



Plasma Build-Up in Vacuum Discharges via Particle-in-Cell simulations

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In collaboration with the Max-Planck-Institut für Plasmaphysik



Outline



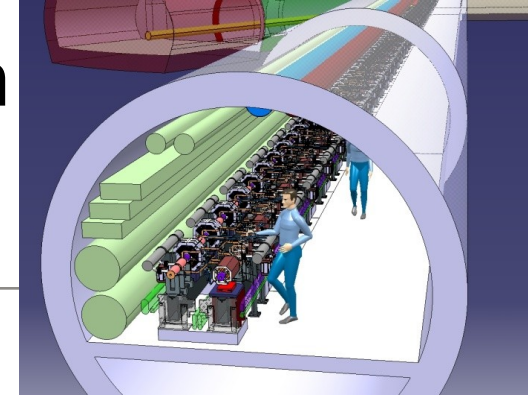
- Introduction: Why and how to model plasma build-up in vacuum discharges?
 - 2D Arc-PIC code description
- Physical discharge model
 - Crucial assumptions and special aspects
- An example simulation



Introduction



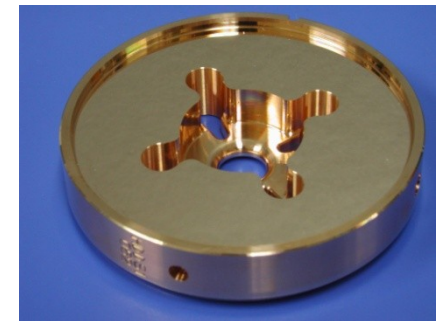
Main concern: Vacuum discharges in CLIC



- Why to study vacuum discharges?
 1. Going to the limits of conventional acceleration techniques → *highest possible gradient*
 2. Estimated power consumption: **415 MW** (LHC: 120 MW) → *cost reduction by efficiency optimisation*
- Knowing how to lower breakdown rate is a key issue in points (1) and (2)



Detail of a CLIC accelerating structure, working at 100 MV/m

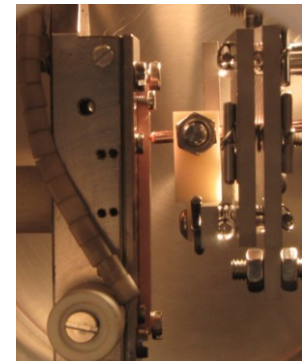
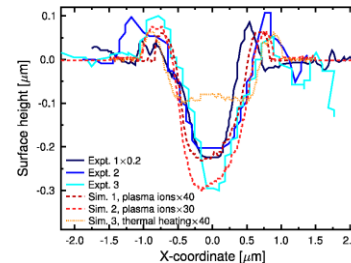
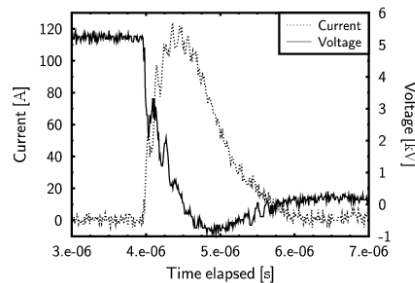
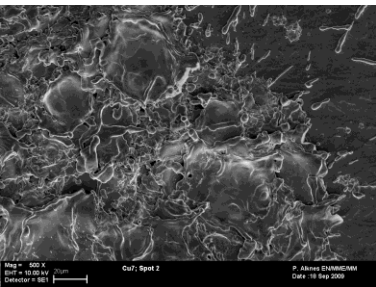
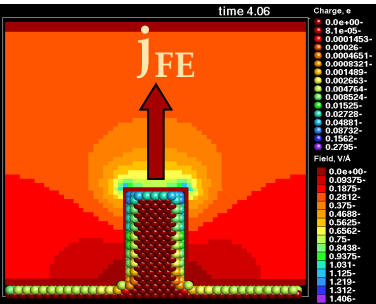




Why to model plasma build-up in vacuum discharges?

- Isn't it already 'too late' once the plasma has formed?
- As a part of our multi-scale model, plasma simulations provide us with a **link between**

1. **Micro- & macroscopic** surface processes: Triggering (nano-scale) → plasma → crater formation (visible effect)
2. **Theory & experiments**: Using reasonable physical assumptions (theory), the aim is to predict the evolution of measurable quantities (experiment)





How to model plasma build-up in vacuum discharges?

Particles:
Continuous
Lagrangian
phase space

Fields:
Discrete
Eulerian
grid points

- The **particle-in-cell** method is probably the most suitable for discharge modelling since it provides us with a
 - **Kinetic description** of the plasma necessary for collisionless plasmas, that are far from a Maxwell-Boltzmann distribution
 - **Self-consistent electrostatic(-magnetic) field** description, crucial for this high-current phenomenon close to an absorbing wall, giving rise to a plasma sheath
- However, vacuum discharges are *non-linear* and *stochastic* in their nature
 - Poses a **challenge** to any numerical method – with each of them having their limitations



Part I: 2D Arc-PIC Code Description



2D Arc-PIC code

- The new 2D Arc-PIC code has been developed and benchmarked last year

2D Arc-PIC Code Description:
Methods and Documentation

Helga Timkó
2010/2011



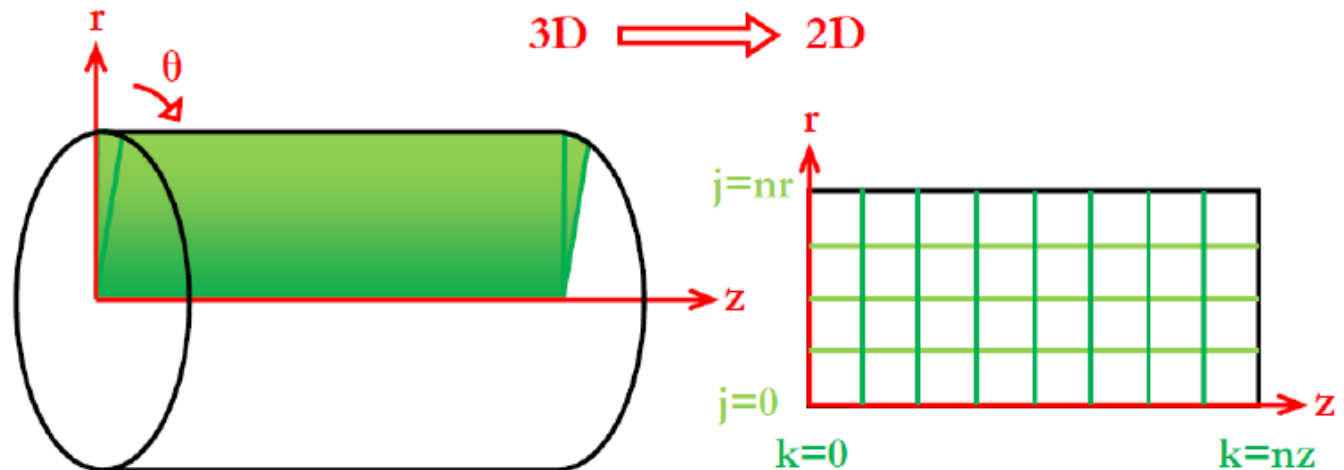
Helsinki Institute of Physics
and
CERN

- Serial **2d3v electrostatic** particle-in-cell code
 - Cylindrical symmetry
 - Monte-Carlo Collision routines adapted from *K. Matyash, IPP*
 - Optional external magnetic field
- Several options for *potential boundary conditions* and *particle injection schemes*
 - Simple options to carry out different tests
 - **Discharge option** (physics model described in Part II)
- Will be **accessible for CERN and HIP**
 - Automatic analysis scripts
 - Extensive code documentation to be published as a CLIC note



What does 2d3v mean?

