

Geant4 Annual Collaboration Meeting

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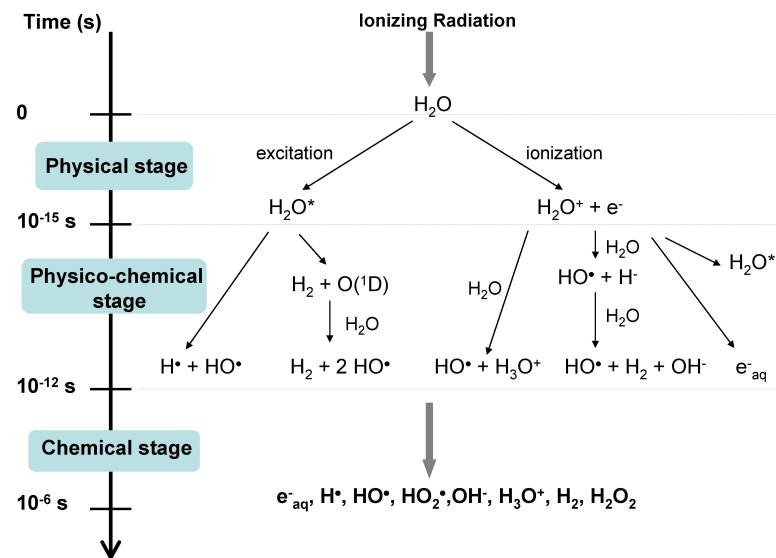
Mesoscopic model of Water Radiolysis in Geant4-DNA

in collaboration with Laurent Desorgher, Flore Chappuis and Sébastien Incerti

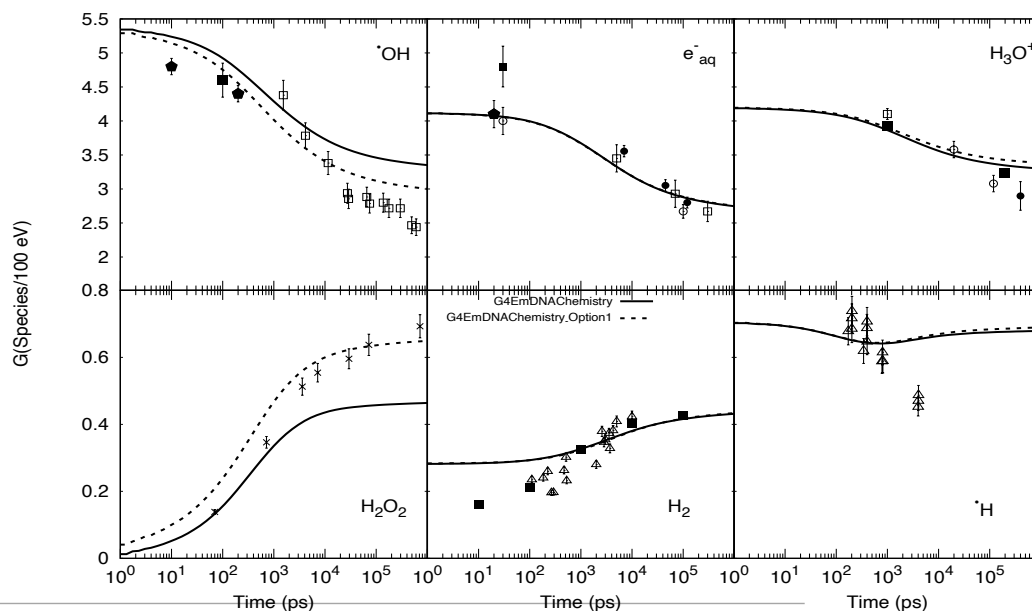
FLASH Radiotherapy

Modeling ultra-high dose rate irradiation requires

- **High radical species concentration**
- **Long time chemical yield evolution (beyond 1 us)**



Electronic state	Decay channel	Fraction
All ionization states	$H_2O^+ + H_2O \rightarrow H_3O^+ + \cdot OH$ (through proton transfer)	100 %
Excitation state A1B1: (1b1) \rightarrow (4a1/3s)	$H_2O^* \rightarrow \cdot OH + H^\bullet$ $H_2O^* \rightarrow H_2O + \Delta E$	65 % 35 %
Excitation state B1A1: (3a1) \rightarrow (4a1/3s)	$H_2O^* \rightarrow HO^+ + \cdot OH + e^-_{aq}$ $H_2O^* \rightarrow \cdot OH + \cdot OH + H_2$ $H_2O^* \rightarrow H_2O + \Delta E$	55 % 15 % 30 %
Excitation state : Rydberg, diffusion bands	$H_2O^* \rightarrow HO^+ + \cdot OH + e^-_{aq}$ $H_2O^* \rightarrow H_2O + \Delta E$	50 % 50 %



