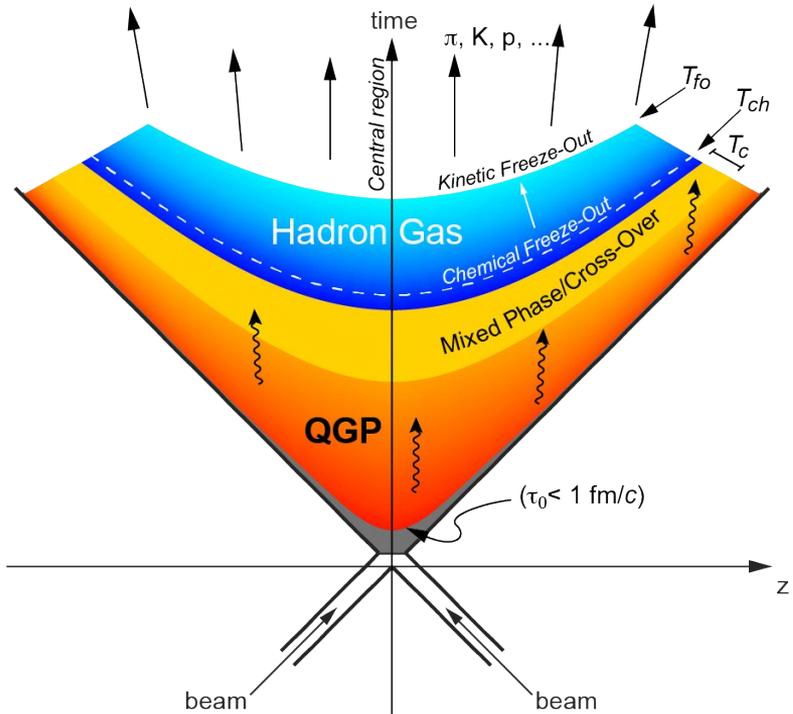


Hadronisation of the QGP

Francesco Prino

INFN – Sezione di Torino

Hadronisation of the QGP



- Hadronization of the QGP medium at the pseudo-critical temperature
 - Transition from a deconfined medium composed of quarks, antiquarks and gluons to color-neutral hadronic matter
 - The partonic degrees of freedom of the deconfined phase convert into hadrons, in which partons are confined
- No first-principle description of hadron formation
 - Non-perturbative problem, not calculable with QCD

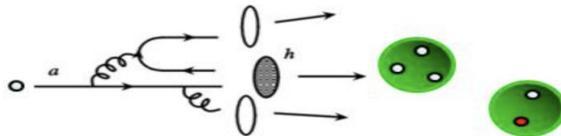
→ Hadronisation from a QGP may be different from other cases in which no bulk of thermalized partons is formed

Independent fragmentation

- Inclusive hadron production from hard scattering processes (large Q^2):
 - Factorization of: PDFs, partonic cross section (pQCD), fragmentation function

$$\sigma_{pp \rightarrow hx} = PDF(x_a, Q^2) PDF(x_b, Q^2) \otimes \sigma_{ab \rightarrow q\bar{q}} \otimes D_{q \rightarrow h}(z, Q^2)$$

- Description of hadronisation effects (heavy quark to meson or baryon) must necessarily resort to models and make use of phenomenological parameters
- **Fragmentation functions** $D_{q \rightarrow h}$ are phenomenological functions to parameterise the *non-perturbative parton-to-hadron transition*
 - z = fraction of the parton momentum taken by the hadron h
 - Do not specify the “microscopic” hadronisation mechanism
 - Parametrised on data and assumed to be “universal”

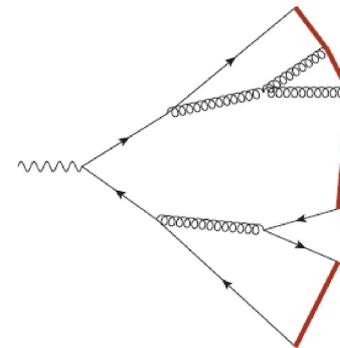


Hadrons from parton showers

- On a microscopic level hadronisation of jets modeled with:
 - Perturbative evolution of a parton shower with DGLAP down to a low-virtuality cut-off Q_0
 - Final stage of parton shower interfaced to a non perturbative hadronisation model

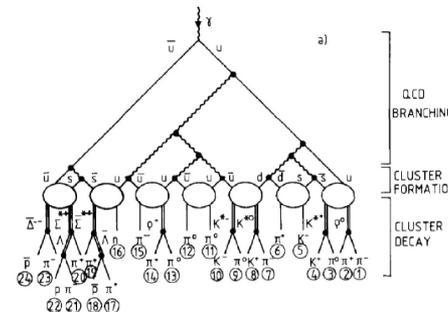
- **String fragmentation** (e.g. Lund model in PYTHIA)

- Strings = colour-flux tubes between q and \bar{q} end-points
- Gluons represent kinks along the string
- Strings break via vacuum-tunneling of (di)quark-anti(di)quark pairs



- **Cluster decay** in HERWIG

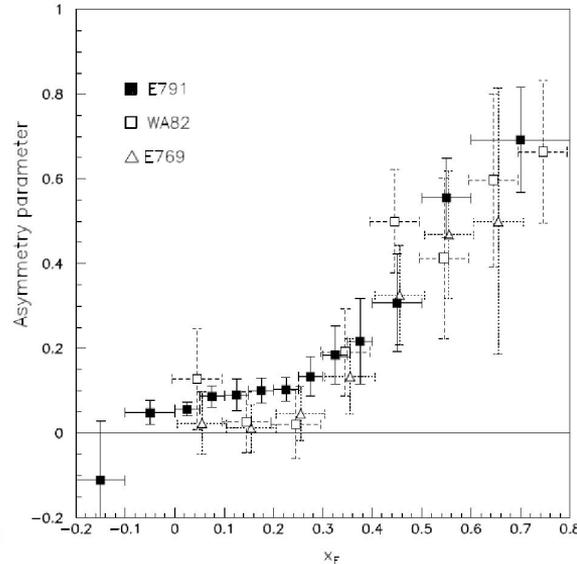
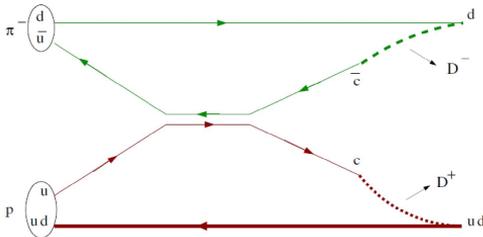
- Shower evolved up to a softer scale
- All gluons forced to split into $q\bar{q}$ pairs
- Identify colour-singlet clusters of partons following color flow
- Clusters decay into hadrons according to available phase space



