

K. Oide (UNIGE)

June 1, 2022

Many thanks to A. Blondel, M. Hofer, M. Koratzinos, N. Muchnoi, D. Shatilov, and all FCC-ee/FCCIS colleagues



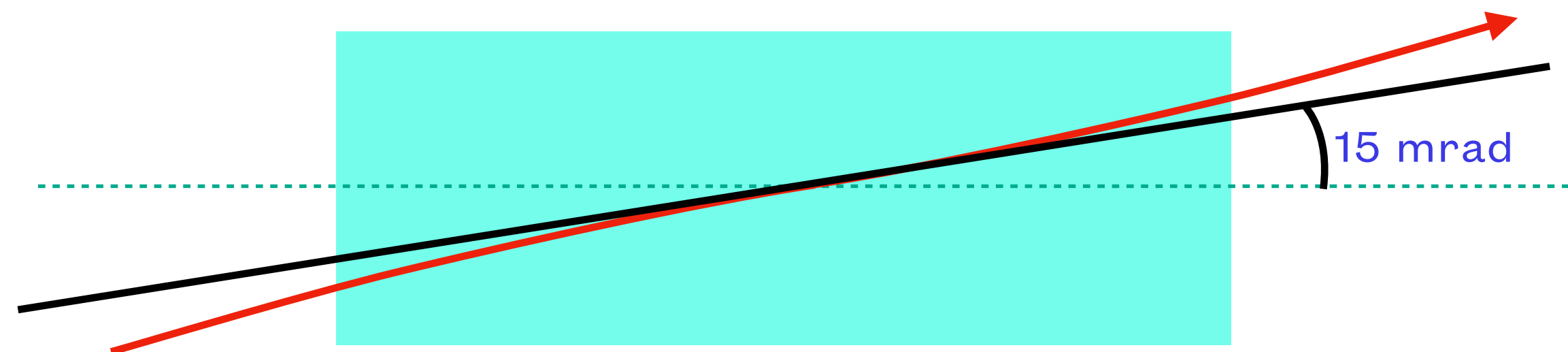
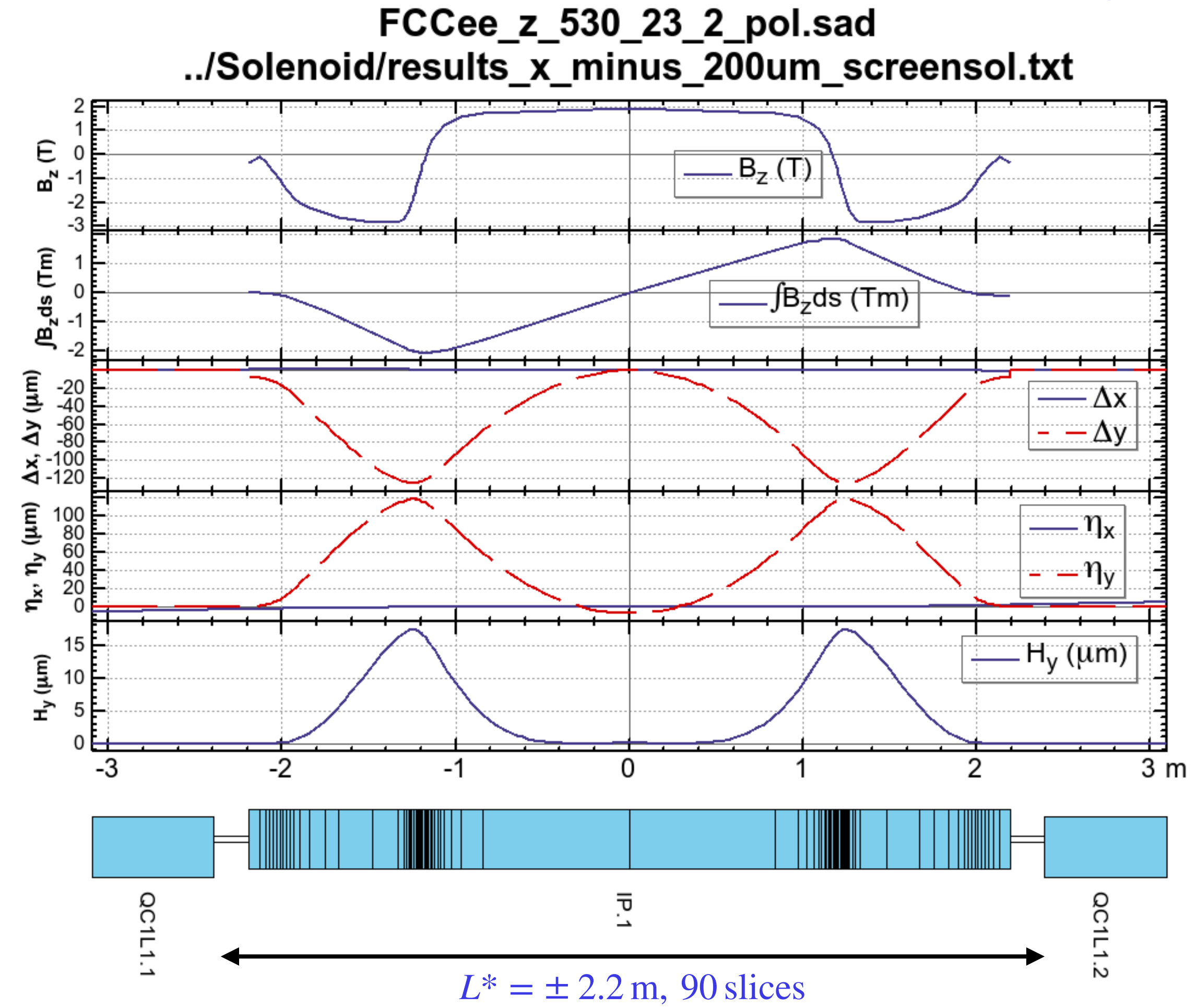
Polarimeter and wigglers integration status

Optics including a realistic solenoid (M. Koratzinos)



- A realistic solenoid + multipole field given by M. Koratzinos has been included into the latest 4 IP lattice.
- The L^* region ($IP_{\pm 2.2}$ m) is divided into 90 slices with *unequal thicknesses* ≥ 5 mm, *along the tilted straight line* (± 15 mrad), not along the solenoid axis.
- No leak of vertical dispersion and x-y coupling to the outside region.
 - α , β , and hor. dispersion leak outside.
 - The leaked optics and hor. dispersion are corrected to the no-solenoid case by tweaking the outer quads.
- The highest contribution to the vertical emittance comes from the middle transition ($s \sim \pm 1.2$ m) of B_z .

~CDR, 2IP optics



Parameters (4 IP, new layout)

$$\beta_x^* = 10 \text{ cm @ Z}$$

Beam energy	[GeV]	45.6	80	120	182.5
Layout		PA31-1.0			
# of IPs		4			
Circumference	[km]	91.174117		91.174107	
Bending radius of arc dipole	[km]	9.937			
Energy loss / turn	[GeV]	0.0391	0.370	1.869	10.0
SR power / beam	[MW]	50			
Beam current	[mA]	1280	135	26.7	5.00
Bunches / beam		10000	880	248	40
Bunch population	[10 ¹¹]	2.43	2.91	2.04	2.37
Horizontal emittance ε_x	[nm]	0.71	2.16	0.64	1.49
Vertical emittance ε_y	[pm]	1.42	4.32	1.29	2.98
Arc cell		Long 90/90		90/90	
Momentum compaction α_p	[10 ⁻⁶]	28.5		7.33	
Arc sextupole families		75		146	
$\beta_{x/y}^*$	[mm]	100 / 0.8	200 / 1.0	300 / 1.0	1000 / 1.6
Transverse tunes/IP $Q_{x/y}$		53.563 / 53.600		100.565 / 98.595	
Energy spread (SR/BS) σ_δ	[%]	0.038 / 0.132	0.069 / 0.154	0.103 / 0.185	0.157 / 0.219
Bunch length (SR/BS) σ_z	[mm]	4.38 / 15.4	3.55 / 8.01	3.34 / 6.00	2.00 / 2.80
RF voltage 400/800 MHz	[GV]	0.120 / 0	1.0 / 0	2.08 / 0	4.0 / 7.25
Harmonic number for 400 MHz		121648			
RF frequency (400 MHz)	MHz	399.994581		399.994627	
Synchrotron tune Q_s		0.0370	0.0801	0.0328	0.0826
Long. damping time	[turns]	1168	217	64.5	18.5
RF acceptance	[%]	1.6	3.4	1.9	3.1
Energy acceptance (DA)	[%]	±1.3	±1.3	±1.7	-2.8 +2.5
Beam-beam ξ_x/ξ_y^a		0.0023 / 0.135	0.011 / 0.125	0.014 / 0.131	0.091 / 0.139
Luminosity / IP	[10 ³⁴ /cm ² s]	182	19.4	7.26	1.24
Lifetime (q + BS)	[sec]	-	-	1065	5090
Lifetime (lum)	[sec]	1129	1070	596	752

^aincl. hourglass.

