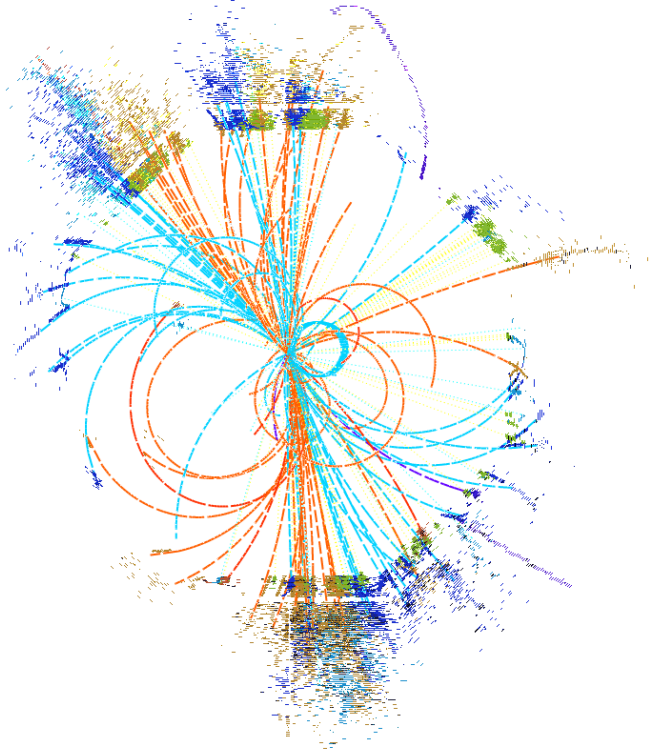


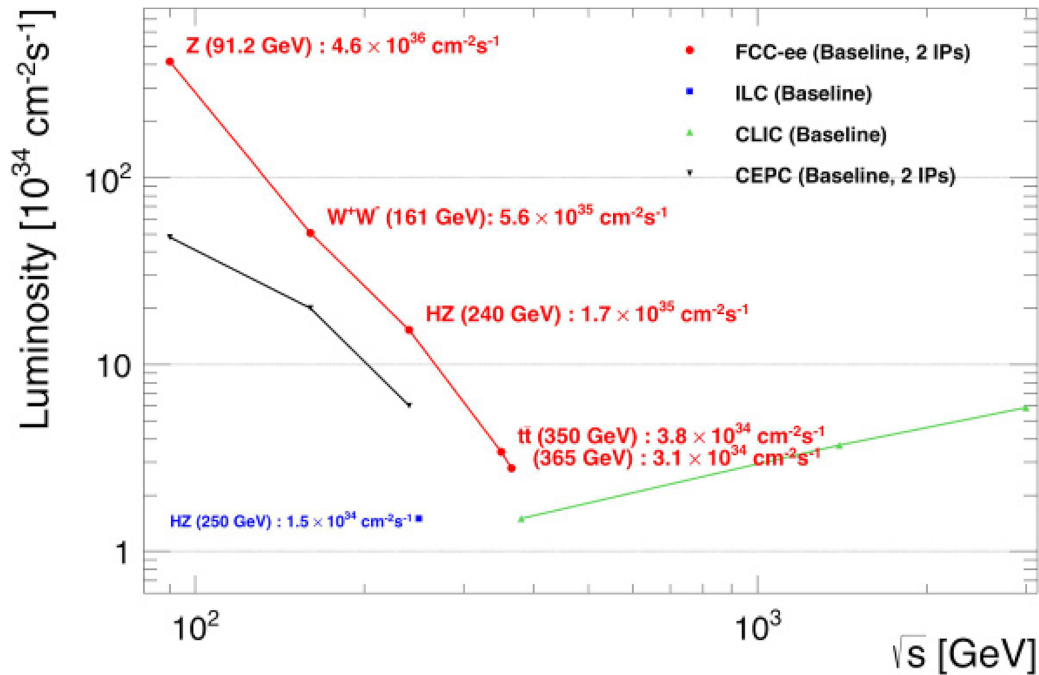
Top physics opportunities at FCC-ee

Philipp Roloff (CERN)
31/05/2022



FCC week 2022
Campus des Cordeliers -
Sorbonne Université

Introduction: FCC-ee energy stages



Relevant for top-quark physics:

240 GeV (“HZ”):

- **FCNC** using $e^+e^- \rightarrow tq$

350 GeV (“ $t\bar{t}$ ”):

- **Threshold scan** for top-quark mass, width, Yukawa coupling, ...

365 GeV:

- O(1 million) top-quark pairs
- **Electroweak couplings**
- **FCNC** using $e^+e^- \rightarrow tq$ and decays in $e^+e^- \rightarrow t\bar{t}$
- Mass from radiative events?



This project is supported from the European Union's Horizon 2020 research and innovation programme under grant agreement No 951754.

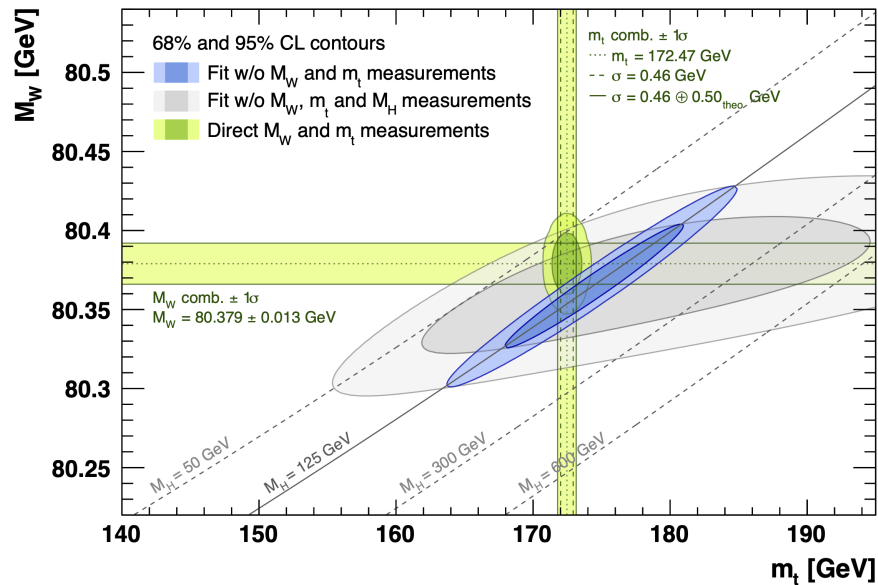
→ **Large amount of complementarity**

Outline

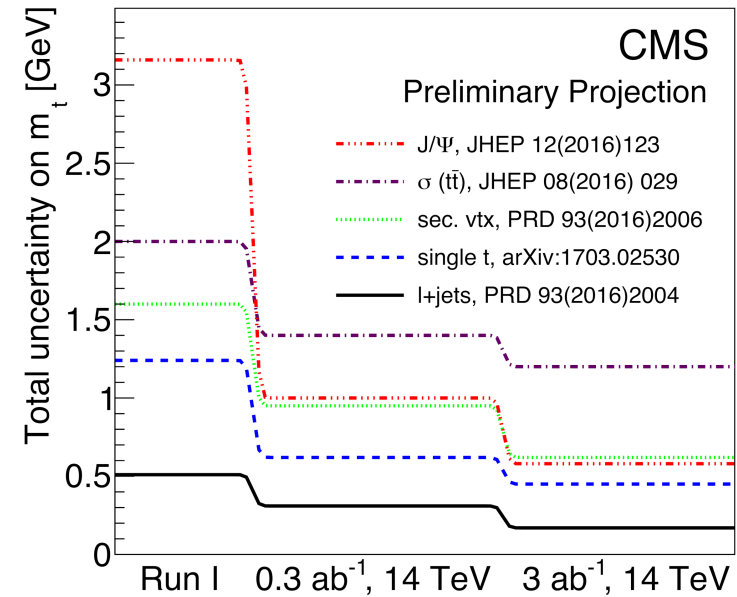
Top-quark at FCC-ee:

- **Mass measurements**
- Electroweak couplings
- Top-quark FCNC
- Common reconstruction issues
- EFT interpretations