- Particles have 2 coordinate and 3 velocity components
 - Collisions are 3D
 - Movements are 2D: Particles are projected into a 2D-slice of a cylinder
- Difference from 3D: In 2D, no turbulent phenomena and associated transport/diffusion can occur





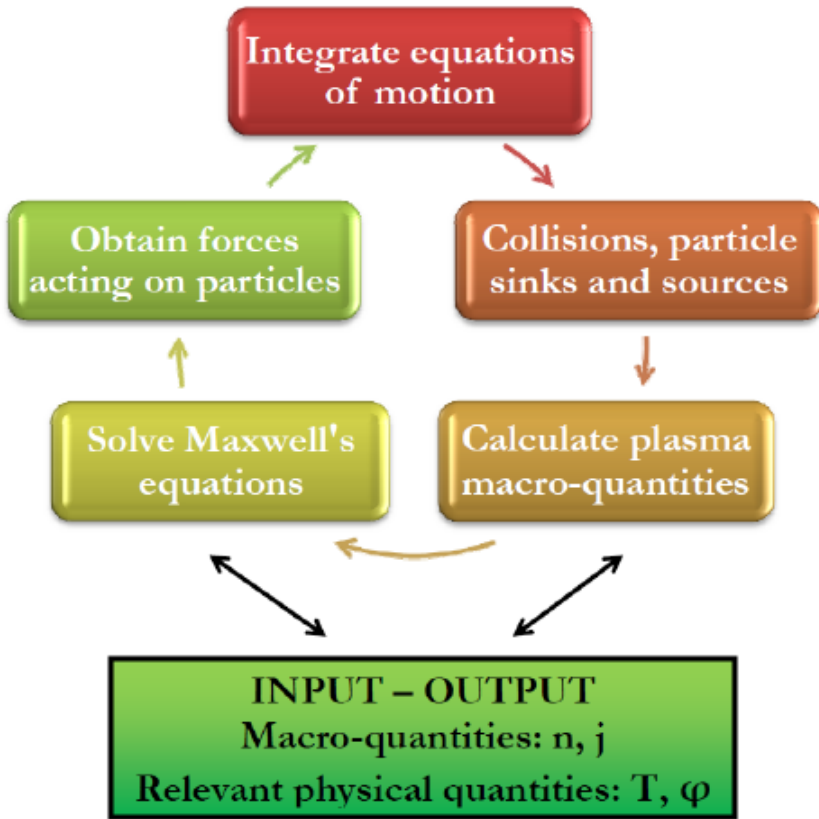
Assumptions embodied in the numerical model

- Dimensionality: **2D**, cylindrical symmetry
 - Electrostatic phenomenon: Even for high currents, **electrostatic** forces exceed magnetic confinement effects
- ∴ A 3D, electromagnetic picture of the problem would be a *higher order correction* to the solution

$$\left(\frac{\partial^2}{\partial r^2} + \frac{1}{r} \frac{\partial}{\partial r} + \frac{\partial^2}{\partial z^2} \right) \varphi = -\frac{e}{\epsilon_0} n_e$$



The PIC method and its limitations



Why discharge modelling is so hard:

$$\Delta x < 3.4\lambda_{Db},$$

- Stability requirements $\Delta t \leq 0.2\omega_{pe}^{-1}$,

- Non-linear problem, while discretisation is linear \Rightarrow prone to numerical instabilities

- Stability diagnostics is built-in

- Limited dynamic range

- Can't cover 1 nA – 100 A

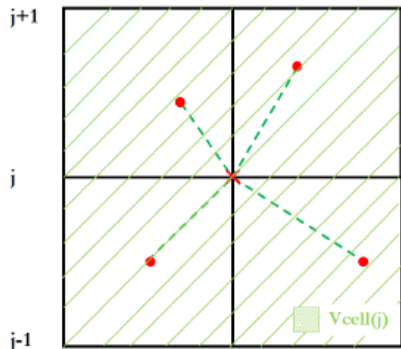
- Memory-heavy simulations

- High density only in a few simulation cells, while memory allocation is homogeneous

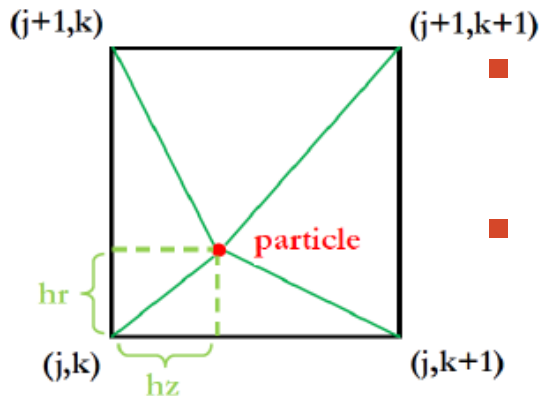


2D Arc-PIC: An efficient code

Some details for those who are familiar with PIC...



- Efficient: All **variables are dimensionless**
 - No unnecessary multiplications
- A well-optimised *finite difference method* **Poisson solver**
 - Using the 'SuperLU' lower-upper triangular matrix factorisation and inversion package

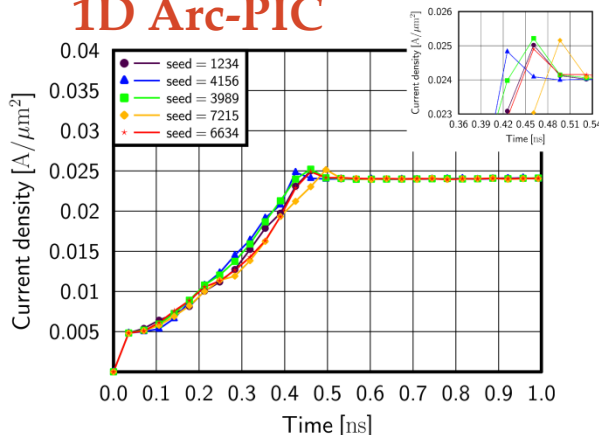


- An accurate implicit **particle mover** using the *Boris method*
- **Charge assignment and field interpolation:** Via 1st order *cloud-in-cell scheme*
 - Guarantees momentum conservation on a uniform grid

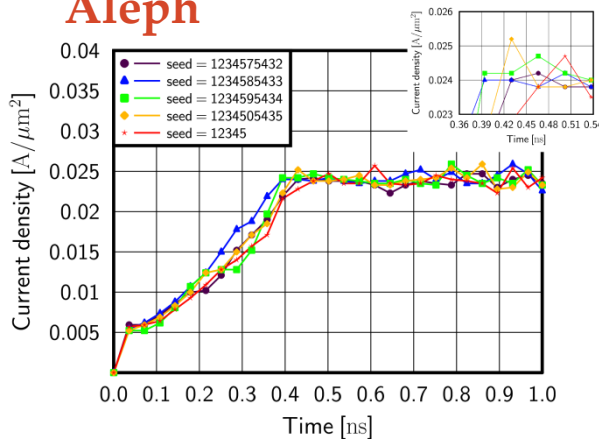


Benchmarking via code-to-code comparisons

1D Arc-PIC



Aleph



- Codes are usually tested via simple test problems that have a known analytic solution
- If the code is then run in a non-linear regime as in the case of breakdowns, subtle, earlier **undiscovered flaws** may lead to a wrong solution of the problem, and we wouldn't even necessarily notice it!
- Code-to-code comparisons are essential for such problems
 - A collaboration on this with **Sandia National Labs** is ongoing since 1.5 years now;
 - Obtained good agreement with a simple 1D discharge model



Part II: The Discharge Model



Phenomena taken into account – Three species: e^- , Cu, Cu^+

Initial
Cu, e^-

- Cu evaporation, enhanced electron field emission from a field emitter tip (Fowler-Nordheim eq)

$$j_{FE} = a_{FN} \frac{(eE_{LOC})^2}{\phi t(y)^2} e^{-b_{FN} \frac{\phi^{3/2} v(y)^2}{eE_{loc}}}, \quad \text{where } E_{loc} = \beta \cdot E$$

$$t(y) = 1, \quad v(y) = 0.956 - 1.062y^2 \quad \text{where } y = \sqrt{\frac{e^3 E_{LOC}}{4\pi\epsilon_0\phi^2}}$$

- Electron field emission also from the flat cathode surface

Create ions

- Collisions, esp. ionisation collisions

More e^- and
Cu

- Sputtering of Cu neutrals at the walls, enhanced MD yield at the cathode above a certain ion flux
- Secondary electron yield due to ion bombardment at the cathode



How the FE tip is modelled...

