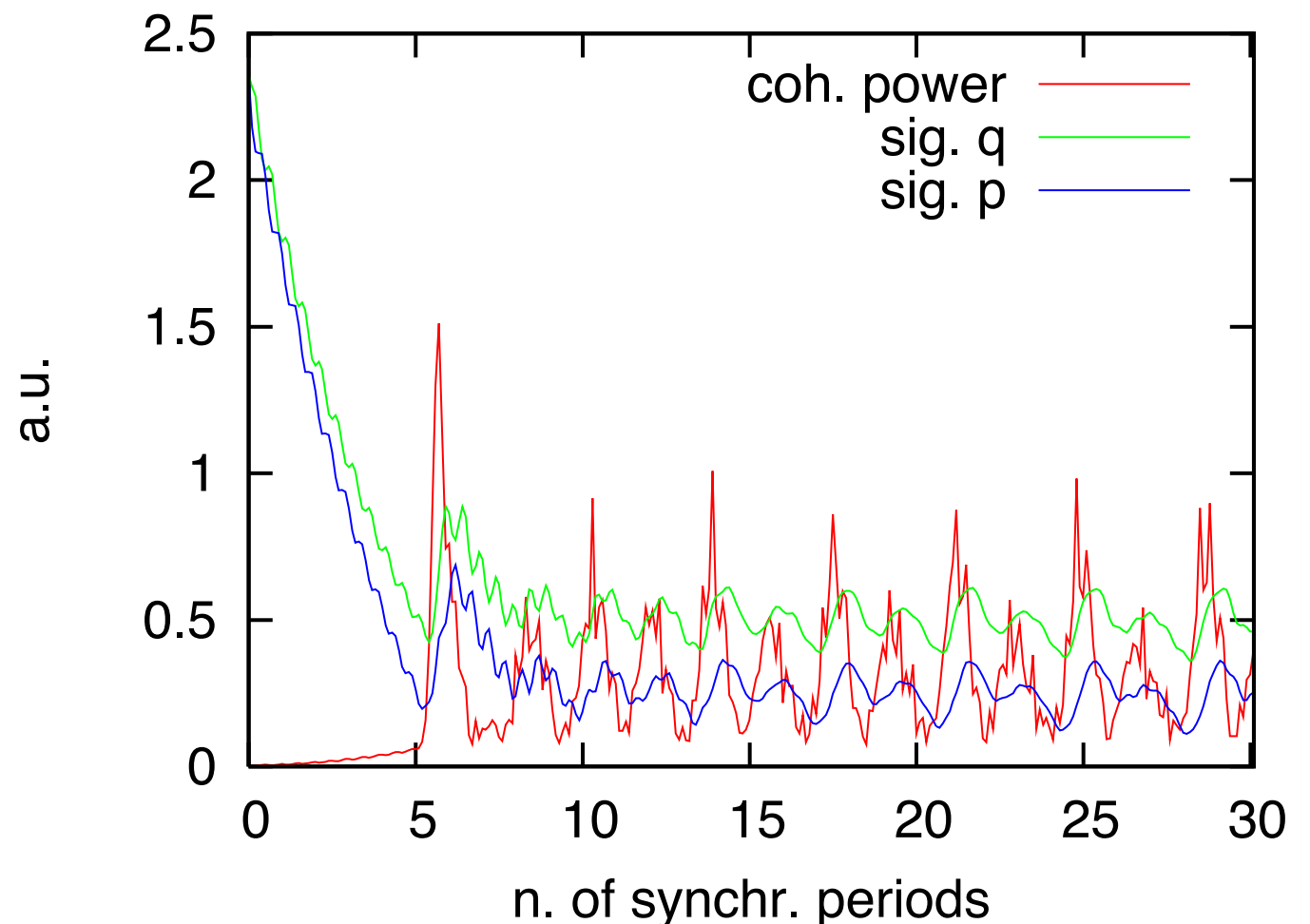
# Bursting behavior



- Microbunching is accompanied by coherent radiation bursts
- Bursts can have periodic or chaotic behavior

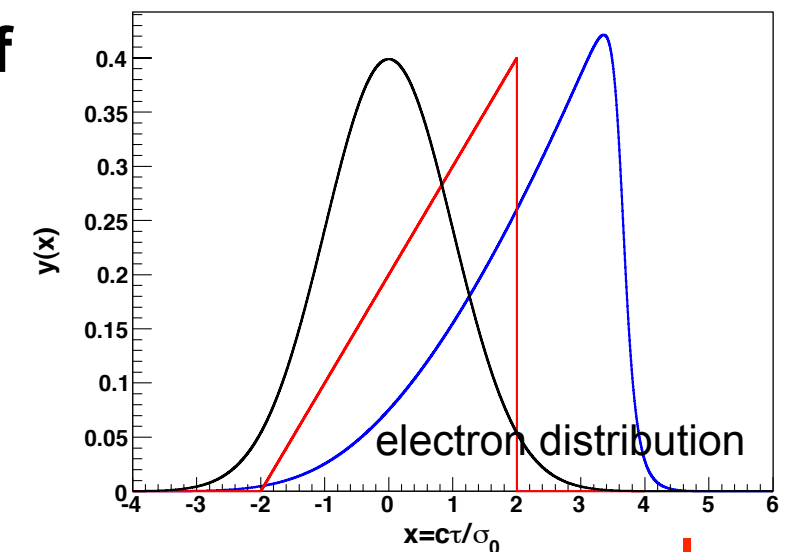
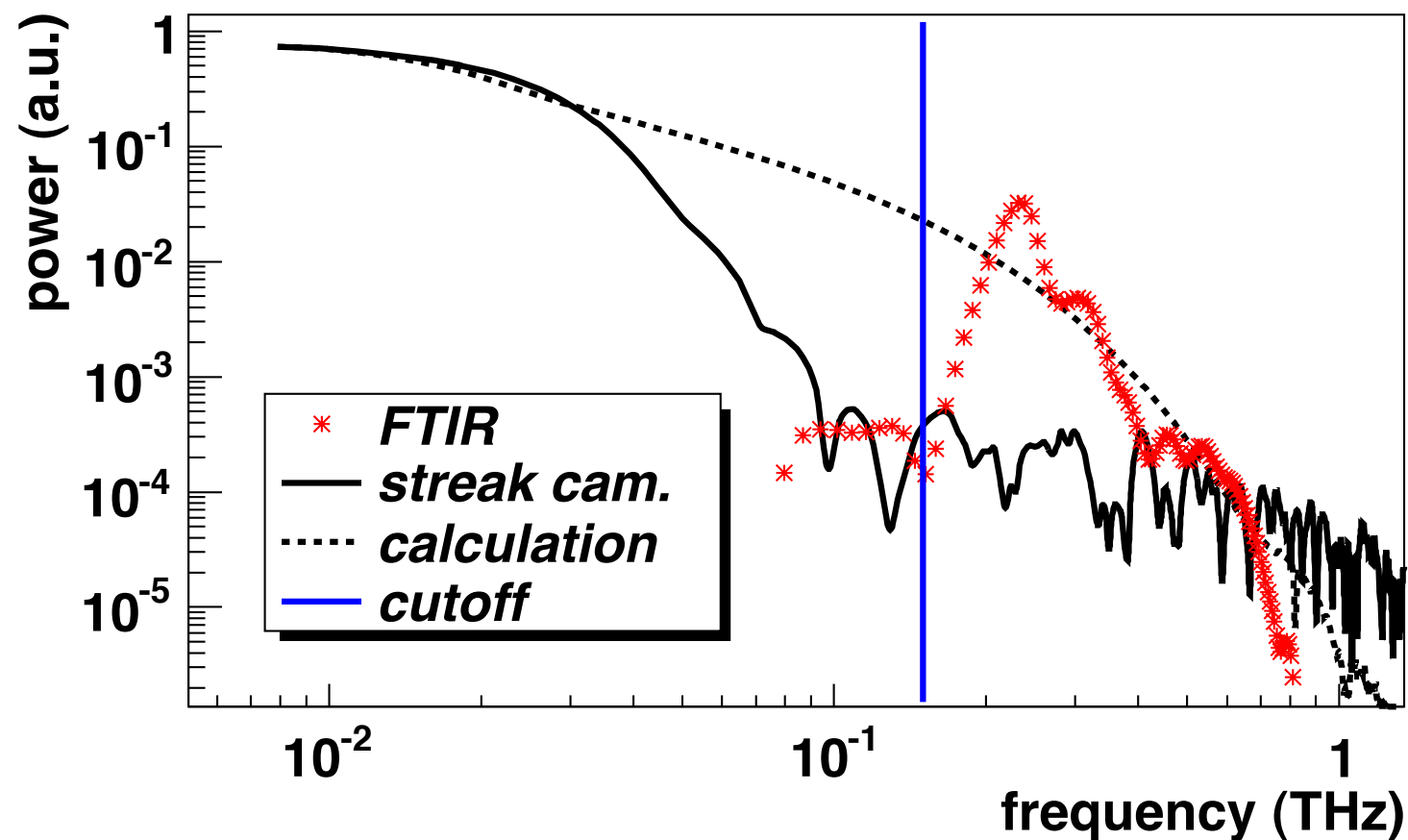
■ Phase space distribution (q,p) and bunch length varies during bursting cycle