Top-quark mass



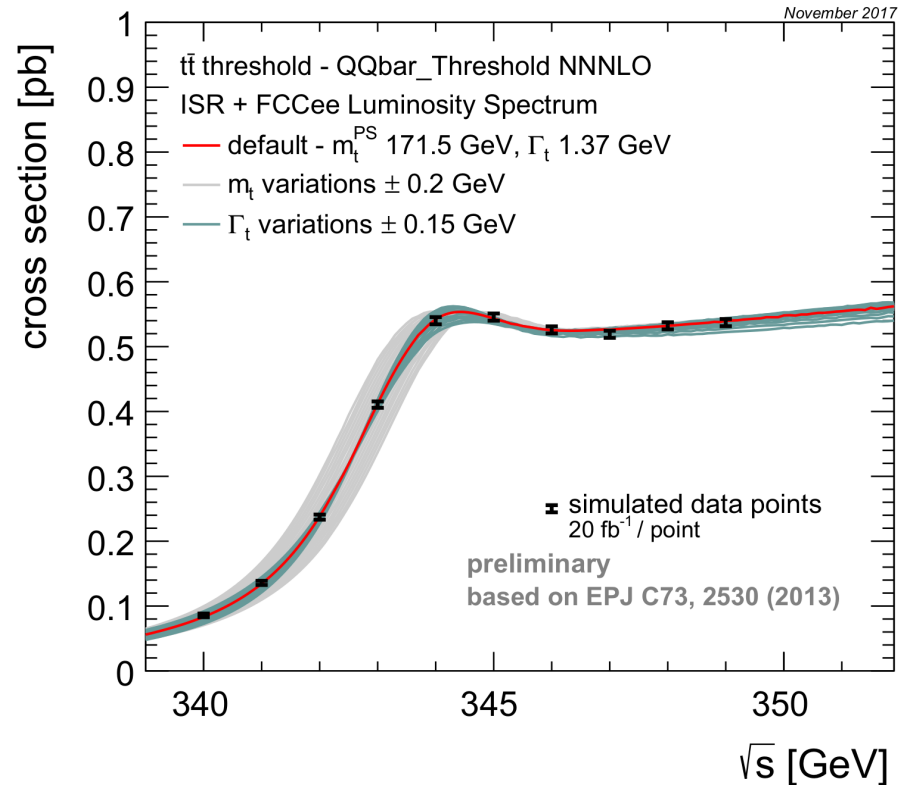
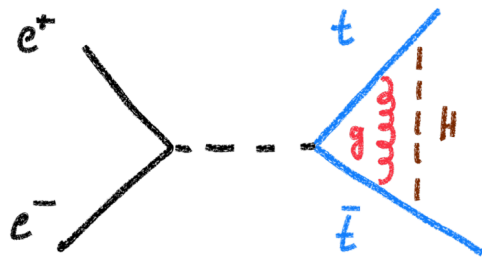
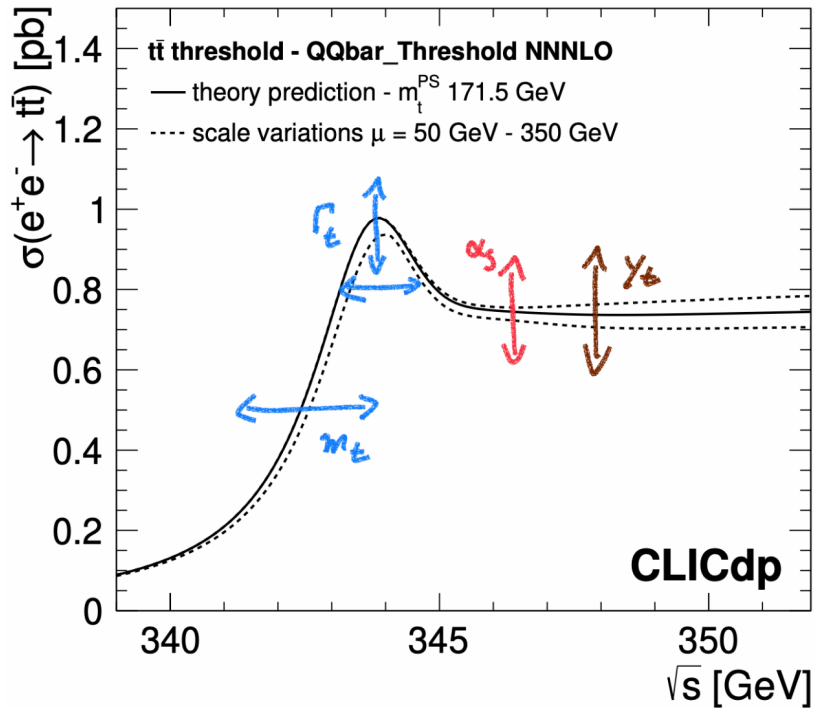
Direct and indirect constraints on top (and W) mass



Complementary methods at e^+e^- collider:

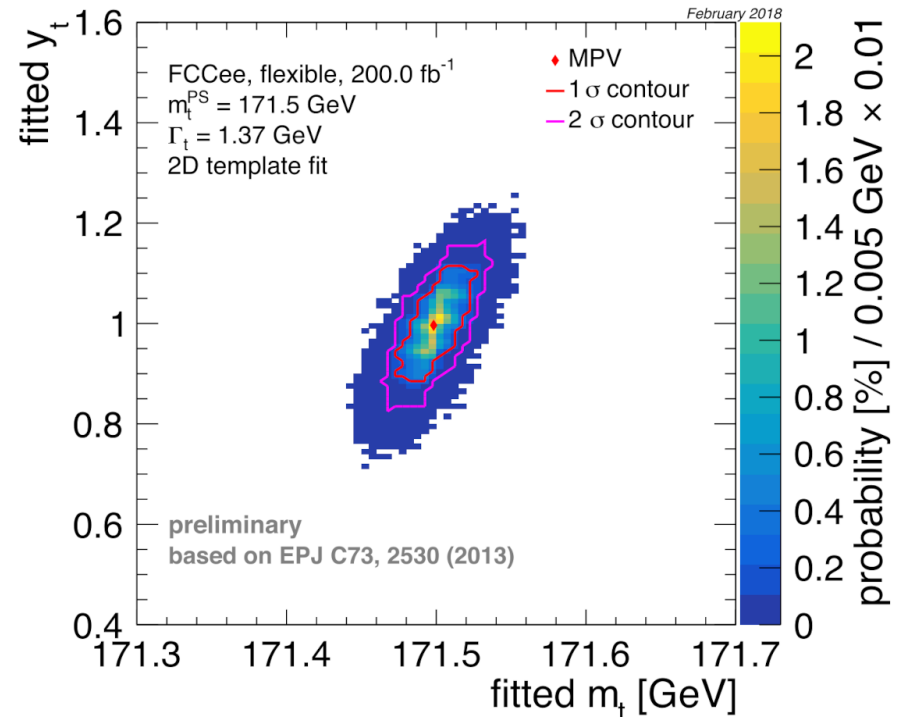
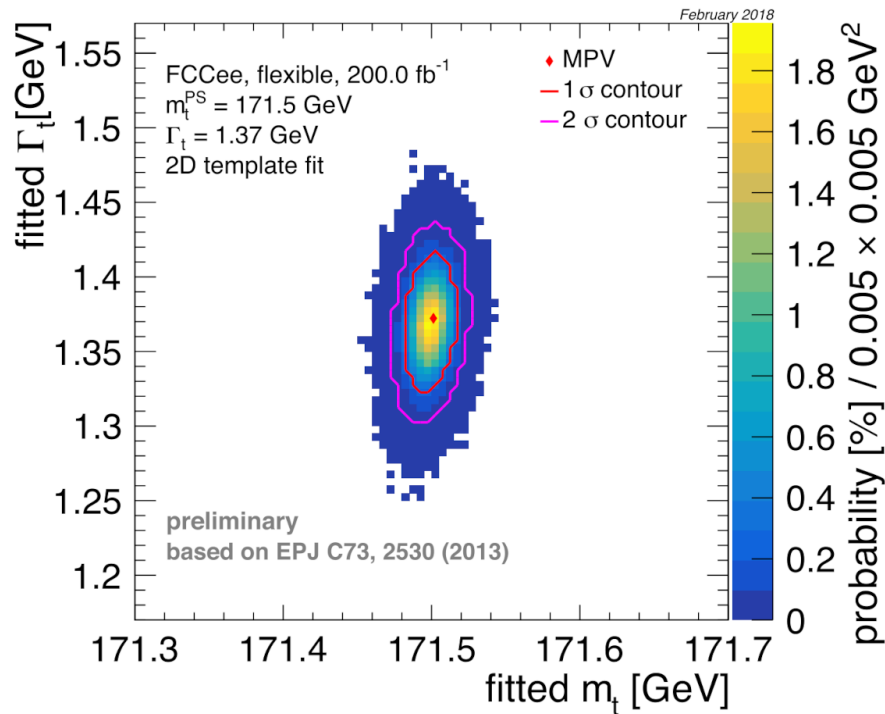
- **Threshold scan**
- **Radiative events**
- MC mass from direct reconstruction