- We simulate a FE tip placed into the middle of the system; geometrically, the tip itself is not resolved
 - **Emission radius:** Assumed FE radius; used to calculate erosion, melting, and current density to current conversion
 - **Injection radius:** In practice, particles are injected within this radius



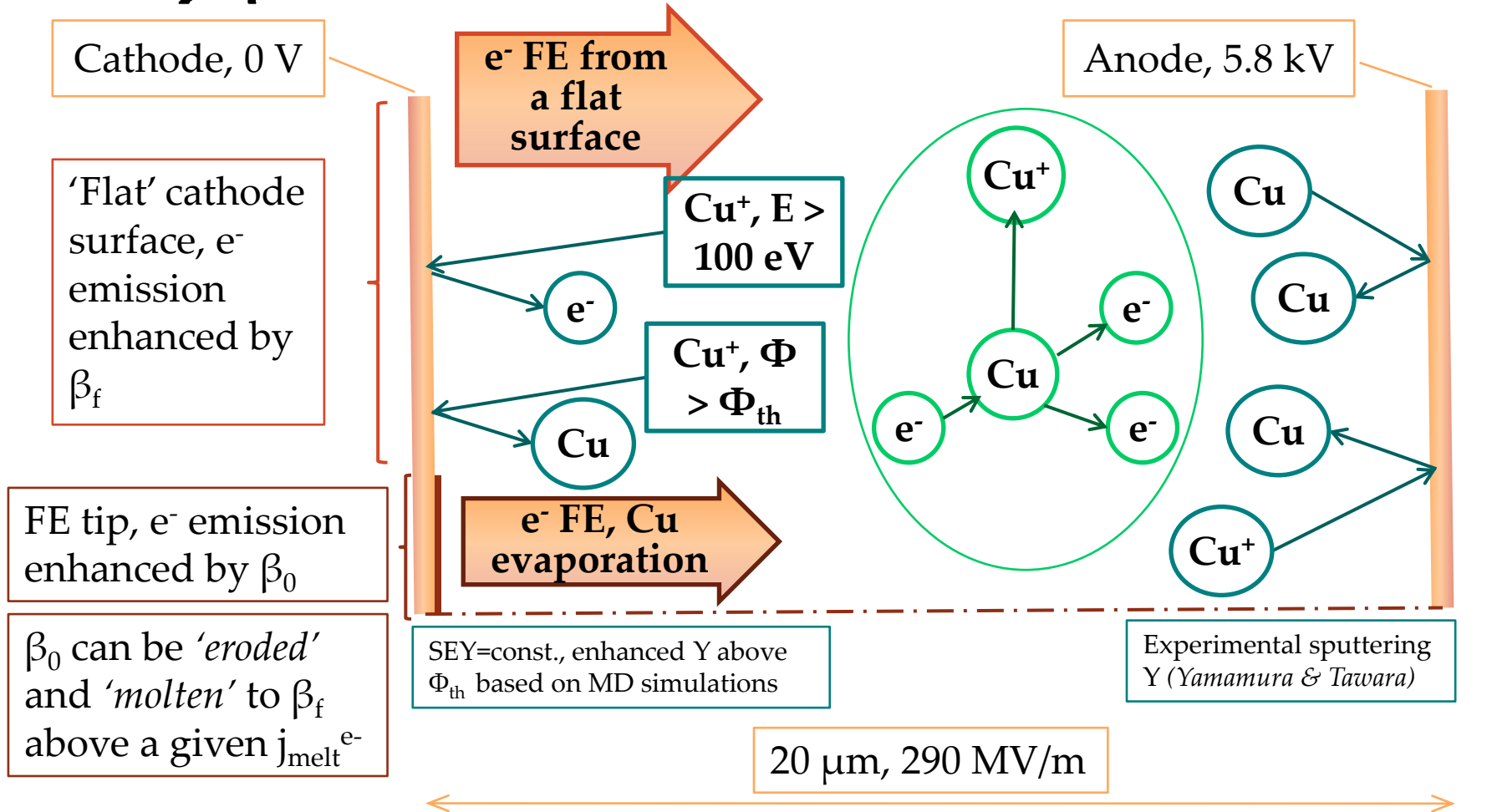
FE tip is source of

- Enhanced FN electron emission, limited to **12** GV/m
- Neutral evaporation in a fixed ratio $r_{\text{Cu/e}}$ (compared to FE)

Grid resolution **high** (note: limited memory, no. of jobs)



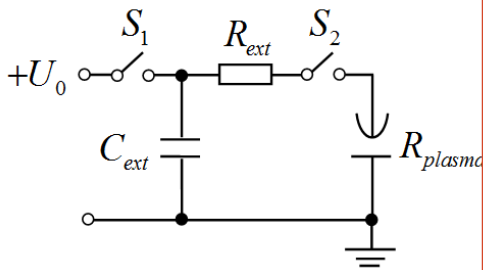
Overview of vacuum discharge boundary conditions





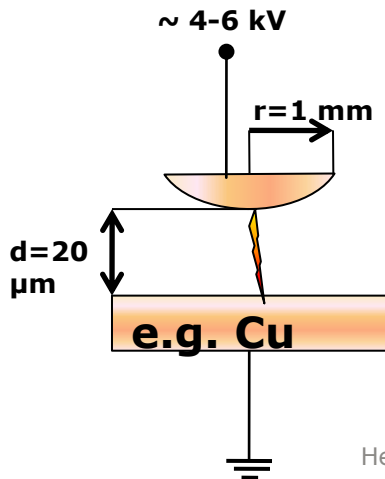
Circuit model – Inspired by the DC setup

EXPERIMENT



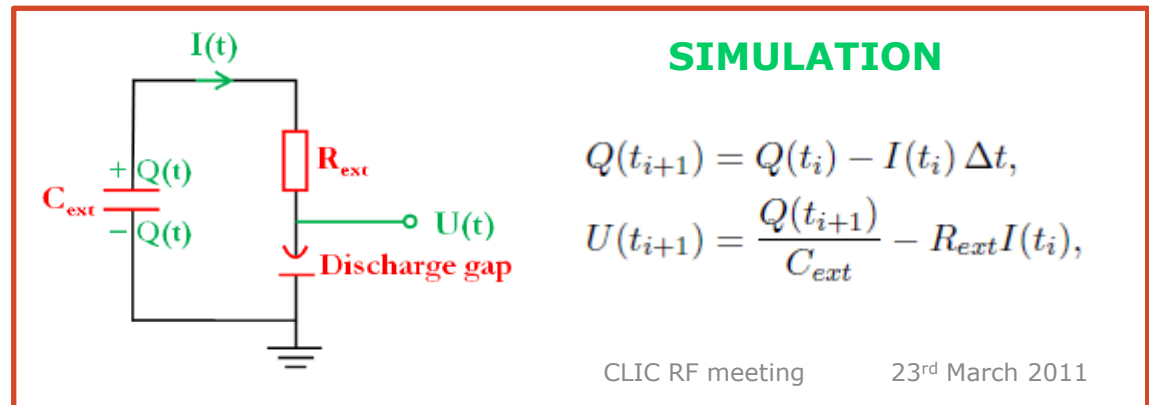
$$R_{ext} = 30\Omega$$

$$C_{ext} = 0.1 - 27.5\text{ nF}$$



Helga Timkó

- A vacuum arc in steady-state has typically a burning voltage of **10 V**, we apply 5 – 6 kV over 20 μm ! Isn't this a contradiction?
- No: The energy available for a breakdown is finite, will be eventually consumed \Rightarrow during the plasma build-up, the **external potential will drop**
 - A vacuum discharge is a transient phenomenon; and one thing we would like to predict is how it's current-voltage characteristic looks like



SIMULATION

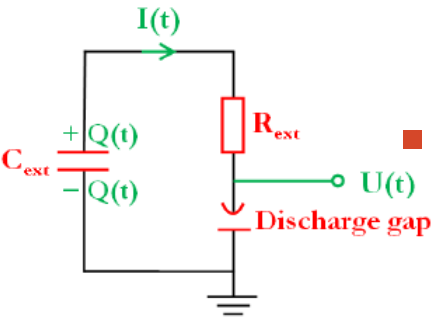
$$Q(t_{i+1}) = Q(t_i) - I(t_i) \Delta t,$$

$$U(t_{i+1}) = \frac{Q(t_{i+1})}{C_{ext}} - R_{ext} I(t_i),$$



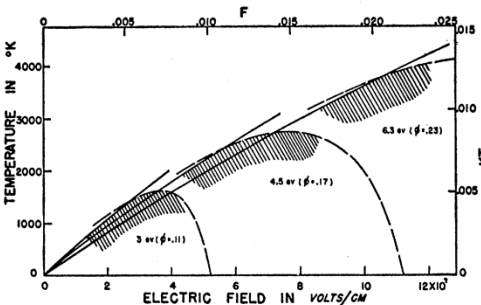
Circuit model – Where does the charge come from?

