

2 Cold Atoms in Space:

3 Community Workshop Summary and Draft Road-Map

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50 **ABSTRACT:**

51 We summarize the discussions at a virtual Community Workshop on Cold Atoms in Space concerning
52 the status of cold atom technologies, the prospective scientific and societal opportunities offered by
53 their deployment in space, and the developments needed before cold atoms could be operated in space.
54 The cold atom technologies discussed include atomic clocks, quantum gravimeters and accelerometers,
55 and atom interferometers. Prospective applications include metrology, geodesy and measurement of
56 terrestrial mass change due, e.g., to climate change, and fundamental science experiments such as tests
57 of the Einstein equivalence principle, searches for dark matter, measurements of gravitational waves
58 and tests of quantum mechanics. We review the current status of cold atom technologies and outline
59 the requirements for their space qualification, including the development paths and the corresponding
60 technical milestones, and identifying possible pathfinder missions to pave the way for missions to
61 exploit the full potential of cold atoms in space. Finally, we present a first draft of a possible road-
62 map for achieving these goals, that we propose for discussion by the interested cold atom, Earth
63 observation and other prospective scientific user communities.

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128 1 Preface

129 This document contains a summary of the **Community Workshop on Cold Atoms in Space** [1]
130 that was held virtually on September 23 and 24, 2021. The purpose of this community workshop was
131 to discuss objectives for a cold atom quantum technology development programme coordinated at the
132 Europe-wide level, and to outline a possible community road-map and milestones to demonstrate the
133 readiness of cold atom technologies in space, as proposed in the Voyage 2050 recommendations [2],
134 and in synergy with EU programmes.

135 The Senior Science Committee (SSC) set up by the ESA Director of Science to advise on the space
136 science programme for the period 2030-2050 drew attention to the potential of cold atom technology
137 in fundamental physics and planetary science as well as in navigation, timekeeping and Earth Obser-
138 vation. The SSC set out a plausible programme of technology development in the Voyage 2050 report
139 that would prepare cold atom payloads for evaluation by the ESA science committees on scientific
140 merit alone, without technical concerns about robustness for the space environment. One aim of the
141 workshop in September 2021 was to engage the cold atom community in defining possible science
142 payloads that might be used to establish a recognised pathway towards the use of cold atoms in the
143 ESA science programme.

144 This community workshop brought together representatives of the cold atom, astrophysics, cos-
145 mology, fundamental physics and earth observation communities to participate in shaping this devel-
146 opment programme. It built upon one organised two years ago [3], which reviewed the landscape of
147 present and prospective cold atom experiments in space. Subsequently, several White Papers were
148 submitted [4–12] in response to the Voyage 2050 call, which outlined possible ultimate goals and re-
149 viewed experiments and technical developments underway that could help pave a way towards these
150 goals.

151 One of the main goals of this workshop was to prepare a Community road-map supported by
152 the cold atom community and the potential user communities interested in its science goals. This
153 Community road-map outlines technological milestones and refines the interim and long-term scientific
154 goals.

155 Sections 2 to 7 summarise the 2-day Community Workshop, while in Section 8 we outline the
156 corresponding Community road-map.

157 2 Introduction

158 Quantum physics was developed in Europe in the first half of the 20th century. In the second half,
159 the first “quantum revolution” took place and was the engine of the main technological and societal
160 transformations in recent decades considering, e.g., solid-state electronics and hence all information
161 and computing technologies. It also enabled the space era thanks, e.g., to onboard semiconductor
162 technologies (solar cells, avionics, communication systems radars, detectors, etc.). Similarly, the first
163 half of the 21st century is being deeply impacted by the second “quantum revolution”, exploiting
164 quantum phenomena so far not applied outside the laboratory: macroscopic quantum coherence,
165 superposition, entanglement, etc.

166 Atomic quantum sensors are a newly-emerging technology of unparalleled accuracy and precision.
167 Spaceborne quantum inertial sensors (e.g., accelerometers, gravimeters, gyroscopes, etc.) are today
168 the most advanced sensing technologies that benefit from this revolution, exploiting matter-wave inter-
169 ferometry with Bose-Einstein condensates, using atom clouds cooled below nanoKelvin temperature.
170 For example, whereas classical accelerometers suffer from high noise at low frequencies, cold atom in-
171 terferometers (CAI) are highly accurate over the entire frequency range and do not need any external
172 calibration.

173 In the past twenty years, gravimetry missions have demonstrated a unique capability to monitor
174 major climate-related changes of the Earth directly from space - quantifying the melt of large glaciers
175 and ice sheets, global sea level rise, continental drought, major flooding events, and also the effects
176 of large earthquakes and tsunamis. Adding to fundamental knowledge of the Earth, a quantum
177 gravimetry mission for climate will provide essential climate variables (ECVs) of unprecedented quality
178 for ground water, mass balance of ice sheets and glaciers, heat and mass transport, as demonstrated
179 – within the limits of past technology – by successful missions like GOCE [13] and GRACE-FO [14].
180 A combination of classical sensors with CAI or, at a later stage, a full quantum sensor will bring the
181 Quantum Mission for Climate to a sensitivity that will open many applications and satisfy user needs
182 with respect to water management and hazard prevention. In this connection, we take special note of
183 the adoption of Quantum Technology for Earth Observation by the European Commission, notably
184 (but not exclusively) in the Horizon Europe programme, under the thrust of Commissioner T. Breton,
185 and of the inclusion of Quantum Technology in the ESA Agenda 2025.

186 Quantum Technology on Earth has revolutionised the measurement of time since the first atomic
187 clocks in the 1950’s, and these now provide the fundamental time frame across the globe. In space,

188 atomic clocks have widespread applications such as satellite-based navigation systems (GPS, GALILEO).
189 Terrestrial clocks based on atomic transitions are now reaching an uncertainty on the order of 10^{-18} ,
190 a level at which a change of height in the Earth’s gravitational field of 1 cm would be detectable as
191 a gravitational redshift. This sensitivity brings both challenges and opportunities. The challenge for
192 terrestrial clocks will be that changes in the local gravitational potential, either by human activity or
193 by alterations in the local water table will destroy the stability of the clock. This issue will certainly
194 drive the siting of such clocks in space, with the implication that space qualification of the quantum
195 technology will be essential for future development. The availability of such sensitive technology in
196 space also offers significant opportunities to explore many aspects of fundamental physics.

197 Mounted on a space platform in a highly eccentric orbit, a sensitive atomic clock would provide
198 an ideal laboratory to test General Relativity beyond current precision as the spacecraft experiences
199 varying gravitational potentials around the orbit. This is a test that is at the heart of General
200 Relativity and all metric theories of gravitation and space-time.

201 Another fundamental aspect of the EEP is the Universality of Free Fall (UFF) tested since the
202 days of Galileo with ever increasing accuracy. Quantum gravimetry using atom interferometers in
203 space will allow pushing tests of UFF to new frontiers, with the potential of unveiling new physics
204 beyond the Standard Model. These experiments represent one of the best ways of exploring the
205 unknown theoretical interface between quantum physics and our best-tested theory of gravity, General
206 Relativity.

207 The deployment of cold atom technology in space will also enable many other sensitive experi-
208 ments in fundamental physics, cosmology and astrophysics, such as searches for ultralight dark matter
209 particles, measurements of gravitational waves from the mergers of massive black holes and phenomena
210 in the early Universe, and ultrasensitive probes of quantum mechanics.

211 The commonality of some subsystems between atomic clocks, gravimeters and fundamental physics
212 experiments means that a well-planned programme of technical development should lead to the avail-
213 ability from space of all these applications in fundamental science, Earth Observation, time keeping
214 and navigation.

215 **3 Atomic Clocks Review**

216 **3.1 Scientific and societal opportunities**

217 **3.1.1 Fundamental science**

218 High-stability and -accuracy atomic clocks combined with state-of-the-art time and frequency links
219 can be used to measure tiny variations in the space-time metric and test the validity of the Einstein’s
220 Equivalence Principle.

221 As predicted by General Relativity, gravity influences the flow of time. When identical clocks
222 experiencing a different gravitational potential are compared by exchanging timing signals, a relative
223 frequency difference proportional to the difference of the gravitational potential at the location of the
224 clocks can be measured. The effect, known as gravitational redshift, has been tested in 2018 to an
225 uncertainty of about 2×10^{-5} [15, 16] by using the clocks on-board the Galileo 5 and 6 satellites. The
226 ACES (Atomic Clock Ensemble in Space) mission [17–19] will perform an absolute measurement of the
227 redshift effect between the PHARAO clock on-board the International Space Station (ISS) and clocks
228 on Earth, improving this limit by an order of magnitude. Optical clock missions on highly elliptical
229 orbits around the Earth or cruising towards the Sun are expected to improve redshift tests by several
230 orders of magnitude and to measure higher-order relativistic effects to high precision.

231 Local Lorentz Invariance (LLI) postulates the independence of any local test experiment from
 232 the velocity of the freely-falling apparatus. Optical clocks can be used to provide very stringent
 233 test of Lorentz symmetry and the Standard Model Extension (SME) [20]. Distant Sr optical lattice
 234 clocks compared through optical fibre links have been used to constrain the Robertson-Mansouri-Sexl
 235 parameter to 1×10^{-8} by searching for daily variations of the relative frequency difference [21]. In [22],
 236 two Yb^+ clocks confined in two traps with quantization axis aligned along non-parallel directions are
 237 compared while the Earth orbits around the Sun. The absence of frequency modulations at the level
 238 of 1×10^{-19} made possible an improvement in the limits on the Lorentz symmetry violation parameter
 239 for electrons.

240 Local Position Invariance (LPI) can also be tested by comparing clocks based on different atomic
 241 transitions. According to LPI, the outcome of any local test experiment is independent of where
 242 and when it is performed in the Universe. Transition frequencies depend differently on the three
 243 fundamental constants: the fine structure constant α , the electron mass m_e/Λ_{QCD} (normalized to the
 244 QCD scale parameter), and the quark mass m_q/Λ_{QCD} . Therefore, comparing atomic clocks based
 245 on different transitions can be used to constrain the time variation of fundamental constants and
 246 their couplings to gravity. As an example, the comparison of two $^{171}\text{Yb}^+$ clocks based on the electric
 247 quadrupole and electric octupole transitions and two Cs clocks repeated over several years has recently
 248 improved the limits on the time variation of the fine structure constant and of the electron-to-proton
 249 mass ratio [23]. At the same time, using the annual variation of the Sun’s gravitational potential, it
 250 was possible to constrain the coupling of both constants to gravity.

251 Atomic clock networks can also be used to place bounds on Topological Dark Matter (TDM)
 252 models. TDM can be expressed as a scalar field that couples to fundamental constants, thus producing
 253 variations in the transition frequencies of atomic clocks at its passage. Cross-comparisons between
 254 atomic clocks connected in a network over large distances can be used to place bounds on the time
 255 variation of the three fundamental constants and determine exclusion regions for the effective energy
 256 scale (inverse of the coupling strength) of the dark matter field as a function of its Compton wavelength
 257 [24, 25]. Clock networks providing redundant measurements are a powerful tool to control systematic
 258 effects and confirm any detection above the noise threshold.

259 Optical clocks have also been proposed for gravitational wave detection [4, 5, 26]. A pair of
 260 clocks in drag-free satellites separated by a long-distance baseline share the interrogation laser via
 261 an optical link. The clocks act as narrow band detectors of the Doppler shift on the laser frequency
 262 due to the relative velocity between the satellites induced by the incoming gravitational wave. The
 263 atom interrogation sequence on the clock transition can be controlled, enabling precise tuning of the
 264 detection window over a wide frequency interval without loss of sensitivity. A frequency range between
 265 about 10 mHz and 10 Hz can be covered, thus bridging the gap between space-based and terrestrial
 266 optical interferometers, as discussed in more detail in Section 5.

267 3.1.2 Metrology

268 The basic ‘second’ in the international system of units SI is the quantity that is fixed with by far the
 269 lowest uncertainty of all units. This is done by primary frequency standards (laser-cooled Cs fountain
 270 clocks) operated at the National Metrology Institutes. Global time scales rely on the comparison
 271 of such high-performance atomic clocks connected in a global network. The Bureau International
 272 des Poids et Mesures (BIPM) generates the International Atomic Time (TAI) based on the cross-
 273 comparison of the best primary frequency standards and, more recently, also optical clocks worldwide.
 274 TAI defines the proper time at the geoid and it is a key ingredient for the generation of UTC (Coor-
 275 dinated Universal Time), recognized today as the official timescale worldwide.

276 Since optical clocks already outperform the primary frequency standards that operate in the mi-
277 crowave domain (see Section 3.2), the international metrology community represented by the Comité
278 International des Poids et Mesures (CIPM) and its committees have devised a road-map for the redefi-
279 nition of the second. This documents the high priority and strong commitment of a large community
280 to the development and operation of optical clocks, with high relevance for society. Such a redefini-
281 tion will enable a more accurate and stable international timescale [27, 28], which is key for precise
282 navigation services via the GNSS network, the synchronization of worldwide exchanges and markets,
283 communication networks, and national defence and security.

284 The coordination of time requires the permanent comparison and synchronisation of national
285 timescales and clocks. With the increasing performance of optical clocks, the demands on the link
286 quality are also increasing. Today’s microwave links achieve neither the necessary stability nor the
287 accuracy required by the new optical clocks [29]. Locally, fibre-optical links can be an alternative [30],
288 but a global network is not within reach. Long-distance time and frequency links enabling frequency
289 comparisons at the level of 1×10^{-18} are urgently needed. Such links may even be combined by space
290 clocks as in the ACES [18] or the proposed Space Optical Clock (SOC) [31] missions. Potentially, a
291 space clock can overcome the limitations on the realization of the SI unit second and of timescales
292 set by the knowledge of the gravity potential on the ground because TAI and UTC are defined on
293 the geoid. Ground clocks that are generally not operated on the geoid must be corrected for the
294 relativistic red shift. Presently, this correction can only be determined with a fractional uncertainty
295 of about 3×10^{-18} , equivalent to 3 cm height [32], which is already larger than the uncertainty of
296 today’s optical clocks (see Section 3.2.1).

297 3.1.3 Earth observation & geodesy

298 In view of climate change and its consequences for society, Earth observation and geodesy are of
299 increasing importance. While highly accurate *geometric* reference frames based on GNSS or VLBI
300 exist, *physical* height reference systems related to the geoid and the flow of water are much less
301 accurate and fall behind the requirements set by a UN resolution for sustainable development [33] by
302 more than an order of magnitude.

303 Presently, physical heights are locally derived by spirit levelling tied to reference points such as tide
304 gauges or global observations from satellite missions like CHAMP [34], GOCE [13], GRACE [35], and
305 GRACE-FO [14]. Although these missions were and are very successful, they lack spatial resolution
306 and require considerable data processing, because the sensors are only sensitive to derivatives of the
307 gravity potential. With clocks at a fractional uncertainty level of 10^{-18} , we now have sensors at hand
308 that are directly sensitive to the gravity potential via the relativistic redshift. Therefore, we have an
309 opportunity to establish a novel technique to realize a height reference system by a network of optical
310 clocks from which the physical height differences at the respective locations can be derived.

311 Present clock performance already provides a height resolution better than the current geodetic
312 state-of-the-art [32], and is likely to reach the millimetre level within the next decade. It is essential to
313 establish links for cross-comparisons of optical clocks that are flexibly accessible and span the globe.
314 Satellite-based approaches fulfill these requirements in an ideal fashion. While satellite-mediated
315 ground-to-ground links with improved performance compared to, e.g., ACES, will enable a fast devel-
316 opment of this field of application, clocks operated in space and linked to the ground can provide even
317 more benefits. They will improve the products from GRACE-like missions and can ultimately serve
318 as an independent, long-term stable and reproducible height reference point for decades and centuries
319 of Earth monitoring.

3.2 Clocks: state-of-the art

3.2.1 Lab-based clocks

Figure 1 shows the historical progress of state-of-the-art laboratory atomic clocks. Caesium (Cs) microwave atomic clocks have been the primary standard for the SI second since 1967, which has helped to motivate the development of several generations of Cs clocks with reduced fractional frequency errors. However, in recent years optical atomic clock technology has matured significantly: the best optical atomic clocks now surpass Cs in relative accuracy by a factor of more than 100. The field of optical clocks encompasses a diverse range of trapped-ion clocks and optical lattice clocks, each with distinct merits. However, optical lattice clocks have the key advantage of using many atoms in parallel, resulting in greater frequency stability and therefore allowing high-precision measurements within a significantly shorter averaging time [36, 37].