Geant4-DNA: Step by Step (SBS) and Independent Reaction Time (IRT) methods

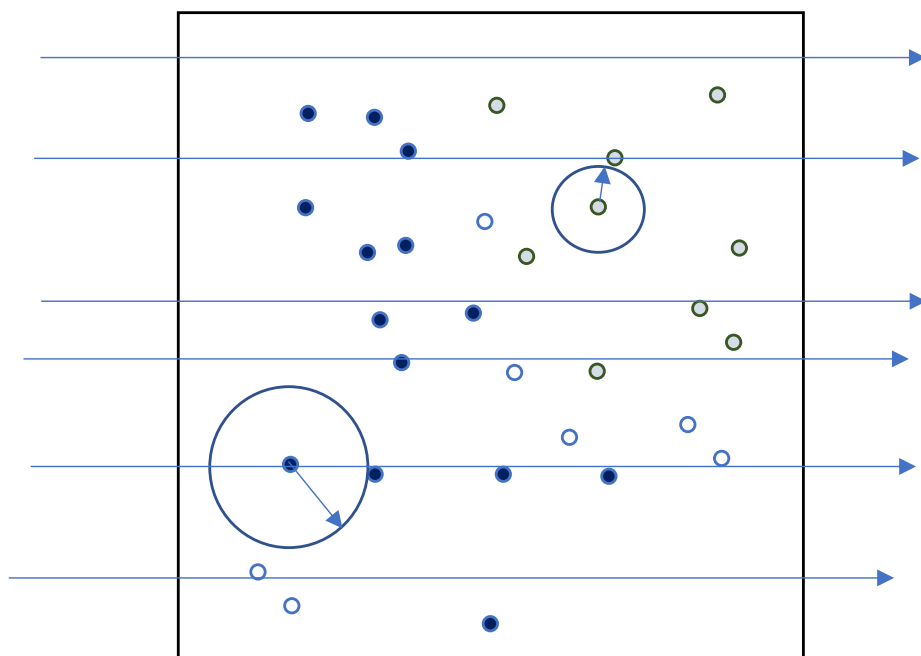
- Using the dynamic time step model
- Describing the diffusion process corresponding to the Brownian motion (SBS)
- Simplifying the multiple particle problem to the two-particle problem in an approximation (IRT)
- Until 1 μs

Computation time is the main drawback

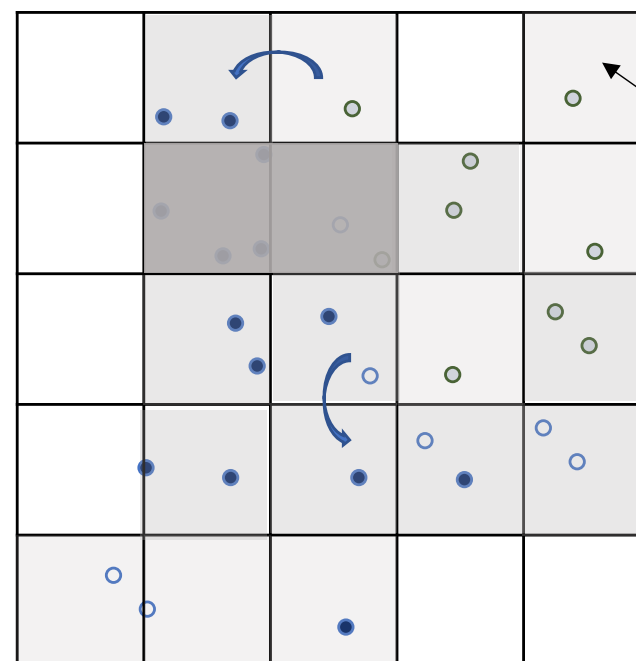
Particle-based model



Compartment-based model



Using Brownian dynamics and
Smoluchowski theory



- ✓ Homogenous
- ✓ Species react with each other in the same voxel

Using Reaction-Diffusion
Master Equation (RDME)