- Another fact: Vacuum arcs carry **10 – 100 A** current at a maximum; what is the physics behind charge depletion and how to implement it?



- We simulate an idealistic ‘pool’ of charges that is immediately accessible, but much can happen in a fraction of a ns! (see Part III)

- One may interpret the capacitance as the capacitance of the discharge gap itself
- **Charge depletion** is modelled implicitly via a reasonable electron FE current cut-off (corresponding to 12 GV/m, which is the range of applicability of pure field emission)



PHYSICAL REVIEW

VOLUME 102, NUMBER 6

JUNE 15, 1956

Thermionic Emission, Field Emission, and the Transition Region

E. L. MURPHY* AND R. H. GOOD, JR.

Department of Physics, Pennsylvania State University, University Park, Pennsylvania

(Received January 16, 1956)



From FE to discharge currents – In practice

- In real life we can observe the **full dynamic range** of a vacuum discharge:

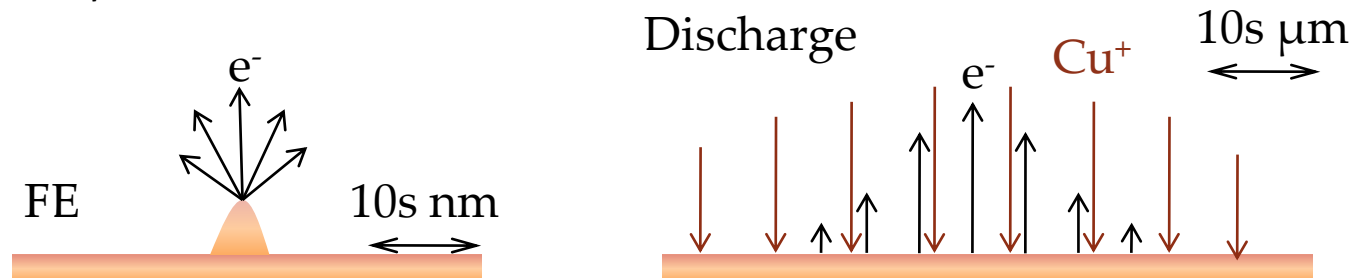
- > 10s pA in ‘weak’ FE phase
- Space charge limited ‘strong’ FE phase, typically ~ nA – μA
- Discharge current, up to 10 – 100 A

- At the same time, the involved **area changes**:

- Typically $10^{-20} - 10^{-14} \text{ m}^2$ for weak FE $\Rightarrow R_{\text{em}} \sim 0.1 - 100 \text{ nm}$
- During the discharge, the bombarded area has $R \sim 10 - 100 \text{ }\mu\text{m}$

Up to **12** orders
of magnitude
difference

Up to **12** orders
of magnitude
difference





From FE to discharge currents – In theory

Cathode

e^- FE from
a flat
surface

e^- FE, Cu
evaporation

- How can we **model this** with a method that can cover 3 – 4 orders of magnitude dynamic range at the most?
 - Start from **strong FE** (0.01 – 0.1 A)
 - **Option 1:** Increase by hand the **emission radius**
 - Would require a dynamic re-weighting of super-particles; non-trivial task because energy and momentum cannot be conserved at the same time
 - **Option 2:** Try to model the expansion of the spot through reasonable **physical assumptions**
 - The region outside the FE tip can be involved in field emitting electrons through a combination of $\beta_f \sim 10 - 15$ and a sheath
 - Motivation: We never measured $\beta < 10 - 15$; also a 'flat' surface will have asperities that can lead to a spreading FE



Part III: An example simulation

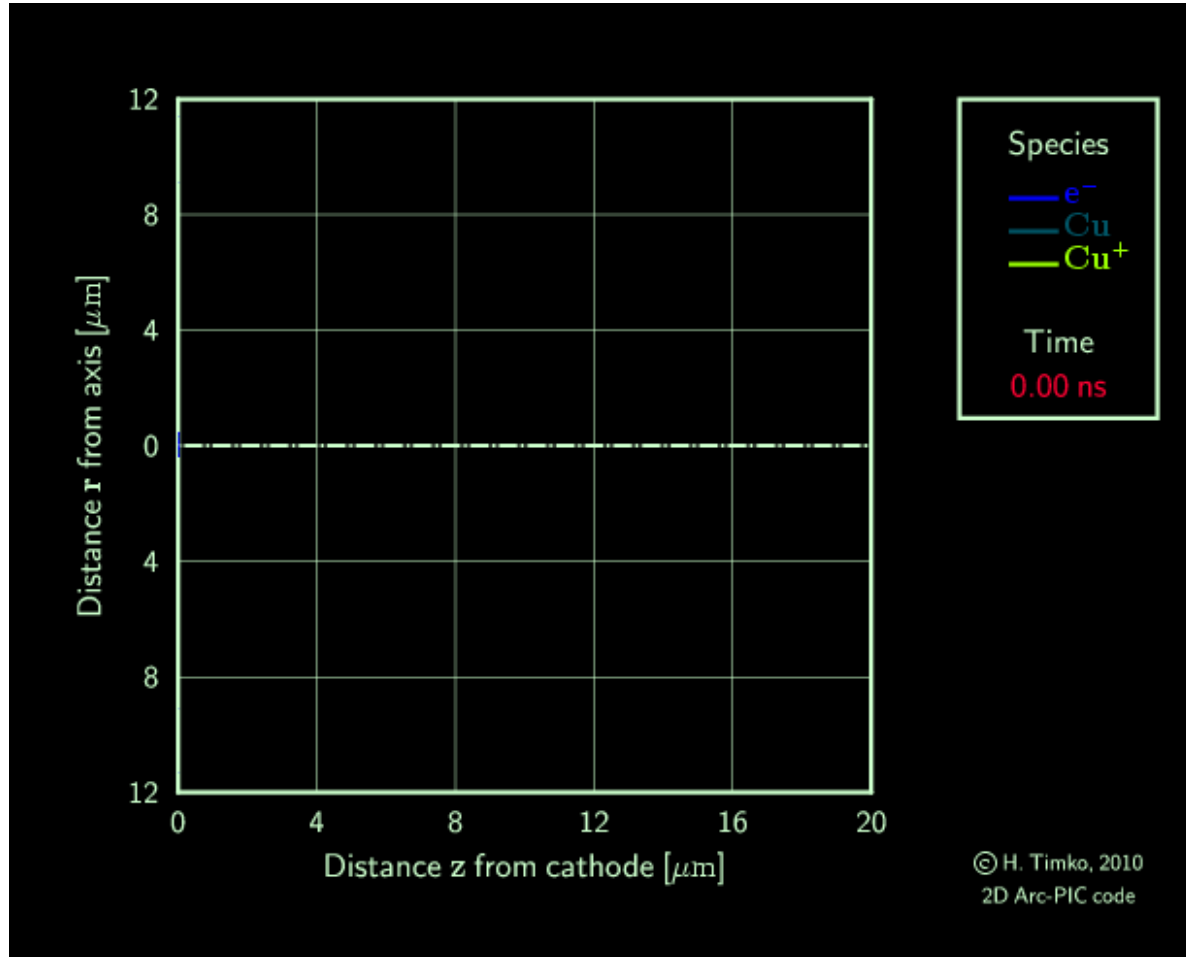


Input parameters

- $R_{em} = 1 \text{ dz} = 0.1 \text{ } \mu\text{m}$
- $R_{inj} = 4 \text{ dz} = 0.4 \text{ } \mu\text{m}$
- $N_{Db} = 1000, r_{Cu/e} = 0.015$
- $j_{melt} = 50 \cdot 10^8 \text{ A/cm}^2$ (upper limit)
- $\beta_0 = 35, \beta_f = 10$
- External circuit: $C = 0.01 \text{ nF}, R = 25 \text{ } \Omega$
- Initial voltage across the gap: 5.8 kV
- System size: 120 by 200 dz (**12 by 20 μm**)
- Gaussian injection; except for
 - Evaporated neutrals: v_r, v_t suppressed by **10**
 - FE electrons **fully Gaussian**

