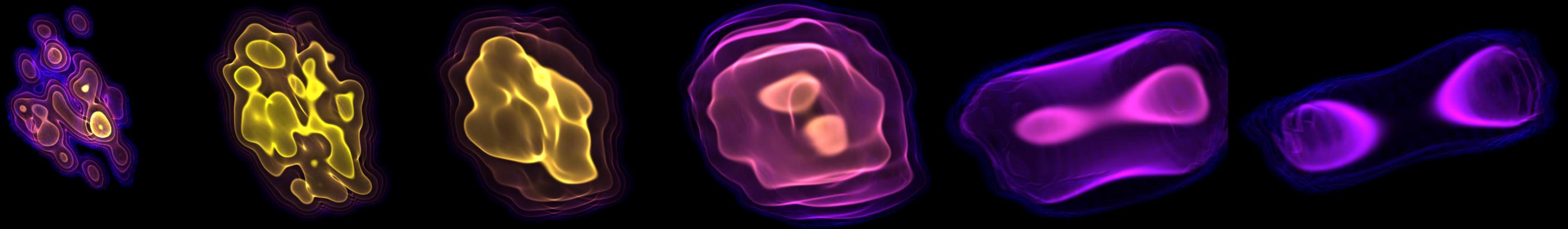




# INTRODUCTION TO THE COLLECTIVE QGP

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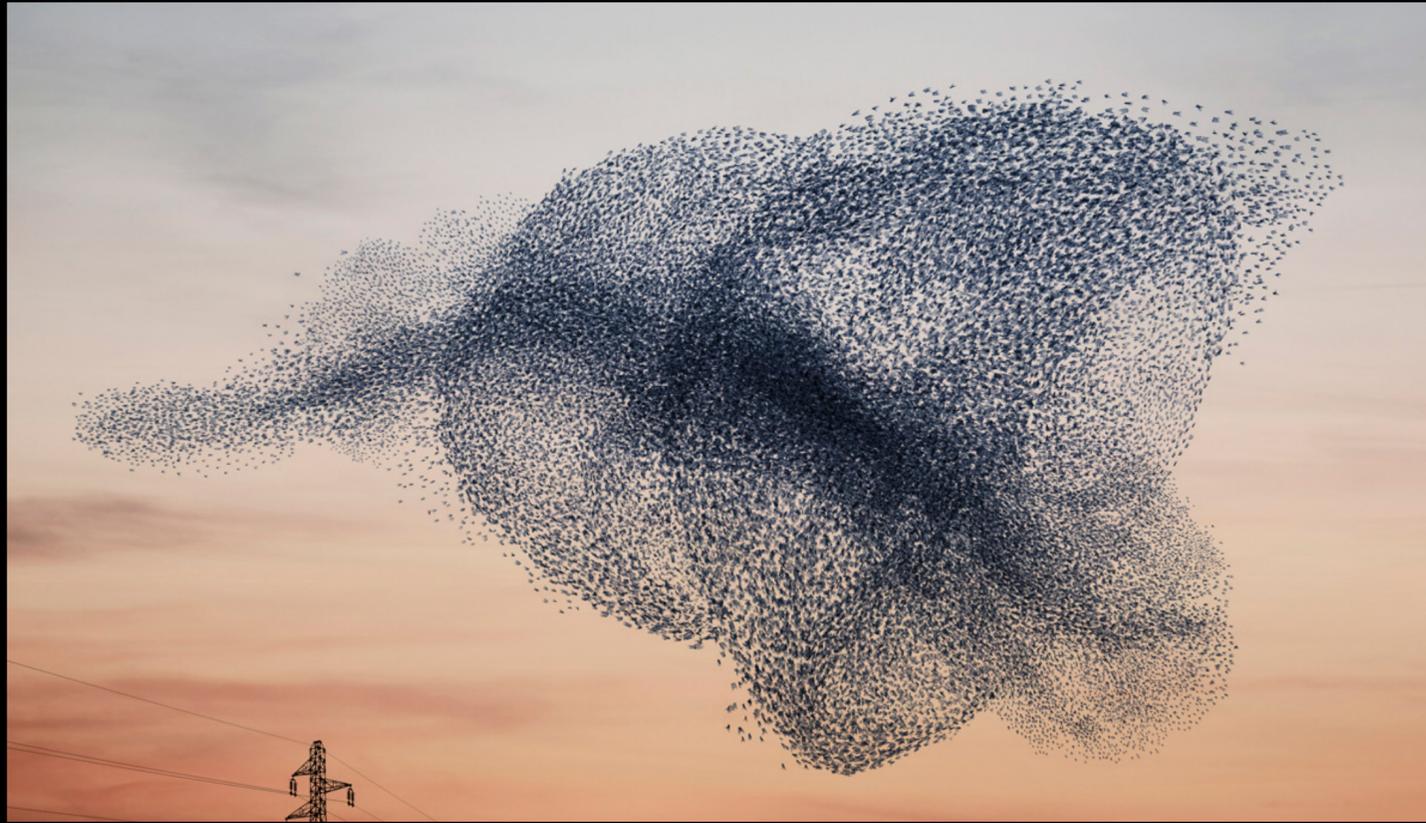
CHUN SHEN



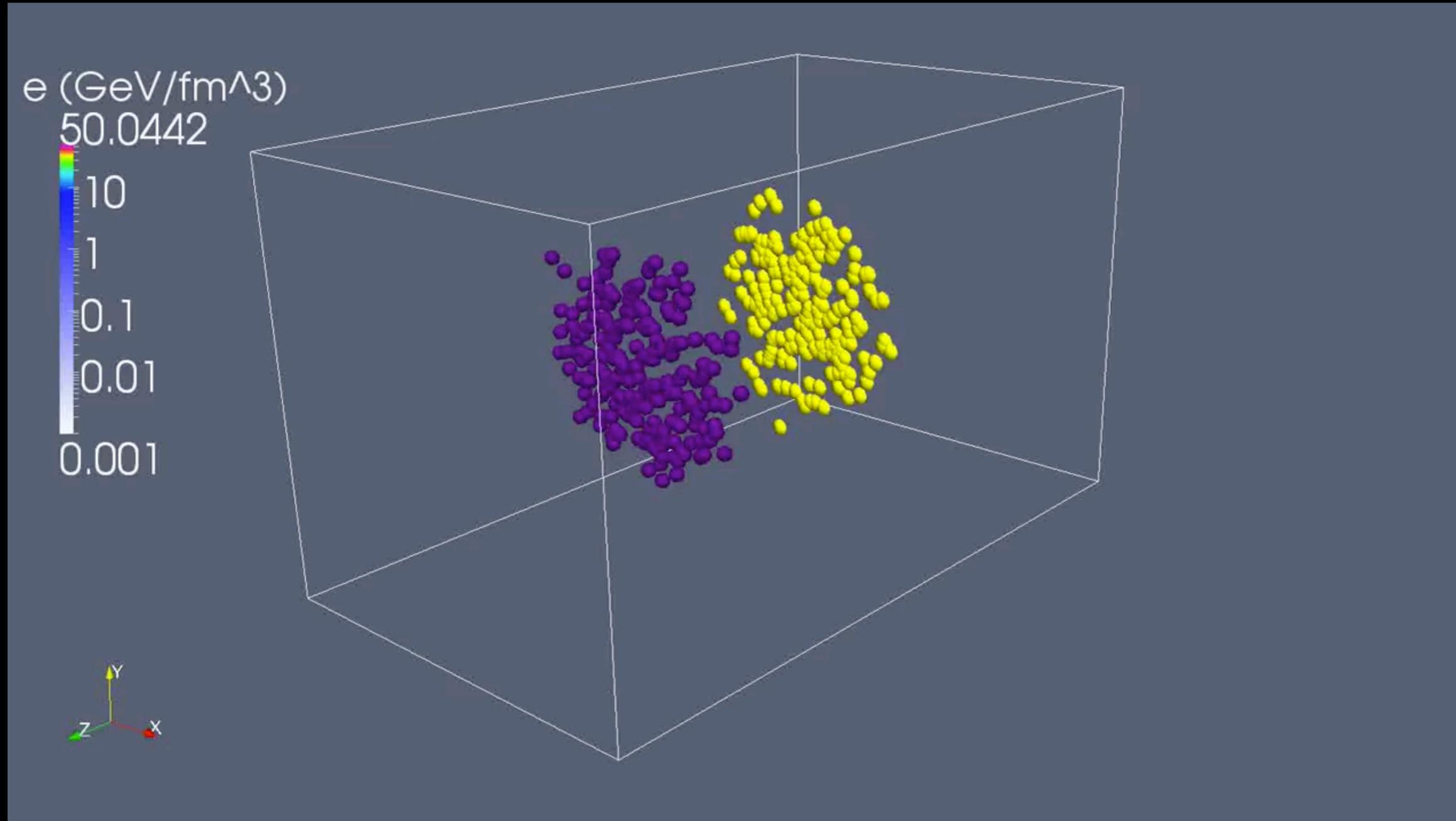
JETSCAPE Summer School  
July 21, 2021

Post your questions in the slack channel:  
**#jul21-jul22-hydro**

# MORE IS DIFFERENT!

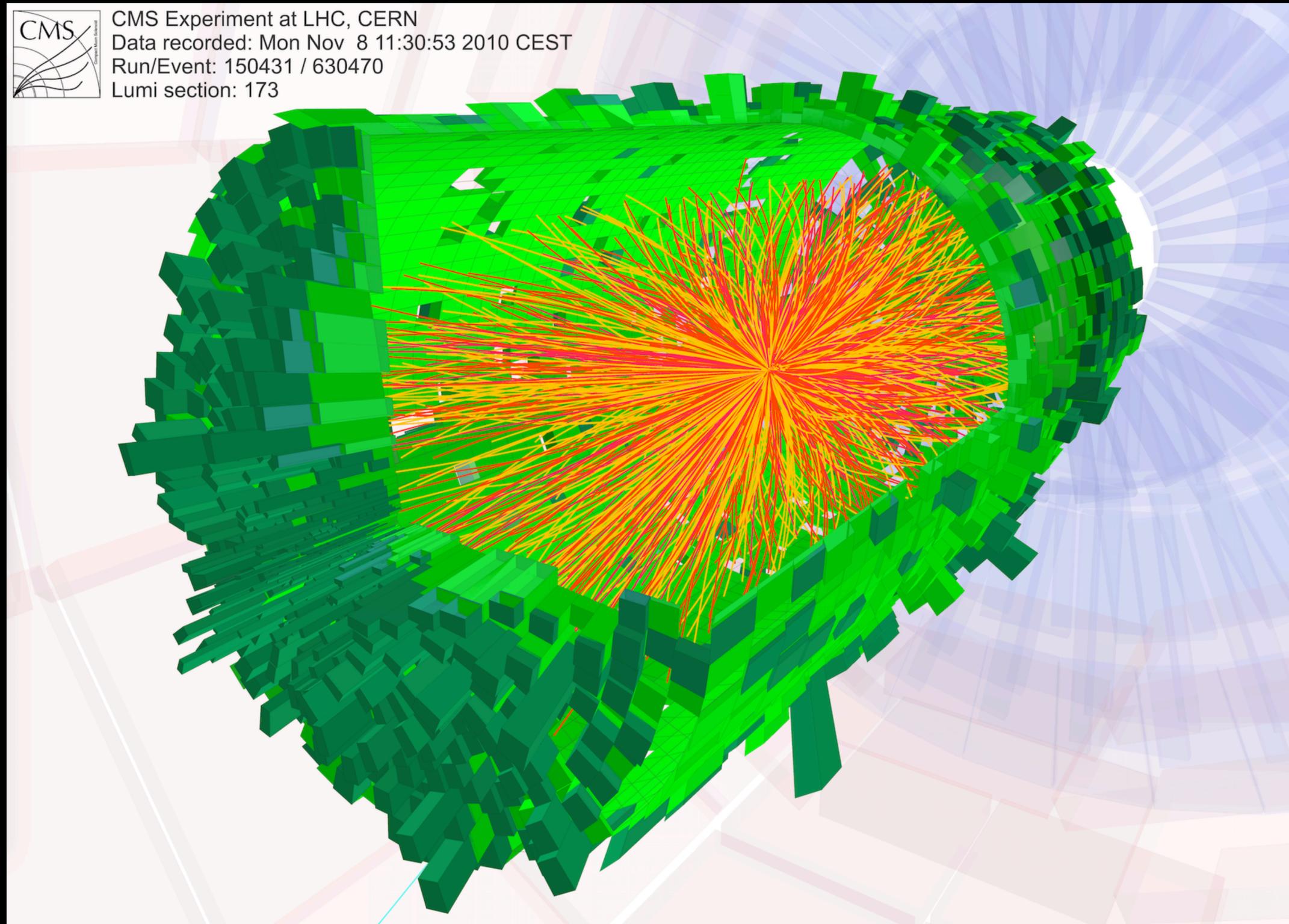


# A “LITTLE BANG”

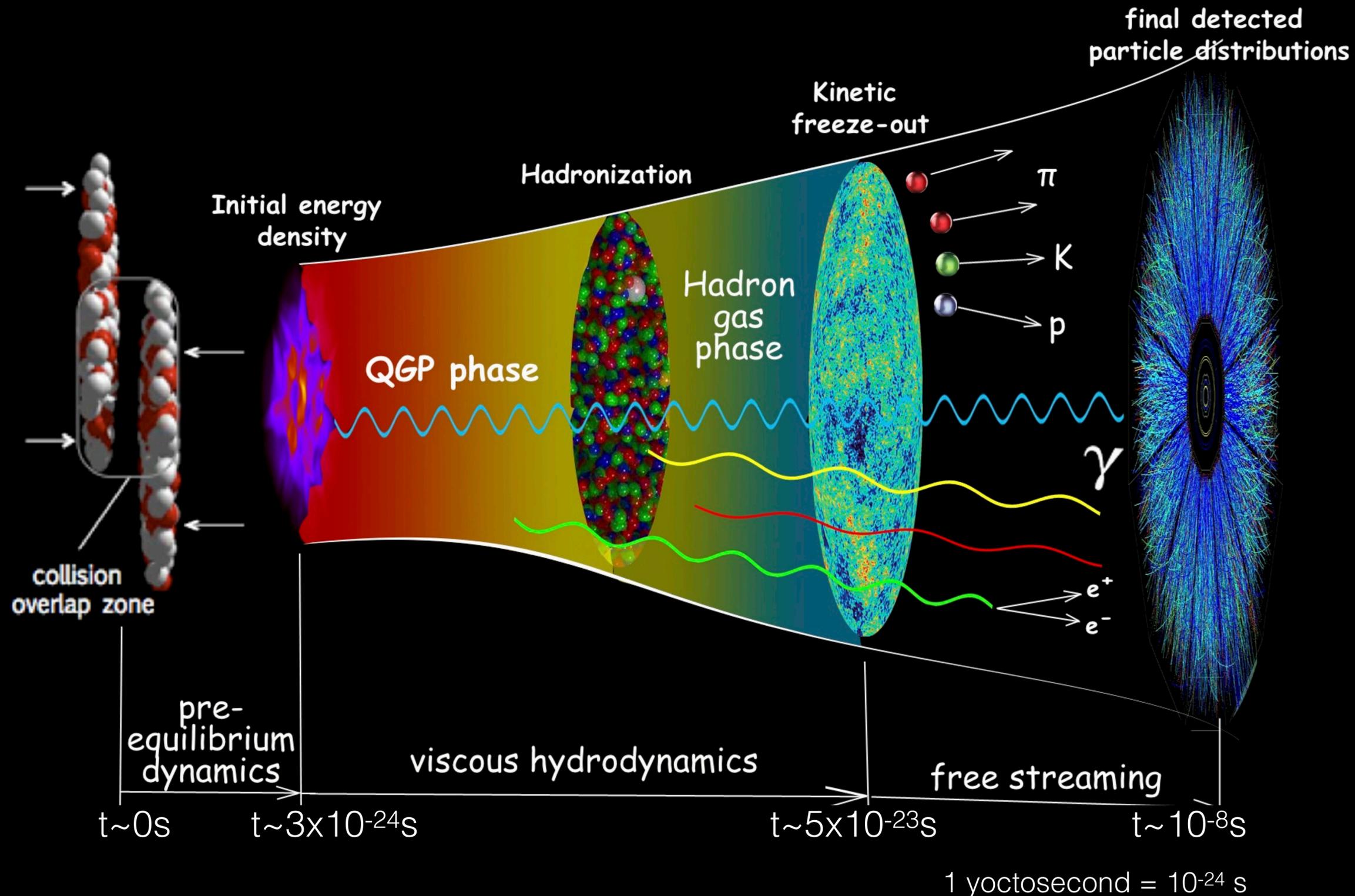


<http://youtu.be/W3h5vQOUJTg>

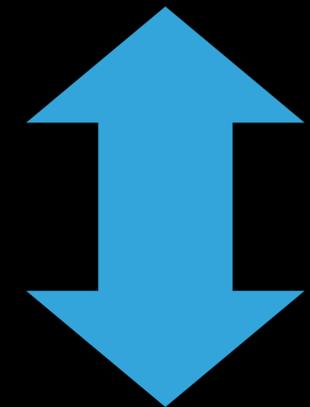
# A PB+PB COLLISION AT THE LARGE HADRON COLLIDER



# RELATIVISTIC HEAVY-ION COLLISIONS



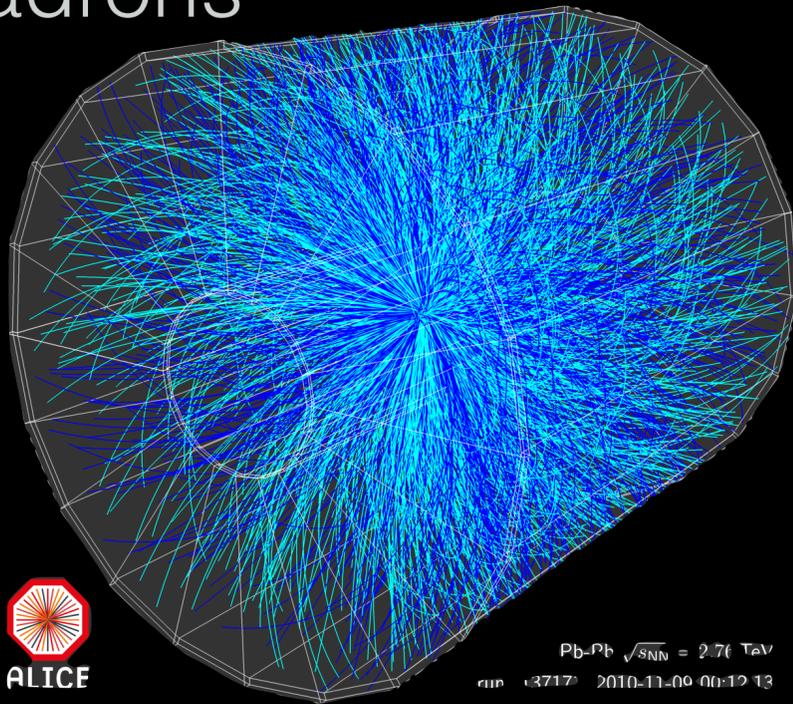
Complex dynamics driven by multiple length scales



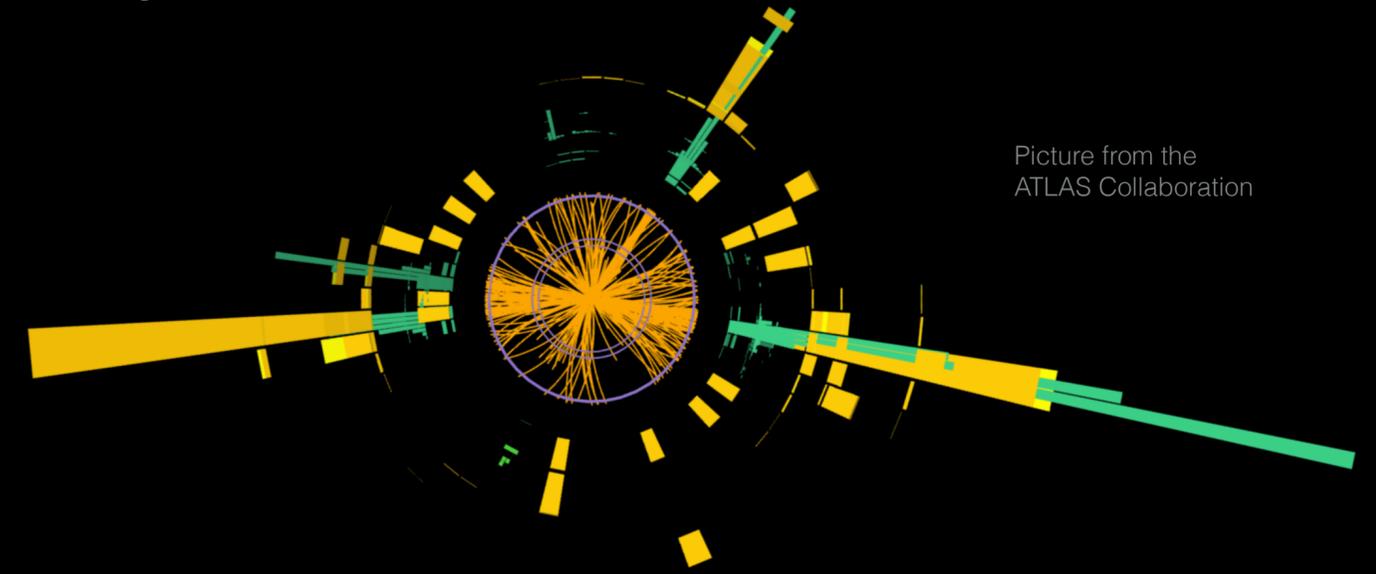
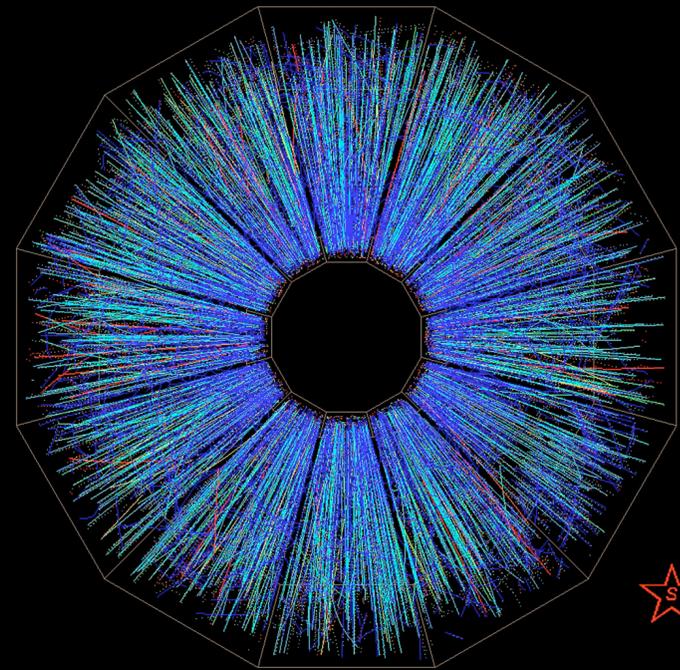
Hybrid multi-stage modeling with event-by-event fluctuations