Reaction-Diffusion Master Equation

$$\begin{aligned} \frac{\partial}{\partial t} \mathbb{P}(\mathbf{u}, t) = & \sum_{i=1}^I \sum_{r=1}^R [a_i^r(\mathbf{u} - \boldsymbol{\nu}_{i,r}) \mathbb{P}(\mathbf{u} - \boldsymbol{\nu}_{i,r}, t) - a_i^r(\mathbf{u}) \mathbb{P}(\mathbf{u}, t)] \\ & + \sum_{i=1}^I \sum_{\substack{j=1 \\ j \neq i}}^I \sum_{\ell=1}^L [\lambda_{i,j}^{\ell}(u_i^{\ell}(t) + 1) \mathbb{P}(\mathbf{u} - \mathbf{e}_{i,j}^{\ell}, t) - \lambda_{i,j}^{\ell} u_i^{\ell}(t) \mathbb{P}(\mathbf{u}, t)], \end{aligned}$$

Event-driven simulation using the “Next-Subvolume Method” (NSM):

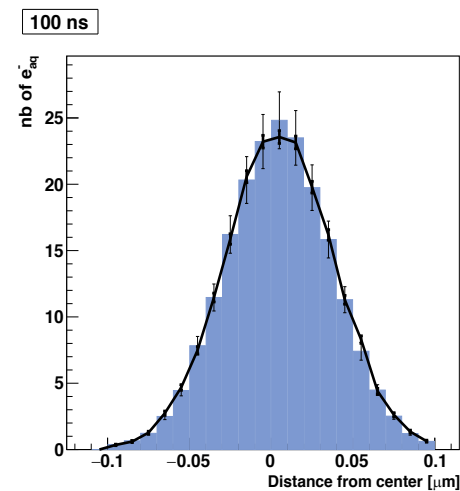
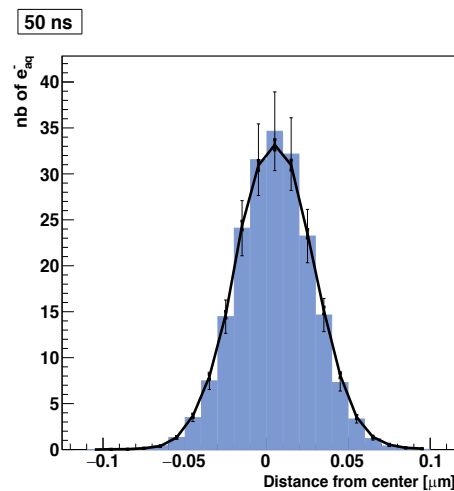
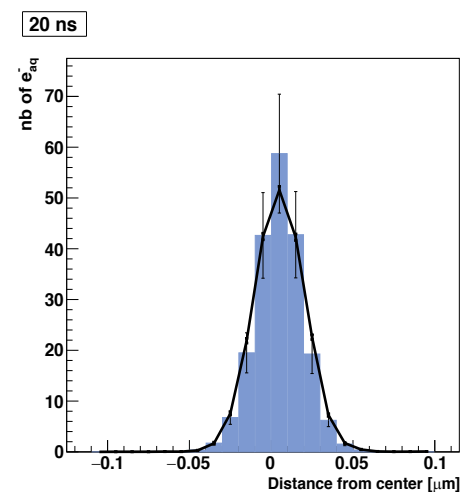
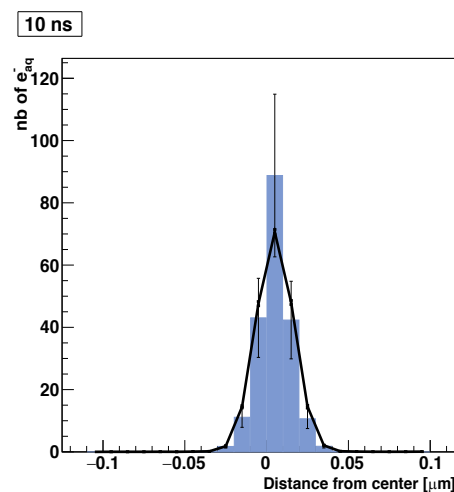
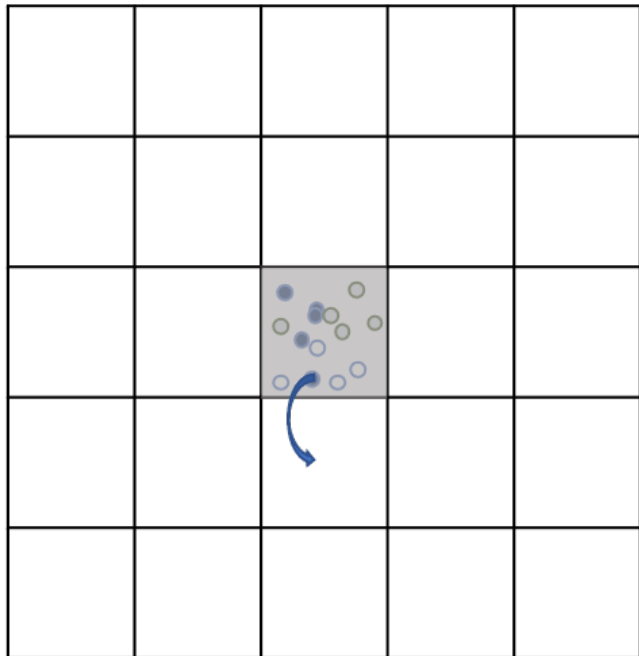
- Calculation of the propensity functions a_i for all voxels
- Sampling of the time when the next event occurs