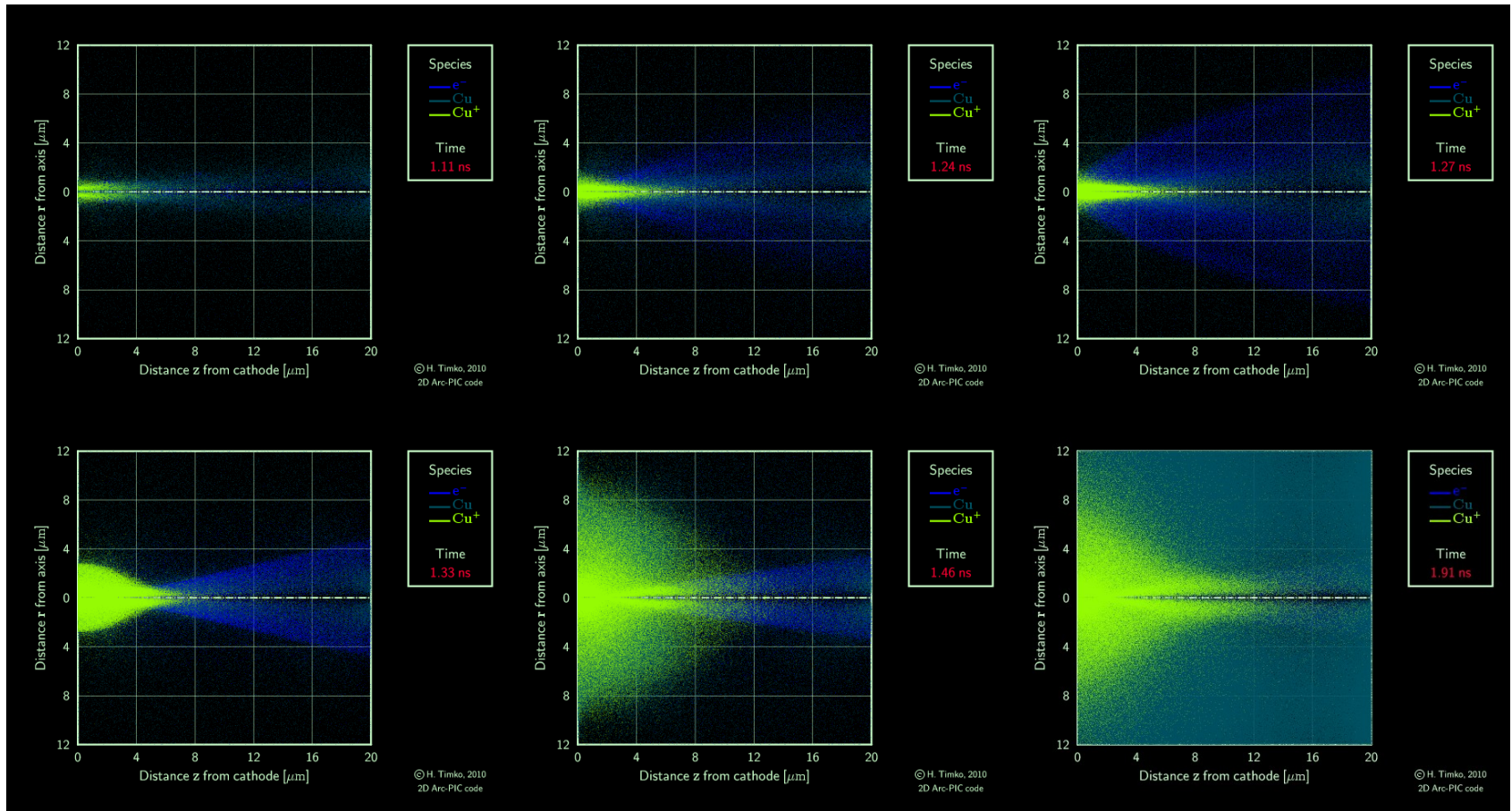


Movie



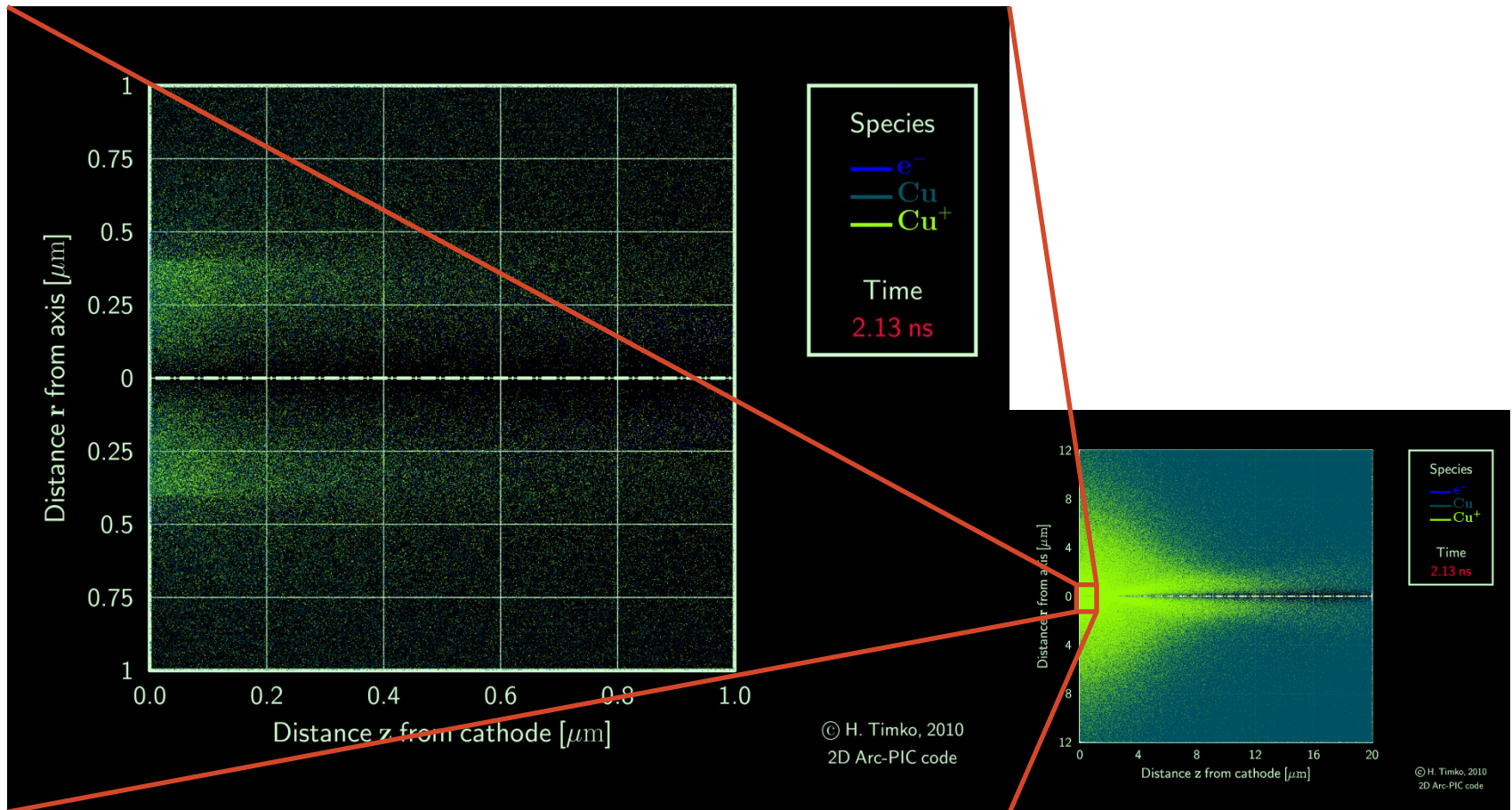


Coordinates



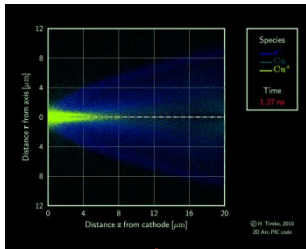


Coordinates – zoomed in

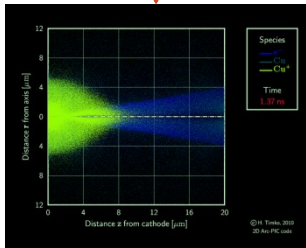




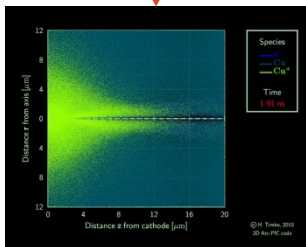
Observations



1.