Leading particle effect

 **WA82, PLB 305 (1993) 402**
 **E791, PLB 371 (1996) 157**

$$A(x_F) = \frac{\left(\frac{d\sigma}{dx_F}\right)^{D^-} - \left(\frac{d\sigma}{dx_F}\right)^{D^+}}{\left(\frac{d\sigma}{dx_F}\right)^{D^-} + \left(\frac{d\sigma}{dx_F}\right)^{D^+}}$$

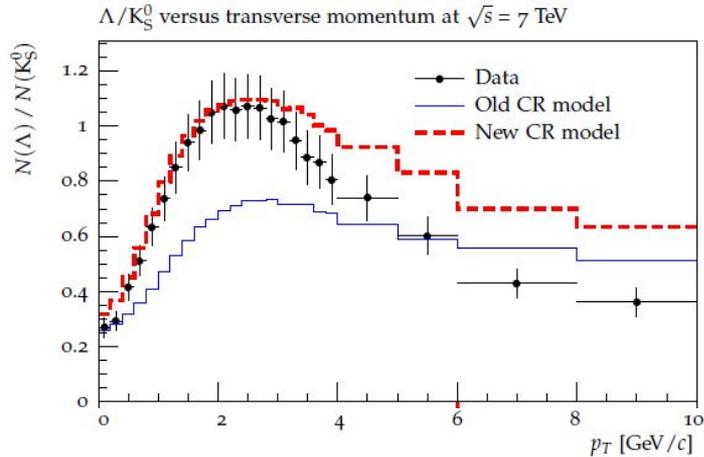


- Measurements of charm production in pion-nucleon collisions
- At **large** x_F : favoured production of hadrons sharing valence quarks with beam hadrons
 - D^- ($[\bar{c}d]$, leading meson shares the d quark with the π^- projectile) favored over D^+ ($c\bar{d}$)
- Break-up of independent fragmentation

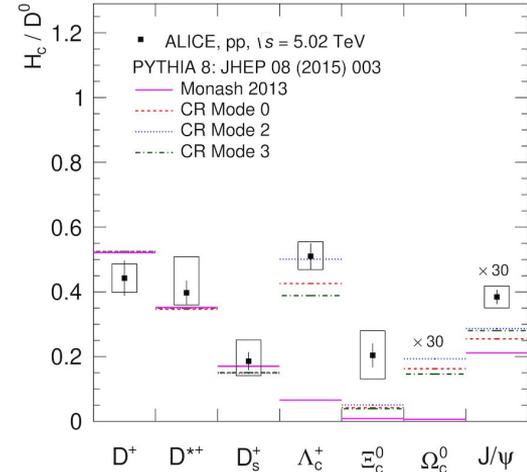
→ A reservoir of particles leads to significant changes in hadronisation

Color reconnection

📖 Christiansen Skands, JHEP 08 (2015) 003



📖 ALICE, arXiv:2105.06335

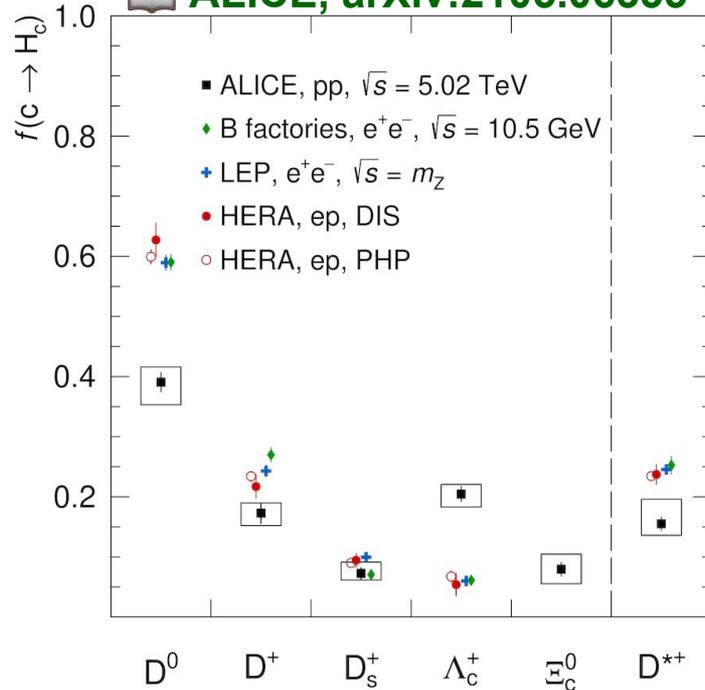


ALICE-PUB-488607

- Baryon/meson ratios underestimated by PYTHIA tuned on e^+e^-
- Better description with Color Reconnection beyond the leading color
 - Suggests that single-particle independent-fragmentation picture is not valid in a hadronic (color-rich) environment

Fragmentation universality?

📖 ALICE, arXiv:2105.06335



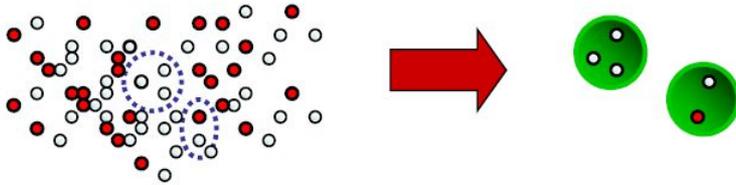
- Evidence of for different fragmentation fractions in pp collisions at LHC and e^+e^- (ep) collisions at lower \sqrt{s}
 - Indication that parton-to-hadron fragmentation depends on the collision system
 - Assumption of their universality not supported by the measured cross sections

ALI-PUB-488617

→ Independent fragmentation picture not valid in color-rich environment
→ Break-down of universality of fragmentation functions