# MULTI-MESSENGER HEAVY-ION PHYSICS

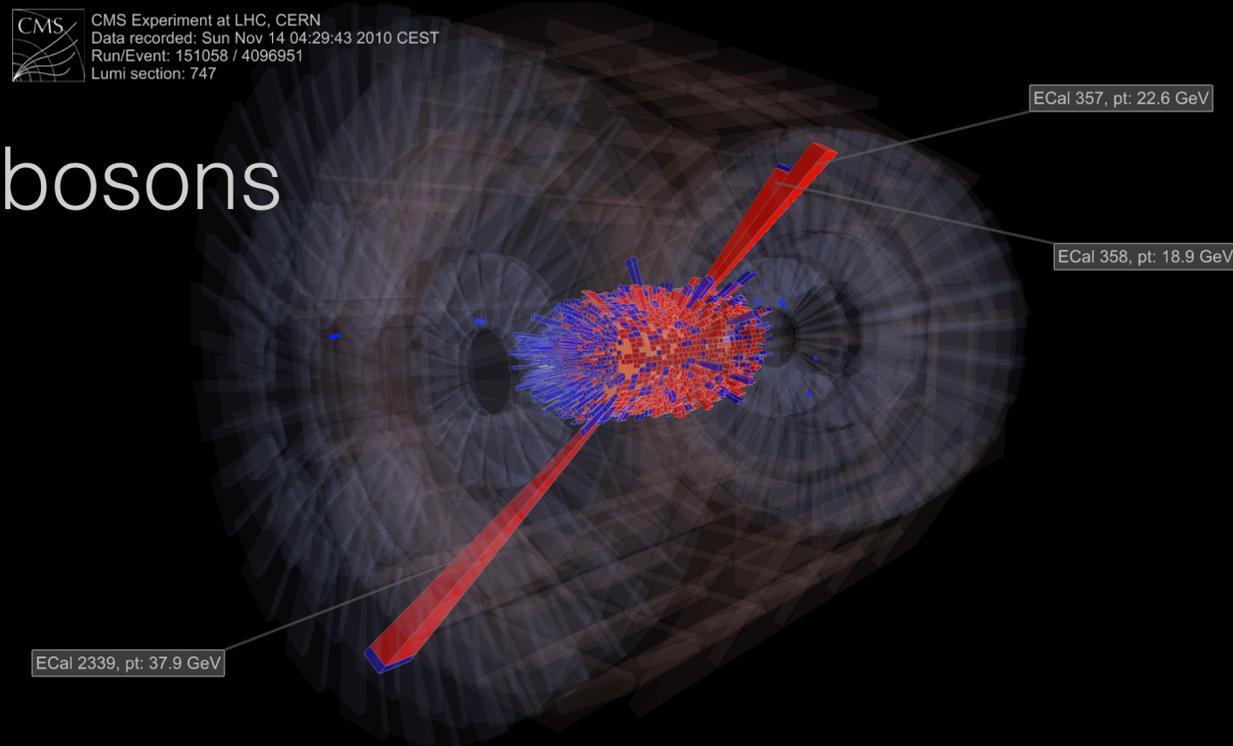
Hadrons



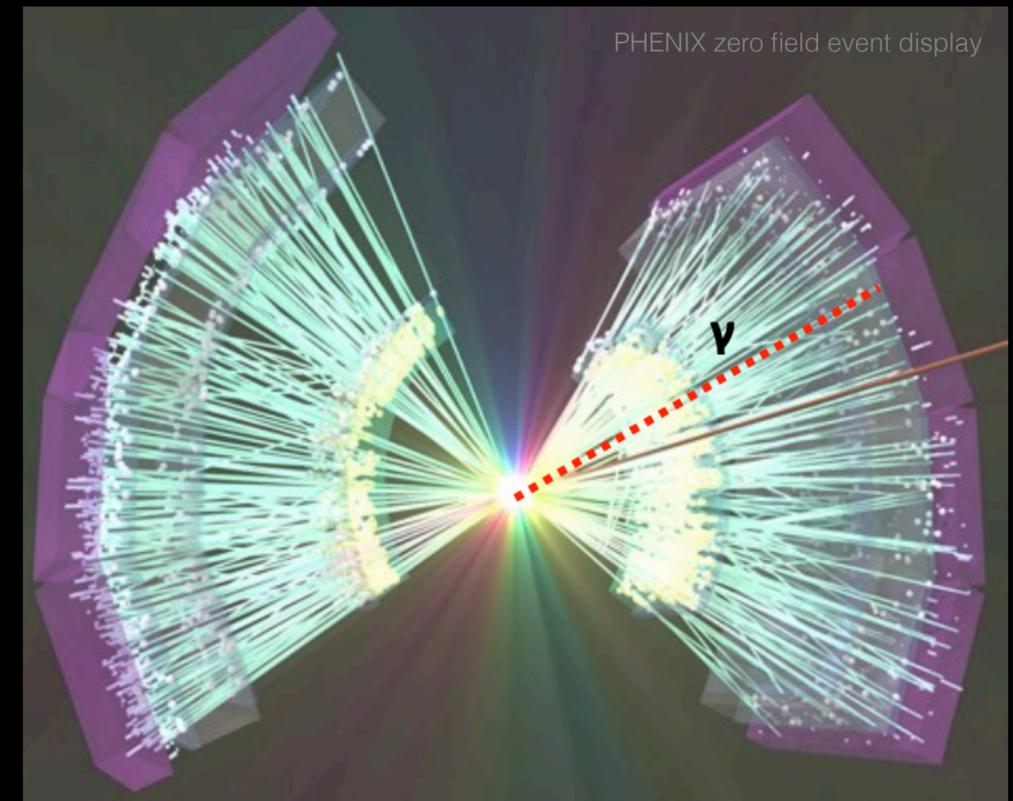
QCD jets



EW bosons

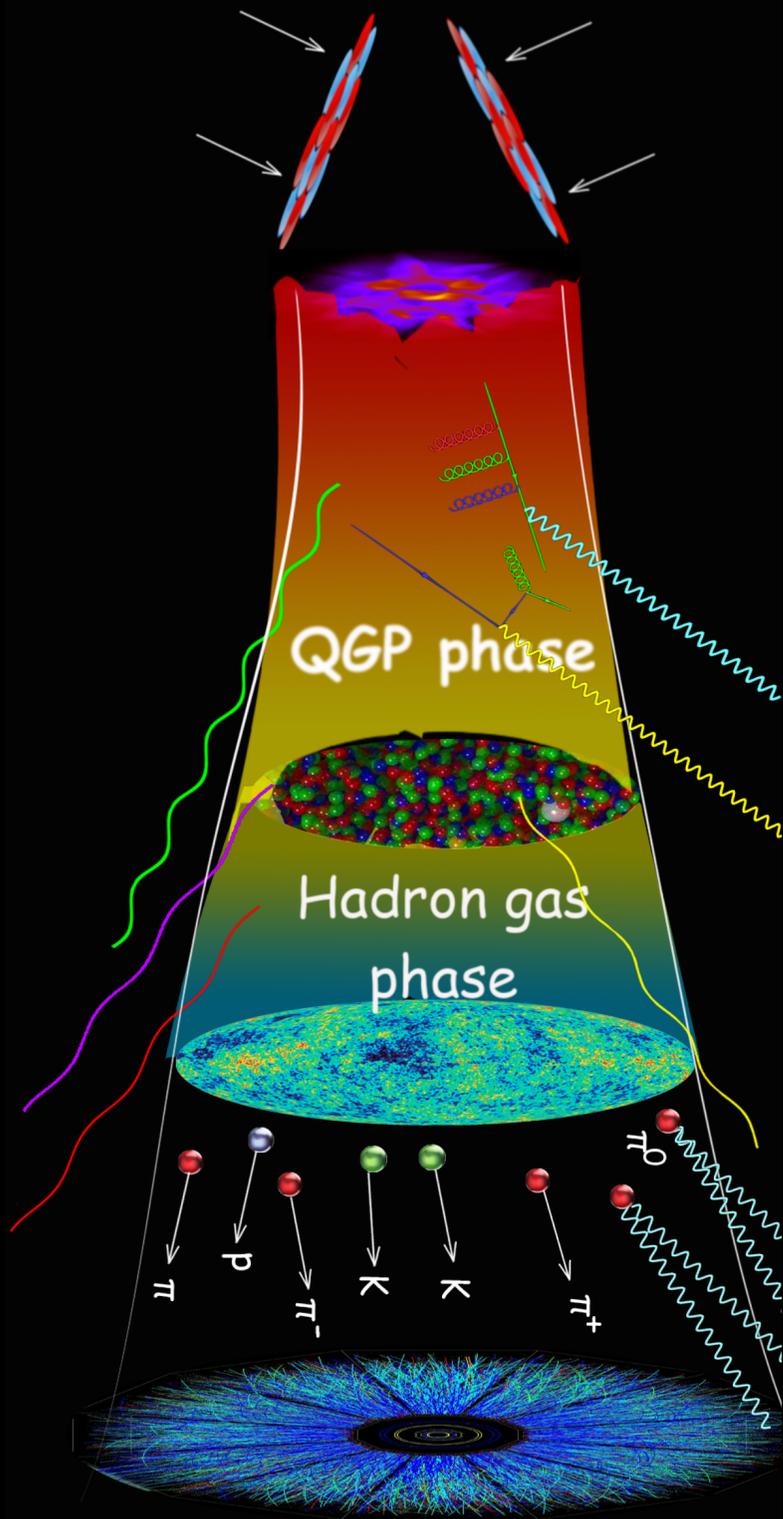


EM radiations



# DEFINING THE QUARK-GLUON PLASMA

Which **properties of hot QCD matter** can we determine from relativistic heavy ion data (LHC, RHIC, and future FAIR/NICA/JPAC)?



Equation of State  $T^{\mu\nu} \iff e, P, s$   
 $c_s^2 = \partial P / \partial e|_{s/n}$

Shear and bulk viscosities  
 $\eta/s(T, \mu_B), \zeta/s(T, \mu_B)$

Charge diffusion  $D_B, D_Q, D_S$

Electromagnetic emissivity

Energy-momentum transport  
 $\hat{q}, \hat{e}, \hat{e}_2, \dots$

Spectra, collective flow, femtoscopy

Anisotropic flow  $v_n$   
Flow correlations

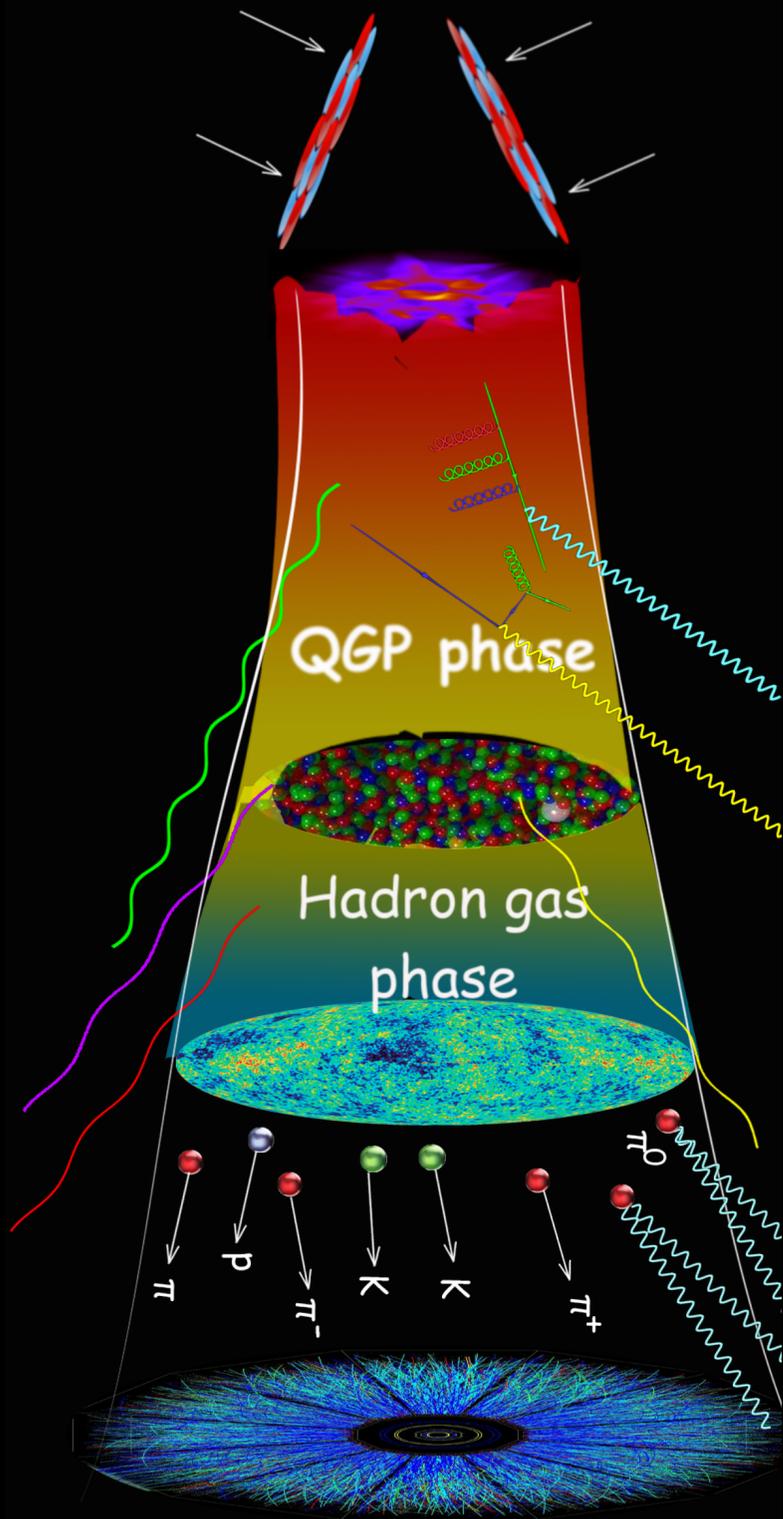
Balance functions

Photons and dileptons

Jets and heavy-quarks

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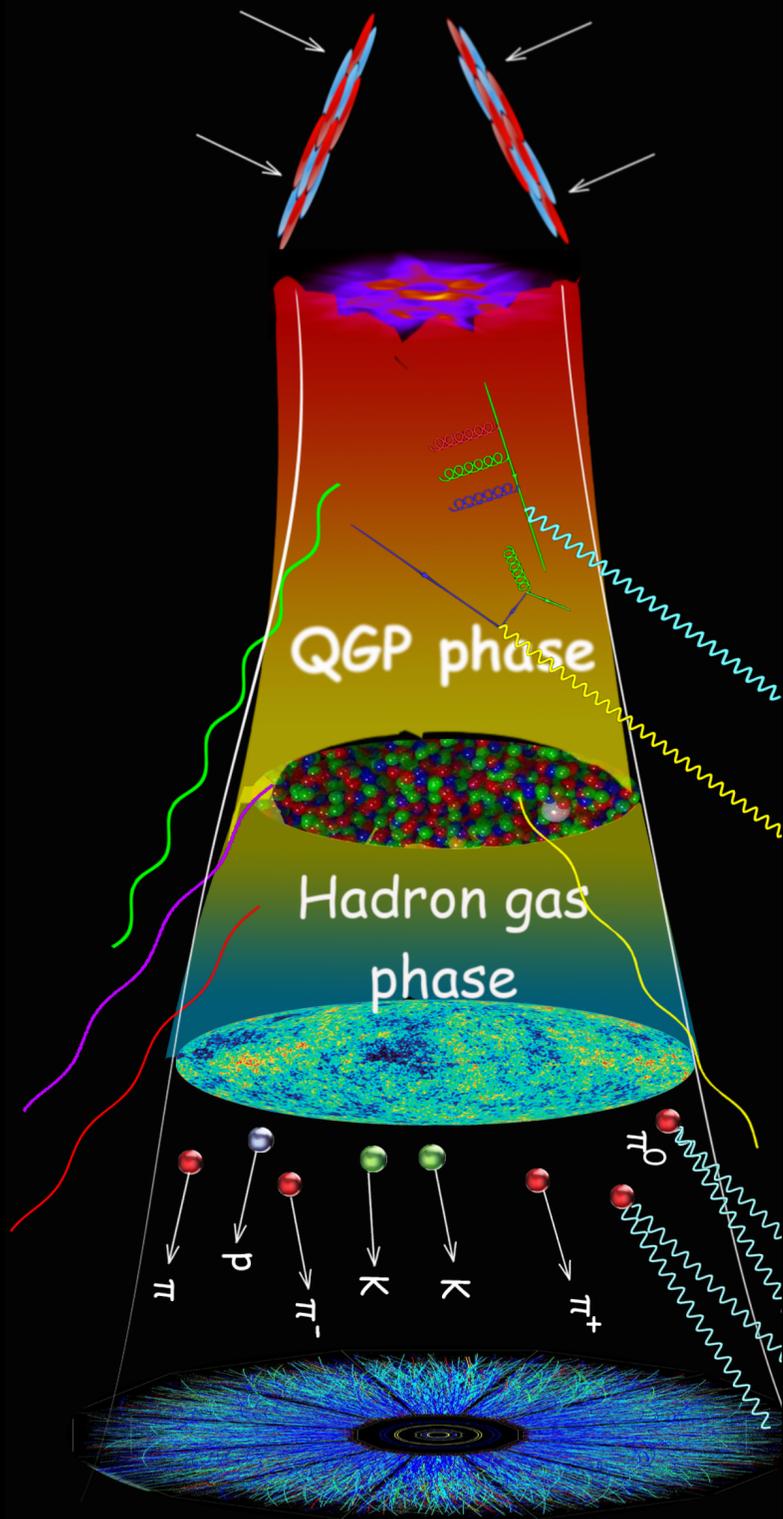
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Spectra, collective flow,  
femtoscscopy

Anisotropic flow  $v_n$   
Flow correlations

Balance functions

Photons and dileptons

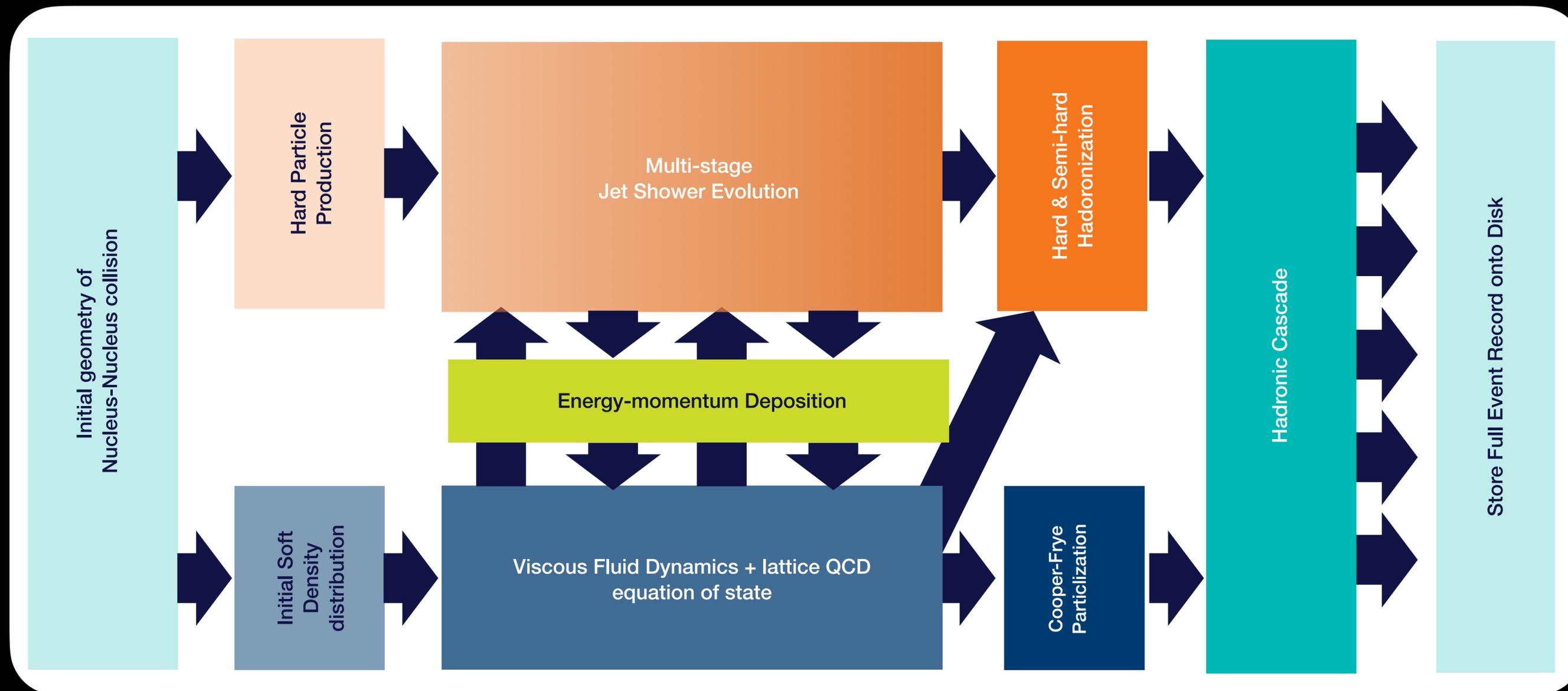
Jets and heavy-quarks

# THE JETSCAPE FRAMEWORK



“The JETSCAPE framework,” arXiv:1903.07706 [nucl-th]