▶ Vitali's talk

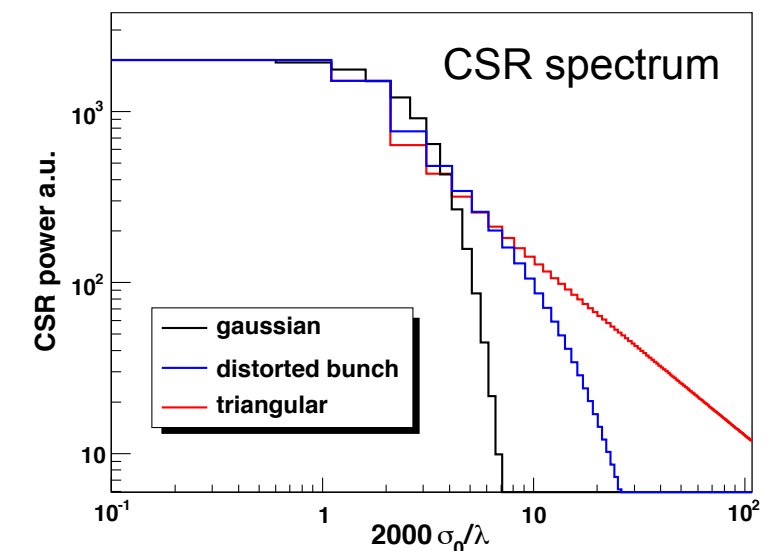


# Measured and Expected Spectra

- The CSR spectrum is the Fourier transform of the electron distribution
- Present Michelson interferometer: No information about low frequencies
  - ▶ Martin Puplett Interferometer
- Expectation from streak cam. measurement below cutoff
- Explanation: substructure or stronger deformation
  - ▶ Single shot measurement needed: **Nicole's talk**



FFT

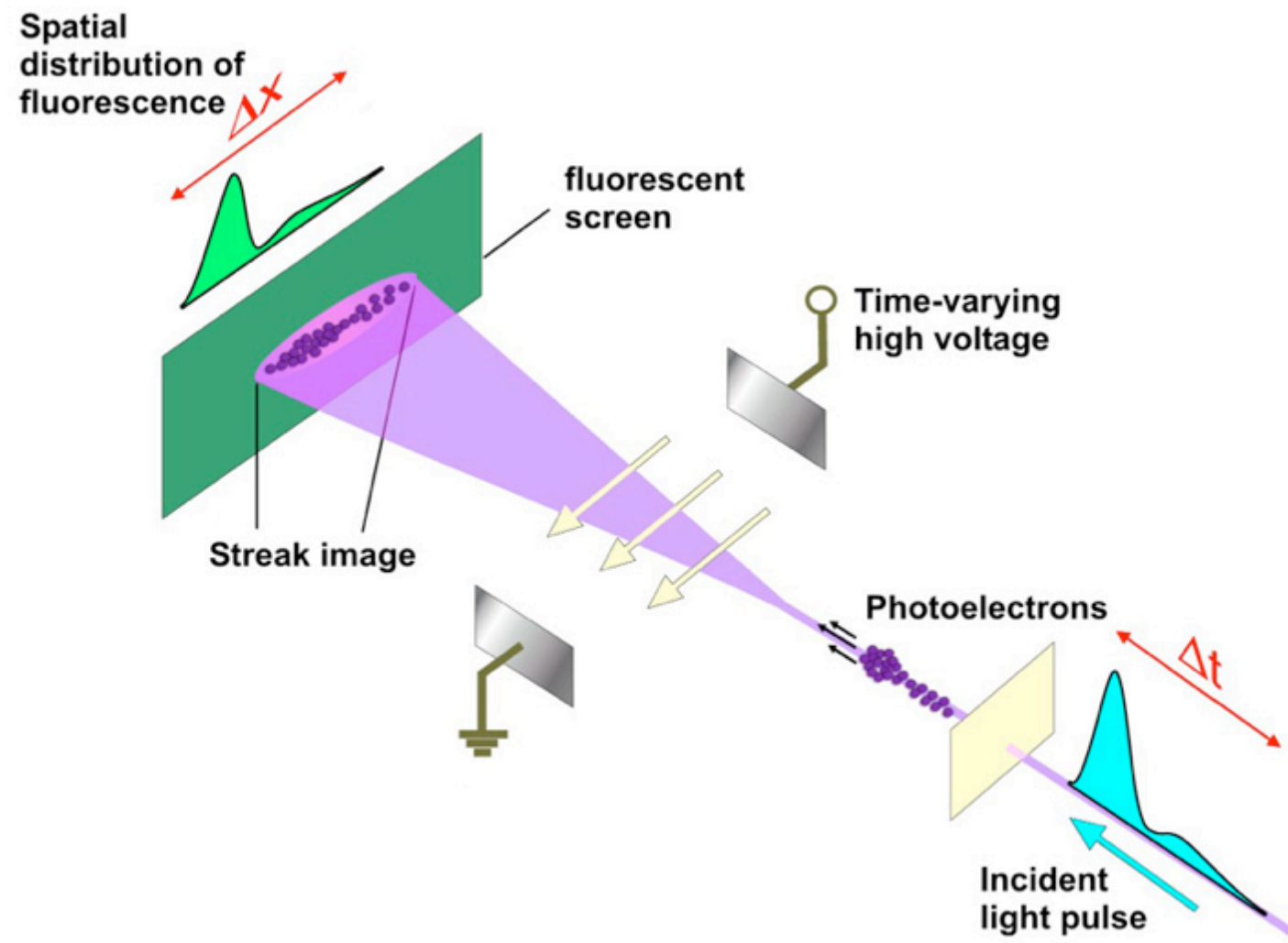


# Overview - Time domain bunch length & shape measurements

- Introduction
- Methods
  - Streak camera (currently in use)
  - Electro-optic techniques (will be implemented)
- Conclusion & outlook