Quark recombination

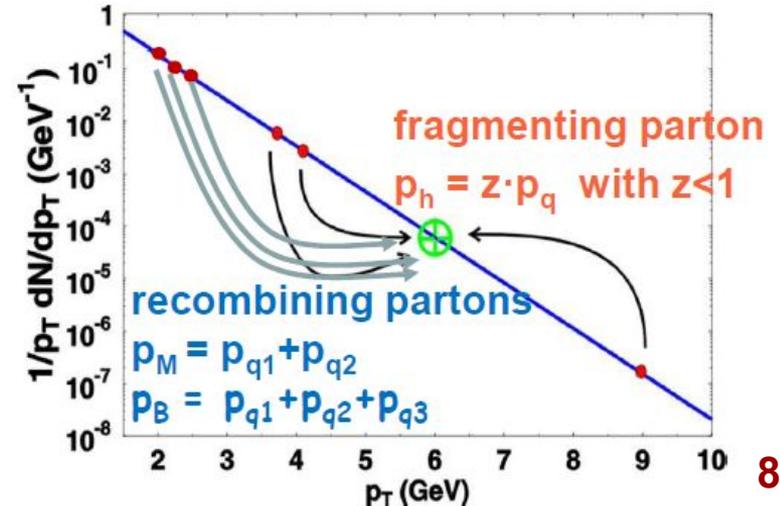
- Phase space at the QGP hadronization is filled with partons
 - Single parton description may not be valid anymore
 - No need to create $q\bar{q}$ pairs via splitting / string breaking
 - Partons that are “close” to each other in phase space (position and momentum) can simply **recombine** into hadrons



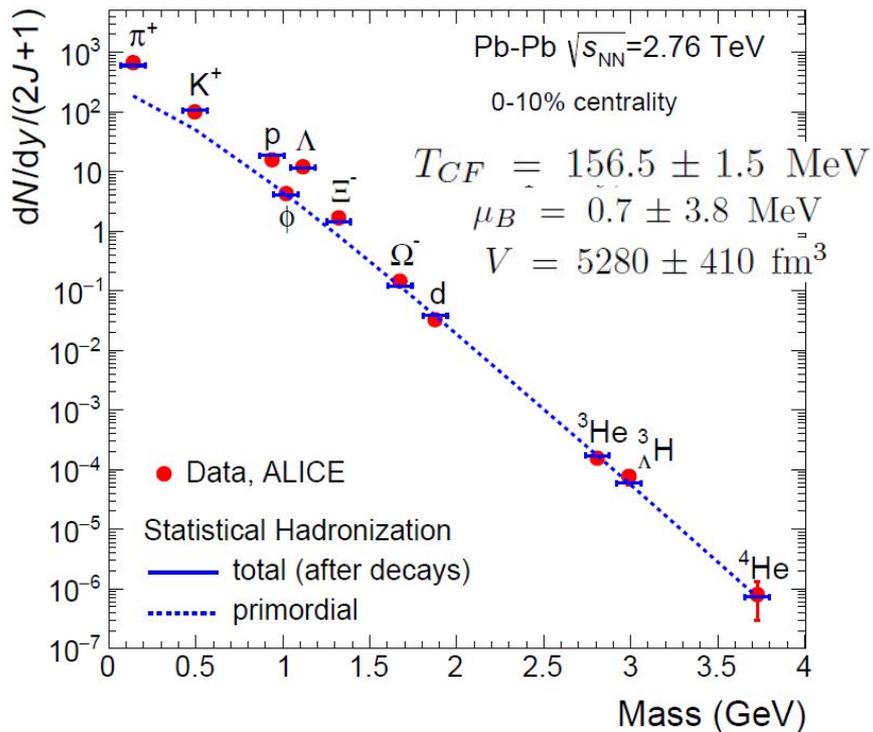
- Recombination vs. fragmentation:
 - Competing mechanisms
 - Recombination naturally enhances baryon/meson ratios at intermediate p_T
 - **Recombination depends on “environment”**, i.e. density and momentum distribution of surrounding (anti)quarks

 Greco et al., PRL 90 (2003) 202302

 Fries et al., PRL 90 (2003) 202303



Statistical hadronisation

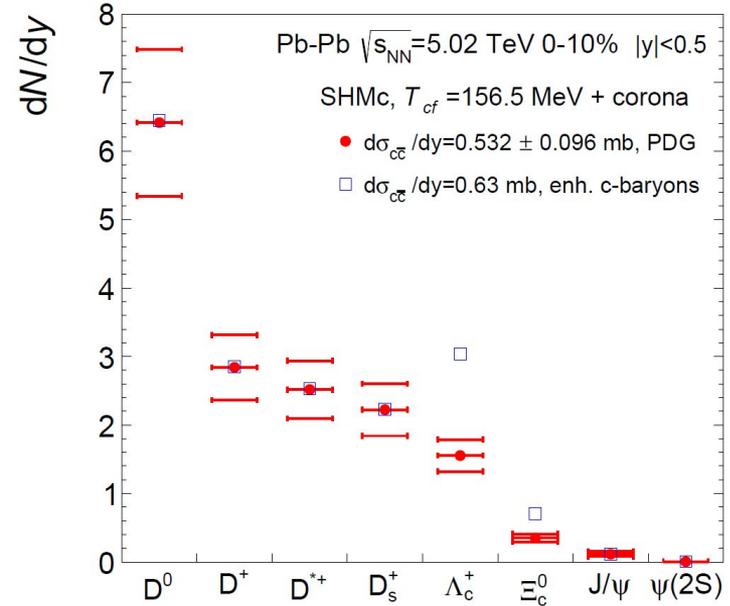


- Abundances of light and strange hadrons (dominated by low- p_T particles) follow the equilibrium populations of a **hadron-resonance gas in chemical and thermal equilibrium** at a freeze-out temperature $T_c \sim 155$ MeV
 - Thermal origin of particle production
 - Macroscopic description of the hadron gas in terms of thermodynamic variables
- Statistical hadronisation models (SHM)
 - Yields depend on hadron masses (and spins), chemical potentials, temperature and volume of the fireball