- A unified event-generator for the high energy nuclear physics community



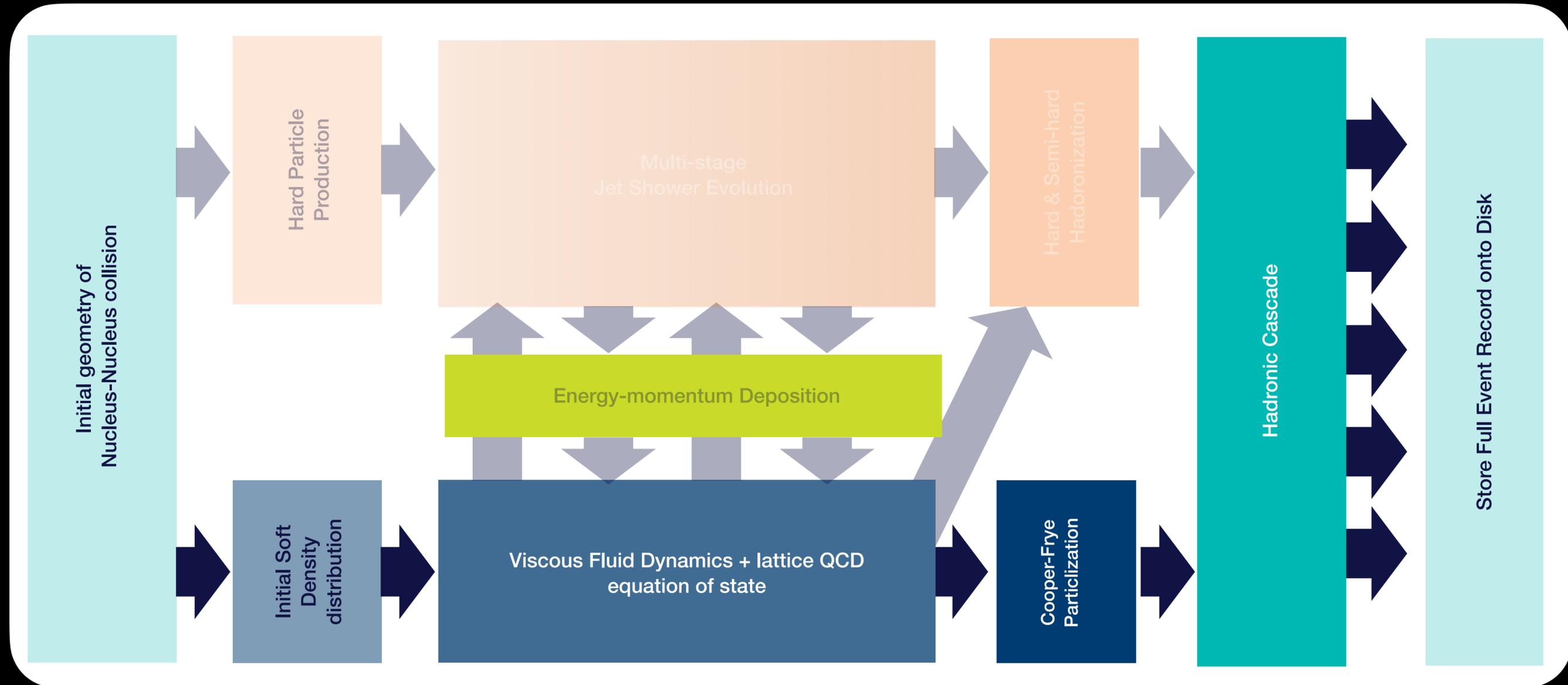
@ Y. Tachibana

# THE JETSCAPE FRAMEWORK



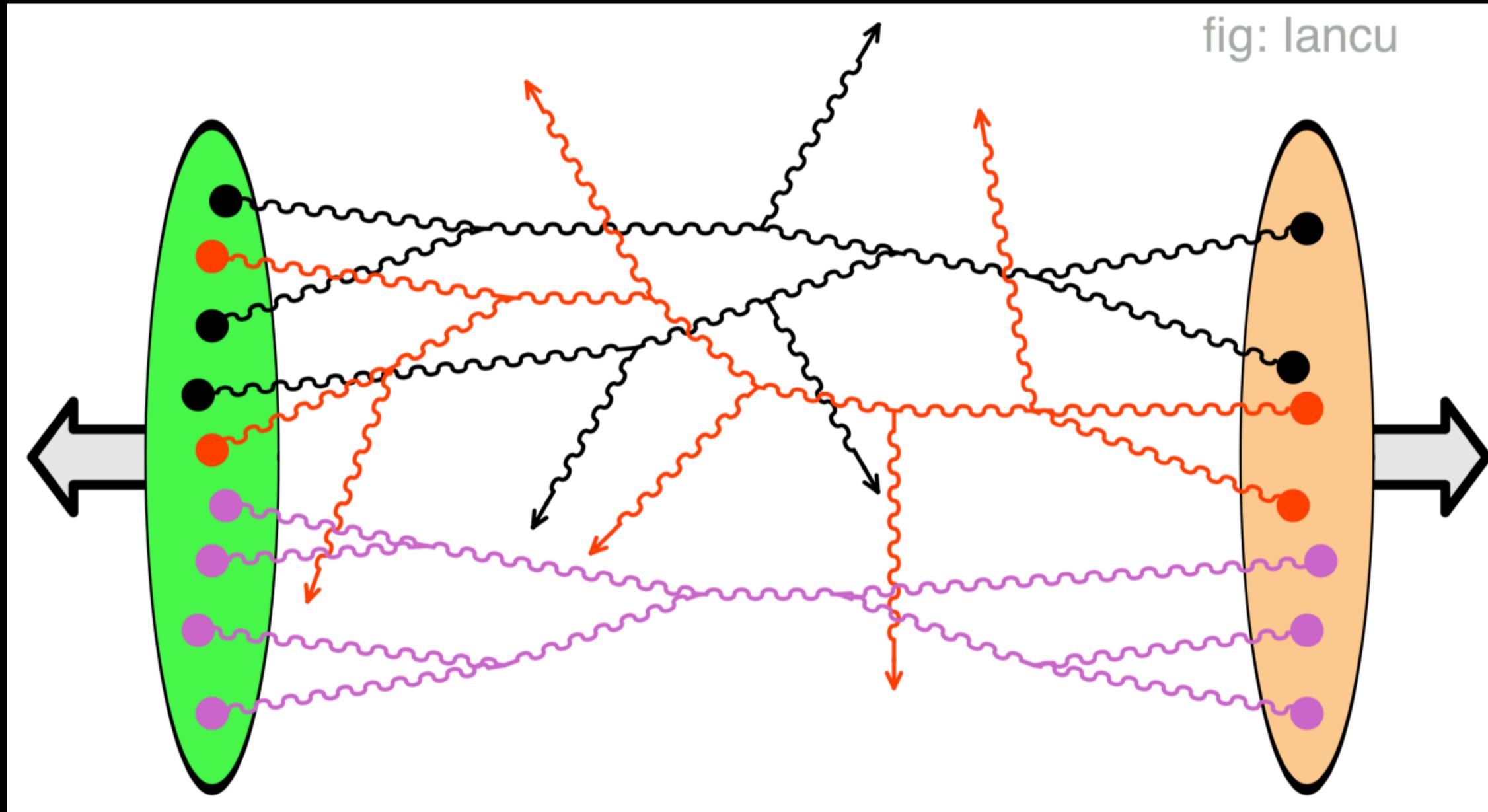
“The JETSCAPE framework,” arXiv:1903.07706 [nucl-th]

- A unified event-generator for the high energy nuclear physics community



@ Y. Tachibana

# INITIAL-STATE OF RELATIVISTIC NUCLEAR COLLISIONS



- Multiple scattering & soft processes dominate

highly non-perturbative

# A ZOO OF INITIAL-STATE MODELS

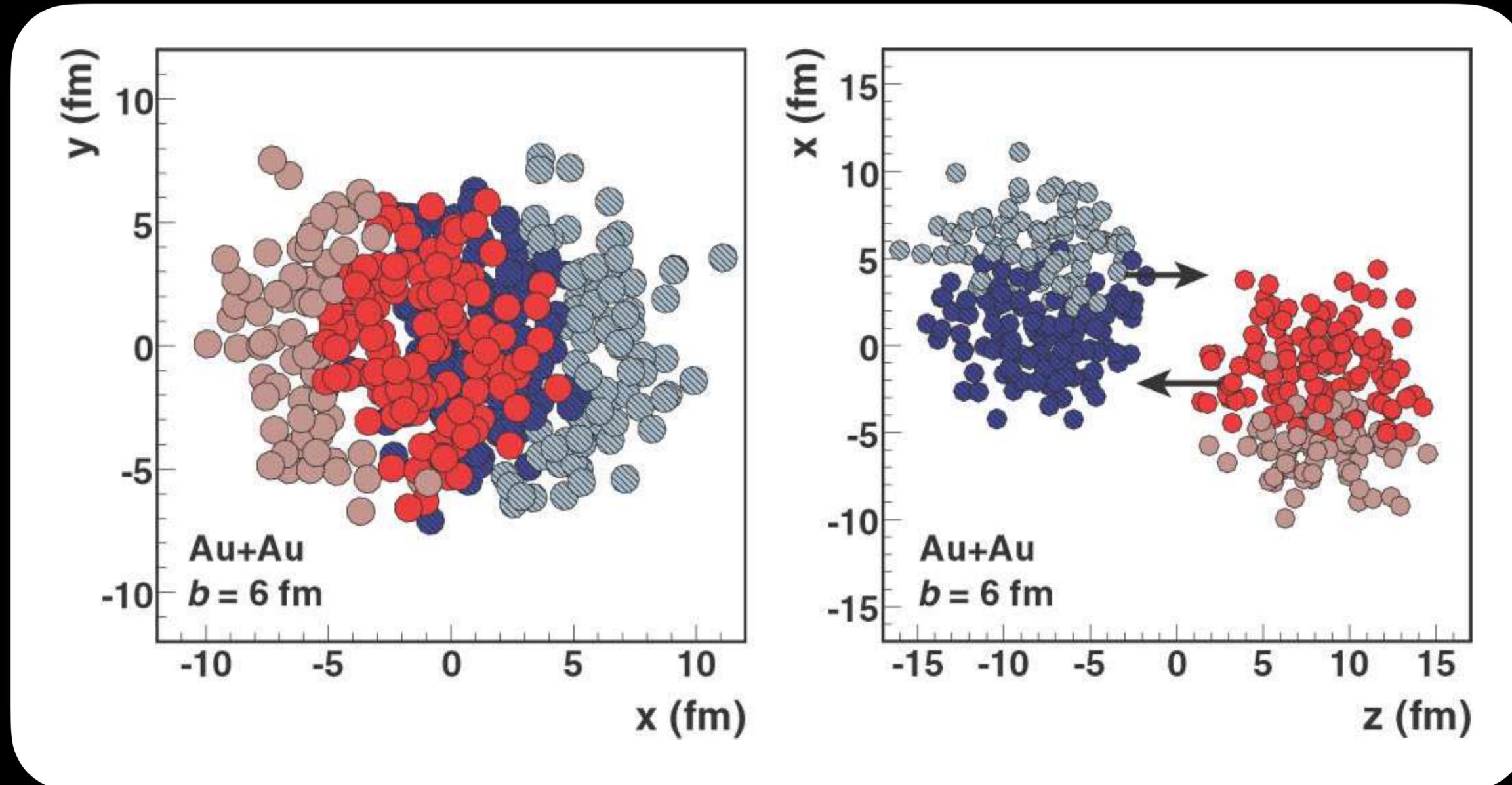


by P. Tribedy

# COLLISION GEOMETRY

Miller, Reygers, Sanders, Steinberg  
Ann. Rev. Nucl. Part. Sci. 57, 205 (2007)

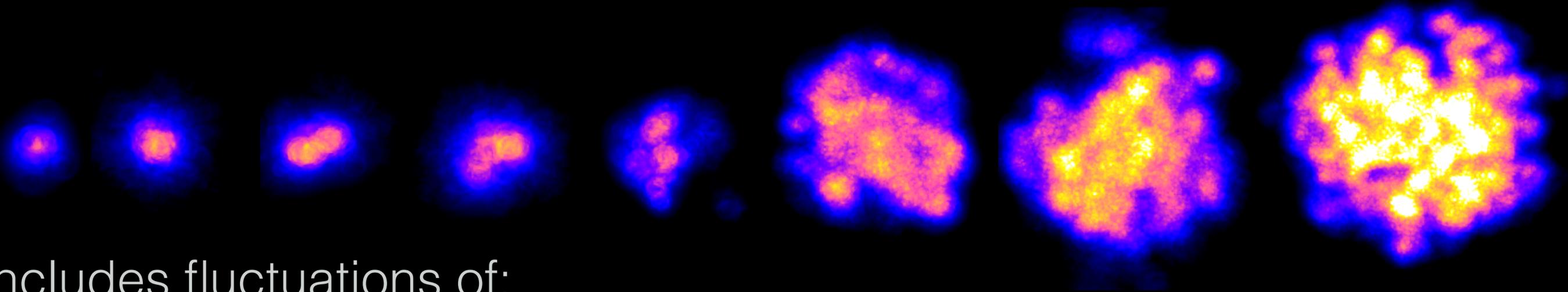
The Glauber model:



Participants in dark colors, spectators in light colors

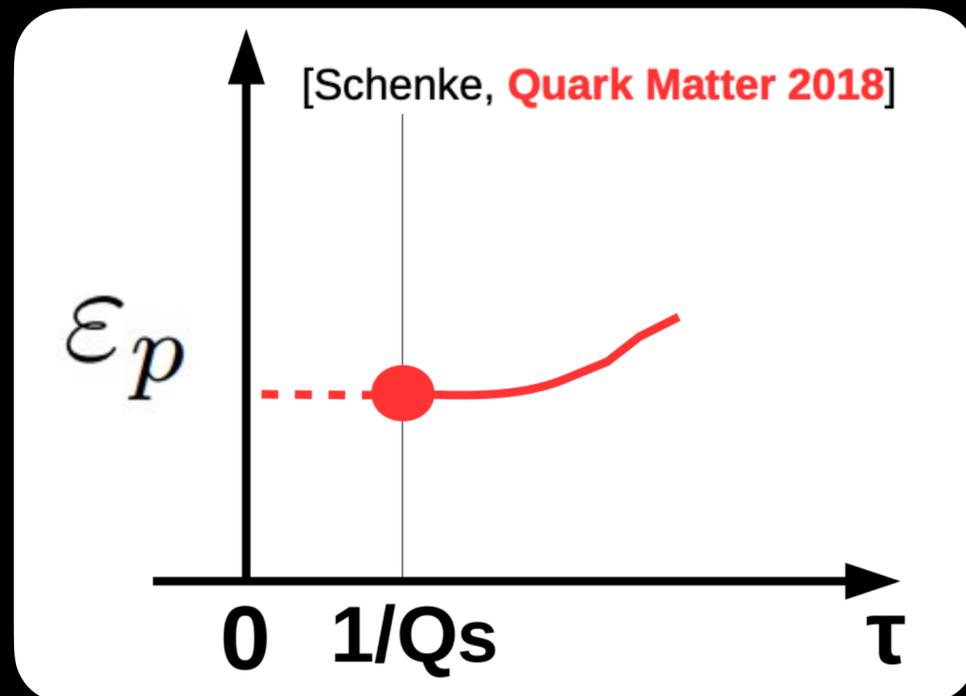
# INITIAL STATE AND PRE-EQUILIBRIUM DYNAMICS: IP-GLASMA

B.Schenke, P.Tribedy, R.Venugopalan, PRL108, 252301 (2012), PRC86, 034908 (2012)



Includes fluctuations of:

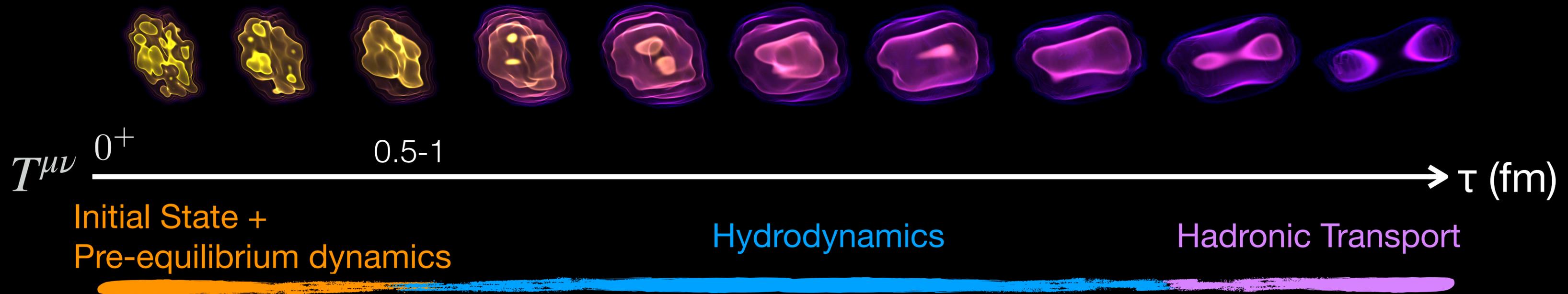
Impact parameter, nucleon positions, quark positions, color charge normalization, color charges



- The Color Glass Condensate (CGC) predicts anisotropic particle productions because of
  1. Local anisotropies in the color fields
  2. Local density gradients
  3. Quantum interference effects

$$\mathcal{E}_p = \varepsilon_p e^{i2\psi_2^p} = \frac{\langle T^{xx} - T^{yy} \rangle + i\langle 2T^{xy} \rangle}{\langle T^{xx} + T^{yy} \rangle}$$

# THE HYBRID THEORETICAL FRAMEWORK



$$T^{\mu\nu}_{\text{pre. eq}} = T^{\mu\nu}_{\text{hydro}}$$

+ Landau Matching  
with lattice EoS

Cooper-Frye  
particlization

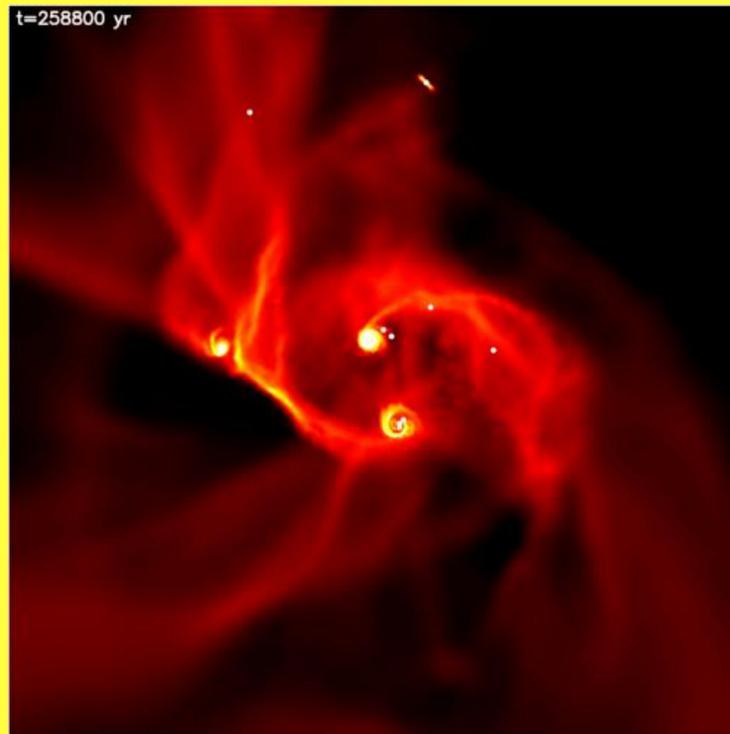
- Continuously connect the system's energy-momentum tensor  $T^{\mu\nu}$  between different stages

# COLLECTIVITY & HYDRODYNAMICS

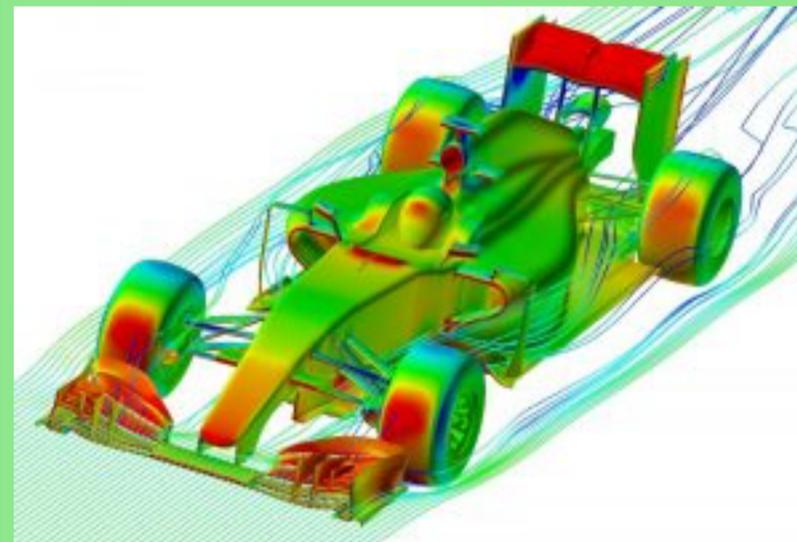
A long wavelength effective description of interacting systems

