

[arXiv:2104.03184]
under submission to JHEP

Impact of NLO corrections to the Higgs boson invisible decay in N2HDM

Kodai Sakurai (Tohoku U.)

Collaborators:

Duarte Azevedo ^A, Pedro Gabriel ^A, Margarete Mühlleitner ^B, Rui Santos ^{A,C}
(^A: Lisbon U., ^B: KIT, ^C: ISEL)

Introduction

- After the discovery of the Higgs boson at the LHC, its properties have been measured in detail.
 - Current data shows that discovered Higgs behaves SM-like.
 - Much parameter space is constrained for extended Higgs sectors.
 - Still we do not know much about the structure of the Higgs sector.
 - Numbers of Higgs fields, symmetries
 - Hierarchy problem
 - Relation with BSM phenomena
 - etc.
- We pursue a relation between Higgs sector and dark matter.

Dark matter searches

- Direct searches of dark matter (XENON1T, LUX, Panda X, DARWIN, etc.)
 - Scalar DM is searched by the spin independent cross section of DM-nuclei scattering.
 - Sensitive DM mass range: $\mathcal{O}(10)\text{GeV} \sim \mathcal{O}(1)\text{TeV}$
- Higgs boson invisible decay (LHC, HL-LHC, ILC, FCC, etc.) **This work**
 - In the SM, $H \rightarrow \text{inv.}$ happens through $H \rightarrow ZZ^*$, but the BR is very small.
 - $H \rightarrow \text{DM DM}$ contributes to this process, thus DM can be tested.
 - Sensitive DM mass range: $< m_h/2$

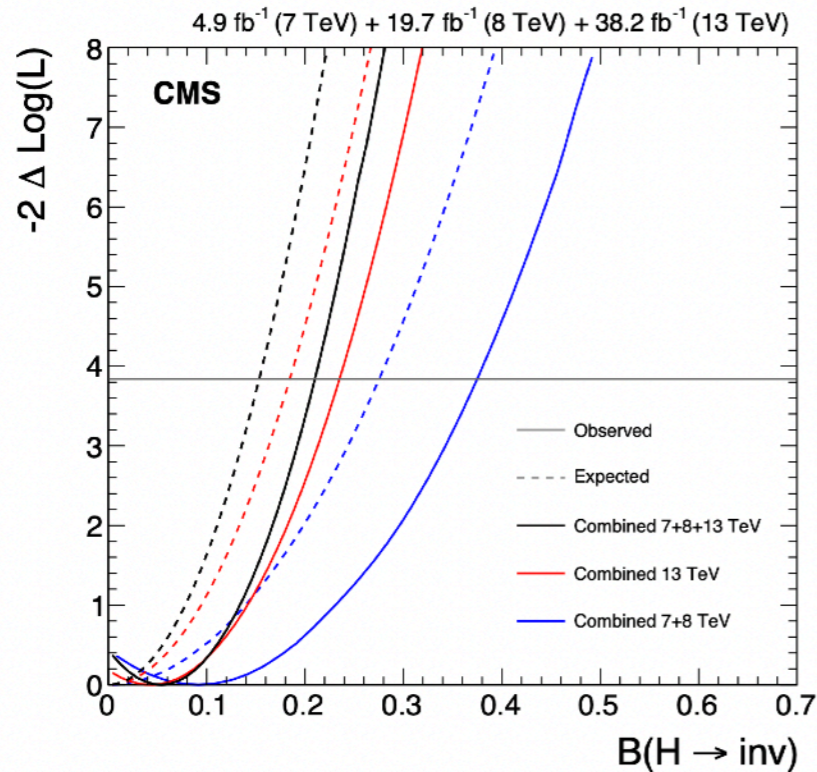
Higgs boson invisible decay

Recent results

Combined results of Run I and Run II at 95% CL.

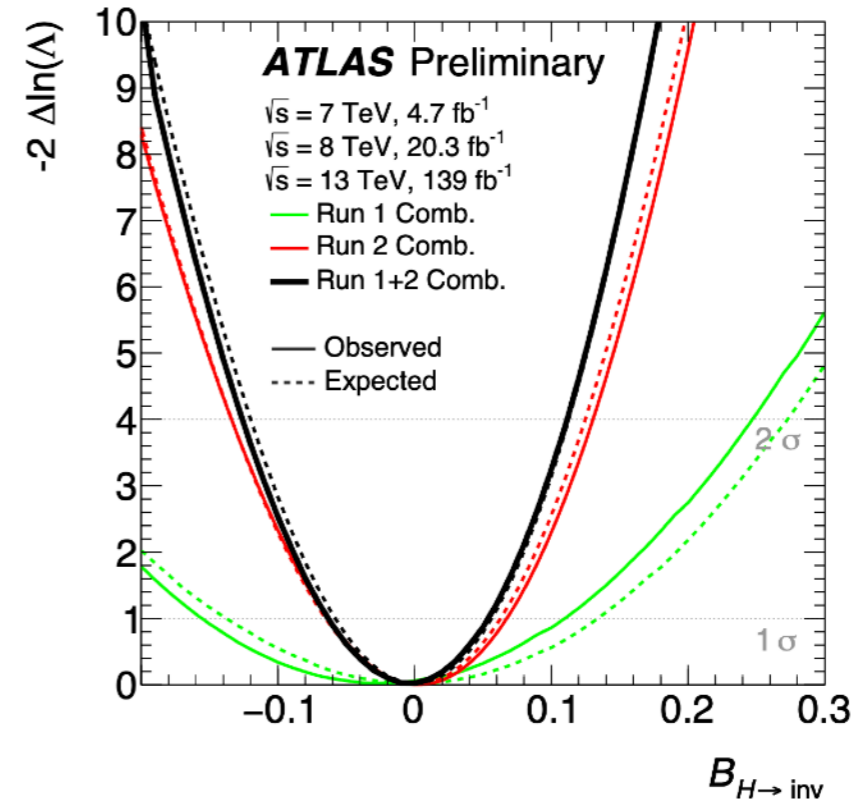
CMS: $BR_{inv.} < 0.19$

[CMS,PLB793, 520 (2019)]