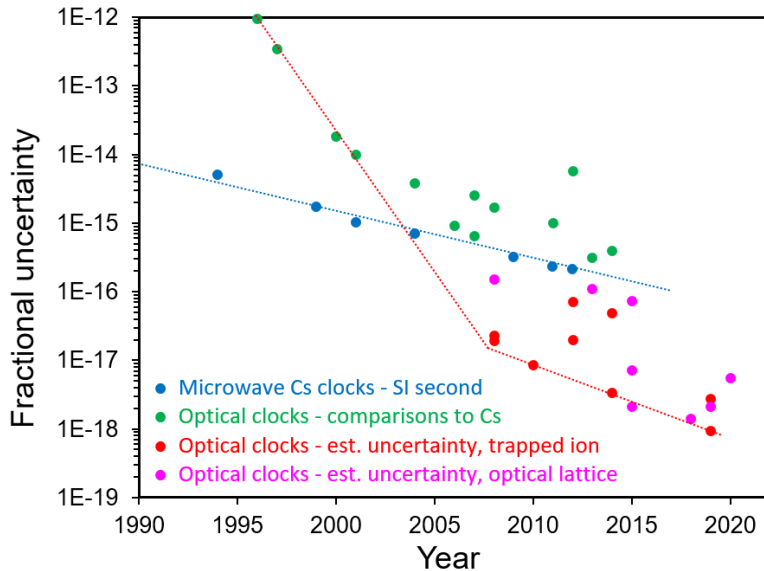


Figure 1. Progress in the relative accuracy of atomic clocks. Cs microwave clocks have steadily improved since the emergence of laser-cooled fountain clocks in the early 1990s [38–40], but two distinct types of optical clock currently compete at a fractional frequency uncertainty of approximately 1×10^{-18} : trapped-ion clocks (Yb^+ [22], Al^+ [41], Hg^+ [42], Sr^+ [43], Ca^+ [44]) and optical lattice clocks (Sr [45], Yb [46], Hg [47], Cd [48]).

To verify the 10^{-18} relative accuracy of the best optical clocks, and to pursue some of the scientific opportunities discussed in Section 3.1, it is important to compare different clocks of comparable precision with each other. Local measurements of optical clocks within a single laboratory have been used to measure general relativistic redshifts down to the millimeter scale [49] and to search for possible variations in local physics induced by dark matter [50–52]. Distant comparisons between clocks in separate laboratories allow large numbers of independent clocks to be included, but must be mediated by a complex frequency link infrastructure. The longest distances are spanned by satellite links, which allow comparison at 10^{-16} fractional frequency uncertainty [29]. However, much higher precision at the 10^{-18} level can be carried out over shorter distances using terrestrial links, either with free-space lasers [53] or telecoms-wavelength lasers sent through optical fibres [30, 54, 55]. The most extensive optical fibre network is operated between European metrology institutes [30], across which

342 several clocks have been compared to search for physics beyond the Standard Model (see Section 3.1.1)
343 [21, 56].

344 The development of laboratory atomic clocks is fuelled by a broad community, which spans univer-
345 sities, industry and several National Metrology Institutes. Optical lattice clocks are now particularly
346 widespread, with more than a dozen strontium (Sr) [54, 57–69] and some ytterbium (Yb) [69–73] clock
347 laboratories in operation worldwide ¹. The commitment of the metrology community to continue
348 investing in optical clocks is highlighted by the CIPM road-map for an optical redefinition of the SI
349 second (see Section 3.1.2). The road-map mandates a research programme likely to span at least the
350 next decade, in which several optical clocks will be developed at 1×10^{-18} relative accuracy and vali-
351 dated through clock-clock measurements. To carry out such measurements, the priority of the optical
352 clock community will be to develop cold atom technology with higher technology readiness levels, ca-
353 pable of combining state-of-the-art accuracy with robust, long-term operation—an investment which
354 should have close synergies with a future programme for cold atoms in space.

355 3.2.2 Transportable clocks

356 Early in the development of optical frequency standards it was recognized that mobile devices (see,
357 e.g., [74]) enable applications (see Section 3.1) of clocks that are impractical if the availability of clocks
358 is restricted to only a few laboratories. The required engineering to develop delicate laboratory systems
359 into robust mobile devices also opens the door to commercialization and space applications of clocks.
360 While there have been several impressive demonstrations of compact optical frequency standards with
361 high performance [75, 76], we focus here on activities that target a clock performance similar to the
362 state-of-the-art of laboratory setups (see Section 3.2.1).

363 To maintain the outstanding frequency stability of optical clocks, ultra-stable interrogation lasers
364 are required. For reasons of seismic and thermal insulation, these are typically neither robust nor
365 compact. Therefore, the further development of these devices was identified by the community as an
366 important challenge [77–79] and supported, e.g., by ESA activities [80–82] and is – with demonstrated
367 fractional frequency instabilities significantly below 10^{-15} – on a good path. As ultra-stable laser
368 systems have numerous applications beyond optical frequency standards, e.g., in atom interferome-
369 try, ultra-stable microwave generation, or optical telecommunication, the continued support of these
370 activities is of high importance.

371 The realization of a full transportable optical clock requires more lasers and a complex physics
372 package, and thus poses a larger challenge. Nevertheless, several such systems working with neutral
373 atoms [83–85] or single ions [44] have been realized, which already outperform the most accurate
374 microwave standards. These setups are developed for space applications [31], and have been used in
375 a geodetic context [86, 87] or to test fundamental aspects of physics [88]. We therefore conclude that
376 the construction and reliable operation of optical clocks with fractional uncertainties of 1×10^{-17} and
377 below and compact dimensions of less than 1 m^3 is already possible today.

378 3.2.3 Free space-time and frequency links

379 Connecting (optical) atomic clocks worldwide lays the basis for applications such as the creation of
380 TAI or a Positioning, Navigation and Timing (PNT) standard, and would also open the route to
381 testing theories of fundamental physics (see Sections 3.1 and 3.3).

382 Currently, primary microwave clocks are connected via satellites [29] in the microwave domain by
383 the existing GNSS infrastructure [89] or dedicated two-way time and frequency transfer (TWTFT)

¹Importantly, these optical lattice clocks use the same Sr and Yb technology as proposed for atom-interferometer science missions such as AEDGE [5].

384 links [90–92]. Demonstrated frequency transfer uncertainties of existing microwave links (MWLs) reach
385 down to the 10^{-16} range after averaging times of weeks [89, 93] and demonstrated time transfer uncer-
386 tainties lie in the nanosecond region [92]. A new generation of MWL equipment is under development
387 [18, 94], which reaches in laboratory tests timing instabilities of < 100 fs for averaging times $\tau = 10$ s to
388 2000 s [18], which is equivalent to fractional frequency transfer uncertainties of $< 5 \times 10^{-17}$ at 2000 s.
389 Similar performances are achieved in the optical domain by Time Transfer by Laser Link (T2L2) [95]
390 and the European Laser Timing (ELT) experiment [96] employing time-of-arrival measurements of
391 laser pulses.

392 A significantly improved uncertainty is achieved by techniques exploiting the optical carrier. Op-
393 tical frequency dissemination using continuous wave laser signals [97] reaches fractional frequency
394 transfer instabilities $< 5 \times 10^{-19}$ already after 100 s of averaging time in path-length stabilized oper-
395 ation [98]. A team at NIST has developed an optical TWFT (OTWFT) technique [53] combining
396 carrier and time-of-flight information, allowing phase-coherent averaging over the signal dropouts
397 that occur inevitably due to atmospheric turbulence [99]. Using this technique, the NIST team has
398 demonstrated sub- 10^{-18} frequency transfer uncertainty and sub-1 fs timing uncertainty at an av-
399 eraging time of 1000 s in a 3-node network of two concatenated 14 km links [100]. Furthermore,
400 they demonstrated OTWFT to a flying drone with similar performance [101]. Despite the proven
401 performance, however, the remaining steps to achieve ground-to-satellite world-wide coverage remain
402 challenging: demonstrate techniques for higher relative speeds between sender and receiver (such as
403 in ground-to-satellite links), in terms of impact of the atmospheric turbulence, signal loss, potential
404 loss of reciprocity and inclusion of relativistic effects. Recently, a first study addressed this scaling
405 to ground-to-satellite connections [102] and came to a positive conclusion regarding the feasibility.
406 Nevertheless, further experimental evidence gradually approaching the long-term ground-to-satellite
407 goal is required. Synergies can be expected with the proposed combination of microwave and optical
408 links in the context of new GNSS constellations [103].

409 3.3 International space activities

410 Space is the ideal laboratory to test general relativity and alternative theories of gravitation with
411 atomic clocks. The large velocities and velocity variations, the access to large variations of the grav-
412 itational potential, and the possibility to establish a global network able to compare ground clocks
413 across continents from space provide new opportunities both for fundamental physics research and
414 for applications in other areas of research, such as clock synchronization and time-scale distribution,
415 geodesy, Earth observation, navigation, etc., as discussed elsewhere in this survey.

416 ACES (Atomic Clock Ensemble in Space) [18] is an ESA mission designed to operate on the
417 International Space Station. The two on-board clocks rely on atomic transitions in the microwave
418 domain. The PHARAO clock, a primary frequency standard based on laser cooled Cs atoms, provides
419 the ACES clock signal with a long-term stability and accuracy of 1×10^{-16} in fractional frequency;
420 the active H-maser SHM is the on-board flywheel oscillator that will be used for the characterization
421 of the PHARAO accuracy. The ACES clock signal is distributed to ground clocks by using two time
422 and frequency links: MWL is a link in the microwave domain; ELT is an optical link using short
423 laser pulses to exchange timing signals. A distributed network of MWL ground terminals will connect
424 the clocks operated in the best research institutes worldwide (SYRTE, PTB, NPL and Wettzell in
425 Europe, NIST and JPL in the US, NICT in Japan) to the ACES clock signal. Satellite laser ranging
426 stations will also be connected to the clock network by using the ELT optical link. The space-to-
427 ground clock de-synchronization measurement produced by MWL and ELT will be used to perform an
428 absolute measurement of the gravitational redshift in the field of the Earth to < 2 ppm, to probe time

429 variations of fundamental constants, and to perform Standard Model Extension (SME) tests. The
 430 possibility of searching for topological dark matter with the ACES network is also being investigated.
 431 ACES is expected to fly to the ISS in the 2024–2025 time frame. The flight model of the ACES payload
 432 is shown in Fig 2.

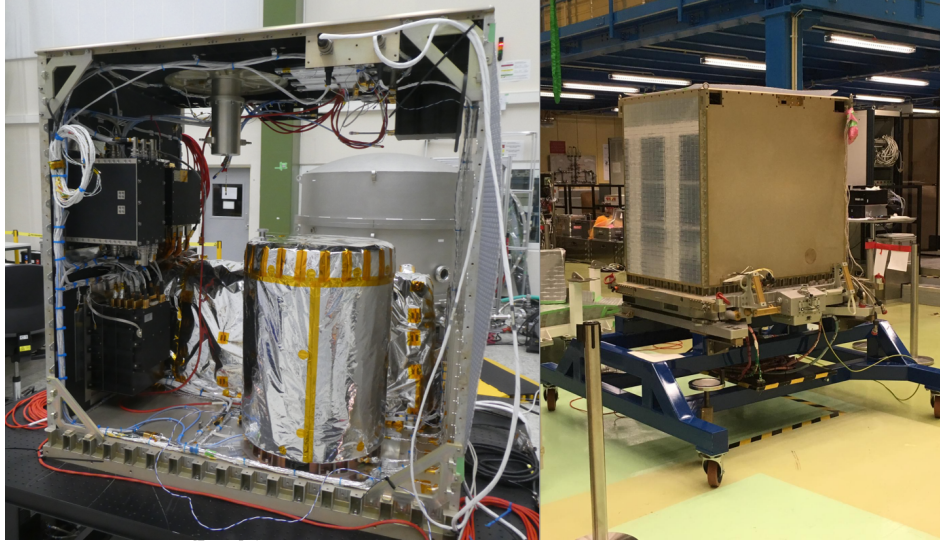


Figure 2. (Left) Flight model of the ACES payload during the assembly phase. SHM (vertical cylinder) and PHARAO (in the background) are installed on the bottom panel. The ACES computer, the PHARAO computer, and the on-board phase comparator are visible on the left panel. MWL electronics (not installed yet) and the antennae are accommodated on the top panel. (Right) The ACES payload installed on the Columbus External Payload Adapter (CEPA) for interface tests.

433 Significant advances in the development of microwave cold-atom clocks have been achieved in
 434 China with the launch and on-orbit operation of the CACES (Cold Atom Clock Experiment in Space)
 435 clock based on laser-cooled Rb atoms [104]. The experiment was successfully operated on the Chinese
 436 space laboratory Tiangong-2. From an analysis of the Ramsey fringes, a stability at the level of
 437 3×10^{-13} could be estimated under free fall conditions. Unfortunately, a full characterization of the
 438 clock in space was not possible due to the absence of a stable frequency reference and of a space-to-
 439 ground link on board Tiangong-2. The clock performance is still to be optimised, but the experiment
 440 clearly demonstrates the robustness of the cold-atom clock technology for space.

441 In the US, the NASA’s Jet Propulsion Lab has successfully demonstrated mercury trapped-ion
 442 clock technology in space [105]. The Deep Space Atomic Clock (DSAC) payload, consisting of a Hg^+
 443 microwave clock and a dedicated GPS receiver, was launched into a 720-km orbit around the Earth
 444 in June 2019. The space clock was compared to the clocks from the US Naval Observatory, and
 445 demonstrated a fractional frequency stability between 3×10^{-15} and 5×10^{-15} at 1 day and 3×10^{-15}
 446 after 23 days. The short-term stability of the clocks, which is below the GPS measurement system
 447 noise, could be estimated as $7 \times 10^{-13}/\tau^{1/2}$, where τ is the integration time. This technology can be
 448 used for navigation, planetary science, and fundamental physics.

449 As discussed above, optical clocks can provide an improvement in stability and accuracy of 2
 450 orders of magnitude with respect to microwave clocks. Following the impressive progress of atomic
 451 clocks based on optical transitions, several initiatives are currently ongoing to advance the required

452 technology to flight readiness.

453 Europe is developing key optical clock technology for space, e.g., cooling lasers, the clock laser,
454 a high-finesse reference cavity, a clock control unit to stabilize the laser frequency on the atomic
455 transition, and the lattice laser. A design study for a Sr clock physics package has been completed.
456 Compact and transportable ground-based prototypes for a Sr optical lattice clock [83] and a Sr ion
457 clock [106] are being characterized. Free-space coherent optical links reaching a fractional frequency
458 uncertainty of 1×10^{-19} in a few days of measurement time are under development [107]. In parallel,
459 the I-SOC Pathfinder platform has been proposed as the ACES follow-on mission. I-SOC Pathfinder is
460 pushing further the microwave and optical link technology [108, 109] developed for ACES to continue
461 operating a worldwide network of optical clocks on the ground to test fundamental laws of physics, to
462 develop applications in geodesy and time & frequency transfer, and to demonstrate key technologies
463 for future atomic clock missions in space.

464 In the US, the FOCOS (Fundamental physics with an Optical Clock Orbiting in Space) mission
465 concept is presently under study [110]. FOCOS relies on an Yb optical lattice clock with 1×10^{-18}
466 stability and accuracy on a highly elliptical orbit around the Earth. A coherent optical link is used to
467 compare the space clock to ground clocks for general relativity tests and timing applications. FOCOS
468 will also serve as a pathfinder for future atom interferometry missions to test the Equivalence Principle,
469 clock constellations in space to hunt for dark matter [24, 25], and gravitational wave observatories [26].

470 In parallel, CACES follow-on experiments based on optical clock technology are under development
471 in China.

472 Finally, major efforts and resources are being invested worldwide to improve the atomic clocks of
473 the Global Navigation Satellite System (GNSS). Currently, available technology relies on the passive
474 H-maser, the Rb atomic frequency standard, and the Cs beam frequency standard [111, 112]. Clocks
475 for navigation satellites have reduced stability (in the $10^{-15} - 10^{-14}$ range for fractional frequency),
476 but offer a more compact design with low mass (3 to 20 kg), low power consumption (30 to 70 W),
477 and long lifetime on orbit. Alternative technologies are under study for the next generation of atomic
478 clocks for navigation. Among them, it is worth mentioning the mercury ion clock technology [105],
479 the pulsed optically pumped Rb clock [113], the Rb optical atomic clock [114], and the iodine fre-
480 quency reference [76, 115] that will soon be tested in the COMPASSO experiment on the ISS platform
481 Bartolomeo [116]. These developments are maturing key technology for space (see Section 6) making
482 it possible not only to deploy compact atomic clocks for global positioning and navigation, but also
483 high-performance atomic clocks for fundamental physics and geodesy.