$$\beta_x^* = 15 \text{ cm (Nov. 29)}$$

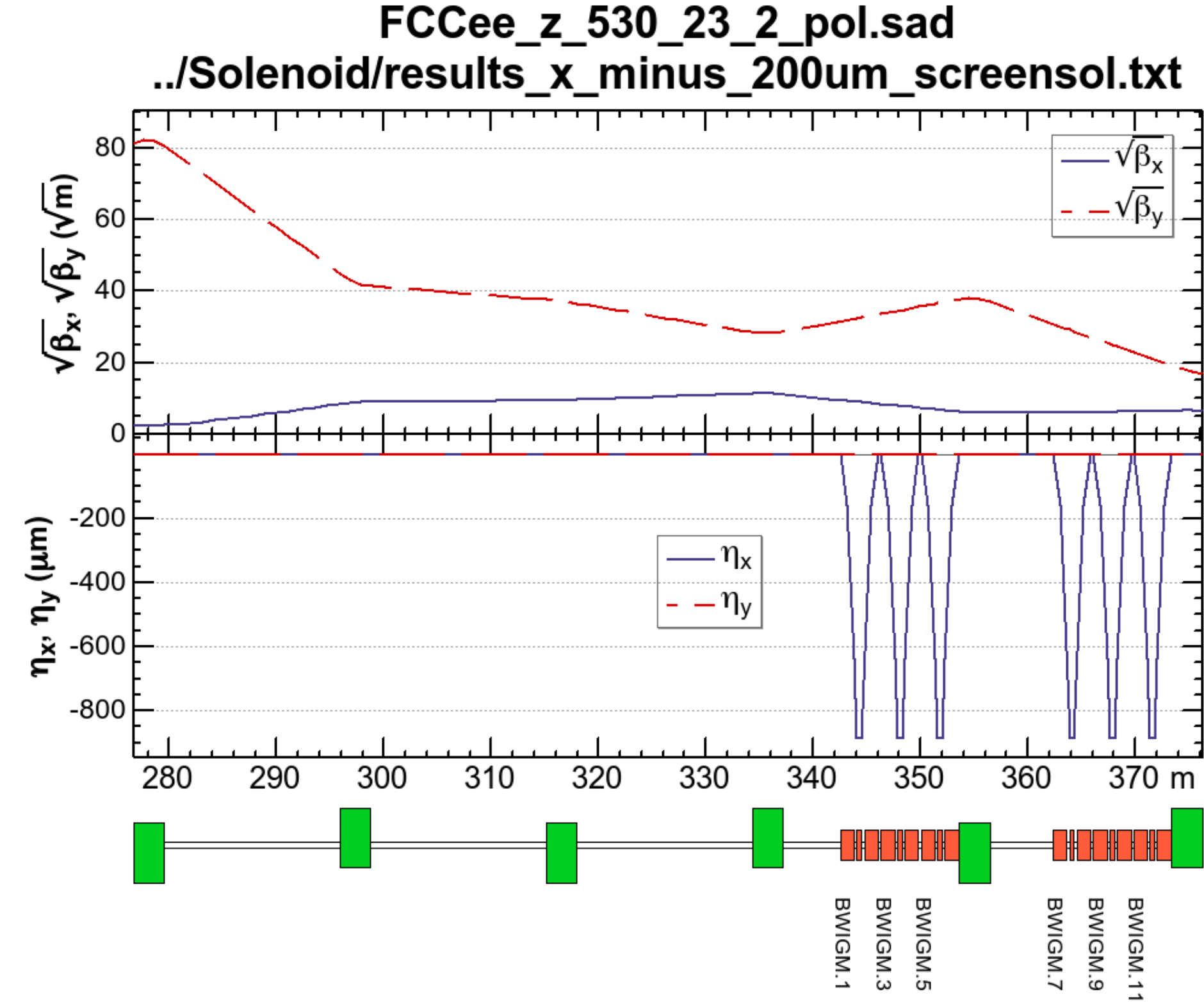
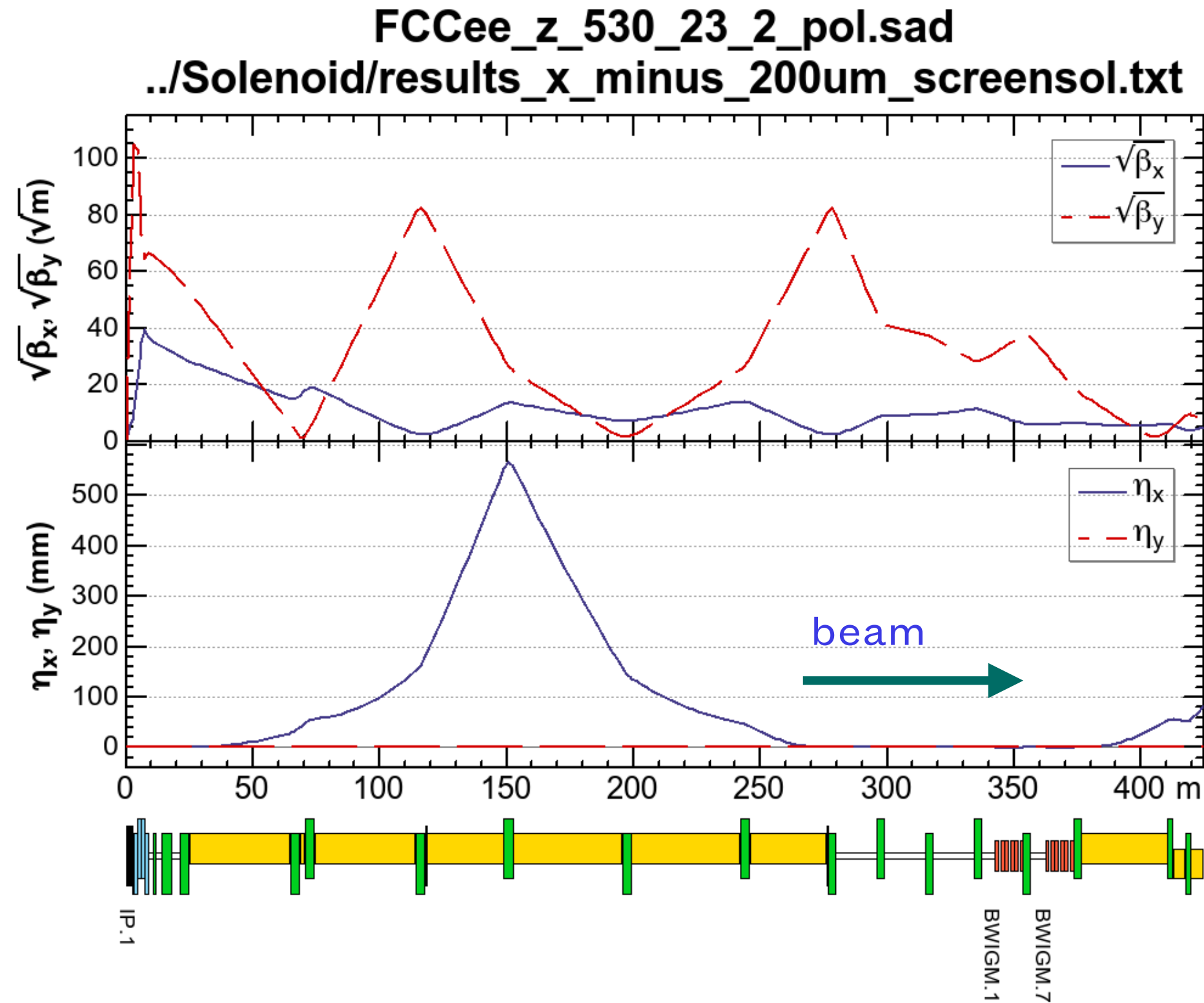
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Bending radius of arc dipole	[km]	9.937			
Energy loss / turn	[GeV]	0.0391	0.370	1.869	10.0
SR power / beam	[MW]	50			
Beam current	[mA]	1280	135	26.7	5.00
Bunches / beam		9600	880	248	36
Bunch population	[10 ¹¹]	2.53	2.91	2.04	2.64
Horizontal emittance ε_x	[nm]	0.71	2.16	0.64	1.49
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Arc sextupole families		75		146	
$\beta_{x/y}^*$	[mm]	150 / 0.8	200 / 1.0	300 / 1.0	1000 / 1.6
Transverse tunes/IP $Q_{x/y}$		53.563 / 53.600		100.565 / 98.595	
Energy spread (SR/BS) σ_δ	[%]	0.039 / 0.130	0.069 / 0.154	0.103 / 0.185	0.157 / 0.229
Bunch length (SR/BS) σ_z	[mm]	4.37 / 14.5	3.55 / 8.01	3.34 / 6.00	2.02 / 2.95
RF voltage 400/800 MHz	[GV]	0.120 / 0	1.0 / 0	2.08 / 0	4.0 / 7.25
Harmonic number for 400 MHz		121648			
RF frequency (400 MHz)	MHz	399.994581		399.994627	
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RF acceptance	[%]	1.6	3.4	1.9	3.1
Energy acceptance (DA)	[%]	±1.3	±1.3	±1.7	-2.8 +2.5
Beam-beam ξ_x/ξ_y^a		0.0040 / 0.152	0.011 / 0.125	0.014 / 0.131	0.096 / 0.151
Luminosity / IP	[10 ³⁴ /cm ² s]	189	19.4	7.26	1.33
Lifetime (q + BS)	[sec]	-	-	1065	2405
Lifetime (lum)	[sec]	1089	1070	596	701

^aincl. hourglass.



- By squeezing β_x^* , bunches/ring (bunch population), bunch length, energy spread also change. All affect the luminosity.
- $\xi_y \lesssim 0.14$ is set as a criterion (also set at $t\bar{t}$ this time).
- The betatron tunes are not yet chosen perfectly considering the instability.

Polarization wigglers (M. Hofer)



- Polarization wigglers can be placed at the straight section “LA*”, located at downstream of each IP.
- Parameters follow CDR’s: can be readjusted, taking the critical energy, etc., into account (M. Hofer).

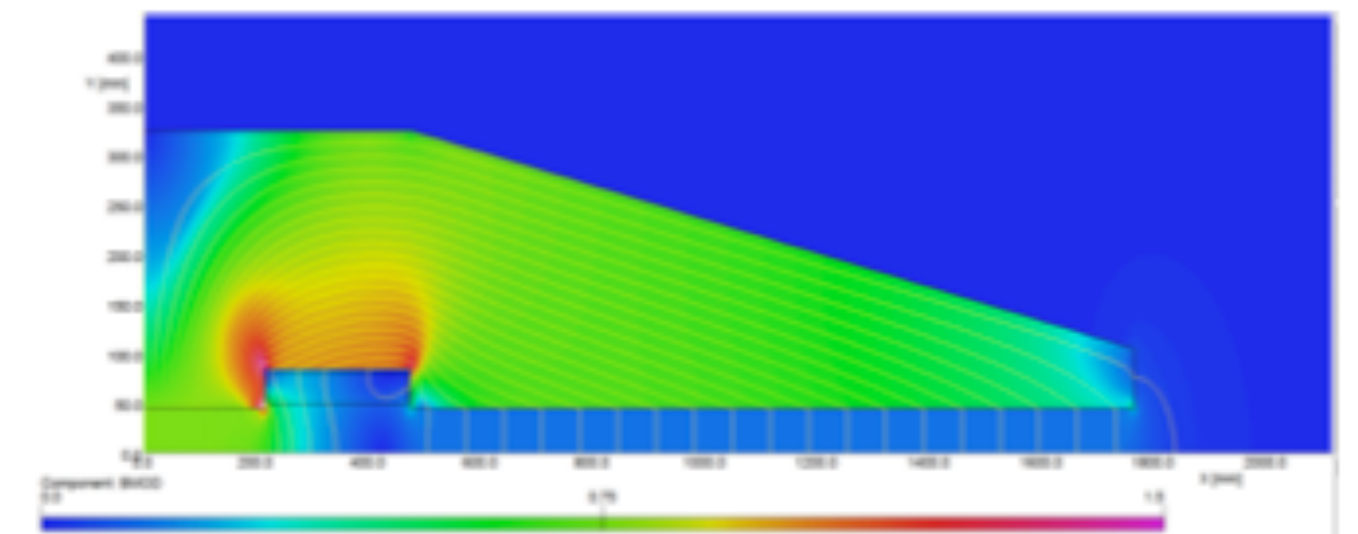
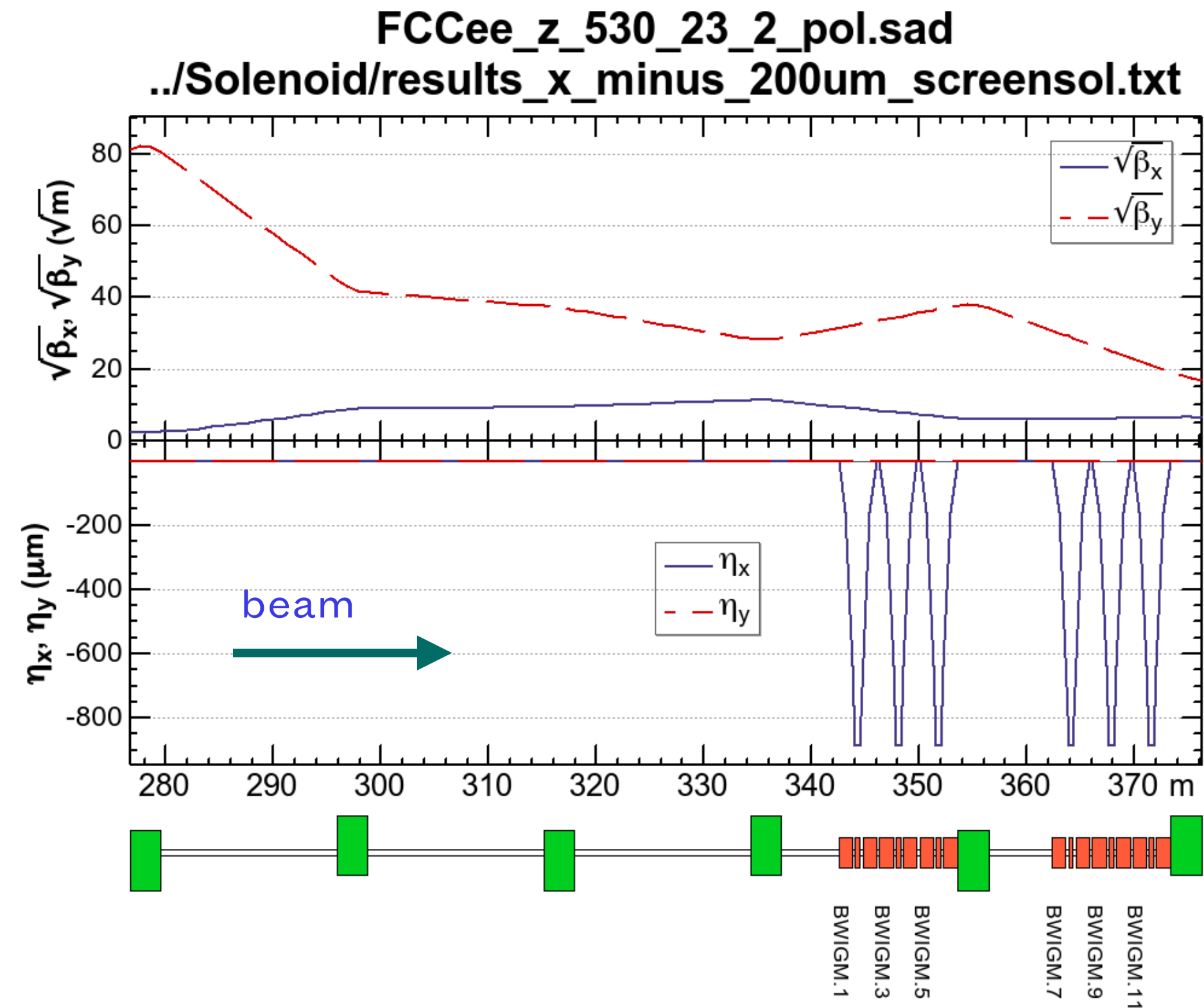


Figure 3.10: Magnetic design of a half unit of the polarisation wiggler. In this representation the beam will travel in the z-direction.