Conservation  
laws  
+  
Equation of  
State

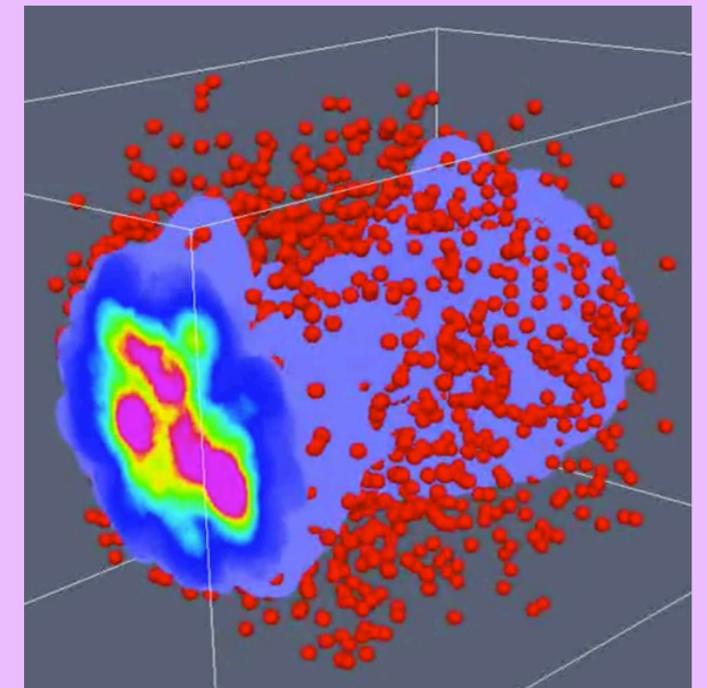
Star formation



Air dynamics of  
race car



Quark-Gluon  
Plasma



Studying collective phenomena in heavy-ion collisions has been **leading** the theory frontier of developing causal viscous relativistic hydrodynamics

# A REALIZATION OF RELATIVISTIC HYDRODYNAMICS

*Top*

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PUBLICATIONS

ABOUT

OUR TEAM

CONTACT

<http://www.physics.mcgill.ca/music/>

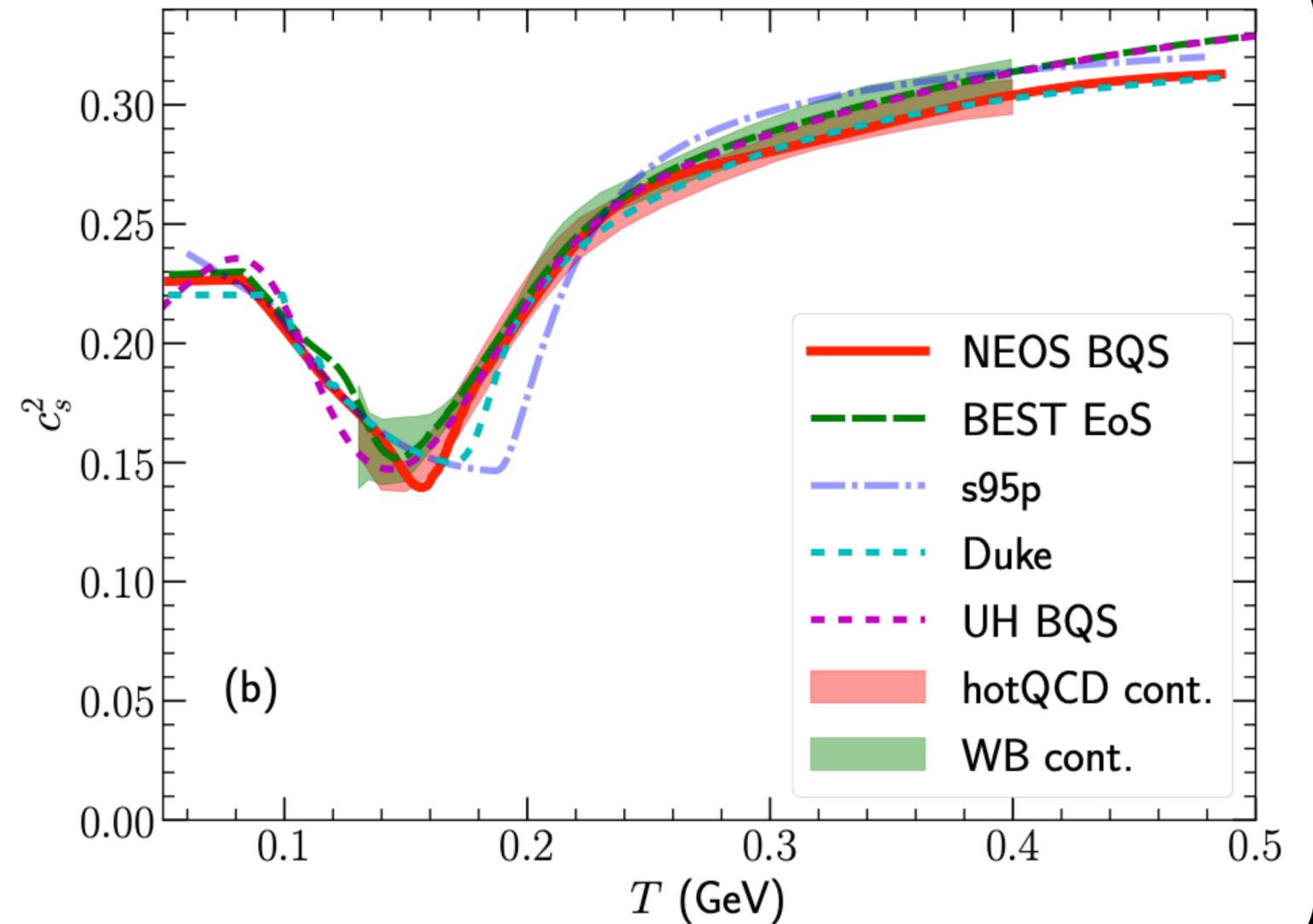
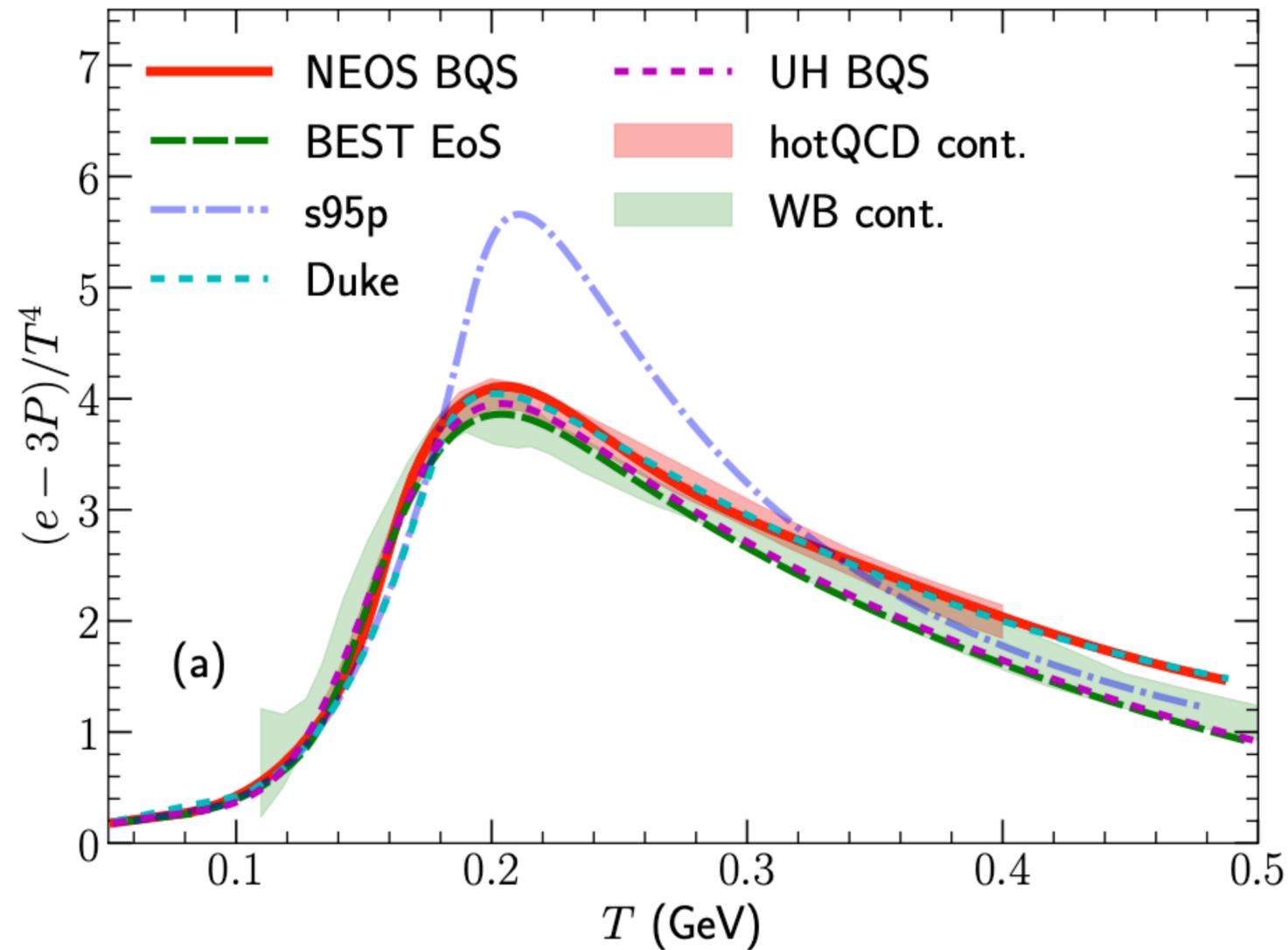
## MUSIC

*A (3+1)D hydrodynamic code for heavy-ion collisions*

DOWNLOAD

# QCD EQUATION OF STATE

A. Monnai, B. Schenke and C. Shen, Int. J. Mod. Phys. A36, 2130007 (2021)



- QCD equation of state are constrained by Lattice QCD calculations

# PRESSURE GRADIENTS DRIVEN DYNAMICS

$\tau = 0.40 \text{ fm}/c$

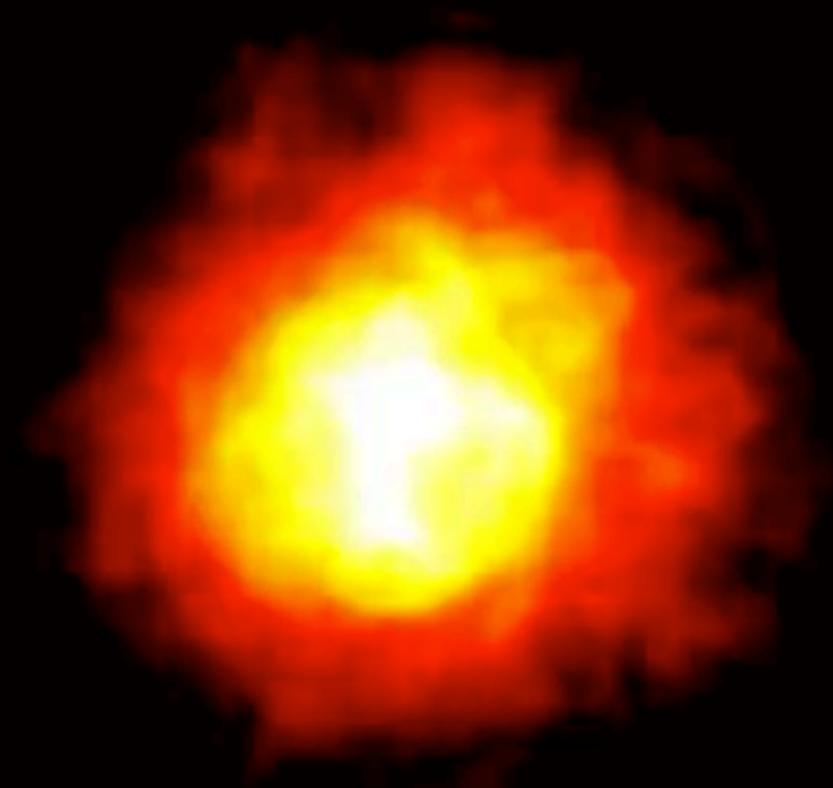
$$Du^\mu = \frac{\nabla^\mu P}{e + P}$$

acceleration

force

moment of inertia

Spatial inhomogeneity  $\rightarrow$  Flow velocity



1 fm

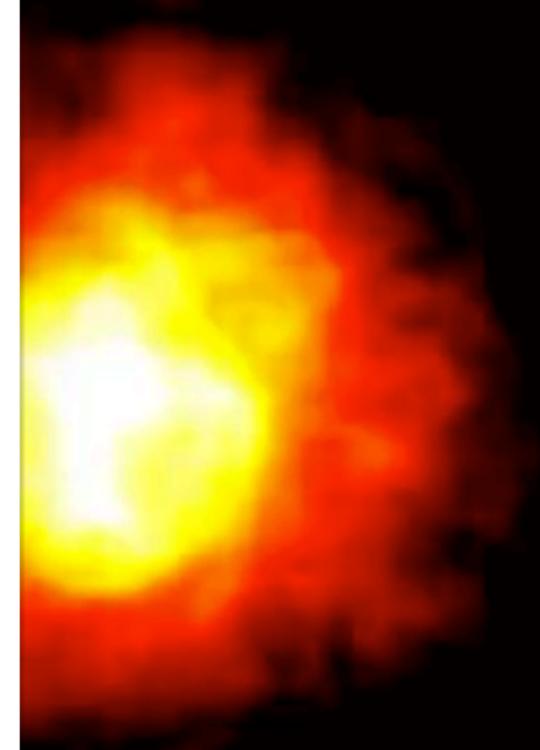
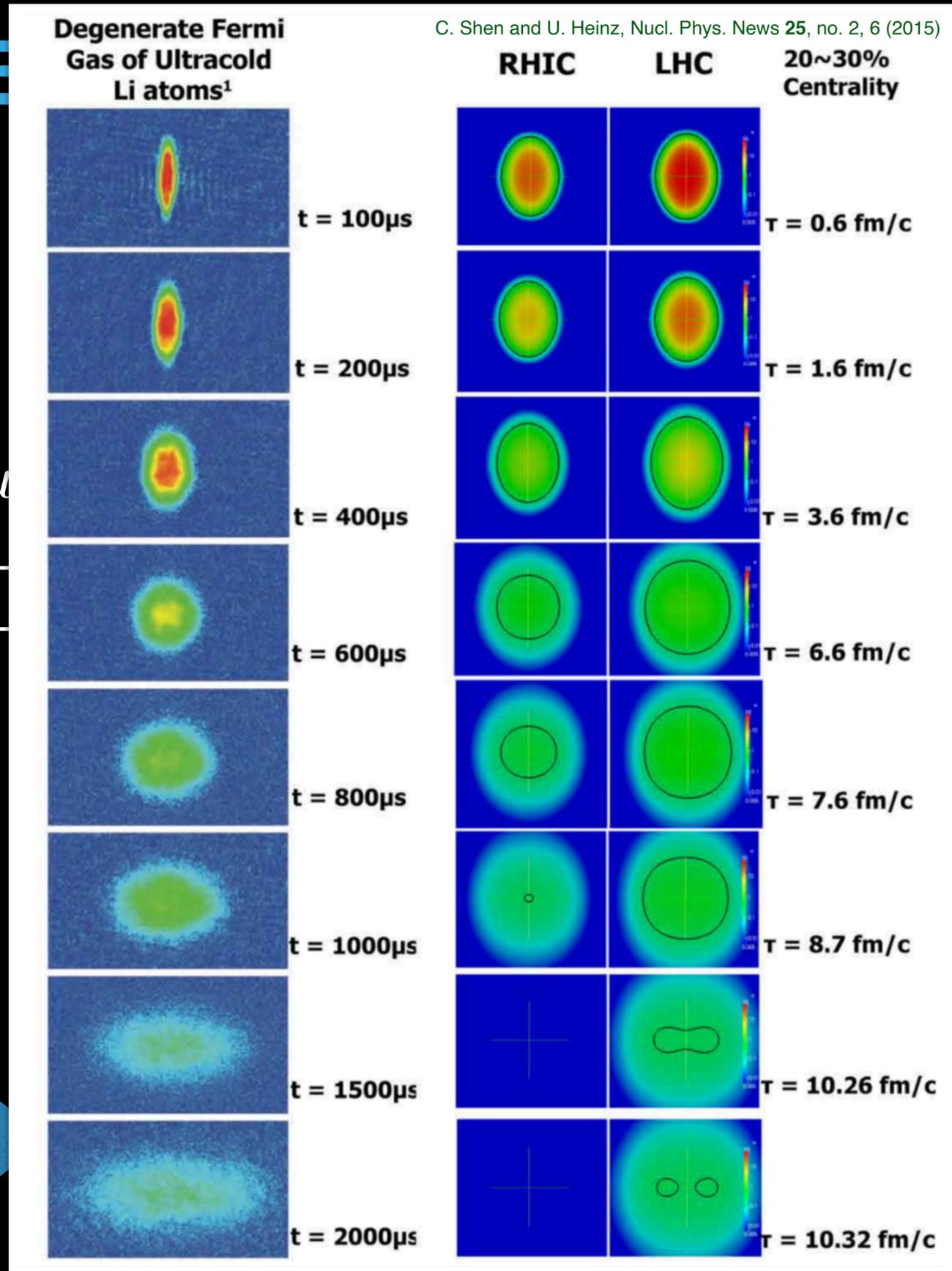
# PRESSURE

# DYNAMICS

$$Du^\mu = \frac{\nabla^\mu \mu}{e + p}$$

acceleration

Spatial  
inhomogeneity



# STUDY QGP TRANSPORT PROPERTIES

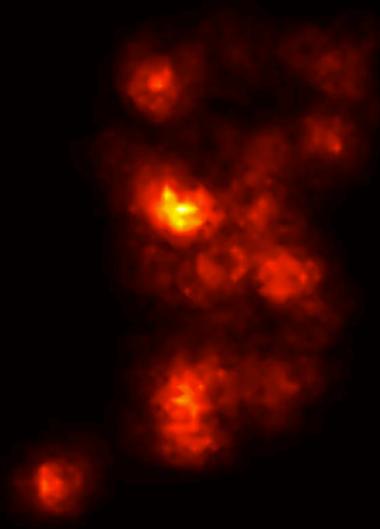
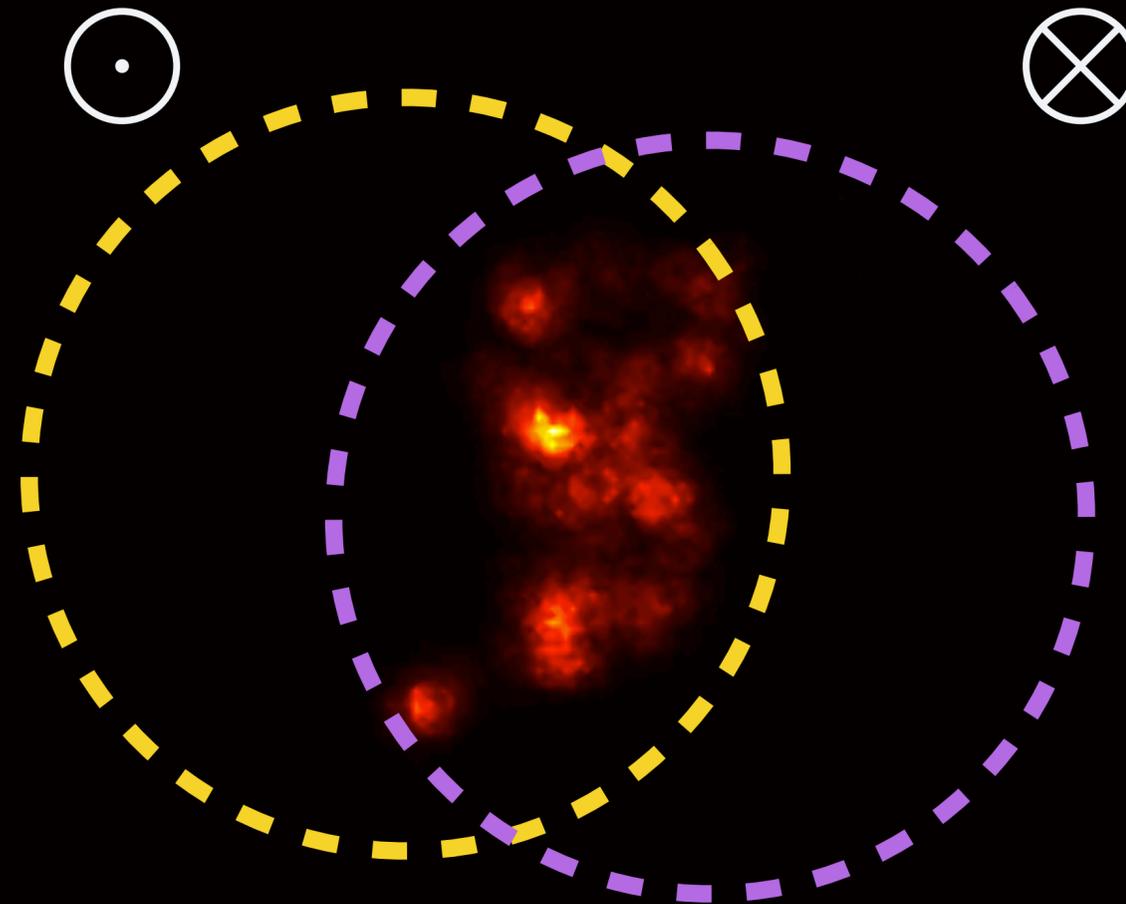
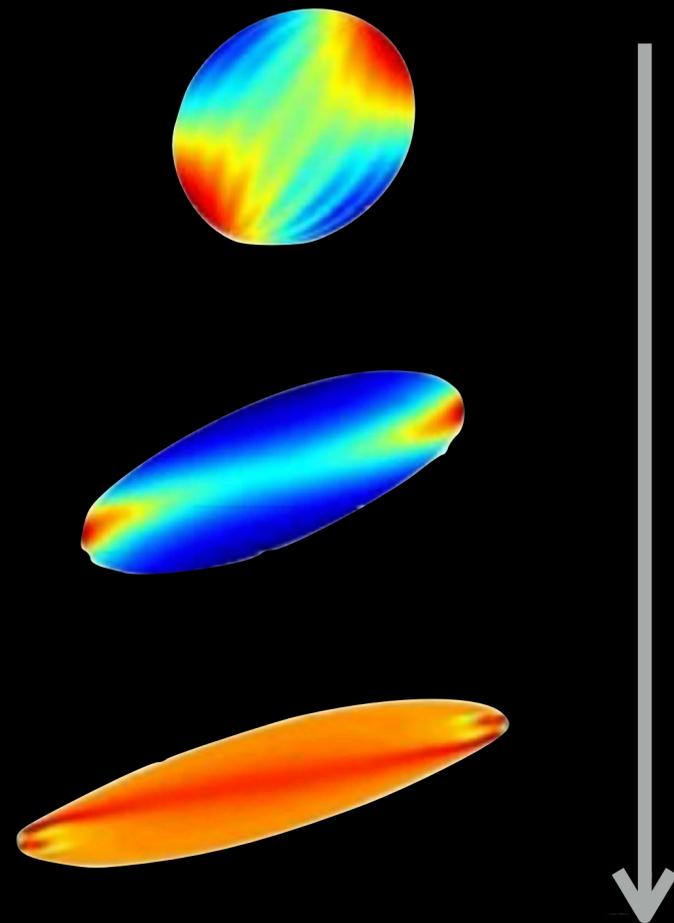
<https://youtu.be/G-Fbon0YQak>