484 3.4 Recommendation: road-map to space clocks

485 As discussed above and in Section 5, there are many possible configurations of space-clock missions.
486 Here we envisage the possibility of three missions, undertaken in stages:

- 487 • Complete ACES and launch it to the ISS with utmost urgency.
- 488 • Implement I-SOC Pathfinder (or an equivalent) on the ISS as an ACES follow-on mission. The
489 payload, containing an active H-maser, a microwave link, and a laser-pulse optical link, is de-
490 signed for comparison of ground-based optical clocks to 10^{-18} fractional frequency precision in
491 1 day. This would have applications in fundamental physics discovery, proof-of-concept optical
492 timescales, and geodesy.
- 493 • Launch a dedicated satellite in a highly elliptical orbit containing a strontium optical lattice
494 clock with a 1×10^{-18} systematic uncertainty and $1 \times 10^{-16}/\sqrt{\tau}$ instability, with a coherent

495 optical link to ground. The goals of such a mission are similar to the ones proposed in FOCOS
496 [110]; strong cooperation would be very beneficial. A mission of this type will enable more
497 precise comparisons across a wider network of ground clocks, and direct searches for new physics
498 including stringent tests of general relativity.

499 Within this road-map we highlight an urgent need to develop coherent free-space optical links
500 capable of clock comparisons at the 10^{-18} level in less than 1 day. Once optical links are in place,
501 a critical element of the road-map is then the qualification of a strontium optical lattice clock for
502 operation in space ². To achieve this, a technology development programme must be undertaken for
503 several components of the clock: optical resonators to stabilize lasers to a noise floor of 1×10^{-16} in
504 fractional frequency; laser sources at six different wavelengths to cool, optically confine and interrogate
505 strontium atoms; compact physics packages with a controlled black-body radiation environment; and
506 compact frequency combs. Further details of the required technologies are outlined in Section 6.

507 For more efficient technology development, the possibility of establishing collaborations between
508 Europe, US, and China should be investigated. Further, synergies should be exploited between the
509 atomic clock missions discussed here and the requirements for the AEDGE mission [5] discussed in
510 Section 5, which would rely on the same cold-strontium technology.

511 4 Quantum Gravimetry for Earth Observation Review

512 4.1 The observation of mass change and EO requirements

513 4.1.1 Earth sciences and gravity field observations

514 The Earth sciences need gravity-field observations from satellites for understanding the Earth and
515 monitoring its changes related to geodynamics and climate change, as well as many other society
516 needs. Satellite earth observations (EO) enable the observation and monitoring of mass and mass
517 transport in the Earth system, and provide a significant contribution to the determination of many
518 Essential Climate Variables (ECVs) as defined by the Global Climate Observing System (GCOS) [117].
519 ECVs monitor phenomena that are changing the world we live in, such as climate change, changing
520 water resources, flooding, melting of ice masses, global sea level rise and atmospheric changes. Better
521 knowledge of such phenomena is bound to lead to significant societal benefits via, e.g., the operational
522 prediction of floods and droughts, prediction of future sea level rise, and in applications regarding
523 water management.

524 For these reasons, several initiatives and studies have been launched in the past years at the
525 international level to foster continued observation and monitoring of mass and mass transport phe-
526 nomena. In 2015 the International Union of Geodesy and Geophysics (IUGG) issued a resolution on
527 “Future Satellite Gravity and Magnetic Mission Constellations” [118] and launched an international
528 multidisciplinary study on science and user needs for the observation of mass transport to understand
529 global change and to benefit society. In the resulting report it was stated that “. . . a satellite gravity
530 infrastructure is needed with increased space-time sampling capability, higher accuracy and sustained
531 observations” [119], see also [120]. Moreover, in 2019 the International Association of Geodesy (IAG)
532 started the “Novel Sensors and Quantum Technology for Geodesy” (QuGe) initiative; in its framework,
533 three working groups have been defined, one specifically devoted to “Quantum gravimetry in space
534 and on ground” [121] and a second one targeting “Relativistic geodesy with clocks” [122] (Se. 3.1).

²Ytterbium could be used in place of strontium, as proposed in FOCOS [110]. The atoms share similar complexity and capability: either would be suitable for an atomic clock mission, or for an atom-interferometer science mission of the type proposed in AEDGE [5].

4.1.2 Past, present and planned gravimetry missions

In the past twenty years, satellite gravity missions have helped form a well-organized user community tracking the Earth mass movements and to study environmental changes on a global scale using data from satellite observations (see Fig. 3 and Table 1).

The general principle of gravity missions is based on precise tracking of satellite position (in free fall) and inter-satellite ranging, combined with the determination of non-gravitational accelerations by means of accelerometers on board the satellites. The technology exploited so far for gravimetry missions is represented by electrostatic accelerometers (EA), as in the GFZ CHAMP mission flying from 2000 to 2010 [34], where the accelerometer provides observations that represent the surface forces acting on the satellite, i.e., all non-gravitational accelerations (drag, solar and Earth radiation pressure), so that the Earth gravity field can be obtained from purely gravitational orbit perturbations (observed by satellite tracking). Based on the same EA technology but measuring orbit perturbations by satellite-to-satellite tracking, the NASA/DLR GRACE mission that flew from 2002 to 2017 [35] and the GRACE-FO mission launched in 2018 [14] have provided and are providing routine measurements of the spatial variations of the Earth gravity field in space and in time on a monthly basis. These missions are based on the concept of flying a pair of low-Earth-orbiting satellites, precisely tracked using the Global Navigation Satellite System (GNSS) and an inter-satellite microwave ranging system, with the accelerometers enabling the measurement of non-gravitational forces. This allows for long-term monitoring of the gravity field and its time variations.

However, the 20-year-long time series of observations needs to be prolonged: this is why several space agencies are working on follow-up missions. ESA plans a Next-Generation Gravity Mission – NGGM [123], scheduled for launch in 2028 and also known as MAGIC (Mass-change and Geosciences International Constellation), in cooperation with the corresponding NASA MCDO mass change satellite initiative (<http://science.nasa.gov/earth-science/decadal-mc>). The MAGIC mission configuration will be based on two pairs of twin satellites: one pair will fly on a quasi-polar orbit, the other one on an orbit with inclination of about 67° [124], with laser ranging between each pair. This will allow for a reduction in the revisit time, providing higher temporal and spatial resolution.

Based on a different measurement concept, gravimetry can also be performed by acquiring observations from a gradiometer, measuring gravity gradients inside the satellite. This was done in the very successful GOCE mission flying from 2009 to 2013 [13], which exploited gradiometry for a unique mapping of the static gravity field, providing models with unprecedented accuracy for a range of geophysical and oceanographic applications (e.g., sea-level currents, a reference system for global height systems, and background data for geophysics and understanding the Earth interior).

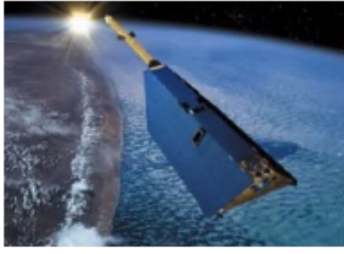
Table 1 summarizes the status of the gravity missions based on classical technology, the accuracies attained so far and the prospects for the near future.

Although the classical gravity field missions have been highly successful, they have not satisfied all the user needs of science and society. These have been summarized in various international reports, in the form of tables such as those provided in [125], see Table 4.1.2.

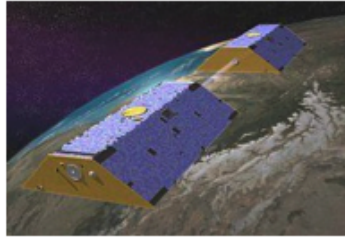
4.1.3 Earth observation requirements

The numbers in Table 4.1.2 point towards mission requirements that deliver measurements with higher sensitivity, greater accuracy, and more long-term stability. In summary, the needs are:

- Higher spatial resolution (implying lower orbits, 300-350 km) for detection of gravity changes due to movements of mass in the Earth system. However, it must be remarked that no space mission will



CHAMP : satellite tracking by GNSS + accelerometry



GRACE and GRACE-FO: orbit determination + satellite-to-satellite tracking + accelerometry



GOCE: orbit determination + gradiometry

Figure 3. The CHAMP [34], GRACE [35] and GOCE [13] satellites and mission concepts.

	CHAMP 2000 - 2010	GRACE/GRACE-FO 2002 - ongoing	NGGM Launch scheduled 2028	GOCE 2009 - 2013
Type of measurement		Monitoring gravity field time variations		Static gravity field
Accuracy of EA	$\sim 10^{-10}$ m/s ²	$\sim 10^{-11}$ m/s ²	$\sim 10^{-11}$ m/s ²	$\sim 10^{-12}$ m/s ²
Geoid undulations	~ 10 cm @ 350 km	~ 10 cm @ 175 km	~ 1 mm @ 500 km every 3 days ~ 1 mm @ 150 km every 10 days	~ 1 cm @ 100 km
Gravity anomalies	~ 0.02 mGal @ 1000 km	~ 1 mGal @ 175 km		~ 1 mGal @ 100 km

Table 1. Accuracies in the determination of the gravity field by “classical” measurements (including the planned ESA-NASA NGGM/MAGIC mission [124]).

Threshold requirements

Spatial resolution	Equivalent water height		Geoid	
	Monthly field	Long-term trend	Monthly field	Long-term trend
400 km	5 mm	0.5 mm/yr	50 μ m	5 μ m/yr
200 km	10 cm	1 cm/yr	0.5 mm	0.05 mm/yr
150 km	50 cm	5 cm/yr	1 mm	0.1 mm/yr
100 km	5 m	0.5 m/yr	10 mm	1 mm/yr

Target objectives

Spatial resolution	Equivalent water height		Geoid	
	Monthly field	Long-term trend	Monthly field	Long-term trend
400 km	0.5 mm	0.05 mm/yr	5 μ m	0.5 μ m/yr
200 km	1 cm	0.1 cm/yr	0.05 mm	5 μ m/yr
150 km	5 cm	0.5 cm/yr	0.1 mm	0.01 mm/yr
100 km	0.5 m	0.05 m/yr	1 mm	0.1 mm/yr

Table 2. Consolidated science and users’ requirements for earth observation, as reported in [125].

579 be able to map the higher-frequency details of the gravity field, due to the atmospheric limitations of
 580 the orbit height. Therefore, a full detailed mapping of the spatial gravity field variations down to a
 581 few km resolution must be supplemented by airborne and ground gravity measurements;

- 582 • Shorter revisit times, which require flying a satellite constellation, e.g., double pairs such as in
583 NGGM/MAGIC. The improved temporal resolution would be crucial for operational service applica-
584 tions such as near real-time flood tracking. A shorter revisit time will also aid in better determination
585 of tidal effects, which must currently be modelled, and represent a limiting factor in the accuracy of
586 current missions.;
- 587 • Greater accuracy in the measurements, by exploiting new technologies such as laser interferometry
588 and cold atom accelerometers, with accelerometers accurate to better than $\sim 10^{-10} - 10^{-11} \text{ m/s}^2$
589 (measurement range of $\pm 10^{-4} \text{ m/s}^2$) and gradiometers accurate to $\sim 10^{-12} \text{ m/s}^2/\sqrt{\text{Hz}}$ for a GOCE-
590 like mission, over a larger spectral measurement band. Improved instrument performance and low-
591 frequency stability will become important for satellite constellations;
- 592 • Extension of the observation time series, which is essential for long-term monitoring of mass trans-
593 port and variations, and especially for understanding the separation of natural and anthropogenic
594 forcing.

595 4.2 Quantum Sensors in the Context of Earth Observation

596 4.2.1 Classical and quantum sensors for gravimetry

597 Quantum sensors based on atom interferometry are extraordinarily sensitive to external forces [126],
598 reaching an accuracy of 40 nm/s^2 for gravimeters [127], $8 \times 10^{-8} \text{ 1/s}^2$ for gradiometers [128, 129]
599 and 70 nrad/s for gyroscopes [130, 131]. In Table 1 some of the most relevant features of quantum
600 accelerometers and the classical electrostatic accelerometers used so far for space accelerometry are
601 compared. On the ground, the best quantum accelerometers are operating at sensitivities of about $5 \cdot$
602 $10^{-8} \text{ (m/s}^2)/\sqrt{\text{Hz}}$ [127] for an interrogation time of about 100–200 ms. A space quantum accelerometer
603 is expected to reach sensitivities in the low $10^{-12} \text{ m/s}^2/\text{Hz}^{1/2}$ when stretching the interrogation times
604 to 20 s, similar to the very best accelerometers, such as used for the GOCE [13] mission, but in a wider
605 measurement band, extending down to lower frequencies. Absence of drifts is a consequence of the
606 absolute character of quantum sensors, with stable scale factors determined by the wavelength of the
607 laser beam-splitters and the duration of the measurement, and the possibility of evaluating accurately
608 systematic effects. On the other hand, they are so far limited to single axis measurements, and have
609 a much higher Size, Weight and Power (SWaP) budget. However, whilst the technology is currently
610 less mature, it is currently being demonstrated in a number of national and international projects as
611 outlined in Section 6.

612 4.2.2 Potential gain in Earth observation by quantum gravimeters

613 The promise of atomic accelerometers for providing better long-term stability, i.e., smaller measure-
614 ment noise at the lowest frequencies, below 10 mHz, will enable the reconstruction of the Earth gravity
615 field to be improved, particularly at low spherical harmonic degrees, if not at all degrees, as seen in
616 Fig. 4 [132]. This shows the uncertainties in the gravity-field recovery as a function of spherical
617 harmonic degree, evaluated in equivalent water height, considering quantum (black) or drifting (red)
618 accelerometers in the left panel, and colour-coded in the right panels. The computations were carried
619 out without any empirical periodic parameter adjustment in the gravity-field reconstruction.

620 The potential gains in Earth observation obtainable using quantum sensors are illustrated in Fig. 5.
621 The ellipses represent the required measurement resolutions for the indicated scientific objectives,
622 with the spatial resolution on the horizontal axis and the temporal resolution on the vertical axis.
623 Also shown are the sensitivity curves of the “classical” CHAMP [34], GRACE [35] and GOCE [13]
624 missions and the prospective sensitivity of a possible quantum gravimetry mission employing atom
625 interferometry.

	Atomic accelerometer	Electrostatic accelerometer
Sensitivity	$4 \times 10^{-8} \text{ m/s}^2/\text{Hz}^{1/2}$ on ground (projection for space at $10^{-12} \text{ m/s}^2/\text{Hz}^{1/2}$ for interrogations of more than 20 s)	$3 \times 10^{-12} \text{ m/s}^2/\text{Hz}^{1/2}$ (demonstrated)
Measurement bandwidth	$\leq 0.1 \text{ Hz}$	[0.005-0.1] Hz
Scale factor	Absolute	Calibration required
Stability	No drift	Drift
Measurement capability	Single axis	Three axes
Proof mass motion	Residual velocities \rightarrow Coriolis acceleration	
SWaP	High	Low
TRL	Intermediate	High

Table 3. Comparison of classical and quantum sensors.