# Streak camera - working principle

- Allows measurement of intensity distribution of visible synchrotron light pulses



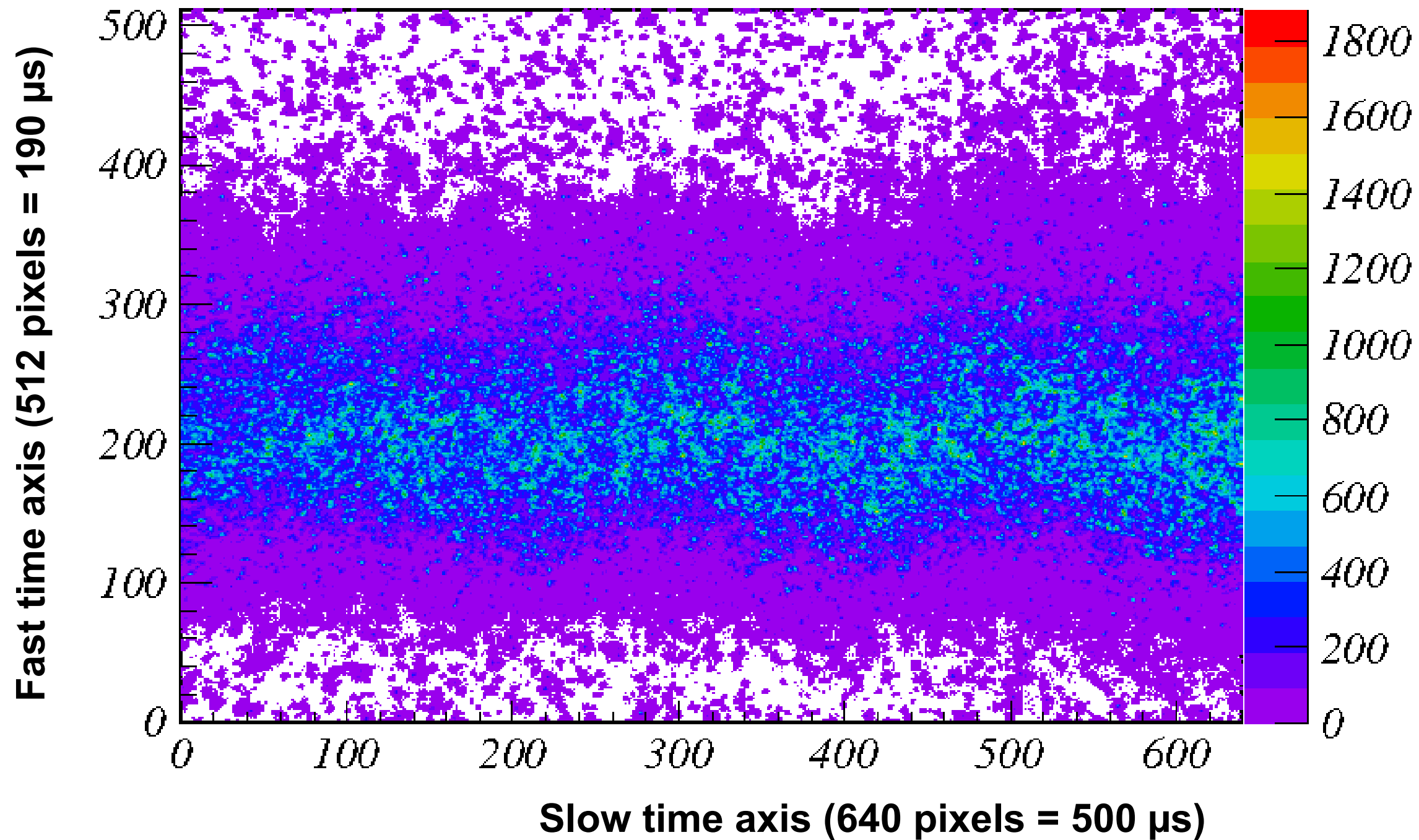
**electrons → photons → electrons → photons → averaging needed**

picture source: <http://www.mpg.de/>

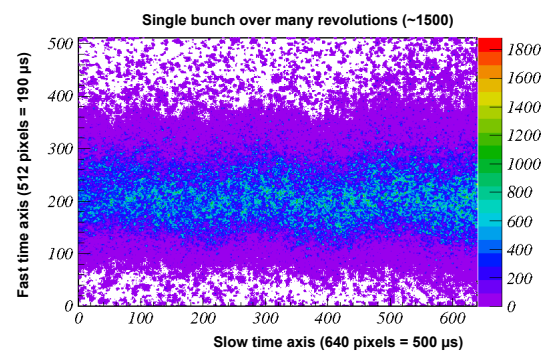


# Obtaining bunch profiles from SC images

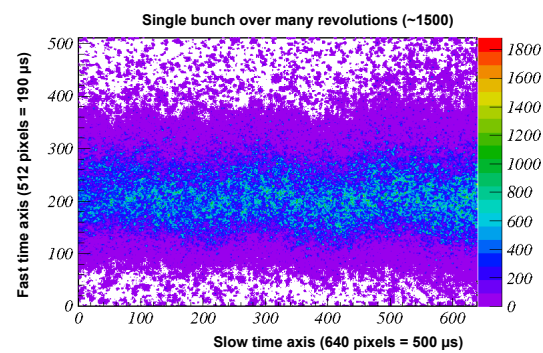
Single bunch over many revolutions (~1500)



