

# 2HDM with Soft CP-violation: Future LHC Search

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- Based on our paper [Phys. Rev. D **102** (2020), 075029, arXiv: 2003.04178], in collaboration with Kingman Cheung, Adil Jueid, and Stefano Moretti.

## I. INTRODUCTION AND MOTIVATION

- CP-violation has been discovered in the meson sector.
- Besides this, there may also other effects: for example, electric dipole moments (EDM, low energy) or collider effects (LHC etc., high energy).
- CP-violation is also a necessary condition to explain the baryon asymmetry in the Universe: quantitatively not enough in the SM, [that's why we need new physics](#).
- Two-Higgs-Doublet Model (2HDM) is a widely studied new physics model which can induce new CP-violation sources, and here we choose it as an example to study its observable CP-violation effects: sensitive to future EDM tests, and [future LHC measurements will also provide complementary cross checks to the EDM tests](#).

## II. THE MODEL AND CONSTRAINTS

We consider the 2HDM with soft  $Z_2$ -symmetry to avoid terrible FCNC

- Mainly following the conventions in [A. Arhrib *et al.*, JHEP **04** (2011), 089; etc].

$$\mathcal{L} = |D\phi_1|^2 + |D\phi_2|^2 - V(\phi_1, \phi_2).$$

- Potential with a soft broken  $Z_2$ -symmetry ( $\phi_1 \rightarrow \phi_1, \phi_2 \rightarrow -\phi_2$ ):

$$\begin{aligned} V(\phi_1, \phi_2) = & -\frac{1}{2} \left[ m_1^2 \phi_1^\dagger \phi_1 + m_2^2 \phi_2^\dagger \phi_2 + \left( m_{12}^2 \phi_1^\dagger \phi_2 + \text{H.c.} \right) \right] + \left[ \frac{\lambda_5}{2} \left( \phi_1^\dagger \phi_2 \right)^2 + \text{H.c.} \right] \\ & + \frac{1}{2} \left[ \lambda_1 \left( \phi_1^\dagger \phi_1 \right)^2 + \lambda_2 \left( \phi_2^\dagger \phi_2 \right)^2 \right] + \lambda_3 \left( \phi_1^\dagger \phi_1 \right) \left( \phi_2^\dagger \phi_2 \right) + \lambda_4 \left( \phi_1^\dagger \phi_2 \right) \left( \phi_2^\dagger \phi_1 \right) \end{aligned}$$

- Nonzero  $m_{12}^2$  will break the  $Z_2$  symmetry softly.
- Scalar doublets:  $\phi_1 \equiv (\varphi_1^+, (v_1 + \eta_1 + i\chi_1)/\sqrt{2})^T$ ,  $\phi_2 \equiv (\varphi_2^+, (v_2 + \eta_2 + i\chi_2)/\sqrt{2})^T$ .

- Here  $m_{1,2}^2$  and  $\lambda_{1,2,3,4}$  must be real, while  $m_{12}^2$  and  $\lambda_5$  can be **complex**  $\rightarrow$  **CP-violation**.
- The vacuum expected value (VEV) for the scalar fields:  $\langle\phi_1\rangle \equiv (0, v_1)^T/\sqrt{2}$ ,  $\langle\phi_2\rangle \equiv (0, v_2)^T/\sqrt{2}$ , and we denote  $t_\beta \equiv |v_2/v_1|$ .
- $m_{12}^2$ ,  $\lambda_5$ , and  $v_2/v_1$  can all be complex, but we can always perform a rotation to keep at least one of them real, thus we choose  $v_2/v_1$  real.
- A relation:  $\text{Im}(m_{12}^2) = v_1 v_2 \text{Im}(\lambda_5)$ .
- Diagonalization: (a) Charged Sector

$$G^\pm = c_\beta \varphi_1^\pm + s_\beta \varphi_2^\pm, \quad H^\pm = -s_\beta \varphi_1^\pm + c_\beta \varphi_2^\pm.$$

- Diagonalization: (b) Neutral Sector

$$G^0 = c_\beta \chi_1 + s_\beta \chi_2, \quad A = -s_\beta \chi_1 + c_\beta \chi_2.$$

- For the CP-conserving case,  $A$  is a CP-odd mass eigenstate.
- For CP-violation case,  $(H_1, H_2, H_3)^T = R(\eta_1, \eta_2, A)^T$ , with

$$R = \begin{pmatrix} 1 & & & \\ & c_{\alpha_3} & s_{\alpha_3} & \\ & -s_{\alpha_3} & c_{\alpha_3} & \\ & & & 1 \end{pmatrix} \begin{pmatrix} c_{\alpha_2} & s_{\alpha_2} & & \\ & 1 & & \\ -s_{\alpha_2} & c_{\alpha_2} & & \\ & & & 1 \end{pmatrix} \begin{pmatrix} c_{\beta+\alpha_1} & s_{\beta+\alpha_1} & & \\ -s_{\beta+\alpha_1} & c_{\beta+\alpha_1} & & \\ & & & 1 \end{pmatrix}.$$

- SM limit:  $\alpha_{1,2} \rightarrow 0$ .
- Mixing angle  $\alpha_2$  is the key parameter which measures the CP-violation effects in the 125 GeV Higgs boson (denoted as  $H_1$  here, whose properties are SM-like).