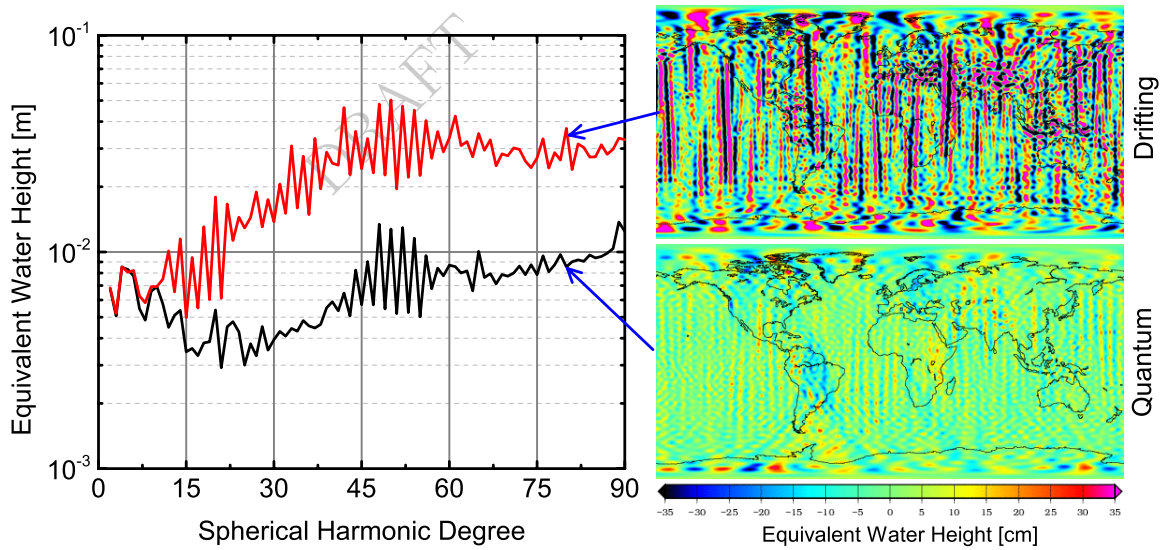


Figure 4. Spectra of gravity field recovery in equivalent water height obtainable with an atom interferometer and an electrostatic accelerometer, shown as black and red lines, respectively, in the left panel and colour-coded in the lower and upper maps in the right panels. Figure taken from [132].

626 4.2.3 Potential gain in Earth observation by chronometric levelling

627 As already mentioned in Sec. 3.1, a combination of ground and space clocks together with high
628 performance time and frequency dissemination capabilities in particular via satellites can benefit the
629 stabilization and long-term validation of physical height networks. Though this approach is today
630 less developed than quantum gravimeters, it is highly appealing because clocks offer access to a new
631 observable in Earth observation, namely to gravity potential differences in addition to the established
632 determination of its derivatives. Time and frequency dissemination via satellite supported by space
633 clocks can thus be a valuable ingredient to establish an improved height reference system as required

634 by the United Nations [33].

635 4.3 Quantum space gravimetry pathfinder mission

636 4.3.1 Concepts for a quantum gravimetry pathfinder mission

637 For the European Union, deploying a quantum space gravimetry (QSG) pathfinder mission within this
 638 decade is a strategic priority to ensure non-dependence and leadership in this field and to pave the
 639 way towards an EU QSG mission within the next decade. In this regard, the pathfinder will represent
 640 a fundamental technological step towards the feasibility of such a mission. On the other hand, we
 641 must consider the importance of the pathfinder in showing the fitness of cold atom interferometry for
 642 the purpose of gravity sensing, even if this first mission will not provide observations allowing for an
 643 improvement in the gravity field recovery. It is to be noted that the challenges inherent to the launch
 644 and operation of a dedicated pathfinder mission led ESA to propose the possibility of embarking the
 645 pathfinder mission on one of the MAGIC satellite pairs, to be launched around 2027 or 2030; this
 646 mission is at the moment at the stage of a phase A study.

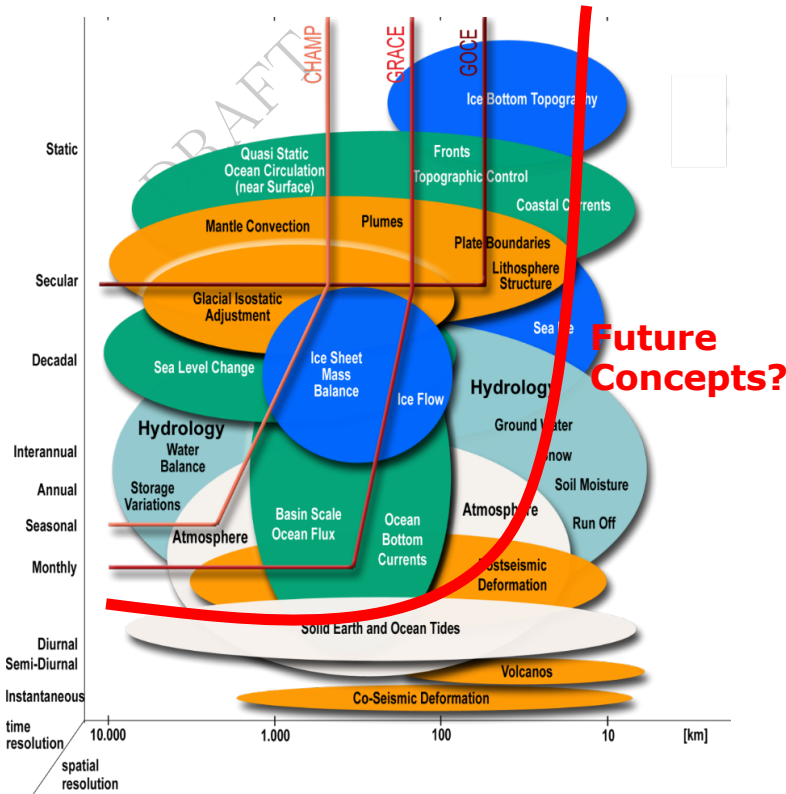


Figure 5. The spatial and temporal resolutions required for the indicated scientific objectives, compared with the sensitivity curves of the “classical” CHAMP [34], GRACE [35] and GOCE [13] missions and the prospective sensitivity of a possible quantum gravimetry mission. Figure adapted from [133].

647 4.3.2 Profile for a quantum gravimetry pathfinder mission

648 The main goal of the pathfinder mission should be to demonstrate the maturity of the cold atom
 649 technology to operate in space. It should also go beyond the present-day performance of ground

650 atom accelerometers (few 10^{-8} $\text{m/s}^2/\sqrt{\text{Hz}}$) by one to two orders of magnitude thanks to the long
651 interrogation times (several seconds) in microgravity. It will also help to demonstrate the technical
652 maturity of key components of cold atom sensors in space, such as the long operation times or the
653 rotation compensation (see Section 6 for further details). Furthermore, the pathfinder mission will have
654 a strategic importance also for geodesists who are looking forward to analyse observations and obtain
655 meaningful geodetic results from the next (fully-fledged) quantum gravimetry mission. The pathfinder
656 will in any case provide interesting observations and results to useful for the recovery of the gravity
657 field, even though a clear improvement will be available to end-users in geodesy and geophysics only
658 from the following quantum gravimetry mission. In fact, this pathfinder mission will allow preparing
659 for missions with larger 2T (more than 10s) at resolutions of $\sim 10^{-11} - 10^{-12}$ $\text{m/s}^2/\sqrt{\text{Hz}}$ suitable for
660 the wide users community.

661 The payload is expected to have a mass of a few hundred kg and would require a few hundred W
662 to operate. In order for the quantum sensor to perform optimally, the platform needs to be designed
663 to meet clear constraints (centre of gravity, rotation compensation, etc.). To operate with optimal
664 performance, the orbit, altitude, flight modes and position within the platform should be chosen to
665 ensure a successful operation of the quantum sensor.

667 **4.4 Recommendation: road-map to quantum EO in space**

668 As discussed above, there are many possible configurations of quantum gravimetry missions. Here we
669 envisage the possibility of three missions, undertaken in stages:

670 • In parallel with the conventional planned gravimetry mission, MAGIC [124], update the quantum
671 instrument specifications and requirements. For the above-mentioned technical reasons, embarking the
672 quantum sensor as a passenger on an SST geodesy mission poses tremendous technical challenges and
673 carries significant technological and programmatic risks for both aspects of the mission (classical and
674 quantum sensors).

675 • Hence the prevailing outcome of the discussions among scientific experts during the workshop
676 is a recommendation to launch a pathfinder mission within this decade with a performance of up to
677 10^{-10} $\text{m/s}^2/\sqrt{\text{Hz}}$ on a dedicated platform. Such a mission would balance the need to have a test of the
678 quantum technology in space and the level of expectation from the quantum gravimetry pathfinder
679 mission. It would also be a clear milestone for other communities, such as the fundamental physics
680 one.

681 • The success of MAGIC and the Pathfinder mission will then enable the implementation of a
682 full-fledged quantum space gravimetry mission to be launched to follow MAGIC. The definition of the
683 mission scenario and the instrument baseline will be based on lessons learned from MAGIC and the
684 Pathfinder mission.

685 **5 Atomic Sensors for Fundamental Science Review**

686 **5.1 Scientific opportunities**

687 The promise of Cold Atom technologies for making precise experimental probes of topics in fundamen-
688 tal science such as general relativity, cosmology, quantum mechanics and the search for new physics
689 beyond the Standard Model has been recognised in many terrestrial and space projects. To cite just a
690 few examples: in the US the MAGIS 100m atom interferometer is under construction at Fermilab [134]
691 and NASA has operated the CAL Bose-Einstein condensate (BEC) experiment successfully for several

692 years on the ISS [135]; in Europe the ELGAR project [136] has been proposed; initial funding has been
 693 provided for a suite of experiments applying Quantum Technology for fundamental physics in the UK,
 694 including the terrestrial AION atom interferometer [137]; in France the MIGA atom interferometer is
 695 under construction [138]; there is a series of German BEC experiments in microgravity using MAIUS
 696 sounding rockets [139]; the MICROSCOPE experiment [140] has tested the Einstein Equivalence Prin-
 697 ciple in space and the follow-up STE-QUEST experiment has been proposed [141]; and in China the
 698 terrestrial ZAIGA atom interferometer [142] is under construction and quantum correlations have been
 699 verified by the Micius satellite experiment [143] over distances exceeding a thousand km.

700 The deployment of cold atom technologies in space offers unique research opportunities in the
 701 fields of fundamental physics, cosmology and astrophysics, as represented in several White Papers
 702 submitted to the ESA Voyage 2050 call for mission concepts [4, 6, 8–12]. We focus in the following on
 703 two of these mission concepts.

704 One is based on the previous STE-QUEST proposal [144], and proposes a double atom interferom-
 705 eter with rubidium and potassium “test masses” in quantum superposition to test the universality
 706 of free fall (UFF). It assumes a single satellite in a 700 km circular orbit, and applies recent develop-
 707 ments on gravity gradient control by offsetting laser frequencies, which enables the atom positioning
 708 requirements to be relaxed by a factor > 100 [7, 145]. This offers the possibility of probing the UFF,
 709 i.e., the Einstein equivalence principle, with an unparalleled precision $\mathcal{O}(10^{-17})$ after 18 months in
 710 orbit [145], see Fig. 6.

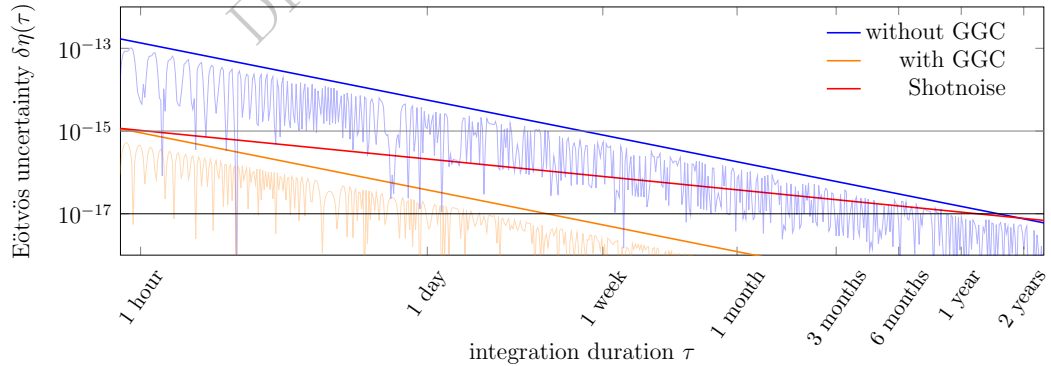


Figure 6. Averaging of systematic uncertainties due to gravity gradients in a UFF test with Rb and K quantum sensors. Gravity Gradient Cancellation (GGC) significantly reduces the systematic contributions, such that the residual differential acceleration may be attenuated to an unprecedented degree through signal demodulation (orange curve). This not only allows for requirements on the source preparation that are greatly reduced compared to other mission proposals as STE-QUEST [144], but also paves the way for more ambitious mission scenarios targeting $\delta\eta \leq 10^{-17}$ in shot-noise limited operation (red curve). In contrast, even though the systematics are integrated down thanks to demodulation, the measurement would be limited by systematics without GGC (blue curve). The figure is taken from [145].

711 The other is the AEDGE concept for a satellite atom interferometer using strontium [5], which
 712 is illustrated in Fig. 7. In the original AEDGE concept [5] the atom clouds were assumed to be
 713 located inside the spacecraft and have sizes ~ 1 m. In addition to this version, here we also consider
 714 in the following the possibility that the clouds are outside the spacecraft and have sizes ~ 100 m, a
 715 concept called AEDGE+. ³ AEDGE can search for waves of ultralight dark matter (ULDM) particles

³See also the Workshop talk by Nan Yu.

716 with masses between $\mathcal{O}(10^{-21})$ and $\mathcal{O}(10^{-15})$ eV and measure gravitational waves in a frequency
717 range between $\mathcal{O}(1)$ and $\mathcal{O}(10^{-2})$ Hz [5], intermediate between the ranges of frequency where the
718 sensitivities of the terrestrial laser interferometers LIGO [146], Virgo [147], KAGRA [148], ET [149] and
719 CE [150] are maximal and the optimal frequencies of the space-borne laser interferometers LISA [151],
720 TianQin [152] and Taiji [153].

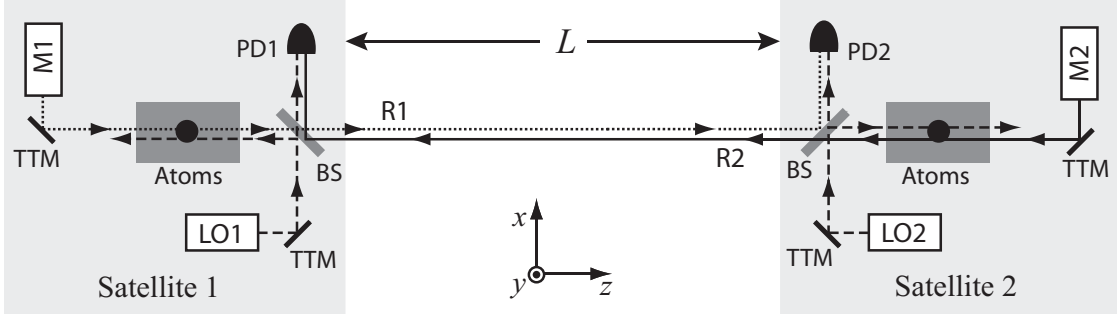


Figure 7. Possible scheme for a satellite atom interferometer experiment [5]. It has two master laser beams $M1$ and $M2$ (dotted and solid lines) and two reference beams ($R1$ and $R2$) there are two local oscillator lasers $LO1$ and $LO2$ (dashed lines) phase-locked with $R2$ and $R1$, respectively. Photo detectors ($PD1$ and $PD2$) measure the heterodyne beatnote between the reference beams $R2$ and $R1$ and the corresponding local lasers $LO1$ and $LO2$, respectively, providing feedback for the laser link. Non-polarizing beam splitters are denoted by BS , and tip-tilt mirrors used for controlling the directions of the laser beams are denoted by TTM . Small offsets between overlapping laser beams have been introduced for clarity. The figure is taken from [154].

721 In the following we present some representative examples of the capabilities of these cold atom
722 concepts for probing fundamental physics, cosmology and astrophysics.

723 5.1.1 Tests of the universality of free fall, UFF

724 The Einstein Equivalence Principle (EEP) is the foundation of all theories of gravitation that describe
725 it as a geometrical phenomenon, i.e., a curvature of space-time. Indeed, the universal coupling to all
726 mass-energy that is implicit in the EEP is necessary for all metric theories of gravitation, including
727 general relativity among many others. As such, the EEP is one of the most foundational building
728 blocks of modern physics. Nonetheless, many theories that go beyond the Standard Model and general
729 relativity and/or account for dark matter/energy entail some violation of the EEP (see e.g. Section
730 5.1.2, or [7] for more examples).