Shear viscosity

no shear viscosity

with shear viscosity

Resistance to deformation  
 $\sim 2\eta \nabla \langle \mu u^\nu \rangle$



Shear viscosity smears out the fine flow patterns  
Flow anisotropy is imprinted to final state particle momenta

# EFFECTS OF BULK VISCOSITY

<https://youtu.be/G-Fbon0YQak>

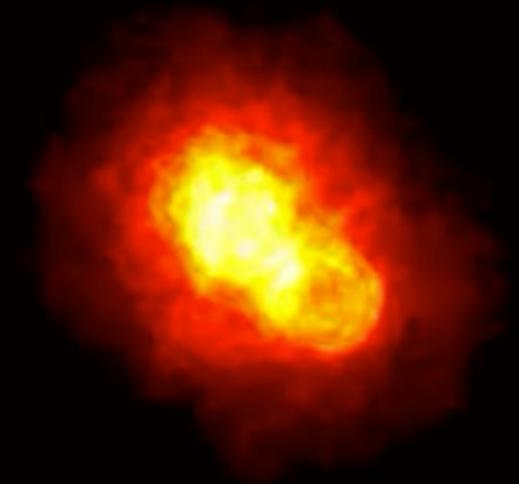
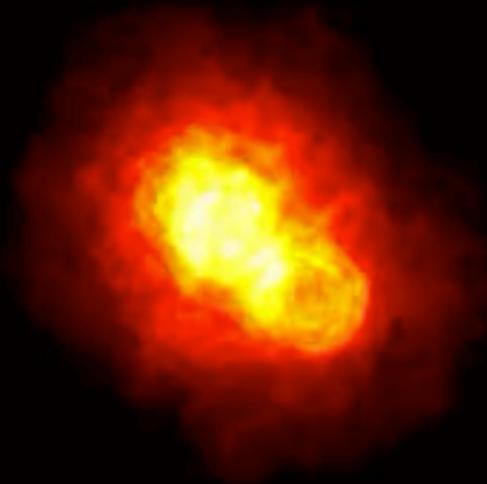
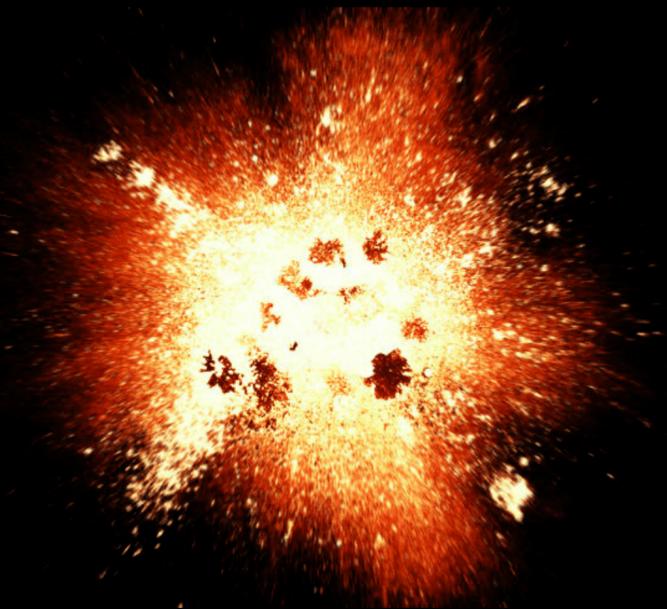
Bulk viscosity

no bulk viscosity

with bulk viscosity

Resistance to  
expansion

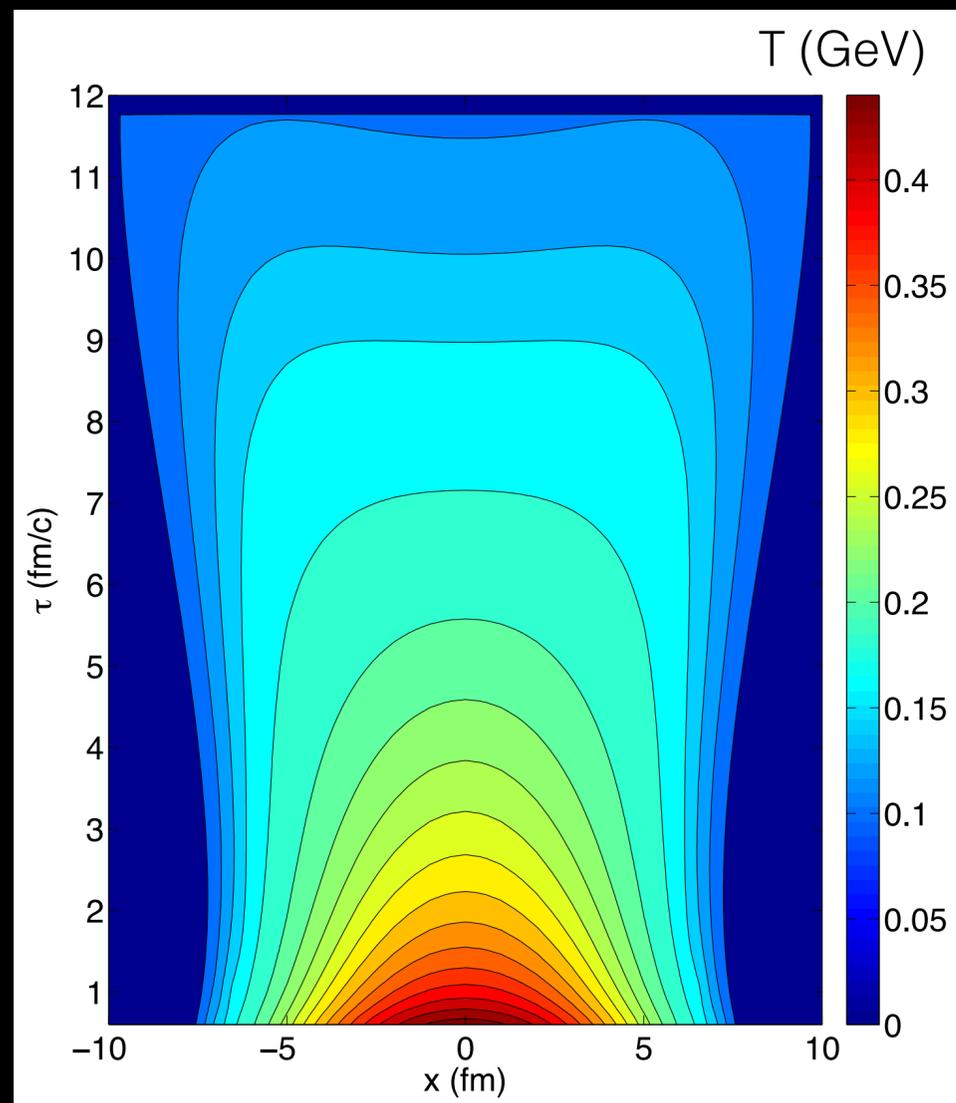
$$\sim -\zeta \partial_{\mu} u^{\mu}$$



- Bulk viscosity slows down radial expansion and produces more entropy

# WHEN TO END?

- Particles are observed, not fluid elements
- How and when to convert fluid to particles (evaporation)
- How far is hydrodynamics valid?



Kinetic equilibrium requires

Scattering rate  $\gg$  expansion rate

$$\tau_{sc}^{-1} \sim \sigma n \propto \sigma T^3 \quad \theta = \partial_\mu u^\mu$$

Fluid description breaks down at

$$\tau_{sc}^{-1} = \theta$$

Approximation: decoupling takes place at a fixed temperature

$$T = T_{fo} \propto \left( \frac{\theta}{\sigma} \right)^{1/3}$$

# COOPER-FRYE PARTICLIZATION

Sample particles on the freeze-out surface (surface of constant (low) energy density) according to

$$E \frac{dN_i}{d^3p} = \frac{g_i}{(2\pi)^3} \int_{\Sigma(T_{fo})} d^3\sigma_\mu p^\mu \left( f_{eq}^i \left( \frac{p^\mu u_\mu}{T} \right) + \delta f^i \right)$$

then feed particles into hadronic cascade (UrQMD/SMASH)

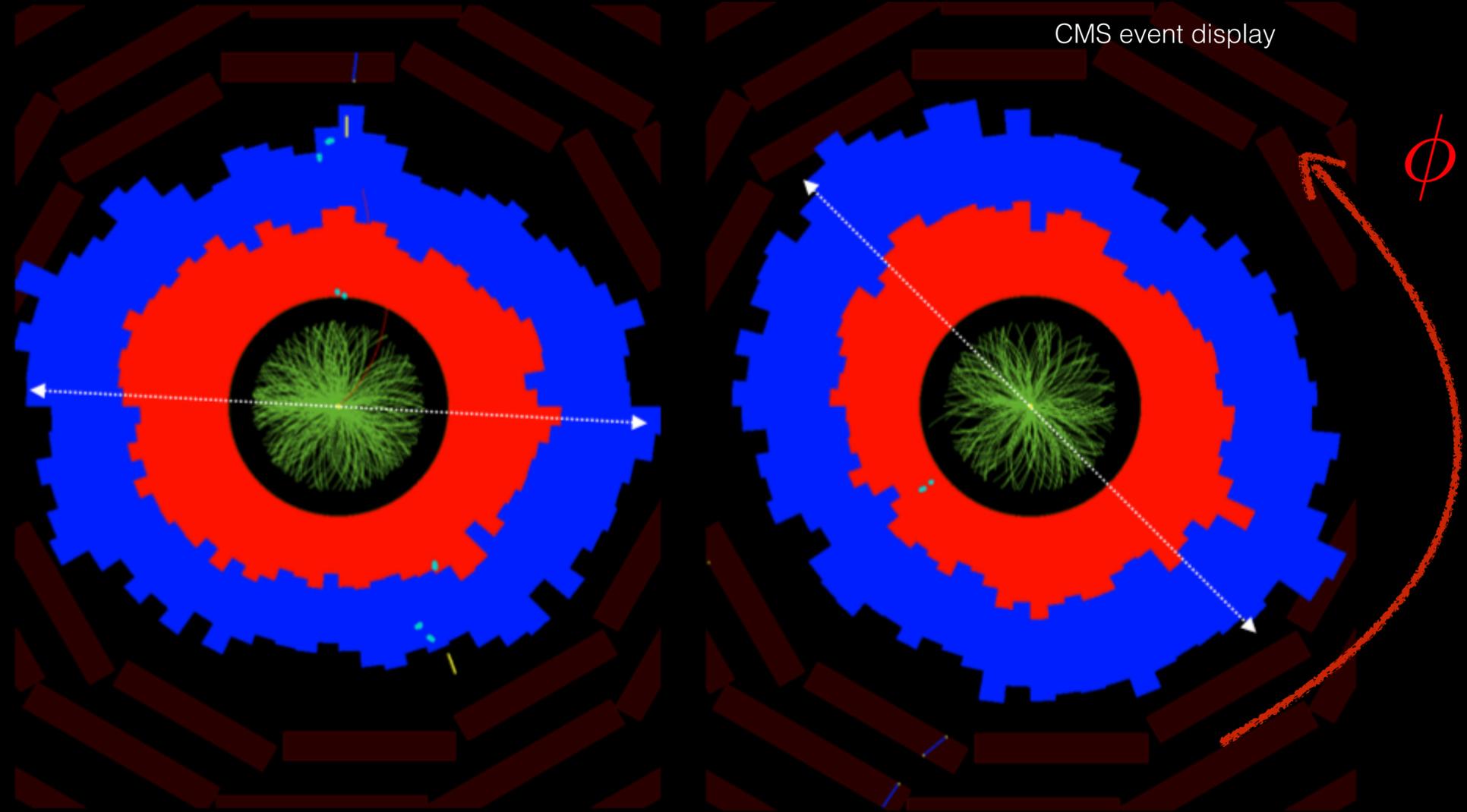
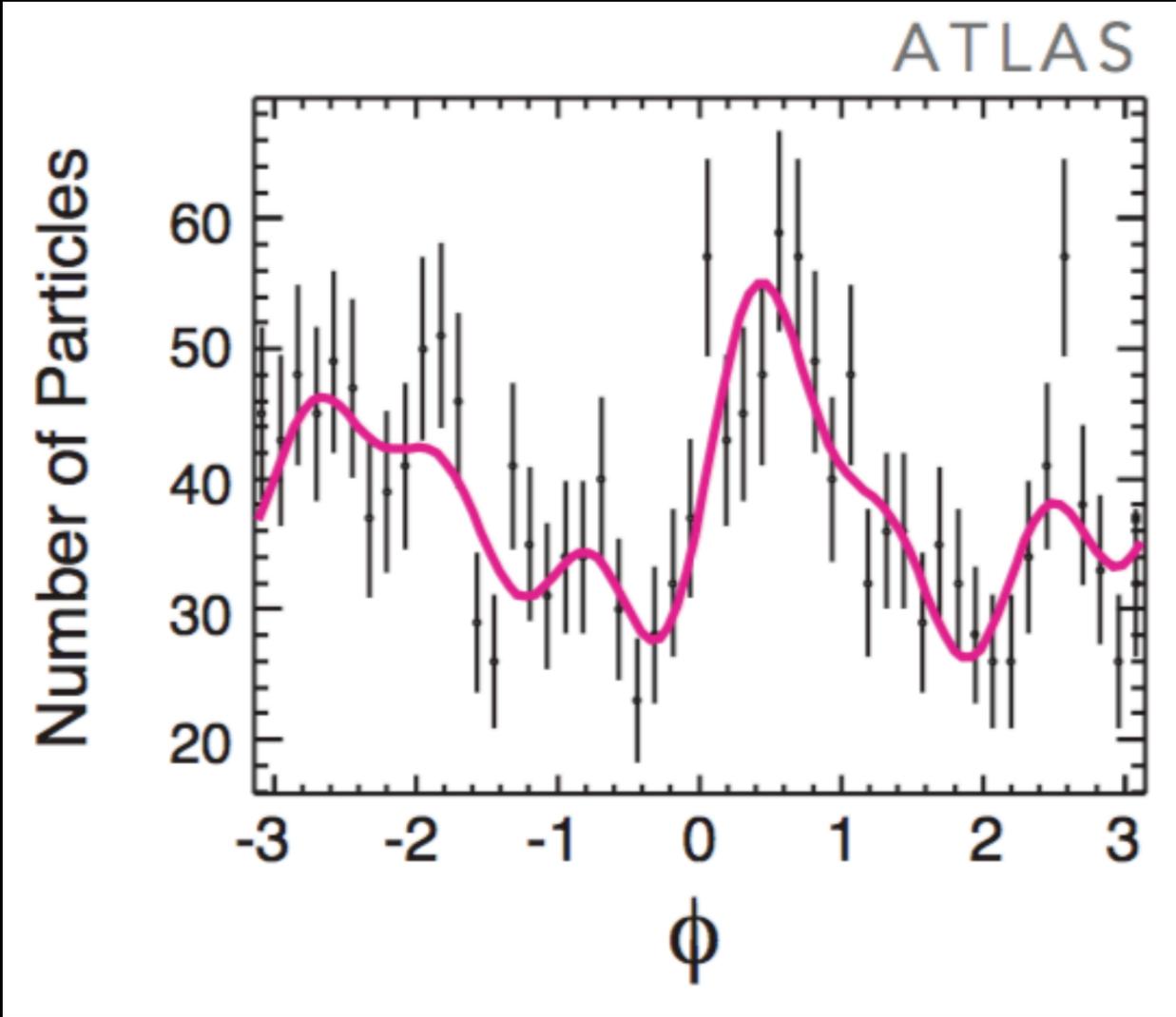
S. A. Bass et al., Prog. Part. Nucl. Phys. 41, 255–369 (1998)

M. Bleicher et al., J. Phys. G25, 1859–1896 (1999)

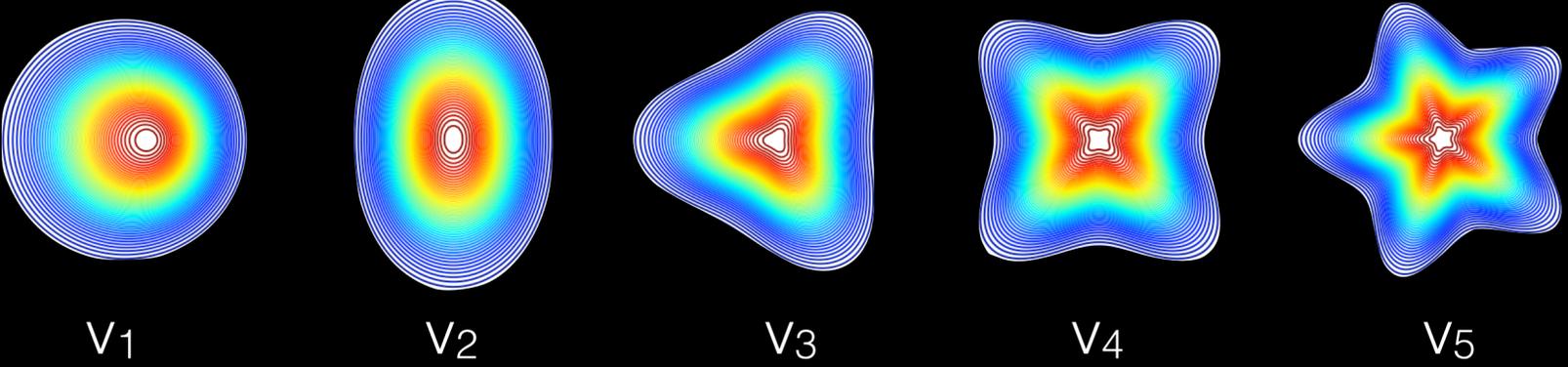
J. Weil, et al. Rev. C 94, 054905 (2016)

which performs resonance decays and scattering according to hadronic cross sections