$$\tau_i = \frac{-\ln(\xi)}{a_i}$$

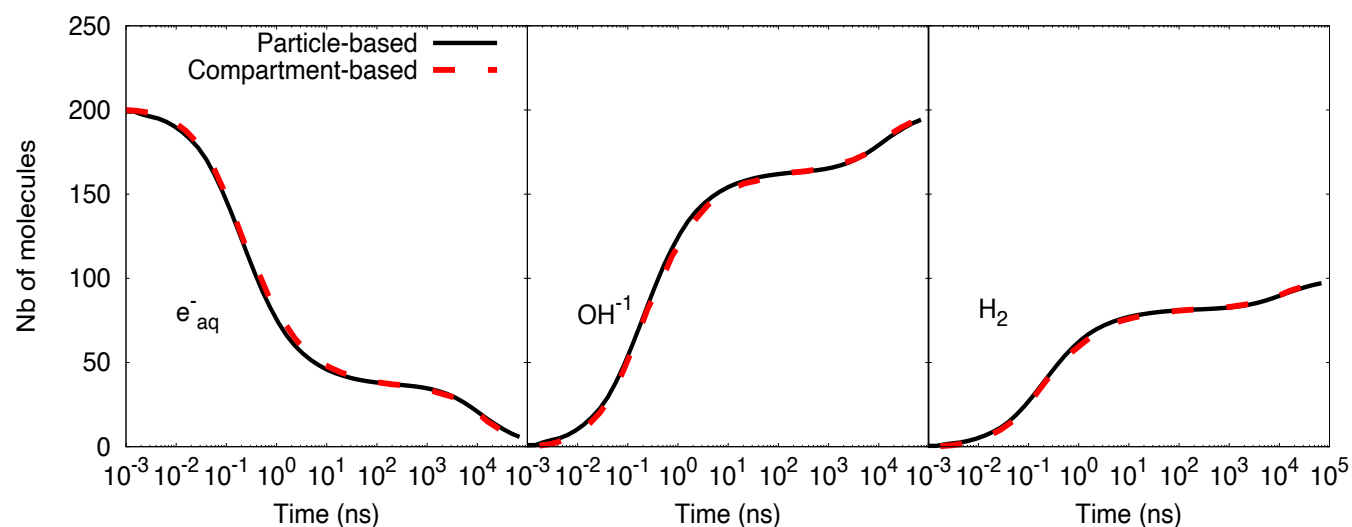
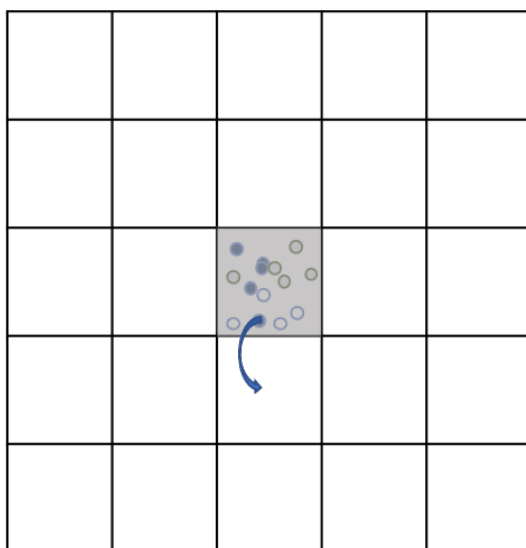
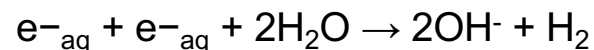
- Sampling which reaction or diffusion will take place according to the propensity function a_i
- Processing the first event in the queue and changing the concentrations in the voxels involved in the event
 - ✓ If the event is a reaction, we eliminate reactants and create products.
 - ✓ If the event is a diffusion, we remove the particle in the voxel where it was located and add the particle in the voxel where it goes.