731 The best known aspect of EEP is the universality of free fall (sometimes also referred to as the weak
732 equivalence principle, WEP). The history of experimental tests of UFF/EEP goes back as far as the
733 Renaissance, and probably beyond. A simple phenomenological figure of merit for all UFF/EEP tests
734 is the Eötvös ratio η_{AB} for two test objects A and B and a specified source mass of the gravitational
735 field:

$$\eta_{AB} = 2 \frac{a_A - a_B}{a_A + a_B}, \quad (5.1)$$

736 where a_i ($i = A, B$) is the gravitational acceleration of object i with respect to the source mass. Note
737 that for a given experiment the data can be interpreted with respect to different source masses (see,
738 e.g., Ref. [155]) with correspondingly different results for η_{AB} .

Class	Elements	η	Year [ref]	Comments
Classical	Be - Ti	2×10^{-13}	2008 [155]	Torsion balance
	Pt - Ti	1×10^{-14}	2017 [158]	MICROSCOPE first results
	Pt - Ti	(10^{-15})	2019+	MICROSCOPE full data
Hybrid	^{133}Cs - CC	7×10^{-9}	2001 [159]	Atom Interferometry
	^{87}Rb - CC	7×10^{-9}	2010 [160]	and macroscopic corner cube
Quantum	^{39}K - ^{87}Rb	5×10^{-7}	2014 [161]	different elements
	^{87}Sr - ^{88}Sr	2×10^{-7}	2014 [162]	same element, fermion vs. boson
	^{85}Rb - ^{87}Rb	3×10^{-8}	2015 [163]	same element, different isotopes
	^{85}Rb - ^{87}Rb	3.8×10^{-12}	2020 [164]	≥ 10 m towers
	^{85}Rb - ^{87}Rb	(10^{-13})	2020+ [165]	
	^{170}Yb - ^{87}Rb	(10^{-13})	2020+ [166]	
Antimatter	^{41}K - ^{87}Rb	10^{-17}	2035+	Atom Interferometry mission
	$\bar{\text{H}}$ - H	(10^{-2})	2020+ [167]	under construction at CERN

Table 4. *State of the art in UFF/EEP tests. Numbers in brackets are results expected in the near future, and we also show the performance of an STE-QUEST-like atom-interferometry mission in the context of this road-map.*

739 Whilst η_{AB} is a useful tool for comparing different experiments it cannot account for the diversity
740 of possible underlying theories, e.g., different types of couplings depending on the source and test
741 objects, or couplings to space-time varying background fields other than local gravity, e.g., [156, 157].
742 Thus, not only best performance in terms of the Eötvös ratio is required, but also a large diversity of
743 test objects and source masses.

744 Table 4 presents the state of the art in UFF/EEP tests, separated into different classes as a function
745 of the type of test-masses employed. In particular, we distinguish between tests using macroscopic
746 test masses and atom-interferometry (AI) tests that use matter waves in a quantum superposition,
747 possibly condensed to quantum degenerate states (Bose Einstein Condensates) with coherence lengths
748 $\geq \mu\text{m}$. The “game changing” results of the MICROSCOPE mission demonstrate the potential of going
749 into a quiet and well-controlled space environment, with potentially “infinite” free fall times. The cold
750 atom interferometry based test described in the context of this road-map is highlighted in red.

751 5.1.2 Ultralight dark matter detection

752 Figure 8 shows examples of the present and prospective sensitivities of searches for the couplings of
753 ultralight scalar dark matter to photons (left panel) and electrons (right panel). Such dark matter,
754 because of its non-universal coupling to the fields of the standard model, is also one example of
755 a violation of the Einstein equivalence principle and the universality of free fall, UFF. The shaded
756 regions are excluded by current experiments including MICROSCOPE [140] and atomic clocks [50]. We
757 also show the prospective sensitivities of rubidium-based terrestrial interferometers (MIGA [138] and
758 ELGAR [136]) and strontium-based terrestrial and space-borne atom interferometers (AION [137] and
759 AEDGE [5], respectively). MIGA, ELGAR and the 100 m and km versions of AION offer significantly
760 greater sensitivity than current experiments (torsion balances, atomic clocks and MICROSCOPE [140])
761 to couplings of scalar ULDM with masses $\lesssim 10^{-12}$ eV to both photons and electrons. A sensitivity of
762 $\sim 10^{-7}$ to the ULDM-photon coupling in this mass range could be obtained with a prospective cold-

763 atom interferometer UFF probe with a precision of 10^{-17} as discussed in the context of this road-map
 764 [7], using Rb and K quantum probes (see also Table 4). As seen in Fig. 8, the AEDGE strontium-based
 765 space-borne atom interferometer concept [5] could offer the greatest sensitivity to both the ULDM-
 766 photon and -electron couplings for masses between 10^{-15} and 10^{-21} eV, with a maximum sensitivity
 767 $\sim 10^{-14}$ for masses between 10^{-17} and 10^{-18} eV.

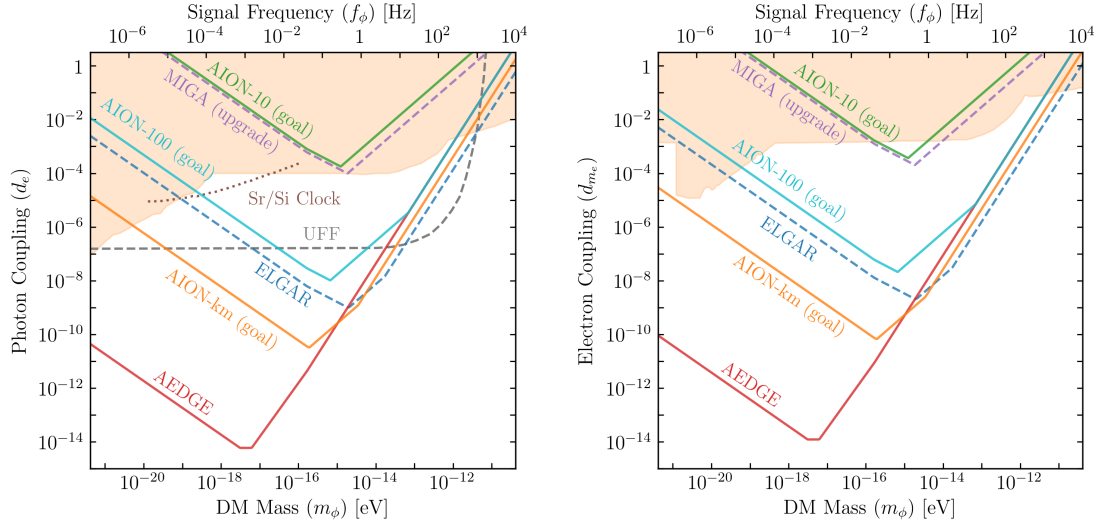


Figure 8. Sensitivities to the possible couplings of scalar ULDM to photons (left panel) and to electrons (right panel) of the terrestrial AION [137], MIGA [138] and ELGAR [136] experiments, and of the AEDGE space-borne concept [5]. Also shown is a combination of the current constraints from MICROSCOPE [140] and terrestrial torsion balance and atomic clock experiments and (in the left panel) the sensitivity of a prospective measurement of the universality of free fall (UFF) with a precision of 10^{-17} [6].

768 5.1.3 Probes of general relativity

769 The measurements of gravitational waves using an atom interferometer in space offer unique prospects
 770 for probing modifications of general relativity. For example, AEDGE measurements of the inspiral of
 771 merging black holes with a combined mass of 10^4 solar masses at a redshift $z \sim 1$ would be sensitive
 772 to the possible appearance of a graviton mass $\lesssim 10^{-26}$ eV, over three orders of magnitude below the
 773 current upper limit from LIGO and Virgo [168]. These measurements could also be used to search for
 774 possible violations of Lorentz invariance in the propagation of gravitational waves, with a sensitivity
 775 complementary to the searches by LIGO/Virgo and for gravitational Čerenkov radiation [168].

776 More classical GR tests using modern optical clocks are measurements of the gravitational Shapiro
 777 delay down to 10^{-8} [169] or tests of the gravitational red-shift at 10^{-9} as in the FOCOS mission [110],
 778 proposed recently in the context of the NASA decadal survey. In both cases these would provide 3-4
 779 orders of magnitude improvements on best current knowledge.

780 There is a proposal to probe models of dark energy by deploying a smart constellation of four satel-
 781 lites in an elliptic orbit around the Sun and making orientation-independent measurements of the dif-
 782 ferential accelerations between each pair of satellites, using as test masses atomic clouds far away from
 783 the spacecraft in open-space vacuum ([https://indico.cern.ch/event/1064855/contributions/
 784 4524214/attachments/2321220/3952720/ECWCAP2021_nyu.UR.pdf](https://indico.cern.ch/event/1064855/contributions/4524214/attachments/2321220/3952720/ECWCAP2021_nyu.UR.pdf)).

785 It has also been suggested to deploy an atomic clock at a distance $\mathcal{O}(150)$ AU to probe the
 786 low-acceleration frontier of gravity and the local distribution of dark matter [10].

787 Another suggestion is to detect the gravito-magnetic field of the galactic dark halo by locating
 788 atomic clocks at Sun-Earth Lagrange points and measuring the time-of-flight asymmetries between
 789 electromagnetic signals travelling in opposite directions, which would be generated partly by the
 790 angular momentum of the Sun and partly by the angular momentum of the dark halo [9].

791 5.1.4 Quantum mechanics

792 It has been proposed to test quantum correlations over astronomical distances [8, 11], e.g., between
 793 the Earth and the Moon or Mars, or between LISA spacecraft. The Micius measurements [143]
 794 already demonstrate that quantum correlations extend over 1200 km and that the apparent effective
 795 correlation speed exceeds 10^7 c, and Earth-Moon experiments could improve these sensitivities by
 796 factors $\sim 2 \times 10^4$ [11].

797 It has also been proposed to test wavefunction collapse and models predicting the violation of the
 798 quantum superposition principle [170, 171] by monitoring the expansion of a cloud of cold atoms [172].
 799 Current results already impose constraints on the distance and rate parameters of continuous sponta-
 800 neous localisation (CSL) models that are comparable with proposed reference values: see [172] for a
 801 detailed discussion.

802 5.1.5 Cosmology

803 AEDGE measurements also offer new opportunities in cosmology, such as unparalleled sensitivity to
 804 possible emissions from collapsing loops of cosmic strings in a network with tension $G\mu \gtrsim \mathcal{O}(10^{-18})$,
 805 more than 3 orders of magnitude below the current limit from the third Advanced LIGO–Virgo ob-
 806 serving run and an order of magnitude beyond the reach of LISA, as seen in the left panel of Fig. 9 [5].
 807 Such measurements could also be sensitive to effects in the early Universe that cause it to deviate
 808 from the conventional expectation of adiabatic expansion, such as a period of matter dominance or
 809 kination, as seen in the right panel of Fig. 9 [173]. Another cosmological opportunity is the search for
 810 a stochastic background of gravitational waves generated by a first-order phase transition in the early
 811 Universe, either in the electroweak sector of the Standard Model or in some extension that includes
 812 a new interaction generated by a massive Boson beyond the reach of present and proposed collider
 813 experiments. The left panel of Fig. 10 compares the sensitivities in the (T_*, α) plane (where T_* de-
 814 notes the critical temperature and α the strength of the transition) of the indicated experiments to
 815 GWs from a generic phase transition with a transition rate $\beta/H = 10^2$, and the right panel shows
 816 the signal-to-noise ratio (SNR) in the $(m_{Z'}, g_{B-L})$ plane expected from AEDGE measurements of the
 817 stochastic GW background from a $U(1)_{B-L}$ -breaking phase transition [174]. In the red regions SNR
 818 > 1000 and the solid gray contour corresponds to SNR = 10 [174].

819 5.1.6 Astrophysics

820 Opportunities in astrophysics are also opened up by these gravitational-wave measurements, including
 821 the observation of mergers of intermediate-mass black holes (IMBHs) that could reveal how the super-
 822 massive black holes at the centres of many galaxies were assembled [5], as illustrated in Fig. 11. As
 823 also seen in Fig. 11, there are good prospects of synergies obtained by networking detectors working in
 824 different frequency ranges, e.g., LISA might measure the initial inspiral stage of IMBH mergers whose
 825 final stages would be measured by AEDGE, and AEDGE measurements of the initial inspiral stages
 826 of mergers of lower-mass black holes could be used to predict the direction and timing of their final
 827 stages, providing advance warning for multimessenger observations. Also, as shown in the left panel

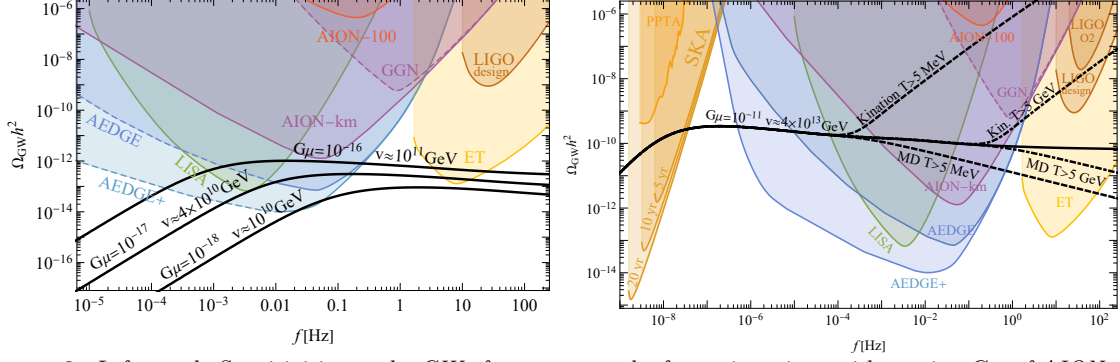


Figure 9. *Left panel:* Sensitivities to the GWs from a network of cosmic strings with tension $G\mu$ of AION-100 and -km, AEDGE [5] and AEDGE+ (a version of AEDGE which would use a $\sim 100\text{m}$ atomic cloud outside the spacecraft [173]), LIGO, ET and LISA. *Right panel:* Possible effects on the spectrum of GWs from cosmic strings with tension $G\mu = 10^{-11}$ of an epoch of matter domination (MD) or of kination [173].

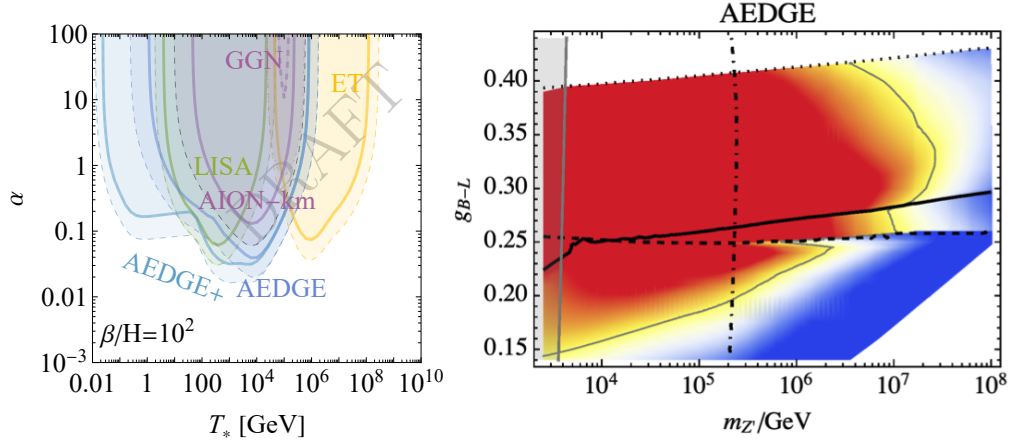


Figure 10. *Left panel:* Sensitivities of AION-100 and -km, AEDGE and AEDGE+ and LISA in the (T_*, α) plane to GWs from generic first-order transitions with a transition rate $\beta/H = 100$ [174]. *Right panel:* The expected signal-to-noise ratio (SNR) with AEDGE for observing the stochastic GW background from a $U(1)_{B-L}$ -breaking phase transition. In the red regions $\text{SNR} > 1000$ and the solid gray contour corresponds to $\text{SNR} = 10$ [174].

828 of Fig. 12, AEDGE could observe [173] the gravitational memory effect due to neutrinos emitted from
 829 a collapsing supernova in our galaxy [175] and, as shown in the right panel of Fig. 12, AEDGE would
 830 also be uniquely sensitive to possible features in the spectrum of cosmological density fluctuations
 831 that could lead to a population of primordial black holes with a density orders of magnitude below
 832 the current astrophysical limits [173].