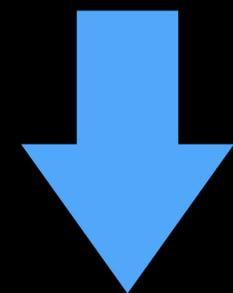
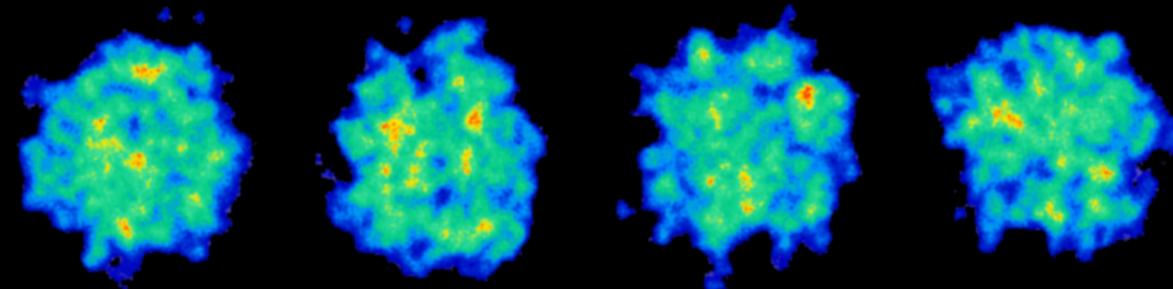
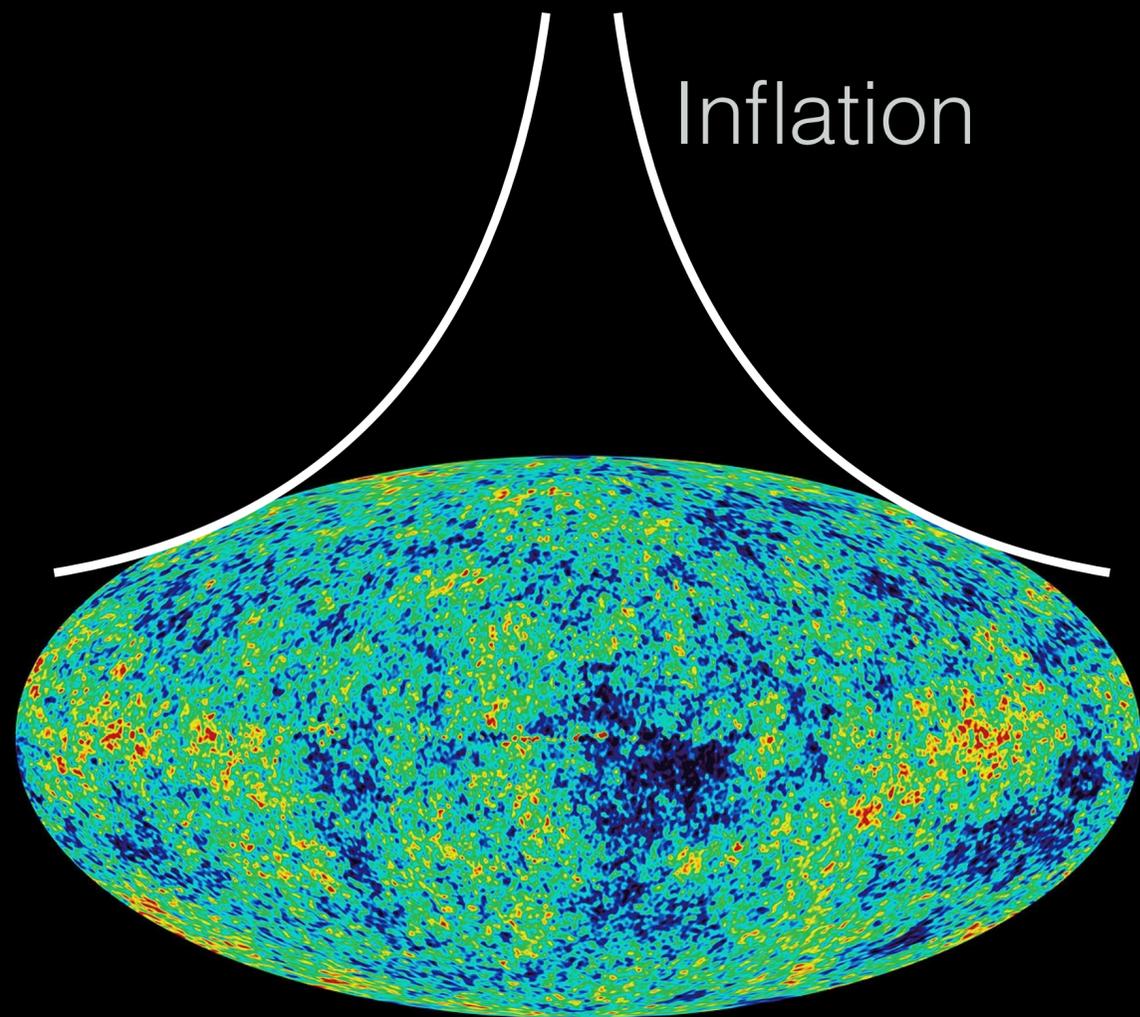
# ANISOTROPIC FLOW



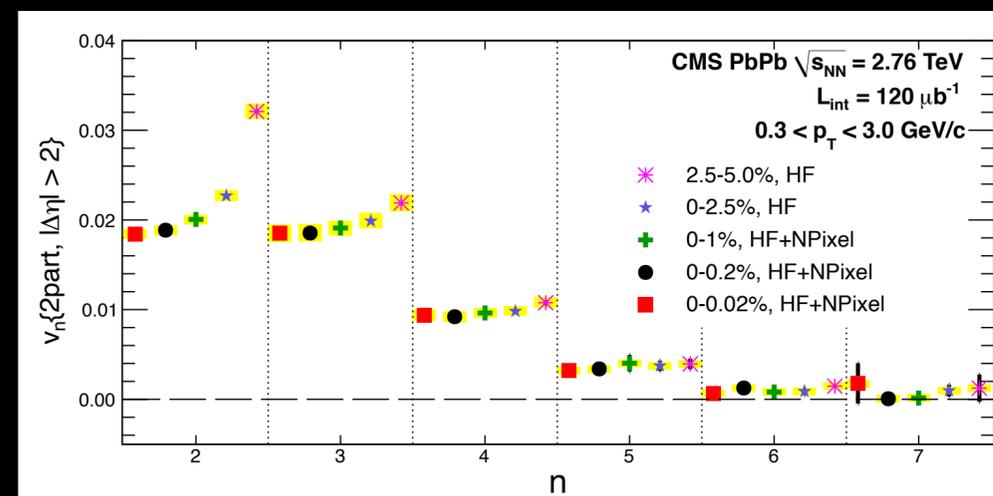
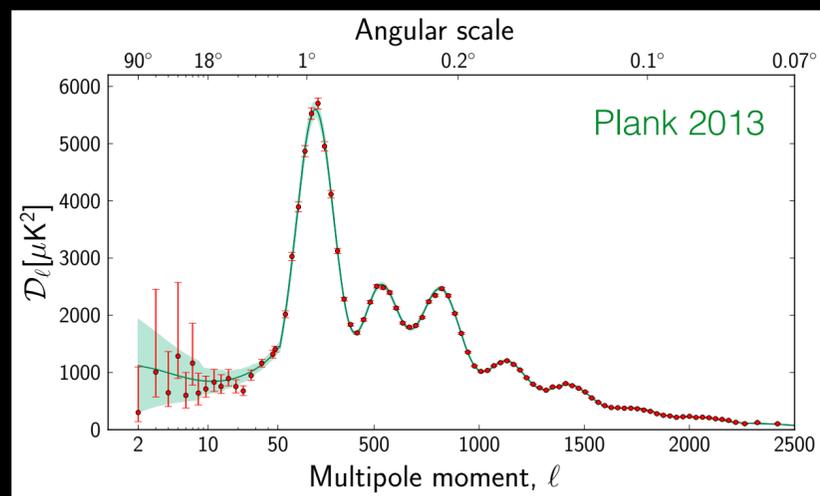
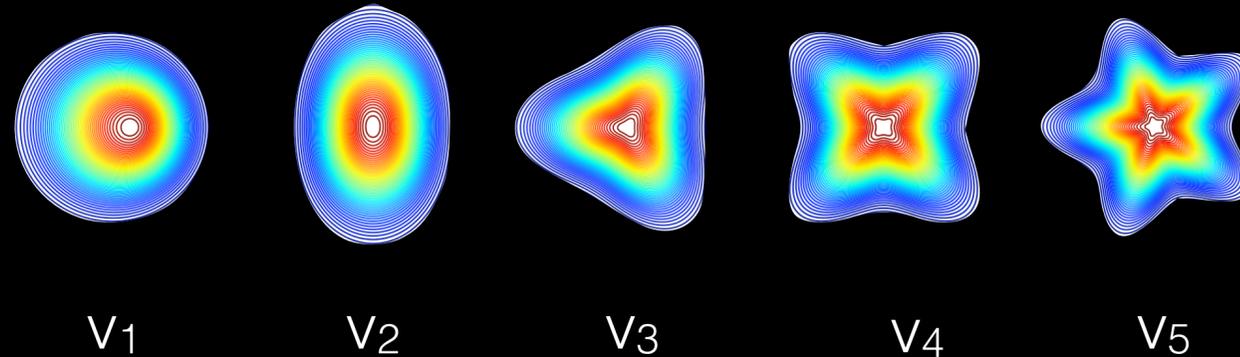
$$\frac{dN}{d\phi} = \frac{N}{2\pi} \left( 1 + 2 \sum_{n=1}^{\infty} v_n \cos(\phi - \Psi_n) \right)$$



# FLUCTUATION POWER SPECTRUM

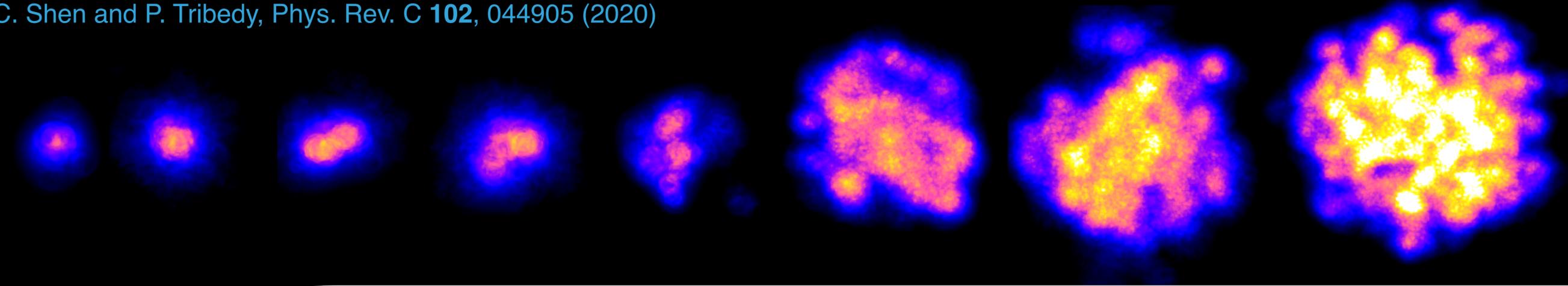


Hydrodynamics

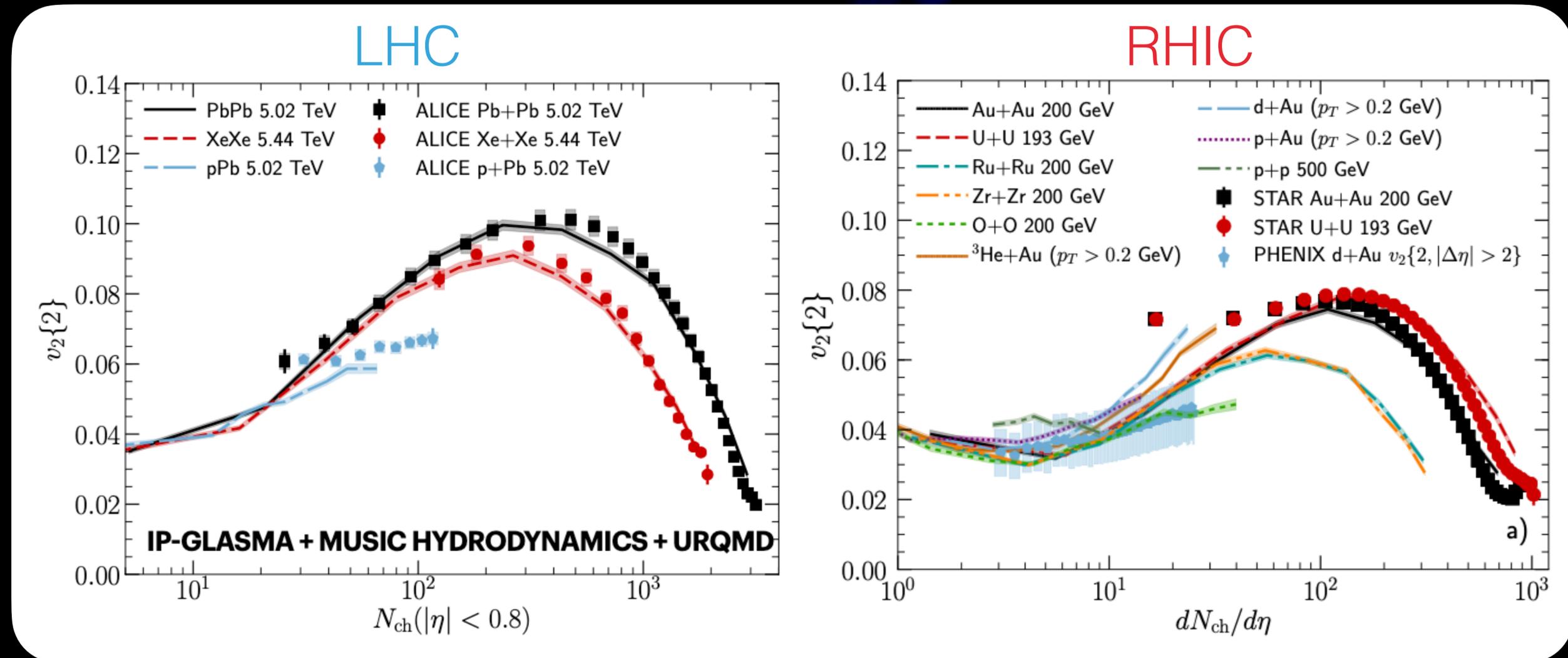


# RUNNING THE GAMUT OF HIGH ENERGY NUCLEAR COLLISIONS

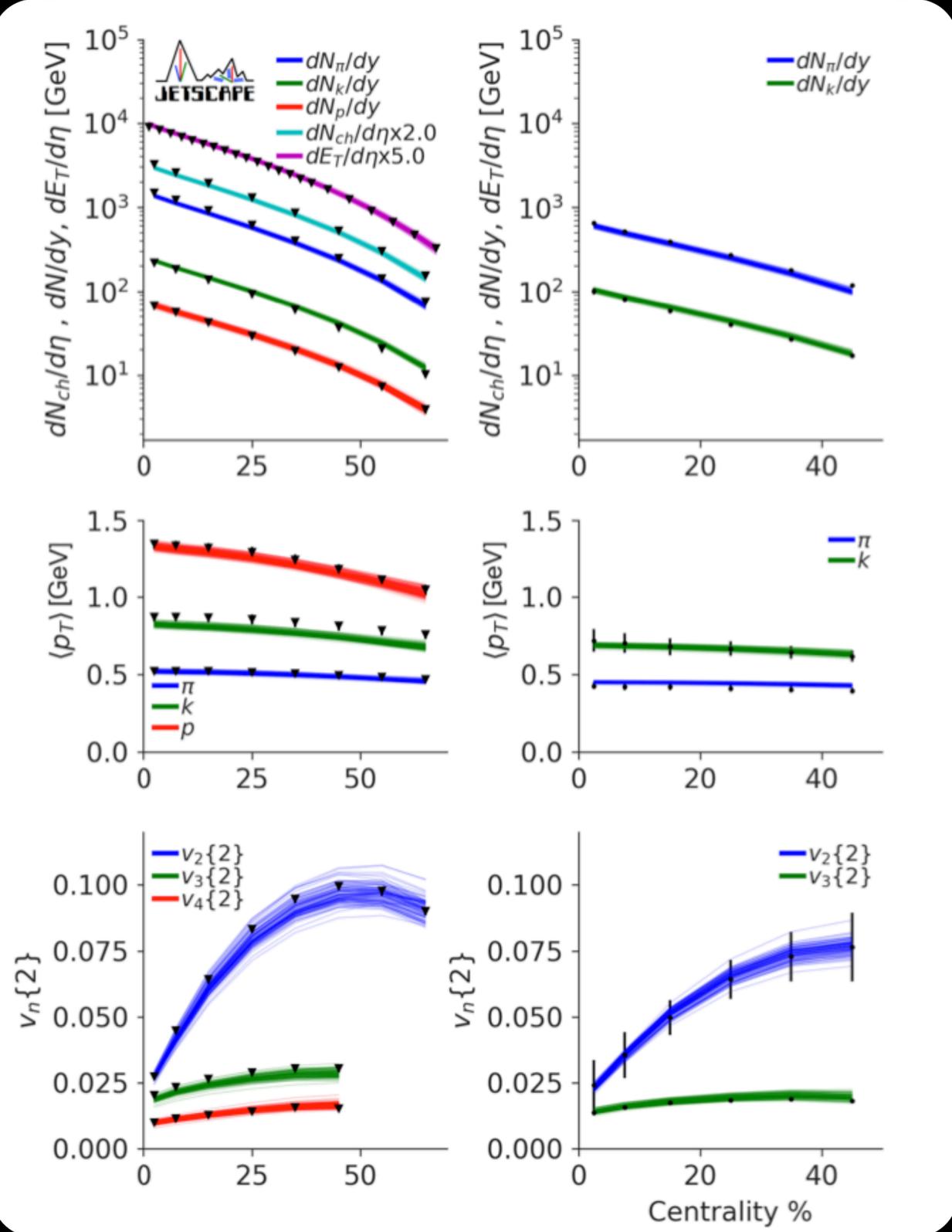
B. Schenke, C. Shen and P. Tribedy, Phys. Rev. C **102**, 044905 (2020)



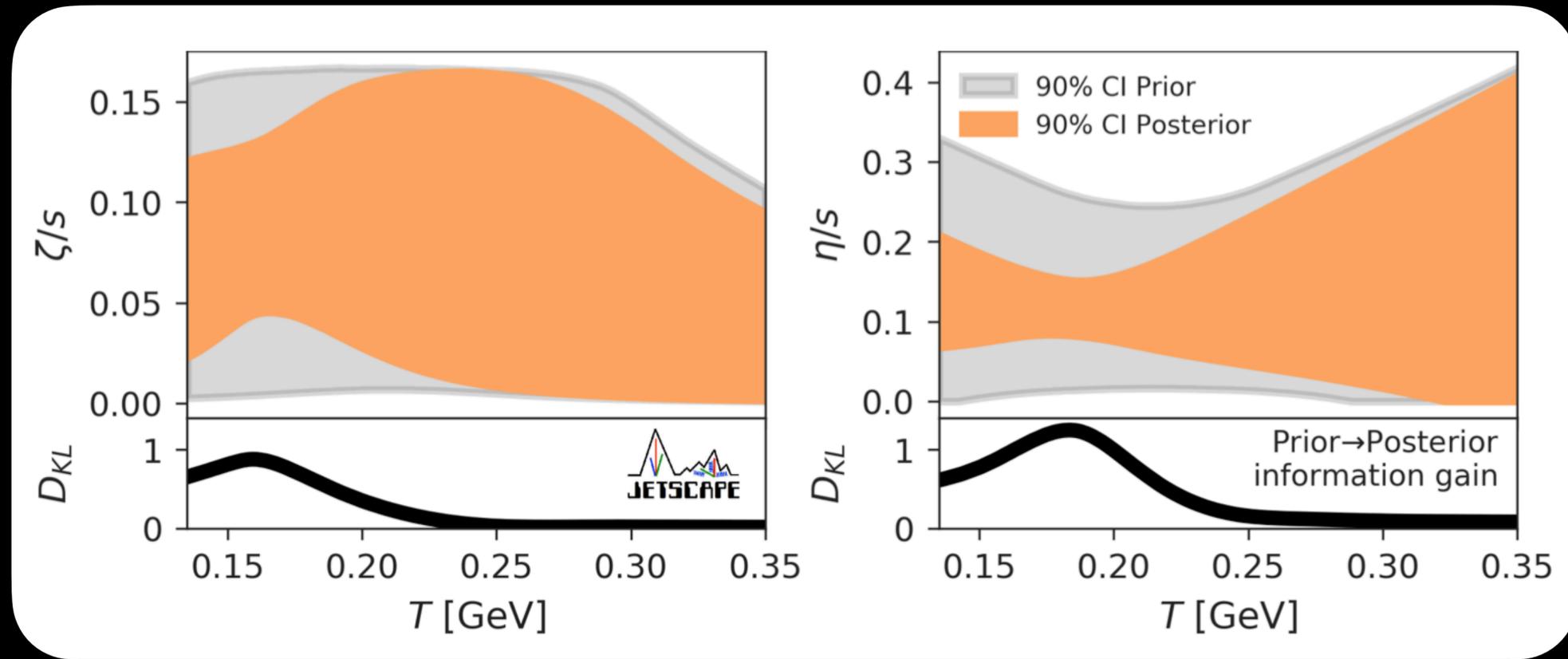
- One single set of model parameters for *ALL* types of collisions at the top RHIC and LHC energies



