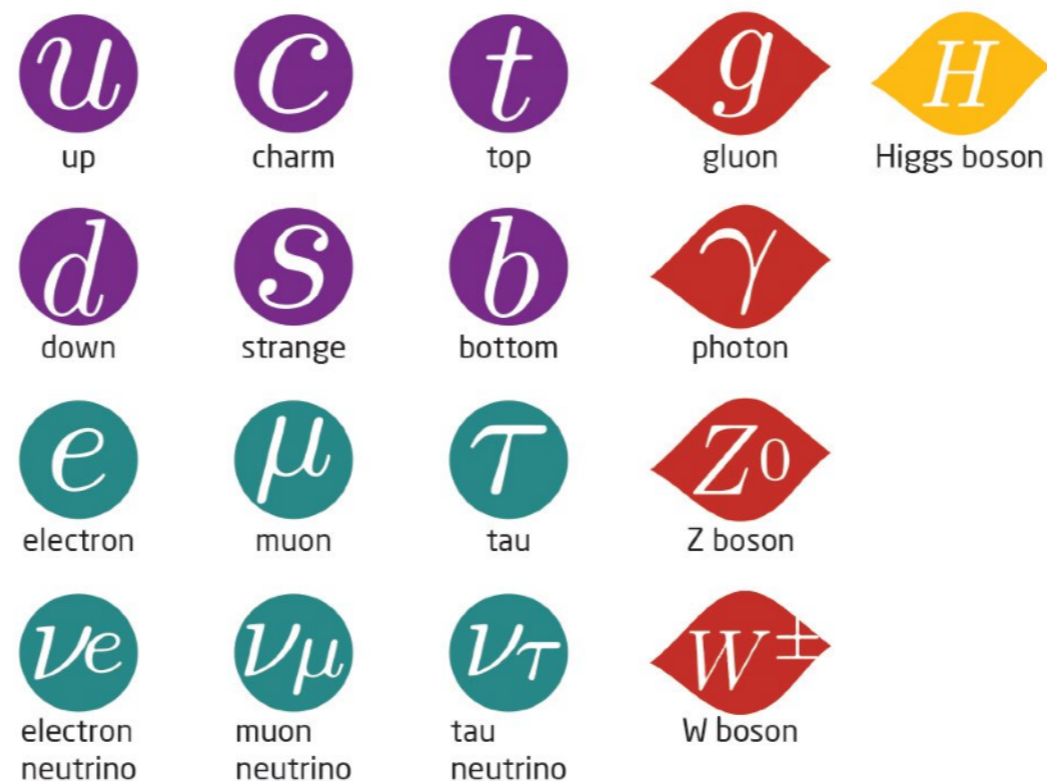


An Introduction to the Standard Model of Particle Physics



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Introduction/Outline

- ◆ An old question and long-standing activity:

What the Universe is made of at the most (or at a more) fundamental level?

Elementary particles and their interaction.

In this brief lecture, we present our knowledge based on many years of experimentation and theoretical speculation.

- ◆ Outline:

- ◆ Experimental findings
- ◆ Theoretical framework
- ◆ The Standard Model of particle physics
- ◆ Electroweak symmetry breaking and the Higgs mechanism

Experimental Findings: *Fermions*

Spin 1/2 matter particles, and their anti-particles, vast range of *masses*



electron

$$m = 0.510998928 \pm 0.000000011 \text{ MeV}$$



muon

$$m = 105.6583715 \pm 0.0000035 \text{ MeV}$$



tau

$$m = 1776.82 \pm 0.16 \text{ MeV}$$



muon
neutrino



electron
neutrino



tau
neutrino

$$\Delta m_{21}^2 = (7.50 \pm 0.20) \times 10^{-5} \text{ eV}^2$$

$$\Delta m_{32}^2 = (2.32_{-0.08}^{+0.12}) \times 10^{-3} \text{ eV}^2$$



up

$$m_u = 2.2_{-0.4}^{+0.6} \text{ MeV}$$



down

$$m_d = 4.7_{-0.4}^{+0.5} \text{ MeV}$$



strange

$$m_s = 96_{-4}^{+8} \text{ MeV}$$



charm

$$m_c = 1.28 \pm 0.03 \text{ GeV}$$



bottom

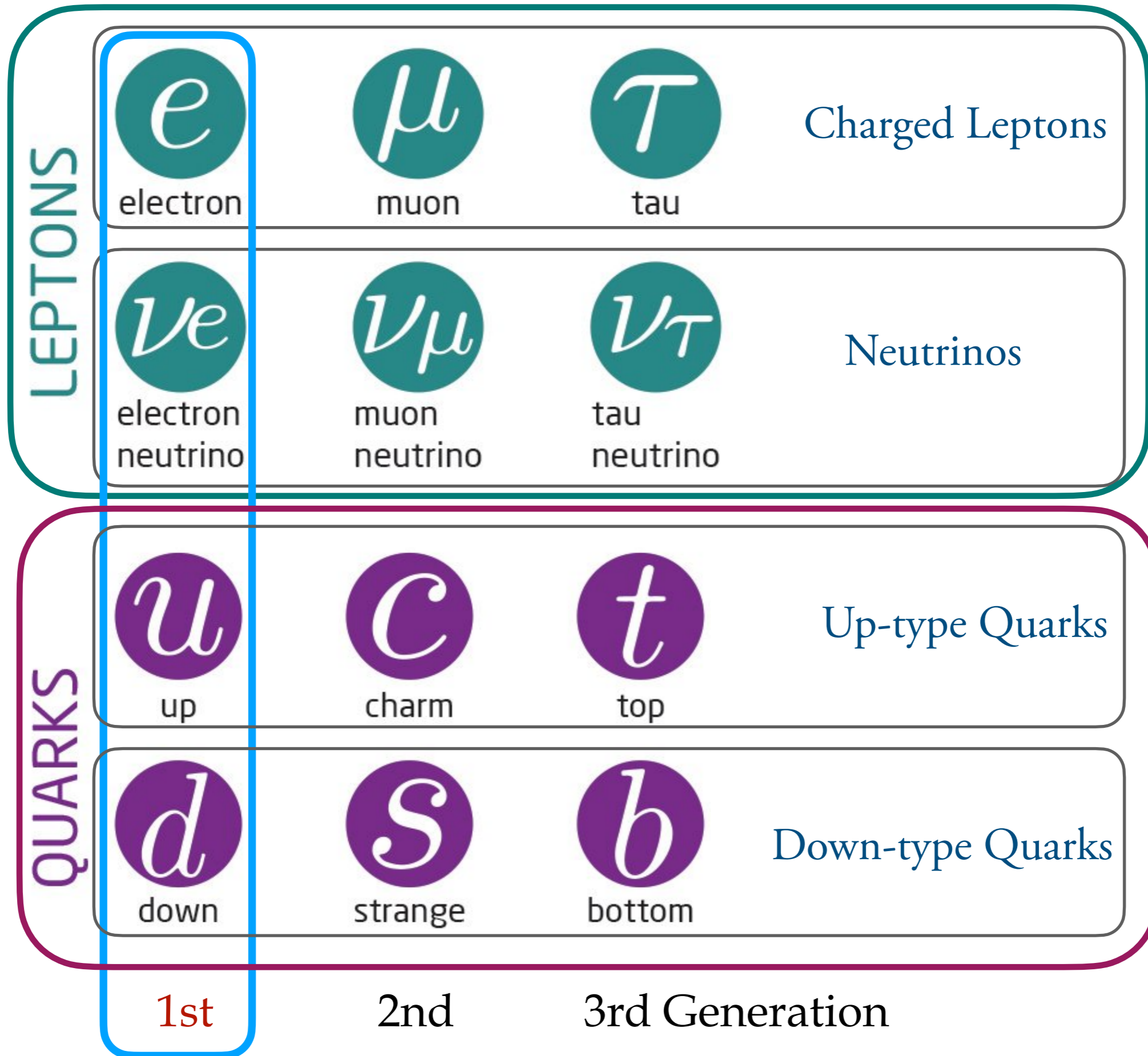
$$m = 4.18_{-0.03}^{+0.04} \text{ GeV}$$



top

$$m = 173.1 \pm 0.6 \text{ GeV}$$

Experimental Findings: *Fermions*



Experimental Findings: *Gauge Bosons*

Spin 1 gauge particles and vast range of *masses* (force carriers)



$$m < 1 \times 10^{-18} \text{ eV}$$

Interacts with electrically charged particles



$$m = 80.399 \pm 0.023 \text{ GeV}$$

Interacts with LH particles



$$m = 91.1876 \pm 0.0021 \text{ GeV}$$

Interacts with all particles



$$m = 0$$

Interacts with quarks (colored particles)

Experimental Findings: *Scalar Boson*

Spin 0 particle with non-zero *mass*



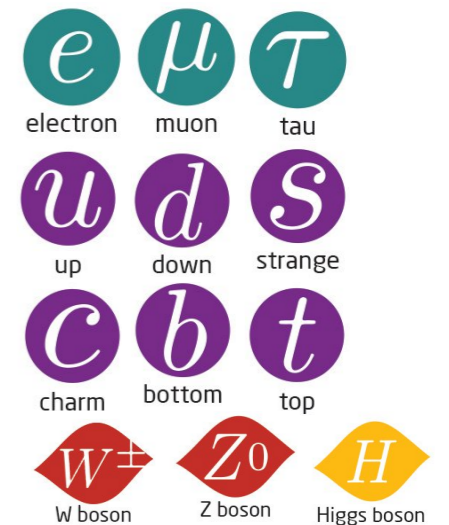
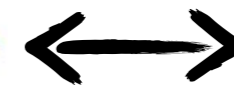
Higgs boson

$$m = 125.18 \pm 0.16 \text{ GeV}$$

◆ Interacts with massive particles, the more massive the stronger the interaction.