- Parameter Set (8):  $(m_1, m_2, m_{\pm}, \beta, \alpha_1, \alpha_2, \alpha_3, \text{Re}(m_{12}^2))$ .

- Relation:

$$m_3^2 = \frac{c_{\alpha_1+2\beta}(m_1^2 - m_2^2 s_{\alpha_3}^2)/c_{\alpha_3}^2 - m_2^2 s_{\alpha_1+2\beta} t_{\alpha_3}}{c_{\alpha_1+2\beta} s_{\alpha_2} - s_{\alpha_1+2\beta} t_{\alpha_3}}$$

or equivalently

$$t_{\alpha_3} = \frac{(m_3^2 - m_2^2) \pm \sqrt{(m_3^2 - m_2^2)^2 s_{2\beta+\alpha_1}^2 - 4(m_3^2 - m_1^2)(m_2^2 - m_1^2) s_{\alpha_2}^2 c_{2\beta+\alpha_1}^2}}{2(m_2^2 - m_1^2) s_{\alpha_2} c_{2\beta+\alpha_1}}.$$

- Useful for different scenarios: mass-splitting scenario or nearly mass-degenerate scenario for the two heavy scalars  $H_{2,3}$ ; in this talk we only discuss the phenomenology for nearly mass-degenerate scenario for simplify.

## Yukawa Couplings:

- Three types of interaction:  $\bar{Q}_L\phi_i d_R$ ,  $\bar{Q}_L\tilde{\phi}_i u_R$ ,  $\bar{L}_L\phi_i\ell_R$ , with  $\tilde{\phi}_i \equiv i\sigma_2\phi_i^*$ .
- The  $Z_2$  symmetry is helpful to avoid the FCNC problem, and with this symmetry, each kind of the above bilinear can couple only to one scalar doublet.
- Four different types (I, II, III, IV)

$Z_2$ Number	$\phi_1$	$\phi_2$	$Q_L$	$u_R$	$d_R$	$L_L$	$\ell_R$	$Z, \gamma, W$	Coupling	$\bar{u}_i u_i$	$\bar{d}_i d_i$	$\bar{l}_i l_i$
Type I	+	-	+	-	-	+	-	+	Type I	$\phi_2$	$\phi_2$	$\phi_2$
Type II	+	-	+	-	+	+	+	+	Type II	$\phi_2$	$\phi_1$	$\phi_1$
Type III	+	-	+	-	-	+	+	+	Type III	$\phi_2$	$\phi_2$	$\phi_1$
Type IV	+	-	+	-	+	+	-	+	Type IV	$\phi_2$	$\phi_1$	$\phi_2$

Useful interactions:

$$\mathcal{L} \supset \sum c_{V,i} H_i \left( \frac{2m_W^2}{v} W^+ W^- + \frac{m_Z^2}{v} Z Z \right) - \sum \left( \frac{m_f}{v} \right) (c_{f,i} H_i \bar{f}_L f_R + \text{H.c.})$$

$c_{V,1}$	$c_{V,2}$	$c_{V,3}$
$c_{\alpha_1} c_{\alpha_2}$	$-c_{\alpha_3} s_{\alpha_1} - c_{\alpha_1} s_{\alpha_2} s_{\alpha_3}$	$-c_{\alpha_1} c_{\alpha_3} s_{\alpha_2} + s_{\alpha_1} s_{\alpha_3}$

$c_{f,i} = R_{ij} c_{f,j}$  where  $j = \eta_1, \eta_2, A$

Type	$c_{u,\eta_1}$	$c_{u,\eta_2}$	$c_{u,A}$	$c_{d,\eta_1}$	$c_{d,\eta_2}$	$c_{d,A}$	$c_{\ell,\eta_1}$	$c_{\ell,\eta_2}$	$c_{\ell,A}$
I	0	$s_\beta^{-1}$	$-it_\beta^{-1}$	0	$s_\beta^{-1}$	$it_\beta^{-1}$	0	$s_\beta^{-1}$	$it_\beta^{-1}$
II	0	$s_\beta^{-1}$	$-it_\beta^{-1}$	$c_\beta^{-1}$	0	$-it_\beta$	$c_\beta^{-1}$	0	$-it_\beta$
III	0	$s_\beta^{-1}$	$-it_\beta^{-1}$	0	$s_\beta^{-1}$	$it_\beta^{-1}$	$c_\beta^{-1}$	0	$-it_\beta$
IV	0	$s_\beta^{-1}$	$-it_\beta^{-1}$	$c_\beta^{-1}$	0	$-it_\beta$	0	$s_\beta^{-1}$	$it_\beta^{-1}$