Top-quark pair production at threshold



→ Fit to theory predictions
 in well-defined
 mass schemes

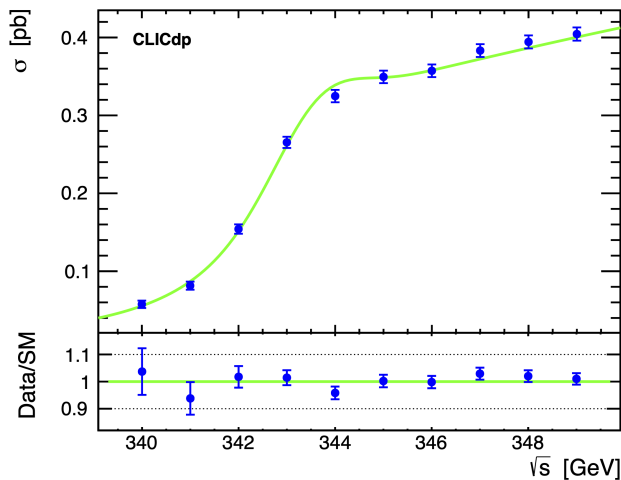
Measurements at the threshold



- Statistical uncertainty on m_t (Γ_t) is **17 (45) MeV** for 200 fb⁻¹
- Theory uncertainty from current NNNLO calculations: **≈40 MeV**
- 3 MeV uncertainty on m_t from centre-of-mass energy (if known with precision better than 10 MeV), 5 MeV from α_s (assuming precision of 2×10^{-4} from lower energies)
- 10% precision on the top Yukawa coupling possible
- Potential improvement on top mass from **differential distributions** → needs further study

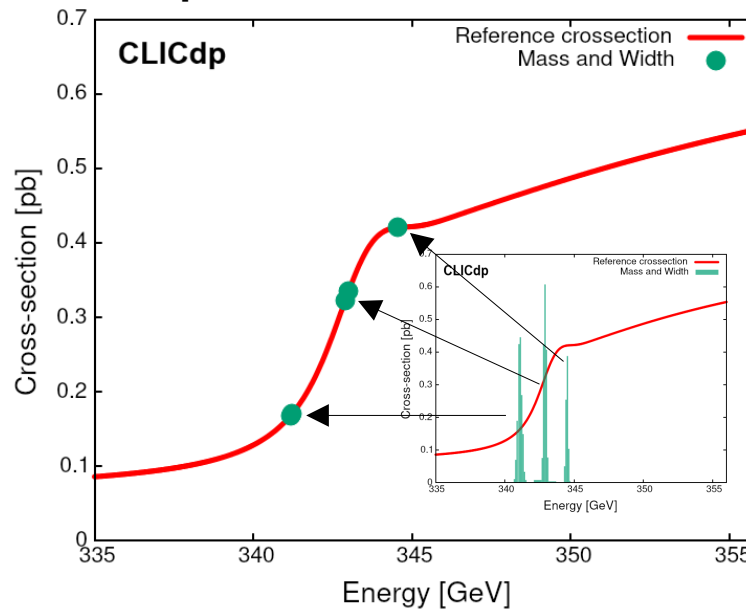
Optimisation of the threshold scan

Baseline scenario:

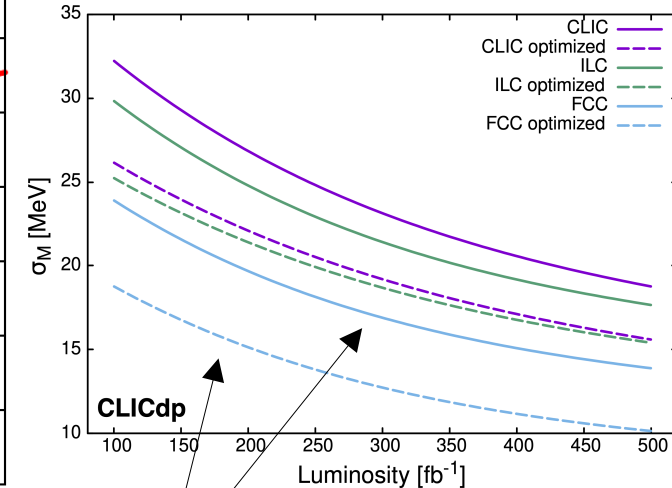


10 points of 10 fb^{-1} each

Optimised for mass & width:

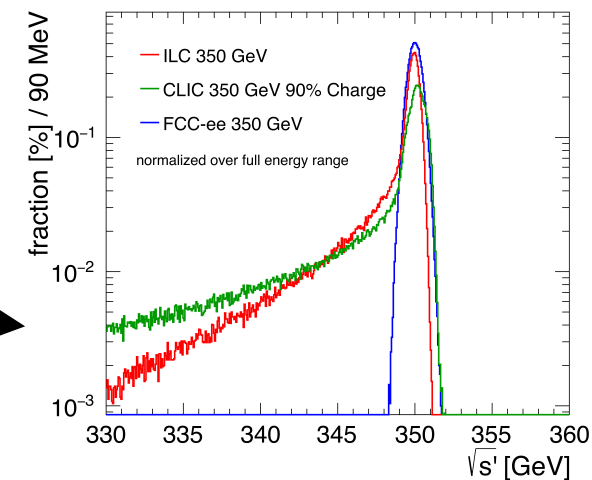


Precision on top mass:



- Optimisation of quantity and centre-of-mass energy for the individual cross section measurements
 → **25% better statistical precision on top mass** compared to 10 equidistant measurements

- Main difference between colliders: luminosity spectra

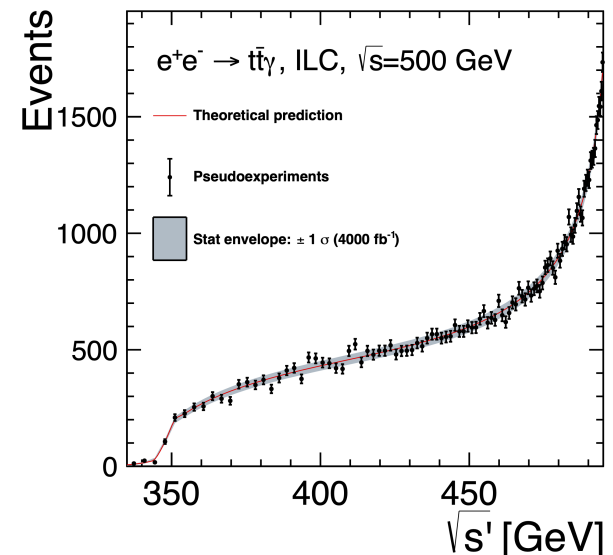
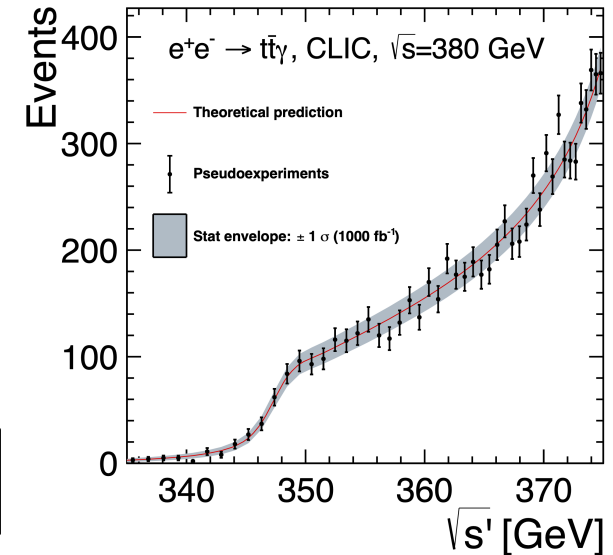


Radiative events: $e^+e^- \rightarrow t\bar{t}\gamma$

- Radiative events allow to extract the top mass in a **well-defined mass scheme above threshold**
→ complementary to threshold scan
- **Example:** matched NNLL threshold + N³LO continuum calculation and CLIC/ILC luminosity spectra
→ limited by statistical uncertainty