Higgs boson



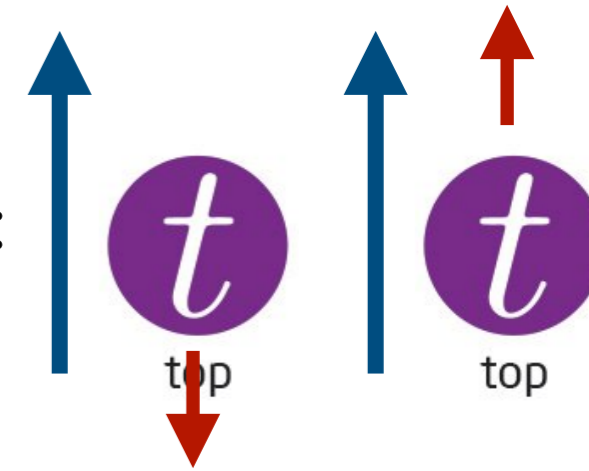
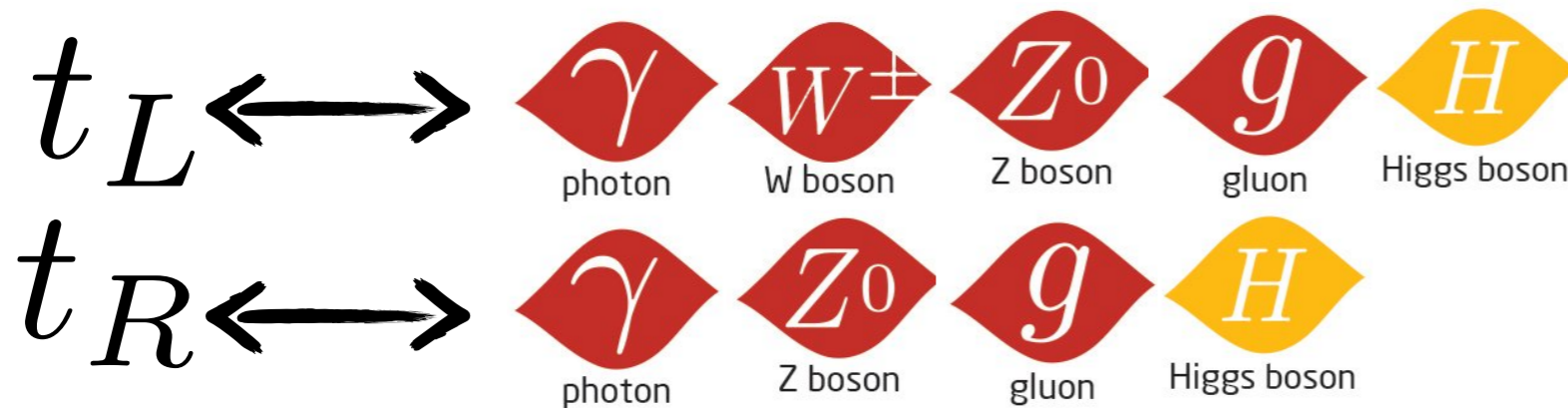
◆ The last elementary particle discovered in 2012 at the LHC

Experimental Findings

- ◆ Measured particle properties:


 $m = 173.1 \pm 0.6 \text{ GeV}$
 $J = 1/2$

- ◆ Spin is a vector quantity (magn., direction). In VHE limit:



- ◆ A Dirac top quark is linear combination of both states.

- ◆ Neutrinos are left-handed

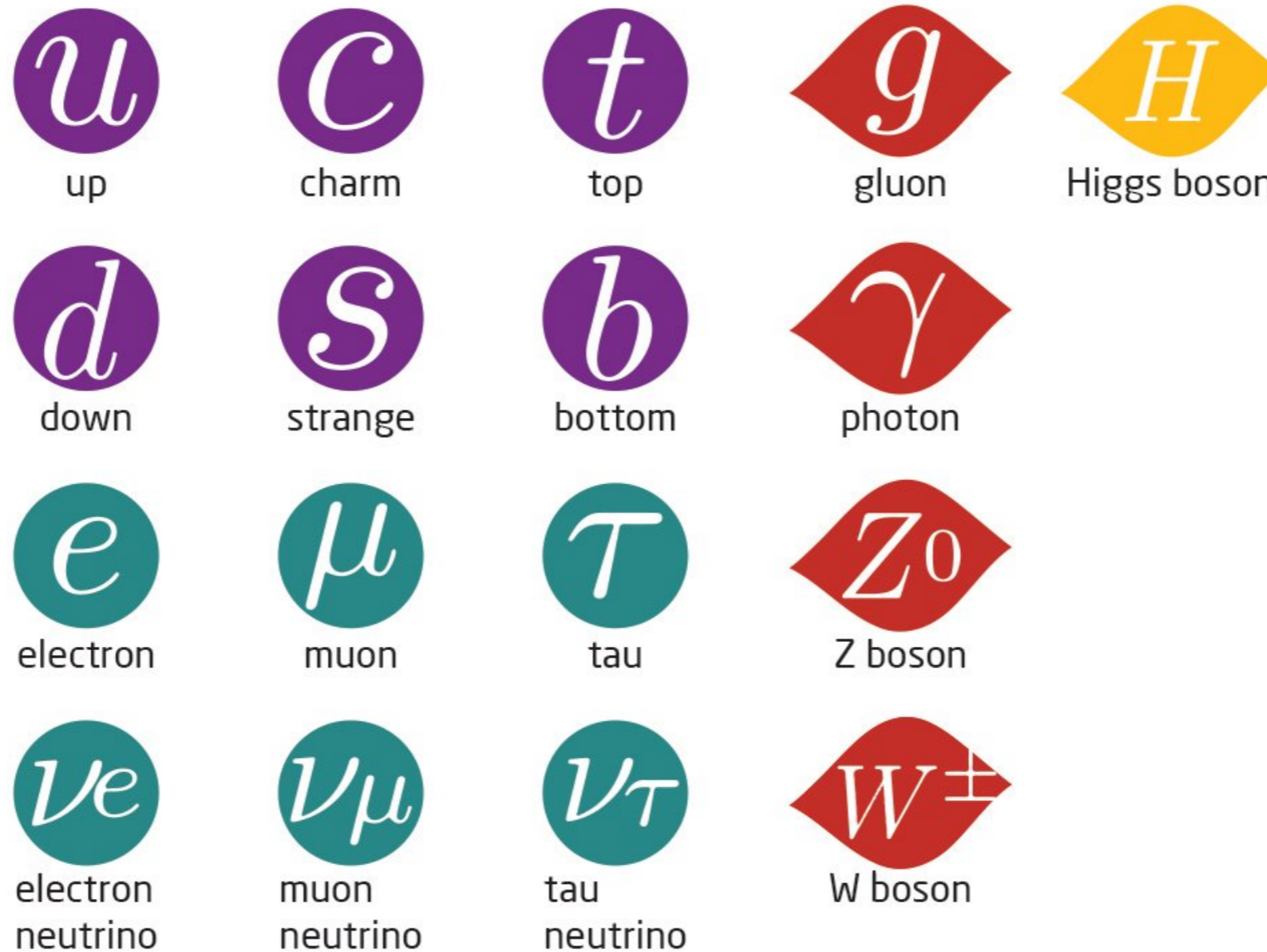
- ◆ Parameters to parametrize the strengths of interactions: quantum numbers

$$1/3, \{R, B, G\}, y_t, \text{etc.}$$

- ◆ There are also anti-particles.

Experimental Findings

◆ Experimentally, we know that what the Universe is made of at *some* fundamental level:



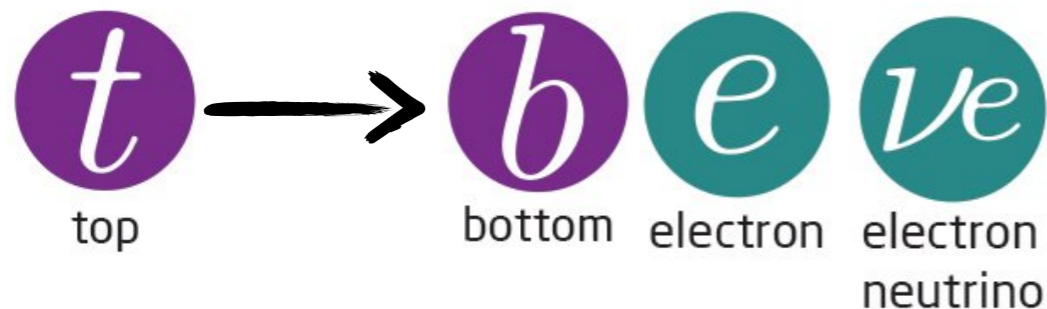
+ anti-particles.

◆ **Next question:** If there is model to understand and describe elementary particles, their properties and interactions in mathematical terms?