ATLAS: $BR_{inv.} < 0.11$

[ATLAS-CONF-2020-052]



Future sensitivity

[J. de Blas et al., JHEP 01, 139 (2020)]

HL-LHC: $BR_{inv.} < 0.019$

ILC: $BR_{inv.} < 0.0026$

FCC: $BR_{inv.} < 0.00024$

Next-to two Higgs doublet model (N2HDM)

The Higgs potential is composed of scalar doublets Φ_1, Φ_2 and singlet Φ_S as

[I. Engeln, P. Ferreira, M. M. Muhlleitner, R. Santos, J. Wittbrodt, JHEP 08 (2020) 085]

$$\begin{aligned}
 V = & m_{11}^2 \Phi_1^\dagger \Phi_1 + m_{22}^2 \Phi_2^\dagger \Phi_2 + \frac{\lambda_1}{2} (\Phi_1^\dagger \Phi_1)^2 + \frac{\lambda_2}{2} (\Phi_2^\dagger \Phi_2)^2 \\
 & + \lambda_3 \Phi_1^\dagger \Phi_1 \Phi_2^\dagger \Phi_2 + \lambda_4 \Phi_1^\dagger \Phi_2 \Phi_2^\dagger \Phi_1 + \frac{\lambda_5}{2} \left[(\Phi_1^\dagger \Phi_2)^2 + \text{h.c.} \right] \\
 & + \frac{1}{2} m_s^2 \Phi_S^2 + \frac{\lambda_6}{8} \Phi_S^4 + \frac{\lambda_7}{2} \Phi_1^\dagger \Phi_1 \Phi_S^2 + \frac{\lambda_8}{2} \Phi_2^\dagger \Phi_2 \Phi_S^2,
 \end{aligned}$$

where Z_2 symmetries $Z_2^{(1)} \times Z_2^{(2)}$ are imposed:

$$Z_2^{(1)} : \Phi_1 \rightarrow \Phi_1, \quad \Phi_2 \rightarrow -\Phi_2, \quad \Phi_S \rightarrow \Phi_S,$$

$$Z_2^{(2)} : \Phi_1 \rightarrow \Phi_1, \quad \Phi_2 \rightarrow \Phi_2, \quad \Phi_S \rightarrow -\Phi_S.$$

There are four different minima that triggers $SU(2)_I \times U(1)_Y \rightarrow U(1)_{EM}$.

broken phase (BP): $\langle \Phi_1 \rangle \neq 0, \langle \Phi_2 \rangle \neq 0, \langle \Phi_S \rangle \neq 0,$ 2HDM+ HS HS: Higgs singlet

dark doublet phase (DDP): $\langle \Phi_1 \rangle \neq 0, \langle \Phi_2 \rangle = 0, \langle \Phi_S \rangle \neq 0,$ IDM+ HS DS: Dark singlet

dark singlet phase (DSP): $\langle \Phi_1 \rangle \neq 0, \langle \Phi_2 \rangle \neq 0, \langle \Phi_S \rangle = 0,$ 2HDM+ DS

full dark phase (FDP): $\langle \Phi_1 \rangle \neq 0, \langle \Phi_2 \rangle = 0, \langle \Phi_S \rangle = 0.$ IDM+ DS

Dark doublet phase (DDP)

In DDP, component fields can be defined by

$$\Phi_1 = \begin{pmatrix} G^+ \\ \frac{1}{\sqrt{2}}(v + \rho_1 + iG^0) \end{pmatrix}, \quad \Phi_2 = \begin{pmatrix} H_D^+ \\ \frac{1}{\sqrt{2}}(H_D + iA_D) \end{pmatrix}, \quad \Phi_S = v_s + \rho_s,$$

There are 6 physical states:

Dark scalars: H_D, A_D, H_D^\pm CP- even Higgs bosons : $\begin{pmatrix} H_1 \\ H_2 \end{pmatrix} = \begin{pmatrix} c_\alpha & s_\alpha \\ -s_\alpha & c_\alpha \end{pmatrix} \begin{pmatrix} \rho_1 \\ \rho_S \end{pmatrix}$

→ H_D (or A_D) can be DM candidate.

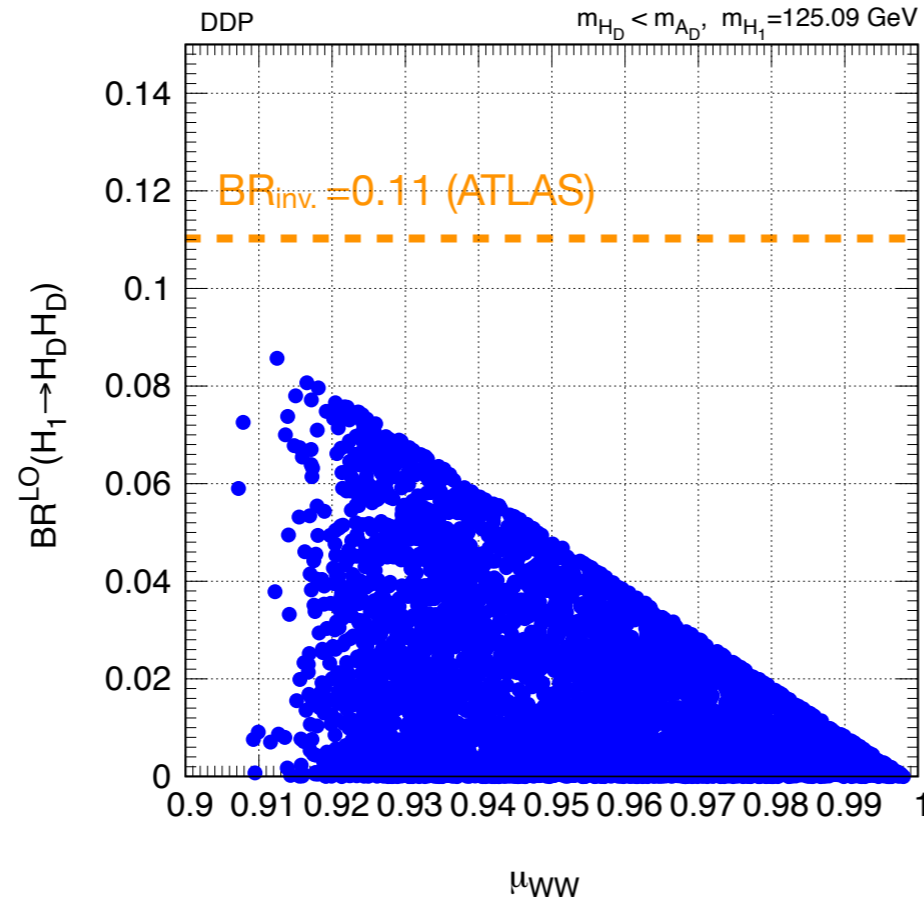
The following 11 parameters are chosen as input parameters:

