



FUTURE
CIRCULAR
COLLIDER

Bunch length measurement studies using Cherenkov Diffraction radiation

gratefully acknowledging:

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FCC-ee bunch length diagnostics

Synchrotron radiation (SR) in LEP

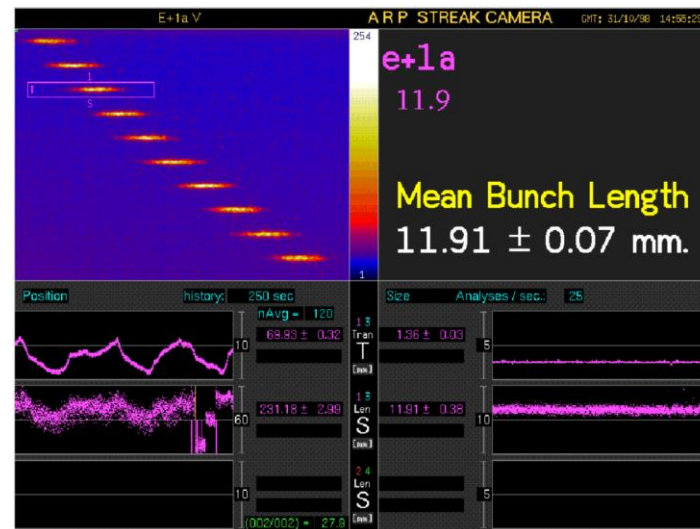
Bunch length measurements using SR
on streak camera

SR in FCC-ee:

Distance of $\sim 100\text{m}$ necessary to separate the photon beam from the electron or positron beam¹ and X-rays dominating the spectrum

Cherenkov Diffraction Radiation (ChDR) at FCC-ee

- Non-invasive
- Simple geometries with small space requirements
- Photon emission at large and well-defined angle



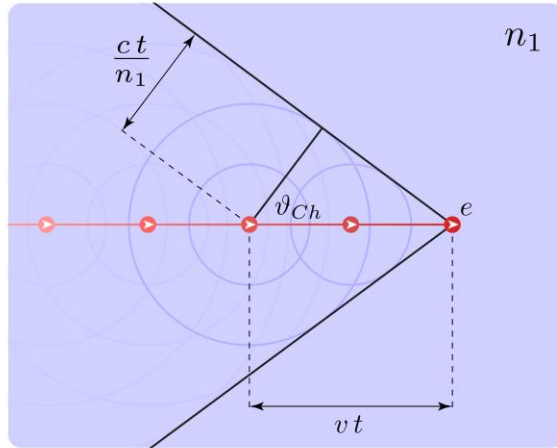
Bunch length measurement in LEP ²

¹ Abada, A., Abbrescia, M., AbdusSalam, S.S. et al. FCC-ee: The Lepton Collider. Eur. Phys. J. Spec. Top. 228, 261–623 (2019). <https://doi.org/10.1140/epjst/e2019-900045-4>

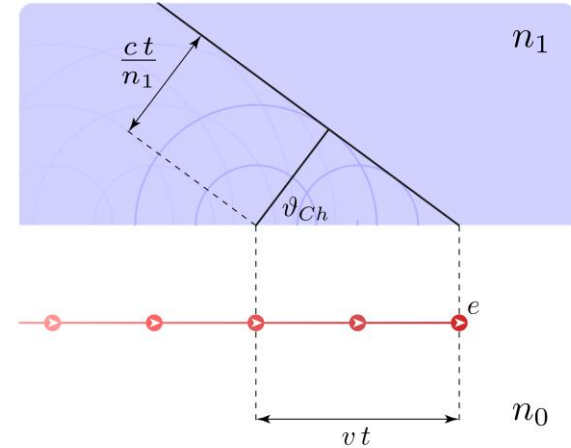
² A. J. Burns, H. Schmickler, Bunch length measurements in LEP. Proceedings DIPAC (1999) <https://cds.cern.ch/record/398768>

Cherenkov (Diffraction) Radiation

Cherenkov Radiation



Cherenkov Diffraction Radiation (ChDR)