→ **Interesting possibility to explore for FCC-ee as well**

| cms energy | CLIC, $\sqrt{s} = 380$ GeV | | ILC, $\sqrt{s} = 500$ GeV | |
|-----------------|----------------------------|----------------|---------------------------|----------------|
| | 500 | 1000 | 500 | 4000 |
| statistical | 140 MeV | 90 MeV | 350 MeV | 110 MeV |
| theory | 46 MeV | | 55 MeV | |
| lum. spectrum | 20 MeV | | 20 MeV | |
| photon response | 16 MeV | | 85 MeV | |
| total | 150 MeV | 110 MeV | 360 MeV | 150 MeV |



Outline

Top-quark at FCC-ee:

- Mass measurements
- **Electroweak couplings**
- Top-quark FCNC
- Common reconstruction issues
- EFT interpretations

Top-quark electroweak couplings

- Top quark pairs are produced via Z/γ^* in electron-positron collisions
- The general form of the coupling can be described as:

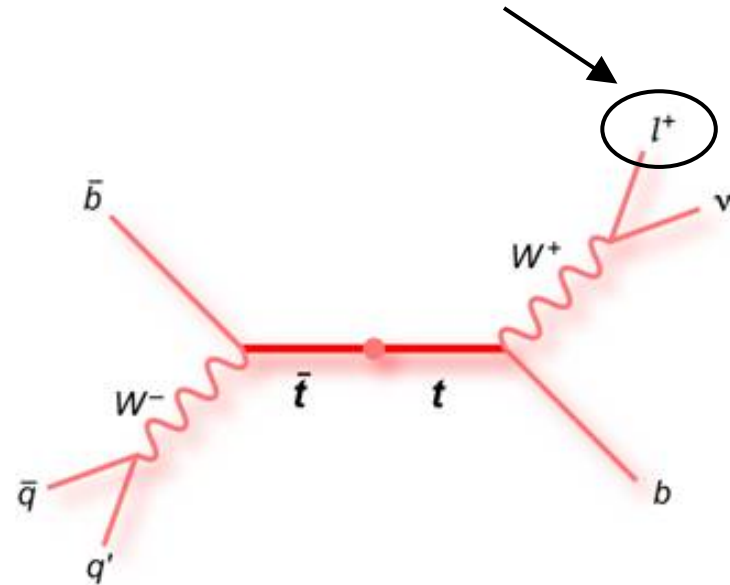
arXiv:hep-ph/0601112

CP conserving

CPV

$$\Gamma_{\mu}^{ttV}(k^2, q, \bar{q}) = -ie \left\{ \gamma_{\mu} (F_{1V}^V(k^2) + \gamma_5 F_{1A}^V(k^2)) + \frac{\sigma_{\mu\nu}}{2m_t} (q + \bar{q})^{\nu} (iF_{2V}^V(k^2) + \gamma_5 F_{2A}^V(k^2)) \right\}$$

- The γ and Z contributions can also be separated using the **lepton energy and angular distributions** in semi-leptonic events
 \rightarrow Form-factor measurement possible at circular colliders with unpolarised beams



Sensitivity to form factors (1)

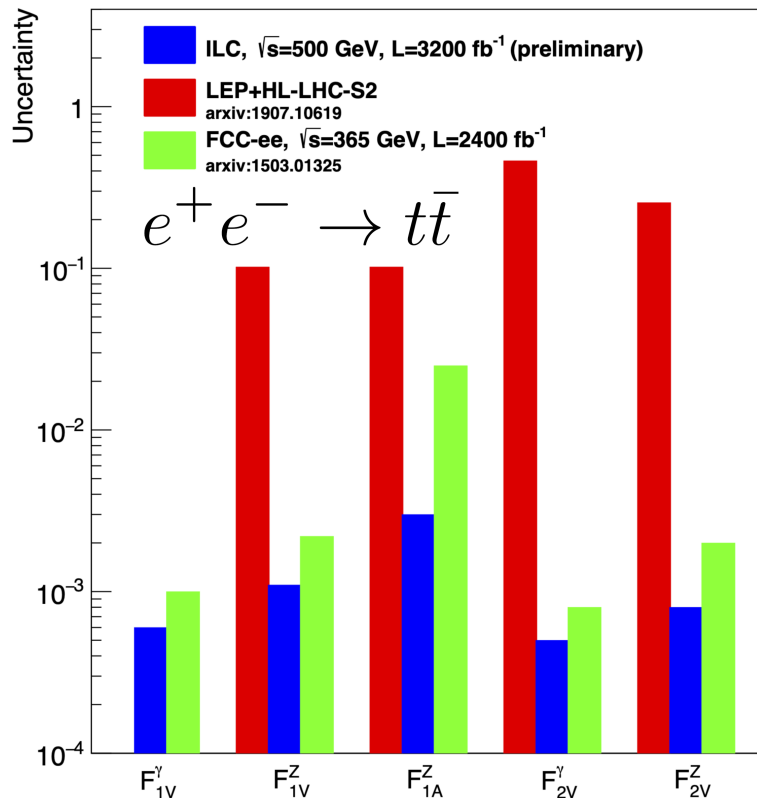
- Top quark pairs are produced via Z/γ^* in electron-positron collisions
- The general form of the coupling can be described as:

arXiv:hep-ph/0601112

CP conserving

CPV

$$\Gamma_{\mu}^{ttV}(k^2, q, \bar{q}) = -ie \left\{ \gamma_{\mu} \left(F_{1V}^V(k^2) + \gamma_5 F_{1A}^V(k^2) \right) + \frac{\sigma_{\mu\nu}}{2m_t} (q + \bar{q})^{\nu} \left(i F_{2V}^V(k^2) + \gamma_5 F_{2A}^V(k^2) \right) \right\}$$



→ FCC-ee provides **significant improvement compared to HL-LHC**

- Generator-level study, results confirmed by full simulation
- For example sensitive to **composite Higgs** models
- ttZ coupling from FCC-ee needed as input for top-Yukawa measurement at FCC-hh
- Further improvement possible, e.g. from addition of fully hadronic final states

JHEP 04, 182 (2015)
R. Pöschl, EPS-HEP 2021

Sensitivity to form factors (2)

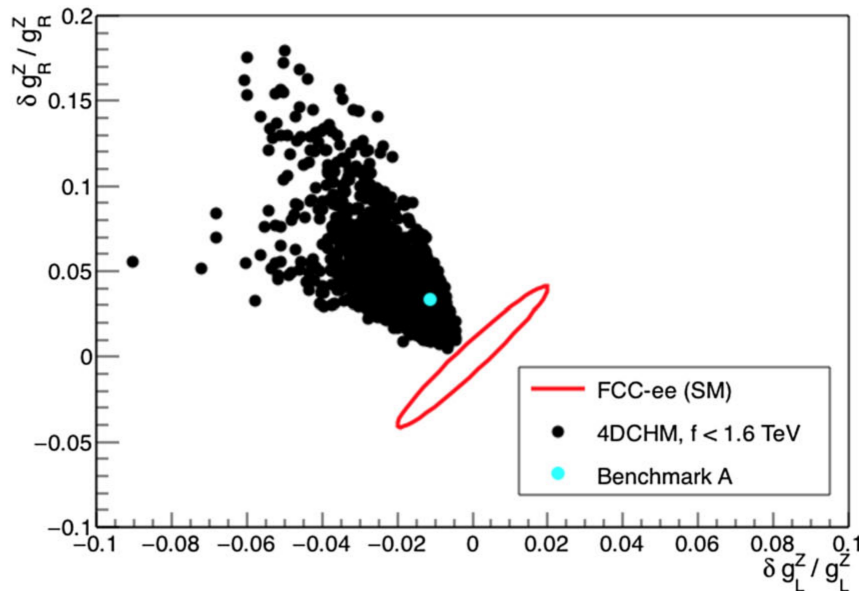
- Top quark pairs are produced via Z/γ^* in electron-positron collisions
- The general form of the coupling can be described as:

arXiv:hep-ph/0601112

CP conserving

CPV

$$\Gamma_{\mu}^{ttV}(k^2, q, \bar{q}) = -ie \left\{ \gamma_{\mu} \left(F_{1V}^V(k^2) + \gamma_5 F_{1A}^V(k^2) \right) + \frac{\sigma_{\mu\nu}}{2m_t} (q + \bar{q})^{\nu} \left(i F_{2V}^V(k^2) + \gamma_5 F_{2A}^V(k^2) \right) \right\}$$