Parameter with pol. wigglers

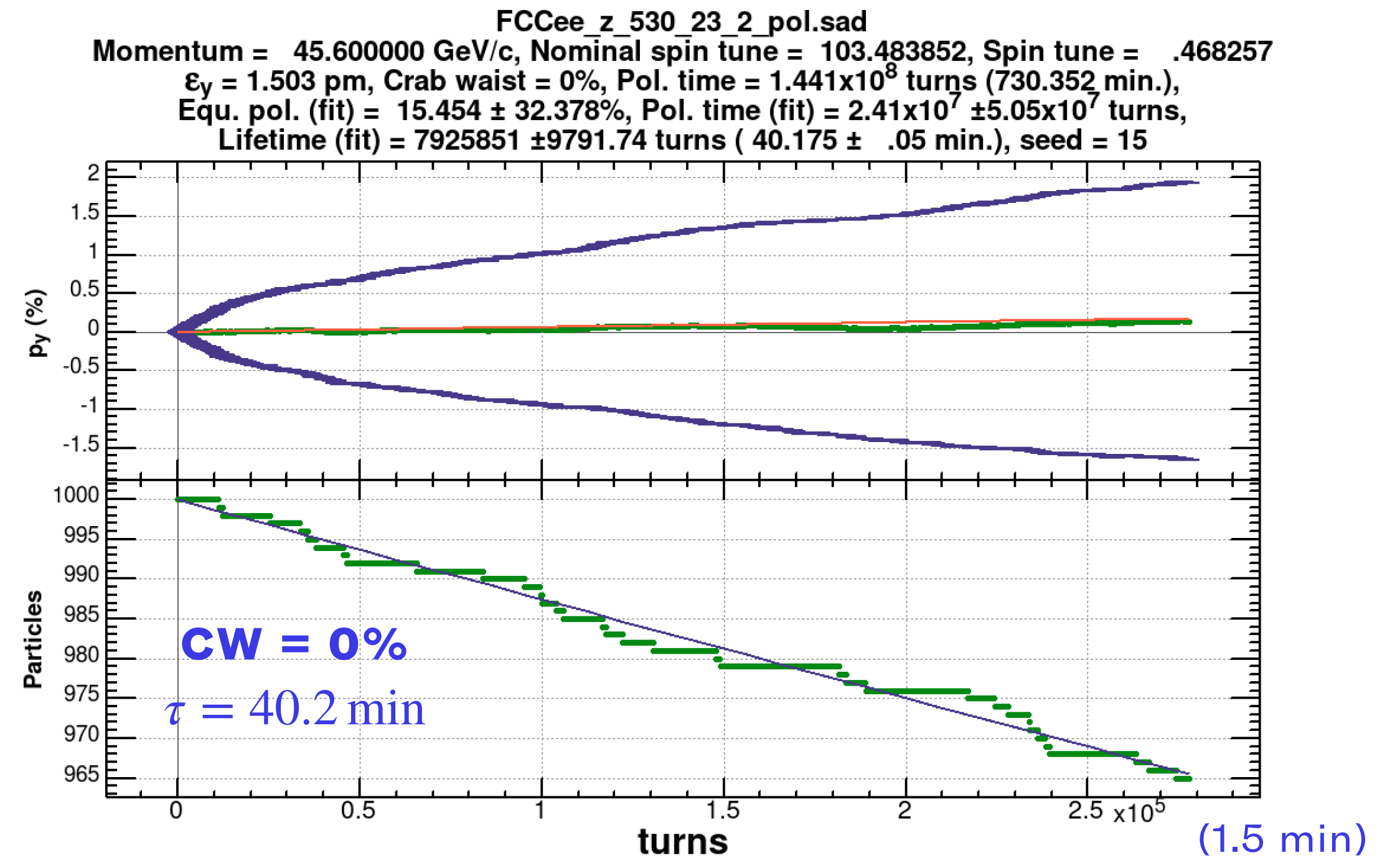
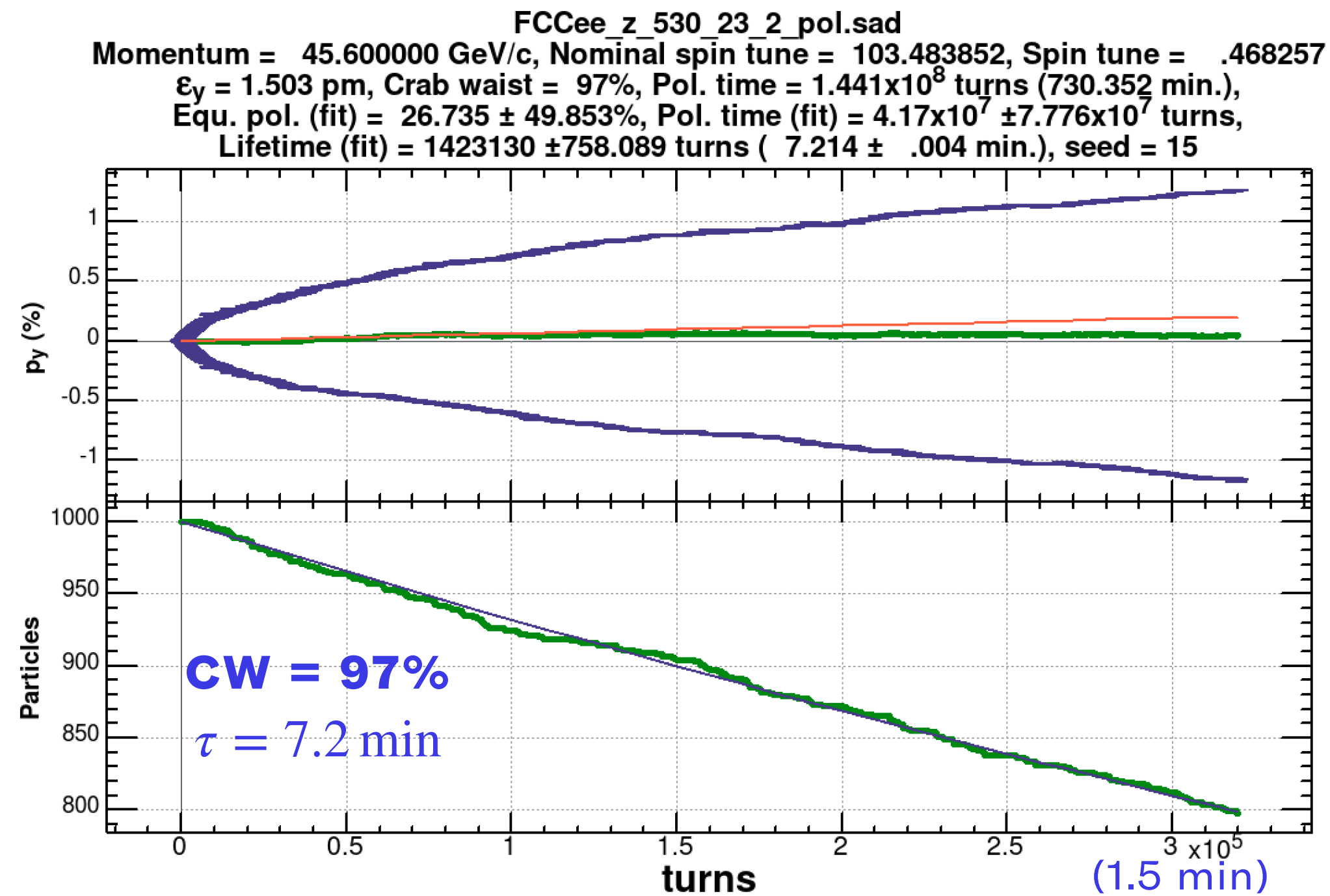


Beam energy	[GeV]	45.6	
Wiggler poles/ring (long/short)		-	48 / 24
Wiggler field	[T]	-	-0.1167 / 0.6
Wiggler length	[m]	-	1.29 / 0.43
Energy loss / turn	[MeV]	39.3	54.8
Horizontal emittance ϵ_x	[nm]	0.702	0.563
Vertical emittance ϵ_y	[pm]	0.426	0.305
Energy spread (SR) σ_δ	[%]	0.040	0.137
Bunch length (SR) σ_z	[mm]	4.5	15.7
Synchrotron tune $4Q_s$		0.0370	0.0359
Long. damping time	[turns]	1160	830
Polarization time	[min]	11887	730
RF acceptance	[%]	1.61	1.37

- The parameters for the pol. wigglers follow CDR.
- It is interesting that the resulting beam parameters such as σ_z , σ_ϵ become very similar to those of colliding bunches with beamstrahlung:

Energy spread (SR/BS) σ_δ	[%]	0.038 / 0.132
Bunch length (SR/BS) σ_z	[mm]	4.38 / 15.4

Tracking simulation for beam lifetime (+polarization)



- Tracking simulations have been performed for Z lattices with pol. wigglers, with solenoid with the latest 4 IP optics.
- The vertical emittance is generated by random vertical misalignments of arc sextupoles. The associated orbit distortion and β -beats are small. This should be almost the best situation.
- 1000 particles, SR in all magnets, no beam-beam.
- An ideal tapering.
- For the initial condition, each particle has zero vertical polarization with a random pol. angle in x-z plane.
- The tracking takes about 1 day on hpc-batch for one sample, for about 3×10^5 turns.

Beam lifetime with pol. wigglers



Wiggler & Solenoid		ON					
Vertical emittance	[pm]	1.5					
β_x^*	[m]	0.1			0.15		
Sexts optimization ^a		SC		SW		C	
Crab waist	[%]	97	0	97	0	97	0
Lifetime	[min]	7.2	40.2	4.5	53.9	15	1800

^aincluding S: solenoid, C: crab 97%, W: pol. wigglers.