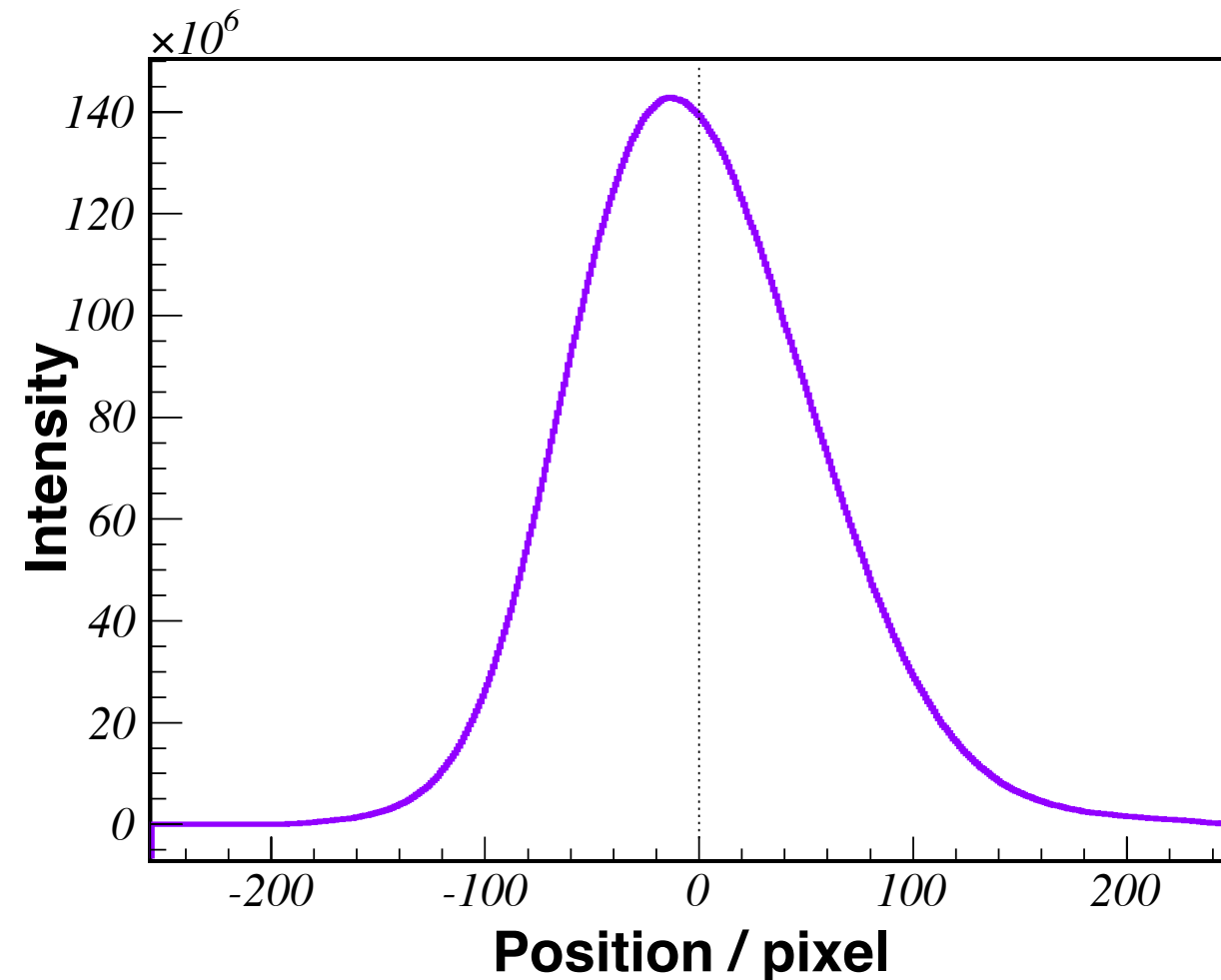
# Obtaining bunch profiles from SC images