Frank-Tamm

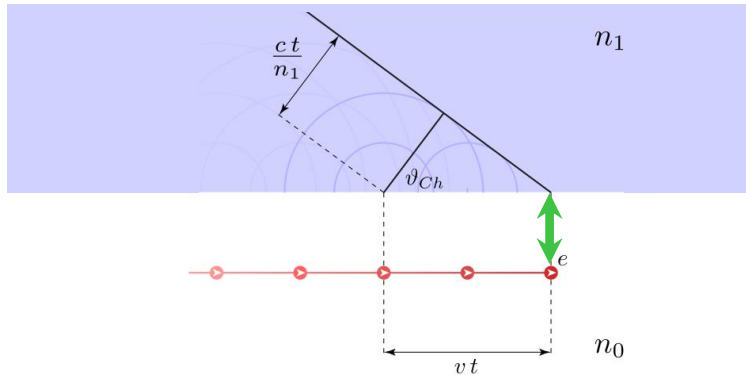
$$\frac{dW}{dl} = \frac{q^2}{4\pi} \mu_0 \int_0^\infty \omega \cdot \left(1 - \frac{1}{\beta^2 n^2(\omega)}\right) d\omega$$

Two analytical models



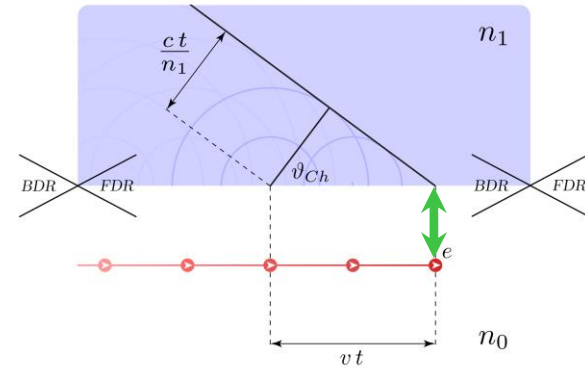
Analytical Models

Stationary Model (1,2)



Electrons moving parallel to the boundary of **infinite** length radiators

Non-Stationary Model (3,4)



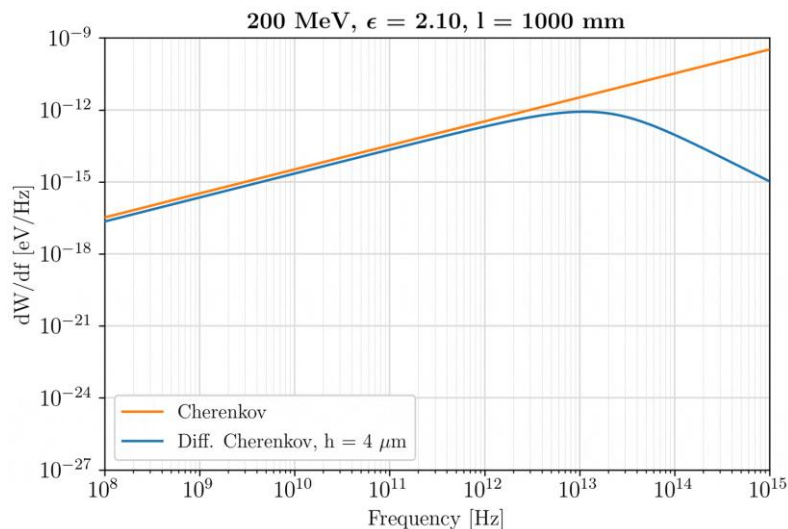
Electrons moving parallel to the boundary of **finite** length radiator