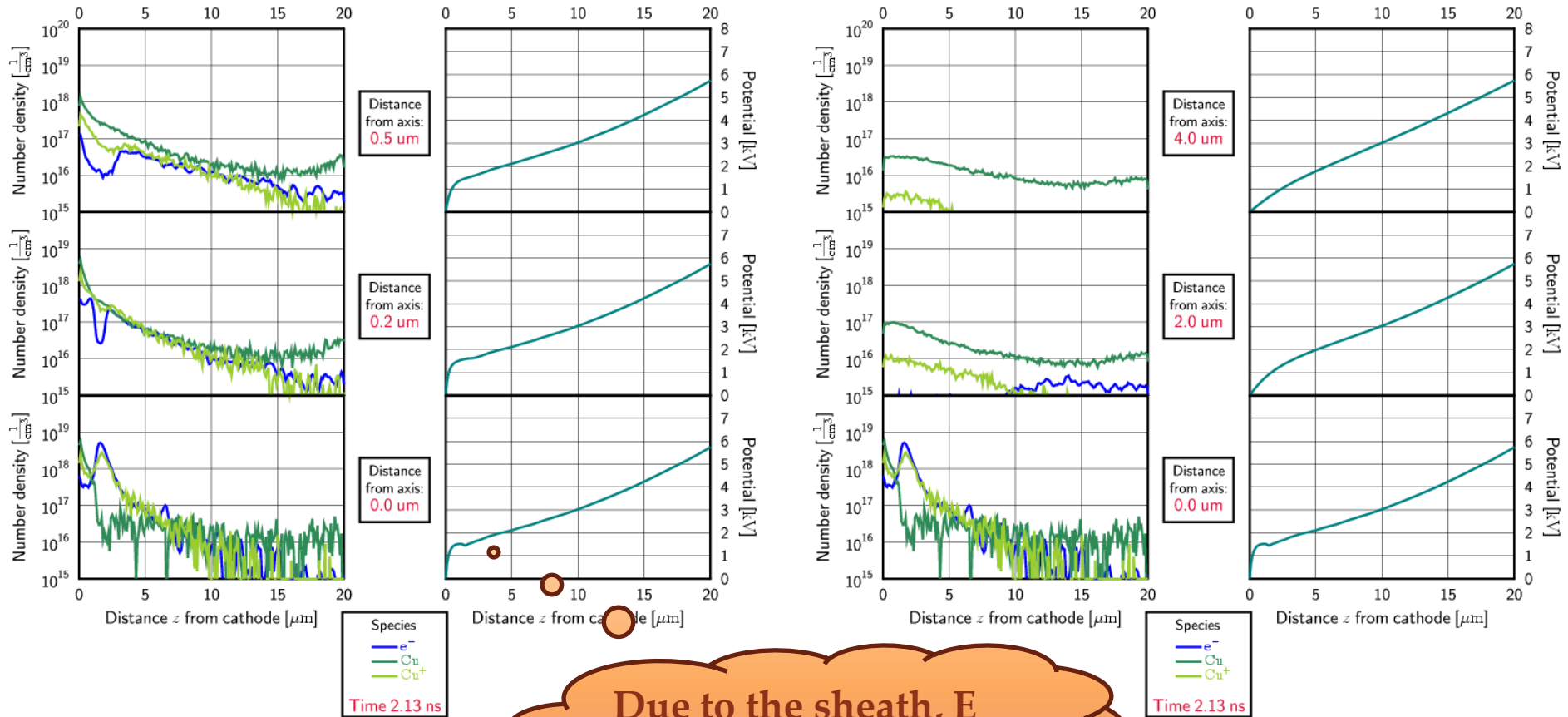
2.



- Fully **cathode dominated** phenomenon
- Although FE starts from a small area, the discharge plasma can **involve a macroscopic area** on the cathode
- Transitions seen:
 1. Transition from **strong FE** to a small **discharge plasma**
 - Sudden ionisation avalanche
 - A plasma sheath forms, the plasma becomes quasi-neutral
 - Focusing effect
 2. Transition from a **surface-defined** phase to a **volume-defined** phase
 - When neutrals fill the whole system
 - Self-maintaining
 - Macroscopic damage