# Obtaining bunch profiles from SC images

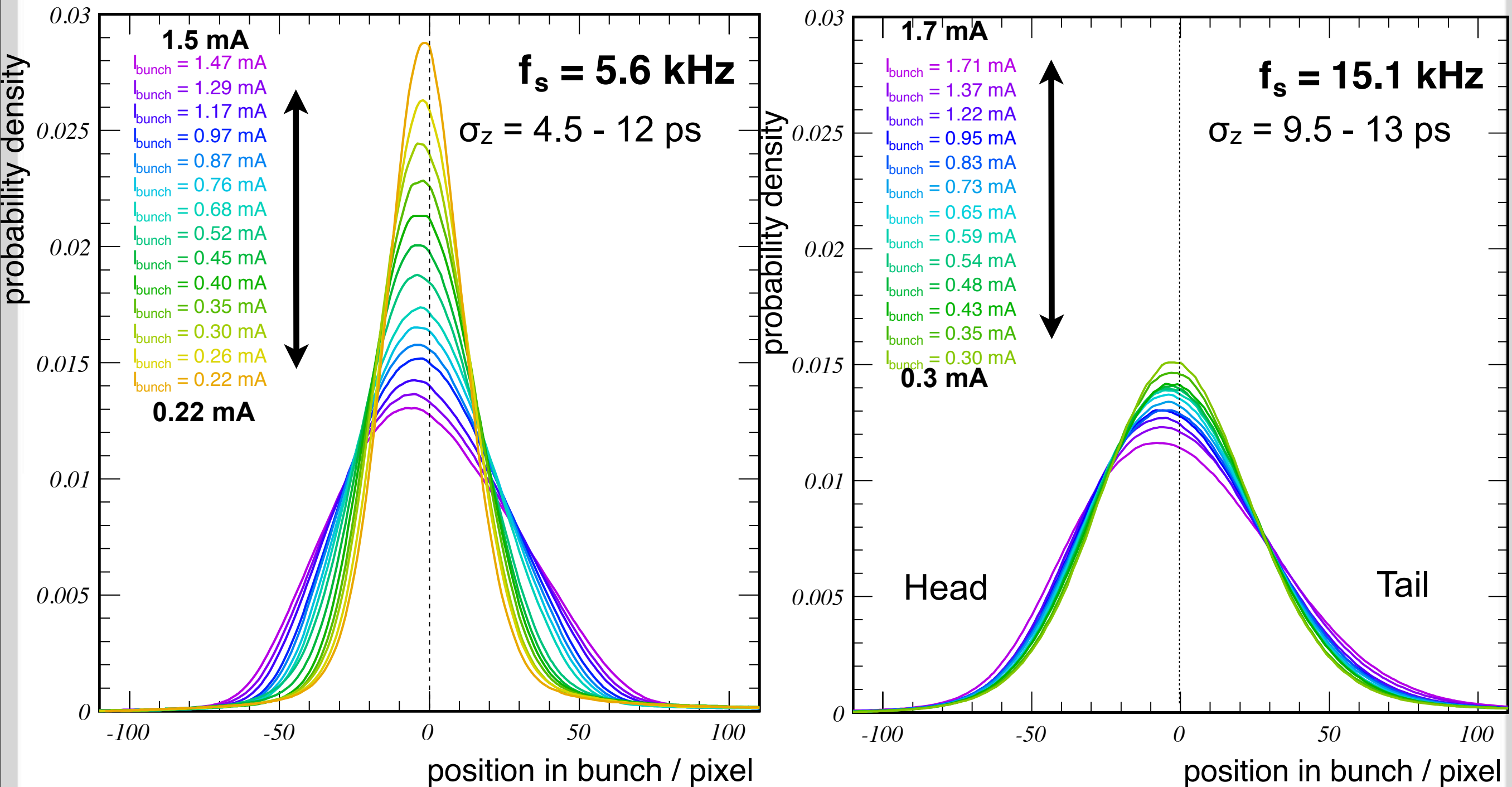


500 images



**Correct oscillation and project onto fast time axis**  
**→ smooth bunch profile**

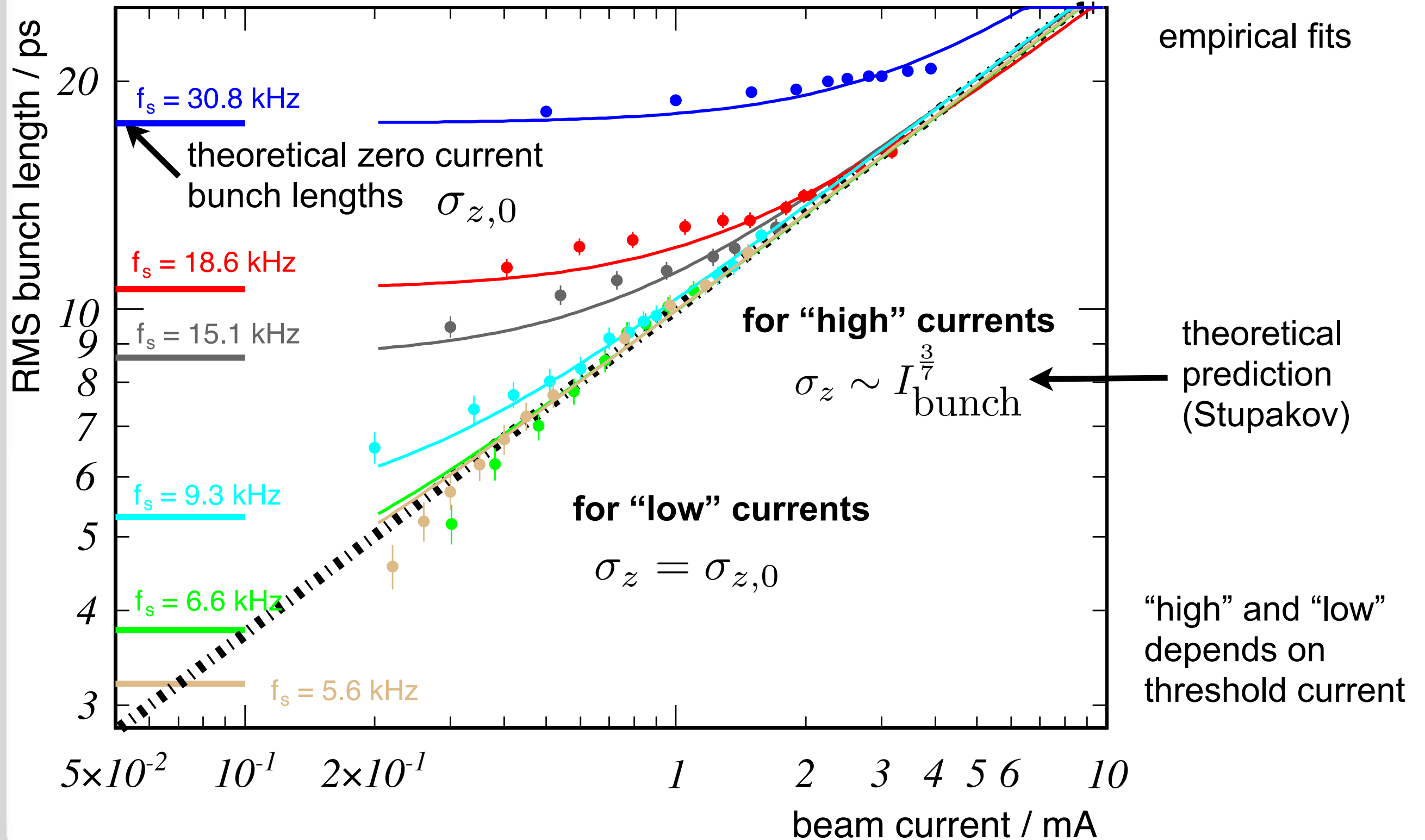
# Normalised bunch profiles for various bunch currents