RDME method (blue histogram) and the SBS (line)

Test 1 : Spatial (radial) distributions of solvated electrons



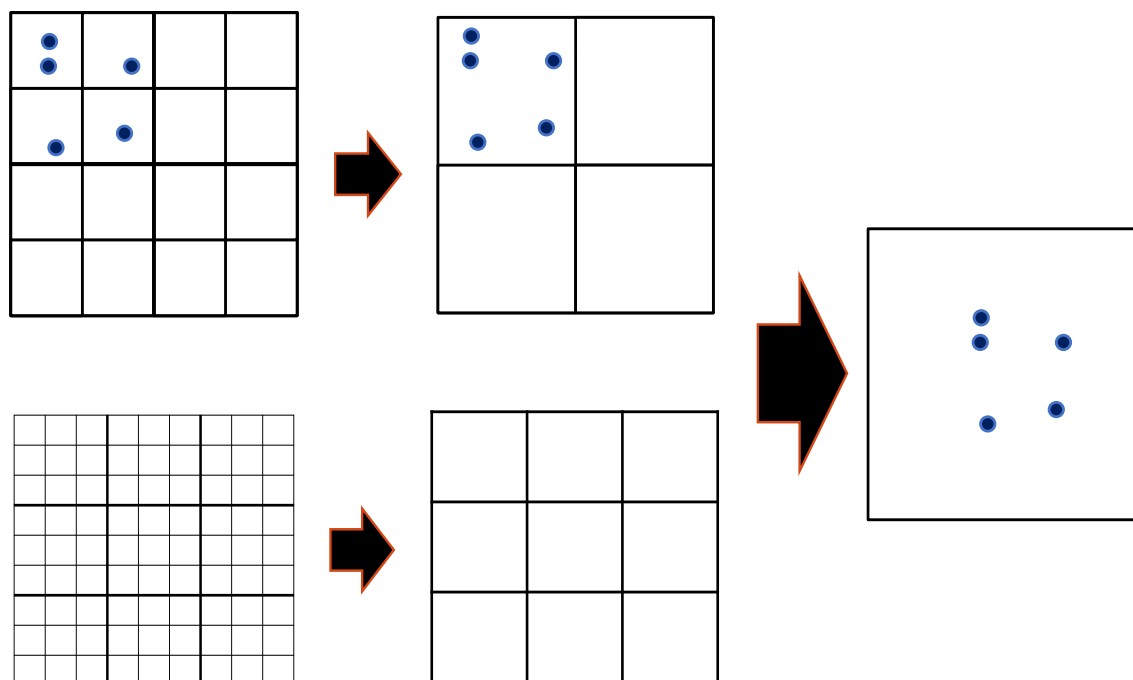
Test 2 : Spatial (radial) distribution and reaction of solvated electrons



Two main drawbacks of the compartment-based model :

- “Well-mixed” condition
- Computational efficiency and physical validity of the model

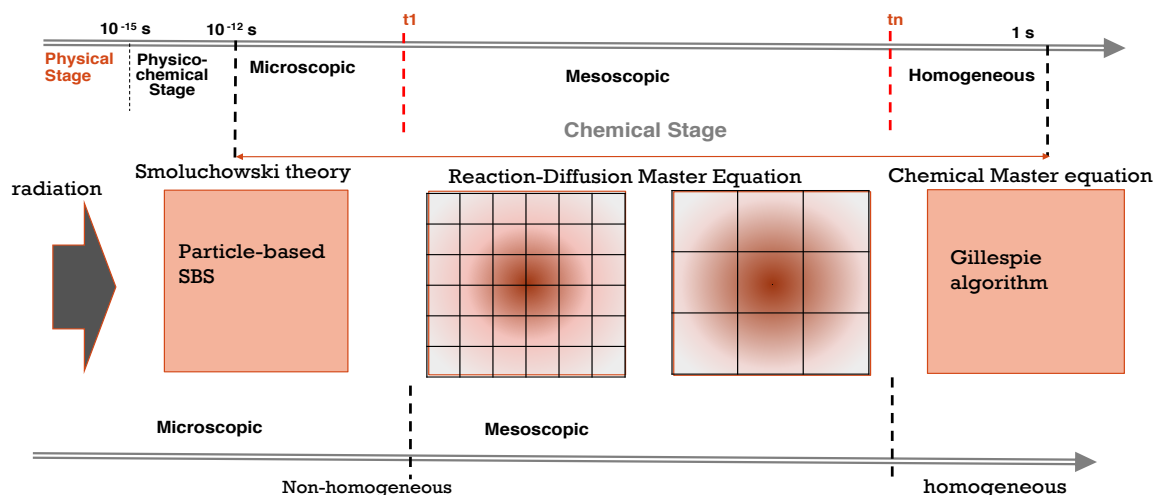
Adaptation of voxel sizes during the evolution time