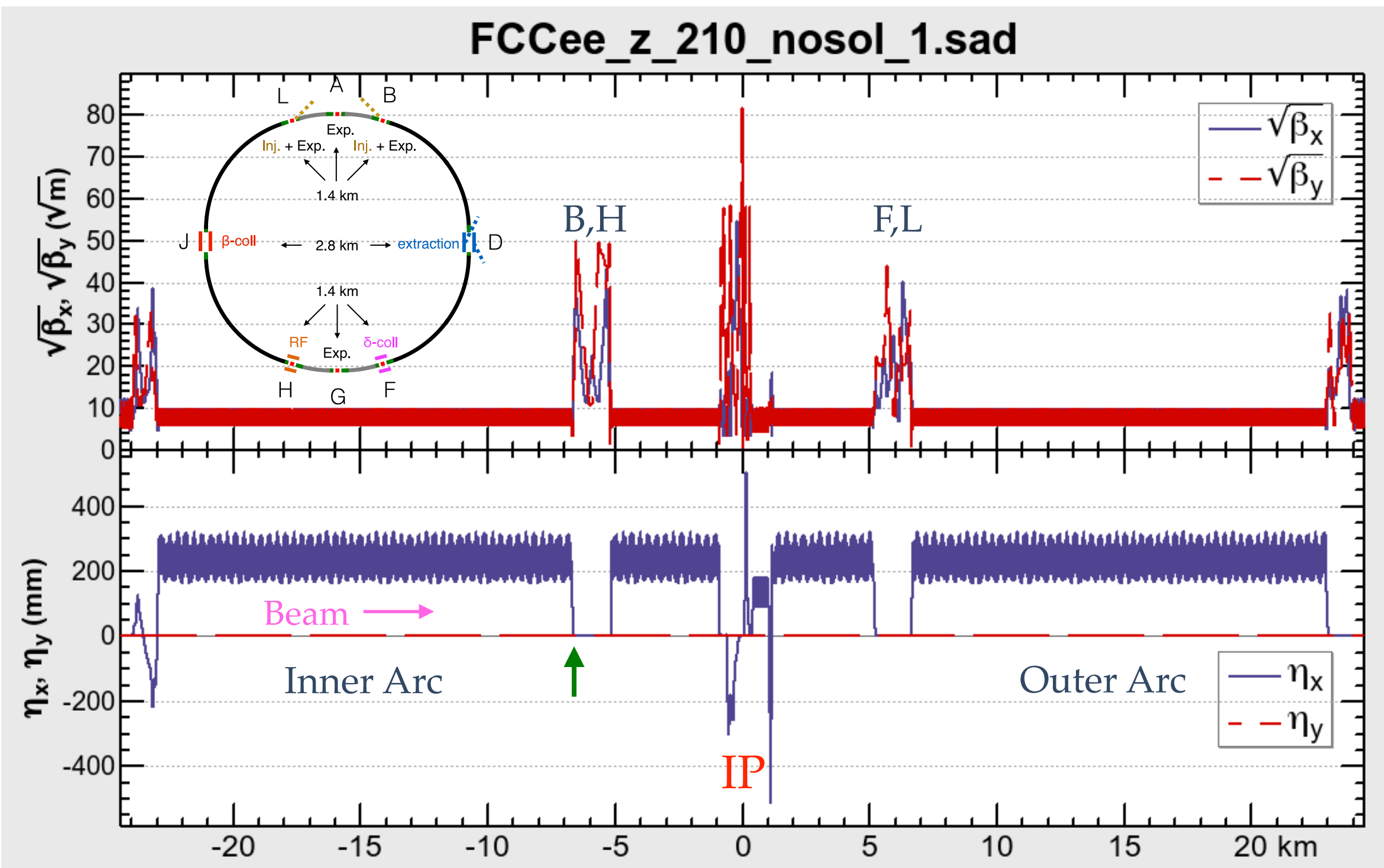
- The polarization wiggler has an impact on the beam lifetime.
- The $\beta_x^* = 10$ cm optics is more affected than the $\beta_x^* = 15$ cm optics.
- Turning off the crab sexts improves the lifetime (S. Shatilov).
- The lifetime depends on the optimization of the sexts.
 - It will not be practical to switch the sextupole settings except crab sexts during an operation: Corrections are needed in the entire ring.
- However, the colliding beams will suffer, due to a similar energy spread as the wigglers. (The luminosity lifetime is 17 minutes at Z).

Placement of polarimeter

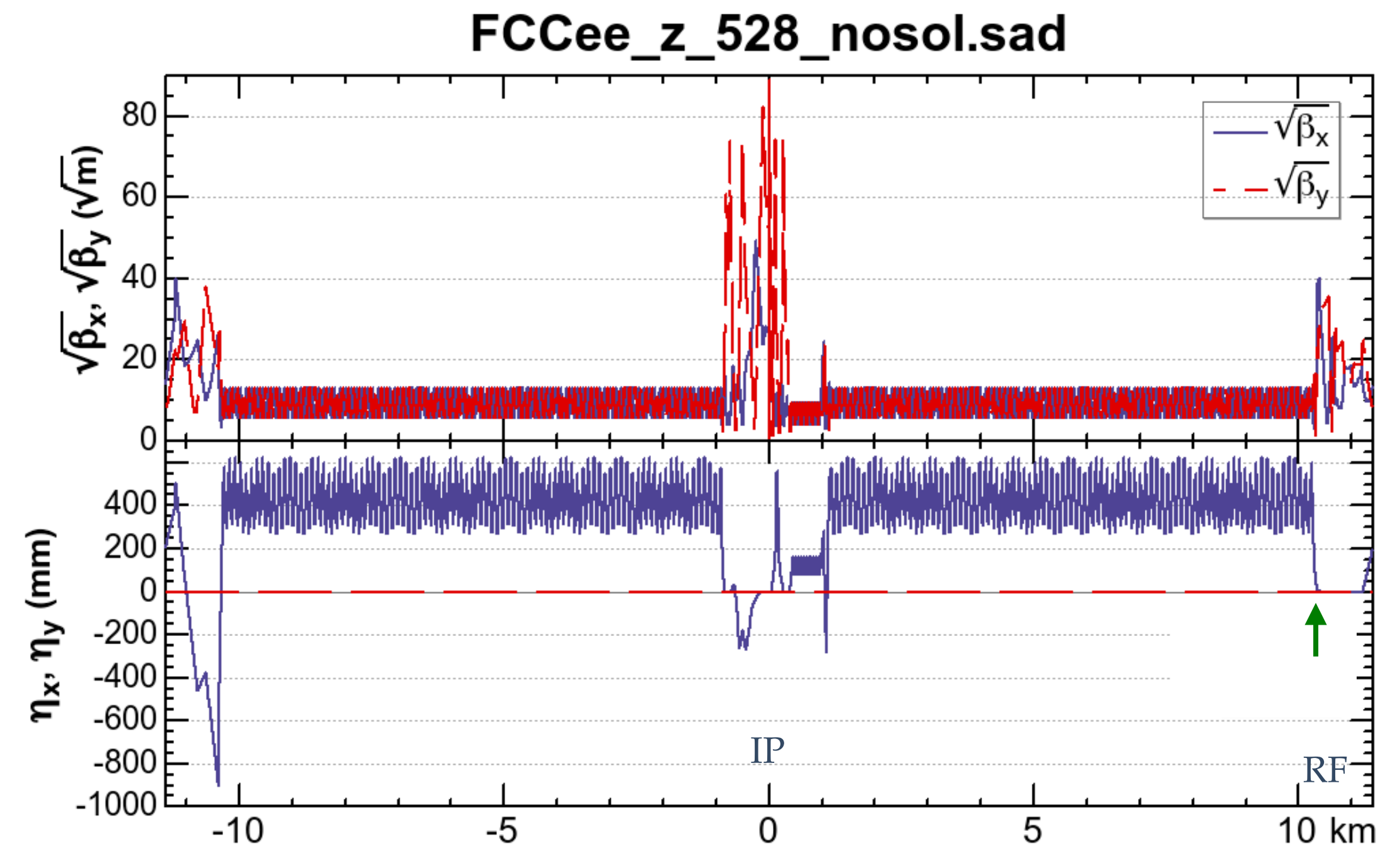


- CDR assigned one of the intermediate straight sections (B, F, H, L) for the polarimeter.
- Now with the new 4-IP compatible tunnel layout, *no such straight sections exist*.
- Candidates using a straight upstream of an IP have been looked first by M. Hofer as shown later.
- Another candidate may be the end of arc, upstream of an RF straight.

Location for the spectrometer (CDR)



4-IP compatible new layout

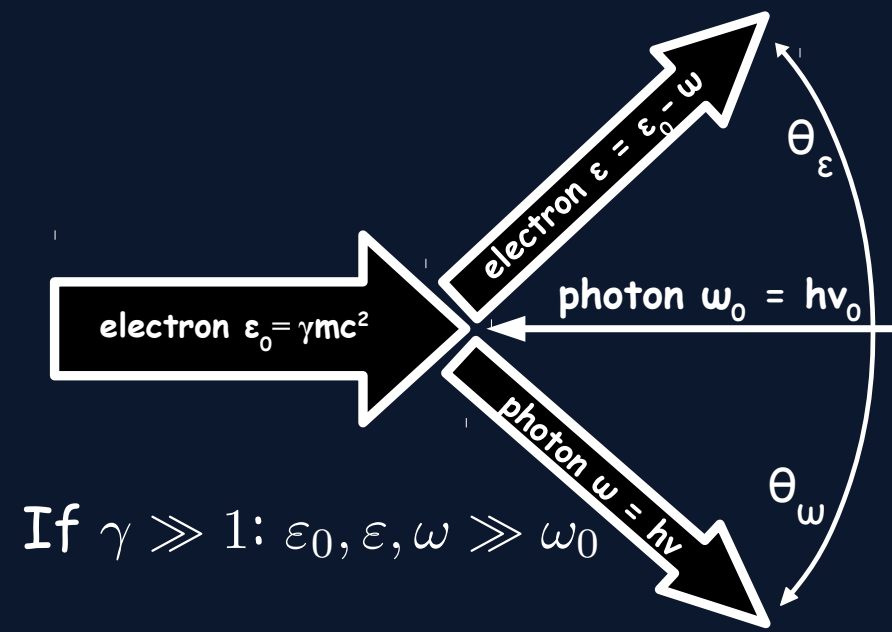


Requirements (N. Muchnoi)

First proposed by:
[Determination of the transverse polarization of high-energy electrons](#)
 V.N. Baier (Novosibirsk, IYF), Valery A. Khoze (Novosibirsk, IYF)
 Published in: Sov.J.Nucl.Phys. 9 (1969), 238-240, Yad.Fiz. 9 (1969), 409-41



Inverse Compton Scattering



Scattering parameter

$$u = \frac{\omega}{\varepsilon} = \frac{\theta_\varepsilon}{\theta_\omega} = \frac{\omega}{\varepsilon_0 - \omega} = \frac{\varepsilon_0 - \varepsilon}{\varepsilon}$$

is in the range

$$u \in [0, \kappa], \text{ where } \kappa = \frac{4\omega_0\varepsilon_0}{(mc^2)^2} \sin^2(\alpha/2)$$

$$\kappa \simeq 1.63 \text{ if } \varepsilon_0 = 45.6 \text{ GeV}, \omega_0 = 2.33 \text{ eV.}$$

$$\text{Scattering angles: } \theta_\omega = \frac{1}{\gamma} \sqrt{\frac{\kappa}{u} - 1}; \quad \theta_\varepsilon = \frac{u}{\gamma} \sqrt{\frac{\kappa}{u} - 1}.$$

Note: $\max(\theta_\varepsilon) = 2\omega_0/mc^2$ (when $u = \kappa/2$). It is $\simeq 10 \mu\text{rad}$ for green light.