h ... Impact Parameter

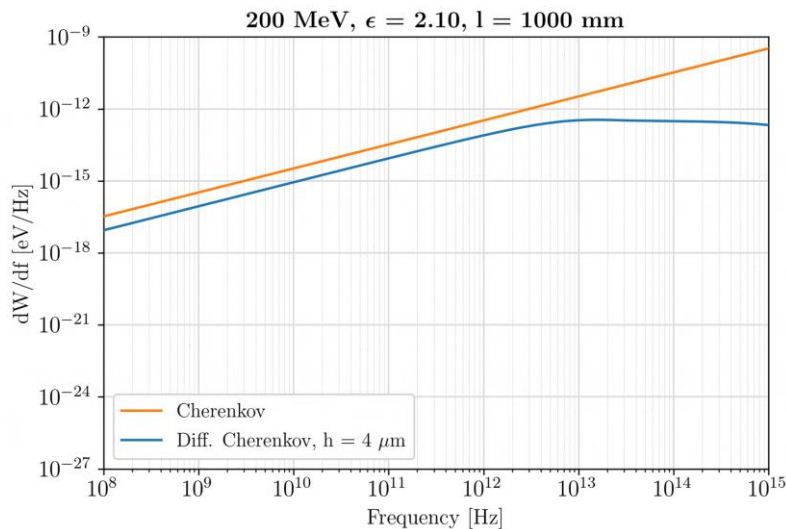
E ... Particle Energy

Impact parameter h

Stationary Model



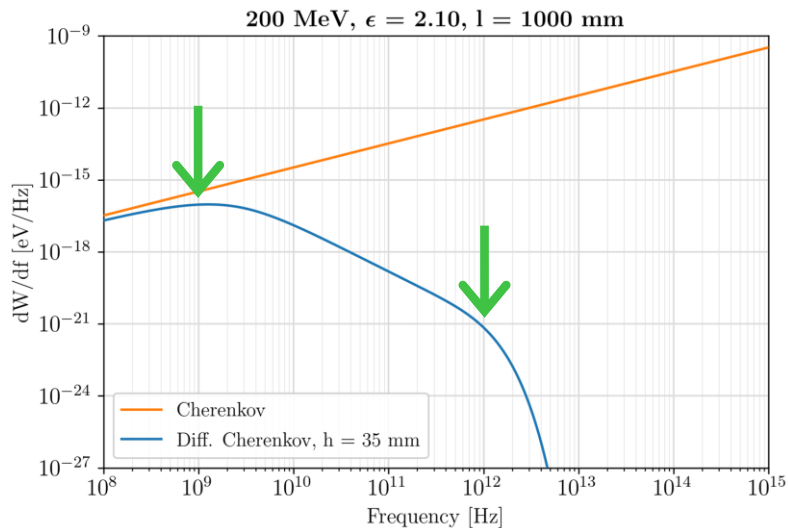
Non-Stationary Model



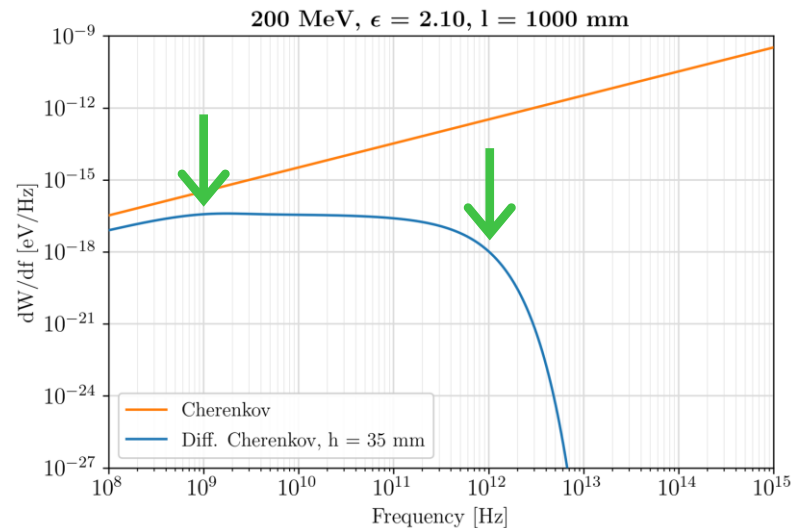
Fixed particle energy, only distance between particle and radiator is increased