Constraints from low- and high-energy experiments:

- Electron EDM sets very strict constraints, but in Type II and III models, a cancellation between different contributions to EDM leads to the result that large  $|\alpha_2| \sim \mathcal{O}(0.1)$  is still allowed [see Refs. S. Inoue *et al.*, Phys. Rev. D **89**, 115023 (2014); Y.-N. Mao and S.-H. Zhu, Phys. Rev. D **90**, 115024 (2014); L. Bian *et al.*, Phys. Rev. Lett. **115**, 021801 (2015); L. Bian and N. Chen, Phys. Rev. D **95**, 115029 (2017); etc.]
- Type II model:  $|\alpha_2| \lesssim 0.1$  due to neutron EDM test.
- Type III model:  $|\alpha_2| \lesssim 0.3$  due to global fit for Higgs signal strengths.
- $m_{2,3} \gtrsim 700$  GeV is favored and  $\beta$  depends weakly on heavy scalars mass in cancellation scenario, thus for  $m_{2,3} \sim 700$  GeV,  $\beta \simeq 0.79$ ; small  $\alpha_1$  is favored and  $\alpha_3$  is free in a very large region  $\sim (0.3 - 1.1)$  for the nearly mass-degenerate scenario.

### III. BENCHMARK POINTS

We choose the benchmark points based on the following reasons:

- Fix  $m_2 = 700$  GeV satisfying the constraints on charged Higgs  $m_{\pm} > 800$  GeV [M. Misiak *et al.*, JHEP **06** (2020), 175], and thus  $\beta = 0.79$ ;
- For the key parameter  $\alpha_2$ , take its largest allowed number (0.1 for Type II and 0.3 for Type III) for both models to obtain largest CP-violation effects.
- We choose  $\alpha_1 = 0.02$  at its best-fit point and  $\alpha_3 = 0.8$  as a central value, and choose  $\mu^2 \equiv \text{Re}(m_{12}^2)/s_{2\beta} = (450 \text{ GeV})^2$  near its largest value due to vacuum stability: CP-violation effects are not sensitive to the values of these parameters;
- Last, calculate  $m_3$  from other parameters.

Summary on the benchmark points and derived couplings:

TABLE I: Benchmark Points for Two-Higgs-doublet Models with Soft CP-violation.

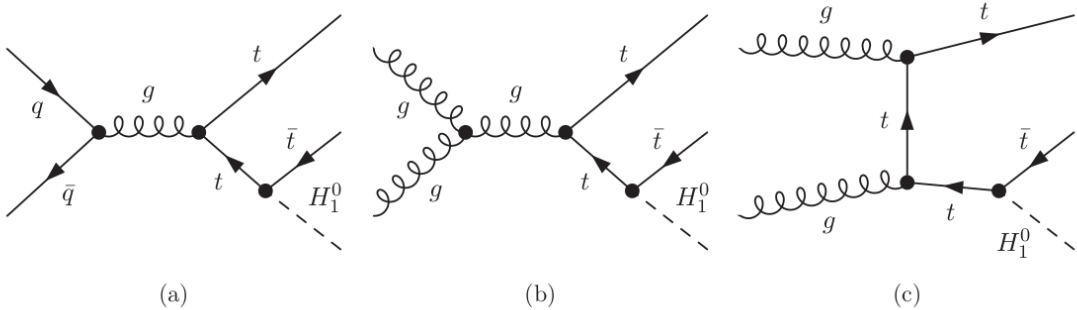
	$m_1$	$m_2$	$m_3$	$m_{\pm}$	$\beta$	$\alpha_1$	$\alpha_2$	$\alpha_3$	$\mu^2 \equiv \text{Re}(m_{12}^2)/s_{2\beta}$
Type II (BP1)	125 GeV	700 GeV	699 GeV	800 GeV	0.79	0.02	0.1	0.8	$(450 \text{ GeV})^2$
Type III (BP2)	125 GeV	700 GeV	696 GeV	800 GeV	0.79	0.02	0.3	0.8	$(450 \text{ GeV})^2$

TABLE II: Couplings derived from the benchmark points in Table I.