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Scattered electrons

$$\text{Beam bending angle: } \vartheta_0 \equiv \gamma\theta_0 = \frac{\int B_\perp(l) dl}{mc/e}, \quad \frac{mc}{e} = 1.704509024 \cdot 10^{-3} [\text{T m}].$$

$$\text{A scattered electron with energy } \varepsilon = \frac{\gamma mc^2}{1+u} \text{ bends more: } \vartheta(u) = \vartheta_0(1+u).$$

Electron angles by scattering and bending, relative to ϑ_0 , in units of $1/\gamma$:

$$\begin{aligned} \vartheta_x &\equiv \vartheta(u) - \vartheta_0 + \gamma\theta_x = u\vartheta_0 - u\sqrt{\kappa/u - 1} \cos(\varphi), \\ \vartheta_y &\equiv \gamma\theta_y = -u\sqrt{\kappa/u - 1} \sin(\varphi). \end{aligned}$$

Two solutions for u :

$$u^\pm = \frac{\kappa + 2\vartheta_0\vartheta_x \pm \sqrt{\kappa^2 - 4(\vartheta_x^2 + \vartheta_y^2(1 + \vartheta_0^2) - \kappa\vartheta_0\vartheta_x)}}{2(1 + \vartheta_0^2)}.$$

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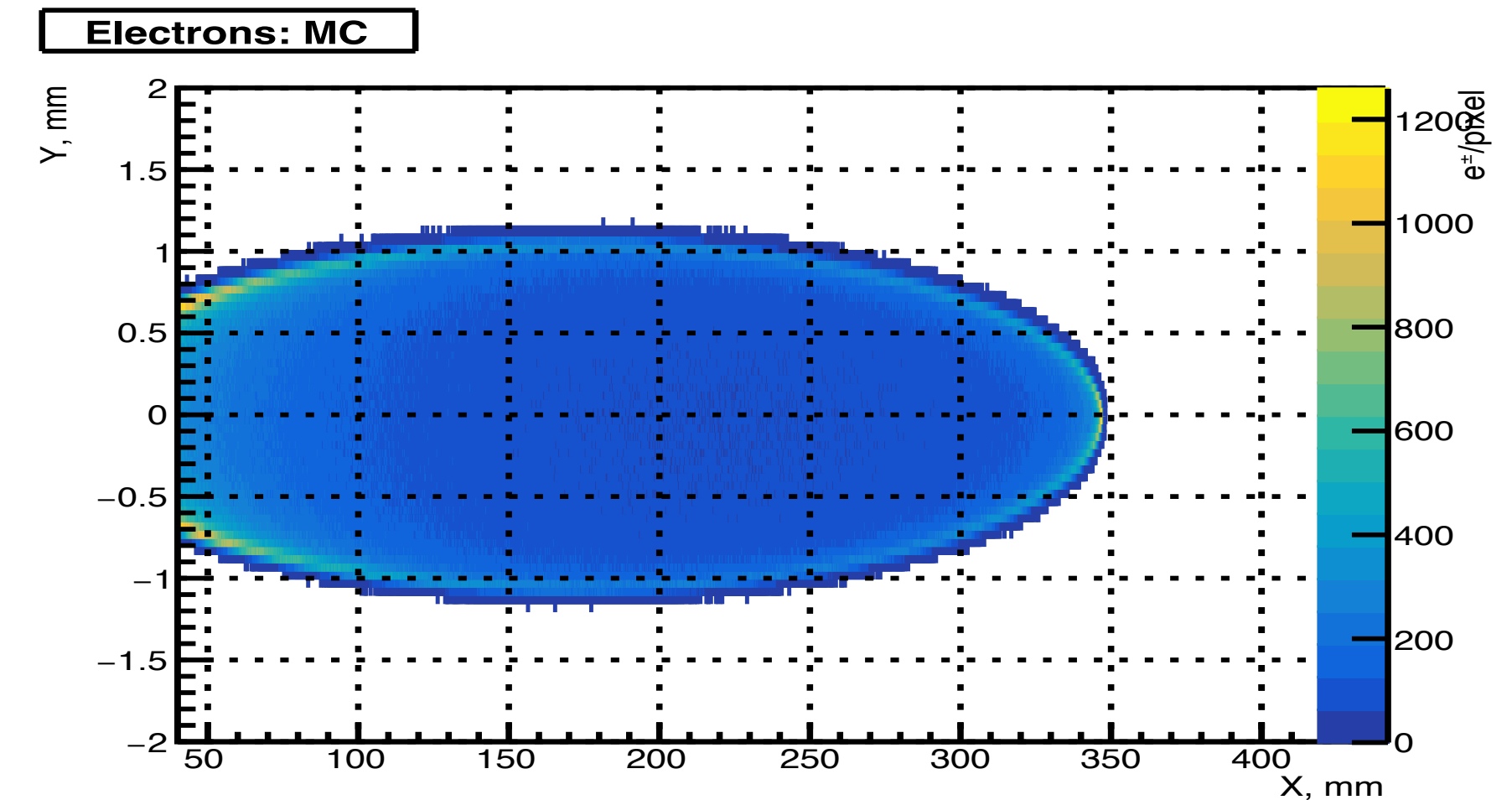
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According to above expressions by N. Muchnoi, the maximum deflected angle for electrons is written as

$$\Delta\theta_{x,\max} \approx u_{\max}\theta_0 = \kappa\theta_0, \quad \kappa \approx 1.63 @ 45.6 \text{ GeV}.$$

If we need a 35 cm horizontal spread of electrons as shown by Muchnoi, at $L = 100 \text{ m}$ downstream of the laser hit point, we need

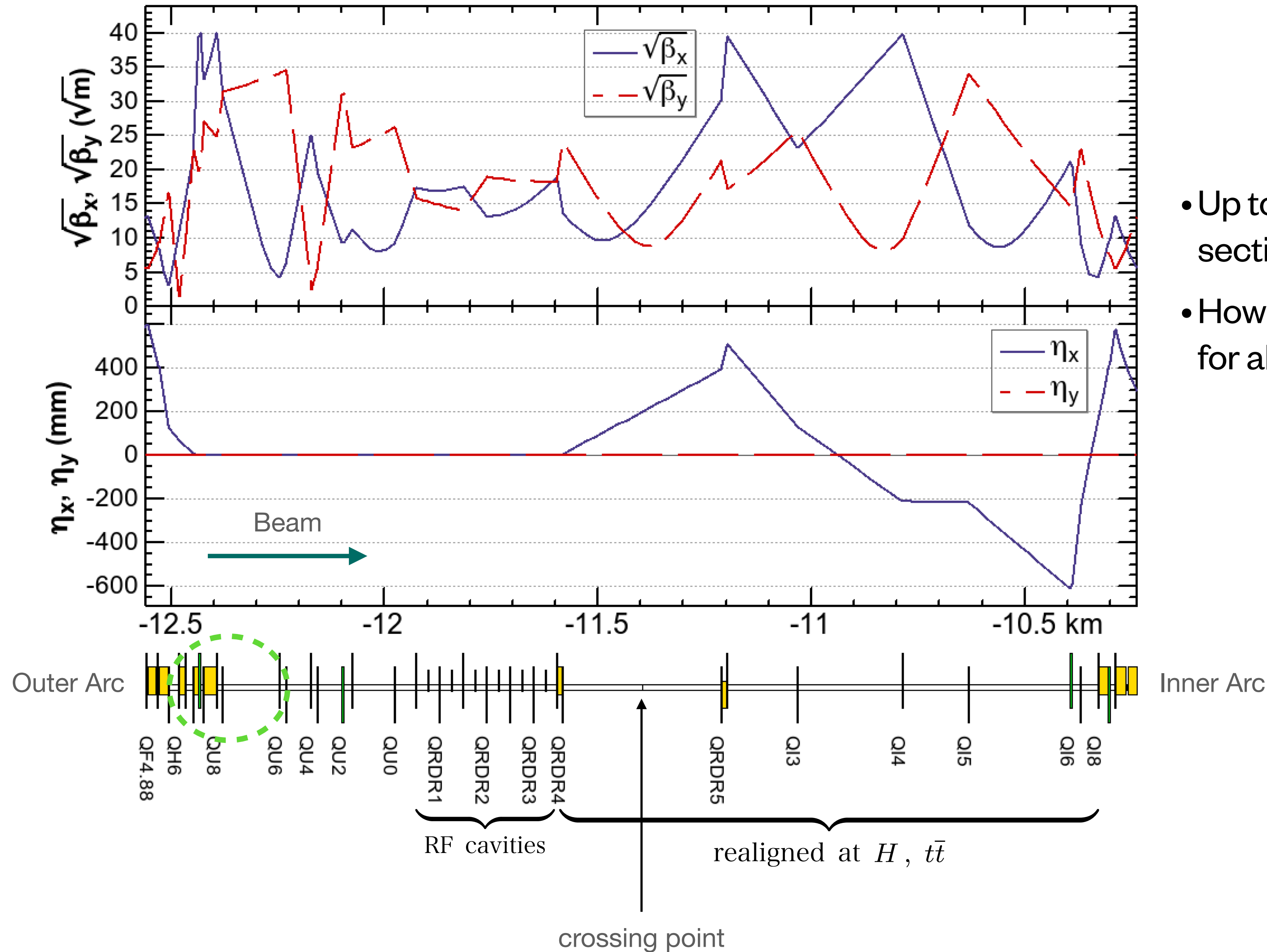
$$\theta_0 = (35 \text{ cm})/(\kappa L) = 2.14 \text{ mrad}.$$