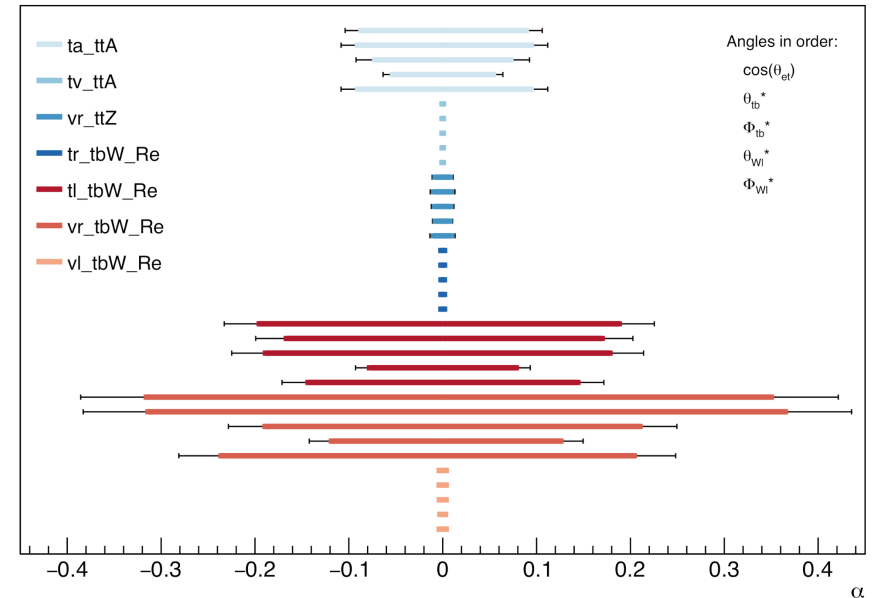
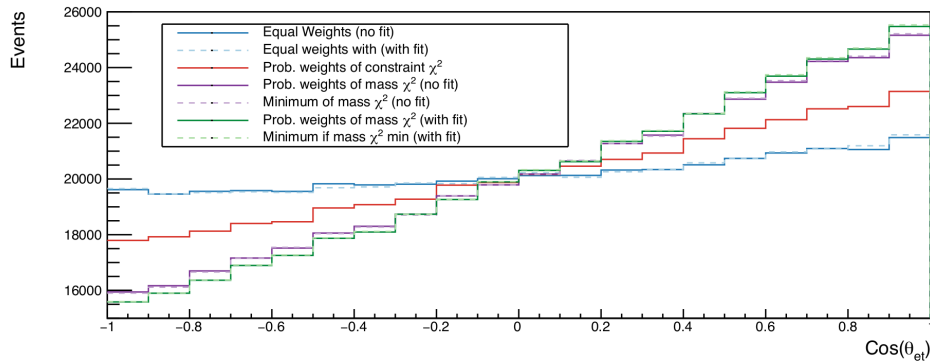


FCC CDR Volume 1

→ FCC-ee provides **significant improvement compared to HL-LHC**

- Generator-level study, results confirmed by full simulation
- For example sensitive to **composite Higgs** models
- ttZ coupling from FCC-ee needed as input for top-Yukawa measurement at FCC-hh
- Further improvement possible, e.g. from addition of fully hadronic final states

Ongoing study



- Delphes samples
- Comparison of different **jet reconstruction** algorithms
- **Kinematic fit** implemented
- Preliminary projections on **single anomalous couplings** from angular distributions

Julie Munch Torndal
Jorgen Beck Hansen

$$\mathcal{L}_{Wtb} = -\frac{g}{\sqrt{2}} \bar{b} \gamma^\mu (\mathbb{V}_L) P_L + (\mathbb{V}_R) P_R) t W_\mu^-$$

$$- \frac{g}{\sqrt{2}} \bar{b} \frac{i\sigma^{\mu\nu} q\nu}{M_W} (\mathbb{g}_L) P_L + (\mathbb{g}_R) P_R) t W_\mu^- + H.c.$$

$$\mathcal{L}_{Ztt} = -\frac{g}{2c_W} \bar{t} \gamma^\mu (\mathbb{X}_{tt}^L) P_L + (\mathbb{X}_{tt}^R) P_R - 2s_W^2 Q_t) t Z_\mu$$

$$- \frac{g}{2c_W} \bar{t} \frac{i\sigma^{\mu\nu} q\nu}{M_Z} (\mathbb{d}_V^Z) + i(\mathbb{d}_A^Z) \gamma_5) t Z_\mu$$

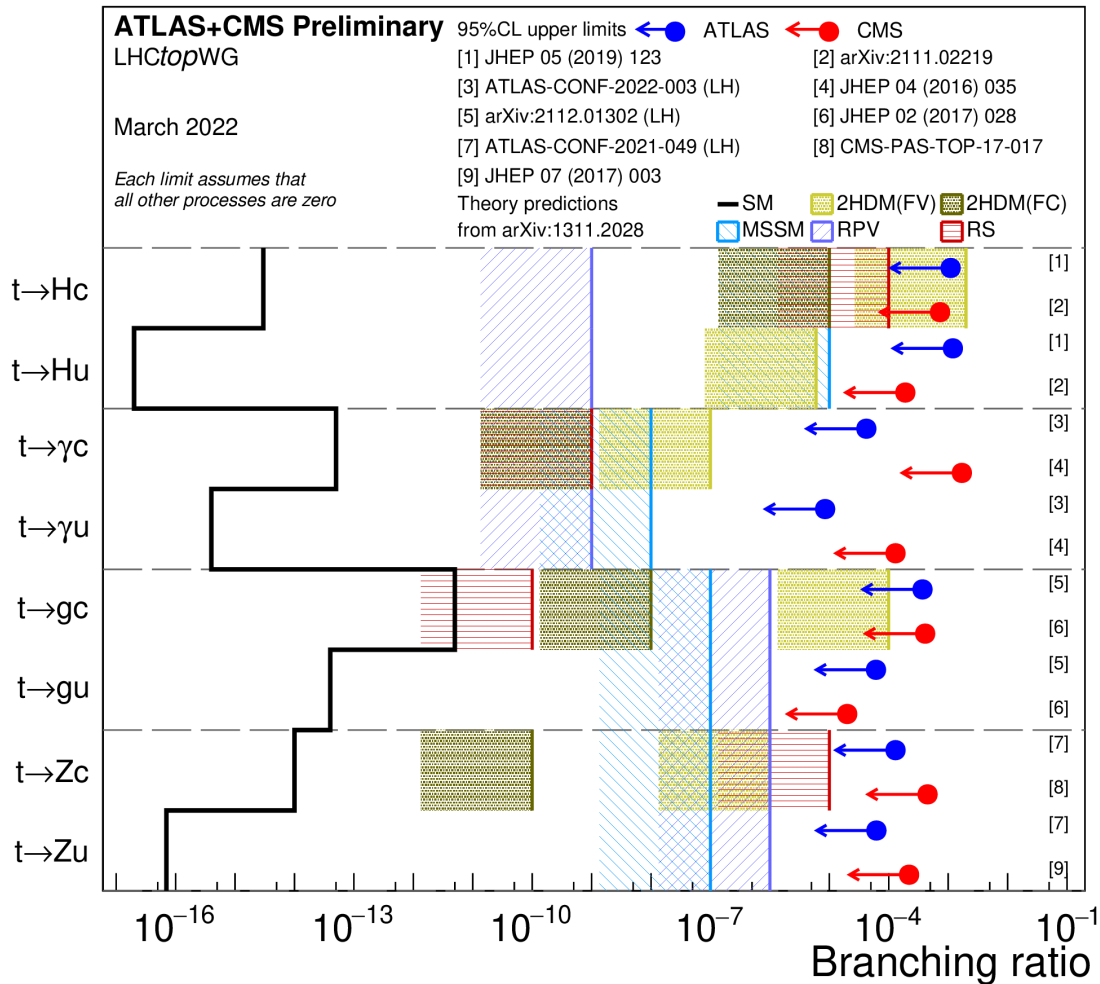
$$\mathcal{L}_{\gamma tt} = -e Q_t \bar{t} \gamma^\mu A_\mu - e \bar{t} \frac{i\sigma^{\mu\nu} q\nu}{m_t} (\mathbb{d}_V^\gamma) + i(\mathbb{d}_A^\gamma) \gamma_5) t A_\mu$$

Outline

Top-quark at FCC-ee:

- Mass measurements
- Electroweak couplings
- **Top-quark FCNC**
- Common reconstruction issues
- EFT interpretations