 **Andronic et al, Nature 561 (2018) 7723, 321**

SHM with charm

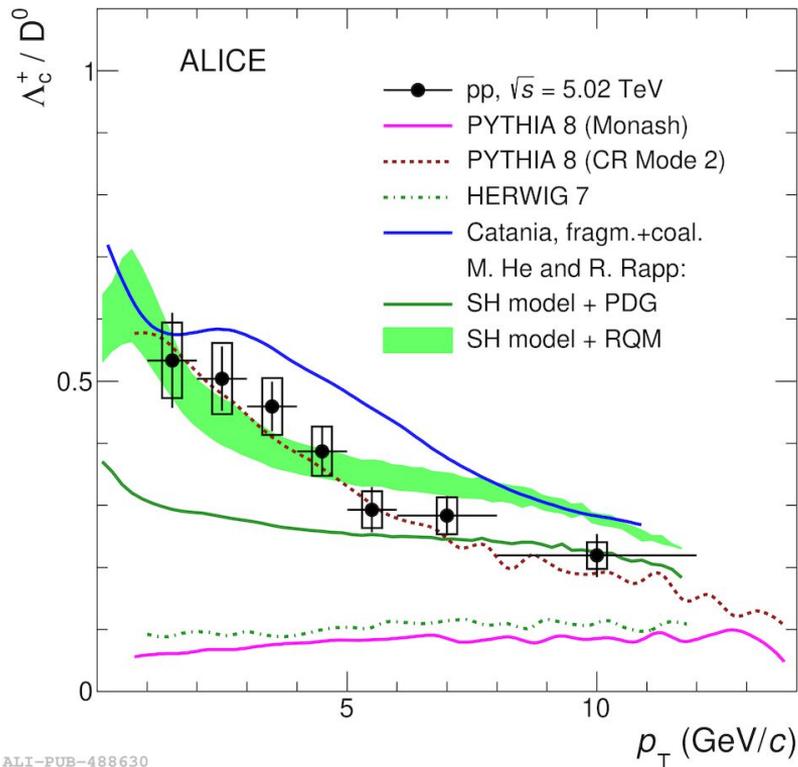
- Charm quarks produced in initial hard scatterings and conserved while traversing the QGP
 - Initial production from pQCD
 - Total yield determined by **charm cross section**, not by the fireball temperature.
 - Accounted for by **charm balance equation** leading to a *fugacity* g_c , which ensures that all initially produced charm quarks are distributed into hadrons at the phase boundary
- Charm quarks **thermalize** in the QGP
- Charm hadrons formed at phase boundary according to thermal weights
 - Relative yields depend on: hadron mass, temperature, and μ_B
- NOTE: significant impact of possible yet-undiscovered excited charm baryon states



📖 **Andronic et al, JHEP 07 (2021) 035**

Baryon/meson ratios in pp: models

📖 ALICE, arXiv:2011.06078



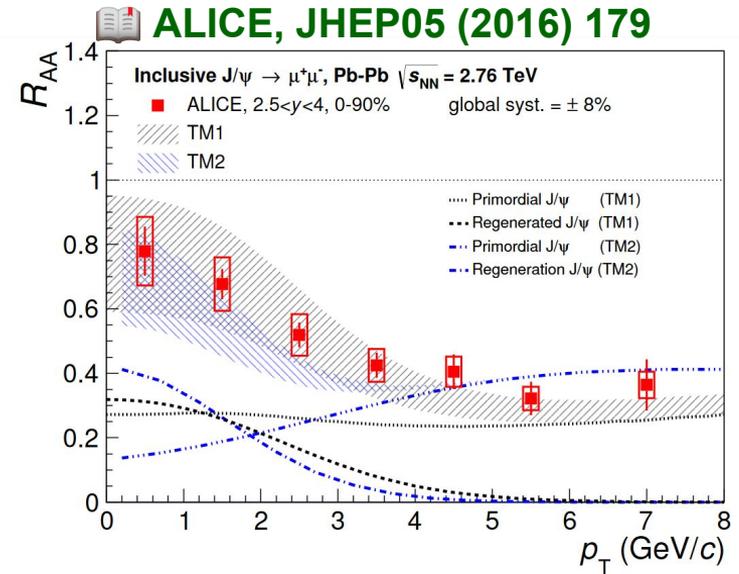
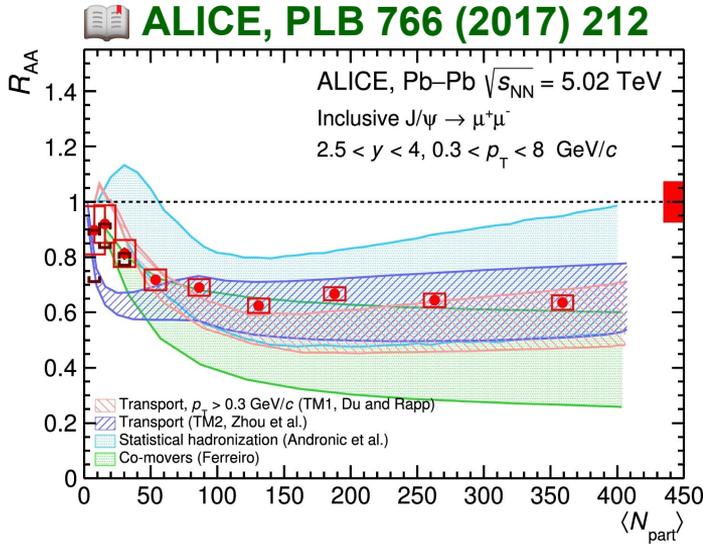
ALI-PUB-488630

- Λ_c^+ / D^0 ratio in pp captured by:
 - PYTHIA (pp paradigm) with CR beyond leading colour
 - i.e. including “interactions” among partons from different MPIs
 - Extensions of models typically used for A-A (QGP paradigm)
 - SHM (with additional baryonic states, important to describe the data)
 - Recombination
- More insight from: Ξ_c / D^0 , Σ_c / D^0 (and Ω_c / D^0) 📖 ALICE, arXiv:2106.08278

Considerations

- **Color reconnection** beyond the leading colour are essentially an “interaction” between partons produced in different hard scatterings (**MPIs**)
 - Analogies with the coalescence mechanism
- Recombination has aspects in common with cluster hadronization model of HERWIG
- **Recombination/coalescence** can be seen as a “dense” limit of hadronization, as opposed to single parton fragmentation
- The coalescence models are essentially a *statistical combination of quarks* at the phase boundary
 - Microscopic realisation of the statistical limit for hadron production? (Recombination mechanism connecting a thermal parton phase with the observed thermal hadron phase)
 **Fries et al., PRC 68 (2003) 044902**
- “Statistical” approach in common between coalescence and SHM but:
 - Degrees of freedom are different: hadrons in SHM vs. quarks in coalescence
 - No assumption of full thermalisation of quarks in coalescence approach
 - Even though light quark spectra in the region where coalescence dominates are commonly taken from a thermal spectrum