**Problem: broadening due to SC resolution and jitter**

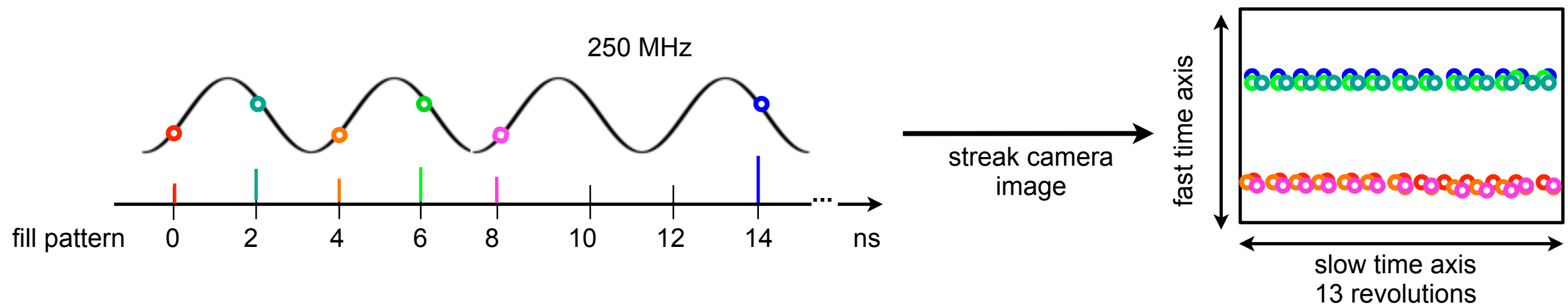


# Current dependent bunch lengthening



# Streak camera - limitations

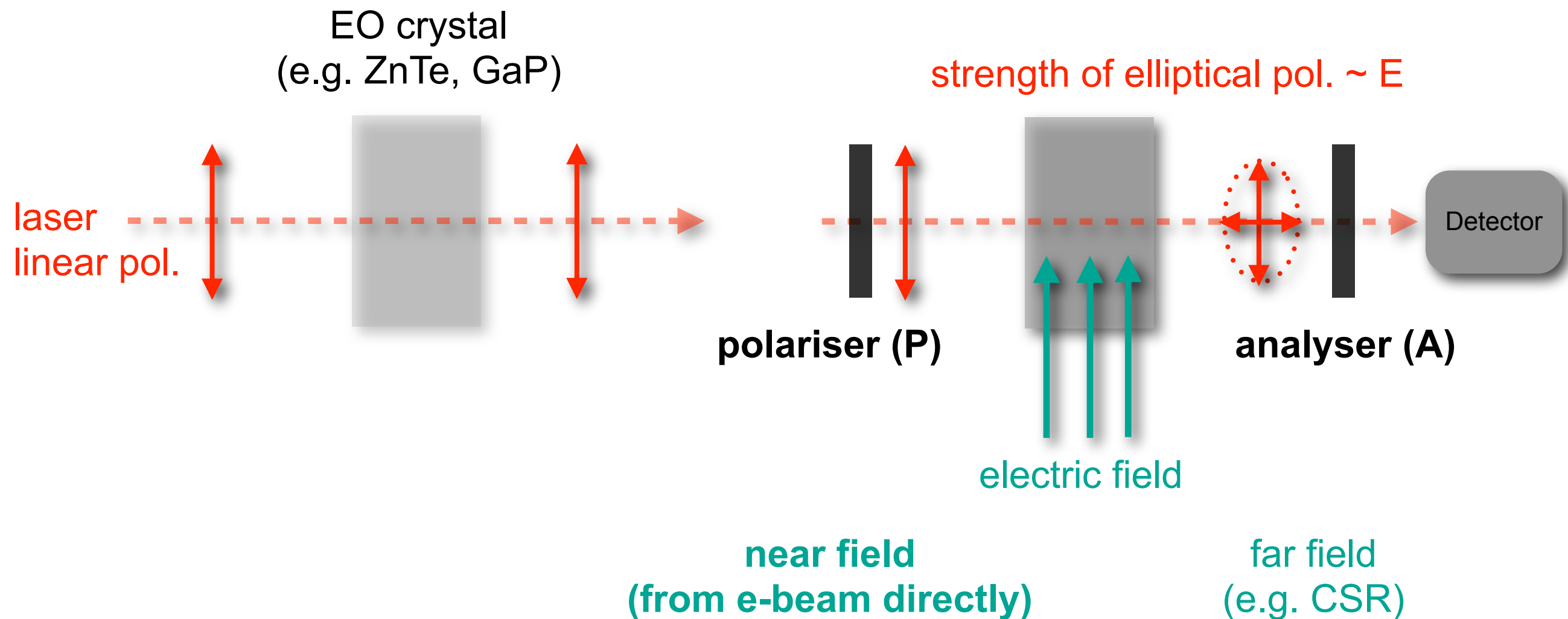
- **resolution:** 1 pixel  $\hat{=}$  0.4 ps further limited by:
  - slit opening
  - jitter on trigger signal
  - laser calibration measurements show:
    - measured pulse length will not go below **1.7 ps (rms)**
    - **value is quadratically subtracted from bunch length**
  
- can only separate bunches in odd and even RF buckets (for slow axis > 100 ns, 100-500  $\mu$ s needed for good signal) because fast sweep is controlled by a consecutive sinusoidal signal at  $f_{RF} / 2 = 250$  MHz



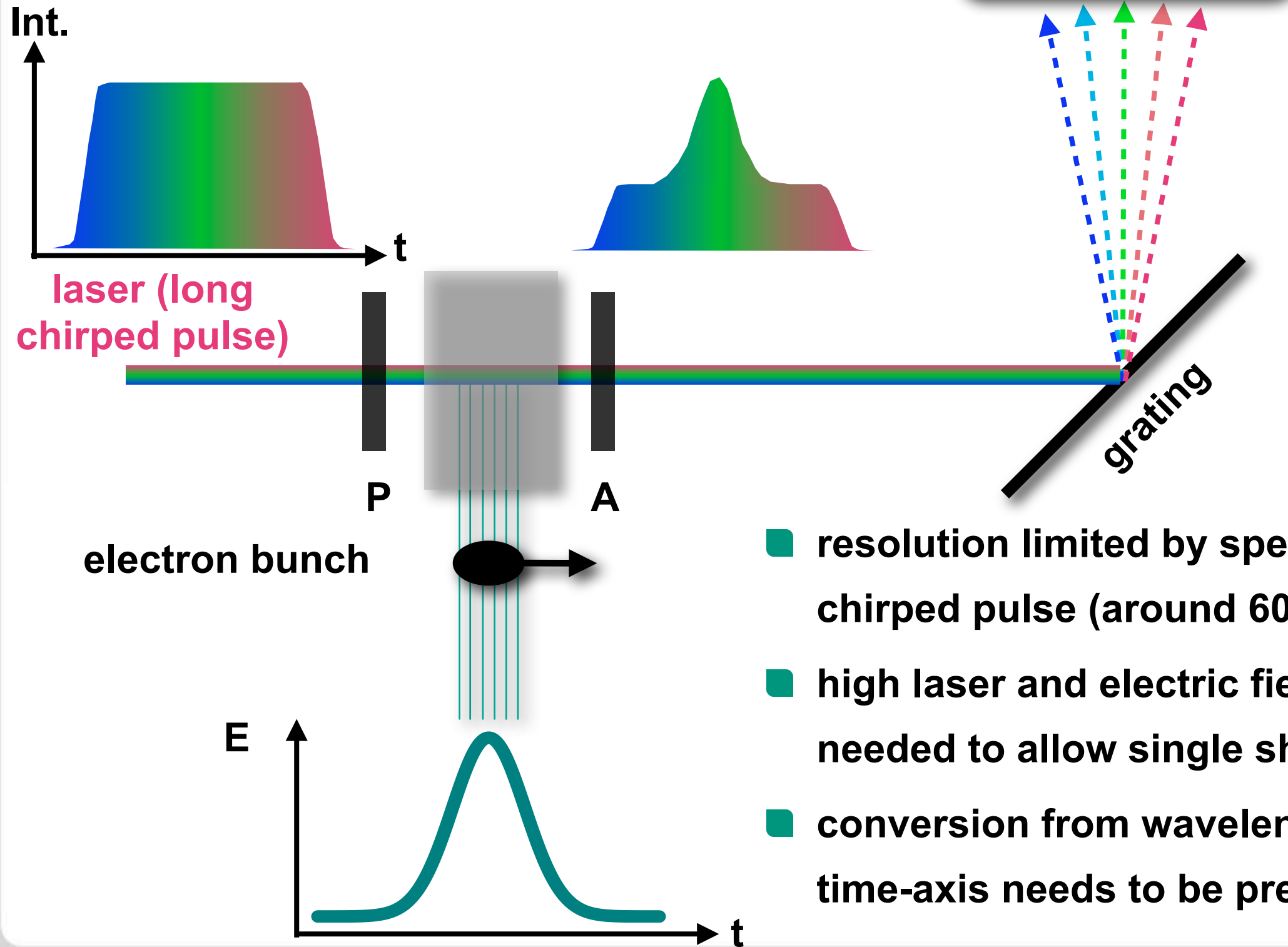
# Electro-optic techniques - working principle

Intensity distribution of electron bunch is modulated on laser pulse which is then analysed