Impact parameter h

Stationary Model



Non-Stationary Model

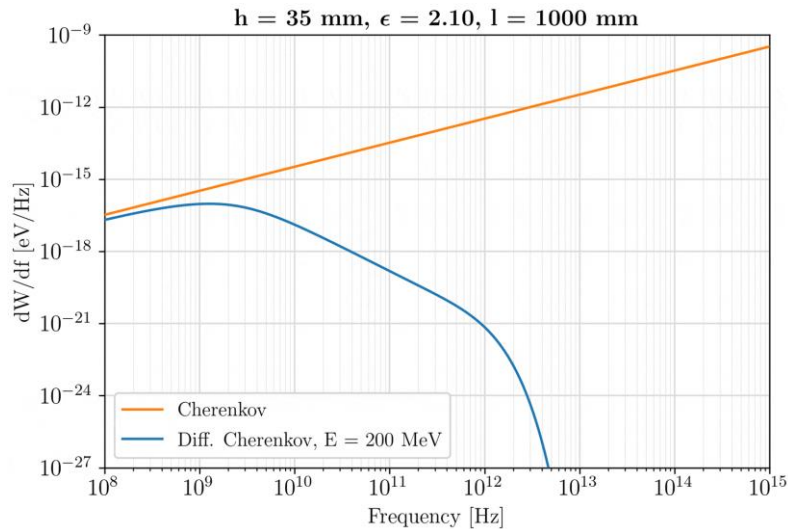


$$\propto 1/h$$

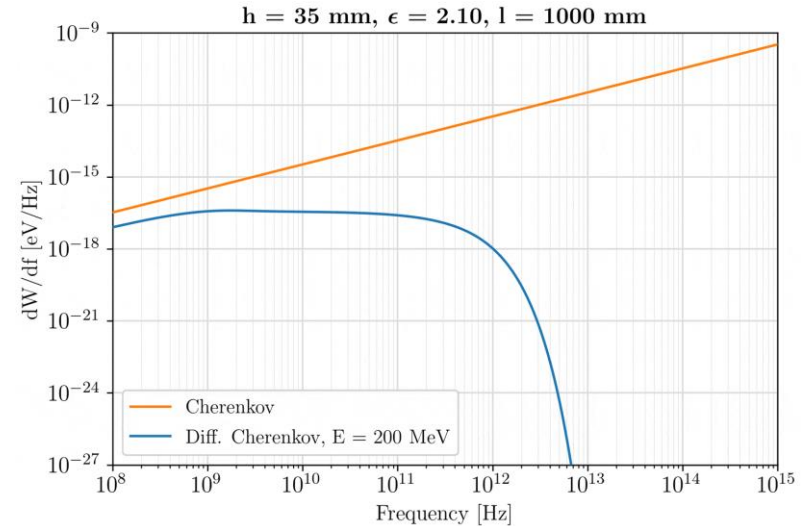
turning points show the same behavior in both models

Energy E

Stationary Model



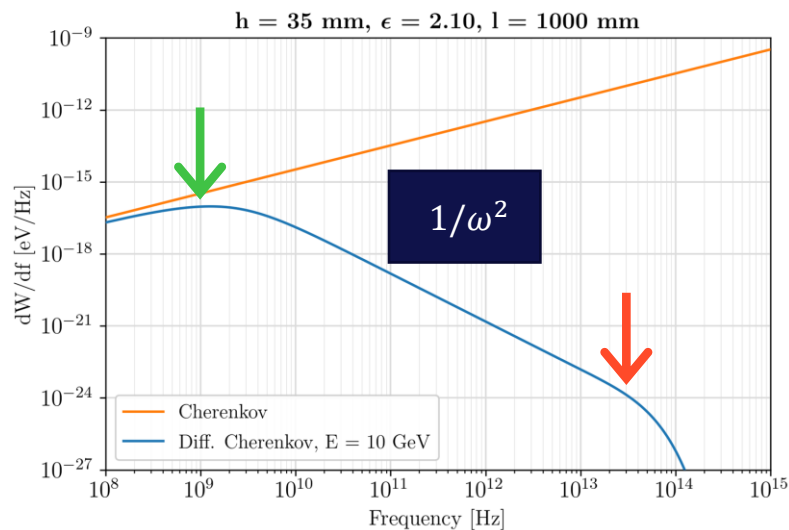
Non-Stationary Model



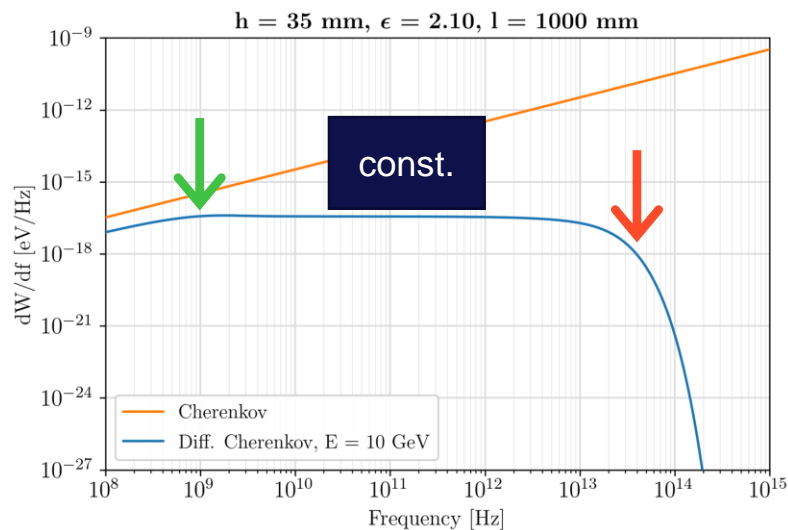
Fixed distance, only particle energy is increased