Heavy quark hadronisation in Pb-Pb



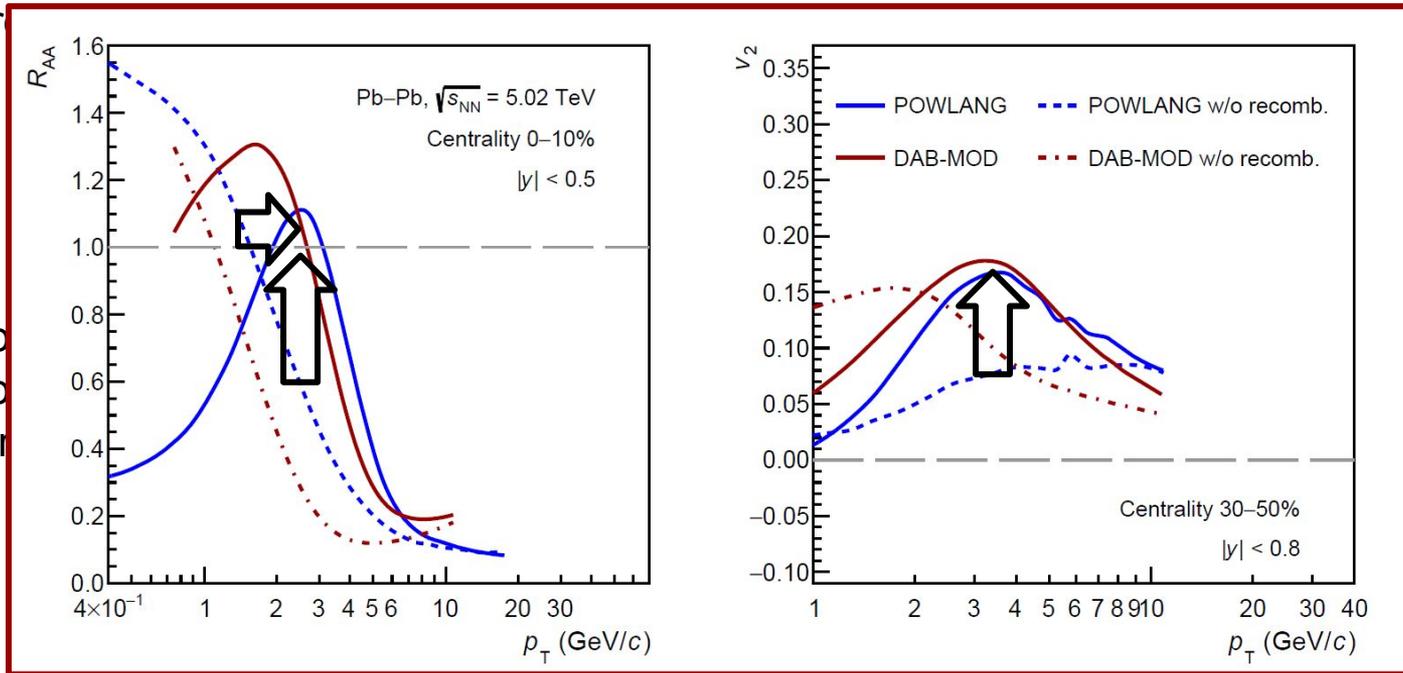
- Evidence from LHC results that charmonia are produced via **(re)combination of $c\bar{c}$ pairs originating from two independent hard scattering processes**
- Data described by:
 - SHM: melting of initially produced $c\bar{c}$ + combination at phase boundary
 - Transport models with in-medium charmonium dissociation + regeneration

Heavy quark hadronisation in Pb-Pb

- Hadronization of heavy quarks via recombination with light quarks from the QGP modifies:
 - **Momentum distributions**
 - HF hadrons pick-up the radial and elliptic flow of the light quark
 - **Hadrochemistry** (i.e. relative abundances of meson and baryon species)
 - Enhanced production of **baryons** relative to mesons
 - Enhanced D_s (B_s) yield relative to non-strange mesons
- Recombination for heavy flavours relevant up to higher p_T than for light flavours
- Recombination for beauty extends up to higher p_T with respect to charm
- Different implementations in different transport models:
 - **Instantaneous coalescence** at the phase boundary based on Wigner function  **Scheibl, Heinz, PRC 59 (1999) 1585**
 - **Resonance recombination** model  **Ravagli, Rapp, PLB655 (2007) 126**
 - **In-medium string formation** between heavy quark and a thermal light quark from the bulk  **Beraudo et al., EPJ C75 (2015) 121**

Heavy quark hadronisation in Pb-Pb

- Hadr
-
-
- Reco
- Reco
- Differ



modifies:

1999) 1585

2007) 126

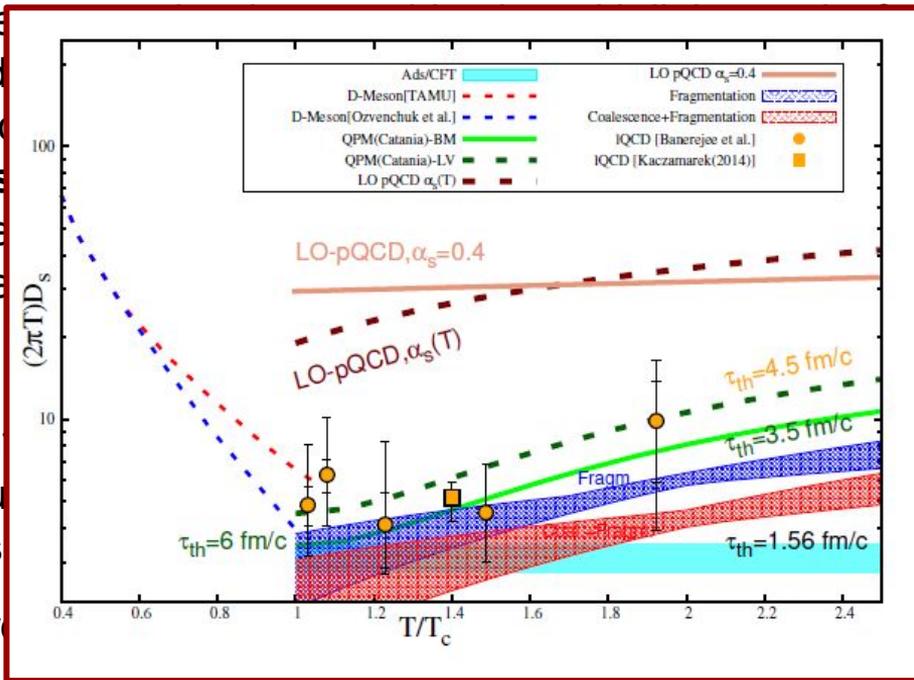
→ Crucial to have hadronisation under control to estimate QGP transport coefficients from HF data-to-model comparison