$$v, v_s, m_X (X = H_D, A_D, H_D^\pm, H_1, H_2), \alpha, m_{22}^2, \lambda_2, \lambda_8$$

$$V \ni m_{22}^2 |\Phi_2|^2 + \lambda_2 |\Phi_2|^4 + \lambda_8 |\Phi_2|^2 \Phi_S^2$$

$BR_{\text{inv.}}$ vs Higgs signal strength

[I. Engeln, P. Ferreira, M. M. Muhlleitner, R. Santos, J. Wittbrodt, JHEP 08 (2020) 085]



$$BR^{\text{LO}}(H_1 \rightarrow H_D H_D) = \frac{\Gamma^{\text{LO}}(H_1 \rightarrow H_D H_D)}{\Gamma_{H_1}}$$

$$= \frac{\lambda_{H_1 H_D H_D}^2}{32\pi^2 m_{H_1} \Gamma_{H_1}} \sqrt{1 - \frac{4m_{H_D}^2}{m_{H_1}^2}}$$

$$\mu_{WW} = \frac{\sigma(pp \rightarrow h_{125} \rightarrow WW)}{\sigma_{\text{SM}}(pp \rightarrow h_{125} \rightarrow WW)}$$

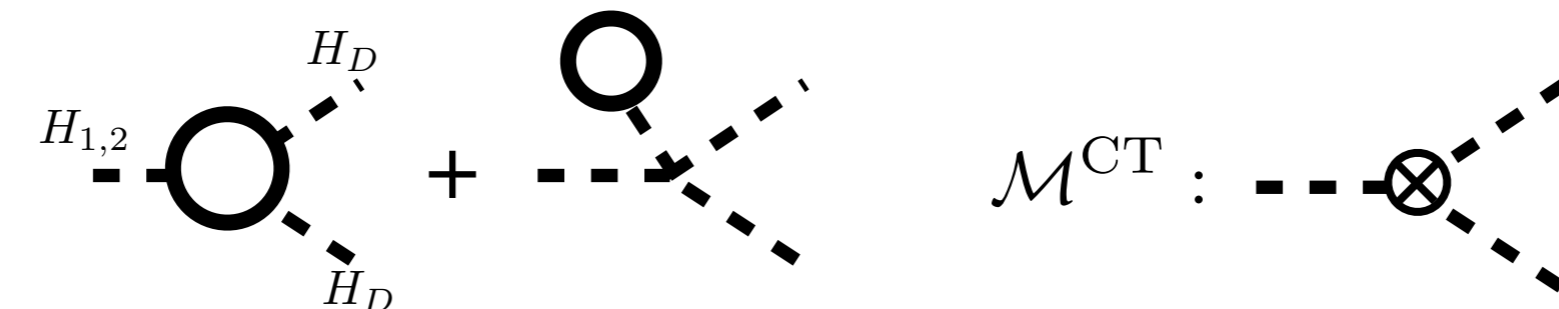
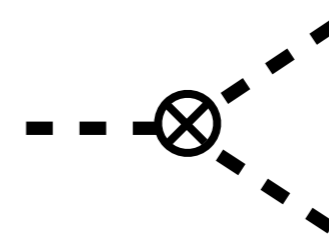
- The constraint from the Higgs signal strength $\rightarrow BR_{\text{inv.}} \lesssim 0.09$
- This is stronger than the current bound of $BR_{\text{inv.}}$ by ATLAS.

Radiative corrections change the picture ?

Calculations of NLO corrections to $H_{1,2} \rightarrow H_D H_D$

- Decay rate at NLO

$$\Gamma^{\text{NLO}}(H_{1,2} \rightarrow H_D H_D) = \Gamma^{\text{LO}} \left[1 + \frac{2}{\lambda_{H_{1,2}H_D H_D}} \text{Re}(\mathcal{M}^{\text{1PI}} + \mathcal{M}^{\text{CT}}) \right]$$

\mathcal{M}^{1PI} : 
 \mathcal{M}^{CT} : 
 $\ni \delta m_{22}^2 + \delta \lambda_8$

- Renormalization

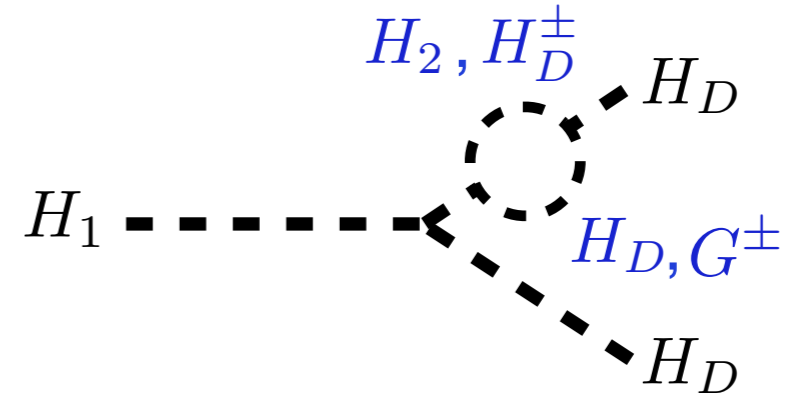
- Masses, mixing angles : OS scheme
- $\delta m_{22}^2, \delta \lambda_8$: We use three different schemes.