## Modulation in electro-optic crystal:



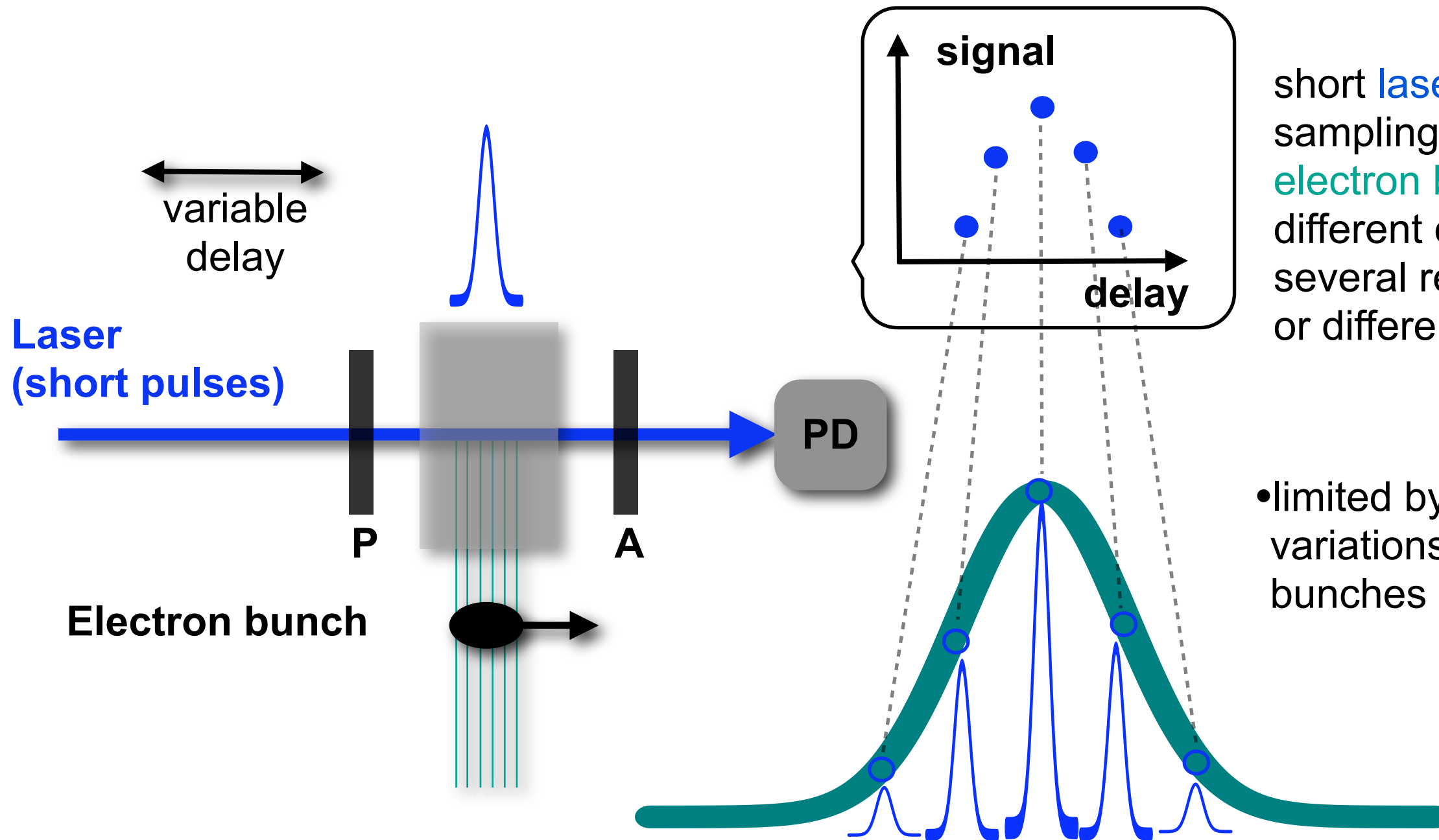
# Spectral decoding (single shot)



- resolution limited by spectral width of chirped pulse (around 60 - 100 nm)
- high laser and electric field intensities needed to allow single shot evaluation
- conversion from wavelength- to time-axis needs to be precise



# Electro-optical sampling (multi shot)



short laser pulses sampling the electron bunch at different delays over several revolutions / or different shots

- limited by ToA-variations of electron bunches

also possible to use “asynchronous sampling” for which the laser is slightly detuned from revolution frequency

# Conclusion & outlook

## ■ Streak camera

- results for bunch length in good agreement with theoretical predictions → better characterisation of the low alpha mode

- deconvolution of bunch shape not yet fully understood (work in progress)

- not properly usable for multi-bunch

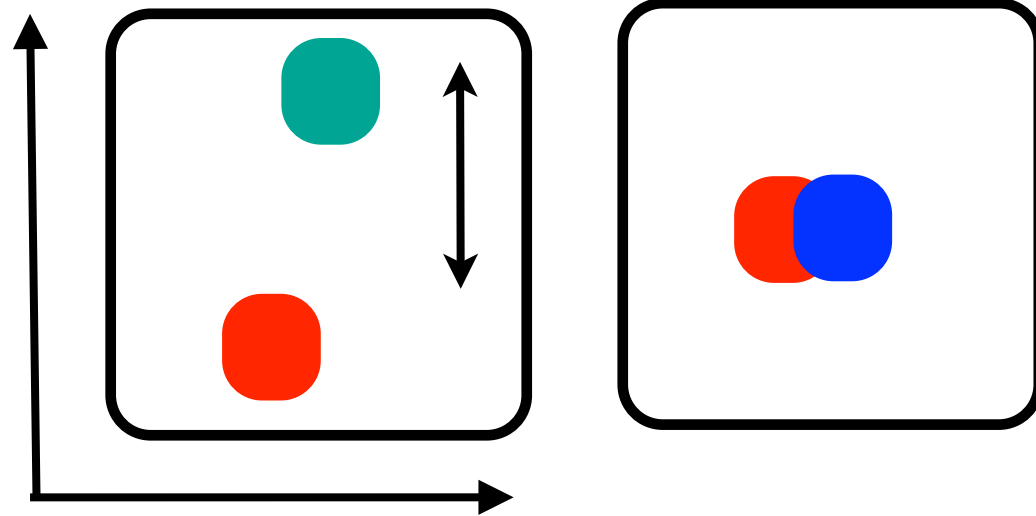
- **EO set up will allow single shot measurements and a better temporal resolution**