833 5.2 Connection to Technology Development Section

834 5.2.1 Optical Clocks

835 As outlined in Section 3.2, several current activities exist to advance the capabilities for optical clocks
 836 in space. Depending on the type, environment, and targeted timescale of these clocks, the achievable
 837 stability varies. Similar to the capabilities, the requirements for the above discussed experiments differ.
 838 LISA, similar to navigational applications and earth observation, require high short-term stability [151,
 839 176], with the stability of the reference directly impacting the quality of the intended measurement.

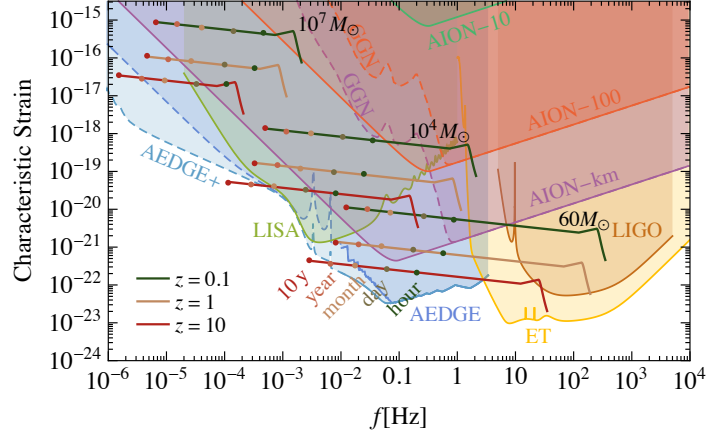


Figure 11. Strain sensitivities of AION-10, -100 and -km, AEDGE and AEDGE+, compared with those of LIGO, LISA and ET and the signals expected from mergers of equal-mass binaries whose masses are $60, 10^4$ and 10^7 solar masses. The assumed redshifts are $z = 0.1, 1$ and 10 , as indicated. Also shown are the remaining times during inspiral before the final mergers [5, 173].

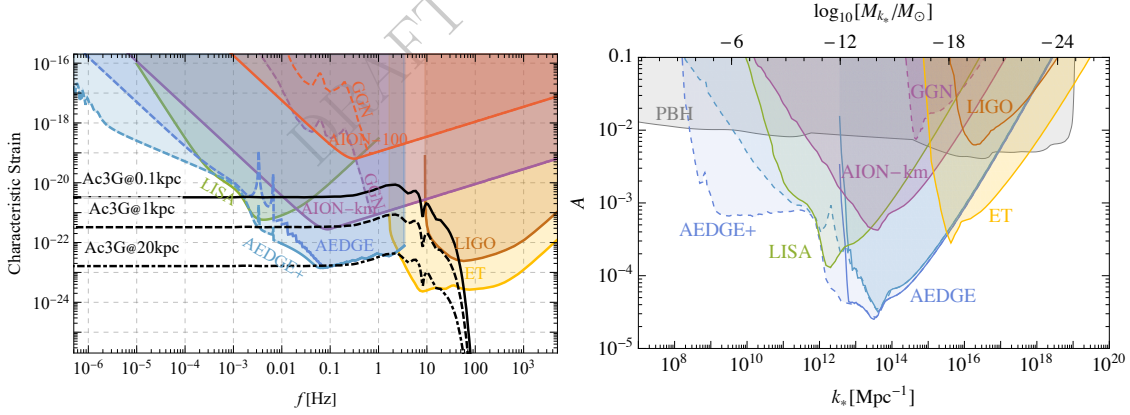


Figure 12. Left panel: The strain sensitivities of AEDGE and other experiments compared with the neutrino gravitational memory signal expected from a core-collapse supernova calculated using model Ac3G in [175]. Right panel: Sensitivities to the amplitude A of a delta function peak in the curvature power spectrum at scale k_* of AION-km, AEDGE and AEDGE+, LIGO, ET and LISA. The gray region is excluded by constraints on primordial black holes. The top axis indicates the horizon mass that corresponds approximately to the mass of the formed primordial black holes [173].

840 On the other hand, space-borne tests of special relativity, as proposed in [177] for instance, or made
 841 using the signals of misaligned Galileo satellites [16], require a high stability at orbit time.

842 As described in Section 3.2.1, the stabilization concept has to be chosen for a specific purpose.
 843 Optical frequency references based on *optical resonators* usually show the best performance on short
 844 time scales, where fluctuations in the resonator length do not impact the stability as severely. If
 845 integrating over longer times, these fluctuations, caused by thermal or mechanical stress, impact the
 846 achievable stability. To increase the long-term stability, efforts have been undertaken to reduce the
 847 impact of outside effects, such as by the choice of spacer material [178] and length of spacer, enclosure
 848 in thermal shields [81], or cryogenic environments [179]. The latter is especially interesting in ground-
 849 based experimental systems, such as for instance in [180].

850 Absolute frequency references based on the spectroscopy of atoms or molecules, on the other
851 hand, benefit from prolonged integration times. In general, the width of the probed line determines
852 the achievable stability. For such references, usually a trade-off has to be made between the required
853 stability and the available SWaP budget. As described in Section 3.3, different concepts have been
854 considered for space operation. We note in particular that space operation, especially outside the
855 International Space Station, requires full automation and high reliability of the system.

856 As outlined above, fundamental experiments require quiet environments to measure the desired
857 effects. While this does not always necessitate operation in orbit, space-qualified optical frequency
858 references are a key technology to enable the research. Section 3.3 details current and planned missions
859 for operation in orbit, demonstrating operation at a stability below 10^{-13} at orbit time. To improve
860 on the current best measurements performed on the ground, the frequency stability of any space-borne
861 frequency reference needs to be below $1 \cdot 10^{-15}$ at orbit time. Based on the current developments and
862 demonstrated optical references in space, this appears to be feasible for both short-term (in the range
863 of seconds to minutes) and long-term operation (in the range of hours).

864 5.2.2 Optical Links

865 Optical links are required to fulfill the scientific goals of various planned and executed missions. Those
866 missions can be divided in such examples with inter-satellite links, such as LISA [151] and AEDGE [5],
867 and those with ground-to-satellite links, such as MICIUS [143]. As outlined in Section 3.2.3, currently
868 mainly microwave links have been established, which do not satisfy the requirements for fundamental
869 science missions.

870 As an obvious example, entangled optical photons, as required for MICIUS, can only be transferred
871 by optical ground to satellite links. The success of MICIUS was a key step towards space-based
872 fundamental quantum entanglement experiments. Future quantum entanglement experiments could
873 be envisaged using two space-borne platforms to eliminate the atmospheric impact on the optical link.

874 Bidirectional ground-to-satellite optical links are a necessity for many applications, such as the
875 proposed Kepler constellation [103]. Additionally, they could play a part in comparisons of optical
876 frequency references operating in different gravitational potentials, i.e., on the ground and in space.

877 Precision in optical inter-satellite links is crucial to the scientific goals of missions employing long-
878 range laser ranging, such as LISA [151], where picometer level changes over the separation of the
879 satellites of the order of $5 \cdot 10^9$ meter will be detectable. In this case, the frequency of the deployed
880 laser enables more precise measurements than achievable with a microwave link.

881 Finally, gravitational wave detection measurements with cold atom sensors require a pair of atom
882 interferometers on two satellites irradiated by the same laser beams to achieve the necessary coupling.
883 Current proposals foresee a linkage over $4 \cdot 10^7$ meter to reach the strain sensitivity displayed in Fig. 11.
884 The achievable precision described in Section 3.2.3, underline the feasibility of missions such as LISA
885 and AEDGE.

886 Outside of space based experiments, also ground-based projects, such as ELGAR [136], require
887 coherent long-distance free-space laser beams. Since the necessary length is short compared to the
888 optical links discussed above and the accessibility of the system, the involved technology is currently
889 at hand.

890 5.2.3 Atom Interferometry

891 In the sections above, laser stabilization and information transfer over optical links has been dis-
892 cussed. The execution of future spaced-based experiments for fundamental science exploitation, such
893 as STE-QUEST [144] and AEDGE [5], requires high-precision atom interferometers, with different

894 interferometer schemes. Whereas, for a test of the weak equivalence principle two different masses,
895 here atomic species, need to be observed in the same place, the detection of gravitational waves and
896 other astrophysical phenomena require elaborate schemes with a single atomic species and optical links
897 between the atom interferometers, interrogated by the same laser.

898 As described in [144], weak equivalence principle experiments are made using two different masses,
899 whose free-fall behaviours are observed and compared. To improve on the current experimental results,
900 experiments with any two different kinds of atomic species could be envisaged. The visibility of any
901 deviation from predictions increases with the interrogation time. As an example, according to current
902 estimates, experiments with ^{85}Rb and ^{87}Rb require interrogation times of 10 s or more in interleaved
903 operation. This enables measurements of differential accelerations better than $10^{-13} \text{ m s}^{-2}$, necessary
904 for the targeted precision in the Eötvös parameter, see table 4. These types of experiments require
905 two species interferometers on a single satellite, which also allows for the increased free-fall time.

906 The detection of gravitational waves, on the other hand, strongly profits from large distances
907 between two atom interferometers in a gradiometric configuration. Such experiments require optical
908 links over long periods with two connected satellites in Earth orbit. The specific interferometer concept
909 requires an atomic species with a clock transition at optical frequencies, e.g., strontium. The free-fall
910 times of the atoms anticipated for these experiments are substantially longer than those discussed
911 above. For example, to enable gravitational wave detection as outlined in Section 5.1, free-fall times
912 in the order of 600 s are required to enable characteristic strain measurements down to 10^{-23} at about
913 80 mHz.

914 Atom interferometry in microgravity has been performed for several years. Experiments have been
915 performed in a drop tower (QUANTUS) [181, 182], on parabolic flights (I.C.E.) [183], on sounding rock-
916 ets (MAIUS) [139], and on the international space station (ISS) (Cold Atom Laboratory, CAL) [135].
917 The planned Bose Einstein Condensate and Cold Atom Laboratory (BECCAL) mission [184] is the
918 next-generation ultra-cold atom laboratory, including high precision atom interferometry, and is being
919 prepared for deployment on the ISS. Important challenges in miniaturization and automation have
920 been addressed in the development of CAL and BECCAL. The next step with the proven technology
921 is leaving the international space station and integrating an atom interferometer into a satellite. With
922 that development, space-borne tests of the weak equivalence principle, as proposed in [144], would
923 come within reach.

924 AEDGE represents the necessary next step in advancing quantum technologies for deployment in
925 space. It requires two optically-linked atom interferometers, increasing the distance and thereby sensi-
926 tivity of gravitational wave detectors with respect to ground-based measurements. The measurement
927 is enabled by employing strontium as opposed to rubidium or potassium. This leads to an additional
928 complexity in the system, such as availability of miniaturized laser systems, electronics, and optics.

929 Based on the present technology in space-based rubidium and potassium systems [135, 139] and
930 ground-based strontium systems [185, 186], the developments required for the next steps appear fea-
931 sible.

932 In this connection, we note that the experimental landscape of atom interferometry projects for
933 fundamental science exploitation has expanded significantly in recent years, with several terrestrial
934 experiments, based on different cold atom technologies, currently under construction, planned or
935 proposed.

936 Four large-scale prototype projects are funded and currently under construction, i.e., MAGIS [134]
937 in the US, MIGA [187] in France, ZAIGA [188] in China and AION [189] in the UK. These will
938 demonstrate the feasibility of atom interferometry at macroscopic scales, paving the way for terrestrial
939 km-scale experiments as the next steps. There are projects to build one or several km-scale detectors,

940 including AION-km at the STFC Boulby facility in the UK, MAGIA-advanced and ELGAR [190] in
941 Europe, MAGIS-km at the Sanford Underground Research facility (SURF) in the US, and advanced
942 ZAIGA in China. It is foreseen that by about 2035 one or more km-scale detectors will have entered
943 operation. These km-scale experiments would not only be able to explore sensitively ultralight dark
944 matter and the mid-frequency band of gravitational waves, but would also serve as the ultimate
945 technology readiness demonstrators for space-based missions like STE-QUEST [144] and AEDGE [5]
946 that would reach the ultimate sensitivity for exploring the fundamental physics goals outlined in this
947 Section.

948 The perspectives for large-scale atom interferometer projects are very rich today, with a central
949 focus on establishing the readiness of cold atom technology for use in experiments to explore funda-
950 mental science. These terrestrial pathfinders are advancing further the relevant technologies, closing
951 gaps and addressing fundamental physics questions.

952 However, in order to deploy effectively strontium or ytterbium on any microgravity platform, in
953 addition to these terrestrial developments a space-borne pathfinder mission or technology demonstrator
954 is key. The development of critical components benefits from synergies between all systems. As such,
955 laser modules developed for clock deployment could be used as the basis for interferometric missions.
956 Similar synergies are present for vacuum generation, frequency stabilization, and low noise electronics
957 between the various systems. With a technology demonstrator for a space-borne optical lattice
958 system, a lot of applied and fundamental missions could be supported and further developments
959 triggered.

960 **5.3 Recommendation: Road-Map for Fundamental Physics in Space**

961 To summarize Section 5.2, which details the requirements to enable the scientific opportunities from
962 Section 5.1, the following recommendations for developments can be made:

- 963 • Build upon the ongoing large-scale terrestrial atom interferometer projects for fundamental sci-
964 ence exploitation, such as MAGIS [134] in the US, MIGA [187] in France, ZAIGA [188] in
965 China and AION [189] in the UK to construct one of more of the proposed km-scale succes-
966 sors, which will enable technology development for space-based missions like STE-QUEST [144]
967 and AEDGE [5]. A terrestrial experiment, such as ELGAR [136], could, additionally, supple-
968 ment existing and future, possibly satellite-based, scientific measurements by targeting relevant
969 gravitational wave frequencies.
- 970 • Perform fundamental tests in ground based microgravity facilities, such as the drop tower, the
971 Einstein Elevator, parabolic flights, and sounding rockets, to develop technology and support
972 scientific findings.
- 973 • Prepare a satellite mission as the next step in cold and condensed atom technology in space with
974 a two-species interferometer based on the available rubidium and potassium sources.
- 975 • Prepare optical frequency references for operation in space to enable local Lorentz invariance
976 and local position invariance tests, as well as support space missions such as LISA. This is in
977 accordance with the recommendations in Section 3.
- 978 • Develop components for deployment in space, with a focus on those with synergies for different
979 missions, for instance optical preparation, laser modules, vacuum generation, and magnetic field
980 control.

- Advance the development of optical lattice systems on the ground, in ground-based microgravity platforms, and in space-based pathfinder missions to enable future gravitational wave detection missions. This includes miniaturization of subsystems and proof-of-principle missions or studies for individual components.

6 Technology Development, Space Qualification and Pathfinders

6.1 Requirements for cold atoms in space

6.1.1 Atomic clock mission

We advocate a single dedicated satellite in a highly elliptical orbit, containing a strontium optical lattice clock with a 1×10^{-18} systematic uncertainty and $1 \times 10^{-16}/\sqrt{\tau}$ instability, and including a coherent optical link for comparisons to ground-based clocks. Such a mission would enable a wide network of ground-based clocks to be compared to each other with 10^{-18} precision in 1 day, which would have applications in fundamental physics discovery, proof-of-concept optical timescales, and geodesy. Furthermore, the clock in elliptical orbit would enable direct searches for new physics, including stringent tests of general relativity (see Sections 3 and 5). To support such a mission, improved optical links must be developed for clock comparisons at 1×10^{-18} . Efforts to realize such links are currently underway in the ACES and I-SOC Pathfinder ESA programmes. However, the bulk of the challenge of a space-clock mission will be to develop a space-qualified strontium optical lattice clock. Present strontium clock technology occupies at least a few m^3 and consists of several complex, delicate components (see Section 6.3) which must all be brought up through the TRL scale.

6.1.2 Earth Observation mission

As outlined in Section 4, quantum sensors offer the perspective of enhancing missions for Earth Observation by embarking them either in a gradiometric configuration on a single satellite for a GOCE-like mission concept, or as accelerometers combined with laser links between satellite pairs for a GRACE-like mission concept in an earth orbit with an altitude of few hundred kilometers and nadir pointing mode. Similar to previous missions in Earth Observation, the targeted mission duration is several years. Anticipated sensitivities of ^{87}Rb atom interferometers with to accelerations or differential accelerations are in the range of 10^{-10} to $10^{-12} \text{ m s}^{-2} \text{ Hz}^{-1/2}$ at low frequencies, complementing current sensor technology. As a rough estimate, the quantum sensor may comprise few hundred kilograms of the payload, and consume few hundred Watts of power. Multiple quantum sensors can either be linked on a single satellite by interrogating them with the same beam splitter laser for a GOCE-like mission, or implemented as accelerometers for drag correction in a GRACE-like mission.