$$\left[\begin{array}{l} \text{OS process-dependent scheme} : \Gamma_{H_i \rightarrow A_D A_D}^{\text{LO}} \stackrel{!}{=} \Gamma_{H_i \rightarrow A_D A_D}^{\text{NLO}} \quad (i = 1, 2) \\ \text{ZEM process-dependent scheme} : (\mathcal{M}_i^{\text{1-loop}}) \Big|_{p_i^2 = p_{A_D}^2 = 0} = 0 \\ \text{(ZEM: Zero External Momentum)} \\ \overline{\text{MS}} \text{ scheme} \end{array} \right.$$

Extra Higgs loop contributions

- Approximate formula ($\overline{\text{MS}}$ scheme)

We take $\cos \alpha \rightarrow 1$, $\lambda_{H_1 H_D H_D} \ll 1$

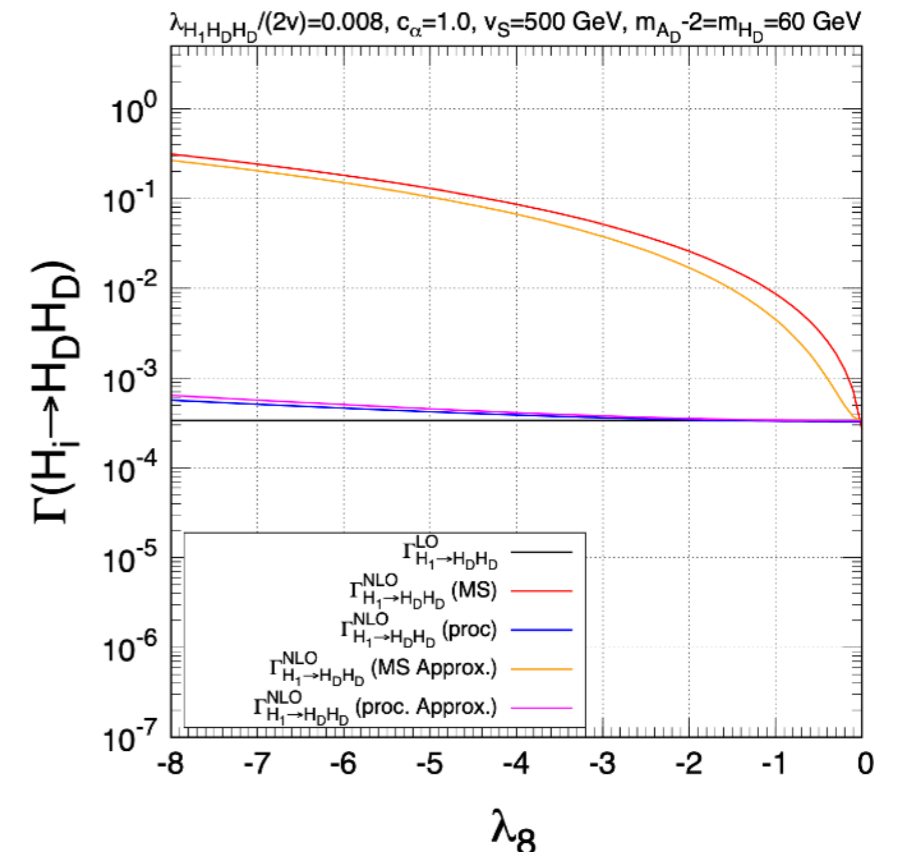


$$\Gamma_{H_1 \rightarrow H_D H_D} \simeq \Gamma^{\text{LO}} \left(1 - \frac{4}{v} \frac{1}{16\pi^2} \left[\underbrace{\lambda_{H_2 H_D H_D}^2}_{\substack{\alpha \rightarrow 0 \\ = (-\lambda_8 v_S)^2}} B_0(m_{H_D}^2, m_{H_2}, m_{H_D}) + 2\lambda_{H_D H_D^\pm G^\pm}^2 B_0(m_{H_D}^2, m_{H_D^\pm}, m_{G^\pm}) \right] \right)$$

[D. Azevedo P. Gabriel, M. Mühlleitner, KS, R. Santos]