Energy E

Stationary Model



Non-Stationary Model



$$\propto 1/h$$

$$\propto \gamma/h$$

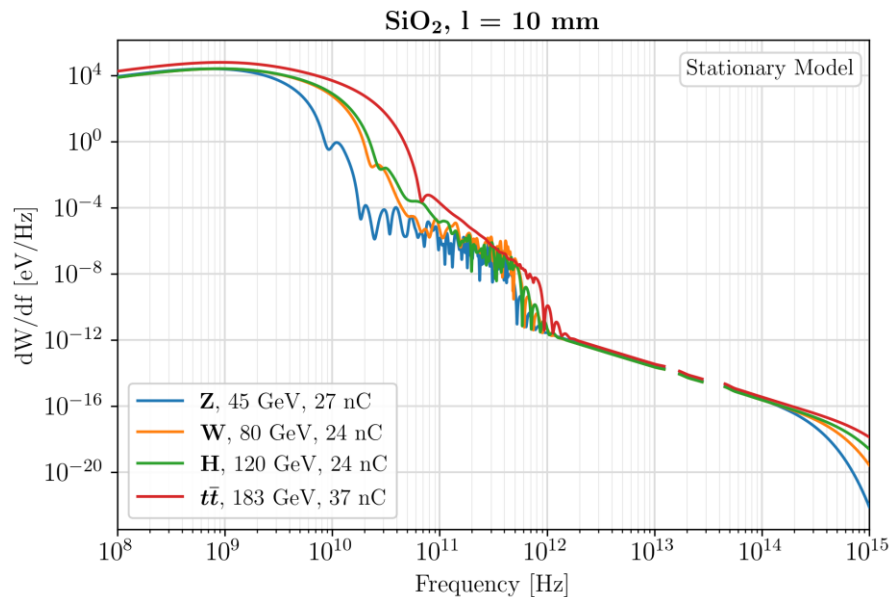
turning points show the same behavior in both models

Coherent and Incoherent ChDR



$$\lambda > \sigma_{\text{bunch}}$$

$$\propto N^2$$



$$\lambda \ll \sigma_{\text{bunch}}$$

$$\propto N$$

$$\frac{dW}{d\omega} = \left(\frac{dW}{d\omega} \right)_1 \cdot \left(N + N(N-1) \cdot |F(\vec{k})|^2 \right)$$