◆ **What is a particle?**

Theoretical Framework: *Quantum Mechanics*

- ◆ A theoretical practical framework for understanding physics at the microscopic scale: **Quantum Mechanics**. A probabilistic understanding of subatomic phenomena.
- ◆ A particle is a *state* in the Hilbert space.
- ◆ However, single particle quantum mechanics is not applicable to particle phenomena: the number/type of particles changes in interactions.



- ◆ Thus we need a more general framework that applies the quantum rules.

Theoretical Framework: *Special Relativity*

◆ Experimental data indicate that **Lorentz symmetry** is respected by particle phenomena.

Conservation of energy-momentum, angular momentum in interaction.

Anti-particles, DOF's, particular kinds of interactions, etc.

◆ A symmetry of nature: **Lorentz invariance** (all inertial observers see same physics: special relativity)

◆ All (physical) quantities classified by how they transform under Lorentz group $SO(1,3)$. (recall: Lorentz group is subgroup of Poincare)

◆ **Wigner**: Unitary irreducible representations are characterized by two invariants: call them **Mass** m and **Spin** J , with 1, 2, $2J+1$ DOF's.
(infinite-dimensional representation)

◆ Particles are in infinite-dimensional irreducible *representations* of the


Lorentz group. $so(1,3) = sl(2, C) = su(2)_L \times su(2)_R$

$$(j_1, j_2) \quad J = j_1 + j_2, j_1 + j_2 - 1, \dots, |j_1 - j_2|$$

Theoretical Framework: *Quantum Field Theory*

- ◆ A particle is a *state* in the Hilbert space.
- ◆ A particles is in infinite-dimensional irreducible *representations* of the Lorentz group.
- ◆ A unique framework including QM plus SR: *Quantum Field Theories*
 - ◆ What is a quantum field?
Infinite number of harmonic oscillators.
Natural object to describes particles.
Particles are excitations of quantum fields.

Theoretical Framework: *Quantum Field Theory*

Higgs particle:  $J = 0$
 $m = 125.18 \pm 0.16 \text{ GeV}$

Higgs field:
$$h(x) = \int \frac{d^3\mathbf{p}}{(2\pi)^3} [a_{\mathbf{p}}(t)e^{i\mathbf{p}\cdot\mathbf{x}} + a_{\mathbf{p}}(t)^\dagger e^{-i\mathbf{p}\cdot\mathbf{x}}]$$

$a_{\mathbf{p}}^\dagger$ Creates a Higgs particle, with momentum \mathbf{p} and energy $E_{\mathbf{p}}^2 = |\mathbf{p}|^2 + m^2$

$(\partial_t^2 + E_{\mathbf{p}}^2)a_{\mathbf{p}}(t) = 0$ Equation of motion of a harmonic oscillator

- ◆ A Higgs particle is a *state* in the Hilbert space. $|\mathbf{p}\rangle$
- ◆ The Higgs particles is infinite-dimensional irreducible representations of the Lorentz group. $(0, 0)$

Theoretical Framework: *Quantum Field Theory*

top (anti)particle:  $J = 1/2$
 $m = 173.1 \pm 0.6 \text{ GeV}$

top (anti) field:
$$t(x) = \sum_s \int \frac{d^3\mathbf{p}}{(2\pi)^3} [a_{\mathbf{p}}^s(t) u_{\mathbf{p}}^s e^{i\mathbf{p}\cdot\mathbf{x}} + b_{\mathbf{p}}^{s\dagger}(t) v_{\mathbf{p}}^s e^{-i\mathbf{p}\cdot\mathbf{x}}]$$


$$\bar{t}(x) = \sum_s \int \frac{d^3\mathbf{p}}{(2\pi)^3} [a_{\mathbf{p}}^{s\dagger}(t) \bar{u}_{\mathbf{p}}^s e^{-i\mathbf{p}\cdot\mathbf{x}} + b_{\mathbf{p}}^s(t) \bar{v}_{\mathbf{p}}^s e^{i\mathbf{p}\cdot\mathbf{x}}]$$

$a_{\mathbf{p}}^{s\dagger}$, $b_{\mathbf{p}}^{s\dagger}$ Creates a top (anti)particle, with momentum \mathbf{p} , spin state s
 $E_{\mathbf{p}}^2 = |\mathbf{p}|^2 + m^2$

$(\partial_t^2 + E_{\mathbf{p}}^2)a_{\mathbf{p}}(t) = 0$ Equation of motion of a harmonic oscillator

- ◆ A top particle is a *state* in the Hilbert space. $|\mathbf{p}, s\rangle$
- ◆ The top particle is in infinite-dimensional irreducible representations of the Lorentz group. $(1/2, 0) + (0, 1/2)$

Theoretical Framework: *Quantum Field Theory*

Z boson particle:  $J = 1$
 $m = 91.1876 \pm 0.0021 \text{ GeV}$

Z field:
$$Z_\mu(x) = \sum_i \int \frac{d^3\mathbf{p}}{(2\pi)^3} [\epsilon_{\mu,\mathbf{p}}^i a_{\mathbf{p}}^i(t) e^{i\mathbf{p}\cdot\mathbf{x}} + \epsilon_{\mu,\mathbf{p}}^{i*} a_{\mathbf{p}}^{i\dagger}(t) e^{-i\mathbf{p}\cdot\mathbf{x}}]$$

$a_{\mathbf{p}}^{i\dagger}$ Creates a Z boson, with momentum \mathbf{p} , spin state i , $E_{\mathbf{p}}^2 = |\mathbf{p}|^2 + m^2$

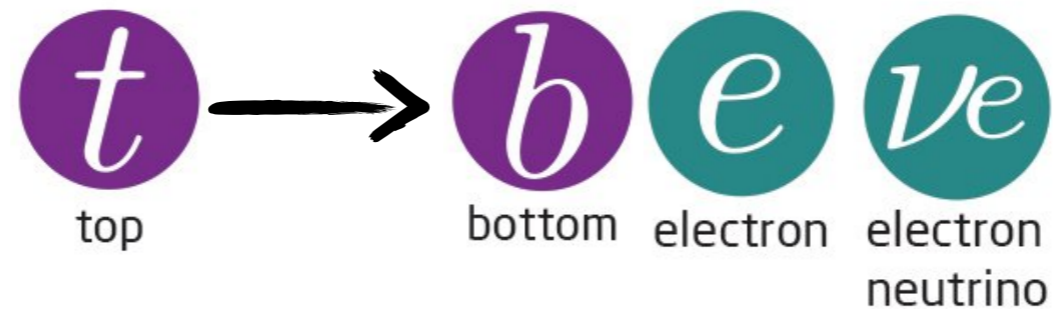
$(\partial_t^2 + E_{\mathbf{p}}^2) a_{\mathbf{p}}(t) = 0$ Equation of motion of a harmonic oscillator

- ◆ A top particle is a *state* in the Hilbert space. $|\mathbf{p}, s\rangle$
- ◆ The top particle is in infinite-dimensional irreducible representations of the Lorentz group. $(1/2, 1/2)$

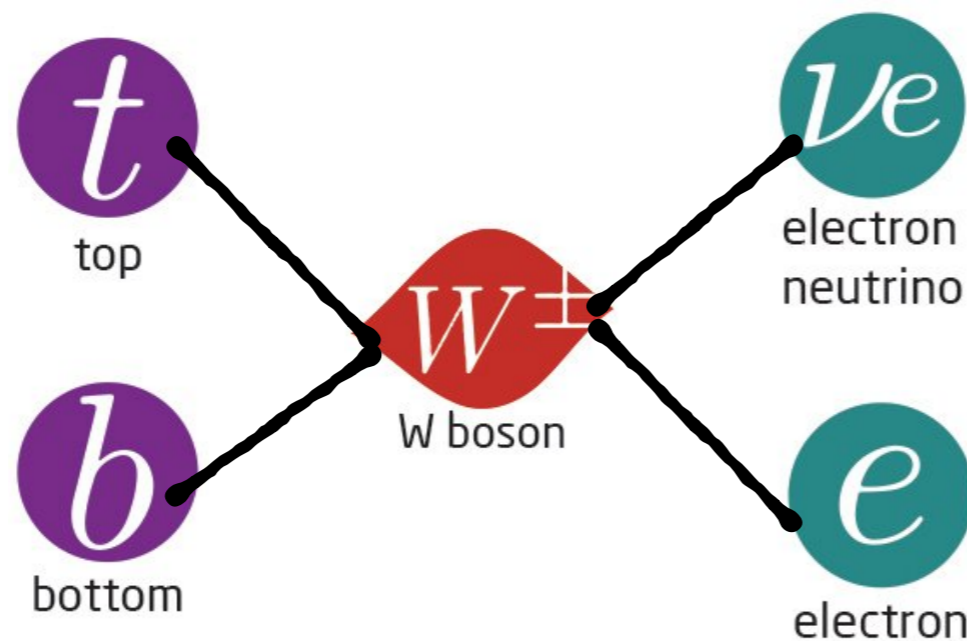
Theoretical Framework: *Quantum Field Theory*

- ◆ Interactions: non-linear terms of quantum fields in the Hamiltonian

Decay of top particle to a bottom, electron and anti-neutrino particles



$$\mathcal{H} \supset t_L(x)b_L(x)W_\mu(x) + e_L(x)\nu_L(x)W_\mu(x)$$



Theoretical Framework: Quantum Electrodynamics

◆ Electron-Photon $U(1)$ interaction

Charged Dirac fermion interacting with massless photon.