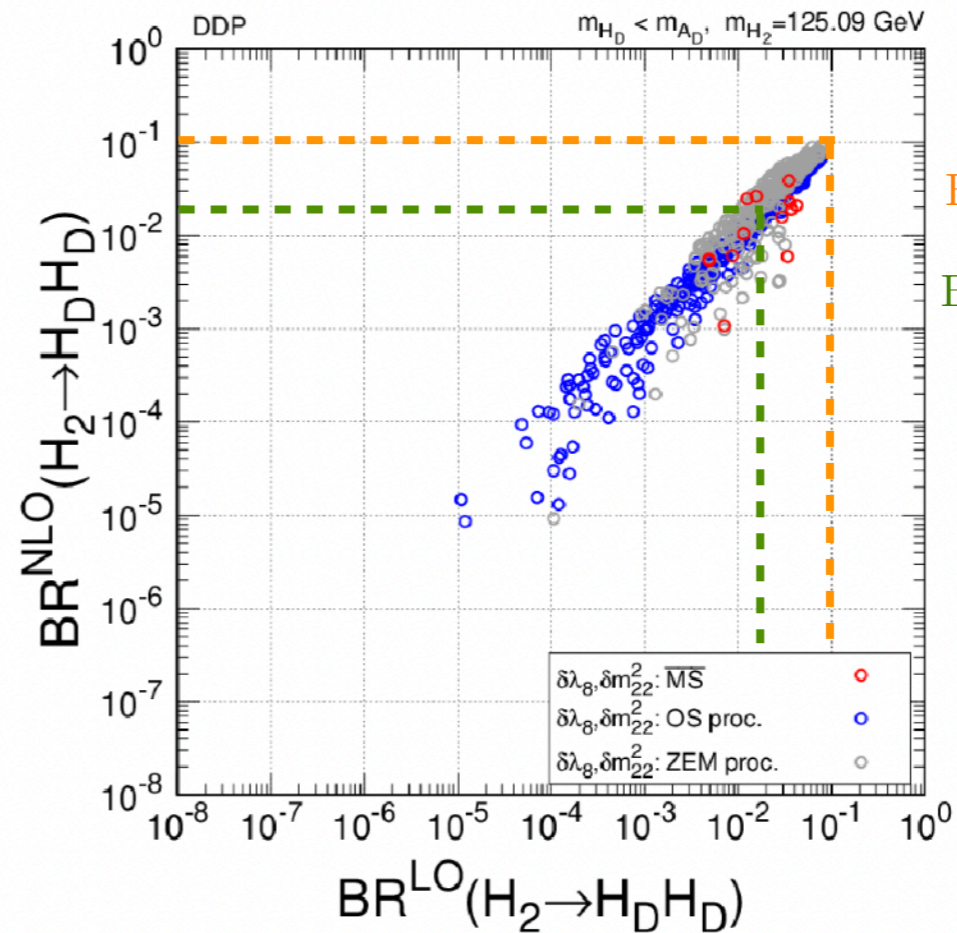
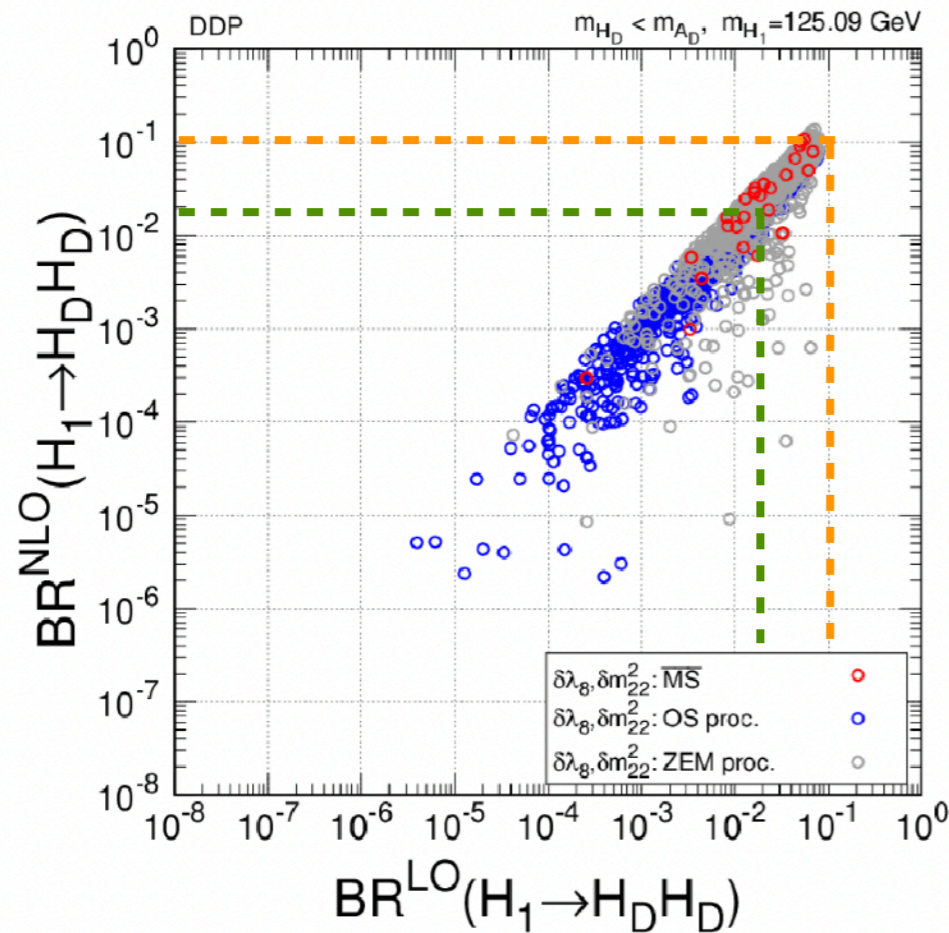
- Many terms suppressed by $\lambda_{H_1 H_D H_D}$.
- The H_2 loop can enhance the corrections.
- For OS proc. scheme, the corrections can be reasonable.

A cancellation between $\mathcal{M}_{H_1 \rightarrow H_D H_D}^{\text{loop}}$ and $\mathcal{M}_{H_1 \rightarrow A_D A_D}^{\text{loop}}$ occurs.



Correlation between BR^{LO} and BR^{NLO}

[D. Azevedo P. Gabriel, M. Mühlleitner, KS, R. Santos]



$BR_{\text{inv.}}(\text{ATLAS}) < 0.11$

$BR_{\text{inv.}}(\text{HL-LHC}) < 0.019$

- We generate parameter points with ScannerS. [M. Mühlleitner, M. O. Sampaio, R. Santos, J. Wittbrodt, arXiv:2007.02985]
 - Theoretical constraints: perturbative unitarity, Higgs potential bounded from below
 - Experimental constraints: DM constraints, extra Higgs searches, Higgs precision, electroweak precision
- Furthermore, we picked up points with the NLO corrections below 100%.
 - For ZEM scheme, some parameter space would be excluded by $BR_{\text{inv.}}(\text{ATLAS})$.
 - At HL-LHC era, effect of the NLO corrections become more important.

Summary

- We calculated NLO corrections to $H_{1,2} \rightarrow H_D H_D$, in dark doublet phase (DDP) in N2HDM. This process contributes to the Higgs boson invisible decay.
- At LO analysis, constraints from Higgs signal strength severe than those from Higgs invisible decay.
- When we include the NLO corrections to the Higgs invisible decay, the situation can be changed.
 - In some parameter regions, $BR(H_1 \rightarrow H_D H_D)^{NLO}$ for ZEM scheme can reach sensitivity of the recent result by ATLAS.
- As a future work, we also study this process in other phases of the N2HDM.