Beam optics of the RF section at Z, W

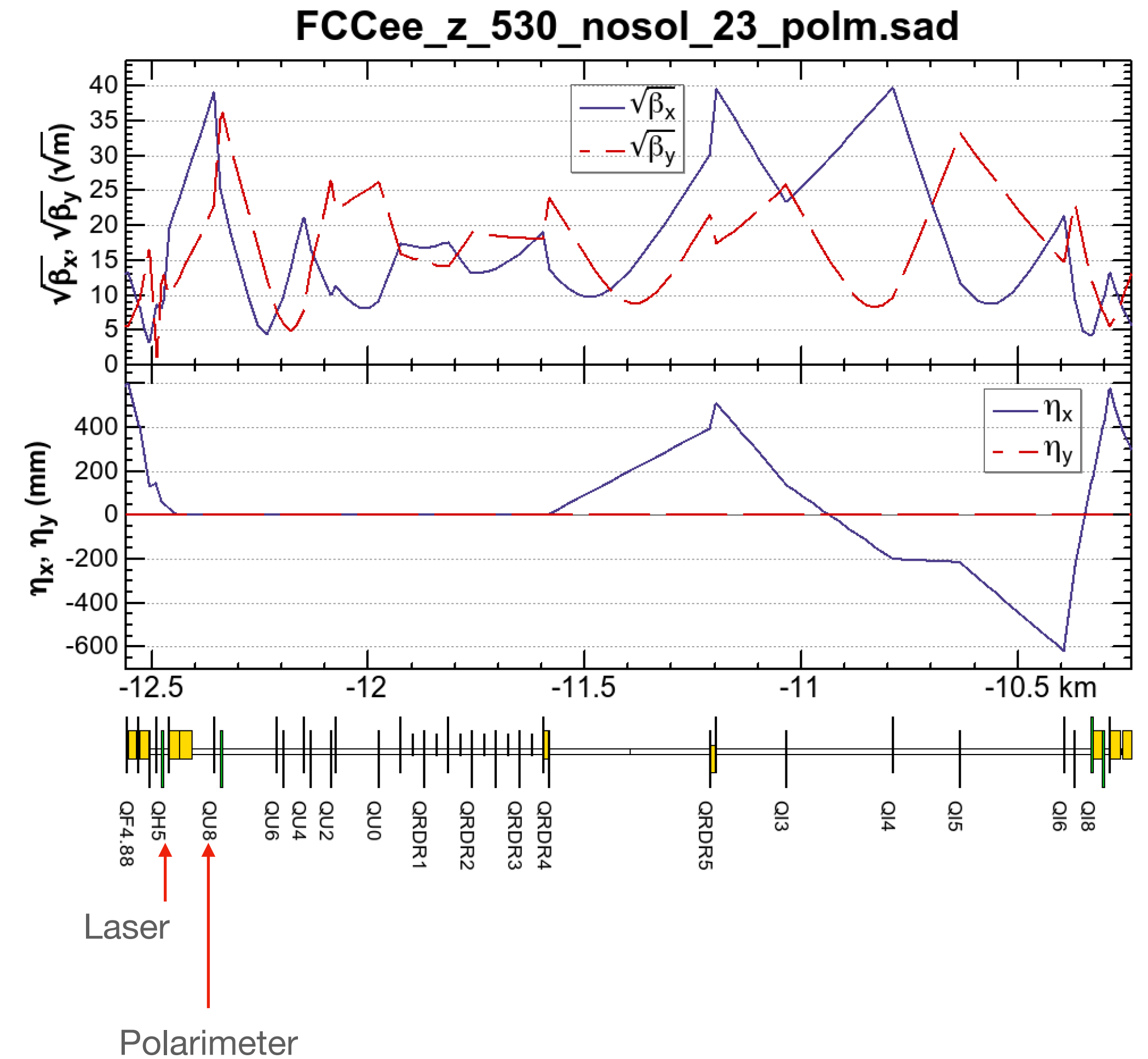
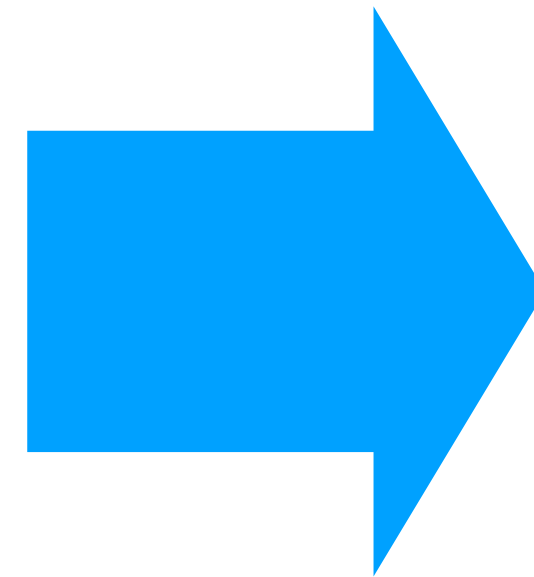
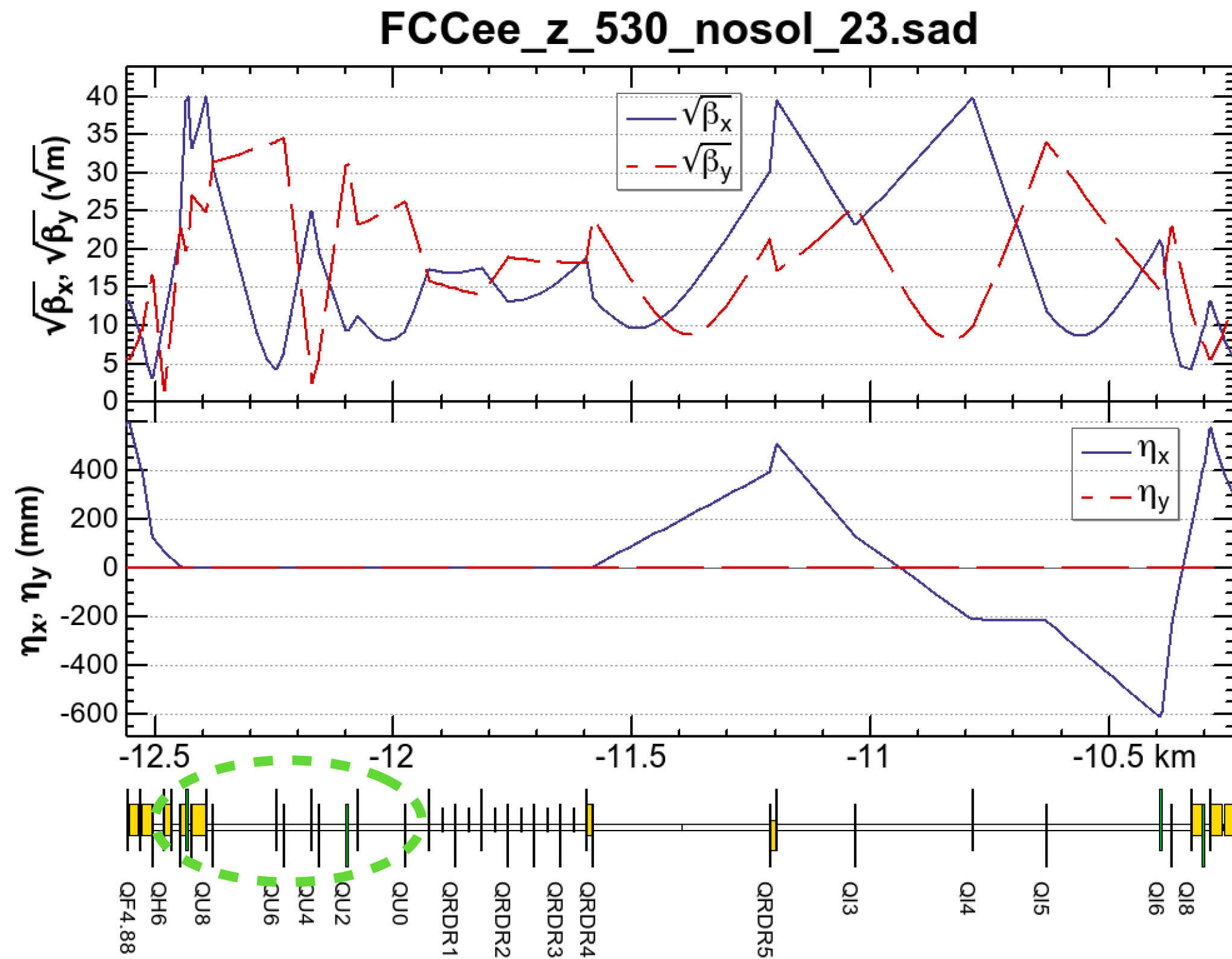


FCCee_z_530_nosol_23.sad



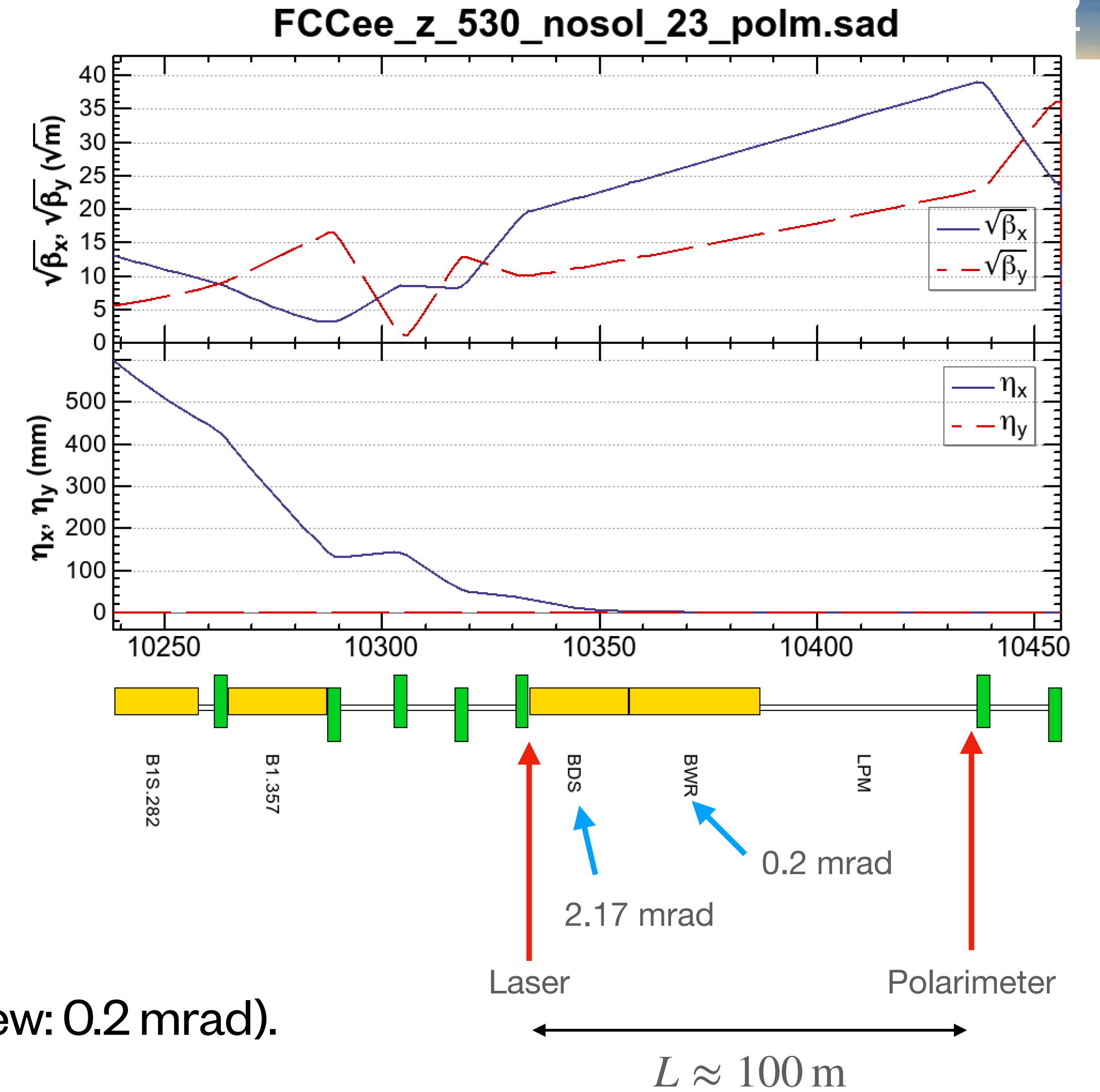
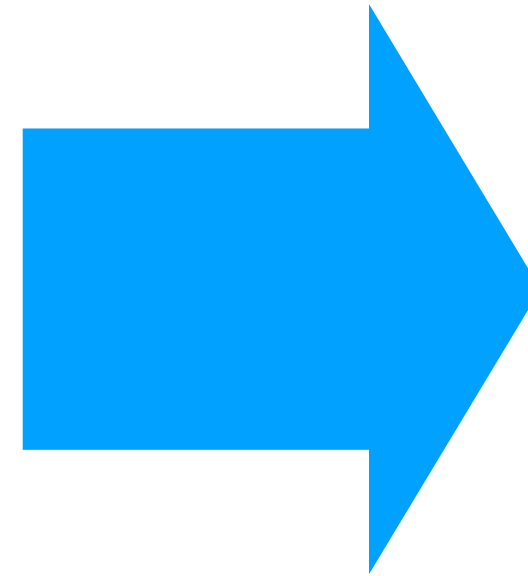
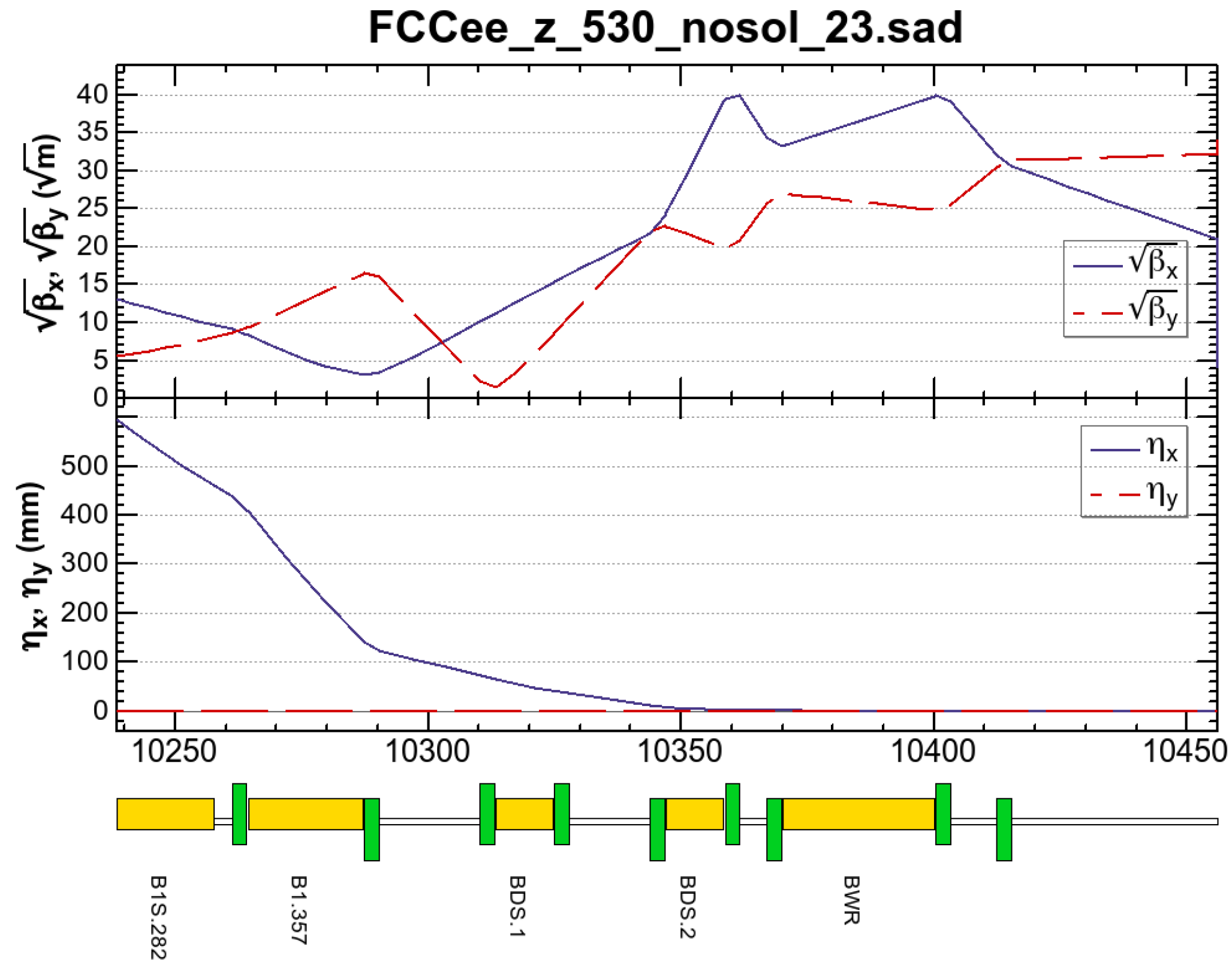
- Up to H , cavities are filled in only one of the RF sections.
- However, we want to make the optics identical for all sections to preserve the periodicity.