$$\psi(x) = \sum_s \int \frac{d^3\mathbf{p}}{(2\pi)^3} [a_{\mathbf{p}}^s(t) u_{\mathbf{p}}^s e^{i\mathbf{p}\cdot\mathbf{x}} + b_{\mathbf{p}}^{s\dagger}(t) v_{\mathbf{p}}^s e^{-i\mathbf{p}\cdot\mathbf{x}}]$$

$$\bar{\psi}(x) = \sum_s \int \frac{d^3\mathbf{p}}{(2\pi)^3} [a_{\mathbf{p}}^{s\dagger}(t) \bar{u}_{\mathbf{p}}^s e^{-i\mathbf{p}\cdot\mathbf{x}} + b_{\mathbf{p}}^s(t) \bar{v}_{\mathbf{p}}^s e^{i\mathbf{p}\cdot\mathbf{x}}]$$



$$A_\mu(x) = \sum_i \int \frac{d^3\mathbf{p}}{(2\pi)^3} [\epsilon_{\mu,\mathbf{p}}^i a_{\mathbf{p}}^i(t) e^{i\mathbf{p}\cdot\mathbf{x}} + \epsilon_{\mu,\mathbf{p}}^{i*} a_{\mathbf{p}}^{i\dagger}(t) e^{-i\mathbf{p}\cdot\mathbf{x}}]$$

$$\mathcal{L} = -\frac{1}{4} F_{\mu\nu} F_{\mu\nu} + i\gamma_\mu \bar{\psi} \partial_\mu \psi - e\gamma_\mu A_\mu \bar{\psi} \psi - m\bar{\psi} \psi$$
$$F_{\mu\nu} = -\frac{1}{4} (\partial_\mu A_\nu - \partial_\nu A_\mu)$$

◆ Abelian $U(1)$ gauge symmetry

$$A_\mu \rightarrow A_\mu + \partial_\mu \alpha$$

$$\psi \rightarrow \psi e^{i\alpha}$$

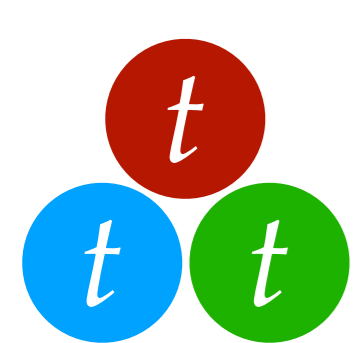
$$\bar{\psi} \rightarrow \bar{\psi} e^{-i\alpha}$$

◆ The unique way a charged particle interacts with massless vector particle.

Theoretical Framework: Quantum Yang-Mills Theory

◆ Quark-Gluon $SU(3)$ interactions

Colored Dirac fermions interacting with massless gluon.



$$t^{r,g,b}(x) = \sum_s \int \frac{d^3\mathbf{p}}{(2\pi)^3} [a_{s,\mathbf{p}}^{r,g,b}(t) u_{s,\mathbf{p}} e^{i\mathbf{p}\cdot\mathbf{x}} + b_{s,\mathbf{p}}^{r,g,b\dagger}(t) v_{s,\mathbf{p}} e^{-i\mathbf{p}\cdot\mathbf{x}}]$$

$$\bar{t}^{r,g,b}(x) = \sum_s \int \frac{d^3\mathbf{p}}{(2\pi)^3} [a_{s,\mathbf{p}}^{r,g,b\dagger}(t) \bar{u}_{s,\mathbf{p}} e^{-i\mathbf{p}\cdot\mathbf{x}} + b_{s,\mathbf{p}}^{r,g,b}(t) \bar{v}_{s,\mathbf{p}} e^{i\mathbf{p}\cdot\mathbf{x}}]$$



$$g_\mu^a(x) = \sum_i \int \frac{d^3\mathbf{p}}{(2\pi)^3} [\epsilon_{\mu,\mathbf{p}}^i a_{\mathbf{p}}^{a,i}(t) e^{i\mathbf{p}\cdot\mathbf{x}} + \epsilon_{\mu,\mathbf{p}}^{i*} a_{\mathbf{p}}^{a,i\dagger}(t) e^{-i\mathbf{p}\cdot\mathbf{x}}]$$

$$\mathcal{L} = -\frac{1}{4} G_{\mu\nu}^a G_{\mu\nu}^a + i\gamma_\mu \bar{\psi}^I \partial_\mu \psi^I - g_s (T^a)^{IJ} \gamma_\mu g_\mu^a \bar{\psi}^I \psi^J - m \bar{\psi}^I \psi^I$$

$$G_{\mu\nu}^a = \partial_\mu g_\nu^a - \partial_\nu g_\mu^a + g_s f^{abc} A_\mu^b A_\nu^c$$

◆ Non-Abelian $SU(3)$ gauge symmetry

$$g_\mu^a \rightarrow g_\mu^a - f^{abc} \alpha^b A_\mu^c$$

$$\psi^I \rightarrow e^{i\alpha^a (T^a)^{IJ}} \psi^J$$

$$\bar{\psi}^I \rightarrow e^{-i\alpha^a (T^a)^{IJ}} \bar{\psi}^J$$

Theoretical Framework: *Higgs Mechanism*

- ◆ Complex Scalar-Photon $U(1)$ interaction

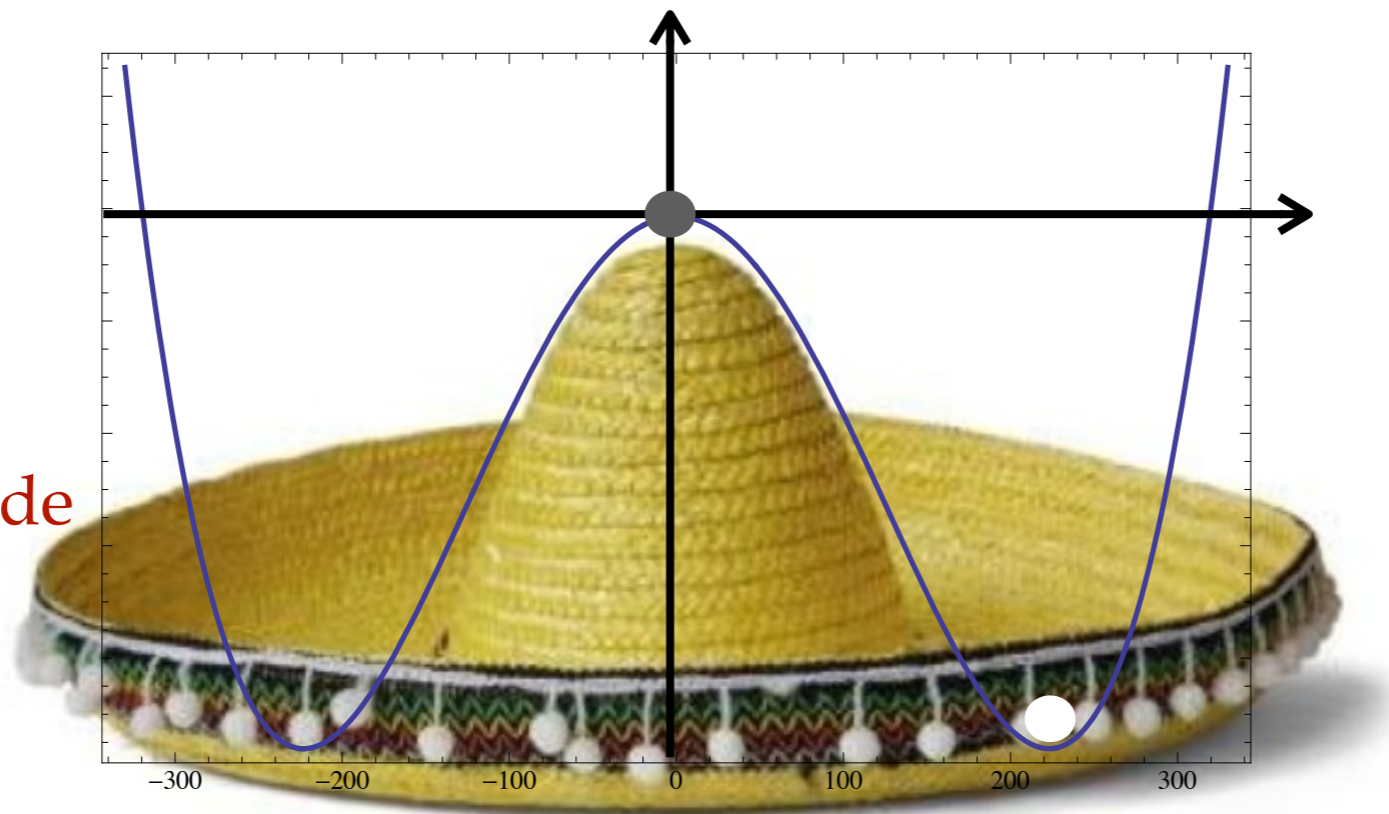
$$\mathcal{L} = -\frac{1}{4}F_{\mu\nu}F_{\mu\nu} + |\partial_\mu\phi|^2 - ieA_\mu(\phi^*\partial_\mu\phi - \phi\partial_\mu\phi^*) + e^2A_\mu^2|\phi|^2 - V(\phi)$$

- ◆ Abelian $U(1)$ gauge symmetry $A_\mu \rightarrow A_\mu + \partial_\mu\alpha$ $\phi \rightarrow \phi e^{i\alpha}$ $\bar{\phi} \rightarrow \bar{\phi} e^{-i\alpha}$

- ◆ Scalar potential $V(\phi) = -m^2|\phi|^2 + \lambda|\phi|^4$

$$\phi = \varphi e^{i\sigma}$$

Goldstone mode
Longitudinal mode



- ◆ Spontaneous symmetry breaking $\langle\phi\rangle = v$

- ◆ Photons receives a mass in the vacuum $m_A = ev$

Theoretical Framework: *Quantum Field Theory*

◆ A quantum field theory for particles physics?