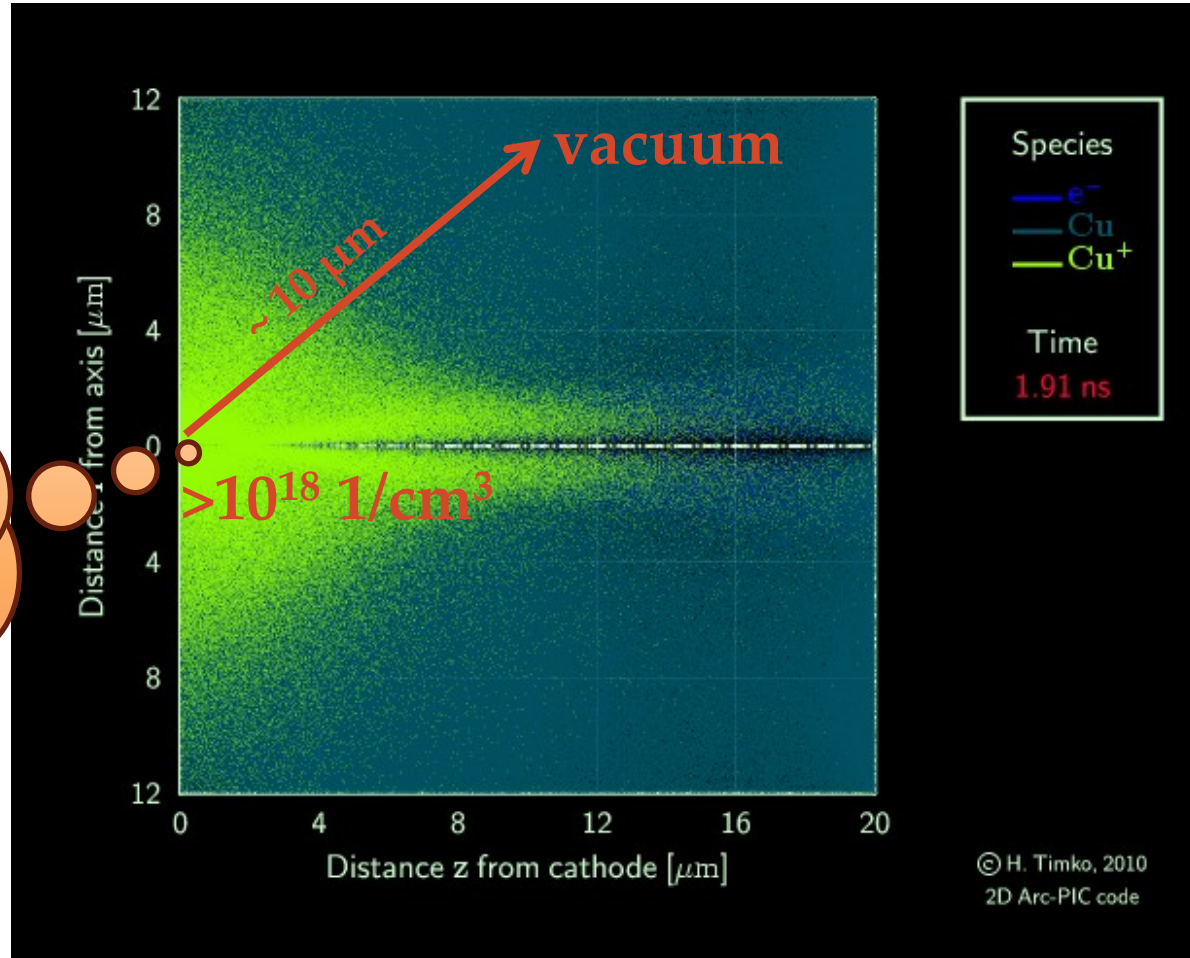
Potential & densities



Due to the sheath, $E \sim 6\text{-}7 \text{ GV/m!}$



Steep gradients



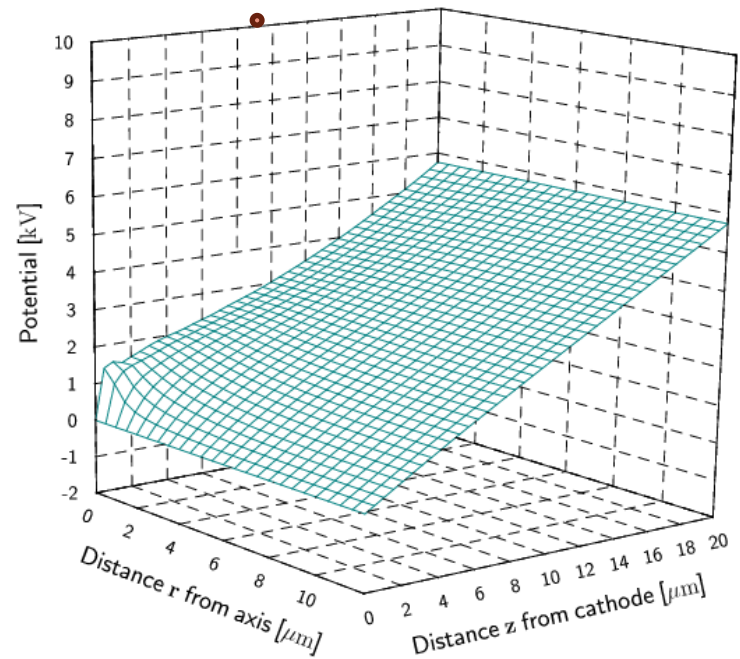
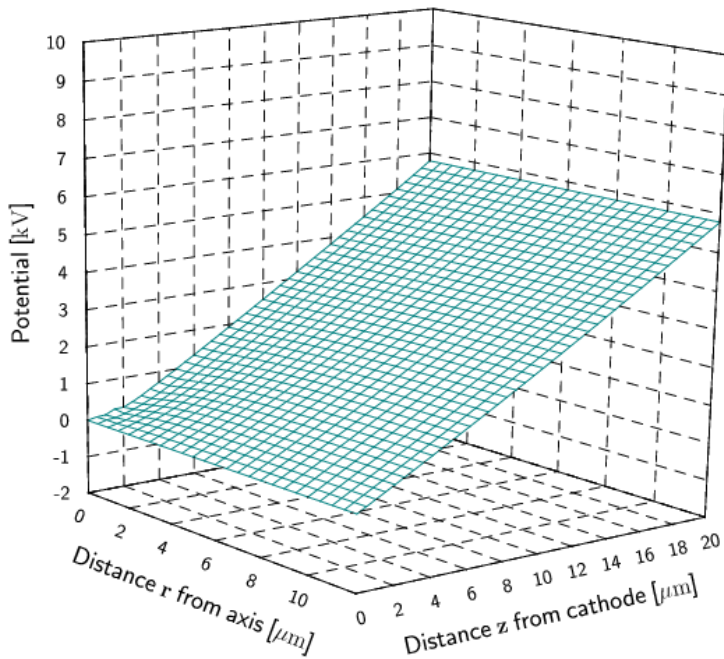
Sheath enhances FE only in a small region!



Full 2D potential



Plasma:
Sheath



FE: Space charge

Time 1.26 ns

Time 2.13 ns

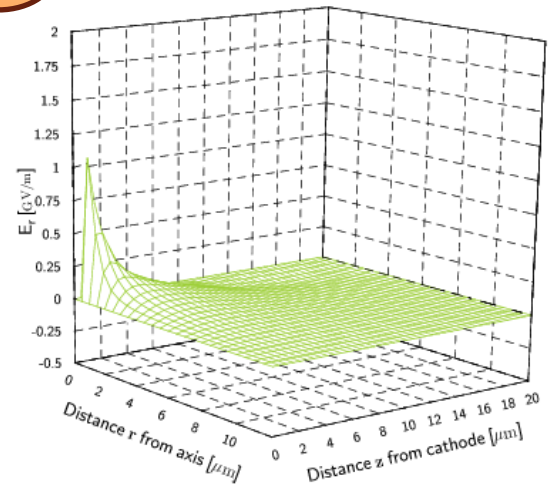
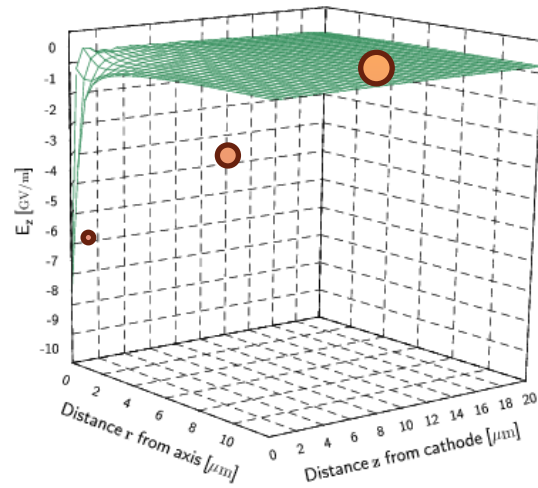


Full 2D E-field

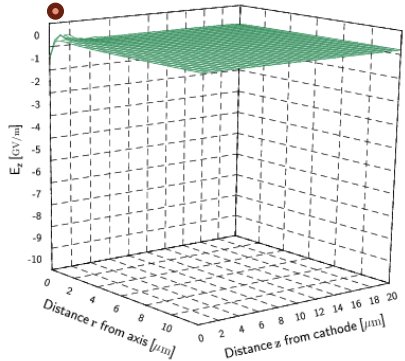


Plasma:
Sheath

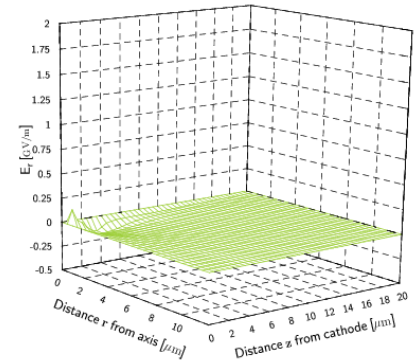
FE: Space
charge



Time 2.13 ns



Time 1.26 ns

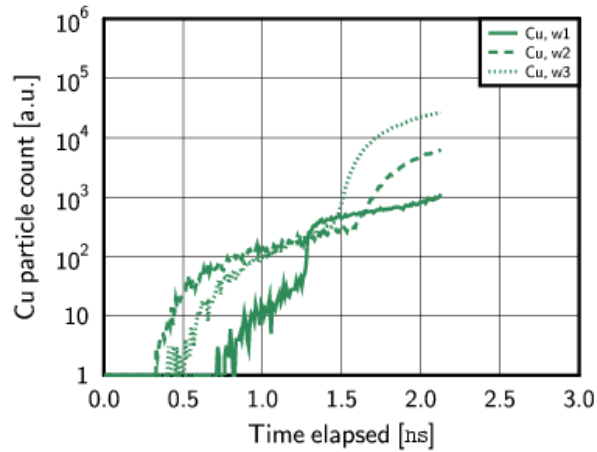
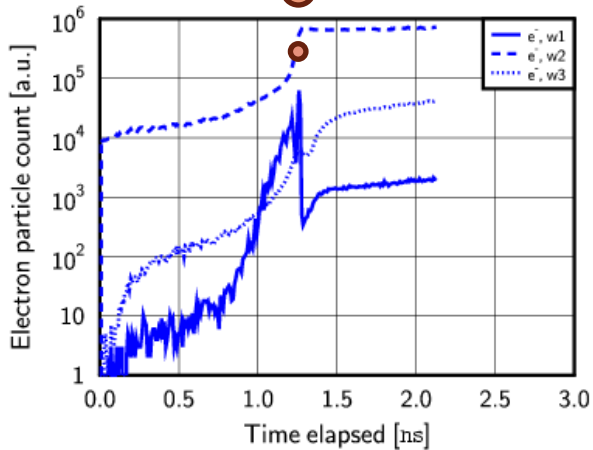