121

15

Heavy quark hadronisation in Pb-Pb

- Hadronization of heavy quarks
 - Momentum dependent
 - HF hadronisation
 - Hadrochemistry
 - Enhancement
 - Enhancement
- Recombination for heavy quarks
- Recombination for heavy quarks
- Different implementations
 - Instantaneous hadronisation
 - boundary based
 - Resonance recombination
 - In-medium string formation between heavy quarks



from the QGP modifies:

quark
species)

heavy flavours

see talk by S. Bass

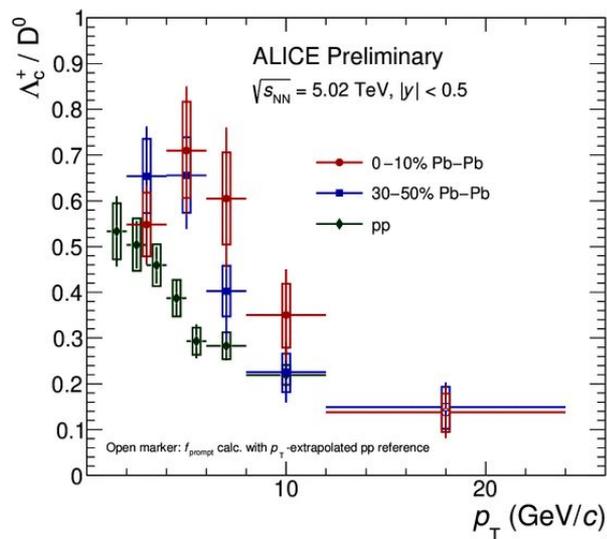
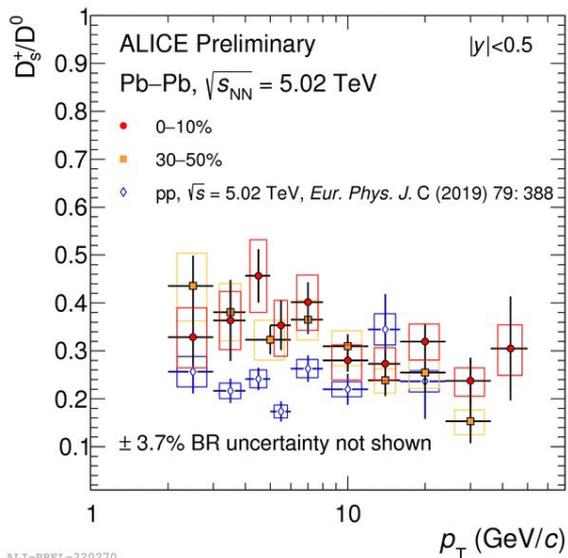
Phys. Rev. C, PRC 59 (1999) 1585

Phys. Lett. B, PLB655 (2007) 126

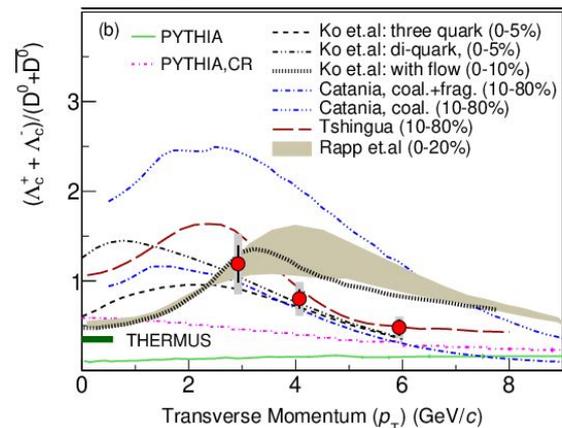
→ Crucial to have hadronisation under control to estimate QGP transport coefficients from HF data-to-model comparison

Charm hadrochemistry

- Baryon/meson and D_s/D ratios in Pb-Pb collisions from LHC Run-2 (and RHIC) hint at an enhancement at low/mid p_T , **consistent with the recombination picture**
- Precise measurements of charmed hadrons in Run-3 and Run-4 crucial to:
 - Assess the role of recombination
 - Improve phenomenological extraction of QGP transport properties (e.g. spatial diffusion coefficient D_s)