◆ **Particles (discovered experimentally)**, $90+19+1=110$ dof's, 3 **Interactions**

$e_L, e_R, \nu_L^e, u_L^r, u_L^g, u_L^b, u_R^r, u_R^g, u_R^b, d_L^r, d_L^g, d_L^b, d_R^r, d_R^g, d_R^b$

$\mu_L, \mu_R, \nu_L^\mu, c_L^r, c_L^g, c_L^b, c_R^r, c_R^g, c_R^b, s_L^r, s_L^g, s_L^b, s_R^r, s_R^g, s_R^b$ + anti-particles

$\tau_L, \tau_R, \nu_L^\tau, t_L^r, t_L^g, t_L^b, t_R^r, t_R^g, t_R^b, b_L^r, b_L^g, b_L^b, b_R^r, b_R^g, b_R^b$

$\gamma, W_T^\pm, W_L^\pm, Z_T, Z_L, g^{rb}, \dots, h$

◆ **18 Parameters**: 12 mass, 2 interaction strengths, 3 mixing angles, 1 phase

◆ **Symmetries (deduced experimentally)**:

Spacetime (global) symmetries: Poincare Group $ISO(1,3)$

Internal (gauge) symmetries: $SU(3)_c, U(1)_{EM}$

◆ Quantum field for each dof. A very messy interacting Lagrangian.

◆ It is the limit of an elegant model in its symmetry breaking phase:

The *Standard Model*.

The Standard Model

- ◆ A particular interacting quantum field theory, explains experiments well.

Symmetry Structure:

Spacetime (global) symmetries: Poincare Group $ISO(1,3)$ (Structure)

Internal (gauge) symmetries: $SU(3)_c, SU(2)_L, U(1)_Y$ (Interactions)

The field content:

Field	$SU(3)_c \times SU(2)_L \times U(1)_Y$	$ISO(1,3)$
$L = \begin{bmatrix} \nu_L \\ e_L \end{bmatrix}$	(1, 2, -1)	(1/2, 0)
e_R^c	(1, 1, 2)	(1/2, 0)
$Q = \begin{bmatrix} u_L \\ d_L \end{bmatrix}$	(3, 2, 1/3)	(1/2, 0)
u_R^c	($\bar{3}$, 1, -4/3)	(1/2, 0)
d_R^c	($\bar{3}$, 1, 2/3)	(1/2, 0)
$H = \begin{bmatrix} \sigma^1 + i\sigma^2 \\ h + i\sigma^3 \end{bmatrix}$	(1, 2, 1)	(0, 0)
g	(8, 1, 0)	(1/2, 1/2)
W	(1, 3, 0)	(1/2, 1/2)
B	(1, 1, 0)	(1/2, 1/2)

+ anti-particles

The Standard Model

- ◆ The most general renormalizable invariant Lagrangian

$$\begin{aligned}\mathcal{L} = & -\frac{1}{4}B_{\mu\nu}B^{\mu\nu} - \frac{1}{4}W_{\mu\nu}^i W_i^{\mu\nu} - \frac{1}{4}G_{\mu\nu}^a G_a^{\mu\nu} \\ & + \bar{L}\gamma_\mu(i\partial_\mu + gW + Y_L g' B)L + \bar{e}_R\gamma_\mu(i\partial_\mu + Y_e g' B)e_R \\ & + \bar{Q}\gamma_\mu(i\partial_\mu + gW + Y_Q g' B + g_s g)Q + \bar{u}_R\gamma_\mu(i\partial_\mu + Y_u g' B + g_s g)u_R + \bar{d}_R\gamma_\mu(i\partial_\mu + Y_d g' B + g_s g)d_R \\ & + y_u Q\bar{u}H + y_d Q\bar{d}\tilde{H} + y_e L\bar{e}\tilde{H} \quad + 2 \text{ families} \\ & + (\partial_\mu H - igWH - iY_H g' BH)^\dagger (\partial_\mu H - igWH - iY_H g' BH) - V(H)\end{aligned}$$

- ◆ The Higgs potential

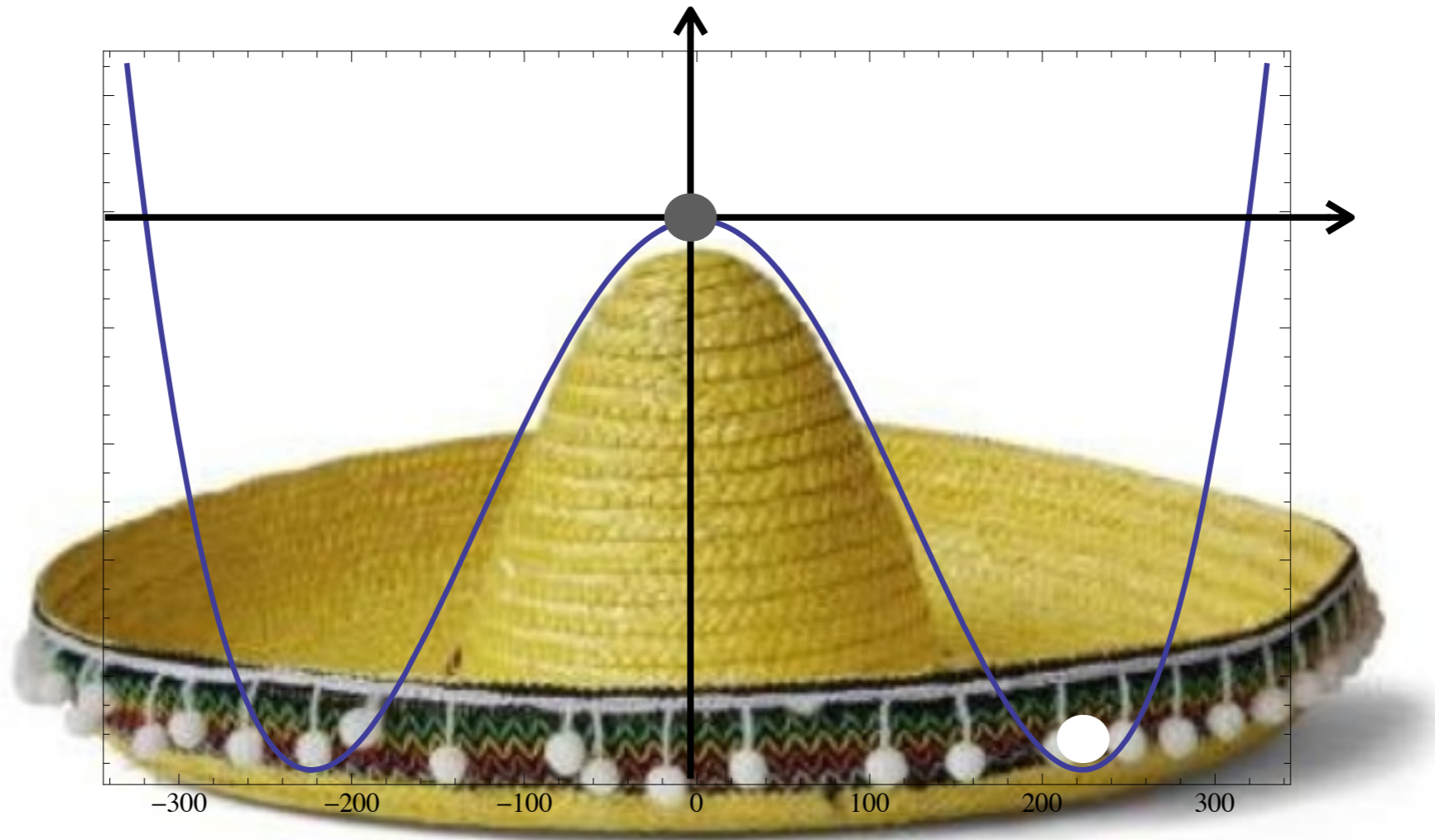
$$V(H) = -m^2 H^\dagger H + \lambda(H^\dagger H)^2$$

- ◆ Besides, there are 19 free parameters. Only 1 mass parameter.
- ◆ The *strong* interaction sector is an easy piece.
- ◆ The *electroweak* sector is non-trivial, as it is accompanied with a Higgs mechanism.