with $F(\vec{k}) = \int S(\vec{r}) \cdot e^{-i\vec{k}\vec{r}} d\vec{r}$

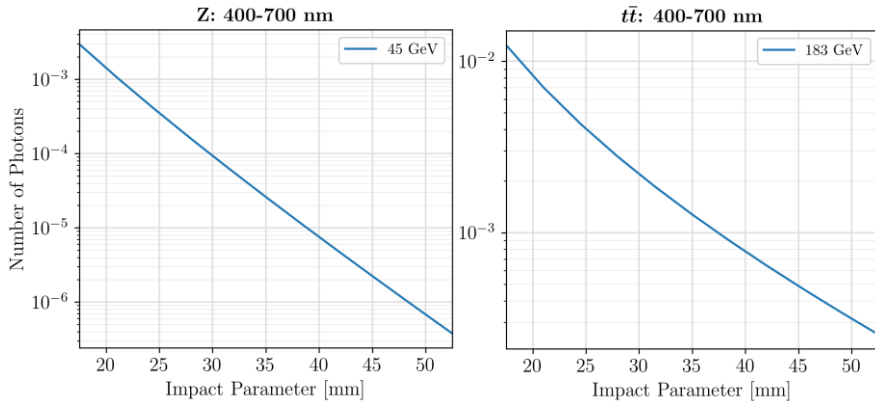
$F(\vec{k})$... bunch form factor

$S(\vec{r})$... particle density distribution

$\left(\frac{dW}{d\omega} \right)_1$... energy spectrum of one particle

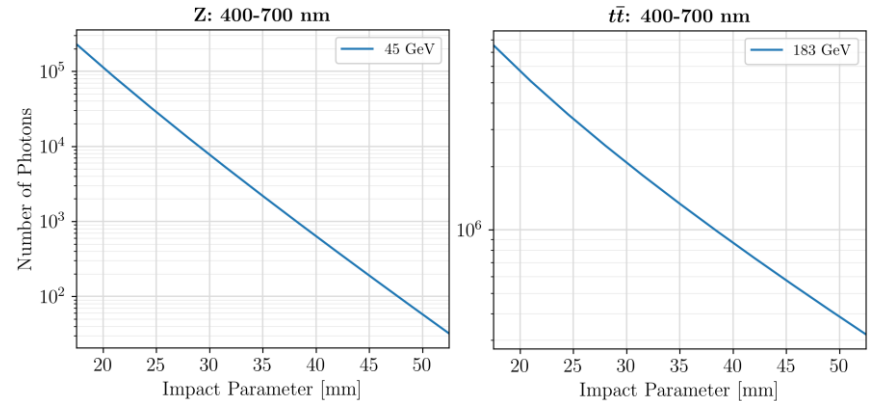
Incoherent ChDR

Stationary Model



$\approx 10^{-5}$ - 10^{-3} photons per bunch
 at nominal distance

Non-Stationary Model

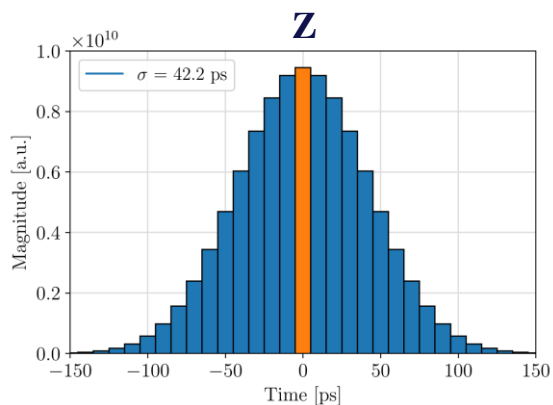


$\approx 10^3$ - 10^6 photons per bunch
 at nominal distance

Ways to increase \rightarrow moving closer + integrating

Incoherent ChDR for Longitudinal profile measurement

Stationary Model



Integrated no. of photons for 100 fs time frame

Impact parameter		15 mm	5 mm	Photons/bunch @ 5 mm
Z	Max. photons/(bunch · minute)	1.47	78.4	0.45
W	Max. photons/(bunch · minute)	4.52	155	0.42
H	Max. photons/(bunch · minute)	5.94	179	0.43
t\bar{t}	Max. photons/(bunch · minute)	20.5	583	0.67

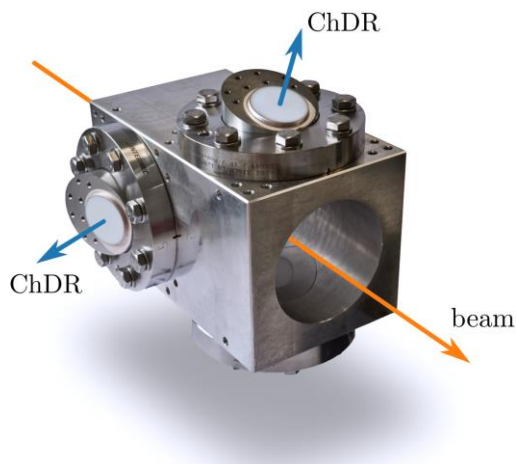
→ Need for ultra-high energy particles to test analytical models