# GLOBAL BAYESIAN CONSTRAINTS ON QGP VISCOSITY

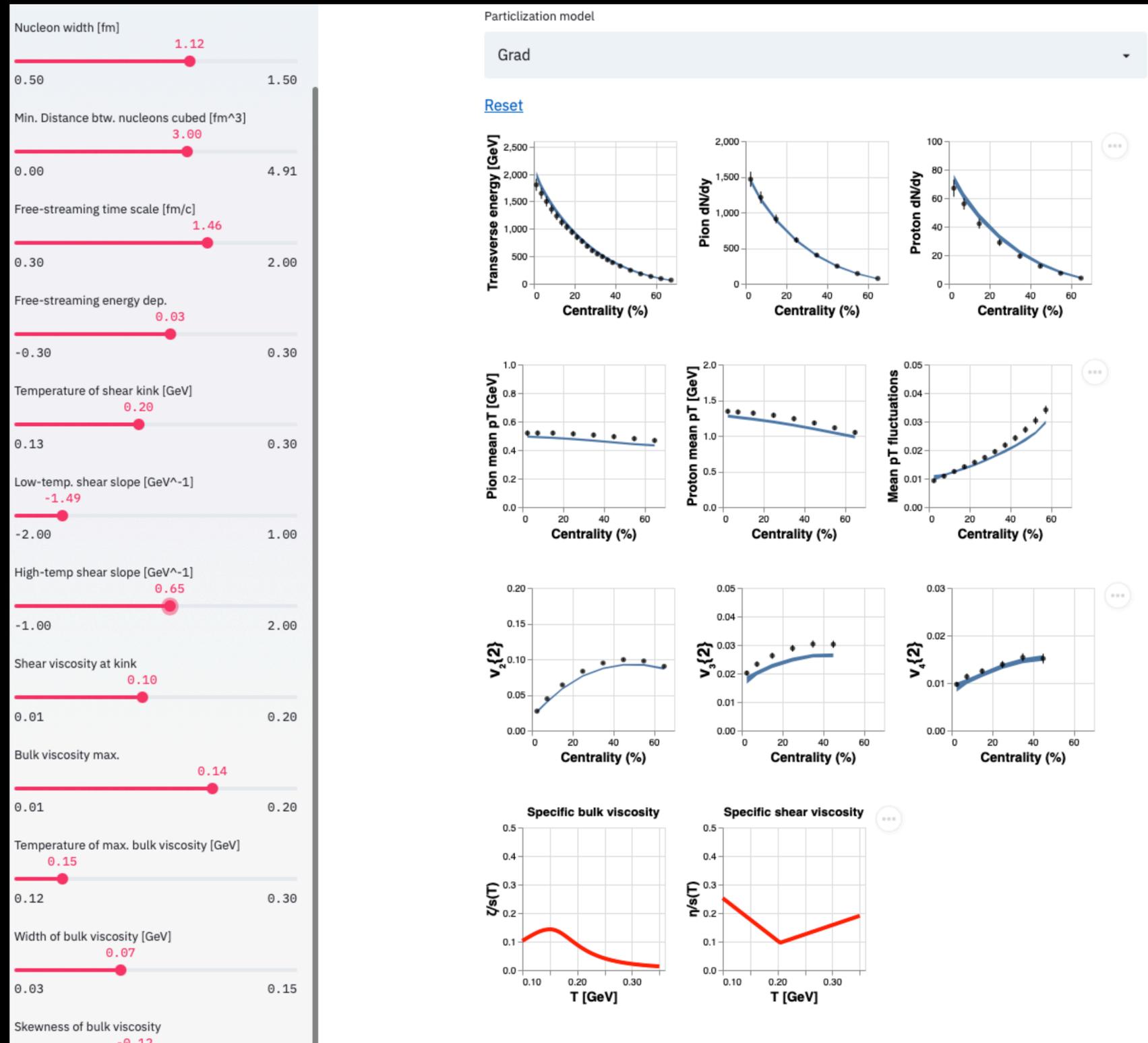


S. Pratt, E. Sangaline, P. Sorensen and H. Wang, Phys. Rev. Lett. 114, 202301 (2015)  
 J. E. Bernhard, J. S. Moreland, S. A. Bass, J. Liu and U. Heinz, Phys. Rev. C94, 024907 (2016)  
 J. E. Bernhard, J. S. Moreland and S. A. Bass, Nature Phys. 15, 1113-1117 (2019)  
 G. Nijs, W. Van Der Schee, U. Gürsoy and R. Snellings, Phys. Rev. Lett. 126, 202301 (2021) & Phys. Rev. C103, 054909 (2021)  
 D. Everett *et al.* [JETSCAPE], Phys. Rev. Lett. 126, 242301 & Phys. Rev. C103, 054904 (2021)



- Precision hadronic measurements can systematically constrain the QGP viscosity

# BUILDING INTUITIONS WITH THE JETSCAPE WIDGET

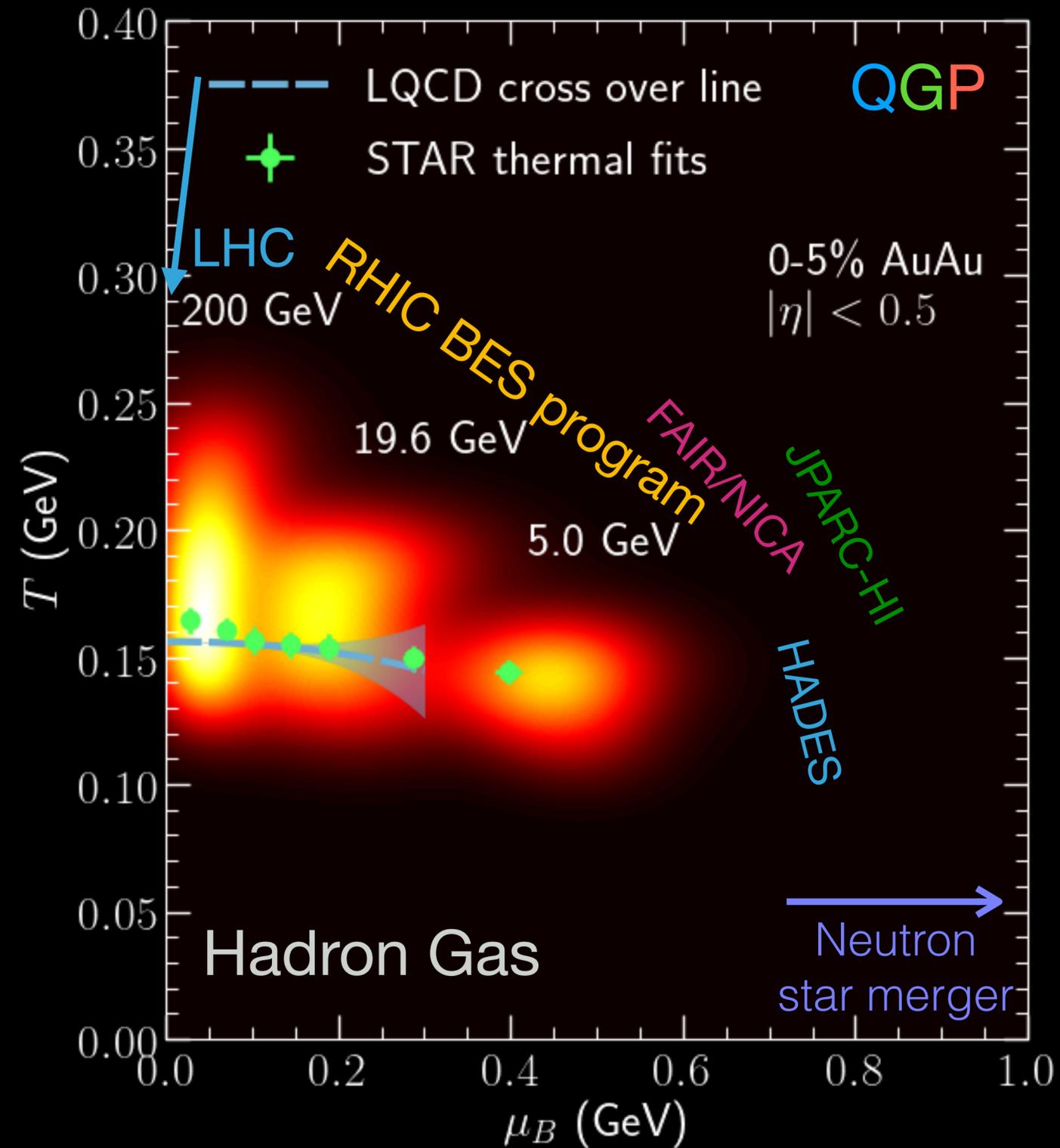
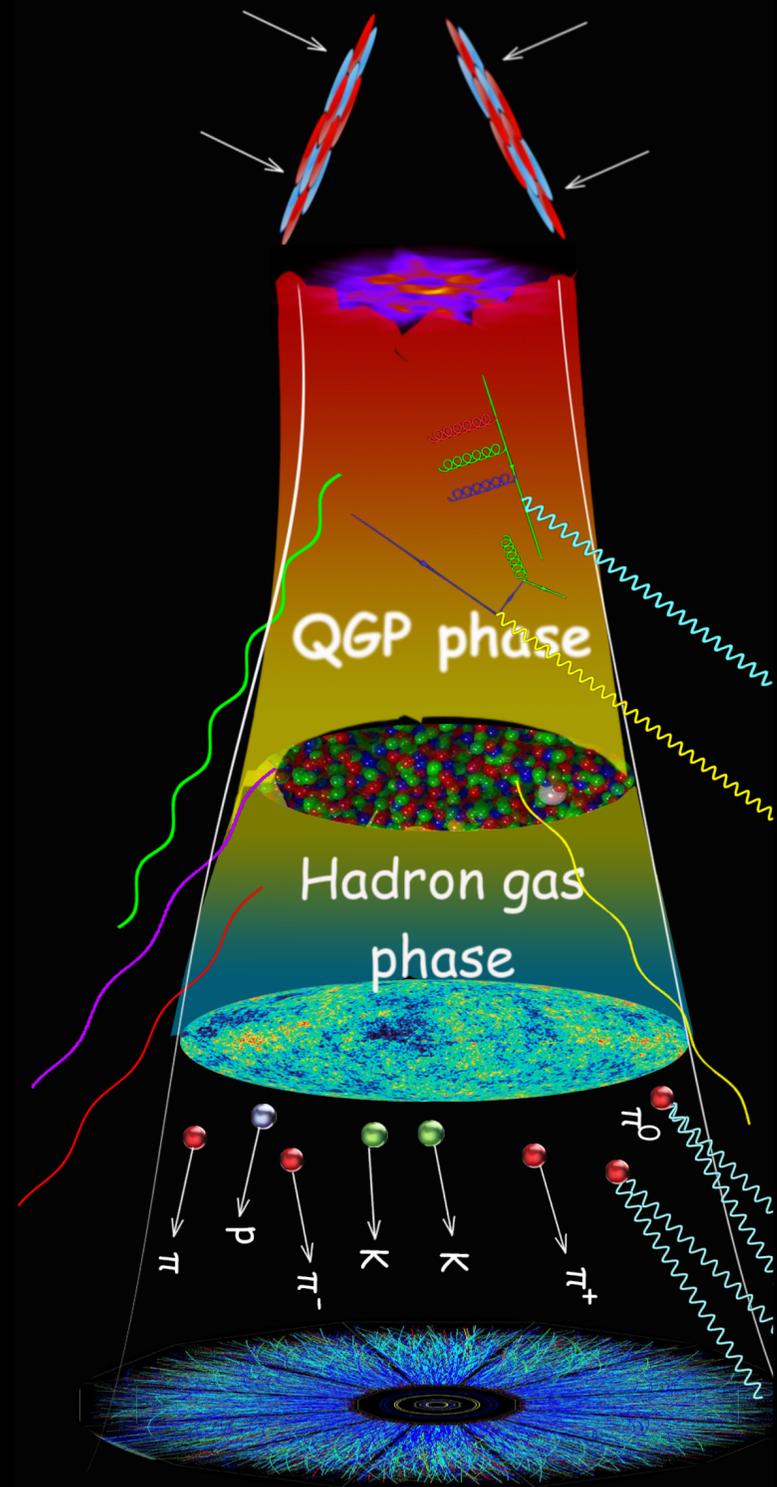


[JETSCAPE Widget](http://jetscape.org/sims-widget/)

<http://jetscape.org/sims-widget/>

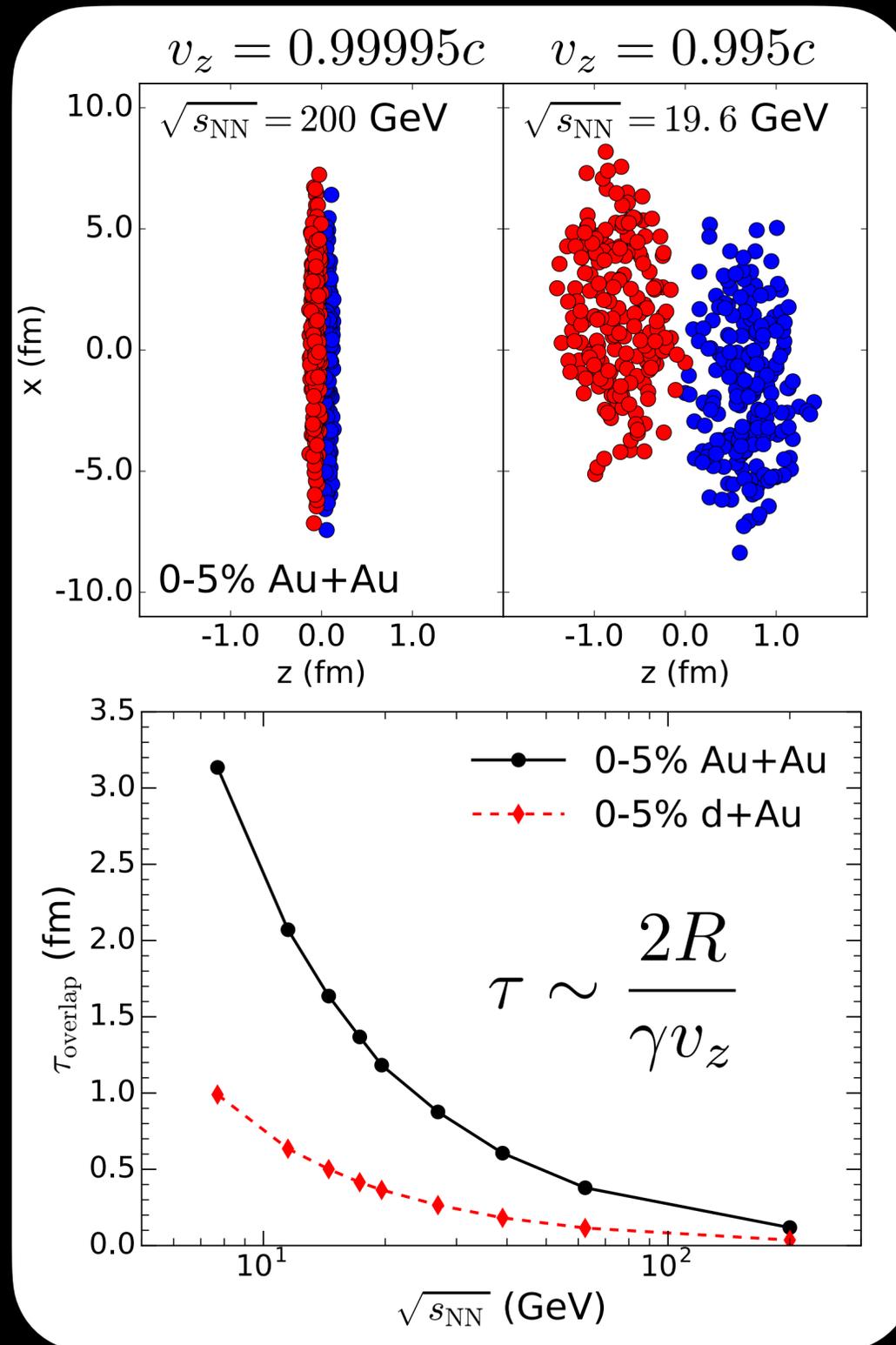
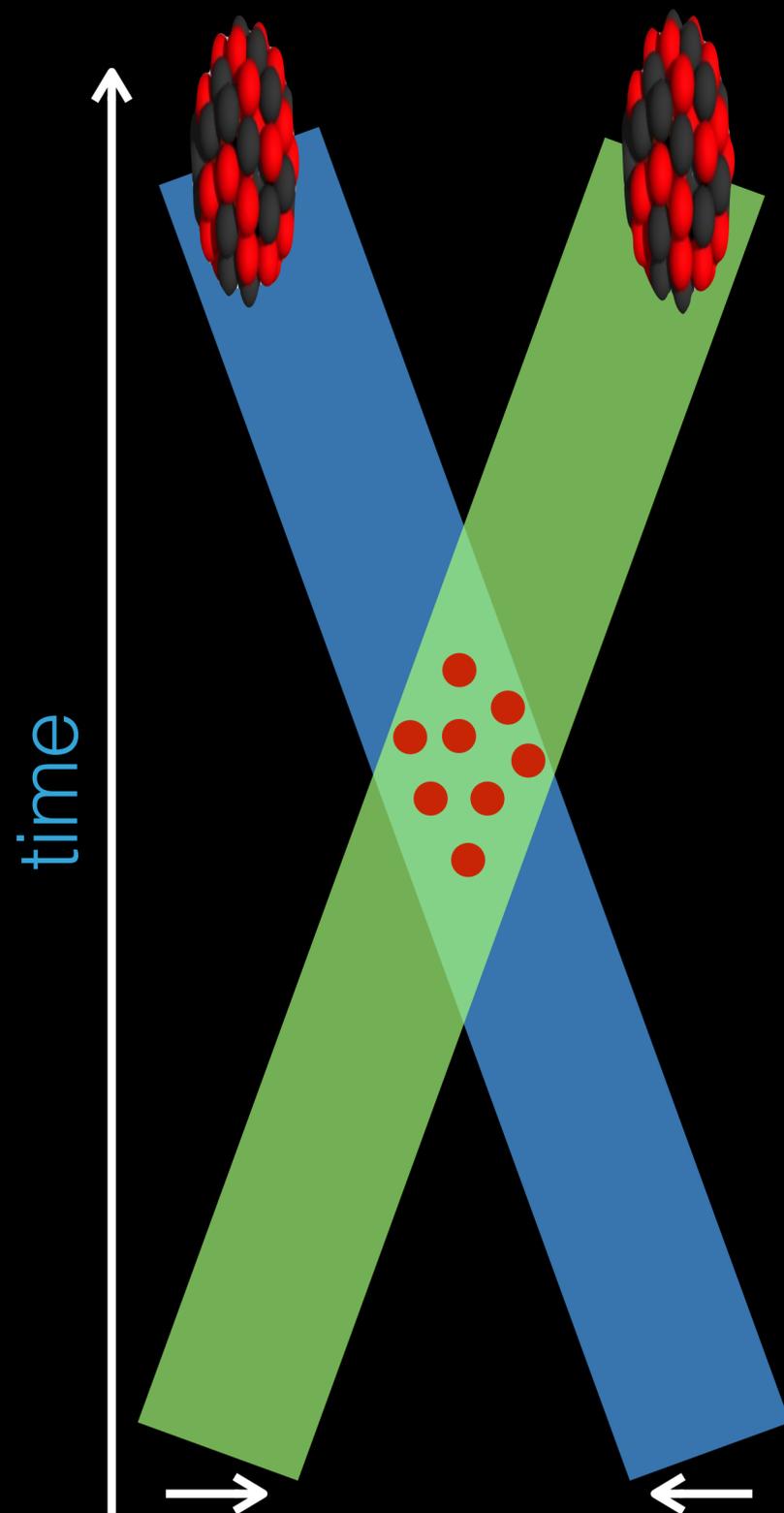


# PROBING THE NUCLEAR MATTER PHASE DIAGRAM



- Search for a critical point & 1st order phase transition
- How does the QGP transport property change with baryon doping?  
 $(\eta/s)(T, \{\mu_q\}), (\zeta/s)(T, \{\mu_q\})$
- Access to new transport phenomena  
*Charge diffusion*

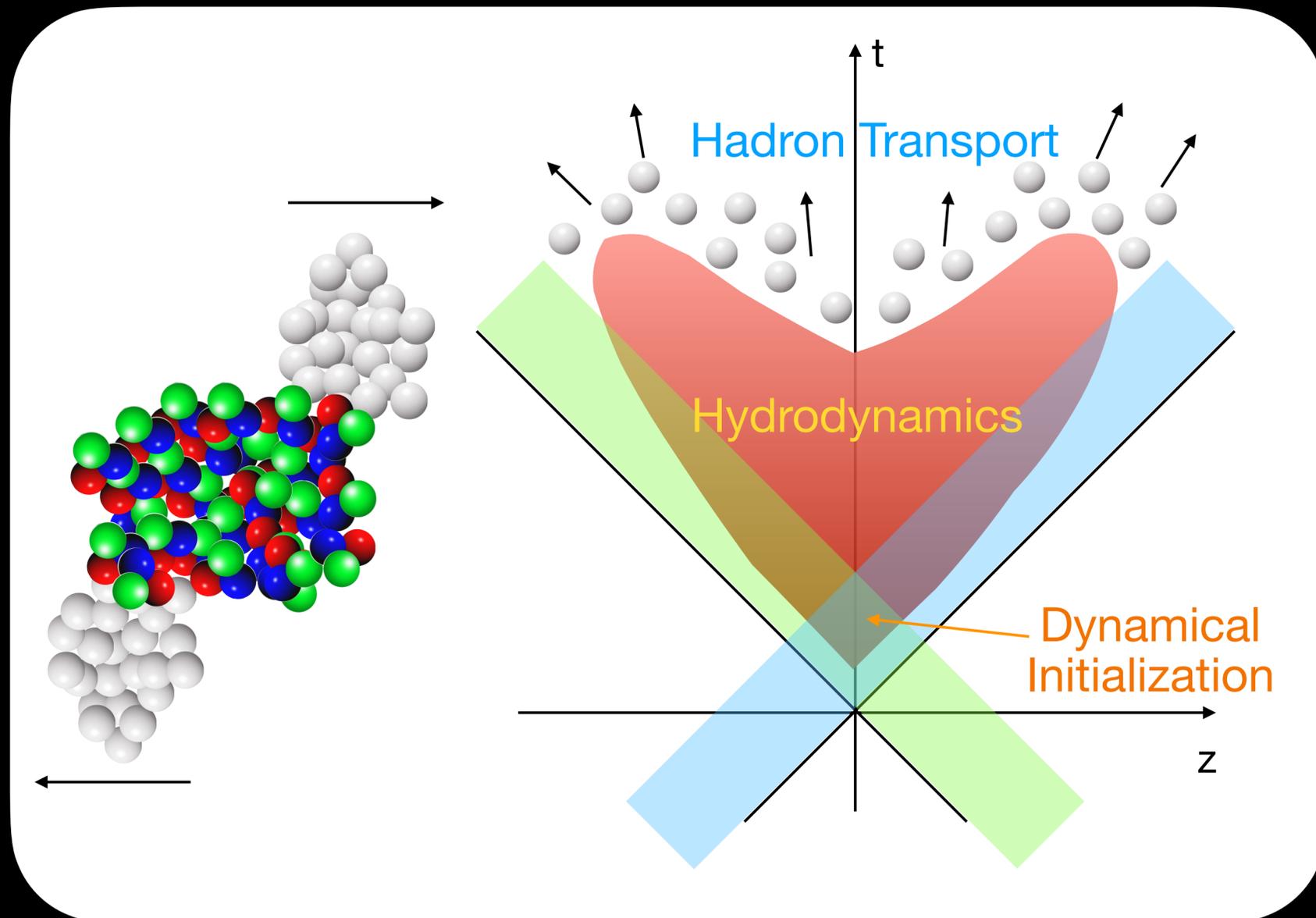
# 3D DYNAMICS BEYOND THE BJORKEN PARADIGM