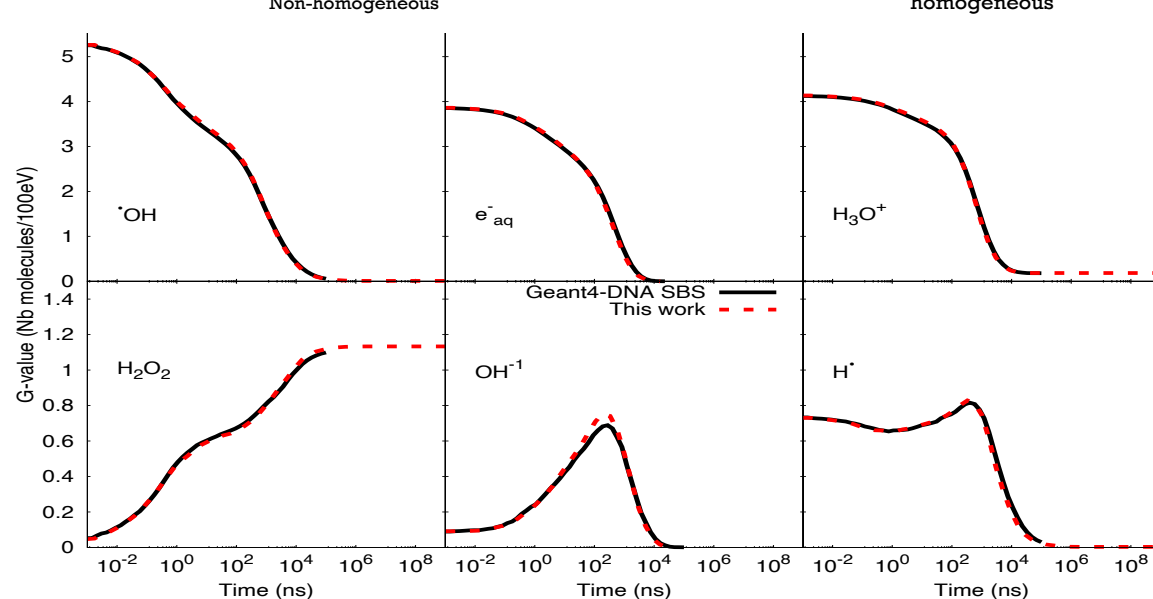
All species of finer voxels are moved to a larger voxel of a coarser mesh after each “transfer time”

End time	1 ns	10 ns	100 ns	1 μ s	10 μ s	100 μ s
Speedup factor	1.3×10^1	1.57×10^1	1.65×10^1	2.5×10^2	2.3×10^3	2.3×10^4

Combination of the SBS model with the compartment-based model



Reaction
$\text{H}^\bullet + \text{e}^-_{\text{aq}} + \text{H}_2\text{O} \rightarrow \text{OH}^- + \text{H}_2$
$\text{H}^\bullet + \text{OH}^\bullet \rightarrow \text{H}_2\text{O}$
$\text{H}^\bullet + \text{H}^\bullet \rightarrow \text{H}_2$
$\text{H}_2\text{O}_2 + \text{e}^-_{\text{aq}} \rightarrow \text{OH}^- + \text{OH}^\bullet$
$\text{H}_3\text{O}^+ + \text{e}^-_{\text{aq}} \rightarrow \text{H}^\bullet + \text{H}_2\text{O}$
$\text{H}_3\text{O}^+ + \text{OH}^- \rightarrow 2\text{H}_2\text{O}$
$\text{OH}^\bullet + \text{e}^-_{\text{aq}} \rightarrow \text{OH}^-$
$\text{OH}^\bullet + \text{OH}^\bullet \rightarrow \text{H}_2\text{O}_2$
$\text{e}^-_{\text{aq}} + \text{e}^-_{\text{aq}} + 2\text{H}_2\text{O} \rightarrow 2\text{OH}^- + \text{H}_2$