Tweak the RF section for polarimeter



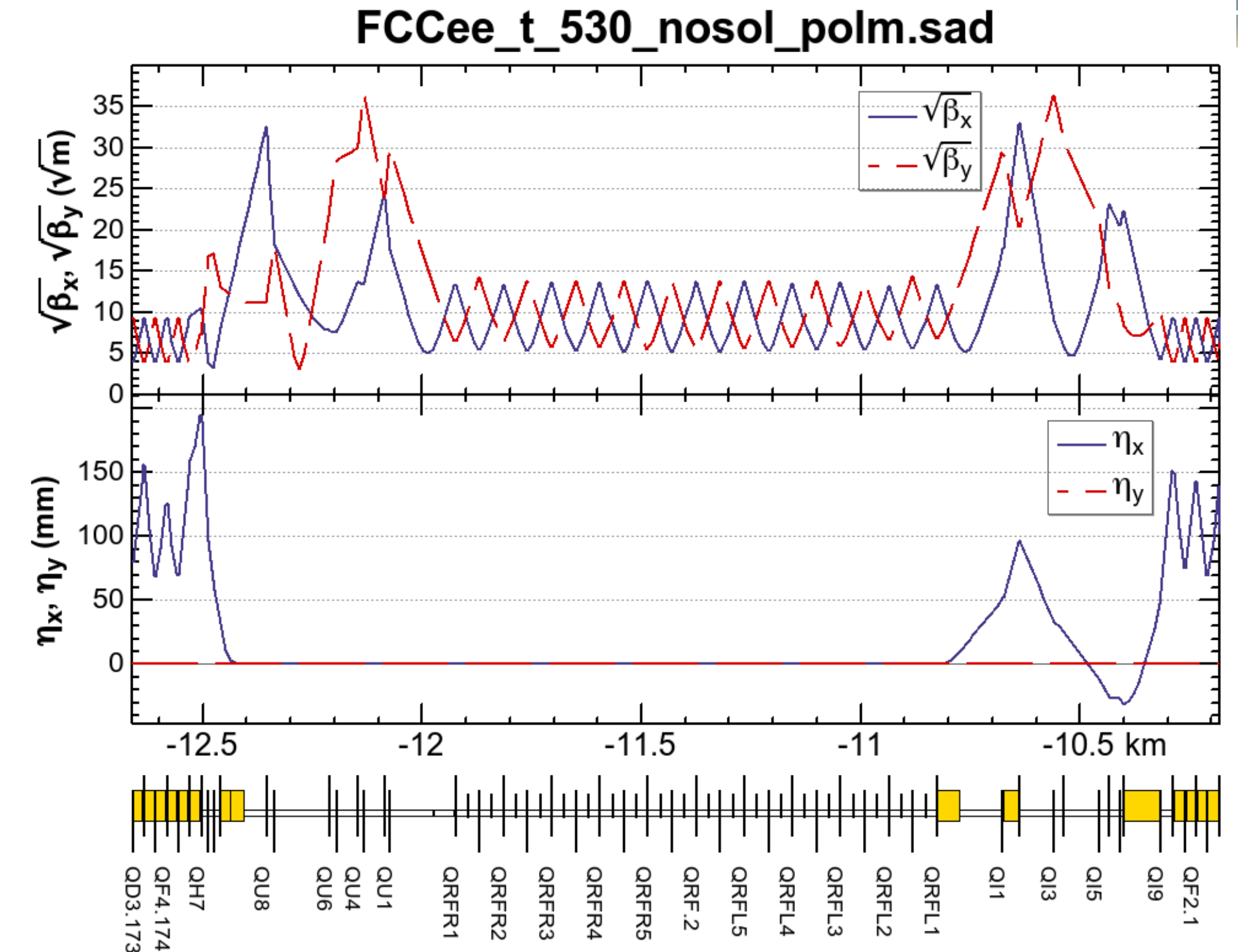
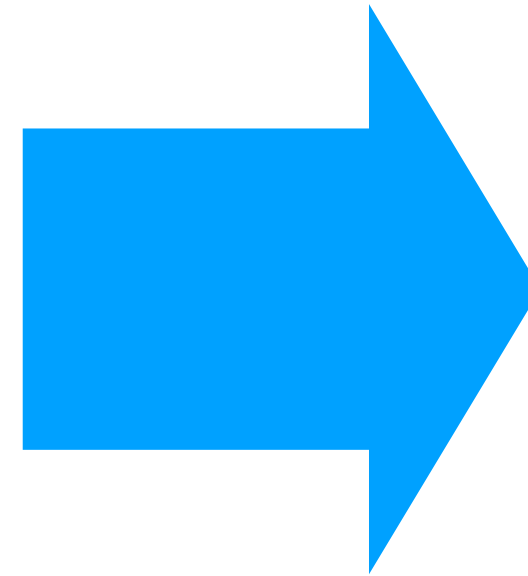
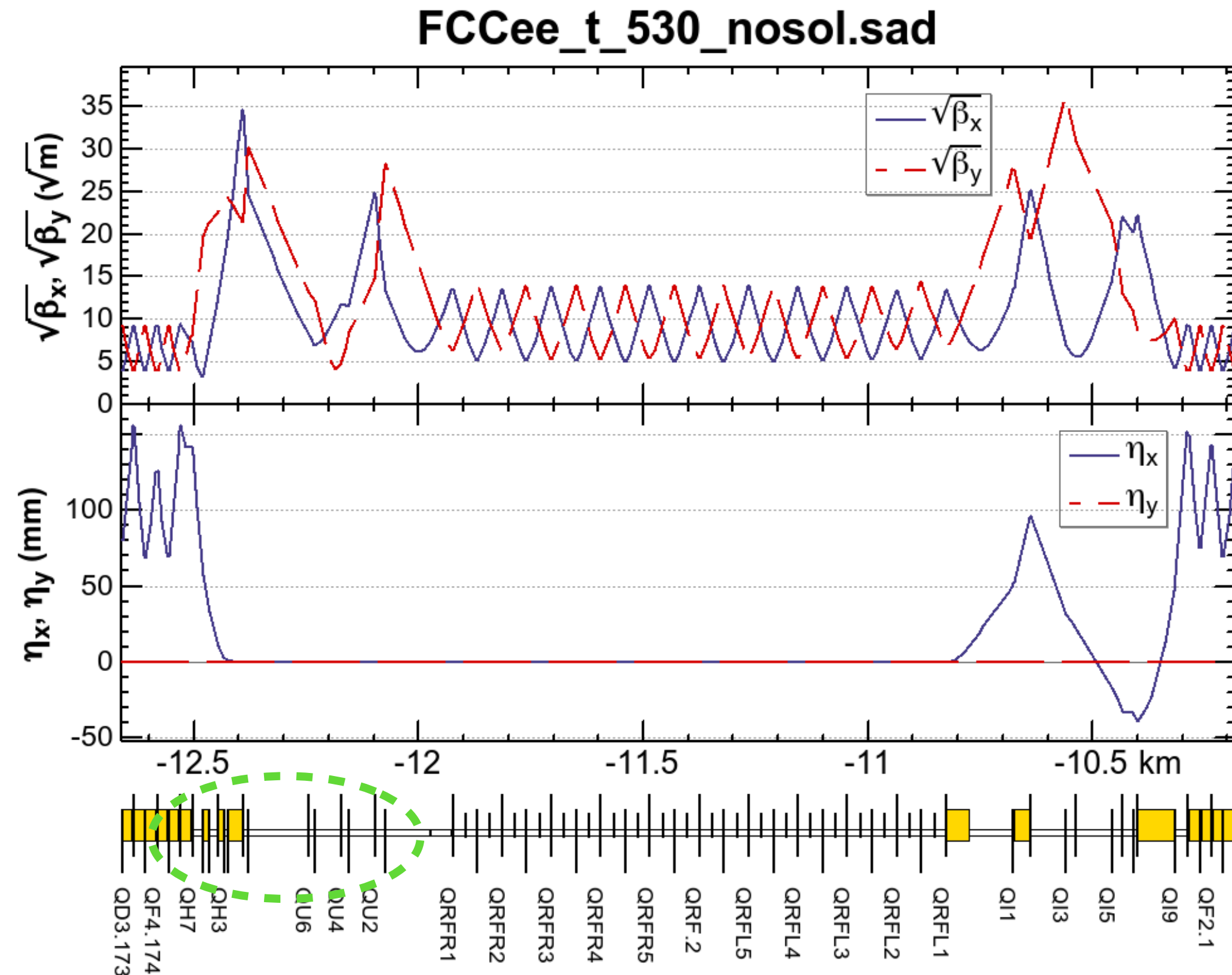
- The upstream of the RF sections is rearranged to install the polarimeter.
- The exact ring geometry is not yet precisely adjusted.

Closer look



- BDS: dispersion suppressor dipole (2.17 mrad total).
- BWR: weak bend to avoid SR hit on RF cavities (old: 0.1 mrad, new: 0.2 mrad).
- Optics for $H/t\bar{t}$ should have the compatible layout of components.