The Electroweak Sector

- ◆ The Higgs potential $V(H) = -m^2 H^\dagger H + \lambda (H^\dagger H)^2$

$H: (1, 2, 1)$



- ◆ The Higgs mechanism for the electroweak symmetry breaking $\langle H \rangle \neq 0$

$$SU(2)_L \times U(1)_Y \rightarrow U(1)_{EM}$$

The Electroweak Sector

- ◆ The Higgs mechanism and electroweak symmetry breaking

$$\mathcal{L} = -\frac{1}{4} (W_{\mu\nu}^a)^2 - \frac{1}{4} B_{\mu\nu}^2 + (D_\mu H)^\dagger (D_\mu H) + m^2 H^\dagger H - \lambda (H^\dagger H)^2$$

$$D_\mu H = \partial_\mu H - ig W_\mu^a \tau^a H - \frac{1}{2} ig' B_\mu H.$$

- ◆ The Higgs field at the local minimum $H = e^{\frac{i\sigma^a \pi^a}{v}} \begin{bmatrix} 0 \\ v + h \end{bmatrix}$

- ◆ The Higgs expectation value $v = \frac{m}{\sqrt{\lambda}}$

- ◆ The Higgs-gauge interaction at the minimum

$$|D_\mu H|^2 = g^2 \frac{v^2}{8} \left[(W_\mu^1)^2 + (W_\mu^2)^2 + \left(\frac{g'}{g} B_\mu - W_\mu^3 \right)^2 \right]$$

- ◆ The mass eigenstates

$$W_\mu^1 \quad W_\mu^2$$

$$Z_\mu \equiv \cos \theta_w W_\mu^3 - \sin \theta_w B_\mu$$

$$A_\mu \equiv \sin \theta_w W_\mu^3 + \cos \theta_w B_\mu$$

$$\boxed{\tan \theta_w = \frac{g'}{g}}$$

The Electroweak Sector

◆ The Lagrangian electroweak symmetry breaking phase:

$$\begin{aligned}
 \mathcal{L}_{\text{gauge}} = & -\frac{1}{4}F_{\mu\nu}^2 - \frac{1}{4}Z_{\mu\nu}^2 + \frac{1}{2}m_Z^2 Z^\mu Z_\mu - \frac{1}{2}(\partial_\mu W_\nu^+ - \partial_\nu W_\mu^+)(\partial_\mu W_\nu^- - \partial_\nu W_\mu^-) \\
 & + m_W^2 W_\mu^+ W_\mu^- - ie \cot \theta_w \left[\partial_\mu Z_\nu (W_\mu^+ W_\nu^- - W_\nu^+ W_\mu^-) \right. \\
 & \quad \left. + Z_\nu (-W_\mu^+ \partial_\nu W_\mu^- + W_\mu^- \partial_\nu W_\mu^+ + W_\mu^+ \partial_\mu W_\nu^- - W_\mu^- \partial_\mu W_\nu^+) \right] \\
 & - ie \left[\partial_\mu A_\nu (W_\mu^+ W_\nu^- - W_\nu^+ W_\mu^-) \right. \\
 & \quad \left. + A_\nu (-W_\mu^+ \partial_\nu W_\mu^- + W_\mu^- \partial_\nu W_\mu^+ + W_\mu^+ \partial_\mu W_\nu^- - W_\mu^- \partial_\mu W_\nu^+) \right] \\
 & - \frac{1}{2} \frac{e^2}{\sin^2 \theta_w} W_\mu^+ W_\mu^- W_\nu^+ W_\nu^- + \frac{1}{2} \frac{e^2}{\sin^2 \theta_w} W_\mu^+ W_\nu^- W_\mu^+ W_\nu^- \\
 & - e^2 \cot^2 \theta_w (Z_\mu W_\mu^+ Z_\nu W_\nu^- - Z_\mu Z_\mu W_\nu^+ W_\nu^-) + e^2 (A_\mu W_\mu^+ A_\nu W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-) \\
 & + e^2 \cot \theta_w \left[A_\mu W_\mu^+ W_\nu^- Z_\nu + A_\mu W_\mu^- Z_\nu W_\nu^+ - W_\mu^+ W_\mu^- A_\nu Z_\nu \right],
 \end{aligned}$$

$$m_W = \frac{v}{2}g$$

$$m_Z = \frac{1}{2 \cos \theta_w} gv = \frac{v}{2} \sqrt{g^2 + g'^2} = \frac{m_W}{\cos \theta_w}$$

$$e = g \sin \theta_w = g' \cos \theta_w$$

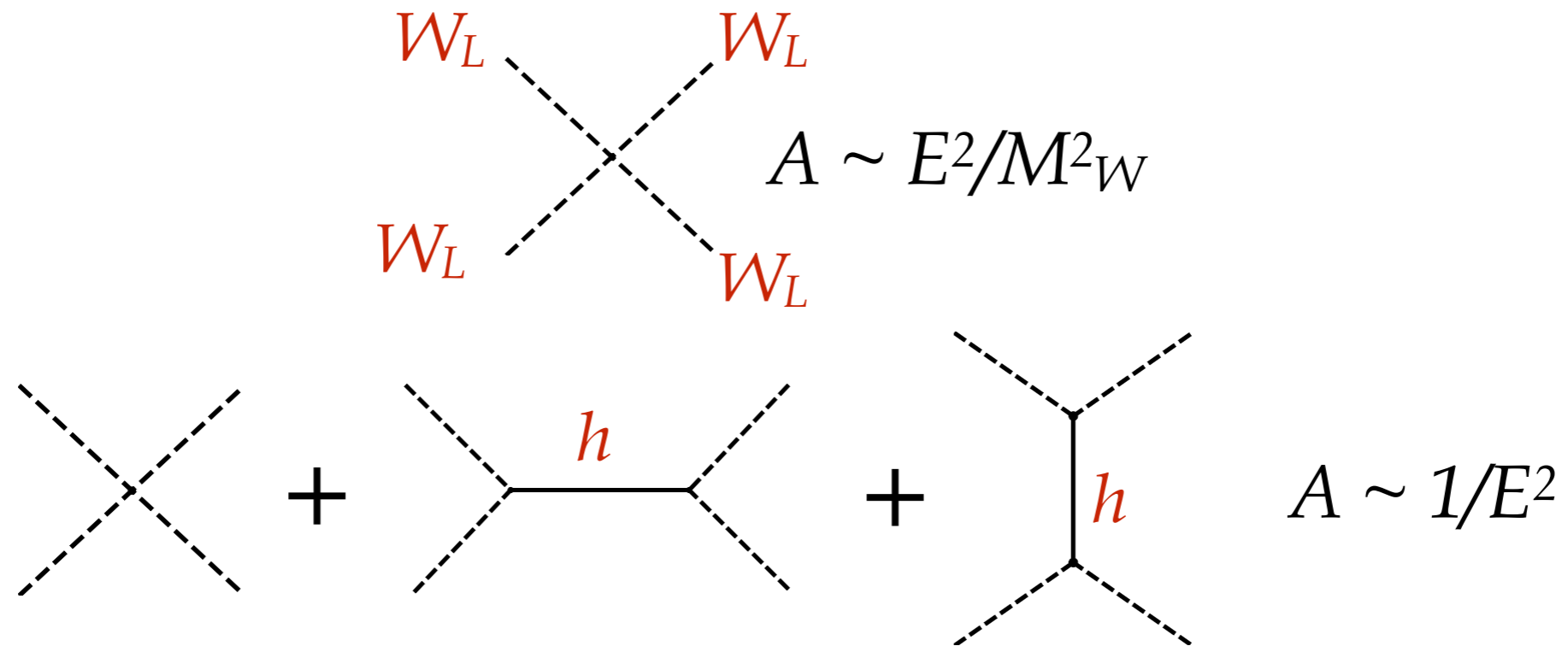
The Electroweak Sector

- ◆ The Lagrangian electroweak symmetry breaking phase:

$$\mathcal{L}_{\text{Higgs}} = -\frac{1}{2}h(\square + m_h^2)h - g\frac{m_h^2}{4m_W}h^3 - \frac{g^2}{32}\frac{m_h^2}{m_W^2}h^4$$

$$+ 2\frac{h}{v}\left(m_W^2 W_\mu^+ W_\mu^- + \frac{1}{2}m_Z^2 Z_\mu^2\right) + \left(\frac{h}{v}\right)^2\left(m_W^2 W_\mu^+ W_\mu^- + \frac{1}{2}m_Z^2 Z_\mu^2\right)$$

- ◆ The Higgs particle unitarizes the scattering of longitudinal modes



- ◆ The SM is unitary and renormalizable up to the Planck scale.