Top-quark FCNC: current status

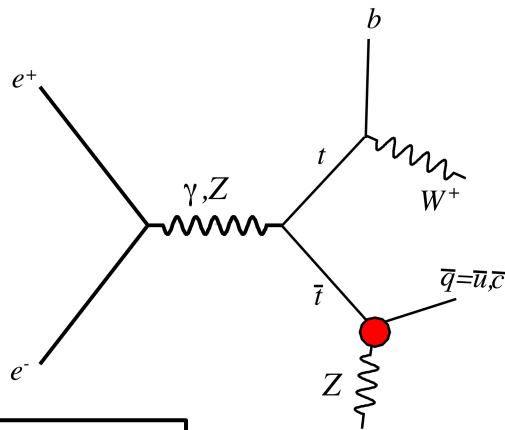


- SM branching ratios strongly suppressed ($10^{-16} \dots 10^{-12}$)
→ **strong enhancement in certain BSM models** possible (update needed?)
- Current 95% CL limits typically at the level of 10^{-5} to 10^{-3}

Top-quark FCNC at FCC-ee

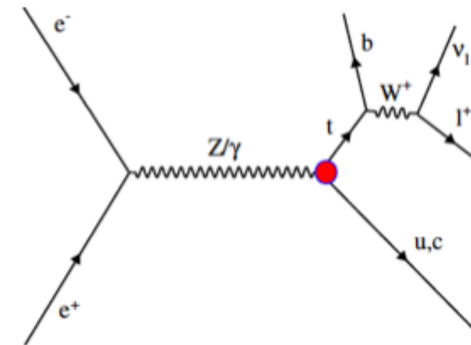
e^+e^- colliders especially competitive for: $t \rightarrow cH$, $t \rightarrow cZ$, $t \rightarrow c\gamma$, $t \rightarrow cg$

In top-quark decays:



At 365 GeV

In single top production:

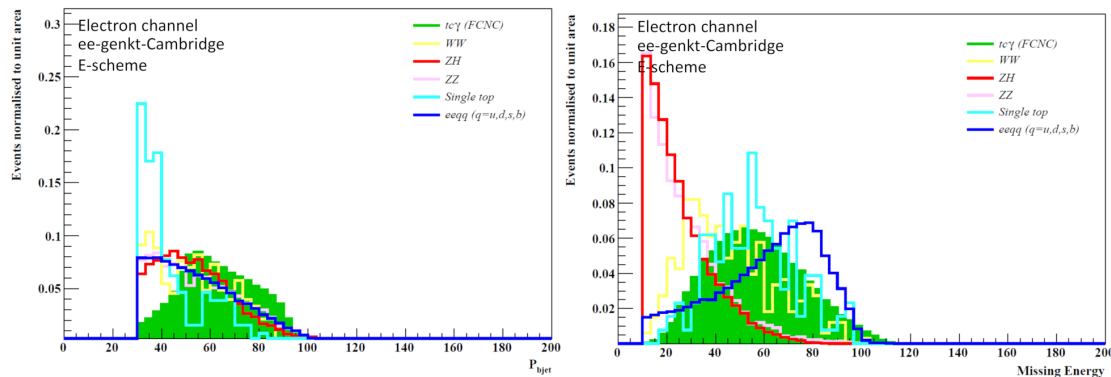
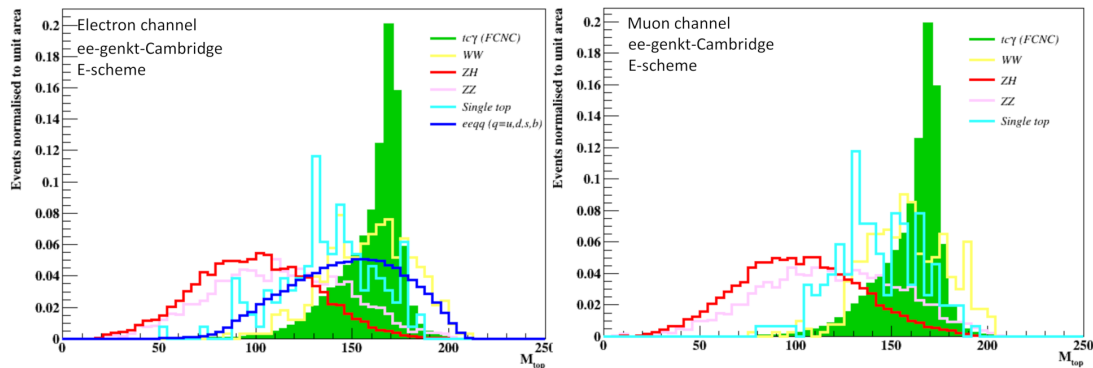


At 240 and 365 GeV

Phys. Lett. B 755, 25 (2017)

- Preliminary results indicate that **combination of both energies and approaches** desirable to improve with respect to HL-LHC
- The ultimate precision will be achieved at FCC-hh

Ongoing study



- Recently started, focussing on **single top production at 240 GeV**
- Delphes samples, different jet algorithms compared
- First projections from cut-and-count approach, **to be improved using multi variate analysis**

Hamzeh Khanpour
Sedigheh Tizchang
Mojtaba Mohammadi
Patrizia Azzi
Emmanuel Francois Perez

Outline

Top-quark at FCC-ee:

- Mass measurements
- Electroweak couplings
- Top-quark FCNC
- **Common reconstruction issues**
- EFT interpretations

Common reconstruction aspects

- **Jet reconstruction:** all state-of-the-art clustering algorithms available in **FastJet** (Durham, generalised k_t , Valencia, ...) <https://fastjet.fr/>

- **Flavour tagging:** **LCFIPlus** (originally developed for linear collider studies), new developments based on **ParticleNet** very promising in fast simulation
Charm tagging important for FCNC decays [Nucl. Inst. Meth. A 808, 109 \(2016\)](#)
[arXiv:2202.03285](#)

- **Kinematic fits:** **MarlinKinFit** (from linear collider studies), **ABCfit++** (ported from LEP algorithm)
Inclusion of ISR from energy loss can be important above threshold
<https://github.com/Torndal/ABCfitplusplus>
[NIM A 624, 184 \(2010\)](#)

- **Charged lepton identification:** for semi-leptonic $t\bar{t}$ events

- **Photon identification:** for radiative $t\bar{t}$ events, $t \rightarrow c\gamma$, ...

→ see also talks by Clément Helsen, Valentin Volkl

Outline

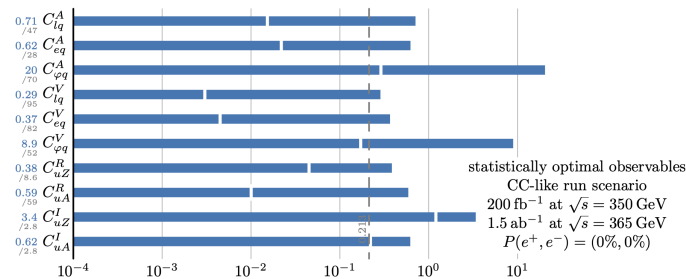
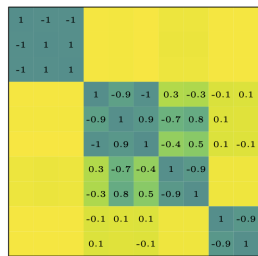
Top-quark at FCC-ee:

- Mass measurements
- Electroweak couplings
- Top-quark FCNC
- Common reconstruction issues
- **EFT interpretations**

Global EFT interpretations

- Global EFT analyses of EW analyses of $e^+e^- \rightarrow t\bar{t}$ production and $e^+e^- \rightarrow tj$ have been demonstrated in recent years

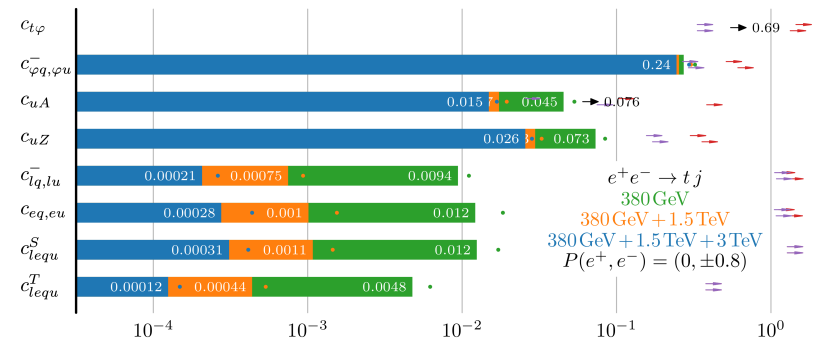
Top-quark electroweak couplings



JHEP 10, 168 (2018)