6.1.3 Fundamental Physics

As discussed in Section 5.2, key technologies in three areas are required for fundamental physics tests: optical clocks, optical links, and atom interferometers. The requirements for optical frequency references are described in the paragraph above. In case of optical links, the requirements depend on the specific mission, and range from single photon transmission in case of entanglement missions to long distance coherent laser light transmission in case of gravitational wave detection. For atom interferometers, the requirements are naturally more restrictive the higher the desired precision, which has implications for the atomic flux, preparation of the atoms, coherent manipulation, and interrogation times. The test of the universality of free fall outlined in Section 5.2 targets a measurement of the Eötvös ratio at the level of $\leq 10^{-17}$, and requires atom interferometers using two different kinds of

1022 atomic species simultaneously (e.g., ^{85}Rb and ^{87}Rb or ^{41}K and ^{87}Rb) with interrogation times of
1023 over 10 s to reach a projected sensitivity to differential accelerations of 10^{-13} ms^{-2} at a cycle time of
1024 10 s in an interleaved operation. For the case of the proposed space-borne gravitational detector, the
1025 scheme is based on strontium atoms, requiring an increased atomic flux, large momentum transfers,
1026 and interrogation times of 600 s to enable characteristic strain measurements down to 10^{-23} at about
1027 80 mHz. These parameters place requirements, e.g., on the atomic source as well as the dimensions of
1028 the central elements, such as the vacuum chamber, affecting the overall design of the sensor head.

1029 Fundamental physics experiments require a variety of different orbital scenarios. For example,
1030 entanglement experiments require large distances to close additional loopholes and test the validity of
1031 quantum mechanics, hence a geostationary or lunar satellite would be of interest. For local position
1032 invariance tests, based on the detection of gravitational red-shift, elliptical orbits with large potential
1033 differences are preferable, whereas local Lorentz invariance tests benefit from short orbital times with
1034 high orbital velocities. A prime candidate for such a mission is a satellite in low Earth orbit, while
1035 nevertheless avoiding vibrations caused by drag in the atmosphere. Orbital heights of 600 km with
1036 orbital times in the order of 90 min appear appropriate. A similar orbit may be chosen for EEP
1037 tests, motivated by the effect of the gravitational field and the absence of vibrations due to drag. The
1038 satellite should have an optical link to an optical frequency reference on the ground. The proposed
1039 gravitational-wave experiment described here would require two satellites in medium Earth orbit with
1040 a longer-baseline optical link in a calm environment to reduce gravitational noise.

1041 In all cases, the proposed mission duration spans multiple years.

1042 **6.2 Technology Development Path and Milestones**

1043 As indicated in the previous Section, the requirements for Cold Atoms in space basically call for three
1044 types of instrument to be developed: Atomic Clocks, Atom Interferometers and Optical Links.

1045 In order to have those instruments introduced and accepted into a space mission, a solid devel-
1046 opment and qualification approach should be established. This is expected to be based on existing
1047 and well-proven approaches currently applied in space projects, that need to be tailored to the specific
1048 technologies and trends to reach a suitable balance between risk and mission objectives. Depending
1049 on the technologies and objectives, the approach could include in-orbit demonstrators or pathfinder
1050 missions. As a guideline, and irrespective of the type of mission (in-orbit demonstrator, pathfinder,
1051 ...) a generic development approach for such instruments would typically include the following steps.

1052 First, the scientific/mission objectives are defined, e.g., a test of the universality of free fall or
1053 a strain measurement to a certain level, together with a high-level baseline mission scenario includ-
1054 ing, e.g., the orbit, in order to derive the expected preliminary mission lifetime and environment
1055 (mechanical, thermal, magnetic field, radiation, ...). In parallel, the technical requirements for the
1056 instrument(s) should be defined (functional, performance, operational, volume/mass/power, inter-
1057 faces, ...). This is based on both a flow-down of mission requirements (top-down) and the review of
1058 existing ground instruments and/or experiments (bottom-up). The outcome of this first step would be
1059 the issue of the consolidated mission definition and technical requirements, e.g., a certain sensitivity
1060 to differential accelerations or phase shifts induced by a gravitational wave.

1061 Once these requirements have been reviewed and agreed by the community, each instrument can
1062 follow its own development path. This includes first the definition of the instrument architecture
1063 and its external interfaces with the spacecraft and with other instruments. Secondly, the instrument
1064 architecture definition is further refined into subsystems, modules or units, e.g., the vacuum system
1065 including peripheral optics, the laser system, or the control electronics. For each of these elements,
1066 interfaces with upper levels are defined, together with technical requirements based on a flow-down

1067 from upper level. The granularity of the instrument architecture definition depends on the type and
1068 complexity of the instrument. The outcome of this step is the issue of the instrument architecture
1069 definition and technical requirements for the subsystems.

1070 The next step is the development of the subsystems, modules or units, whose approach is tailored
1071 to the specific element and the maturity of its underlying technology. It is usual practice to start the
1072 development at Breadboard level to demonstrate the basic functionalities and performance, and to
1073 develop further to an Elegant Breadboard and/or Engineering Model (EM). An Engineering Model is
1074 fully representative of the Flight Model in terms of form, fit and function, but does not require the use
1075 of qualified high-reliability parts. Fully validated at EM level, it has demonstrated full functionality
1076 and performance in a relevant environment and has reached TRL6. **TRL5?**

1077 Once all subsystems have demonstrated compliance to their technical requirements, they are in-
1078 tegrated into the instrument, which is in turn validated and verified according to an agreed method.
1079 It is likely that instruments based on Cold Atom technologies will not be able to reach their full
1080 performance on-ground, and therefore appropriate verification methods will have to be defined (e.g.,
1081 based on a combination of test and analysis/extrapolation through modelling, and/or microgravity
1082 test facilities such as a drop tower, Einstein Elevator, or zero-g Airbus flight). In the event of successful
1083 validation and verification at instrument level according to EM standards, the instrument will have
1084 reached TRL6.

1085 From there, the instrument will follow a qualification phase. For complex instruments like the
1086 ones we are considering here, this will most probably involve a Qualification Model (QM) that is fully
1087 representative of the Flight Model in terms of build standard (using qualified high-reliability parts),
1088 and that will be subject to a qualification test campaign according to agreed qualification levels and
1089 duration. This qualification step also includes the qualification of all lower-level elements, including
1090 their materials, parts and processes, in accordance with the requirements applicable to the mission
1091 (e.g., due to launch loads, the operational environment. etc.). After successful completion of the
1092 qualification phase, the instrument will have reached TRL7, and the manufacturing of the Flight
1093 Model is released.

1094 **6.3 Technology Readiness Level**

1095 **6.3.1 Atomic clock mission**

1096 Once optical links are in place, several technologies must be developed with improved TRL in order to
1097 launch a strontium optical lattice clock into space: optical resonators to stabilize lasers to a noise floor
1098 of 1×10^{-16} in fractional frequency, laser sources at six different wavelengths to cool, optically confine
1099 and interrogate strontium atoms, compact physics packages with a controlled black-body radiation
1100 environment, and compact frequency combs.

1101 **6.3.2 Earth Observation**

1102 Key concepts have been demonstrated, including gravimeters [191] with sensitivity $4.2 \cdot 10^{-8} \text{m/s}^2/\text{Hz}^{1/2}$
1103 and gradiometers [128, 129] with sensitivity $3 \cdot 10^{-8} \text{s}^{-2} \text{Hz}^{-1/2}$, both operating with ^{87}Rb atoms, as
1104 well as matter-wave collimation of BECs and BEC interferometers in a drop tower and onboard of a
1105 sounding rocket, utilising atom-chip technology for fast and robust production of ^{87}Rb BECs. The
1106 latter relied on adaptation and developments of the physics package, the laser system, and the control
1107 electronics to realise compact and robust setups. Further developments are required for operation in
1108 the specific conditions imposed in satellite missions on a component level, which is partially ongoing,
1109 but also for demonstrating the desired performance which relies on the extended free fall times in a
1110 microgravity environment.

1111 **6.3.3 Fundamental Physics**

1112 As outlined above, different scenarios for testing the limits of quantum mechanics with cold and con-
1113 densed atoms exist. As such, the TRL differs widely for the involved components. At this time,
1114 payload for experiments on cold Rb atoms and BECs as well as quantum entanglement have been op-
1115 erated on satellites or the ISS. To achieve the targeted sensitivities for the discussed missions, further
1116 developments for components, such as laser systems, vacuum technology, radiation-hard electronics
1117 and autonomous operation are necessary to accommodate, for instance, high-precision Rb/K or Sr
1118 interferometers. Specific payloads, such as a setup for BEC experiments and interferometry, or com-
1119 ponents, such as frequency combs, have been successfully operated on sounding rockets and therefore
1120 feature a higher TRL than other parts. Finally, several systems have not yet been installed into either
1121 of such systems and require developments to comply with vibrational loads during launch, budget
1122 (mass, size, and power) limitations, and other environmental conditions.

1123 **6.4 Technology evolution**

1124 Operating quantum sensors based on cold atoms on a satellite implies a completely new technology
1125 going to space. Between various mission scenarios utilising atomic clocks or atom interferometers
1126 for earth observation or fundamental physics several general building blocks are shared, including
1127 a physics package with a vacuum system surrounded by optics, coils and other peripherals, a laser
1128 system with laser sources and optical benches for light distribution and switching, an electronics
1129 system with various controllers, e.g., laser drivers, and a computer for executing sequences, collecting,
1130 storing and evaluating data, leading to potential synergies in technology developments. Within these
1131 subsystems, it is crucial to identify critical components and to start their development without delay
1132 for a mission within this decade. While different missions may require modified components imposing a
1133 new verification, this does not imply a completely new development, as the concepts, their capabilities
1134 and the approach for verification are known.

1135 Mission-specific technology developments that may focus on performance, miniaturisation, ro-
1136 bustness, lifetime or other relevant topics, as required, will typically follow a stepwise approach. On a
1137 conceptual level, ground-based facilities, although incompatible with deployment in space, can serve
1138 to test and verify experimental procedures, sequences, and concepts for a future mission. Initially,
1139 the system needs to be defined based on the necessary functionalities. Top-level examples are, e.g.,
1140 an atom interferometer based on Rb or Sr, a Sr optical lattice clock, optical frequency dissemination
1141 based on fibres, free space, and ground-space-ground communication with mission-specific performance
1142 requirements. The next step is to identify suitable subsystems (e.g., a laser system or vacuum sys-
1143 tem/science chamber) with respect to performance, to define components (e.g., a laser head or an atom
1144 chip) and develop either as required. This may include reliability and partial environmental tests on
1145 a subsystem level, depending on the estimated critically. The subsystems have then to be integrated,
1146 and subjected to end-to-end verification and performance tests. Subsequently, the full ground system
1147 is to be implemented and tested, including reliability and partial environmental tests. Facilities such
1148 as the microgravity simulator in Bordeaux, the drop tower in Bremen, or the Einstein Elevator in
1149 Hannover offer the possibility for operating a payload or parts thereof in up to a few seconds of micro-
1150 gravity. Additional options for such tests are early flight tests, as enabled by a zero-g Airbus flight or
1151 a sounding rocket. Gravity, the available microgravity time of the aforementioned facilities, or special
1152 (e.g., environmental) constraints of a mission may lead to the recommendation of a pathfinder mission
1153 with opportunities sponsored by ESA, the EU or national agencies. Finally, after the development
1154 and verification steps, the definition and planning of a full mission concludes the technology evolution.

1155 **6.5 Development milestones**

1156 Preceding or in parallel to the technology developments, several scientifically-justifiable milestones can
1157 be defined to assess the maturity on a conceptual level. These are related to the demonstration of
1158 basic functionalities and concepts, including feasibility studies. A starting point is the definition of
1159 the mission concept and the scientific motivation, be it for earth observation, fundamental physics
1160 or other purposes. Critical concepts can then be tested in ground-based setups (e.g., trapping and
1161 cooling atoms with novel atom’s chips/gratings), in certain cases with reduced performance (e.g., due
1162 to reduced free fall time), but still demonstrating their basic feasibility. This may include a special
1163 scheme for an atom interferometer up to a large-scale device for gravitational wave detection as in
1164 MIGA, MAGIS, ELGAR or AION. Depending on the possibility for extrapolation, the confidence
1165 in the modelling and understanding (e.g., due to different behaviour in the absence of gravitational
1166 sag, non-moving atoms), deploying a compact test setup in a microgravity facility such as the drop
1167 tower can demonstrate source performance, interrogation procedures, and detection of the atoms,
1168 accompanied by refined modelling, without the need for components qualified for a satellite mission.
1169 On the side of the mission concept, the orbit needs to be defined and evaluated accordingly, including
1170 the estimated implications on the payload and performance. The latter requires a simulator for the
1171 atom interferometer, clock or other relevant payload element to be developed. It can subsequently
1172 provide the modelling of the measurement output, including dependencies on internal and external
1173 disturbances compared to the desired signal. Within a dedicated pathfinder mission on a satellite,
1174 demonstrating, e.g., a high-contrast atom interferometer with extended free-fall times and long-term
1175 operation, and performing statistical and systematic studies, provide further milestones for assessing
1176 the maturity of sensors.

1177 **6.5.1 In-orbit validation**

1178 To date, following the successful operation of quantum sensors in laboratories, key technologies and
1179 concepts have been demonstrated, e.g., in dedicated microgravity experiments on BEC generation and
1180 interferometry with rubidium atoms. Limited microgravity time on the available platforms prevented
1181 long-term operation, extensive statistics and a detailed systematic analysis in this special environment.

1182 A dedicated satellite platform for a pathfinder avoids conflicts of programmatic or technical con-
1183 straints due to interface or other requirements of either part of the payload in joint mission con-
1184 cepts. Other currently existing or planned payloads have to provide multiple functionalities and are
1185 consequently neither dedicated nor optimised for quantum sensors. Despite considerable efforts for
1186 miniaturisation and robustness for accommodation in the available microgravity platforms, a satellite
1187 mission will impose additional constraints and requirements on the payload and the operation of the
1188 quantum sensor. This step towards a full-blown mission utilising quantum sensors motivates a timely
1189 pathfinder mission.

1190 Several examples of pathfinder missions have been mentioned in earlier Sections. Here we discuss
1191 as an example some aspects of a prospective mission deploying a quantum sensor with rubidium BECs
1192 on a satellite. Such a system offers the opportunity to achieve multiple goals. It enables the technology
1193 demonstration of a BEC source, beam splitters, detection, remote control, and autonomous execution
1194 of sequences on a satellite up to the uninterrupted operation of an atom interferometer over weeks
1195 to months, validating the maturity of the individual key components and functionalities. Further-
1196 more, it can serve for testing and validating onboard data evaluation and autonomous optimisation of
1197 parameters for the source, interferometer, and other manipulations of the atoms, reducing the need
1198 for user intervention. Depending on the satellite bus and orbit, the quantum sensor is subjected to

1199 specific disturbances, necessitating mitigation strategies such as, e.g., rotation compensation with a
1200 higher dynamic range than for stationary setups on Earth. Testing such techniques for free fall times
1201 of several seconds is crucial for future high-performance sensors. Finally, only a pathfinder mission can
1202 provide a detailed performance evaluation for a satellite-based quantum sensor due to the persistent
1203 microgravity, enabling the accumulation of extensive statistics in the satellite-specific environment.

1204 The higher level of maturity shown by the technology demonstration in such a pathfinder mis-
1205 sion would have a direct impact on proposals for an Earth Observation mission based on Rb BEC
1206 interferometers or a fundamental physics mission testing the universality of free fall with Rb/K dual-
1207 species BEC interferometers. Future missions with optical lattice clocks would also benefit from a
1208 pathfinder mission with a Rb BEC interferometer for validating vacuum technology, parts of the
1209 control electronics, the experiment control computer, onboard data evaluation, and autonomous op-
1210 eration. Introducing other atomic species for atom interferometry such as Sr implies more similarities
1211 with the outlined pathfinder than a clock-type mission due to additional shared concepts, but will in
1212 addition require dedicated development activities for the atomic source and laser systems.