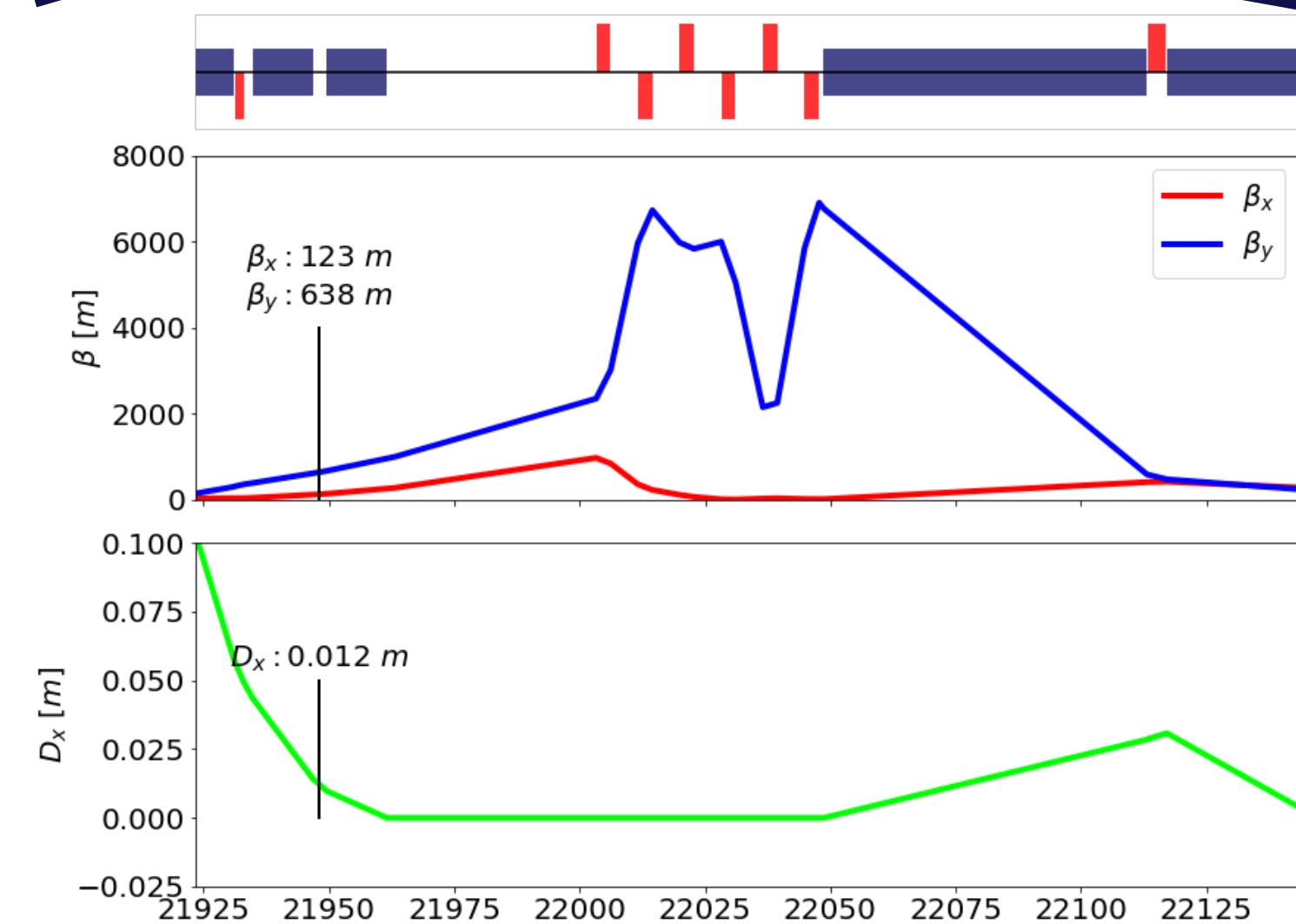
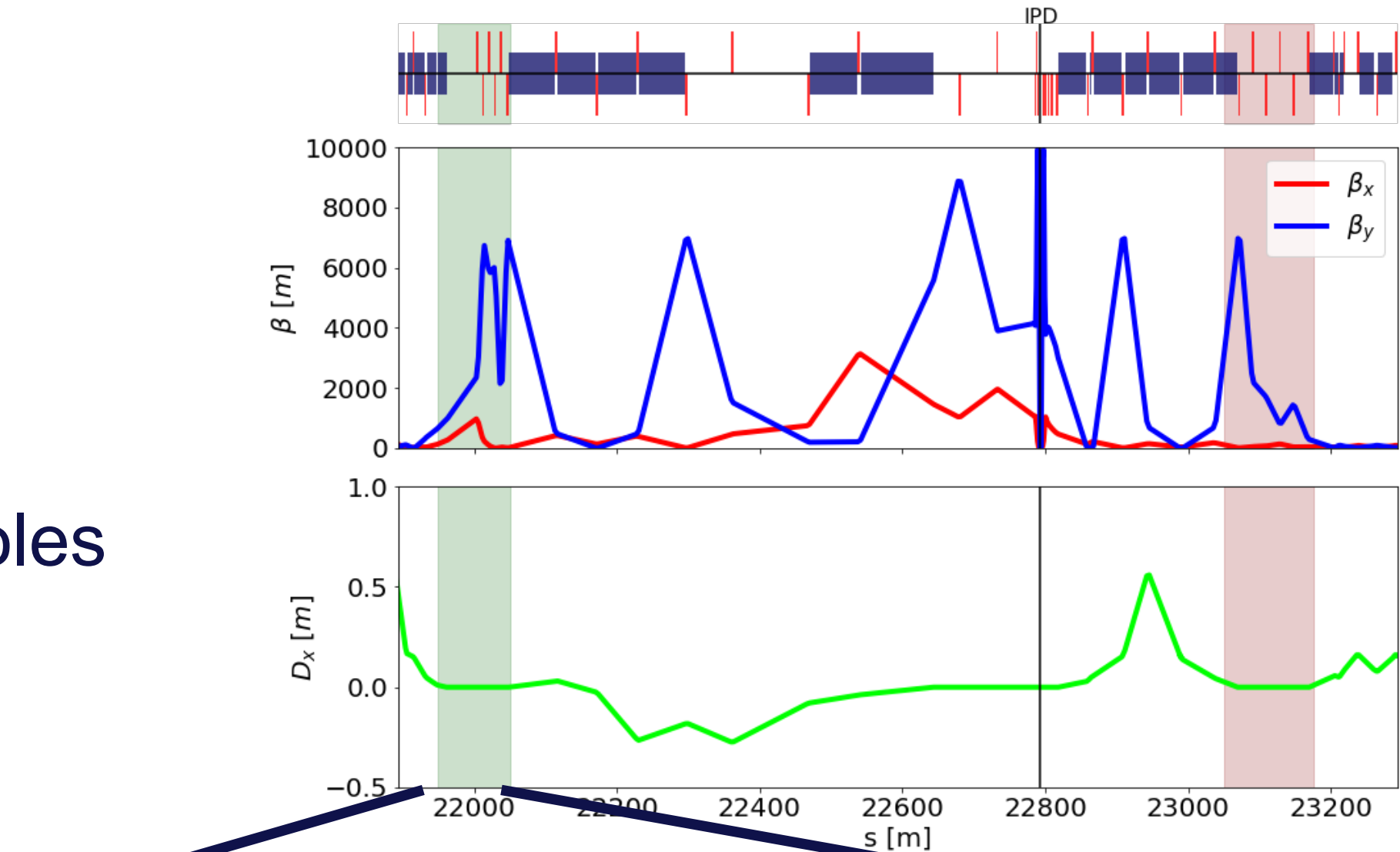
Optics for $H/t\bar{t}$



- The modified lattice is indeed compatible for $H/t\bar{t}$.
 - No need to move quads upstream of the RF cavities, except one (QU0) located at the electrostatic separator.

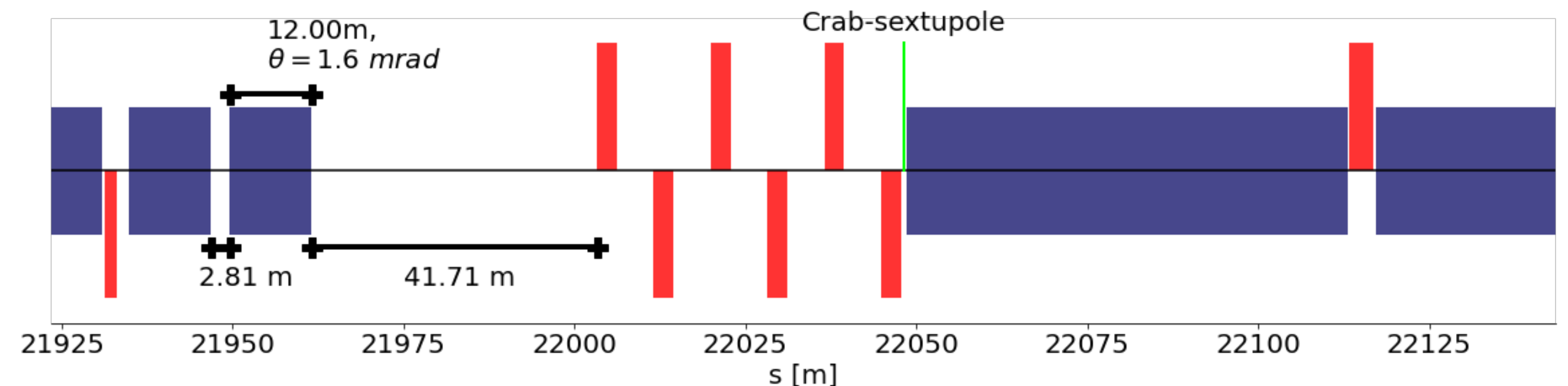
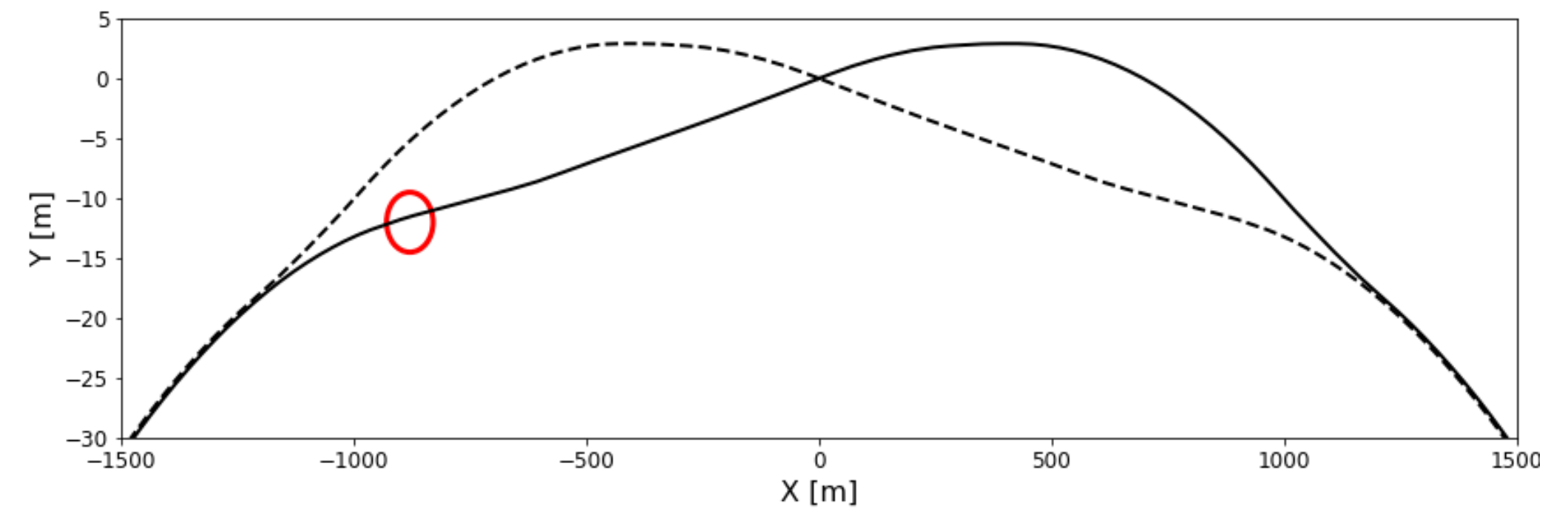
Polarimeter in 4-IP lattice

- Modification compatible with Z and $t\bar{t}$ optics
- Phase advance between IP and first arc sextupoles is partly used to optimize dynamic aperture
 - These changes could have implications on optics matching and Dynamic aperture
- More drift space could be recovered by moving crab sextupole and dipoles closer to IP
 - Change in the geometry could affect background in the detector



Polarimeter in 4-IP lattice

- By moving a few quadrupoles, free space after spectrometer dipole created
 - Drift space is less than half of baseline solution
 - Sufficient space on either side for detectors
- Shorter drift space not impossible, but changes required [see [ref](#)]:
 1. Change laser wavelength from 532nm to 266nm
 2. Changes on the detector (smaller pixels)



Summary



- The effect of polarization wigglers placed downstream of each IP has been looked at by particle trackings.
 - A more or less realistic field of the detector/compensation solenoids are included.
- Impact on the beam lifetime due to the large energy spread caused by the wigglers can be an issue.
 - For pilot bunches, it can be recovered by turning off the crab sextupoles.
 - However, the lifetime for colliding beams may matter, as they have the similar energy spread by the beamstrahlung as the wigglers.
 - The effect is larger in $\beta_x^* = 10$ cm optics than $\beta_x^* = 15$ cm.
 - It can be worsened by machine errors.
- There are at least two candidates for the location of the polarimeter:
 - Upstream in the RF straight section:
 - The measurement is done through a weak bend to protect the RF.
 - The separation of two beams must be compatible with requirements from the RF.
 - Upstream of an IP:
 - No interference with the other beam.
 - Relatively short available space and small bending angle.
 - May need a short wavelength laser.
 - Otherwise pushing components toward the IP by ~ 50 m will be necessary.