STAR, PRL 124 (2020) 172301

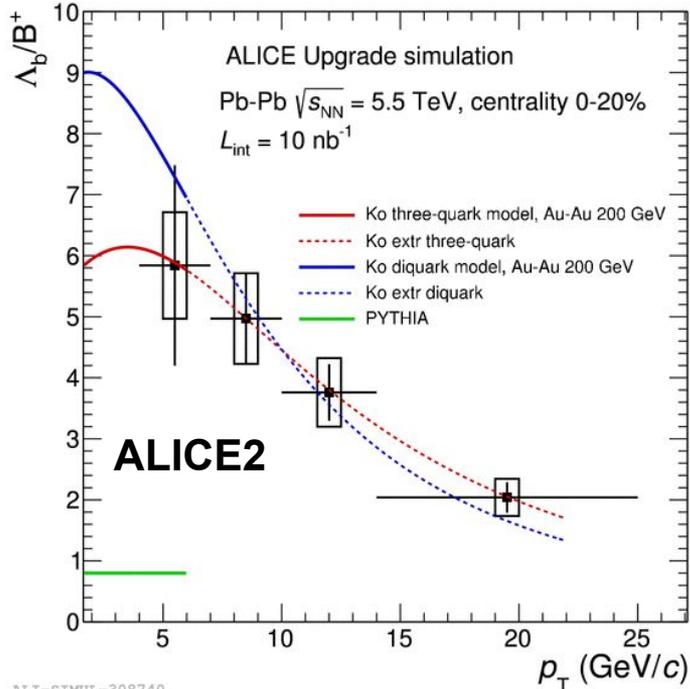


Beauty hadronisation in Pb-Pb

- More sensitive extraction of the spatial diffusion coefficient D_s via **data-to-model comparison** of **beauty** hadrons as compared to charm
 - Better controlled theoretical calculation of the transport coefficient
 - More robust modelling of their transport (Boltzmann/Langevin) in the QGP
 - Larger mass ($\sim 3x$ charm quark mass) \rightarrow longer relaxation time ($> \tau_{\text{QGP}}$)
 - Preserve stronger memory of the thermalisation process providing enhanced sensitivity on their coupling strength
- Need to have under control b quark hadronisation
 - Crucial to measure beauty-hadrons down to low p_T ($< 5-10$ GeV/c)
- Combined measurement of **beauty-hadron** R_{AA} and v_n and the relative abundances of different beauty-hadron species (in particular **baryon-to-meson** ratios) down to low p_T crucial to simultaneously constrain the **heavy-quark diffusion coefficient** and the **hadronisation mechanism** in the beauty sector

Beauty hadronisation in Pb-Pb

- ALICE3 in Run-5: ideal setup for full reconstruction of beauty baryons from their hadronic decays
 - Low production rate, very small branching ratios, and several particles in the final state



- For instance: reconstruction of $\Lambda_b^0 \rightarrow \Lambda_c^+ \pi^-$ (BR = $4.9 \cdot 10^{-3}$)
 - Will be affected by large uncertainties and limited to $p_T > 4-5$ GeV/c in Run3 and Run4
 - With ALICE3 it will greatly benefit from the large improvement in $\Lambda_c^+ \rightarrow pK\pi$ purity

see talk by G.M. Innocenti

Multi-charm hadron yields

- Crucial new insight by measuring **baryons** containing **multiple charm quarks**
(Ξ_{cc}^+ , Ξ_{cc}^{++} , Ω_{cc}^+ , Ω_{ccc}^{++} , and T_{cc}^+)
 - Production in single-parton scattering strongly disfavoured as compared to single-charm Λ_c^+ baryons
 - Yields of multicharm/single-charm hadrons predicted to be largely enhanced in A-A compared to pp collisions in SHM and coalescence models

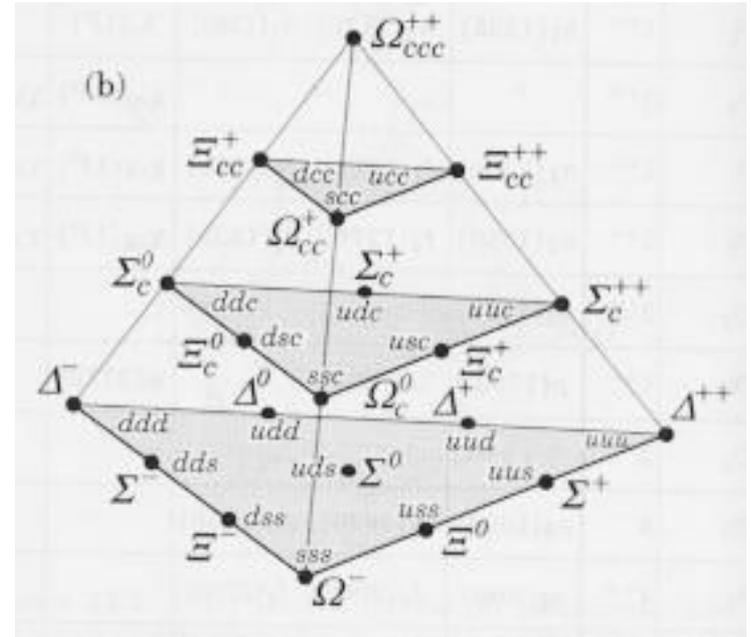
📖 [Becattini, PRL 95 \(2005\) 022301](#)

📖 [He et al., PLB 746 \(2015\) 59](#)

📖 [Yao, Muller, PRD 97 \(2018\) 074003](#)

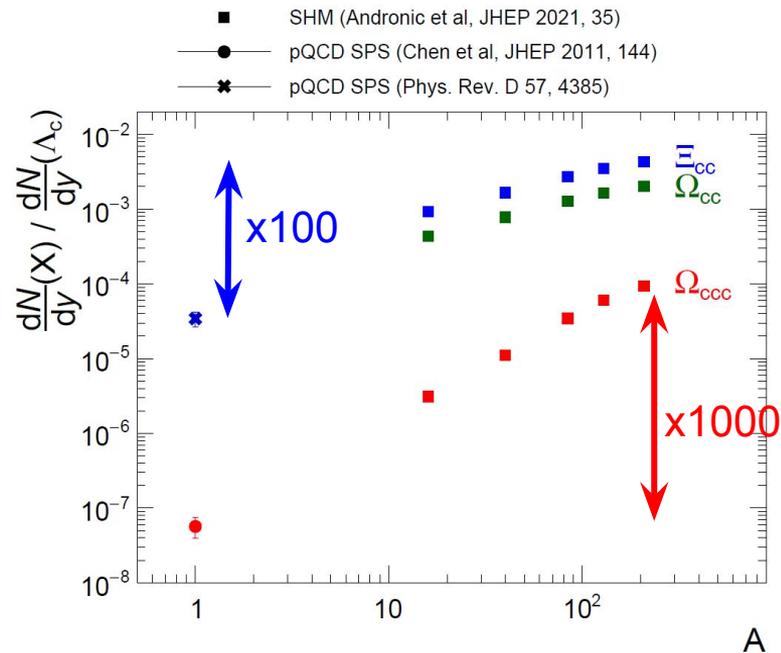
📖 [Cho, Lee, PRC 101 \(2020\) 024902](#)

📖 [Andronic et al, JHEP 07 \(2021\) 035](#)