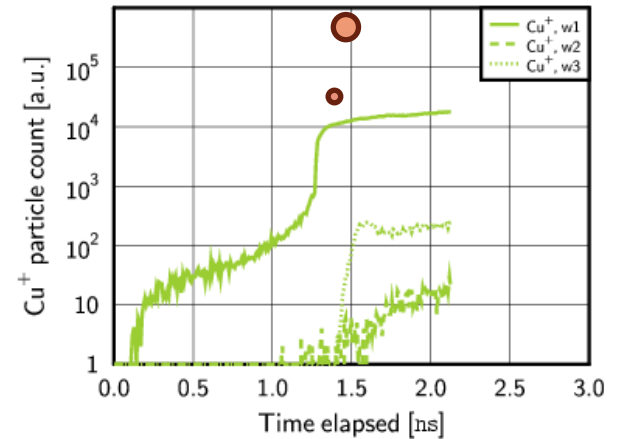
Absorbed particle counts



Breakdown
⇒ becomes
conductive



Cu⁺ follows
the Cu curve

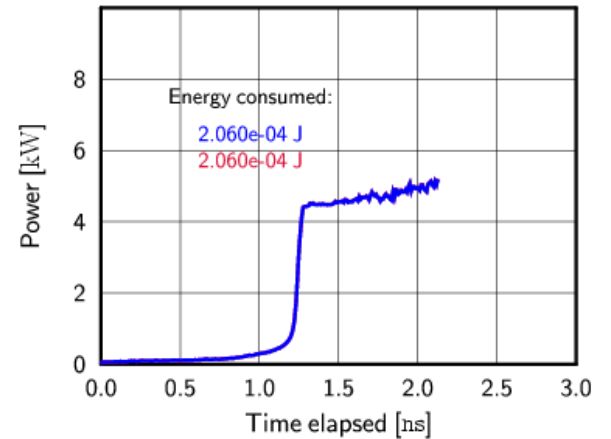
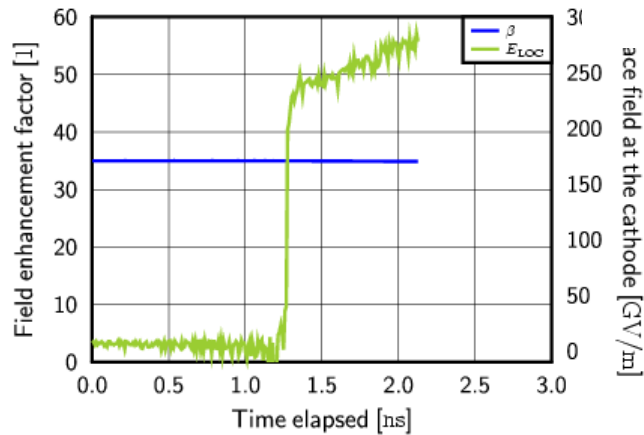
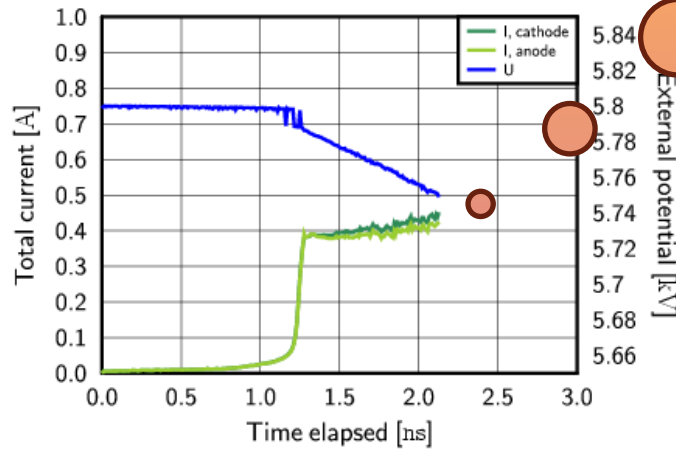




Other diagnostics



Limited FN:
imitates current
depletion!
Growing current:
expanding spot





Conclusions



- The 2D Arc-PIC code has been developed and its simulations give us **new type of insight** into the physics of breakdown plasmas
- The code is available for CERN and HIP, but obtaining reliable results is an art of itself
 - Extremely **time-consuming**, because the result is highly sensitive to input parameters (exponential dependencies)
 - Requires a deep **knowledge of the PIC method**, in order to filter out unphysical effects



Outlook



-
- Personally, I am about to finish my PhD work by completing the above last study on 2D discharge plasmas
 - DC/RF comparison planned
 - Perhaps even a study of an external magnetic field effect

 - It is uncertain yet how long I will continue as a PhD Student at CERN, but HIP has plans to place another PhD Student to CERN sometime in the future



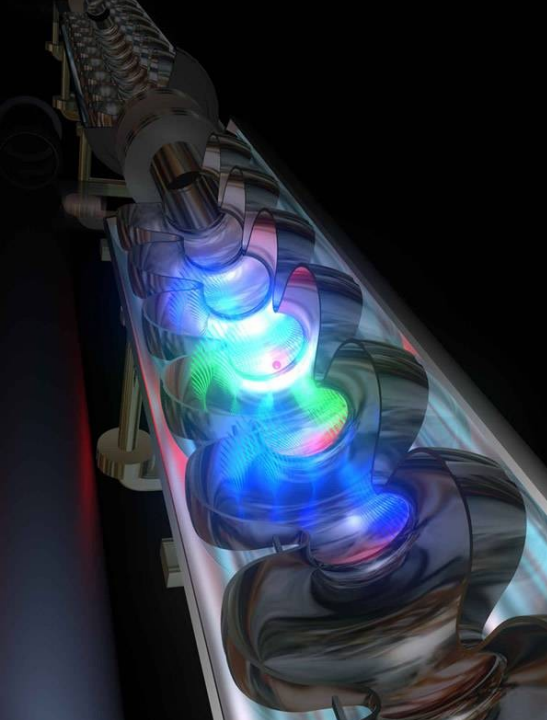
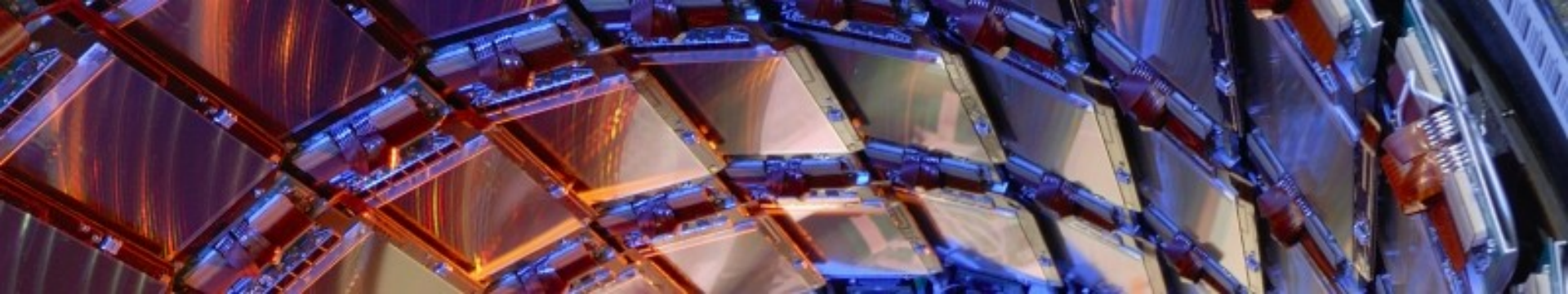
My special thanks to...



... our collaborators at the Max-Planck-Institut für Plasmaphysik, in Greifswald, Germany,

Ralf Schneider and *Konstantin Matyash*,

who taught me the PIC method, showed me all important tricks, and advised me how to write my own code.



Interested in more?
Come to our *MeVArc*
Breakdown workshop
27-30th June 2011, in
Helsinki!

<http://beam.acclab.helsinki.fi/hip/mevarc11/>

Thank you!