Buck up

Parameter range for scan analysis

We scan input parameters in the following range:

$$1 \text{ GeV} < m_{H_D} < 62 \text{ GeV}, \quad 1 \text{ GeV} < m_{A_D} < 1500 \text{ GeV} \quad (m_{A_D} > m_{H_D})$$

$$65 \text{ GeV} < m_{H_D^\pm} < 1500 \text{ GeV}, \quad 10^{-3} \text{ GeV}^2 < m_{22}^2 < 5 \cdot 10^5 \text{ GeV}^2,$$

$$1 \text{ GeV} < v_S < 5000 \text{ GeV}, \quad -\pi/2 < \alpha < \pi/2,$$

$$0 < \lambda_2 < 4\pi, \quad -4\pi < \lambda_8 < 4\pi.$$

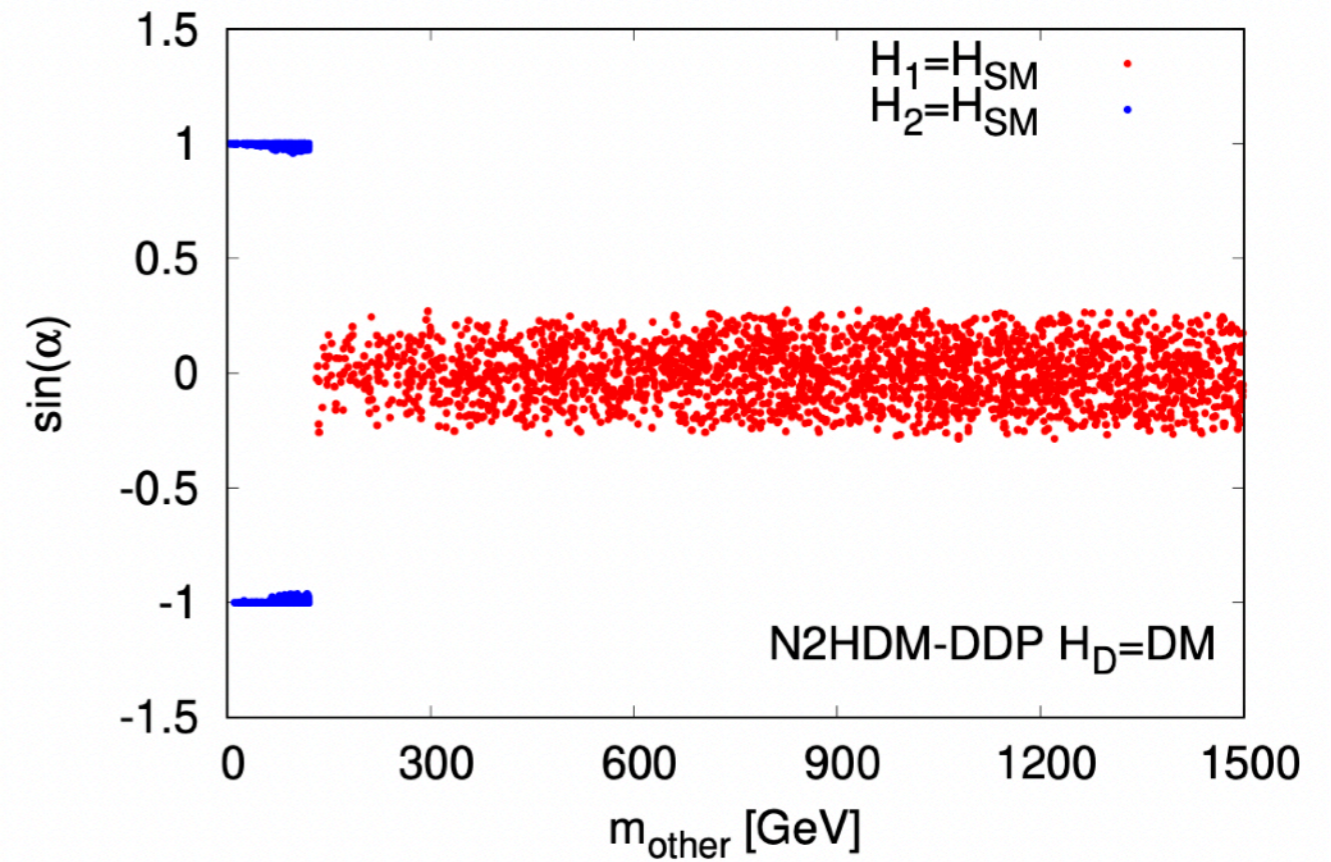
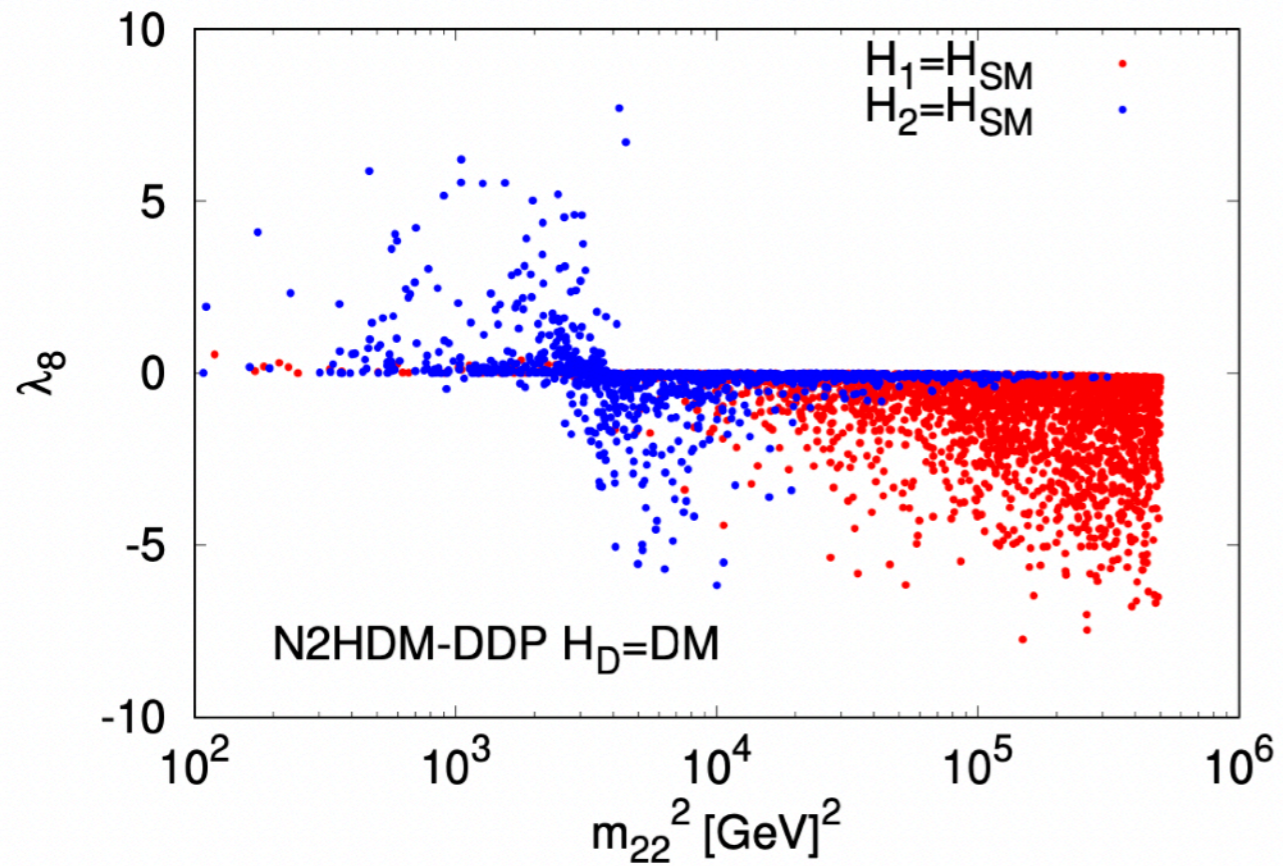
In scenario 1 we take the remaining parameters as