The Electroweak Sector

- ◆ Fermion-Higgs coupling: masses and interactions

$$\mathcal{L}_{\text{Yukawa}} = +y_u Q\bar{u}H + y_d Q\bar{d}\tilde{H} + y_e L\bar{e}\tilde{H}$$

- ◆ In the electroweak symmetry breaking vacuum, fermions are massive and interact with the physical Higgs particle

$$H = e^{\frac{i\sigma^a \pi^a}{v}} \begin{bmatrix} 0 \\ v + h \end{bmatrix}$$

$$\mathcal{L}_{\text{mass}} = (y_u v)u\bar{u} + (y_d v)d\bar{d} + (y_e v)e\bar{e}$$

$$\mathcal{L}_{\text{int}} = y_u h u\bar{u} + y_d h d\bar{d} + y_e h e\bar{e}$$

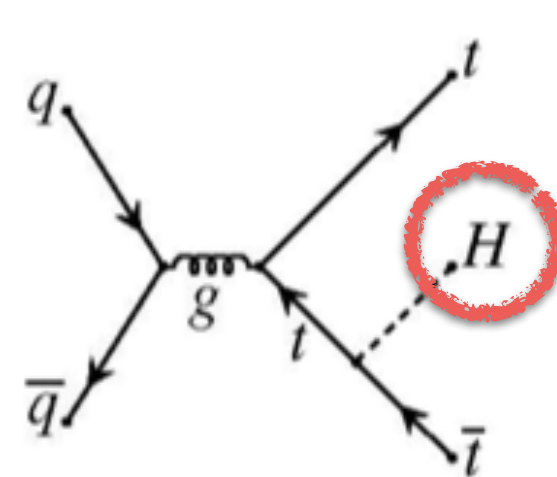
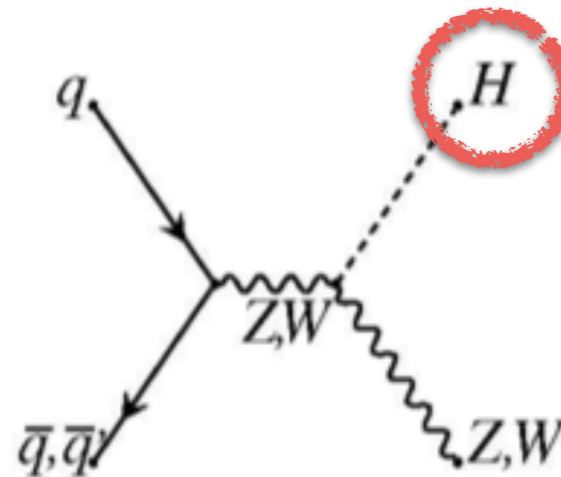
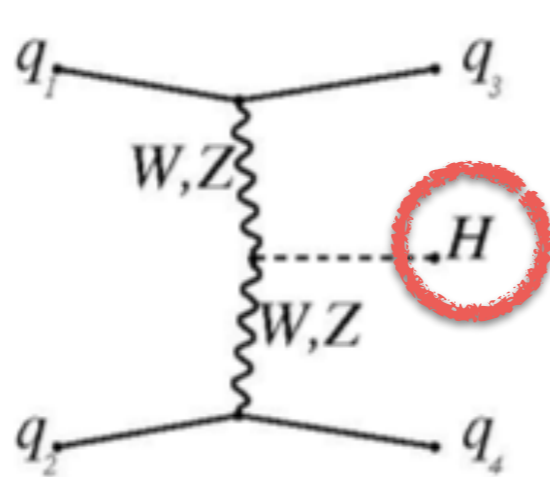
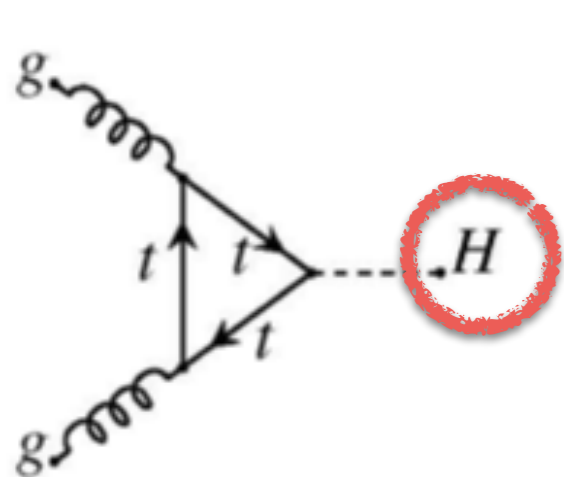
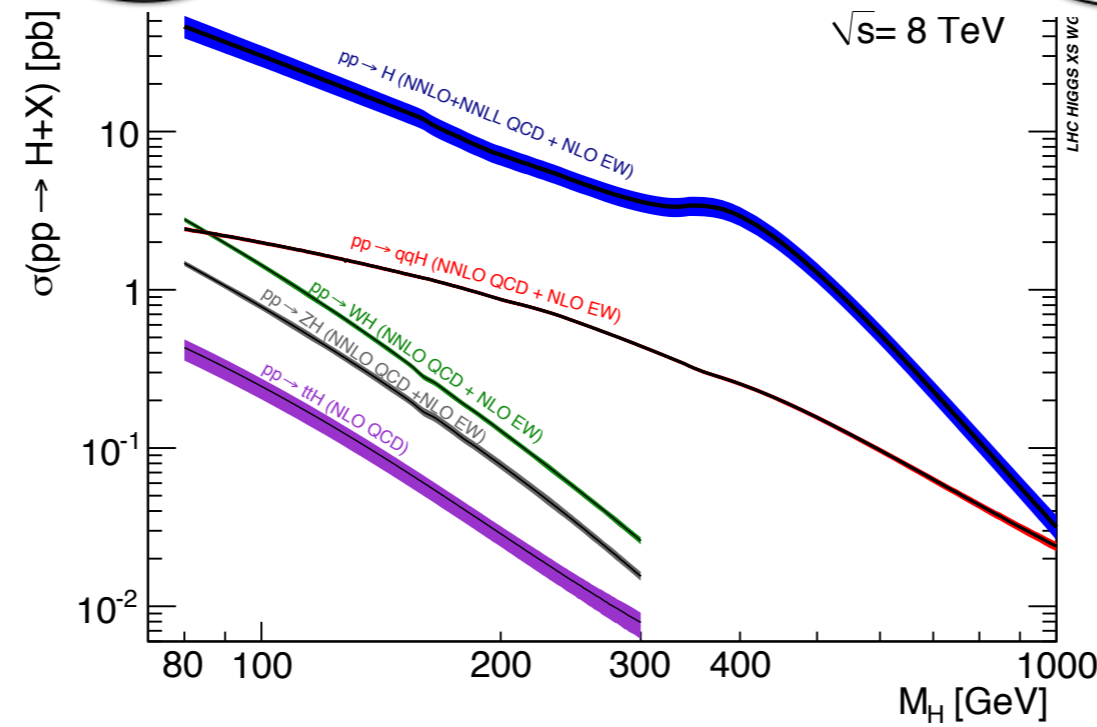
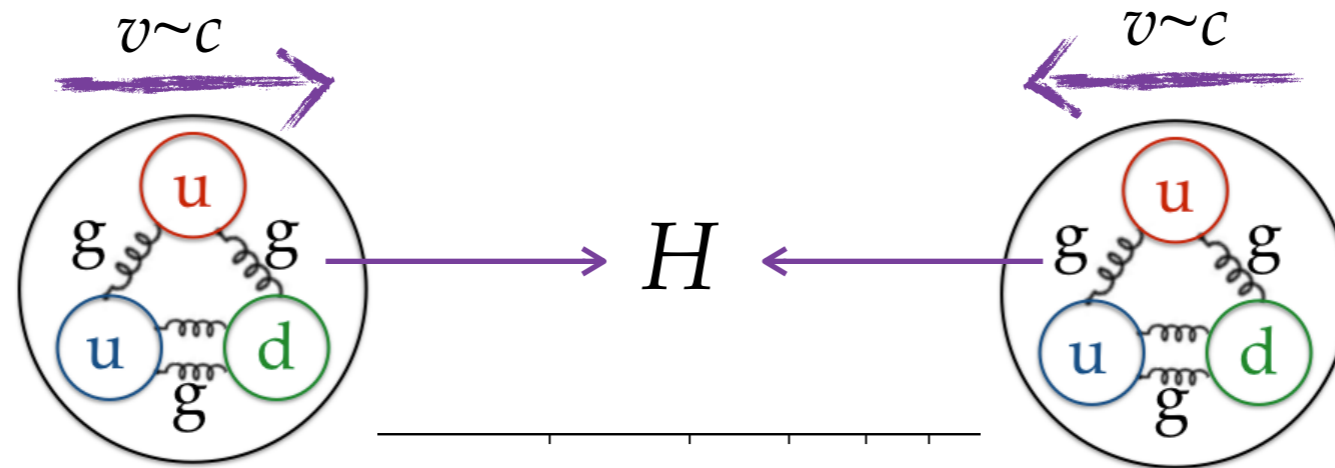
- ◆ The mass and the strengths of interaction are proportional to Yukawa couplings.

- ◆ The heavier the particle, the more strongly coupled to the Higgs.

- ◆ The Higgs is the origin of the mass in the Standard Model.