Currently investigating possible tests in SPS North Area

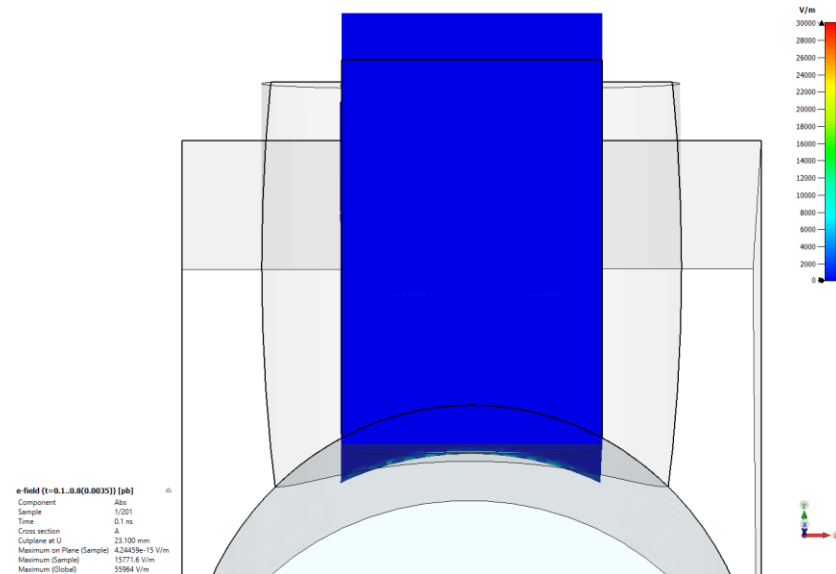
- 40-300 GeV electrons
- up to 10^7 particles per spill

Coherent ChDR

ChDR radiators to be tested at CLEAR



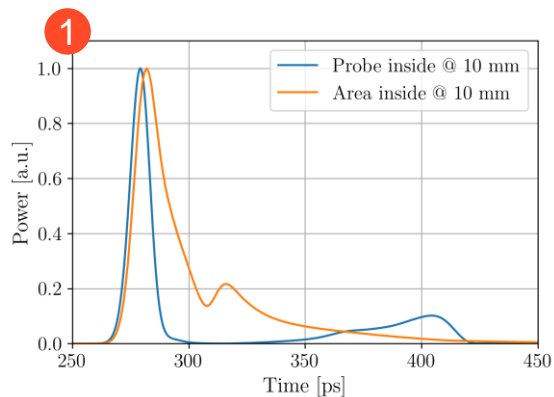
E-field, transverse plane (xy-plane tilted)



- 36 mm diameter Alumina rods
- brazed to DN 60 flange, vacuum tight
- curvature for \varnothing 80 mm beam pipe

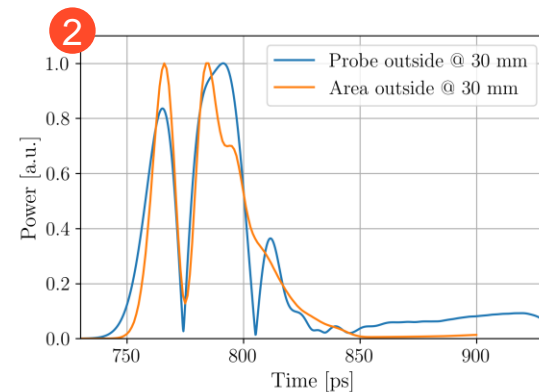
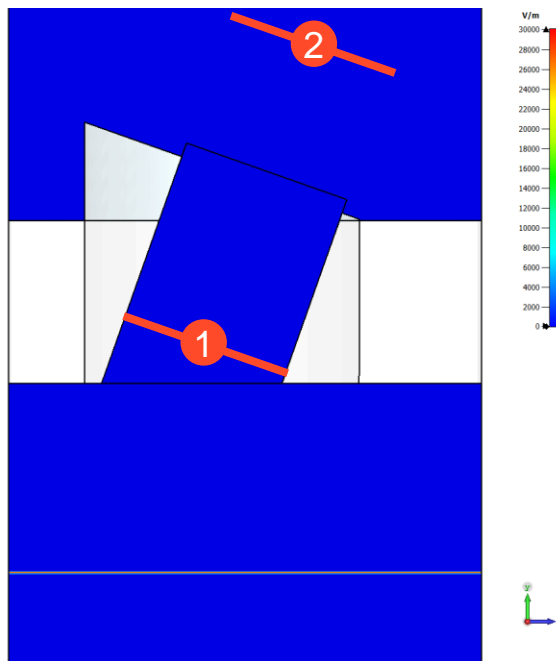
Coherent ChDR