$$m_{H_1} = 125.09 \text{ GeV}, \quad 130 \text{ GeV} < m_{H_2} < 1500 \text{ GeV}$$

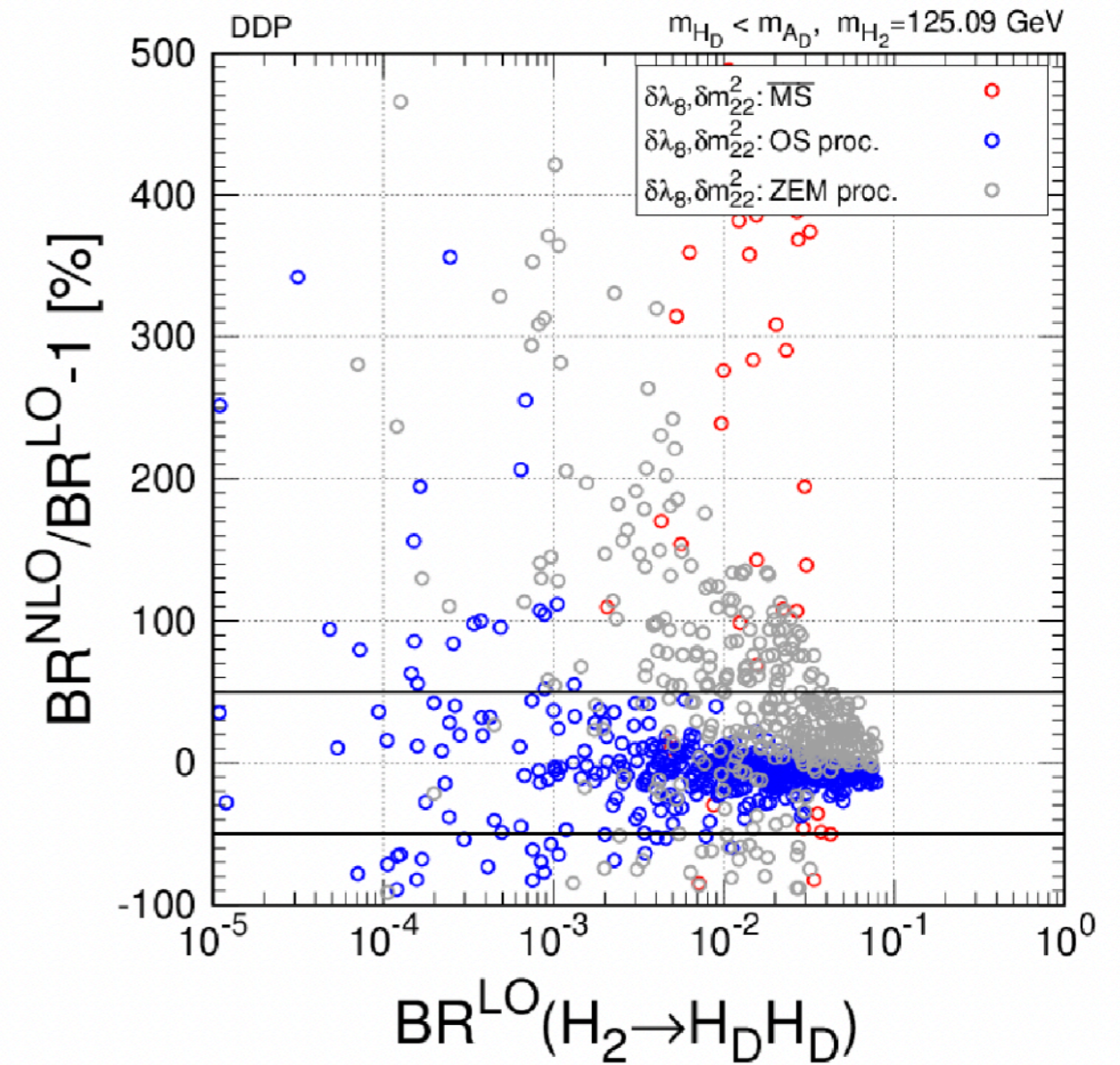
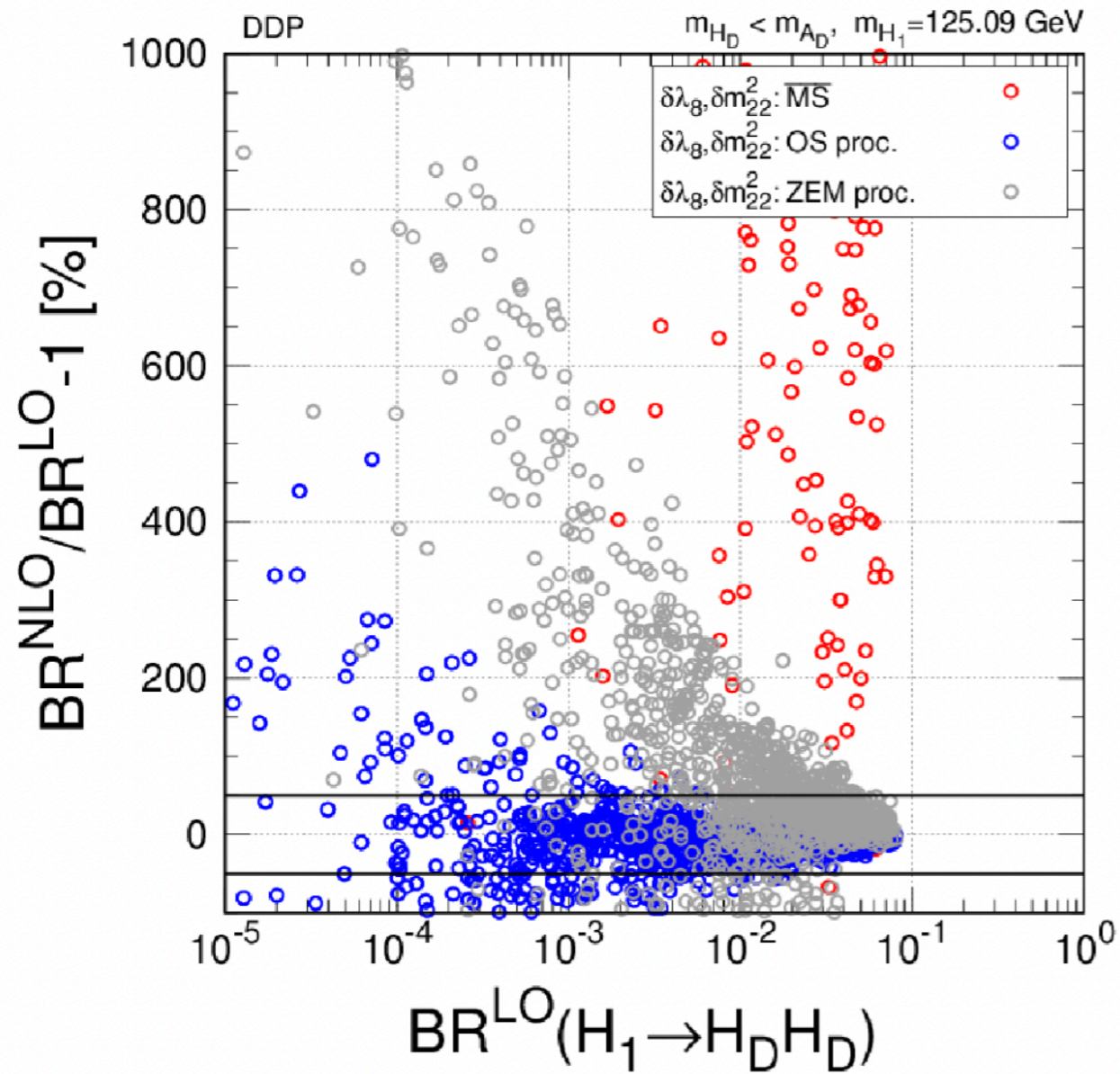
In scenario 2, we set as