Multi-charm baryon yields

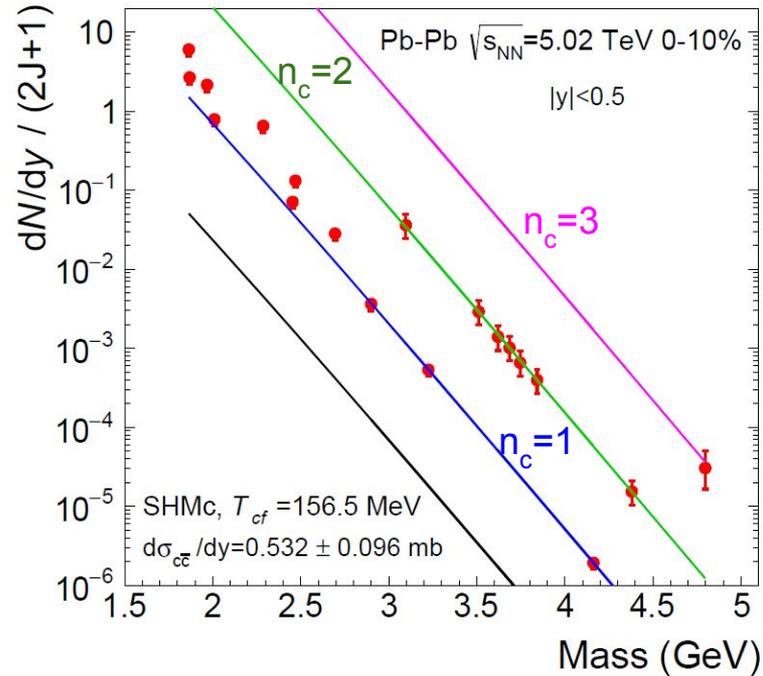
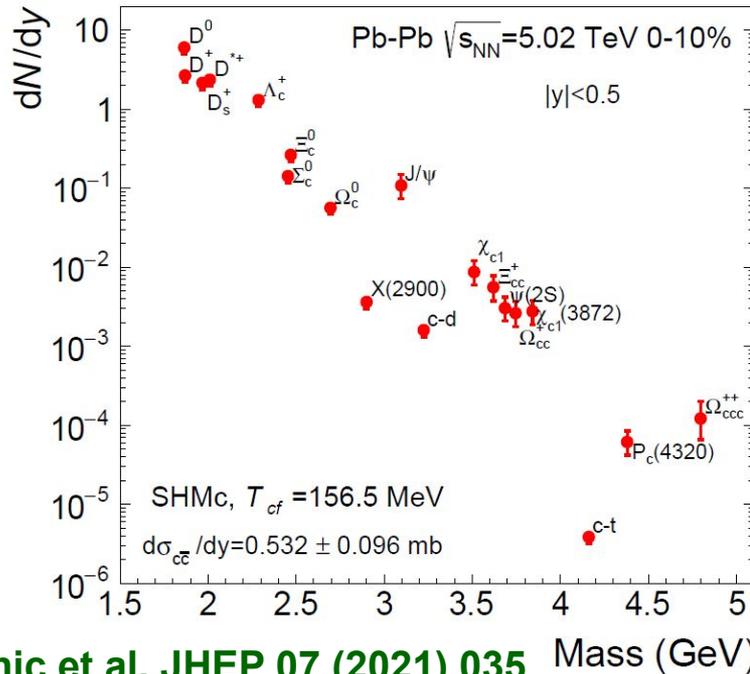
- Crucial new insight by measuring **baryons** containing **multiple charm quarks** (Ξ_{cc}^+ , Ξ_{cc}^{++} , Ω_{cc}^+ , Ω_{ccc}^{++} , and T_{cc}^+)
 - Production in single-parton scattering strongly disfavoured as compared to single-charm Λ_c^+ baryons
 - Yields of multicharm/single-charm hadrons predicted to be largely enhanced in A-A compared to pp collisions in SHM and coalescence models
 - Factor of about 100 for Ξ_{cc} and up to about 1000 for the yet undiscovered Ω_{ccc}
- **Direct window on hadron formation from QGP**



more details in talk by D. Chinellato

Multi-charm baryons in SHMc

- Emergence of unique pattern, due to g_c^n and mass hierarchy
- Unique testing ground for **charm deconfinement and thermalisation**
 - Enhanced sensitivity to deviations from full equilibrium due to g_c^n dependence



Multi-charm in recombination models

- Models including hadronisation via quark coalescence predict large yields of multi-charm baryons in A-A collisions at LHC energies
 - Large abundance of charm quarks -> finite probability that two or three charm quarks from different hard scatterings coalesce into a multi-charm baryon
- In general, in the recombination approach hadron yields depend on:
 - Quark phase-space density (from transport / hydro)
 - Characteristics of hadron (radius and binding energy) usually encoded in Wigner function

$$\frac{dN_{\Xi_{cc}}}{dp_T} \propto \int f_l(x_l, p_l) f_c(x_c, p_c) f_c(x_c, p_c) W_{\Xi_{cc}}(x_1, x_2, x_3, p_1, p_2, p_3)$$

- Different approaches for multi charm hadrons in different models:
 - *Instantaneous* or “*sequential*” quark coalescence at hadronisation assuming either that charm quarks are *fully* or *partially* kinetically equilibrated in the QGP
 - 📖 He et al., PLB 746 (2015) 59
 - 📖 Zhao et al, PLB 771 (2017) 349
 - 📖 Cho, Lee, PRC 101 (2020) 024902
 - *In-medium dynamical evolution* in which bound *heavy diquarks* and formed and dissociated in the QGP
 - 📖 Yao, Muller, PRD 97 (2018) 074003

Conclusions

- Measurements of the production of several **heavy-flavour hadron species** can provide crucial progress in the understanding of the *QGP transport properties* and the *QGP hadronisation*
 - Characterize the common microscopic dynamics underlying the interactions of heavy quarks with the QGP and their hadronisation
- **Beauty**: precise measurements of hadrochemistry, p_T spectra and v_n for different meson and baryon species down to low p_T
 - Precise determination of the QGP diffusion coefficient
- **Baryons with multiple charm quarks**
 - Direct window on hadron formation from the QGP
 - Enhanced sensitivity to the degree of equilibration of charm quarks in the medium
- ALICE3 has **unique capabilities** to perform precise measurements of these probes in LHC Run-5 and beyond