Numerical studies with CST



```
e-field (t=time_start_end(time_step);x=0) [pE]
Component      Abs
Sample         1/165
Time           0 ns
Maximum (Sample) 0 V/m
Maximum (Global) 1.0366e+07 V/m
```

E-field, Median plane (yz-plane)

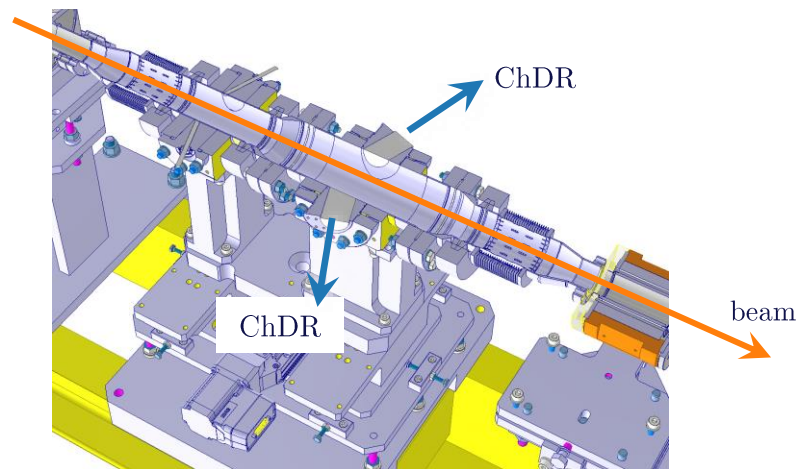


Electron bunch
5 ps Gaussian, 300 pC, 200 MeV

Upcoming experiment

Coherent ChDR experiments at CLEAR

- Coherent ChDR can be tested at low energies
 - CLEAR facility at CERN typically provides 1-5 ps electron bunches with energies up to 220 MeV
 - measure transfer function and benchmark simulations in the low frequency part of the spectrum
- Vacuum chamber with ChDR inlets to be expected during June
 - foreseen installation during summer shut down of CLEAR
- Electro-optical probing
 - Transverse and longitudinal electric field modulus and polarization



Beam line integration at CLEAR



EO-probe by Kapteos (www.kapteos.com)

Summary

ChDR possible candidate for bunch length diagnostics at FCC

Incoherent ChDR

- ultra-high energy particles needed for validation of incoherent ChDR
- investigating possible testing at SPS North Area

Coherent ChDR

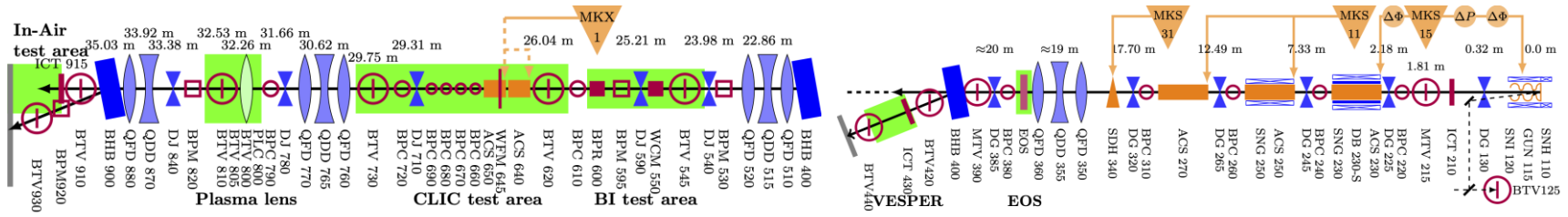
- CLEAR provides suitable parameters to test with short bunches at low energies
- all vacuum components ready for installation in the coming weeks
- experiments scheduled after summer

→ Experimental validation/benchmarking of different models necessary



Thank you
for your attention.

CLEAR



Beam parameter (end of linac)	Value range
Energy	60 - 220 MeV
Bunch charge	0.01 - 0.5 nC
Normalized emittances	3 μm for 0.05 nC per bunch 20 μm for 0.4 nC per bunch (in both planes)
Bunch length	$\sim 100 \mu\text{m}$ - 1.2 mm
Relative energy spread	$< 0.2 \%$ rms ($< 1 \text{ MeV}$ FWHM)
Repetition rate	1 - 5 Hz (25 Hz with upgrade)
Number of micro-bunches in train	1 and more than 100
Micro-bunch spacing	1.5 GHz