$$1 \text{ GeV} < m_{H_1} < 120 \text{ GeV}, \quad m_{H_2} = 125.09 \text{ GeV}.$$

Allowed parameter regions



Size of NLO corrections for the BR



Approximate formula for OS proc. scheme

We take $\cos \alpha \rightarrow 1$, $\lambda_{H_1 H_D H_D} \ll 1$.

$$\begin{aligned} 2\text{Re} \left(\mathcal{M}_{H_1 \rightarrow H_D H_D}^{\text{NLO}} \right) \mathcal{M}_{H_1 \rightarrow H_D H_D}^{\text{LO}} &\simeq \frac{-4}{v} \lambda_{H_1 H_D H_D} \left(\Sigma_{H_D H_D}(m_{H_D}^2) - \Sigma_{A_D A_D}(m_{A_D}^2) \right) \\ &- \frac{2}{16\pi^2} \lambda_{H_1 H_D H_D}^2 \lambda_{H_2 H_D H_D}^2 C_0(m_{H_D}^2, m_{H_D}^2, m_{H_1}^2; m_{H_D}, m_{H_2}, m_{H_D}) \\ &+ \frac{2}{16\pi^2} \lambda_{H_1 A_D A_D}^2 \lambda_{H_2 A_D A_D}^2 C_0(m_{A_D}^2, m_{A_D}^2, m_{H_1}^2; m_{A_D}, m_{H_2}, m_{A_D}), \end{aligned}$$

$$\lambda_{H_1 H_D H_D} \stackrel{\alpha \rightarrow 0}{=} -\frac{1}{v} \left(2(m_{H_D}^2 - m_{22}^2) - \lambda_8 v_S^2 \right)$$

$$\lambda_{H_2 H_D H_D} \stackrel{\alpha \rightarrow 0}{=} -\lambda_8 v_S.$$

$$\lambda_{H_1 A_D A_D} \stackrel{\alpha \rightarrow 0}{=} \lambda_{H_1 H_D H_D} |_{m_{H_D} \rightarrow m_{A_D}}; \quad \lambda_{H_2 A_D A_D} \stackrel{\alpha \rightarrow 0}{=} \lambda_{H_2 H_D H_D}.$$