The Electroweak Sector

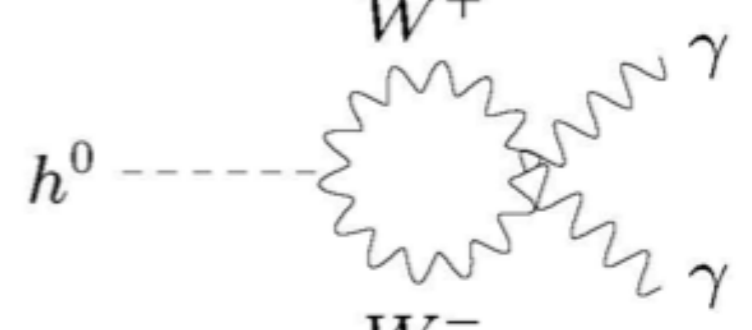
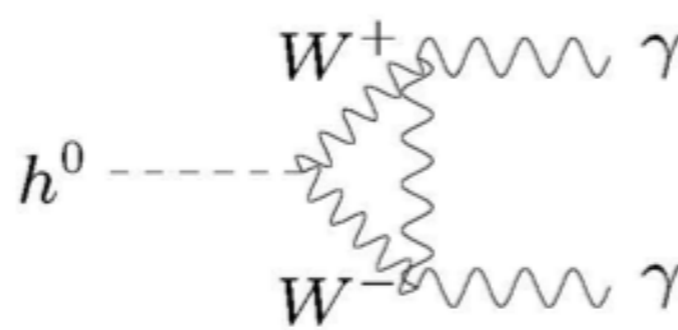
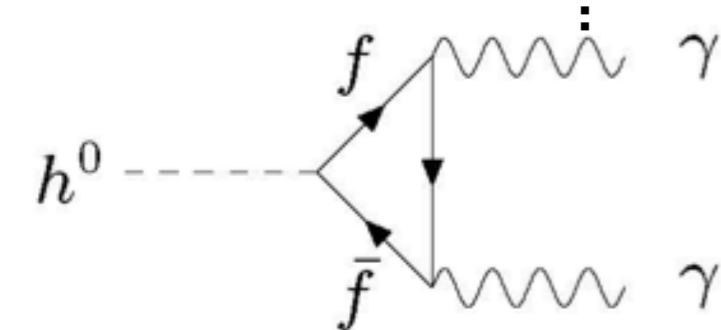
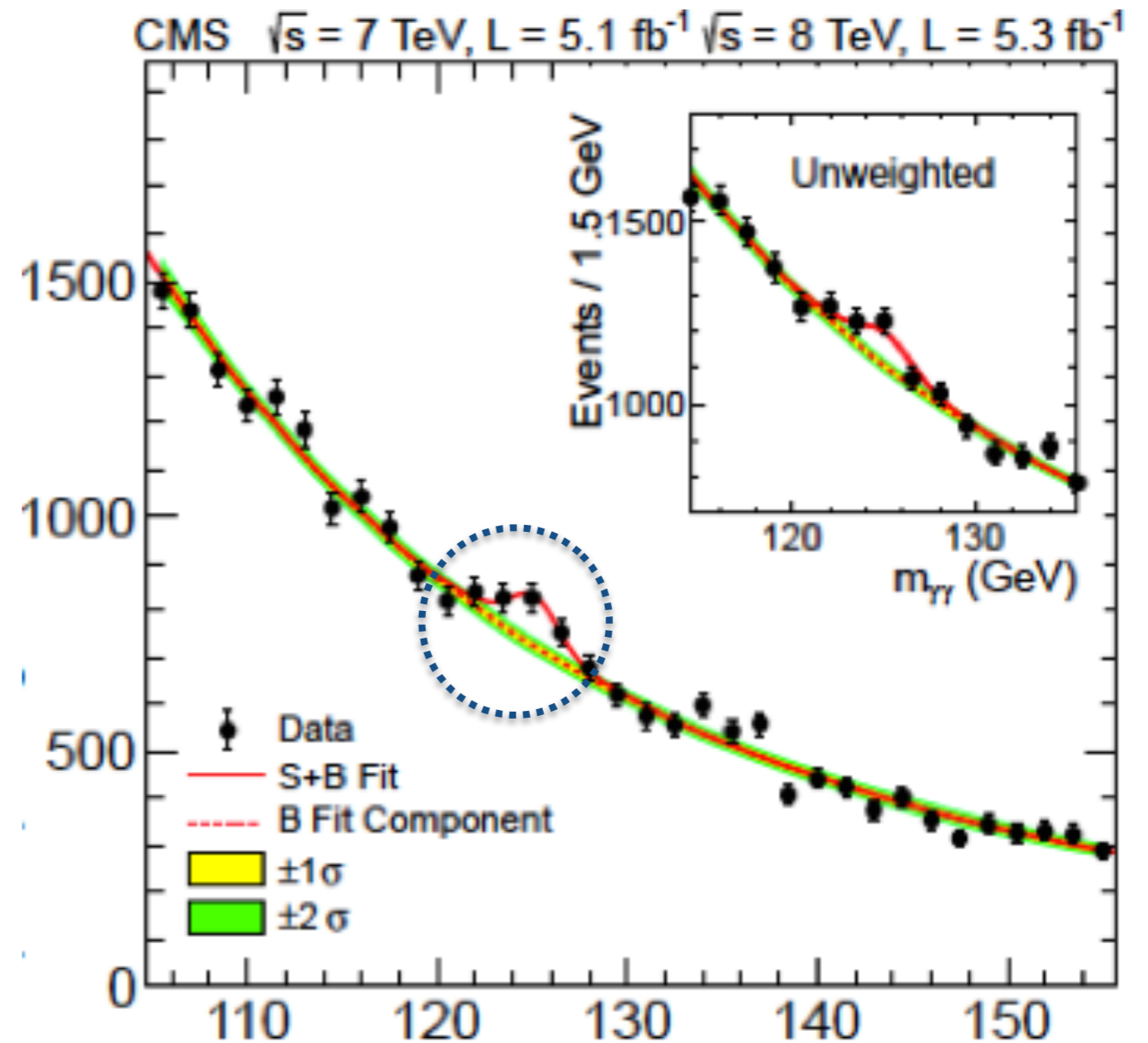
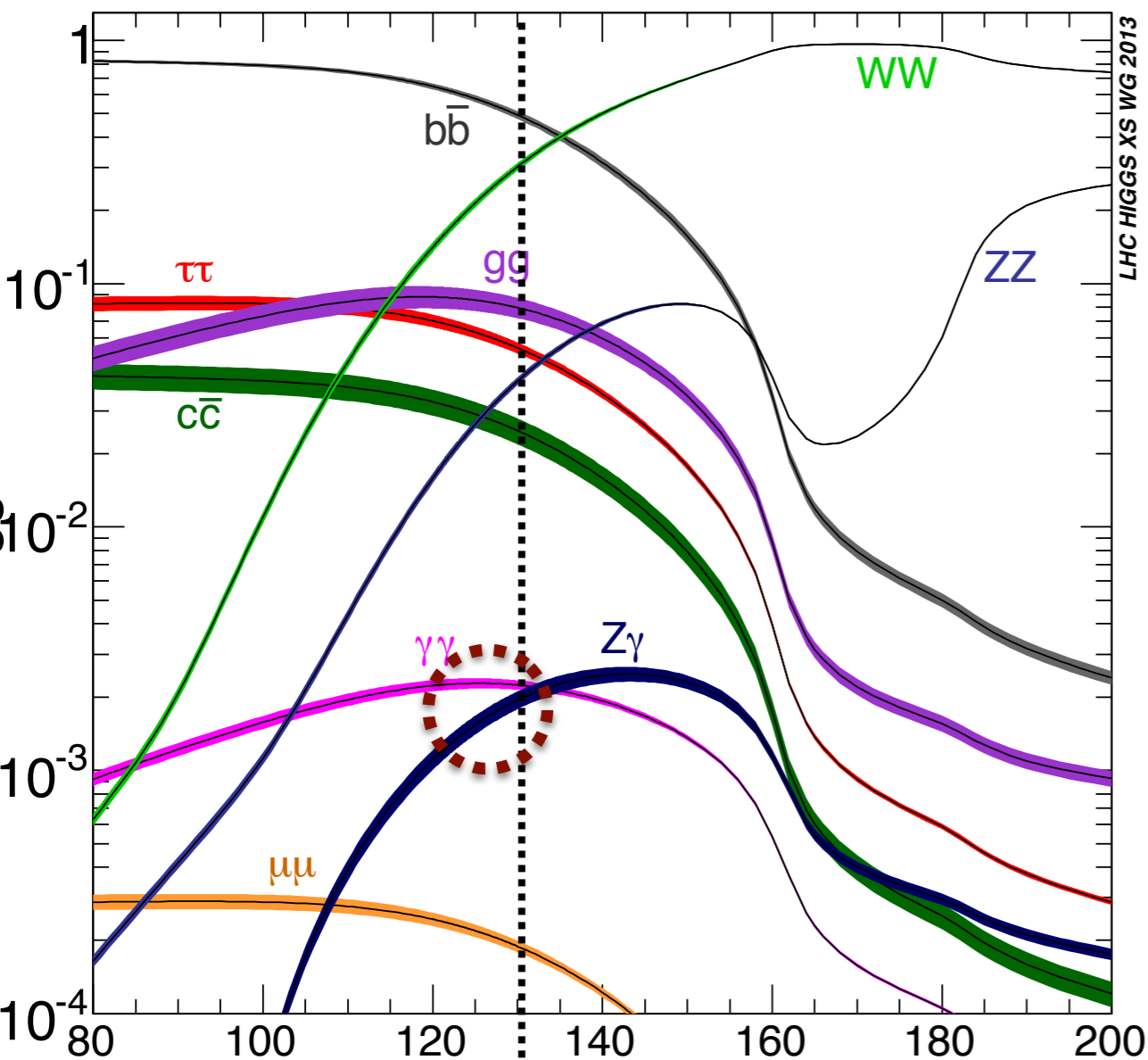
- ◆ The Higgs particles has been discovered 50 years after it was proposed.



The Electroweak Sector

◆ The Higgs particles has been discovered 50 years after it was proposed.

Higgs decays 10^{-22} second after its production to the SM particles.



The End