NB: This example uses “statistically optimal observables” which make the best use of the fully differential $bW^+b\bar{W}^-$ distributions

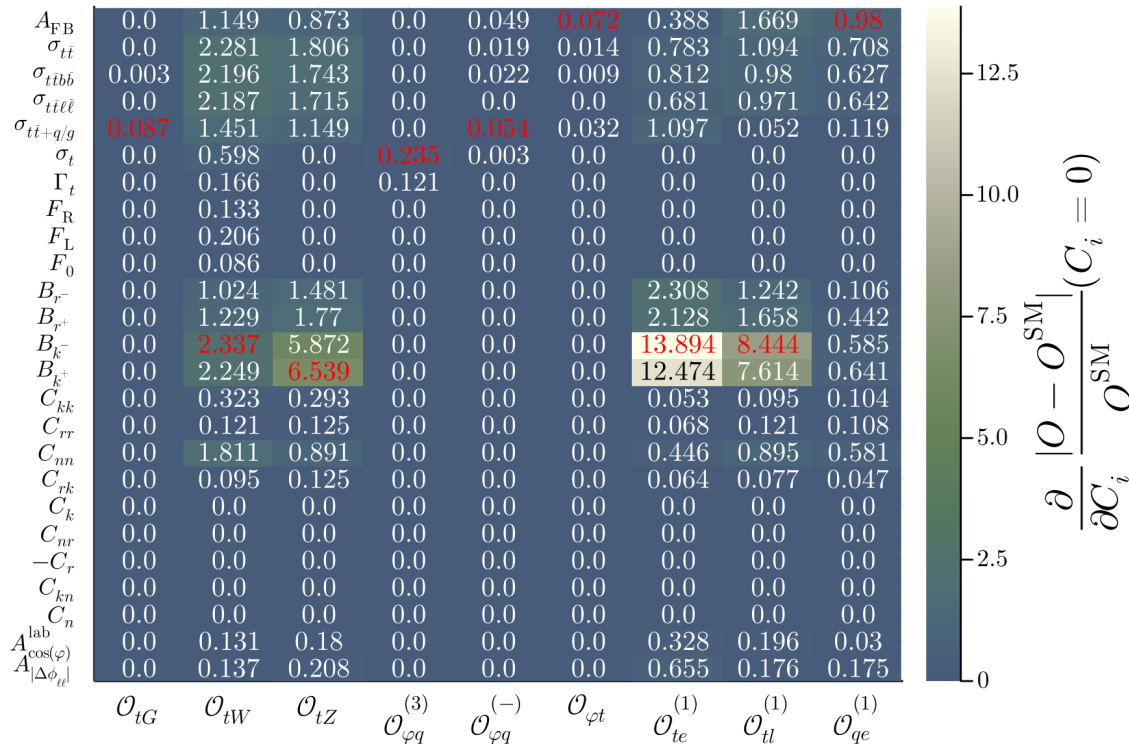
Top-quark FCNC: example from CLIC



CERN-2018-009-M

- **To be optimised for FCC-ee conditions** (large statistics, but no beam polarisation) **and projections**
- Combined FCC-ee + FCC-hh EFT analysis would be very interesting (also for comparison with other collider options...)

Ongoing study



Generator-level (MadGraph)

- New study of EFT-sensitive $t\bar{t}$ observables at FCC-ee
- Global fit is final aim
- Transition to Whizard planned
- Started to look at reconstructed observables with Delphes samples

Cornelius Grunwald
 Laetitia Guerry
 Kevin Kröninger
 Romain Madar
 Stéphane Monteil
 Lars Röhrig

Summary and conclusions

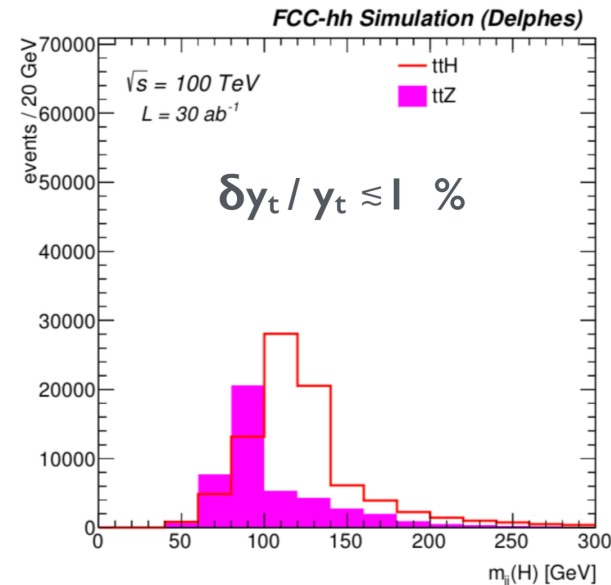
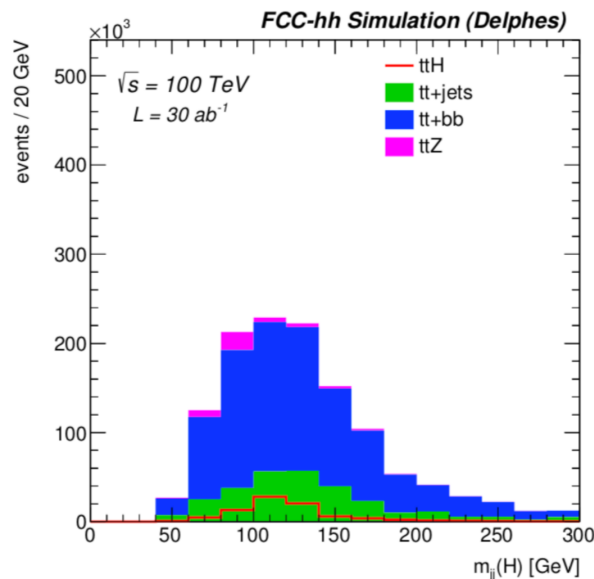
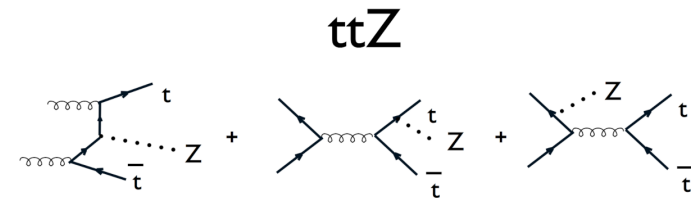
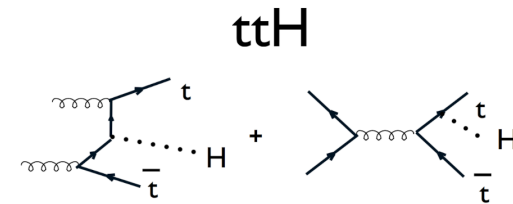
- The **top-quark** plays a crucial role at FCC-ee below, at and above the pair-production threshold
- Well-defined program:
 - A **threshold scan** is the best possible mass measurement
 - Operation well above threshold improves the **top-quark EW couplings** by at least an order of magnitude
 - **Top-quark FCNC-effects** can be problem in single-top production and in decays
- Interesting **reconstruction** issues to be studied in ongoing and future physics potential studies, in particular kinematic fitting and jet reconstruction in complex events
- Top-quark production would also be a good **detector benchmark channel** in full simulation
- Global **EFT interpretations** to be adopted and optimised for FCC-ee

Thank you!