	$c_{t,1}$	$c_{t,2}$	$c_{t,3}$	$c_{V,1}$	$c_{V,2}$	$c_{V,3}$
Type II (BP1)	$1.01 - 0.099i$	$0.603 - 0.707i$	$-0.767 - 0.687i$	0.995	-0.086	-0.055
Type III (BP2)	$0.974 - 0.293i$	$0.460 - 0.679i$	$-0.906 - 0.659i$	0.955	-0.226	-0.192

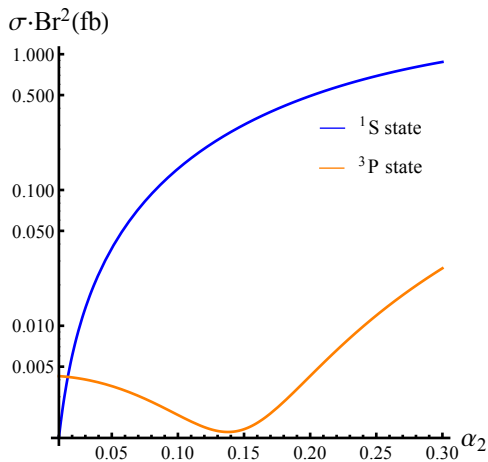
## IV. PHENOMENOLOGICAL STUDIES

Two examples: (A) Final state distribution for  $pp \rightarrow t\bar{t}H_1 \rightarrow \ell^+\ell^-\nu\bar{\nu} + 4b$



- $t\bar{t}H_1$  cross section can reach about 383 fb at  $\sqrt{s} = 13$  TeV LHC with  $p_T^H > 50$  GeV.
- A lot of CP-observables, and the best one is to study the azimuthal angle  $\Delta\phi$  between the two leptons from top quarks: its asymmetry  $\mathcal{A} \equiv \frac{N(\Delta\phi > \pi/2) - N(\Delta\phi < \pi/2)}{N(\Delta\phi > \pi/2) + N(\Delta\phi < \pi/2)}$  is sensitive to the CP-structure in  $t\bar{t}H_1$  coupling which is helpful to prob CP-violation.

(B) VBF channel:  $pp(VV) \rightarrow H_{2,3} \rightarrow t\bar{t}({}^1S) \rightarrow b\bar{b}\ell^+\ell^-\nu\bar{\nu}u$  (in preparation)



- The VBF vertex  $H_{2,3}VV$  must be CP-even at tree level, while the decay vertex  $t\bar{t}H_{2,3}$  must contain CP-odd component to form the  ${}^1S$  state, which can be measured through final state distribution.
- The discovery of  ${}^1S$  state  $t\bar{t}$  pair from VBF  $H_{2,3}$  resonance will be the signature of CP-violation.
- No interference with SM background due to CP analysis: behave as a perfect peak structure.
- Interference between  $H_{2,3}$  is important: peak cross section almost  $\propto [c_{V,2}\text{Im}(c_{t,2}) + c_{V,3}\text{Im}(c_{t,3})]^2 \sim s_{\alpha_2}^2$ , and  ${}^3P$  state almost disappears since  $c_{V,2}\text{Re}(c_{t,2}) + c_{V,3}\text{Re}(c_{t,3}) \ll 1$ .
- Cross sections for  ${}^1S$  and  ${}^3P$  states are shown in the upper plot, for the largest allowed  $\alpha_2 = 0.3$ ,  $\sigma_{VV \rightarrow H_{2,3} \rightarrow t\bar{t}({}^1S)} \times \text{Br}_{t \rightarrow b\ell\nu}^2$  can reach about **0.8 fb** for  $m_{2,3} \sim 700$  GeV.

## V. SUMMARY

- We chose the widely studied 2HDM with soft CP-violation to analyze its high- and low-energy constraints, and showed that a large CP-violation mixing angle  $\alpha_2 \simeq 0.1(0.3)$  is still allowed for Type II(III) model.
- We chose two processes to study the CP-violation effects at LHC: asymmetry of lepton azimuthal angle for  $pp \rightarrow t\bar{t}H_1 \rightarrow \ell^+\ell^-\nu\bar{\nu} + 4b$ , and the  $^1S$   $t\bar{t}$  state from VBF  $H_{2,3}$  resonance as the probe of CP-violation ([in preparation](#)).
- For the VBF process,  $^3P$  state is negligible and  $^1S$  state will not interfere with SM background,  $\sigma_{1S} \times \text{Br}_{t \rightarrow b\ell\nu}^2$  can reach about 0.8 fb for the largest allowed CP-violation angle  $\alpha_2 = 0.3$ , and the spin-correlation can be probed through final state distribution.



The end,  
thank you!

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