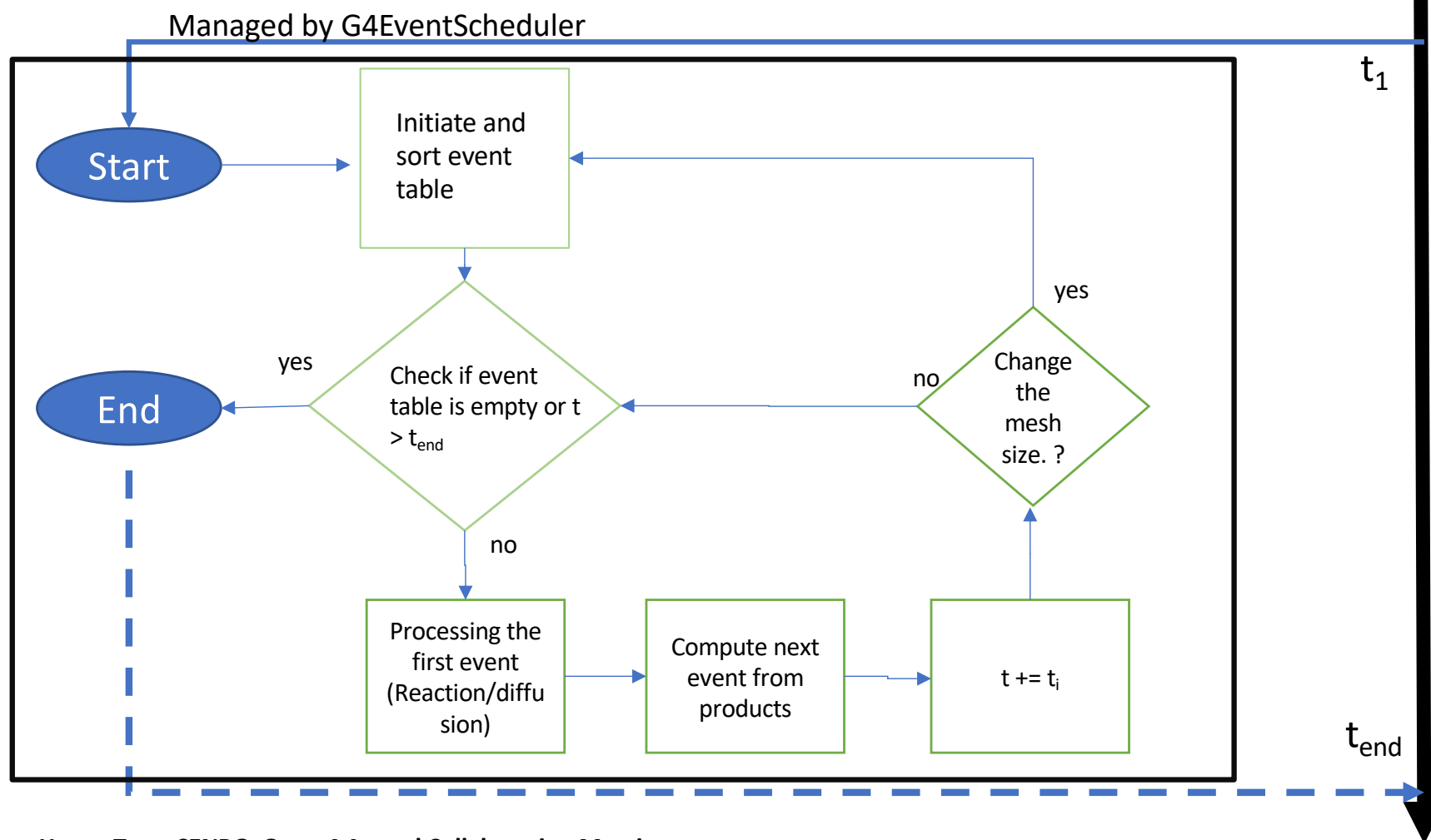


Just published :