1213 7 Workshop Summary

1214 As discussed in Section 2, the discovery of quantum mechanics in the first part of the 20th century made
1215 possible many of the technological innovations developed in the second half of the century. We are now
1216 witnessing the breakout from the laboratory of many quantum phenomena not yet applied, which offer
1217 sensor technologies of unparalleled accuracy for timing, accelerometry, gravimeters, etc.. The potential
1218 of this second quantum revolution has been recognized by the Senior Science Committee advising
1219 ESA on its Voyage 2050 programme, which has recommended an intensive programme of R&D to
1220 prepare quantum sensor technologies for deployment in space. Many of the cutting-edge developments
1221 of quantum technologies currently taking place in laboratories around Europe and elsewhere were
1222 discussed in this Workshop. Realizing their full potential in space-borne applications of immediate
1223 value to society as well as to fundamental science will require a community effort to outline high-level
1224 objectives and a road-map for achieving them that optimizes the synergies between different mission
1225 concepts.

1226 Atomic clocks have already attained a precision of 10^{-18} , and the ACES mission is in an advanced
1227 state of preparation for deployment on the ISS. Atomic accelerometers have already exhibited a preci-
1228 sion of $4 \times 10^{-8} \text{ m/s}^2/\sqrt{\text{Hz}}$ on the ground, and offer drift-free stability extending to frequencies below
1229 10 mHz. There has been a series of Bose-Einstein Condensate (BEC) experiments in micrograv-
1230 ity using MAIUS sounding rockets, the CAL BEC experiment has operated successfully for several
1231 years on the ISS, the MICROSCOPE experiment has tested the Einstein Equivalence Principle (EEP)
1232 in space, and the MAGIS, MIGA, ZAIGA and AION atom interferometer experiments to look for
1233 ultralight dark matter and pave the way for future measurements of gravitational waves are under
1234 construction.

1235 We present below a first draft for this community road-map, based on the cold atom achieve-
1236 ments so far, the ongoing research, and the high-level objectives for the future. The draft road-map is
1237 centred around three topics: atomic clocks, quantum accelerometry, and atom interferometry, and is
1238 oriented towards the following objectives: next-generation standards for time standards and naviga-
1239 tion, next-generation Earth observation and its potential for monitoring mass and climate change, and
1240 fundamental science including tests of relativity, searches for dark matter and novel measurements of
1241 gravitational waves. We stress the existence of an ongoing technology development programme includ-

1242 ing terrestrial and space-borne pathfinder projects, and the need for follow-on pathfinder experiments
1243 on Earth and in space.

1244 Milestones in the road-map towards space clocks discussed in Section 3 include the completion
1245 of ACES [17] and its deployment on the ISS, to be followed by a follow-on mission such as I-SOC
1246 Pathfinder [108, 109]. Its objectives would include a comparison of ground-based optical clocks with
1247 a precision of 10^{-18} over a day (see Fig. 1), which would have applications in fundamental physics
1248 experiments as well being as a proof-of-concept for establishing timescales and in geodesy. This
1249 should be followed by a dedicated satellite in a highly elliptical orbit containing a strontium optical
1250 lattice clock with similar precision and a coherent optical link to ground, with goals similar to those of
1251 FOCOS [110]. Such a mission would enable more precise comparisons across a wider network of ground
1252 clocks, and stringent tests of general relativity. The development of coherent free-space optical links
1253 will be key, to be accompanied by the qualification of a strontium optical lattice clock for operation in
1254 space, which will require a technology development programme for several clock components. There
1255 are multiple synergies between these atomic clock missions and the requirements for a fundamental
1256 science mission such as AEDGE [5] based on strontium atom interferometry.

1257 As discussed in Section 4, quantum accelerometry has exciting potential (see Figs. 4 and 5), and we
1258 envisage three gravimetry missions aimed at realizing it. The first of these is the planned conventional
1259 gravimetry mission MAGIC [124]. It will be necessary, in parallel, to update the quantum instrument
1260 specifications and requirements. For the technical reasons discussed in Section 4, deploying a quan-
1261 tum sensor as a passenger on a conventional geodesy mission would pose severe technical challenges,
1262 implying significant technological and programmatic risks for both the classical and quantum aspects
1263 of such a joint mission. For this reason, the discussions among scientific experts during the workshop
1264 led to a recommendation to launch a separate quantum pathfinder mission within this decade on a
1265 dedicated platform, with a target performance of 10^{-10} m/s²/√Hz. Such a mission would combine the
1266 need for a test of the quantum technology in space with the optimizing the results to be expected from
1267 a quantum gravimetry pathfinder mission. It would also serve as a milestone for other communities,
1268 such as that interested in applications of cold atoms to probes of fundamental physics. The success of
1269 MAGIC and the quantum gravimetry pathfinder mission would pave the way for a full-fledged quantum
1270 space gravimetry mission to follow on from MAGIC, whose definition would be based on the experience
1271 gained with MAGIC and the pathfinder mission.

1272 We outlined in Section 5 the requirements for enabling the opportunities for exploring funda-
1273 mental science, some of which are illustrated in Figs. 8 and 11. The first step is to construct and
1274 operate the ongoing large-scale terrestrial atom interferometer projects for fundamental science, such
1275 as MAGIS [134] in the US, MIGA [138] in France, ZAIGA [142] in China and AION [137], to be fol-
1276 lowed by one or more of the proposed km-scale experiments such as [136] and the successors to MAGIS,
1277 ZAIGA and AION, which will serve as ultimate conceptual technology readiness demonstrators for a
1278 space-based mission such as AEDGE [5]. In parallel, there should be a satellite mission demonstrating
1279 cold and condensed atom technology in space, building on the experience with [192] and [139] and using
1280 a two-species interferometer (see [144]), based on the available rubidium and potassium sources. It will
1281 also be necessary to prepare optical frequency references for operation in space (see also Section 3),
1282 which will also support space missions such as LISA [151]. This will require advancing strontium
1283 development on the ground, in ground-based microgravity platforms, and in space-based pathfinder
1284 missions, including individual components, the miniaturization of subsystems and proof-of-principle
1285 missions.

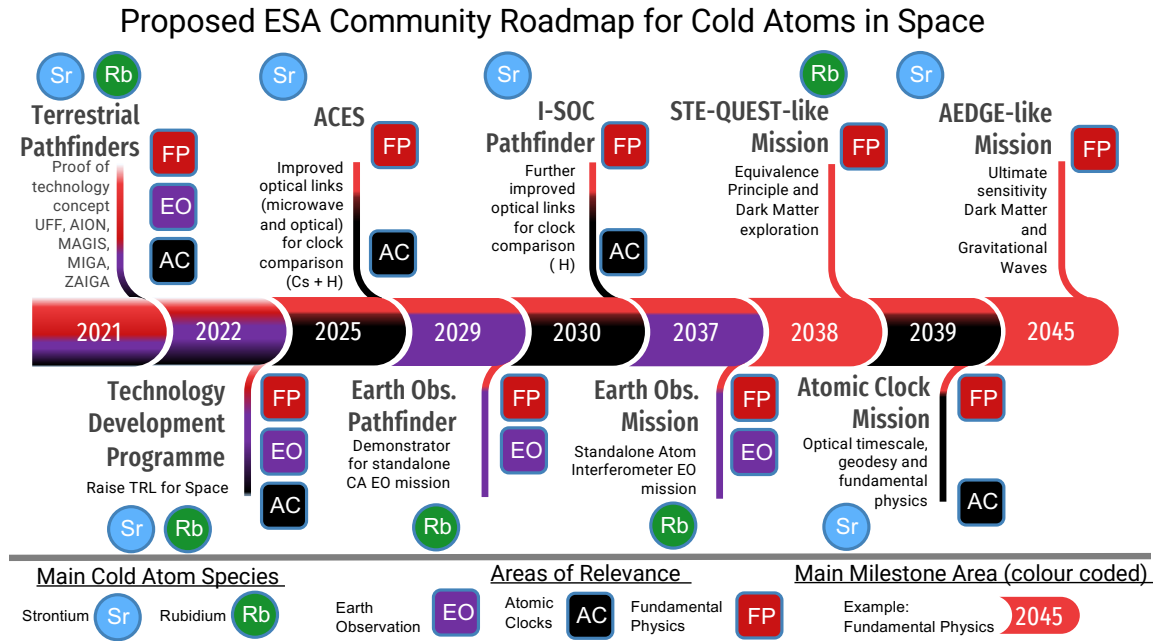


Figure 13. A first draft of the community road-map proposed for discussion. The figure shows the main milestones of the road-map, where the colour code indicates the relevance for the three main areas of Earth Observation (purple), Atomic Clocks (black) and Fundamental Physics (red). The main Cold Atom species are indicated with circles coloured blue for strontium and green for rubidium. These do not necessarily indicate that a milestone is based on this Cold Atom species, but may also indicate that this milestone will contribute to its space readiness. The years indicated in each milestone represent the starting date of the milestone activity, assuming preparatory work took place before. The further the timeline extends into the future, the more uncertain the milestone starting date becomes. Further details about each of the milestones and their interdependences are given in Section ??.

1286 8 Proposed ESA Community Road-Map for Cold Atoms in Space – Draft 1287 Version

1288 The road-map part will be finalized AFTER the workshop write-up is assembled. Espe-
1289 cially section 6 will be an important input to the road-map (first draft in Fig. 13), but
1290 also other sections will inform it.

1291 Once the final main milestones have been agreed, this section will be expanded to provide a
1292 detailed discussion of the individual milestones and their interdependence. The current draft is to
1293 provide an idea on how the roadmap could be structured and what content it could feature.

1294 8.1 2021 Terrestrial Pathfinders Underway

1295 R&D and prototyping is currently underway for several terrestrial atom interferometer experiments
1296 on scales from 10 m to 100m that are under construction. These include the following experiments,

1297 listed together with the atom species they use: MAGIS (Sr), MIGA (Rb), ZAIGA (Rb) and AION
1298 (Sr). These experiments are directed primarily towards objectives in fundamental science such as the
1299 search for ultralight dark matter, tests of the Einstein Equivalence Principle (Universality of Free Fall),
1300 and future measurements of gravitational waves that will provide tests of general relativity as well as
1301 advances in astrophysics and cosmology. These projects will serve to demonstrate on larger scales
1302 techniques that have been developed in smaller-scale laboratory experiments, verifying the proposed
1303 technological concepts. The technical advances made in these pathfinder experiments will also find
1304 applications to atomic clocks and in Earth Observation.

1305 **8.2 2022 Development Programme Launch**

1306 In parallel with the construction, commissioning and operation of these terrestrial pathfinder exper-
1307 iments, it will be necessary to start without delay a programme to raise the TRLs of the associated
1308 technologies, demonstrating their robustness and reliability, and reducing their size, weight and power
1309 requirements, so that they become realistic candidates for deployment in space-borne experiments. In
1310 addition to the sensor technologies used directly in the experimental apparatus, such as atomic clocks,
1311 accelerometers and interferometers, it will be necessary to raise the TRLs of ancillary technologies
1312 such as optical links. This technology development programme will be essential for the deployment
1313 in space of atomic clocks, applications to Earth Observation and experiments in fundamental physics.
1314 Technologies using Sr are currently less mature than those using Rb, but both will require substantial
1315 development effort.

1316 **8.3 2025 ACES**

1317 The ACES experiment is currently being prepared for launch by 2025. It will measure the gravitational
1318 redshift between the PHARAO clock on-board the ISS and clocks on Earth, improving on current
1319 measurements of the redshift effect by an order of magnitude. In addition to providing the first in-
1320 orbit demonstration of the operation of an atomic clock using cesium, as well as the operation of a
1321 hydrogen maser, it will also pioneer the deployment of improved optical links for atomic clocks in
1322 space. ACES will serve as a pathfinder for future projects deploying atomic clocks in space as well as
1323 providing important new tests of general relativity, paving the way for future cold atom experiments
1324 on fundamental physics in space. The experience gained with ACES will be particularly relevant for
1325 subsequent experiments using strontium such as I-SOC.

1326 **8.4 2029 Earth Observation Pathfinder Mission**

1327 As discussed in the main text, gravimeters and accelerometers based on cold atom technology show
1328 great promise for future Earth Observation missions, in view of the high precision, stability and low-
1329 frequency performance they offer. However, we judge that it would be premature to plan a standalone
1330 Earth Observation mission using cold atoms, and that a prior pathfinder mission will be required. For
1331 the reasons discussed in the text, we consider that it not be advantageous to combine this quantum
1332 pathfinder mission with an Earth Observation mission using classical technology. While relevant
1333 primarily for Earth Observation, this mission will also pave the way for subsequent fundamental
1334 science missions using atomic clocks. It would use rubidium atoms, whose terrestrial development is
1335 relatively mature, and its operational experience would be relevant to an STE-Quest-like fundamental
1336 physics mission as well as to the subsequent standalone Earth Observation mission, both of which
1337 would use rubidium.

1338 **8.5 2030 I-SOC Pathfinder**

1339 I-SOC Pathfinder would push further the microwave and optical link technologies being developed for
1340 ACES, with a view to continue the operation of a worldwide network of optical clocks on the ground
1341 to test fundamental laws of physics, to develop applications in geodesy and time & frequency transfer,
1342 and to demonstrate key technologies for future atomic clock missions in space. Its main objective
1343 would be to increase the versatility of atomic clocks in space, acting as a pathfinder for a subsequent
1344 mission to exploit the full capabilities of atomic clocks, also for applications in fundamental physics.
1345 It would use strontium, which shows great promise for providing an accurate time standard as well as
1346 testing fundamental physics principles.

1347 **8.6 2037 Earth Observation Mission**

1348 This would be a standalone Earth Observation to deliver the prospective improvements in spatial
1349 and temporal resolution over classical Earth Observation missions such as GRACE and GOCE that
1350 are illustrated in Fig. 5. The full definition of the mission will be informed by the lessons learned
1351 from the next-generation classical MAGIC mission and the Pathfinder mission outlined in Section 8.4.
1352 Although the primary purpose of this mission would be Earth Observation, the technical developments
1353 it requires will also benefit the STE-QUEST-like fundamental physics mission outlined in Section 8.7,
1354 which will also use rubidium.

1355 **8.7 2038 STE-QUEST-like Mission**

1356 Building on experience with the successful MICROSCOPE mission and development work undertaken
1357 for the previous STE-QUEST proposal, this mission would deploy a double atom interferometer with
1358 rubidium and potassium “test masses” in quantum superposition to test the Einstein equivalence
1359 Principle (universality of free fall, UFF) and search for ultralight dark matter. It would use a single
1360 satellite in a 700 km circular orbit, and offers the possibility of probing the Einstein Equivalence
1361 Principle, with a precision $\mathcal{O}(10^{-17})$, as seen in Fig. 8. This is essentially a fundamental physics
1362 mission that would, however, build upon the development work and space-borne experience with
1363 rubidium, as provided by the Earth Observation missions described in Sections 8.4 and 8.6.

1364 **8.8 2039 Atomic Clock Mission**

1365 This mission would translate the high precision of the most accurate atomic clocks shown in fig. 1 into
1366 a global time standard that would take metrology to the next level, with corresponding advantages for
1367 navigation, geodesy and fundamental physics. It would use a dedicated satellite in a highly elliptical
1368 orbit containing a strontium optical lattice clock with a 10^{-18} systematic uncertainty and $10^{-16}/\sqrt{\tau}$
1369 stability, and a coherent optical link to ground. In addition to enable more precise comparisons across
1370 a wider network of ground clocks, it would provide direct searches for new physics including stringent
1371 tests of general relativity than possible with previous missions. It would, in particular, on previous
1372 operational experience with the I-SOC Pathfinder mission and ACES.

1373 **8.9 2045 AEDGE-like Mission**

1374 This would be a fundamental science mission based on atom interferometry using strontium. It would
1375 provide the ultimate sensitivity to ultralight dark matter, as seen in Fig. 8, and gravitational waves in
1376 the deciHz band intermediate between the maximum sensitivities of LIGO/Virgo/KAGRA and other
1377 terrestrial laser interferometers and the space-borne laser interferometer LISA, as seen in Fig. 11. The
1378 configurations considered assume two satellites in medium Earth orbit separated by $\sim 40,000$ km

1379 using atom clouds that might be either inside or possibly outside the satellites It would be based
1380 upon developments pioneered by many of the pathfinders described above including the terrestrial
1381 atom interferometers now under construction, ACES, I-SOC Pathfinder and the proposed dedicated
1382 atomic clock missions. It would have many elements such as techniques to minimize the size, weight
1383 and power requirements for atomic clocks, as well as optical links, in common with missions using
1384 rubidium atoms such as the dedicated Earth Observation and STE-QUEST-like missions.

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