- Geometry-Based initial conditions  
[C. Shen and S. Alzhirani, Phys. Rev. C 102, 014909 \(2020\)](#)
- Classical string-based initial conditions  
[A. Bialas, A. Bzdak and V. Koch, Acta Phys. Polon. B49 \(2018\)](#)  
[C. Shen and B. Schenke, Phys.Rev. C97 \(2018\) 024907](#)
- Transport model based initial conditions  
[I. A. Karpenko, P. Huovinen, H. Petersen and M. Bleicher, Phys. Rev. C91 \(2015\) 064901](#)  
[L. Du, U. Heinz and G. Vujanovic, Nucl. Phys. A982 \(2019\) 407-410](#)
- Color Glass Condensate based models  
[M. Li and J. Kapusta, Phys. Rev. C 99, 014906 \(2019\)](#)  
[L. D. McLerran, S. Schlichting and S. Sen, Phys. Rev. D 99, 074009 \(2019\)](#)  
[M. Martinez, M. D. Sievert, D. E. Wertepny and J. Noronha-Hostler, arXiv:1911.10272 + arXiv:1911.12454 \[nucl-th\]](#)
- Holographic approach at intermediate coupling  
[M. Attems, et al., Phys.Rev.Lett. 121 \(2018\), 261601](#)  
[Slack: #jul21-jul22-hydro](#)

# HYDRODYNAMICS WITH SOURCES

Energy-momentum current and net baryon density are fed into hydrodynamic simulations as source terms



$$\partial_{\mu} T^{\mu\nu} = J_{\text{source}}^{\nu}$$

$$\partial_{\mu} J^{\mu} = \rho_{\text{source}}$$

M. Okai, K. Kawaguchi, Y. Tachibana, and T. Hirano, Phys. Rev. C95, 054914 (2017)

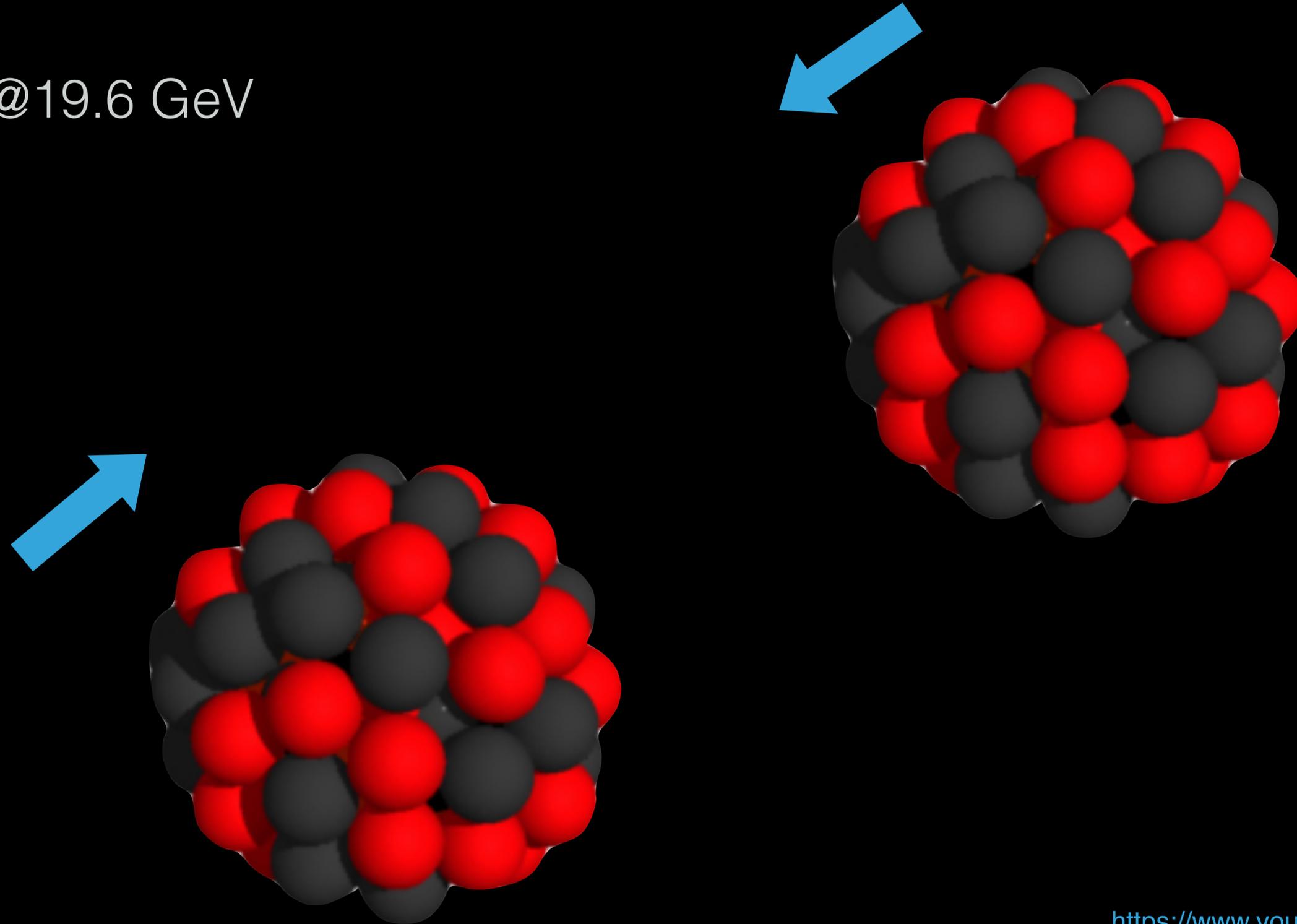
C. Shen and B. Schenke, Phys. Rev. C97 (2018) 024907

L. Du, U. Heinz and G. Vujanovic, Nucl. Phys. A982 (2019) 407-410

Y. Akamatsu, M. Asakawa, T. Hirano, M. Kitazawa, K. Morita, K. Murase, Y. Nara, C. Nonaka and A. Ohnishi, Phys. Rev. C98, 024909 (2018)

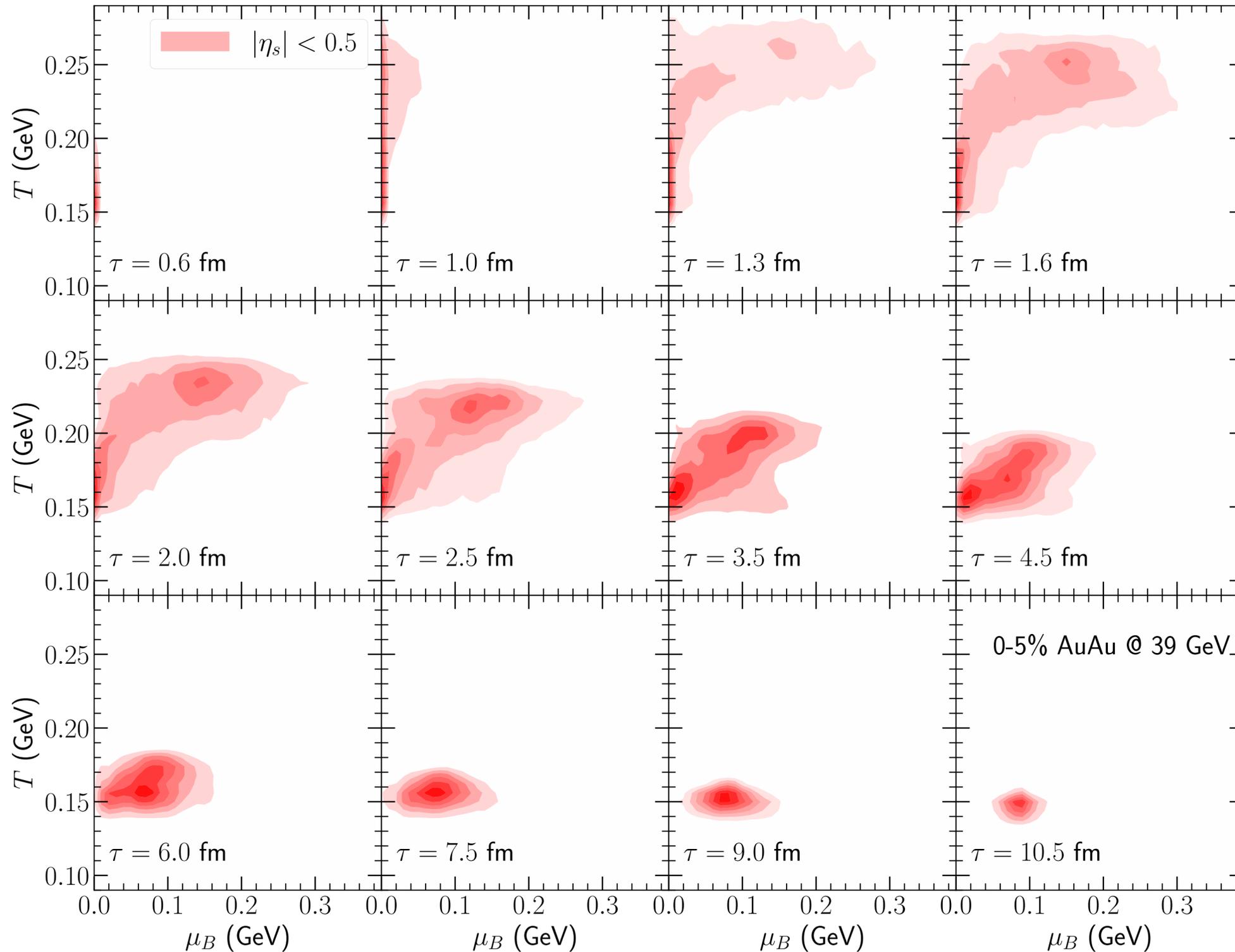
# RELATIVISTIC HEAVY-ION COLLISIONS

0-5% AuAu@19.6 GeV



<https://www.youtube.com/watch?v=gFV-9VeqzKE>

# FLOWING THROUGH THE QCD CROSSOVER REGION

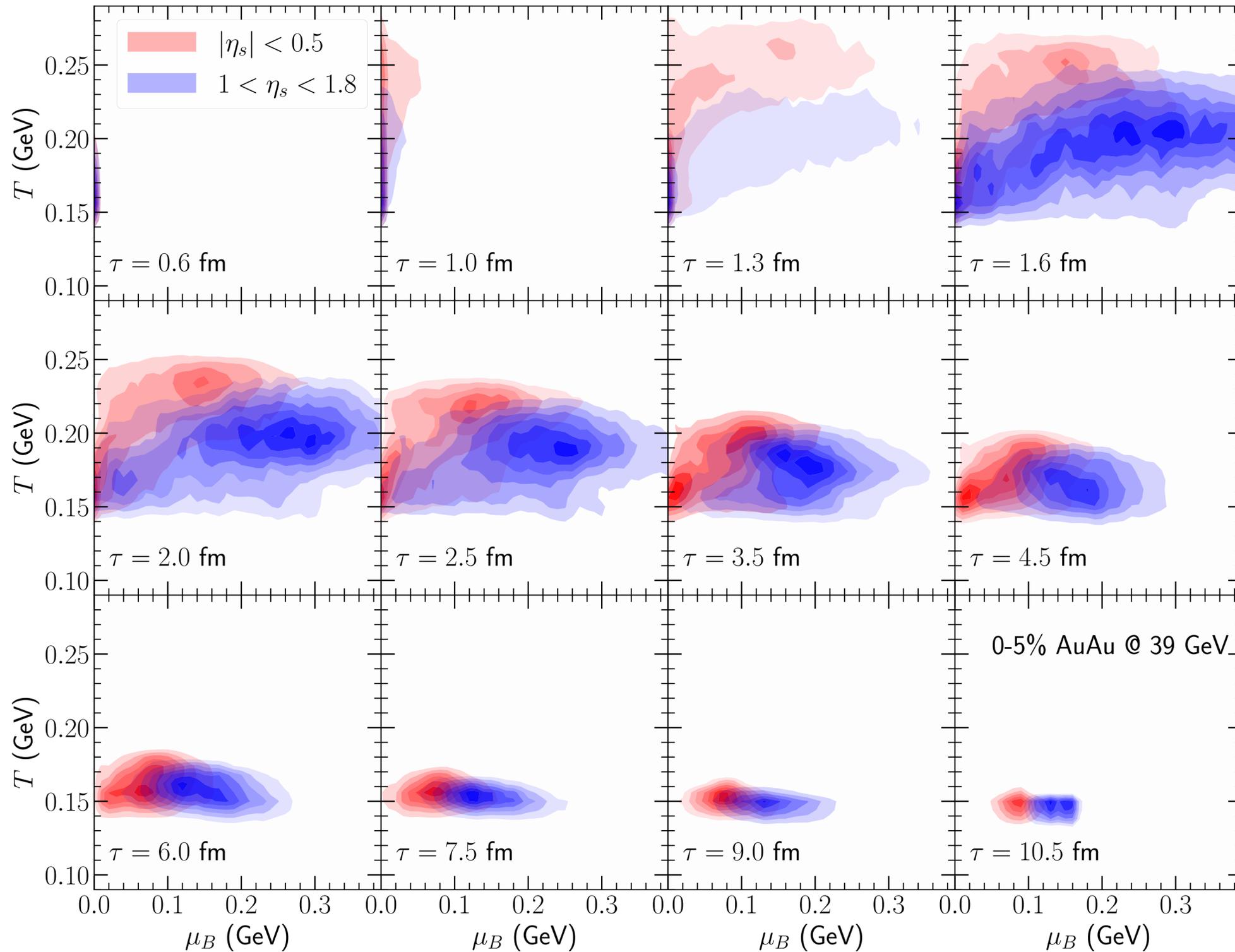


Nuclei overlap  
Dynamical Initialization stage  
Baryon dopping

Hydrodynamics evolution

Switching to hadronic  
transport

# FLOWING THROUGH THE QCD CROSSOVER REGION



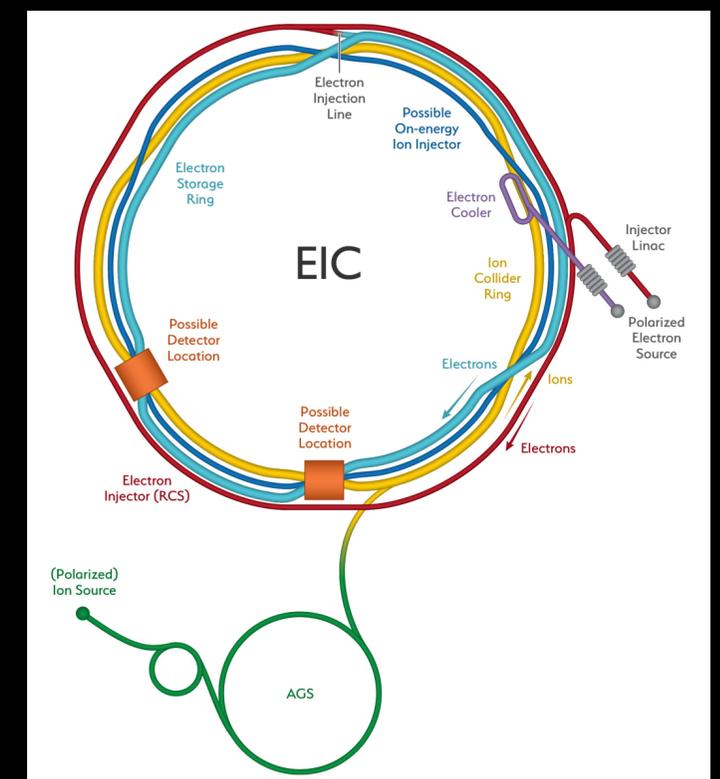
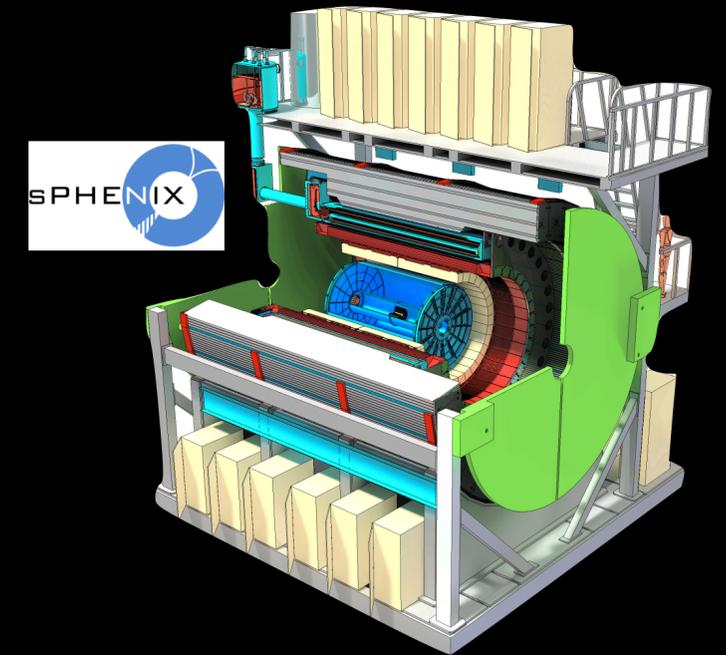
Nuclei overlap  
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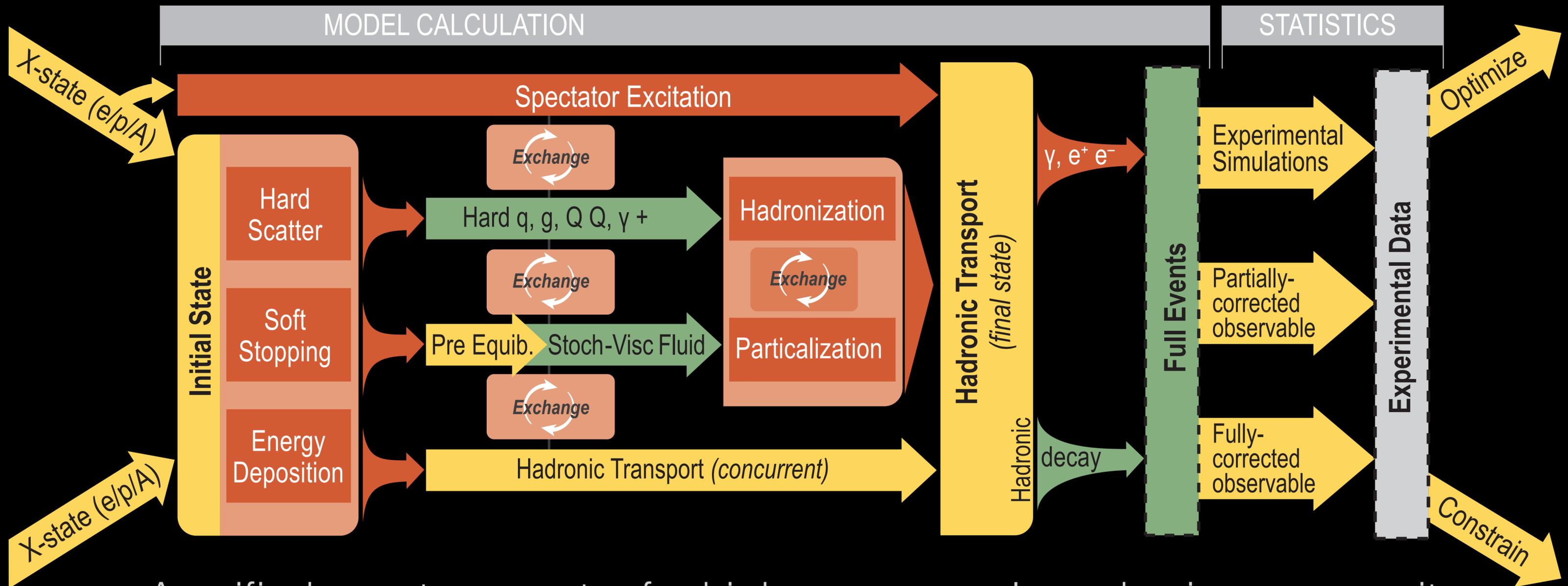
# THE ERA OF MULTI-MESSENGER HEAVY-ION PHYSICS

- RHIC: STAR upgrade and sPHENIX program  
Probing QCD at high net baryon density  
Study fully resolved jets, Upsilon states, and heavy quarks as QGP structure probes
- LHC: ALICE, CMS, ATLAS upgrades  
High energy and high luminosity frontier  
Precision measurements for rare probes
- HADES, FAIR, NICA, J-PAC-HI  
Phase structure of hot QCD matter
- Future Electron-Ion Collider  
Tomography of nucleon and nucleus



# THE NEXT GENERATION JETSCAPE FRAMEWORK

- The XSCAPE Project



- A unified event-generator for high energy nuclear physics community

# SUMMARY

- The vibrant experimental programs with precision measurements have been driving heavy-ion physics to the **multi-messenger** era
  - **Unified** theoretical + statistical frameworks are *essential* to unravel physics
- Viscous relativistic hydrodynamics provides a **robust, reliable, efficient, and accurate** description of QGP evolution in heavy-ion collisions
  - state-of-the-art **lattice QCD** inputs
  - a few remarkable **quantitative predictions**
  - model parameters has **direct connection** to the physics properties of the strongly-couple QGP