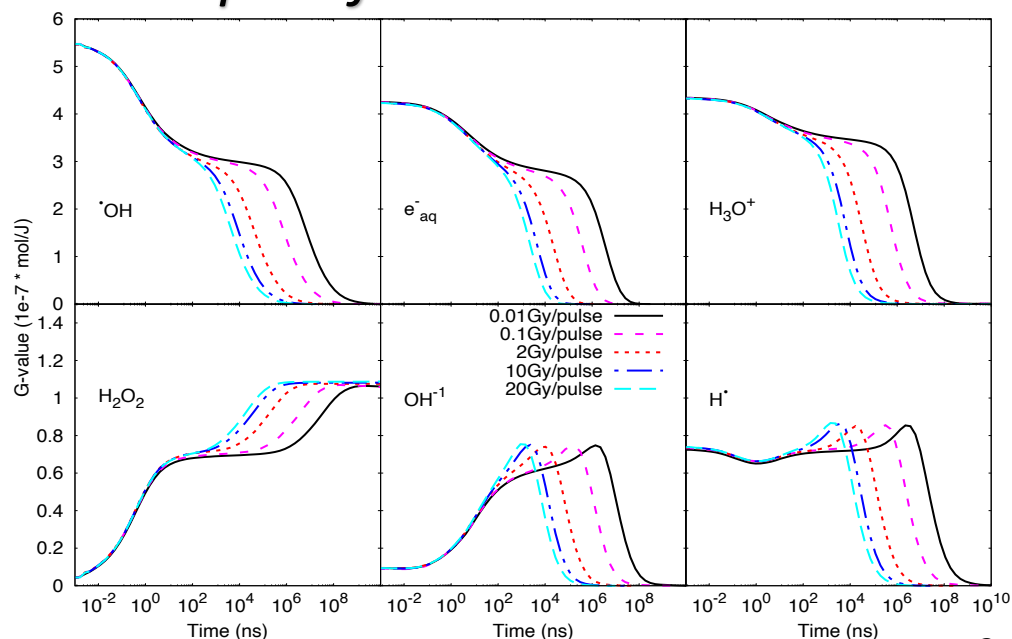
Tran et al., Int. J. Mol. Sci. 2021, 22

Stepping algorithm

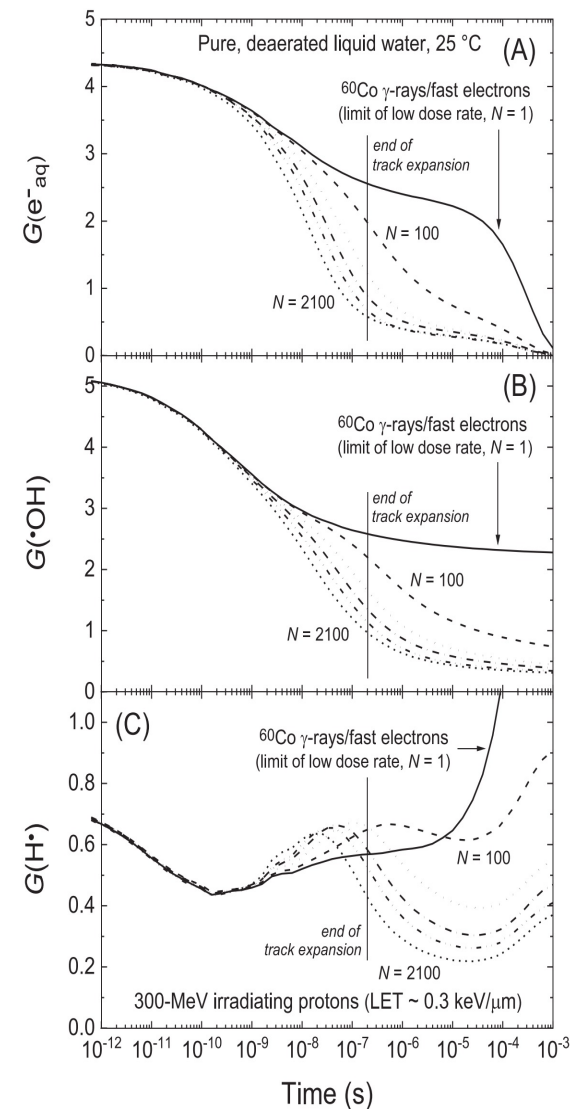
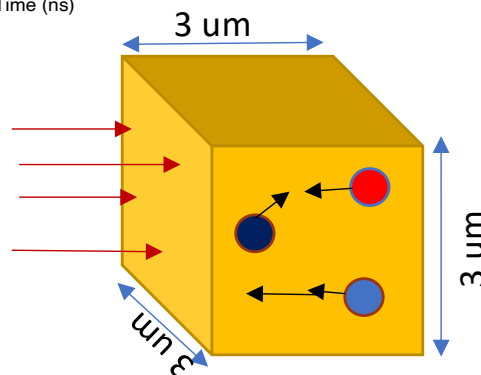
Particle-based model
(G4Scheduler)



Example of deaerated water



- Electron beam of 1 MeV
- Incident electrons are shot onto the volume until total deposited energy reaches **1-20 Gy (FLASH)** or about **0.01 Gy (CONV)**
- Produced species starts **simultaneously** (pulse length not taken into account)
- The results are normalized to the deposited energy using **G-value (mol/J)** from **1 ps** until reaching steady states



Alanazi et al. Radiation Research, 2021

Conclusion

- Coarse-grained model
- Simulating from heterogeneous -> homogeneous states
- Taking into account secondary reactions at long time (beyond 1 us)

The first prototype of model could be released from version Geant4 11 and feedback is welcome

Thank you very much