**Thank you for your attention!**

# Streak camera triggering

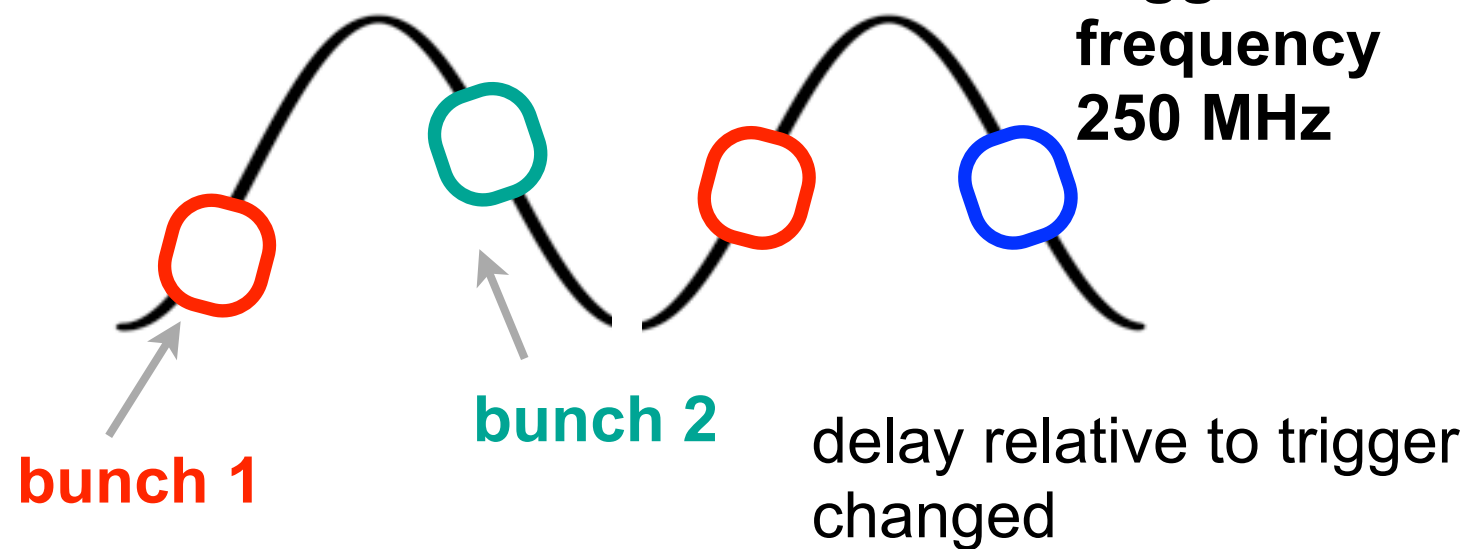
fast  
time axis

image on screen



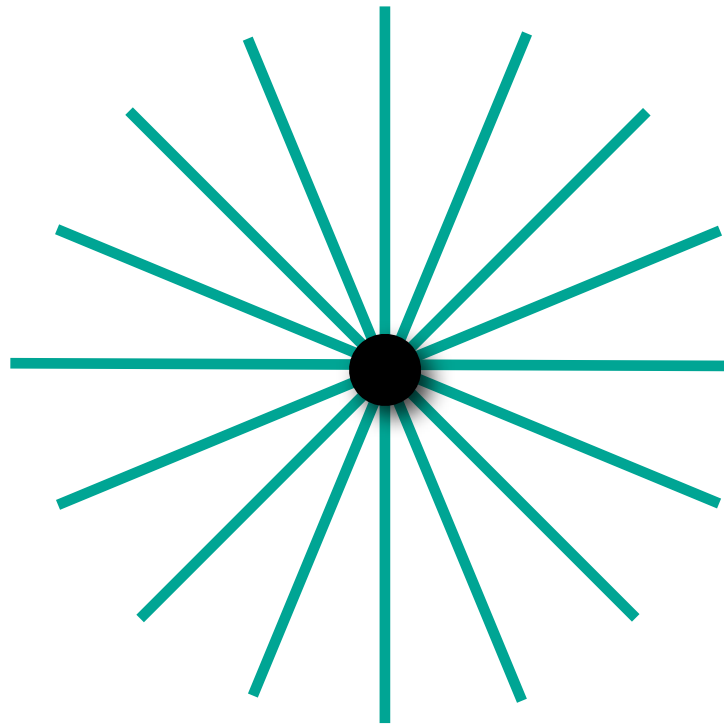
slow  
time axis

trigger  
frequency  
250 MHz



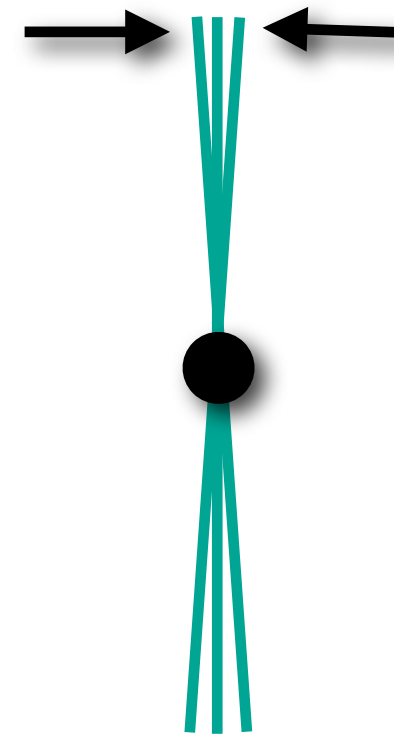
# Coulomb field

■ for a single electron



at rest

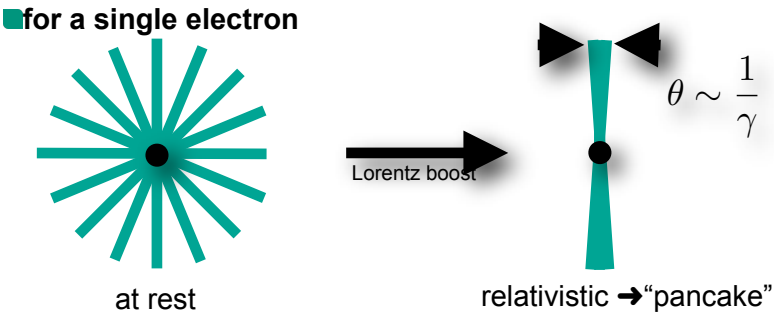
→  
Lorentz boost



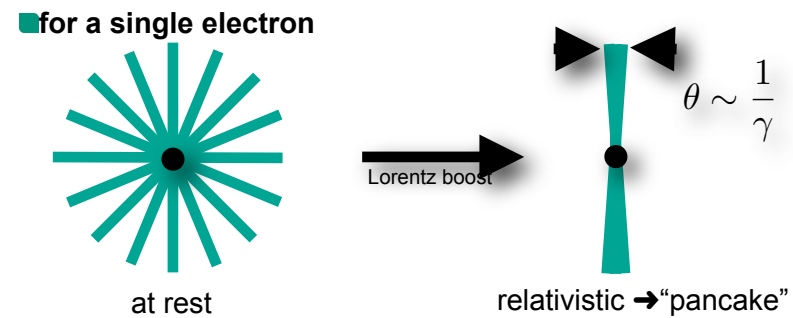
$$\theta \sim \frac{1}{\gamma}$$

relativistic → “pancake”

# Coulomb field



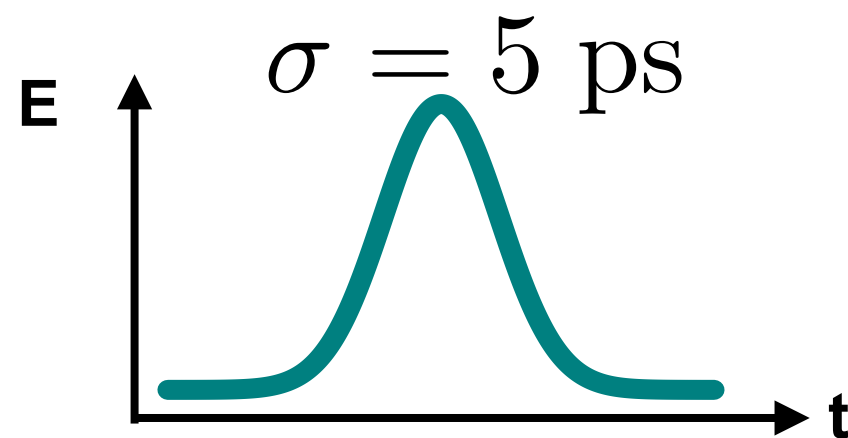




## ■ for a highly relativistic “long” ( $>1\text{ps}$ ) electron bunch

→  $E_{r,Q}(t) \sim Q(t)$  (every electron has their own really thin pancake; pancakes don't overlap)

→ Frequency components are given by Fourier transform



FFT