Backup slides

top-Yukawa coupling at FCC-hh

- production ratio $\sigma(ttH)/\sigma(ttZ) \approx y_t^2 y_b^2 / g_{ttZ}^2$
- measure $\sigma(ttH)/\sigma(ttZ)$ in $H/Z \rightarrow bb$ mode in the boosted regime, in the semi-leptonic channel
- perform simultaneous fit of double Z and H peak
- (lumi, scales, pdfs, efficiency) uncertainties cancel out in ratio
- assuming g_{ttZ} and κ_b known to 1% (from FCC-ee),
 → measure y_t to 1%



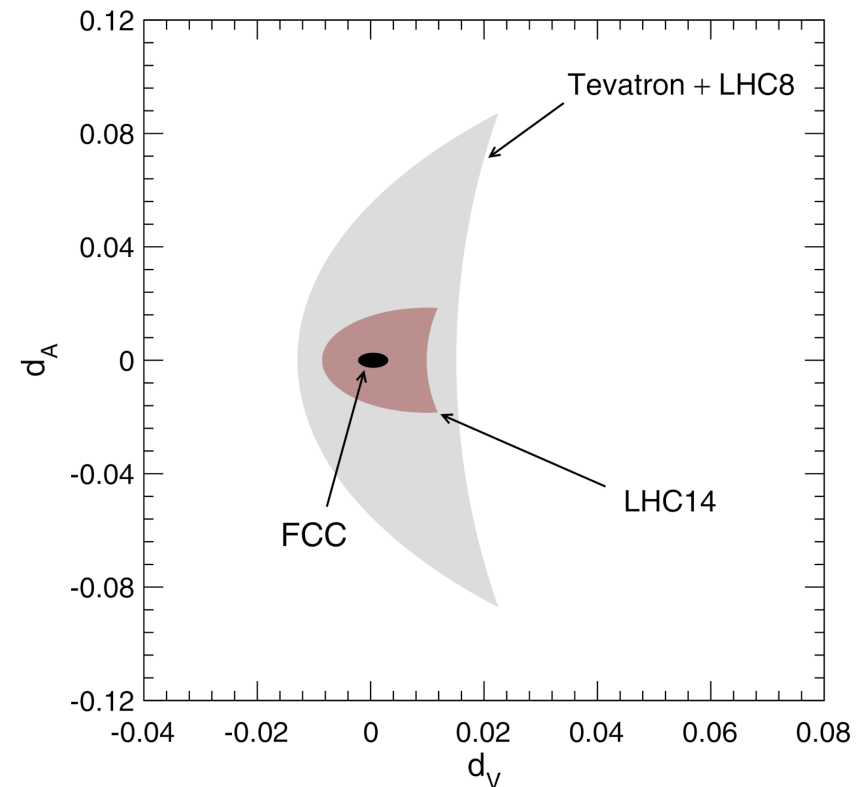
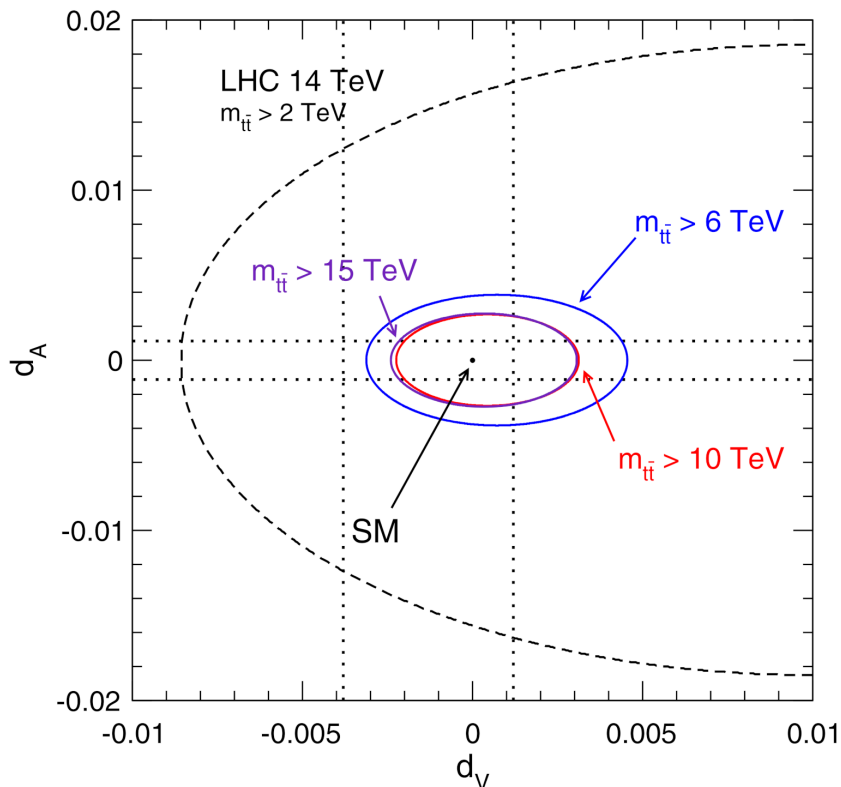
Anomalous top-gluon couplings from $pp \rightarrow t\bar{t}$

Strongly boosted:

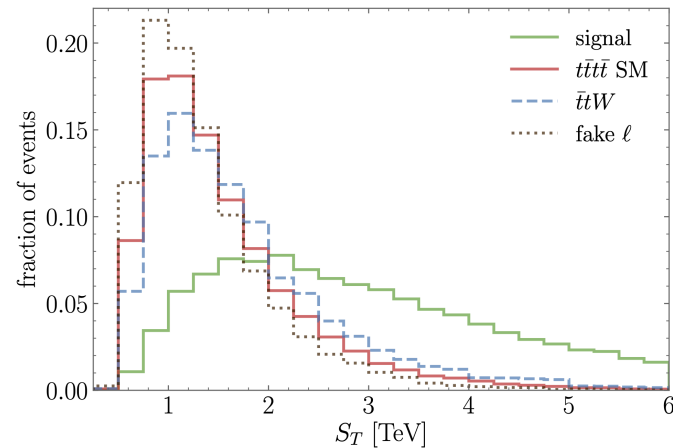
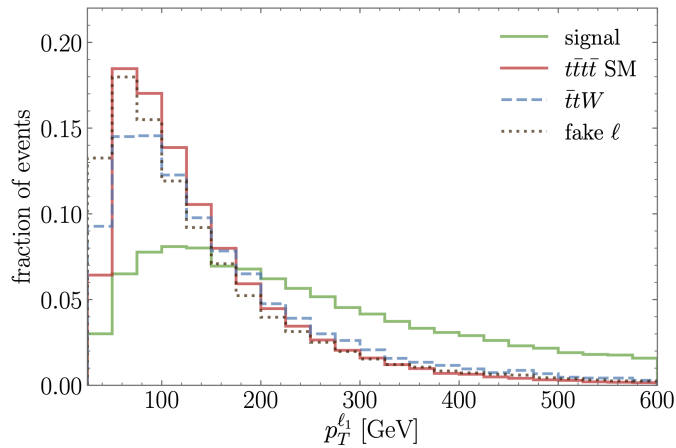
$m_{t\bar{t}} > 10$ TeV is optimal choice from cross section analysis

$$\delta\mathcal{L} = \frac{g_s}{m_t} \bar{t} \sigma^{\mu\nu} (d_V + i d_A \gamma_5) \frac{\lambda_a}{2} t G_{\mu\nu}^a$$

$d_V(d_A)$: chromomagnetic (chromoelectric) dipole moment



pp \rightarrow $t\bar{t}t\bar{t}$ at FCC-hh

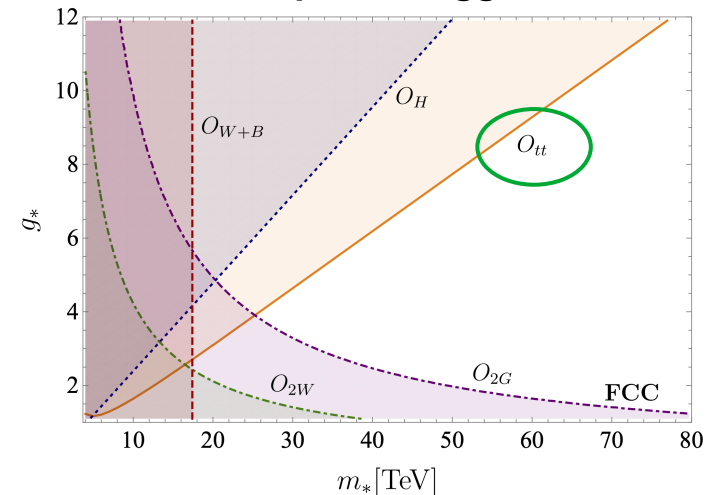


Example: same-sign di-lepton final state

| | |
|---|---|
| FCC-hh $pp \rightarrow t\bar{t}t\bar{t}$ 100 TeV, 30 ab^{-1} : | $\Lambda/\sqrt{ c_{tt} } > 6.5 \text{ TeV}$ |
| CLIC $e^+e^- \rightarrow t\bar{t}$ 3 TeV, 3 ab^{-1} : | $\Lambda/\sqrt{ c_{tt} } > 7.7 \text{ TeV}$ |
| ILC $e^+e^- \rightarrow t\bar{t}$ 1 TeV, 1 ab^{-1} : | $\Lambda/\sqrt{ c_{tt} } > 4.1 \text{ TeV}$ |

FCC-hh: same-sign di-lepton and tri-lepton final states combined

Composite Higgs



95% CL limits from individual operators